

Upper bound on the smuon mass from vacuum stability in the light of muon $g-2$ anomaly

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in collaboration with Yutaro Shoji, Takeo Moroi

Phys. Lett. B 831 (2022) 137163 [arXiv:2203.08062]

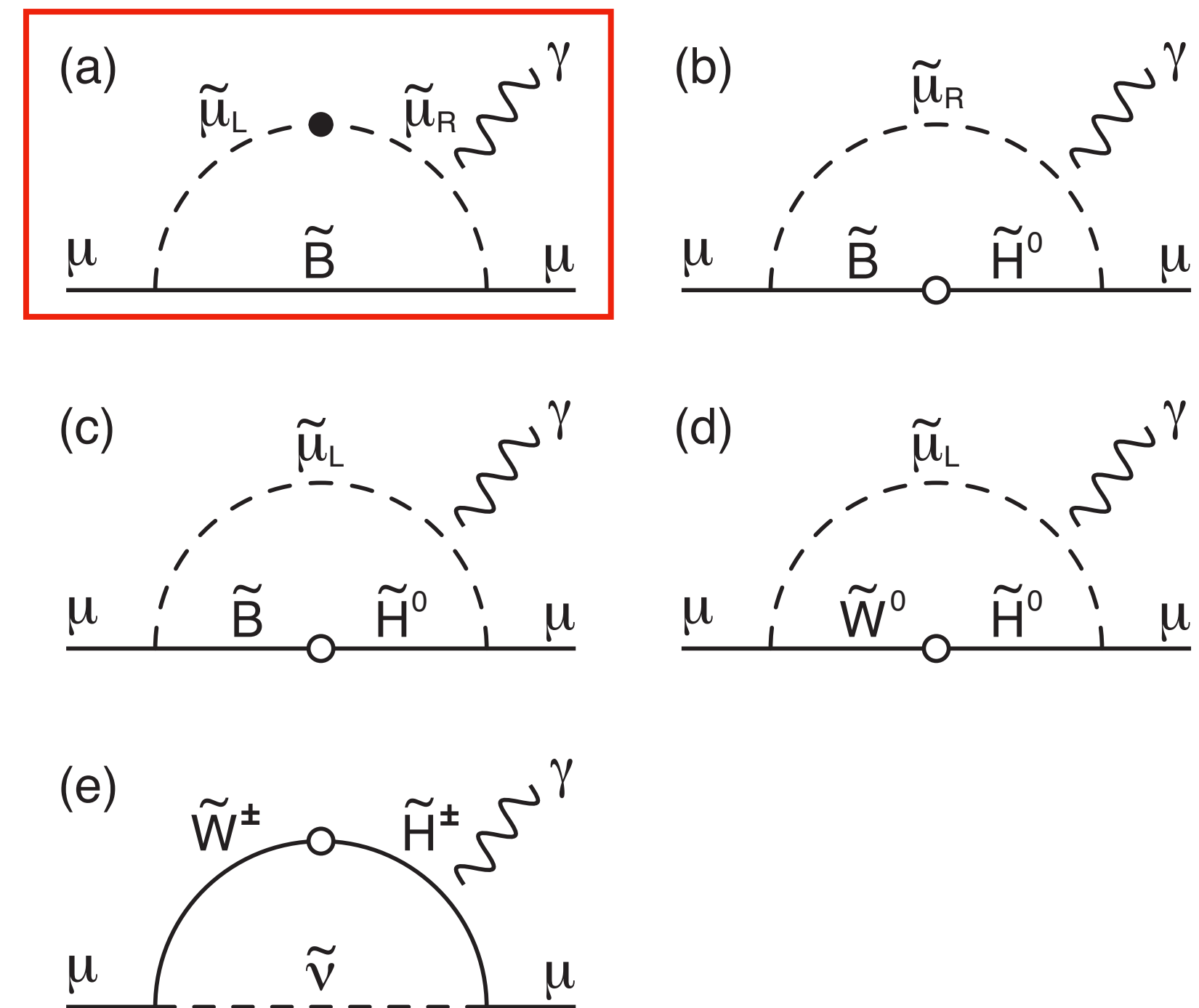
MSSM and muon $g - 2$

► Muon $g - 2$ anomaly in previous / on-going experiments

- SM prediction $a_\mu^{\text{SM}} = (11\,659\,181.0 \pm 4.3) \times 10^{-10}$ T. Aoyama [2006.04822]
- BNL + Fermilab 2021 $a_\mu^{\text{BNL+FNAL}} = (11\,659\,206.1 \pm 4.1) \times 10^{-10}$ Muon $g - 2$ collaboration [2104.03281]
- Combined $\Delta a_\mu = (25.1 \pm 5.9) \times 10^{-10}$, 4.2σ anomaly

► MSSM can resolve this anomaly if its contribution is enhanced with

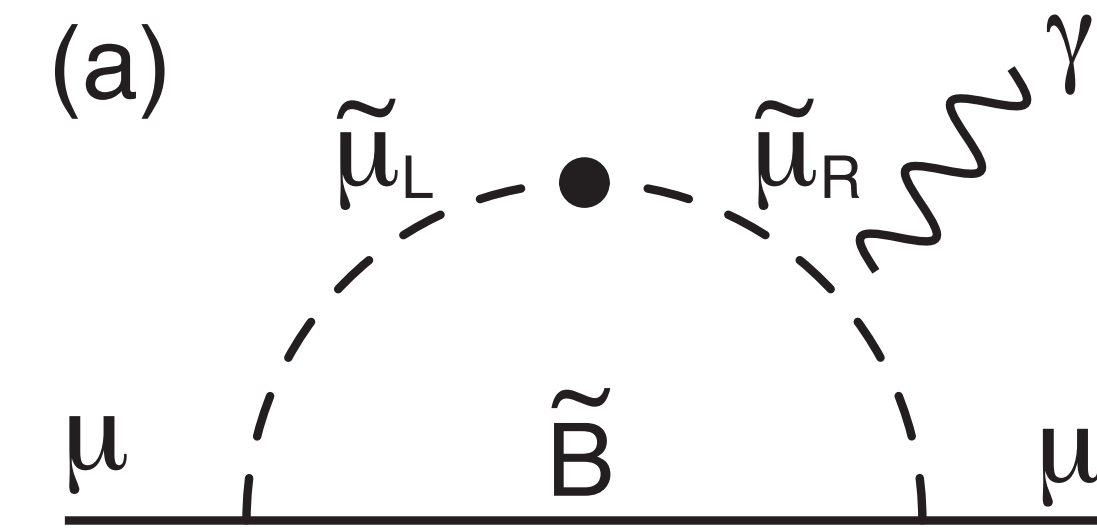
- Light sleptons
- Light EWinos
- Sizable $\tan\beta$



