



The MUonE Project

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The muon $g-2$ anomalous magnetic moment*

Why study the anomalous magnetic moment of the muon?

Because, it is one of the most precisely measured quantities in particle physics. It puts severe limits in deviations from the Standard Model and opens a window to new physics

An experimental measurement includes all effects, known and unknown, that exist in the real world (electromagnetic, weak, strong, gravitational plus any other unknown interaction)

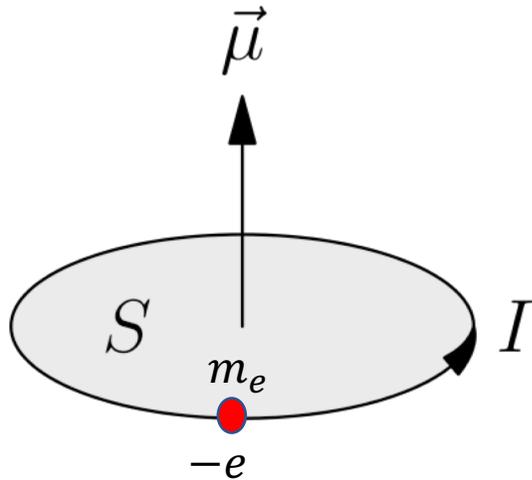
On the theory side a considerable effort is underway in order to reduce the uncertainty in the Standard Model which is dominated by hadronic correction

The muon ($g-2$) is astonishing as an observable. It has a classical meaning but it is a non trivial quantum structure.

*Not an anomalous physical quantity but discrepancy between measurement and theory

The Basics

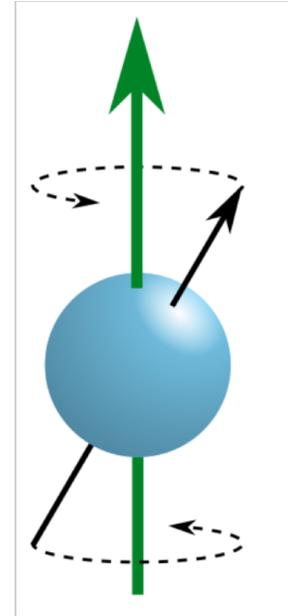
Orbiting electron



magnetic moment: $\mu = \frac{-e}{2m_e} L$

gyromagnetic ratio: $\gamma \equiv \frac{\mu}{L} = \frac{-e}{2m_e}$

Isolated electron



1935, Dirac (QM): $\gamma_e = g_e \frac{-e}{2m_e}$

$g_e = 2$

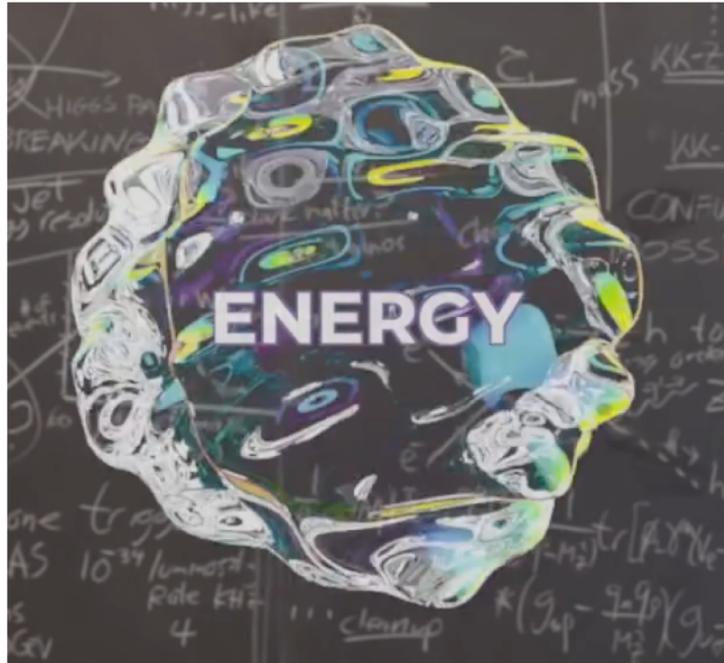
1948, QED : $g_e = 2(1 + \frac{\alpha}{2\pi} + \dots)$

with $a \approx \frac{1}{137}$

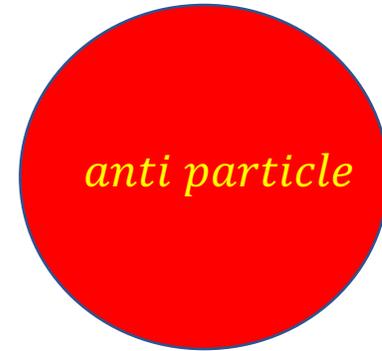
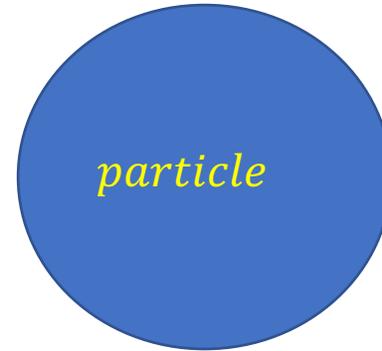


