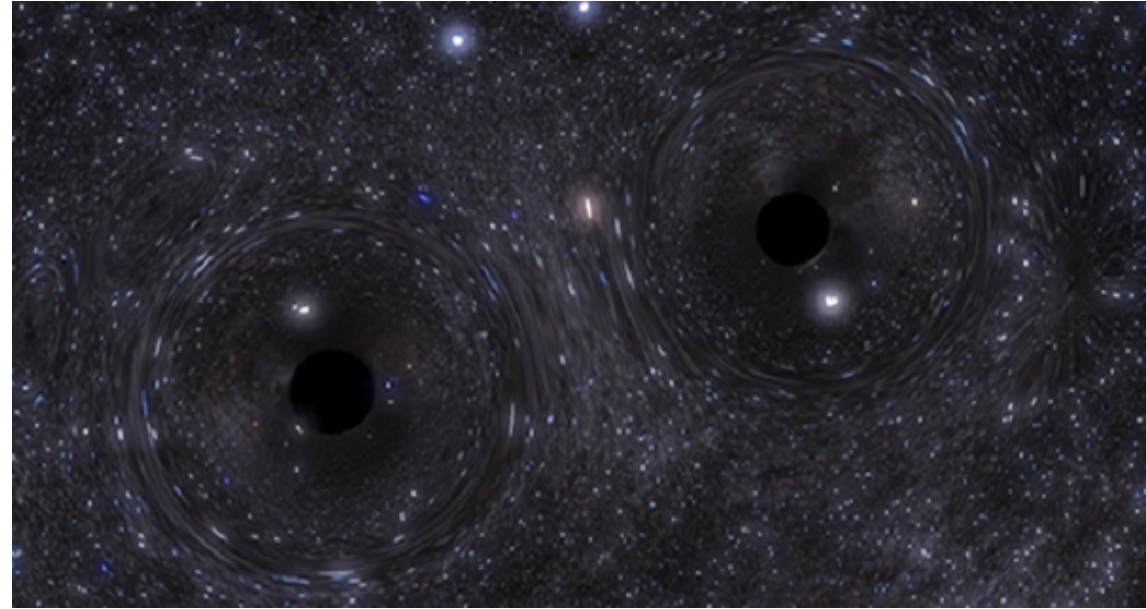
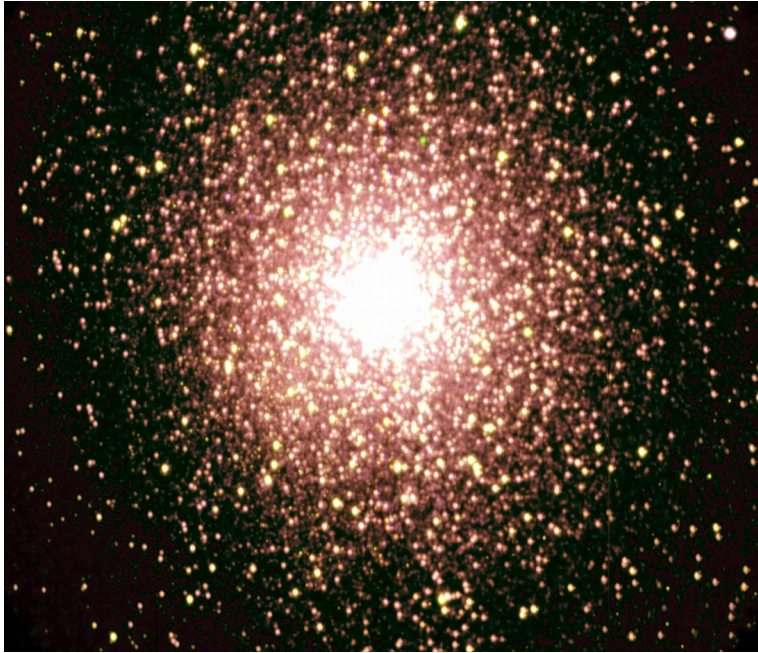


Coalescing binary black holes originating from globular clusters



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INNOVATIVE ECONOMY
NATIONAL COHESION STRATEGY



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The recent breakthroughs

- 2015 - **detection of gravitational waves** by aLIGO → GW Astronomy, a new window onto the Universe
- **Detection of coalescing black hole binaries:** GW150914, GW151226, GW170104, GW170608, GW170814 and **LVT151012**
- Observation evidence that BBHs merge within Hubble time
- **Evidence for massive stellar BHs with masses of 30 and up to 60 solar masses**
(their formation requires an origin from low metallicity environments (Belczynski et al. 2010, 2016))
- **GW150914 - the “brightest” source ever observed**

$$L_{GW} = 200_{-20}^{+30} M_{\odot} s^{-1} = 3.6_{-0.4}^{+0.5} \times 10^{56} \text{erg s}^{-1}$$

Expect a lot of discoveries in near future by Advanced LIGO/VIRGO detectors !!!

Where does it fit into broad astrophysical picture?

- evolution of binaries in the field (Belczynski et al. 2016)
- formation of binaries in dense clusters**
- population III

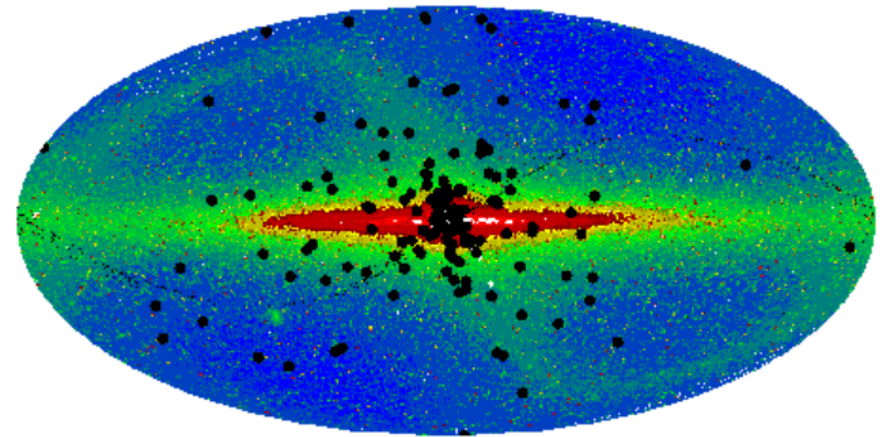


Globular Clusters

- ★ Spherical collections of stars that orbits a galactic core as a satellite. More than 1000 extragalactic GC (HST) up to 375 Mpc.
~157 GC in Milky Way (Harris catalog)
- ★ GC contain 10000 to several millions stars
- ★ Most of stars are old Population II (metal-poor) stars
- ★ Stars are clumped closely together, especially near the centre of the cluster --> close dynamical interactions → tight binary systems containing compact objects
- ★ Globular Clusters in the Milky Way are estimated to be at least 1 billion years old. 50% GC within 5kpc, the most distant 130 kpc



NGC 104 aka 47 Tucanae



Credit: M. Benacquista & Downing, 2011, the distribution of 157 GC in the Milky Way from Harris catalog

Code description

- We use the MOCCA (MOnte Carlo Cluster simulAtor) code developed by Mirek Giersz, Henon (1971), Stodolkiewicz (1982), Abbas et al. (2016, 2017). Similar to the code used by the Northwestern group (Rodriguez et al.)
- Well tested, allows to investigate individual interactions, while ensuring that the evolution of cluster is accurate and computationally efficient.
- BIGSURVEY – 2000 MOCCA models, range of metallicities and sizes to match the population of GCs in the Milky Way
- Matches Milky Way but is not a fit. Many degeneracies.

