

Neutron Star Constraints on Dark Matter

Raghuveer Garani

Université Libre de Bruxelles
and
INFN Firenze

Based on
2009.10728
in collaboration with A. Gupta and N. Raj

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Prelude: Stellar Frontiers for Dark Sectors

- Energy losses \implies significantly alter minimal cooling paradigm
- Energy transport \implies modifications to stellar models
- Capture of weakly interacting particles \implies neutrino fluxes/heating/black hole formation

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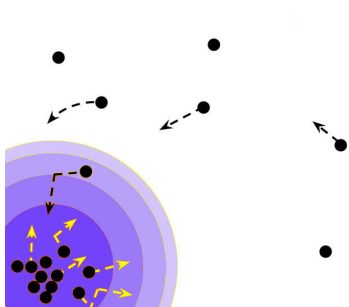
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Prelude: Stellar Frontiers for Heavy Dark Sectors

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- Dynamics governed by the equation

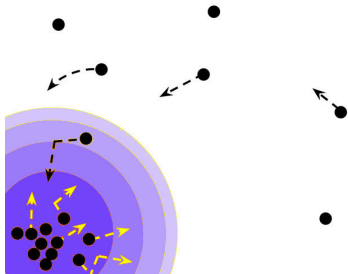
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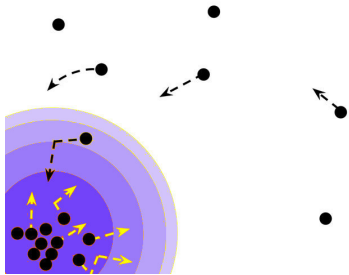
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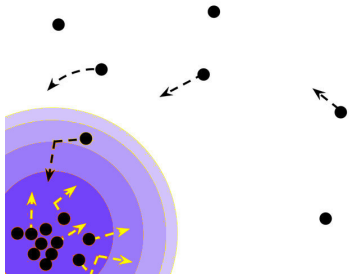
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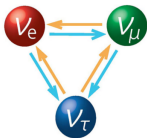
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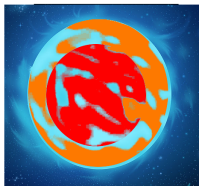
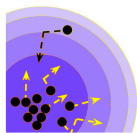
Neutrinos [Press and Spergel '85](#), [Griest et.al. '86](#), [Gould '87,++](#), [RG et.al.'17](#)



Black Hole formation

[Goldman et.al. '89](#), [Kouvaris et.al.'10 '11](#)

['12](#), [McDermott et.al. '12...](#), [RG et.al. '18](#)



Heating cold and old objects

[Kouvaris '07,](#)

['10](#), [Bertone et.al. '08,](#)

[McCullough et.al. '10](#), [Baryakhtar](#)

[et.al. '17](#), [Bell et.al. '18](#), [RG and](#)

[Heeck '19](#), [RG and Tinyakov '19](#)

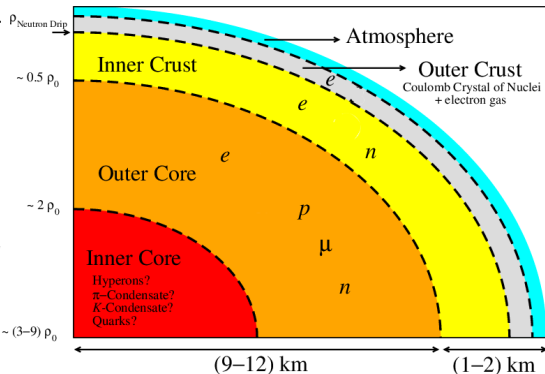
- Introduction
- Dark Matter Thermalization in Neutron Stars
- Neutron Star Heating Constraints on Dark Matter
- Conclusions & Outlook