$g_e = 2.00238$

The Basics



Strong energy around the electron



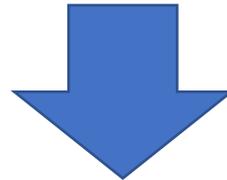
QED
Weak Forces
Strong Forces

Muon has a g_μ in analogy to the electron

STATUS in 2006

Experimental: $2.00233184160 \pm 0.00000000063$

Theoretical: $2.00233183608 \pm 0.00000000108$



Agreement in :

Experimental: $2.00233184160 \pm 0.00000000063$

Theoretical: $2.00233183608 \pm 0.00000000108$

Muon has a g_μ

Let's disentangle the part coming from the "cloud":

$$\text{Fraction} = \frac{(\text{measured } g) - (1935s \text{ prediction})}{(1935s \text{ prediction})} \quad \Rightarrow \quad \alpha = \frac{g - 2}{2}$$

In terms of α :

Experimental:

$$0.00116592080 \pm 0.00000000031$$

Theoretical:

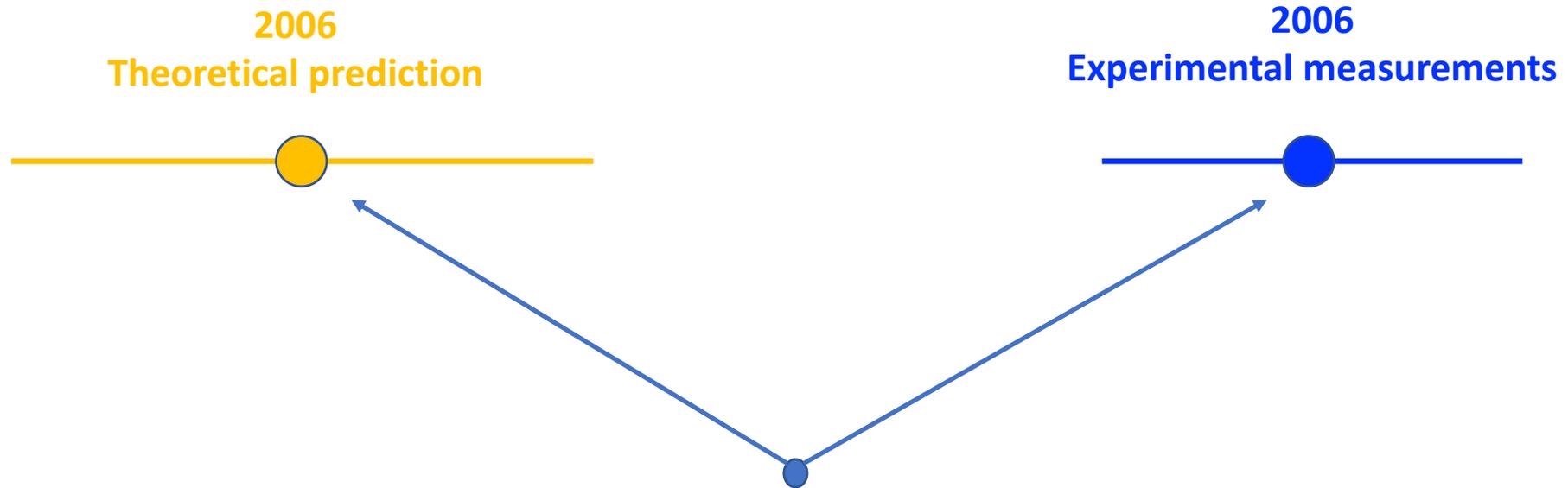
$$2.00116591804 \pm 0.00000000054$$

*keep the part of
disagreement*

Exp: 2080 ± 31

Th: 1804 ± 54

Muon g_μ : situation in 2006



Options:

1. One of these is wrong
2. There are some physical phenomena that theory doesn't include

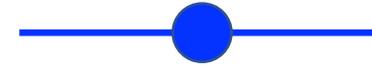
Muon g_μ : situation in 2021

2021
Theoretical prediction

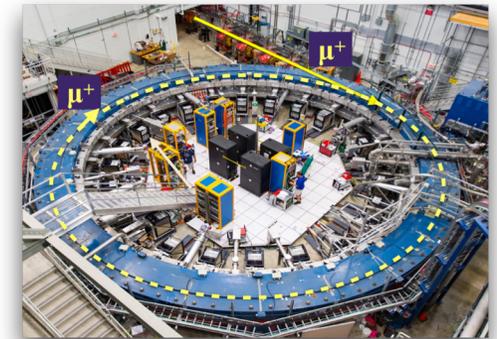
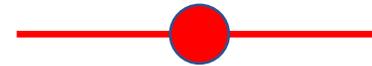