Summary of simulations

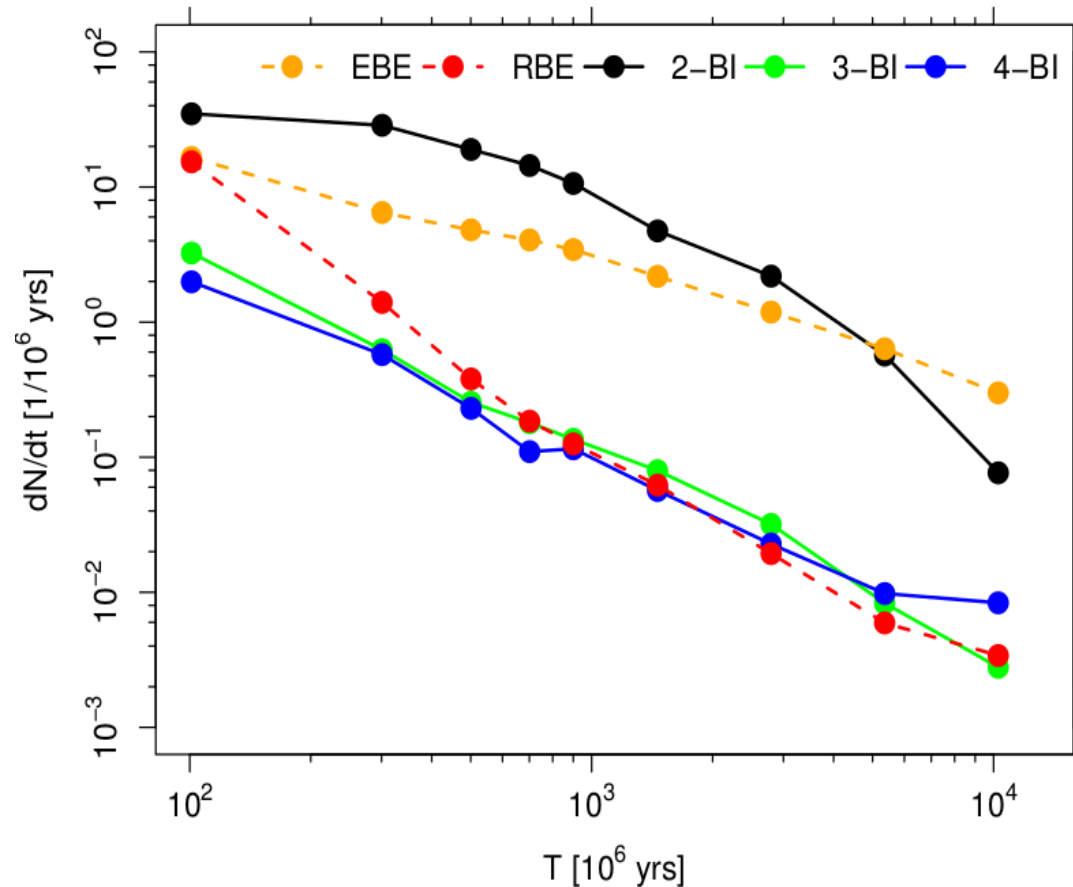
Metallicity	Total mass [10^6 Msun]	Mass range of clusters [10^6 Msun]	Number of models	Number of BHBH mergers
0.02	51.7	0.024-0.61	258	735
0.006	19.6	0.63	31	1857
0.005	49.4	0.024-0.61	243	3042
0.001	141	0.02-1.08	423	9169
0.0002	18.9	0.63	30	2276

Table : About 2000 models. BH and NS kicks are the same, 265 km/s, except the case of mass fallback Belczynski et al.(2002). Two segment IMF (Kroupa 2001) was used for all models, with $M_{min} = 0.08M_{\odot}$ and $M_{max} = 100.0M_{\odot}$. If the binary fraction, f_b , is equal to 0.95 then binary parameters are chosen according to Kroupa (1995) (eigenevolution, mass feeding algorithm), otherwise eccentricity distribution is thermal, mass ratio distribution is uniform and semi-major distribution is uniform in logarithm, between $2(R_1 + R_2)$ and 100 AU. R_t - tidal radius, R_h - half-mass radius, W_0 - King model parameter, Z - cluster metallicity. For each initial number of objects different combinations of parameters are used to generate the initial model. The number of models with different metallicities are as follows: 63, 831, 487, 64 and 503 for $Z = 0.0002, 0.001, 0.005, 0.006$ and 0.02, respectively.

Merging BBHs and Colliding BHs From Globular Clusters

Number of merging BH binaries or colliding BH within Hubble time per unit time (1 Myr) as a function of merger time for black holes.

Five different interactions, which can lead to the emission of **chirp GW signal** (dashed lines) due to the coalescence of two BHs in a binary system or a **burst GW signal** (solid lines) due to the collision of two BHs.

