

Effective field theory approach to neutrino-less double beta decay

Vincenzo Cirigliano

Institute for Nuclear Theory
University of Washington

Outline

- Introduction: neutrino mass, Lepton Number, and $0\nu\beta\beta$ decay
- ‘End-to-end’ EFT framework for LNV and $0\nu\beta\beta$
 - $0\nu\beta\beta$ from **high-scale dynamics** (LNV @ dim 5)
 - $0\nu\beta\beta$ from **(multi)TeV-scale dynamics** (LNV @ dim 7, 9, ...)
- Conclusions & outlook

Special thanks to collaborators:

W. Dekens, J. de Vries, M. Graesser, M. Hoferichter, E. Mereghetti, S. Pastore, M. Piarulli,
U. van Kolck, A. Walker-Loud, R. Wiringa

Neutrino mass and new physics

- Massive neutrinos provide concrete evidence of physics beyond the SM

The Standard Model

The diagram illustrates the Standard Model's prediction for neutrino mass. On the left, a list of fermions ψ_i for $i=1,2,3$ is shown: $\begin{pmatrix} \ell_L \\ e_R \\ q_L \\ u_R \\ d_R \end{pmatrix}_i$. Arrows point from ℓ_L and q_L to two separate boxes. The top box contains $\begin{pmatrix} \nu_L \\ e_L \end{pmatrix}$, with ν_L circled in red. The bottom box contains $\begin{pmatrix} u_L \\ d_L \end{pmatrix}$. In the center, a black mug displays the Standard Model Lagrangian: $\mathcal{L} = -\frac{1}{4} F_{\mu\nu} F^{\mu\nu} + i\bar{\psi}\not{D}\psi + \text{h.c.} + \chi_i y_{ij} \chi_j \phi + \text{h.c.} + |D_\mu \phi|^2 - V(\phi)$. A large blue arrow points from the mug to the right, where the text "No neutrino mass" is written.

Understanding origin and nature of neutrino mass is an open problem, with implications for baryogenesis, DM, structure formation, ...

Neutrino mass and new physics

- Lorentz invariance \Rightarrow two options: Dirac or Majorana

Dirac mass:

$$m_D \bar{\psi}_L \psi_R + \text{h.c.}$$

Majorana mass:

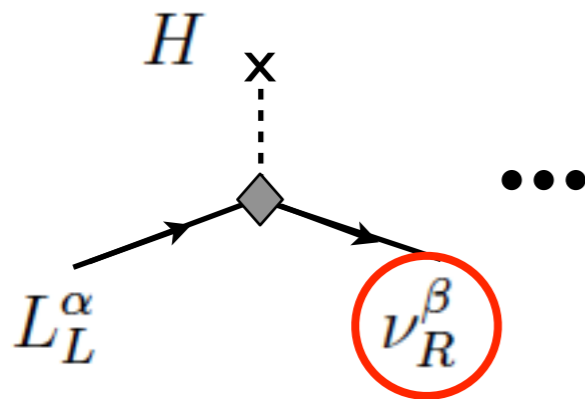
$$m_M \psi_L^T C \psi_L + \text{h.c.}$$

Neutrino mass and new physics

- Lorentz invariance \Rightarrow two options: Dirac or Majorana
- $SU(2)_W$ invariance \Rightarrow need **new degrees of freedom**

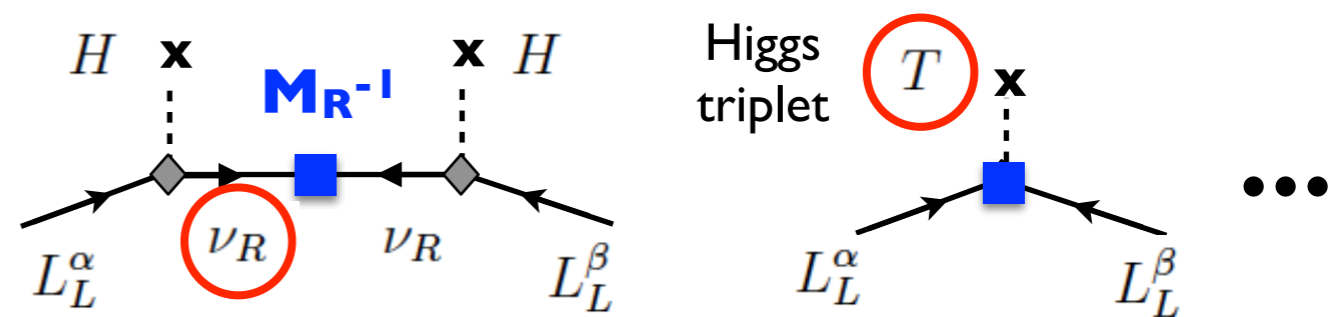
Dirac mass:

$$m_D \overline{\psi}_L \psi_R + \text{h.c.}$$



Majorana mass:

$$m_M \psi_L^T C \psi_L + \text{h.c.}$$

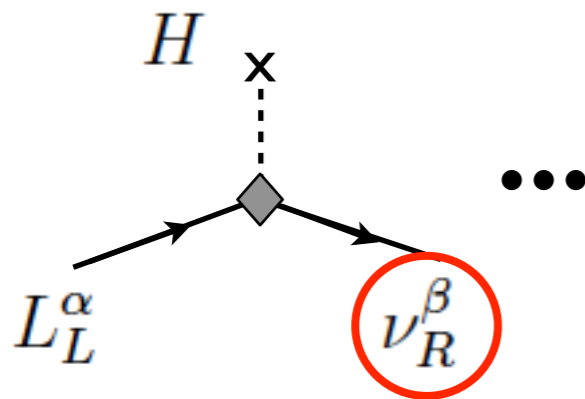


Neutrino mass and new physics

- Lorentz invariance \Rightarrow two options: Dirac or Majorana
- $SU(2)_W$ invariance \Rightarrow need **new degrees of freedom**

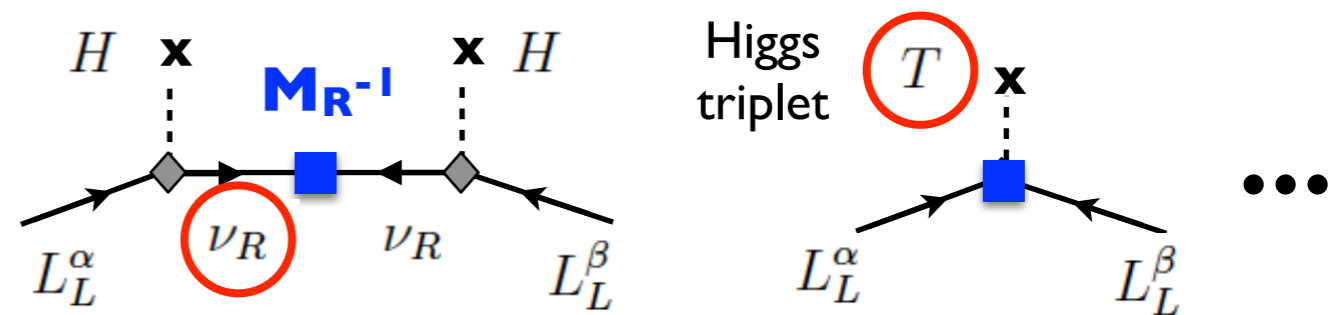
Dirac mass:

$$m_D \overline{\psi}_L \psi_R + \text{h.c.}$$



Majorana mass:

$$m_M \psi_L^T C \psi_L + \text{h.c.}$$



- Violates $L_{e,\mu,\tau}$, conserves L

- Violates $L_{e,\mu,\tau}$ and L ($\Delta L=2$)

Which option is realized in nature?

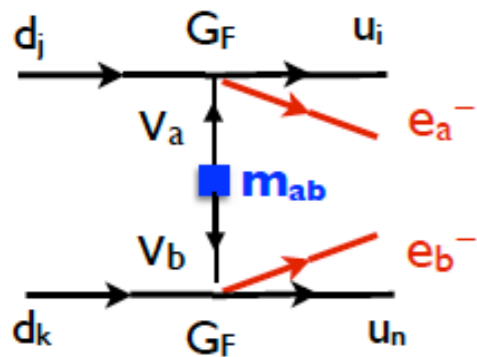
- Smallness of ν mass and chiral nature of the weak interactions implies that *neutrino-less processes are the best probes of $\Delta L=2$ interactions*



A Majorana neutrino with helicity=+1 (R-handed) will produce μ^+ .
But fraction of R-helicity ν 's produced in $\pi^+ \rightarrow \mu^+ \nu_\mu$ is $\sim (m_\nu/E_\nu)^2 < 10^{-16}!!$

Which option is realized in nature?