Not much change in theoretical calculations

2006
Experimental measurements



2021
New Fermilab experimental measurements

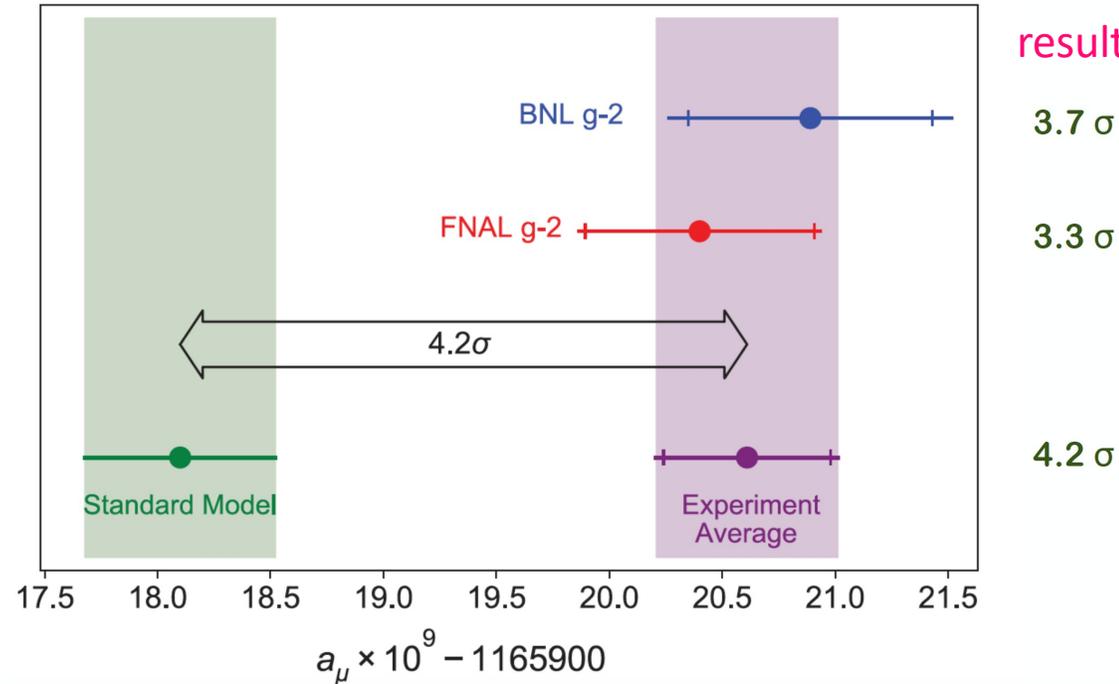


Muon g-2 measurements

[Phys.Rev.Lett. 126 \(2021\) 141801](#)

FNAL confirmed BNL:
the experimental
result is robust

SM: Muon g-2
Theory Initiative



BNL E821	$(116592089 \pm 63) \times 10^{-11}$	Dominant Statistical
FNAL E989 Run 1	$(116592040 \pm 54) \times 10^{-11}$	uncertainties
Weighted Average	$(116592061 \pm 41) \times 10^{-11}$	0.35 ppm

Expected improvements: factor 2 from FNAL Run 2+3; more from Run 4+5

Muon g_μ : situation in 2021

What does this discrepancy tell us?

1935 quantum
calculations

2.00233184160

1% correction

0.1% correction

10% correction

0.01% correction

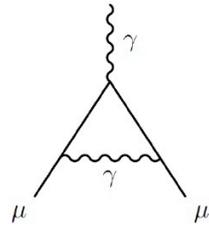
decreasingly smaller corrections

Muon anomalous magnetic moment

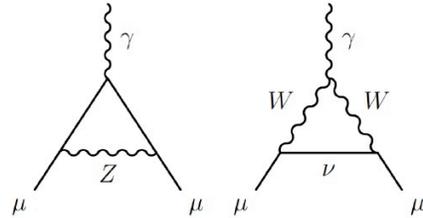
Currently accepted Standard Model prediction:
White Paper of the Muon g-2 Theory Initiative

[Aoyama et al., Phys.Rept.887\(2020\)1](#)

