

**The shape of a pulsar radio beam:  
fan beams, not the nested cones**

Jarek Dyks

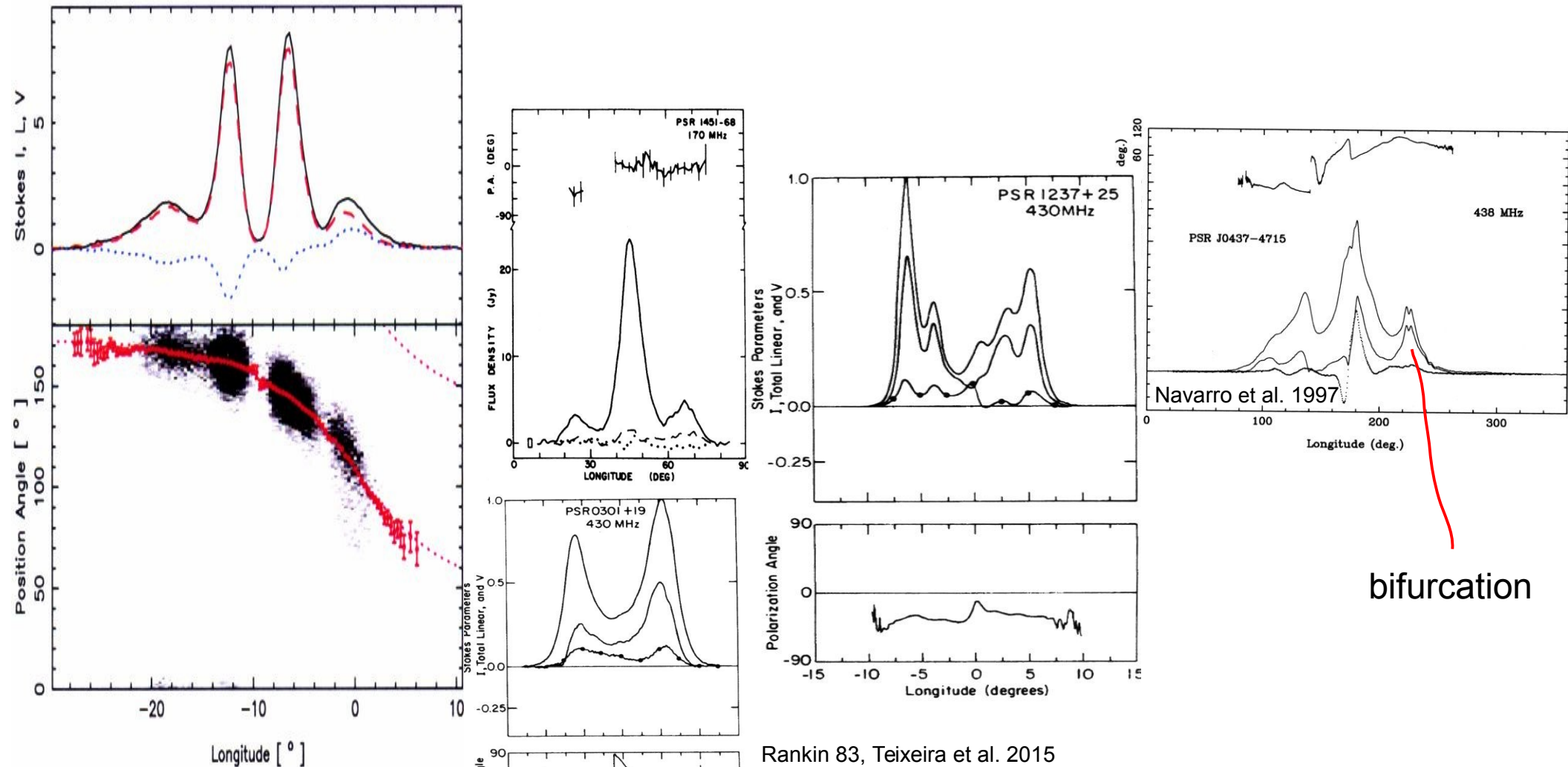
in collaboration with: B. Rudak, M. Pierbattista, L. Saha

Nicolaus Copernicus Astronomical Center  
Polish Academy of Sciences  
Torun

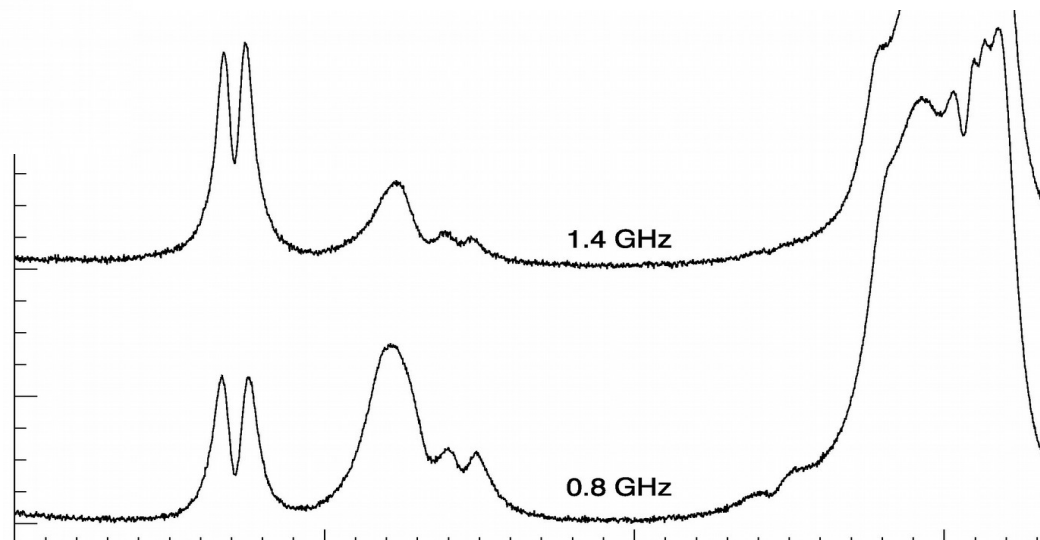
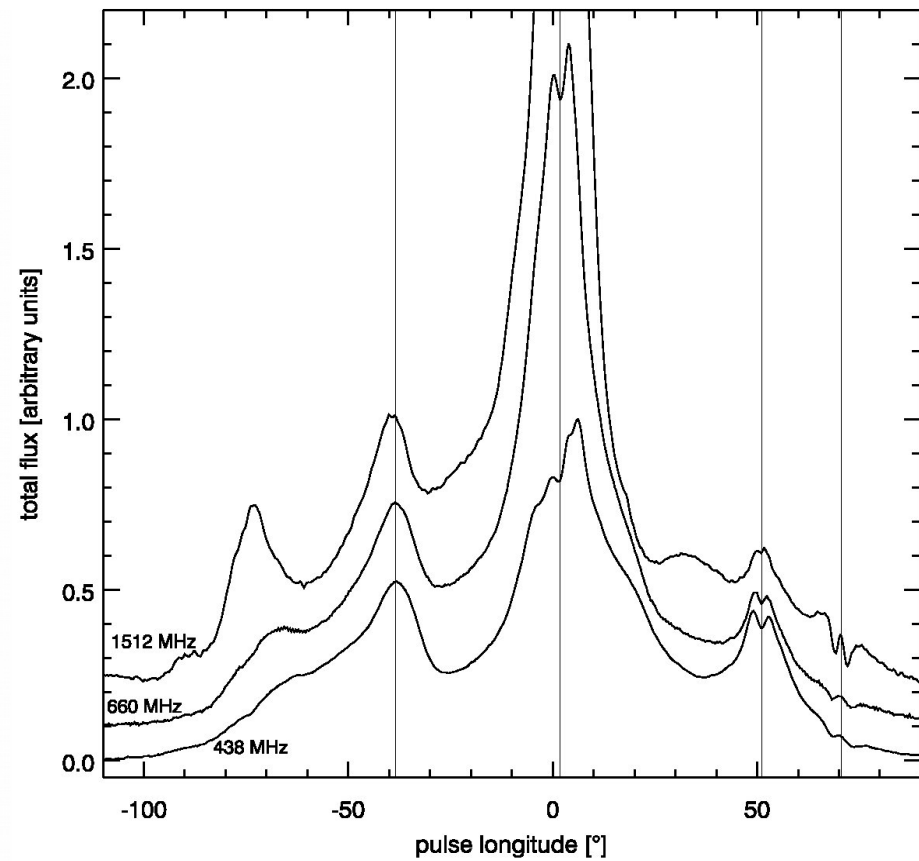
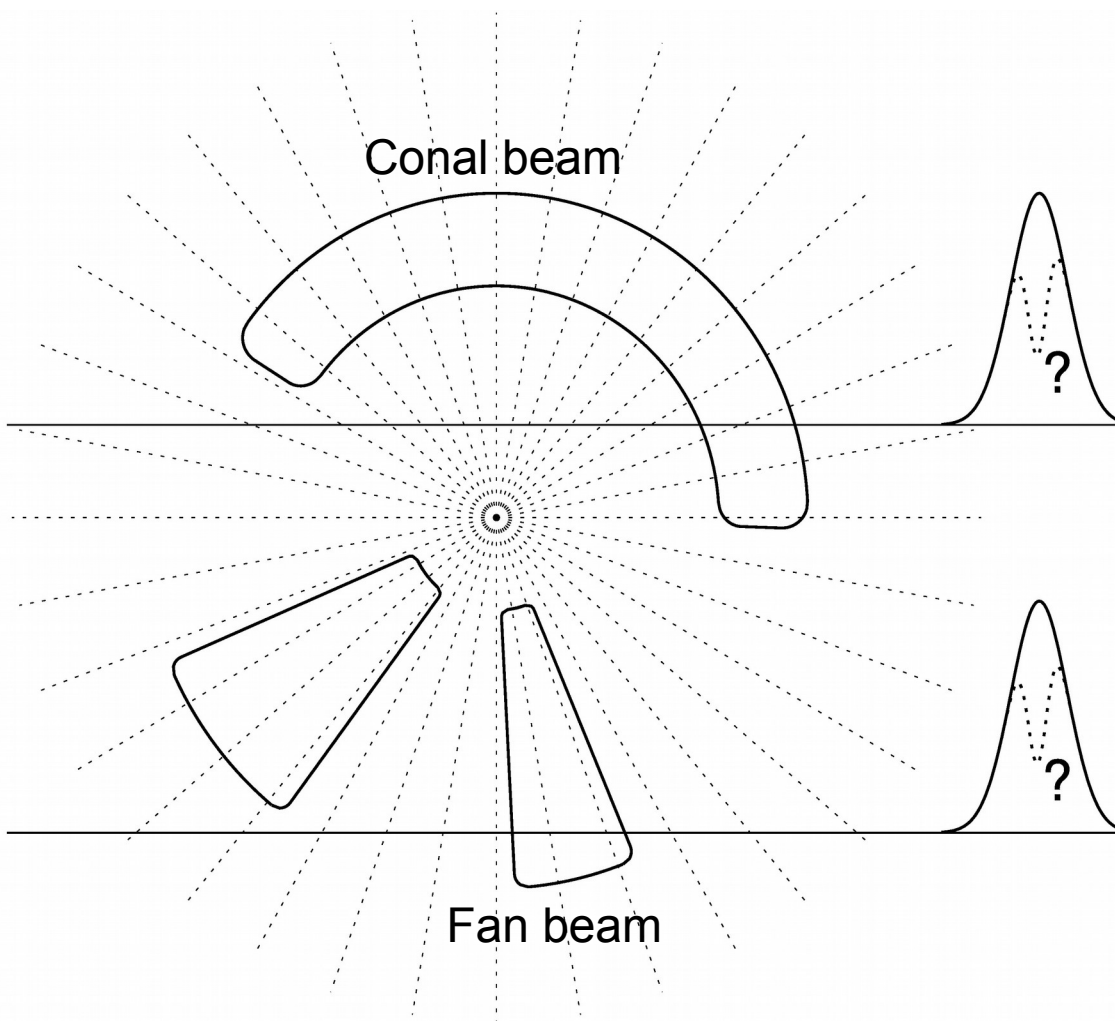
Lyne & Manchester 1988: beams are **patchy**  
 (random distribution of radio-bright spots)

Sure they are, however:

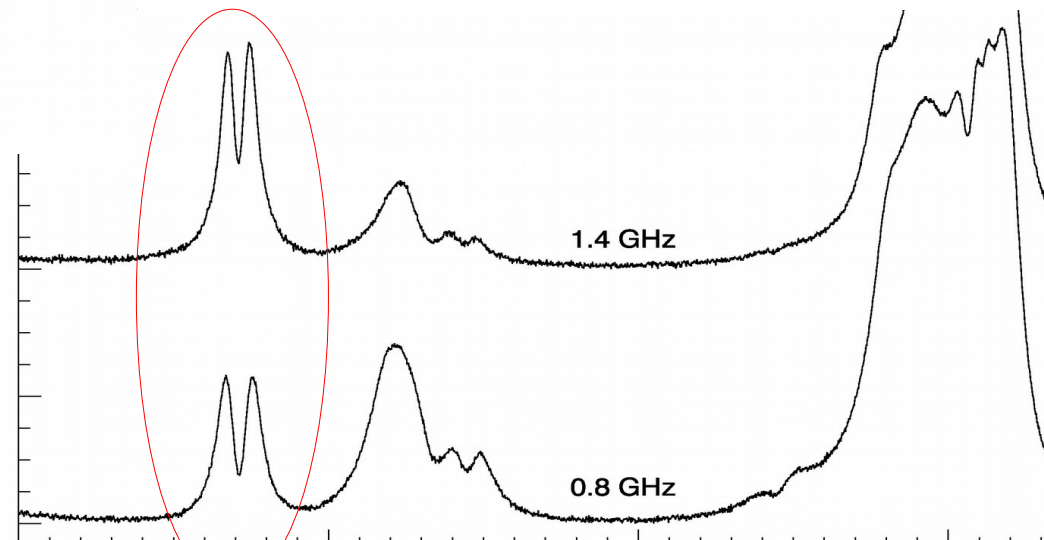
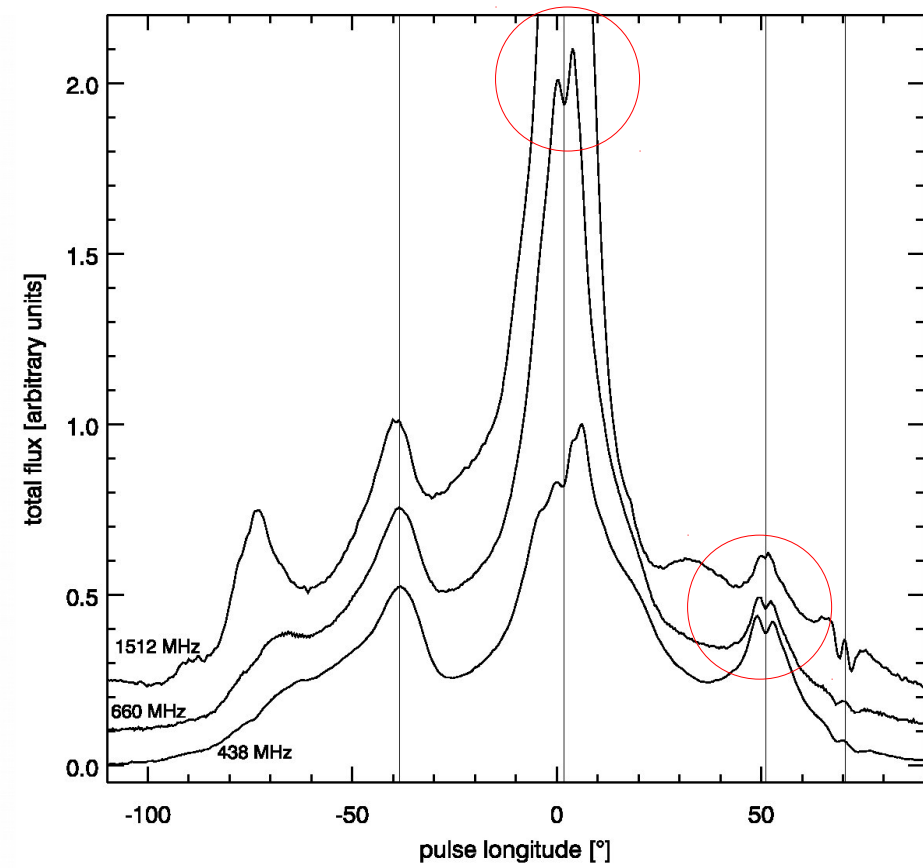
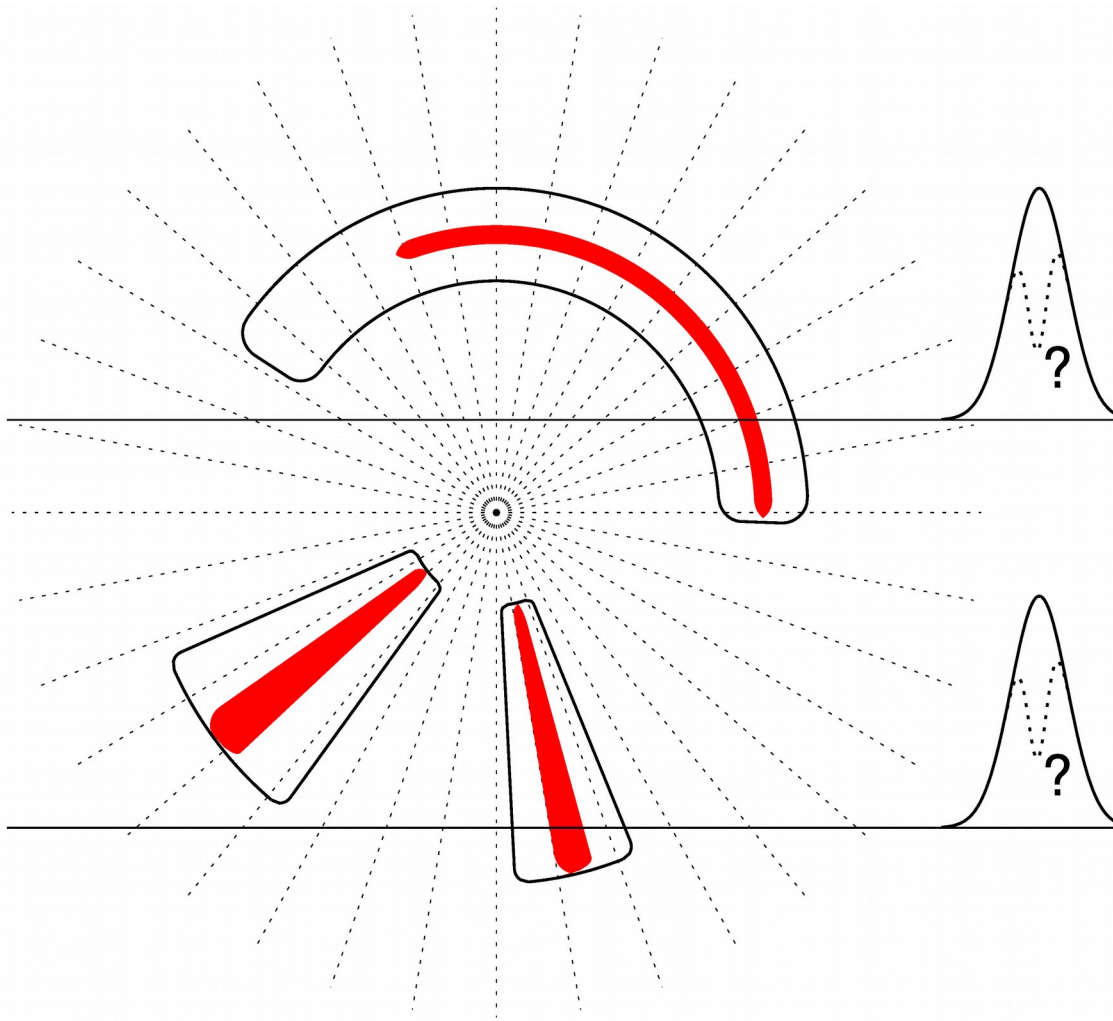
How the patches are elongated?  
 Azimuthally? Or in colatitude?



