

Singlet-doublet Dirac dark matter and neutrino masses

Andrés Felipe Rivera R. (UdeA)

In collaboration with **Diego Restrepo** (UdeA -COL), **Walter Tangarife** (LUC -USA)

Based on [PHYSICAL REVIEW D 100, 035029 \(2019\)](#)

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Bogotá, Colombia





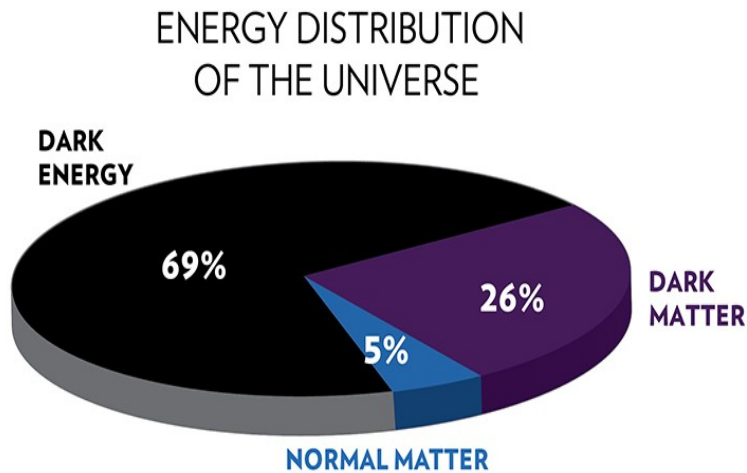
Outline

- 1 Overview: problems - neutrino **Majorana** vs **Dirac**
- 2 The Dirac model
 - DM candidate
 - Neutrino masses
 - Predictions
- 3 Numerical results
- 4 **Majorana** vs **Dirac** model
- 5 Conclusions