Introduction: Neutron Stars

- Much about neutron star interiors unknown

- We consider a phenomenological NS profile. Exotic phases not considered. Brussels-Montreal energy density functionals which are fitted to APR

et.al. '13, Goriely et.al. '13



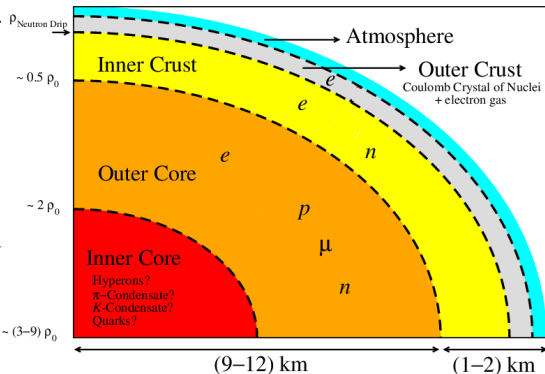
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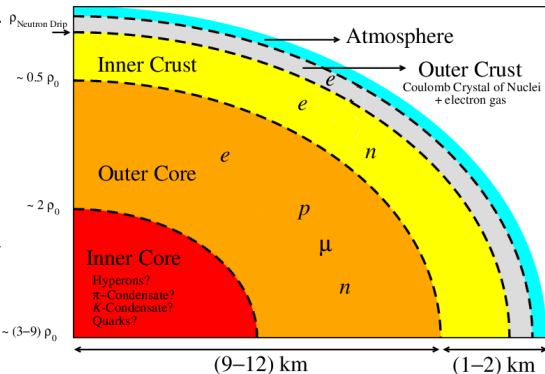
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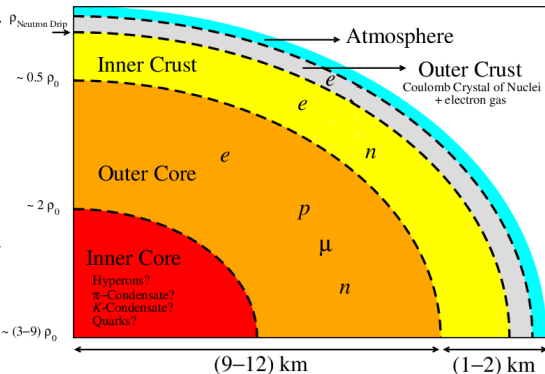
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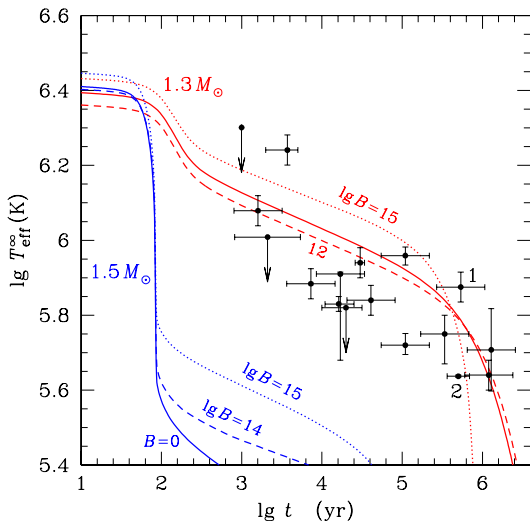
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Introduction: Neutron Star Temperature



Potekhin '11

Introduction: Dark Matter in Celestial Objects

- Sufficiently weak, $\sigma n_{\star} R_{\star} \sim 1$
- The maximal capture rate

$$C_{\star} = \pi R_{\star}^2 \left(1 + \frac{v_e^2}{v_{\infty}^2} \right) \left(\frac{\rho_{\text{DM}}}{m_{\text{DM}}} \right) v_{\infty}$$

	$\sigma_{\star} [\text{cm}^2]$	$\sim M_{\text{max}}/\text{Gyr}$
Sun	10^{-35}	$10^{-11} M_{\odot}$
Earth	10^{-33}	$10^{-10} M_{\text{E}}$
Moon	10^{-32}	$10^{-9} M_{\text{m}}$
White Dwarf	10^{-39}	$10^{-19} M_{\odot}$
Neutron Star	10^{-45}	$10^{-15} M_{\odot}$

NS Heating Constraints on Dark Matter: General Picture

Two ways to heat-up

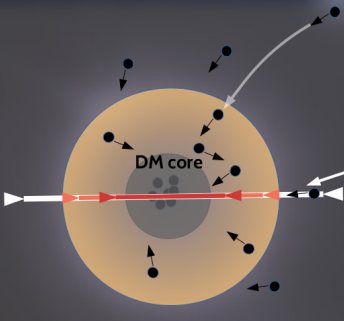
- Kinetic Heating: In-falling DM heats up the neutron star. Potentially observable by James Webb Space Telescope, the Thirty Meter Telescope, or the European Extremely Large Telescope [Baryakhtar et.al. '17](#), [Raj et.al. '17](#), [Bell et.al. '18](#)

$$T_{\text{kin}}^{\text{max}} \simeq 1700 \text{ K} \left(\frac{C}{C_{\star}} \right)^{1/4} \left(\frac{\rho_{\text{DM}}}{0.4 \text{ GeV/cm}^3} \right)^{1/4} .$$