- Smallness of ν mass and chiral nature of the weak interactions implies that *neutrino-less processes are the best probes of $\Delta L=2$ interactions*



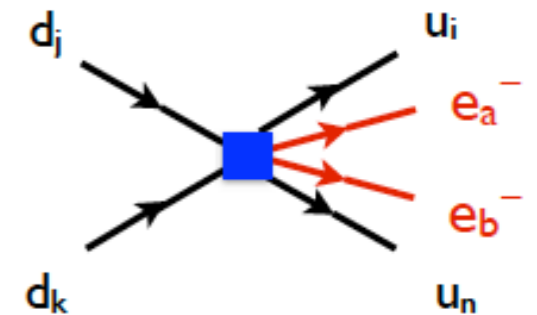
$$(N, Z) \rightarrow (N - 2, Z + 2) + e^- + e^-$$

$$K^+ \rightarrow \pi^- l_1^+ l_2^+ \quad B^+ \rightarrow h^- l_1^+ l_2^+$$

$$\tau^- \rightarrow l^+ h_1^- h_2^-$$

...

$$pp \rightarrow ll + 2 \text{ jets}$$

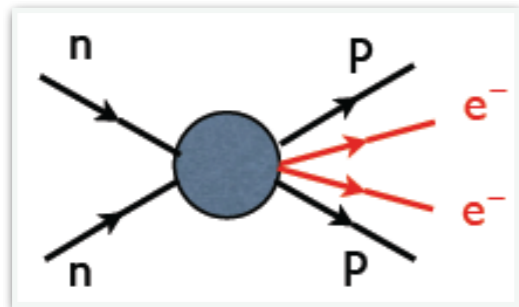


- $0\nu\beta\beta$ provides in many scenarios the strongest sensitivity to LNV couplings (“Avogadro’s number wins”, P. Vogel)
- Other processes can be very competitive in models with low-scale LNV

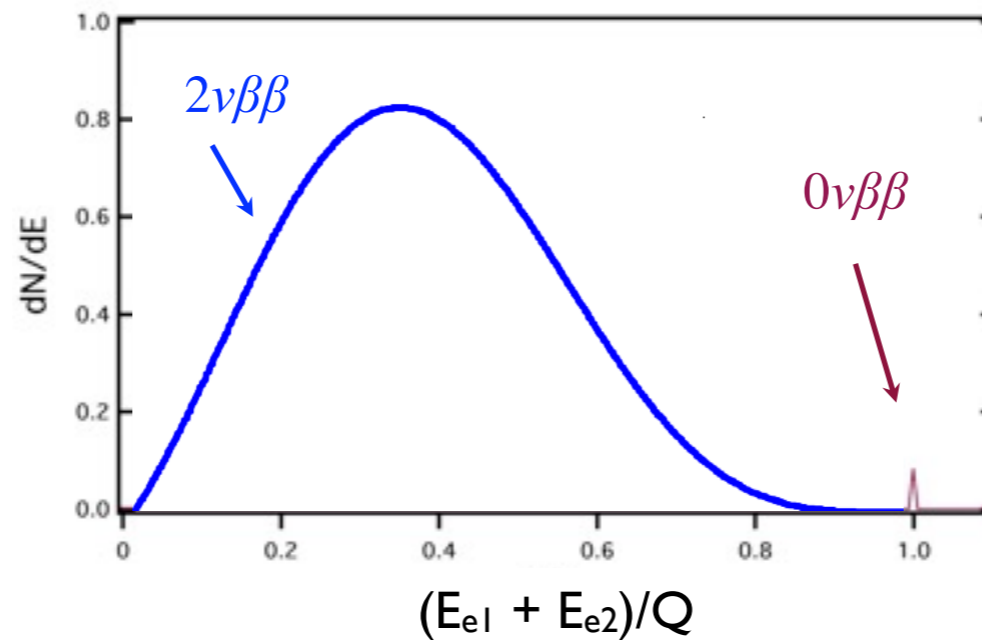
Neutrinoless double beta decay

$$(N, Z) \rightarrow (N - 2, Z + 2) + e^- + e^-$$

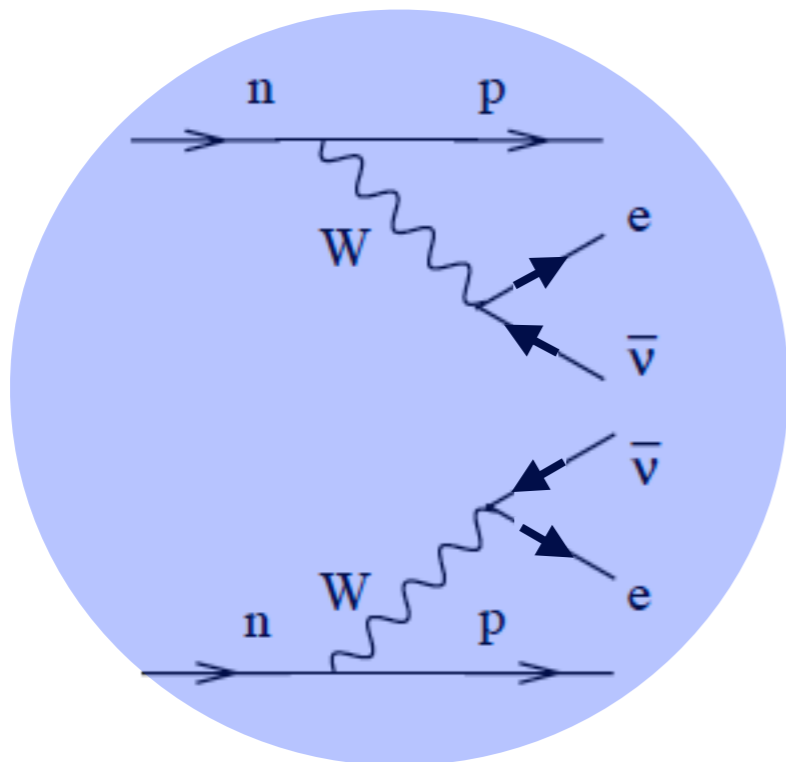
$$T_{1/2} > \# 10^{25} \text{ yr}$$



$\Delta L=2$



Potentially observable in certain even-even nuclei (^{48}Ca , ^{76}Ge , ^{136}Xe , ...) for which single beta decay is energetically forbidden

