

Relativistic effects with cross-correlations

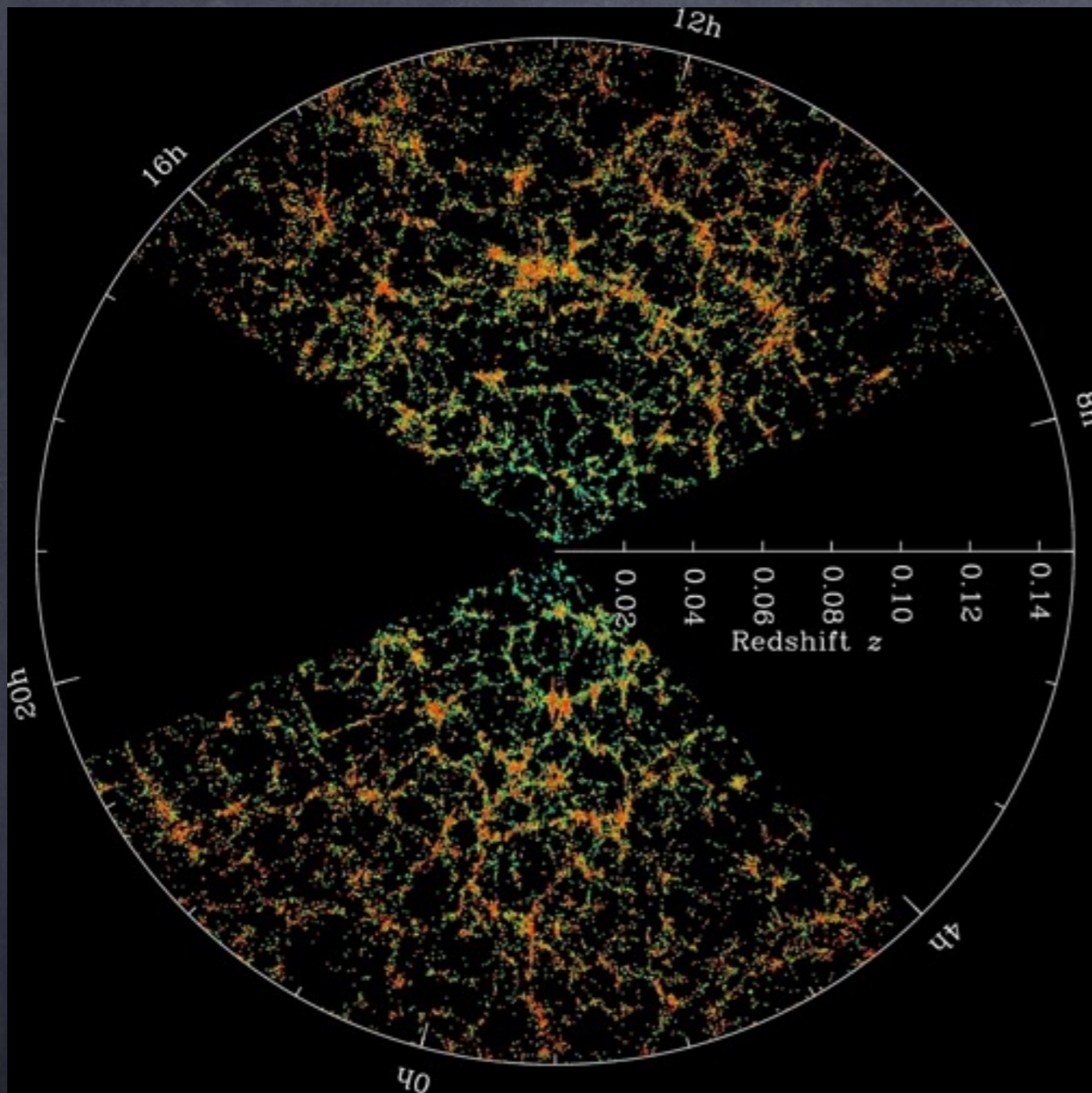
Enea Di Dio

in collaboration with
Francesco Montanari, Ruth Durrer, Julien Lesgourgues,
Matteo Viel, Vid Irsic

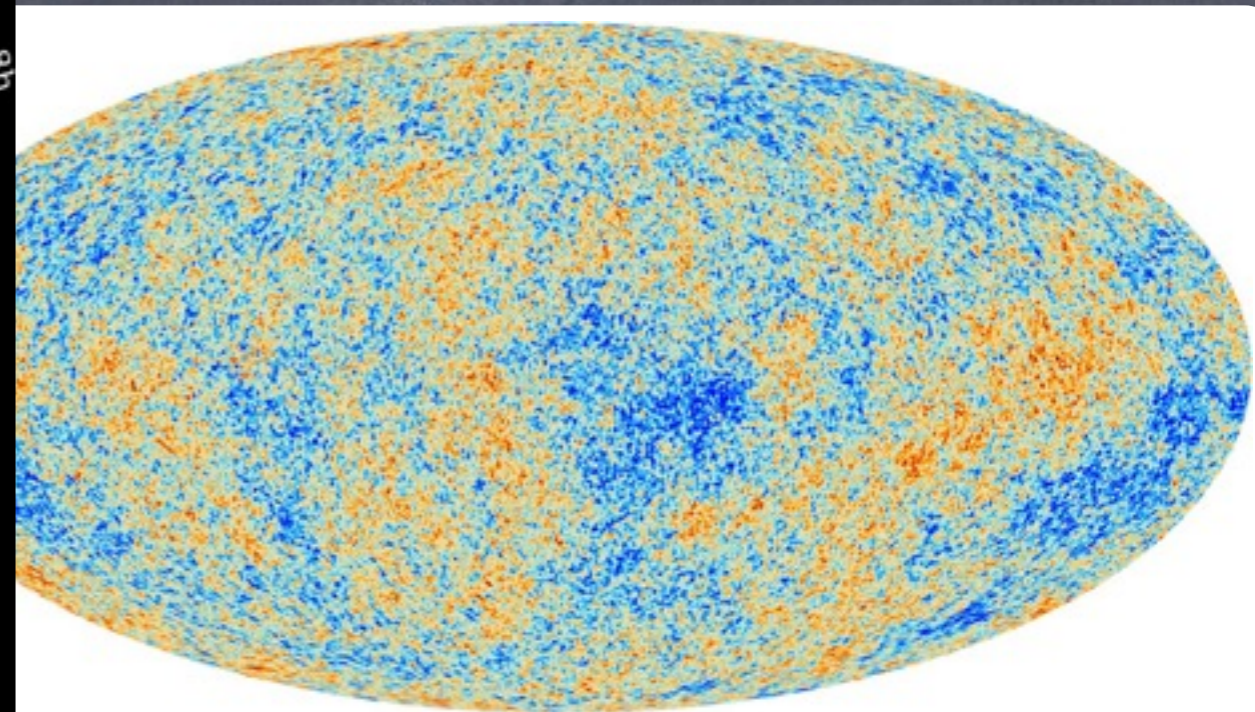
28th Texas Symposium on
Relativistic Astrophysics

Geneva, 14 December

Large Scale Structures



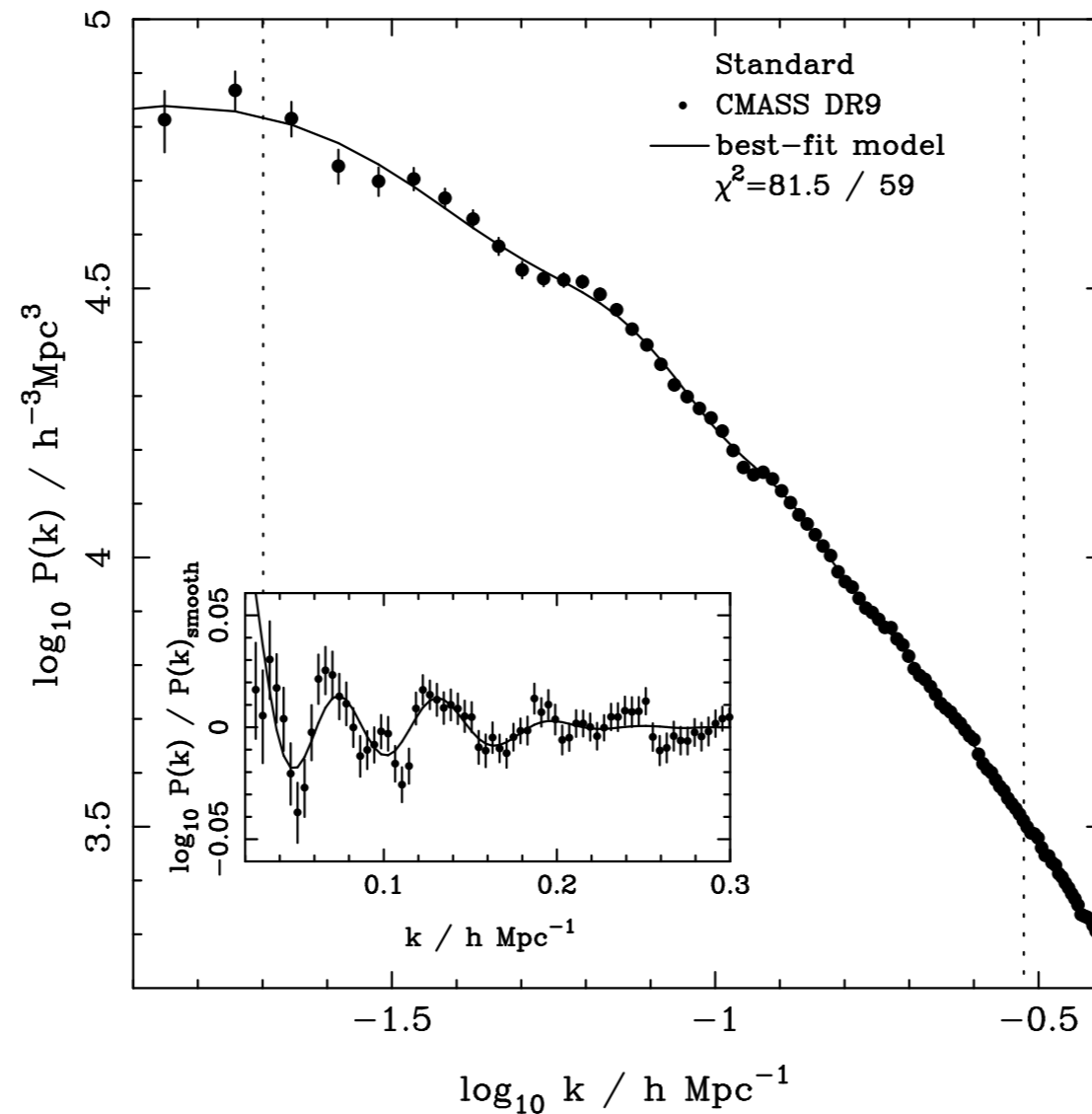
$$2 \sum_{\ell=2}^{2500} (2\ell + 1) \sim 10^7$$



Planck Collaboration

$$(3000)^3 = 2.7 \times 10^{10}$$

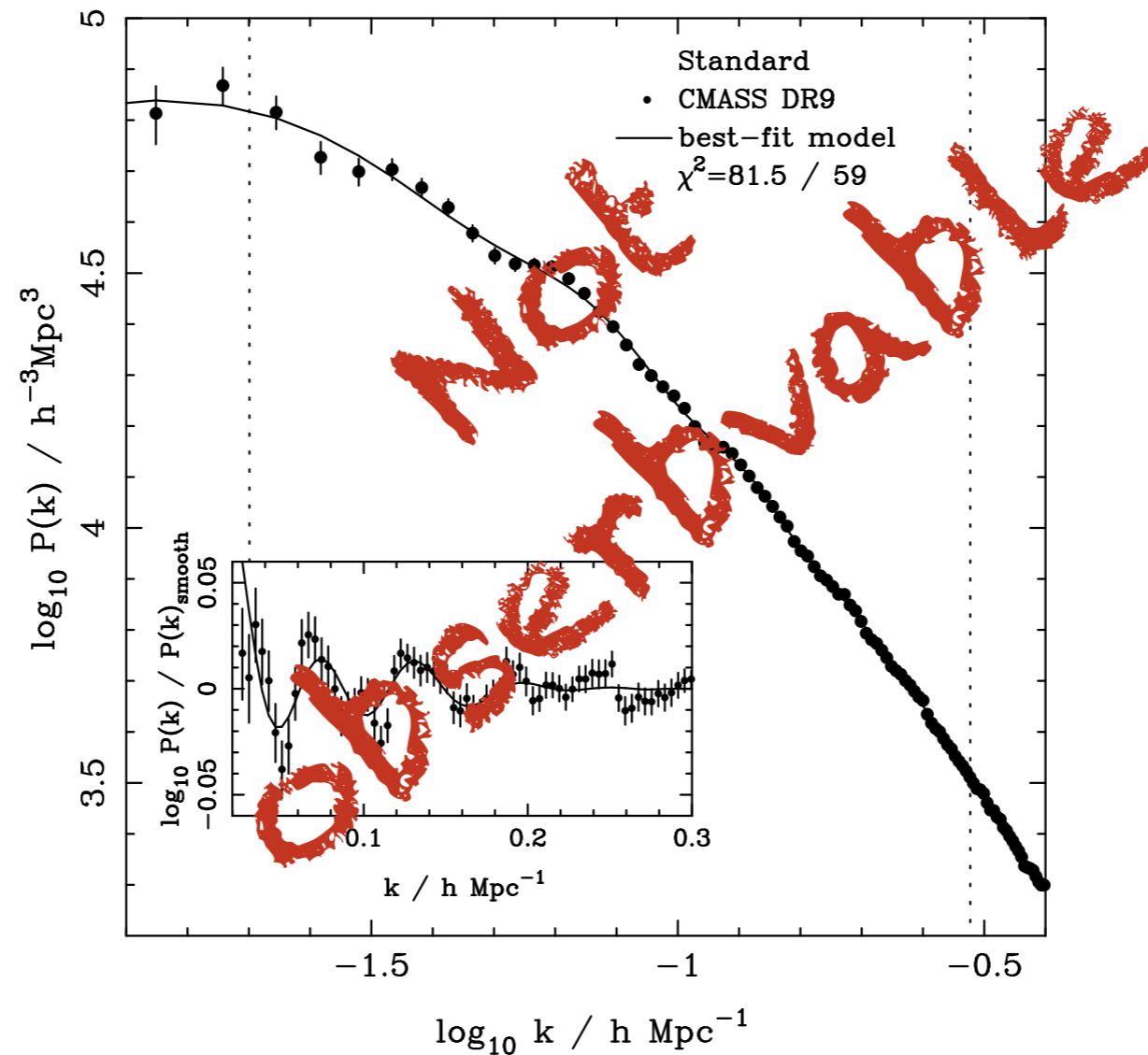
Large Scale Structures



Anderson et al '12 [arXiv:1203.6594]