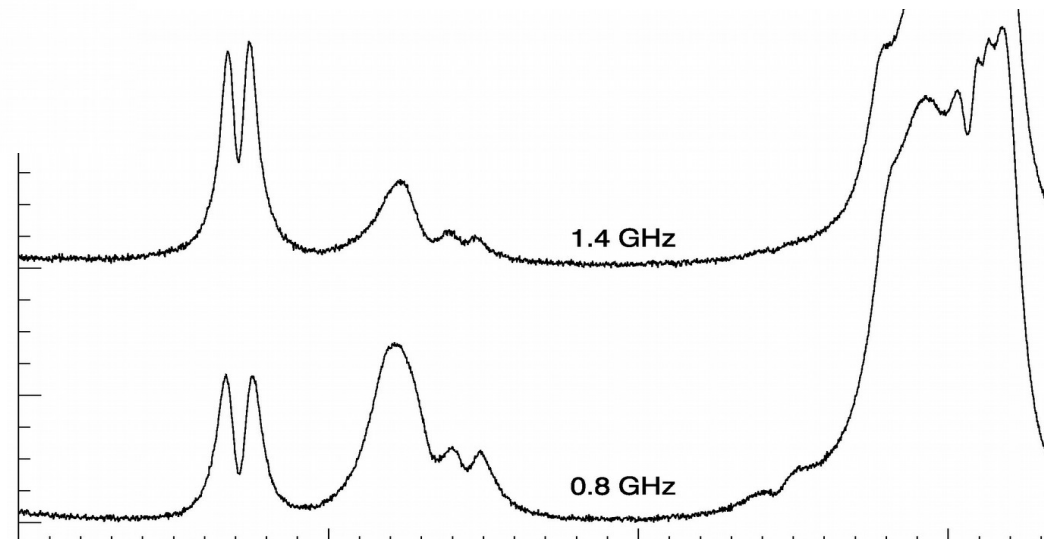
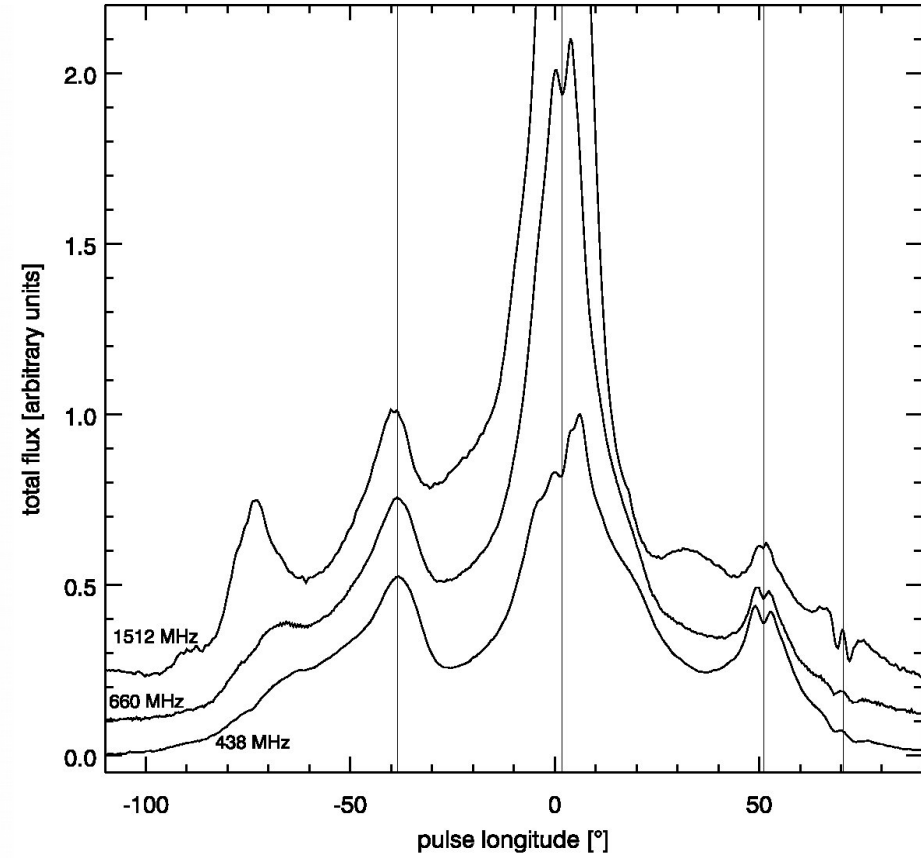
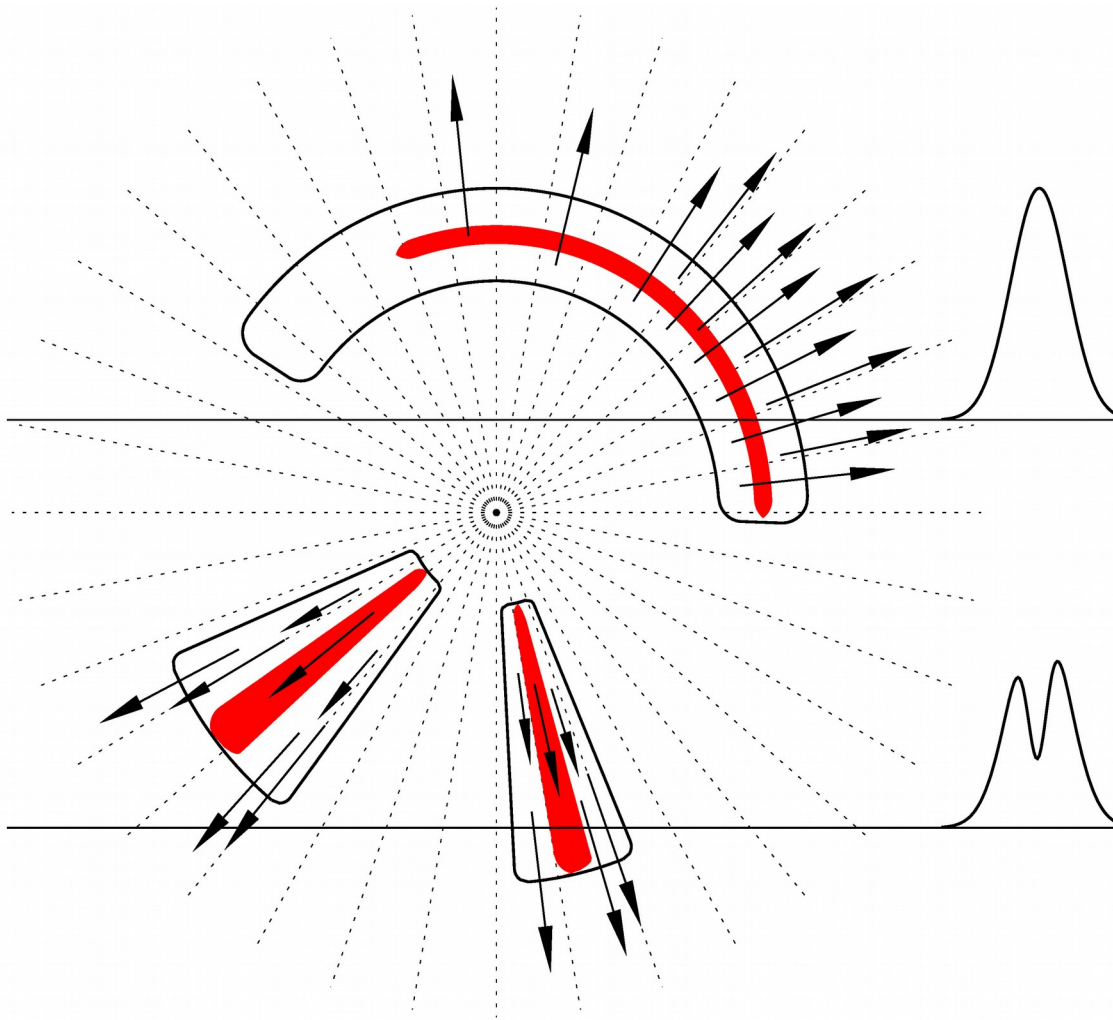
# Bifurcations do not survive if beam geometry is conal



# Bifurcations do not survive if beam geometry is conal

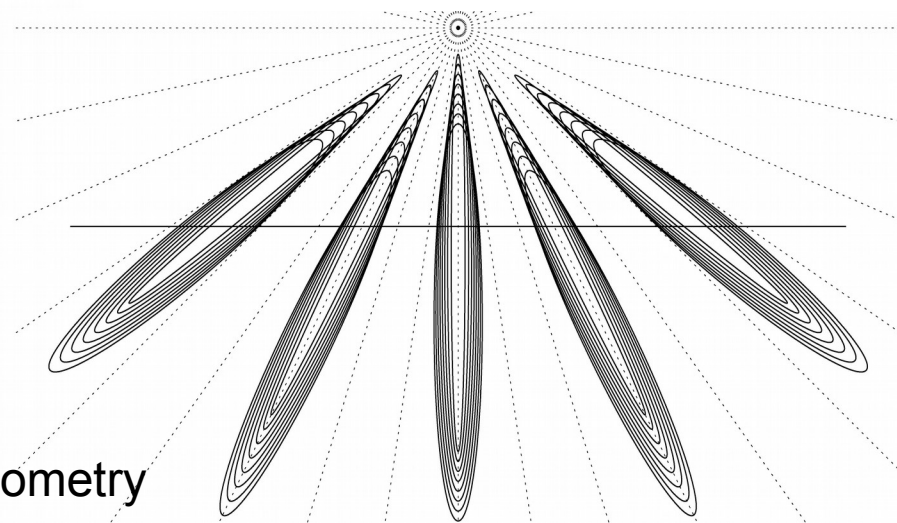
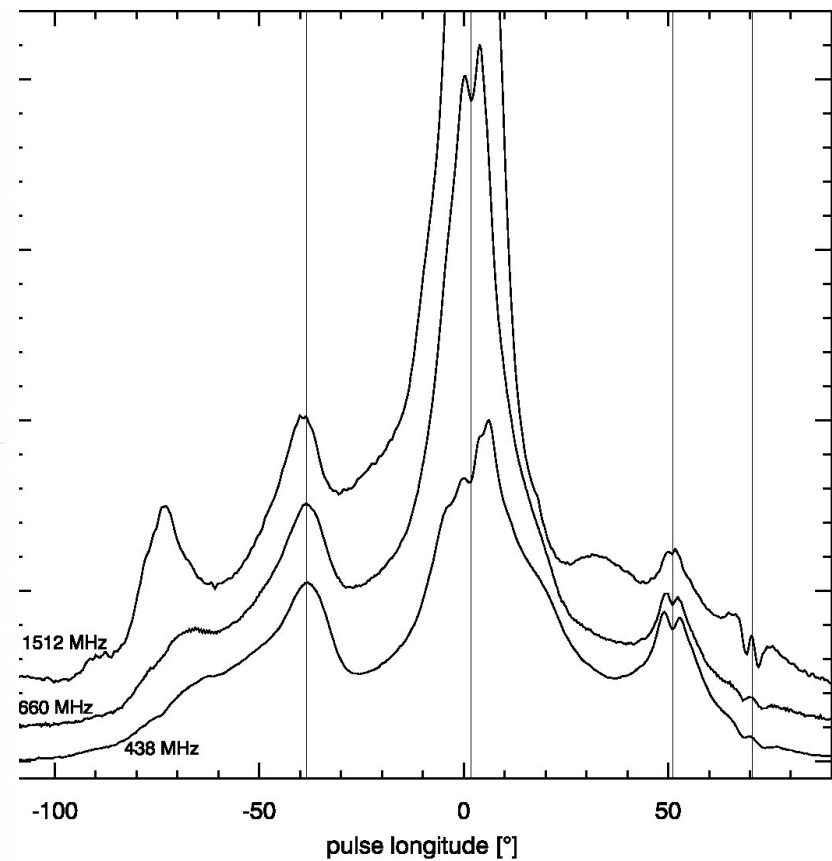
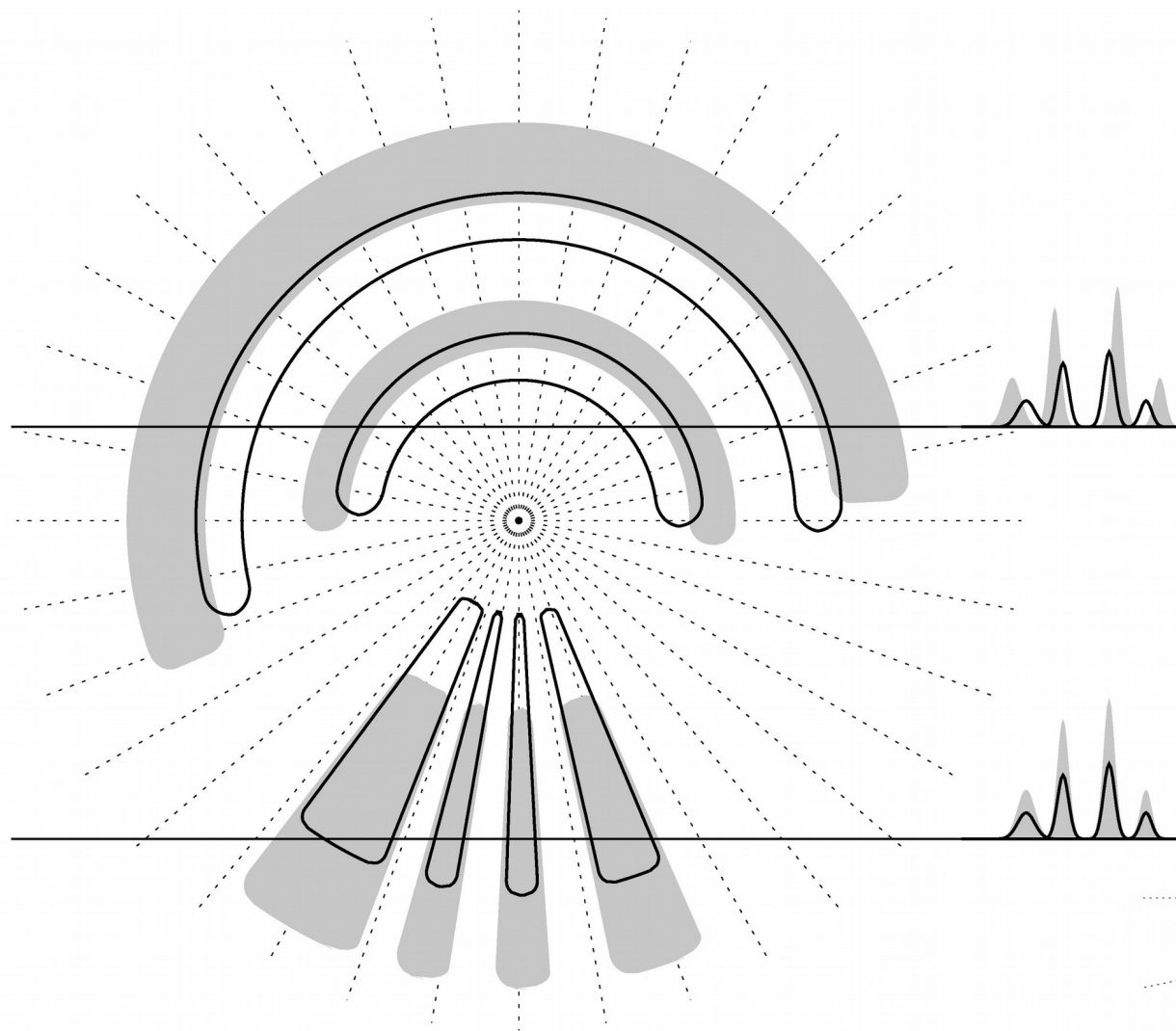


