

# FourIER *phase* SpecTrum Analysis ( $\Phi$ ESTA / FIESTA)

## Parametrising Stellar Variability in Fourier Space

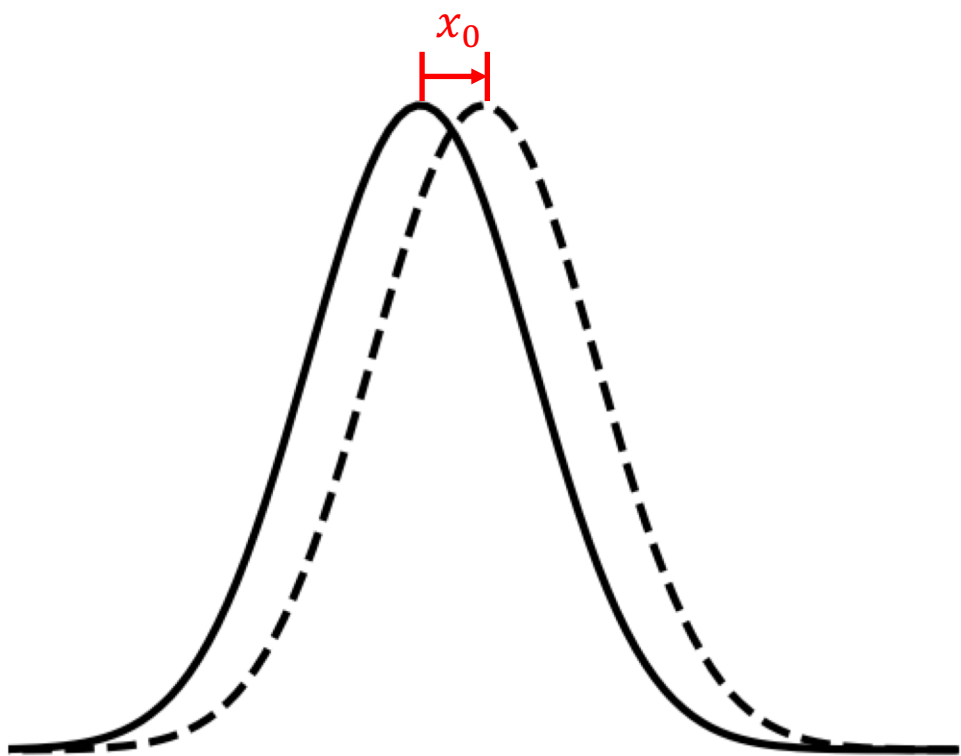
Jinglin Zhao<sup>1</sup>

PhD supervisor: Chris Tinney<sup>1,2</sup>

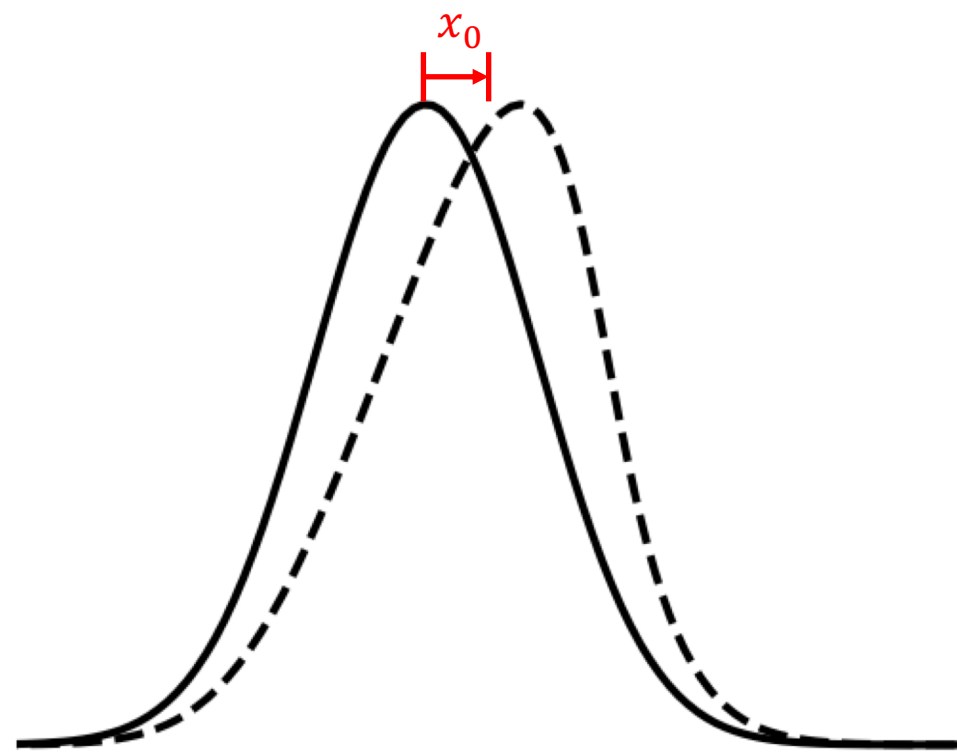
1. Exoplanetary Science at UNSW, School of Physics, UNSW Sydney

2. Australian Centre for Astrobiology, UNSW Sydney

# Challenge

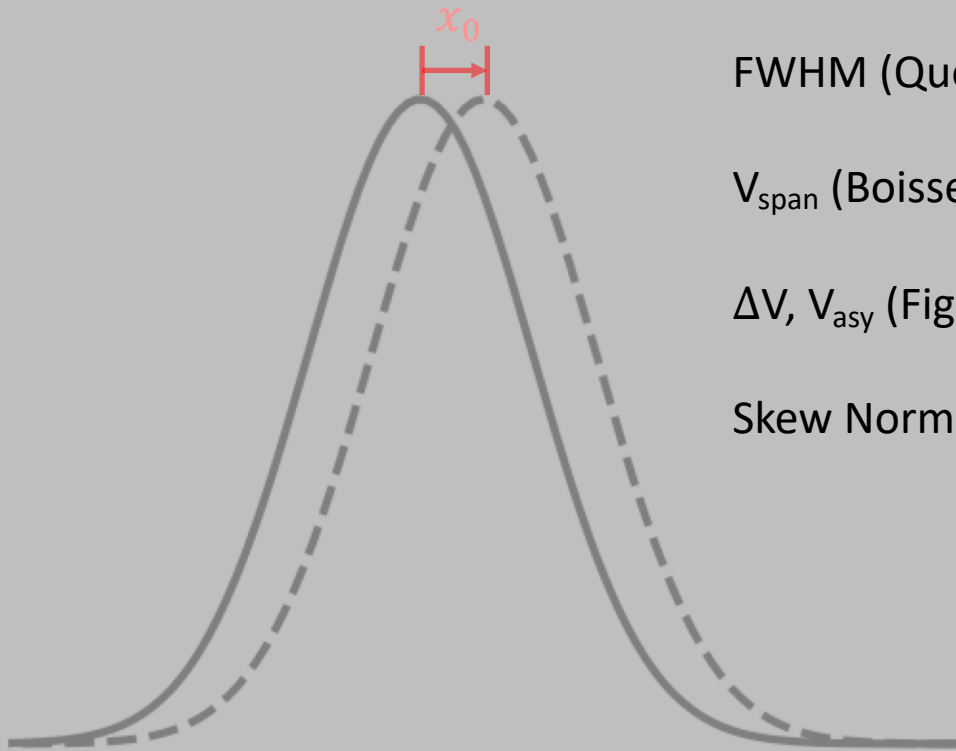


Intrinsic shift (orbiting companions)



Apparent shift (stellar variability)

# Challenge



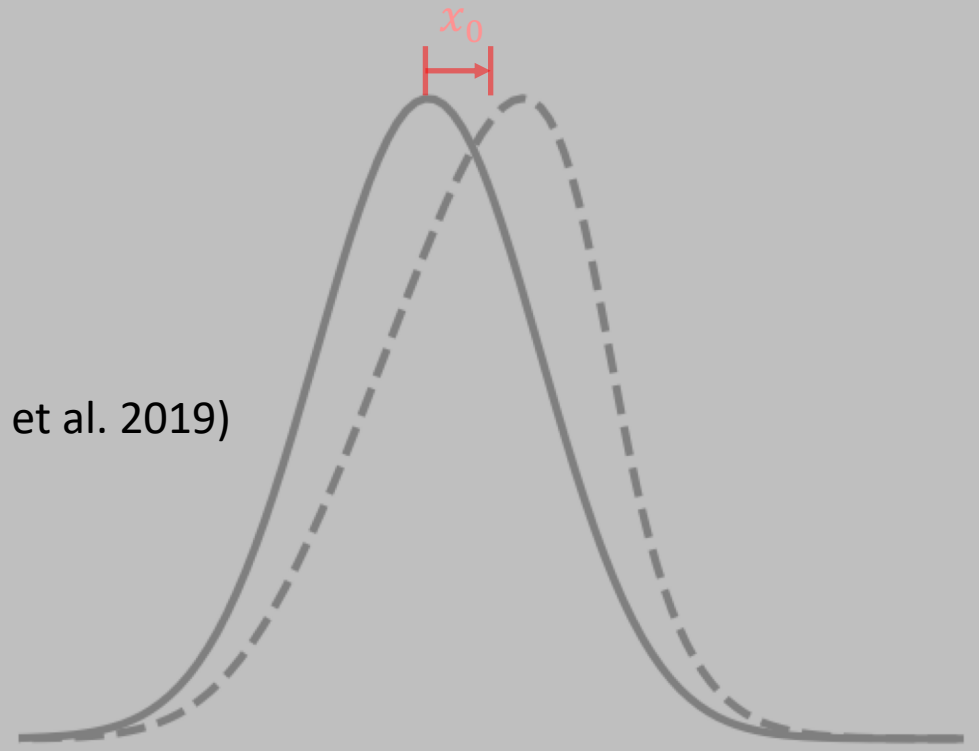
Bisector (Queloz et al. 2001)

FWHM (Queloz et al. 2009)

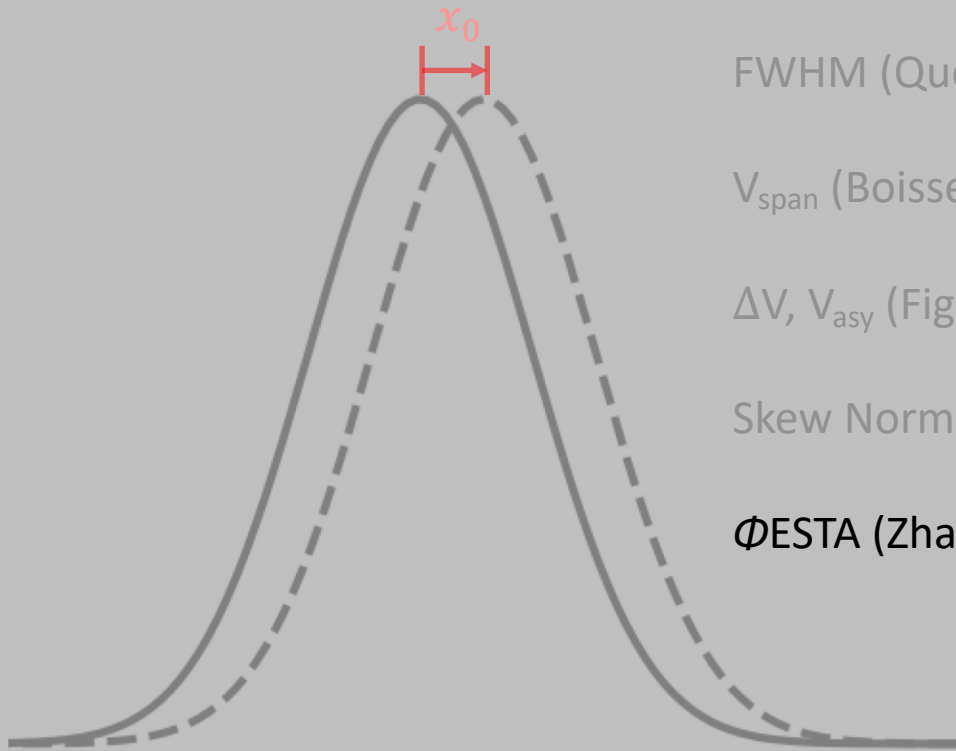
$V_{\text{span}}$  (Boisse et al. 2011)

$\Delta V$ ,  $V_{\text{asy}}$  (Figueira et al. 2013)

Skew Normal density (Simola et al. 2019)



# Challenge



Bisector (Queloz et al. 2001)

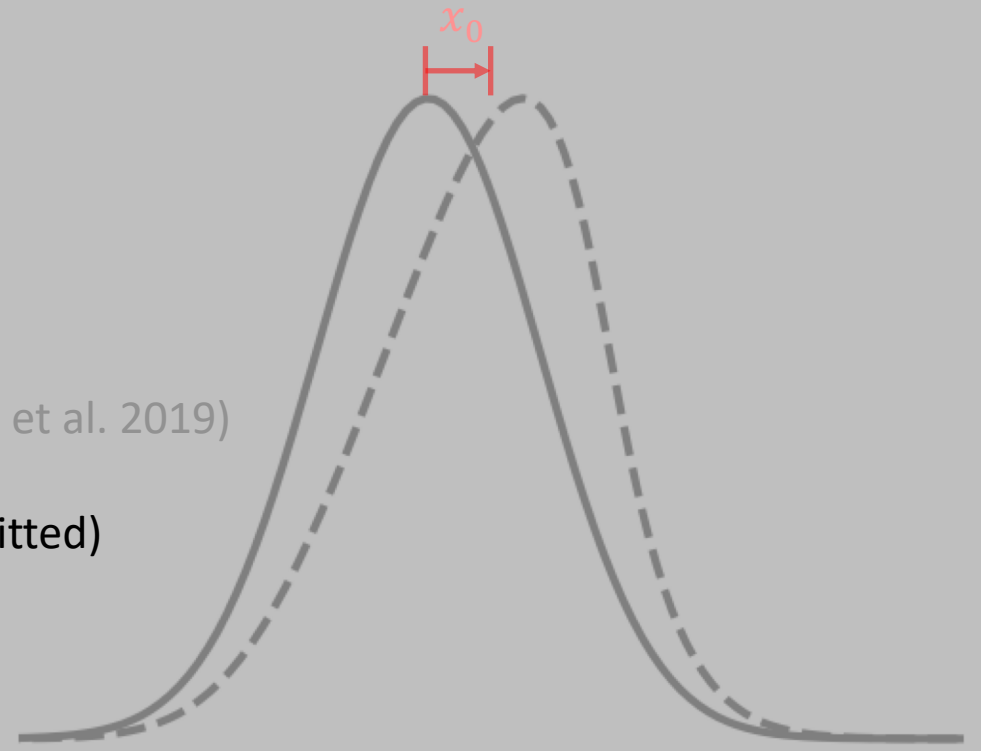
FWHM (Queloz et al. 2009)

$V_{\text{span}}$  (Boisse et al. 2011)

$\Delta V$ ,  $V_{\text{asy}}$  (Figueira et al. 2013)

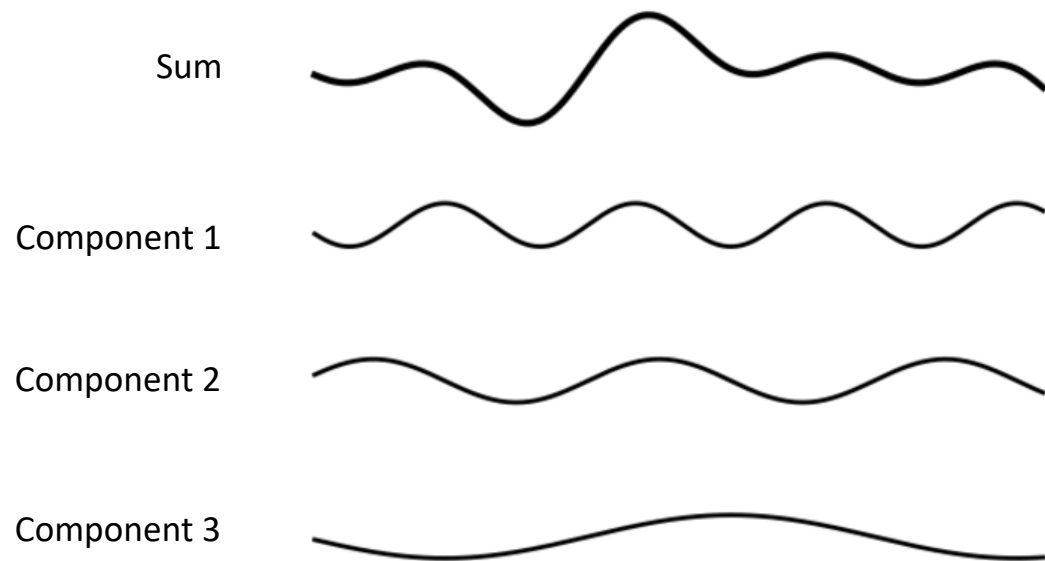
Skew Normal density (Simola et al. 2019)

