

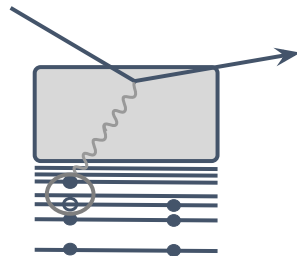
Ex fissio ad astra:  
Extending optical models to the fission fragment region

Kyle Beyer  
with Amy Lovell, Cole Pruitt, and Brian Kiedrowski

ISNET-9, Washington University in St. Louis, May 2023



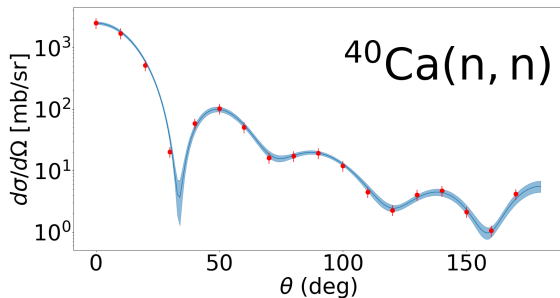
- 1 measure  $\mathcal{D}^{\text{direct}} = \left\{ \frac{d\sigma_{\alpha}}{d\theta}, \sigma_{\text{el}}, \sigma_t \right\}$



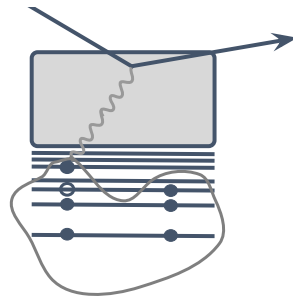
$$\frac{d\sigma_{\alpha}}{d\theta} \propto |\langle \alpha | \mathcal{T} | \alpha \rangle|^2$$

# Workflow for phenomenology of compound nucleus reactions

- 1 measure  $\mathcal{D}^{\text{direct}} = \left\{ \frac{d\sigma_{\alpha}}{d\theta}, \sigma_{\text{el}}, \sigma_t \right\}$
- 2 calibrate optical model potential  $V(r, E, A, Z; \zeta)$  to maximize posterior likelihood  $p(\zeta | \mathcal{D}^{\text{direct}})$



Courtesy of Pablo Giuliani and Daniel Odell



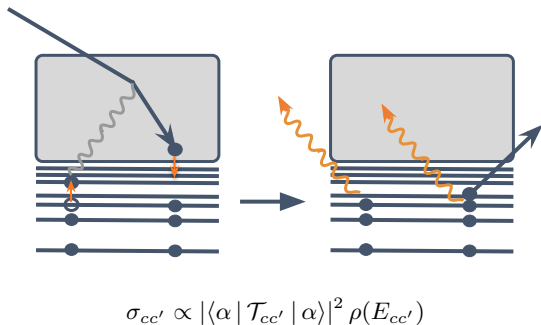
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- 3 apply optical model to generate transmission coefficients for compound-nucleus reactions

Using Hauser-Feshbach formalism de-excitation of compound nucleus is Markovian process:

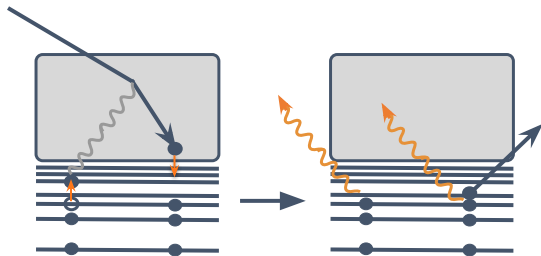
$$p_{cc'}(\alpha) = \frac{|\langle \alpha | \mathcal{T}_{cc'} | \alpha \rangle|^2 \rho(E_{c'})}{\sum_{c''} |\langle \alpha | \mathcal{T}_{cc''} | \alpha \rangle|^2 \rho(E_{c''})}$$



Often requires significant **extrapolation** of OMP away  $A, Z \in \mathcal{D}^{\text{direct}}$

