

# Constraining gravitational parity violation

*Mostly based on:  
arXiv:2004.01253*

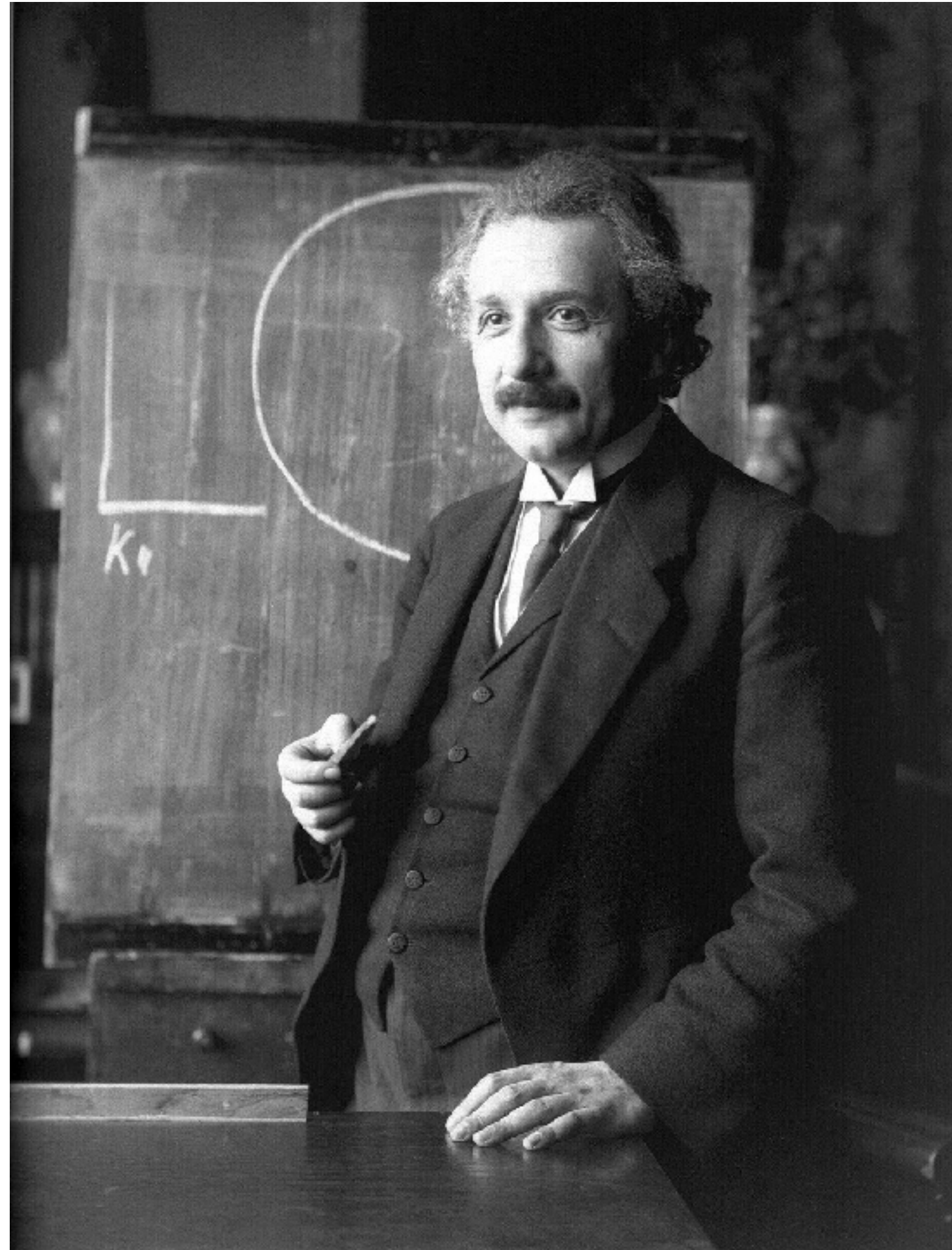
**Alejandro *Cárdenas-Avenida***

*Programa de Matemática, Konrad Lorenz Fundación Universitaria  
Illinois Center for Advanced Studies of the Universe, University of Illinois at Urbana-Champaign*

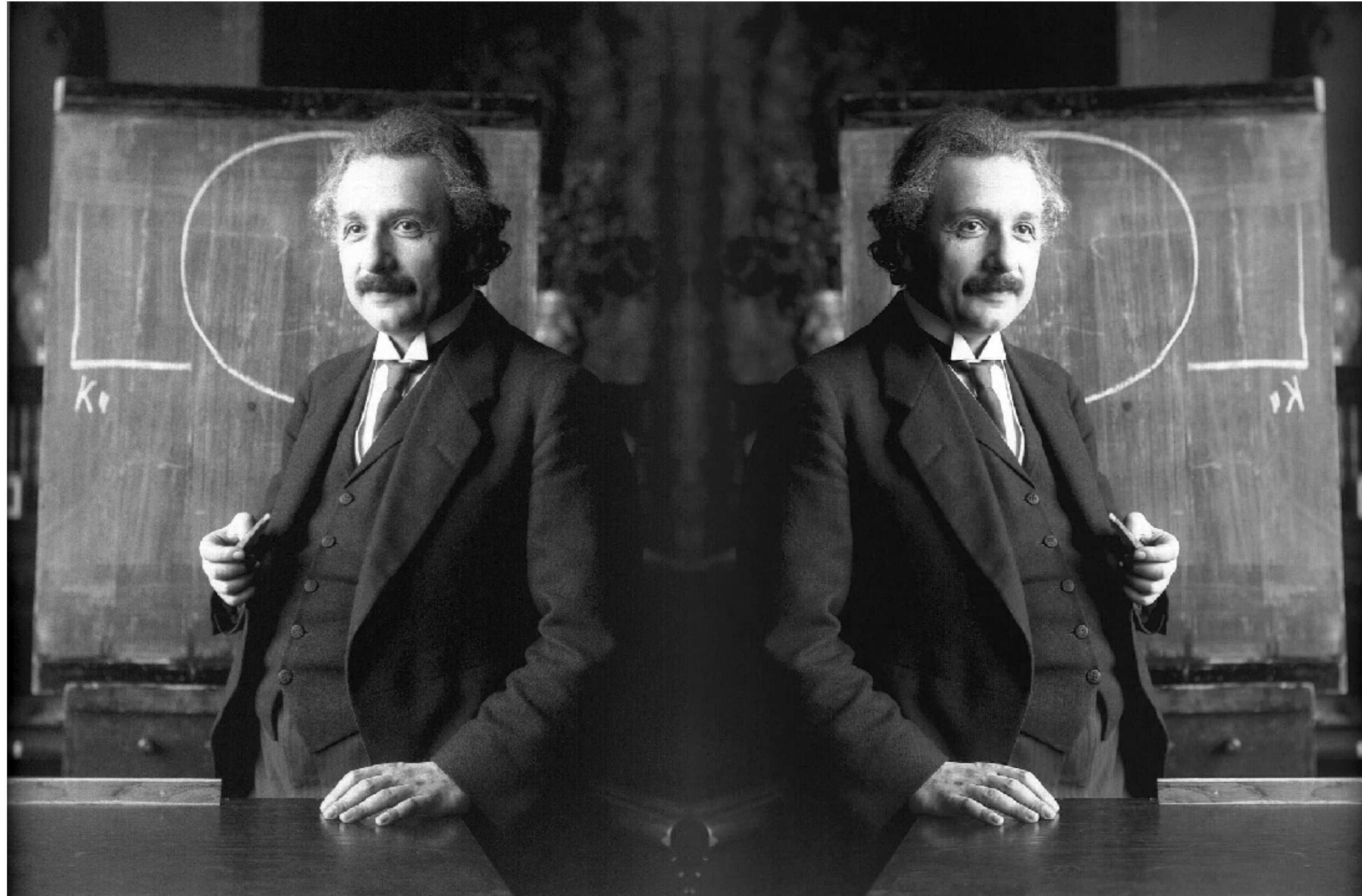
in collaboration with

**Hector *Silva*, Miguel *Holgado* and Nicolás *Yunes***

# Was Einstein right or left handed?



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Jackiw & Pi (2003)

## Dynamical Chern-Simons theory

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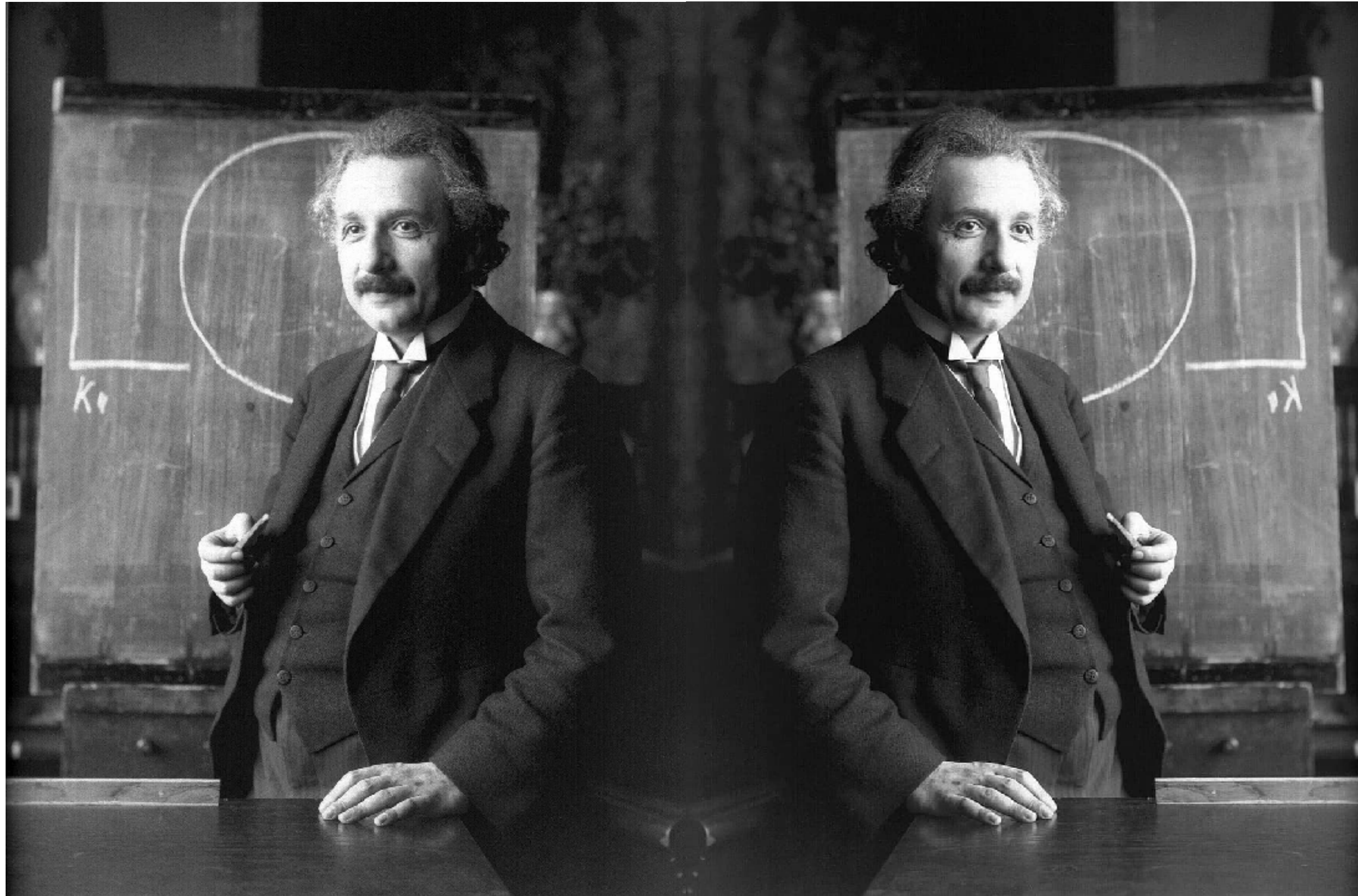
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## Dynamical Chern-Simons theory

- Theoretical novelty

Ashtekar, Balachandran & Jo (1989)  
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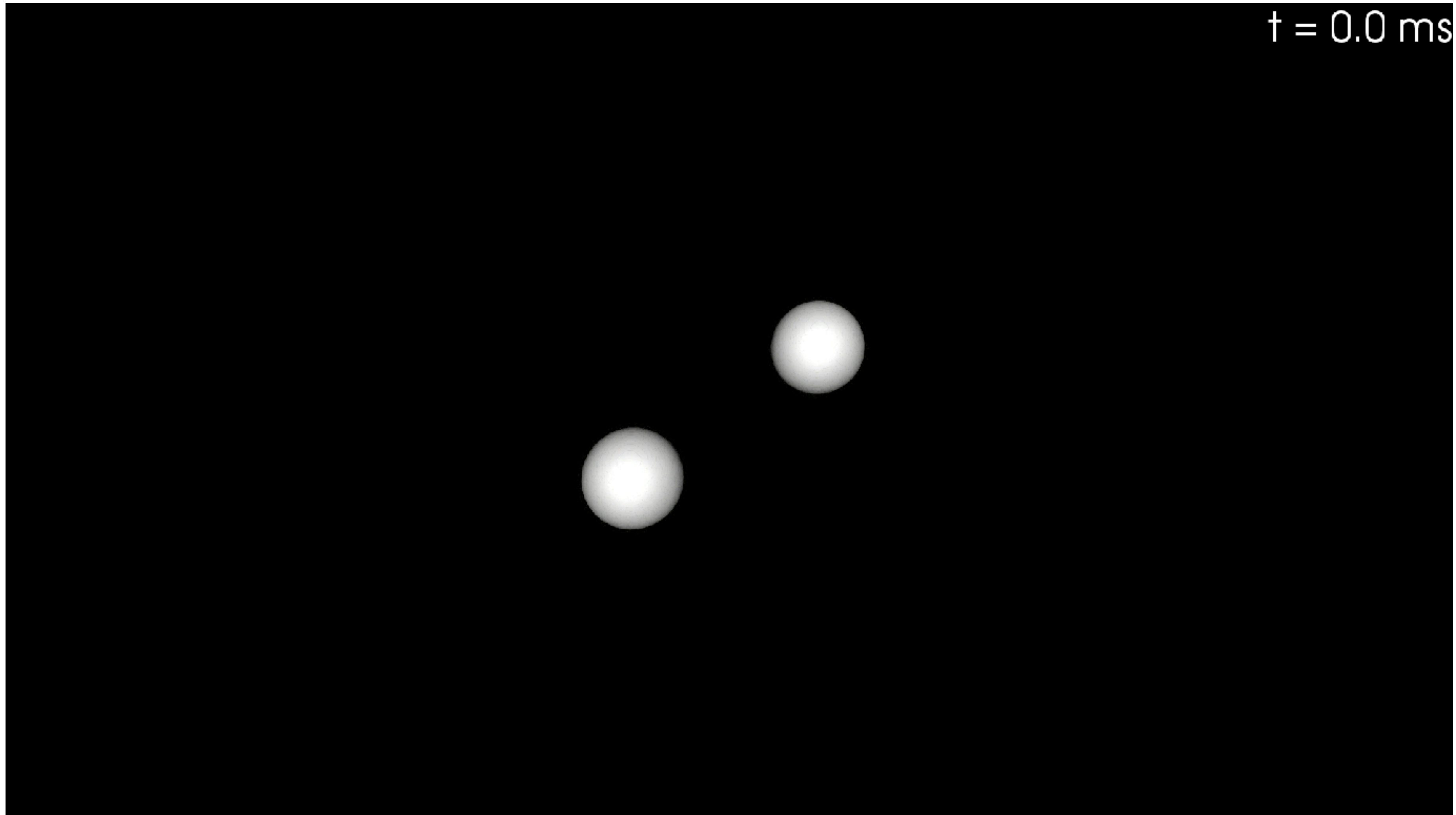
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# LIGO-VIRGO Collaboration (LVC): The last dance (GW170817)

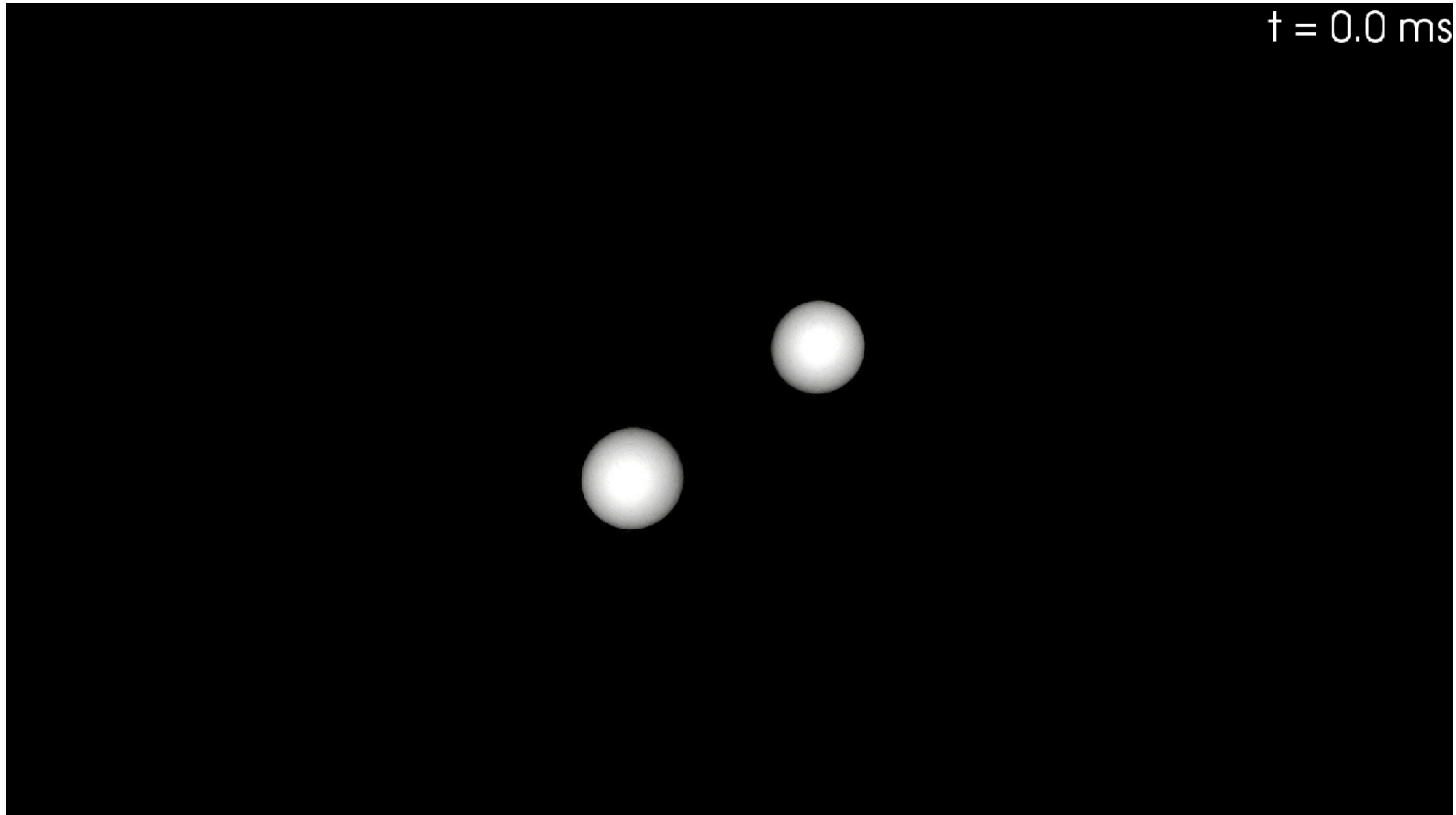
The LIGO Scientific Collaboration and The Virgo Collaboration (2017)



Credit: W. Kastaun/T. Kawamura/B. Giacomazzo/R. Ciolfi/A. Endrizzi

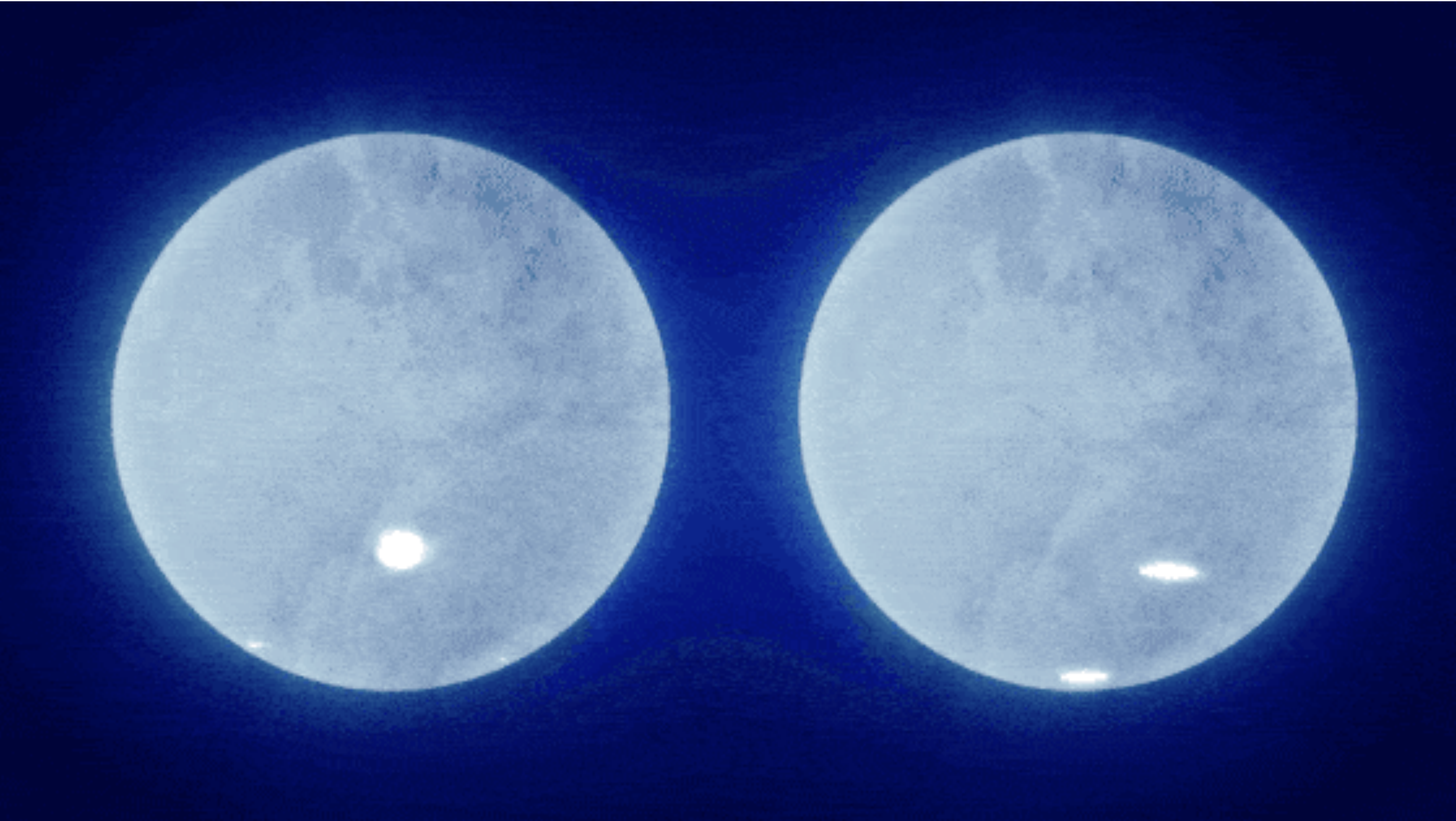
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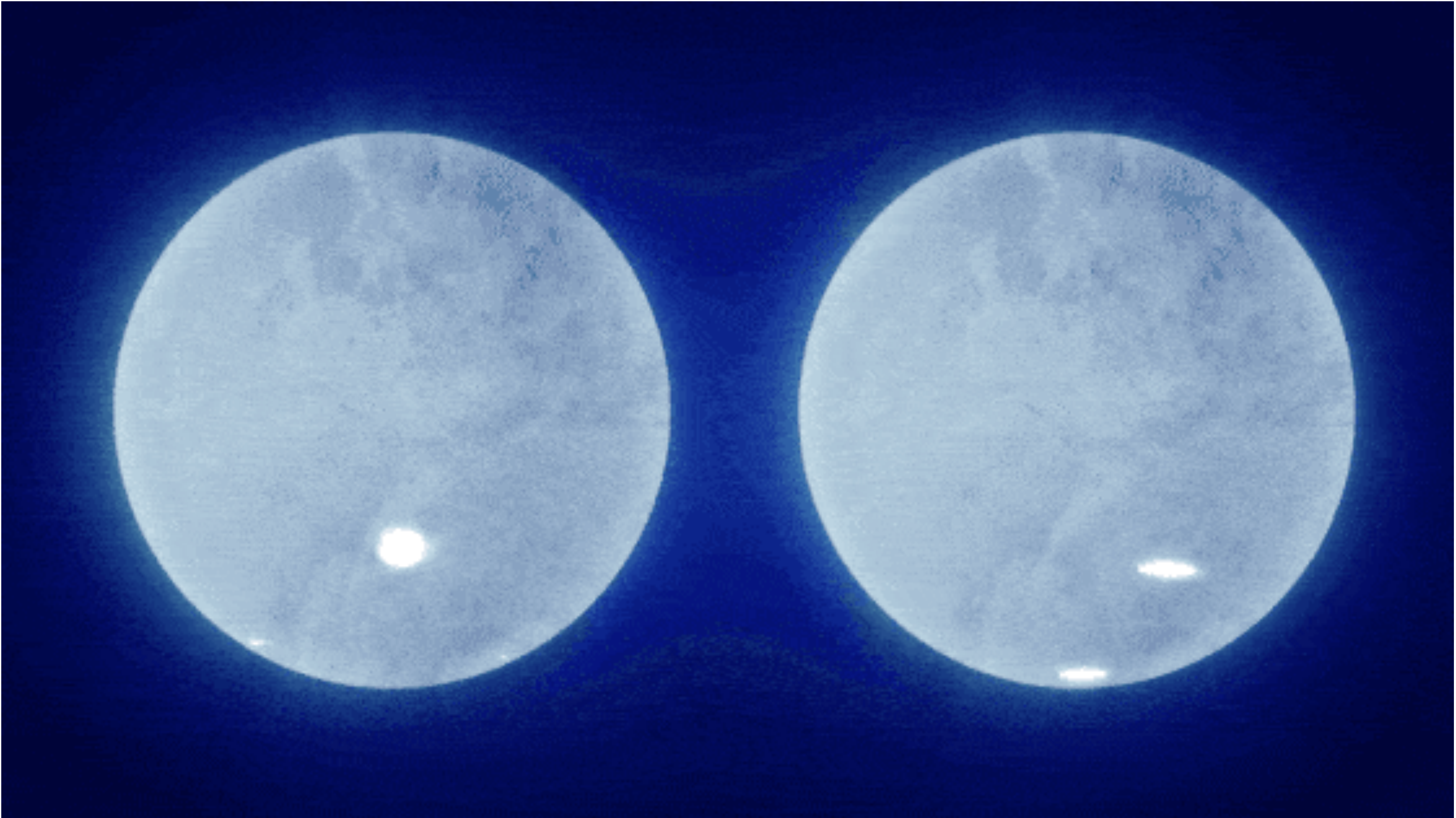
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# NICER: PSR J0030+0451