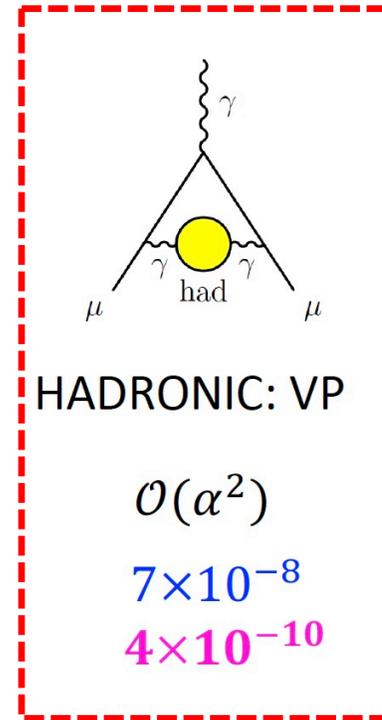
$$a_{\mu}^{SM} = a_{\mu}^{QED} + a_{\mu}^{EWK} + a_{\mu}^{had}$$



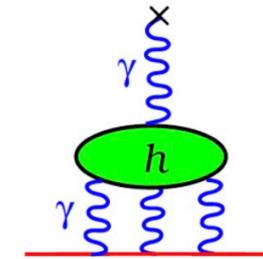
QED



EWK



HADRONIC: VP



HADRONIC: Light-By-Light

Order	$\mathcal{O}(\alpha)$	$\mathcal{O}(G_F m_{\mu}^2) = \mathcal{O}\left(\frac{\alpha}{s_W^2} \frac{m_{\mu}^2}{M_W^2}\right)$
SIZE	10^{-3}	10^{-9}
Uncertainty	10^{-12}	10^{-11}

$$\mathcal{O}(\alpha^2)$$

$$7 \times 10^{-8}$$

$$4 \times 10^{-10}$$

$$\mathcal{O}(\alpha^3)$$

$$10^{-9}$$

$$2 \times 10^{-10}$$

Hadronic contributions

-not calculable by pQCD-

QED LO term (Schwinger) = $\alpha/2\pi \sim 0.00116$

QED corrections known up to 5 loops,
uncertainty related to missing 6 loops!



Dominant Theoretical uncertainty

LO Hadronic Vacuum Polarization

Relative uncertainty: 0.6%

New Lattice QCD result for $\alpha_\mu^{HVP,LO}$

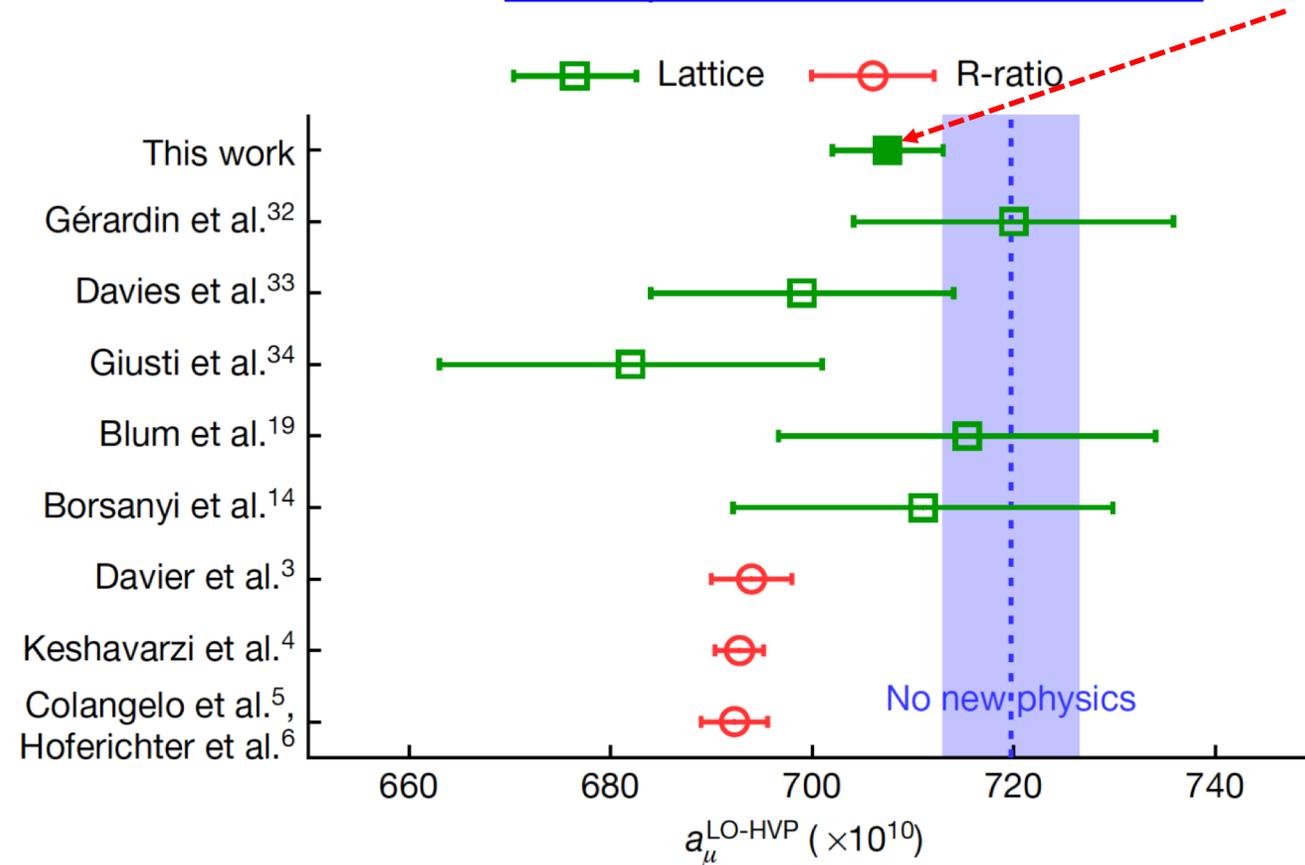
Great progress: the BMW collaboration reached 0.8% precision

