

# Bound states and dark matter

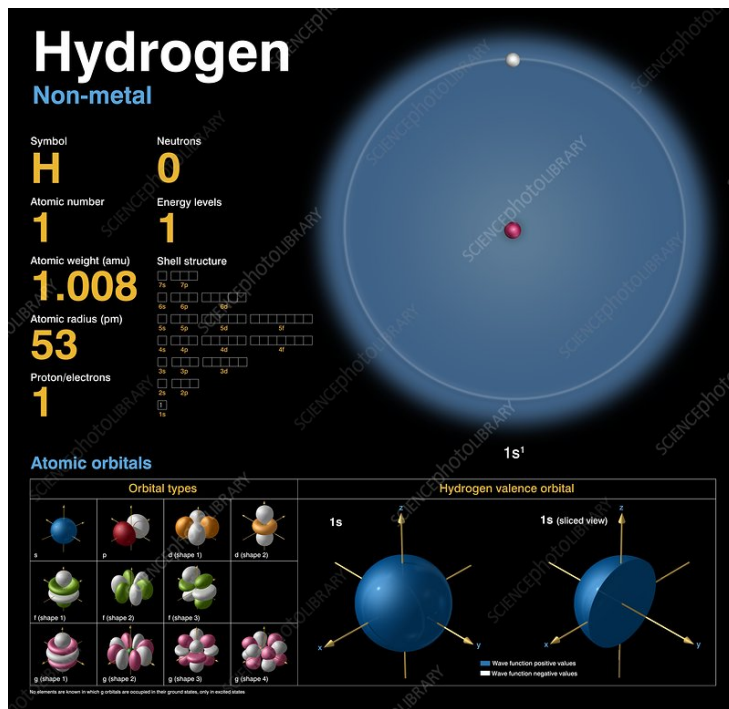
**Camilo A. Garcia Cely**  
*Alexander von Humboldt fellow*



Materia Oscura in Colombia (MOCa)

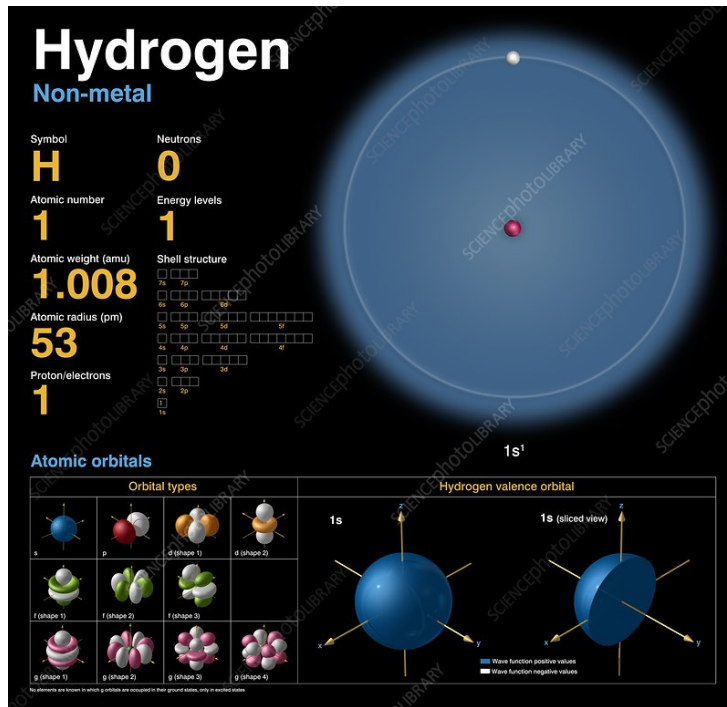
Oct 7, 2020

# Ordinary matter is in the form of bound states.

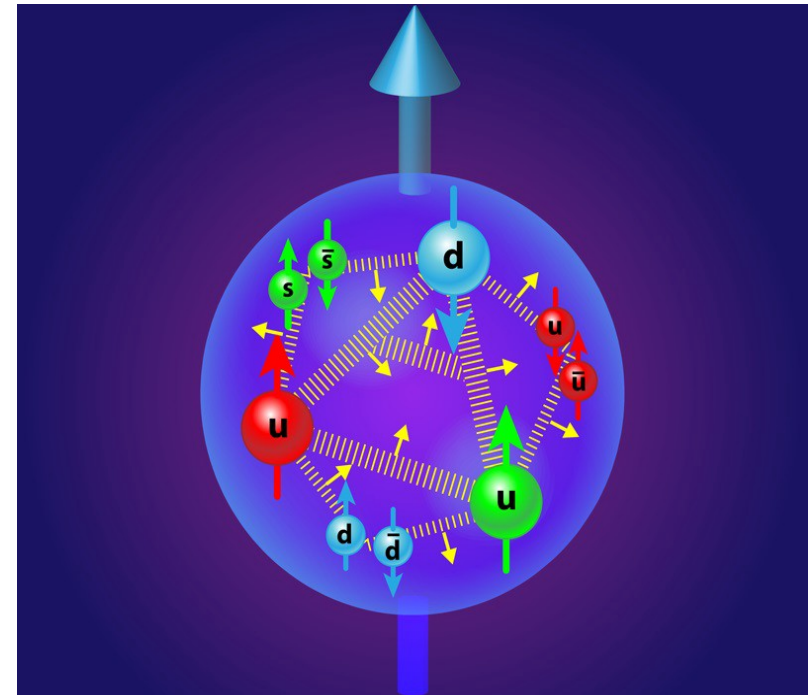


The simple example is hydrogen, which is a bound state of one proton and one electron.

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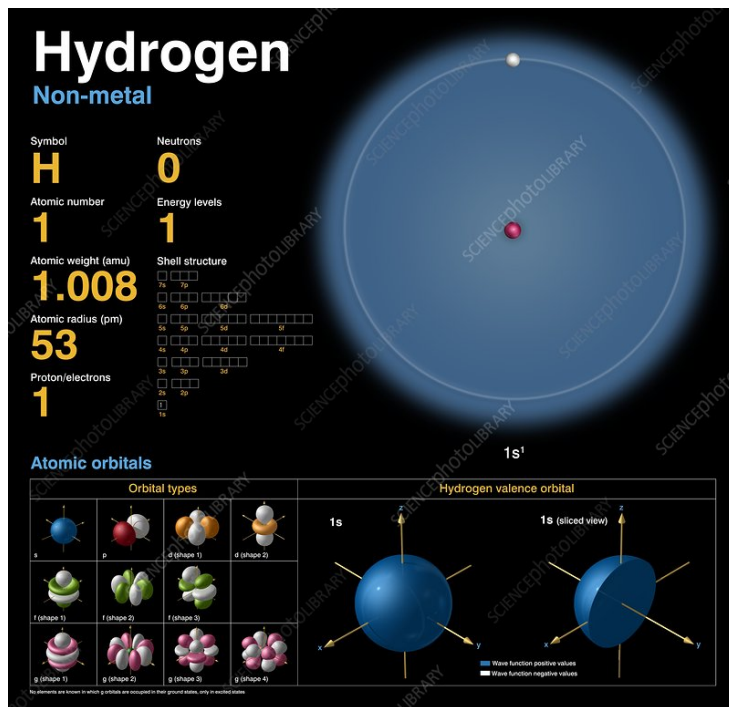


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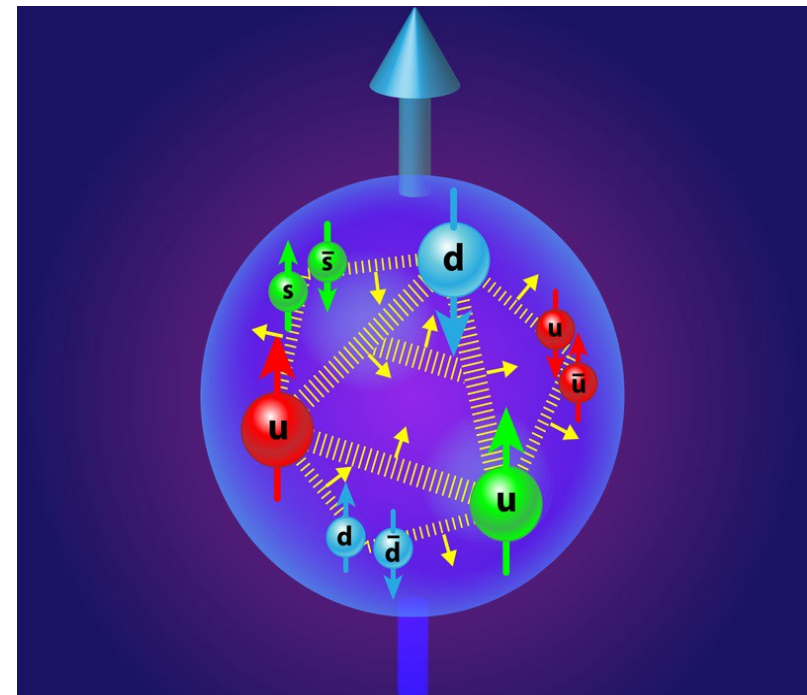


Another example is the proton itself, which is a bound state of the elementary particles of QCD.

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The simple example is hydrogen, which is a bound state of one proton and one electron.



Another example is the proton itself, which is a bound state of the elementary particles of QCD.