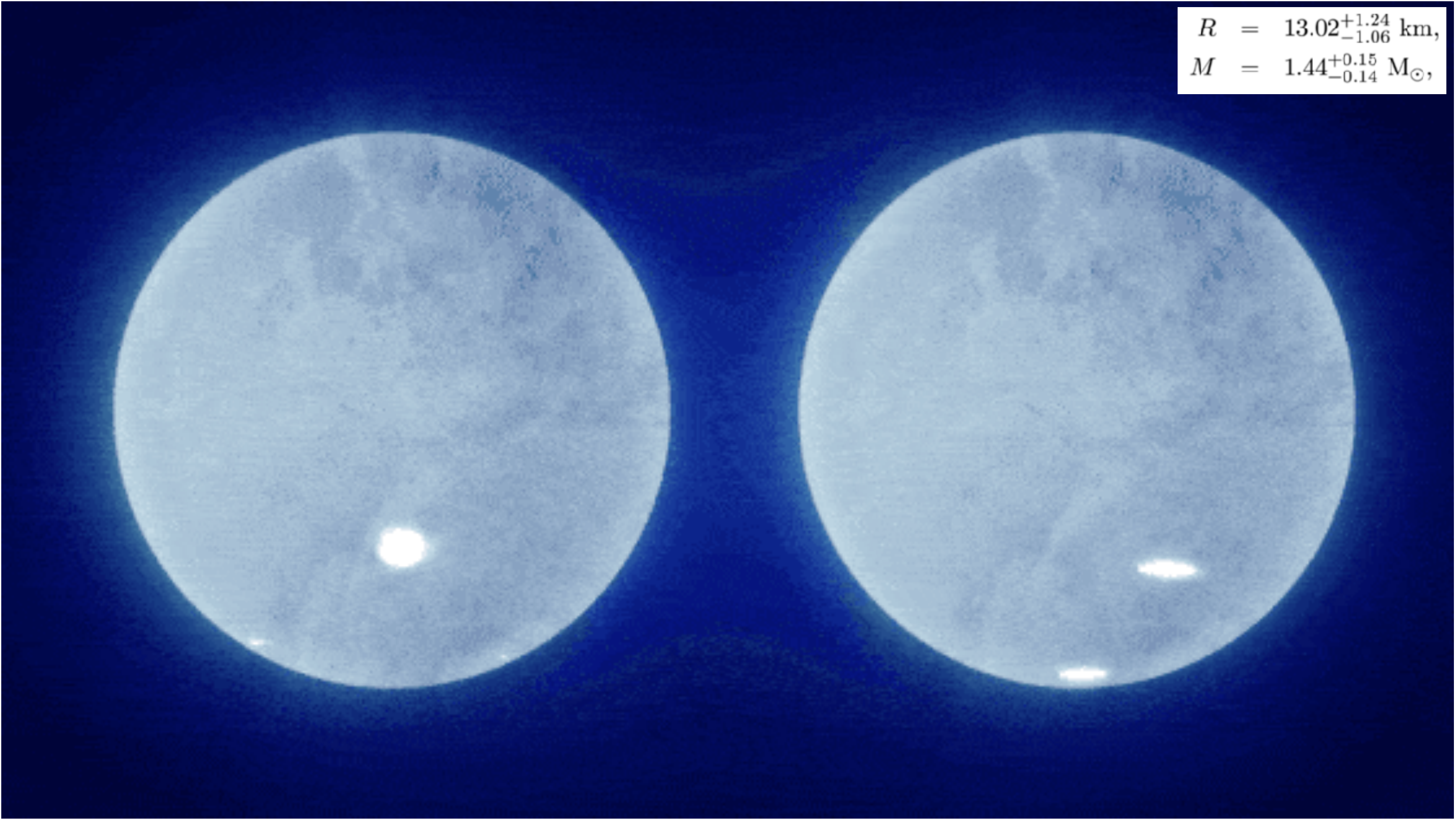
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Riley et al. (2019); Miller et. al., (2019)

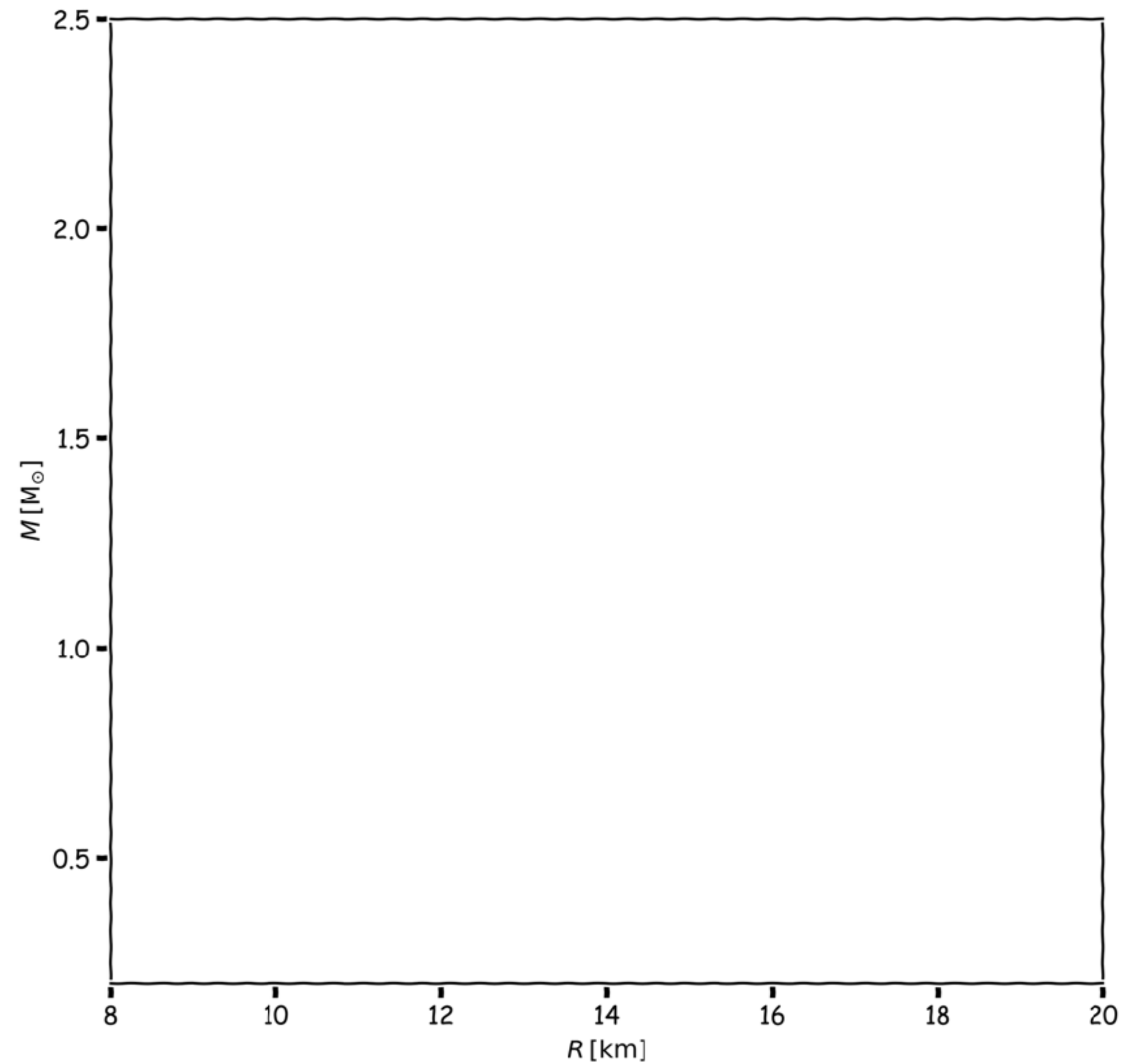


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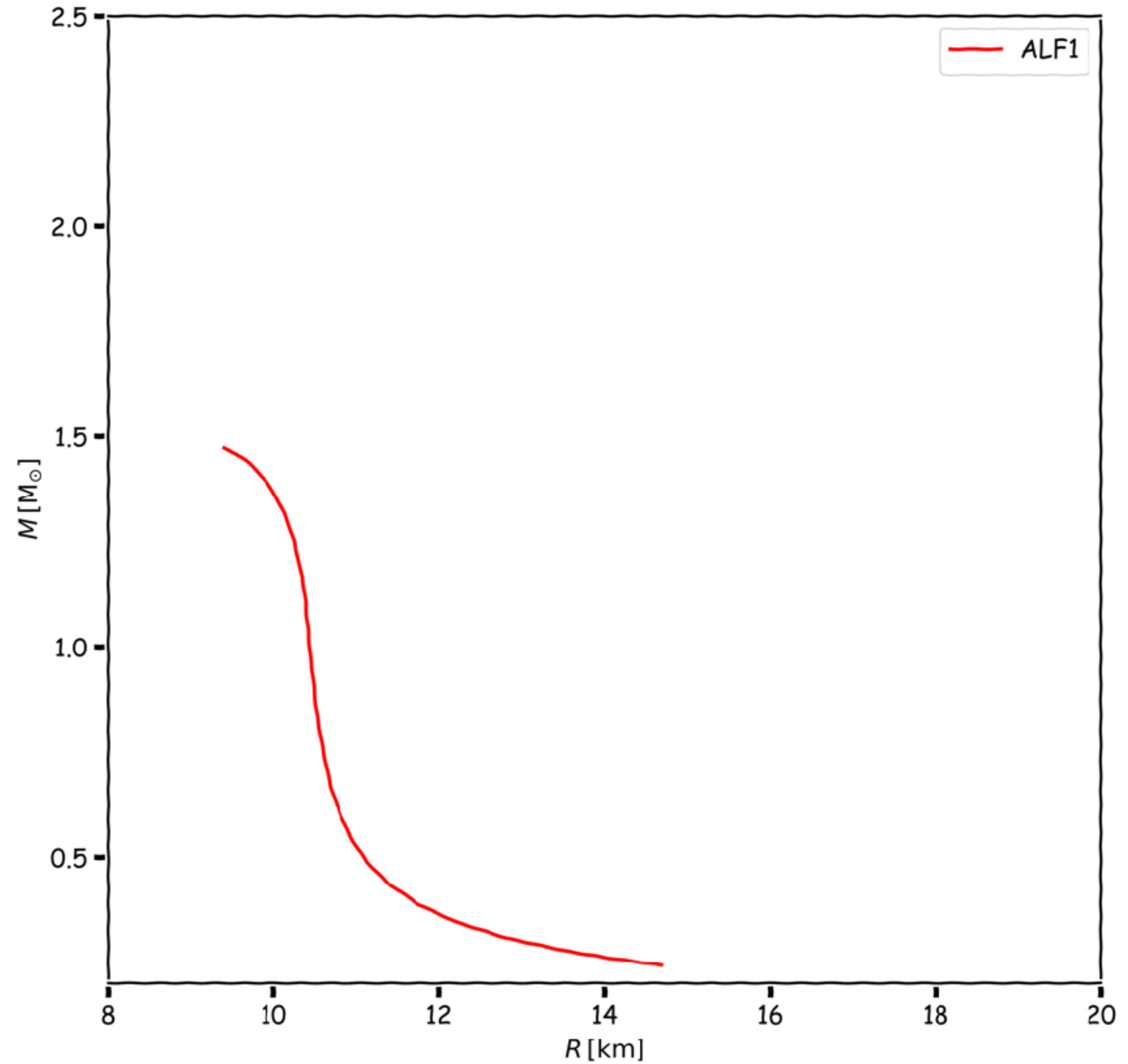
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# What is the equation of state of a neutron star?

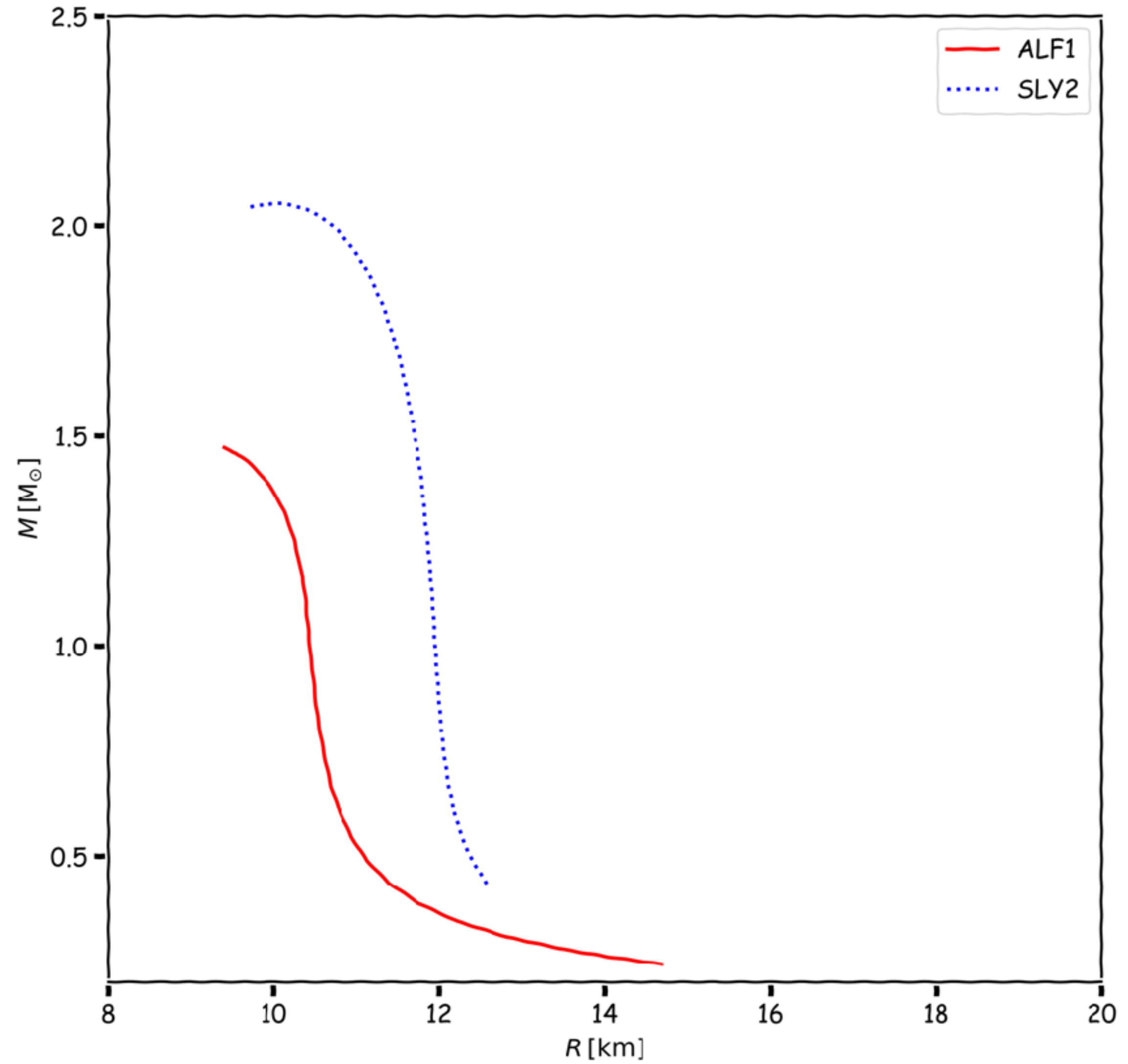


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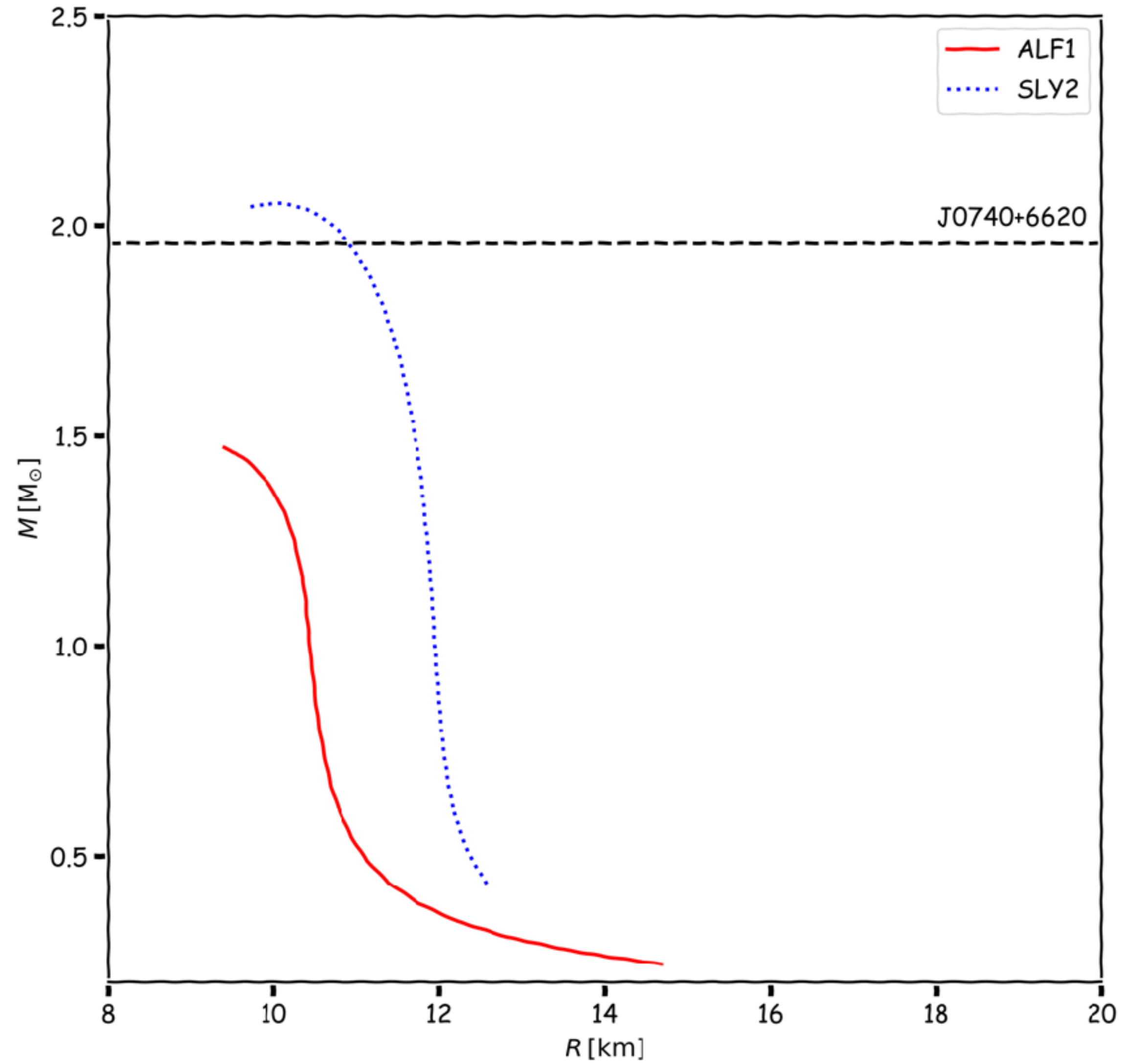