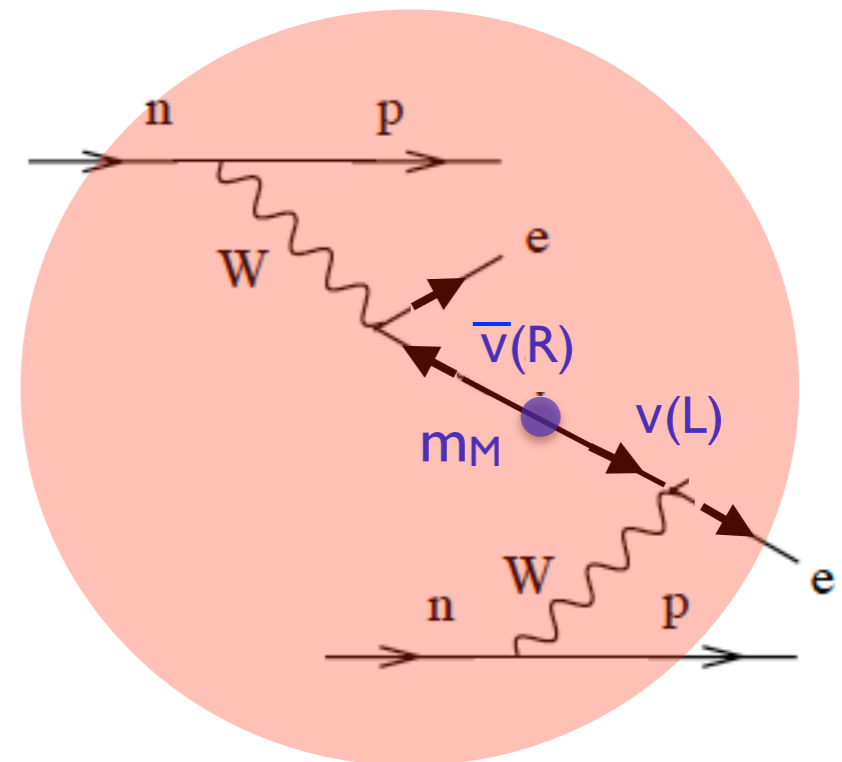


Simplest mechanism:
Majorana mass term



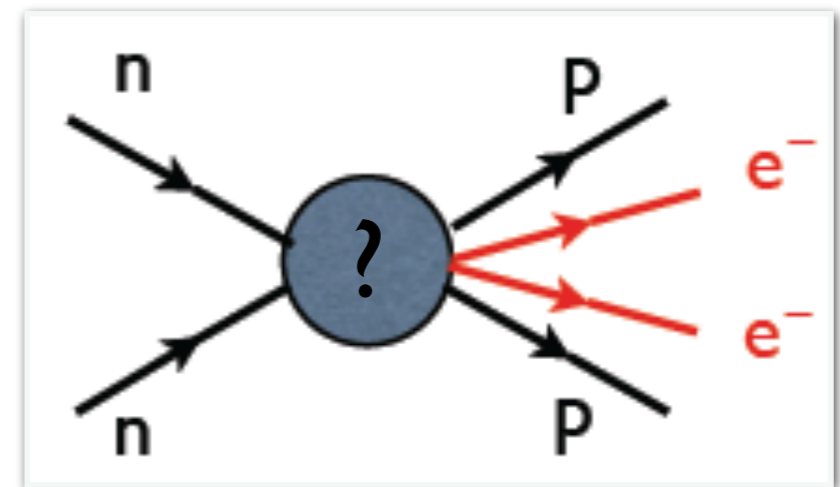
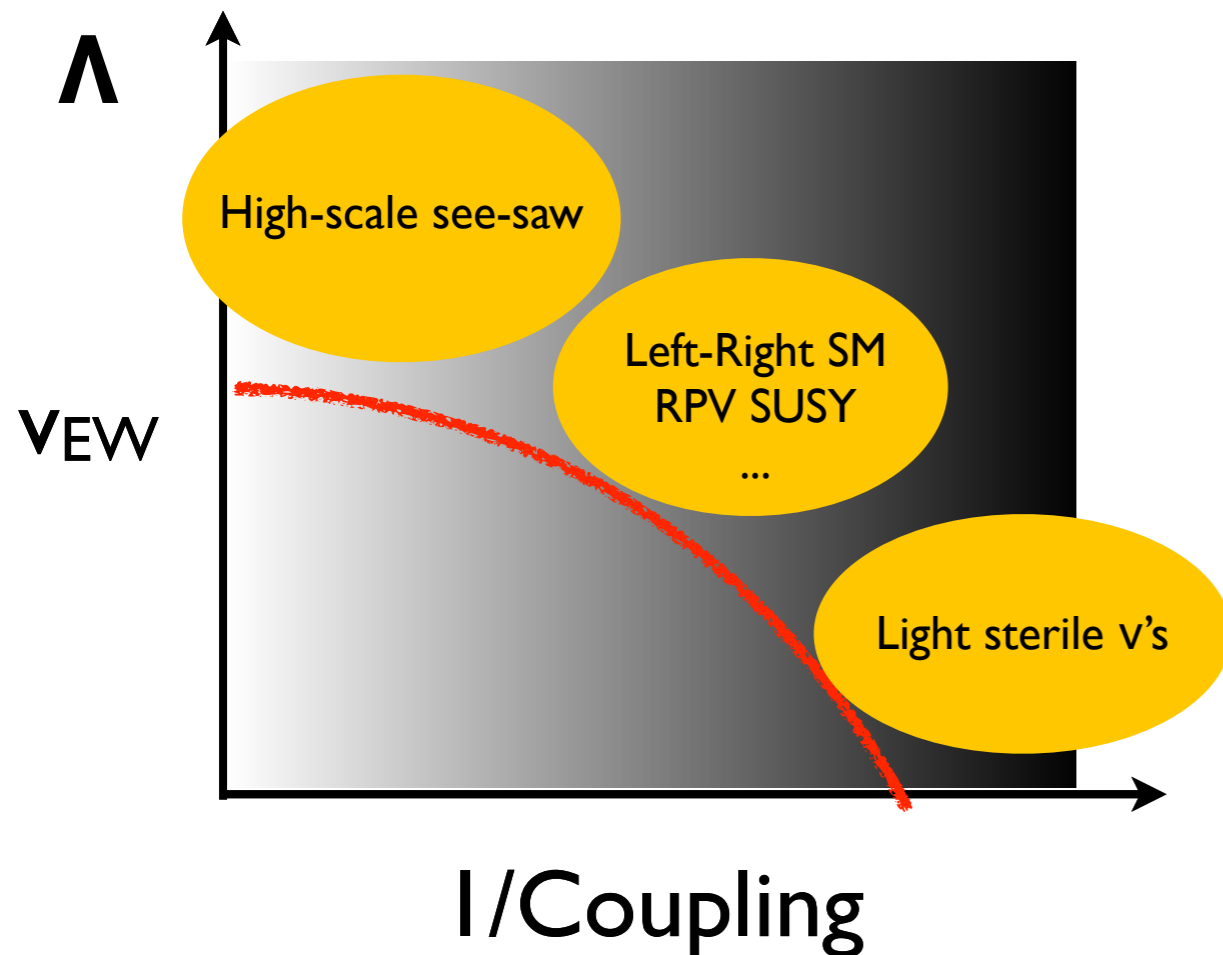
But not the only one!

Furry 1939



$0\nu\beta\beta$ physics reach

- Ton-scale $0\nu\beta\beta$ searches ($T_{1/2} > 10^{27-28}$ yr) will probe LNV from a broad range of mechanisms

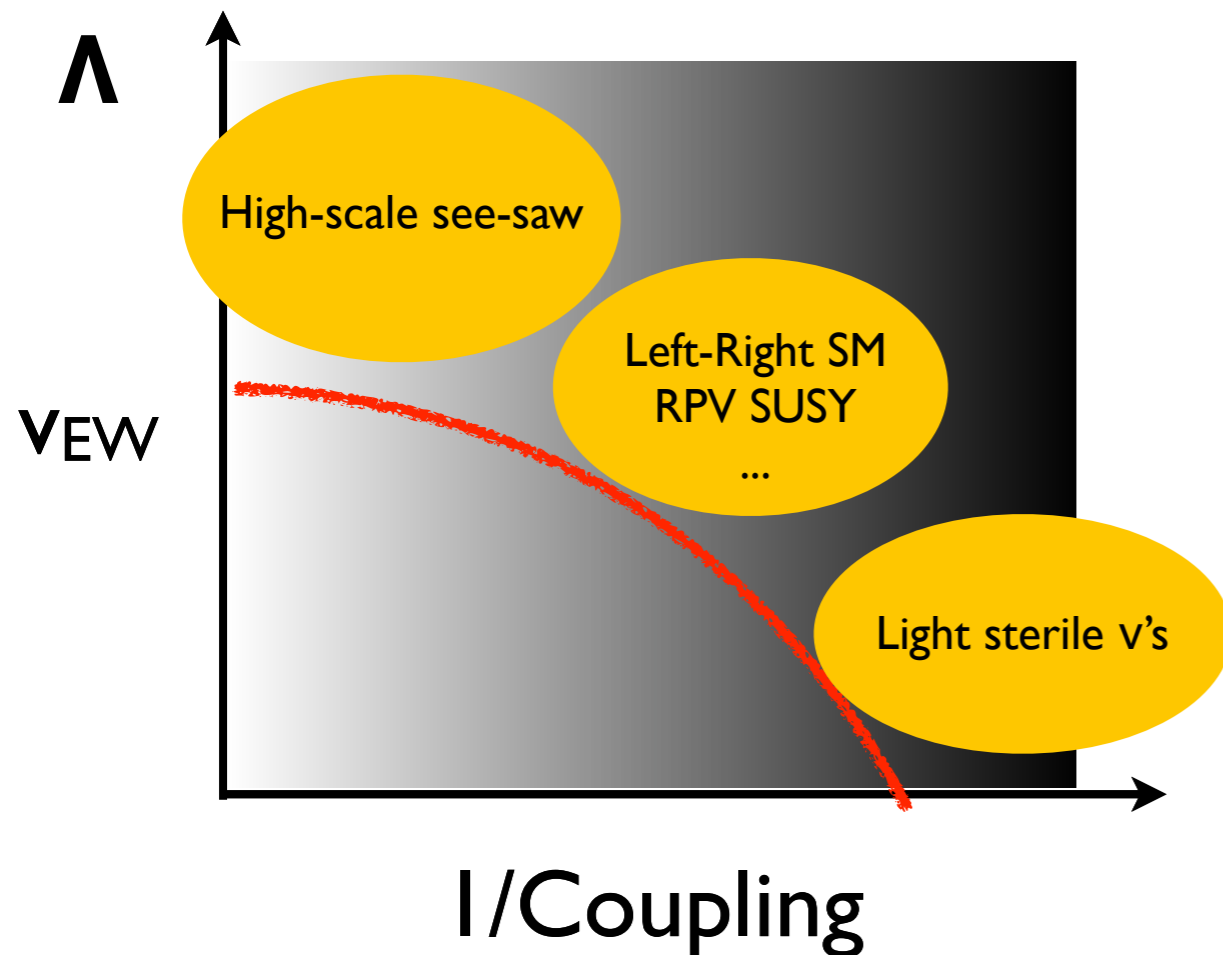


See [VC-Dekens-deVries-Graesser-Mereghetti 1806.02780](#) and references therein

Snowmass white paper: [2203.21169](#)

$0\nu\beta\beta$ physics reach

- Ton-scale $0\nu\beta\beta$ searches ($T_{1/2} > 10^{27-28}$ yr) will probe LNV from a broad range of mechanisms