$\Phi$ ESTA (Zhao & Tinney, submitted)

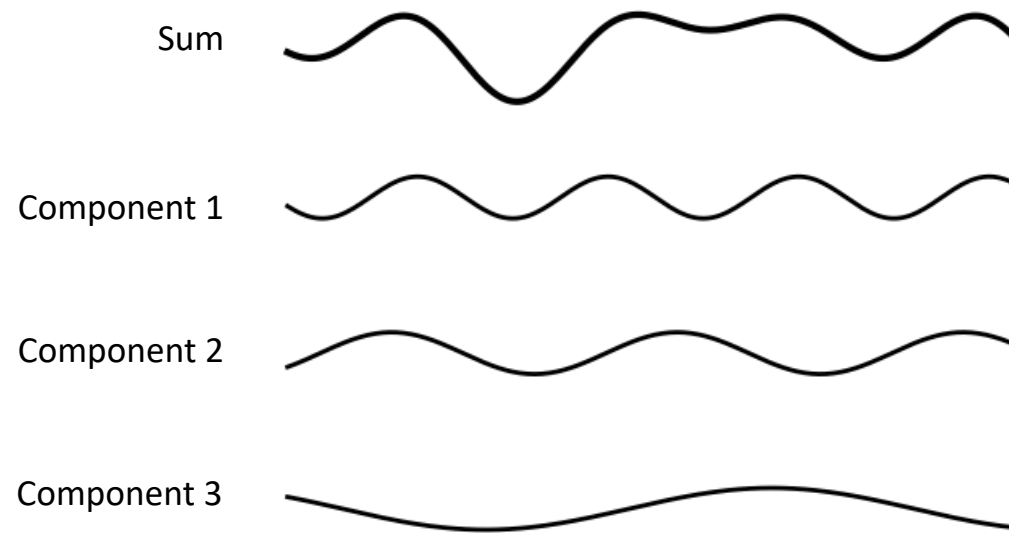


# Entrée

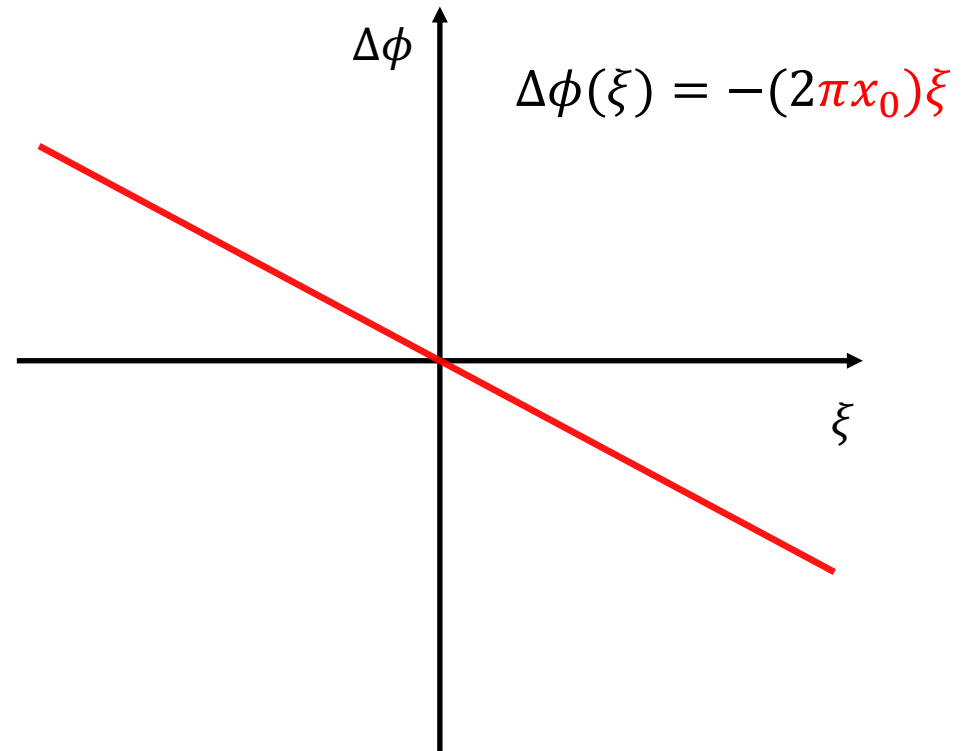
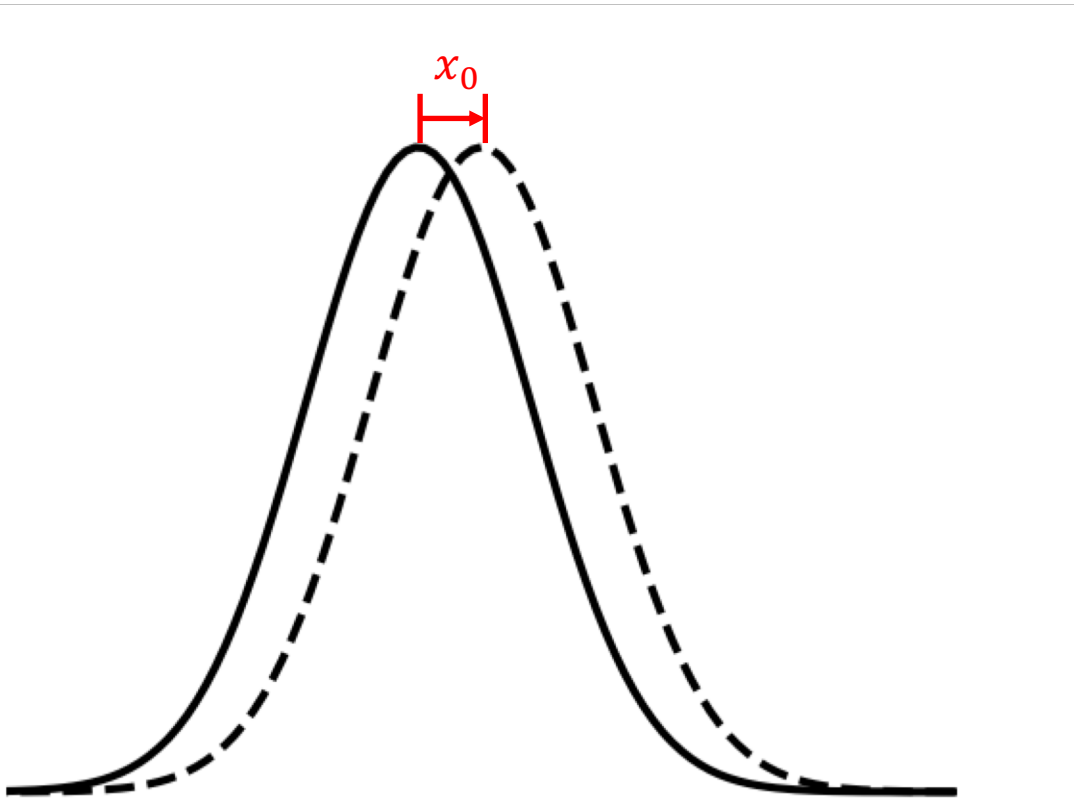
Signal shifted



Signal deformed

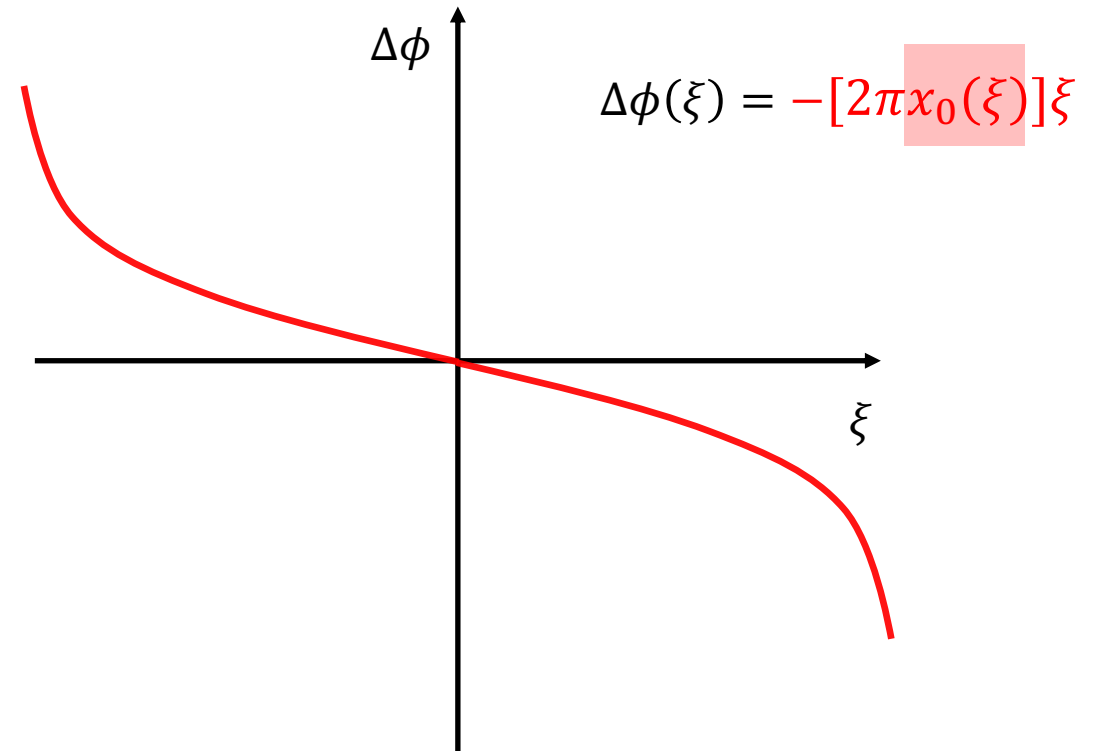
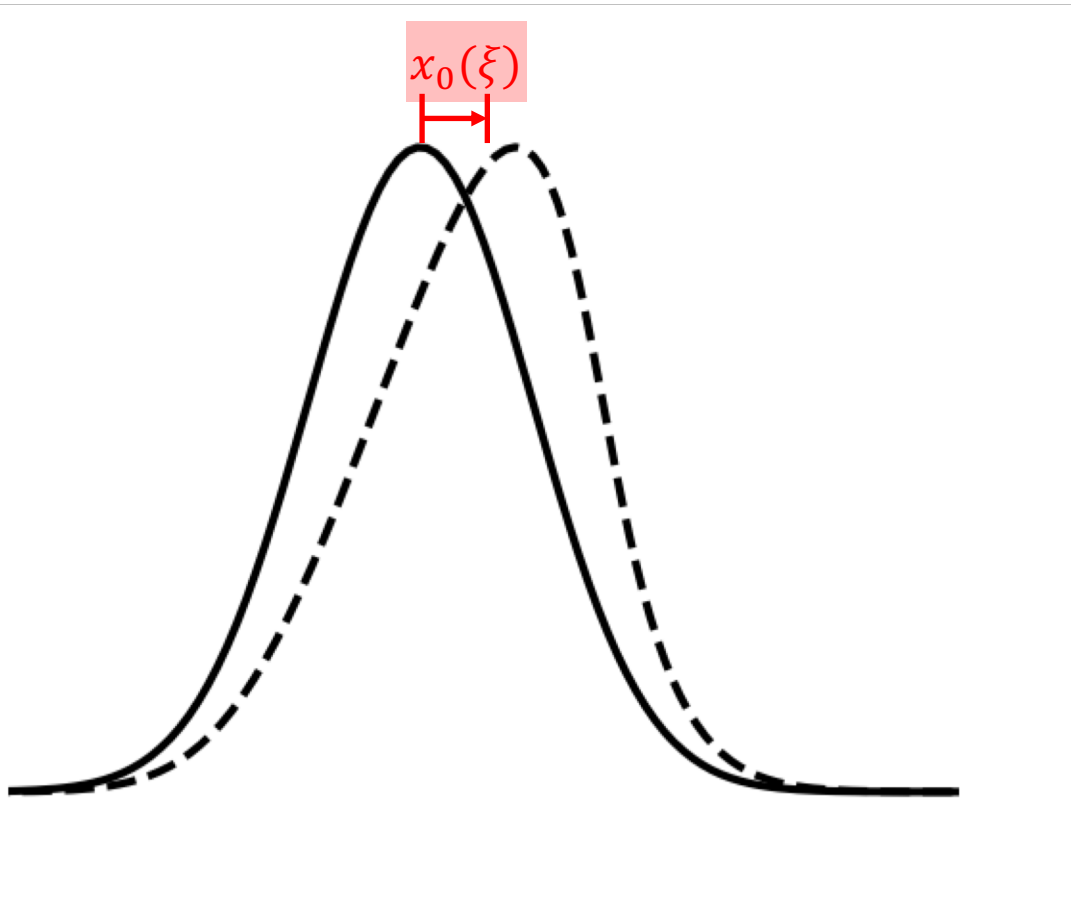


# Translation Property – Line Shift

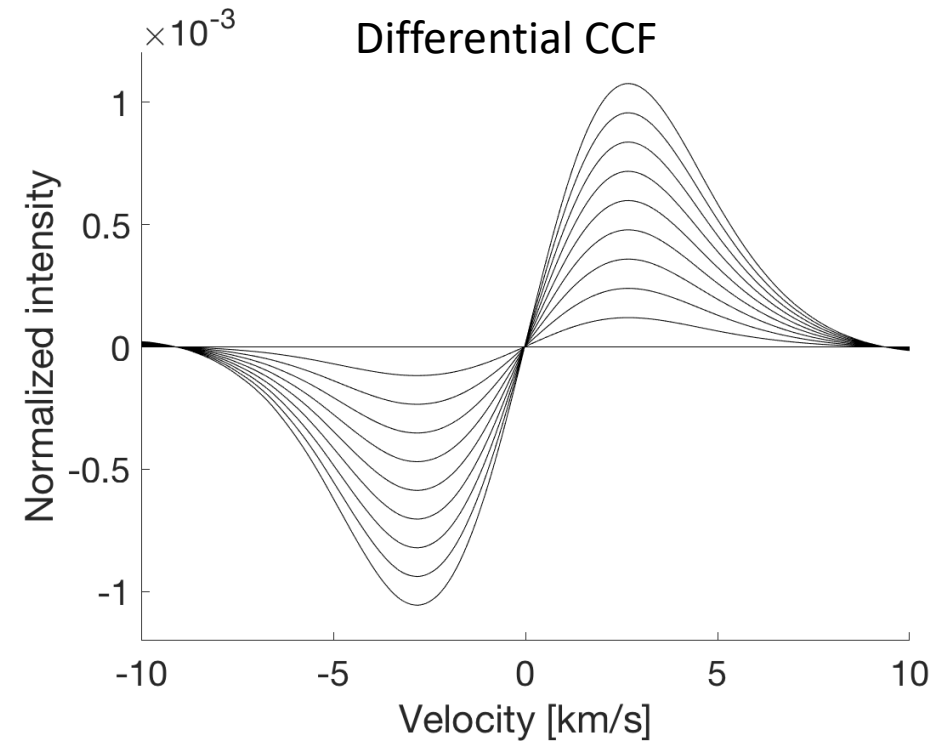
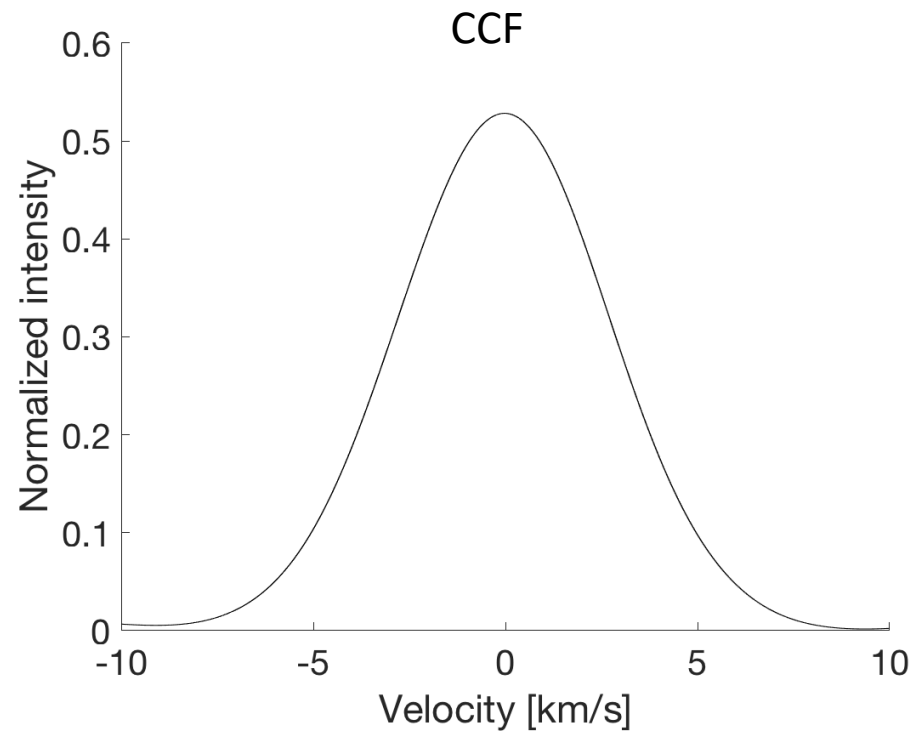