Relation to the EW vacuum stability

- ▶ Diagram (a) is also enhanced by large $|\mu|$

$$- a_\mu \simeq \frac{\alpha_Y m_\mu^2 M_1 \mu}{4\pi m_{\tilde{\mu}_L}^2 m_{\tilde{\mu}_R}^2} \tan \beta \cdot f_N \left(\frac{m_{\tilde{\mu}_L}^2}{M_1^2}, \frac{m_{\tilde{\mu}_R}^2}{M_1^2} \right)$$



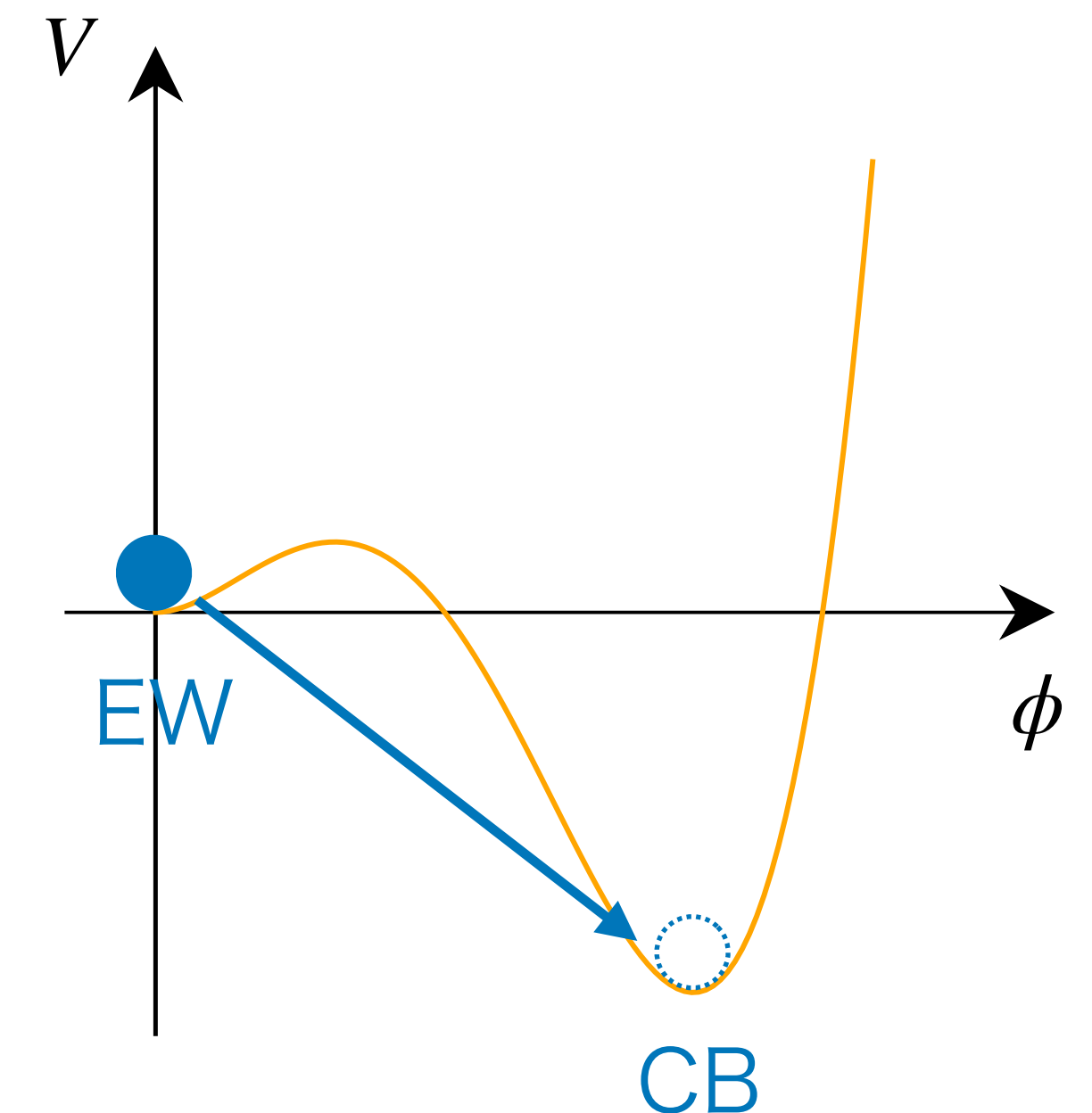
- ▶ Hierarchy $|\mu| \gg m_{\tilde{\mu}}$ may generate a charge breaking minimum

- $V = V_2 + V_3 + V_4$

- $V_3 \supset -TH^\dagger \tilde{\ell}_L \tilde{\mu}_R^\dagger$ with $T \simeq Y_\ell \mu \tan \beta$

- ▶ Larger $m_{\tilde{\mu}} \rightarrow$ Need larger μ to explain muon $g - 2$
 \rightarrow More unstable EW vac

- Stability of the EW vacuum puts an upper bound on $m_{\tilde{\mu}}$
 for models that resolve muon $g - 2$ anomaly



Master formula of decay rate

$$\gamma = Ae^{-\mathcal{B}}$$

Coleman '77

A : NLO part

mass dimension 4

\mathcal{B} : Bounce action (LO part)

can be calculated with, for example,

CosmoTransitions [C. L. Wainwright \[1109.4189\]](#)

Gradient Flow [SC+ \[1906.10829\]](#)

- ▶ Evaluation of A is more involved but important

Recent developments

▶ Single-field bounce

- General gauge theory

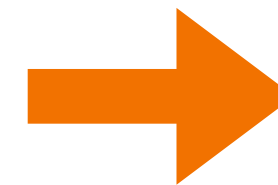
Endo, Moroi, Nojiri, & Shoji [1703.09304], [1704.03492]

- Application to the SM (and beyond)

Isidori, Ridolfi & Strumia [hep-ph/0104016]

Andreassen, Frost & Schwartz [1707.08124]