It weakens the discrepancy with the measurement

tension $\sim 2\sigma$ with the standard dispersive approach

Should be checked by other independent calculations

[Borsanyi et al., Nature 593 \(2021\)](#)



$$\text{BMW(Lattice QCD): } \alpha_\mu^{HVP,LO} = (7075 \pm 55) \times 10^{-11}$$

$$\text{WP20(R-ratio): } \alpha_\mu^{HVP,LO} = (6931 \pm 40) \times 10^{-11}$$



The MuonE project

Measure the effective electromagnetic coupling in the space like region via scattering data* :



Scatter a 150 GeV muon beam on a Graphite (or Beryllium) fixed target

$$\mu^{\pm}(p_1)e^{-}(p_2) \rightarrow \mu^{\pm}(p_3)e^{-}(p_4)$$

* C.M. Carloni Calame, M. Passera, L. Trentadue, G. Venanzoni, Phys. Lett. B 746 (2015) 325, <http://dx.doi.org/10.1016/j.physletb.2015.05.020> , arXiv:1504.02228 [hep-ph].



The fundamental constrain



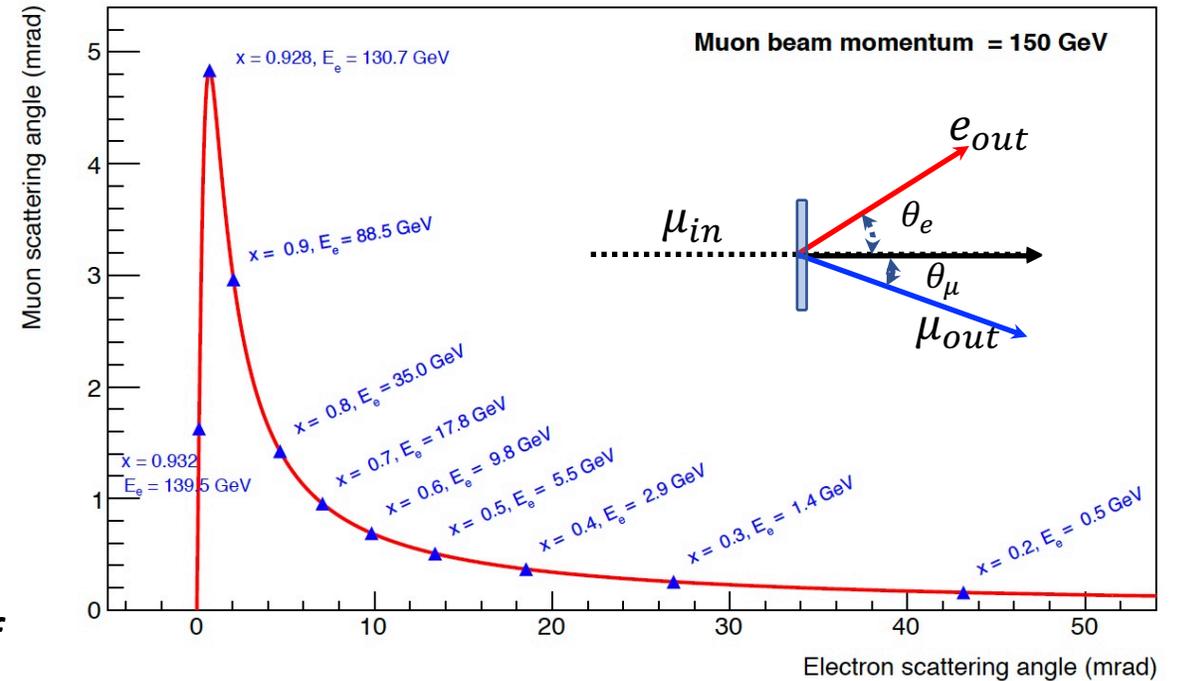
For elastic μe scattering



$$\tan\theta_\mu = \frac{2\tan\theta_e}{(1 + \gamma^2 \tan^2\theta_e) \left(1 + \frac{E_1 m + M^2}{E_1 m + m^2}\right) - 2}$$