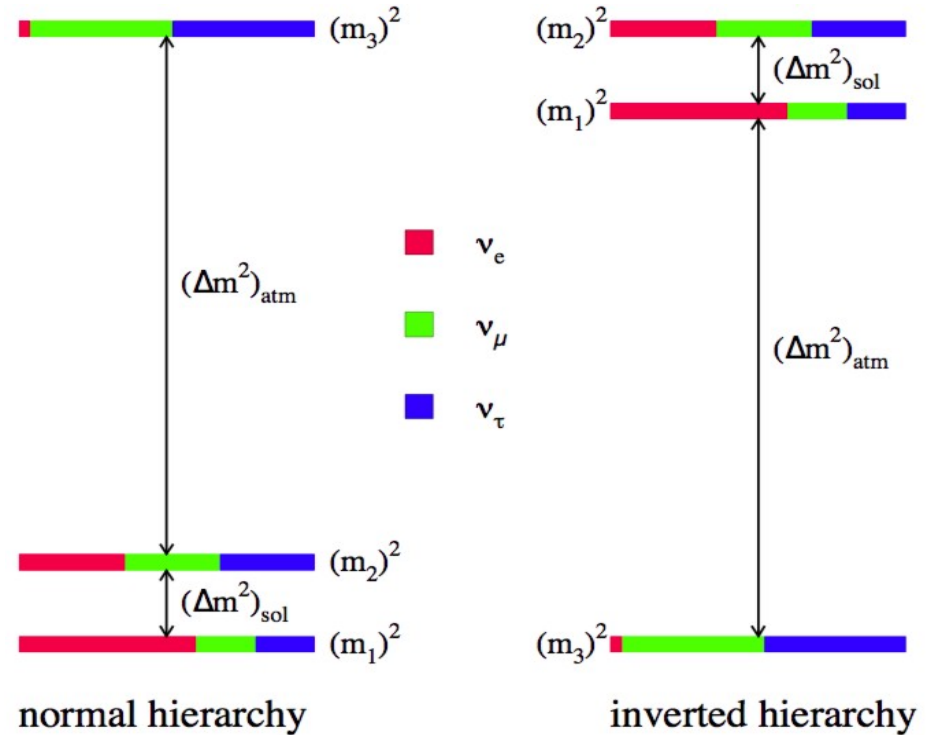
1. Problems

Dark matter



<https://chandra.harvard.edu>
Planck 2018

Neutrinos masses



ARXIV:1307.5487



Scotogenic models

Ma,
Phys.Rev.D73:077301,2006



Singlet-doublet: Majorana case

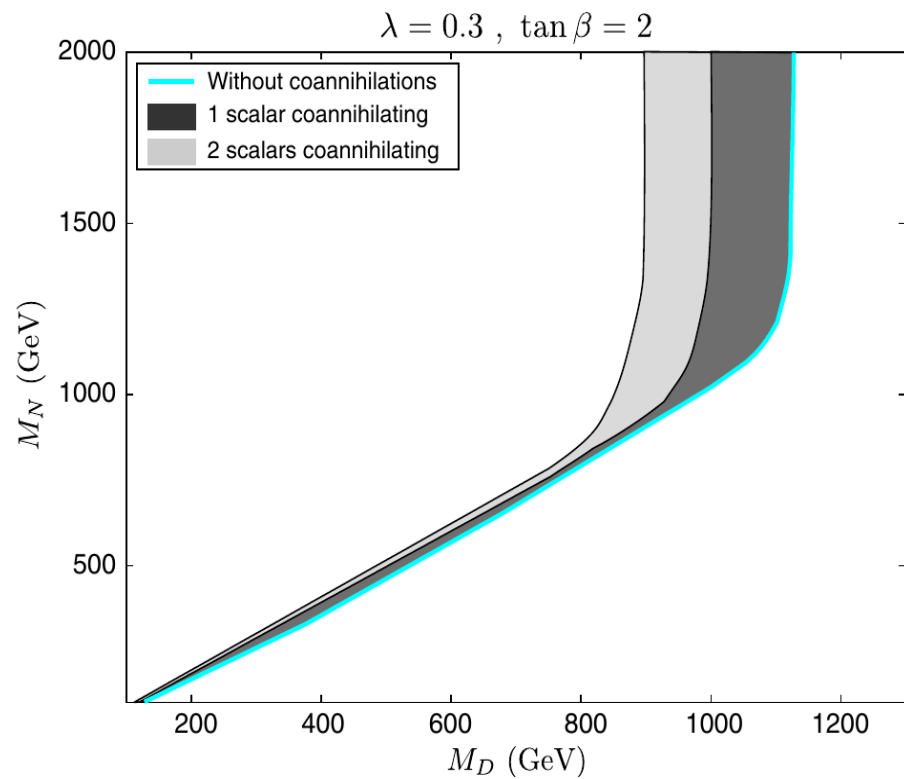
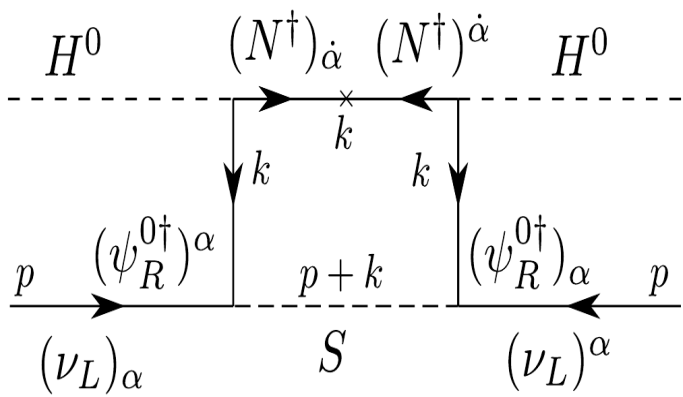
~MSSM ~ Bino-higgsino

$$\mathcal{L} \supset M_D \epsilon_{ab} R_d^a \tilde{R}_u^b - \frac{1}{2} M_N N N + \text{h.c}$$

Neutrinos (Weinberg operator)

PRD 43.1566 (1979)

$$\mathcal{L} = \Lambda^{d=5} \bar{L}^c \tilde{H}^* H L$$

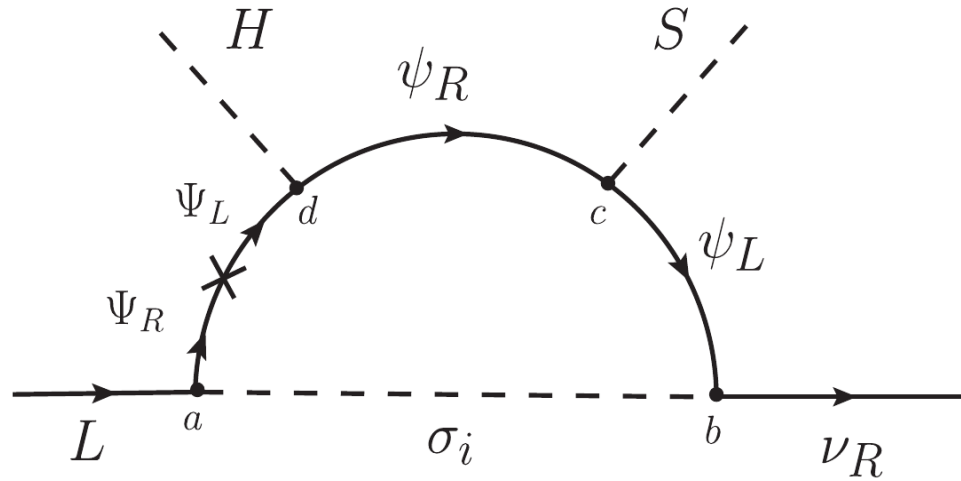


PRD 92, 013005 (2015)

2. Dirac case

$$\mathcal{L}_5^D = -\frac{g_{\alpha\beta}}{\Lambda} \bar{L}_\alpha \tilde{H} \nu_{R\beta} S + \text{H.c.}$$