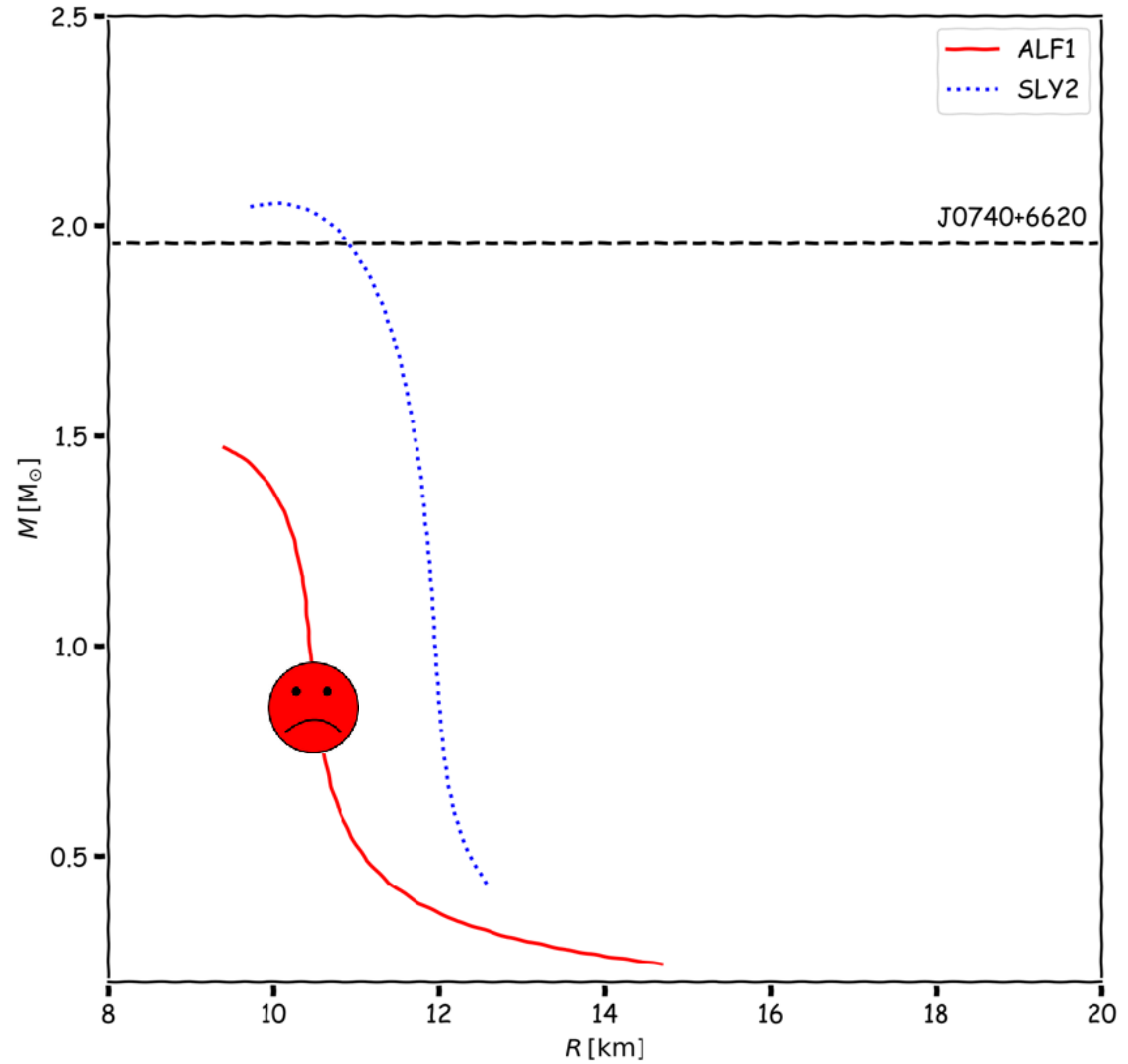
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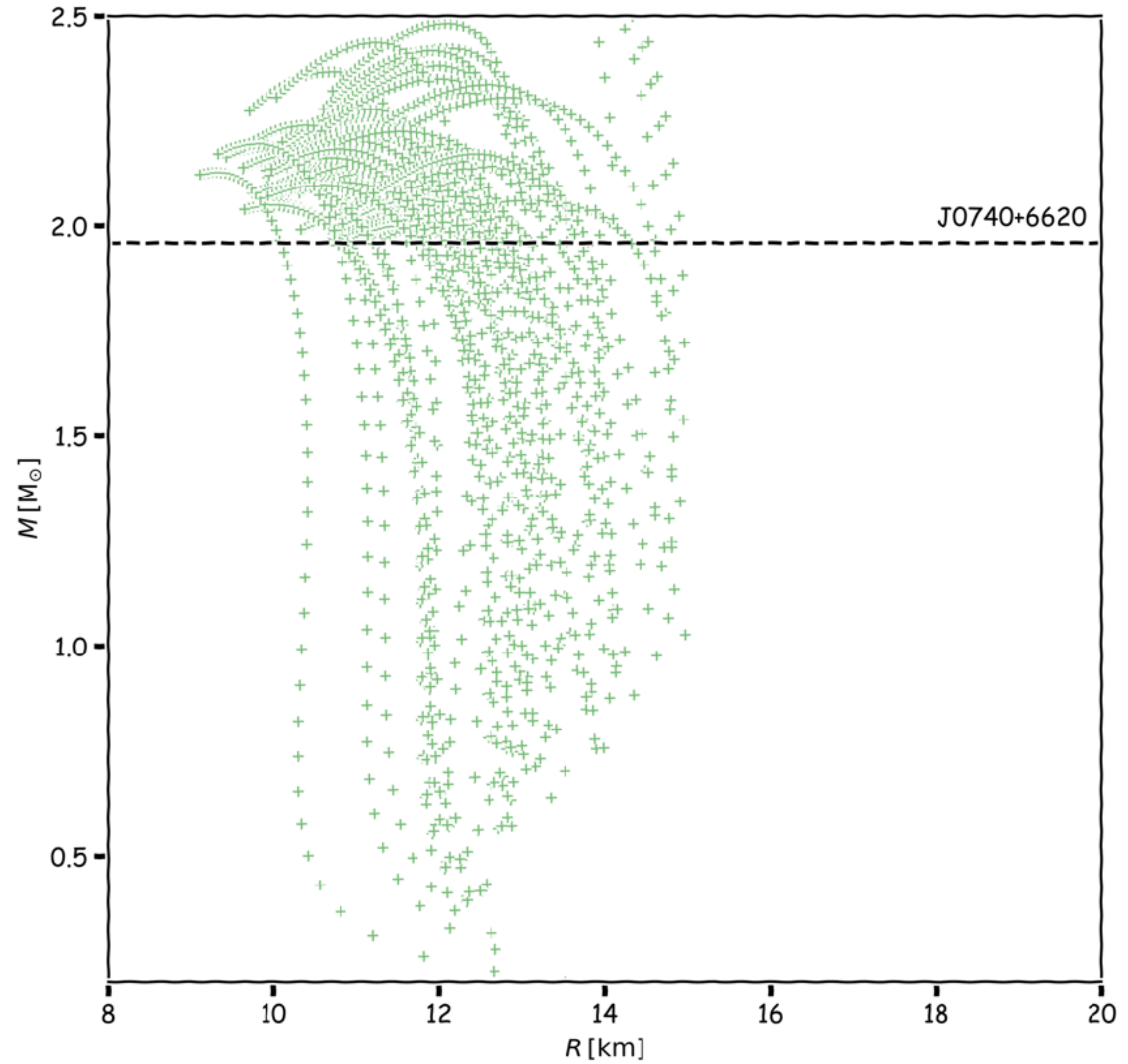
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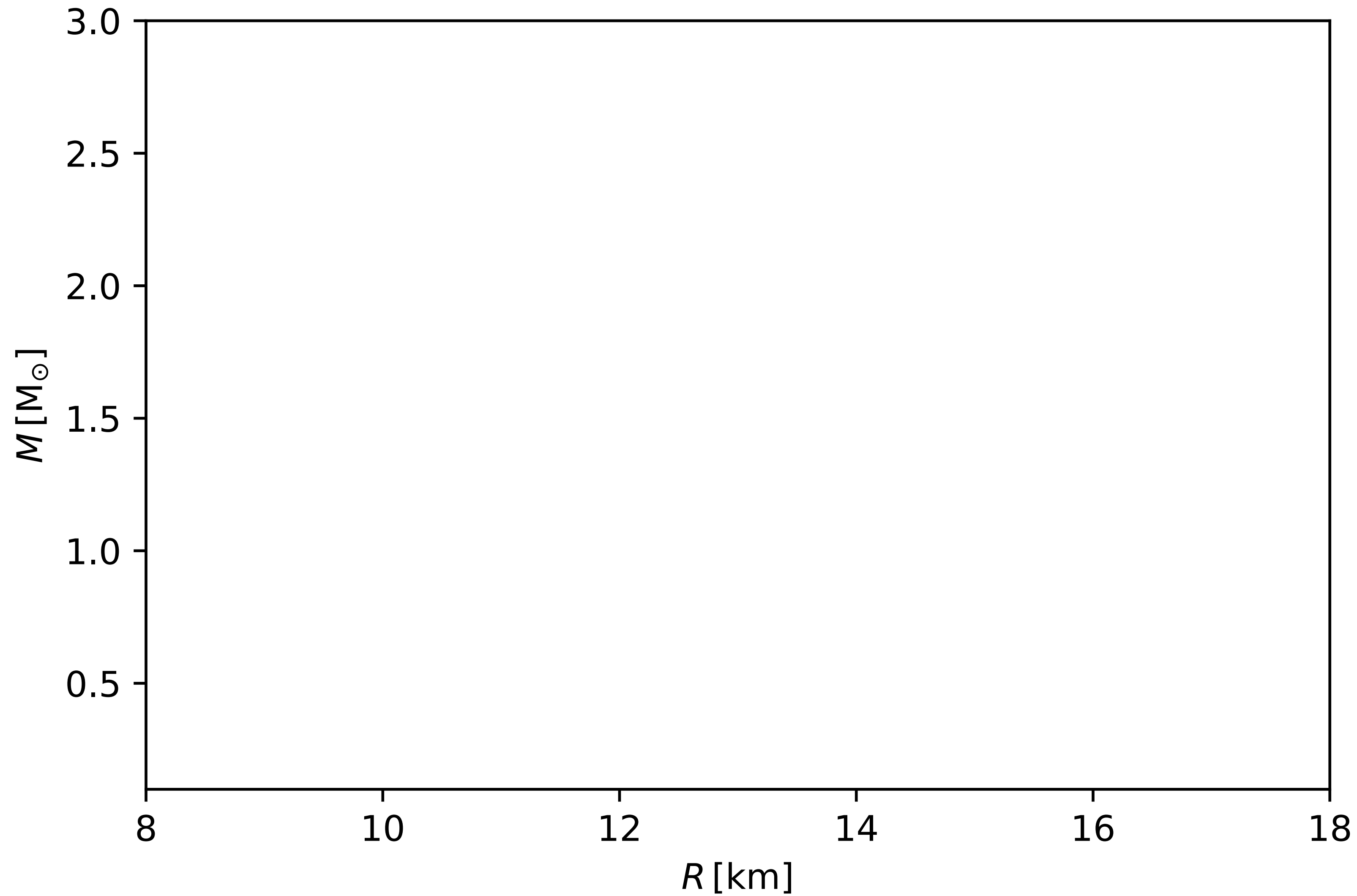
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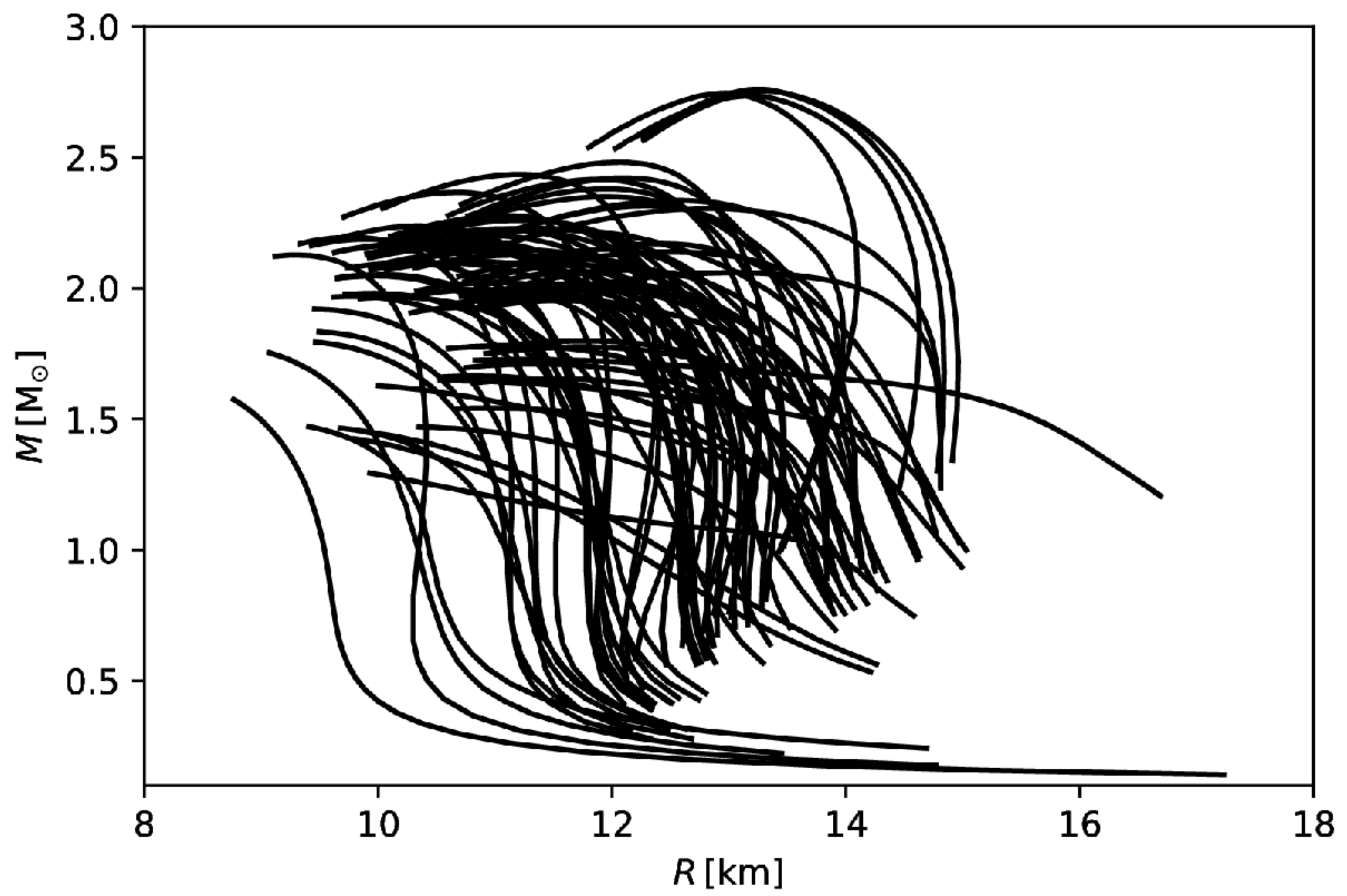
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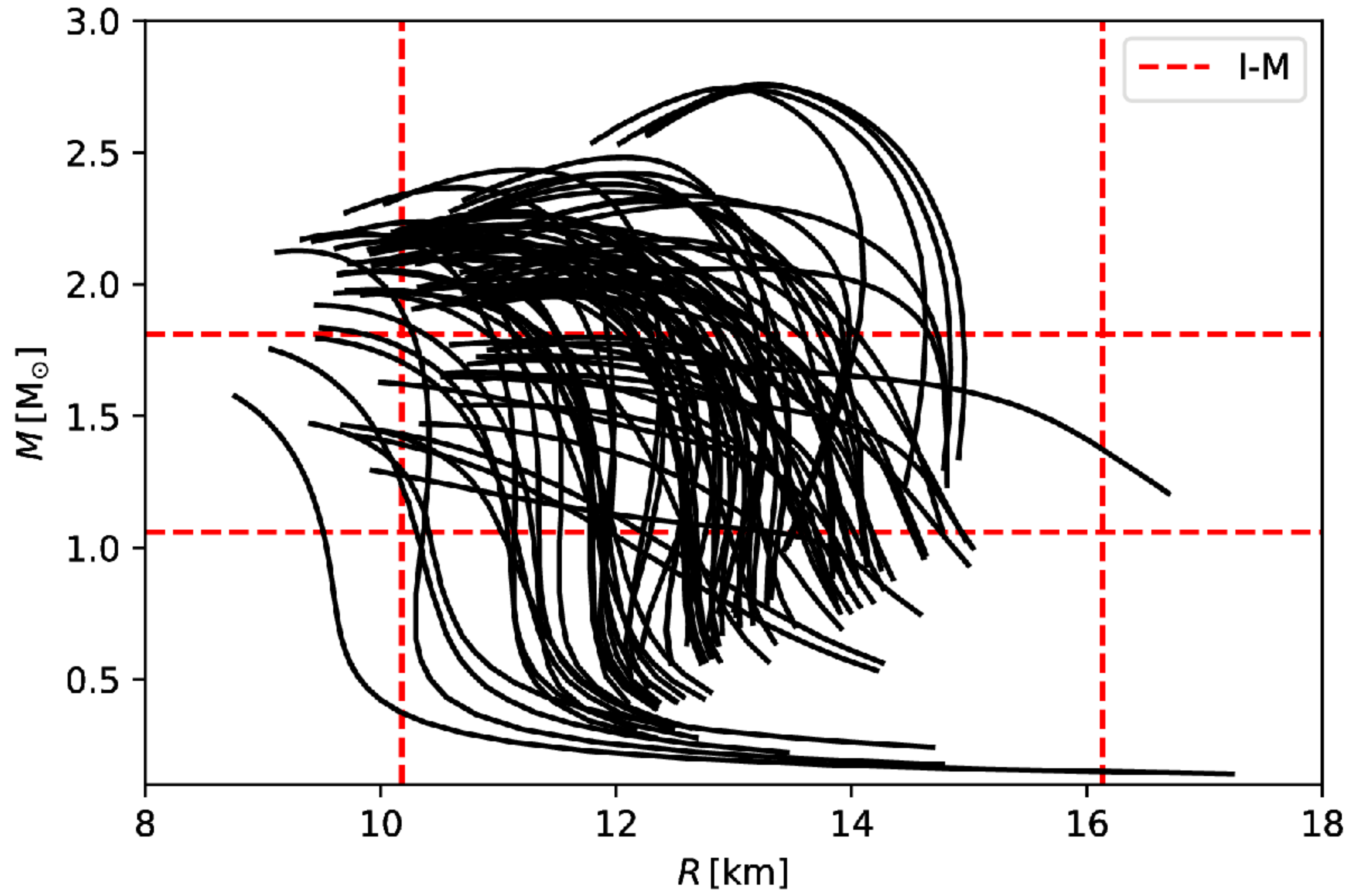
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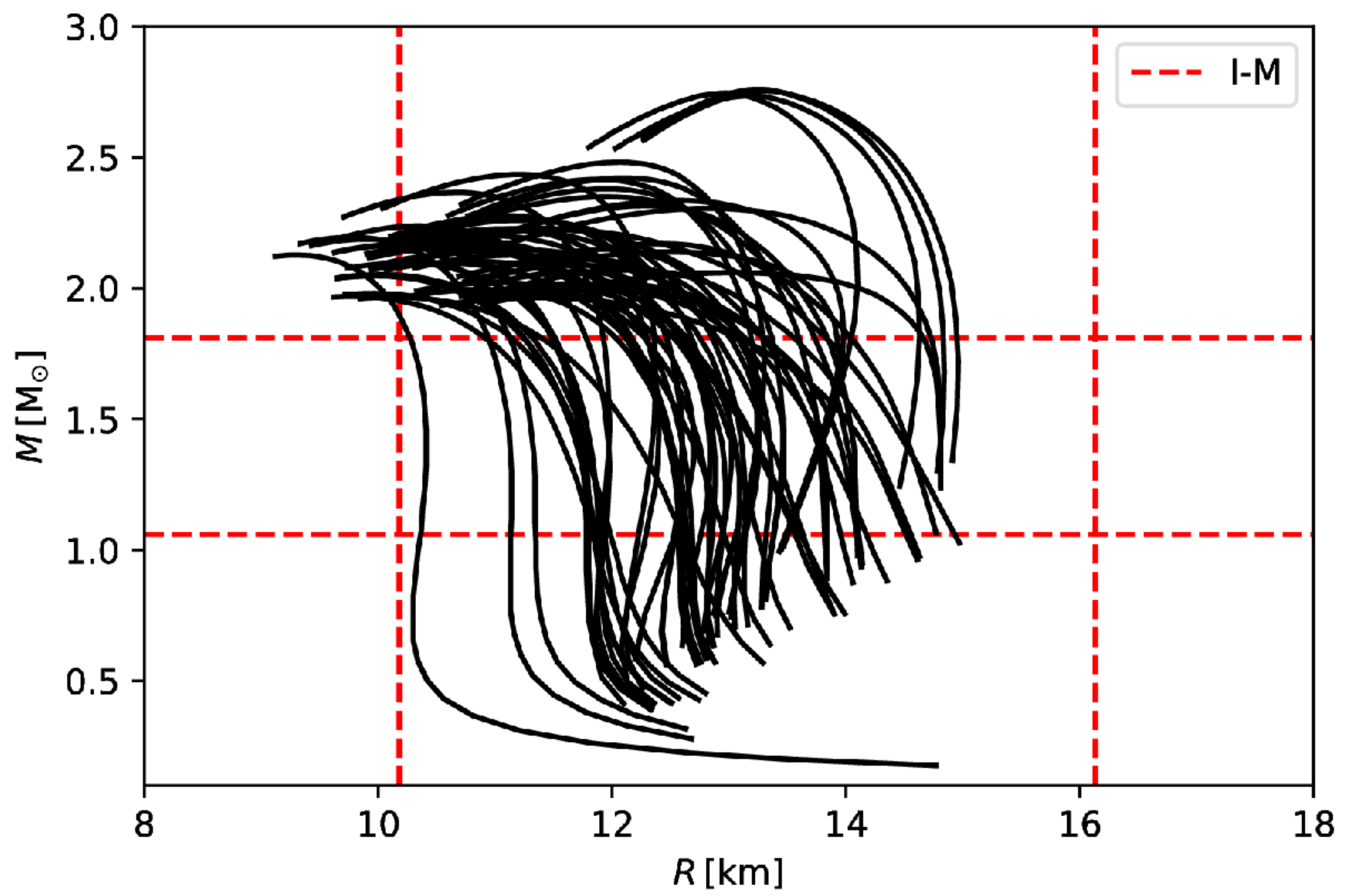
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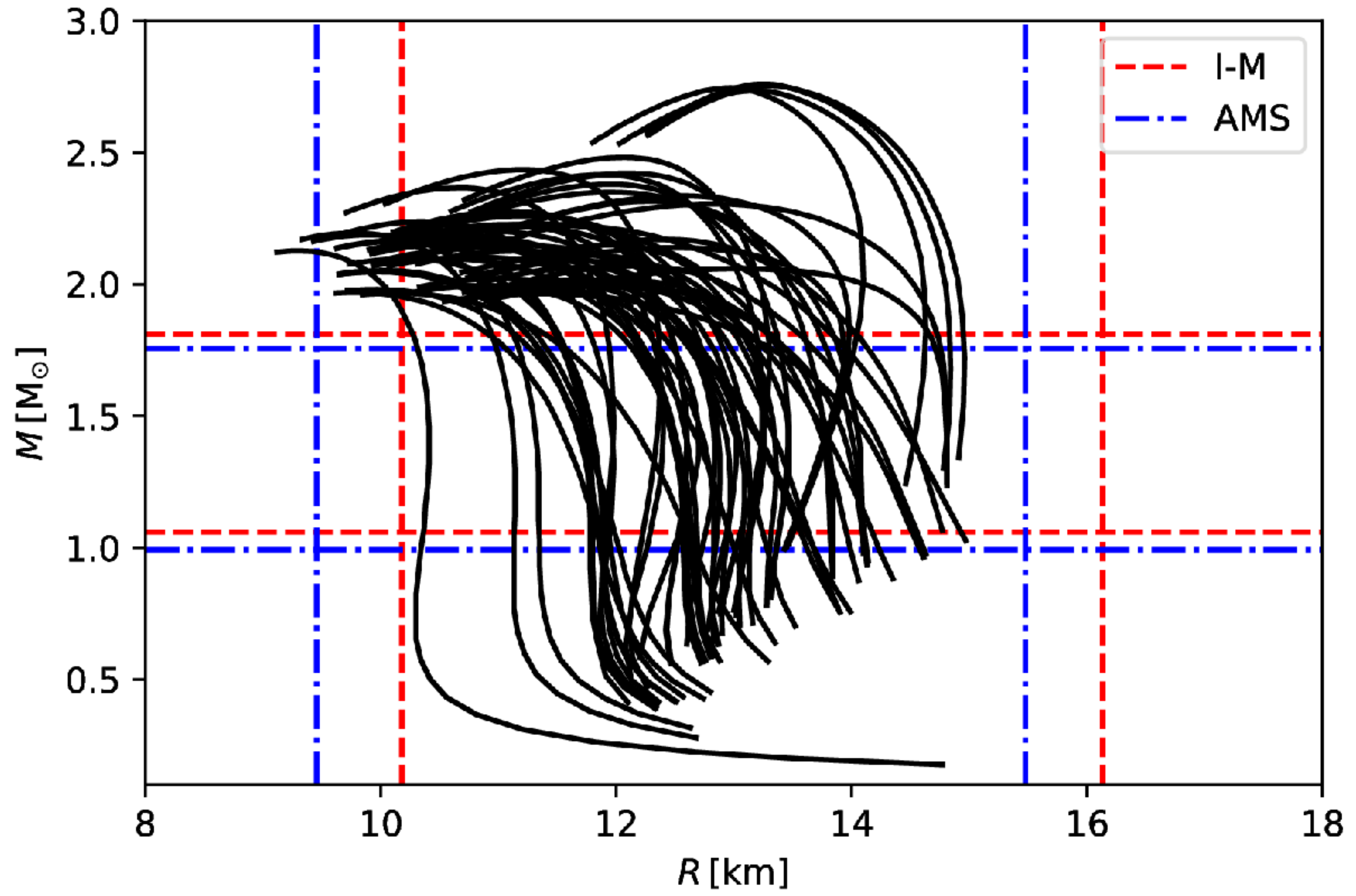


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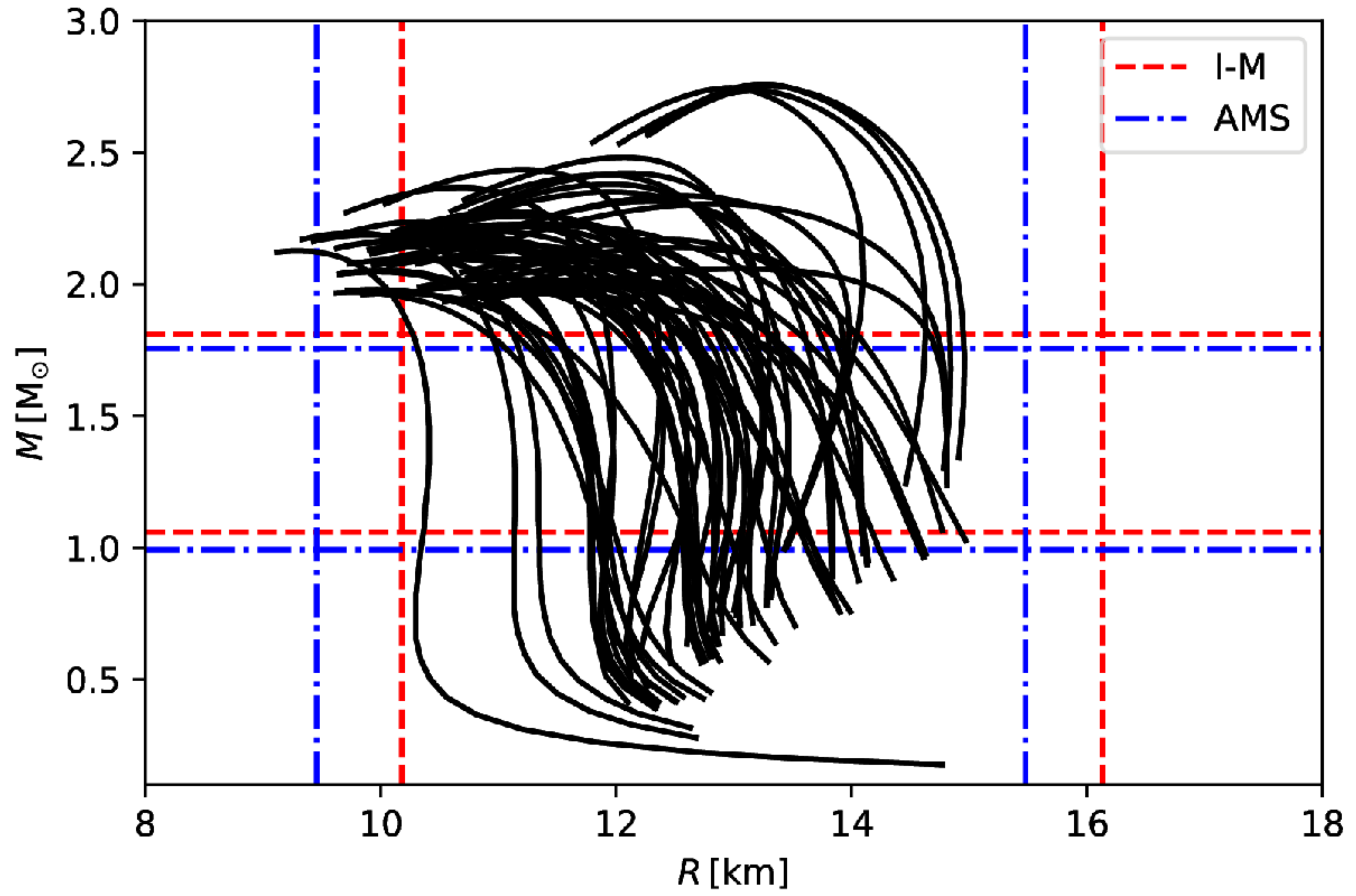




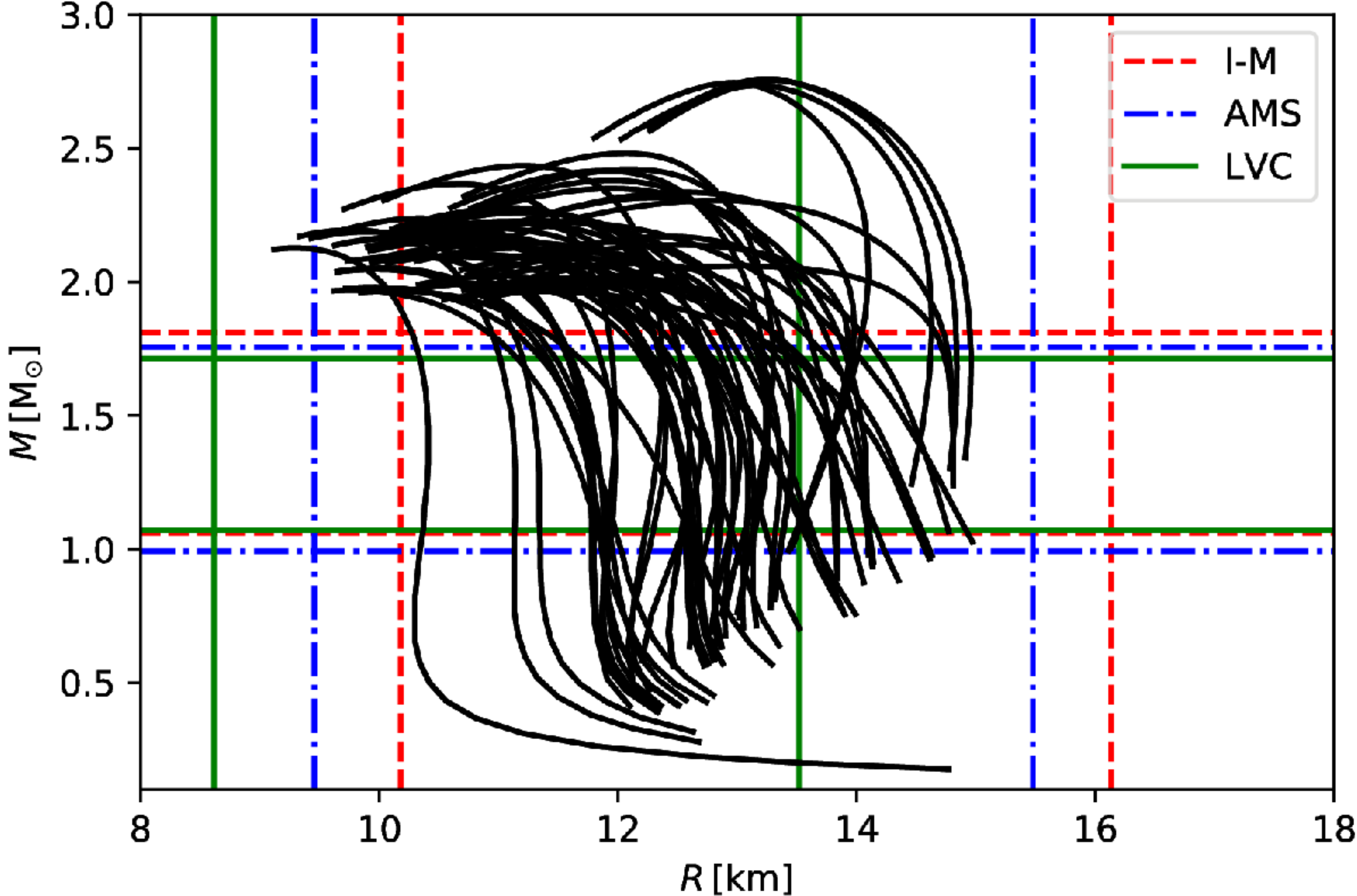
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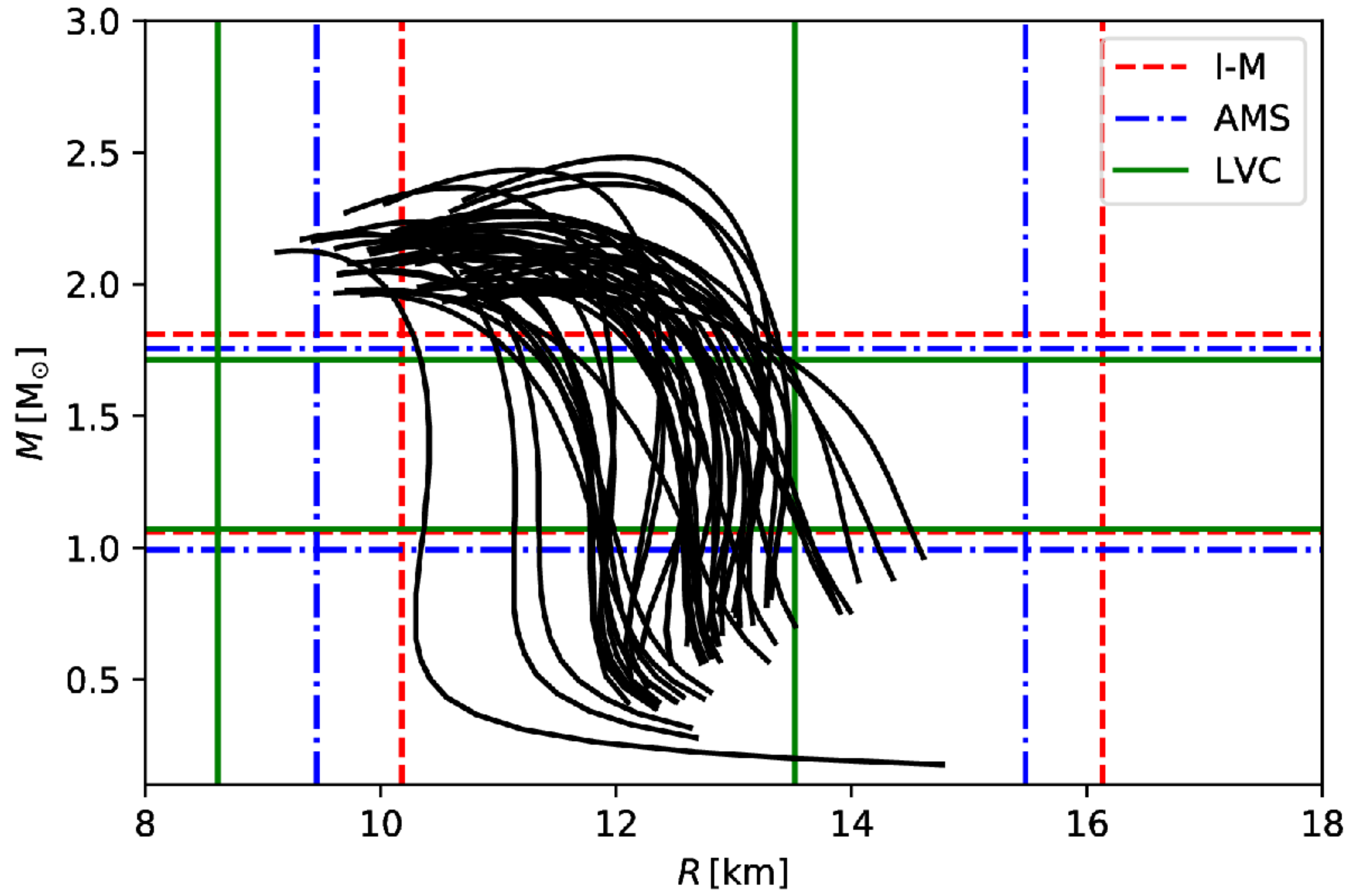
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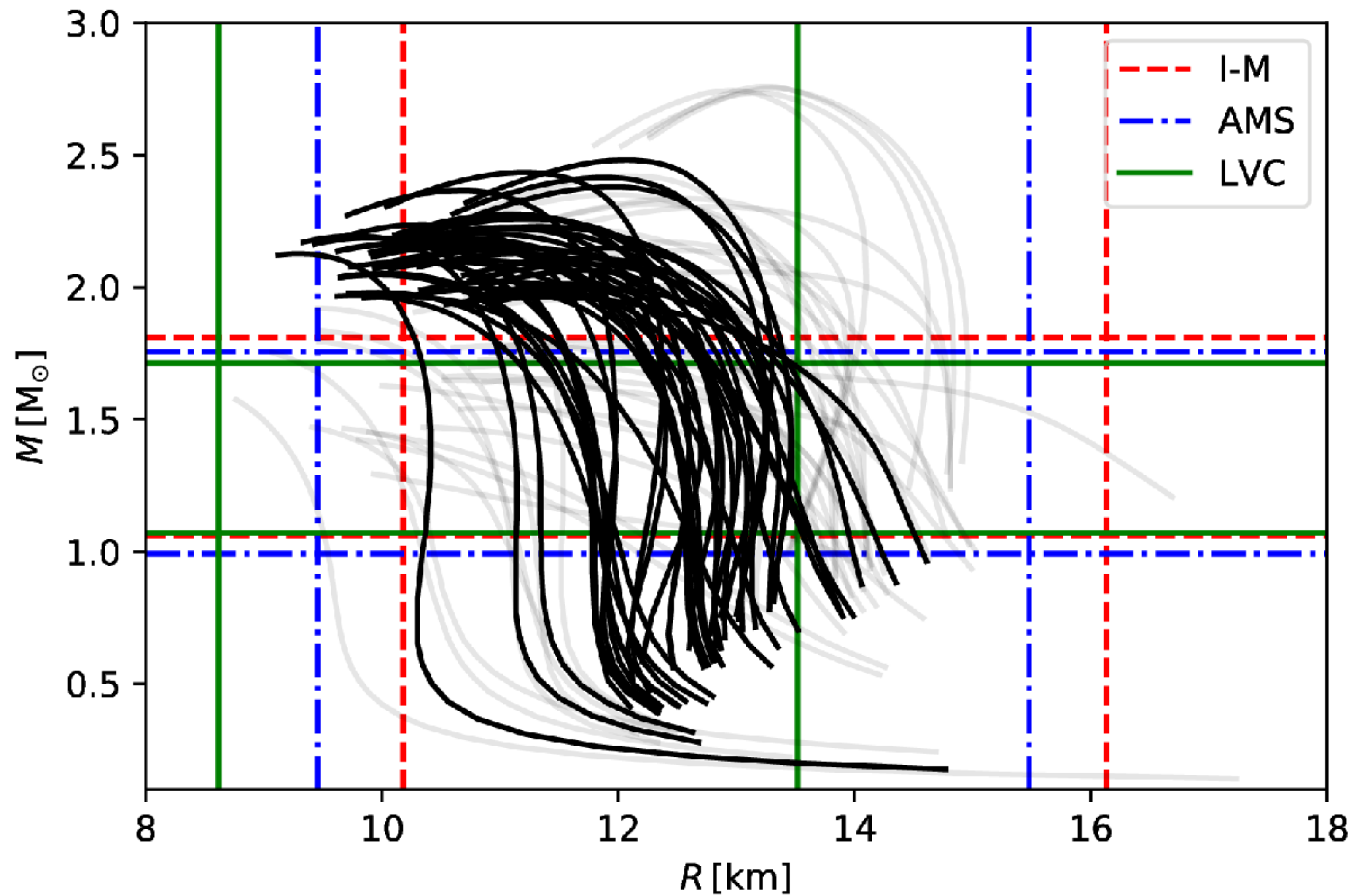
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# (Quasi) Universal relations