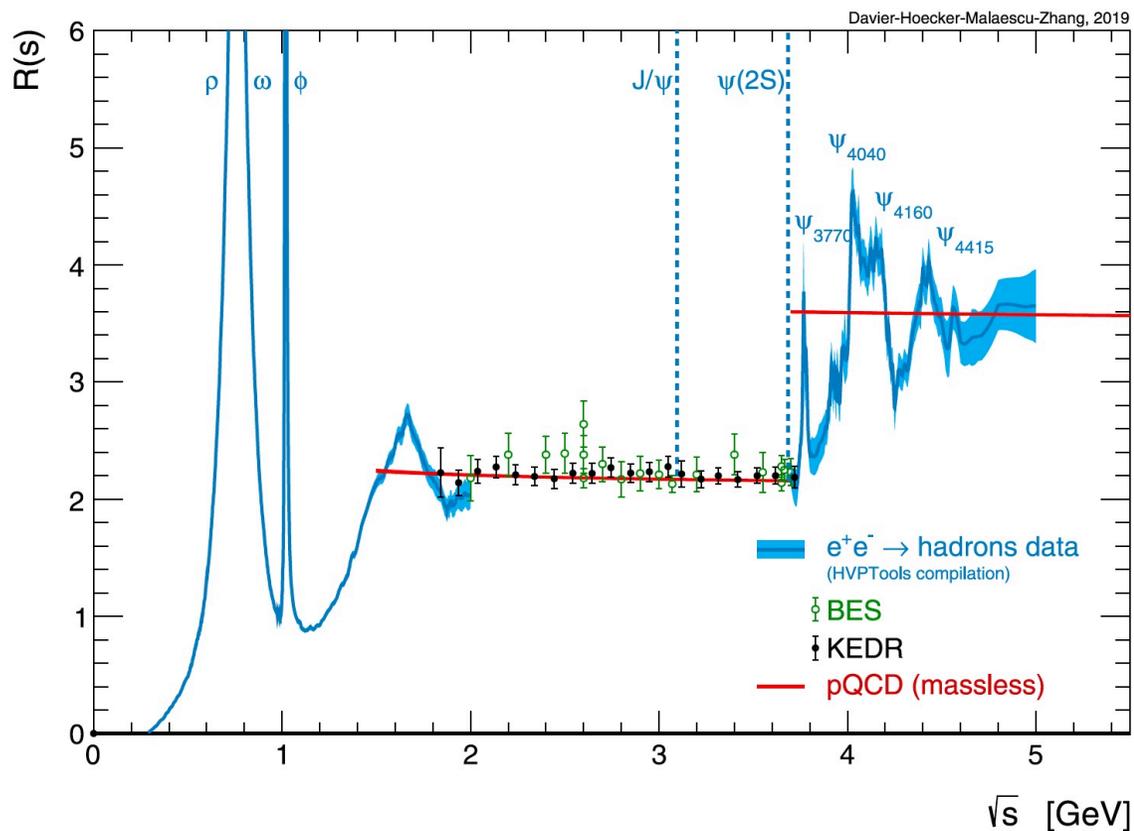
1. This is the fundamental constraint to discriminate elastic scattering events from the background of radiative events and inelastic processes.

2. At the same time, due to the small angles between the incoming muon and the outgoing electron, a detector of medium to small transverse surface will suffice.