*It is natural to ask whether dark matter is made of bound states or if it is an elementary particle that can form them.*

# I. Dark matter forming bound states

This is rather common...

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Simple assumption:  
extend the SM with  
an electroweak  
multiplet

Quantum Numbers		
$SU(2)_L$	$U(1)_Y$	Spin
2	1/2	0
	1/2	1/2
3	0	0
	0	1/2
	1	0
4	1	1/2
	1/2	0
	1/2	1/2
	3/2	0
5	3/2	1/2
	0	0
	0	1/2
7	0	0

Inert doublets  $\sim 0.5-20$  TeV

Higgsino DM  $\sim 1$  TeV

Wino DM  $\sim 2.9$  TeV

Fermionic 5-plet  $\sim 10$  TeV

Scalar 7-plet  $\sim 25$  TeV

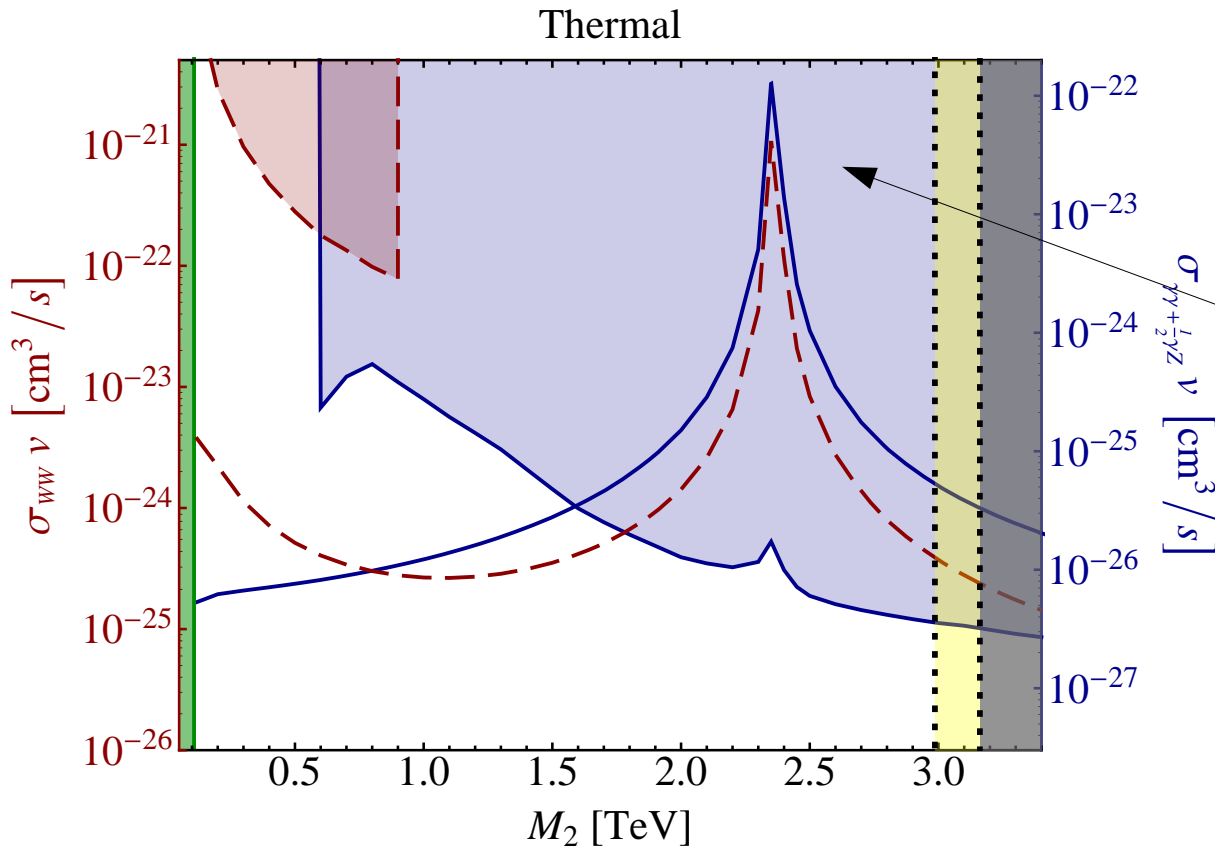
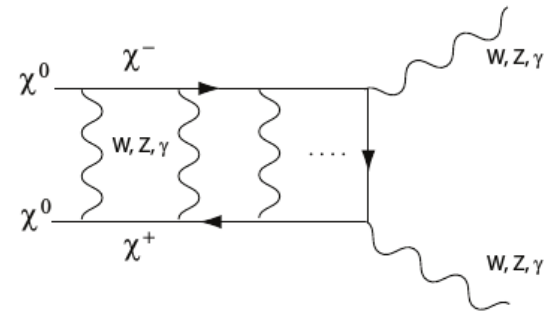
Cirelli, Fornengo, Strumia (2005)

# Indirect detection of Winos

In the early Universe  
 $\sigma v \sim 1 \text{ pb} \approx 3 \times 10^{-26} \text{ cm}^3/\text{s}$ .

Sommerfeld Effect

Hisano et al (2004)



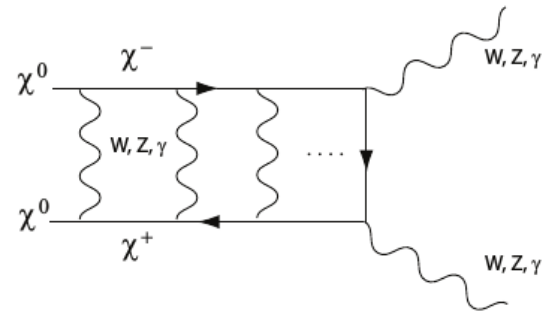
Cohen et al (2013)

*This signalizes the existence of a wino-wino bound state with a very small binding energy*