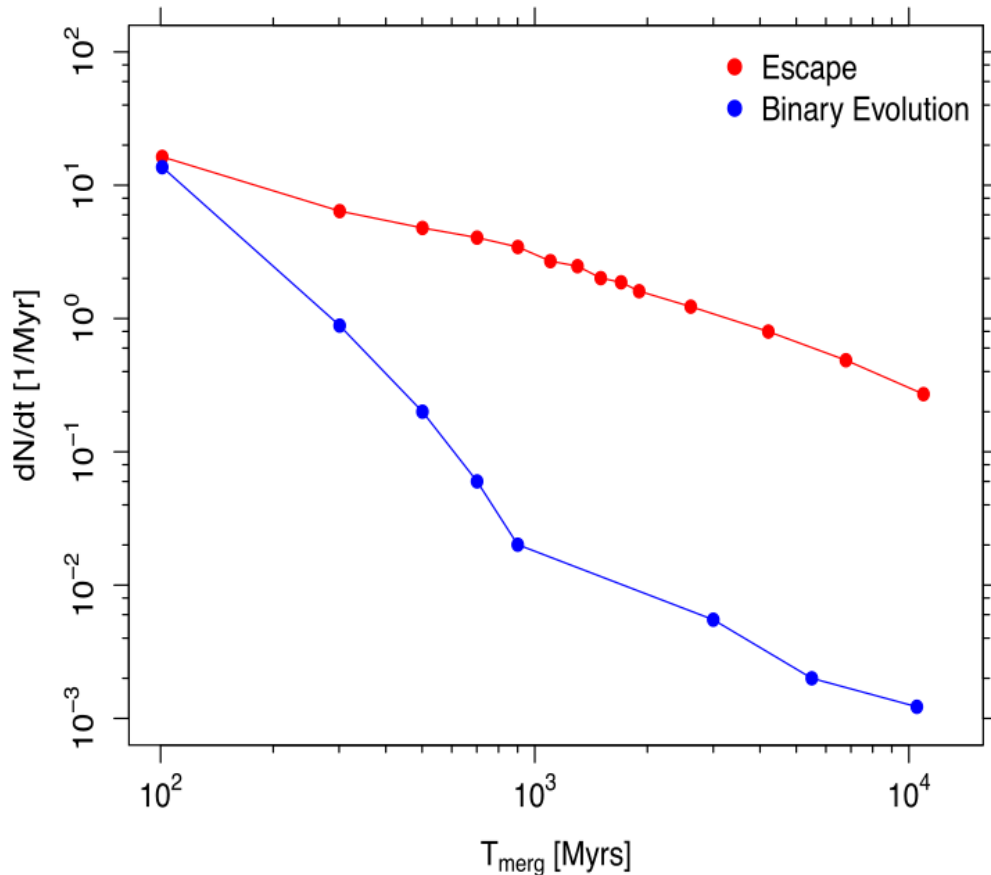


- Merger of BBH – a chirp signal
 - EBE -ejected binary evolution
 - RBE – retained binary evolution
- Colliding 2 BHs – a burst signal due to dynamical 2-body, 3-body or 4-body interactions

BBH Mergers due GW radiation from Globular Clusters

Number of merging BBH binaries within Hubble time per unit time (1 Myr) as a function of merger time for black holes with $M_{\text{BH}} < 100 M_{\text{sun}}$

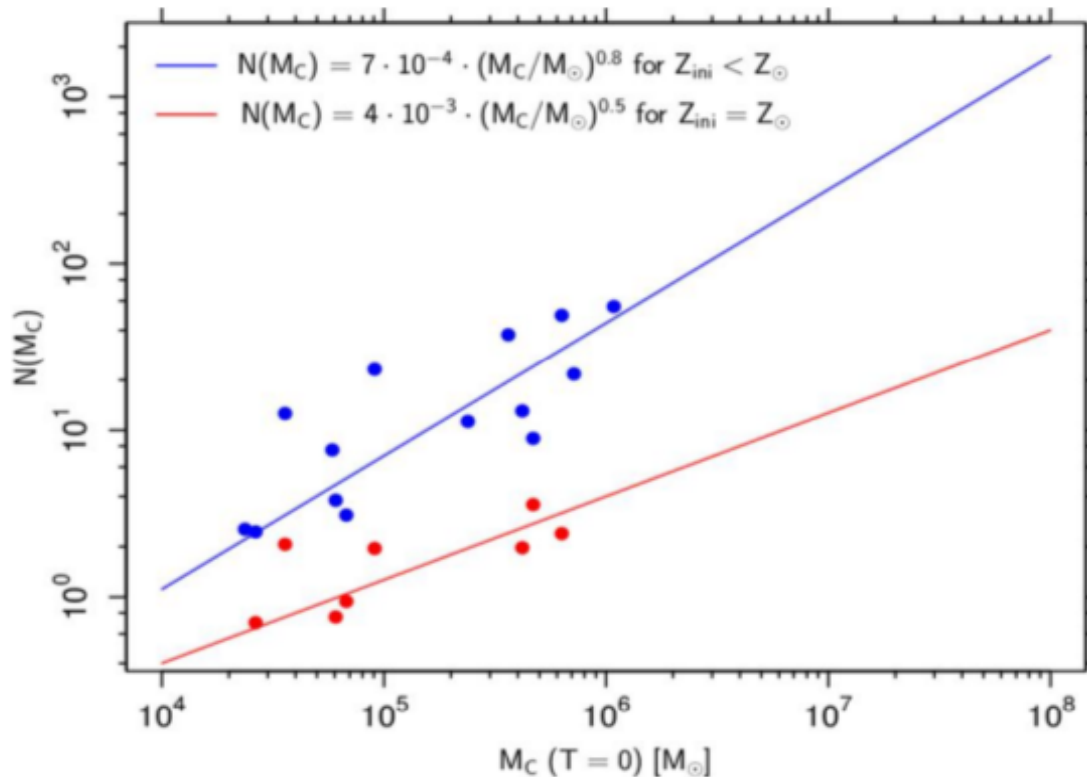
BBH in GC: 3 000; BBH ejected from GC $\sim 15\,000$,



- Path to BBH merger
 - escaping binaries (dominating)
 - binary evolution inside GC
- Mass distribution?
- BBH production efficiency ?

Dependence on the cluster mass

- Analysis (cont) & Results



Normalized number of BBHs as a function of initial cluster mass M_c with fitted function $N(M_c)$ (BBH production efficiency).

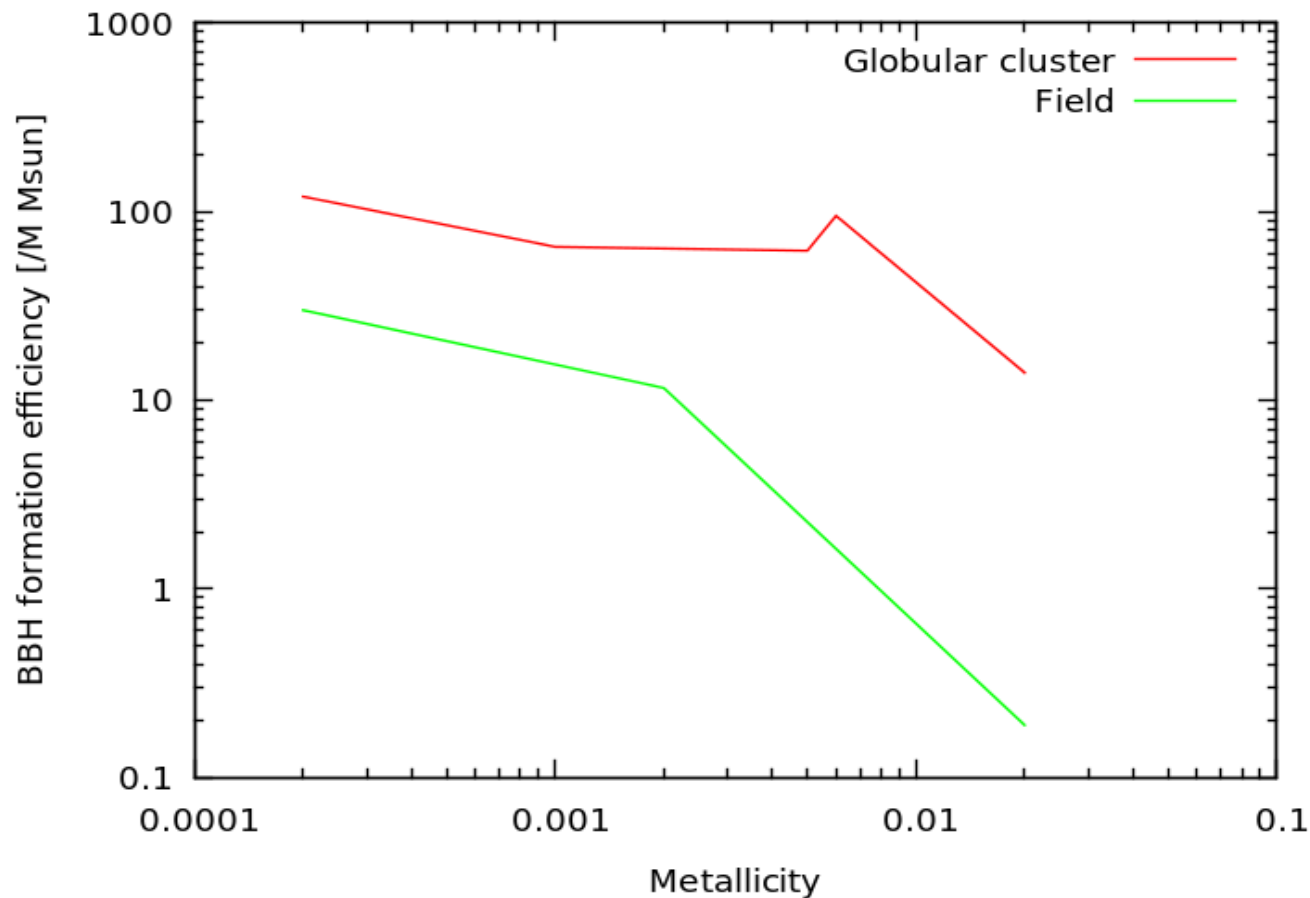
- Normalization function:

$$N(M_c) = \frac{n}{n_s \cdot M_c / 10^6 M_\odot}$$

- $Z < 0.02$ – 17 269 merger events
- $Z = 0.02$ – 865 mergers
- Regardless of the metallicity, if the mass of a GC model is large, then the number of merging BBHs is higher.
- Low-metallicity clusters have a greater ratio of producing merging BBHs compared to higher metallicity cluster models.
- If clusters have larger initial masses then they will produce more merging BBHs.

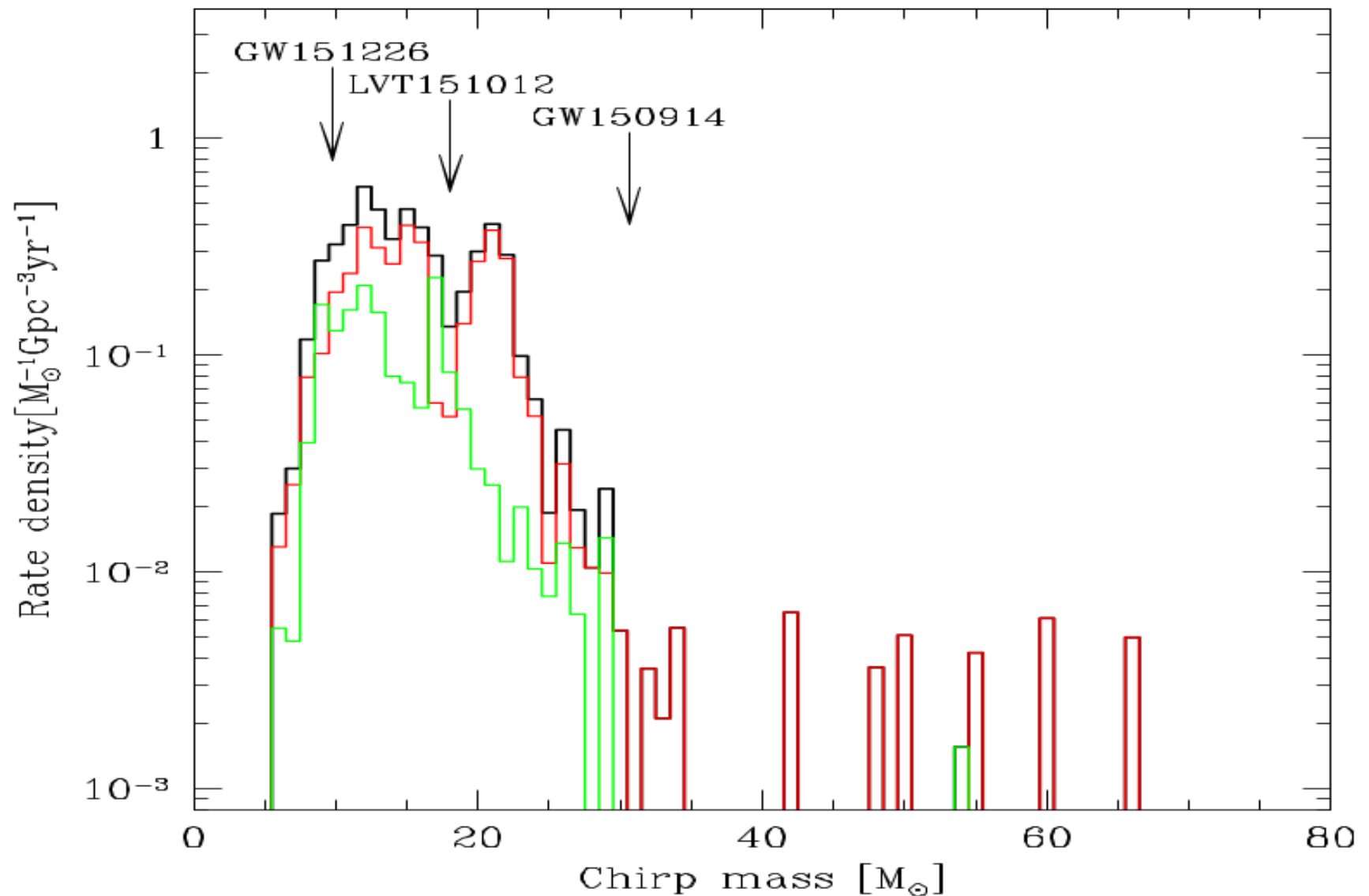
BBH production efficiency:GC vs Field

Number of merging BBH binaries per 10^6 solar masses of stars.
Field data from Belczynski et al 2016