- If  $h(x) = f(x - x_0)$ , then  $\hat{h}(\xi) = e^{-2\pi i x_0 \xi} \hat{f}(\xi)$
- Phase shift  $\Delta\phi(\xi) = -(2\pi x_0)\xi$

# Translation Property – Line Deformation



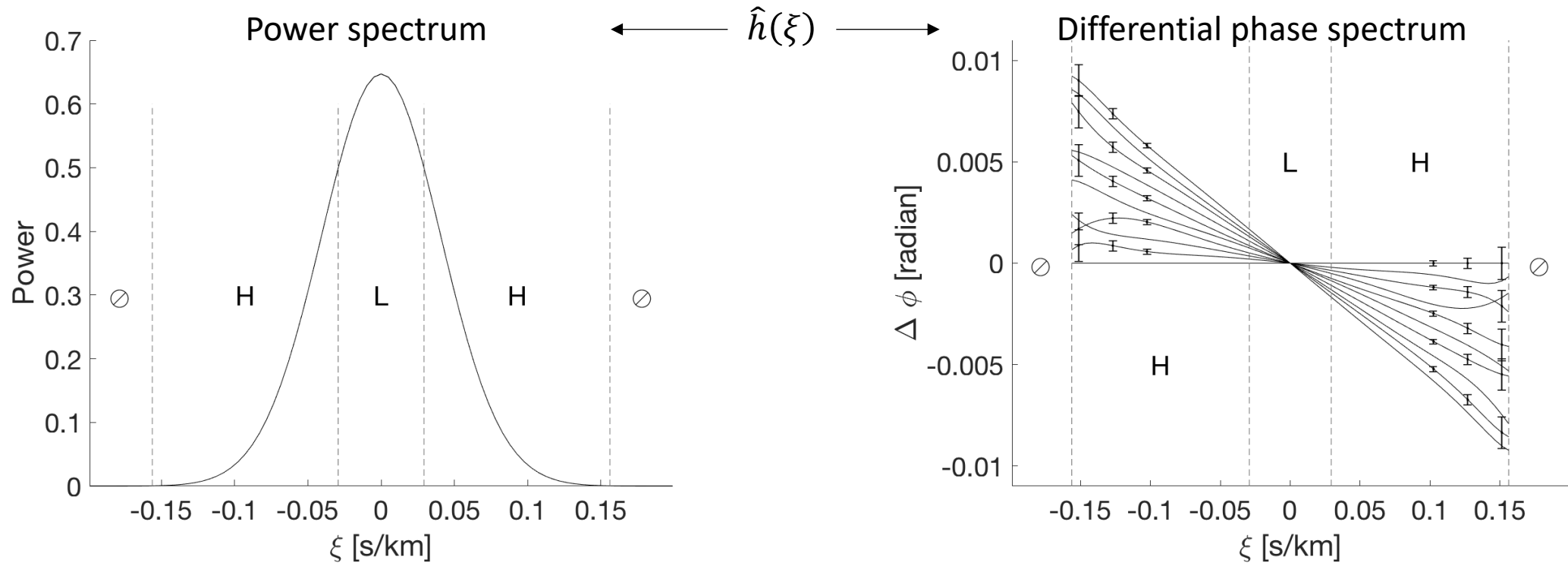
- Phase shift  $\Delta\phi(\xi) = -[2\pi x_0(\xi)]\xi$



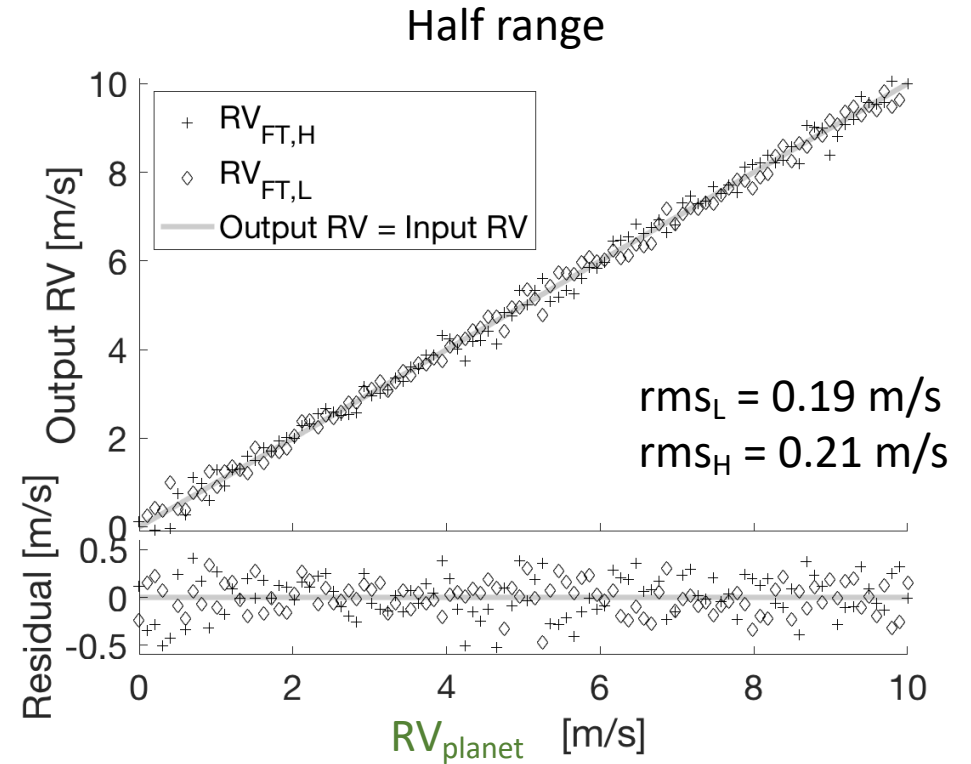
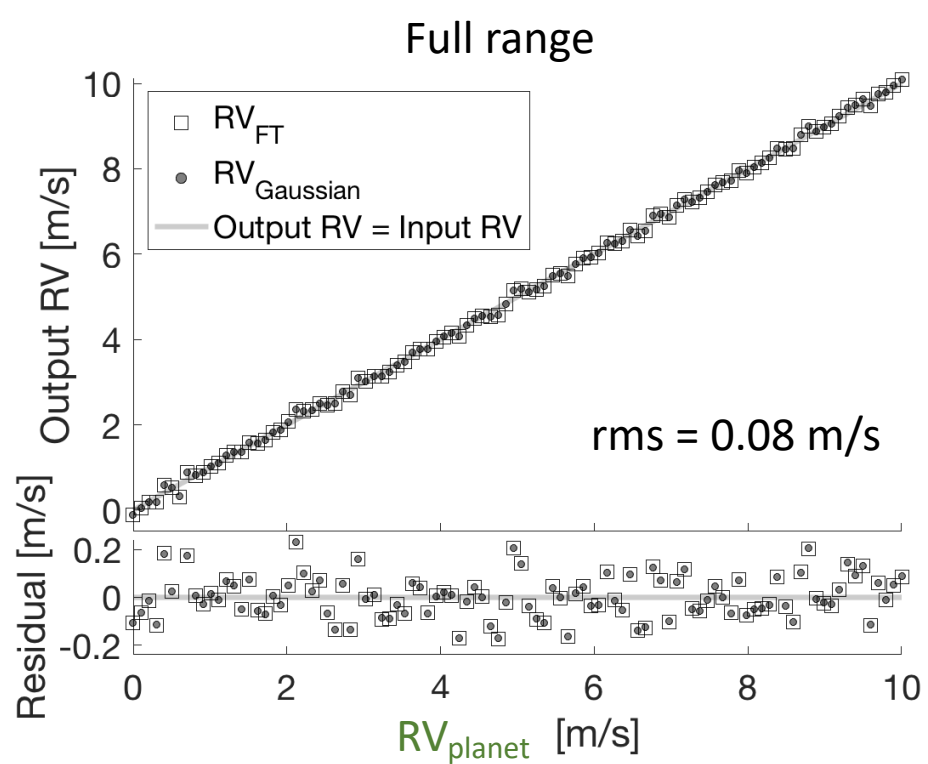
Line Shift – Velocity Domain

SOAP simulator (Boisse et al. 2012; Dumusque et al. 2014)



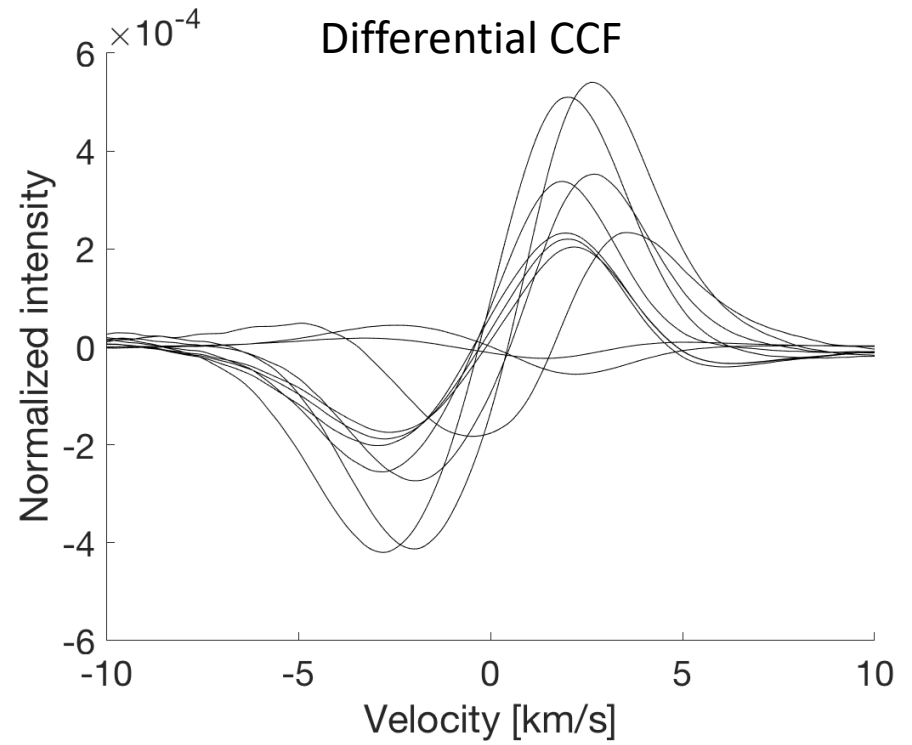
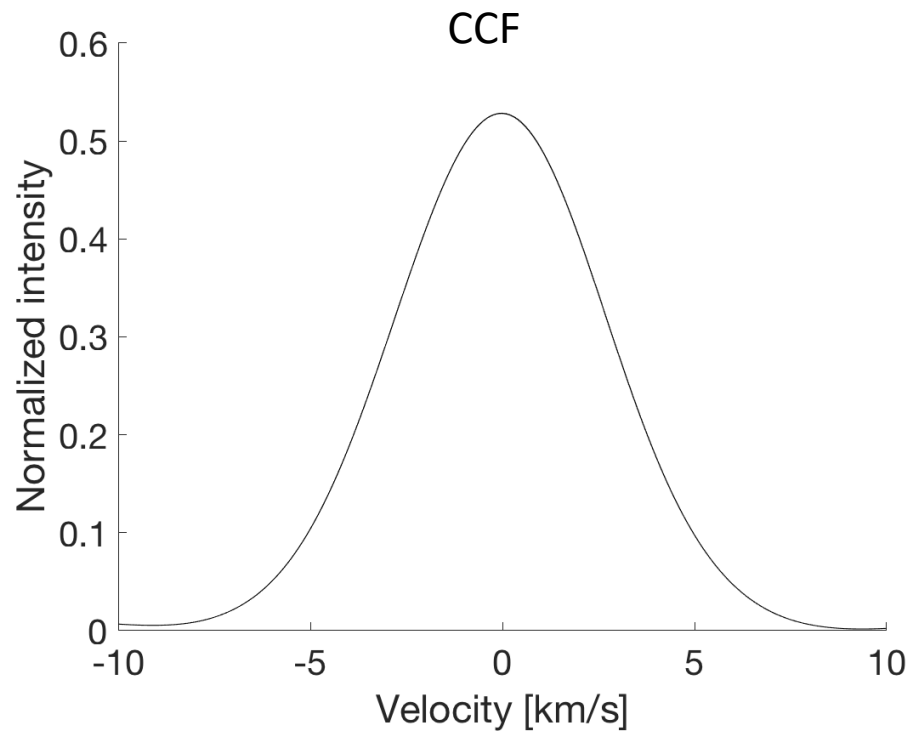