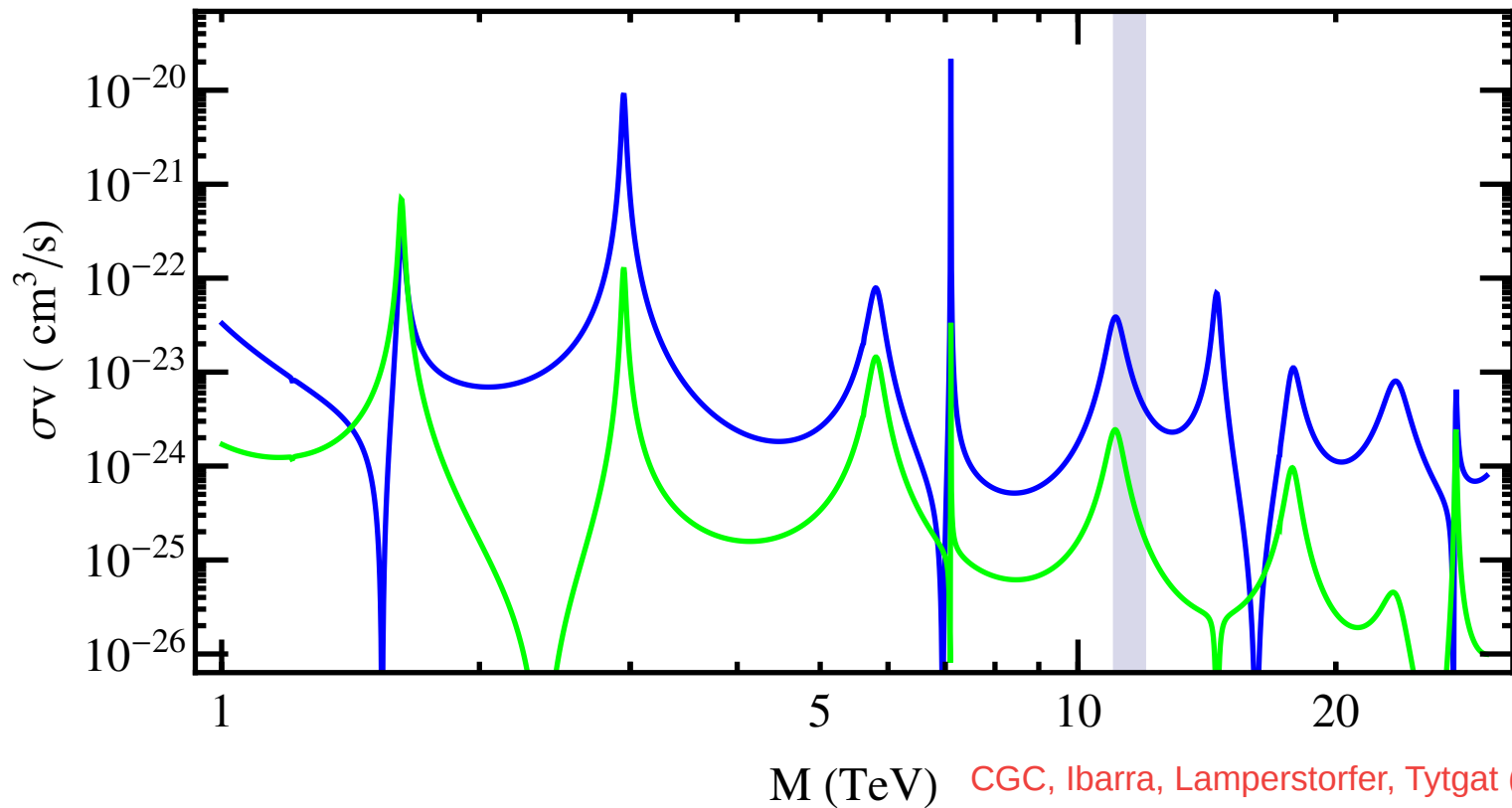


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Fermionic 5-plet

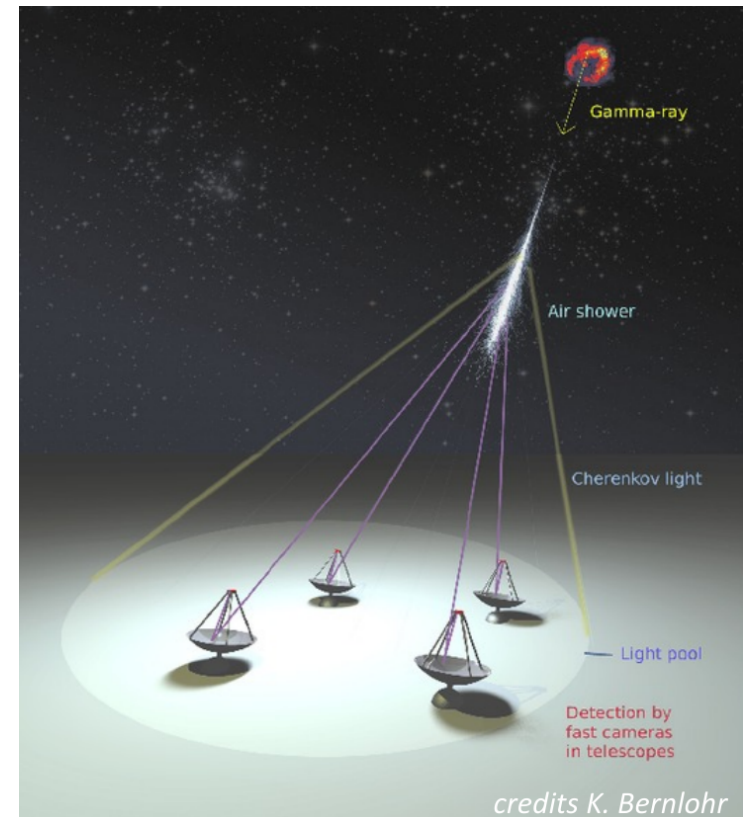


CGC, Ibarra, Lamperstorfer, Tytgat (2015)

# How do we search for this?

Indirect Searches with **gamma-ray telescopes**

H.E.S.S.

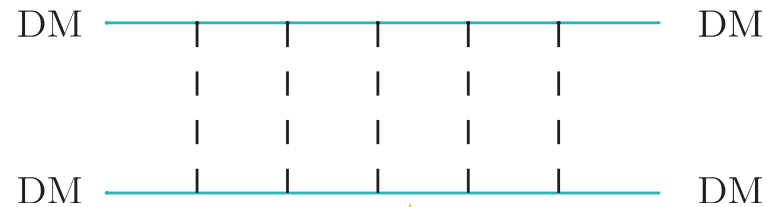


# This is rather common...

$$V(r) = \pm \alpha \frac{e^{-m_\phi r}}{r}$$

$$\alpha m_{\text{DM}} \gtrsim m_\phi$$

Any dark matter  
sector containing a  
light mediator

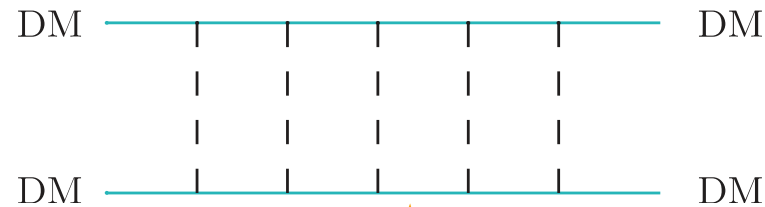


# This is rather common...

$$V(r) = \pm\alpha \frac{e^{-m_\phi r}}{r}$$

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Any dark matter sector containing a **light mediator**



For electroweak multiplets, the mediators are the electroweak bosons and the shallow bound states are formed for  $m_{\text{DM}} \gtrsim m_W/\alpha \sim \text{TeV}$ .

# Searches at the intensity frontier

PRL **116**, 151801 (2016)

PHYSICAL REVIEW LETTERS

15 APRIL 2016

Bound states

$$1.68m_\nu < \alpha_D m_\chi$$

**Probing the Dark Sector with Dark Matter Bound States**

Haipeng An,<sup>1</sup> Bertrand Echenard,<sup>2</sup> Maxim Pospelov,<sup>3,4</sup> and Yue Zhang<sup>1</sup>

