

Model dependence of cosmic rays propagation parameters

Yoann Génolini

December 17th, 2015

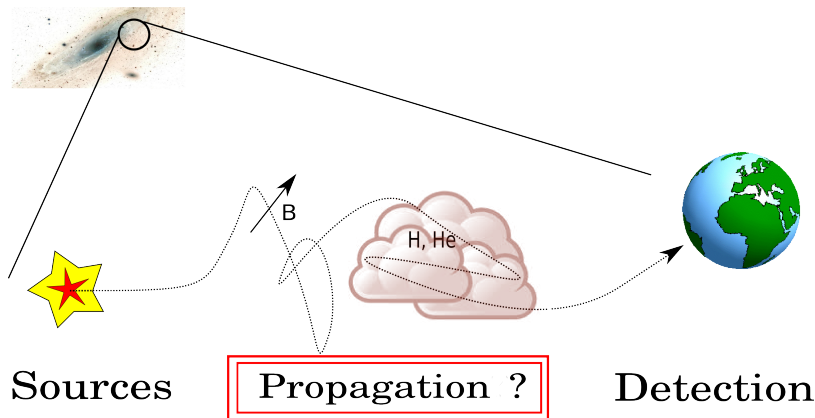
LAPTh

Y. Génolini, A. Putze, P. Salati, and P. D. Serpico, *A&A* 580, A9 (2015) [arXiv:1504.03134]

Outline

- 1 Why propagation is interesting ?
- 2 Modeling the propagation
- 3 Measuring CRs parameters
- 4 Quantifying uncertainties

We don't measure directly the sources !



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The model has to take into account :

- Sources spectra :

→ $Q(E_k) \propto R^\alpha$, with $R(E_k) = p/(Ze)$ and $\alpha \in [-2.5, -2.0]$

- Transport (In the case of a weak electromagnetic turbulence) :

→ Diffusion in phase space (x, p) $D_x = D_0 \cdot \beta \cdot R^\delta$
→ Convective wind u .

- Interaction with the ISM :

→ Energy losses
→ Spallation $(\sigma_\alpha, \sigma_{\alpha \rightarrow \beta})$

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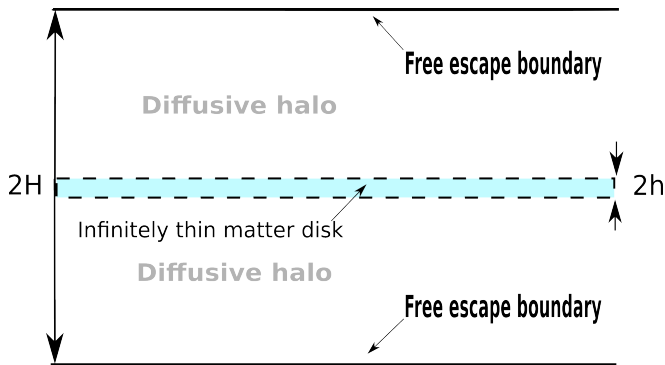
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A Simplified propagation equation for : $E_k > 10 \text{ GeV/nuc}$

- Interaction with the ISM
- Radioactivity
- Diffusion in space
- Source term

$$\frac{\partial f_a}{\partial t} + \sigma_a v_a n_{ISM} f_a + \frac{f_a}{\tau_a} - \nabla_{\mathbf{x}} \cdot (D_x \nabla_{\mathbf{x}} f_a) = q_a + \sum_{Z_\beta \geq Z_a}^{Z_{max}} \sigma_{b \rightarrow a} v_b n_{ISM} f_b + \frac{f_b}{\tau_b}$$

Galaxy model :



Surface density of the disc $\mu = 2.4 \text{ mg.cm}^{-2}$.