Line Shift – Inverse Velocity Domain



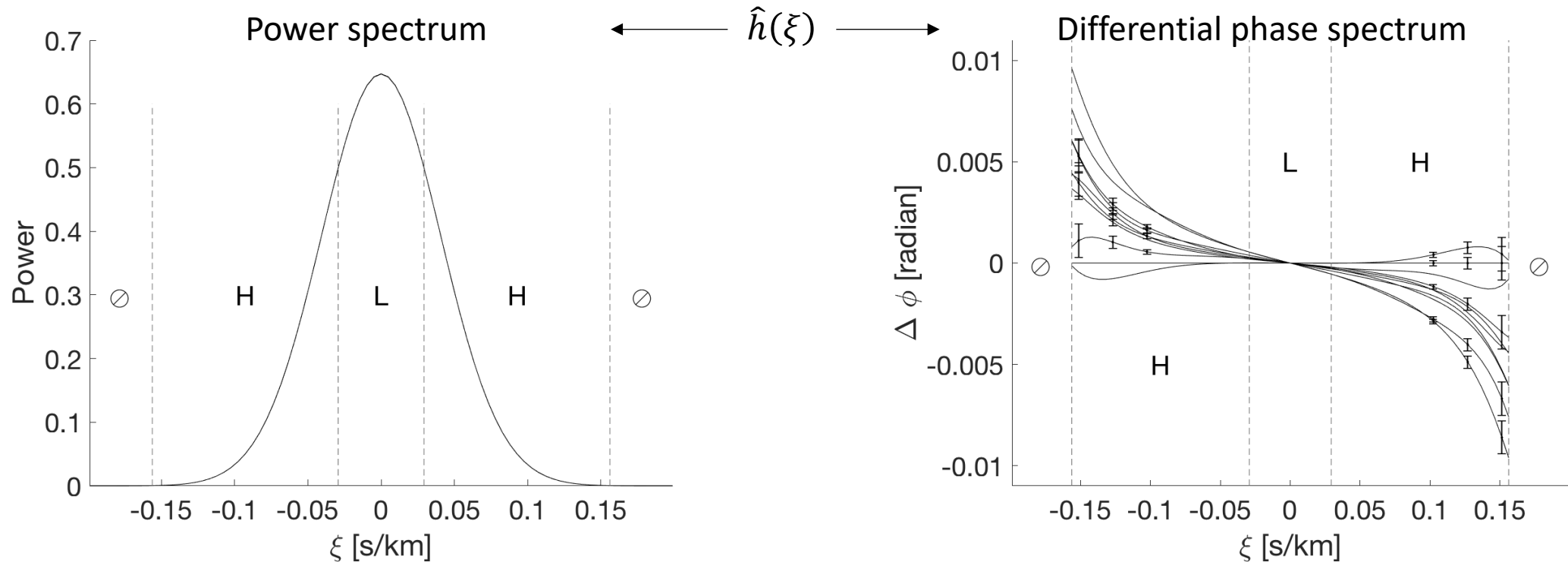
# Line Shift – $\phi$ ESTA Measurements

$$RV_{Gaussian} = RV_{FT} = RV_{FT,L} = RV_{FT,H} = RV_{planet}$$

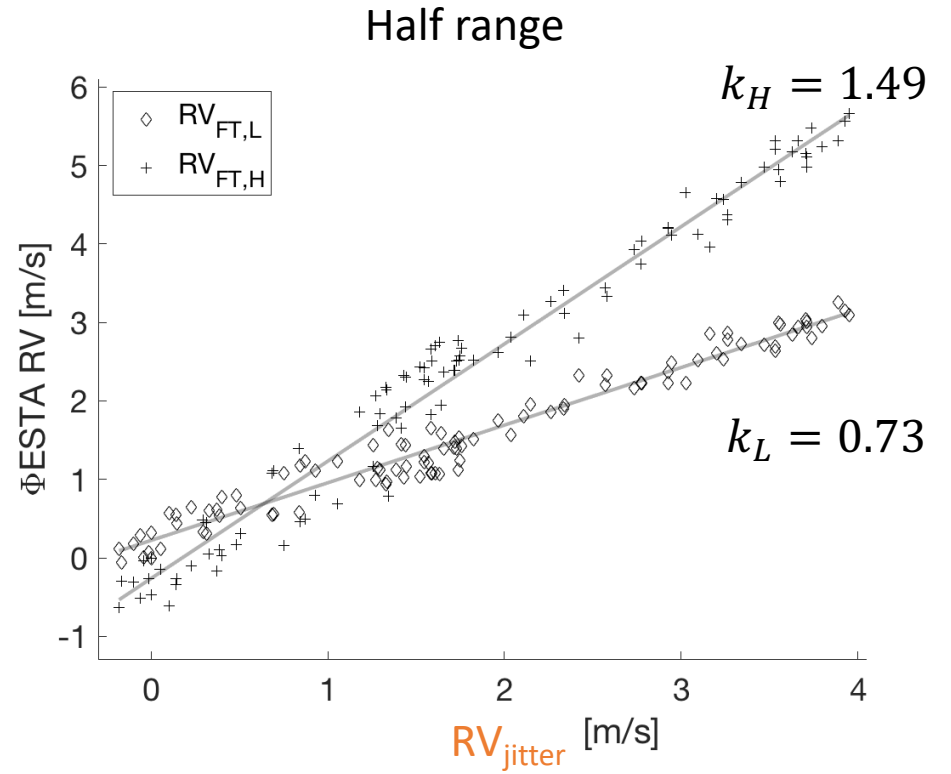
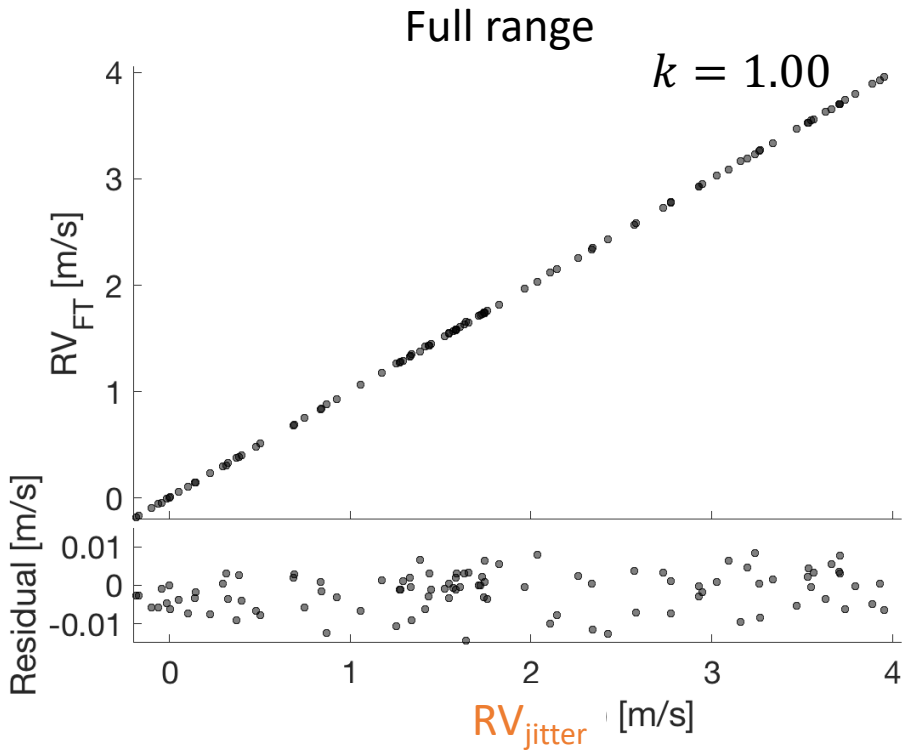


Line Deformation – Velocity Domain

SOAP simulation (3 starspots)

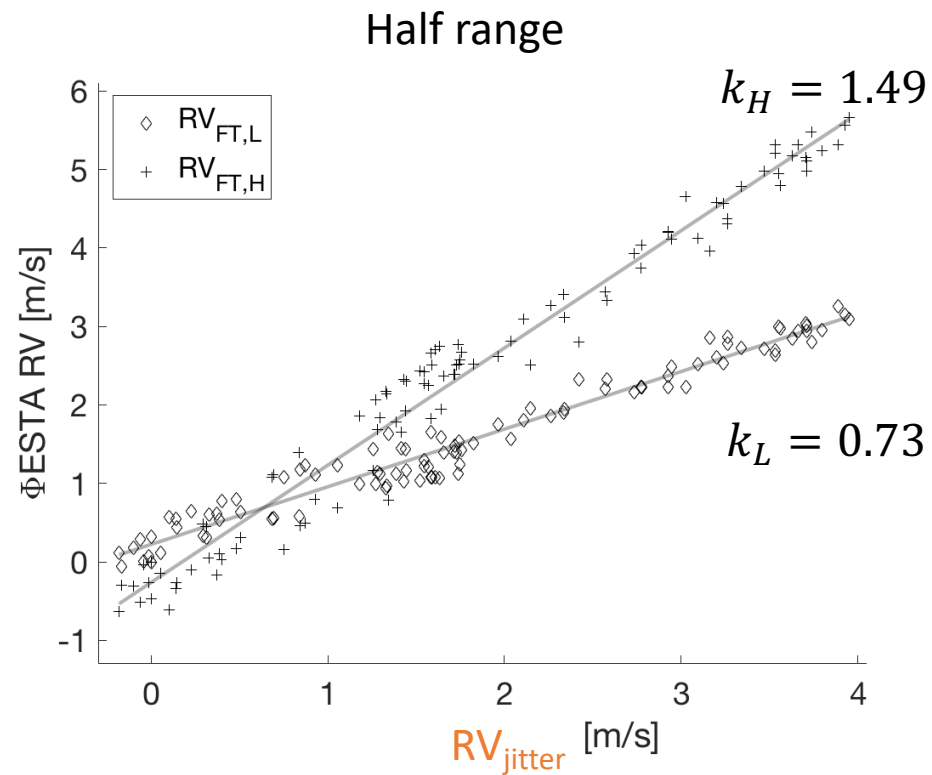
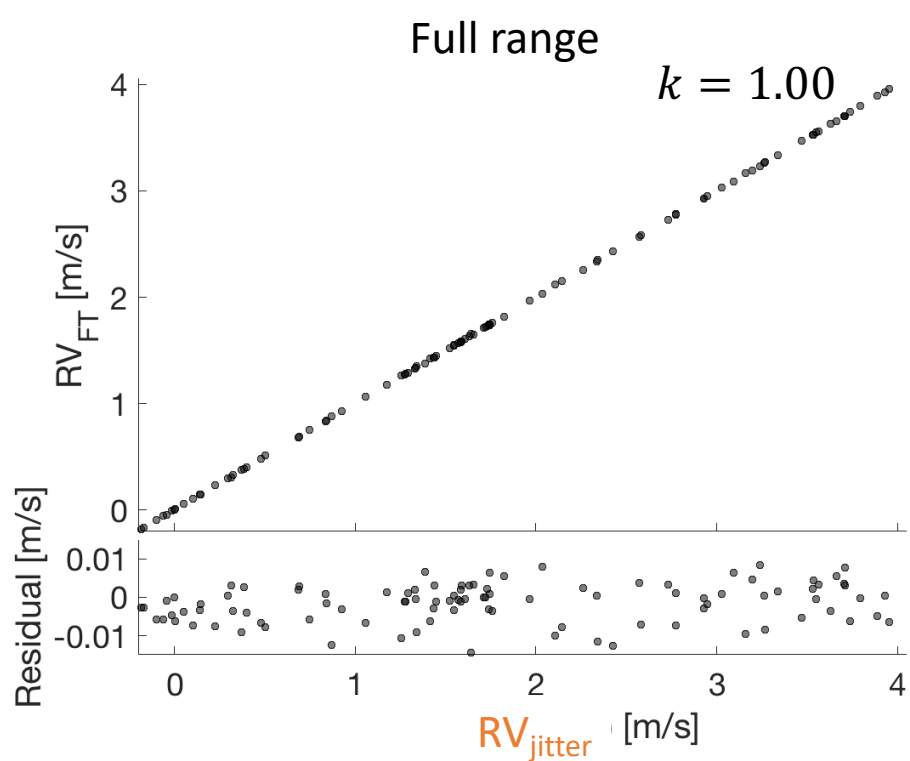


Line Deformation – Inverse Velocity Domain



## Line Deformation – $\Delta$ ESTA Measurements

$$\begin{aligned}
 RV_{FT} &= RV_{\text{Gaussian}} = RV_{\text{jitter}} \\
 RV_{FT,L} &= k_L RV_{\text{jitter}} \quad (k_L < 1) \\
 RV_{FT,H} &= k_H RV_{\text{jitter}} \quad (k_H > 1)
 \end{aligned}$$

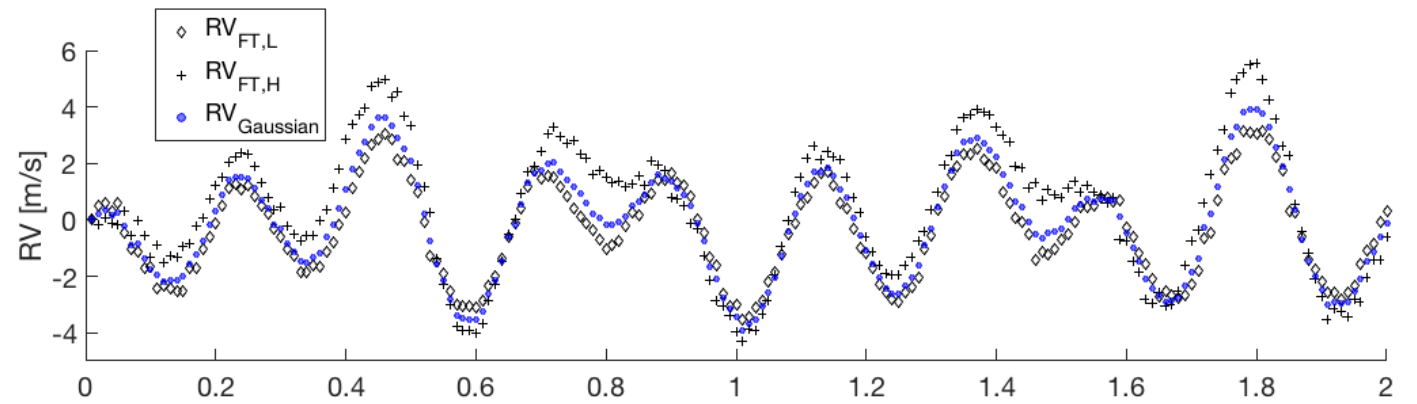


## Line Deformation – $\Delta$ ESTA Measurements

$$\begin{aligned}
 \text{RV}_{\text{FT}} &= \text{RV}_{\text{Gaussian}} = \text{RV}_{\text{jitter}} \\
 \text{RV}_{\text{FT,L}} &= k_L \text{RV}_{\text{jitter}} \quad (k_L < 1) \text{ less sensitive to jitter} \\
 \text{RV}_{\text{FT,H}} &= k_H \text{RV}_{\text{jitter}} \quad (k_H > 1) \text{ more sensitive to jitter}
 \end{aligned}$$

$$RV_{\text{Gaussian}} - RV_{\text{FT,L}} \propto RV_{\text{jitter}}$$

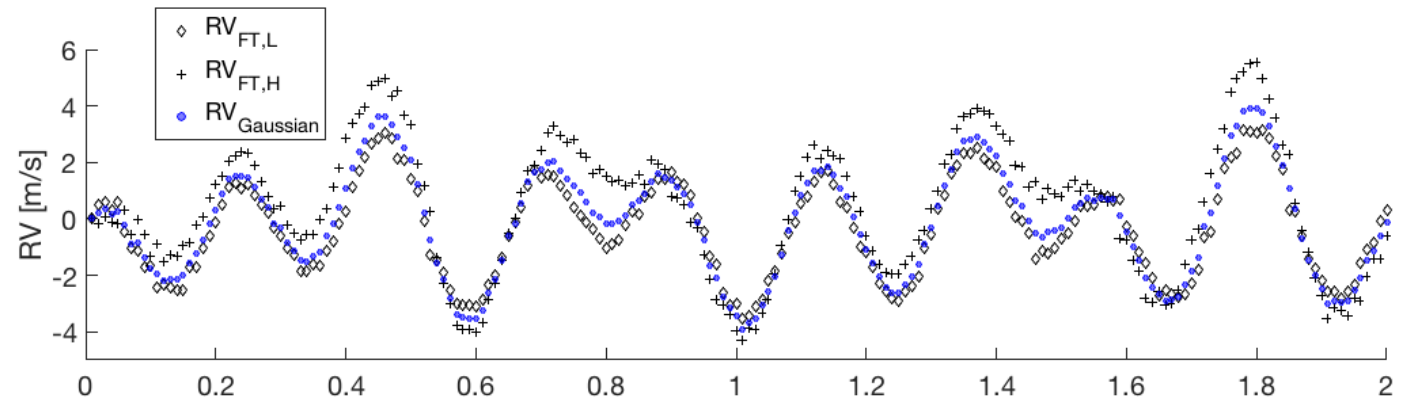
$$RV_{\text{FT,H}} - RV_{\text{Gaussian}} \propto RV_{\text{jitter}}$$



Stellar rotation phase

# $\Phi$ ESTA Jitter Metrics

- $\Delta RV_L = RV_{\text{Gaussian}} - RV_{\text{FT,L}} \propto RV_{\text{jitter}}$
- $\Delta RV_H = RV_{\text{FT,H}} - RV_{\text{Gaussian}} \propto RV_{\text{jitter}}$