# Bifurcations do not survive if beam geometry is conal





# Weak RFM is natural for stream-shaped / fan-beam emitters



Dyks, Rudak & Demorest 2010  
Navarro et al. 1997  
Osłowski et al. 2014

spoke-like geometry

Prediction: all / most pulsars, including the normal ones (non-millisecond) may have profiles created by fan beams which point at the dipole axis

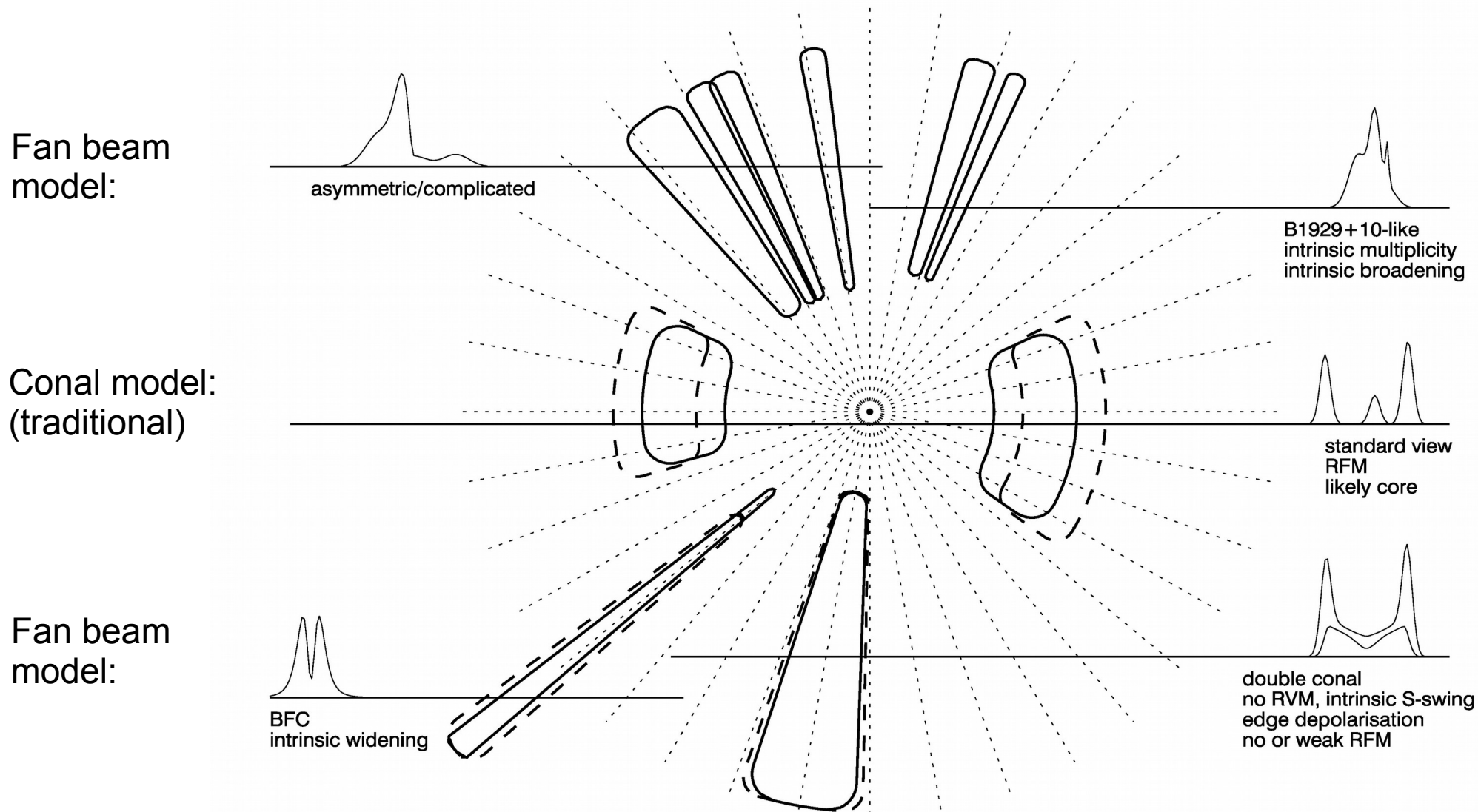
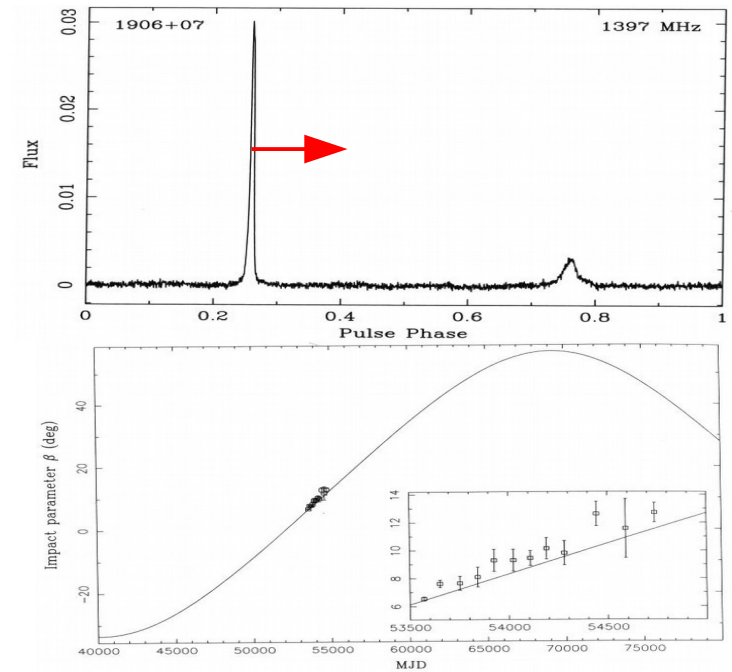


Fig. from Dyks, Rudak & Demorest 2010

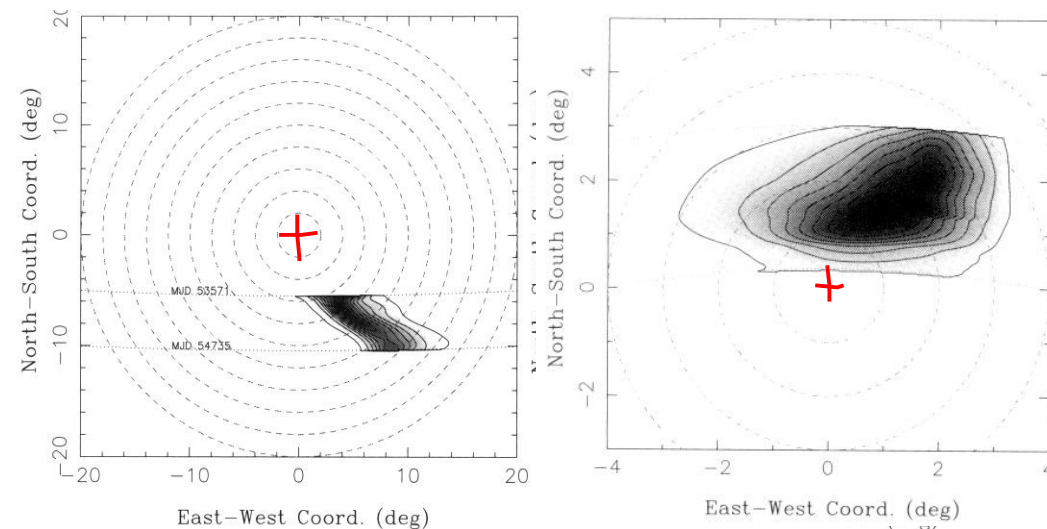
# Beam mapping for precessing pulsars: J1906+0746

Young pulsar:  $P = 0.14$  s, age =  $10^5$  yr  
 $P_{\text{orb}} = 4$  hr,  $P_{\text{prec}} = 165$  yr,  $t_{\text{obs}} = 4$  yr



Desvignes et al. 2012

Observed beam maps:  
red cross: magnetic dipole axis



J1141-6545  
Manchester et al. 2010



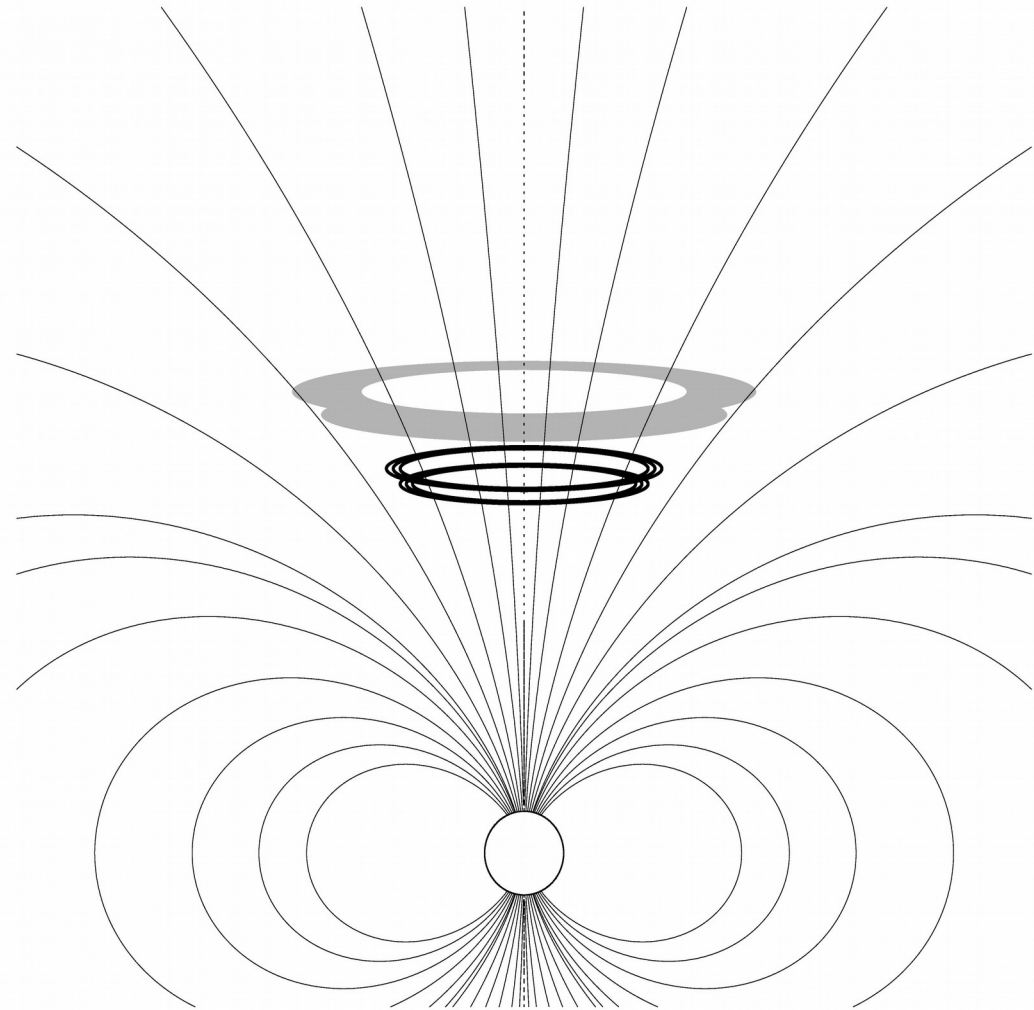
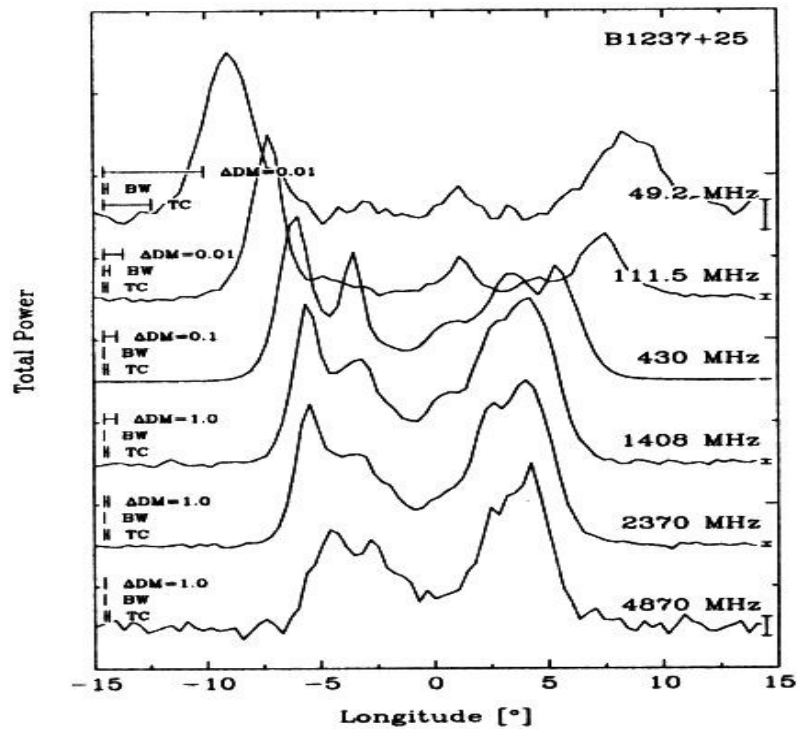
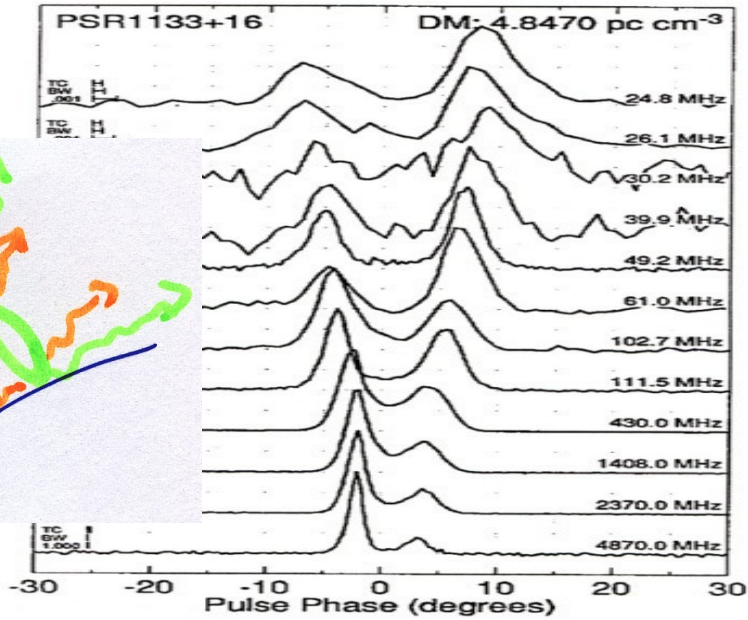
Well, aren't all these pulsars:

- with notches
- with bifurcated components,
- young,
- precessing,
- and millisecond

just peculiar?