Analytical resolution of the propagation equation :

For a stable nucleus :

$$\mathcal{J}_a(E_k) = \left\{ Q_a + \sum_{Z_b \geq Z_a}^{Z_{max}} \sigma_{b \rightarrow a} \mathcal{J}_b \right\} / \{ \sigma^{\text{diff}} + \sigma_a \} \quad (1)$$

Primary and secondary source terms.

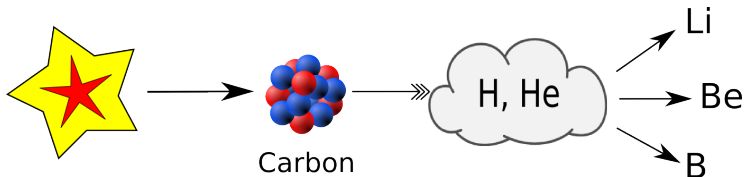
$$\text{Where : } \sigma^{\text{diff}} = \frac{2D m_{ISM}}{\mu v H}.$$

$$\text{and } Q_a = \frac{1}{4\pi} \frac{q_a}{n_{ISM}} \equiv N_a \left(\frac{\mathcal{R}}{1 \text{ GV}} \right)^\alpha.$$

Outline

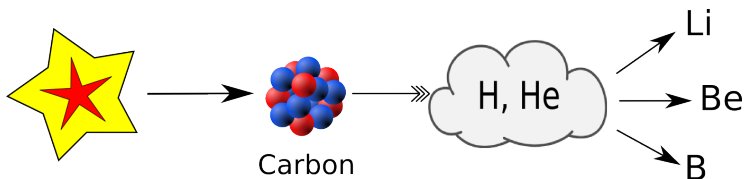
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Secondary/primary ratio :

$$\mathcal{J}_B(E_k) = \left\{ Q_B + \sum_{Z_b \geq Z_B}^{Z_{max}} \sigma_{b \rightarrow B} \mathcal{J}_b \right\} / \{ \sigma^{\text{diff}} + \sigma_B \} \quad (2)$$

Hypothesis :

- $Q_B = 0$
- Double nuclei system (B,C)

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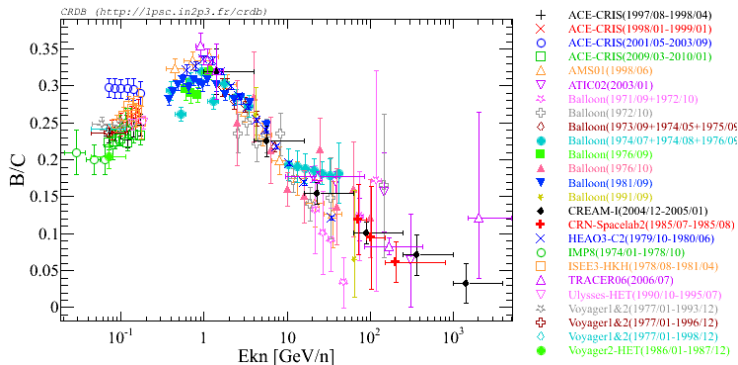
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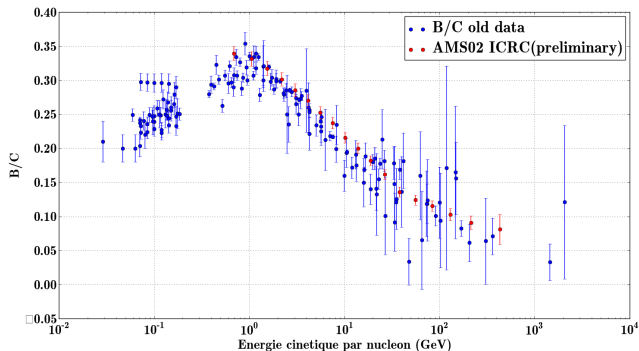
$$\frac{\mathcal{J}_B(E_k)}{\mathcal{J}_C(E_k)} = \sigma_{C \rightarrow B} / \{ \sigma^{\text{diff}} + \sigma_B \} .$$

When : $\sigma_B \ll \sigma^{\text{diff}} \Rightarrow \frac{\mathcal{J}_B}{\mathcal{J}_C} \propto R^{-\delta}$

Experimental data :



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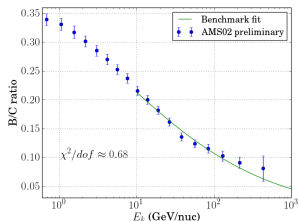


New data with AMS02 !..and soon CALET !