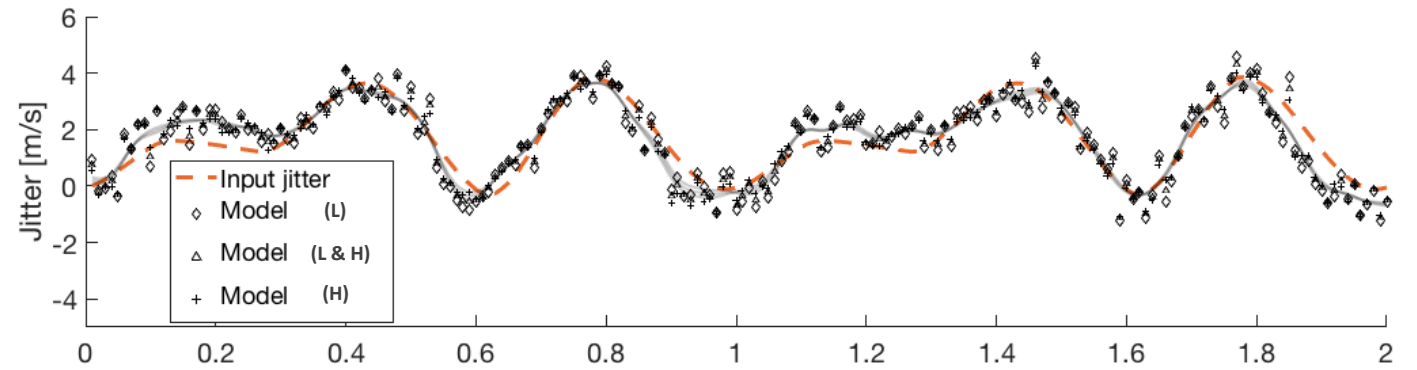
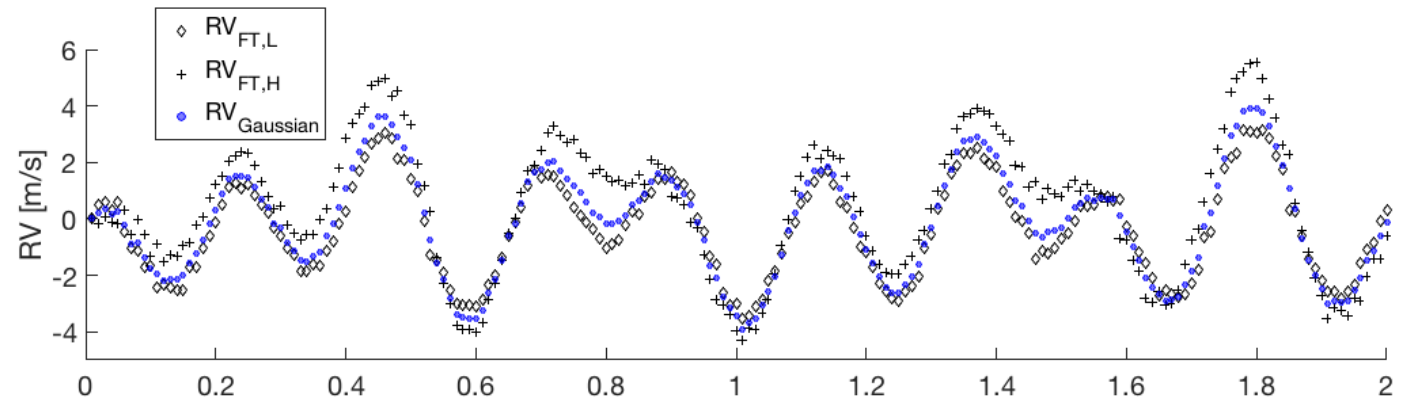


Stellar rotation phase



# $\Phi$ ESTA Jitter Model

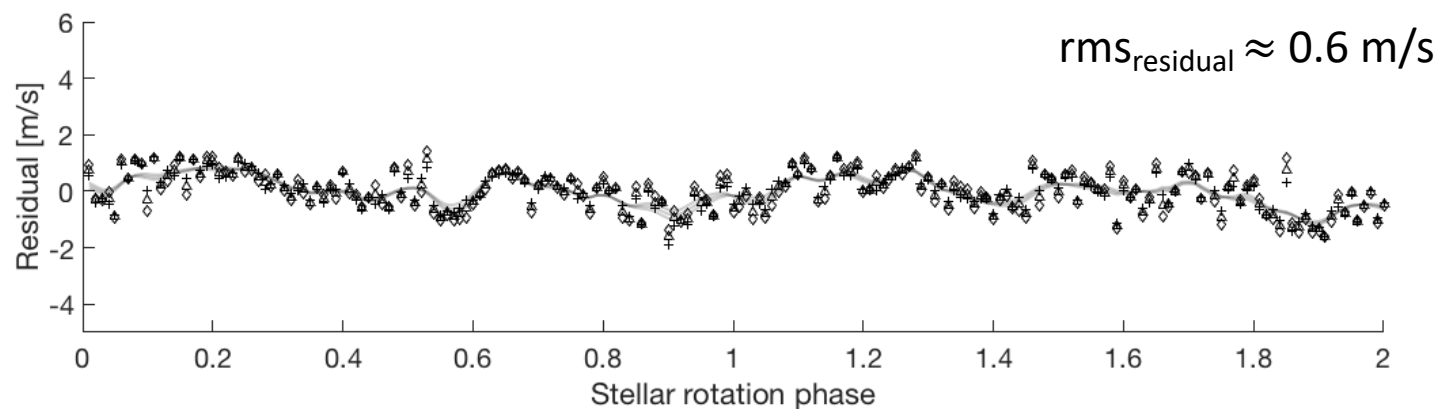
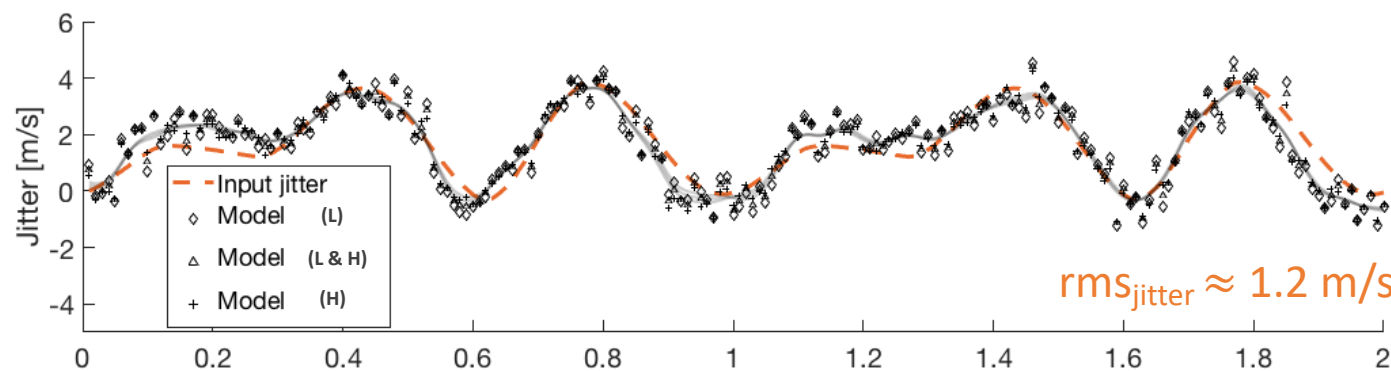
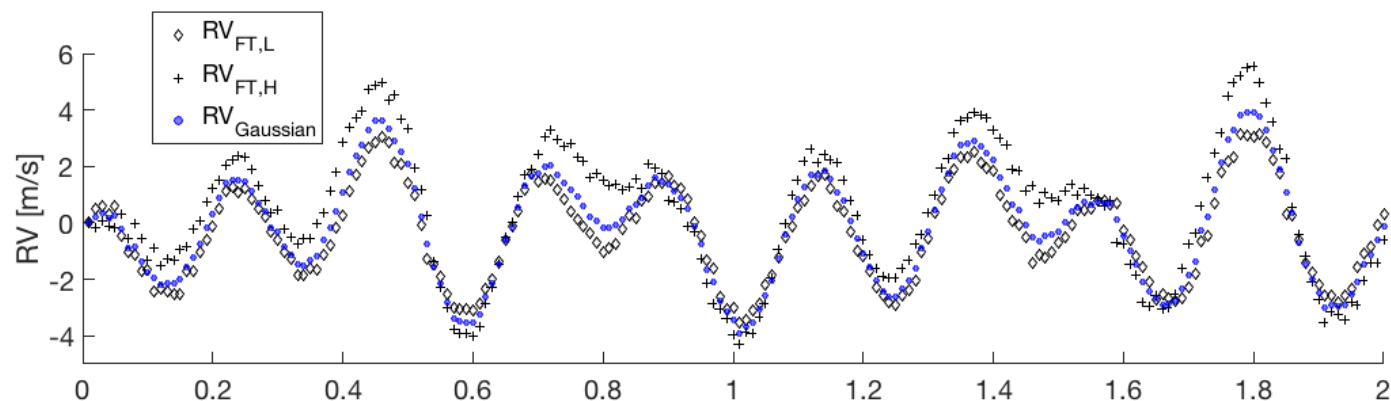
- $\Delta RV_L = RV_{\text{Gaussian}} - RV_{\text{FT,L}} \propto RV_{\text{jitter}}$
- $\Delta RV_H = RV_{\text{FT,H}} - RV_{\text{Gaussian}} \propto RV_{\text{jitter}}$
- Linear combination of  $\Delta RV_L$  and  $\Delta RV_H \propto RV_{\text{jitter}}$



Stellar rotation phase

# $\Phi$ ESTA Jitter Model

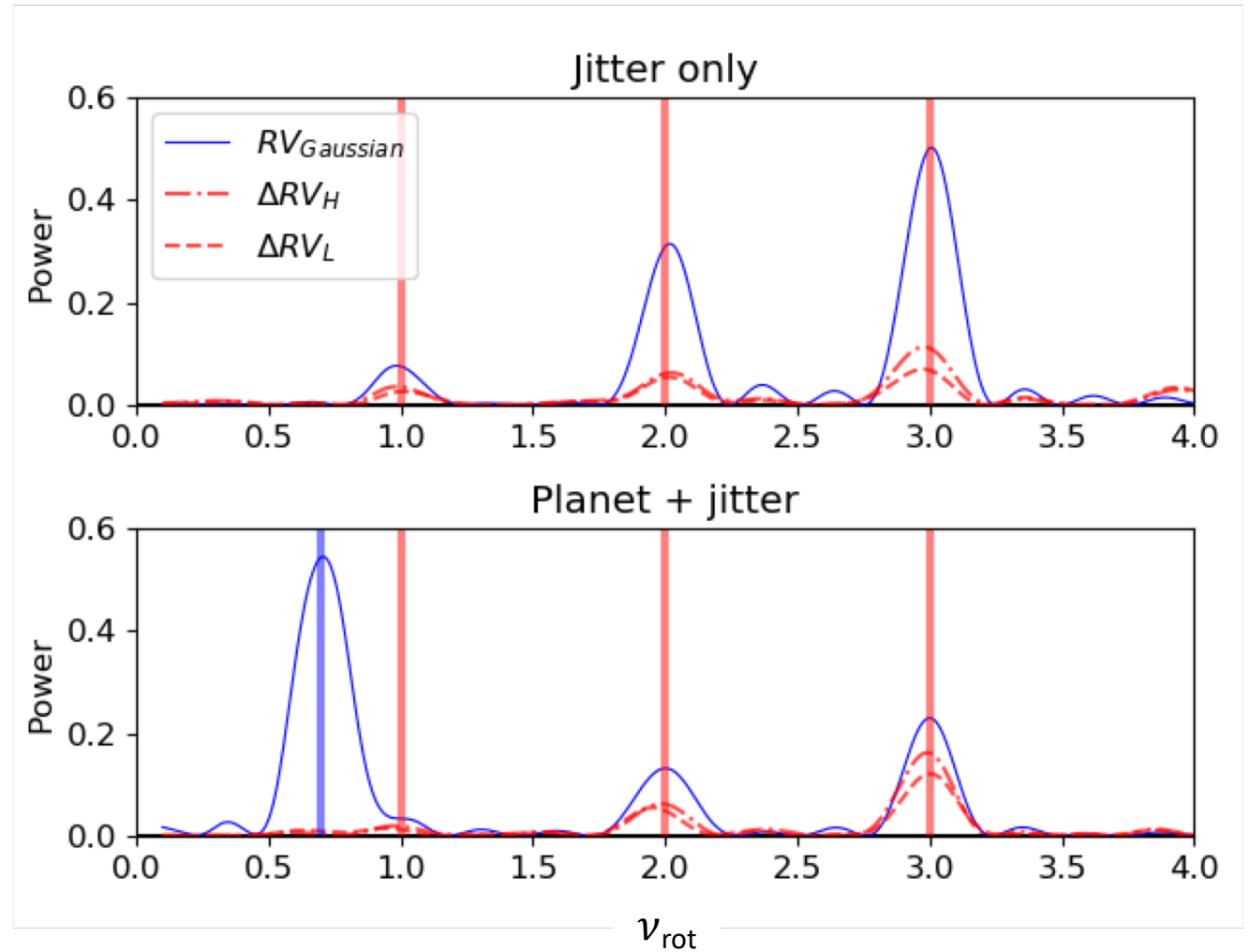
- $\Delta RV_L = RV_{\text{Gaussian}} - RV_{\text{FT,L}} \propto RV_{\text{jitter}}$
- $\Delta RV_H = RV_{\text{FT,H}} - RV_{\text{Gaussian}} \propto RV_{\text{jitter}}$
- Linear combination of  $\Delta RV_L$  and  $\Delta RV_H \propto RV_{\text{jitter}}$



# Application

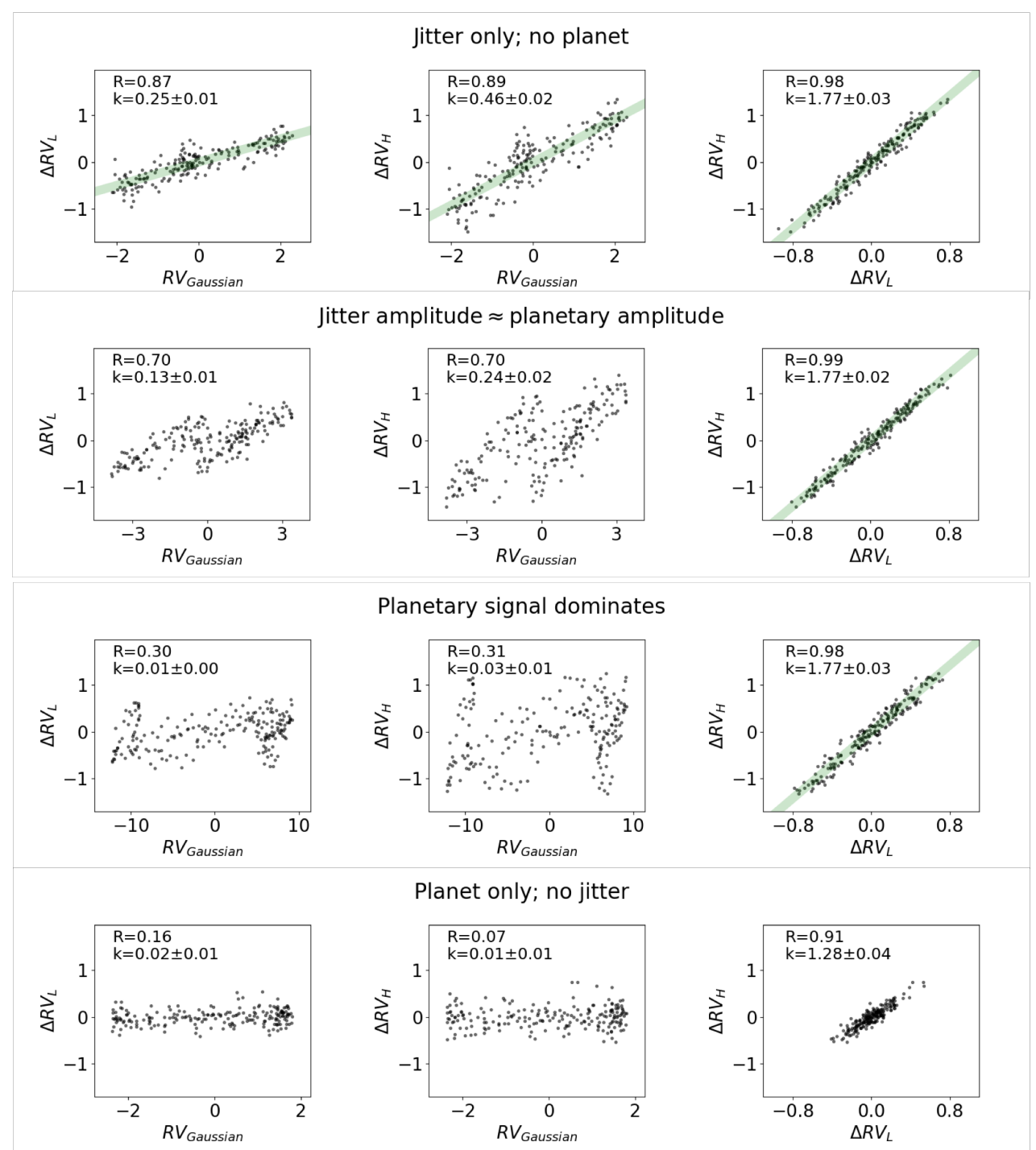
## Periodogram Analysis

- Stellar jitter: 3 spots
- Input  $v_{\text{orb}} = 0.7 v_{\text{rot}}$
- CCF S/N = 2,000 (SNR  $\sim$  50/pixel)