$$P_{\text{obs}}(k, \mu, z) = b(z)^2 (1 + \beta(z) \mu^2)^2 P(k, z)$$

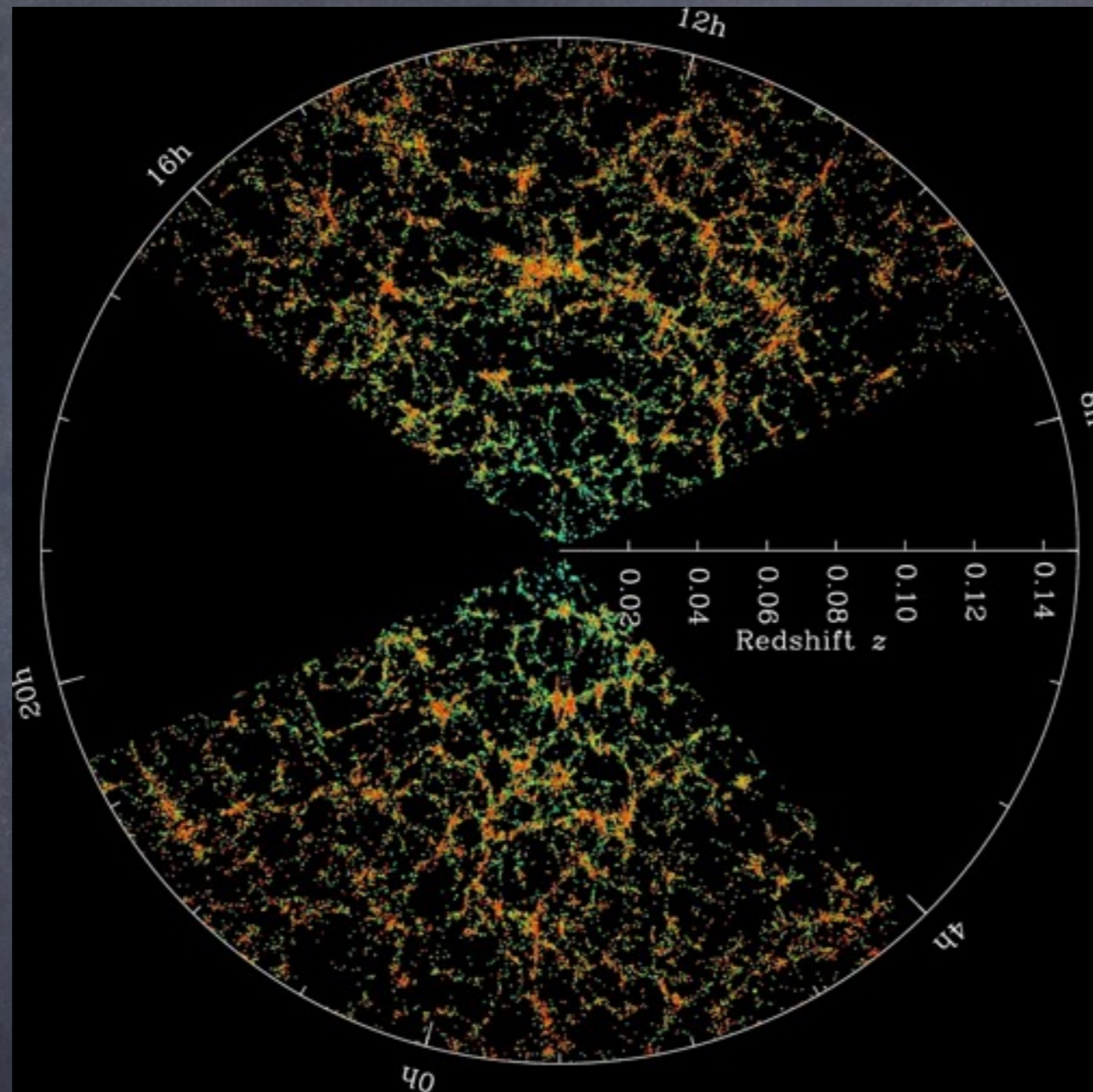
Large Scale Structures



Anderson et al '12 [arXiv:1203.6594]

$$P_{\text{obs}}(k, \mu, z) = b(z)^2 (1 + \beta(z) \mu^2)^2 P(k, z)$$

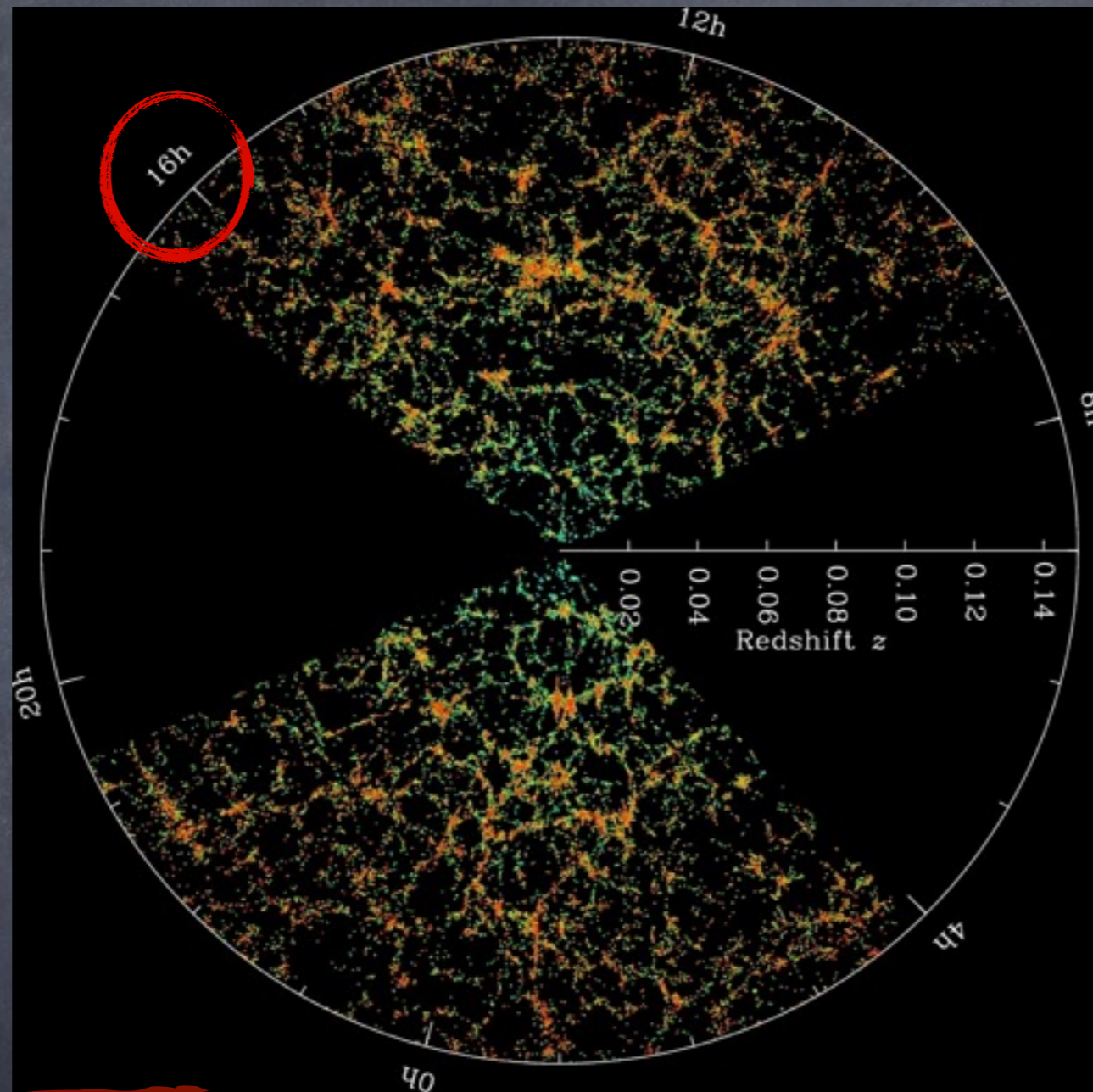
What do we really observe?



Angular position \mathbf{n} Redshift z

$$N(\mathbf{n}, z) d\Omega_{\mathbf{n}} dz$$

What do we really observe?

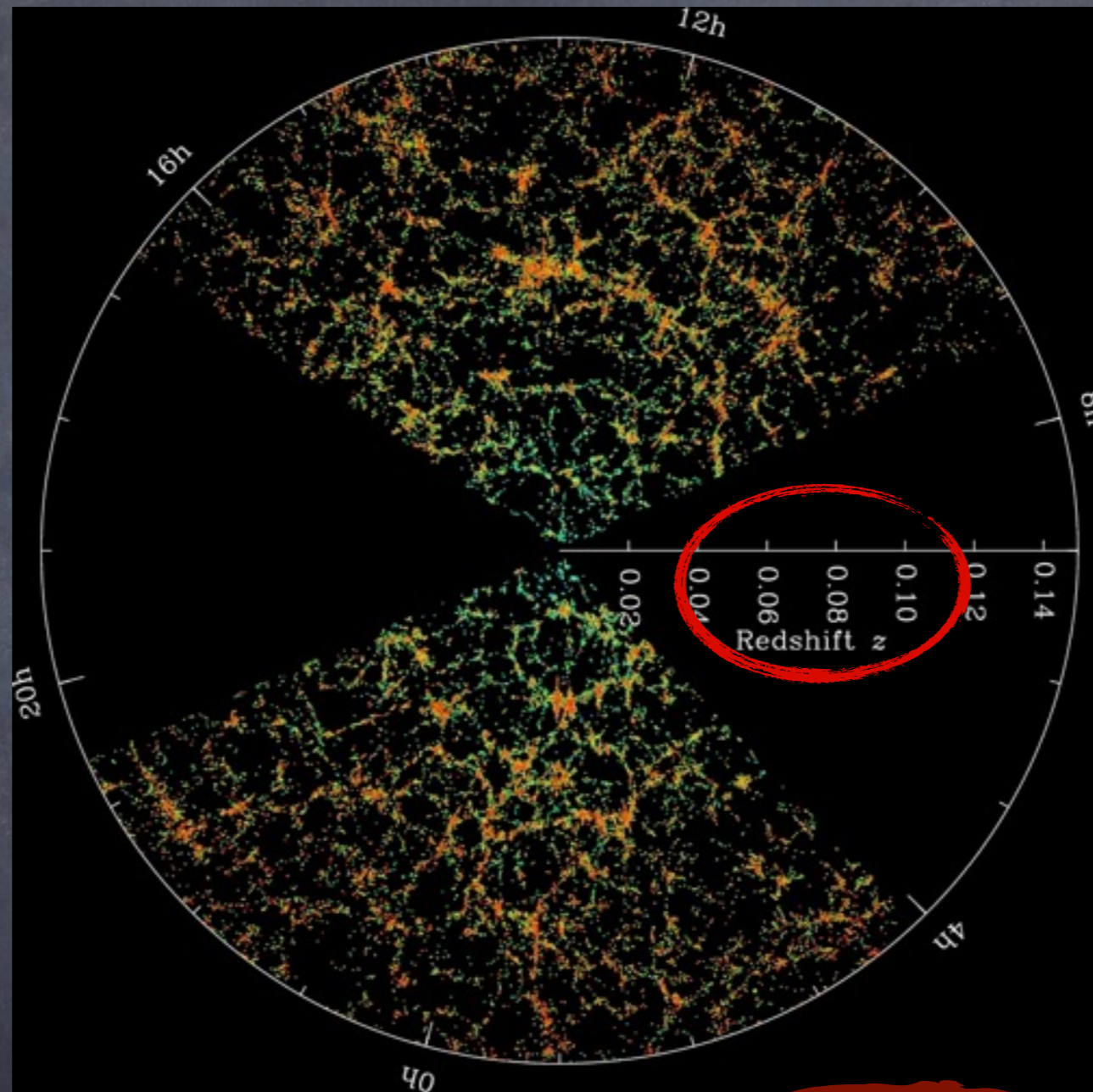


Angular position \mathbf{n}

Redshift z

$$N(\mathbf{n}, z) d\Omega_{\mathbf{n}} dz$$

What do we really observe?

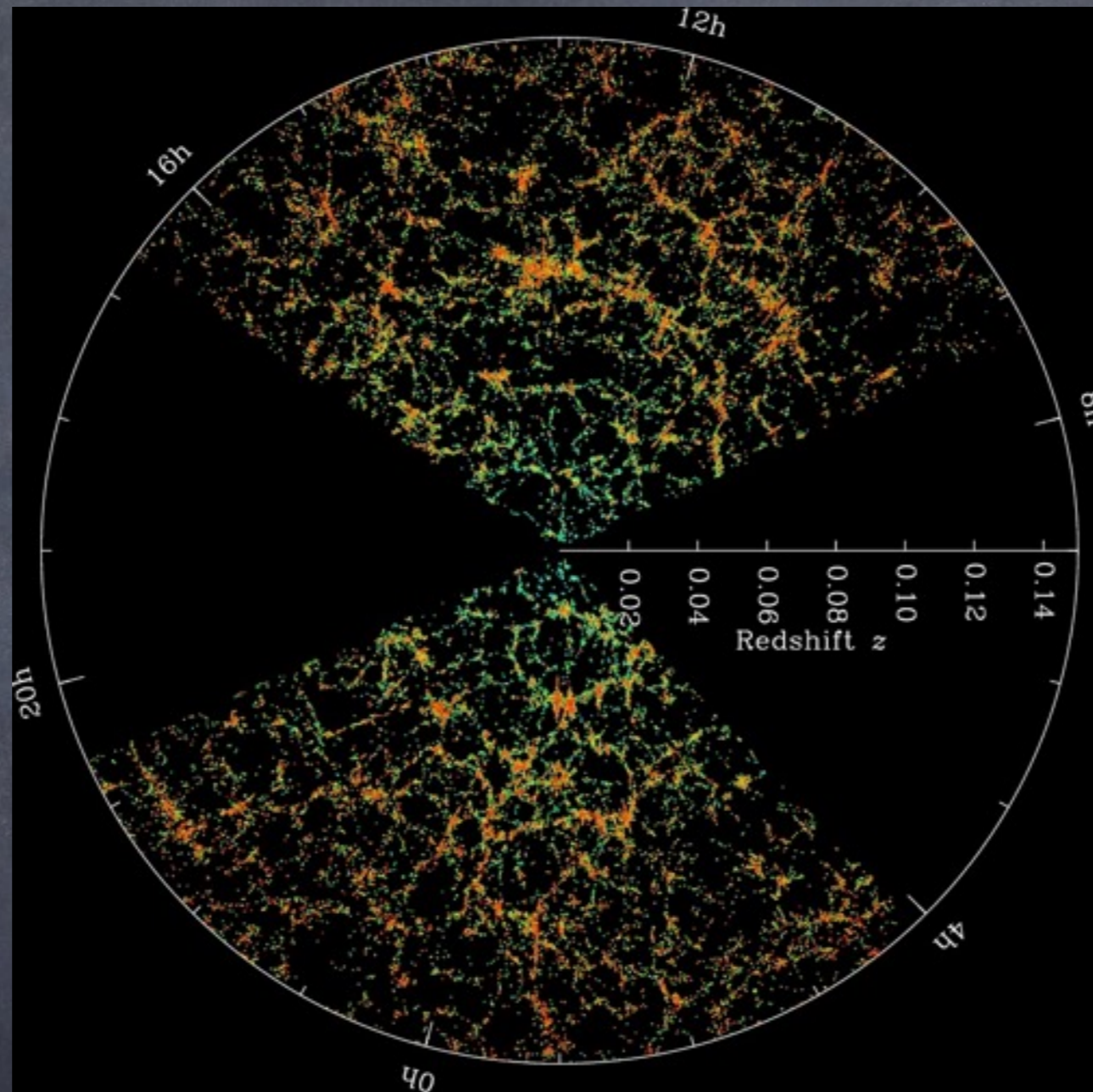


Angular position \mathbf{n}

Redshift z

$$N(\mathbf{n}, z) d\Omega_{\mathbf{n}} dz$$

What do we really observe?