Benchmark model :

The goal is to minimize :

$$\chi_{B/C}^2 = \sum_i \left\{ \frac{\mathcal{F}_i^{\text{exp}} - \mathcal{F}_i^{\text{th}}(\text{Parameters..})}{\sigma_i} \right\}^2$$



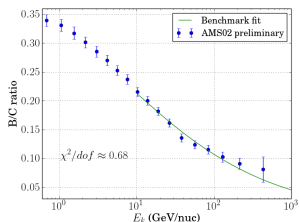
Reference parameter values

D_0 [kpc ² /Myr]	$(5.8 \pm 0.7) \cdot 10^{-2}$
δ	0.44 ± 0.03
$\chi_{B/C}^2/\text{dof}$	$5.4/8 \approx 0.68$
$\gamma = \alpha - \delta$ (fixed)	-2.78

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- Primary boron contribution
- Production cross-section uncertainties
- Destruction cross-section uncertainties
- Geometry framework

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Primary boron ?

[Blasi, 2009], [Blasi and Serpico, 2009],
[Mertsch and Sarkar, 2009], [Mertsch and Sarkar, 2014]
→ **Secondary species may be formed at sources !**

- Confinement inside a SNR at TeV/nuc :

$$X_{SNR} \approx 0.17 \text{ g cm}^{-2} \frac{n_{ISM}}{\text{cm}^{-3}} \frac{T_{SNR}}{2.10^4 \text{ yr}}$$

- Galactic diffusion at TeV/nuc :

$$X_{Diff} \approx 1.2 \text{ g cm}^{-2}$$

⇒ **Order of 10% !**

Primary boron ?

At high energy...

$$\frac{\mathcal{J}_B(E_k)}{\mathcal{J}_C(E_k)} = \left\{ \frac{Q_B}{\mathcal{J}_C} + \sigma_{C \rightarrow B} + \sum_{Z_b > Z_C}^{Z_{max}} \sigma_{b \rightarrow B} \frac{\mathcal{J}_b}{\mathcal{J}_C} \right\} / \{ \sigma^{\text{diff}} + \sigma_B \}$$

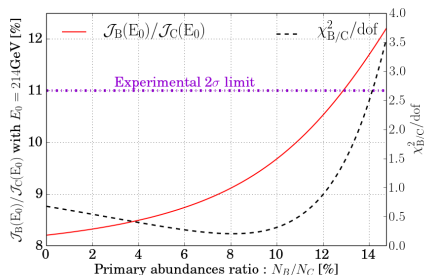
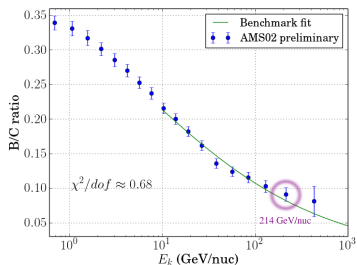
$$\propto \frac{N_B}{N_C}$$

$$HE$$

...it leads to a plateau.

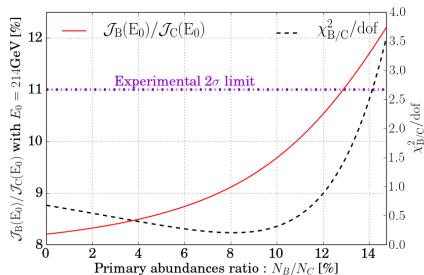
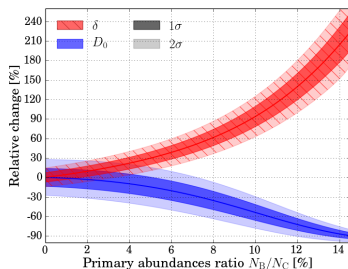
Primary boron ?