# Application Classifications

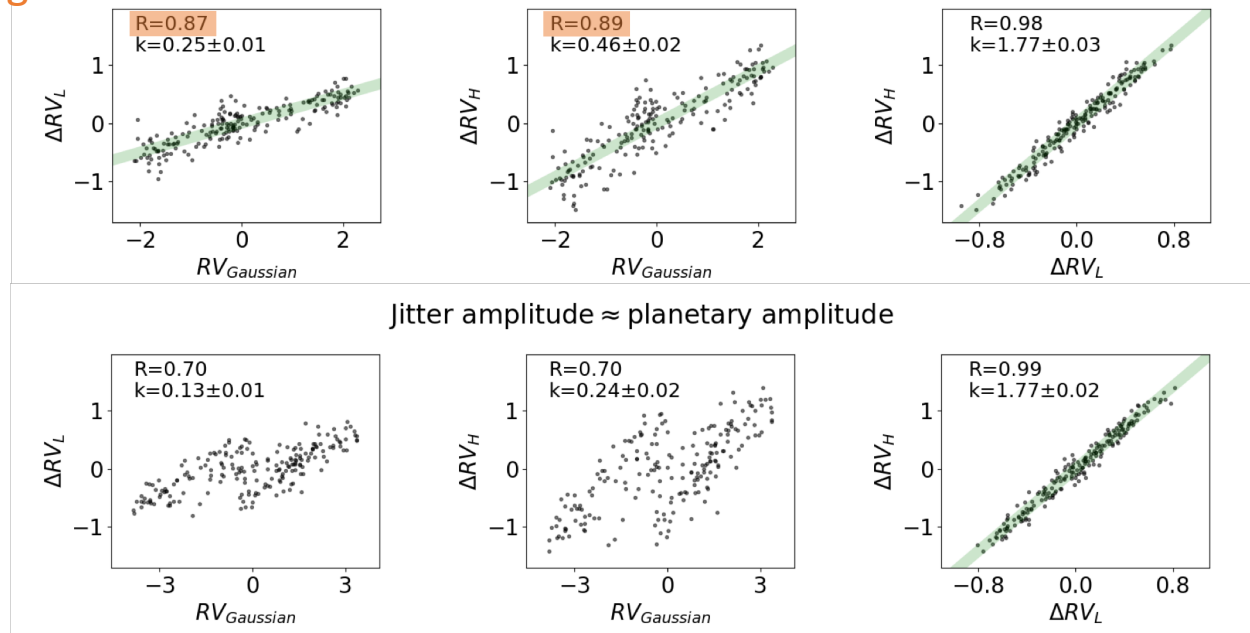
- Jitter amplitude  $\approx 2$  m/s
- $RV_{\text{planet}}$  amplitude = 0, 2, 10 m/s
- CCF S/N = 10,000



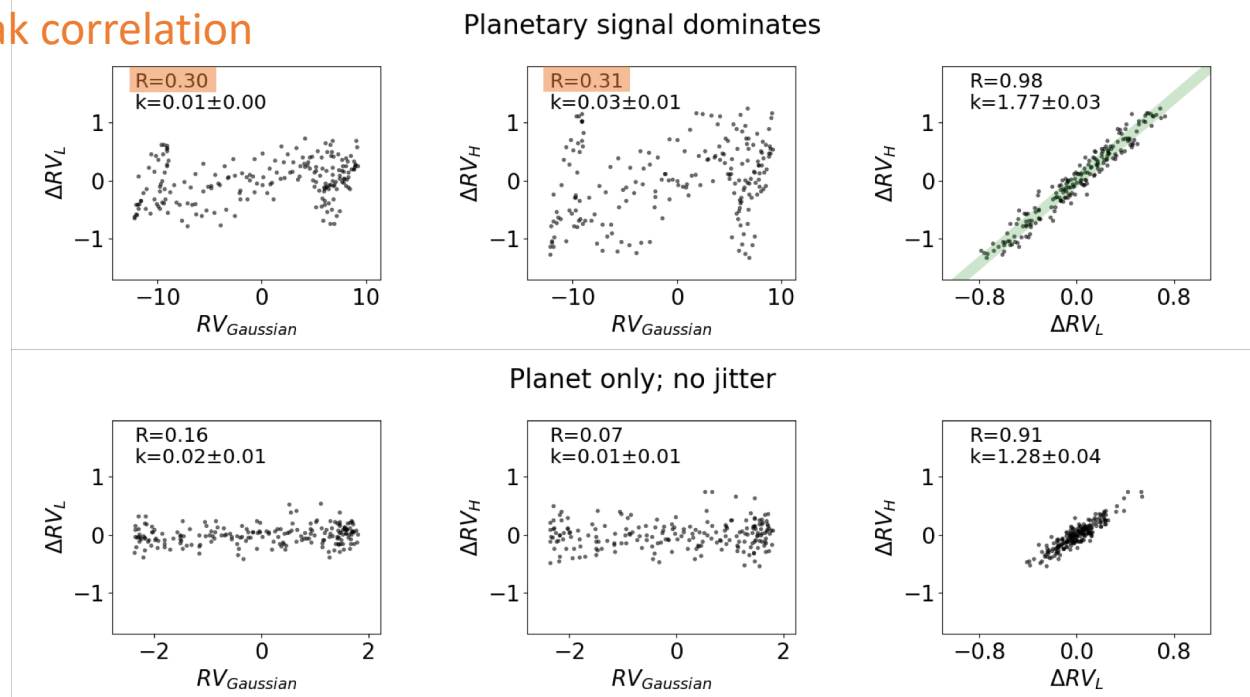
# Application Classifications

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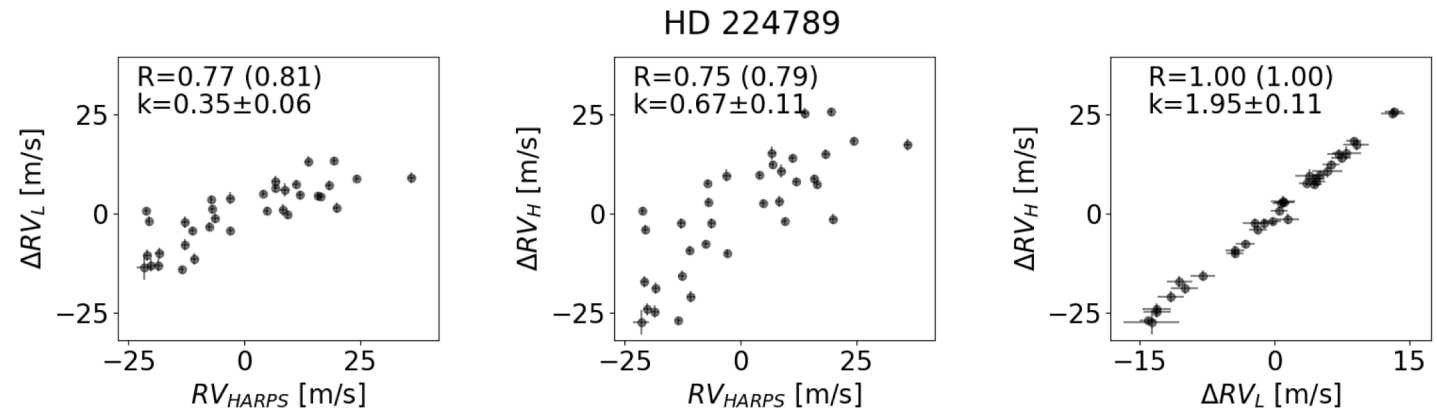
## Strong correlation



## Weak correlation



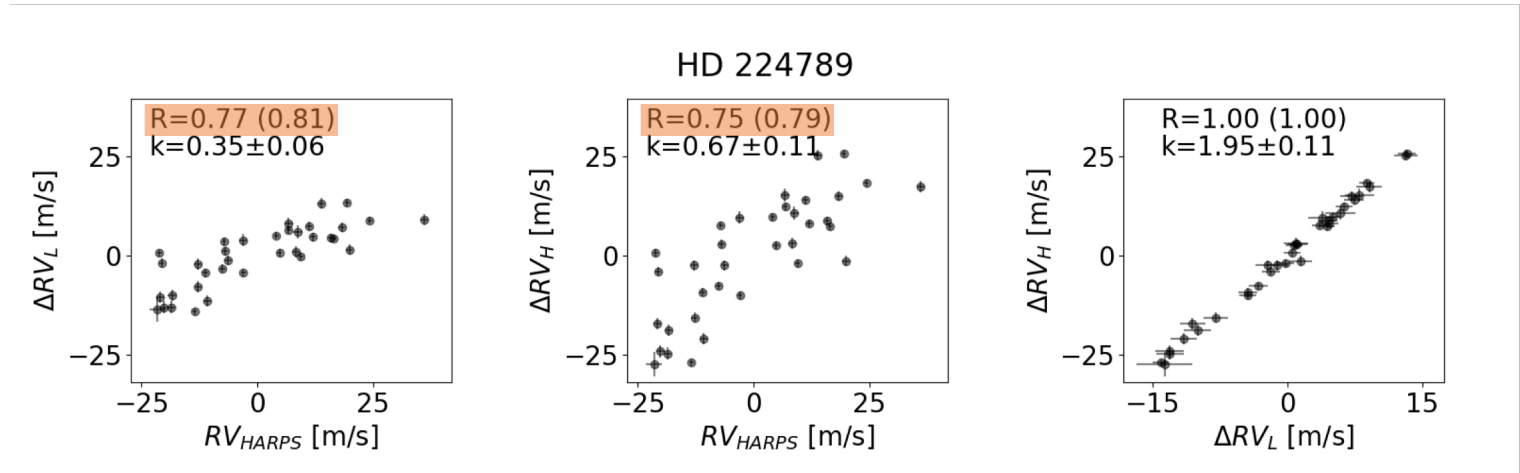
ΦESTA on  
HARPS  
*An Active  
Star*



- $\text{Log } R'_{HK} = -4.46$  (Figueira et al. 2013)
- Jitter amplitude  $\sim 30$  m/s
- CCF S/N  $\sim 4000$ ; HARPS SNR = 106/pixel
- Median  $RV_{\text{noise}} = 0.63$  m/s

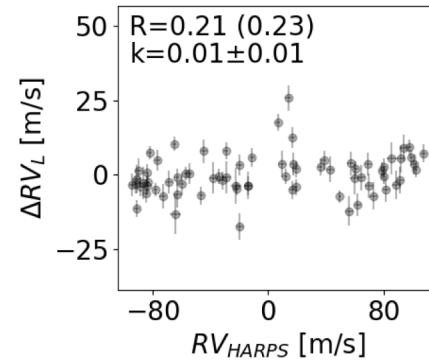
ΦESTA on  
HARPS  
*An Active  
Star*

Strong correlation due to stellar jitter

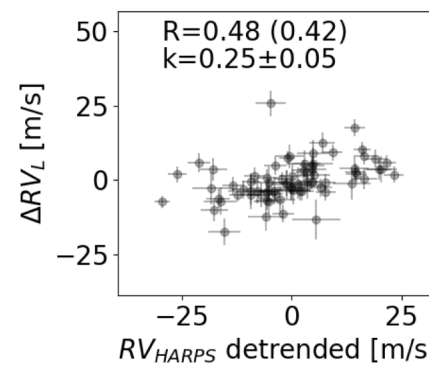
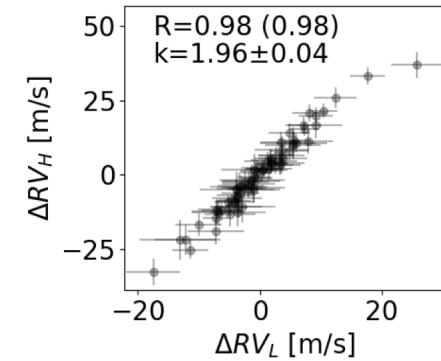
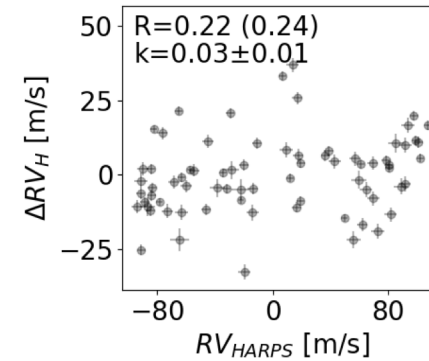


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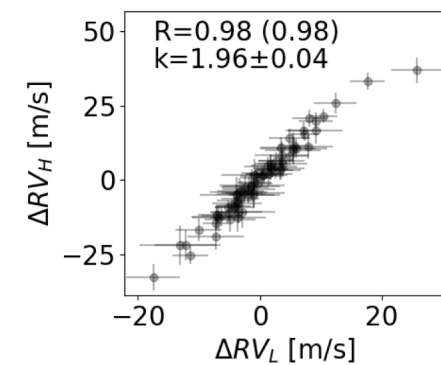
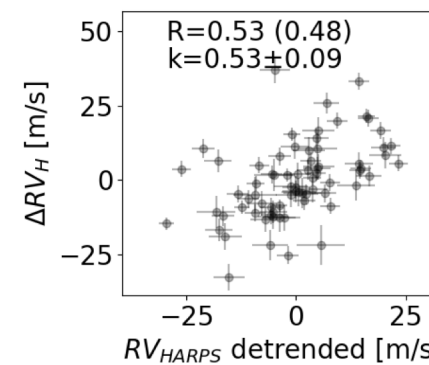
$\Phi$ ESTA on  
HARPS  
An Active  
Planet-host  
Star



HD 103720 (planet not removed)



HD 103720 (planet removed)

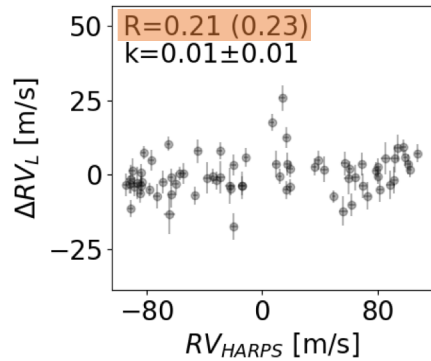


- $\text{Log } R'_{\text{HK}} = -4.46$  (Figueira et al. 2013)
- Planetary orbital amplitude  $\sim 80$  m/s; jitter amplitude  $\sim 9$  m/s (Moutou et al. 2015)
- CCF S/N  $\sim 1400$ ; HARPS SNR = 35/pixel
- Median  $\text{RV}_{\text{noise}} = 2$  m/s

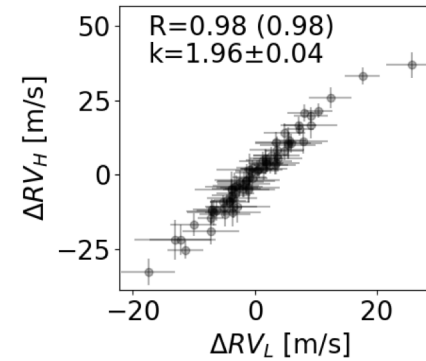
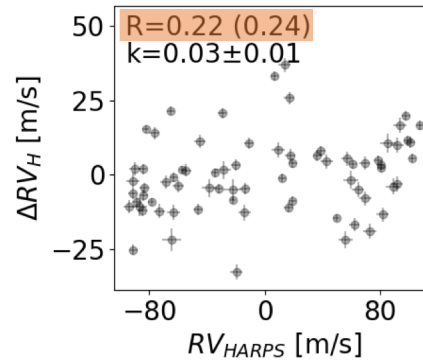