SC, Moroi & Shoji [1707.09301], [1803.03902]



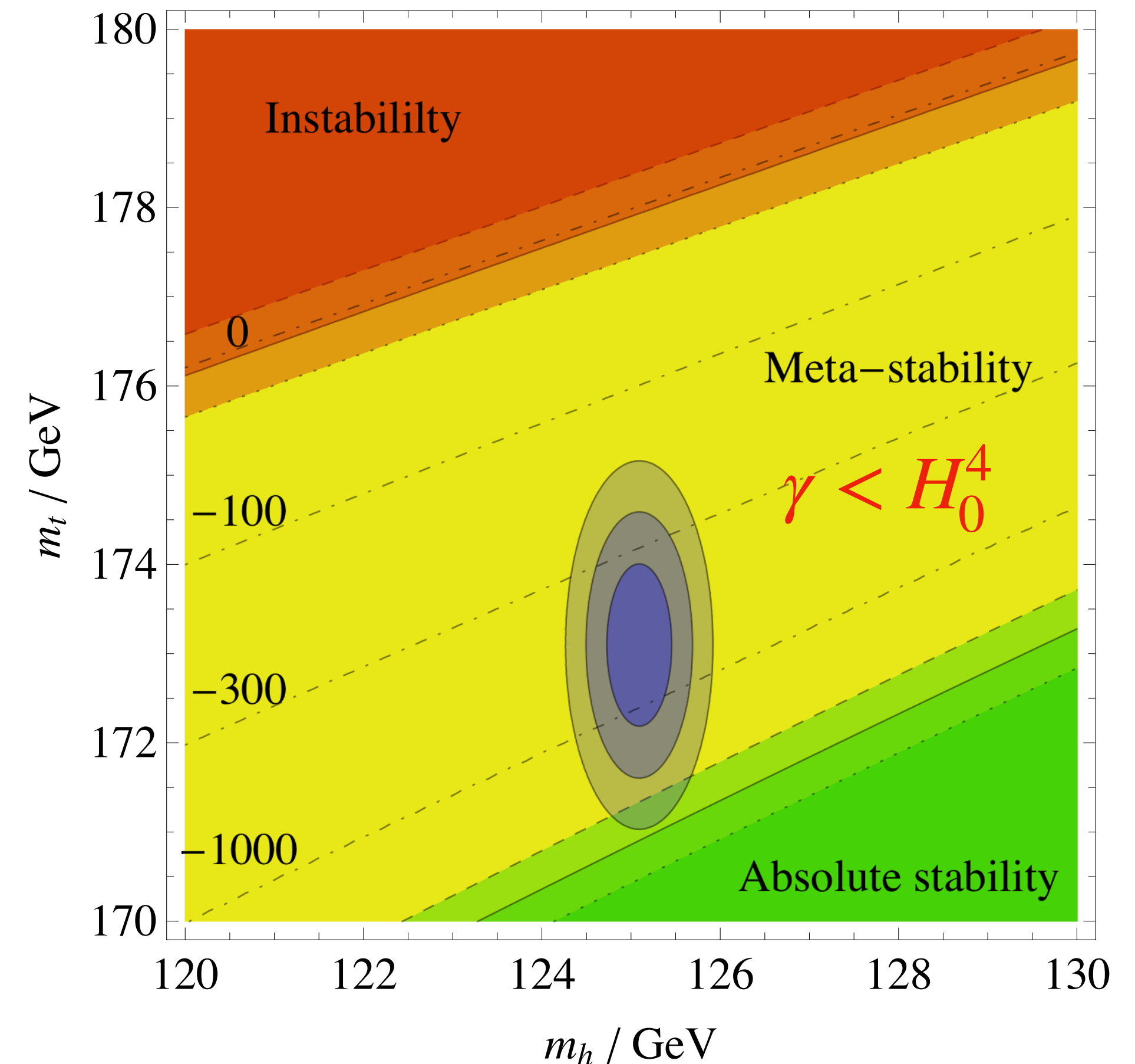
▶ Multi-field bounce

- General gauge theory

SC, Moroi & Shoji [2007.14124]

