

Holographic Complex CFTs

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In collaboration with **A. F. Faedo, C. Hoyos & D. Mateos**

Based on **1909.04008**

Walking behaviour



Fixed Point Annihilation

$$\beta = \frac{\partial g}{\partial \log \mu} = (\alpha - \alpha_*) - (g - g_*)^2$$

Fixed Point Annihilation

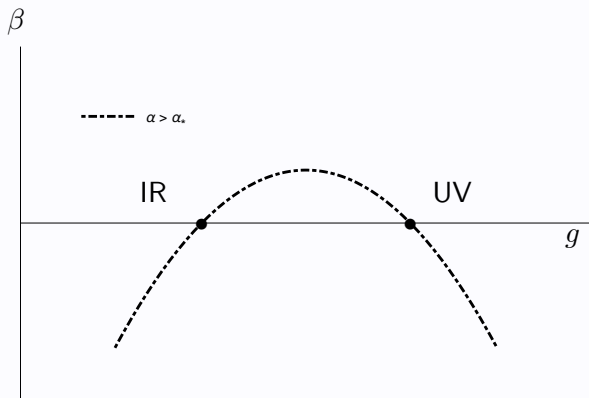
$$\beta = \frac{\partial g}{\partial \log \mu} = (\alpha - \alpha_*) - (g - g_*)^2 = 0$$

$$g_{\pm} = g_* \pm \sqrt{\alpha - \alpha_*} \quad (\alpha - \alpha_*) > 0$$

Fixed Point Annihilation

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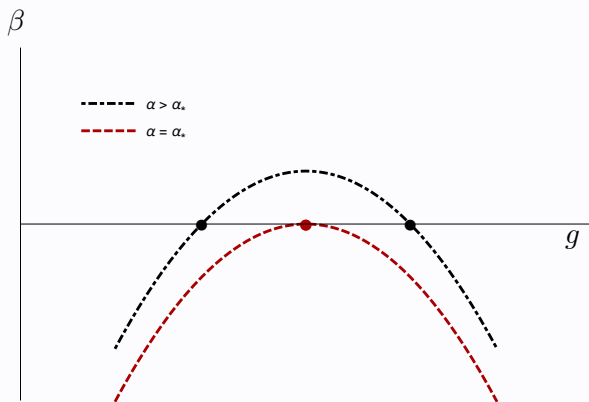
$$g_{\pm} = g_* \pm \sqrt{\alpha - \alpha_*} \quad (\alpha - \alpha_*) > 0$$



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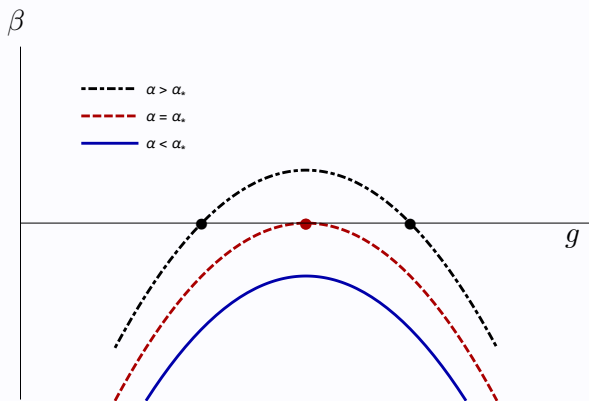
$$g_{\pm} = g_* \quad (\alpha - \alpha_*) = 0$$



Fixed Point Annihilation

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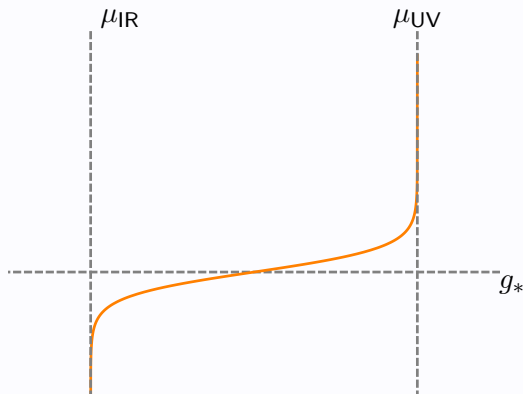
$$g_{\pm} = g_* \pm i\sqrt{|\alpha - \alpha_*|} \quad (\alpha - \alpha_*) < 0$$



Fixed Point Annihilation

$$\beta = \frac{\partial g}{\partial \log \mu} = (\alpha - \alpha_*) - (g - g_*)^2 = 0$$

$$\frac{\mu_{\text{IR}}}{\mu_{\text{UV}}} = \exp\left(\int_{g_{\text{UV}}}^{g_{\text{IR}}} \frac{dg}{\beta(g)}\right) \approx e^{-\pi/\sqrt{\alpha_* - \alpha}}$$