Asymmetric dark matter interacting  
with a Stueckelberg field

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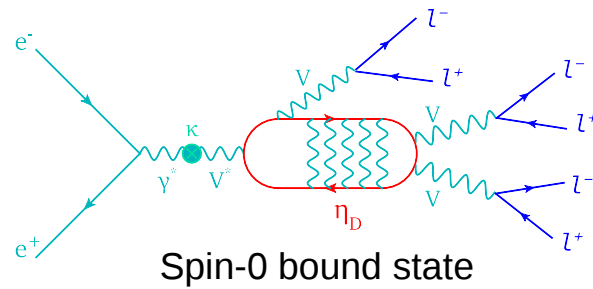
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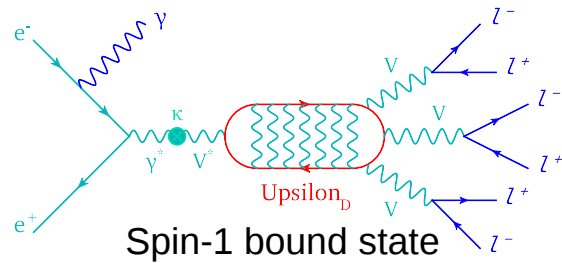
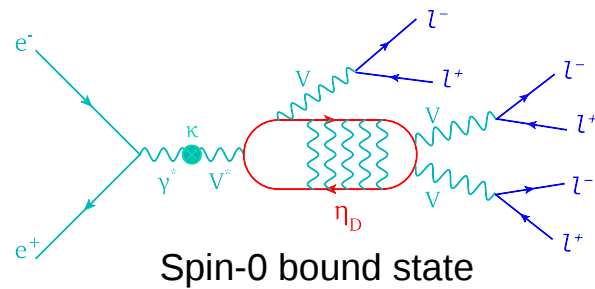
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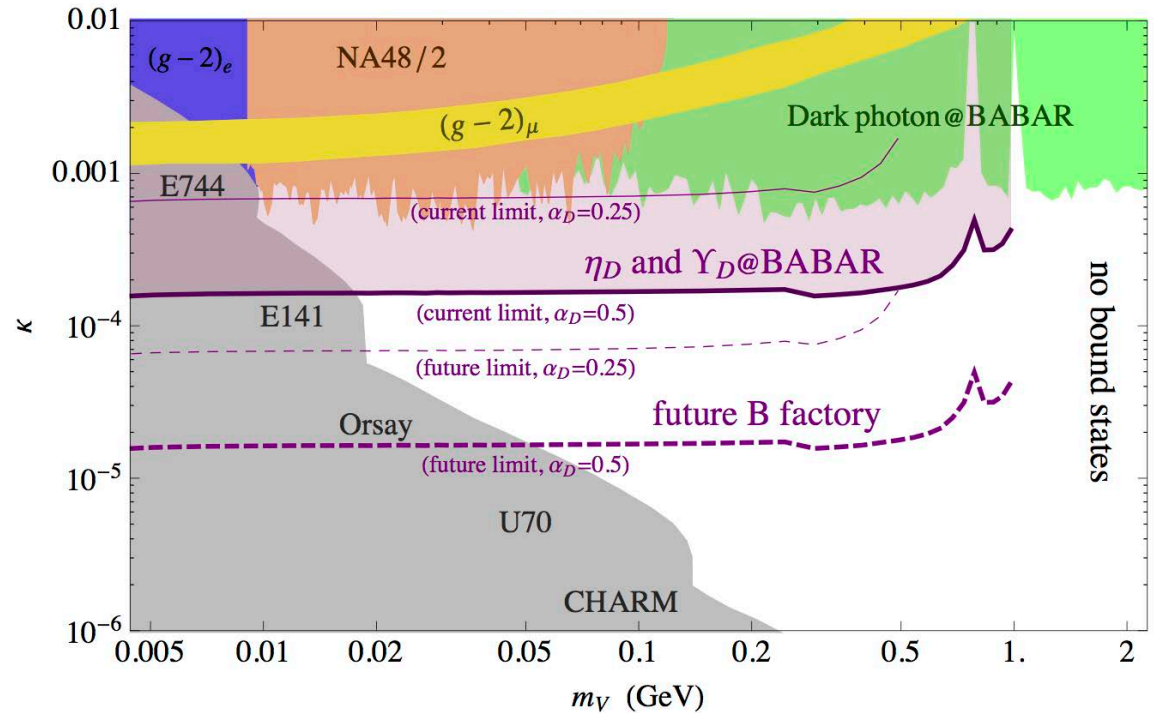
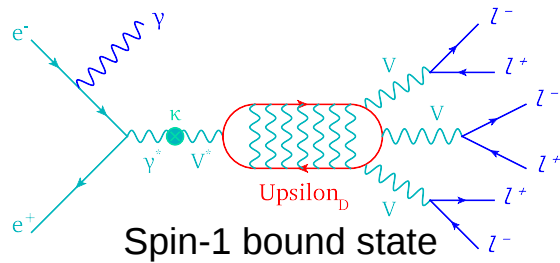
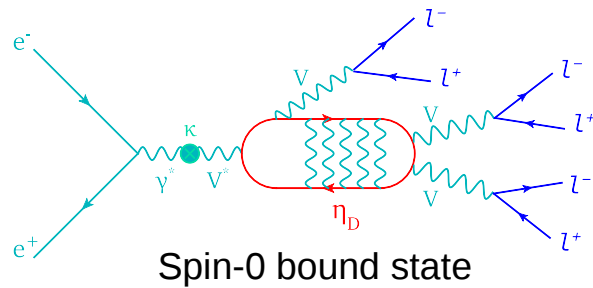
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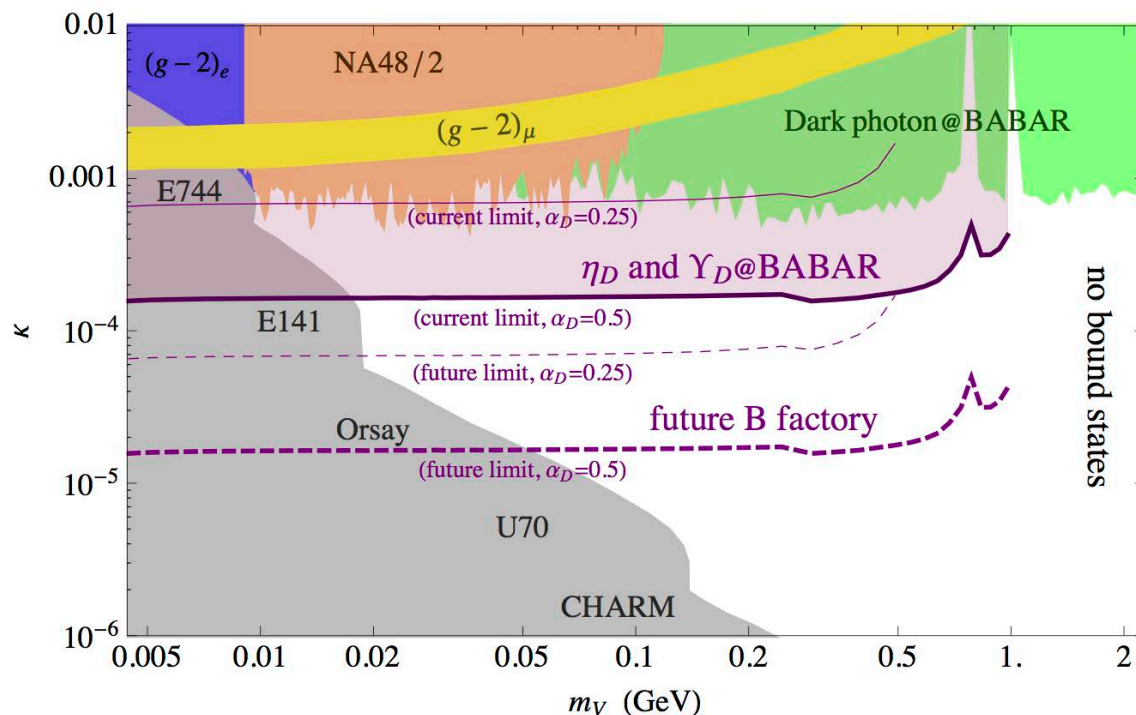
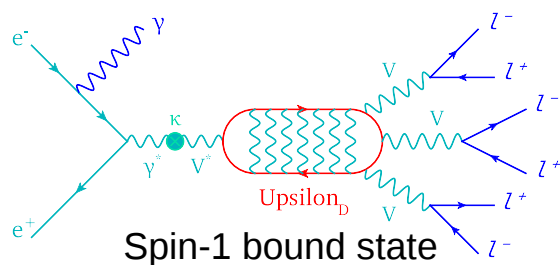
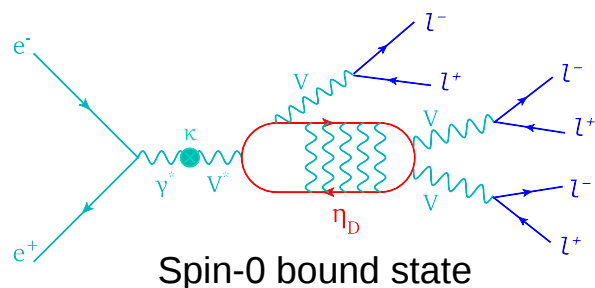
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## Asymmetric dark matter interacting with a Stueckelberg field

### Bound states

$$1.68m_V < \alpha_D m_\chi$$



### Some interesting aspects remain unexplored:

- Asymmetric vs. symmetric dark matter
- Realistic dark sector with the Higgs Mechanism giving mass to the light mediator
- Searches at Belle II

Duerr, CGC, Ferber, Schmidt-Hoberg (PRELIMINARY WORK)

## II. Dark matter as a bound state

Based on

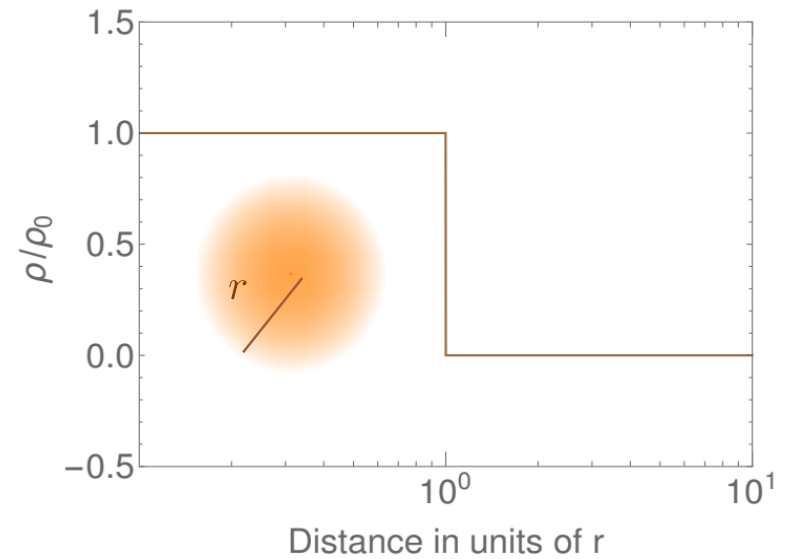
PHYSICAL REVIEW LETTERS **124**, 041101 (2020)

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### **Finite-Size Dark Matter and its Effect on Small-Scale Structure**

Xiaoyong Chu<sup>1,\*</sup> Camilo Garcia-Cely<sup>2,†</sup> and Hitoshi Murayama<sup>3,4,5,2,‡</sup>

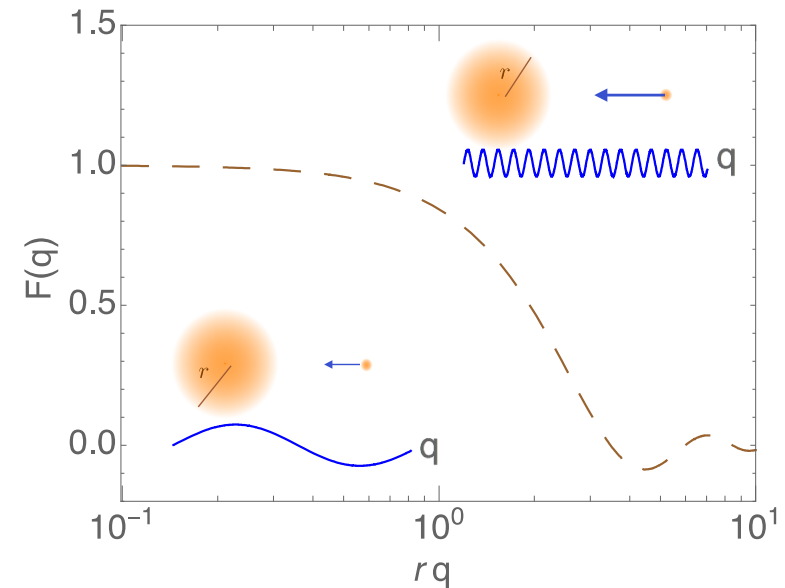
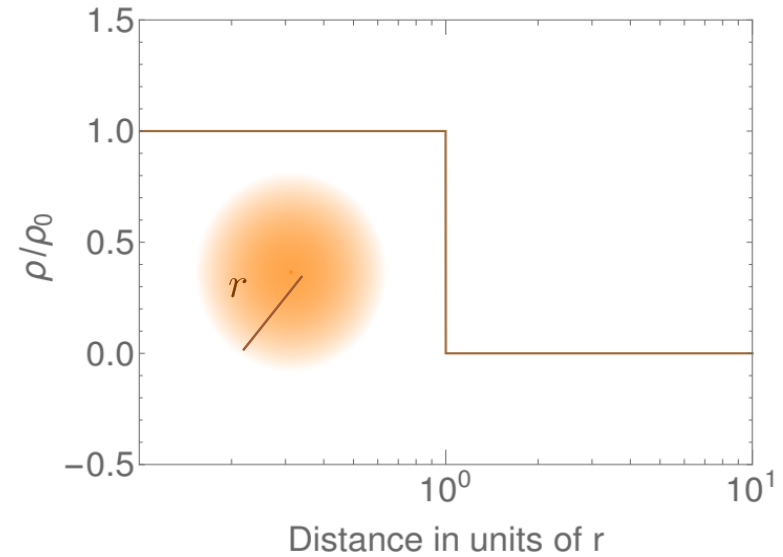
# How do we know something has a finite size?