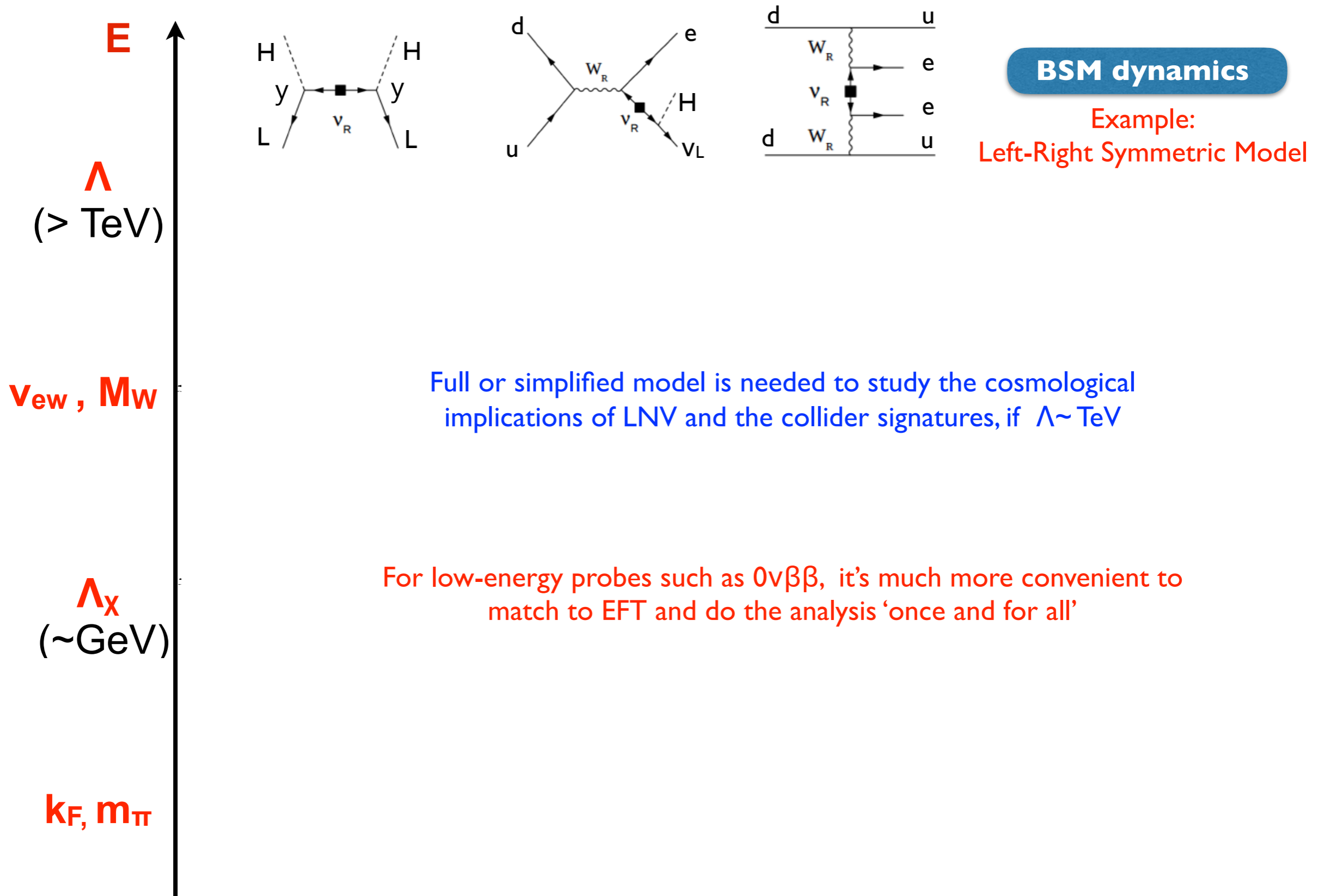


Impact of $0\nu\beta\beta$ searches and relation to other probes of LNV is best analyzed through a **tower of EFTs** that connect LNV scale Λ to nuclear scales, with controllable uncertainties

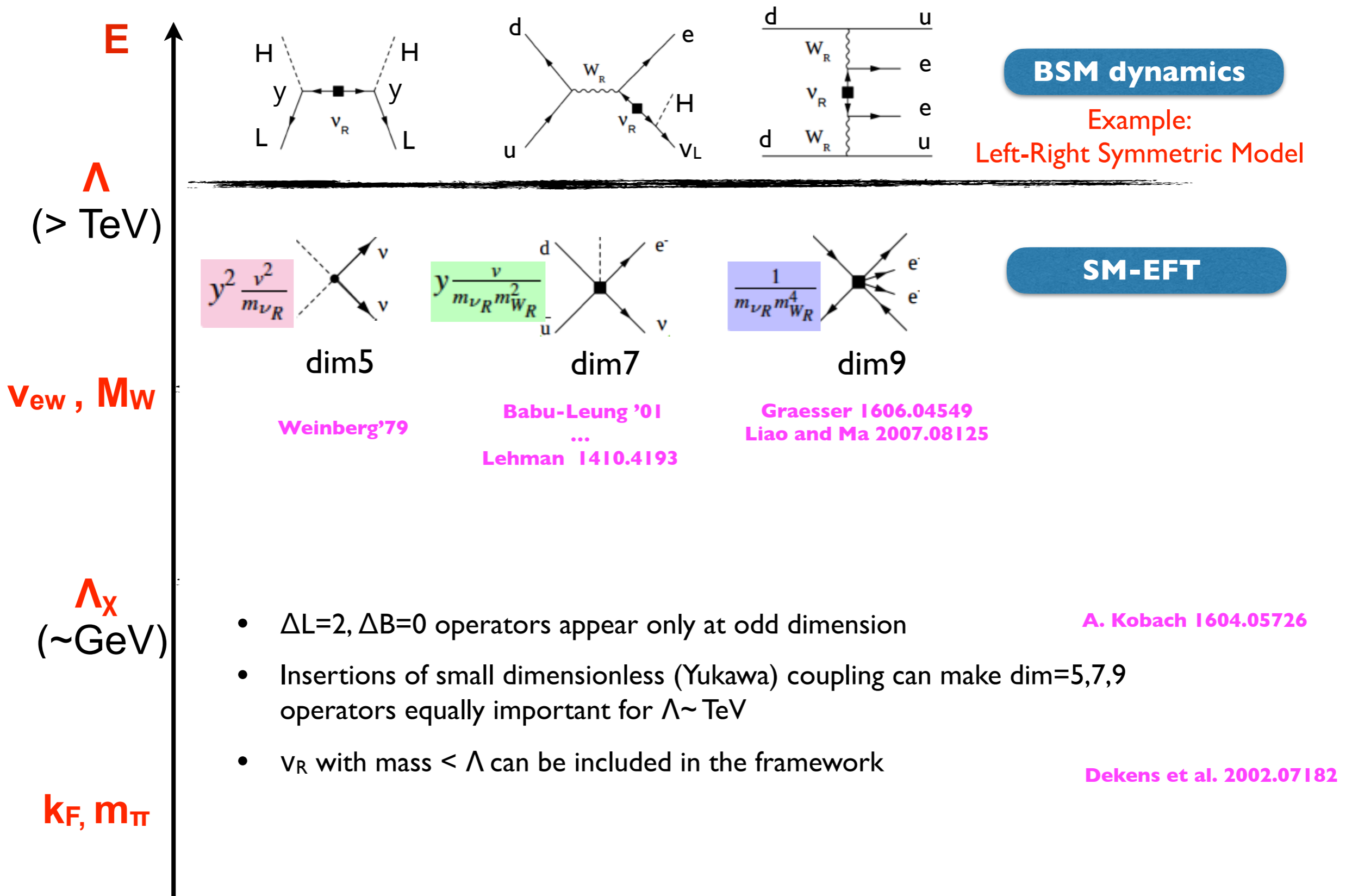
See [VC-Dekens-deVries-Graesser-Mereghetti 1806.02780](#) and references therein

Snowmass white paper: [2203.21169](#)