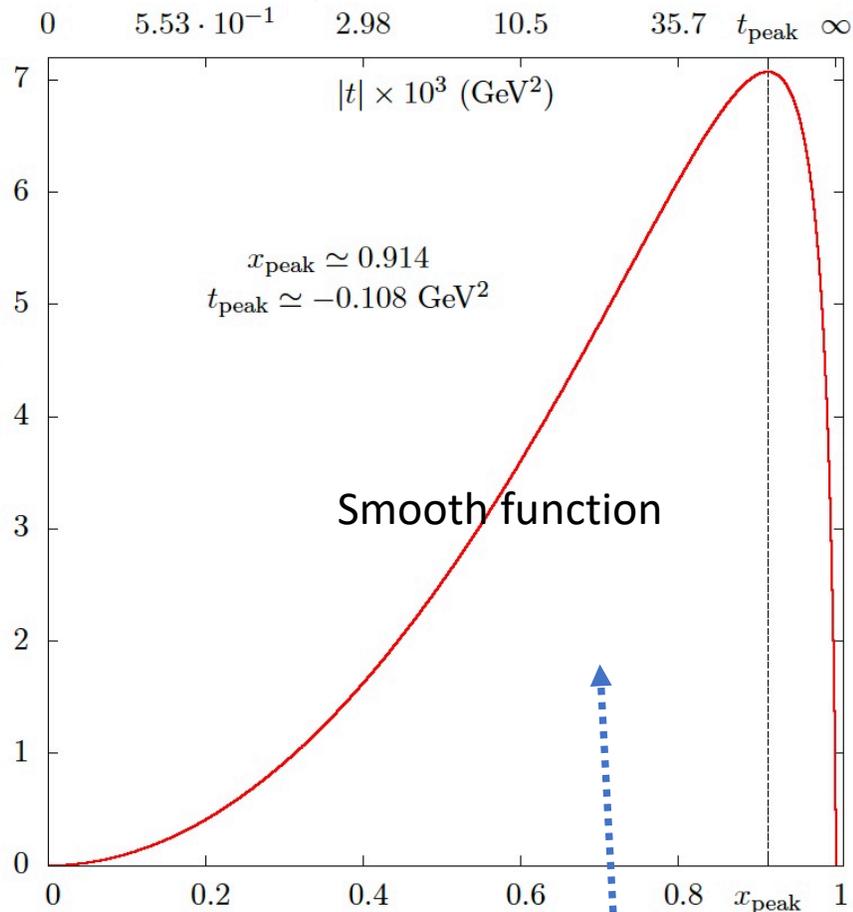




$$a_{\mu}^{had,LO} = \frac{\alpha}{3\pi} \int_0^{\infty} \frac{ds}{s} K_{\mu}^2(s) R(s)$$



$$a_{\mu}^{HLO} = \frac{\alpha}{\pi} \int_0^1 dx (1-x) \Delta\alpha_{had}[t(x)]$$



$$(1-x) \cdot \Delta\alpha_{had} \left(\frac{x^2 m_{\mu}^2}{x-1} \right) \times 10^5$$

a_{μ}^{HLO} Is the total area under this curve



How to...

In principle :

Assuming a **150 GeV** muon beam with intensity **1.3×10^7 muons/s** (presently available at CERN) incident on a Beryllium or Graphite target (**40 layers, each 1.5 cm thick**) and three years of data taking, one can reach an integrated luminosity of **$1.5 \times 10^7 \text{ nb}^{-1}$** , which would correspond to a statistical error of **0.3%** on the value of $\alpha_{\mu}^{HVP,LO}$. This will consolidate the muon g-2 and allow a firmer interpretation of upcoming measurements at Fermilab¹ and J-PARC².

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1. Fermilab Muon g-2 Collab, <http://muon-g-2.fnal.gov>
 2. J-PARC g-2/EDM Collab, <http://g-2.kek.jp>

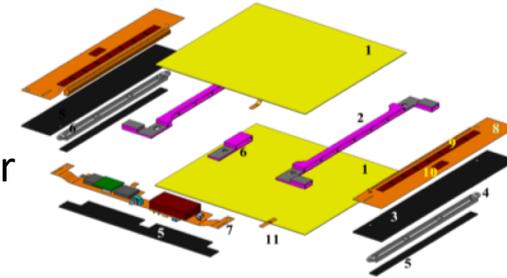


*How to...

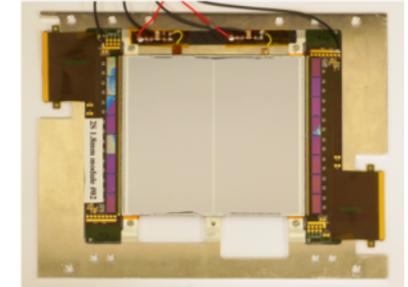


In practice :

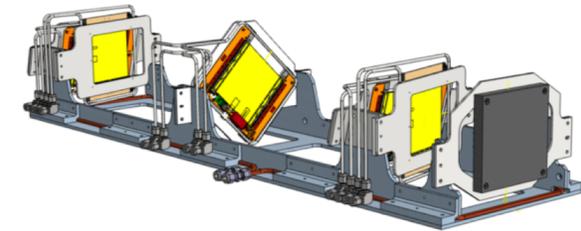
1. Get profit of current R&D for the CMS Phase II Outer Tracker