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$$\frac{d\sigma}{d\Omega} = \frac{d\sigma}{d\Omega} \Big|_{\text{pointlike}} |F(q)|^2.$$

Fourier Transform  
of the density



# Realistic example

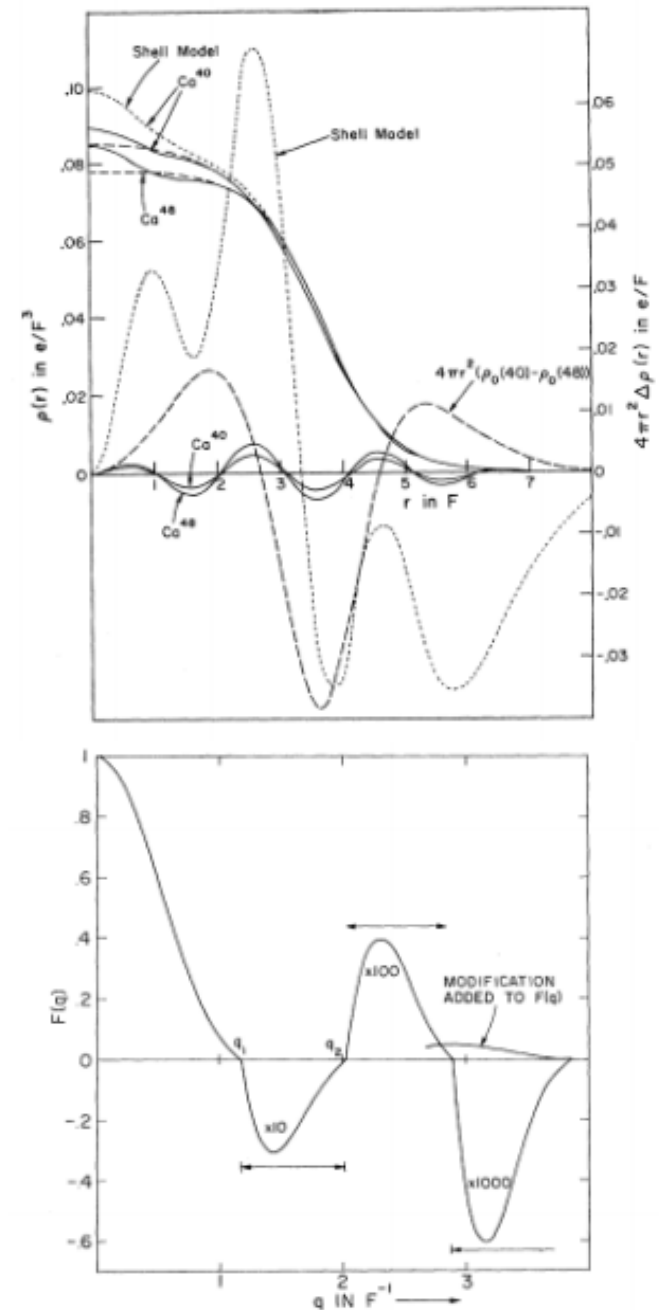
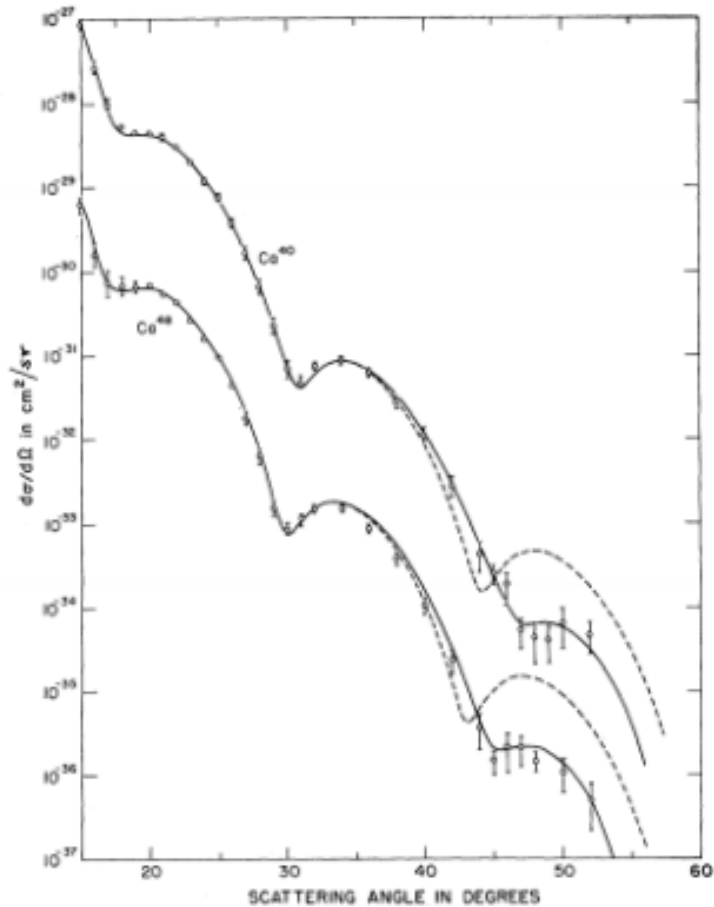
VOLUME 19, NUMBER 9

PHYSICAL REVIEW LETTERS

28 AUGUST 1967

## SCATTERING OF 750-MeV ELECTRONS BY CALCIUM ISOTOPES\*

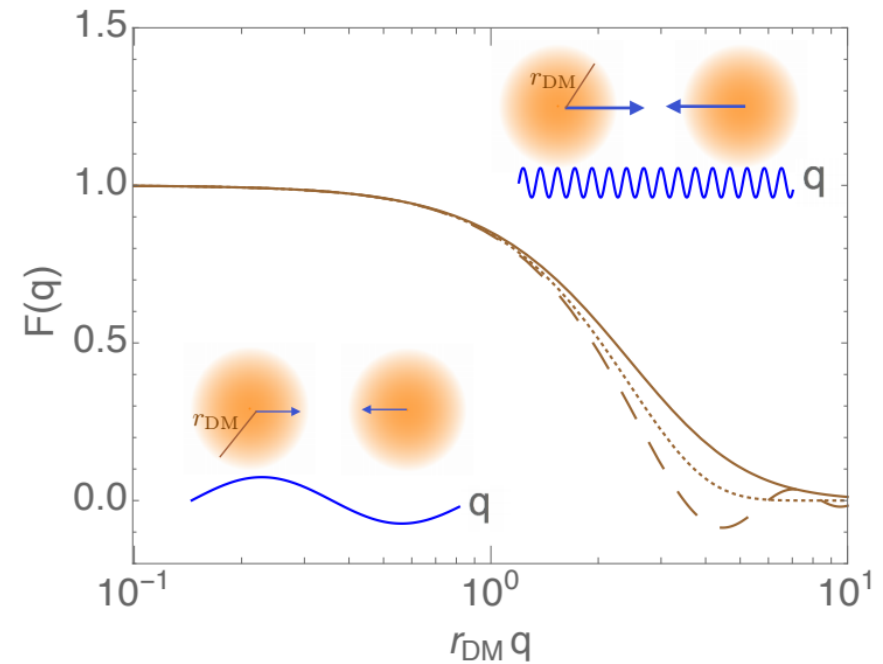
$$\frac{d\sigma}{d\Omega} = \frac{d\sigma}{d\Omega} \Big|_{\text{pointlike}} |F(q)|^2.$$



# Dark Matter with a finite size

Suppose that dark matter has a finite size that is larger than its Compton wavelength: Puffy DM

Chu, CGC, Murayama (2019)