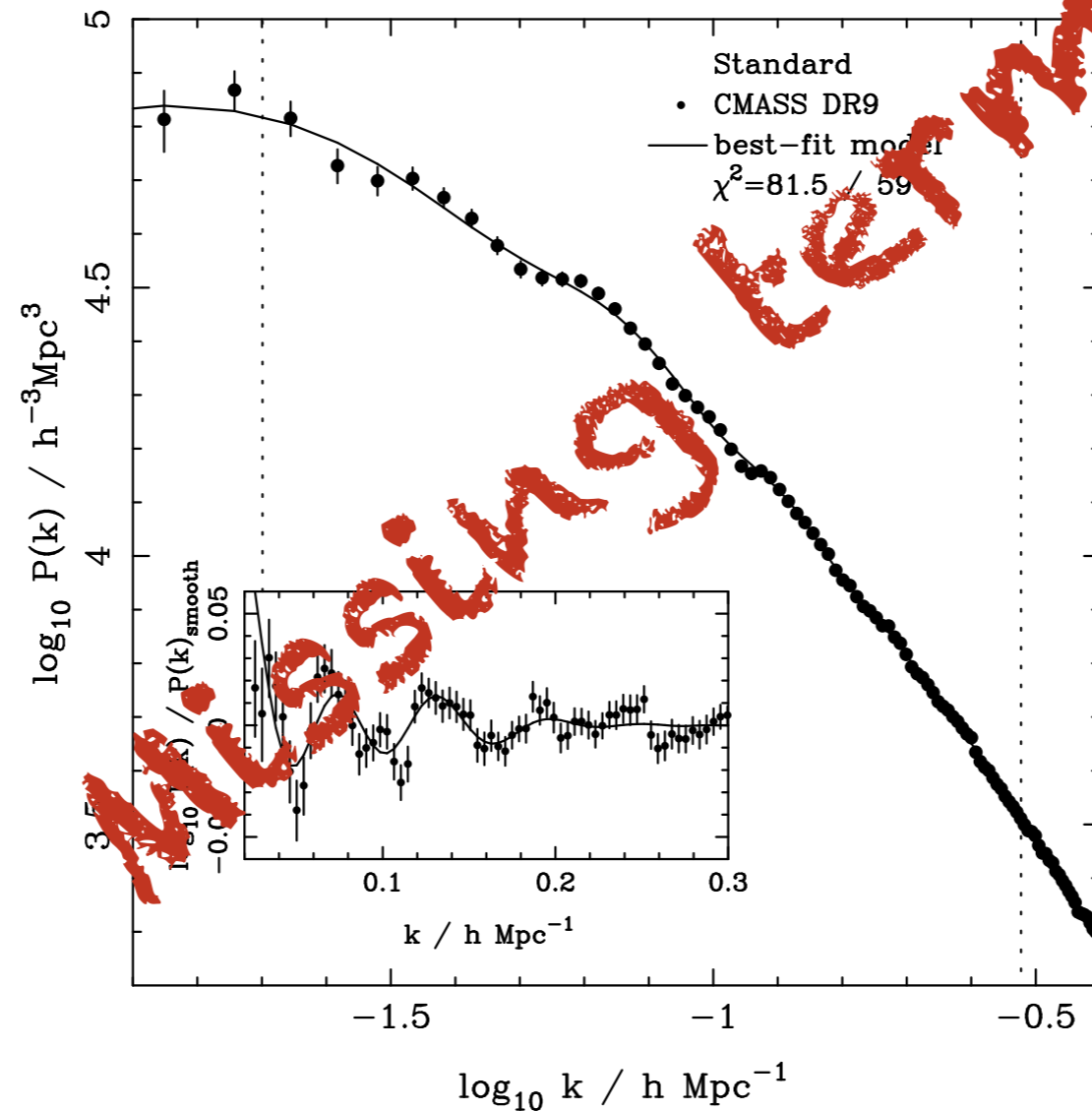


Info about
mass,
spectral type,
...

Angular position \mathbf{n} Redshift z

$$N(\mathbf{n}, z) d\Omega_{\mathbf{n}} dz$$

Large Scale Structures



Anderson et al '12 [arXiv:1203.6594]

$$P_{\text{obs}}(k, \mu, z) = b(z)^2 (1 + \beta(z) \mu^2)^2 P(k, z)$$

Large Scale Structures

$$\Delta_N(\mathbf{n}, z, m_*) = b(z) D_{cm}(L > \bar{L}_*) + \mathcal{H}^{-1} \partial_r \mathbf{n} \cdot \mathbf{v} \quad \text{Standard}$$

$$\begin{aligned} & - \frac{2-5s}{2} \int_0^r \frac{r-r'}{rr'} \Delta_\Omega (\Psi + \Phi) dr' \\ & + \left(5s + \frac{2-5s}{\mathcal{H}r} + \frac{\dot{\mathcal{H}}}{\mathcal{H}^2} - f_{\text{evo}}^N \right) \mathbf{n} \cdot \mathbf{v} + (f_{\text{evo}}^N - 3) \mathcal{H}v \\ & + \left(5s + \frac{2-5s}{\mathcal{H}r} + \frac{\dot{\mathcal{H}}}{\mathcal{H}^2} - f_{\text{evo}}^N \right) \int_0^r (\dot{\Psi} + \dot{\Phi}) dr' \\ & + \left(5s + \frac{2-5s}{\mathcal{H}r} + \frac{\dot{\mathcal{H}}}{\mathcal{H}^2} - f_{\text{evo}}^N \right) \Psi \\ & + \frac{2-5s}{r} \int_0^r (\Psi + \Phi) dr \\ & + (5s - 2) \Phi + \Psi + \mathcal{H}^{-1} \dot{\Phi} \end{aligned}$$

Relativistic
Effects

Bonvin & Durrer [arXiv:1105.5280],
Challinor & Lewis [arXiv:1105.5292],
Yoo [arXiv:1009.3021]

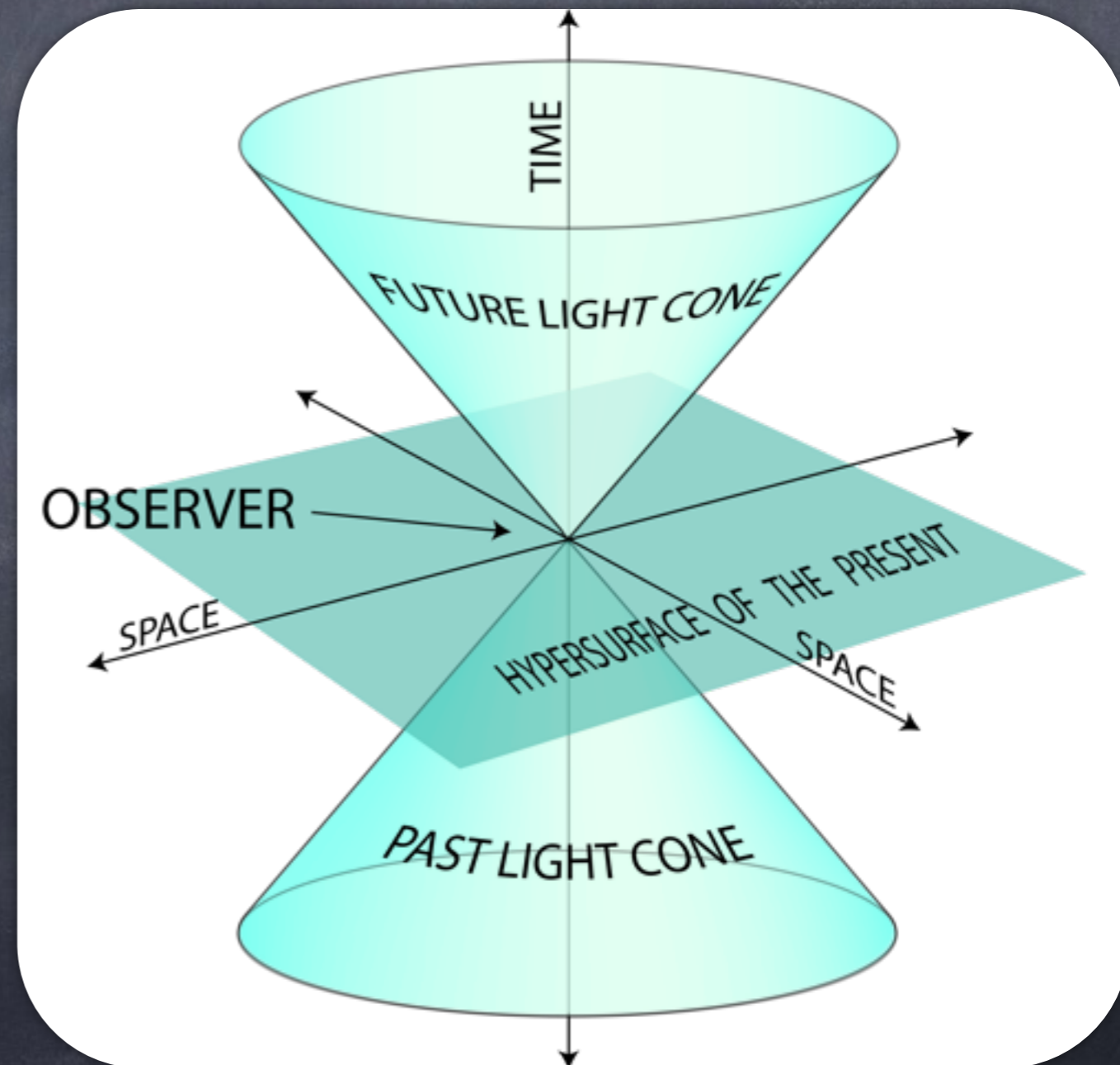
What do we really observe?

To compute $\Delta(\mathbf{n}, z) \equiv \frac{N(\mathbf{n}, z) - \langle N \rangle (z)}{\langle N \rangle (z)}$
we have to consider:

What do we really observe?

To compute $\Delta(\mathbf{n}, z) \equiv \frac{N(\mathbf{n}, z) - \langle N \rangle(z)}{\langle N \rangle(z)}$
we have to consider:

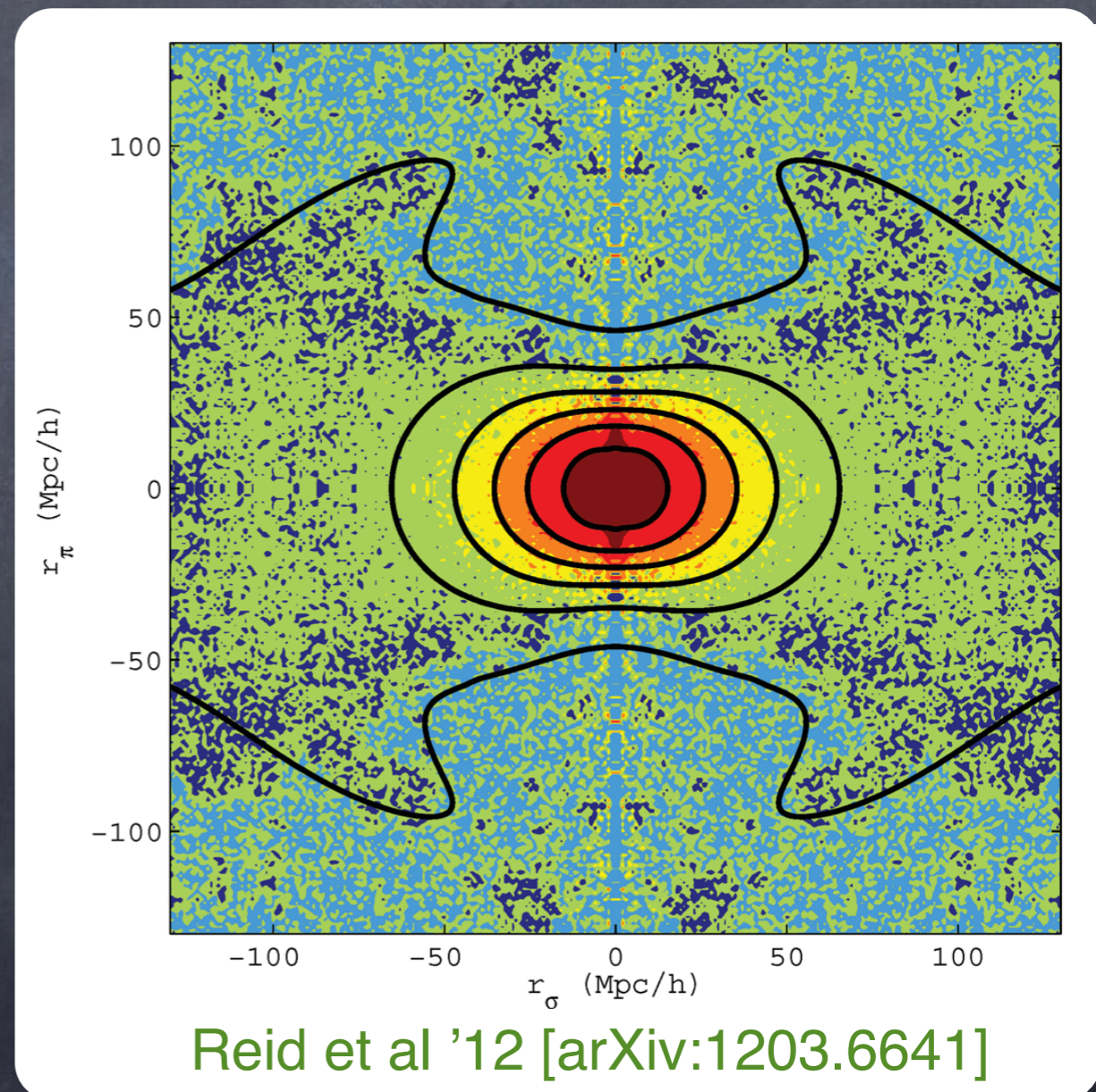
- observation on the past lightcone



What do we really observe?