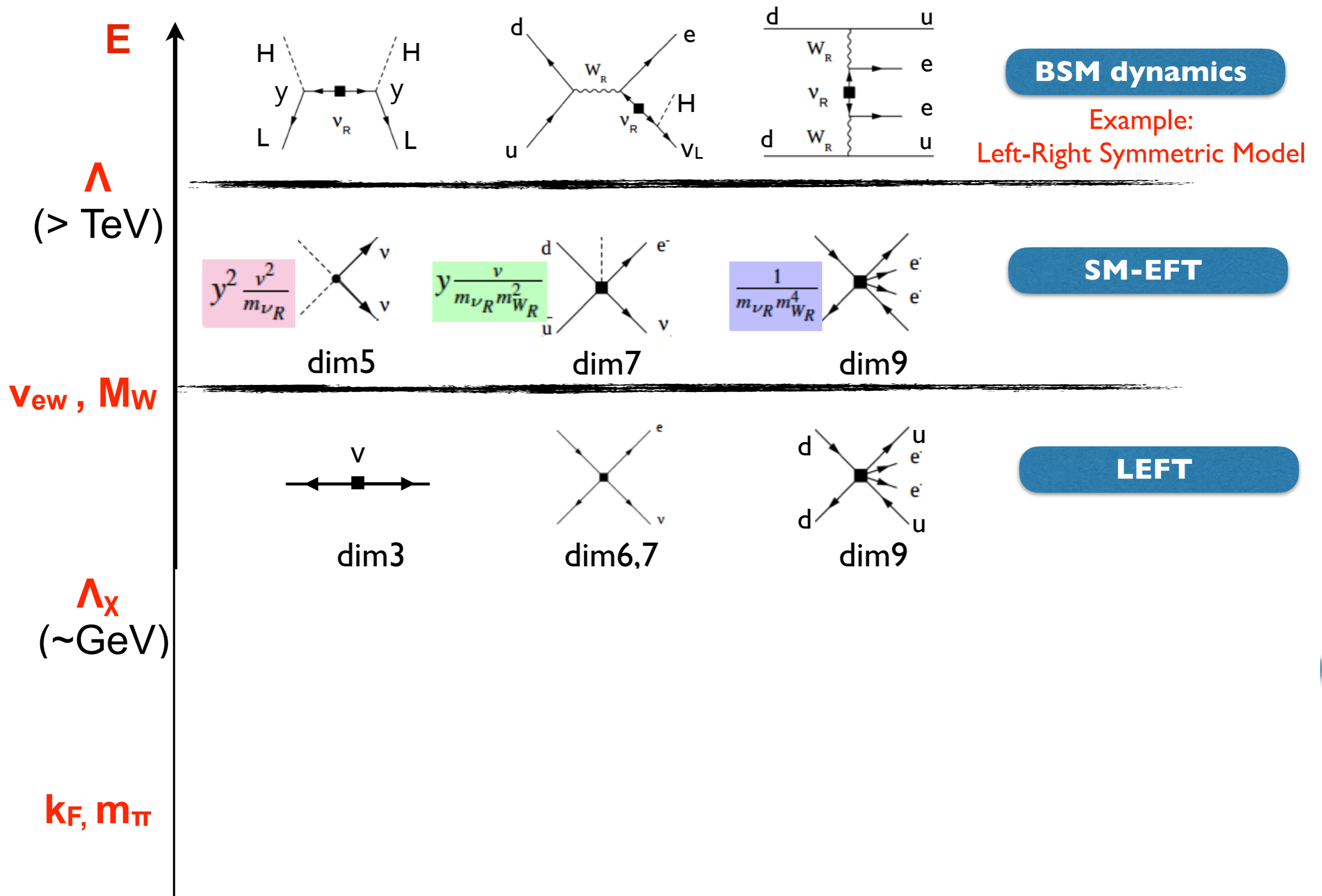
'End-to-end' EFT framework



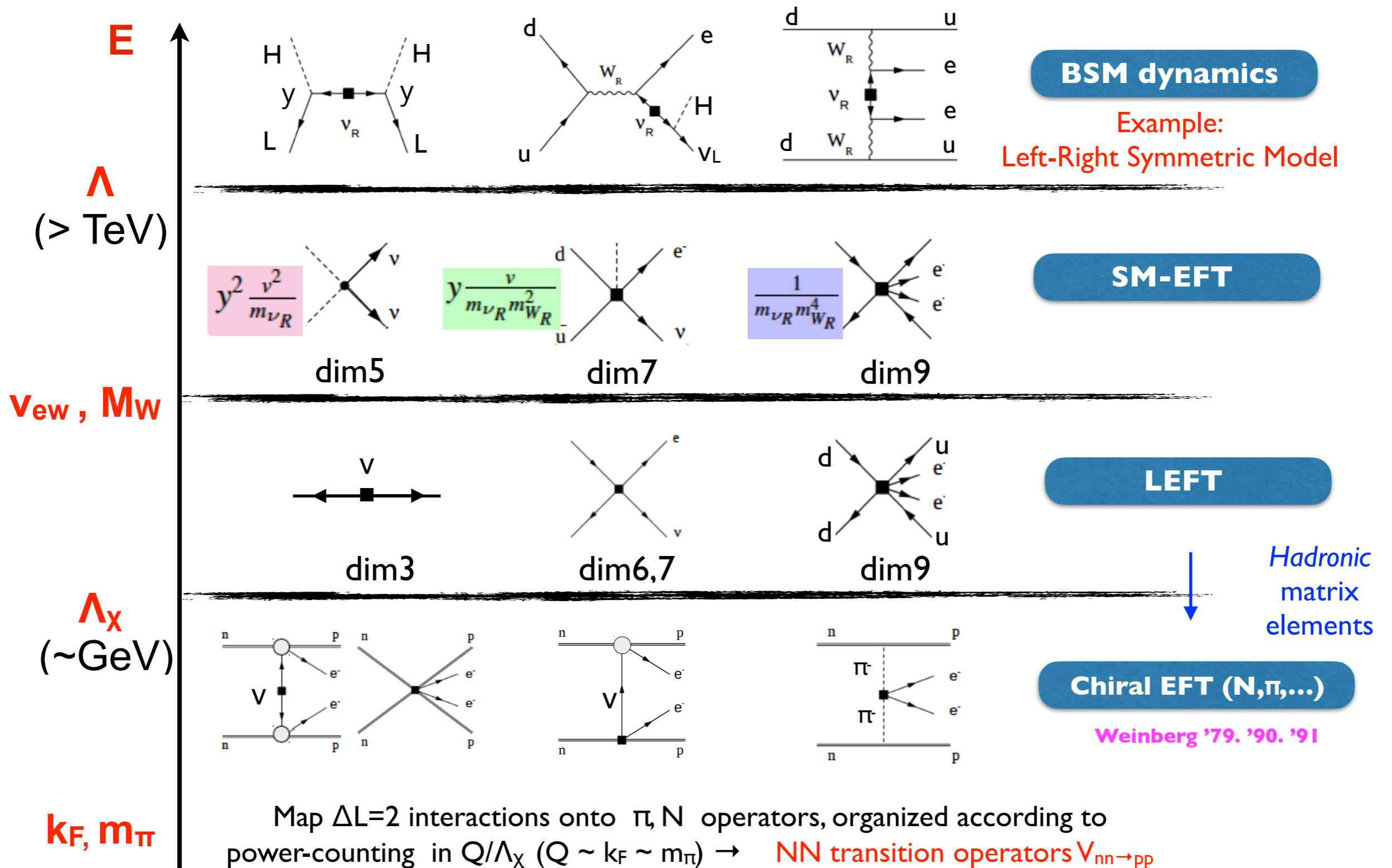
'End-to-end' EFT framework



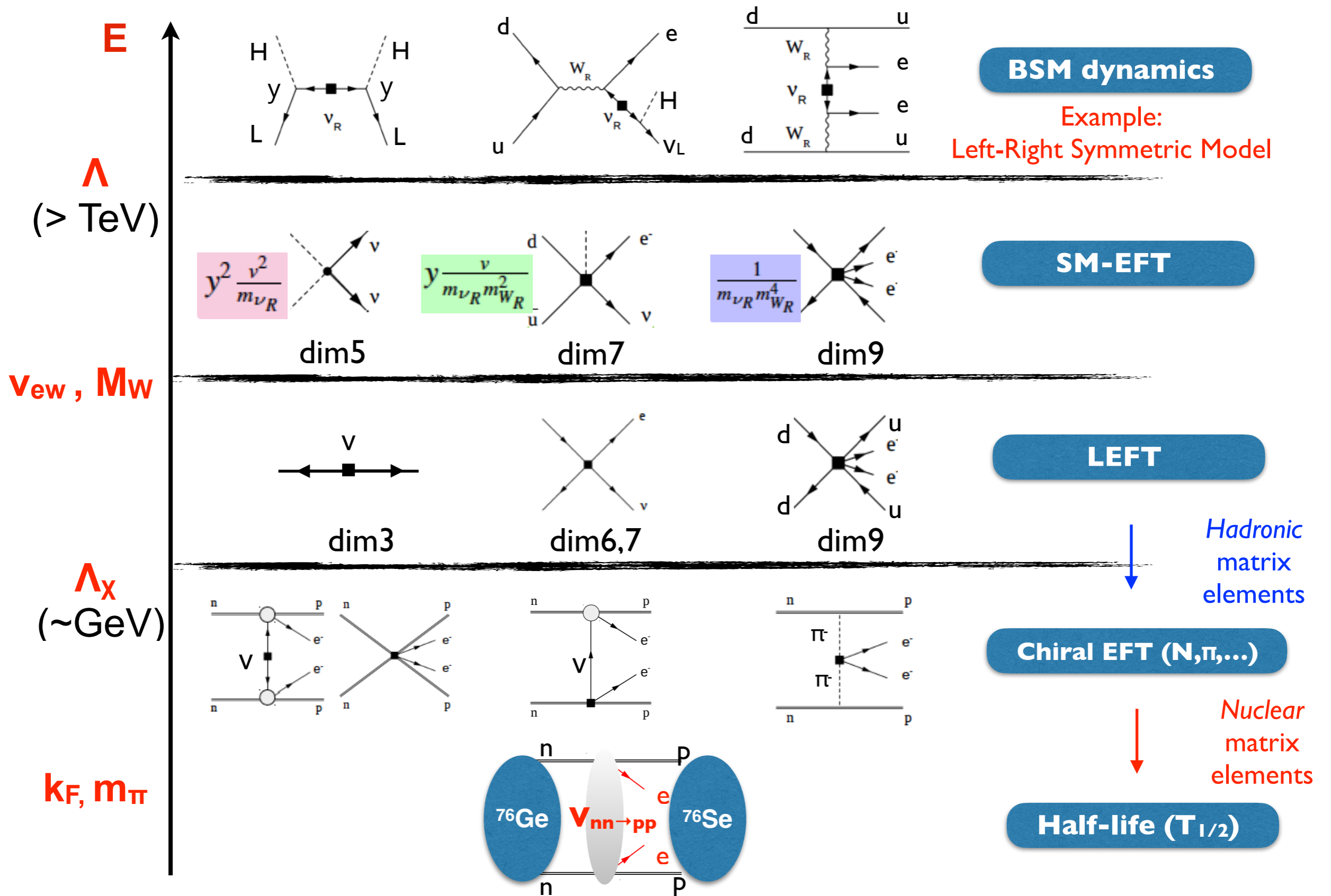
'End-to-end' EFT framework



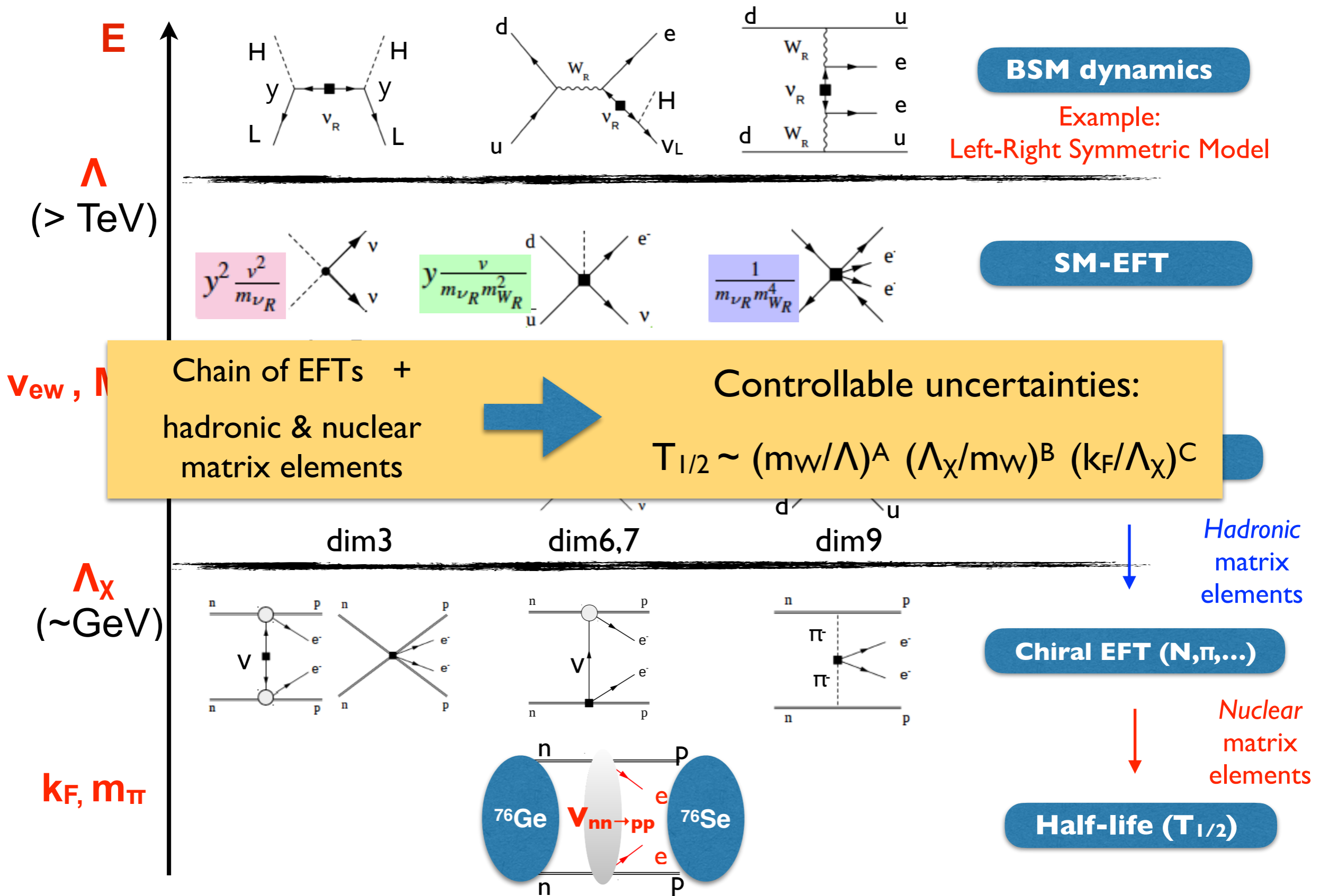