# Dark Matter with a finite size

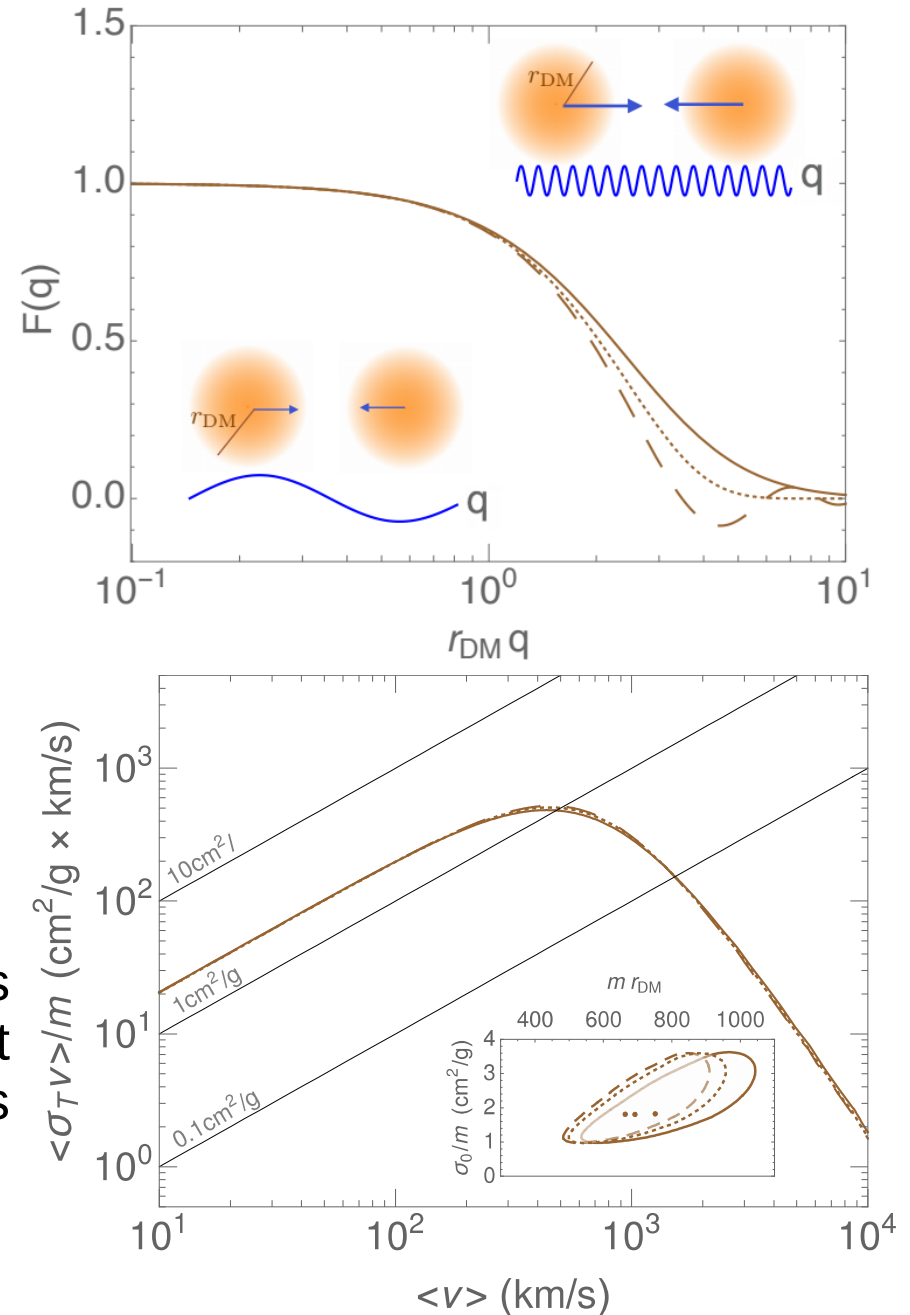
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Chu, CGC, Murayama (2019)

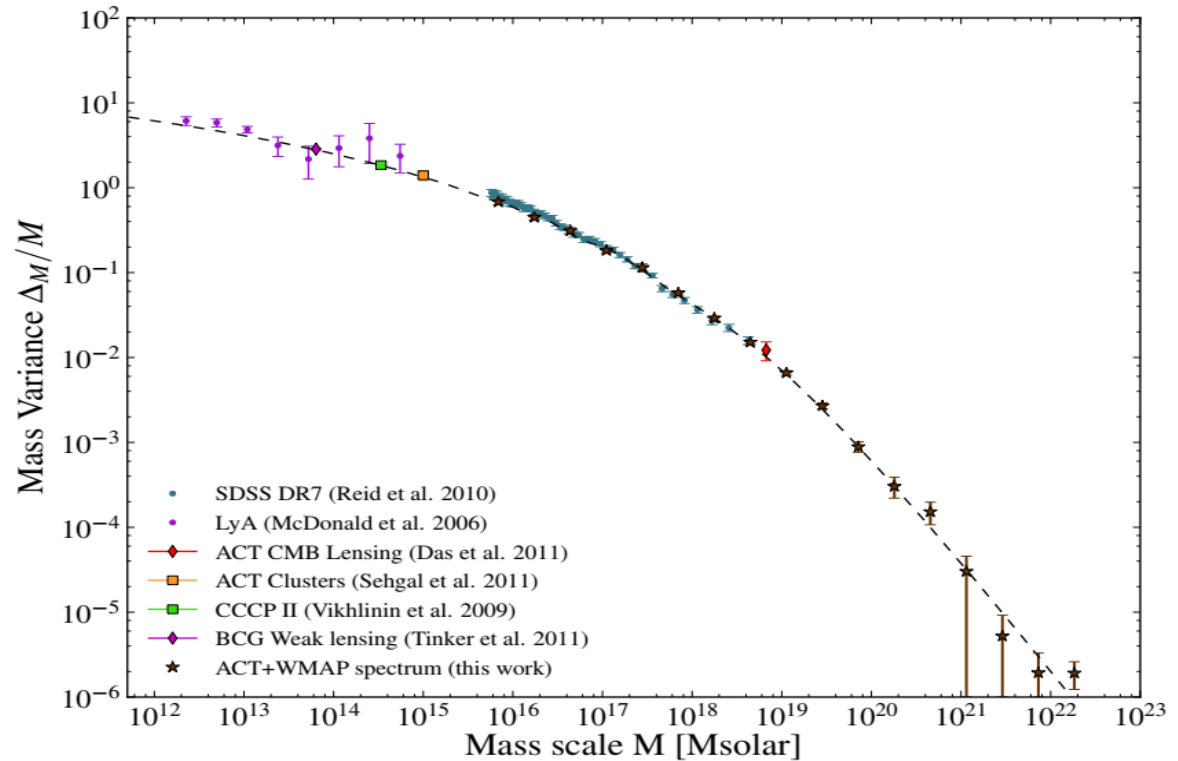
Shape	$\rho(r)$	$r_{\text{DM}}$	$F(q)$
tophat	$\frac{3}{4\pi r_0^3} \theta(r_0 - r)$	$2\sqrt{3}r_0$	$\frac{3(\sin(r_0 q) - r_0 q \cos(r_0 q))}{r_0^3 q^3}$
dipole	$\frac{e^{-r/r_0}}{8\pi r_0^3}$	$\sqrt{3/5}r_0$	$\frac{1}{(1+r_0^2 q^2)^2}$
Gaussian	$\frac{1}{8r_0^3 \pi^{3/2}} e^{-r^2/(4r_0^2)}$	$\sqrt{6}r_0$	$e^{-r_0^2 q^2}$

Table I: Form factors for different density distributions.

It is possible to obtain small cross section at cluster ( $v \sim 1000$  km/s) but small cross section in smaller objects (galaxies)



# Is this useful?



Hlozek et al. (2012)

- Core vs. cusp problem
- Diversity problem
- Too-big-to-fail problem
- Missing satellites

Heated debates!!!