Local merger rate density for BBH merger

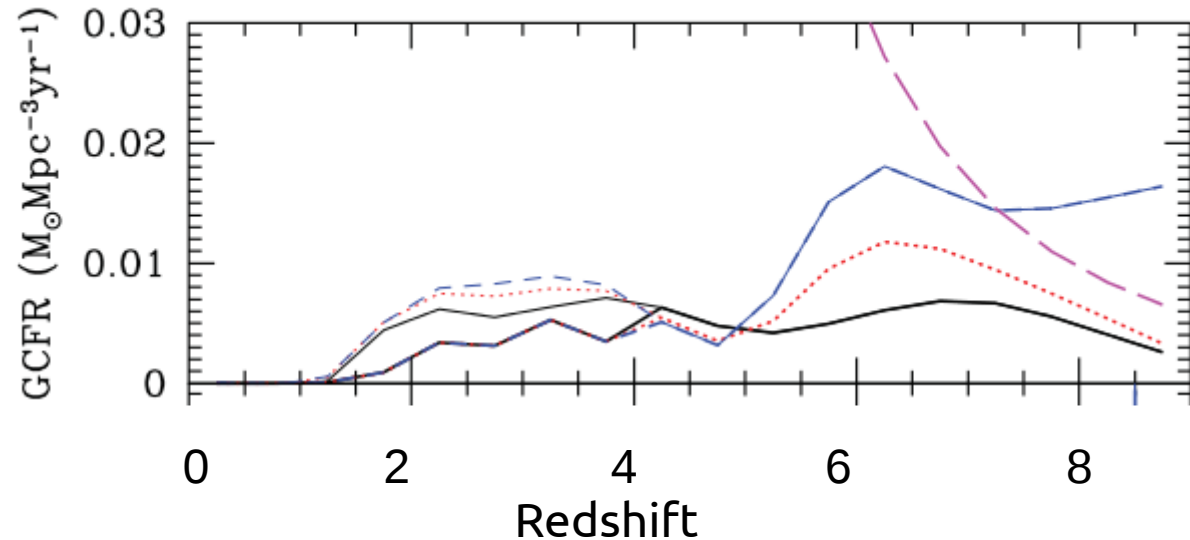
The dominant contribution – escaping BHBH



Merger rates in clusters

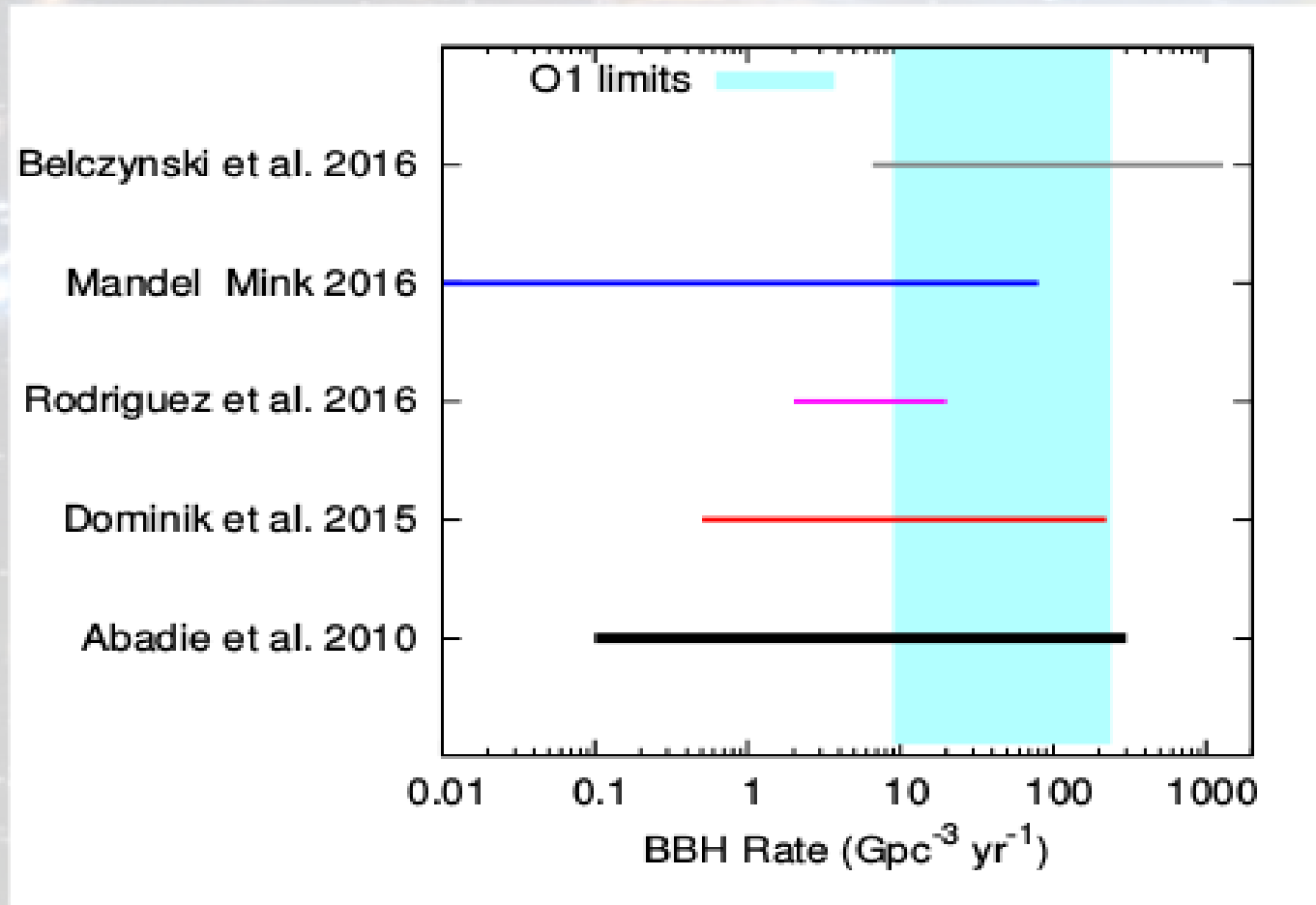
- Globular Cluster formation rate

Katz & Ricotti 2013



- GC mass composition
- GC metallicity
- The local merger rate (Abbas, Szkudlarek, Rosinska, Bulik, Giersz 2017)
 - $5.4 \text{ Gpc}^{-3}/\text{yr}$
 - $30 \text{ Gpc}^{-3}/\text{yr}$ if we include GC with $10^7 M_{\text{sol}}$,
- Systematic uncertainties to be understood