Constraining $\frac{N_B}{N_C}$:



Primary boron ?

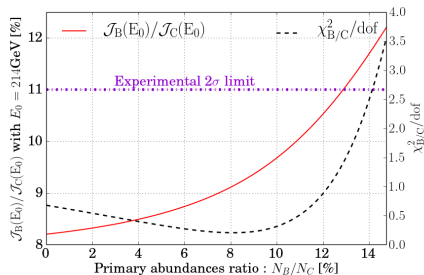
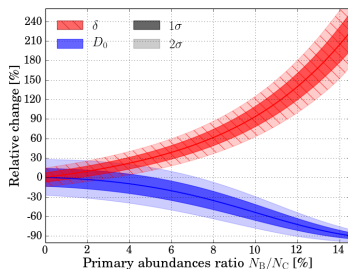
Scan on $\frac{N_B}{N_C}$:



→ Huge impact on the determination of delta !

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Models of cross sections :

The different models for calculating cross section :

- are based on old data.
- extrapolate values to high energy.
- in some cases data do not exist at all.

$$\frac{\mathcal{J}_B(E_k)}{\mathcal{J}_C(E_k)} = \sum_{Z_b \geq Z_C}^{Z_{max}} \sigma_{b \rightarrow B} \frac{\mathcal{J}_b}{\mathcal{J}_C} / \{ \sigma^{\text{diff}} + \sigma_B \}$$

⇒ Typical differences of 10 % are commonly observed.

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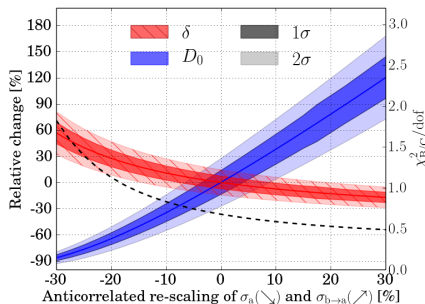
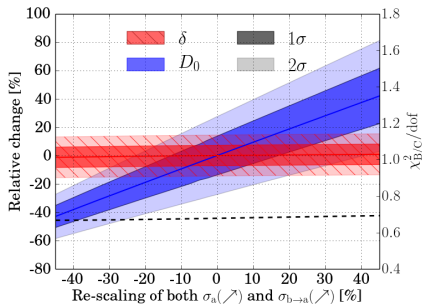
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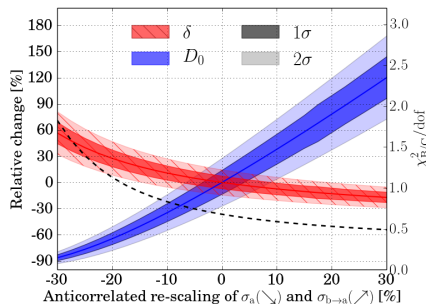
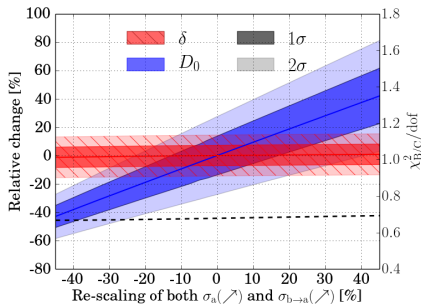
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Dependence of propagation parameters on a systematic rescaling :



→ Huge impact again !

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Summary of the main systematics :

	Wind	1D/2D geometry	Cross-sections	Primary boron
$\Delta D_0/D_0$	-40%	-2 to -13%	$\pm 60\%$	0 to -90%
$\Delta \delta/\delta$	+15%	0 to +1%	$\pm 20\%$	0 to +100%

Prospects, what we need at zero order :

- ① Find a way to quantify primary boron contribution.
- ② New precise measurements of nuclear cross-sections.