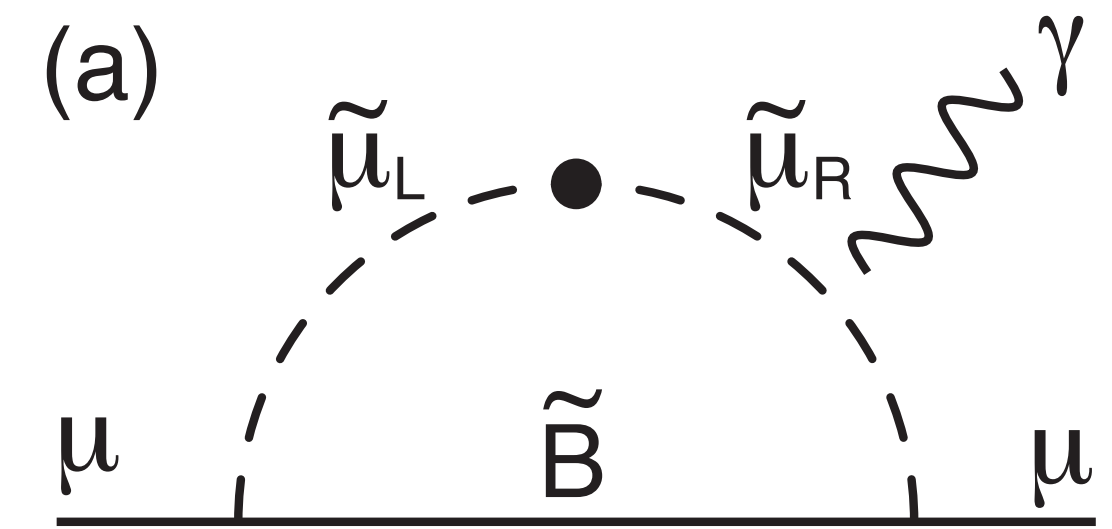
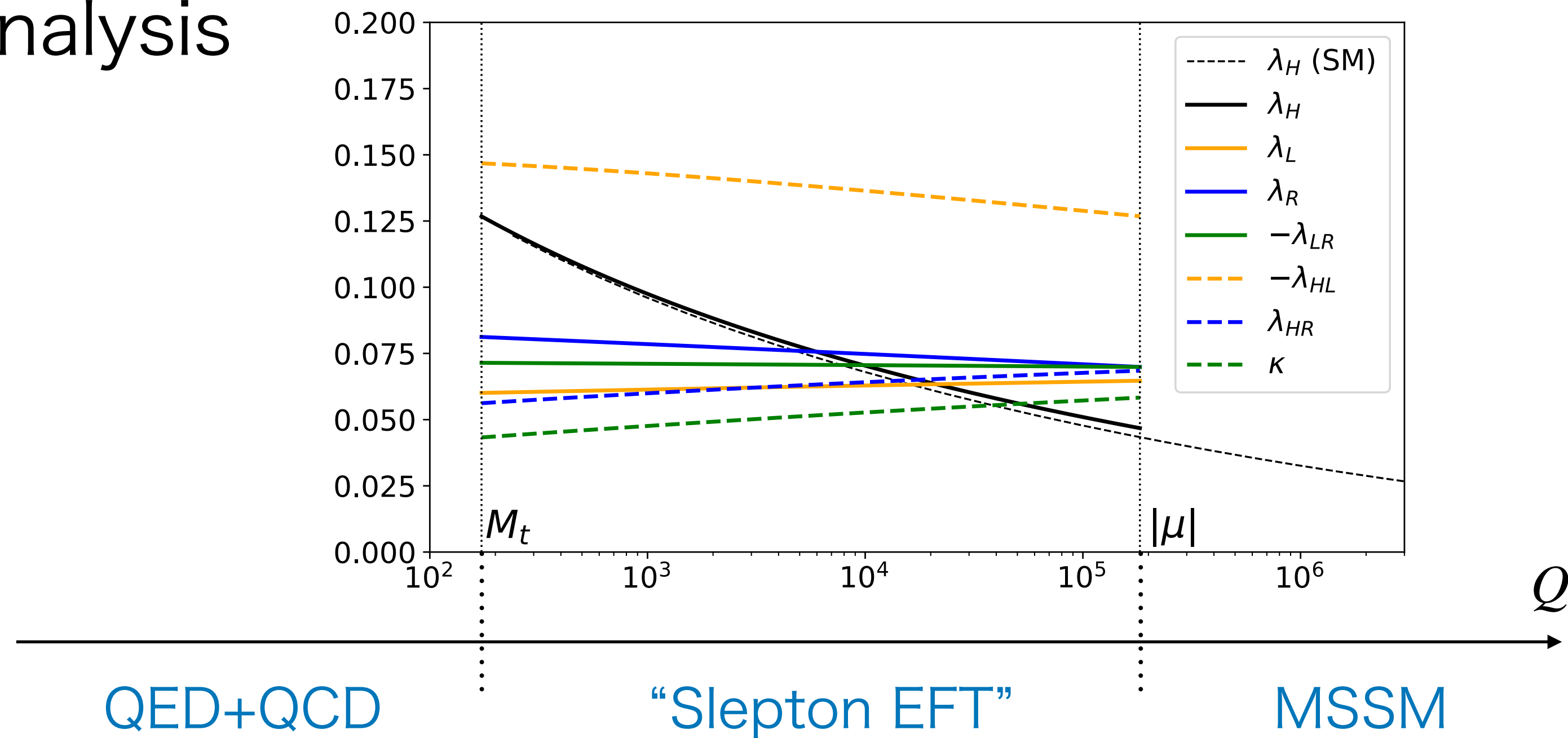
- Application to the MSSM

SC, Moroi & Shoji [2203.08062]