BBH merger rate: $9 - 240 \text{ Gpc}^{-3} \text{ yr}^{-1}$

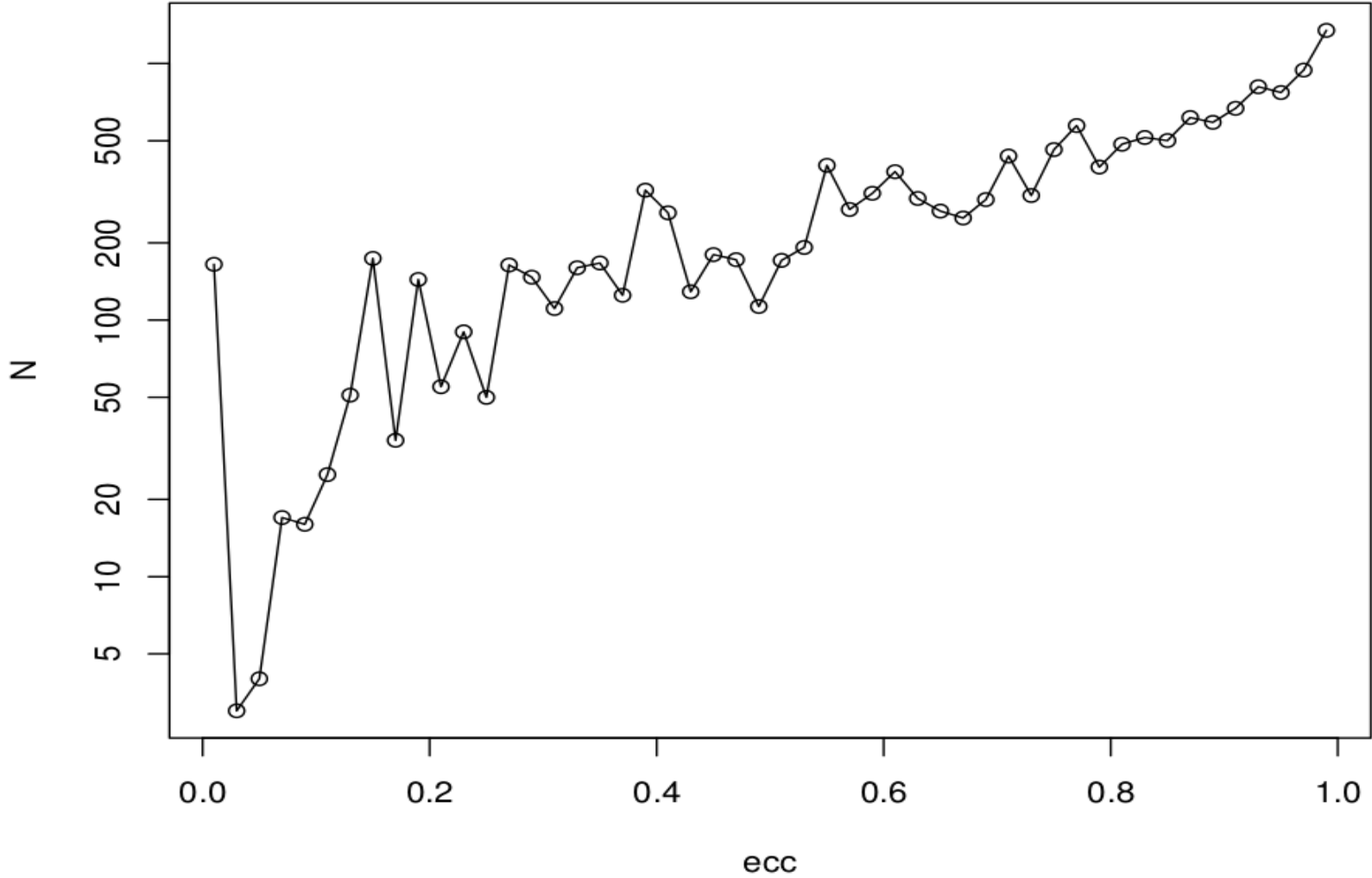


Field vs Globular Clusters

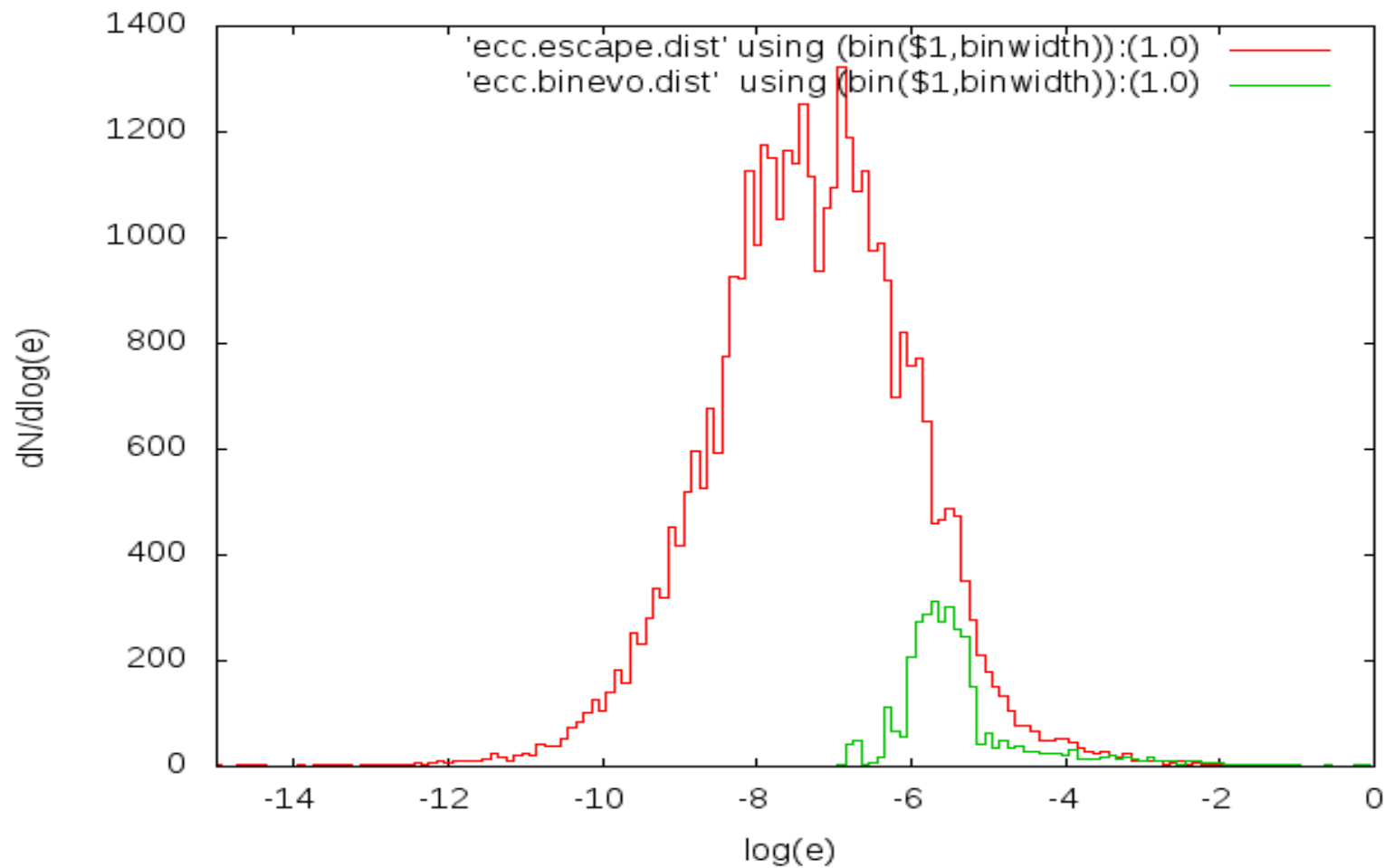
- Can we use spins to distinguish the two?
- GC formation – exchanges, non aligned spins
- Are spins aligned in field evolution?

- Can we use eccentricities to distinguish the two?
- In the field only 0.1% with $e > 0.01$ (Kowalska et al. 2011)
- In GC, dynamically-formed binaries highly eccentric ?