Yagi & Yunes (2013)

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$I$

Moment of inertia

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*I*

Moment of inertia

*LOVE*

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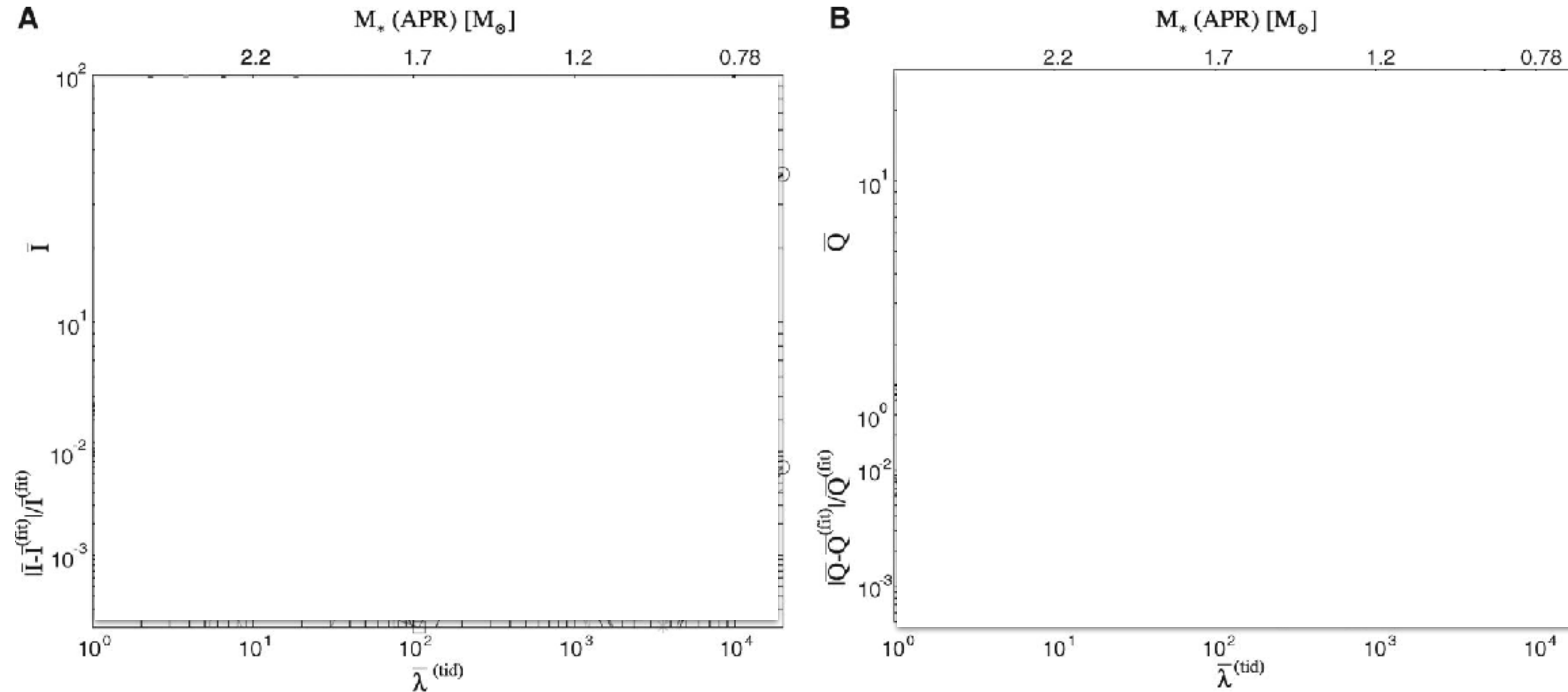
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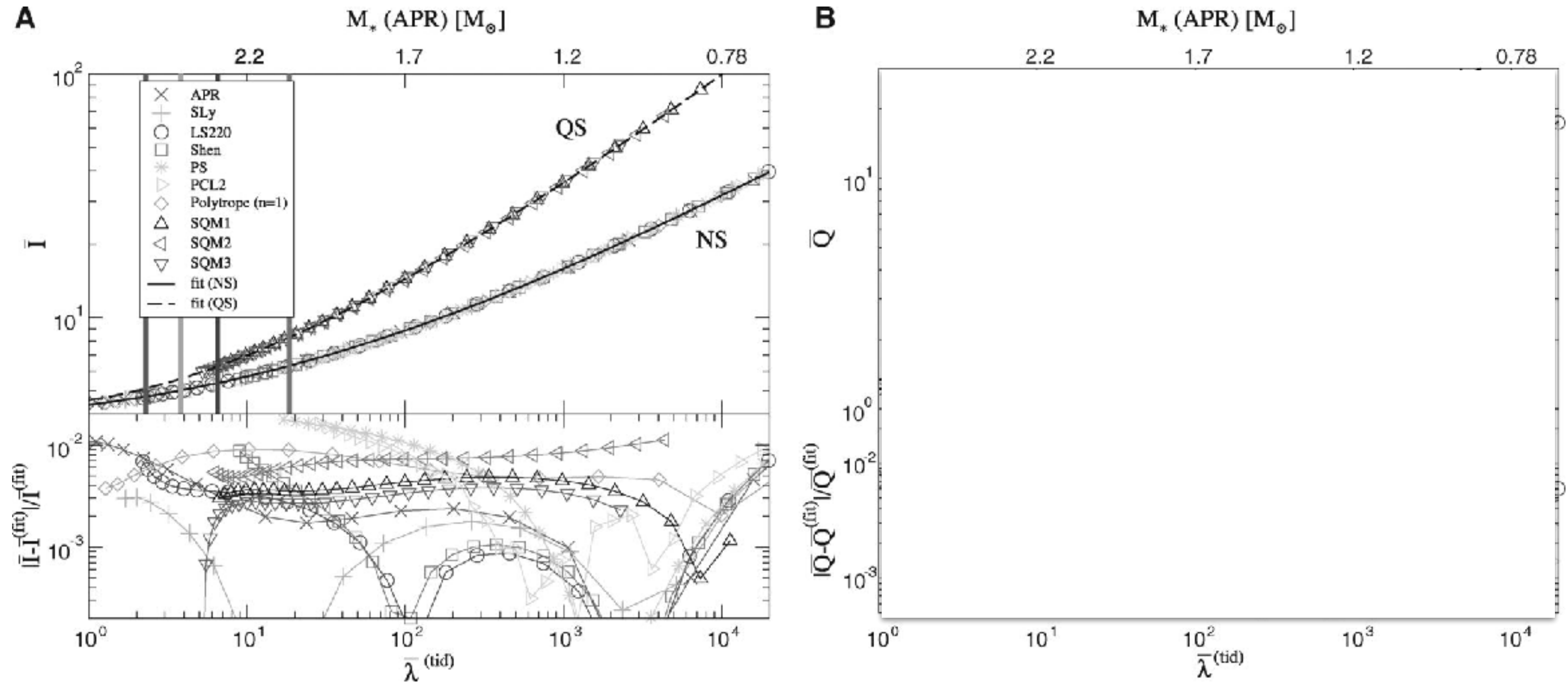
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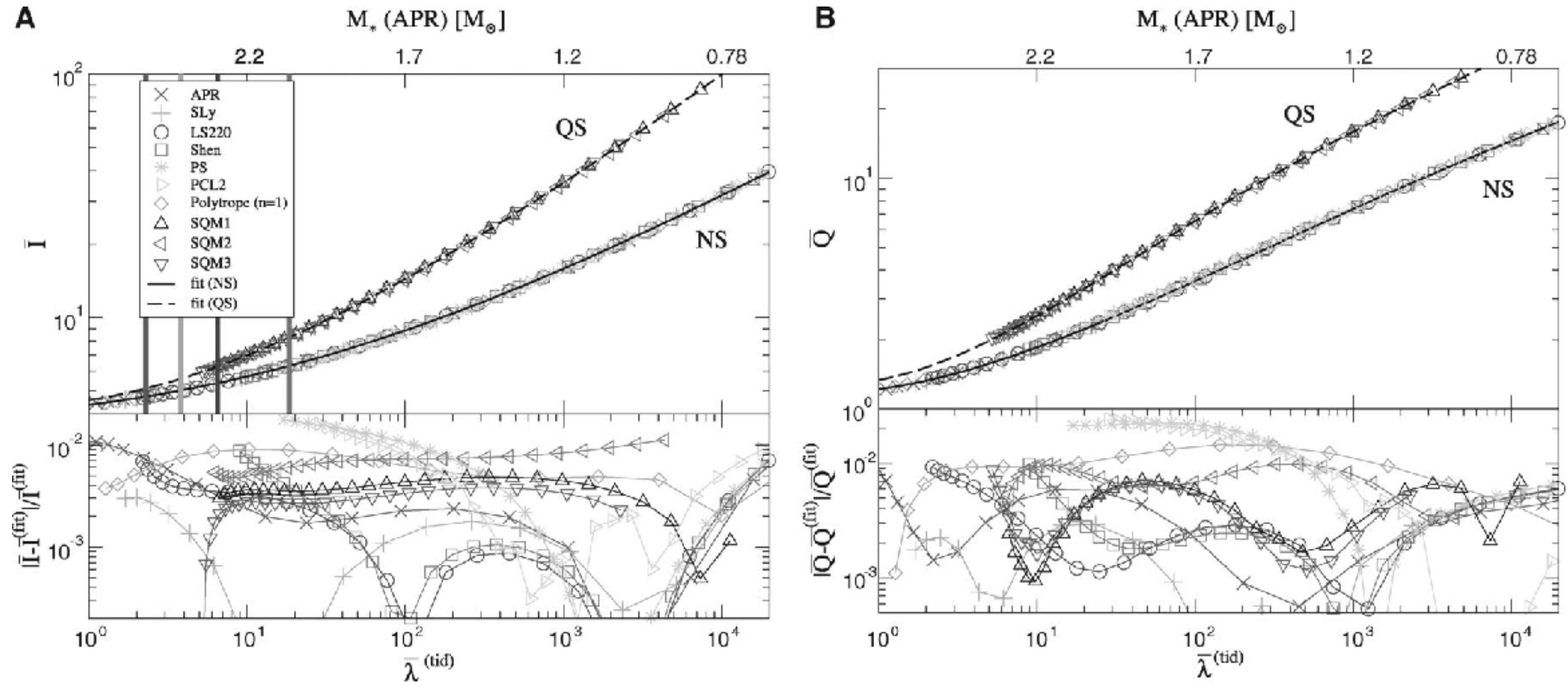
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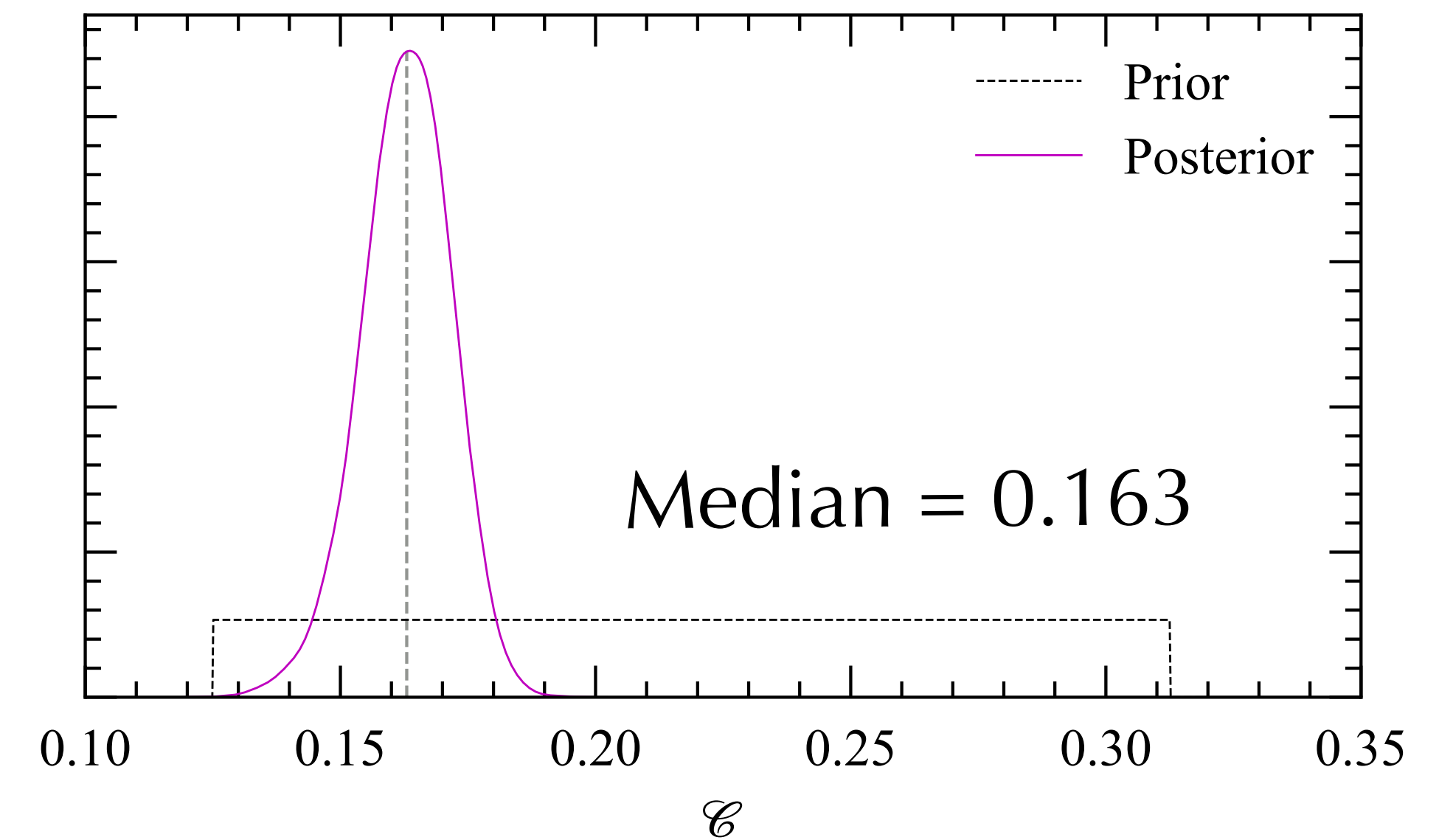
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# An inference scheme to get astrophysical properties

Landry & Kumar (2017)  
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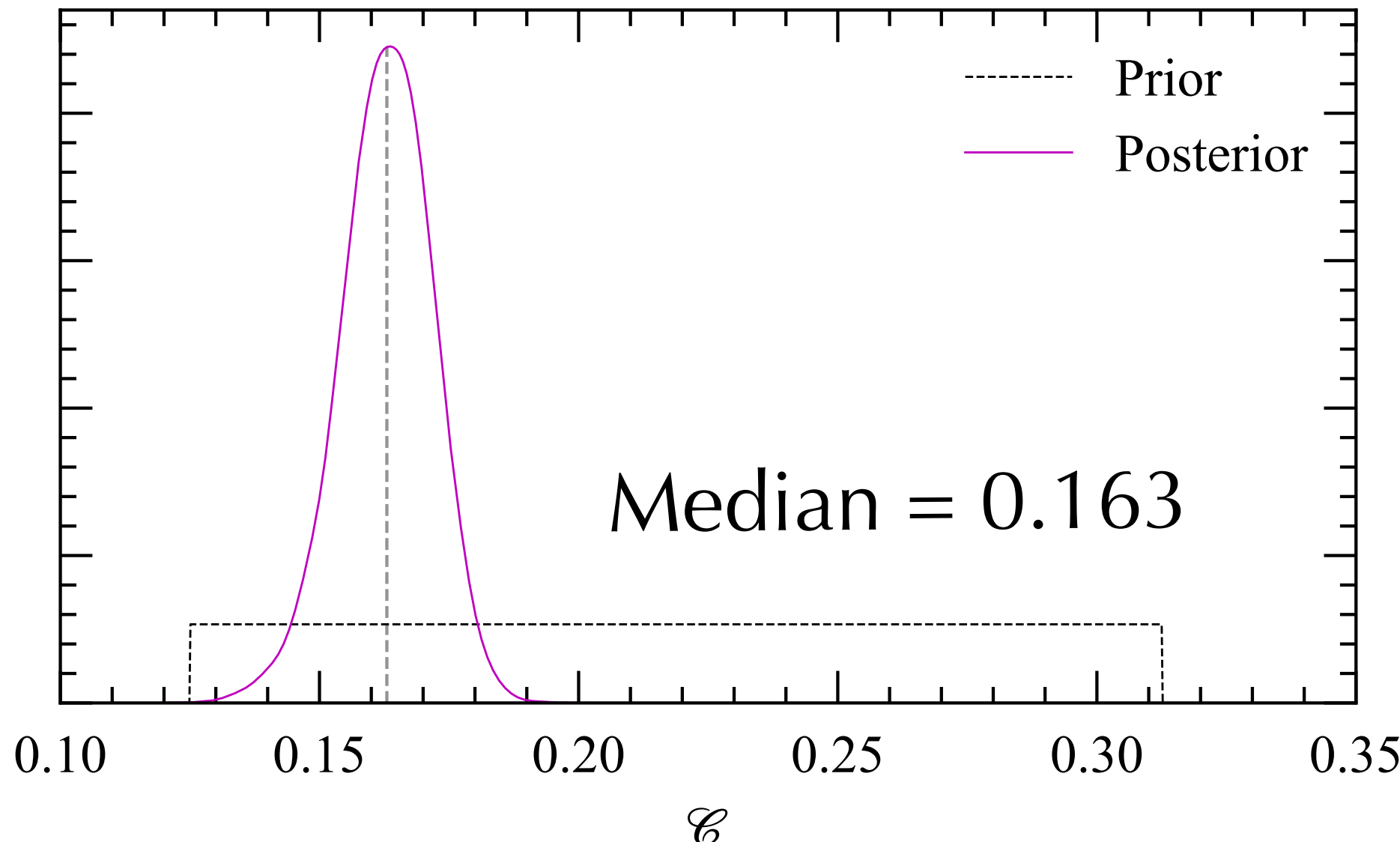
$$P(GM/Rc^2 \mid \text{NICER})$$



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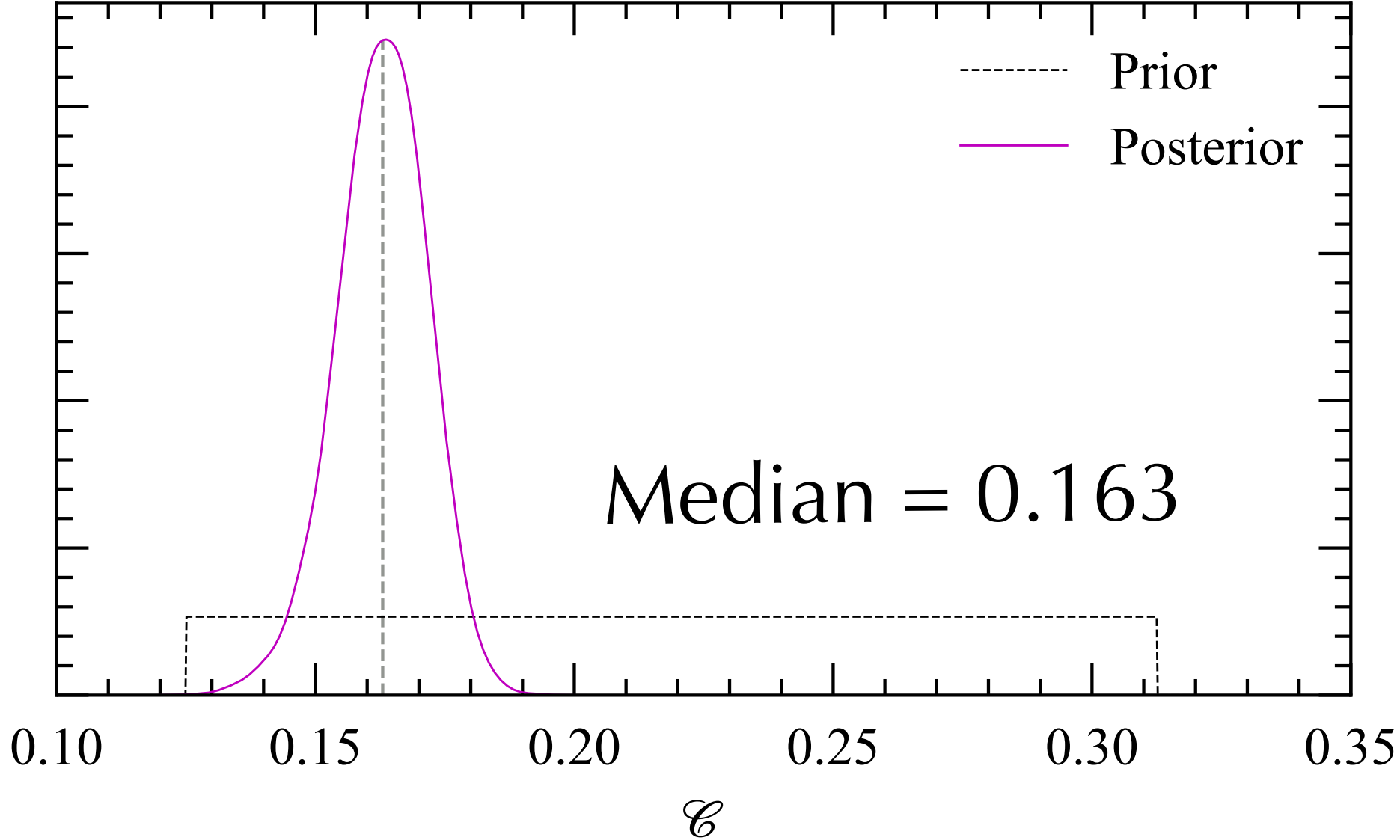