PRD 97, 095092 (2018)



$$= \sum_{i=1}^2 h_b^{\alpha i} \times \Lambda_i \times h_a^{\beta i}$$

$$\mathcal{M}_{\alpha\beta} = (U_{\text{PMNS}})_{\alpha\beta} (m_\nu)_\beta$$

The new model: SDFDM

Particle content

Leptons and scalars fields	$(\text{SU}(2)_L, \text{U}(1)_Y)$	\mathbb{Z}_2 (DM)	\mathbb{Z}'_2	$U(1)_{B-L}$
$L_\beta = \begin{pmatrix} \nu_L \\ l_L \end{pmatrix}_\beta$	$(2, -1/2)$	+	+	-1
l_R^α	$(1, 0)$	+	+	-1
$H = (H^+, \frac{h^0+v}{\sqrt{2}})^T$	$(2, 1/2)$	+	+	0
S	$(1, 0)$	+	-	0
σ_i	$(1, 0)$	-	-	0
ψ_L	$(1, 0)$	-	+	-1
ψ_R	$(1, 0)$	-	-	-1
$\Psi = \begin{pmatrix} \Psi^0 \\ \Psi^- \end{pmatrix}$	$(2, -1/2)$	-	-	-1
ν_R^α	$(1, 0)$	+	-	-1

L and V

$$\mathcal{L} \supset -M_\Psi \bar{\Psi} \Psi - V(H, \sigma_i, S) \\ + [h_a^{\beta i} \bar{L}_\beta \Psi \sigma_i + h_b^{\alpha i} \bar{\psi}_L \nu_{R\alpha} \sigma_i + h_c \bar{\psi}_R \Psi_L S \\ + h_d \bar{\Psi} \tilde{H} \psi_R + \text{H.c.}],$$



Radiative
neutrino masses

$$V(H, \sigma_i, S) = -\mu^2 H^\dagger H + \frac{\lambda_1}{2} (H^\dagger H)^2 + \frac{1}{2} m_{\sigma_i}^2 \sigma_i^2 \\ + \lambda_i^{\sigma H} H^\dagger H \sigma_i^2 + \frac{\lambda_i^\sigma}{2} \sigma_i^4 + \frac{1}{2} m_S^2 S^2 \\ + \lambda_{SH} H^\dagger H S^2 + \lambda^{S\sigma_i} S^2 \sigma_i^2 + \frac{\lambda^S}{2} S^4.$$



Higgs Mixing

- EWPT: STU

$$\mathcal{L} \supset \frac{h_1 \cos \alpha + h_2 \sin \alpha}{v} \times \left(2m_W^2 W_\mu^+ W^{\mu-} + m_Z^2 Z_\mu Z^\mu - \sum_f m_f \bar{f} f \right)$$

- DM particle

$$m_{\psi^0} = \begin{pmatrix} M_\Psi & \frac{h_d v}{\sqrt{2}} \\ 0 & M_N \end{pmatrix}$$

Where: $M_N = h_c v_S / \sqrt{2}$

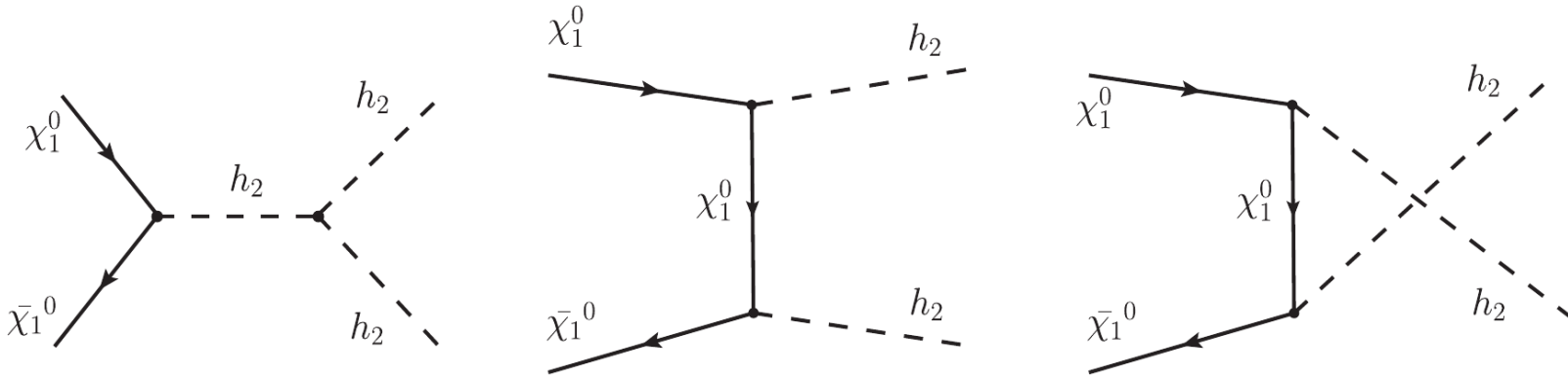
- Bi-unitary diagonalization

$$V^* m_{\psi^0} U^\dagger = m_{\chi_i^0}^{\text{diag}} \quad \rightarrow \quad \chi_j^0 = (\chi_L, \chi_R^\dagger)_j$$