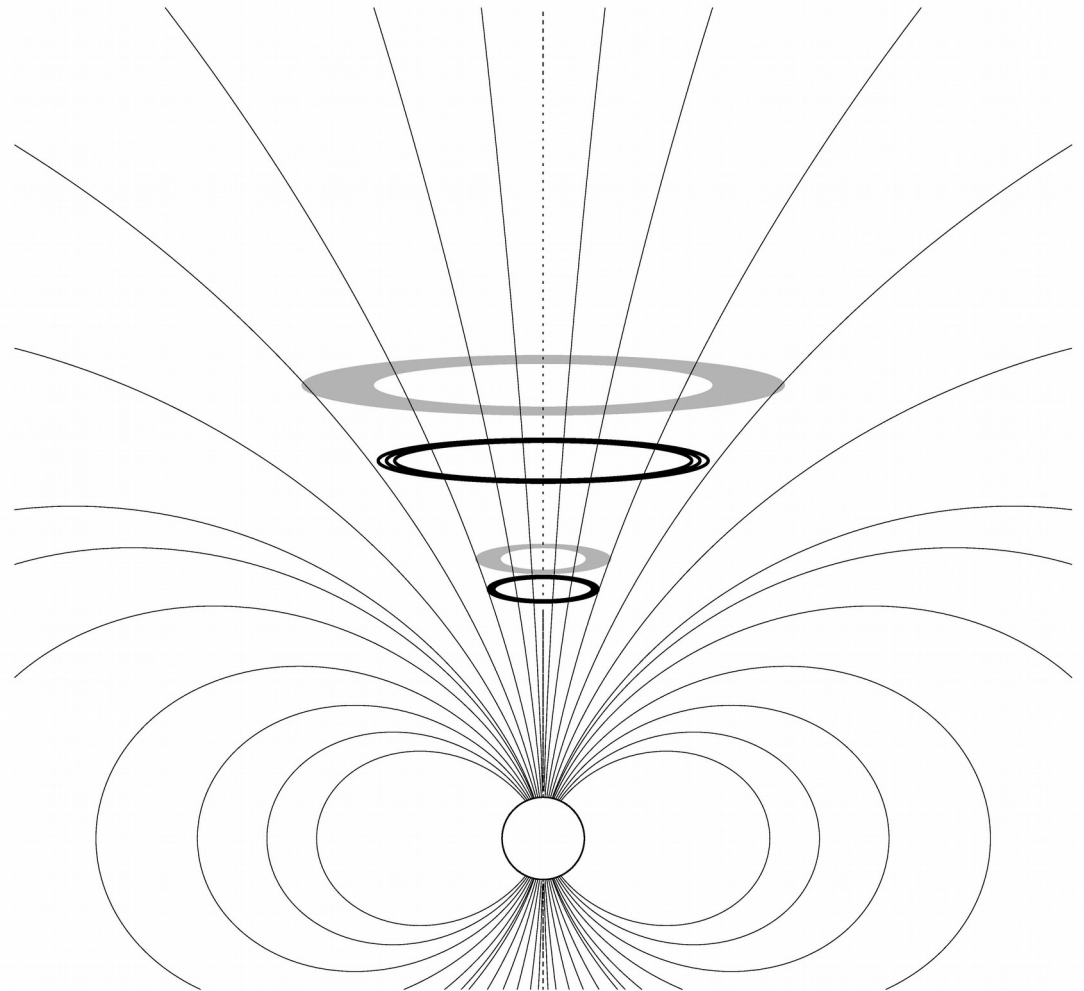
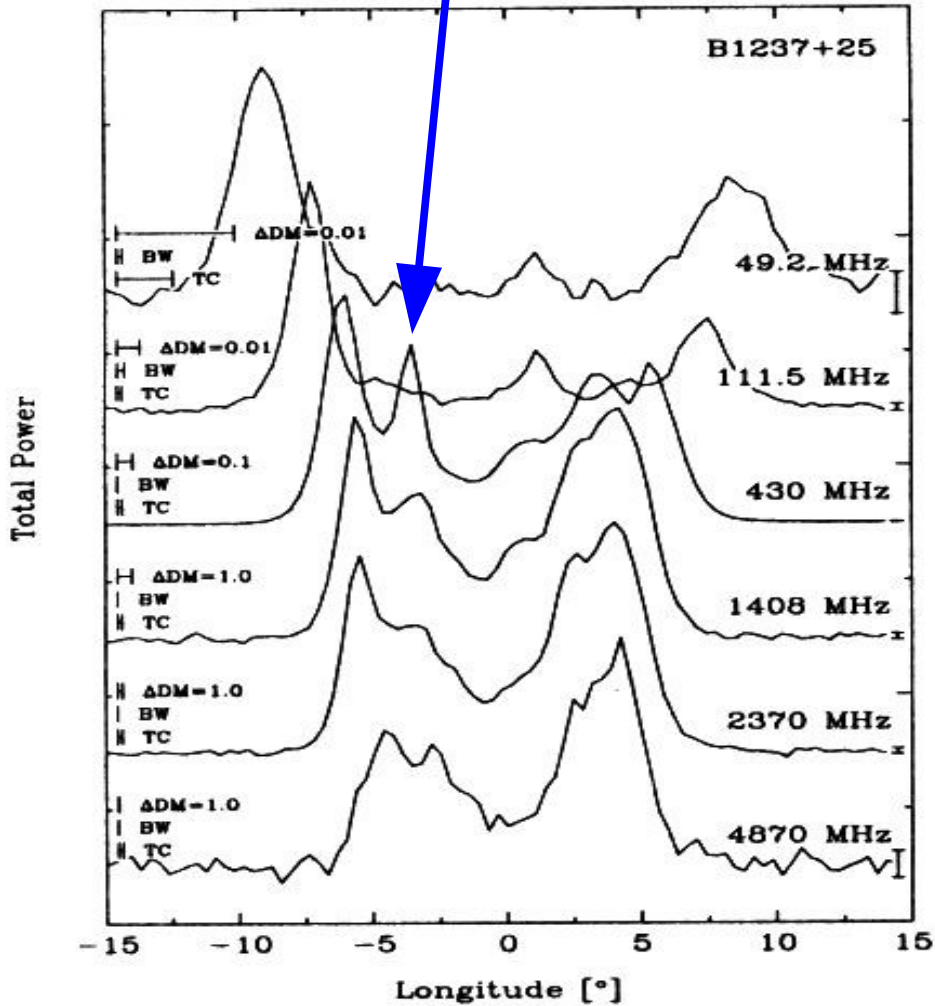
The stream model also works better for normal pulsars

# Radius-to-frequency mapping – conal version

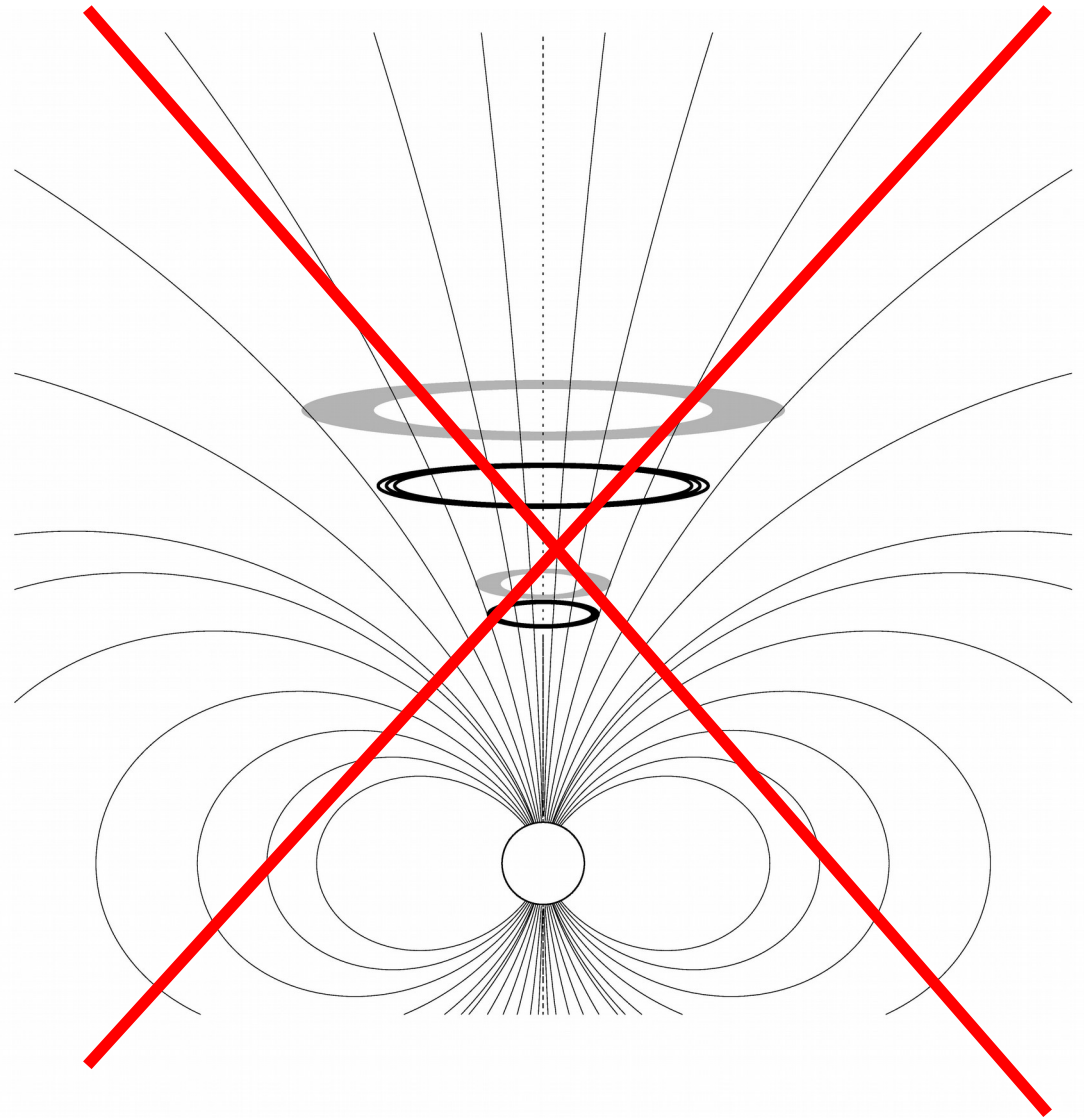
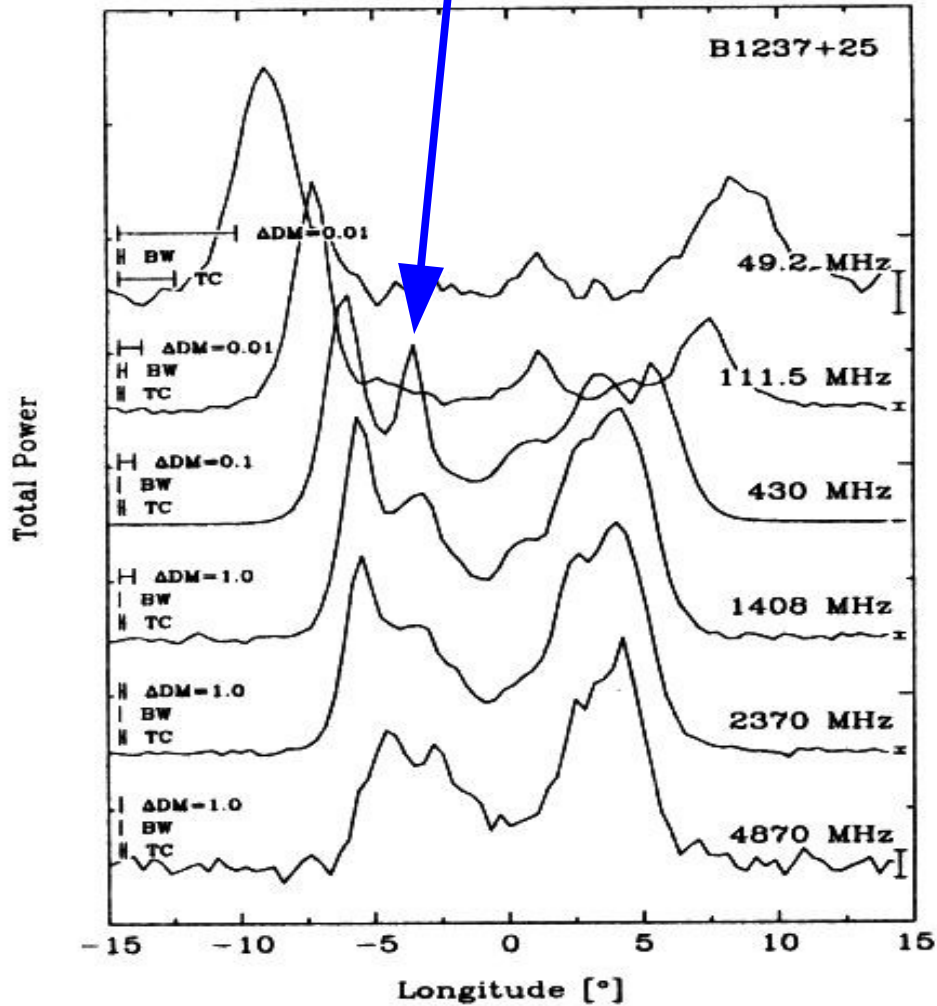


**Grey: low nu**  
**Black: high nu**

RFM is weaker for the inner pair of components -  
- caused by less spreading inner B-field lines?