# Can we globally optimize to both direct and compound reactions?

- 1 measure  $\mathcal{D}^{\text{direct}} = \left\{ \frac{d\sigma_{\alpha}}{d\theta}, \sigma_{\text{el}}, \sigma_t \right\}$
- 2 measure  $\mathcal{D}^{\text{compound}} = \left\{ \sigma_{cc'} \right\}$
- 3 calibrate optical model potential  $V(r, E, A, Z; \zeta)$  to **both direct and compound observables** by maximizing posterior likelihood  $p(\zeta | \mathcal{D}^{\text{direct}}, \mathcal{D}^{\text{compound}})$



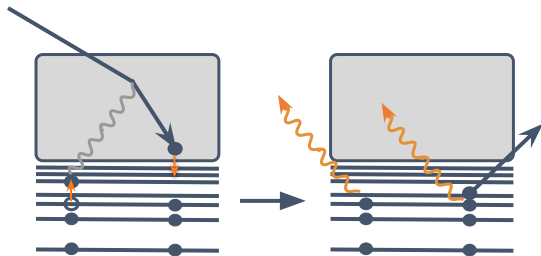
$$\sigma_{cc'} \propto |\langle \alpha | \mathcal{T}_{cc'} | \alpha \rangle|^2 \rho(E_{cc'})$$

## Challenges:

- computational cost of evaluating posterior likelihood
- high-dimensional parameter and observable space

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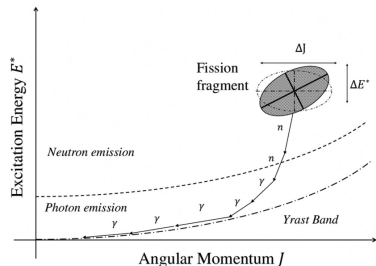
## Challenges:

- computational cost of evaluating posterior likelihood  $\rightarrow$  **emulators**
- high-dimensional parameter and observable space  $\rightarrow$  **MCMC**

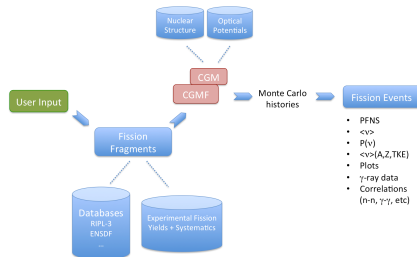
# Fission as case study for fitting to compound nucleus reactions

Why do we care about fission fragments?

- **predictive fission modeling:** [Lovell and Neudecker, 2021]
- **cross sections for fission fragments:** nuclear non-proliferation, forensics and safeguards [Hebborn et al., 2022]
- **cross sections for r-process nuclei:** neutron capture processes in supernovae and compact-object mergers sensitive to isovector terms in optical potentials [Goriely and Delaroche, 2007]



[Marin et al., 2021] arXiv:2104.06166



Goal: Globally optimize OMP to observables including prompt neutron-fragment correlations with [github.com/beykyle/cgmf](https://github.com/beykyle/cgmf) [Talou et al., 2021]

## But first, are fission observables even sensitive to the optical model?

- Propagate predictive posterior distribution of 3 OMPs through CGMF to fission observables
- Brute force approach - 40K cpu-hours
- Python bindings added to CGMF for massively parallel UQ using `mpi4py`
- replace scattering kernel with `OMPLib`

Uncertainty-quantified OMPs - potential priors for global fitting:

Phenomenological models fit to  $\mathcal{D}^{\text{direct}}$  [Pruitt et al., 2020]:

- KDUQ
- CHUQ

Microscopic model derived from N3LO  $\chi$ EFT forces in nuclear matter folder to nuclear density distributions

- WLH [Whitehead et al., 2021]