'End-to-end' EFT framework



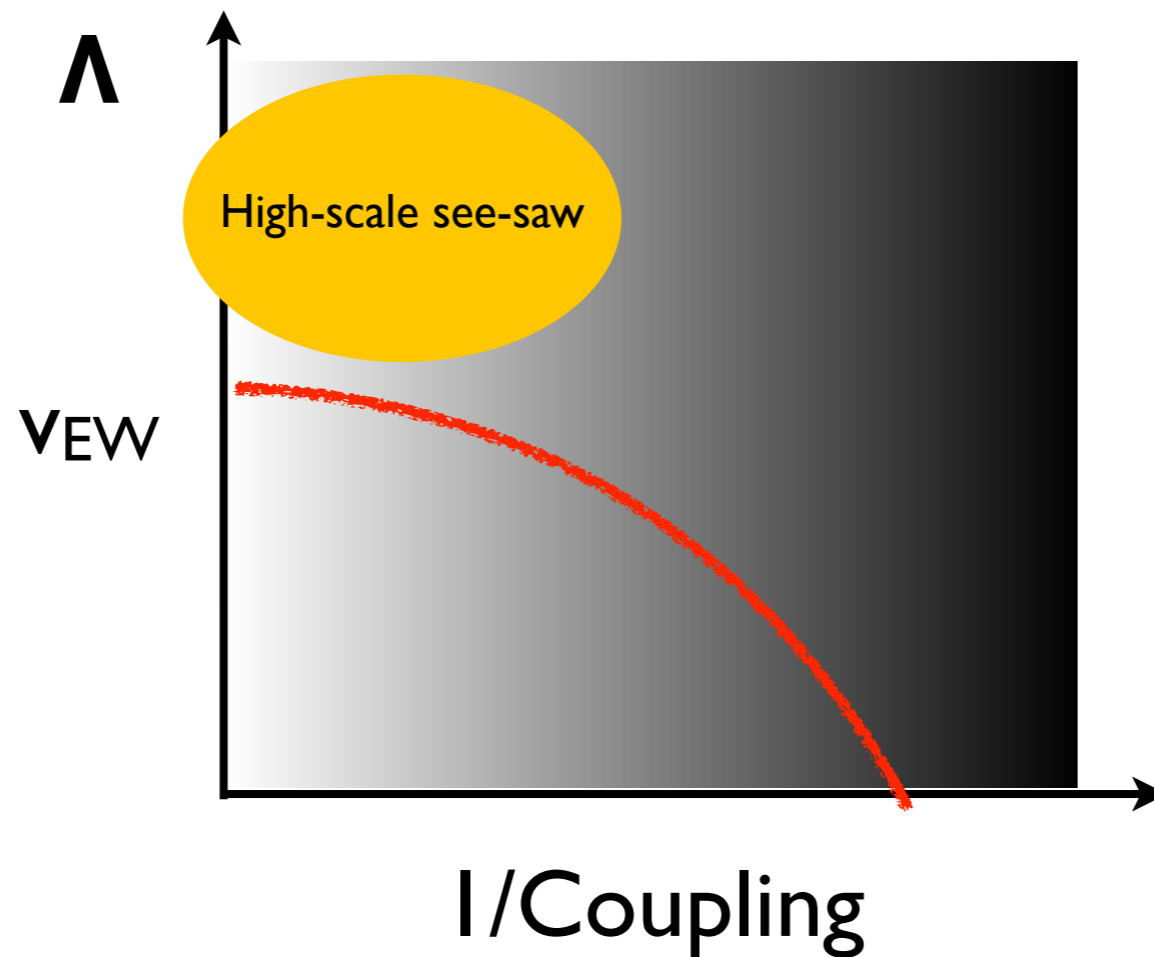
'End-to-end' EFT framework



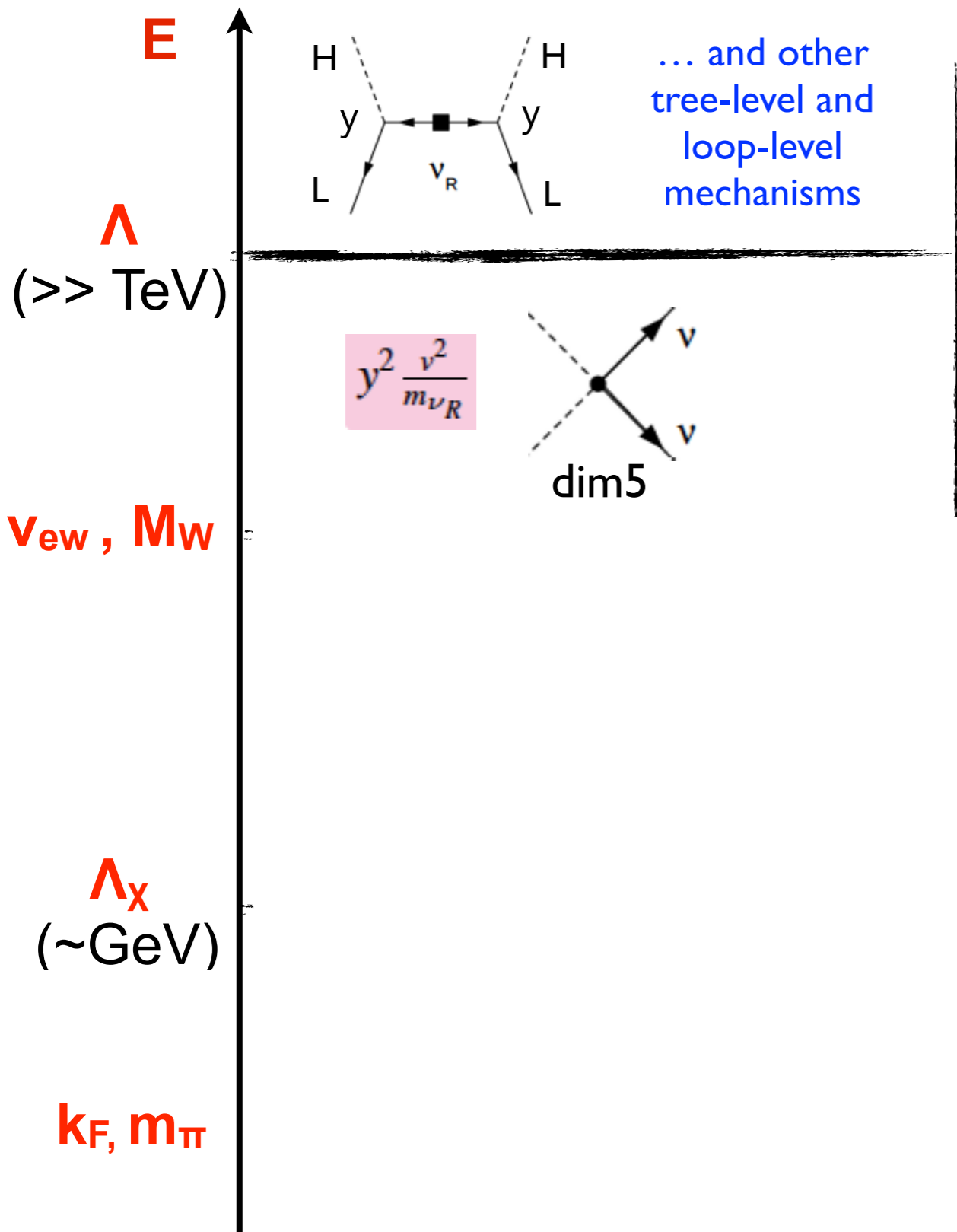
'End-to-end' EFT framework



$0\nu\beta\beta$ from high-scale LNV (dim-5 operator)