- Annihilations: If DM capture and annihilation are in equilibrium [Kouvaris '07](#), [Kouvaris et.al. '10](#)

$$T_{\text{ann}}^{\text{max}} \simeq 2480 \text{ K} [\rho_{\text{DM}} / (0.4 \text{ GeV/cm}^3)]^{0.45}$$

Dark Matter Thermalization in NS



Thermalisation time of DM

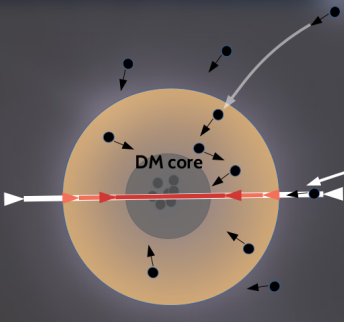
Through successive collisions, DM losses energy and accumulates in the star center.

The orbits are shrinking and reach :

$$r_{th}^{NS} = 4.3 \text{ m} \left(\frac{T_{core}}{10^5 \text{ K}} \right)^{1/2} \left(\frac{1 \text{ GeV}}{m_\chi} \right)^{1/2}$$

- Need to ensure thermalization to test maximal heating from DM annihilations in NS

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Thermalization: phase space [RG. A. Gupta and N. Raj]

- Interaction rate in Fermi-degenerate medium is given by Fermi's golden rule

$$d\Gamma = 2 \frac{d^3 k'}{(2\pi)^3} S(q_0, q) ,$$

$$S(q_0, q) = \int \frac{d^3 p'}{(2\pi)^3 2E_{p'} 2E_{k'}} \int \frac{d^3 p}{(2\pi)^3 2E_p 2E_k} \times \\ (2\pi)^4 \delta^4(k + p - k' - p') |\mathcal{M}|^2 f(E_p) (1 - f(E_{p'})) ,$$

- Thermalization time is given by

$$\tau_{\text{therm}} = - \int_{E_0}^{E_f} \frac{dE_i}{\int d\Gamma \times (E_i - E_f)} .$$

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Thermalization: response function

- For non-relativistic neutrons

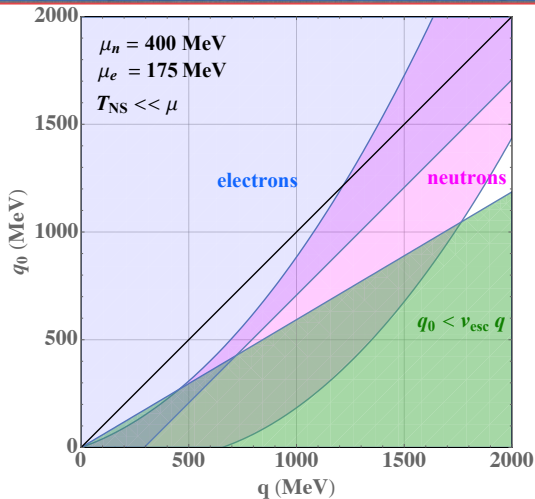
$$S^{\text{non-rel}}(q_0, q) = \frac{|\mathcal{M}|^2}{16\pi m_\chi^2} \frac{q_0}{q} \Theta\left(\mu - \frac{1}{4} \frac{(q_0 - q^2/2m_T)^2}{q^2/2m_T}\right),$$

- For relativistic electrons inside NS

$$S^{\text{rel}}(q_0, q) = \frac{|\mathcal{M}|^2}{16\pi m_\chi^2} \frac{q_0}{q} \Theta(2\mu + q_0 - q).$$