Prior

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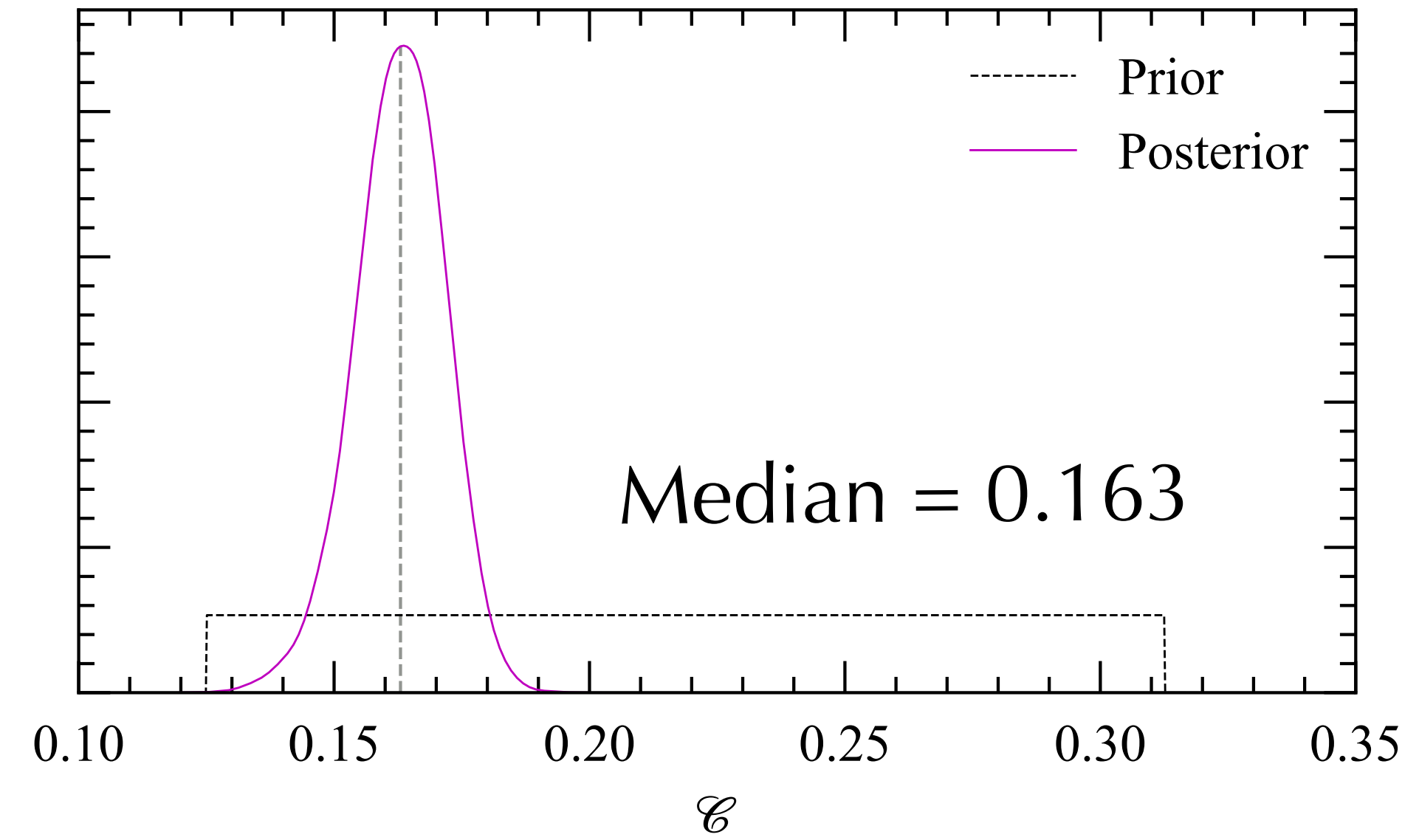
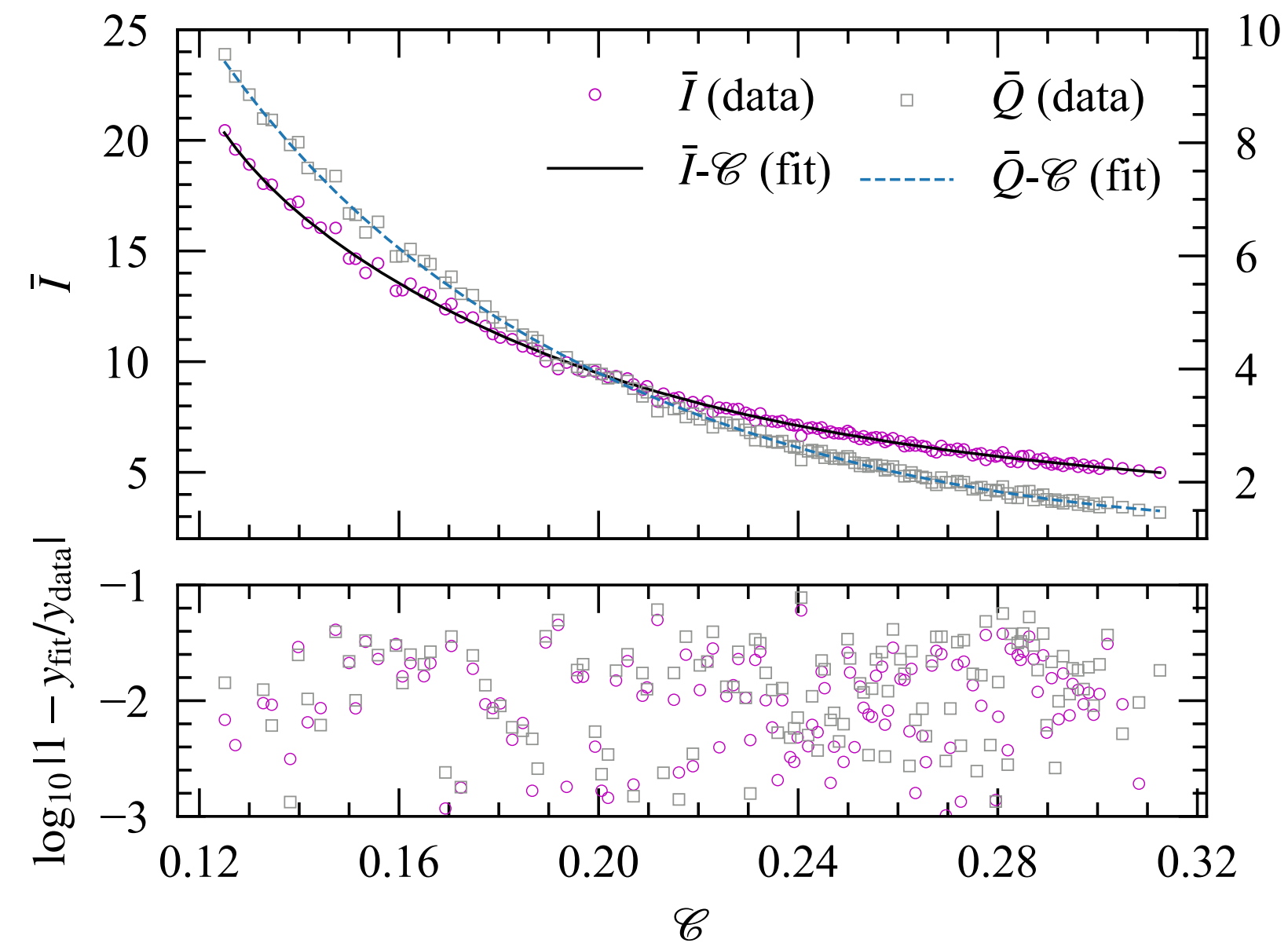
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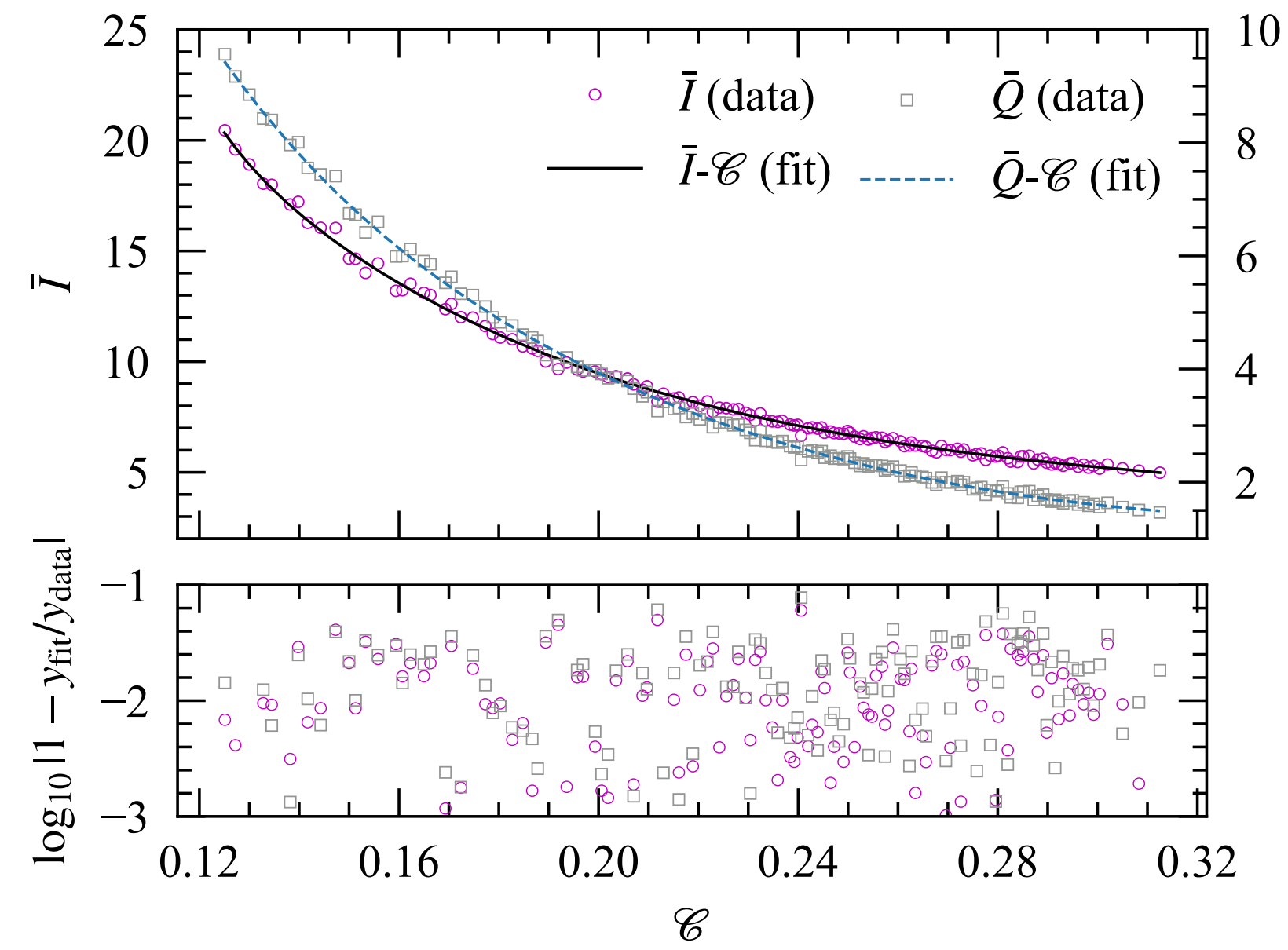
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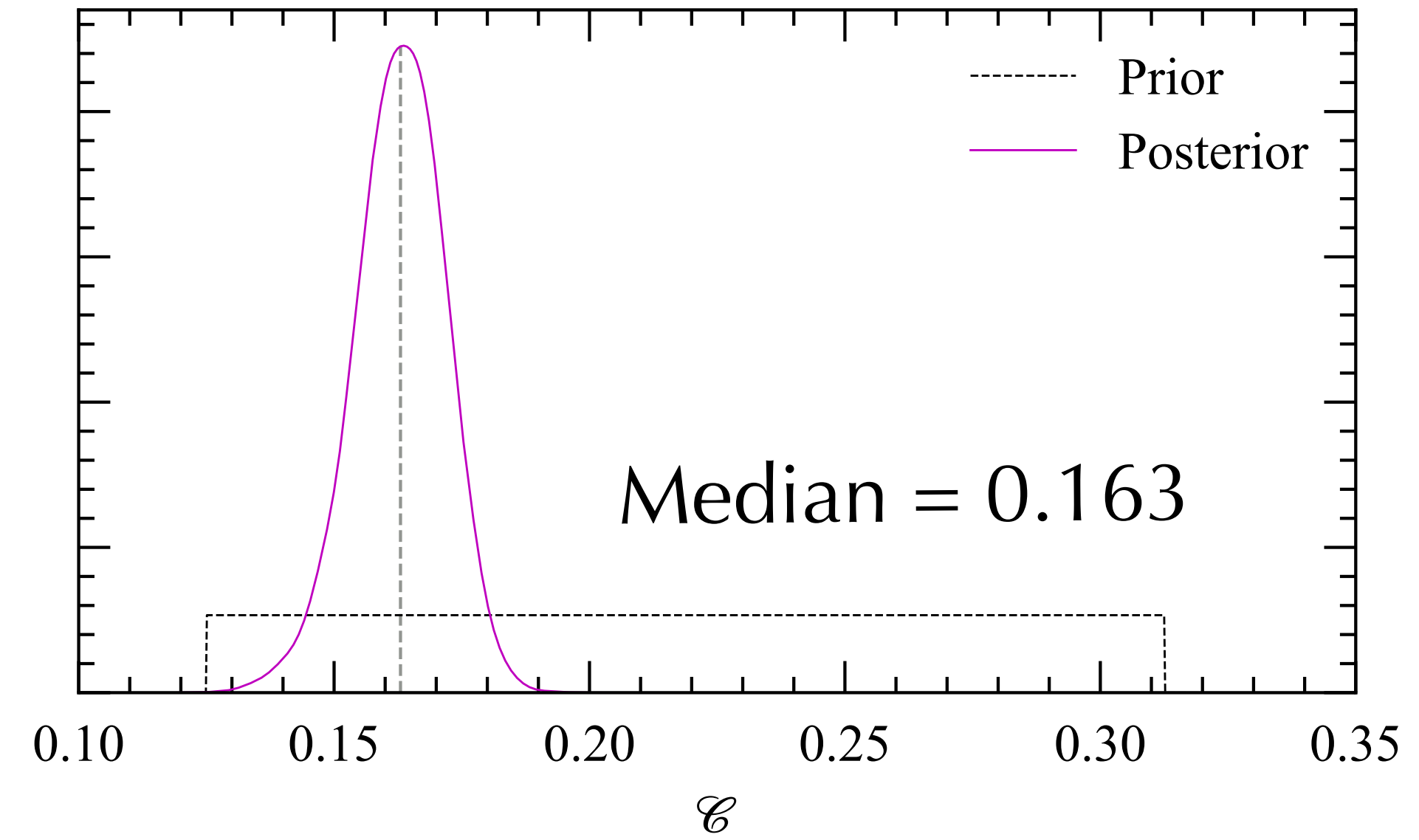
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Likelihood



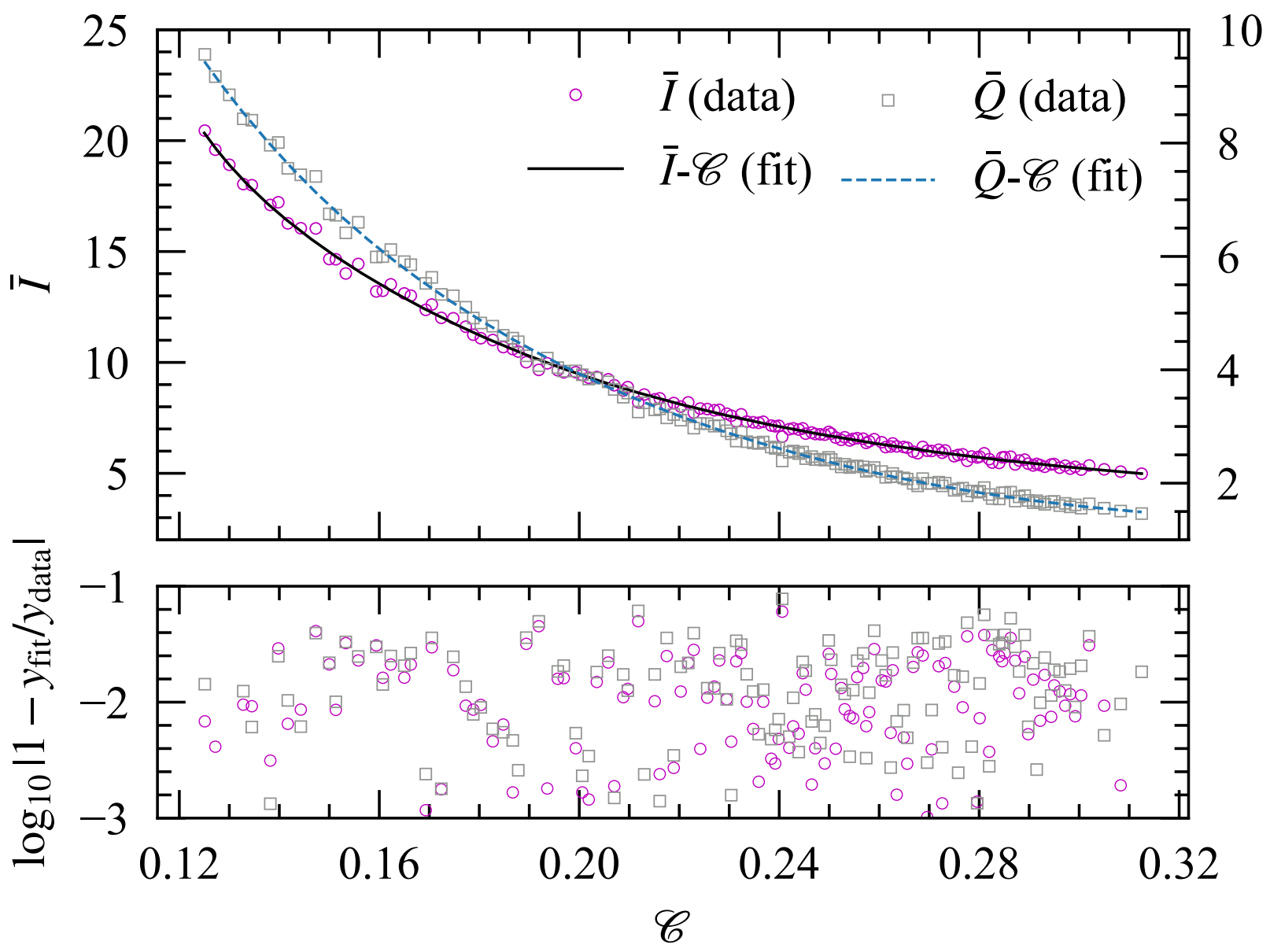
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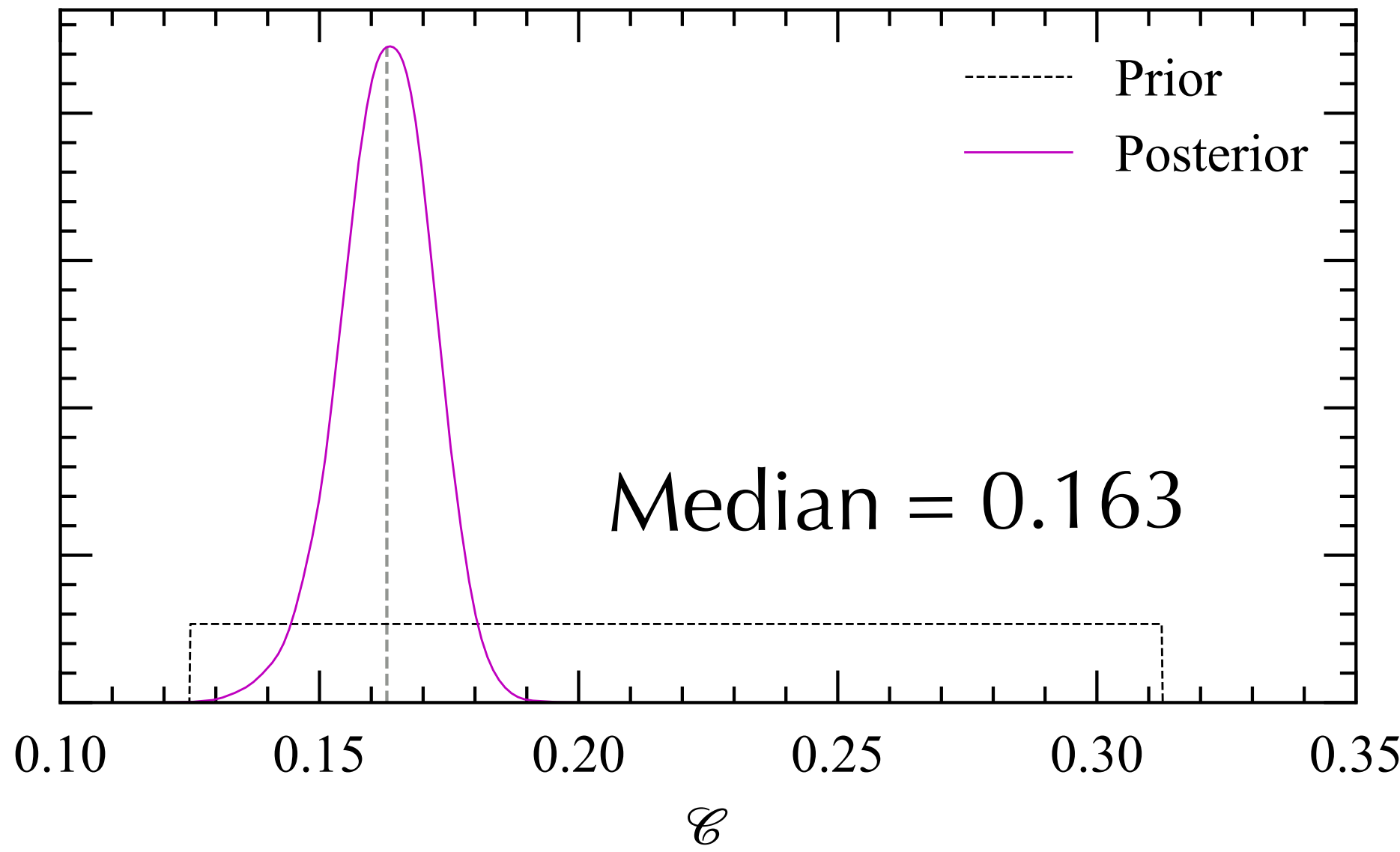
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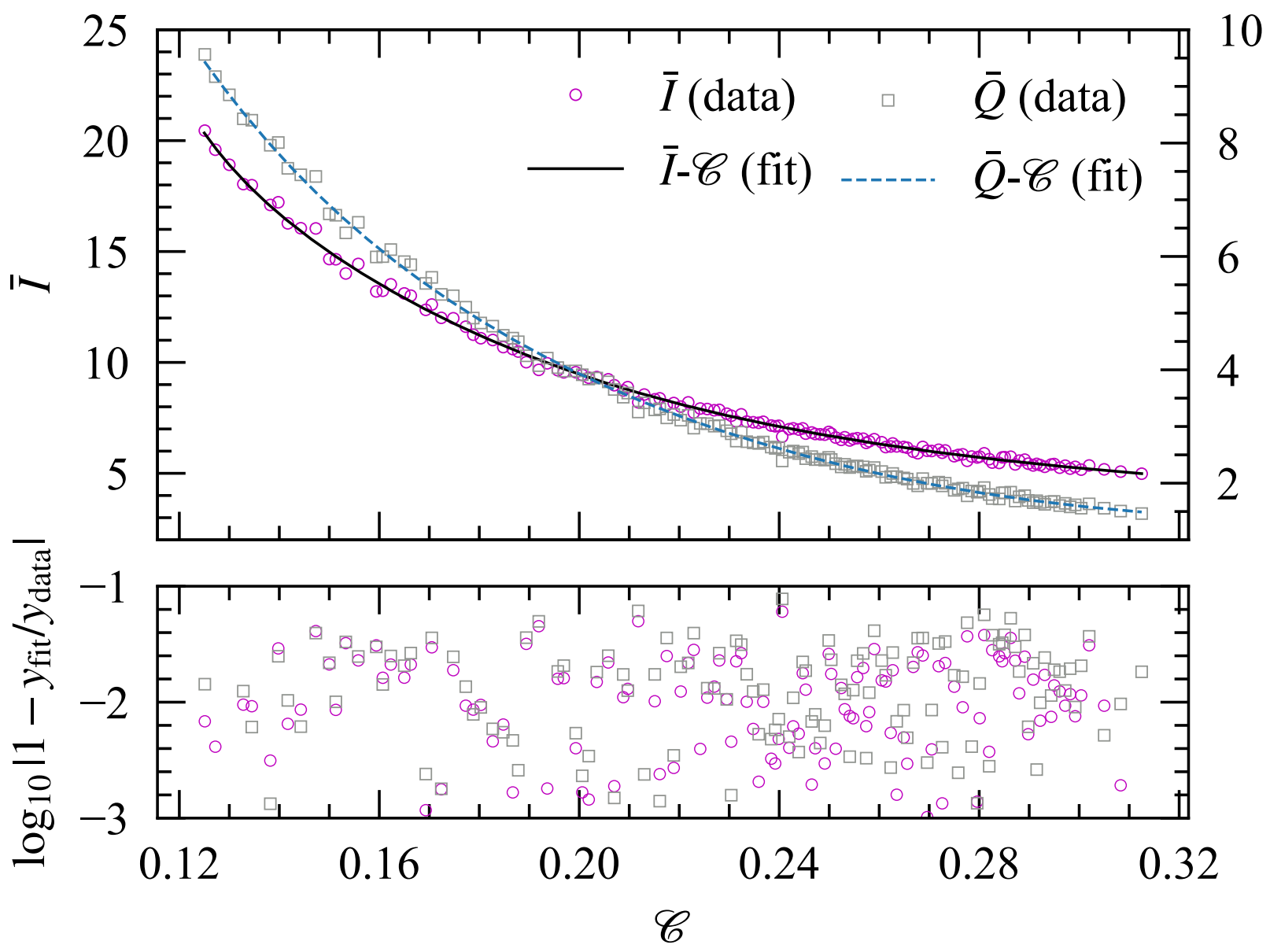
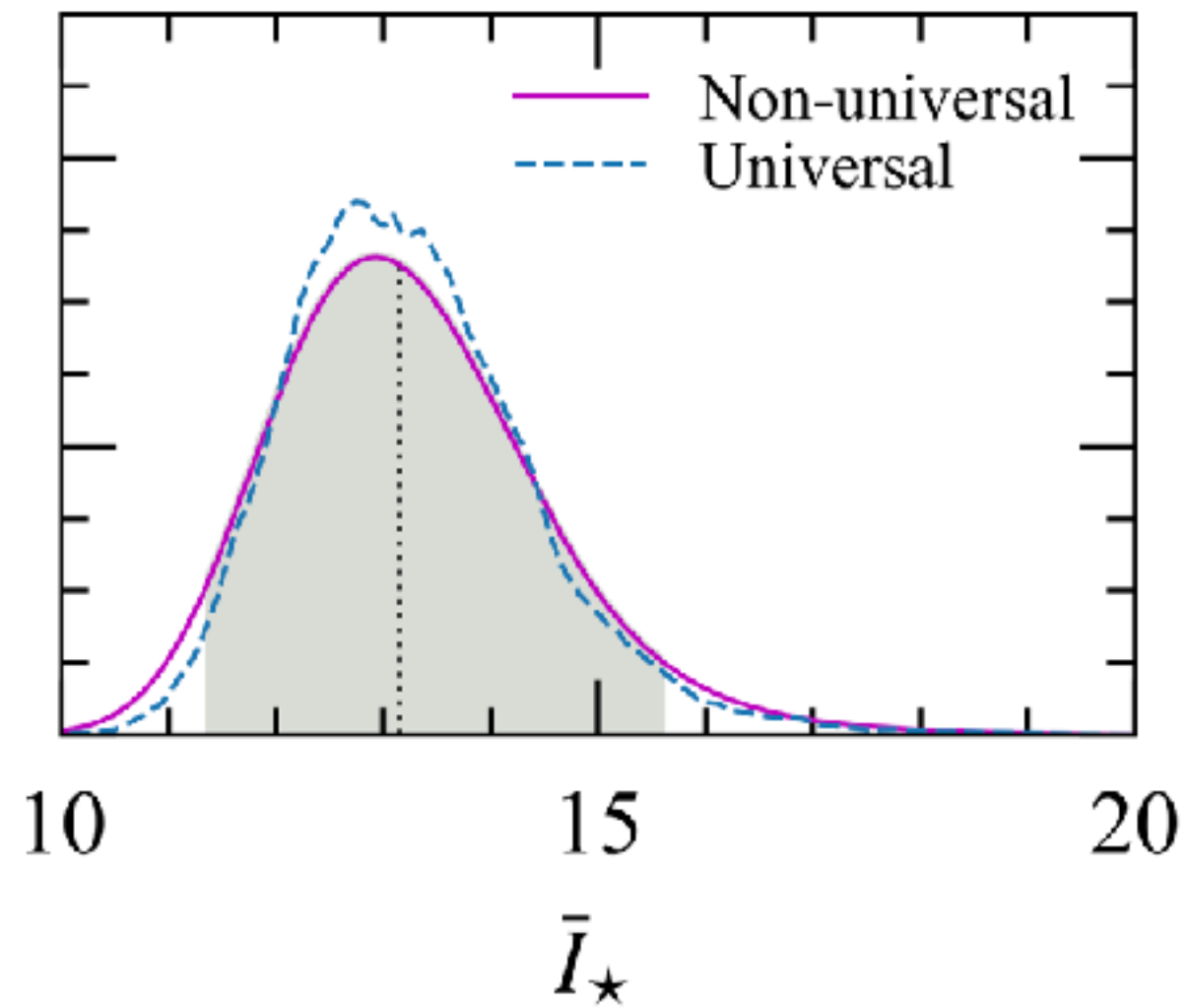
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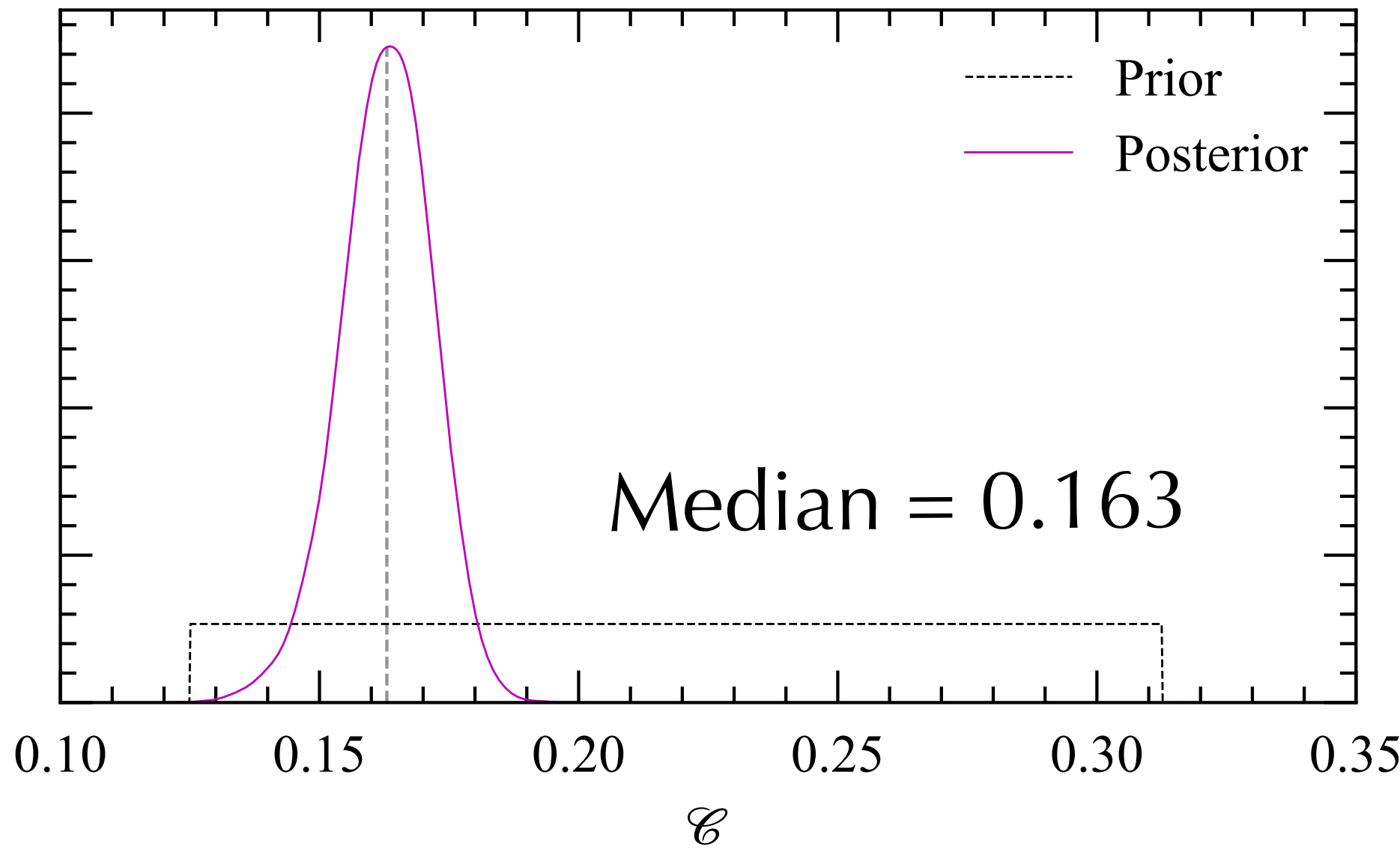
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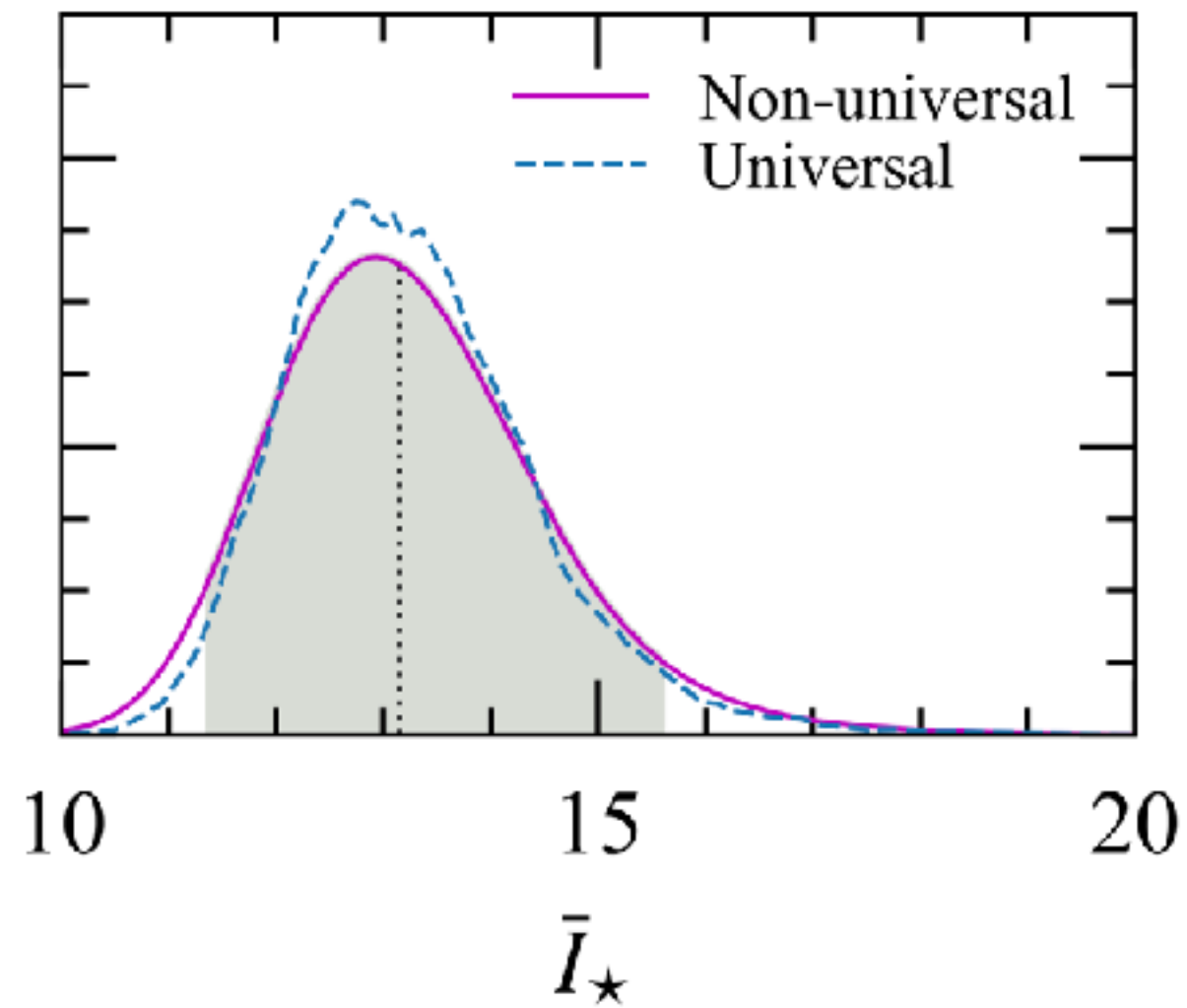
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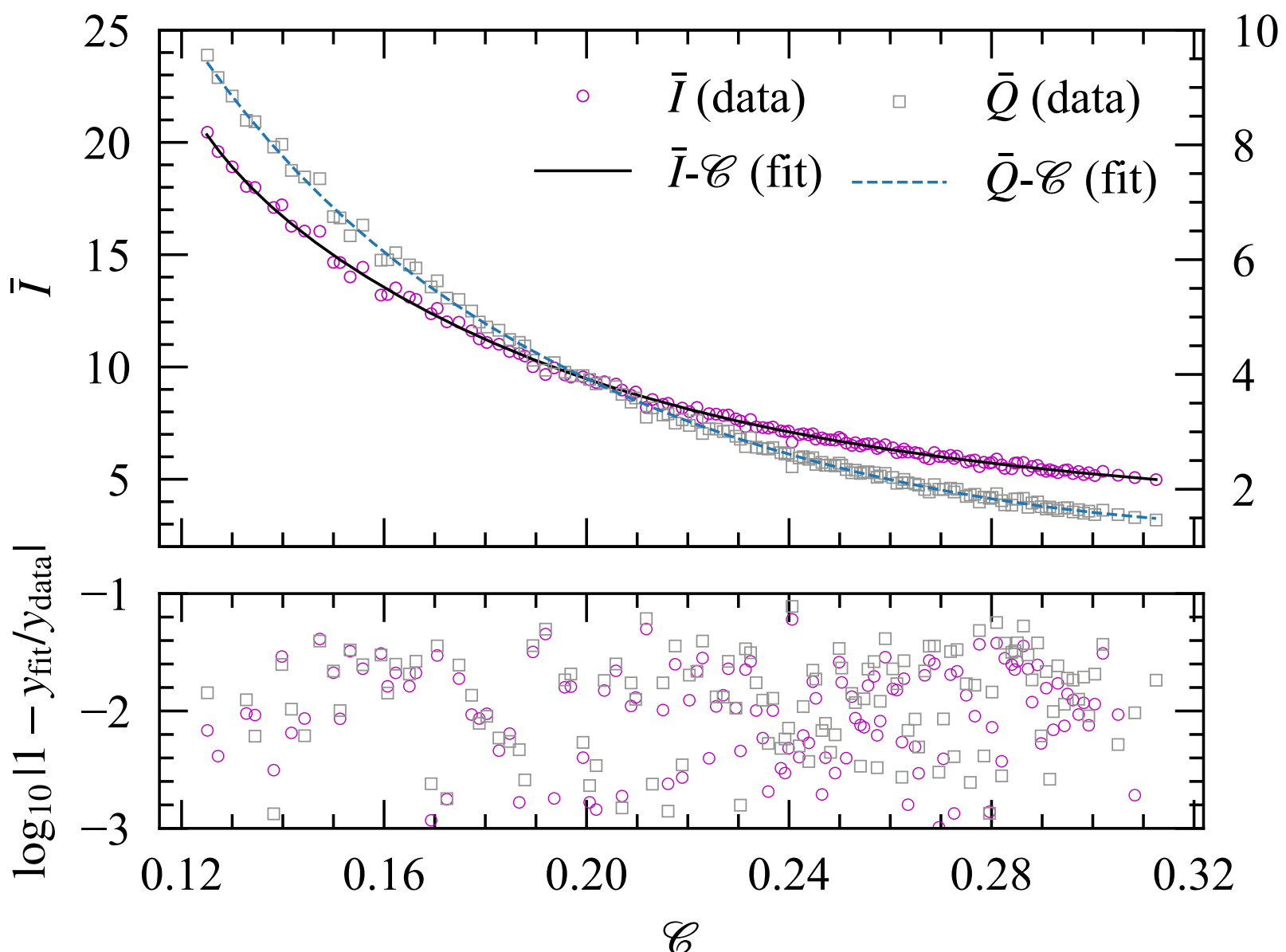
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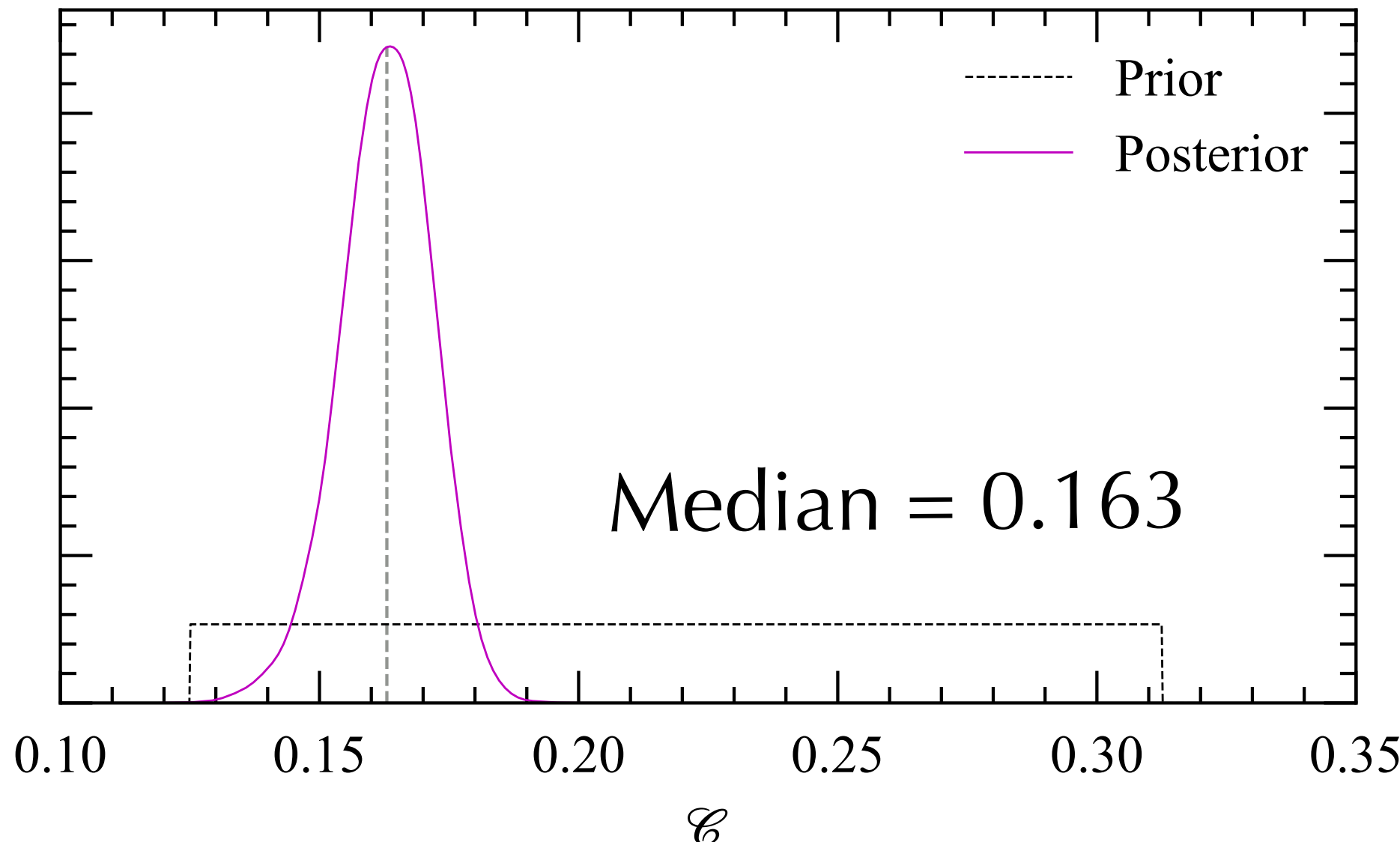
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Posterior