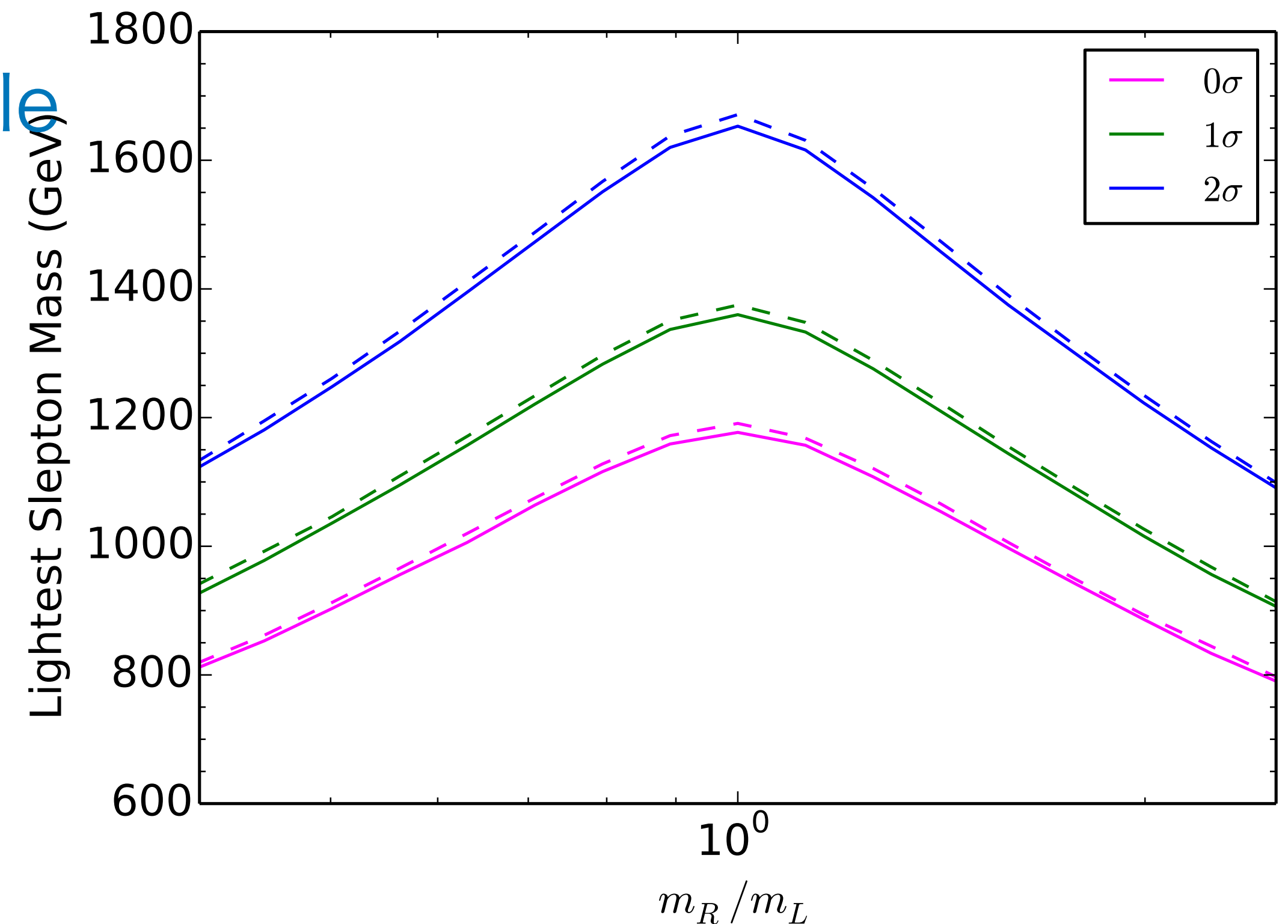
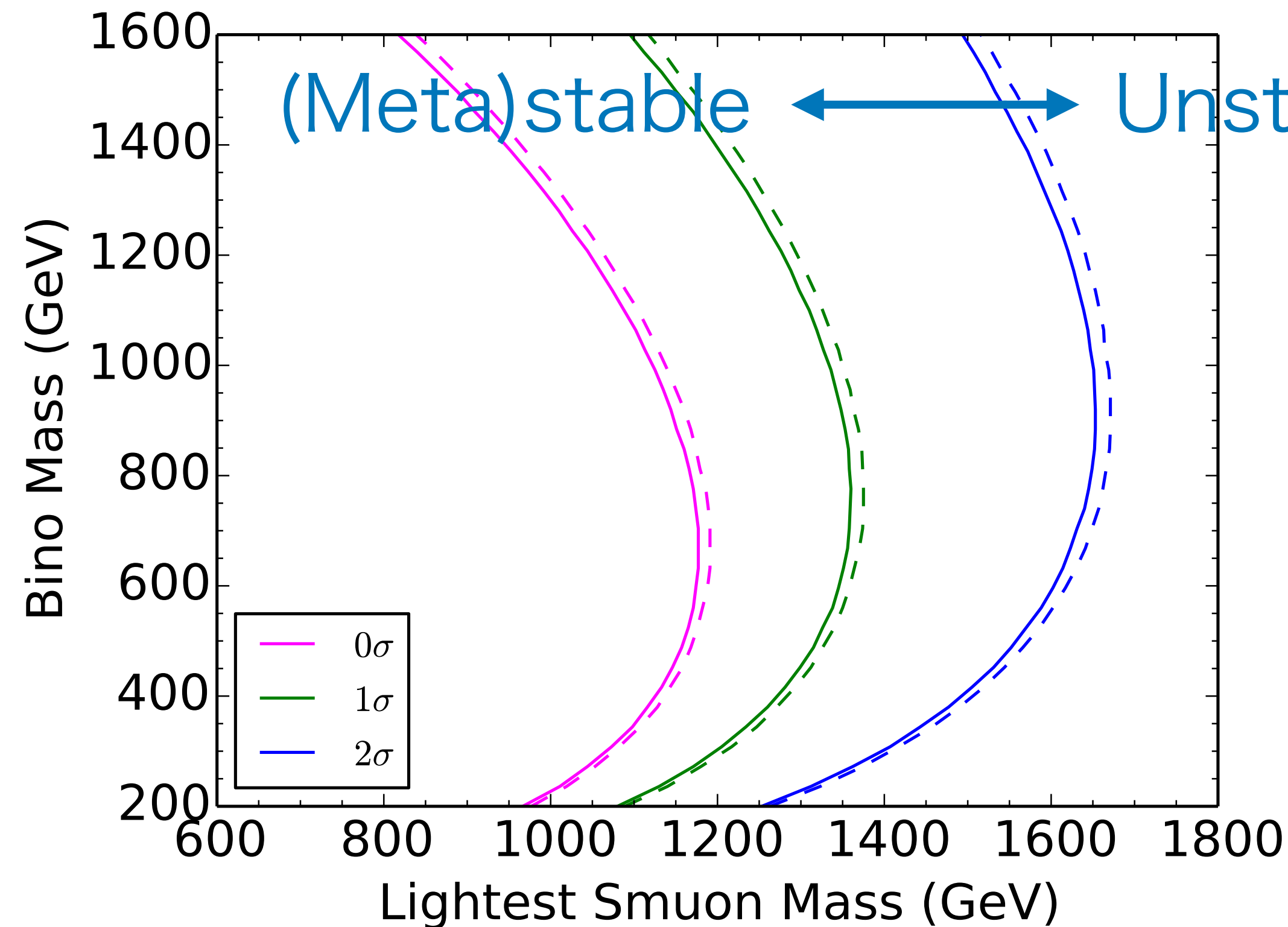
Model setup

- ▶ 2 hierarchical scales of the MSSM particles
 - EW scale M_t : smuon $\tilde{\mu}$, bino \tilde{B}
 - SUSY scale $|\mu|$: Other MSSM particles
- ▶ EFT analysis