Holographic Realisation

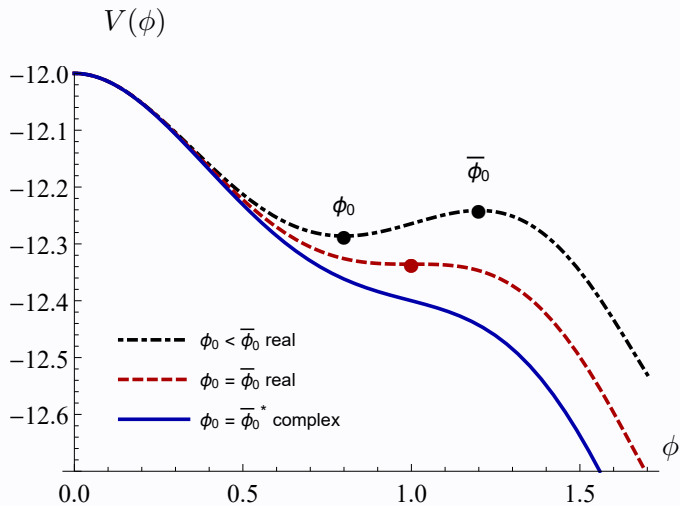
$$S = \frac{1}{2\kappa_5^2} \int d^5x \sqrt{-g} \left(R - \frac{1}{2} \partial_\mu \phi \partial^\mu \phi - V(\phi) \right)$$

$$V = 3 \left(6 \left(\frac{dW}{d\phi} \right)^2 - 4W^2 \right)$$

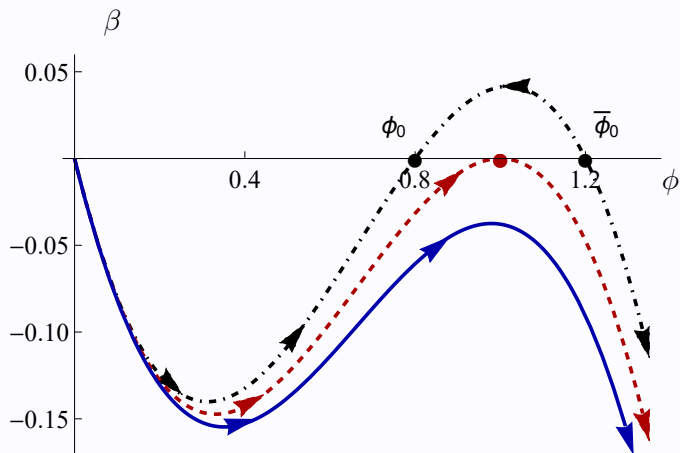
$$\beta(\phi) = -6 \frac{d \log W}{d\phi}$$

$$\frac{dW}{d\phi} = \frac{W_0}{L} \phi (\phi - \phi_0) (\phi - \bar{\phi}_0)$$

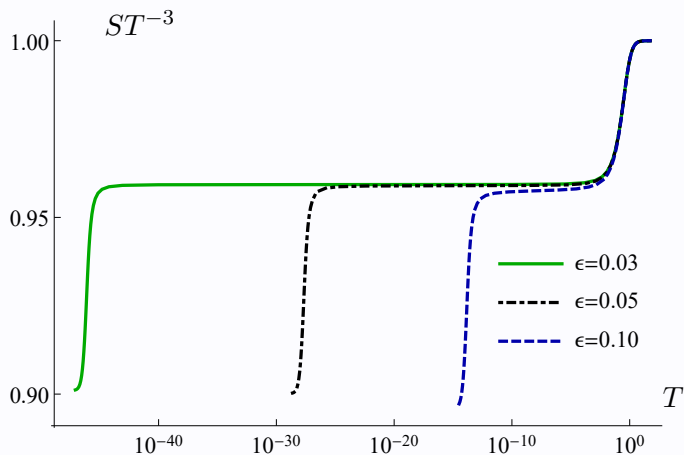
Holographic Realisation



Holographic Realisation

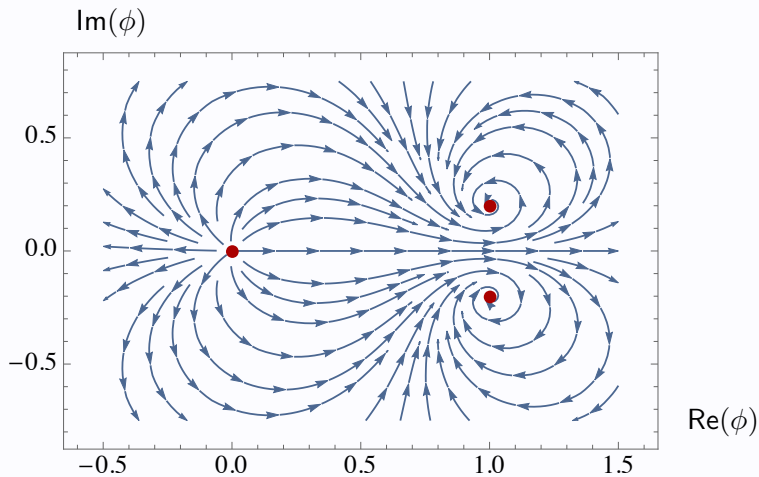


Holographic Realisation



$$\frac{\mu_{\text{IR}}}{\mu_{\text{UV}}} = \exp\left(\int_{g_{\text{UV}}}^{g_{\text{IR}}} \frac{dg}{\beta(g)}\right) \approx e^{-\pi/\sqrt{\alpha_* - \alpha}}$$

Holographic Realisation



Conclusion

We provided a holographic realization of fixed point annihilation at strong coupling and discussed the existence of complex CFTs at the fixed points.