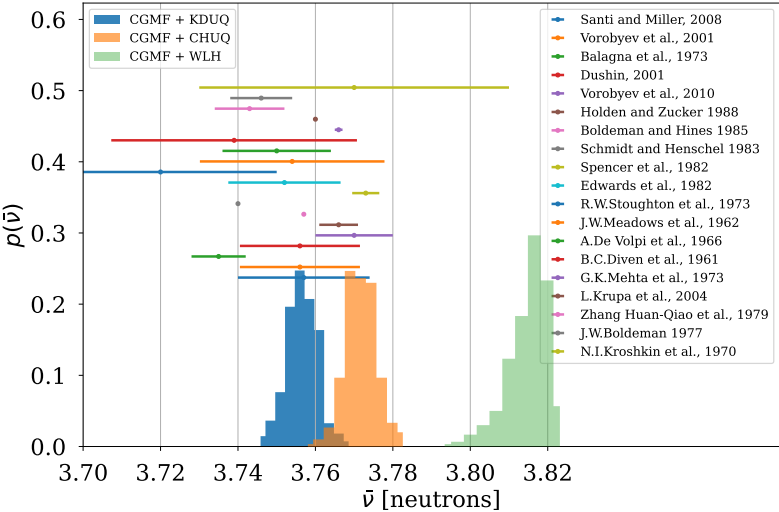
There are many observables we can use from  $\mathcal{D}^{\text{fission}}$ , all are noisy, convolved and depend on assumptions unrelated to OMP to model. Experiments are difficult, uncertainties may be missing/under-reported.





# Are neutron yields sensitive to the optical model?

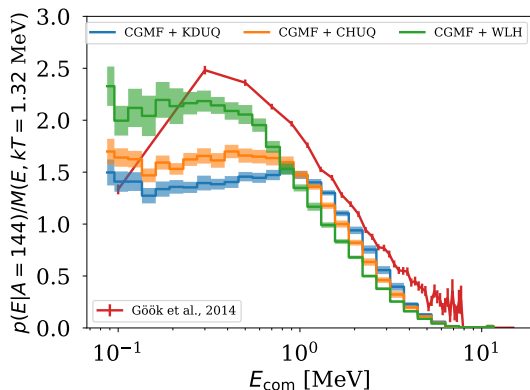
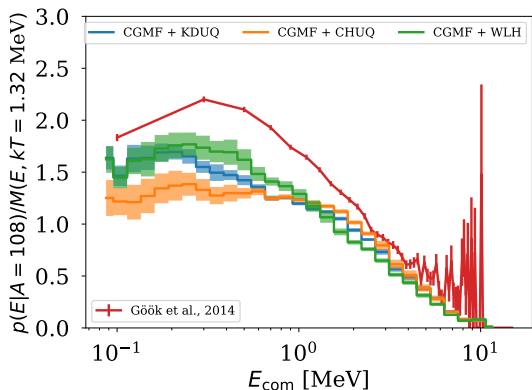
Posteriors propagated through to average neutron multiplicity per fission event in  $^{252}\text{Cf}(sf)$





# Are neutron energies conditional on $A$ sensitive to the optical model?

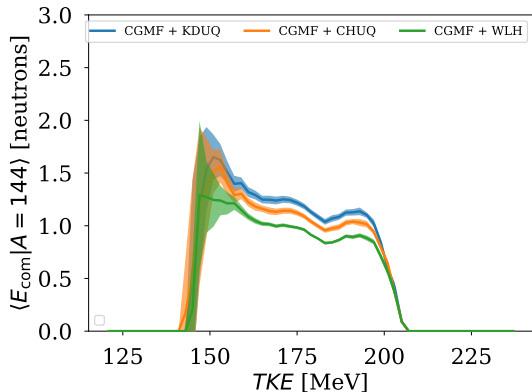
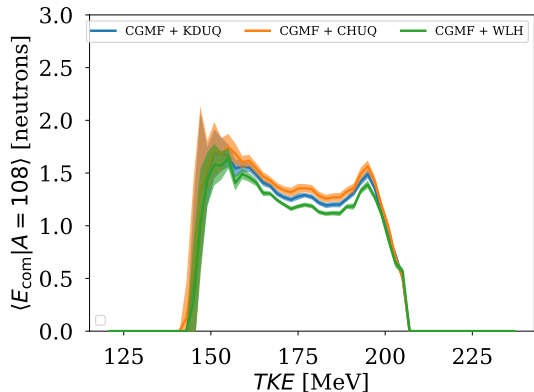
Credible intervals in  $p(E_{\text{com}}|A)$  in  $^{252}\text{Cf}(sf)$