MSSM with light smuons

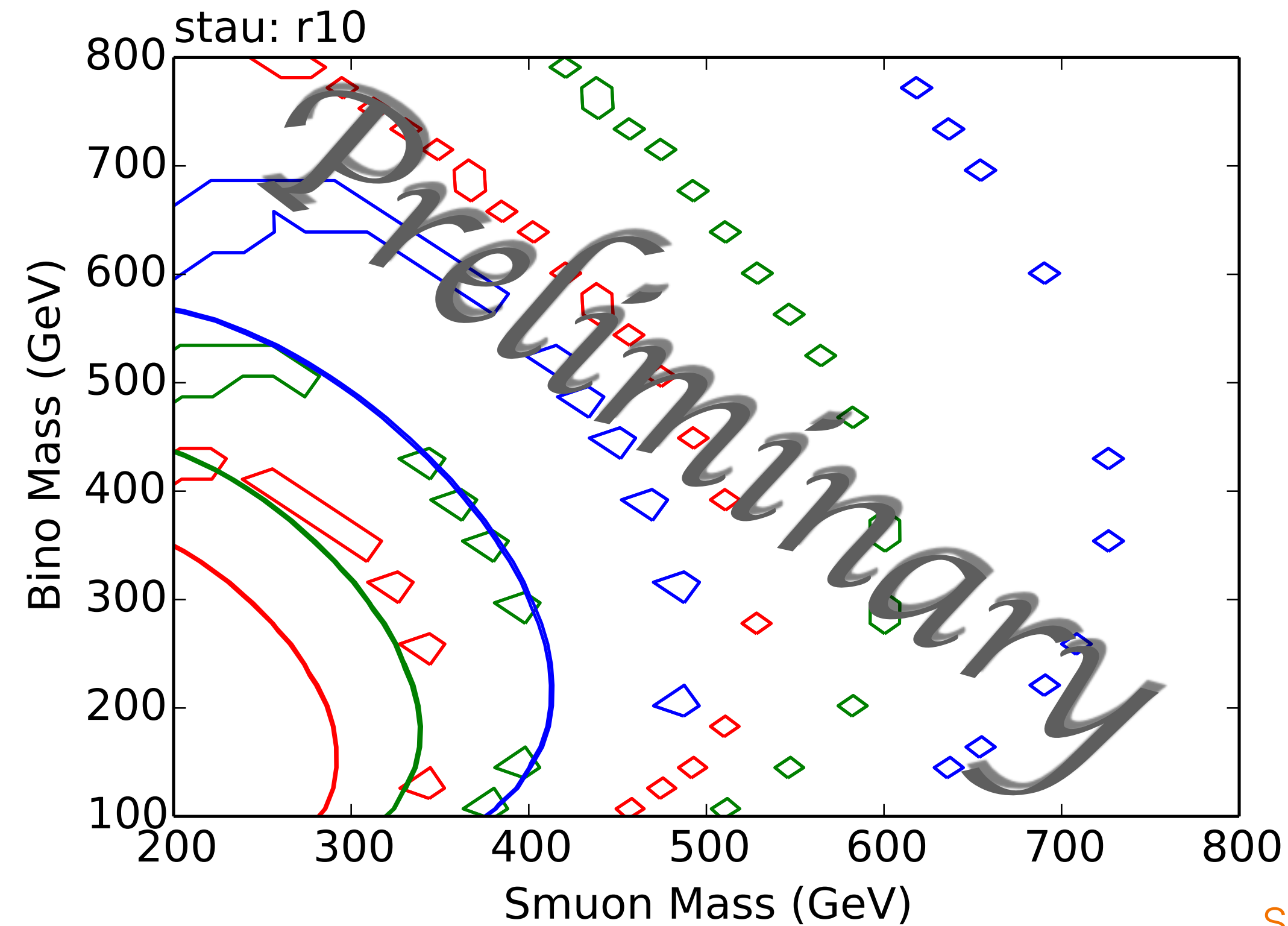
- ▶ $|\mu|$ is fixed to resolve the muon $g - 2$ anomaly to the 0/1/2- σ level



- ▶ Upper bound on the lightest smuon mass $\lesssim 1-2$ TeV

MSSM with light sleptons

- ▶ What if all 3 generations of sleptons are light?
 - ▶ Given that $T_\ell \simeq Y_\ell \mu \tan \beta$ & $Y_\tau \gg Y_\mu$, CCBs in the stau direction are more dangerous



SC, Moroi & Shoji [22xx.xxxxx]

So Chigusa, PPC 2022 (6/7) @ St. Louis

Conclusion

- ▶ Hierarchy $|\mu| \gg m_{\tilde{\mu}}$, which is sometimes required to enhance the MSSM contribution to the muon $g - 2$, destabilizes the EW vacuum
 - The stability of the EW vacuum puts an upper bound on the smuon mass $m_{\tilde{\mu}}$
- ▶ Using recently-developed semi-analytic results, we evaluate the decay rate of the EW vacuum in the MSSM and obtain upper bounds
 - Upper bound on the lightest smuon mass $\lesssim 1-2 \text{ TeV}$

Thanks!

Backup slides

Functional determinant I

- ▶ The decay rate γ is related to the Euclidean partition function

$$Z \equiv \langle \text{FV} | e^{-HT} | \text{FV} \rangle \simeq \int_{\phi(t_i)=\text{FV}}^{\phi(t_f)=\text{FV}} \mathcal{D}\phi e^{-S_E[\phi]} \propto \exp(i\gamma VT)$$

- ▶ The path integral is dominated by solutions of the EOM
 - The imaginary part comes from non-trivial solutions: “bounce”

$$\gamma = \frac{1}{VT} \text{Im} \frac{\int_{1\text{-bounce}} \mathcal{D}\Psi e^{-S_E}}{\int_{\text{FV}} \mathcal{D}\Psi e^{-S_E}}$$

- ▶ Expansion of S_E around the bounce (FV) results in Gaussian integrals

$$- S_E[\bar{\phi} + \Psi] = S_E[\bar{\phi}] + \frac{1}{2} \int d^4x \Psi \mathcal{M} \Psi + \mathcal{O}(\Psi^3)$$

$$\gamma = A e^{-\mathcal{B}} ; A = \frac{1}{VT} \left| \frac{\text{Det } \mathcal{M}}{\text{Det } \widehat{\mathcal{M}}} \right|^p$$

Functional determinant II

- ▶ Example: single real scalar field

$$S_E[\phi] = \int d^D x \left[\frac{1}{2} (\partial_\mu \phi)^2 + V(\phi) \right] \Rightarrow \mathcal{M} = -\partial^2 + \frac{\delta^2 V}{\delta \phi^2} \Big|_{\bar{\phi}}$$

$$\mathcal{M} = \bigoplus_{\ell=0}^{\infty} (\mathcal{M}_\ell)^{(\ell+1)^2} ; \quad \mathcal{M}_\ell = - \left(\partial_r^2 + \frac{D-1}{r} \partial_r - \frac{\ell(\ell+2)}{r^2} \right) + \frac{\delta^2 V}{\delta \phi^2} \Big|_{\bar{\phi}}$$

- ▶ Gel'fand-Yaglom theorem

With Ψ_ℓ & $\widehat{\Psi}_\ell$ s.t. $\mathcal{M}_\ell \Psi_\ell = 0$; $\widehat{\mathcal{M}}_\ell \widehat{\Psi}_\ell = 0$,

$$\frac{\text{Det } \mathcal{M}_\ell}{\text{Det } \widehat{\mathcal{M}}_\ell} = \left(\frac{\Psi_\ell(r \rightarrow 0)}{\widehat{\Psi}_\ell(r \rightarrow 0)} \right)^{-1} \frac{\Psi_\ell(r \rightarrow \infty)}{\widehat{\Psi}_\ell(r \rightarrow \infty)}$$