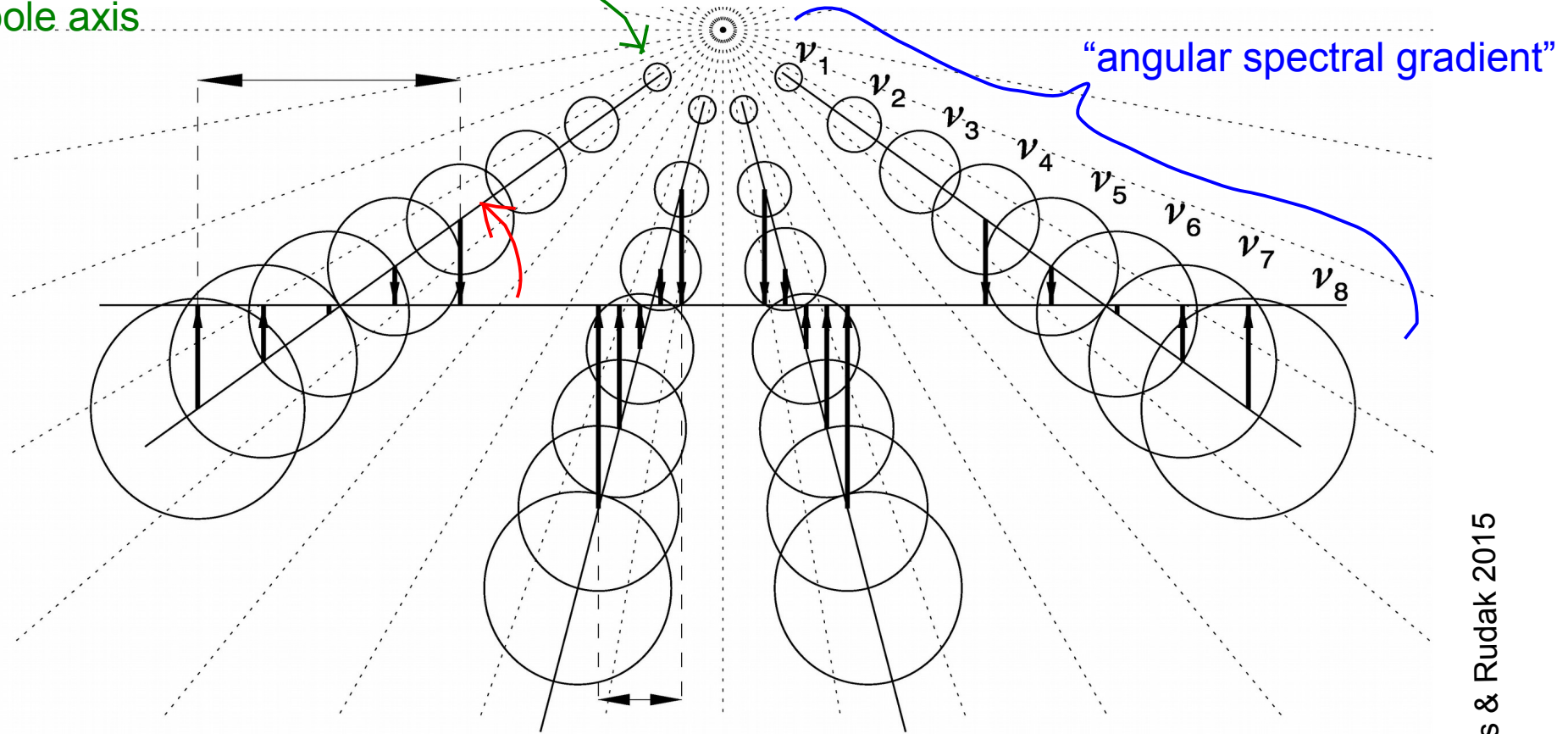
RFM is weaker for the inner pair of components -  
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Radius-to-frequency mapping – stream model version  
**circles = fixed intensity contours at a given nu**

all streams anchored at same distance from dipole axis



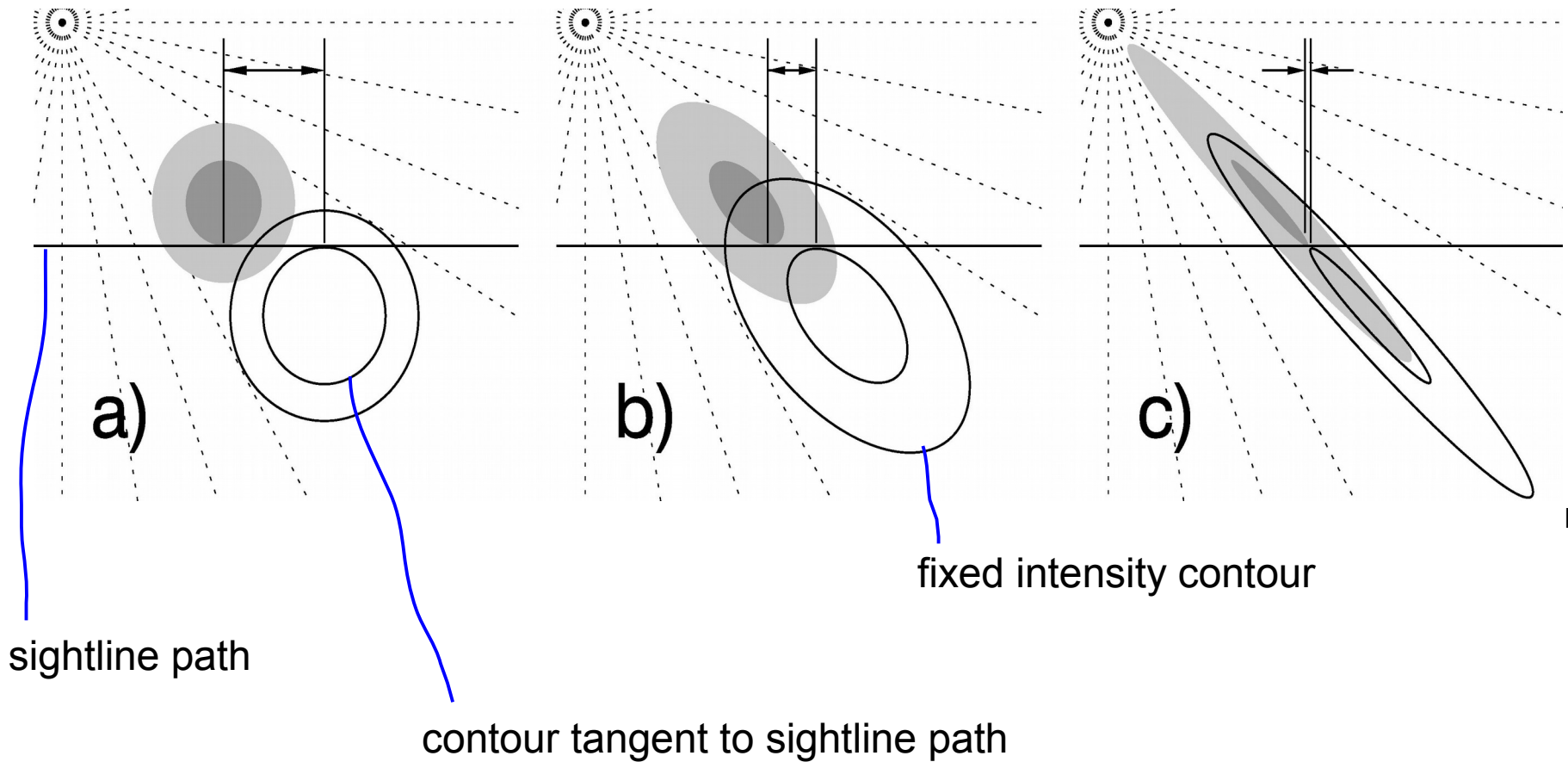
Red arrow: Cut angle

Inner streams are cut more orthogonally => smaller RFM

The fixed-nu beams are not expected to be circular:

slightly-bent B-field lines

strongly-bent B-field lines (MSPs)

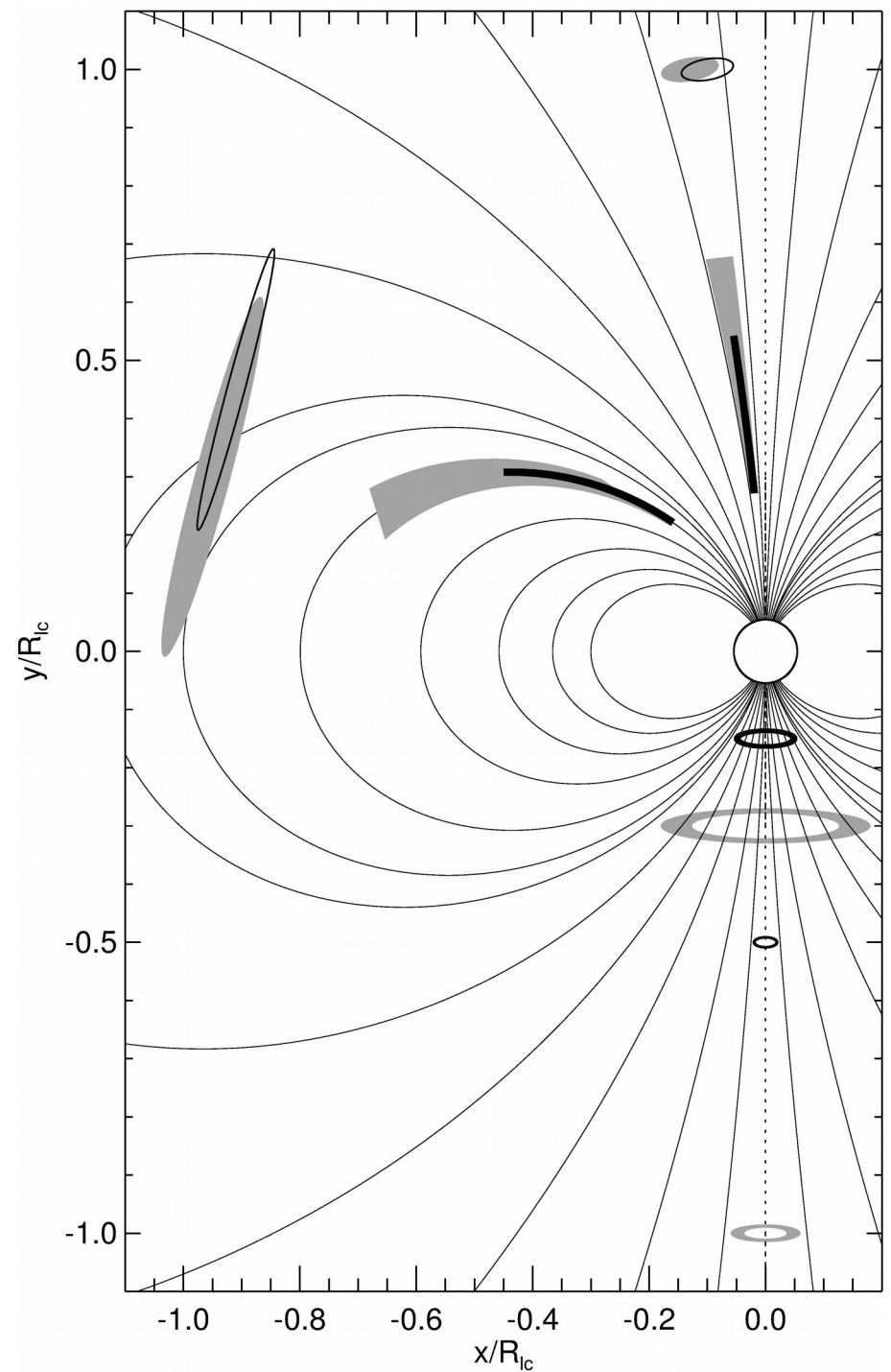


DR2015

Fixed-intensity contours at two frequencies are shown for three beam elongations.

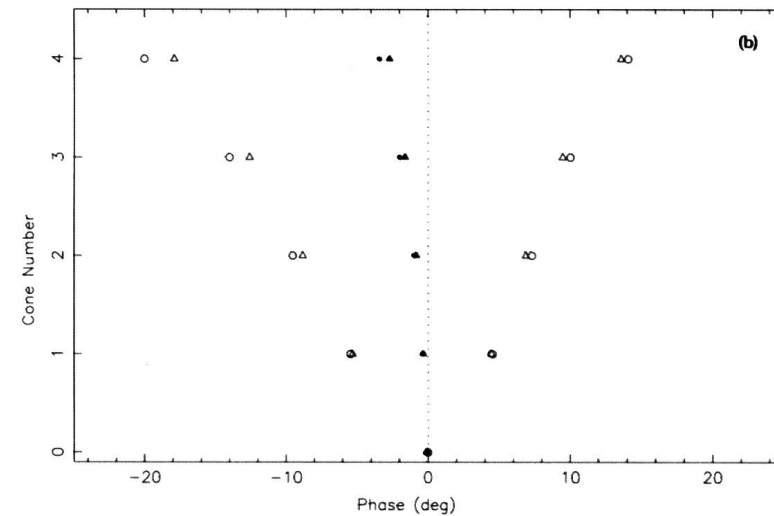
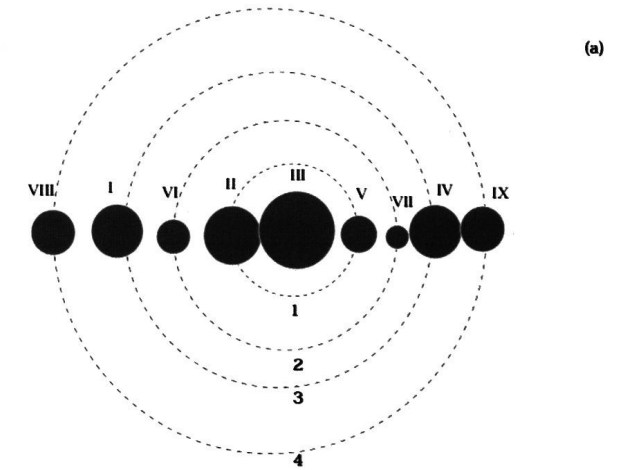
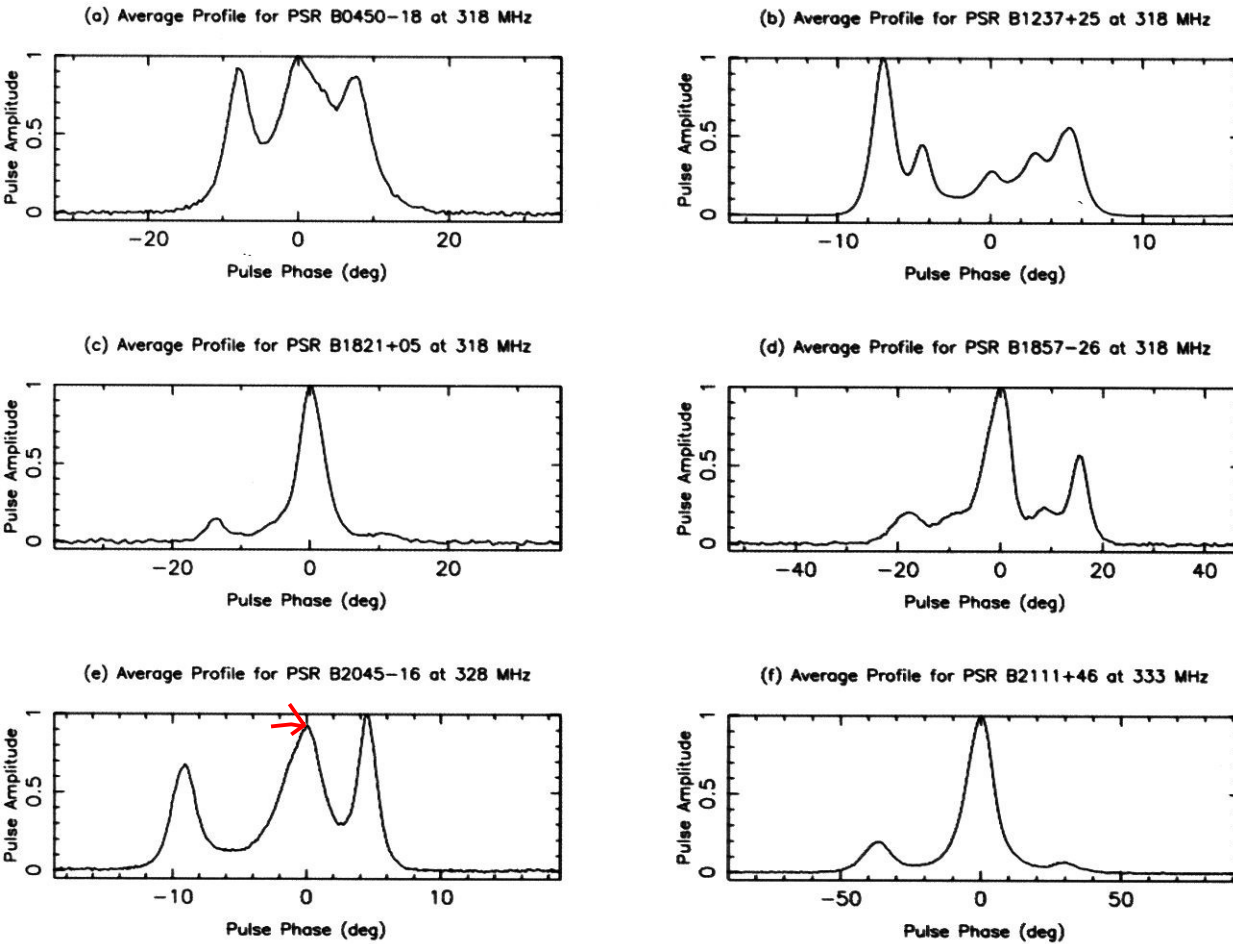


MSPs have more flaring B-field lines  
=> why do they exhibit so weak RFM?



Because the streams flowing along  
their bent B-field lines  
more easily produce fan-beams!

# Lag of 'core' with respect to the centroid of 'conal' pairs



Core lags the centroid of flanking components

The lag is larger:

- for more peripheric pairs of components
- at a lower frequency.