CHUQ and KDUQ disagree on  $A, E$  dependence away from stability - but both reproduce  $\mathcal{D}^{\text{direct}}$ . Issues with WLH limited to heavy fragment region.



## Are neutron energies conditional on $A$ & $TKE$ sensitive to the optical model?

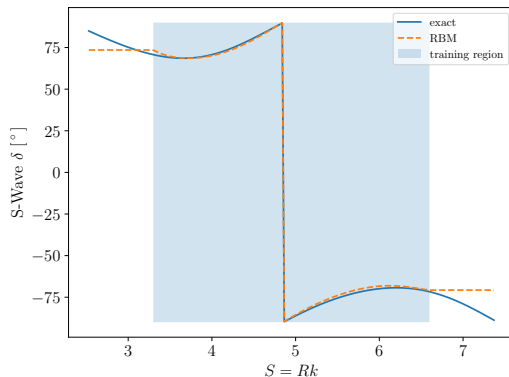


This can be measured with current experiments, and extracted event-by-event from past experiments

# Reduced basis emulators for Monte Carlo Hauser-Feshbach

$$\text{MCMC} \times \text{MCHF} = \text{MC}^2!$$

- 1000x speedup for test problem - big implications for Monte Carlo Hauser-Feshbach
- intrusive nature allows us to emulate history-by-history correlations
- empirical interpolation to “affinize” potential: big speedup but hurts extrapolation
- embedding emulator in production code CGMF
- Stick around for Daniel Odell's talk next
- (python note)book: [nuclear-rbm](#)



RBM emulator of S-wave phase shift  $\delta_0$  of the Woods-Saxon potential as width  $S$  is perturbed

### Conclusion:

- we can constrain reaction models away from stability by studying fission, but it requires emulation and careful Bayesian calibration

### Path forward:

- incorporate RBM emulators into CGMF
- calibrate OMP to cross sections in FF region ( $\mathcal{D}^{\text{direct}}$ ), and  $n$ -fragment correlations ( $\mathcal{D}^{\text{fission}}$ )
- include excitation energy sharing at scission in parameter space?
- treat deformations in (emulated) coupled channels approach?
- utilize Green's function formalism to understand Hauser-Feshbach better?
- handle unreported experimental error/covariances robustly?

### Some lessons learned from ISNET-9:

- history-by-history (rather than histogram) treatment of observables  $\mathcal{D}$
- Bayesian model mixing - let the model learn  $A, Z$  dependence?
- benefit of interacting with diverse multi-disciplinary community







Thanks for your time!

Thank you to the organizers, as well as to Pablo Giuliani, Kyle Godbey and Daniel Odell for teaching me emulators!

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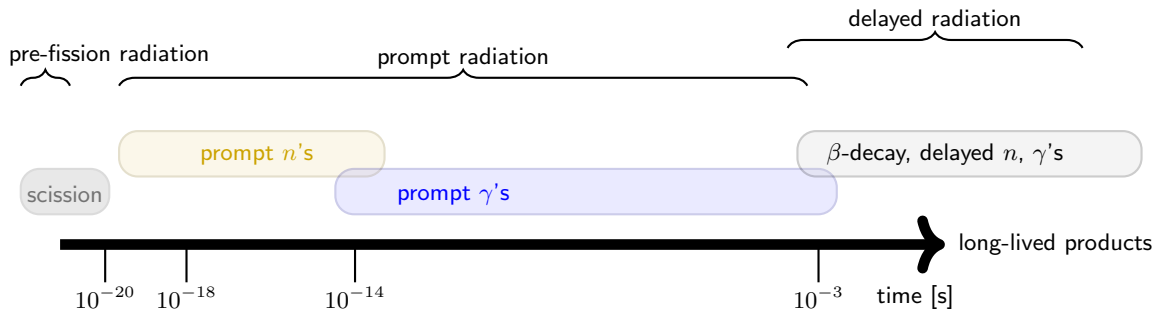