χ_1^0, χ_2^0

Dark matter

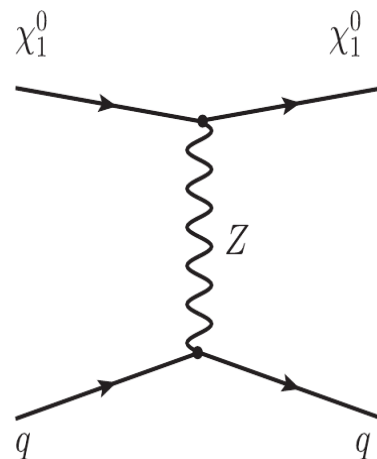
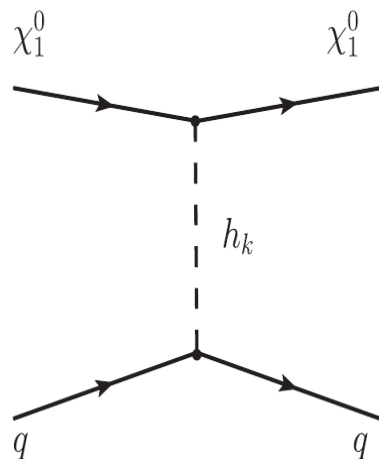
New channel $\chi_1^0 \bar{\chi}_1^0 \rightarrow h_2 h_2$



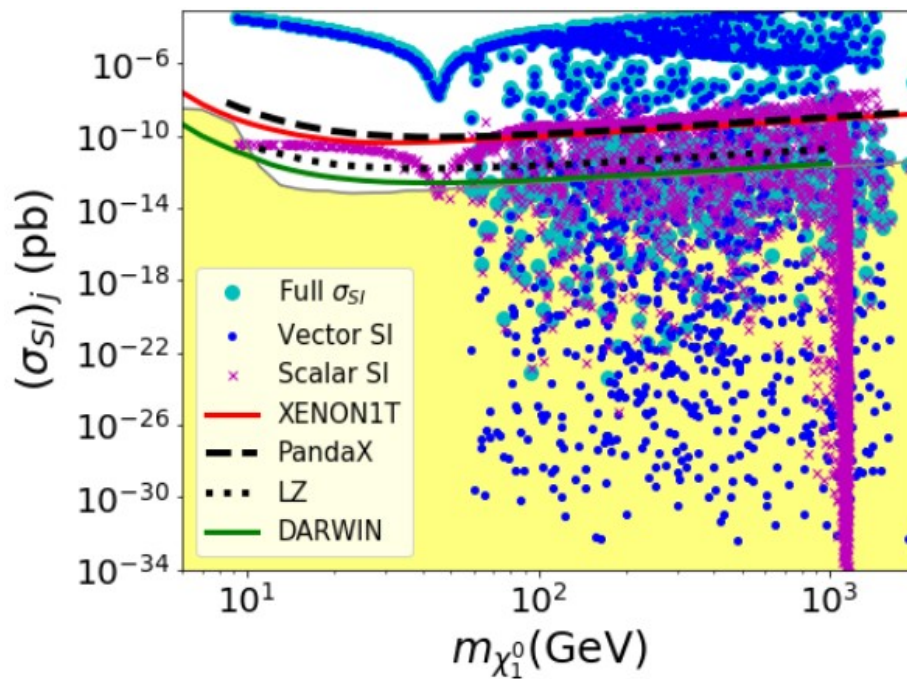
$$\Omega_\chi h^2 \approx 2 \frac{1.04 \times 10^9 x_f}{M_{\text{Pl}} \sqrt{g_*(m_\chi)} (a + 3b/x_f)}$$

$$\langle \sigma v \rangle \approx a + bv^2 + \mathcal{O}(v^4)$$

Direct detection



$$\sigma_N^{\text{SI}} = \sigma_{N,e}^{\text{SI}} + \sigma_{N,o}^{\text{SI}}$$



3. Numerical results



Comput. Phys. Commun.
185, 1773 (2014)

Comput. Phys. Commun.
176, 367 (2007)