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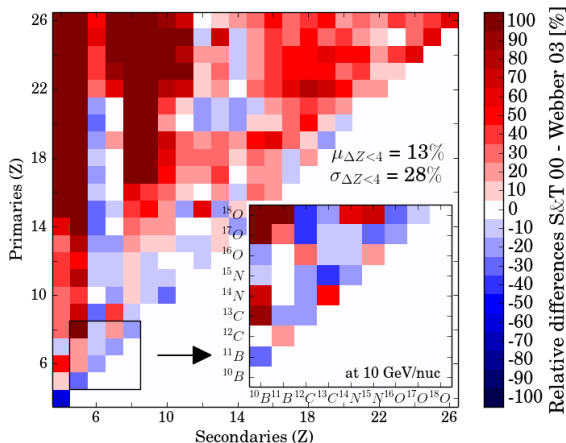
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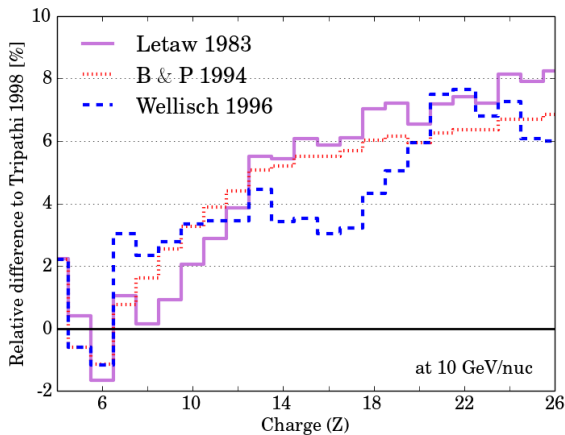
Thanks for listening !

Backup slides !

2-Models of production cross sections :



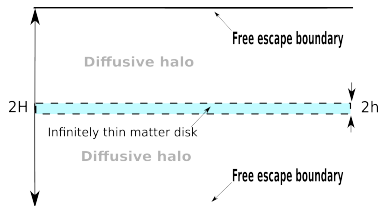
3-Models of **destruction** cross sections :



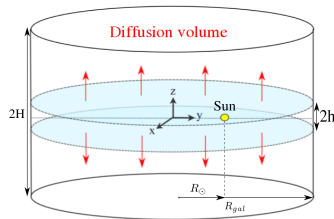
4-1D/2D diffusion models ?

The two commonly used geometries :

1D



2D



1D/2D diffusion models ?

Geometry	Plane – 1D	Cylindrical – 2D homogeneous source distribution	Cylindrical – 2D realistic source distribution
D_0 [kpc^2/Myr]	$(5.8 \pm 0.7) \cdot 10^{-2}$	$(5.7 \pm 0.7) \cdot 10^{-2}$	$(5.0 \pm 0.6) \cdot 10^{-2}$
$\Delta D_0^{\text{1D}}/D_0^{\text{1D}}$	N/A	-2%	-13%
δ	0.441 ± 0.031	0.439 ± 0.031	0.445 ± 0.032
$\Delta \delta^{\text{1D}}/\delta^{\text{1D}}$	N/A	0%	+1%
$\chi_{\text{B/C}}^2/\text{ndof}$	$5.4/8 \approx 0.68$	$5.4/8 \approx 0.68$	$5.5/8 \approx 0.69$

→ Tiny impact !