$\Phi$ ESTA on  
HARPS  
An Active  
Planet-host  
Star

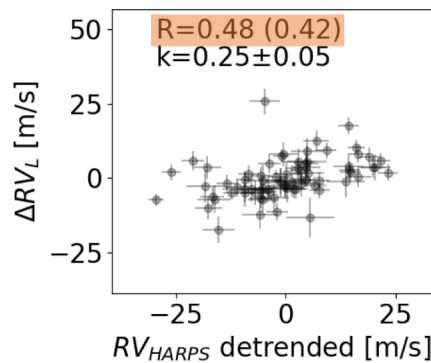
Weak correlation



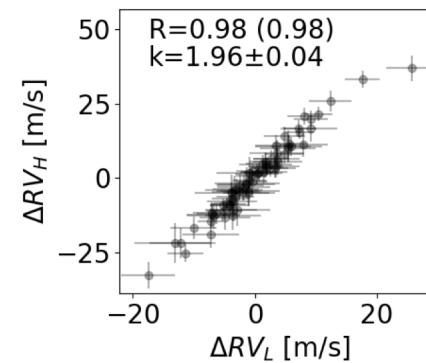
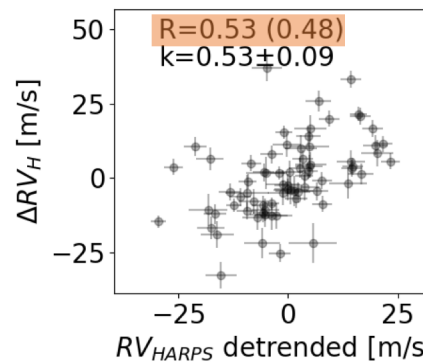
HD 103720 (planet not removed)



Moderate correlation

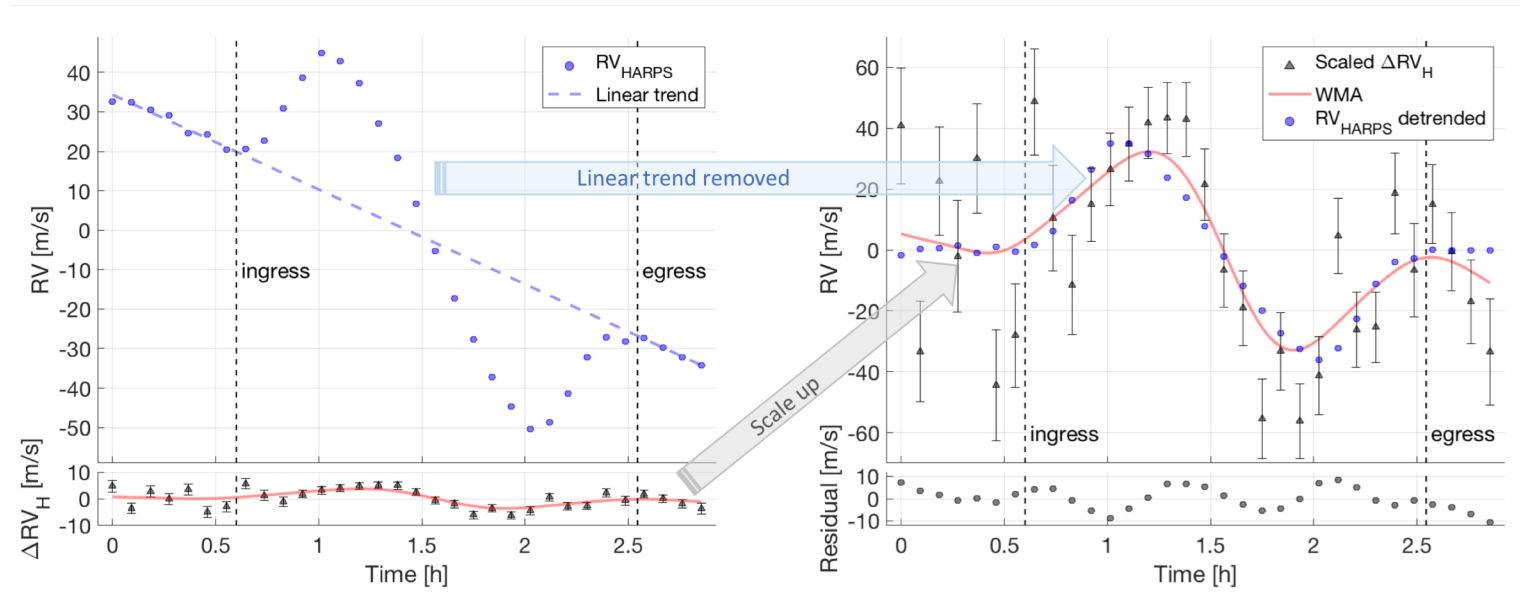


HD 103720 (planet removed)



- $\text{Log } R'_{\text{HK}} = -4.46$  (Figueira et al. 2013)
- Planetary orbital amplitude  $\sim 80$  m/s; jitter amplitude  $\sim 9$  m/s (Moutou et al. 2015)
- CCF S/N  $\sim 1400$ ; HARPS SNR = 35/pixel
- Median  $\text{RV}_{\text{noise}} = 2$  m/s

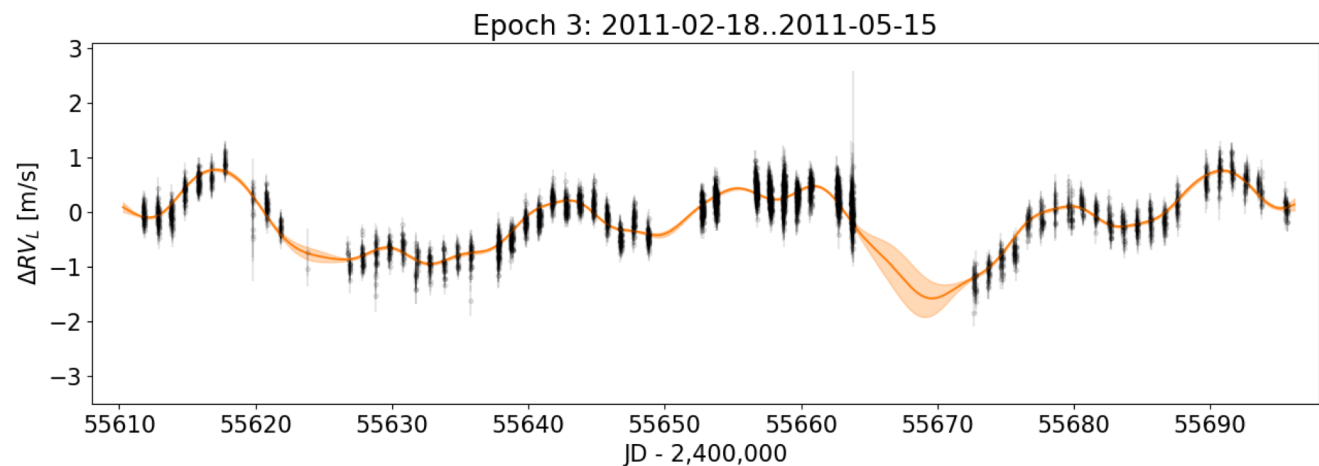
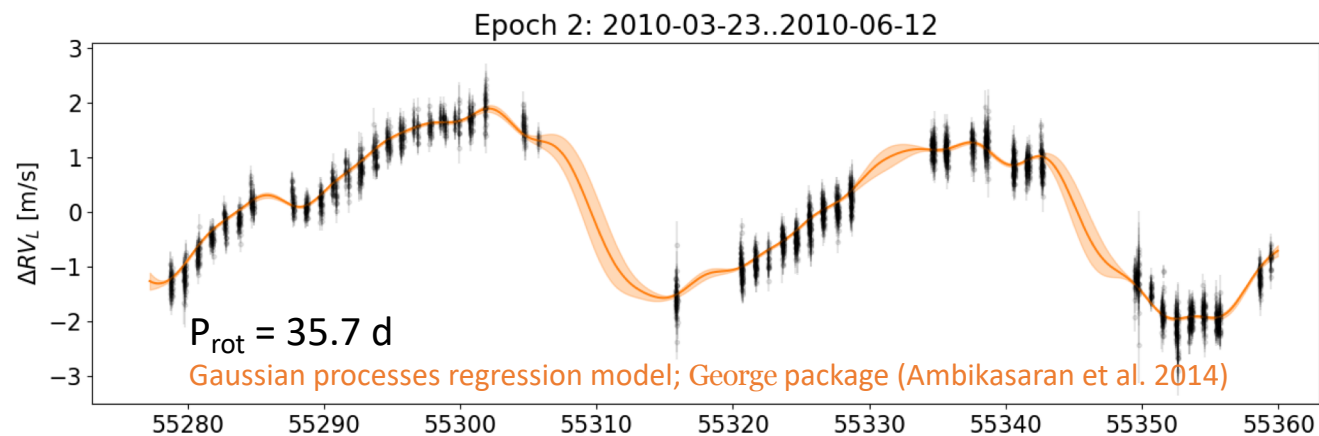
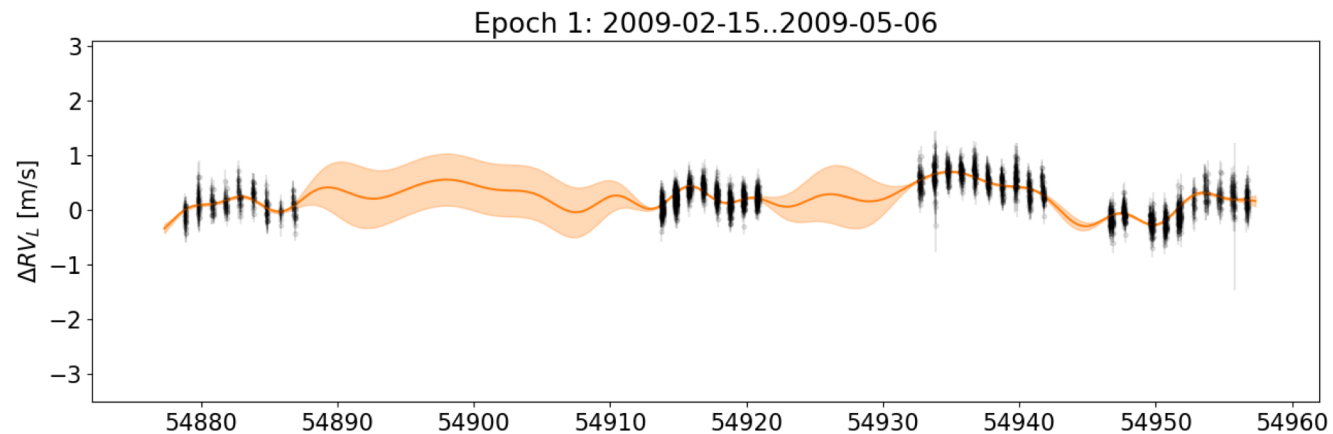
$\Phi$ ESTA on  
HARPS  
Rossiter-  
McLaughlin  
effect



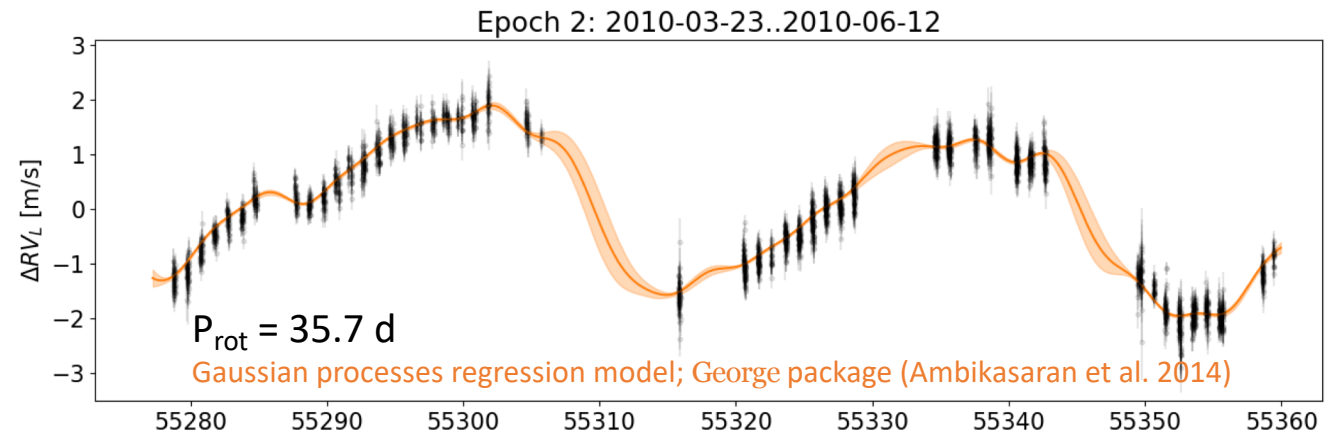
- Linear trend: binary (HD 189733 B) + exoplanet (HD 189733 b)
- Rossiter-McLaughlin velocity anomaly amplitude  $\sim 40$  m/s
- $\Phi$ ESTA jitter model constructed with  $\Delta RV_H$
- Residual amplitude  $\sim 10$  m/s

$\Phi$ ESTA on  
HARPS  
 *$\alpha$  Centauri B*

The  $\Delta RV_L$  in this slide was computed using an older version of  $\Phi$ ESTA; the scale can be slightly different but the trends of jitter metrics remain consistent with the latest version.



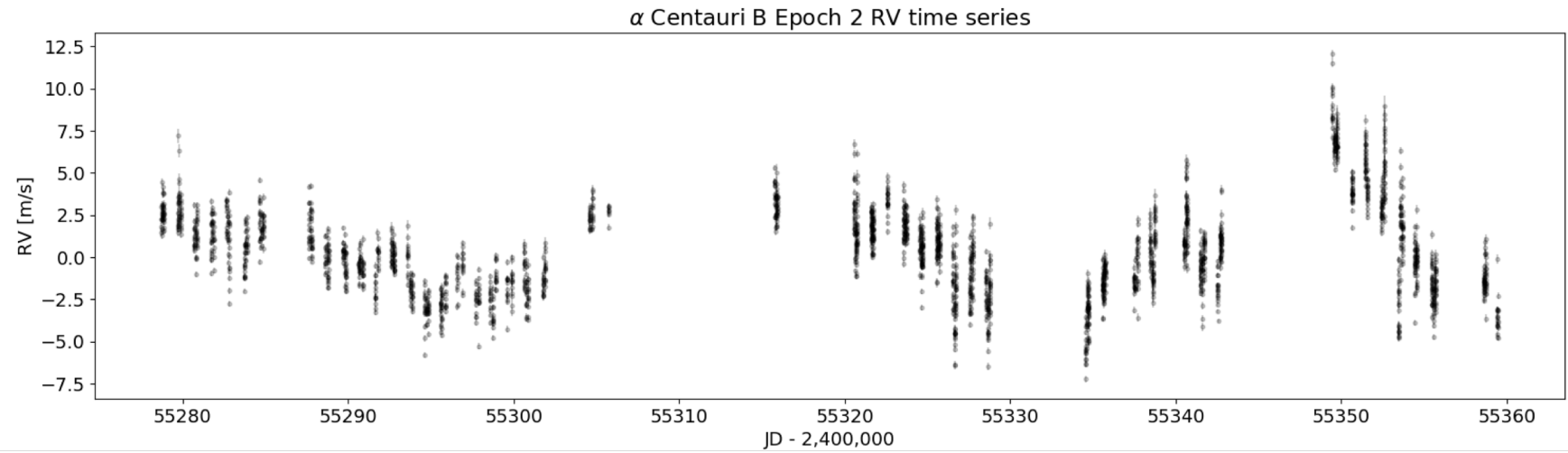
ΦESTA on  
HARPS  
*α Centauri B*



- > 2400 observations
- CCF S/N  $\sim 10,000$ ; HARPS SNR = 250/pixel
- Median  $RV_{\text{noise}} = 0.2 \text{ m/s}$