To compute $\Delta(\mathbf{n}, z) \equiv \frac{N(\mathbf{n}, z) - \langle N \rangle(z)}{\langle N \rangle(z)}$
we have to consider:

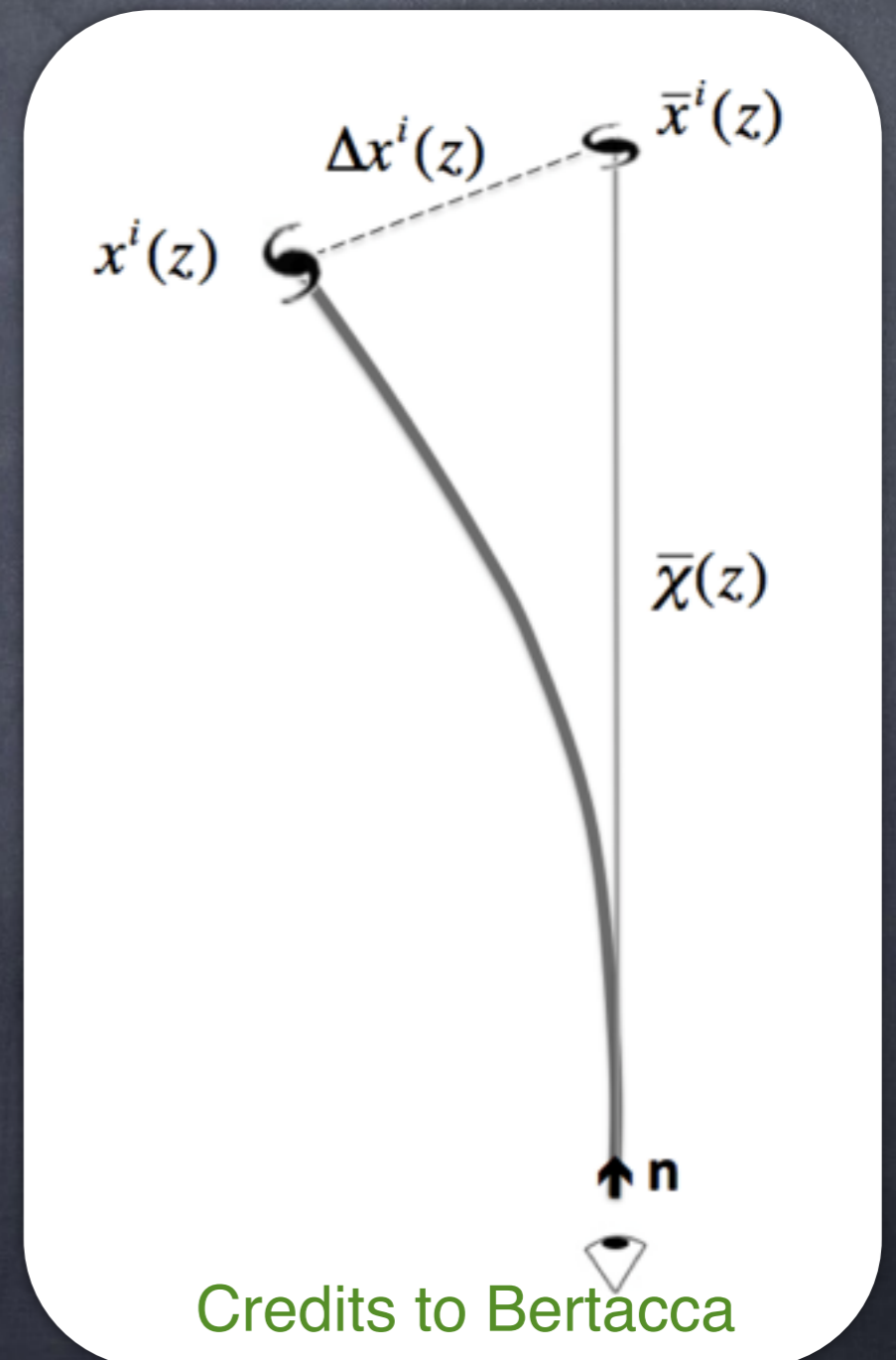
- observation on the past lightcone
- redshift perturbed by peculiar velocity



What do we really observe?

To compute $\Delta(\mathbf{n}, z) \equiv \frac{N(\mathbf{n}, z) - \langle N \rangle(z)}{\langle N \rangle(z)}$
we have to consider:

- observation on the past lightcone
- redshift perturbed by peculiar velocity
- light deflection



Large Scale Structures

$$\begin{aligned}
 \Delta_N(\mathbf{n}, z, m_*) &= b(z) D_{cm}(L > \bar{L}_*) + \mathcal{H}^{-1} \partial_r \mathbf{n} \cdot \mathbf{v} \\
 &\sim D \\
 &- \frac{2-5s}{2} \int_0^r \frac{r-r'}{rr'} \Delta_\Omega(\Psi + \Phi) dr' \\
 &+ \left(5s + \frac{2-5s}{\mathcal{H}r} + \frac{\dot{\mathcal{H}}}{\mathcal{H}^2} - f_{\text{evo}}^N \right) \mathbf{n} \cdot \mathbf{v} + (f_{\text{evo}}^N - 3) \mathcal{H}v \\
 &+ \left(5s + \frac{2-5s}{\mathcal{H}r} + \frac{\dot{\mathcal{H}}}{\mathcal{H}^2} - f_{\text{evo}}^N \right) \int_0^r (\dot{\Psi} + \dot{\Phi}) dr' \\
 &+ \left(5s + \frac{2-5s}{\mathcal{H}r} + \frac{\dot{\mathcal{H}}}{\mathcal{H}^2} - f_{\text{evo}}^N \right) \Psi \\
 &+ \frac{2-5s}{r} \int_0^r (\Psi + \Phi) dr \\
 &+ (5s - 2) \Phi + \Psi + \mathcal{H}^{-1} \dot{\Phi}
 \end{aligned}$$

Bonvin & Durrer [arXiv:1105.5280],
 Challinor & Lewis [arXiv:1105.5292],
 Yoo [arXiv:1009.3021]

Large Scale Structures

$$\Delta_N(\mathbf{n}, z, m_*) = b(z) D_{cm}(L > \bar{L}_*) + \mathcal{H}^{-1} \partial_r \mathbf{n} \cdot \mathbf{v}$$

$$- \frac{2-5s}{2} \int_0^r \frac{r-r'}{rr'} \Delta_\Omega(\Psi + \Phi) dr'$$

$$\sim \frac{\mathcal{H}}{k} D$$

$$+ \left(5s + \frac{2-5s}{\mathcal{H}r} + \frac{\dot{\mathcal{H}}}{\mathcal{H}^2} - f_{\text{evo}}^N \right) \mathbf{n} \cdot \mathbf{v} + (f_{\text{evo}}^N - 3) \mathcal{H}v$$

$$+ \left(5s + \frac{2-5s}{\mathcal{H}r} + \frac{\dot{\mathcal{H}}}{\mathcal{H}^2} - f_{\text{evo}}^N \right) \int_0^r (\dot{\Psi} + \dot{\Phi}) dr'$$

$$+ \left(5s + \frac{2-5s}{\mathcal{H}r} + \frac{\dot{\mathcal{H}}}{\mathcal{H}^2} - f_{\text{evo}}^N \right) \Psi$$

$$+ \frac{2-5s}{r} \int_0^r (\Psi + \Phi) dr$$

$$+ (5s-2) \Phi + \Psi + \mathcal{H}^{-1} \dot{\Phi}$$

Bonvin & Durrer [arXiv:1105.5280],
Challinor & Lewis [arXiv:1105.5292],
Yoo [arXiv:1009.3021]

Large Scale Structures

$$\begin{aligned}
 \Delta_N(\mathbf{n}, z, m_*) &= b(z) D_{cm}(L > \bar{L}_*) + \mathcal{H}^{-1} \partial_r \mathbf{n} \cdot \mathbf{v} \\
 &\quad - \frac{2-5s}{2} \int_0^r \frac{r-r'}{rr'} \Delta_\Omega(\Psi + \Phi) dr' \\
 &\quad + \left(5s + \frac{2-5s}{\mathcal{H}r} + \frac{\dot{\mathcal{H}}}{\mathcal{H}^2} - f_{\text{evo}}^N \right) \mathbf{n} \cdot \mathbf{v} + (f_{\text{evo}}^N - 3) \mathcal{H}v \\
 &\quad + \left(5s + \frac{2-5s}{\mathcal{H}r} + \frac{\dot{\mathcal{H}}}{\mathcal{H}^2} - f_{\text{evo}}^N \right) \int_0^r (\dot{\Psi} + \dot{\Phi}) dr' \\
 &\quad + \left(5s + \frac{2-5s}{\mathcal{H}r} + \frac{\dot{\mathcal{H}}}{\mathcal{H}^2} - f_{\text{evo}}^N \right) \Psi \\
 &\quad + \frac{2-5s}{r} \int_0^r (\Psi + \Phi) dr \\
 &\quad + (5s - 2) \Phi + \Psi + \mathcal{H}^{-1} \dot{\Phi}
 \end{aligned}$$

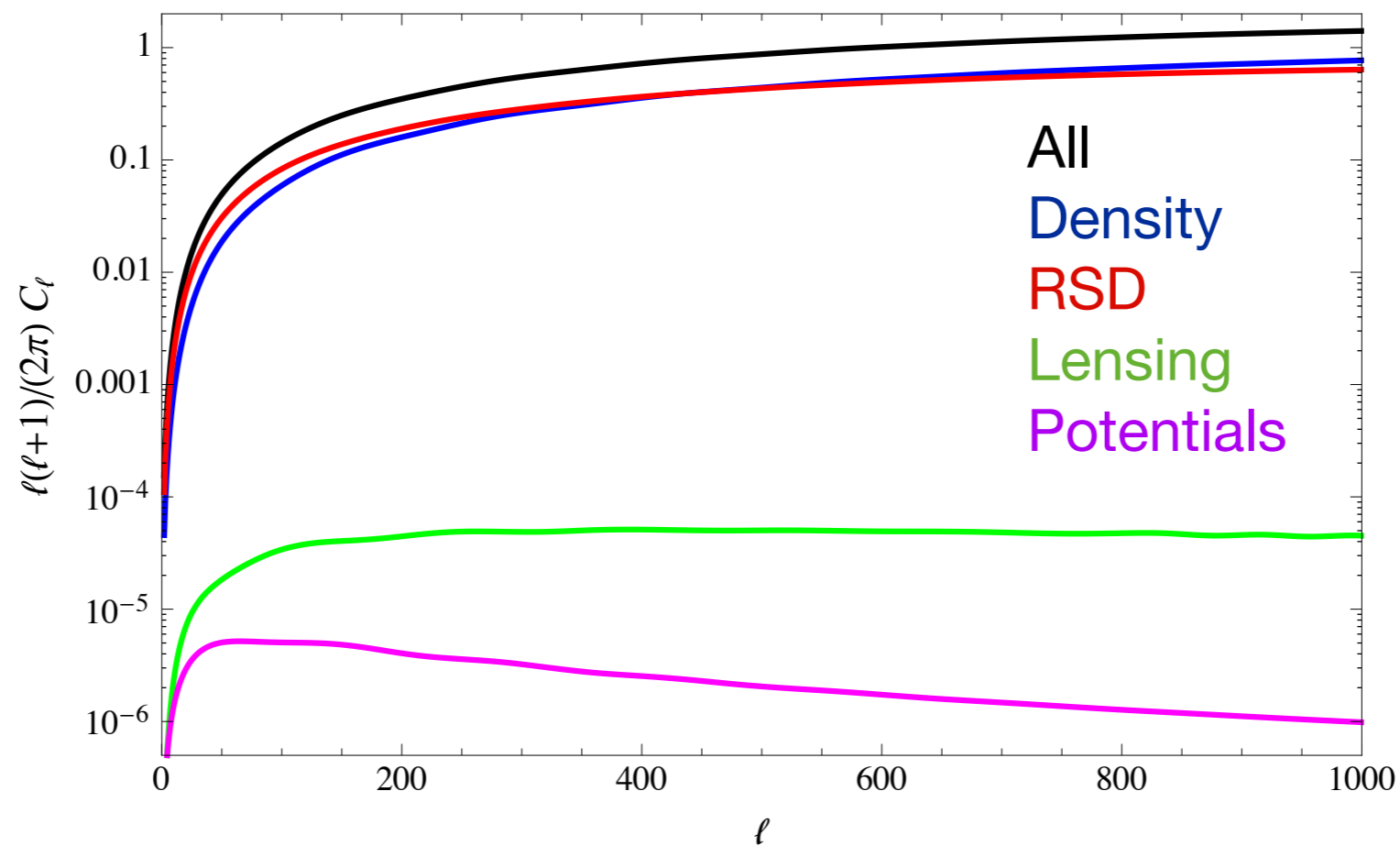
$\sim \left(\frac{\mathcal{H}}{k} \right)^2 D$

Bonvin & Durrer [arXiv:1105.5280],
 Challinor & Lewis [arXiv:1105.5292],
 Yoo [arXiv:1009.3021]

z-dependent angular power spectrum

Power spectrum

$$c_\ell(z_1, z_2) = \langle a_{\ell m}(z_1) a_{\ell m}(z_2) \rangle = 4\pi \int \frac{dk}{k} \mathcal{P}(k) \Delta_\ell(z_1, k) \Delta_\ell(z_2, k)$$

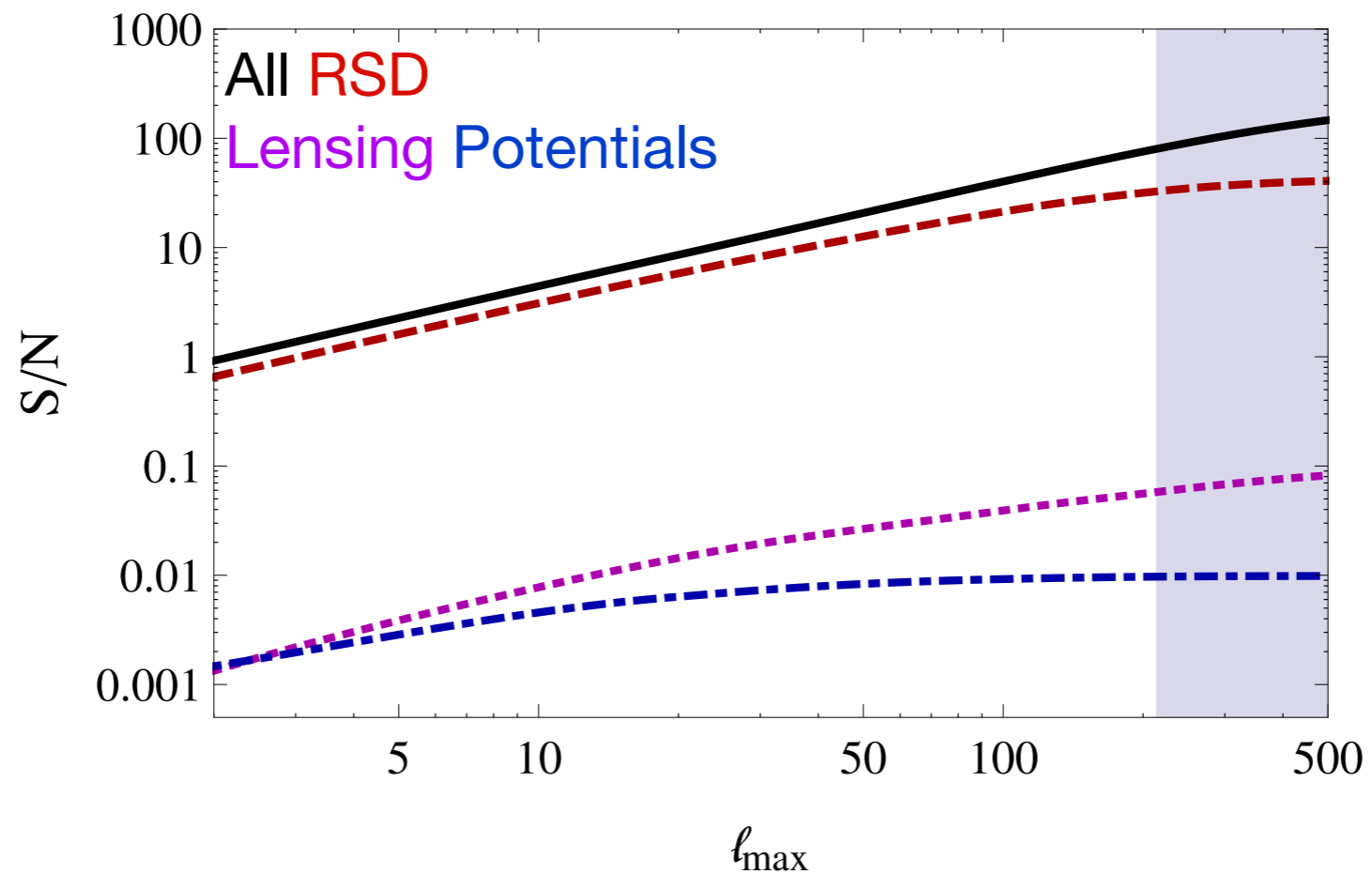


Lensing Potential

Cumulative Signal to Noise

$$\left(\frac{S}{N}\right)^2 = \sum_{\ell=2}^{\ell_{\max}} \left(\frac{C_{\ell} - \tilde{C}_{\ell}}{\sigma_{\ell}}\right)^2$$