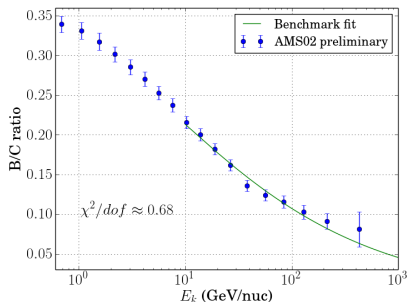
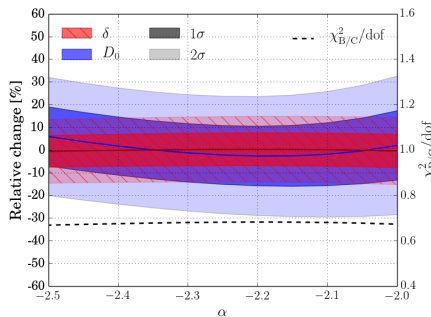
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$\Delta D_0^{1D} / D_0^{1D}$	N/A	-2%	-13%
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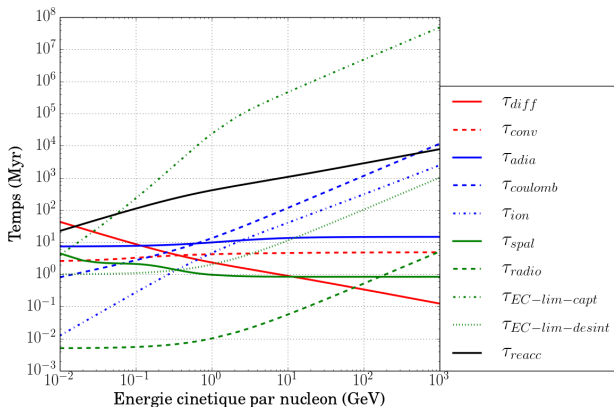
→ **Tiny impact !**

Test of the model

Independence of the spectral index α :



Simplifying the equation :



Models of production cross sections :

Main production channels $\sigma_{\text{CNO}} \rightarrow \text{B}$ at 10 GeV/nuc	Webber 03 [mb]	S&T 2000 [%]	Webber 98 [%]	Webber 93 [%]
$\sigma \left(\begin{matrix} {}^{12}_6\text{C} \rightarrow {}^{10}_5\text{B} \\ {}^{12}_6\text{C} \rightarrow {}^{11}_5\text{B} \end{matrix} \right)$	14.0	-2.2	22	26
$\sigma \left(\begin{matrix} {}^{13}_6\text{C} \rightarrow {}^{10}_5\text{B} \\ {}^{13}_6\text{C} \rightarrow {}^{11}_5\text{B} \end{matrix} \right)$	47.0	13	14	18
$\sigma \left(\begin{matrix} {}^{13}_6\text{C} \rightarrow {}^{10}_5\text{B} \\ {}^{13}_6\text{C} \rightarrow {}^{11}_5\text{B} \end{matrix} \right)$	4.70	48	-2.1	0
$\sigma \left(\begin{matrix} {}^{13}_6\text{C} \rightarrow {}^{10}_5\text{B} \\ {}^{13}_6\text{C} \rightarrow {}^{11}_5\text{B} \end{matrix} \right)$	40.0	-26	2.2	4.3
$\sigma \left(\begin{matrix} {}^{14}_7\text{N} \rightarrow {}^{10}_5\text{B} \\ {}^{14}_7\text{N} \rightarrow {}^{11}_5\text{B} \end{matrix} \right)$	9.90	40	0.14	1.0
$\sigma \left(\begin{matrix} {}^{14}_7\text{N} \rightarrow {}^{10}_5\text{B} \\ {}^{14}_7\text{N} \rightarrow {}^{11}_5\text{B} \end{matrix} \right)$	27.2	1.8	-8.9	-11
$\sigma \left(\begin{matrix} {}^{15}_7\text{N} \rightarrow {}^{10}_5\text{B} \\ {}^{15}_7\text{N} \rightarrow {}^{11}_5\text{B} \end{matrix} \right)$	9.20	-7.0	-71	-71
$\sigma \left(\begin{matrix} {}^{15}_7\text{N} \rightarrow {}^{10}_5\text{B} \\ {}^{15}_7\text{N} \rightarrow {}^{11}_5\text{B} \end{matrix} \right)$	28.0	-0.40	-27	-28
$\sigma \left(\begin{matrix} {}^{16}_8\text{O} \rightarrow {}^{10}_5\text{B} \\ {}^{16}_8\text{O} \rightarrow {}^{11}_5\text{B} \end{matrix} \right)$	10.7	-22	-7.7	8.4
$\sigma \left(\begin{matrix} {}^{16}_8\text{O} \rightarrow {}^{10}_5\text{B} \\ {}^{16}_8\text{O} \rightarrow {}^{11}_5\text{B} \end{matrix} \right)$	24.0	2.8	-9.4	-11
$\sigma \left(\begin{matrix} {}^{17}_8\text{O} \rightarrow {}^{10}_5\text{B} \\ {}^{17}_8\text{O} \rightarrow {}^{11}_5\text{B} \end{matrix} \right)$	3.60	56	0.27	0
$\sigma \left(\begin{matrix} {}^{17}_8\text{O} \rightarrow {}^{10}_5\text{B} \\ {}^{17}_8\text{O} \rightarrow {}^{11}_5\text{B} \end{matrix} \right)$	19.7	22	1.4	0
$\sigma \left(\begin{matrix} {}^{18}_8\text{O} \rightarrow {}^{10}_5\text{B} \\ {}^{18}_8\text{O} \rightarrow {}^{11}_5\text{B} \end{matrix} \right)$	0.70	89	6.3	4.3
$\sigma \left(\begin{matrix} {}^{18}_8\text{O} \rightarrow {}^{10}_5\text{B} \\ {}^{18}_8\text{O} \rightarrow {}^{11}_5\text{B} \end{matrix} \right)$	12.0	53	2.2	0.80