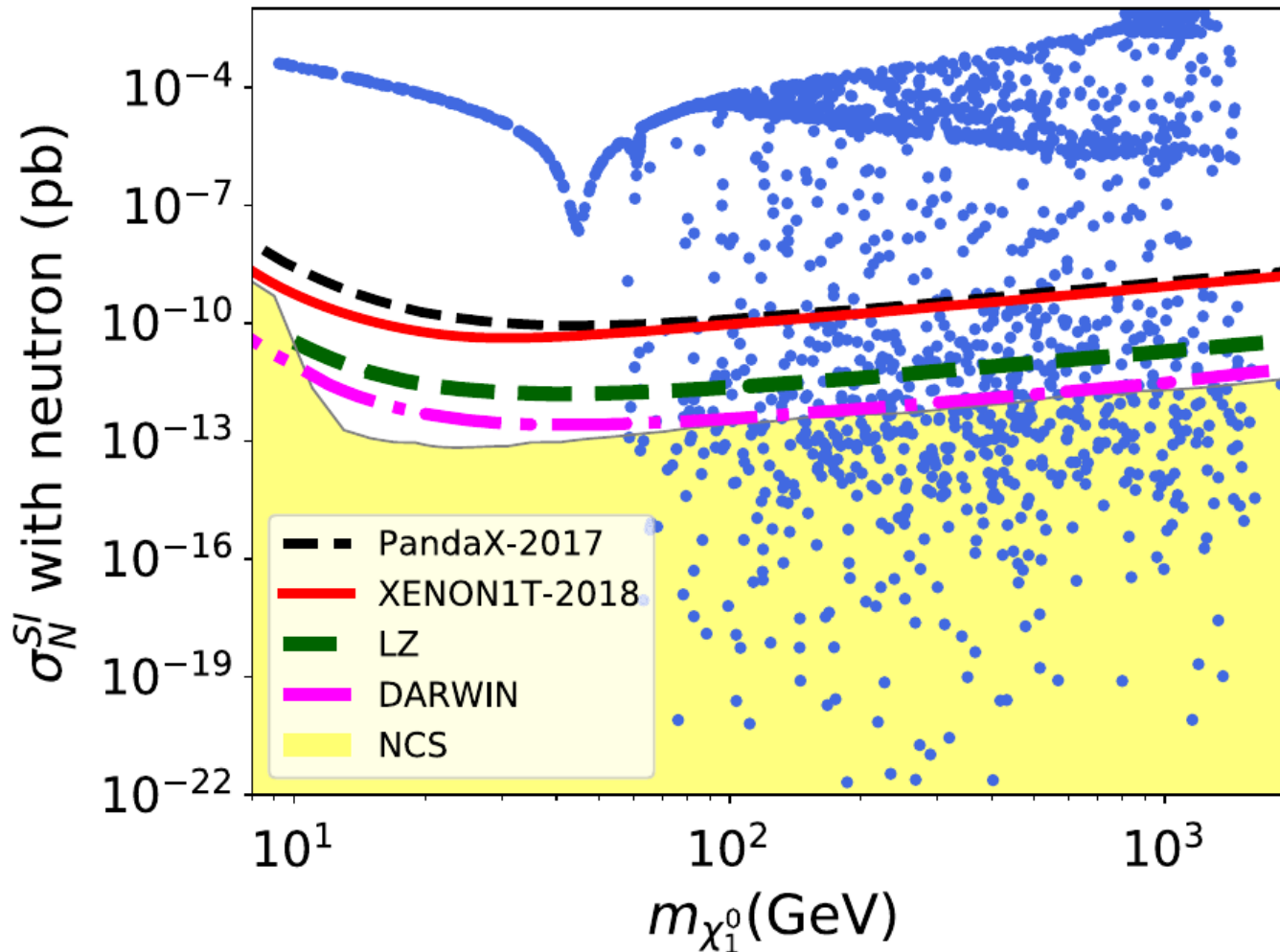
Comput. Phys. Commun. 183,
2458 (2012)