$\bar{z}=1, \Delta z=0.01$



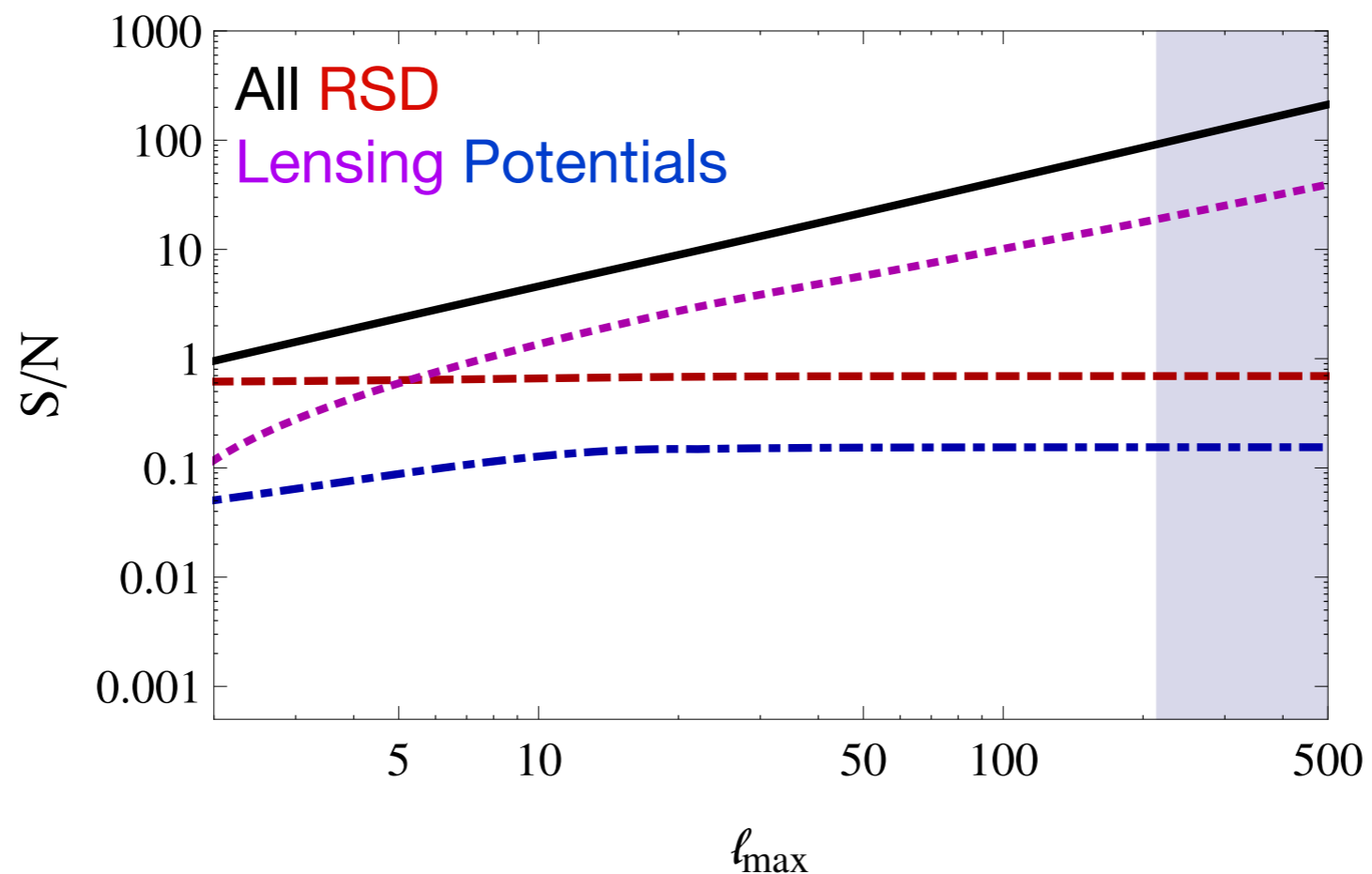
Euclid

Lensing Potential

Cumulative Signal to Noise

$$\left(\frac{S}{N}\right)^2 = \sum_{\ell=2}^{\ell_{\max}} \left(\frac{C_{\ell} - \tilde{C}_{\ell}}{\sigma_{\ell}}\right)^2$$

$\bar{z}=1, \Delta z=0.5$

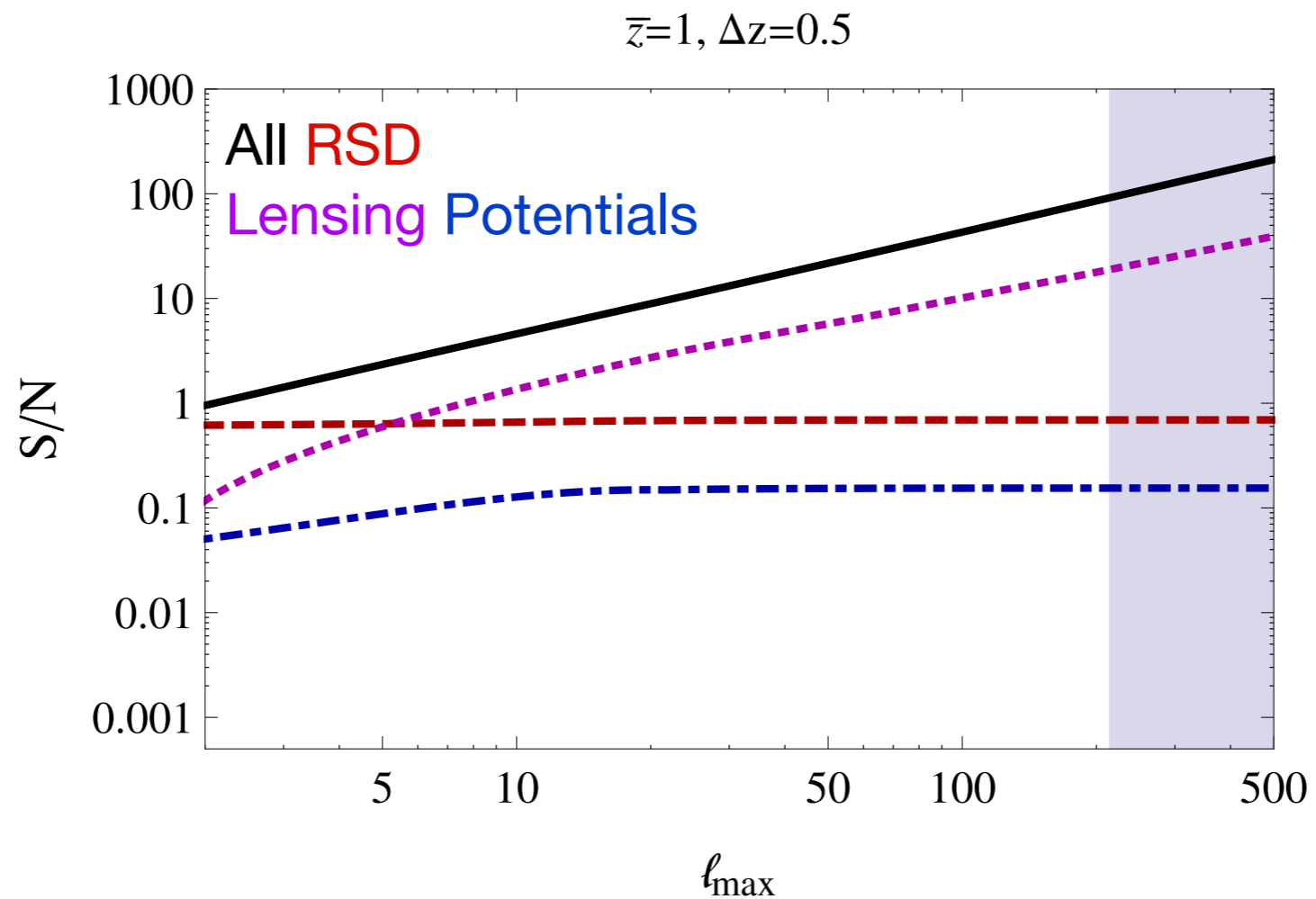


Euclid

Lensing Potential

Cumulative Signal to Noise

$$\left(\frac{S}{N}\right)^2 = \sum_{\ell=2}^{\ell_{\max}} \left(\frac{C_{\ell} - \tilde{C}_{\ell}}{\sigma_{\ell}}\right)^2$$



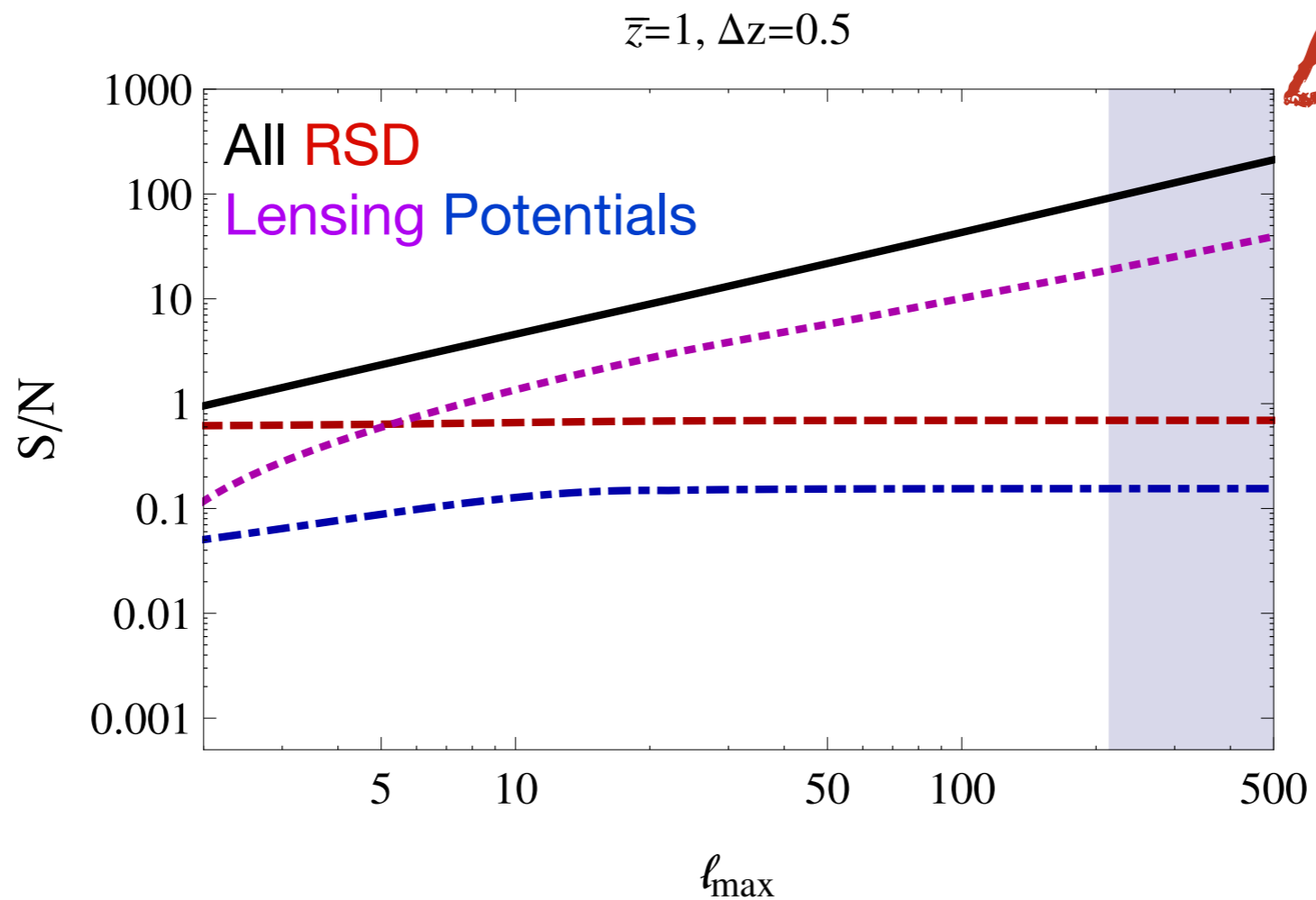
Euclid

See
Montanari's
Talk

Lensing Potential

Cumulative Signal to Noise

$$\left(\frac{S}{N}\right)^2 = \sum_{\ell=2}^{\ell_{\max}} \left(\frac{C_{\ell} - \tilde{C}_{\ell}}{\sigma_{\ell}}\right)^2$$



Theoretical bias?

Euclid

See
Montanari's
Talk

Relativistic Effects

Relativistic Effects

Are relativistic effects relevant for the **standard analysis**?

- No, but.. (Yoo and Seljak [ArXiv:1308.1093], Yoo et al [arXiv:1206.5809], Alonso et al [1505.07596])
- cosmic magnification for deep survey
(see also Raccanelli et al [ArXiv:1311.6813], Alonso et al [1505.07596], Montanari and Durrer [ArXiv:1506.01369])

Relativistic Effects

Are relativistic effects relevant for the **standard analysis**?

- No, but.. (Yoo and Seljak [ArXiv:1308.1093], Yoo et al [arXiv:1206.5809], Alonso et al [1505.07596])
- cosmic magnification for deep survey
(see also Raccanelli et al [ArXiv:1311.6813], Alonso et al [1505.07596], Montanari and Durrer [ArXiv:1506.01369])

If not relevant in standard analysis, can we think to an **alternative analysis** to measure them?

- imaginary power spectrum
(McDonald [Arxiv:0907.5220])
- dipole and octupole in galaxy correlation functions
(Raccanelli et al [ArXiv:1306.6646], Bonvin et al [Arxiv:1309.1321])
- multitracer and shot-noise canceling techniques
(Yoo et al [arXiv:1206.5809])

Relativistic Effects

Are relativistic effects relevant for the **standard analysis**?

- No, but.. (Yoo and Seljak [ArXiv:1308.1093], Yoo et al [arXiv:1206.5809], Alonso et al [1505.07596])
- cosmic magnification for deep survey
(see also Raccanelli et al [ArXiv:1311.6813], Alonso et al [1505.07596], Montanari and Durrer [ArXiv:1506.01369])

If not relevant in standard analysis, can we think to an **alternative analysis** to measure them?