Mass deficits at galactic scales

Remarkably successful  
at large scales

At low scales  
N-body simulations  
are needed

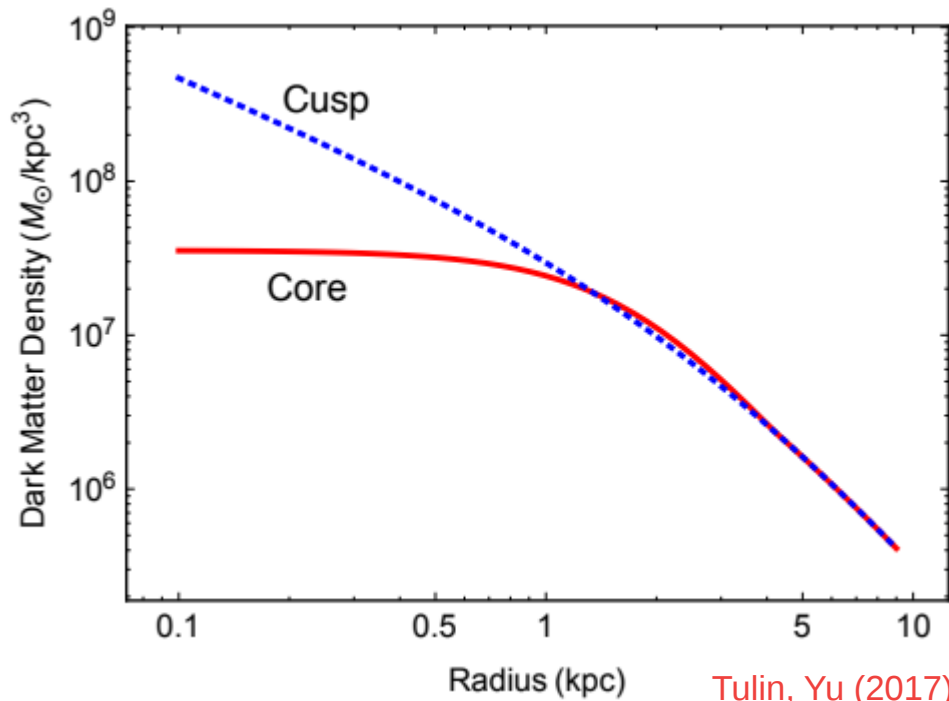


# Core vs. cusp problem

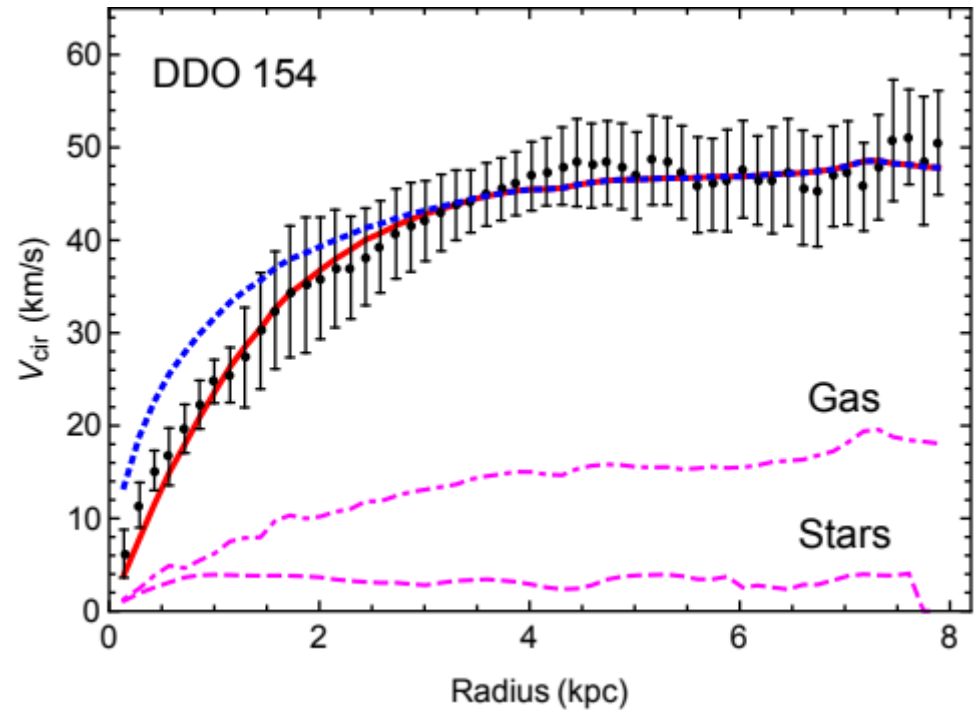
rotation curves again!

This is the seemingly mass deficit observed in objects such as dwarf galaxies when compared to the predictions of collisionless dark matter

Moore (1994)  
Flores et al. (1994)  
Naray et al. (2011)



Tulin, Yu (2017)



$$\rho_{\text{NFW}}(r) = \frac{\rho_s}{(r/r_s)(1 + r/r_s)^2},$$

J. F. Navarro, C. S. Frenk, and S. D. M. White (1997)

## Plausible explanations

- Baryonic effects (supernovae, star formation,...)
- Non-circular motions
- Systematic errors in the modelling of the internal dynamics of galaxies

## Dark matter solution?

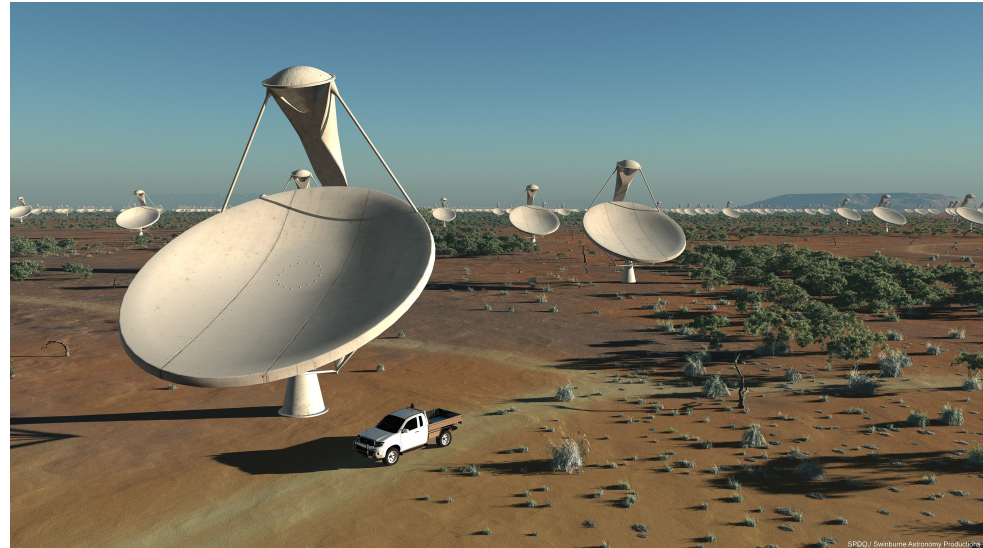
- postulate dark matter interactions that become relevant at small scales, without modifying the physics at large scales.

# The future is data rich. For example...

*The SKA will combine the signals received from thousands of small antennas spread over a distance of several thousand kilometres to simulate a single giant radio telescope*

→ *extremely high sensitivity and angular resolution*

It has the potential to observe hundreds of nearby spiral galaxies at resolutions below 100 pc, providing a large and detailed sample of rotation curves.



By SKA Project Development Office and Swinburne Astronomy Productions - Swinburne Astronomy Productions for SKA Project Development Office, CC BY-SA 3.0, <https://commons.wikimedia.org/w/index.php?curid=11314493>

# Debate

## Plausible explanations

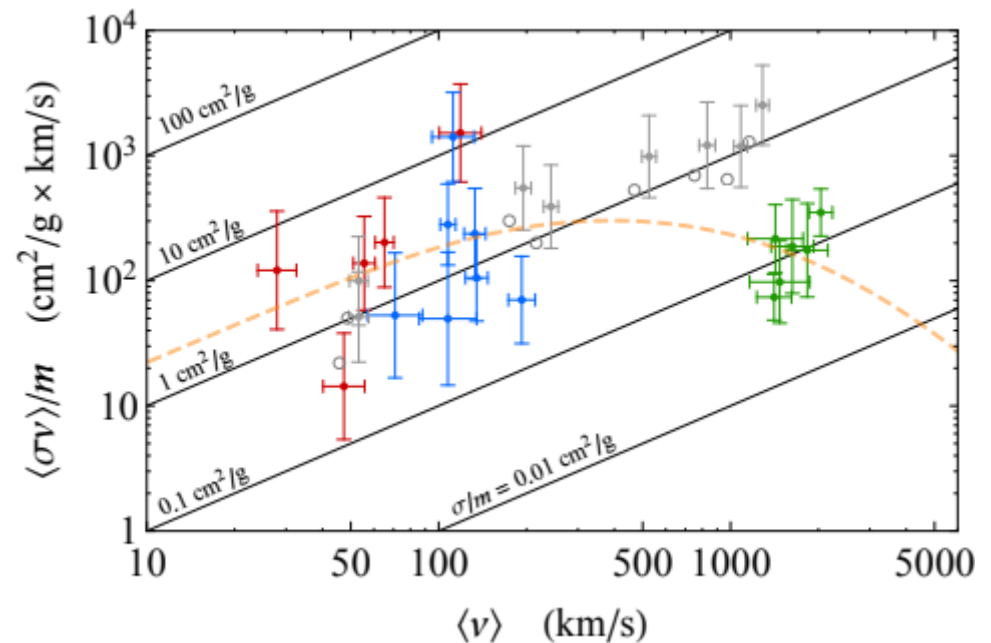
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## Dark matter halos as particle colliders

Kaplinghat, Tulin, Yu (2017)