Scan: SHARA + MicrOmegas + SPHENO

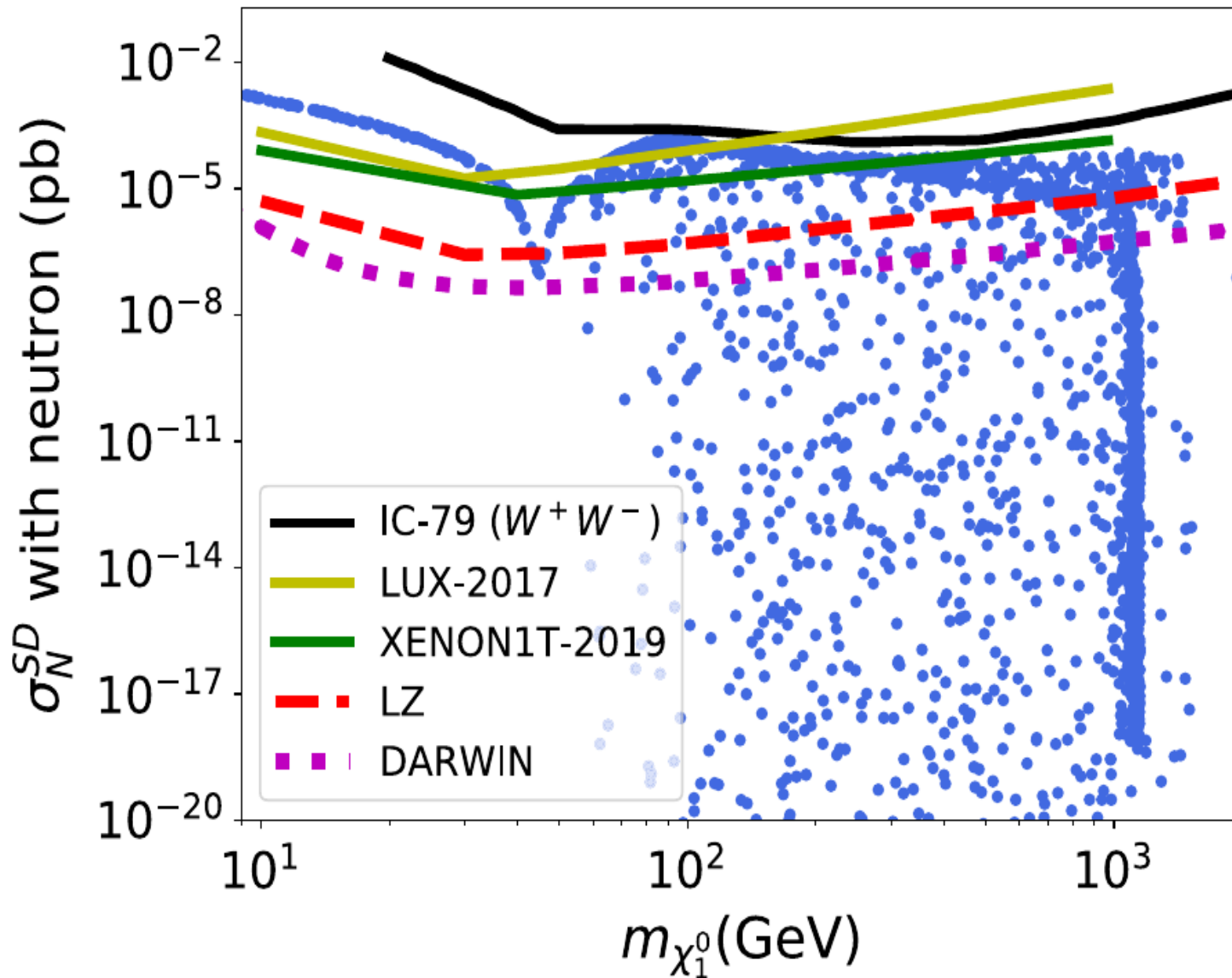


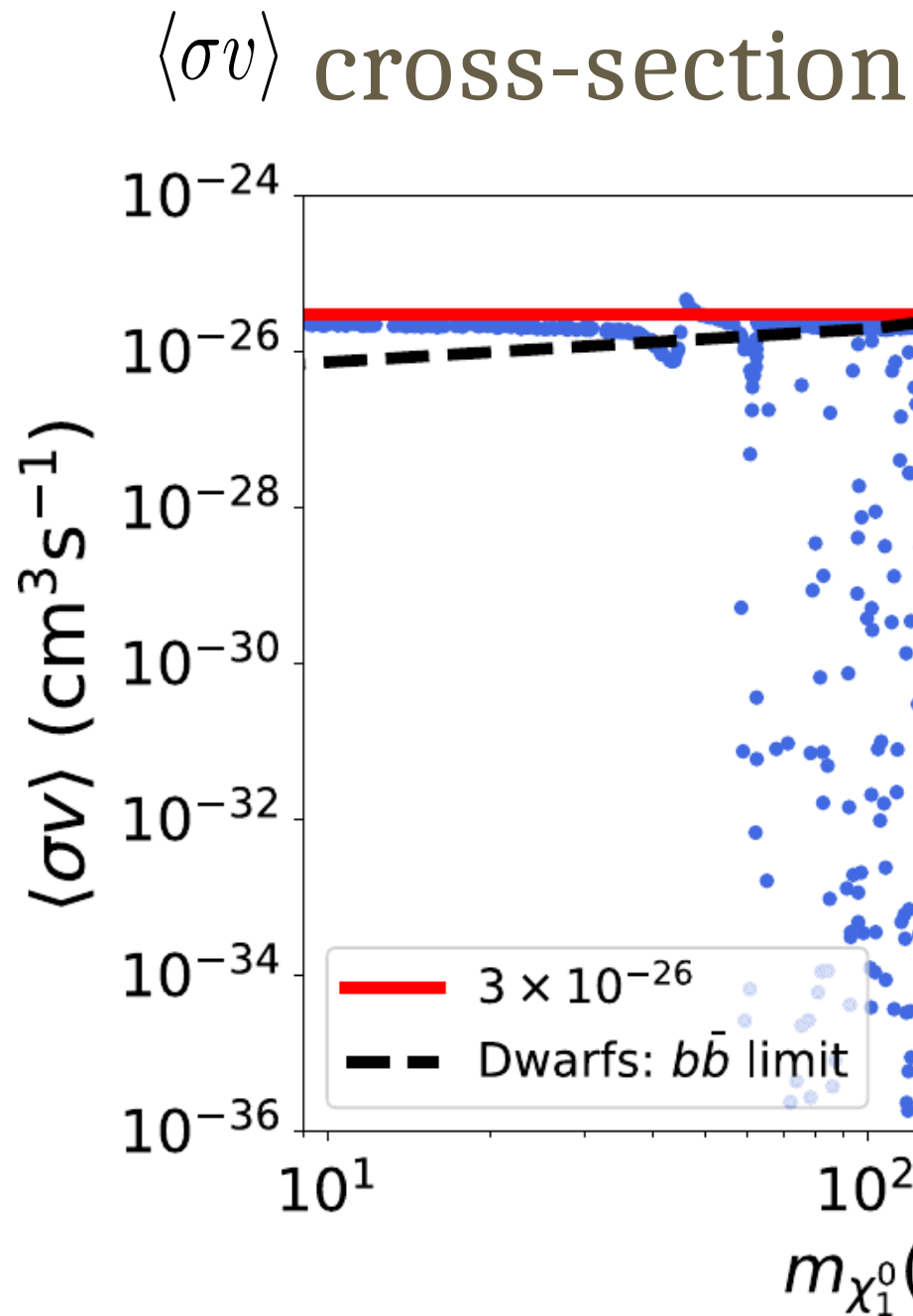
- DM
- Neutrino physics
- STU

- Potential perturbativity
- LFV ...