Gel'fand+ '60, Kirsten+ '03, '04

M. Endo+ [1704,03492] for proof in this context



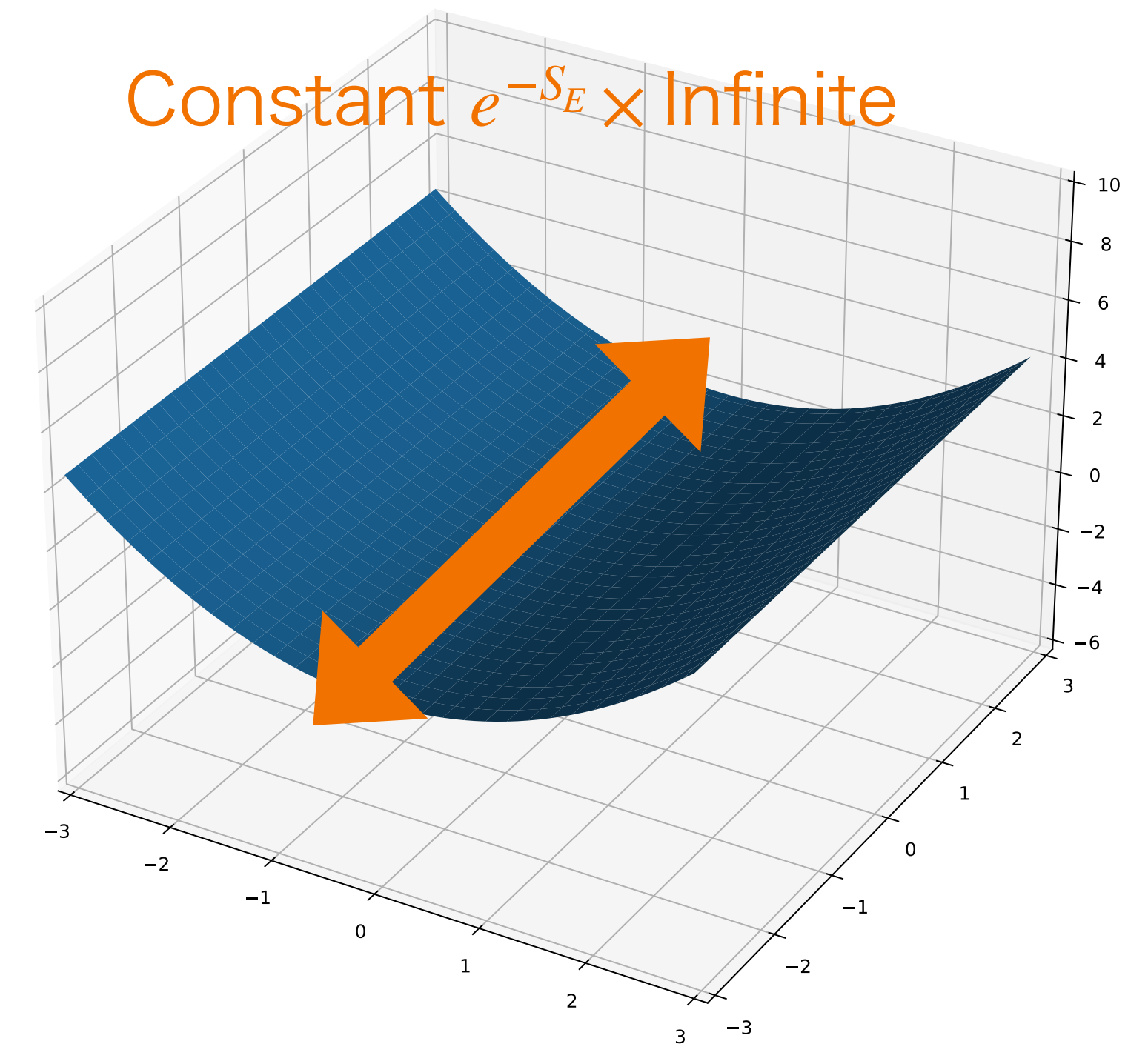
Next Task

Solve differential equation

$$\mathcal{M}_\ell \Psi_\ell = 0$$

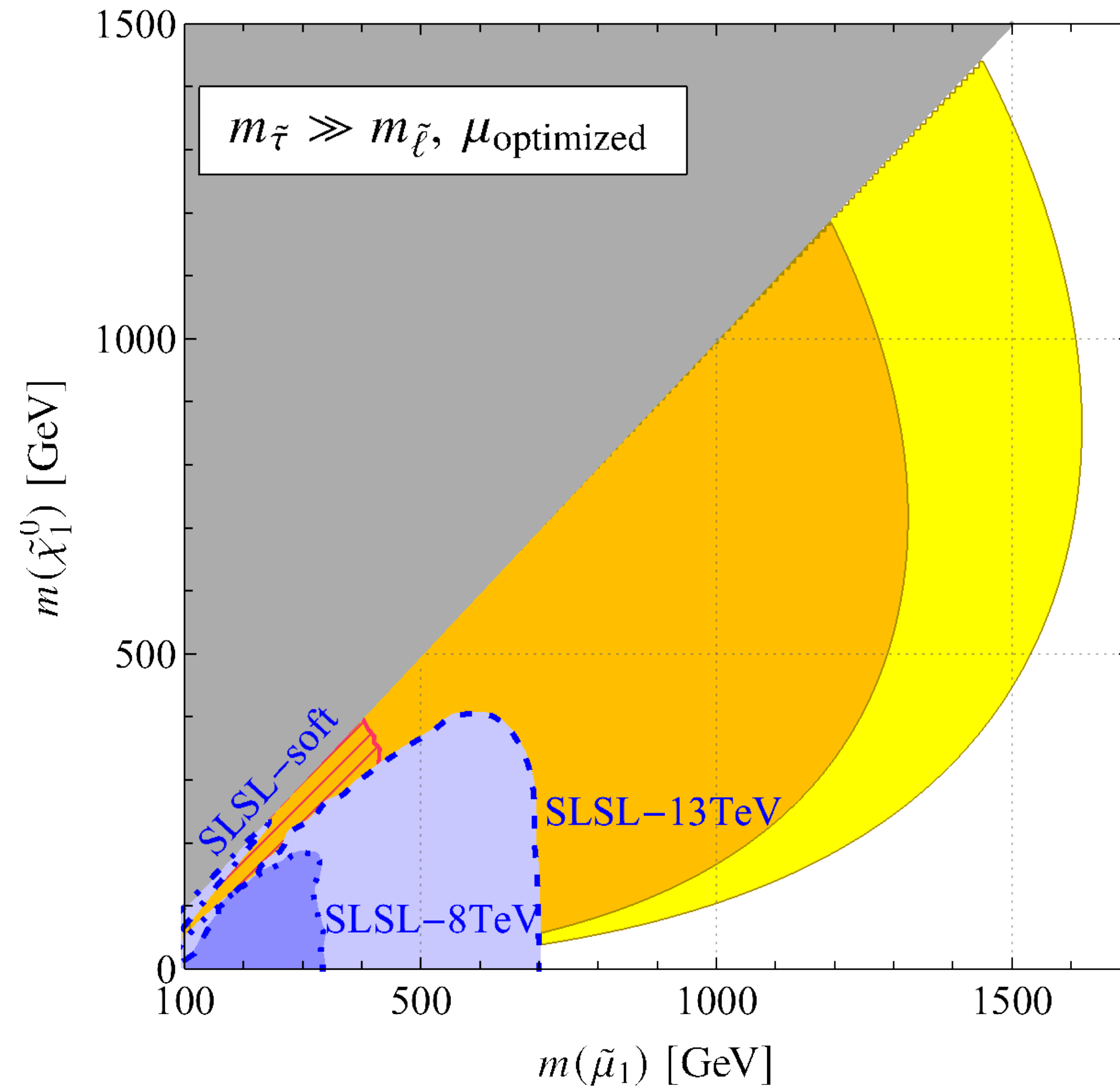
Zero mode

- ▶ $\text{Det } \mathcal{M}_\ell = 0$ leads to divergence
 - equivalent to existence of zero mode $\mathcal{M}_\ell \Psi_\ell = 0$ & $\lim_{r \rightarrow \infty} \Psi(r) = 0$