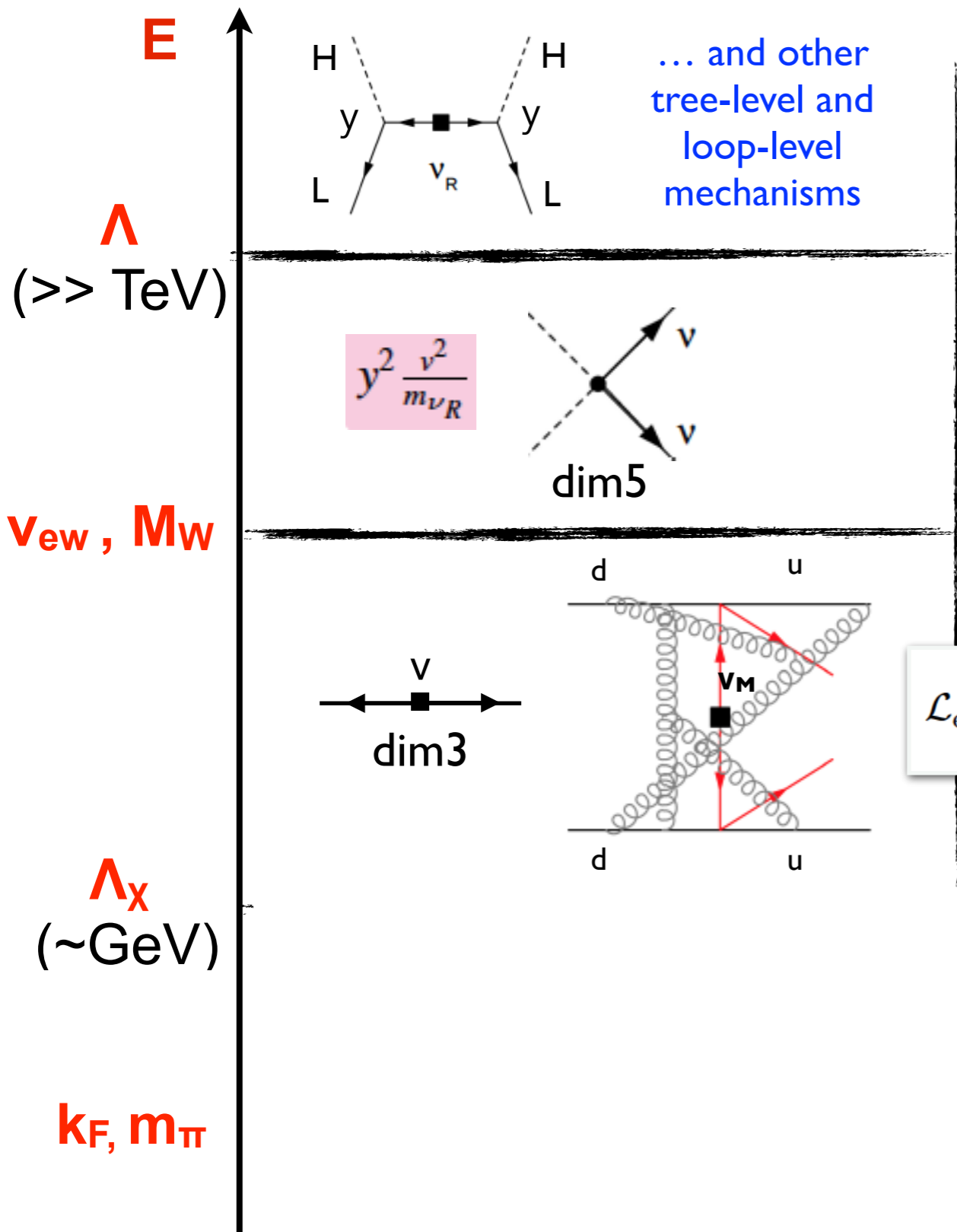
High scale LNV



- LNV originates at very high scale ($\Lambda \gg v$) \rightarrow dominant low-energy remnant is Weinberg's dim-5 operator:

$$\mathcal{L}_5 = \frac{w_{\alpha\alpha'}}{\Lambda} L_\alpha^T C \epsilon H H^T \epsilon L_{\alpha'}$$

High scale LNV



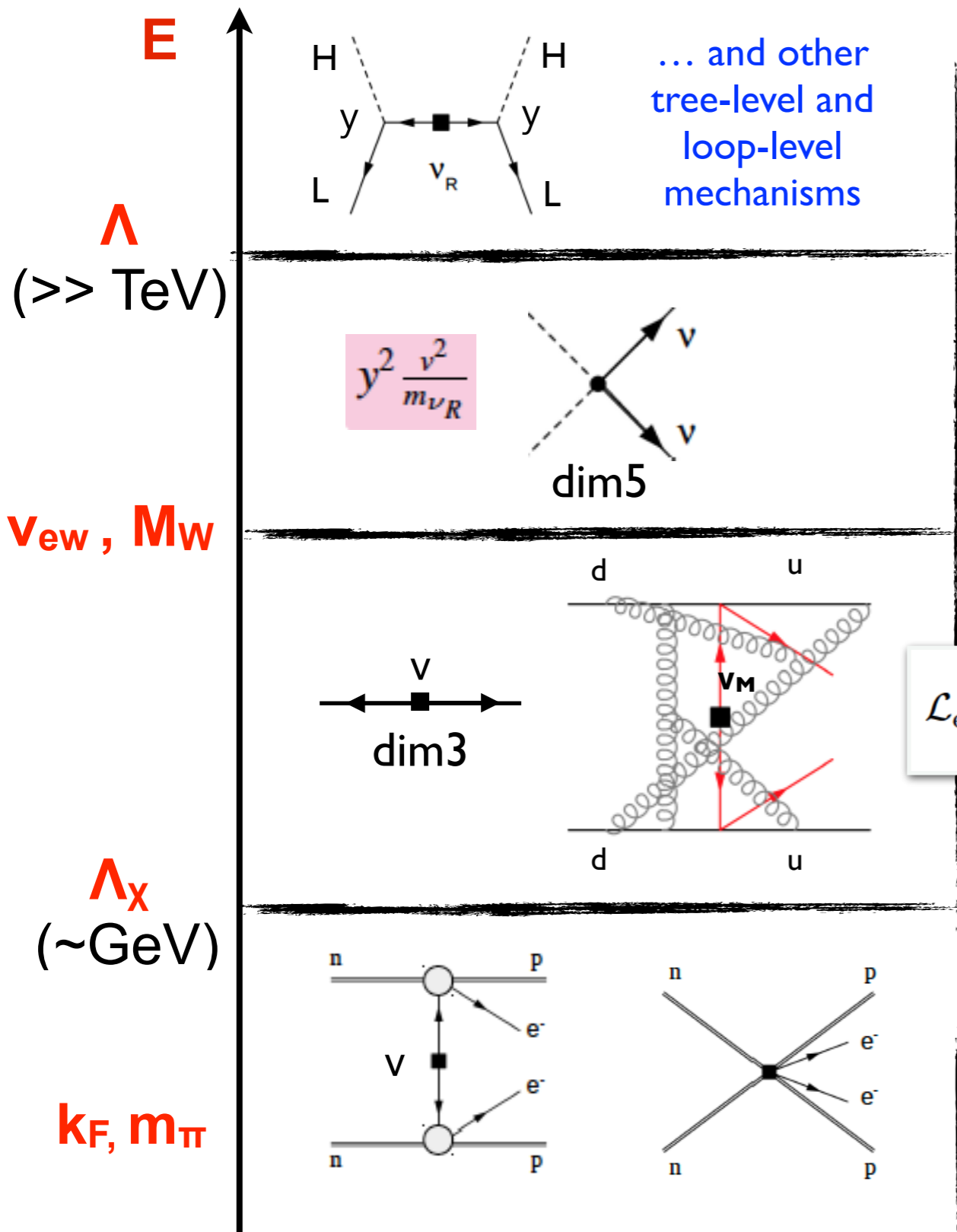
- LNV originates at very high scale ($\Lambda \gg v$) \rightarrow dominant low-energy remnant is Weinberg's dim-5 operator:

$$\mathcal{L}_5 = \frac{w_{\alpha\alpha'}}{\Lambda} L_\alpha^T C \epsilon H H^T \epsilon L_{\alpha'}$$

- Below the weak scale this is just the neutrino Majorana mass ($m_{\beta\beta} \sim w_{ee} v^2/\Lambda$)

$$\mathcal{L}_{\text{eff}} = \mathcal{L}_{\text{QCD}} - \frac{4G_F}{\sqrt{2}} V_{ud} \bar{u}_L \gamma^\mu d_L \bar{e}_L \gamma_\mu \nu_{eL} - \frac{m_{\beta\beta}}{2} \nu_{eL}^T C \nu_{eL} + \text{H.c.}$$

High scale LNV



... and other tree-level and loop-level mechanisms

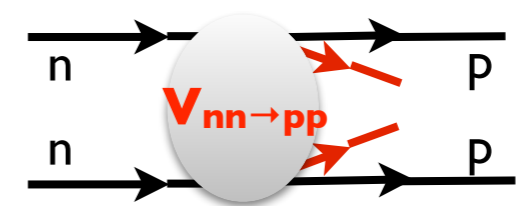
- LNV originates at very high scale ($\Lambda \gg v$) \rightarrow dominant low-energy remnant is Weinberg's dim-5 operator:

$$\mathcal{L}_5 = \frac{w_{\alpha\alpha'}}{\Lambda} L_\alpha^T C \epsilon H H^T \epsilon L_{\alpha'}$$

- Below the weak scale this is just the neutrino Majorana mass ($m_{\beta\beta} \sim w_{ee} v^2/\Lambda$)

$$\mathcal{L}_{\text{eff}} = \mathcal{L}_{\text{QCD}} - \frac{4G_F}{\sqrt{2}} V_{ud} \bar{u}_L \gamma^\mu d_L \bar{e}_L \gamma_\mu \nu_{eL} - \frac{m_{\beta\beta}}{2} \nu_{eL}^T C \nu_{eL} + \text{H.c.}$$