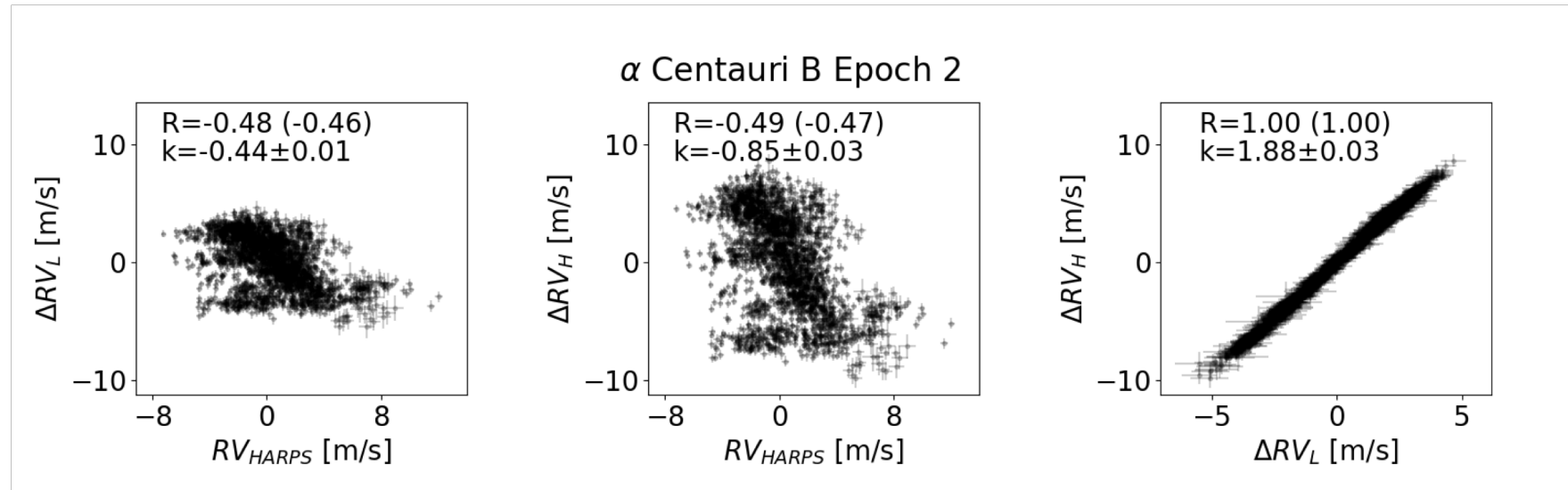
The  $\Delta RV_L$  in this slide was computed using an older version of  $\Phi$ ESTA; the scale can be slightly different but the trends of jitter metrics remain consistent with the latest version.

ΦESTA on  
HARPS  
*α Centauri B*



- Binary removed (2<sup>nd</sup> order polynomial, Dumusque et al. 2012)
- Linear trend corrected

$\Phi$ ESTA on  
HARPS  
 *$\alpha$  Centauri B*



- Planet candidate orbiting  $\alpha$  Centauri B?
- Binary not corrected removed / systematics?
- Correlation between  $\Phi$ ESTA jitter metrics and stellar jitter can be non-linear?

# Summary

- $\Phi$ ESTA measurement of line deformation  $x_0(\xi)$

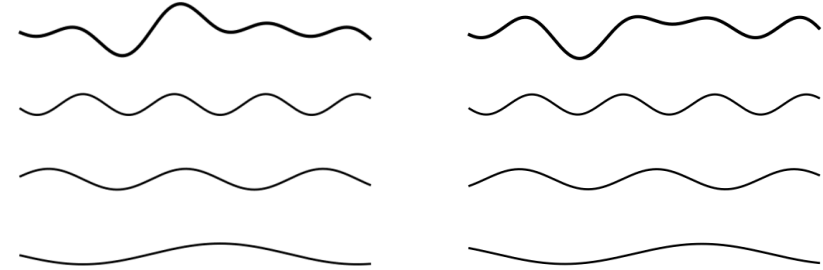
- $RV_{FT,L} = k_L RV_{jitter}$  ( $k_L < 1$ )
- $RV_{FT,H} = k_H RV_{jitter}$  ( $k_H > 1$ )

- $\Phi$ ESTA jitter metrics

- $\Delta RV_L = RV_{Gaussian} - RV_{FT,L} \propto (1/4) RV_{jitter}$
- $\Delta RV_H = RV_{FT,H} - RV_{Gaussian} \propto (1/2) RV_{jitter}$

- Application

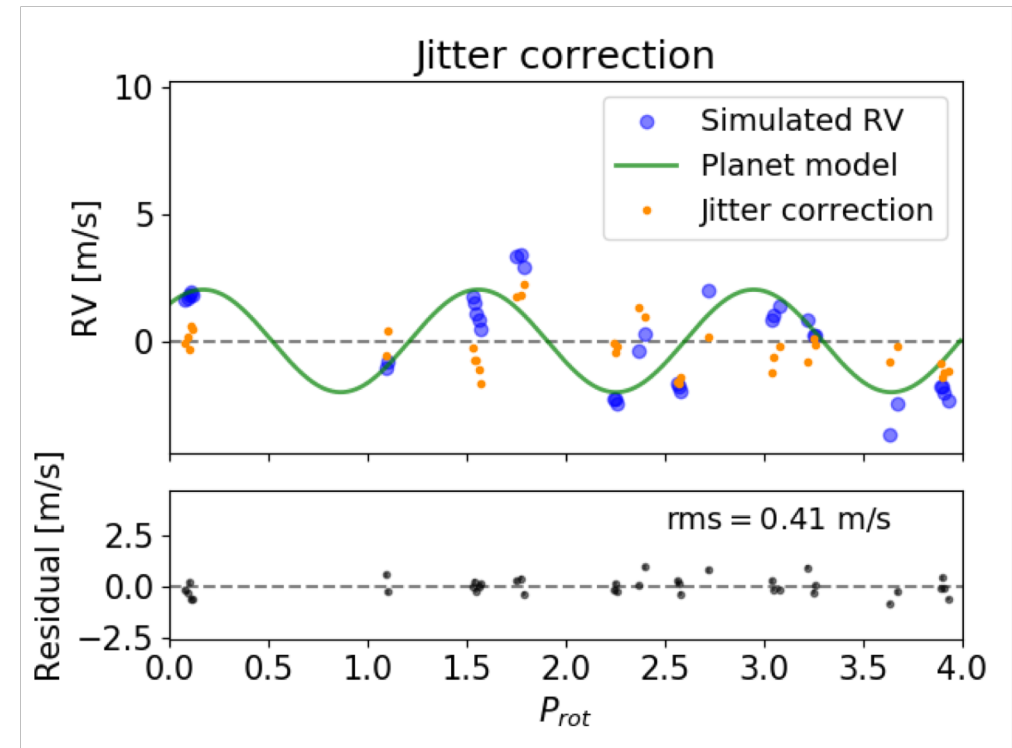
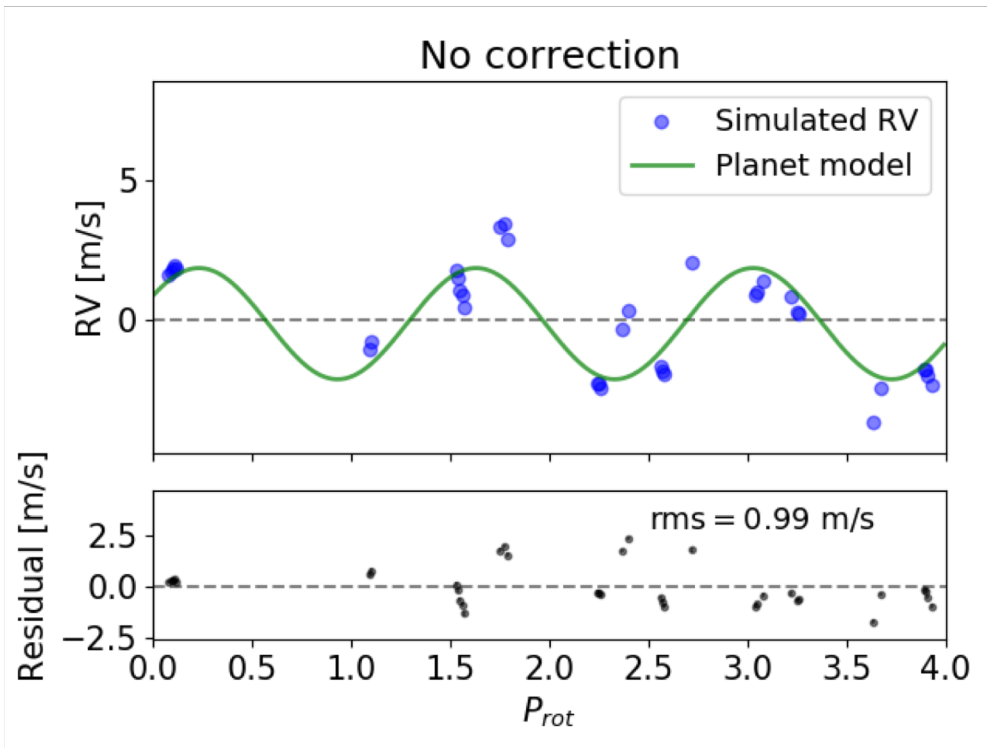
- Periodogram analysis (activity indicator)
- Classifications (linearity)
  - Active star (HD 224789)
  - Active planet-host star (HD 103720)
  - Rossiter-McLaughlin effect (HD 189733)
  - $\alpha$  Centauri B – remain unsolved



- Collaborations?
- Postdoc positions?
- [jinglin.zhao1@unsw.edu.au](mailto:jinglin.zhao1@unsw.edu.au)

# Supplementary Material





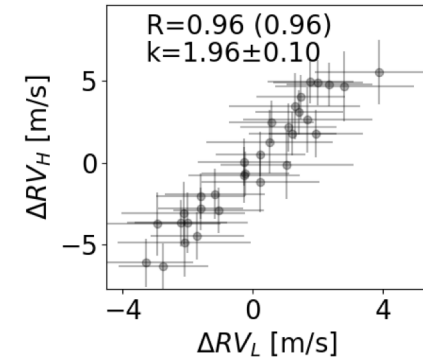
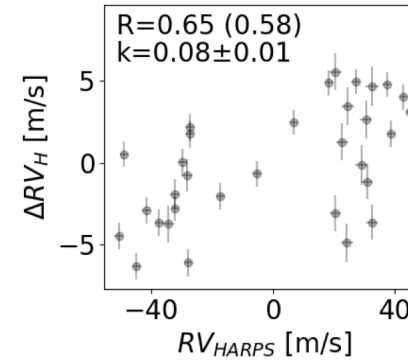
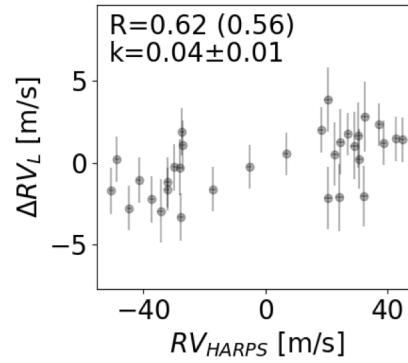
## Jitter Correction

$$RV = \text{ESTA jitter Model} + \text{Keplerian Orbits}$$

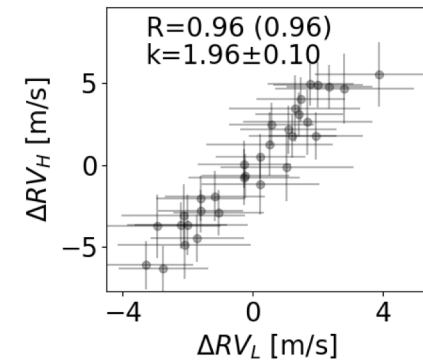
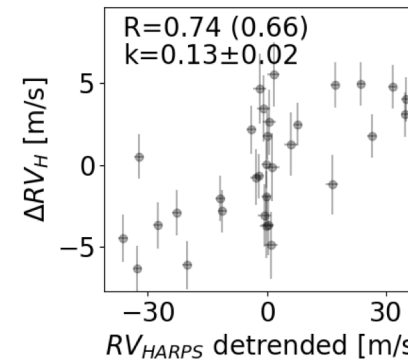
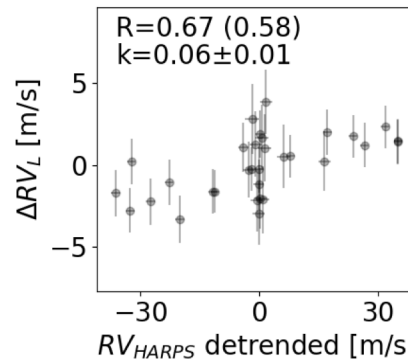
Triples the percentage of planets recovered to within 10% of input orbital parameters (Zhao & Tinney, submitted).

$\Phi$ ESTA on  
HARPS  
*Rossiter-McLaughlin*  
*effect*

HD 189733 (companions not removed)



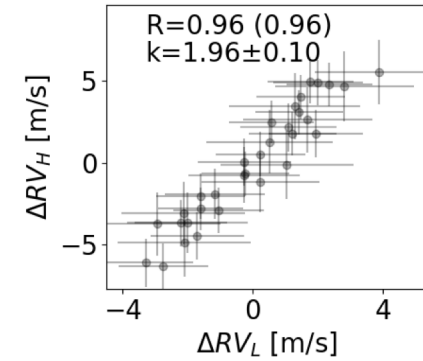
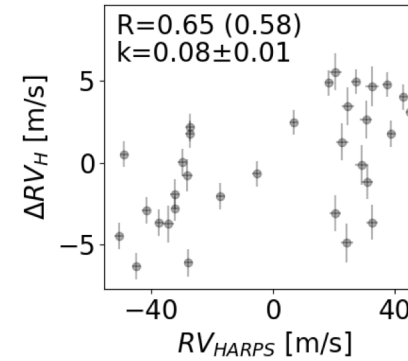
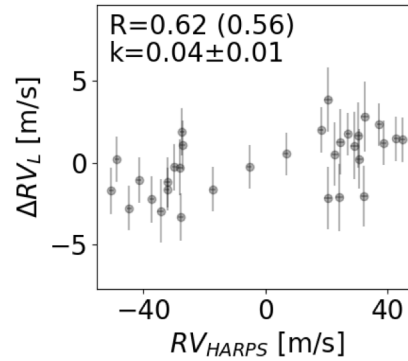
HD 189733 (companions removed)



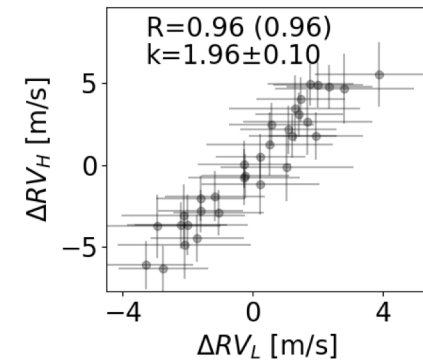
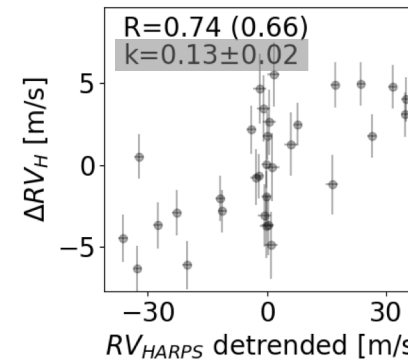
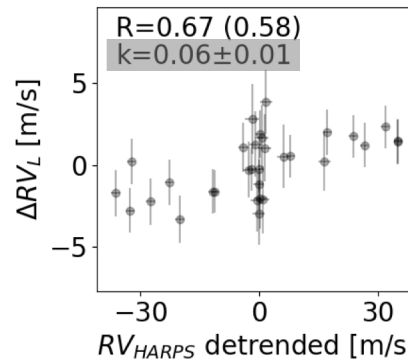
- CCF S/N  $\sim 2600$ ; HARPS SNR = 85/pixel
- Median  $RV_{\text{noise}} = 0.83$  m/s

$\Phi$ ESTA on  
HARPS  
Rossiter-  
McLaughlin  
effect

HD 189733 (companions not removed)



HD 189733 (companions removed)



- $k$  underrepresented
- $k$  dependency on spot temperature (Zhao & Tinney, submitted)