B0329 + 54  
Gangadhara & Gupta 2001

# Lag of 'core' with respect to the centroid of 'conal' pairs

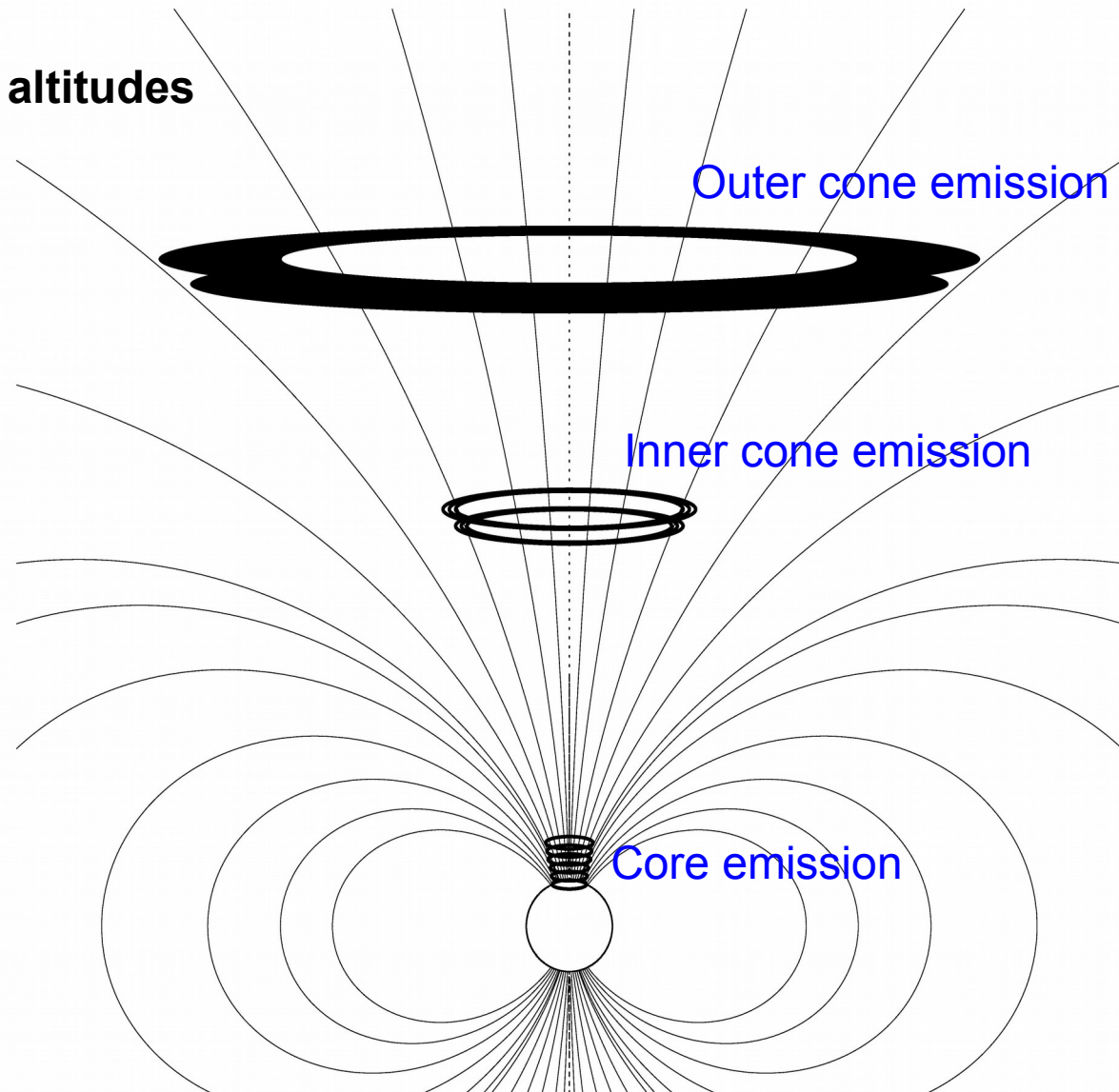
Conal interpretation:

**separate emission rings at different altitudes**

Aberration-retardation (AR) shift:

Higher = closer to the observer =  
= detected earlier in the profile

Higher = corotating faster =  
= aberrated more forward =  
= observed earlier in the profile



# Lag of 'core' with respect to the centroid of 'conal' pairs

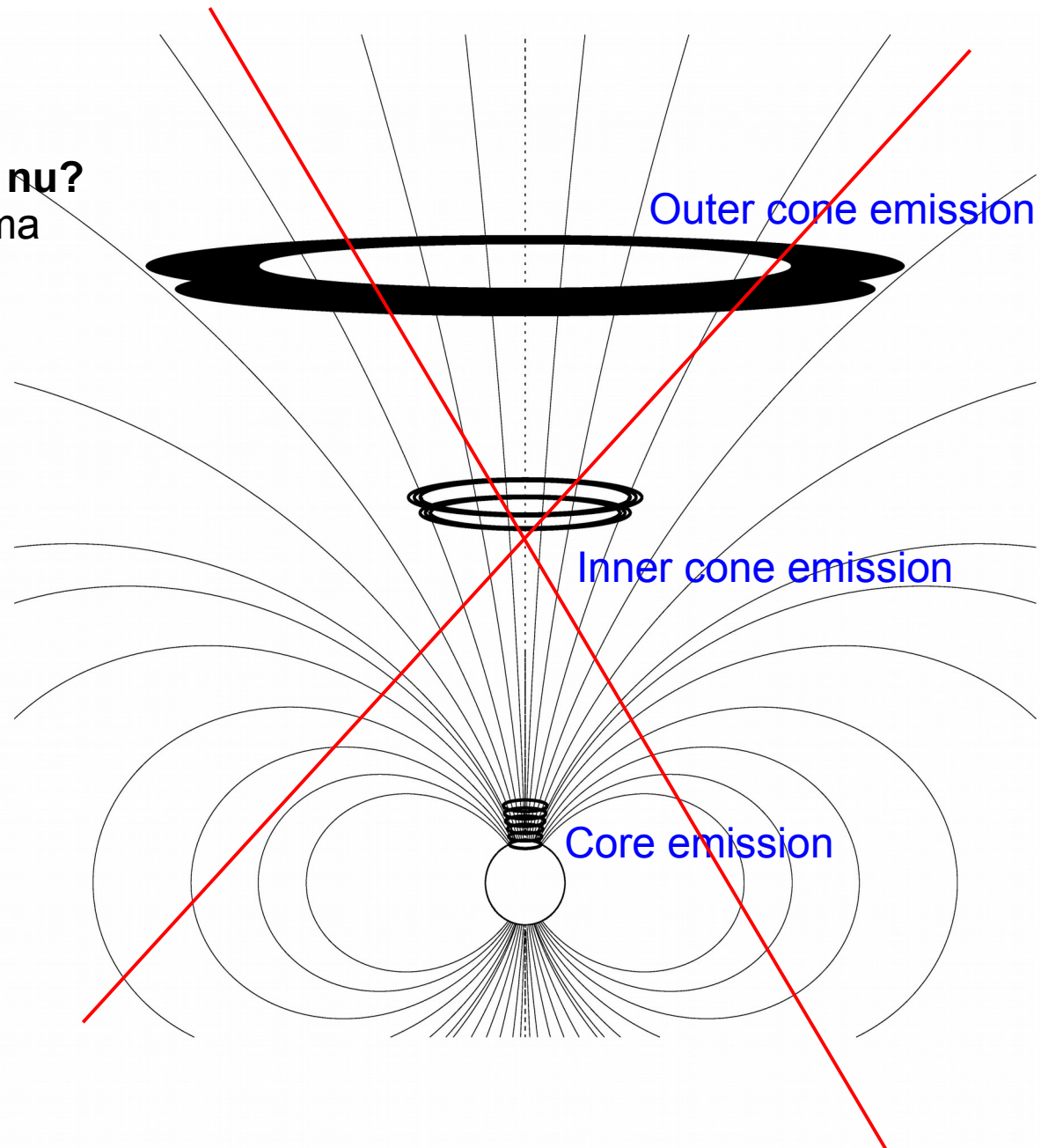
Problems:

**Why disparate altitudes despite same  $\nu$ ?**

Why core from small region of high plasma density?

Might there be any **natural reason** for the smaller shift of inner components?

The **Ptolemaic complexity** disappears when a bunch of streams is used instead of cones





Lag of 'core' –  
 - stream version  
 5 similar / identical streams

$$\text{AR shift} = 2r / R_{lc} = k \theta^2$$

$\theta$  – angular distance  
 from dipole axis

Theta is smaller for inner streams

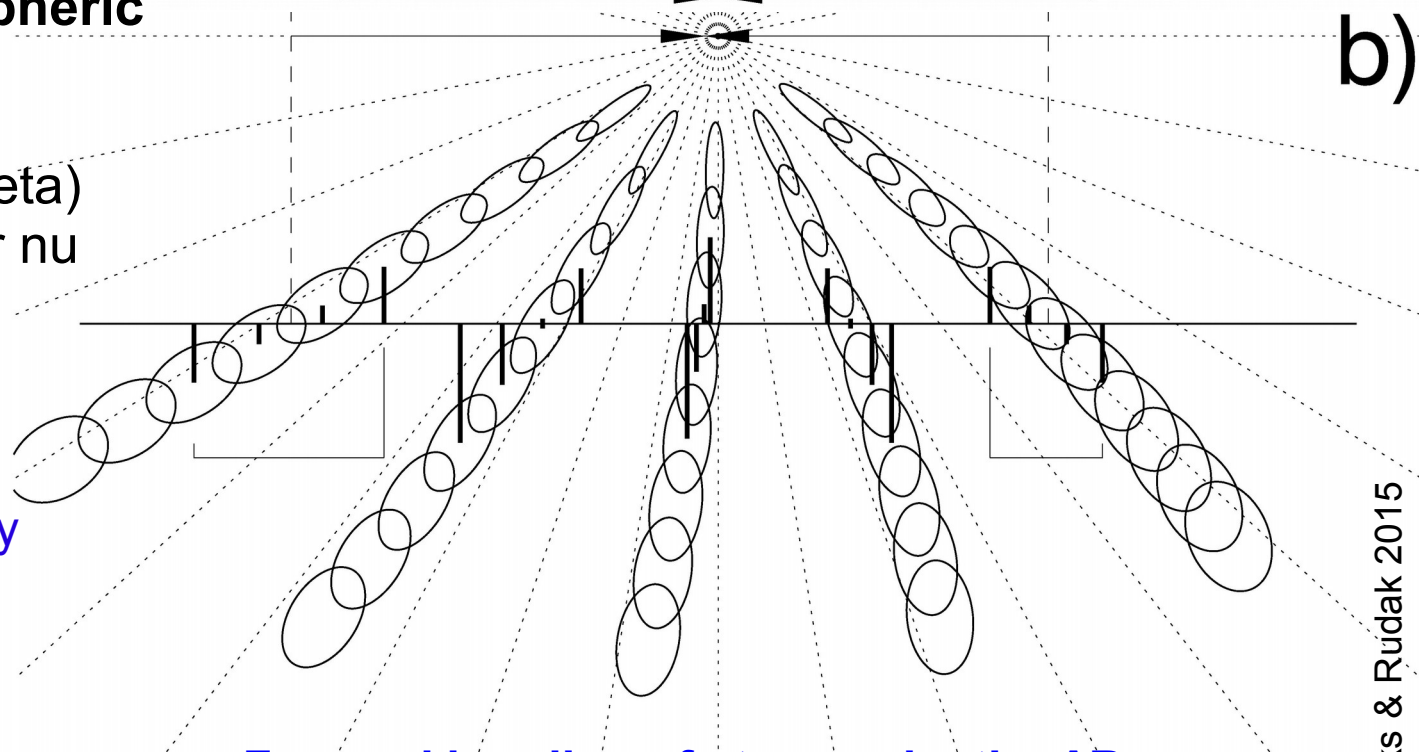
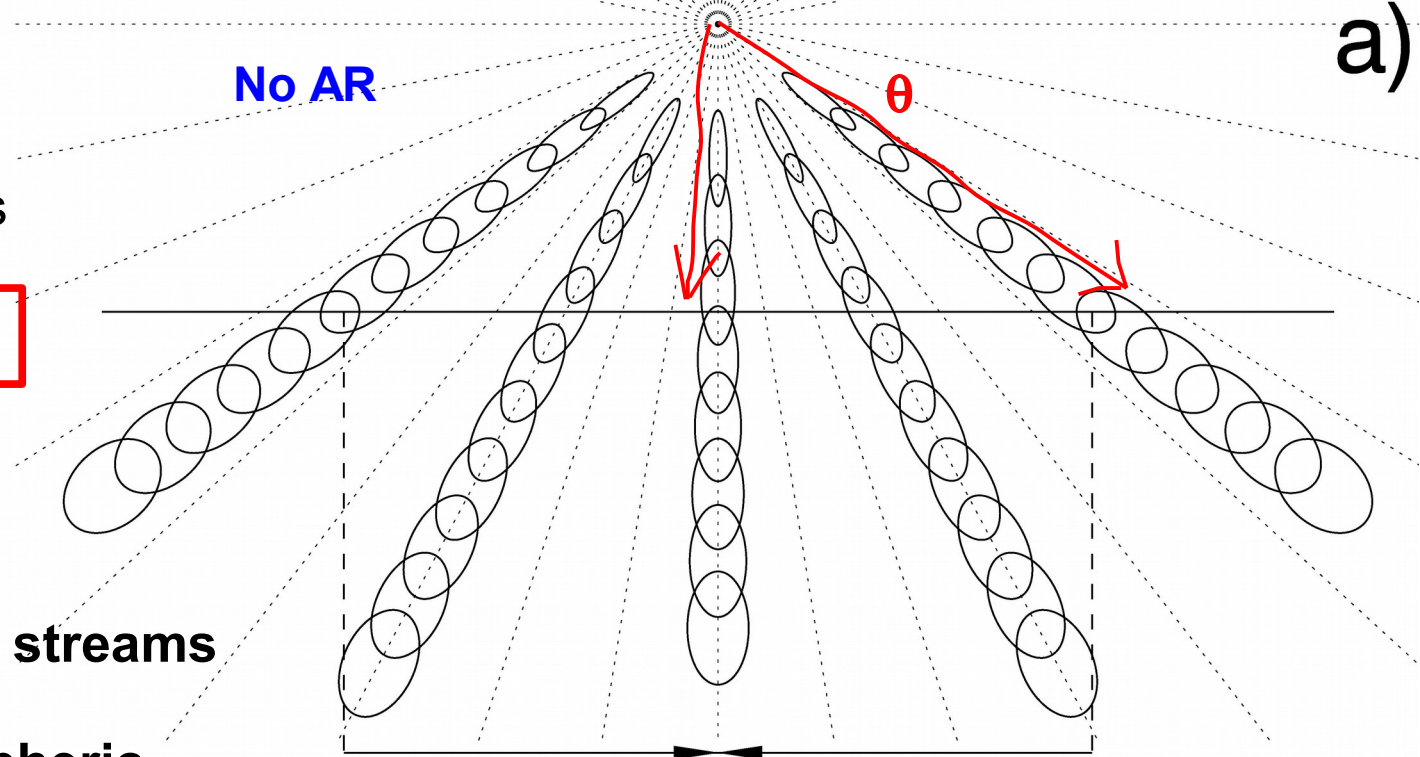
=> stronger shift for peripheric  
 components

lower nu at larger r (and theta)  
 => shift is stronger at lower nu

Note: Core lag results naturally  
 from the stream geometry

You do not need to put your  
 rings at disparate heights!

No AR

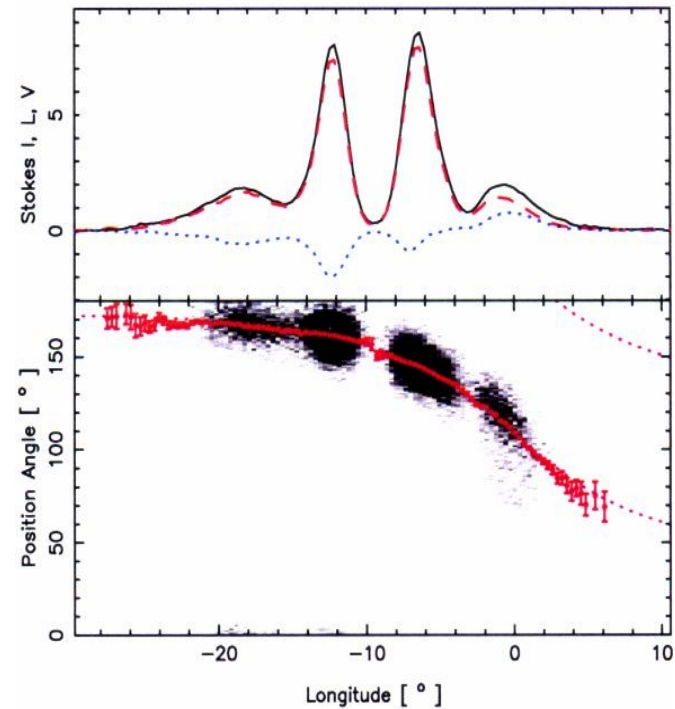


Forward bending of streams by the AR

a)

b)

# PSR J0631+1036 – isn't this an obvious nested cone profile?



Teixeira et al. 2014

Traditional conal model: **No** the profile **does not seem** to have conal origin.