Eccentricity of BBH at ejection



Eccentricities of coalescing BBH at 10 Hz ...but 3-body interactions

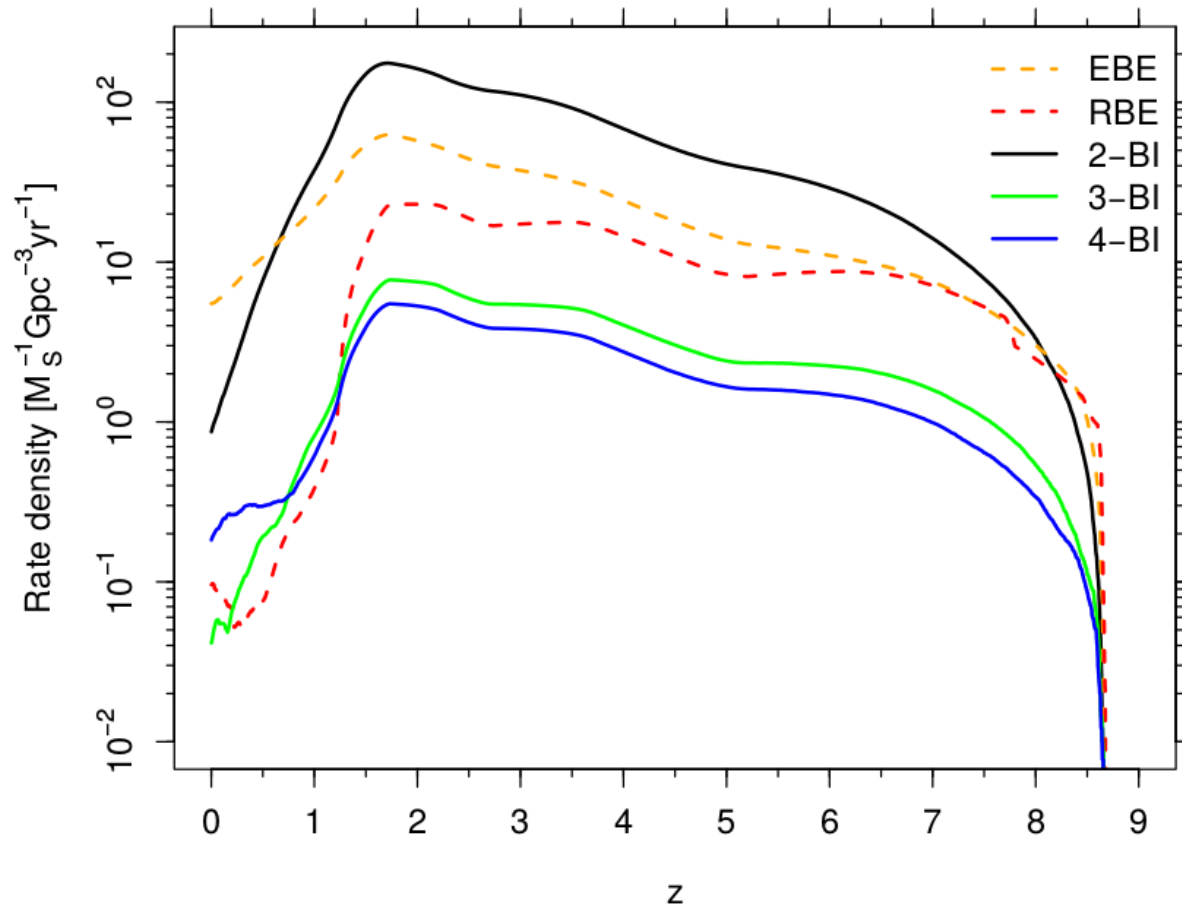


Globular clusters and gravitational waves

- Binary/Stellar evolution produces a number of interesting objects and exotic binary systems in globular clusters.
- Dense stellar environments of globular clusters are conducive to forming hard binaries with evolved compact objects.
- Dynamical interactions in globular clusters can eject a lot of binary systems that could be potential sources of gravitational waves.
- Numerous studies have used star cluster evolution codes to predict the number of gravitational wave events (mostly BBH mergers) originating from Globular Clusters.
 - Monte Carlo Codes: Downing et al. (2011), Rodriguez et al. (2015) and Rodriguez, Chatterjee & Rasio (2016), Askar et al. (2016).
 - Direct N-body Codes: Banerjee, Baumgardt & Kroupa (2010), Tanikawa (2013), Bae, Kim & Lee (2014) and Mapelli (2016).

Work in progress

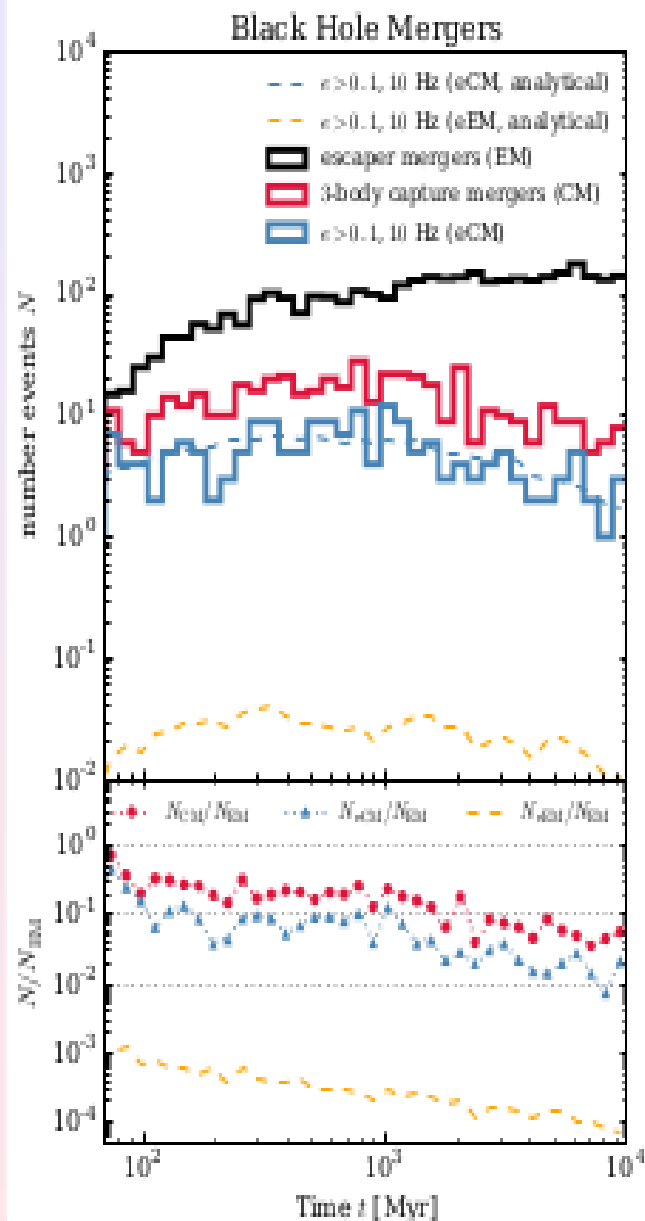
30 % of globular cluster models contain IMBHs, 100-10000 M_{sol} (Giersz et al. 2015).
One of formation scenario: built up BH mass due to mergers in dynamical interactions and mass transfer in binaries