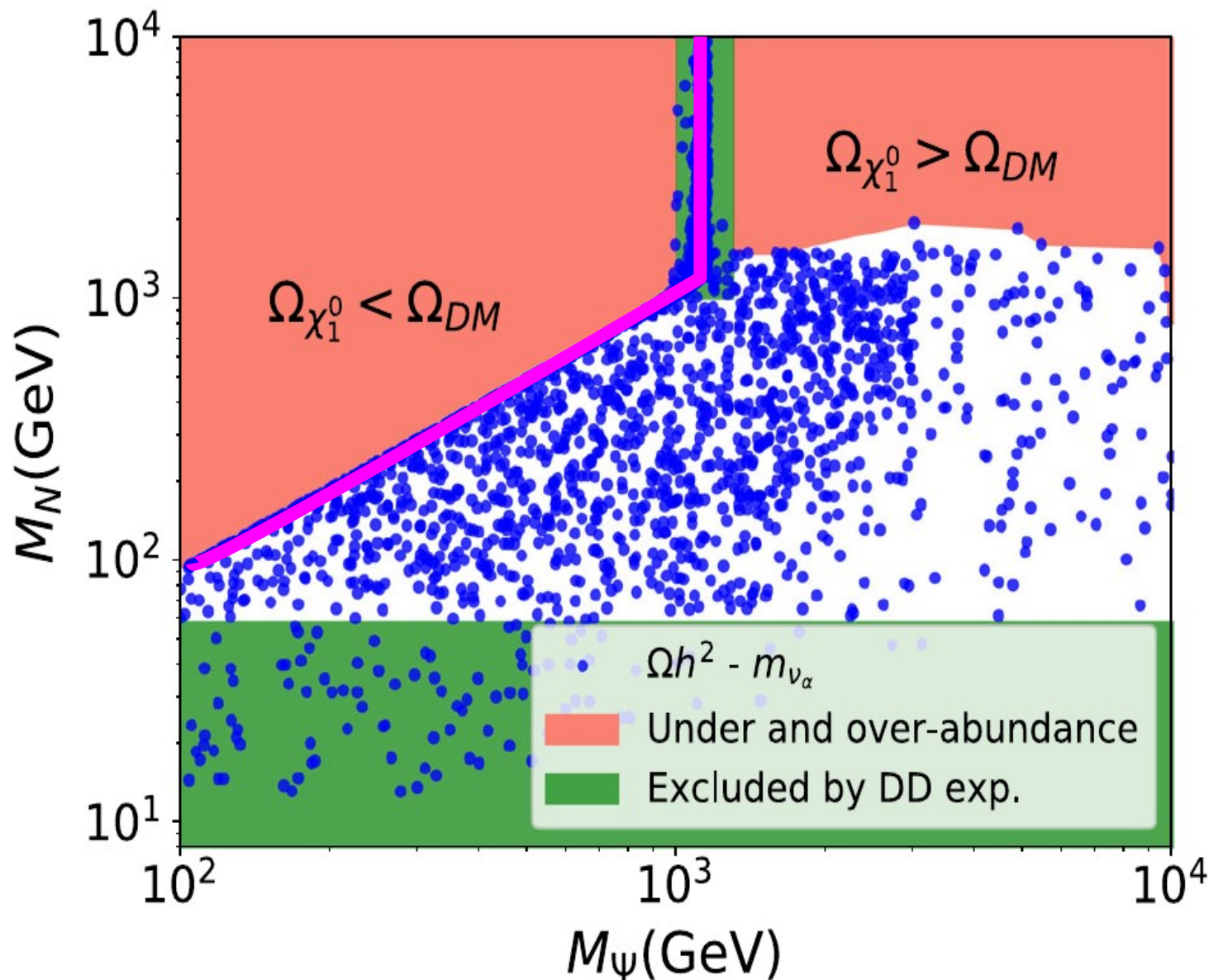


Spin dependent cross-section





4. Majorana vs Dirac DM



Conclusions

- We were able to have **Dirac DM and Dirac neutrinos** in the SDFDM model.
- The new **S Higgs-scalar** plays an important role in order to get the relic abundance and also for the neutrino physics.
- The model has **signals** for direct-indited, LFV ...
- The model could be tested in the future by experiments such as **DARWIN**. [J. Cosmol. Astropart. Phys. 11 \(2016\) 017](#)
- We find that the allowed parameter space of this model is **broader** than the well-known Majorana dark matter scenario.





Thank you!



Backup

V co-positivity

$$\lambda_1 \geq 0, \quad \lambda_i^\sigma \geq 0, \quad \lambda^S \geq 0, \quad (3)$$

$$\frac{\lambda_i^{\sigma H}}{2} + \sqrt{\lambda_1 \lambda_i^\sigma} \geq 0, \quad \frac{\lambda_{SH}}{2} + \sqrt{\lambda_1 \lambda^S} \geq 0, \quad \frac{\lambda^{S\sigma}}{2} + \sqrt{\lambda_i^\sigma \lambda^S} \geq 0, \quad (4)$$

$$\begin{aligned} & \sqrt{\lambda_1 \lambda_i^\sigma \lambda^S} + \frac{\lambda_i^{\sigma H}}{2} \sqrt{\lambda^S} + \frac{\lambda_{SH}}{2} \sqrt{\lambda_i^\sigma} + \frac{\lambda^{S\sigma_i}}{2} \sqrt{\lambda_1} \\ & + \sqrt{2 \left(\frac{\lambda_i^{\sigma H}}{2} + \sqrt{\lambda_1 \lambda_i^\sigma} \right) \left(\frac{\lambda_{SH}}{2} + \sqrt{\lambda_1 \lambda^S} \right) \left(\frac{\lambda^{S\sigma_i}}{2} + \sqrt{\lambda_i^\sigma \lambda^S} \right)} \geq 0. \end{aligned} \quad (5)$$