**Cone size ratio:**  $R_{\rho} = \rho_{\text{in}} / \rho_{\text{out}} = 0.74 - 0.87$  (observed)

	MD	R93	G93		K94 ( $P^{-\kappa}$ )		K94 ( $P^{-0.5}$ )		
$\nu$ (GHz)	1.0	1.0	1.4	1.4	4.75	10.55	1.4	4.75	10.55
$R_F$ (per cent)	100	50	10	10	10	10	10	10	10
$\rho_{\text{in}}$ ( $^{\circ}$ )	4.1	4.3	4.9	5.3	4.5	4.77	4.9	4.4	4.5
$\rho_{\text{out}}$ ( $^{\circ}$ )	5.1	5.8	6.3	6.23	5.76	5.48	6.3	5.9	5.5
$R_{\rho}$	0.8	0.74	0.78	0.85	0.78	0.87	0.78	0.75	0.82

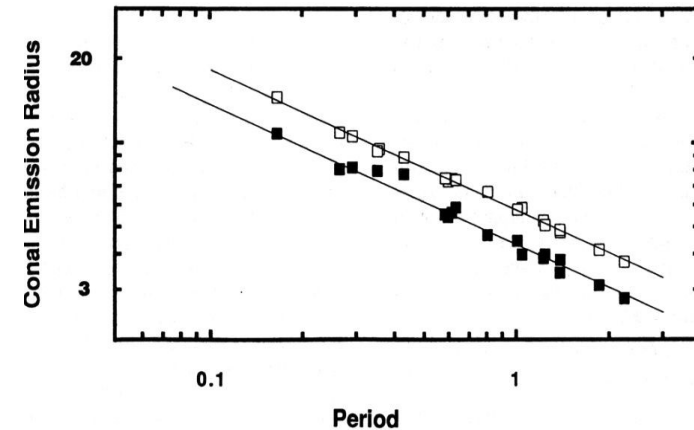
Rankin, Gil, Kramer, Mitra and their collaborators (1993 - 1999)

**All observers find the same average cone size ratio:**

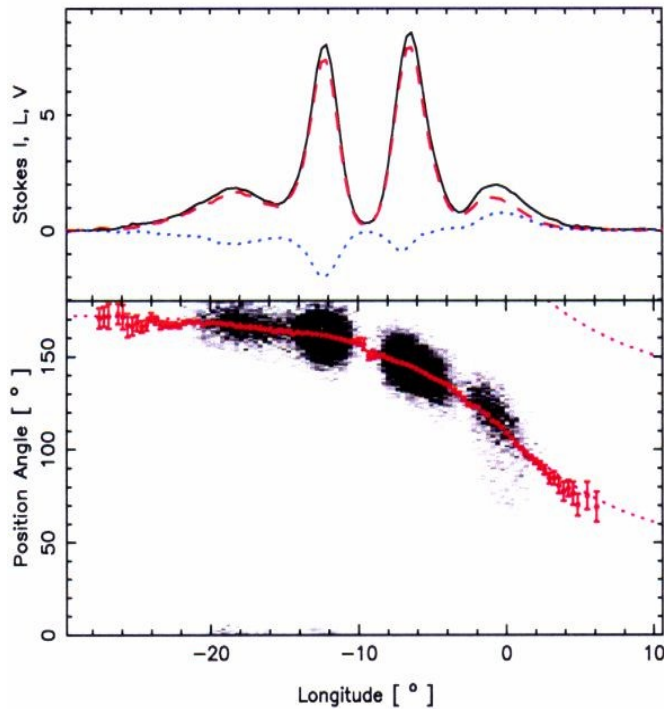
$$R_{\rho} \sim 0.8$$

(for slightly different pulsar samples,  
but for Rankin's assumptions about the core component).

Theoretically supported by the geometry of critical field lines  
(Wright 2003)

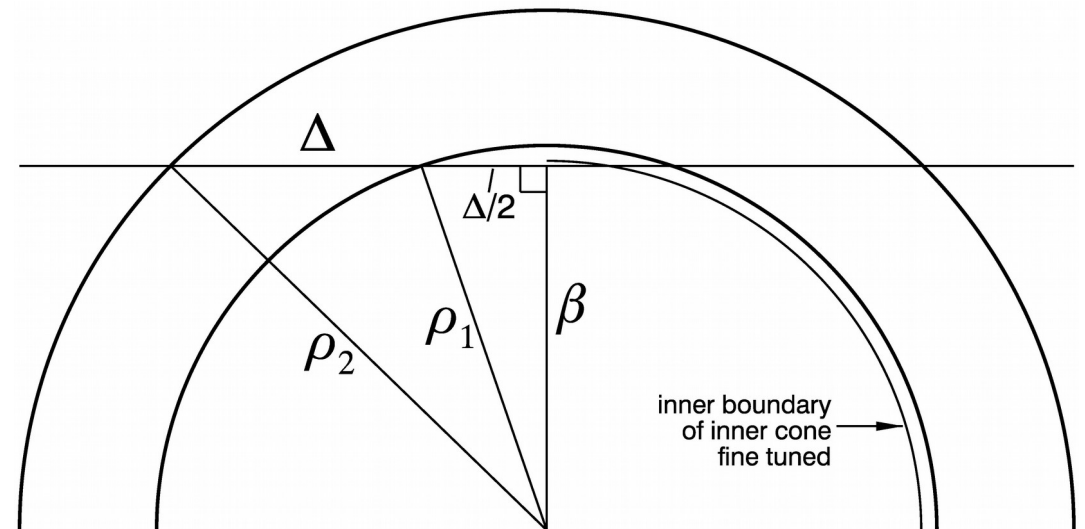


# PSR J0631+1036 – a profile that should not have been observed (according to the conal model)



Teixeira et al. 2016

$$W_{in} / W_{out} = 1 / 3 \text{ (observed)} \Rightarrow \beta / \rho_{in} = 0.95 !$$

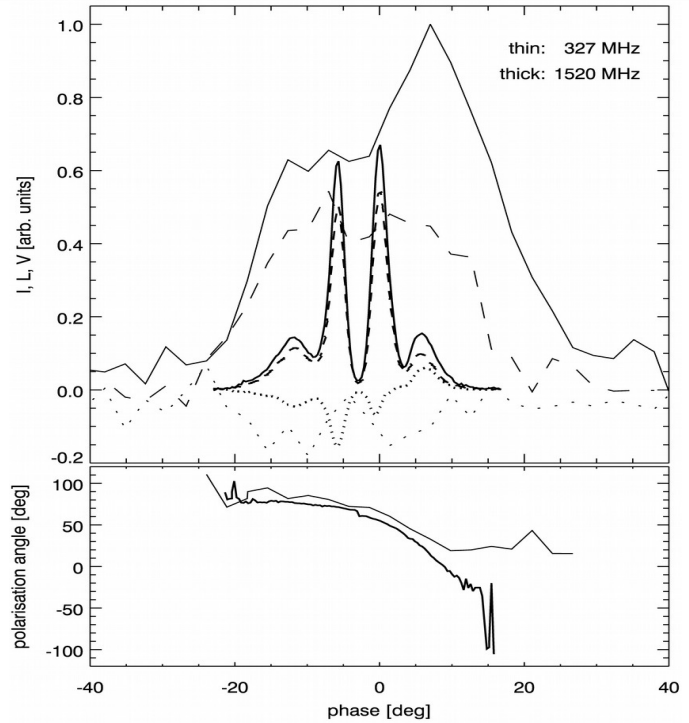
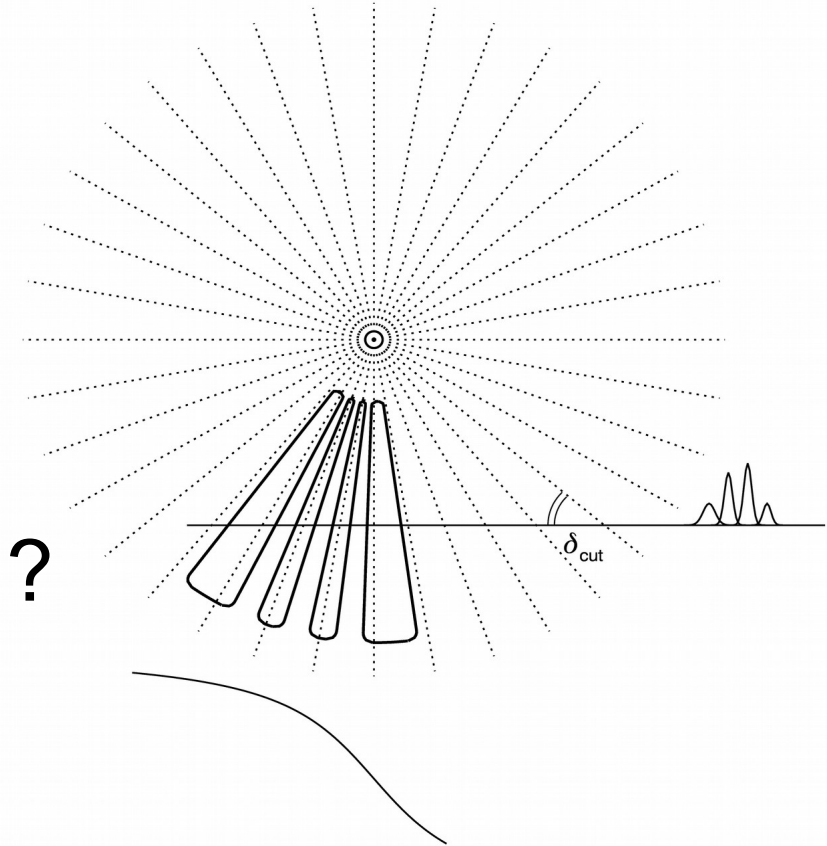


**Sightline path nearly tangent to inner cone => extremely fine tuning to get  $R_w = 1 / 3$**

**Deep central minimum unexpected:** inner boundary of inner cone  
needs to be **squeezed** between  $\rho_1$  and  $\beta = 0.95 \cdot \rho_1$   
=> even smaller chance to observe such a profile

**One profile with equal peak separations is expected per 330 M+Q type profiles  
(assuming  $\Delta_{\phi} = 6 \text{ deg} \pm 0.5 \text{ deg}$ )**

# A more reasonable beam model for J0631+1036



Is J0631 an exception with  $R_{\rho} \ll 0.75$ ?

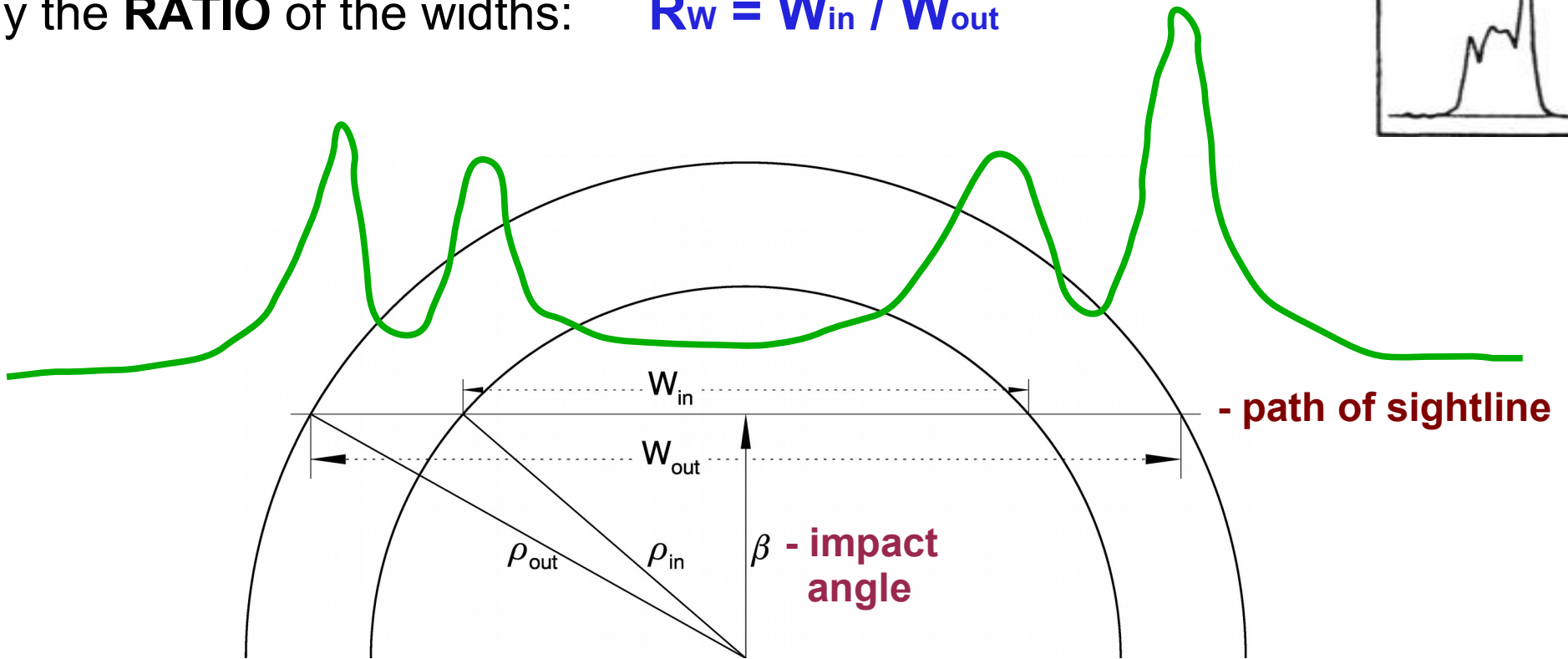
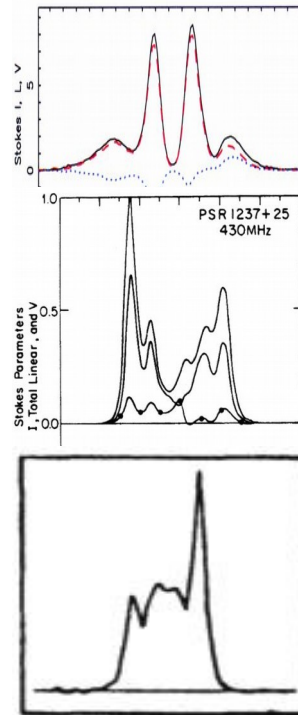
Let us check **Rw distribution for the whole population** of Q and M pulsars  
(with 4 and 5 components):

Conal radii:  **$\rho_{in}$ ,  $\rho_{out}$**  - not measurable (directly)

Peak-to-peak separations (widths):  **$W_{in}$ ,  $W_{out}$**  - directly measurable  
for inner and outer pair of components.