 - implies existence of flat direction of Euclidean action
- ▶ Flat direction is often result of symmetry
 - Spacetime translation of bounce ($\ell = 1$ of h)
 - Classical dilatation ($\ell = 0$ of h) ← **NEW**
 - Gauge symmetry ($\ell = 0$ of gauge field)

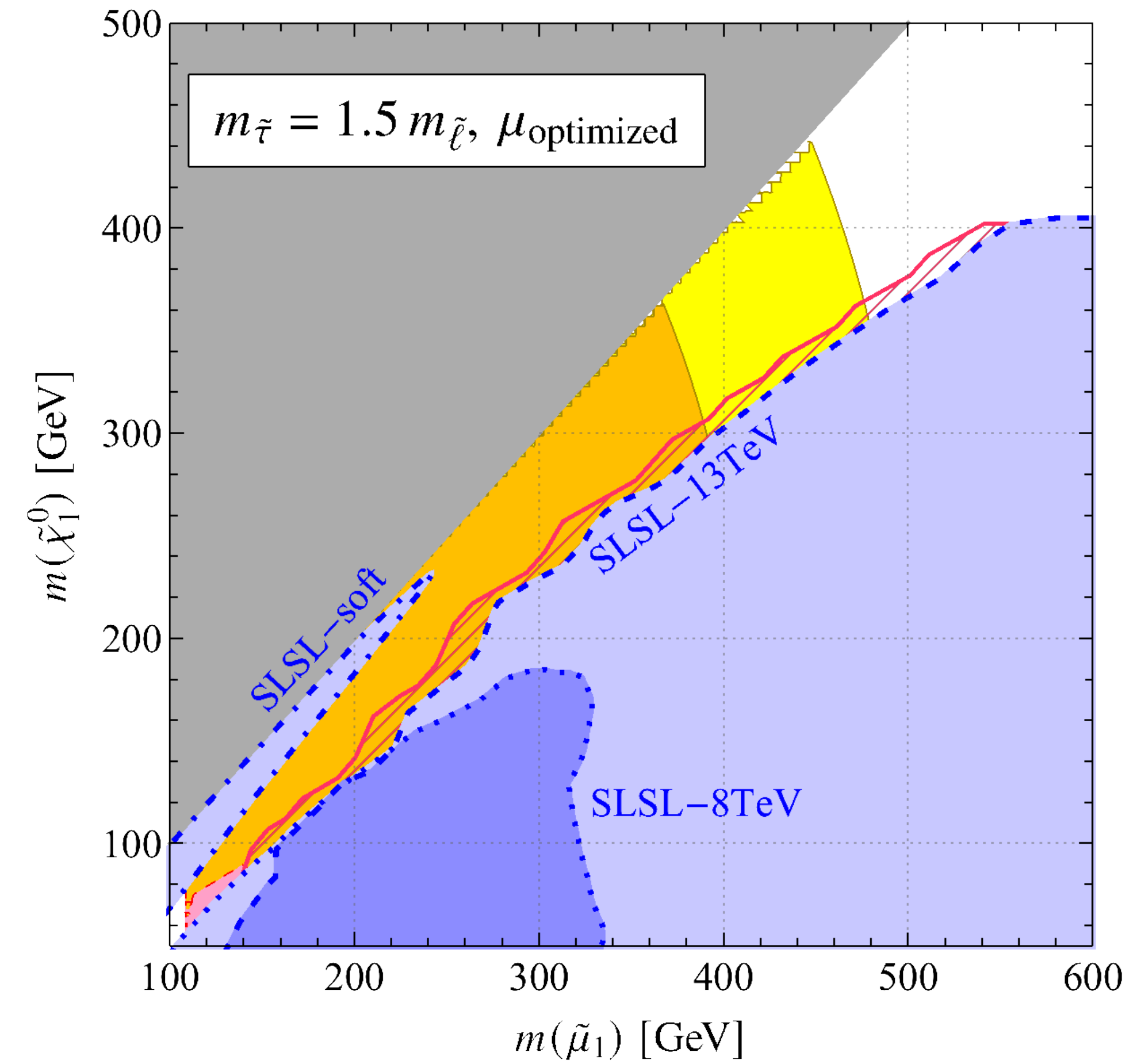


Collider constraints

M. Endo+ [2104.03217]



- Smuon only



- 3 generations