Likelihood



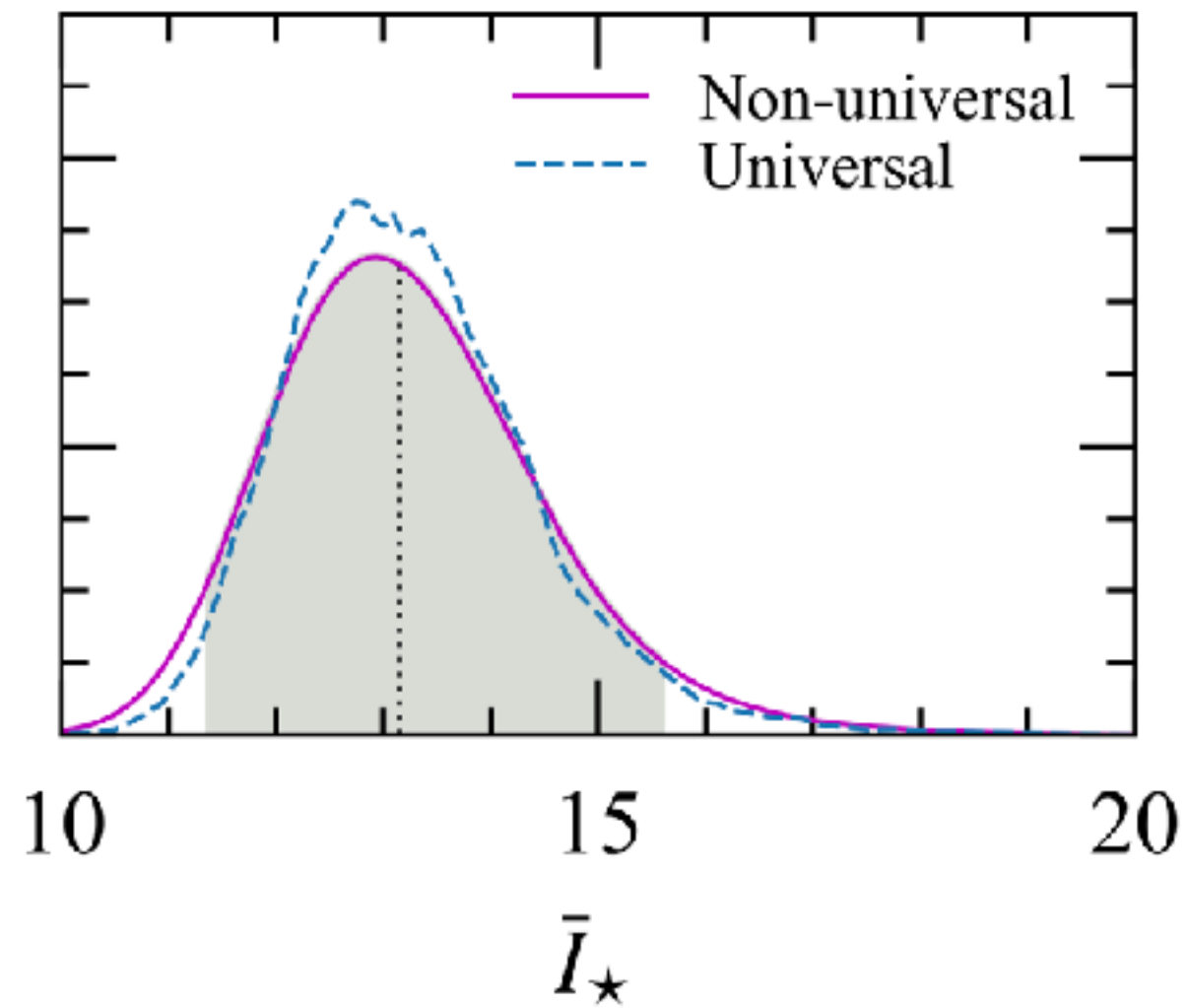
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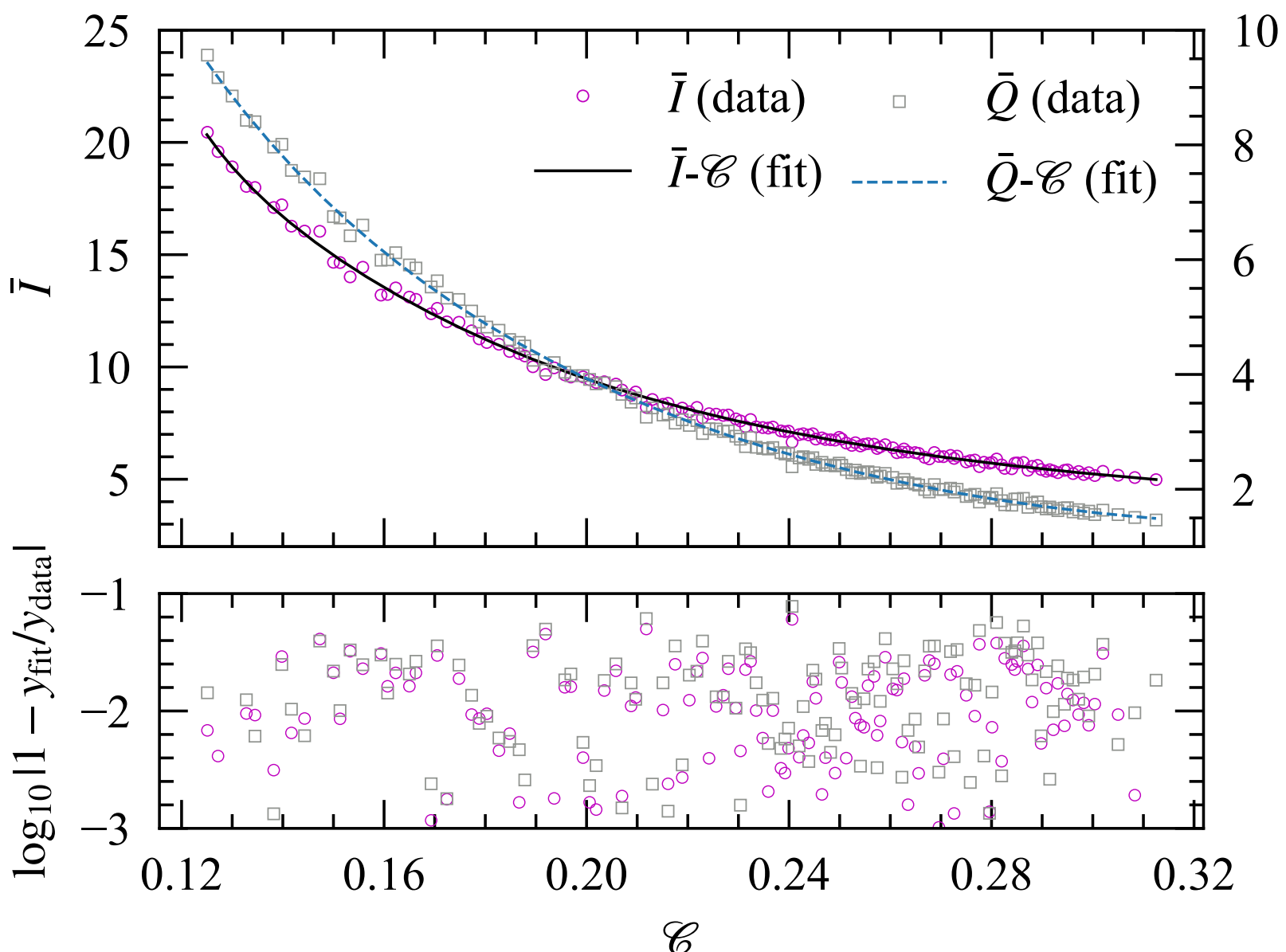
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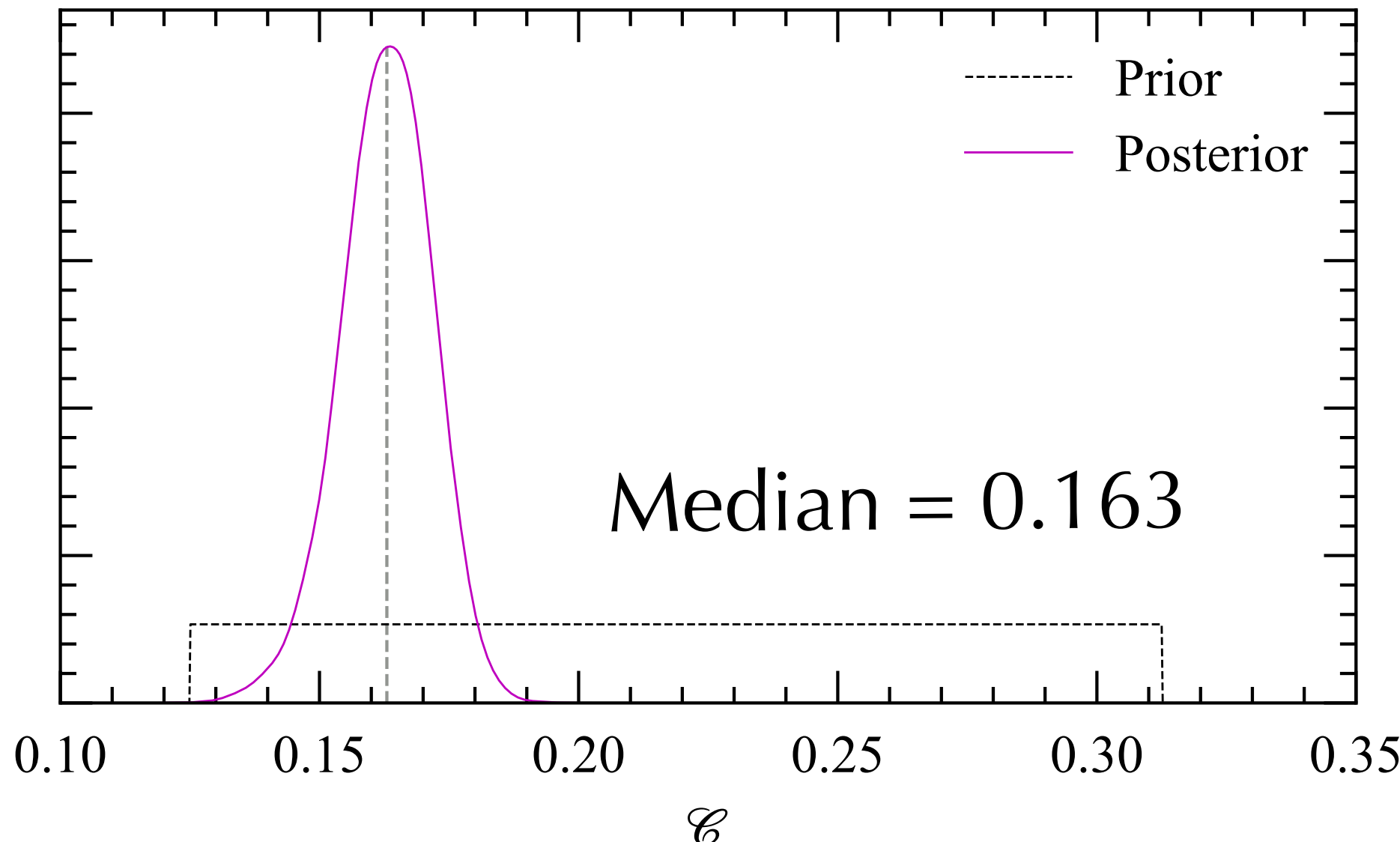
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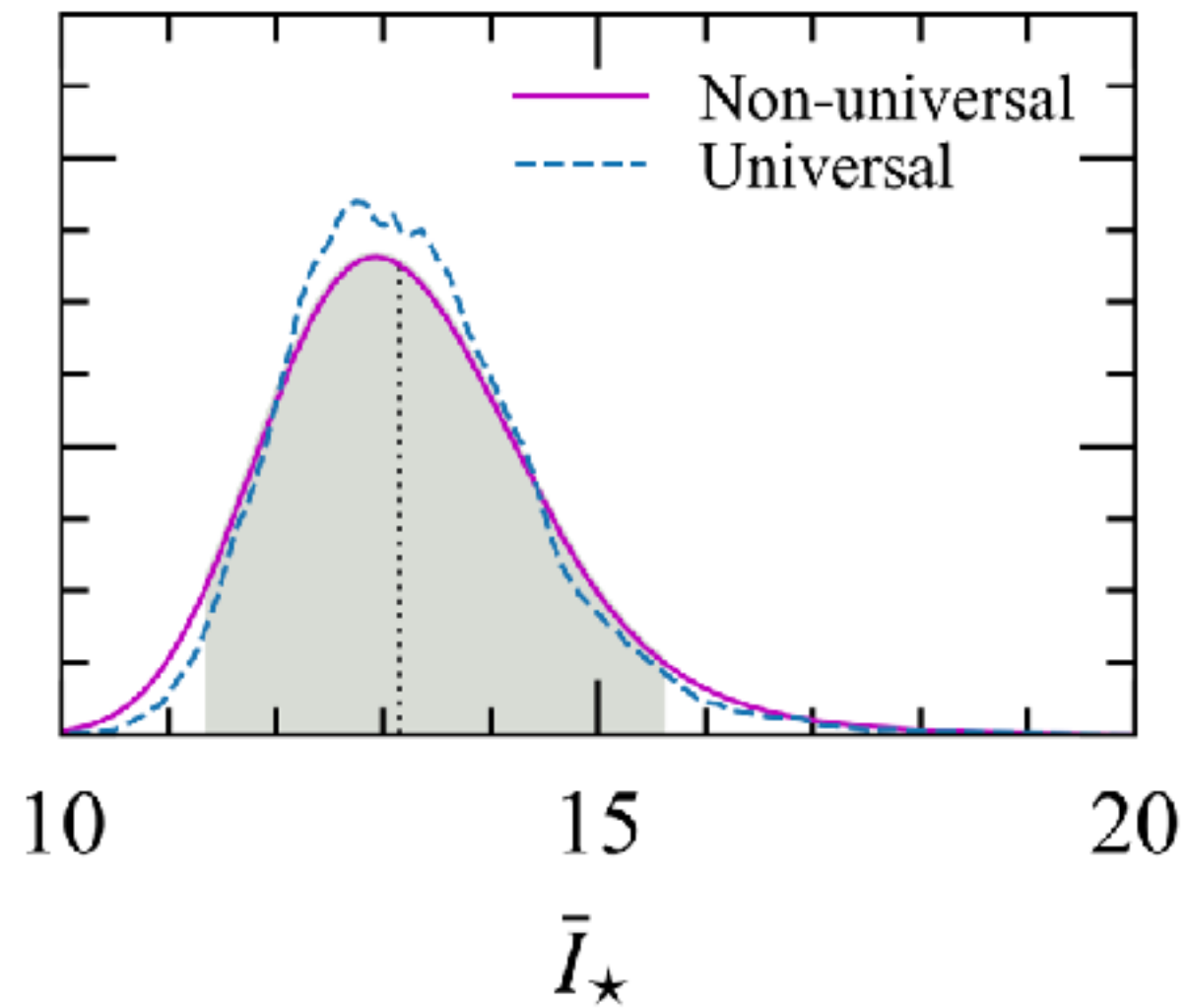