Propagation equation :

- Convection
- Interaction with the ISM
- Radioactivity
- Diffusion in phase space
- Source term

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 \frac{\partial f_a}{\partial t} + & \mathbf{u} \cdot \nabla_{\mathbf{x}} f_a - \frac{1}{3} (\nabla_{\mathbf{x}} \cdot \mathbf{u}) p \frac{\partial f_a}{\partial p} + \nabla_{\mathbf{p}} \cdot (b(\mathbf{p}) f_a) + \sigma_a v_a n_{ISM} f_a + \\
 \frac{f_a}{\tau_a} - & \nabla_{\mathbf{x}} \cdot (D_x \nabla_{\mathbf{x}} f_a) - \nabla_{\mathbf{p}} \cdot (D_p \nabla_{\mathbf{p}} f_a) = \\
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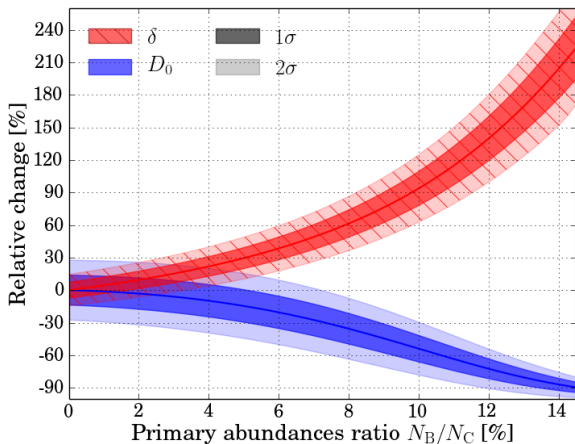
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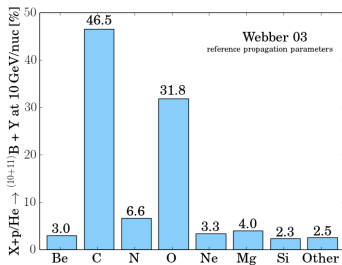
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Primary boron ?

Scan on $\frac{N_B}{N_C}$:



Different weights at $10\text{GeV}/nuc$:



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The origin of the positron excess in cosmic rays.
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