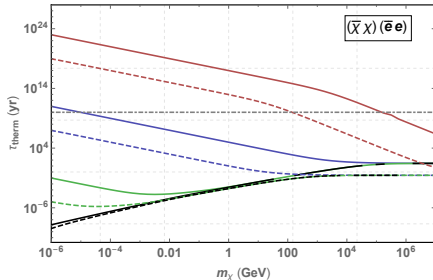
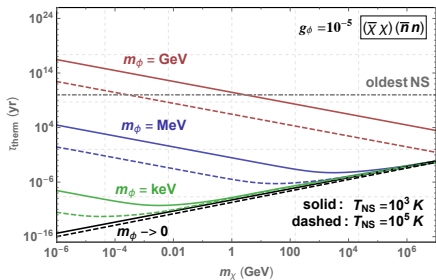
RG, A. Gupta and N. Raj

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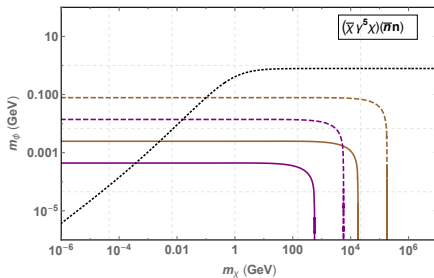
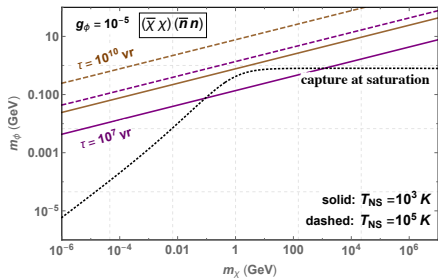


RG, A. Gupta and N. Raj

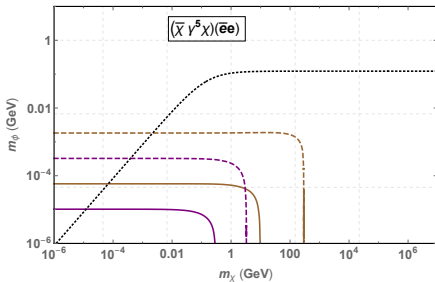
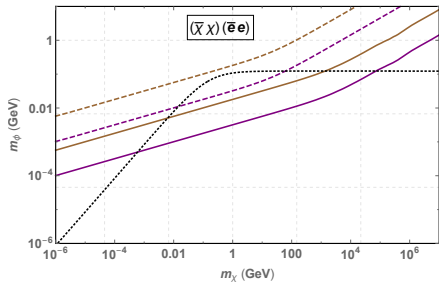
Example application: scalar operators



Parameter space for DM-neutron interactions



Parameter space for DM-electron interactions



Comments on the annihilation cross section

- After DM thermalizes with NS, does capture and annihilation equilibrate? Recall: annihilation heating heats NS up to 2400 K.
- The equilibration time is given by $\tau_{\text{eq}} = (V_{\text{th}}/C\langle\sigma v\rangle_{\text{ann}})^{1/2}$.
- Parameterize $\langle\sigma v\rangle_{\text{ann}} = a + b v^2$. For s-wave annihilation

$$a > 7.5 \times 10^{-54} \text{ cm}^3/\text{s} \left(\frac{\text{Gyr}}{\tau_{\text{NS}}} \right)^2 \left(\frac{C_{\text{sat}}}{C} \right) \left(\frac{\text{GeV}}{m_\chi} \frac{T_{\text{NS}}}{10^3 \text{ K}} \right)^{3/2}$$

and for p-wave

$$b > 2.9 \times 10^{-44} \text{ cm}^3/\text{s} \left(\frac{\text{Gyr}}{\tau_{\text{NS}}} \right)^2 \left(\frac{C_{\text{sat}}}{C} \right) \left(\frac{\text{GeV}}{m_\chi} \frac{T_{\text{NS}}}{10^3 \text{ K}} \right)^{1/2}$$

Conclusions and Outlook

- Neutron stars are unique laboratories to probe particle nature of dark matter.
- Considered realistic Neutron Star profile and developed formalism for DM scattering in Fermi-degenerate medium for arbitrary degeneracy.
- Heating of old Neutron stars can constrain several DM models. Kinetic heating can heat old NS up to 1700 K and heating from annihilation can lead to NS temperature of 2400 K. Decisively testable by future infrared telescopes such as JWST.
- For signals from annihilation heating: the requirement to thermalize is a strong criterion! DM-nucleon (electron) momentum dependent operators DO NOT thermalize with NS efficiently \implies signals from kinetic heating the only way.

Thank You !