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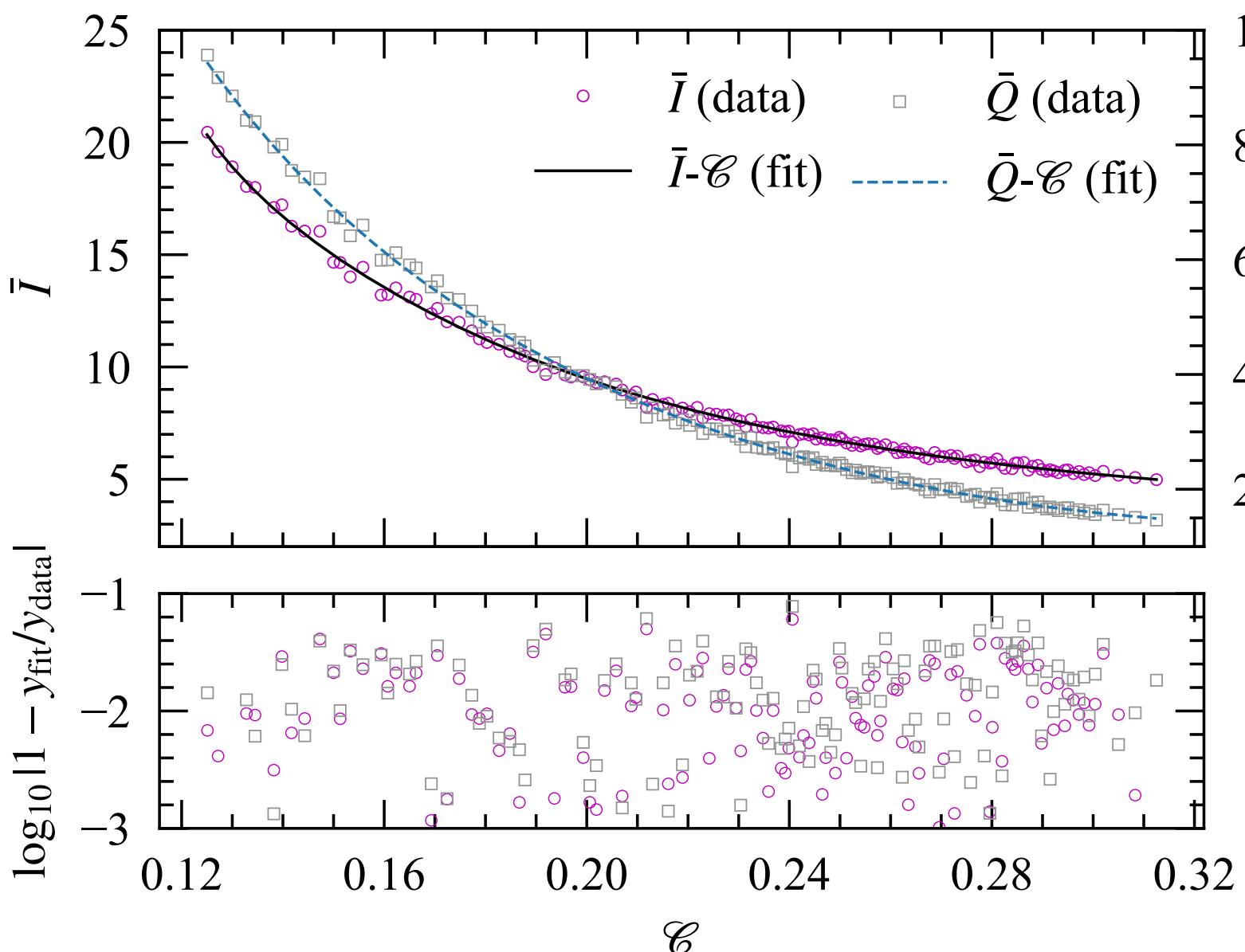
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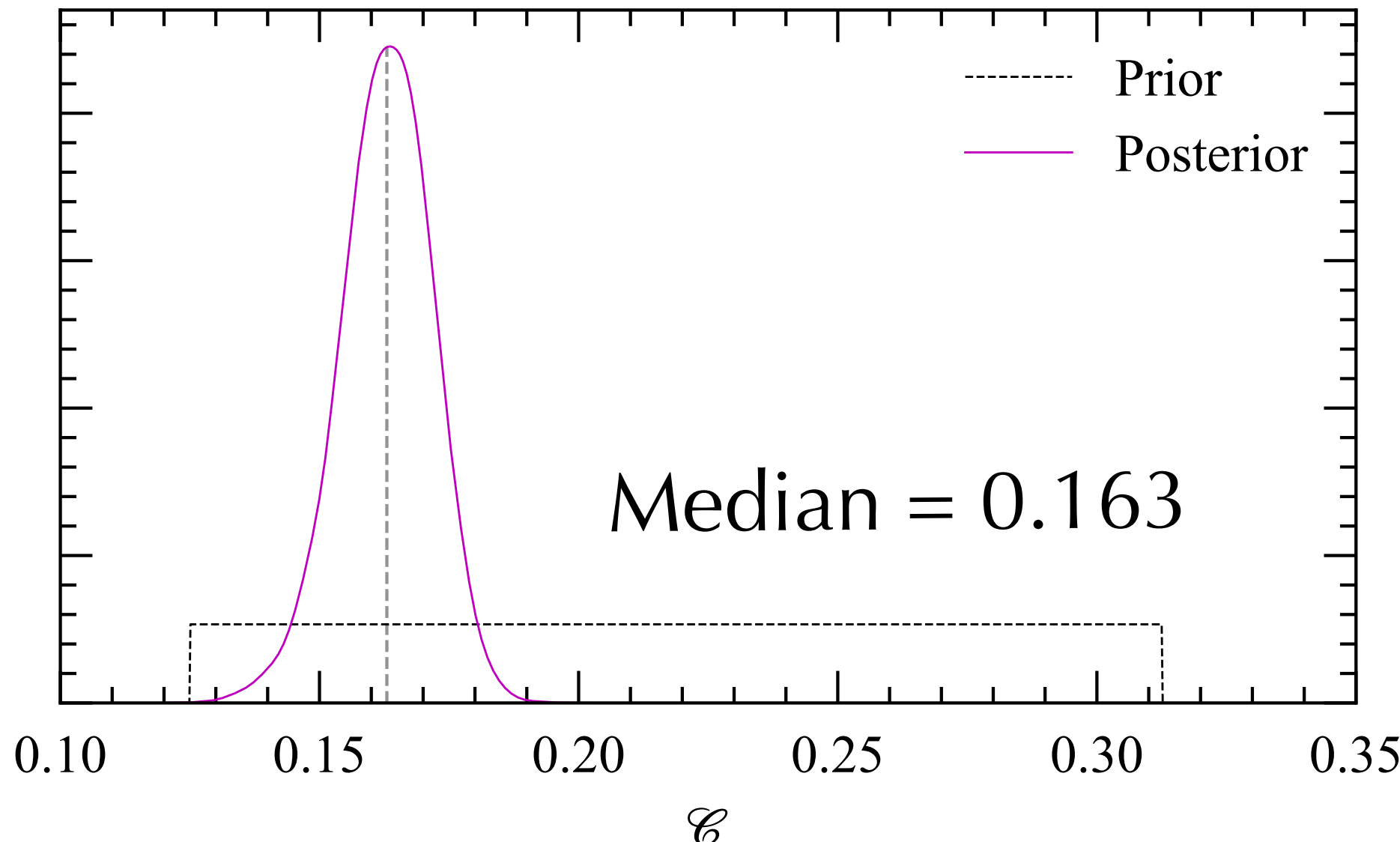
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Posterior



Likelihood



Parameter	Median	<b>PSR J0030+0451</b>	
$\bar{I}_\star$ (10)	1.31	$I_\star$ ( $10^{45}$ g cm <sup>2</sup> )	1.71
$\bar{\lambda}_\star$ ( $10^2$ )	4.97	$Q_\star$ ( $10^{43}$ g cm <sup>2</sup> )	1.49
$\bar{Q}_\star$	5.92	$e_\star$ ( $10^{-1}$ )	1.56

Landry & Kumar (2017)  
Silva, Holgado, **ACA** & Yunes (2020)

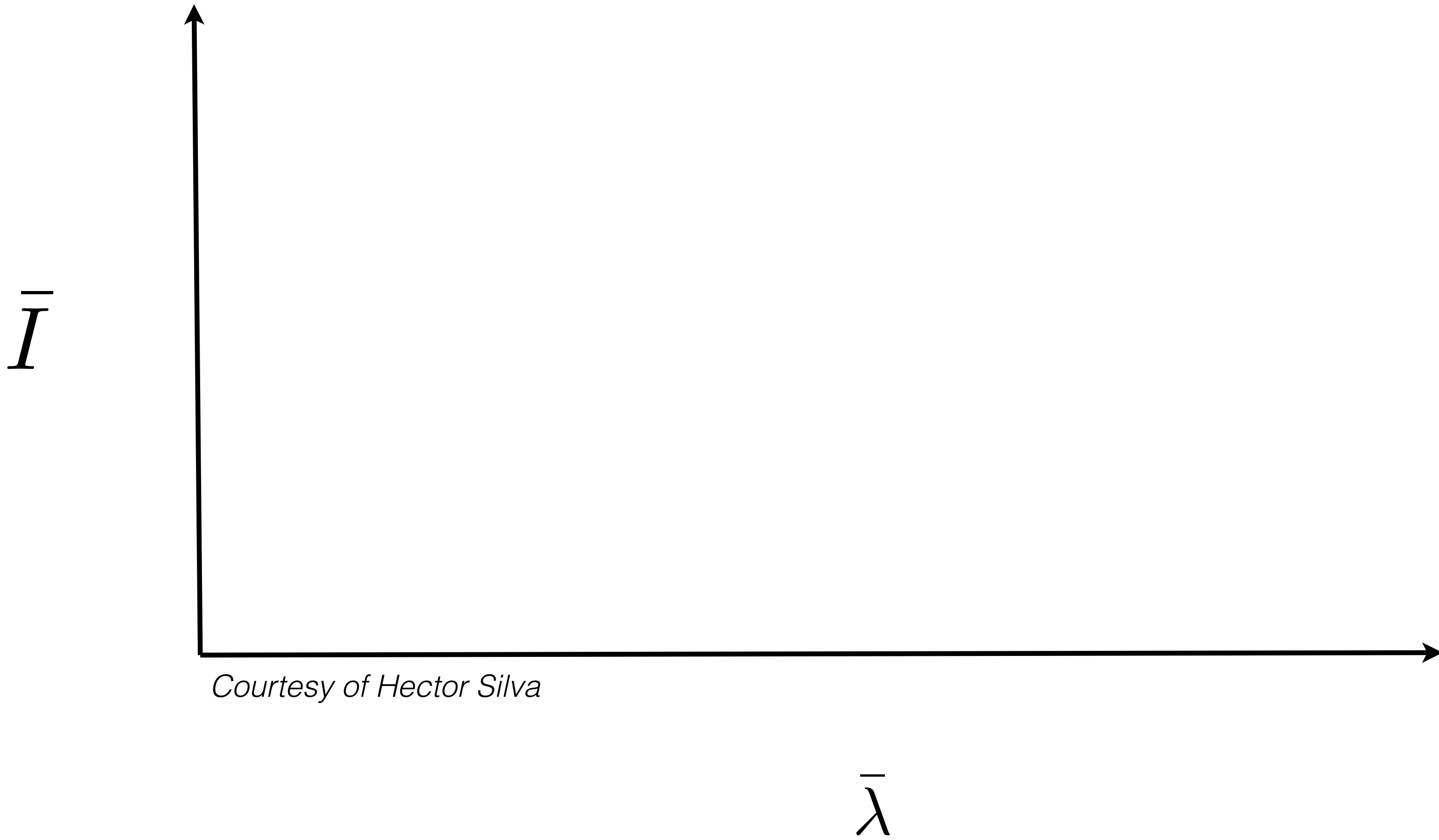
# A multimessenger test of general relativity

*Courtesy of Hector Silva*

Yunes & Yagi (2013), Gupta et al (2018)  
Silva, Holgado, **ACA** & Yunes (2020)



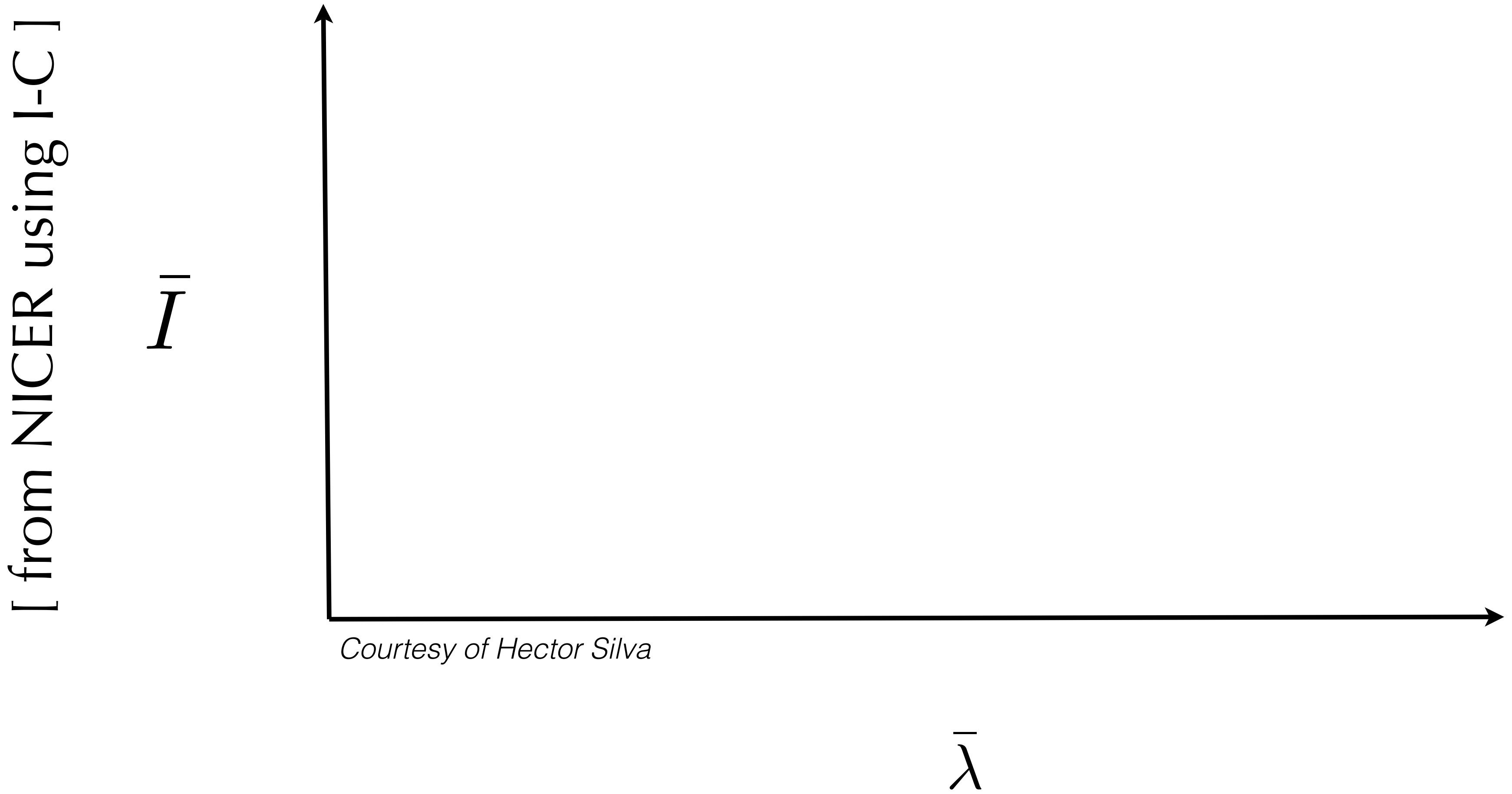
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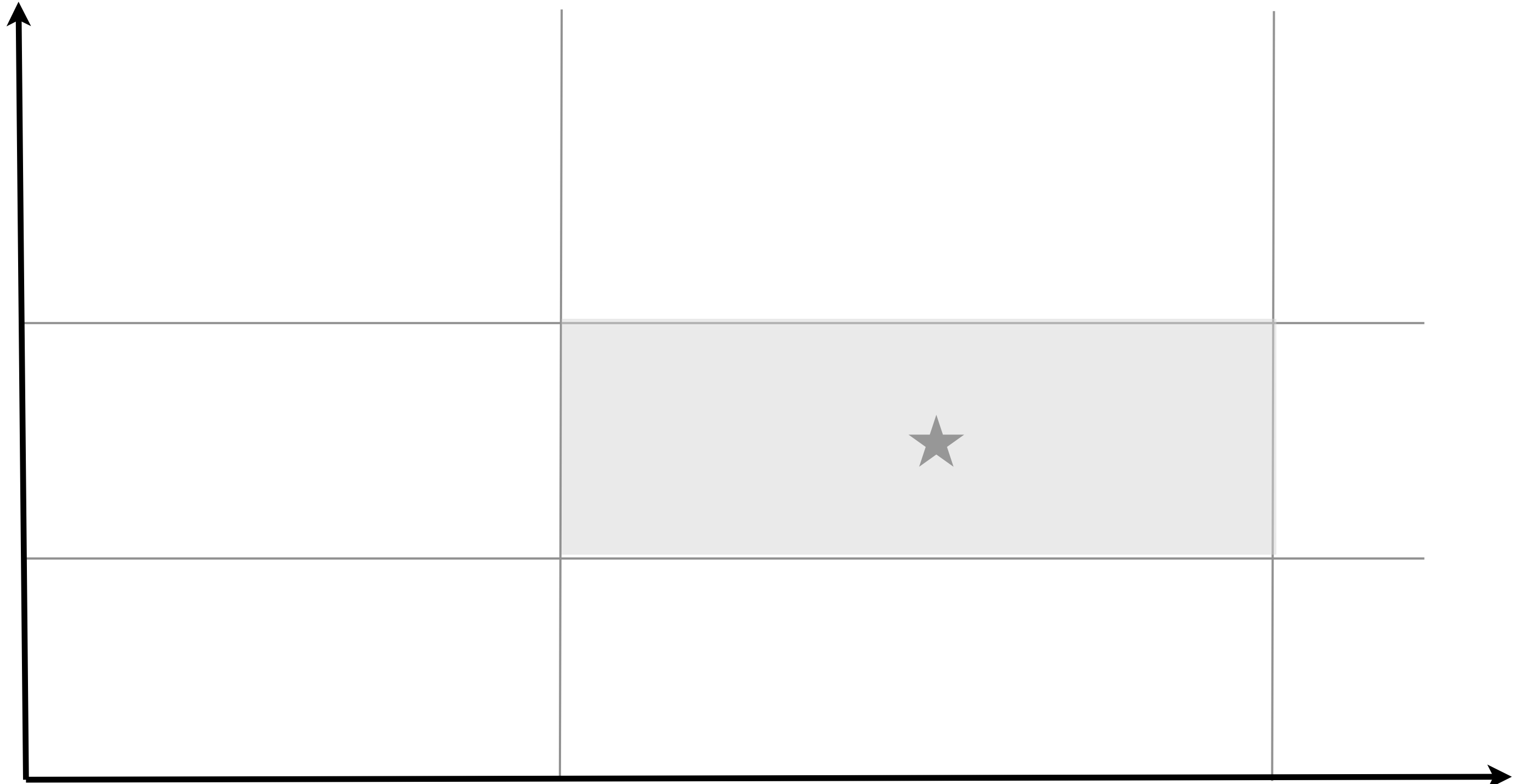
Yunes & Yagi (2013), Gupta et al (2018)  
Silva, Holgado, **ACA** & Yunes (2020)

[ from LIGO / Virgo ]

# A multimessenger test of general relativity

[ from NICER using I-C ]

$\bar{I}$



Courtesy of Hector Silva

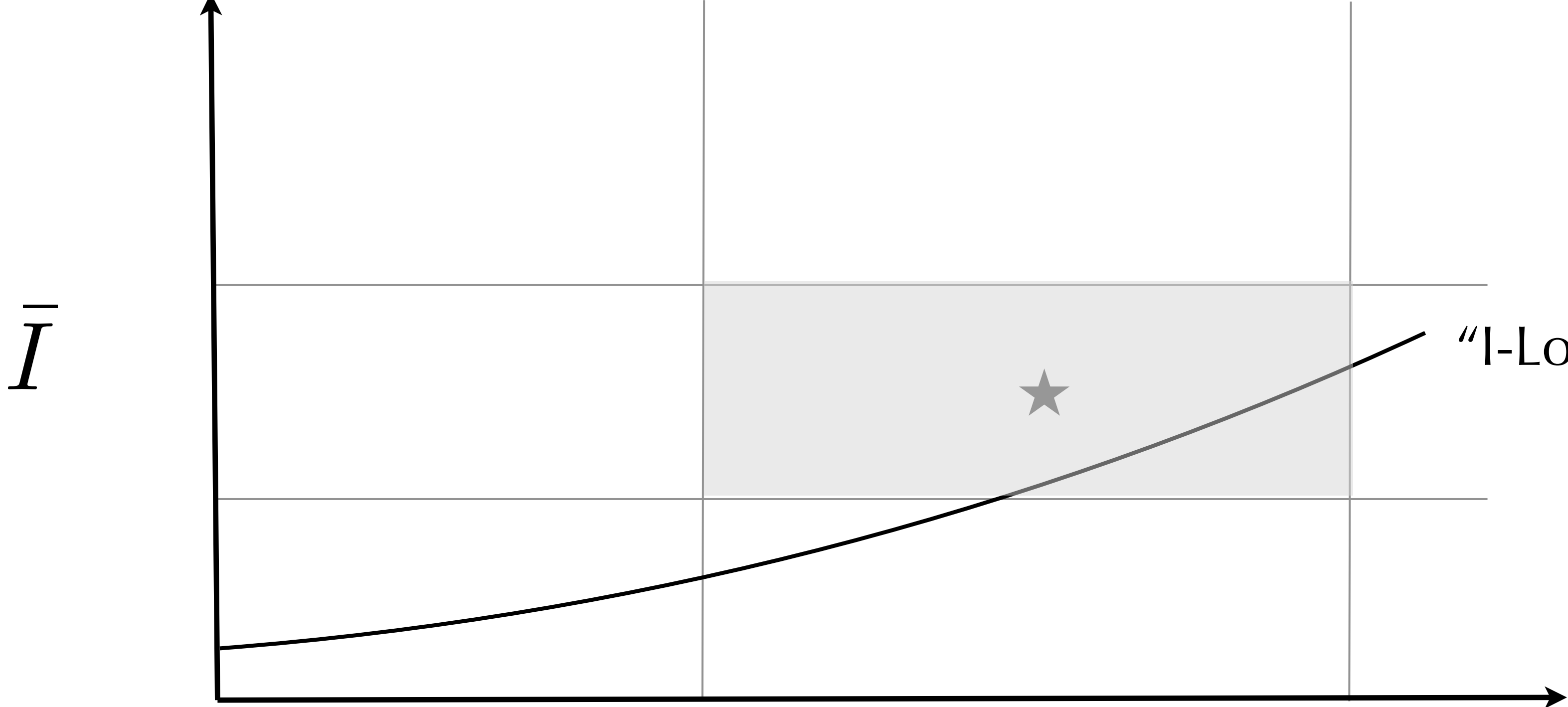
$\bar{\lambda}$

[ from LIGO / Virgo ]

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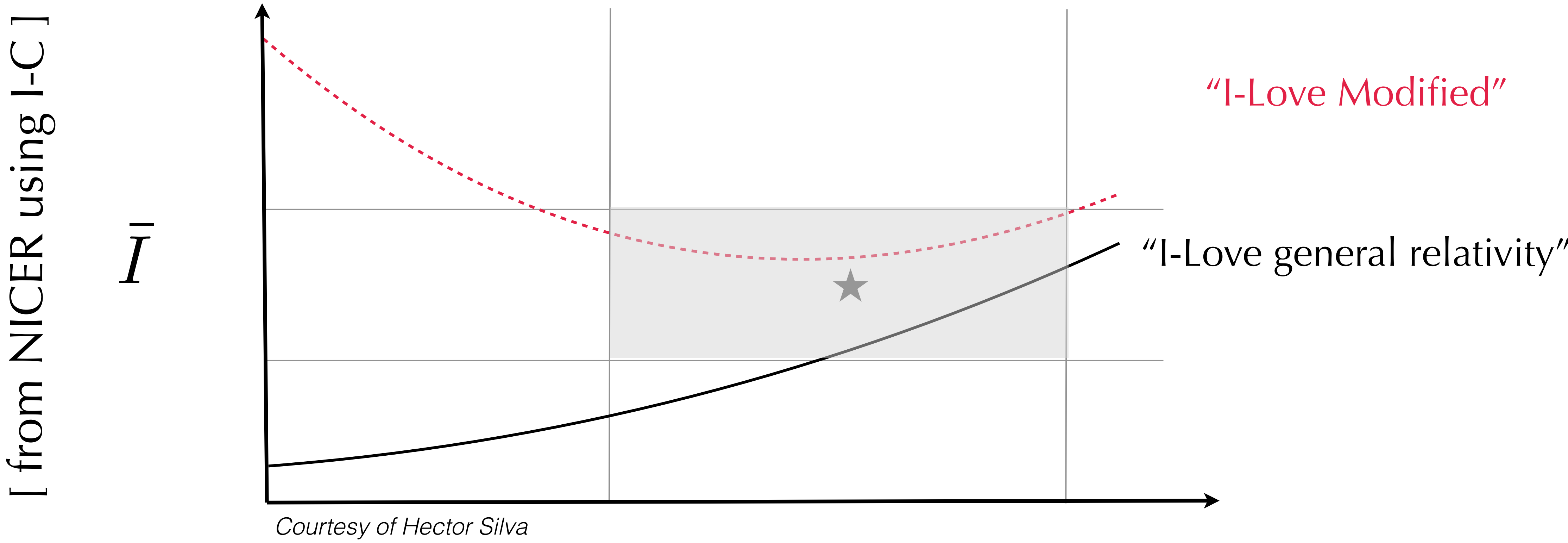


Courtesy of Hector Silva

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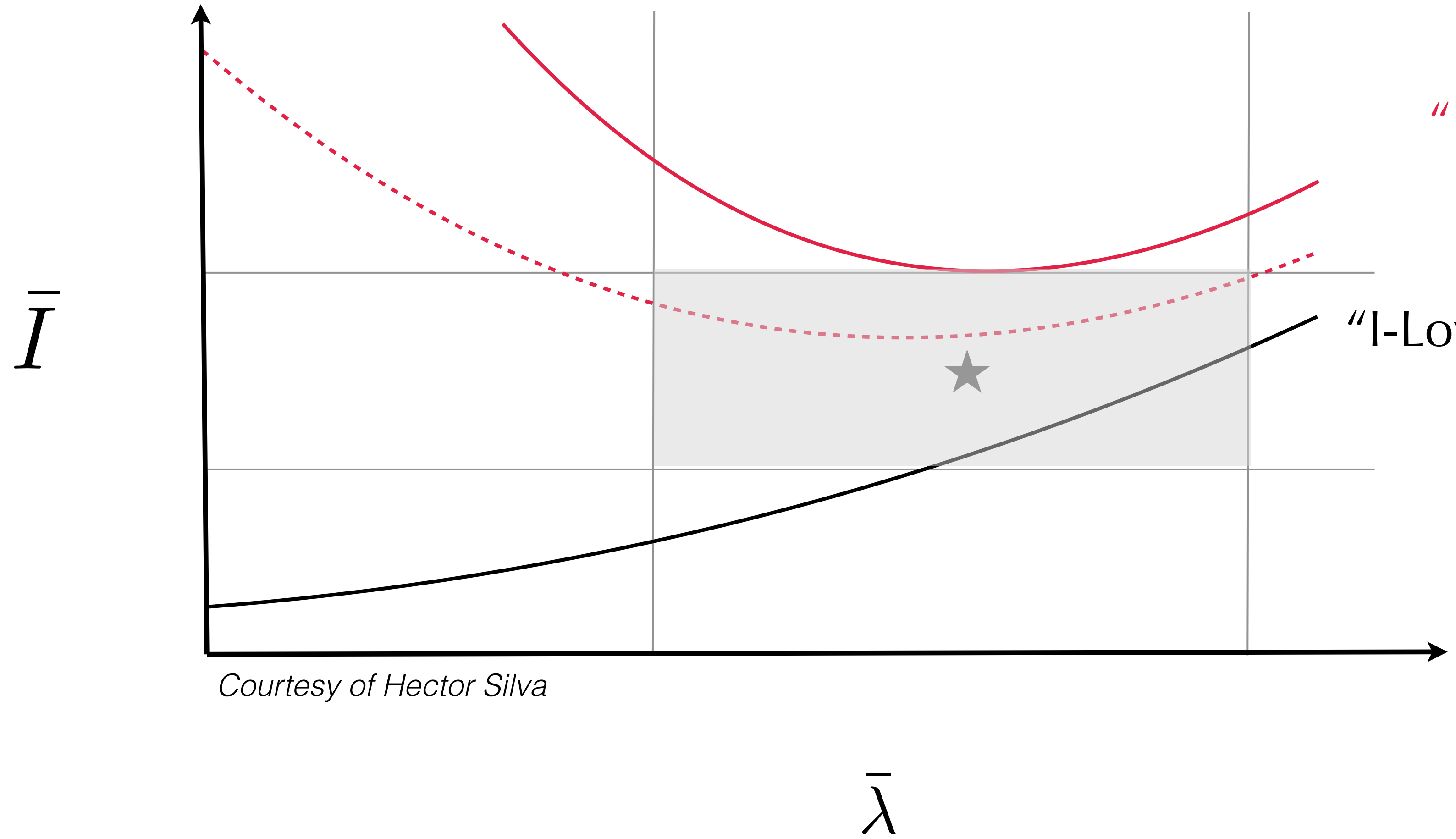
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# «I-Love parametrizations»