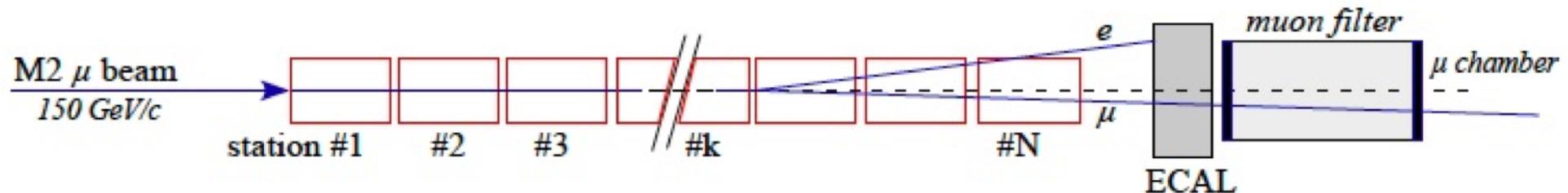
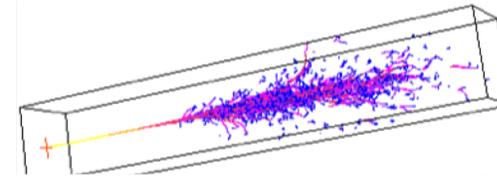
- 1. 2S silicon sensors
- 2. Al-CF spacer
- 3. CF support
- 4. Al-CF spacer
- 5. CF stiffener
- 6. Al-CF short spacer
- 7. Service Hybrid
- 8. FE Hybrid
- 9. CBC
- 10. CIC
- 11. HV tab



2. 40 stations: CMS modules (10 cm x 10 cm) equipped with plates of 1.5 cm Graphite each one, and spaced by 1 m



3. With an electromagnetic at the end a muon detector at the end

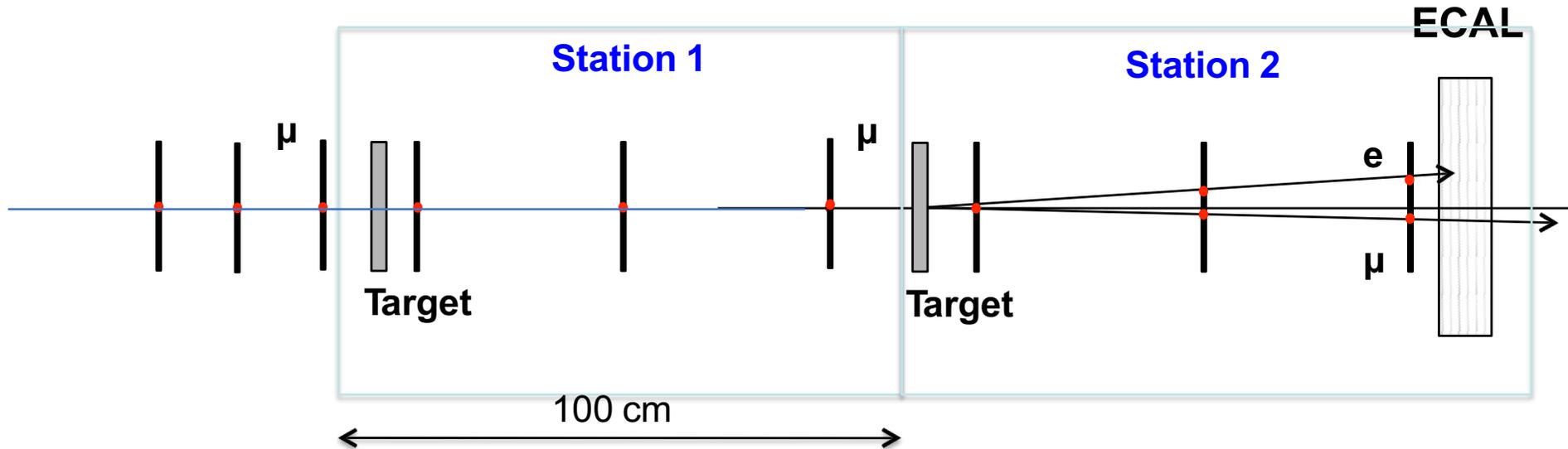




The MUonE Test Run (2021)



Test run set up :



Tracker: 18 CMS 2Smodule ~95 mm x 95 mm

Calorimeter: 25 PbWO4 crystal , ~140 x 140 mm
total length ~ 4-5 m + services

- the apparatus will be in a thermalized volume
- will run with 2 full stations plus 3 tracking planes for the incoming μ



The INPP MUonE Group

We joined the MUonE in summer 2020

Members of the INPP group

Panagiotis	Assiouras
Giannis	Kazas
Dimitris	Loukas
Kostas	Papadopoulos
Aristotelis	Kyriakis