- imaginary power spectrum
(McDonald [Arxiv:0907.5220])
- dipole and octupole in galaxy correlation functions
(Raccanelli et al [ArXiv:1306.6646], Bonvin et al [Arxiv:1309.1321])
- multitracer and shot-noise canceling techniques
(Yoo et al [arXiv:1206.5809])

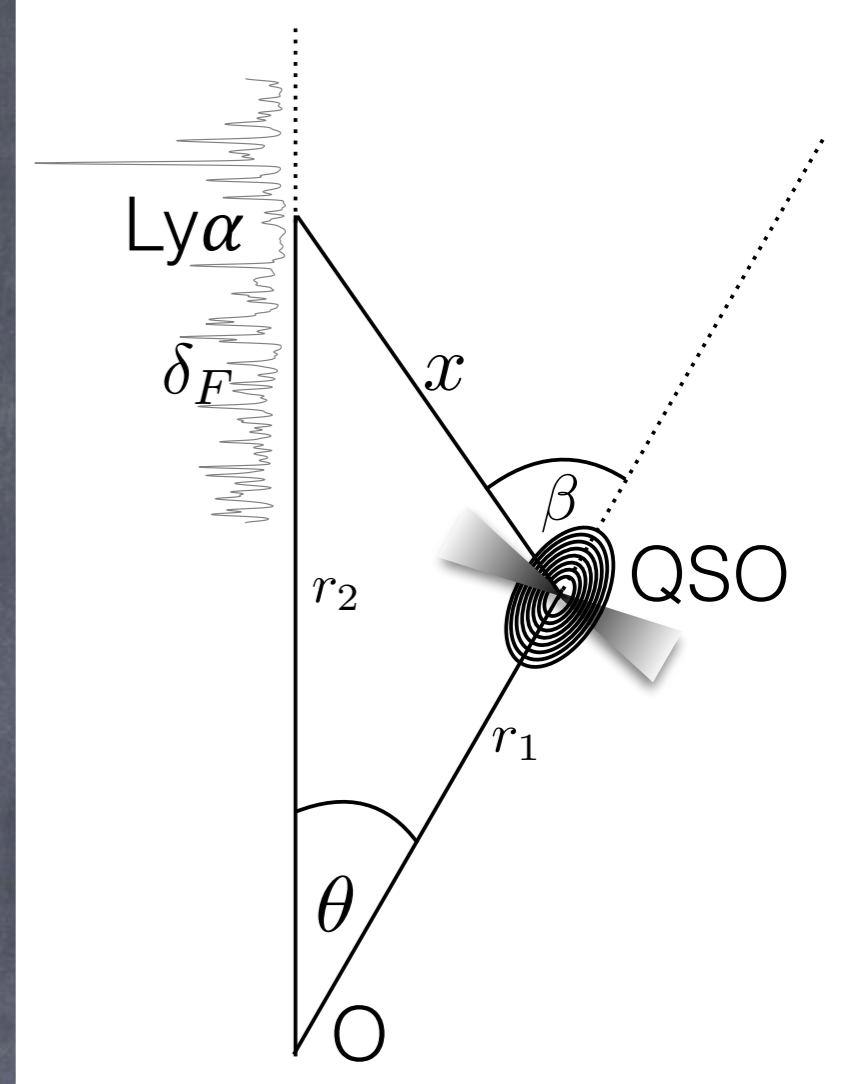
Multi-tracers

Quasars x Ly-alpha correlation

Irsic , ED, Viel [arXiv:1510.03436]

$$\xi_{Q\alpha}(z_1, z_2, \theta) = \langle \Delta_Q(\mathbf{n}_1, z_1) \delta_F(\mathbf{n}_2, z_2) \rangle$$

Large bias factor difference

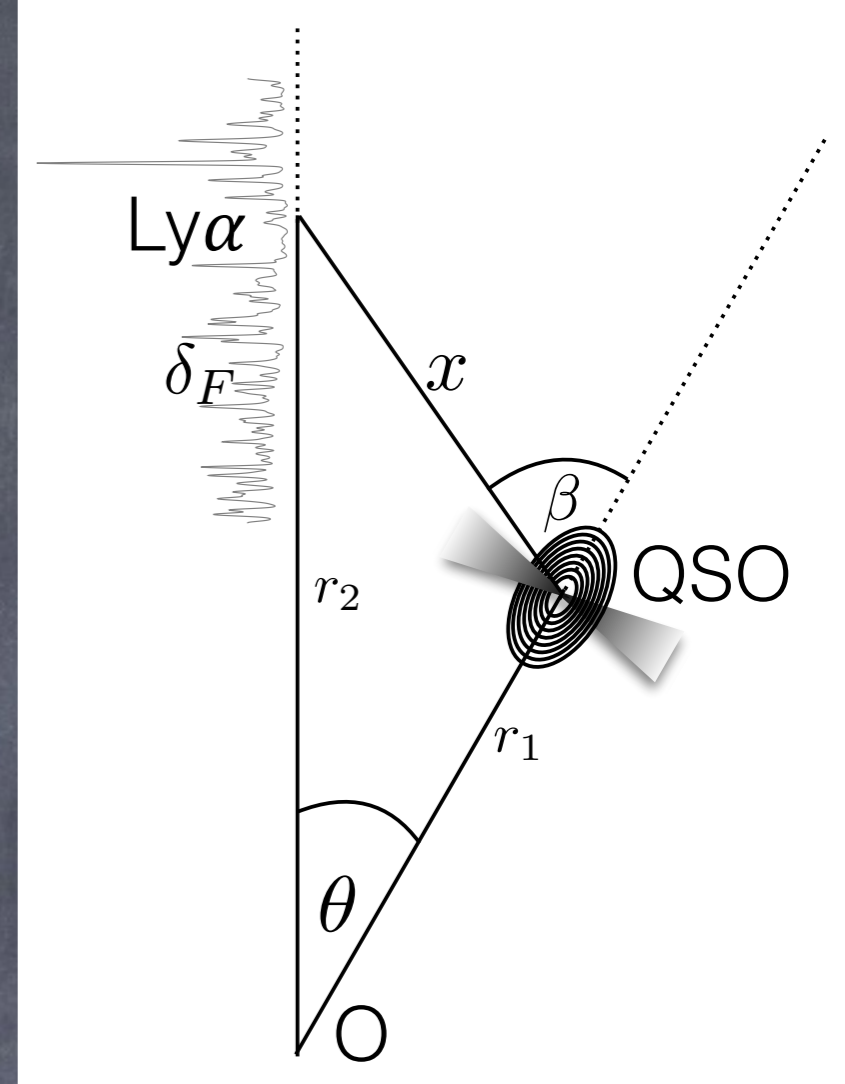


Quasars x Ly-alpha correlation

Irsic , ED, Viel [arXiv:1510.03436]

$$\xi_{Q\alpha}(z_1, z_2, \theta) = \langle \Delta_Q(\mathbf{n}_1, z_1) \delta_F(\mathbf{n}_2, z_2) \rangle$$

Large bias factor difference



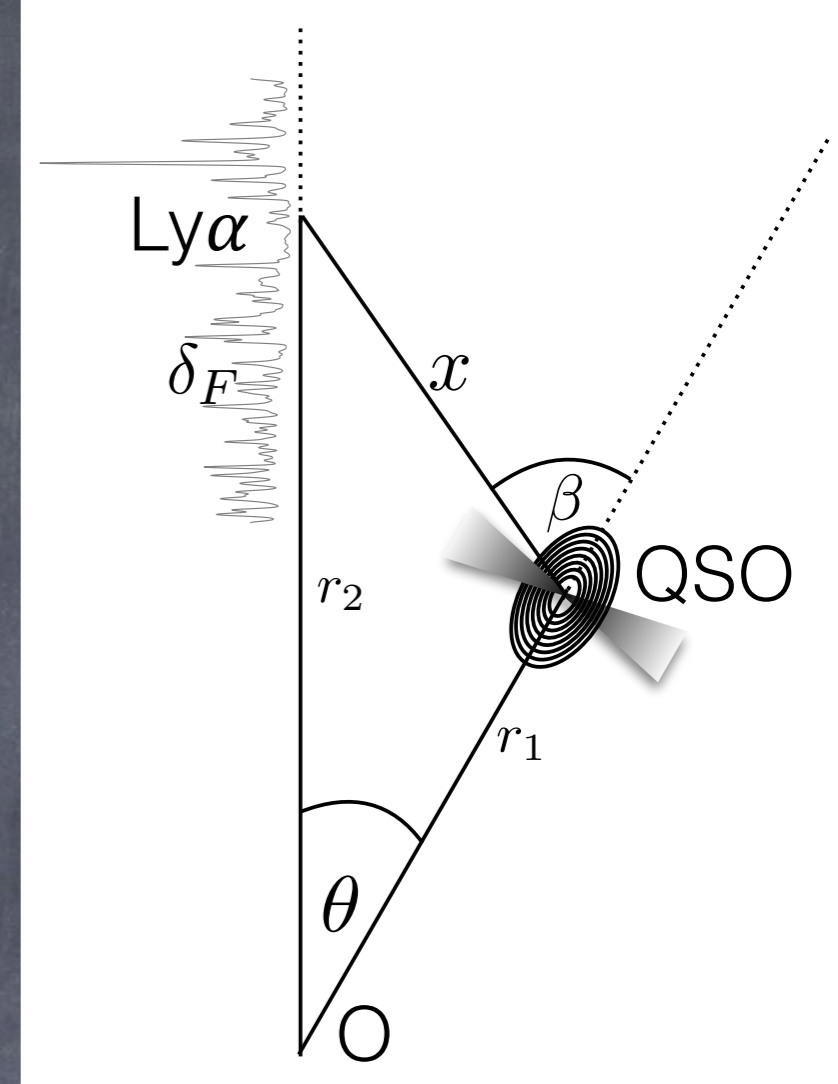
$$\delta_F(\mathbf{n}, z) = b_\alpha \delta^{\text{sync}} + b_v \mathcal{H}^{-1} \partial_r \mathbf{n} \cdot \mathbf{v} - \bar{\tau}(z) \left[- \left(2 + \frac{\dot{\mathcal{H}}}{\mathcal{H}^2} \right) \frac{\delta z}{1+z} + \mathbf{n} \cdot \mathbf{v} + \Psi + \mathcal{H}^{-1} \dot{\Phi} - 3\mathcal{H}v \right]$$

Quasars x Ly-alpha correlation

Irsic , ED, Viel [arXiv:1510.03436]

$$\xi_{Q\alpha}(z_1, z_2, \theta) = \langle \Delta_Q(\mathbf{n}_1, z_1) \delta_F(\mathbf{n}_2, z_2) \rangle$$

Large bias factor difference



$$\delta_F(\mathbf{n}, z) = b_\alpha \delta^{\text{sync}} + b_v \mathcal{H}^{-1} \partial_r \mathbf{n} \cdot \mathbf{v} - \bar{\tau}(z) \left[- \left(2 + \frac{\dot{\mathcal{H}}}{\mathcal{H}^2} \right) \frac{\delta z}{1+z} + \mathbf{n} \cdot \mathbf{v} + \Psi + \mathcal{H}^{-1} \dot{\Phi} - 3\mathcal{H}v \right]$$

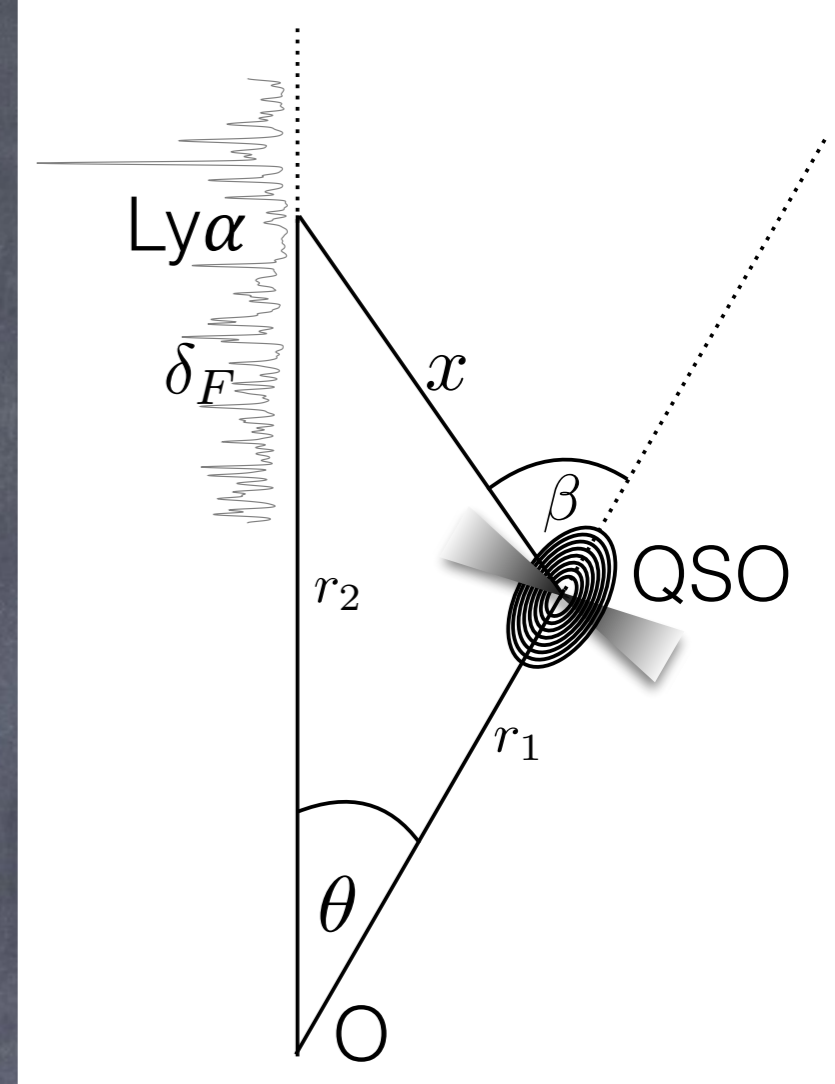
Standard

Quasars x Ly-alpha correlation

Irsic , ED, Viel [arXiv:1510.03436]

$$\xi_{Q\alpha}(z_1, z_2, \theta) = \langle \Delta_Q(\mathbf{n}_1, z_1) \delta_F(\mathbf{n}_2, z_2) \rangle$$

Large bias factor difference



$$\delta_F(\mathbf{n}, z) = b_\alpha \delta^{\text{sync}} + b_v \mathcal{H}^{-1} \partial_r \mathbf{n} \cdot \mathbf{v} - \bar{\tau}(z) \left[- \left(2 + \frac{\dot{\mathcal{H}}}{\mathcal{H}^2} \right) \frac{\delta z}{1+z} + \mathbf{n} \cdot \mathbf{v} + \Psi + \mathcal{H}^{-1} \dot{\Phi} - 3\mathcal{H}v \right]$$