**Innovation:** do **not** study the distribution of widths.

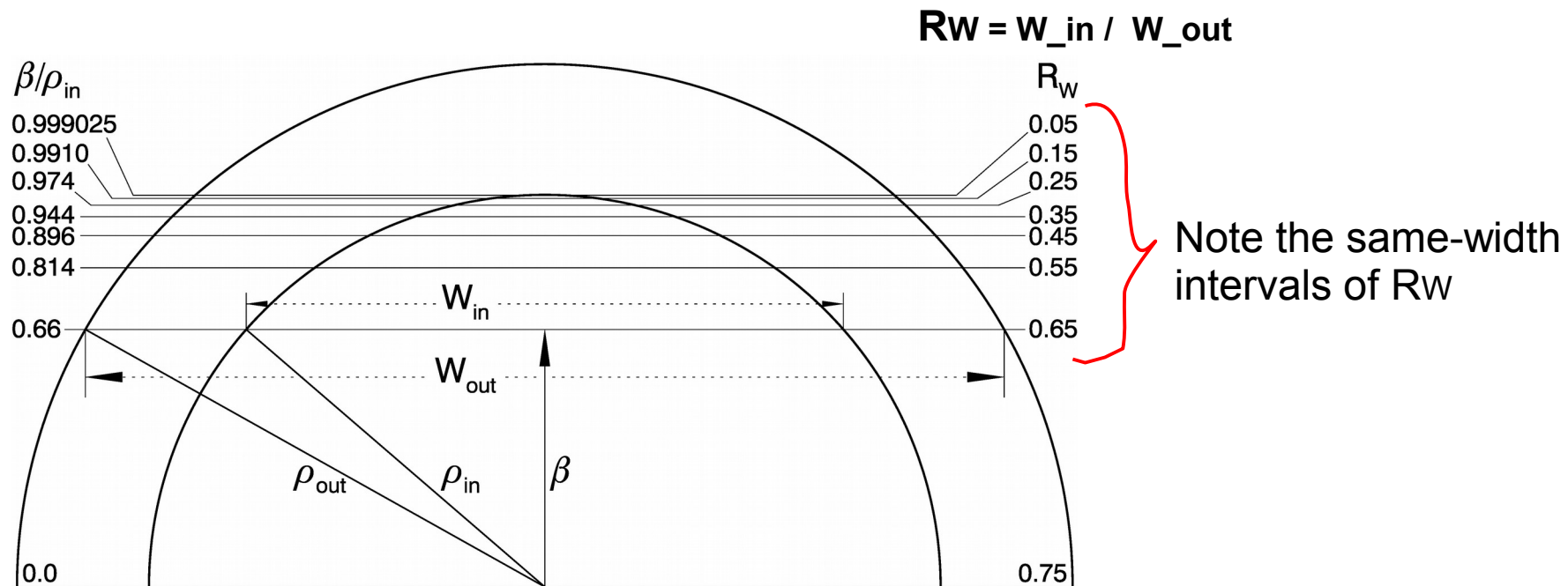
Study the **RATIO** of the widths:  **$R_w = W_{in} / W_{out}$**



Cone size ratio fixed => Ratio of peak-to-peak separation ( **$R_w$** ) depends only on beta

**Average** cone size ratio  $R_{rho}$  is determined based on the conal model  
=> **definite prediction for  $R_w$  distribution**

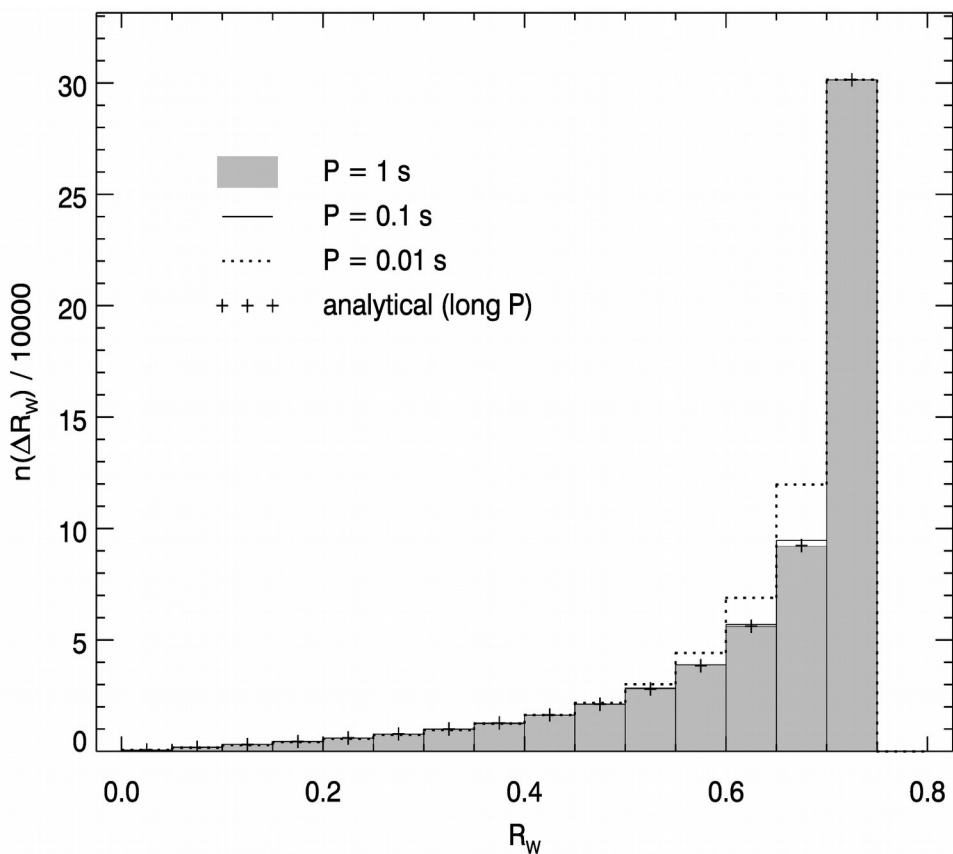
Intervals of viewing angle that correspond to a fixed interval in  $R_w$  ( $\Delta R_w = 0.1$ )



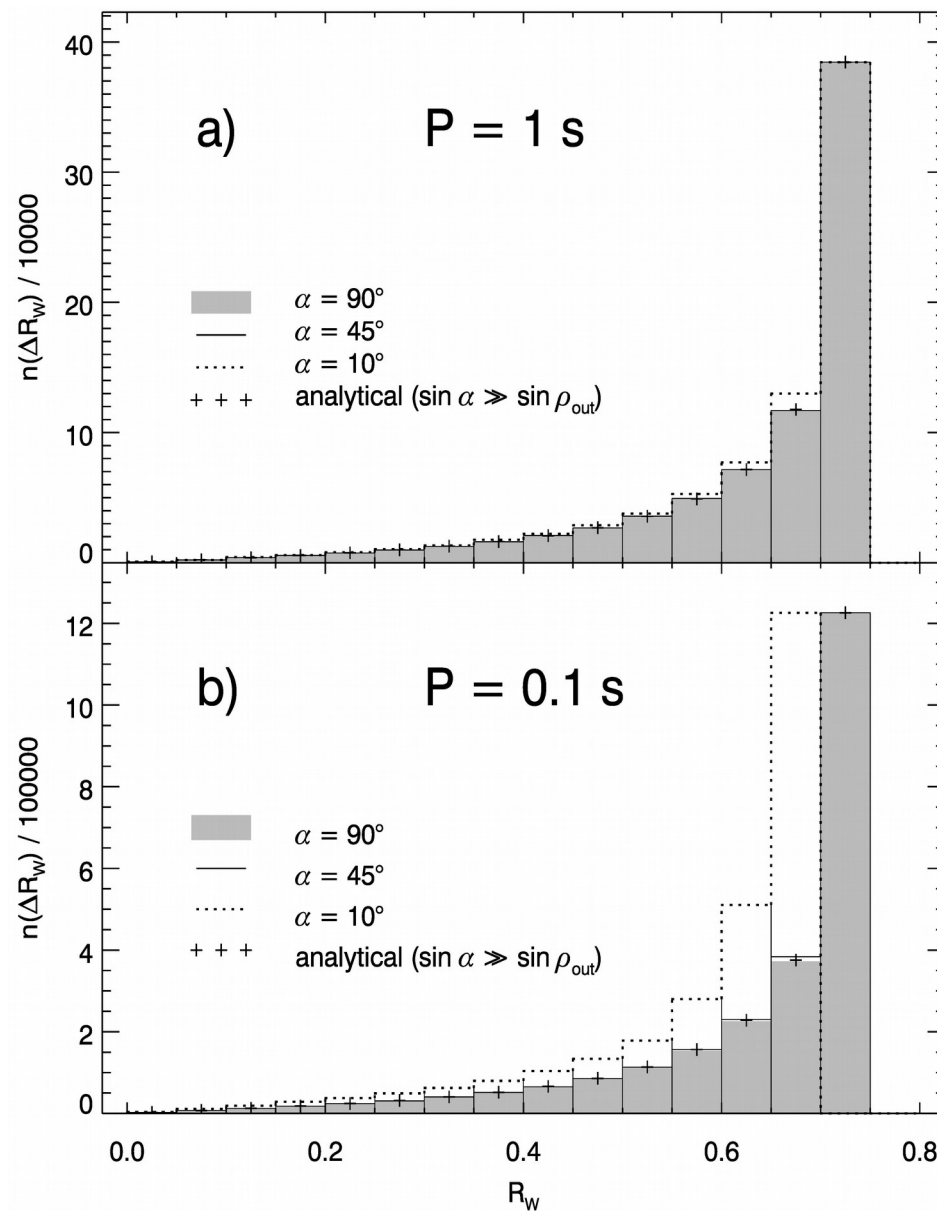
Except from the peripheric region,  $R_w = \sim 0.7$  should vastly dominate in the data

Ratios of widths instead of widths => **method sensitive only to beam shape**  
 but **independent of all parameters that just rescale the beam**  
 (period, dipole tilt, frequency, emission altitude)

Marginal dependence on period

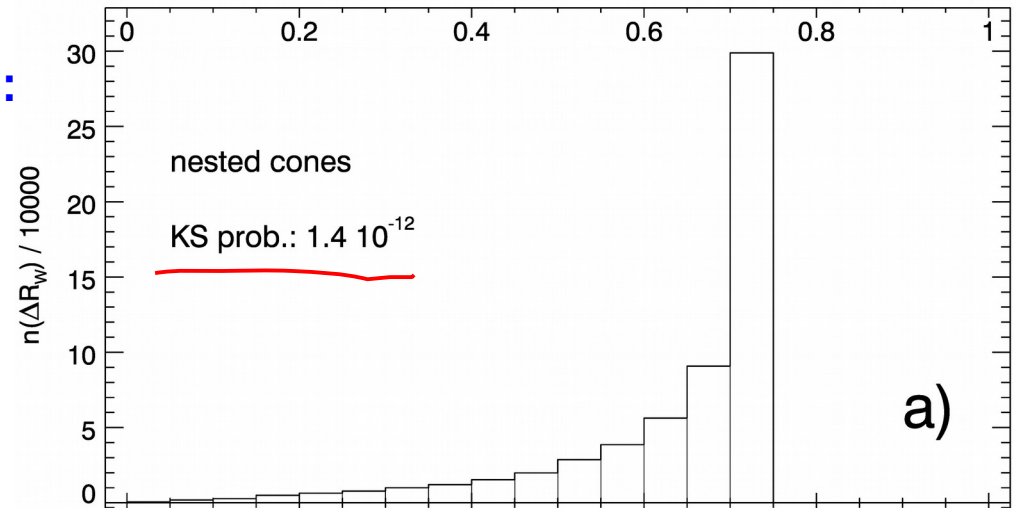


Marginal dependence on dipole tilt (alpha)

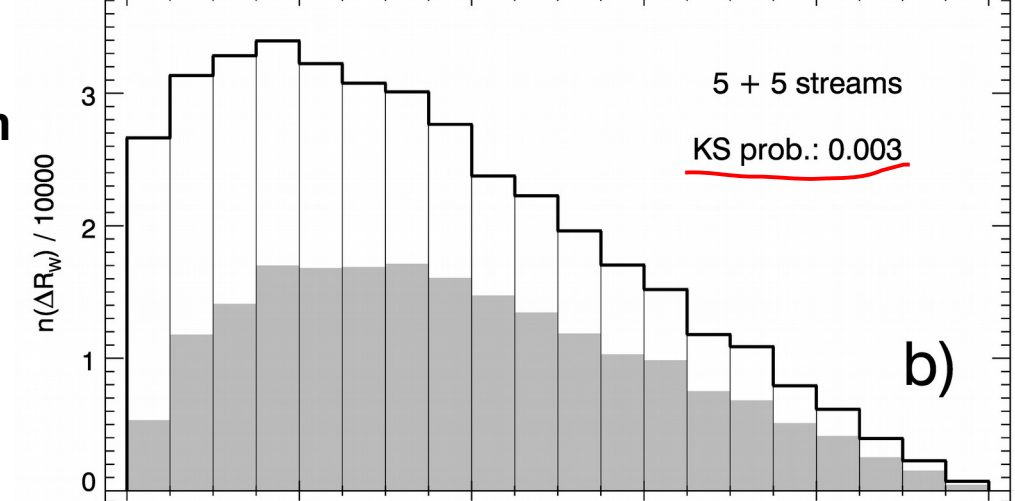




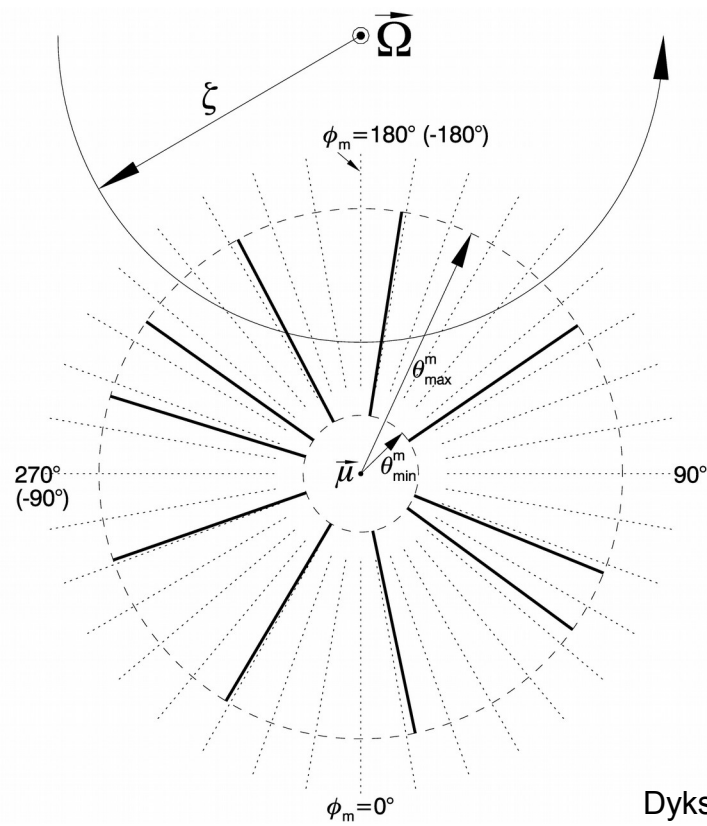
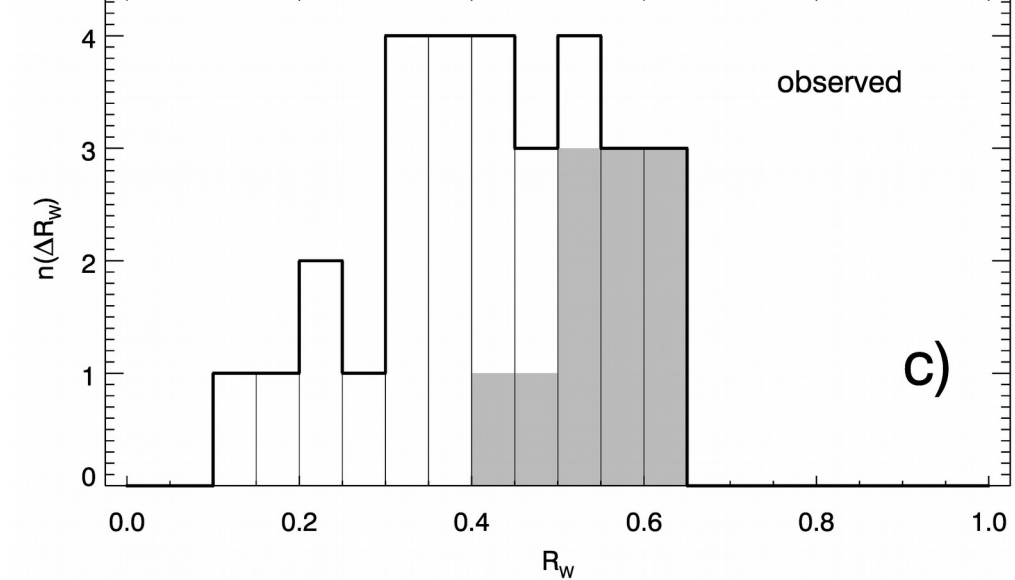
**Nested cones:  
( $R_{\text{rho}} = 0.75$ )**



**Fan beams  
(5 + 5 random  
streams):**



**Observed:  
(30 pulsars  
of Q and M  
type)**



## CONCLUSIONS

Fan beam geometry **works better in explaining the main nu-dependent phenomena** in both the normal and millisecond pulsars (RFM, core lag, lack of RFM in MSPs).

Fan beams provide a **better model for the observed  $R_w$  statistics**.

Fan beams are also able to **explain 'peculiarities'** such as the bifurcated components, double notches and polarisation distortions (see poster by Lab Saha).

Plasma streams (columns) **more natural than rings at disparate altitudes**.

Several important implications, eg.:

- outer boundary of radio beam not circular => existing estimates of  $r$  wrong
- dipole tilt distributions based on circular core shape not valid anymore
- radio pulse may lag the dipole axis phase (not just precede due to AR)

**The conal beams may well not exist in pulsars at all.**