Silva, Holgado, **ACA** & Yunes (2020)



# «I-Love parametrizations»

$$\bar{I} = \bar{\lambda}^{2/5} \left[ c_0 + \right]$$

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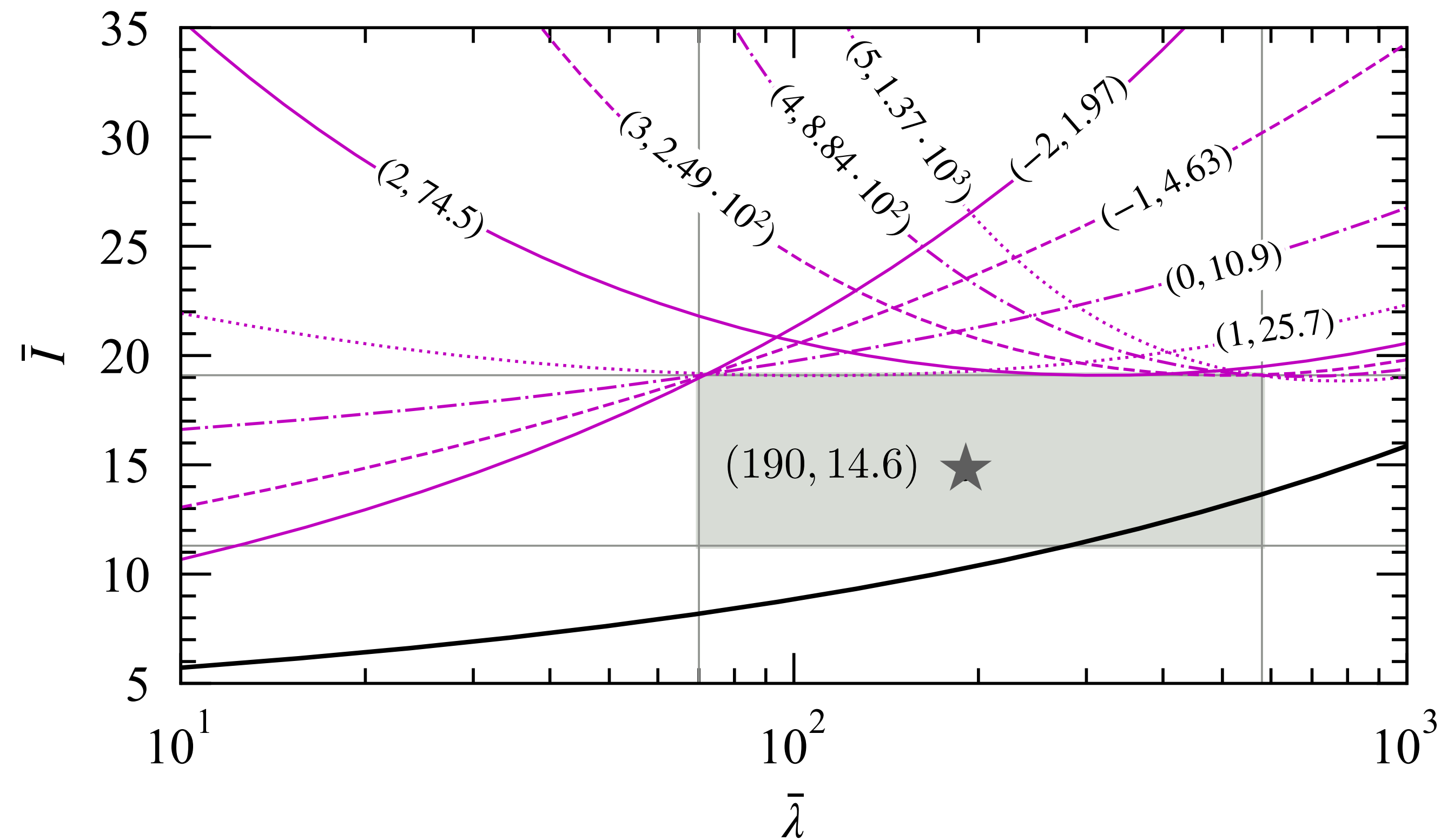
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Newtonian

post-Minkowskian

non-GR



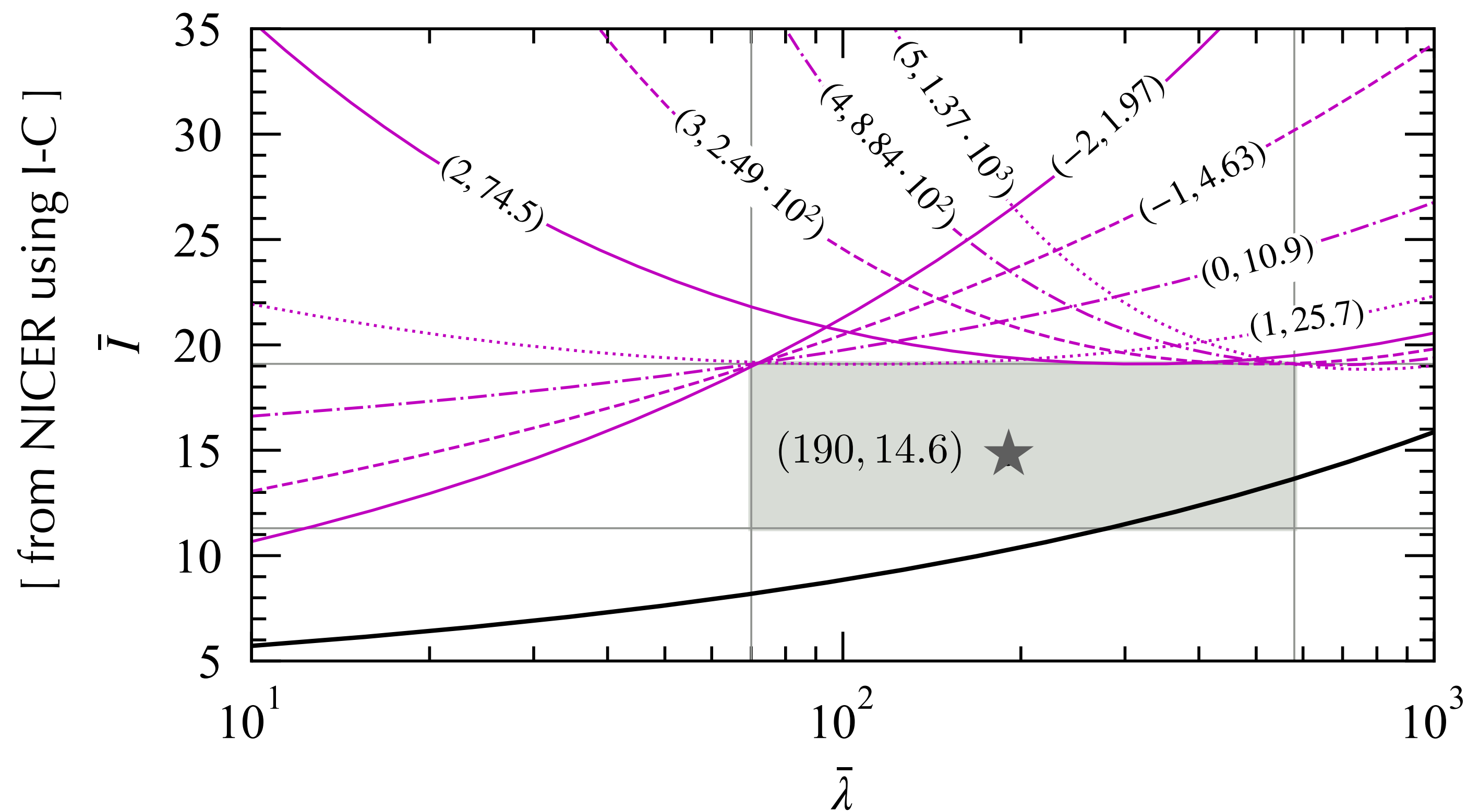
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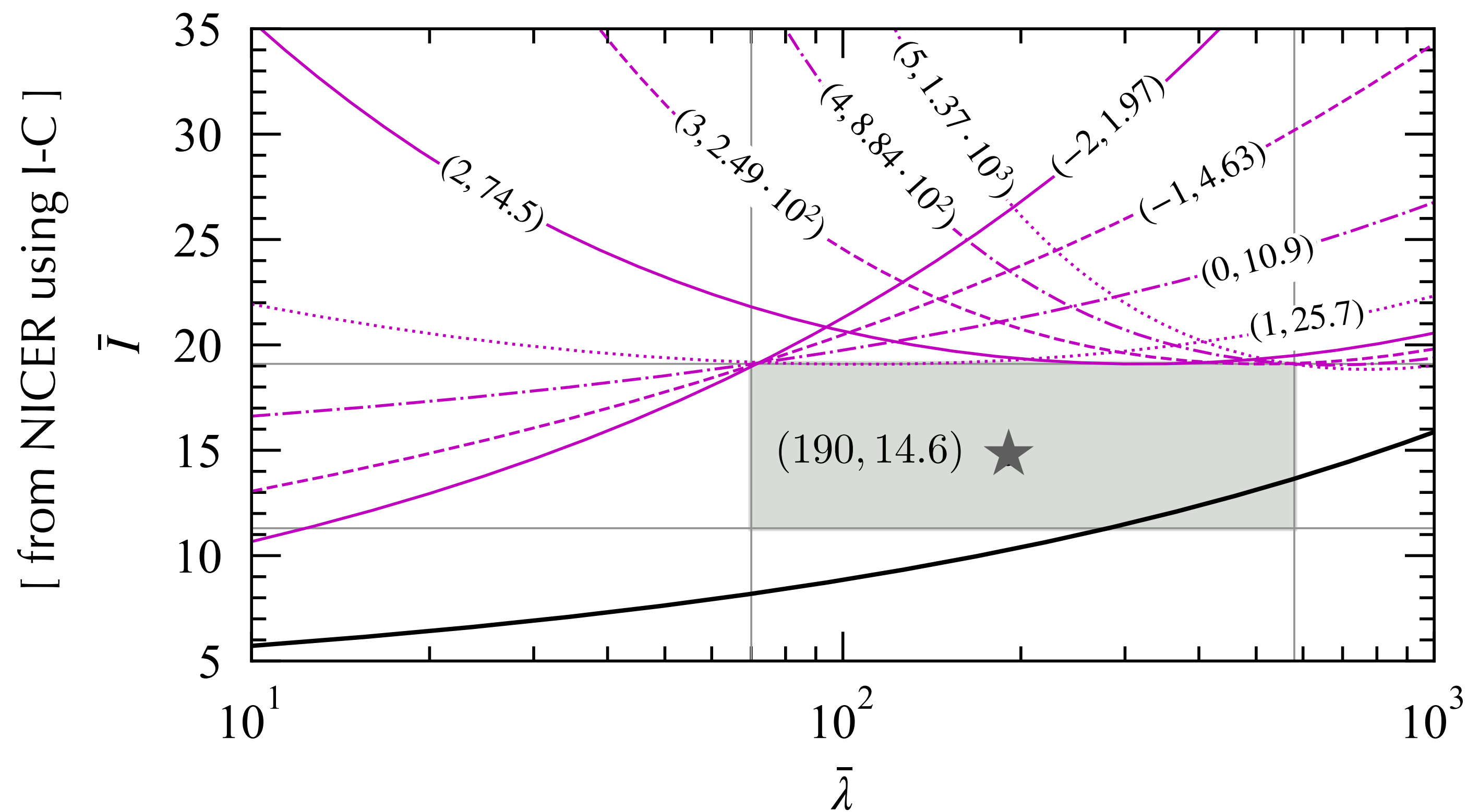
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post-Minkowskian

non-GR



$$\beta_{\text{CS}} \approx 3 \left( \alpha_{\text{CS}} / M^2 \right)^2, \quad b_{\text{CS}} = 4$$

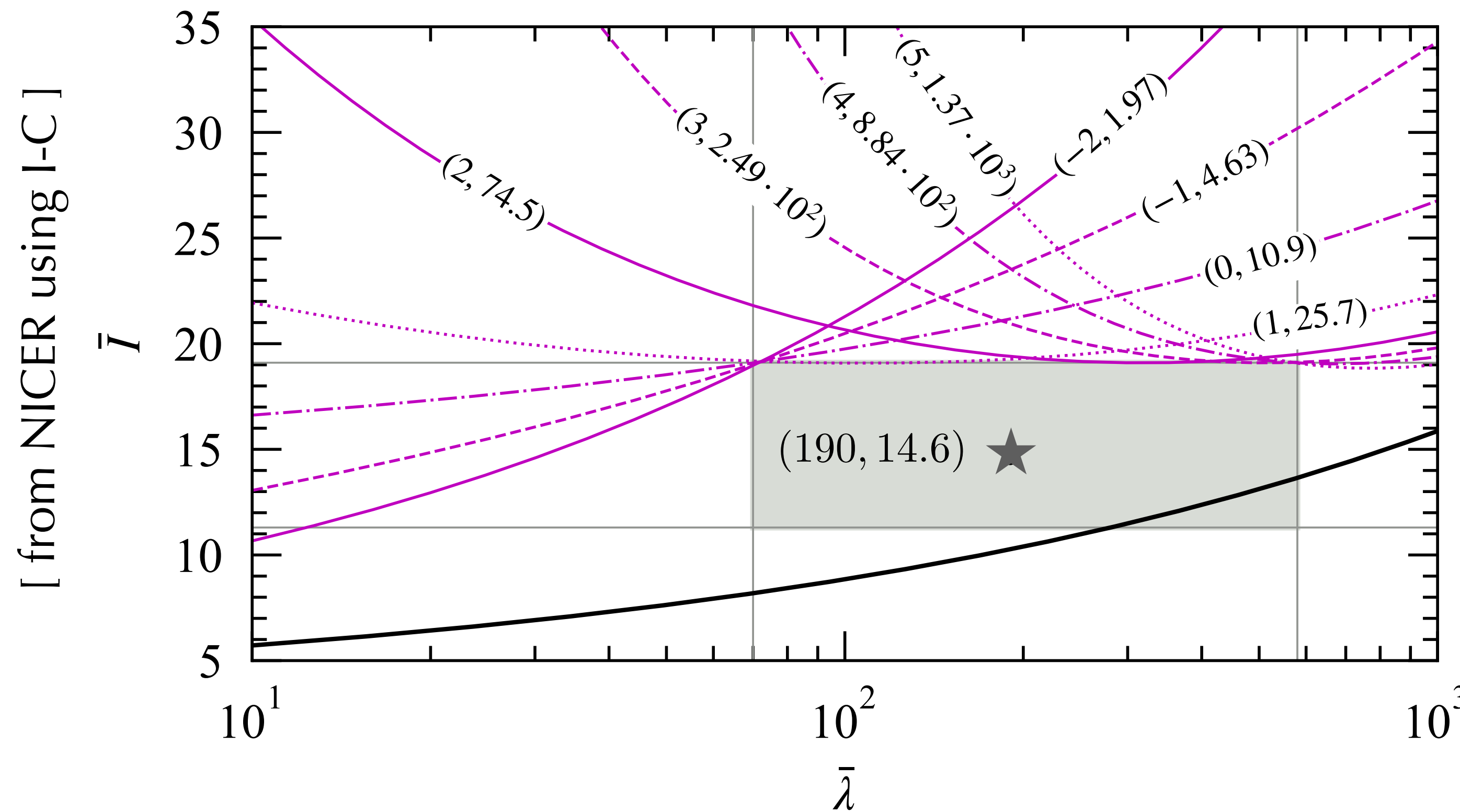
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Newtonian

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non-GR



$$\sqrt{\alpha_{\text{CS}}} \leq 8.5 \text{ km} \ll 10^8 \text{ km}$$

$$\beta_{\text{CS}} \approx 3 (\alpha_{\text{CS}}/M^2)^2, \quad b_{\text{CS}} = 4$$



# Conclusions

- We derived the first measurements of the **moment of inertia**, the **quadrupole moment**, the **surface eccentricity** and the **Love number** of an isolated neutron star.
- We performed the first **theory-agnostic** and **equation-of-state independent** test of general relativity
- Consistency with general relativity places the **most stringent constraint** on **gravitational parity violation** to date

Thank you!

*More details:  
[arXiv:2004.01253](https://arxiv.org/abs/2004.01253)*

# Backup

# Precision Tests of General Relativity

**Theory-Specific:**

**Theory-Agnostic:**

# Precision Tests of General Relativity

## Theory-Specific:

- e.g., *Extra Scalar Field, Lorentz-violating, Massive Gravity, Nondynamical fields*

*c.f., Berti, et. al., CQG Topical Review (2015)  
K.Yagi & L. C. Stein, CQG Focus Issue(2016)*

## Theory-Agnostic:

# Precision Tests of General Relativity

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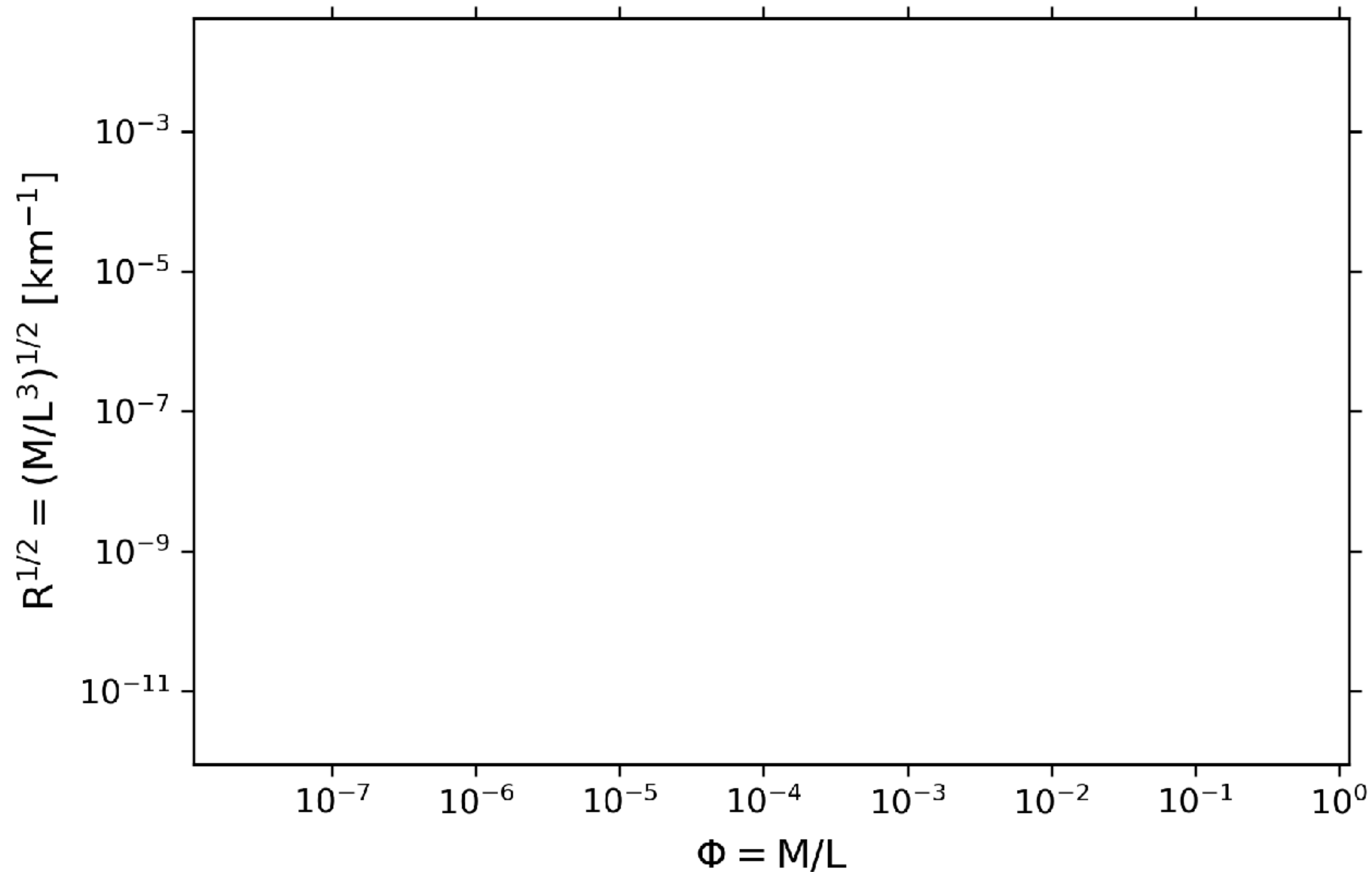
## Theory-Agnostic:

*Will & Nordtvedt (1972)*

- Parameterized post-Newtonian (PPN)
- **Bumpy BHs** *Ryan (1995); Collins & Hughes (1995)*
- Parameterized Post-Einsteinian (PPE)

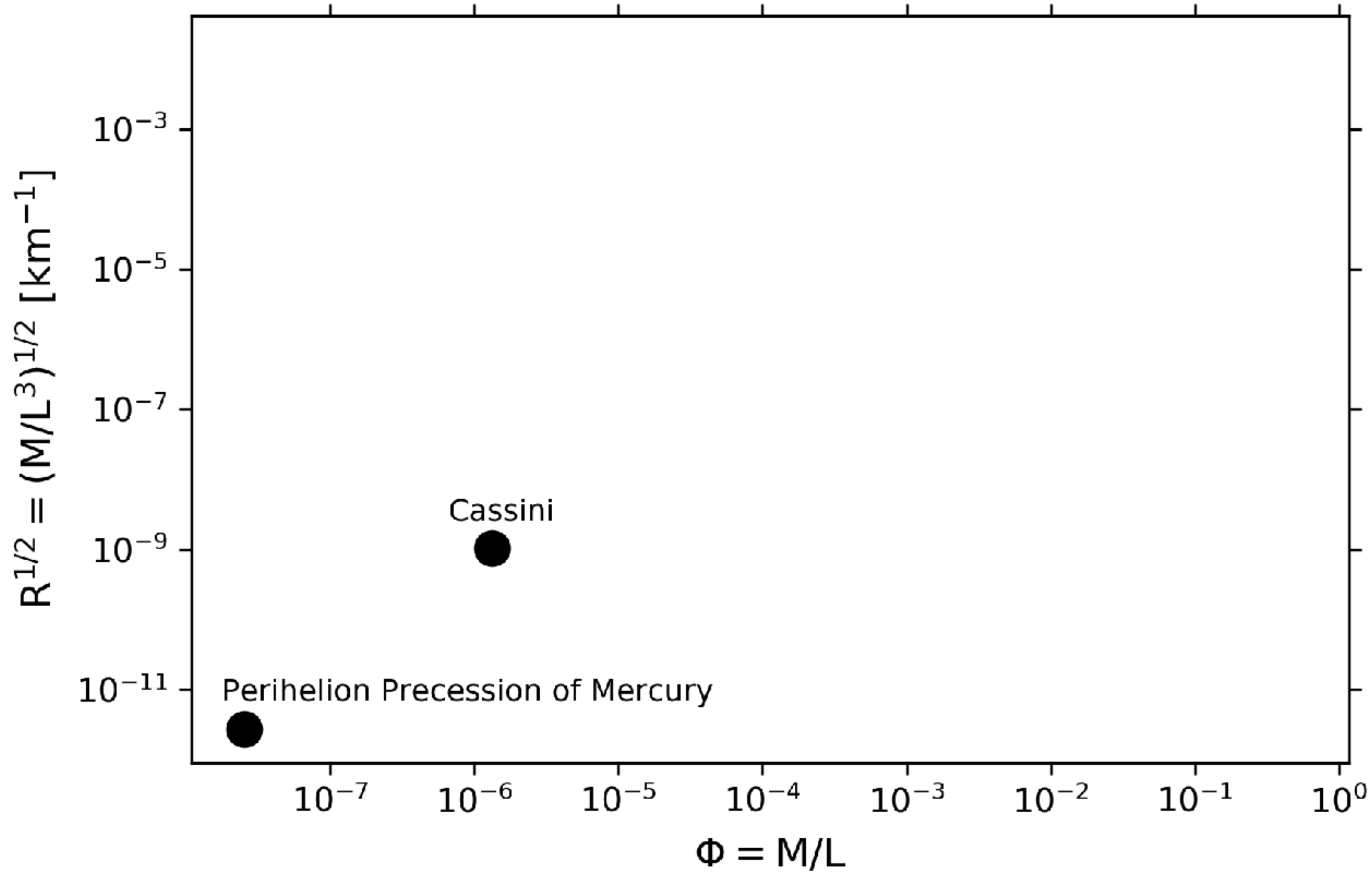
*Yunes & Pretorius (2009)*

# The strong-field regime



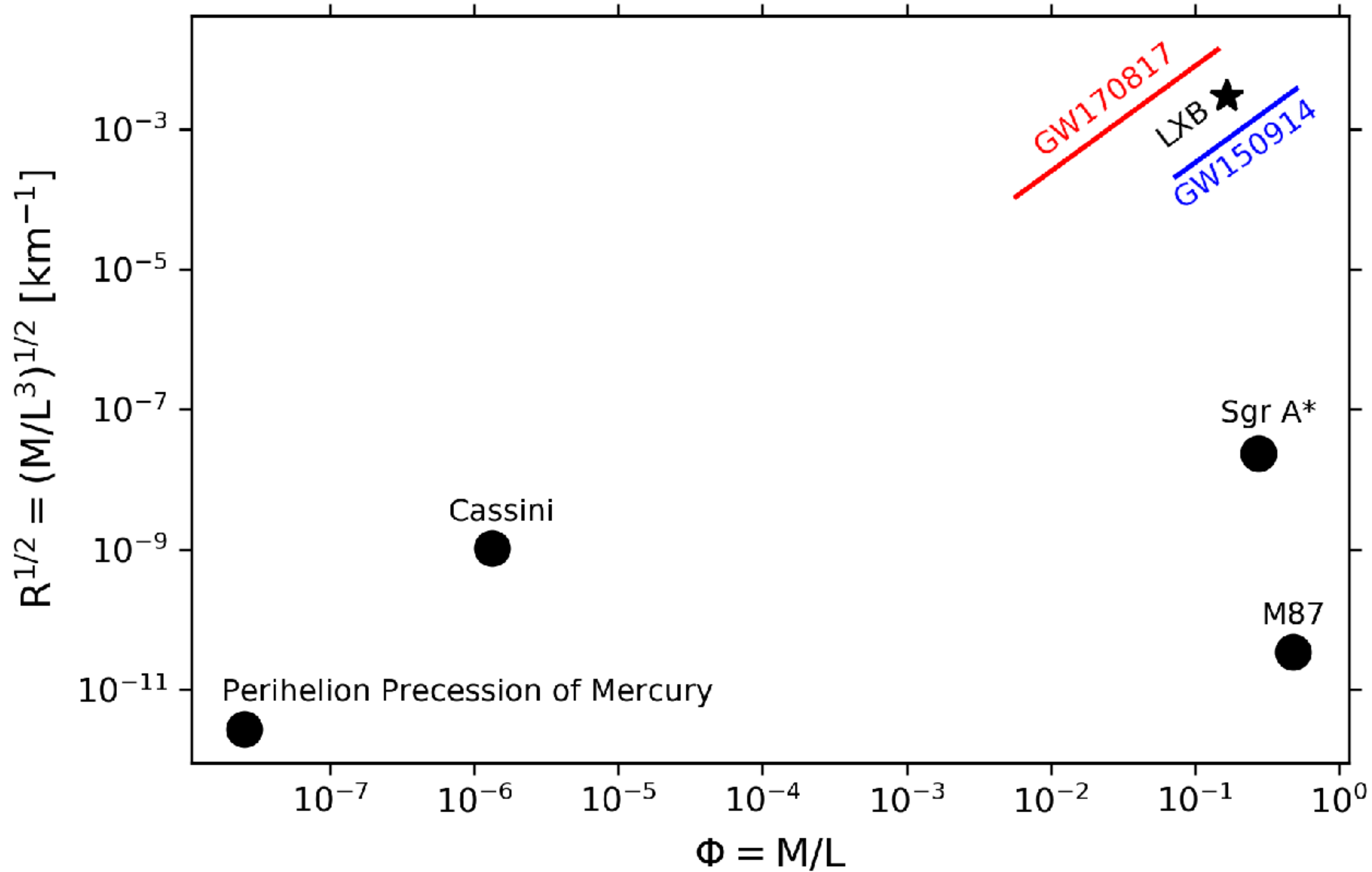
*c.f., Psaltis (2008)  
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