Summary

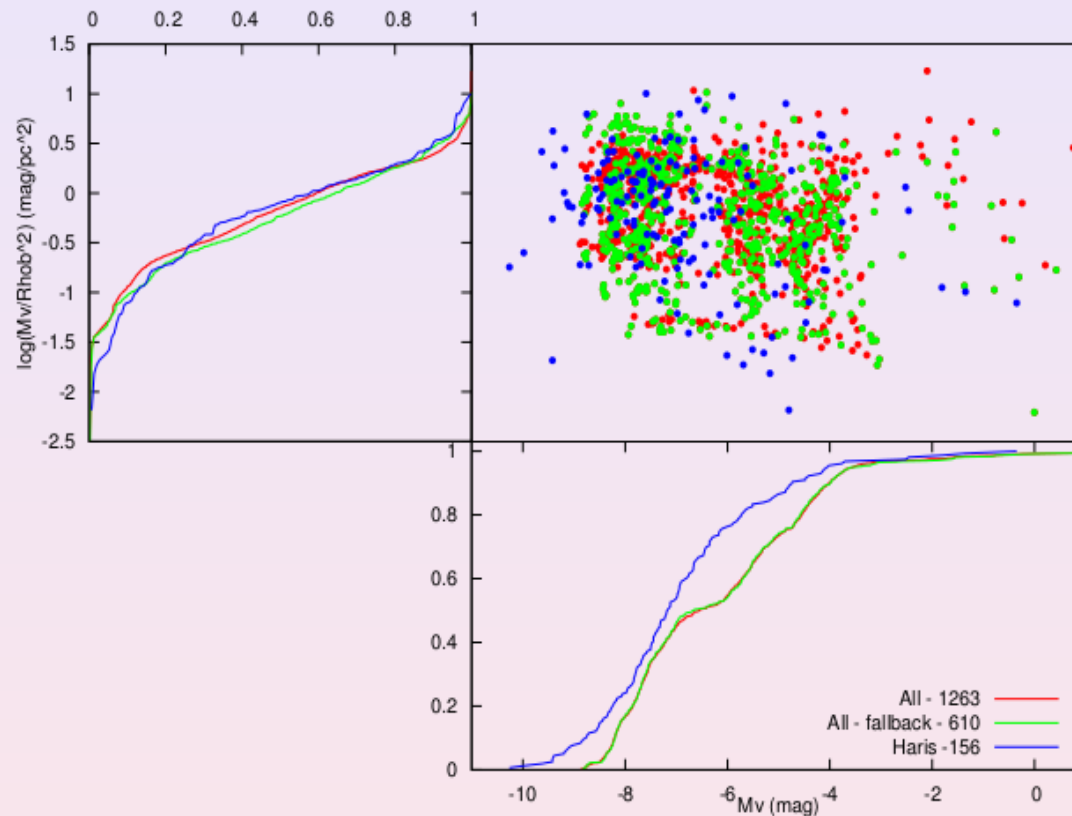
- We have explored mergers of BBHs from 1000 GC using well tested MOCCA code.
- The dominant contribution is from ejected BBH and low metallicity models
- The local merger rate density of BBH from globular cluster for LIGO/VIGO detectors (masses of BH < 100 Msol) is
5.4-30 Gpc⁻³/yr (Abbas,Szkudlarek,Rosinska,Bulik,Giersz 2017)
- Rates are in the low end of the observed values
 - Depends on assumptions on cluster mass and metallicity distribution
- Mass distribution of BBH consistent with aLIGO/Virgo observations
 - Predict a tail of higher mass object merging inside clusters
- The number of eccentric BBH systems ejected from clusters or merged in GC will not be a significant source for Advanced LIGO/Virgo (..but BH in triple systems etc)
- The IMBH (> 100 Msol) is formed in 30 % GC models → many BH-BH collisions
- **Expect a lot of discoveries in near future !!!**

BH-BH Mergers in 3-body Interactions



- 500,000 strong [BH-BH]-BH interactions were selected from more than 6,000,000 interactions in more than 2,000 MOCCA simulations;
- All selected interactions were **redone** by the Fewbody code with included PN terms;
- Number of BH-BH Mergers with **eccentricity larger than 0.1** is about **two orders of magnitude** larger than previous analytical estimates;
- In all MOCCA simulations (without PN terms) there was only **one** BH-BH merger in [BH-BH]-BH interaction, but in **redone** interactions there were more than 500 such interactions!
- Addition of dissipative effects during BH interactions can increase BH-BH merger rate by **2 to 3 orders of magnitude**.

Model vs Milky Way Globular Clusters

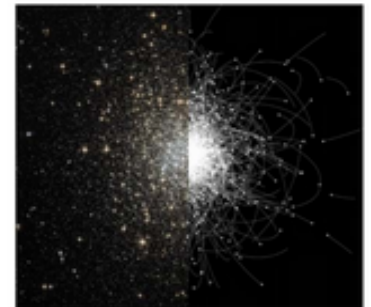


Models for the Survey were not selected to match the observed Milky Way GCs. Except for few bright (massive and intermediate mass) Galactic GCs, the agreement with the observational properties of Galactic GCs is quite good. Despite this agreement, **any combination of global observational properties of GCs cannot be used to clearly distinguish between different cluster models** because there is a strong degeneracy with respect to the initial conditions.

It can be assumed that the Survey cluster models are representative of the MW GC population.

Stellar dynamics and Globular Clusters

- Stellar dynamics describes systems of many point mass particles whose mutual gravitational interactions determine their orbits.
- Globular clusters are excellent laboratories for stellar dynamics.
- Evolution of star clusters can be numerically modelled using sophisticated *N-body* and Monte Carlo codes.
- Dynamical evolution of such collisional system is governed by a number of physical processes that include
 - 2-body Relaxation of Stars
 - Stellar Evolution
 - External Tidal Fields
 - Binary Formation and Interactions
- **MOnte Carlo Cluster simulAtor (MOCCA):** Code to evolve real size globular clusters (Giersz et al. 2013) - <http://moccacode.net/>
 - Based on the application of the Monte Carlo method to star clusters, known as Hénon's Method (1971).
 - Precision and detailed output of MOCCA simulations is comparable to N-body codes, but MOCCA is much faster (can simulate the evolution of a cluster with million stars up to a Hubble time within a day).



Local Merger Rate Density of BBH Mergers

- Calculated local merger rate density can be 3 to 5 times higher:
 - Uncertainties in initial cluster mass: In order to reproduce the more massive and bright observed GCs, we will need to have initial cluster masses larger than what were simulated in the survey models. (up to $10^7 M_{\odot}$)
 - Recall the production efficiency:

$$Z = 0.02 \rightarrow N(M_c) = 4 \times 10^{-3} \cdot (M_c/M_{\odot})^{0.5} \quad Z < 0.02 \rightarrow N(M_c) = 7 \times 10^{-4} \cdot (M_c/M_{\odot})^{0.8}$$

- Additionally, the uncertainty in the metallicity composition of GCs in early galaxies and the uncertainties connected with stellar IMF and the maximum stellar mass may also introduce an additional increase in the merger rate.
- Expected rate of events in the first LIGO observing run (O1):
 - 0.36 to 1.8 detections
 - In agreement with Rodriguez, Chatterjee & Rasio (2016).