Neutrino matrix

$$\begin{aligned}
\mathcal{M}_{\alpha\beta} &= \sum_{i=1}^2 \sum_{j=1}^2 \frac{U_{j1} V_{j2}}{16\pi^2} \times h_b^{\alpha i} h_a^{\beta i} m_{\chi_j^0} \\
&\times \left[\frac{m_{\chi_j^0}^2 \ln(m_{\chi_j^0}^2) - m_{\sigma_i}^2 \ln(m_{\sigma_i}^2)}{(m_{\chi_j^0}^2 - m_{\sigma_i}^2)} \right], \\
&= \sum_{i=1}^2 h_b^{\alpha i} \times \Lambda_i \times h_a^{\beta i}, \tag{19}
\end{aligned}$$

where Λ_i is the loop factor, defined as

$$\begin{aligned}
\Lambda_i &= \sum_{j=1}^2 \frac{U_{j1} V_{j2}}{16\pi^2} \times m_{\chi_j^0} \times \left[\frac{m_{\chi_j^0}^2 \ln(m_{\chi_j^0}^2) - m_{\sigma_i}^2 \ln(m_{\sigma_i}^2)}{(m_{\chi_j^0}^2 - m_{\sigma_i}^2)} \right], \\
&= \sum_{j=1}^2 \frac{U_{j1} V_{j2}}{16\pi^2} \times m_{\chi_j^0} \times \left[\frac{m_{\chi_j^0}^2}{(m_{\chi_j^0}^2 - m_{\sigma_i}^2)} \ln \left(\frac{m_{\chi_j^0}^2}{m_{\sigma_i}^2} \right) \right]. \tag{20}
\end{aligned}$$

Yukawa couplings

$$h_a^{1i} = 0,$$

$$h_a^{2i,3i} = \text{free},$$

$$h_b^{\alpha 1} = -\frac{1}{\Lambda_1} \left(\frac{h_a^{32} m_{\nu 2} U_{\alpha 2} - h_a^{22} m_{\nu 3} U_{\alpha 3}}{h_a^{22} h_a^{31} - h_a^{21} h_a^{32}} \right),$$

$$h_b^{\alpha 2} = -\frac{1}{\Lambda_2} \left(\frac{h_a^{31} m_{\nu 2} U_{\alpha 2} - h_a^{21} m_{\nu 3} U_{\alpha 3}}{h_a^{22} h_a^{31} - h_a^{21} h_a^{32}} \right).$$

SI cross sections

$$\sigma_{N,o}^{\text{SI}} = \frac{G_F^2 m_N^2}{4\pi A^2} (\cos^2 \theta_L + \cos^2 \theta_R)^2 \\ \times [(1 - 4\sin^2 \theta_W)Z - (A - Z)]^2,$$

$$\chi_{Lj} = V_{ji} N_{Li} = \begin{pmatrix} \cos \theta_L & \sin \theta_L \\ -\sin \theta_L & \cos \theta_L \end{pmatrix} \begin{pmatrix} \Psi_L^0 \\ \psi_L \end{pmatrix},$$

$$\chi_{Rj}^\dagger = U_{ji} N_{Ri}^\dagger = \begin{pmatrix} \cos \theta_R & \sin \theta_R \\ -\sin \theta_R & \cos \theta_R \end{pmatrix} \begin{pmatrix} (\Psi_R^0)^\dagger \\ (\psi_R)^\dagger \end{pmatrix},$$

$$\sigma_{N,e}^{\text{SI}} \approx \frac{m_N^4 f_N^2}{\pi v^2} \left(\frac{g_{\chi_1^0 \chi_1^0 h_1}}{m_{h_1}^2} + \frac{g_{\chi_1^0 \chi_1^0 h_2}}{m_{h_2}^2} \right)^2,$$

$$g_{\chi_1^0 \chi_1^0 h_k} = \frac{-i}{\sqrt{2}} \sin \theta_R (h_d \cos \theta_L Z_{k1}^H + h_c \sin \theta_L Z_{k2}^H).$$

Scan



Parameter	Range
M_Ψ (GeV)	10^2-10^4
m_{σ_i} (GeV)	$10^3-2 \times 10^4$
v_S (GeV)	10^2-10^5
$ h_c , h_d $	$10^{-6}-3$
$\lambda^{H\sigma_i}, \lambda^S, \lambda^{S\sigma_i}, \lambda_{SH}, \lambda^{\sigma_i}$	$10^{-4}-3$
$ h_a^{2i,3i} $	$10^{-6}-1$

Symbol	$(SU(2)_L, U(1)_Y)$	Z_2	Spin
N	$(1, 0)$	—	$1/2$
\tilde{R}_u	$(2, +1/2)$	—	$1/2$
R_d	$(2, -1/2)$	—	$1/2$

$$\mathcal{L} = \frac{1}{2} c_{\alpha\beta}^{d=5} \left(\overline{L}_\alpha^c \tilde{H}^* \right) \left(\tilde{H}^\dagger L_\beta \right) + \text{h.c.}$$