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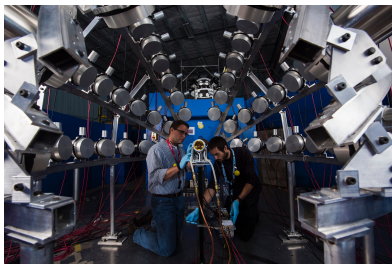
## Backup slides

## Fission and its observables



Goal: learn properties of neutron-rich nuclei by studying **prompt  $n$ 's**, **prompt  $\gamma$ 's**, & **fragments** from fission

# Fission and its observables



Chi-Nu experimental array at LANSCE  
(courtesy of M. Devlin)

$n$ -fragment correlations:

- [Göök et al., 2014]  $^{252}\text{Cf}$
- [Göök et al., 2018]  $^{235}\text{U}$

$\gamma$ -fragment correlations:

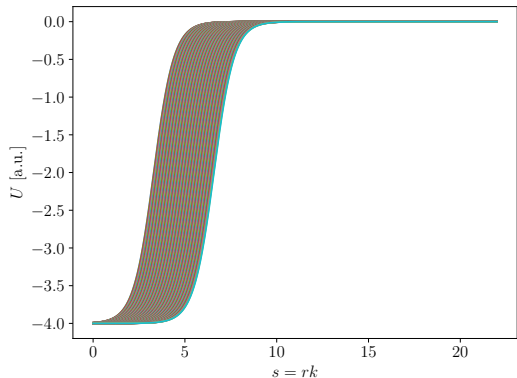
- [Travar et al., 2021]  $^{252}\text{Cf}$
- [Giha et al., 2023]  $^{239}\text{Pu}$
- [Wilson et al., 2021]  $^{252}\text{Cf}$ ,  $^{238}\text{U}$ ,  $^{232}\text{Th}$

$n$ - $\gamma$ -fragment correlations?

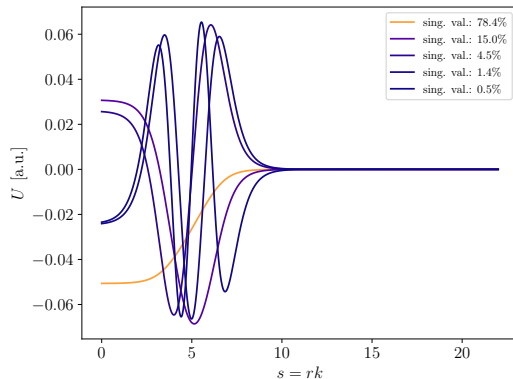
- Giha et al., ongoing at Gammasphere

Ideally, we would like an  $n$ - $\gamma$ -fragment correlated measurement with  $\sim$ amu isotopic resolution