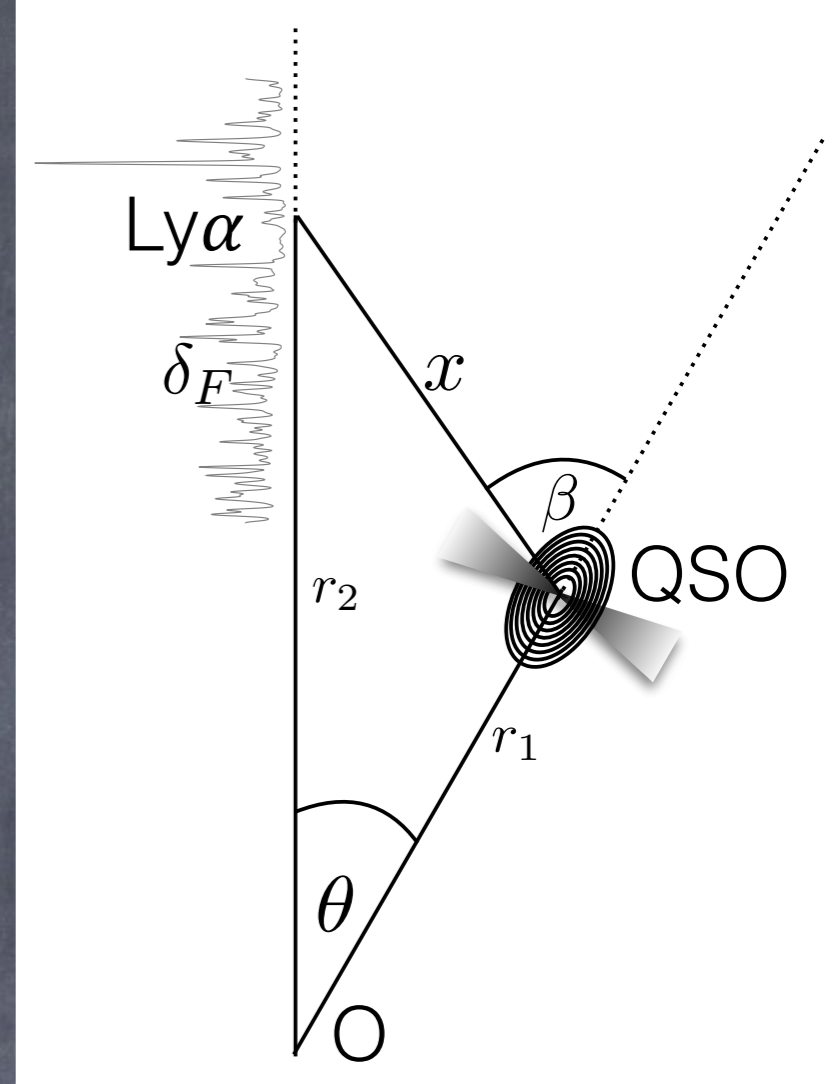
Relativistic

Quasars x Ly-alpha correlation

Irsic , ED, Viel [arXiv:1510.03436]

$$\xi_{Q\alpha}(z_1, z_2, \theta) = \langle \Delta_Q(\mathbf{n}_1, z_1) \delta_F(\mathbf{n}_2, z_2) \rangle$$

$$\xi_{Q\alpha} = \xi_{Q\alpha}^{\text{newt}} + \xi_{Q\alpha}^{\text{magnification}} + \xi_{Q\alpha}^{\text{relativistic}}$$



Quasars x Ly-alpha correlation

Irsic , ED, Viel [arXiv:1510.03436]

$$\xi_{Q\alpha}(z_1, z_2, \theta) = \langle \Delta_Q(\mathbf{n}_1, z_1) \delta_F(\mathbf{n}_2, z_2) \rangle$$

$$\xi_{Q\alpha} = \xi_{Q\alpha}^{\text{newt}} + \xi_{Q\alpha}^{\text{magnification}} + \xi_{Q\alpha}^{\text{relativistic}}$$

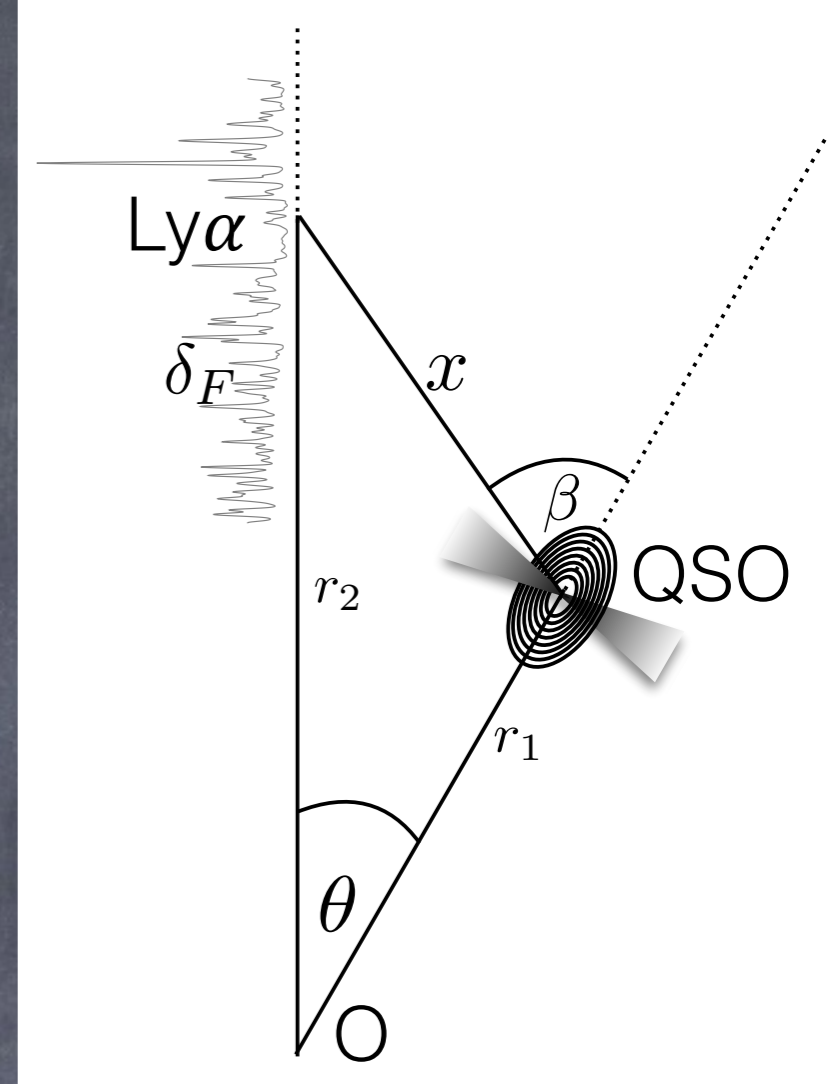
$$\xi_{Q\alpha}^{\text{newt}} \sim b_Q b_\alpha \int \frac{dk}{2\pi^2} k^2 P(k) j_0(kx)$$

$$+ b_v \int \frac{dk}{2\pi^2} k^2 f^2 P(k) \left[\frac{1}{5} j_0(kx) - \frac{4}{7} j_2(kx) + \frac{8}{35} j_4(kx) \right]$$

$$+ (b_Q b_v + b_\alpha) \int \frac{dk}{2\pi^2} k^2 f P(k) \left[\frac{1}{3} j_0(kx) - \frac{2}{3} j_2(kx) \right]$$

Order $\mathcal{O}(1)$

Even spherical Bessel functions



Quasars x Ly-alpha correlation

Irsic , ED, Viel [arXiv:1510.03436]

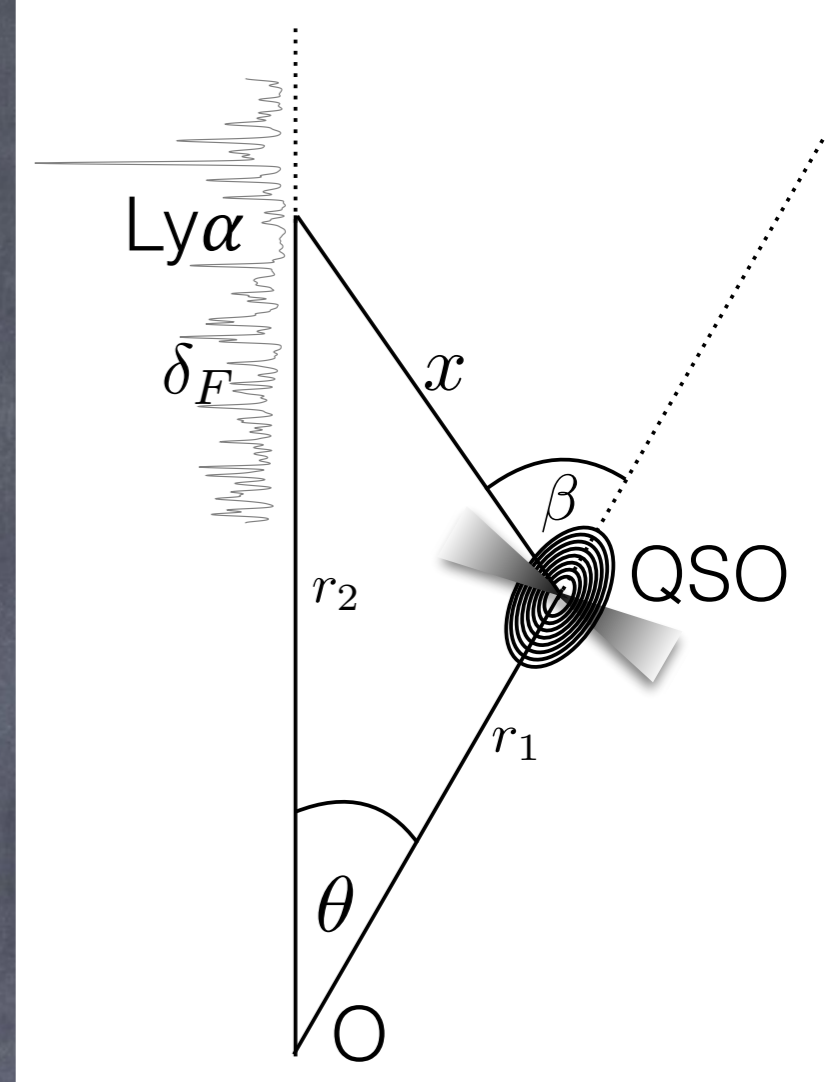
$$\xi_{Q\alpha}(z_1, z_2, \theta) = \langle \Delta_Q(\mathbf{n}_1, z_1) \delta_F(\mathbf{n}_2, z_2) \rangle$$

$$\xi_{Q\alpha} = \xi_{Q\alpha}^{\text{newt}} + \xi_{Q\alpha}^{\text{magnification}} + \xi_{Q\alpha}^{\text{relativistic}}$$

$$\begin{aligned} \xi_{Q\alpha}^{\text{Doppler}} &\sim (-b_Q \mathcal{R}_\alpha + \mathcal{R}_Q b_\alpha) \int \frac{dk}{2\pi^2} k^2 f P(k) j_1(kx) \frac{\mathcal{H}}{k} \\ &+ (-\mathcal{R}_\alpha + \mathcal{R}_Q b_\nu) \int \frac{dk}{2\pi^2} k^2 f^2 P(k) \left[\frac{3}{5} j_1(kx) - \frac{2}{5} j_3(kx) \right] \frac{\mathcal{H}}{k} \\ &+ \mathcal{R}_\alpha \mathcal{R}_Q \int \frac{dk}{2\pi^2} k^2 f^2 P(k) \left[\frac{1}{3} j_0(kx) - \frac{2}{3} j_2(kx) \right] \left(\frac{\mathcal{H}}{k} \right)^2 \end{aligned}$$

Order $\mathcal{O}(\mathcal{H}/k)$

Odd spherical Bessel functions



Quasars x Ly-alpha correlation

Irsic, ED, Viel [arXiv:1510.03436]

$$\xi_{Q\alpha}(z_1, z_2, \theta) = \langle \Delta_Q(\mathbf{n}_1, z_1) \delta_F(\mathbf{n}_2, z_2) \rangle$$

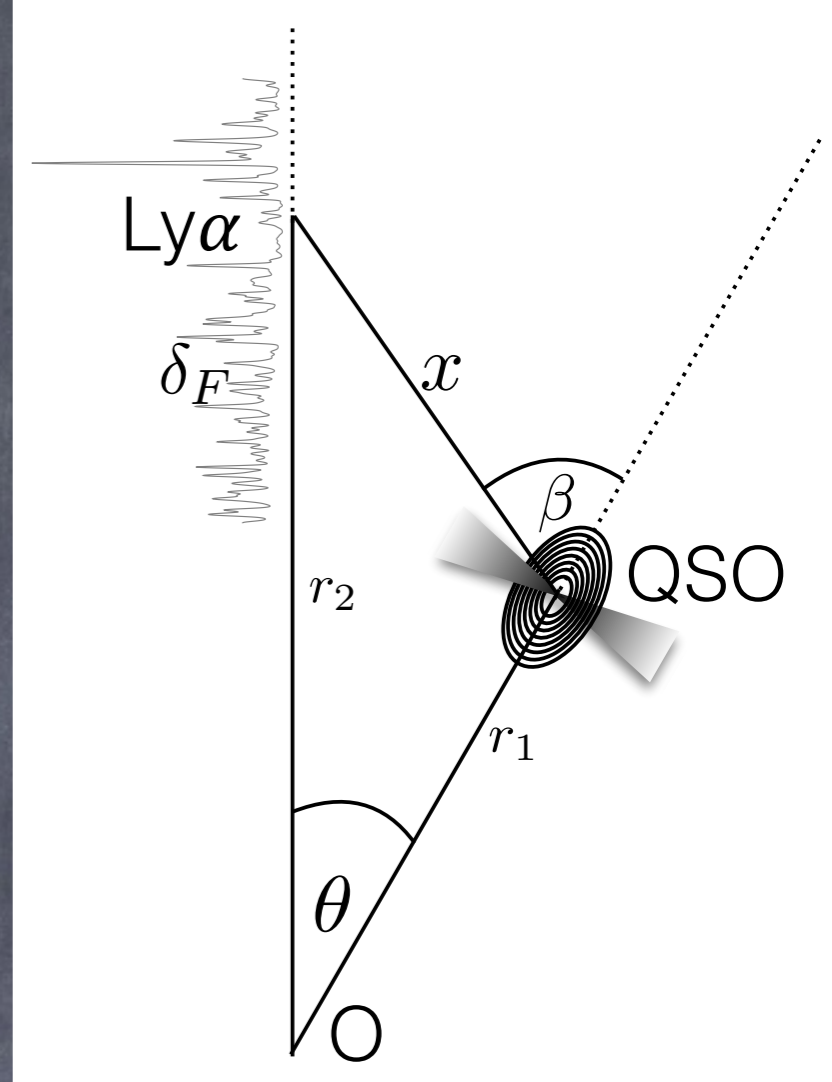
$$\xi_{Q\alpha} = \xi_{Q\alpha}^{\text{newt}} + \xi_{Q\alpha}^{\text{magnification}} + \xi_{Q\alpha}^{\text{relativistic}}$$

$$\begin{aligned} \xi_{Q\alpha}^{\text{Doppler}} \sim & \int \frac{dk}{2\pi^2} k^2 f P(k) j_1(kx) \frac{\mathcal{H}}{k} \\ & + \int \frac{dk}{2\pi^2} k^2 f^2 P(k) \left[\frac{3}{5} j_1(kx) - \frac{2}{5} j_3(kx) \right] \frac{\mathcal{H}}{k} \\ & + \mathcal{R}_\alpha \mathcal{R}_Q \int \frac{dk}{2\pi^2} k^2 f^2 P(k) \left[\frac{1}{3} j_0(kx) - \frac{2}{3} j_2(kx) \right] \left(\frac{\mathcal{H}}{k} \right)^2 \end{aligned}$$