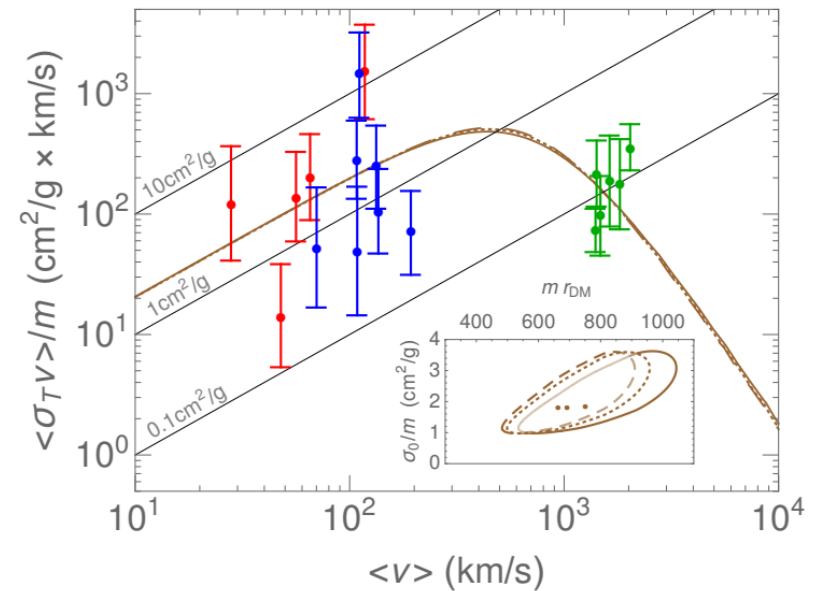
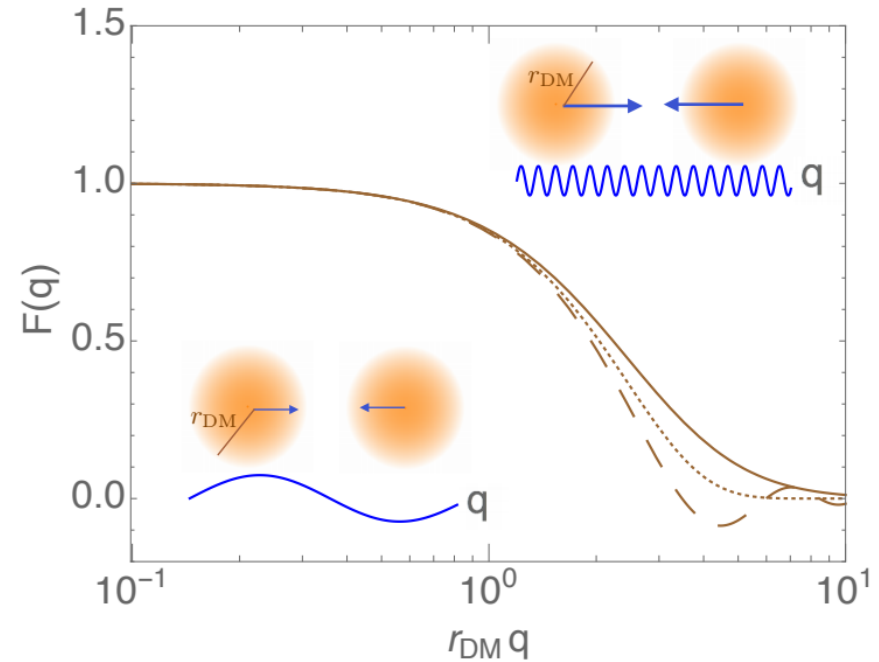
# Maybe dark matter is a bound state

Suppose that dark matter has a finite size that is larger than its Compton wavelength: Puffy DM

Chu, CGC, Murayama (2019)

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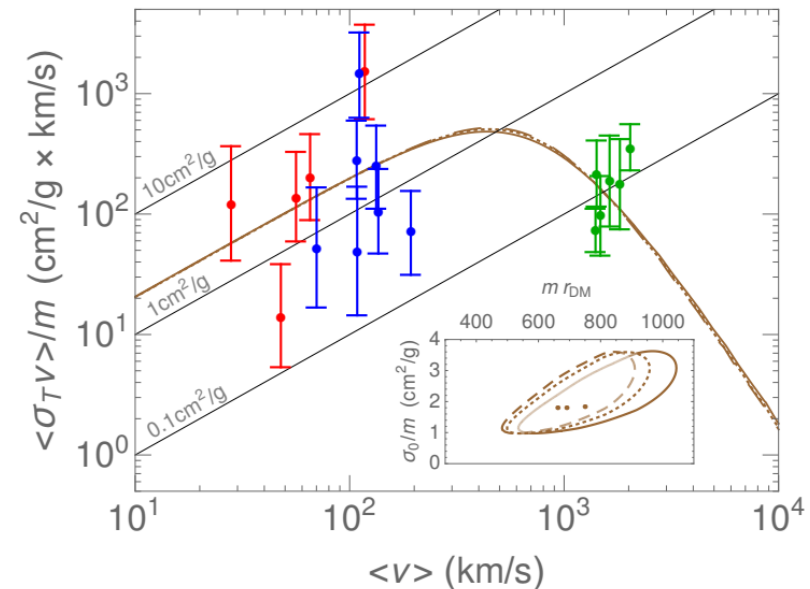
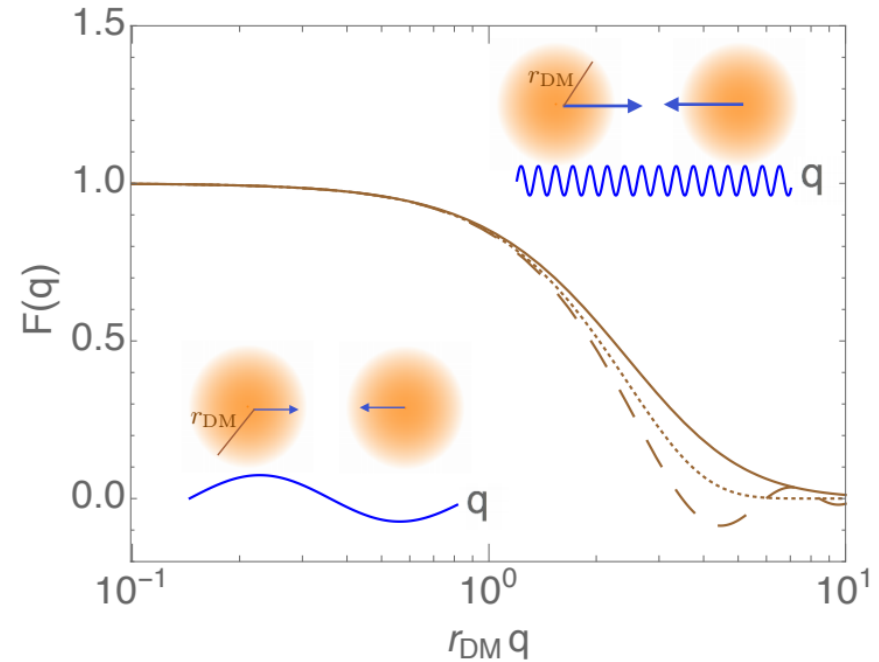
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Table I: Form factors for different density distributions.

The way the non-relativistic cross section varies with the velocity is largely independent of the dark matter internal structure when the range of the mediating force is short.



# A model of puffy dark matter

a QCD-like theory of dark matter

Particle	$SU(3)_D$	$U(1)_D$	Description
$c$	<b>3</b>	2/3	Dark charm quark
$d$	<b>3</b>	-1/3	Dark down quark
$\gamma_D$	<b>1</b>	0	Dark photon
$\eta$	<b>1</b>	0	Pseudoscalar meson $d\bar{d}$
$D^+$	<b>1</b>	1	Pseudoscalar meson $c\bar{d}$
$\rho$	<b>1</b>	0	Vector meson $d\bar{d}$
$\Sigma_c$	<b>1</b>	0	Dark baryon $cdd$
$\Delta^-$	<b>1</b>	-1	Dark baryon $ddd$
DM	<b>1</b>	0	Bound state of $A \Sigma_c$ baryons

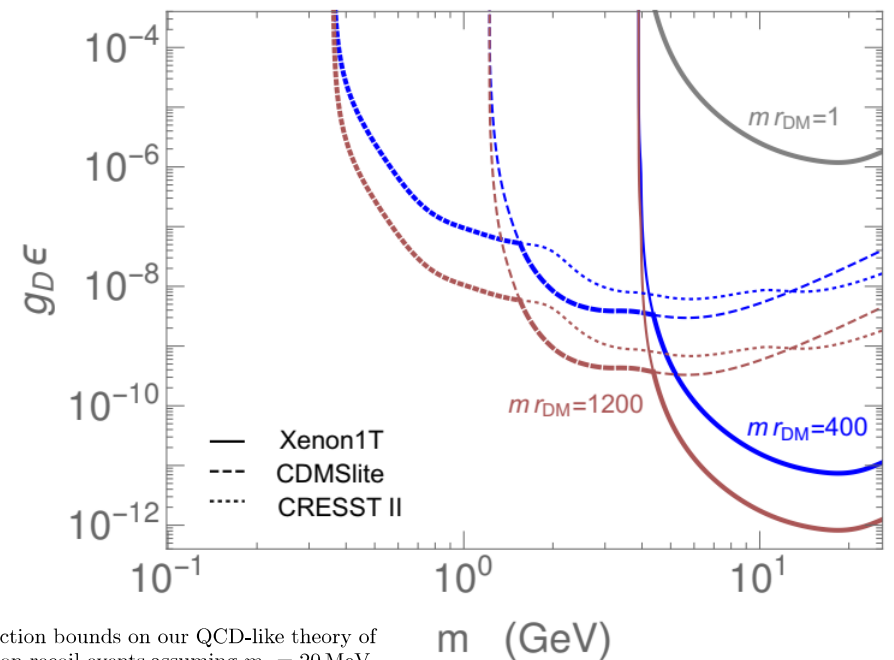
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$\rho$	<b>1</b>	0	Vector meson $d\bar{d}$
$\Sigma_c$	<b>1</b>	0	Dark baryon $cdd$
$\Delta^-$	<b>1</b>	-1	Dark baryon $ddd$
DM	<b>1</b>	0	Bound state of $A \Sigma_c$ baryons

Chu, CGC, Murayama (2019)

low-threshold direct detection experiments have the potential to probe Puffy Dark Matter.



Direct detection bounds on our QCD-like theory of Puffy DM from nucleon recoil events assuming  $m_{\gamma_D} = 20$  MeV. For a heavier dark photon, this bound scales with  $m_{\gamma_D}^2$ .



# Conclusions

- *Bound states are generally predicted in dark matter sectors with light mediators.*
- *They play an important role for indirect detection. Particularly for multi-TeV dark matter (searches with gamma-ray telescopes).*
- *They are also important for studying the collision of dark matter particles in dark matter halos.*

Thanks for your attention