# Affine-decomposition of a Woods-Saxon potential with Empirical Interpolation Method

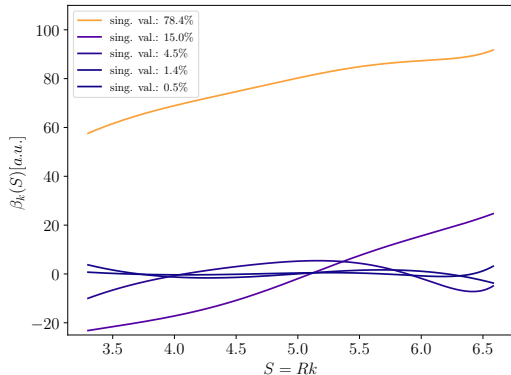


$N$  training potentials  $U(s, S_i)$  for  $S \in T = \{S_i\}_{i=1}^N$

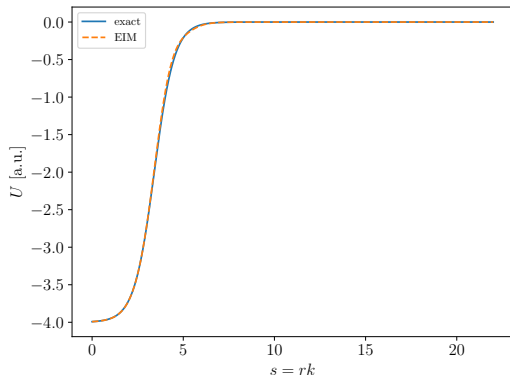


$M = 5$  principal components of the training set;  
 $\{U_{\kappa}(s)\}_{\kappa=1}^M$

## Affine-decomposition of a Woods-Saxon potential with Empirical Interpolation Method



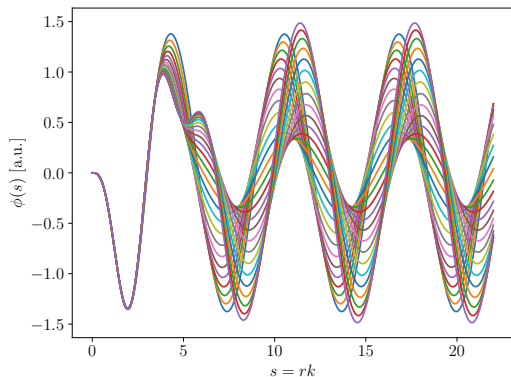
$$\beta_\kappa(S) = \sum_{j=1}^M (U_\kappa(s_j))^{-1} U(s_j, S)$$



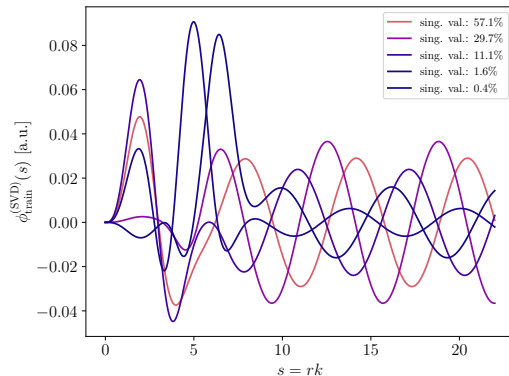
$$R = 3.1 \text{ fm}, k \approx 1.09 \text{ fm}^{-1}; S \approx 3.41$$

$$\{S_i\} \subset [3.29, 6.59]$$

# Building a reduced basis for our scattering problem



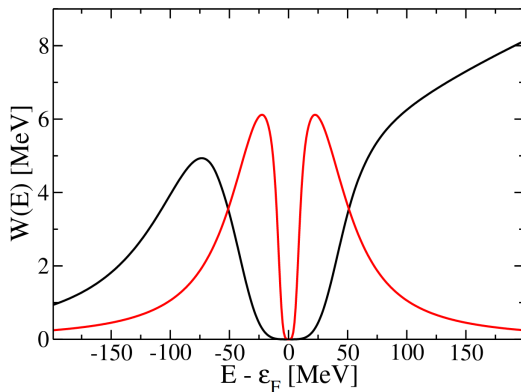
$N$  high-fidelity training solutions with free solution subtracted  $\{\psi_i(s) - \phi_0\}_{i=1}^N$



$P = 5$  principal components of the training set  $\{\phi_j\}_{j=1}^P$



# Long-range correlations at low energy



Energy dependence of imaginary **volume** and **surface** terms in a phenomenological DOM [Waldecker, 2011]. **Surface** term dominates at low energy due to LRCs!