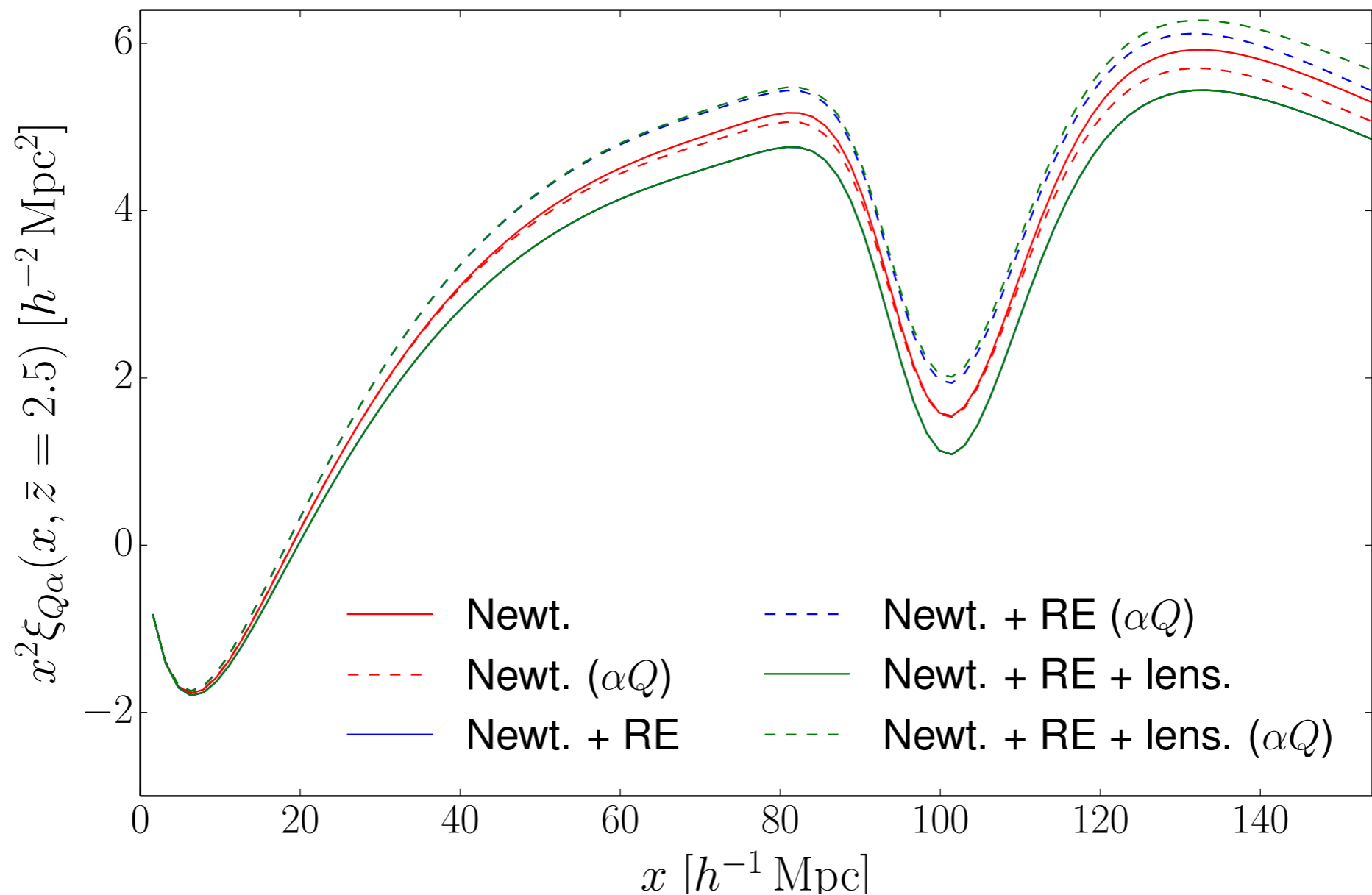
Order $\mathcal{O}(\mathcal{H}/k)$ $\mathcal{O}(\mathcal{H}^2/k^2)$

~~Even~~

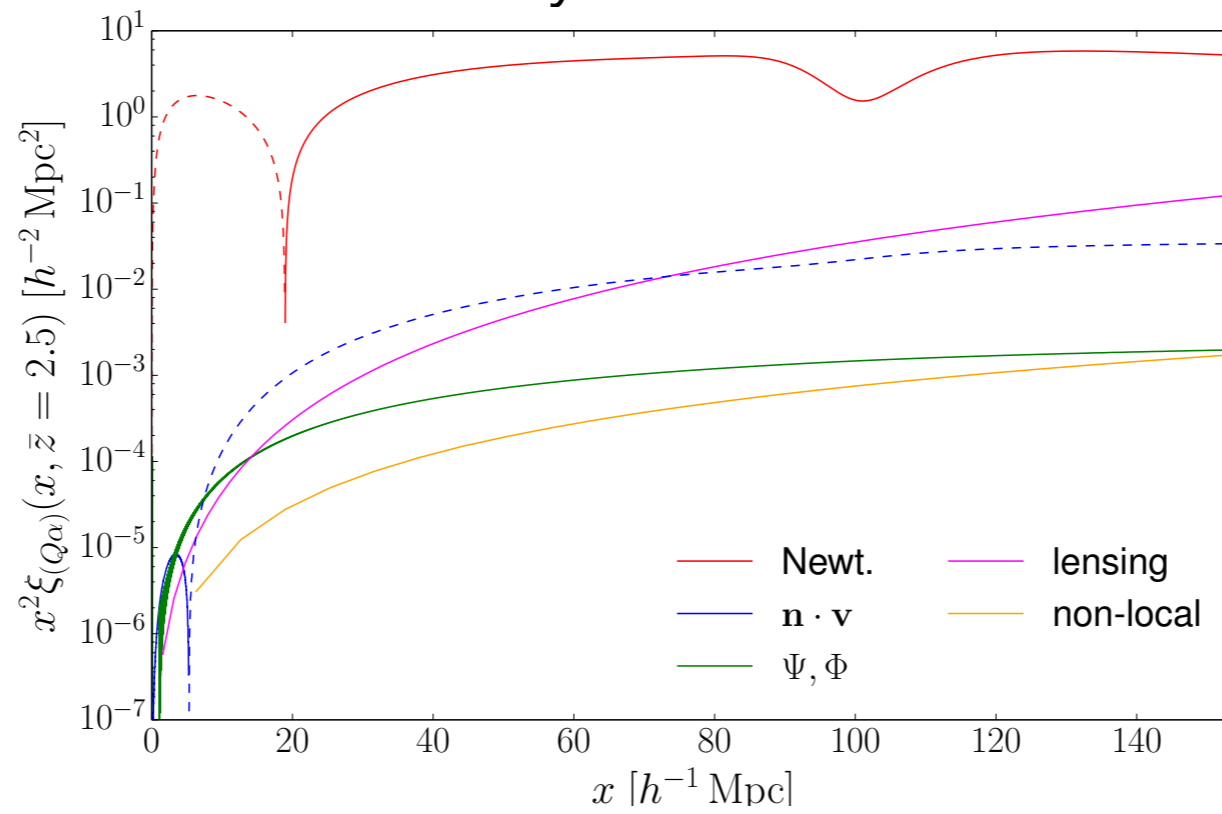
~~Odd~~ spherical Bessel functions



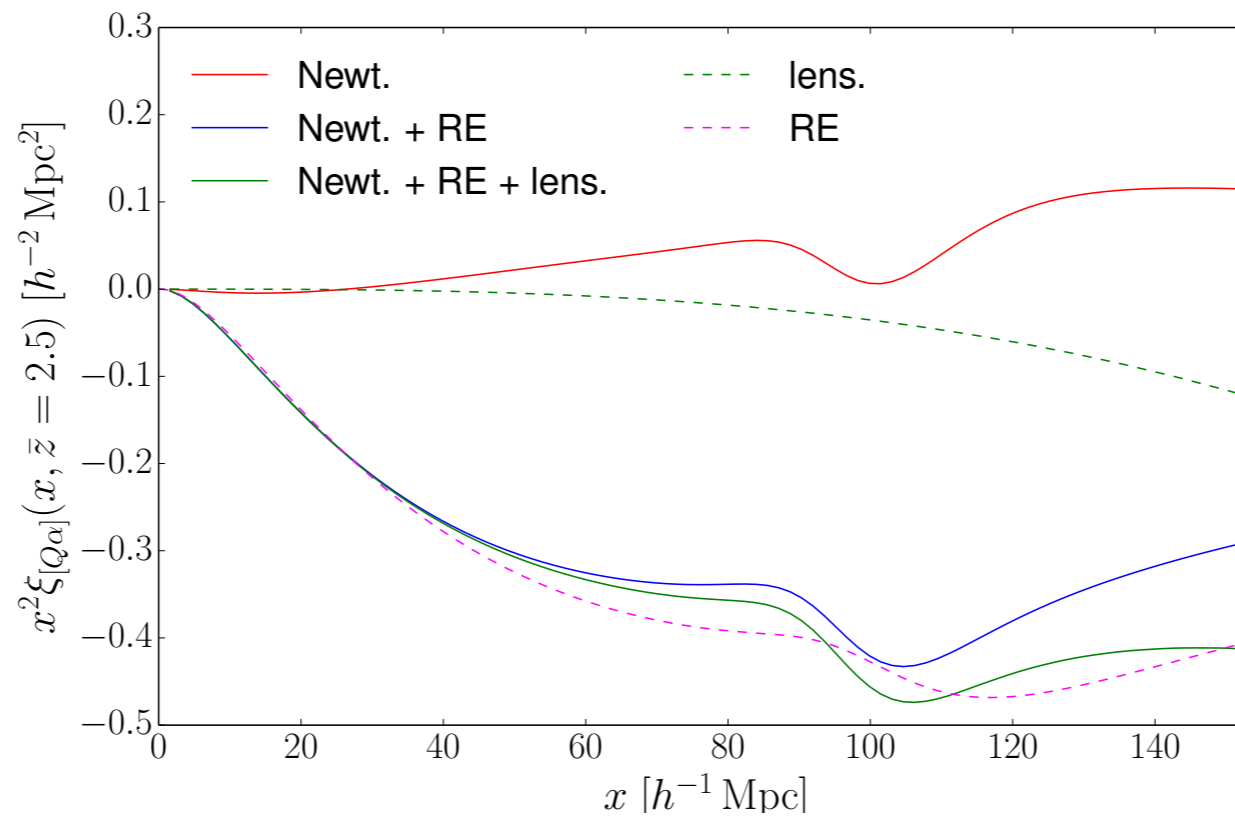
Relativistic effects on Lyman- α forest



Symmetric

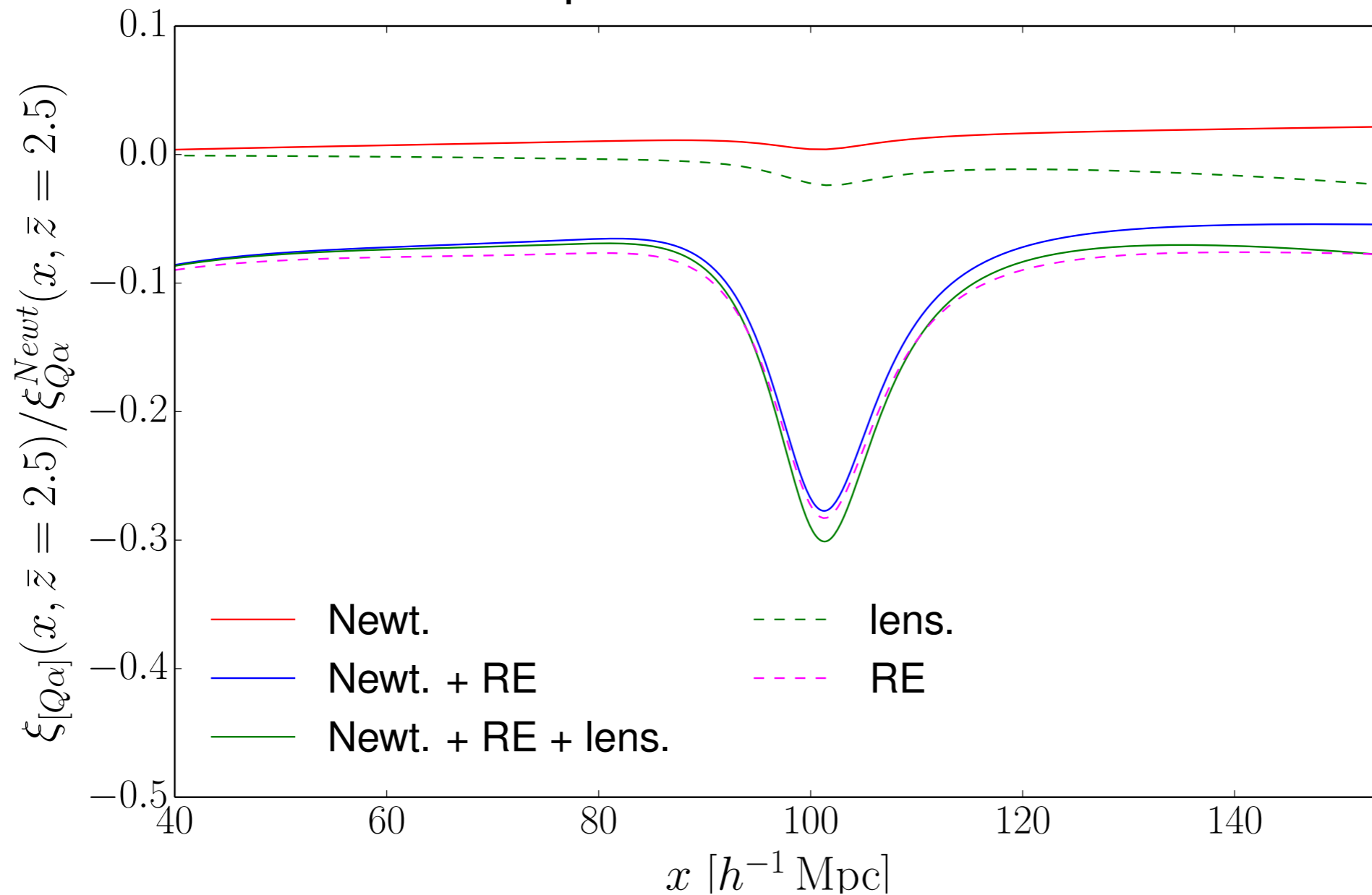


Anti-Symmetric



Relativistic effects on Lyman- α forest

Amplitude of effect



Single tracer vs multi-tracers

	single	multi
Leading order correction	$\mathcal{O}(\mathcal{H}^2/k^2)$	$\mathcal{O}(\mathcal{H}/k)$
Parity	even	odd
Relevant scales	super-Hubble	all
Limited by	cosmic variance	shot noise
Forecasted detection	No	Yes