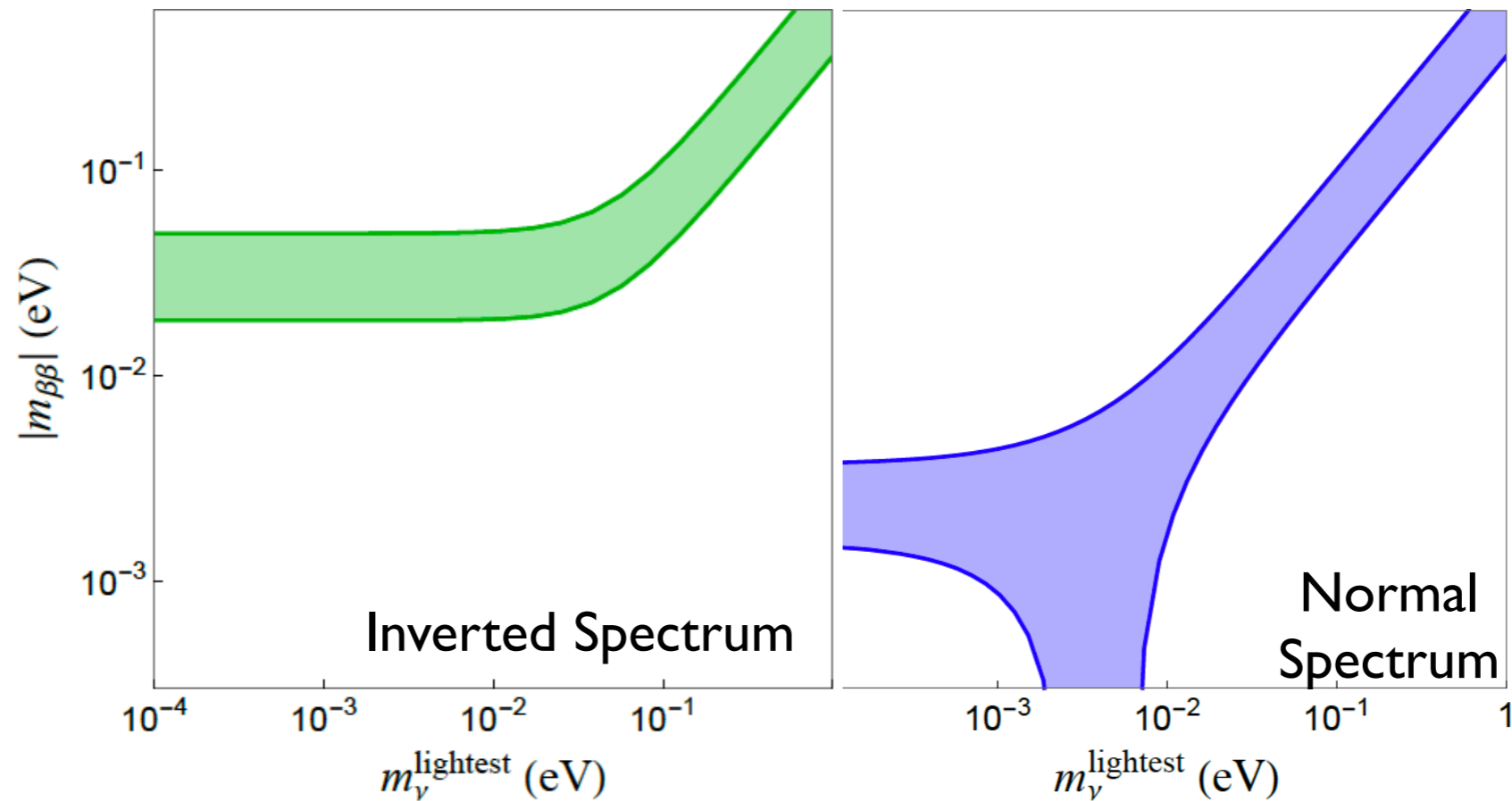
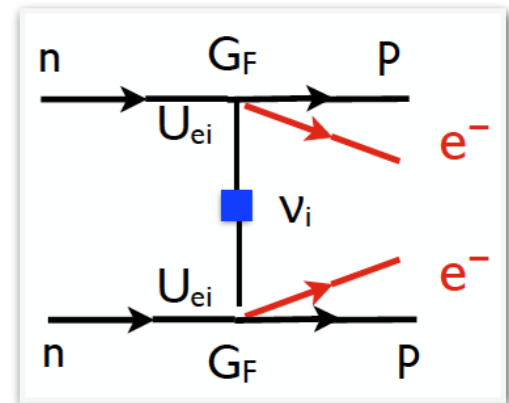
- $0\nu\beta\beta$ mediated by *active* ν_M with potential $V_{nn \rightarrow pp}$ with long- and short-range components proportional to $m_{\beta\beta}$



Discovery potential / target

- In this case $0\nu\beta\beta$ is a *direct* probe of ν Majorana mass: $\Gamma \propto |M_{0\nu}|^2 (m_{\beta\beta})^2$

$$\langle m_{\beta\beta} \rangle^2 = \left| \sum_i U_{ei}^2 m_{\nu i} \right|^2$$

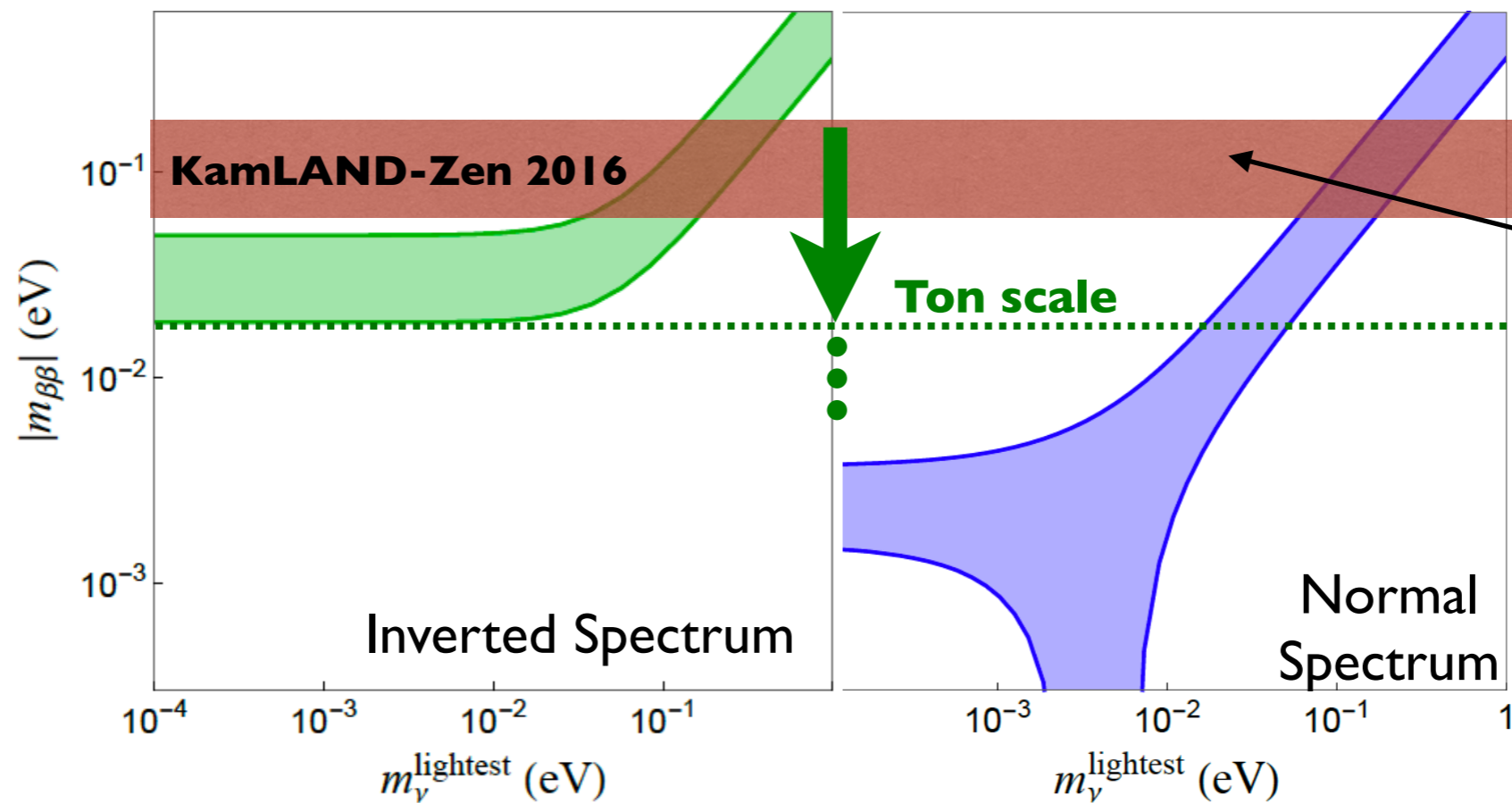
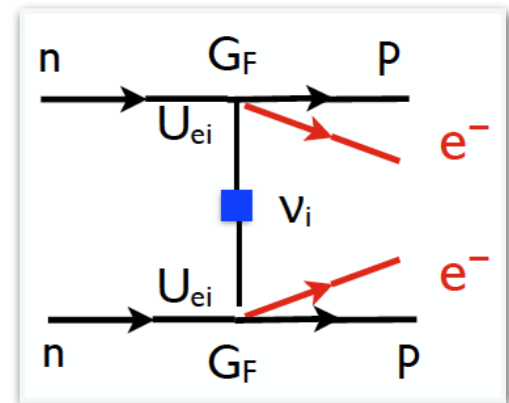


Bands: unknown Majorana phases

Discovery potential / target

- In this case $0\nu\beta\beta$ is a *direct* probe of ν Majorana mass: $\Gamma \propto |M_{0\nu}|^2 (m_{\beta\beta})^2$

$$\langle m_{\beta\beta} \rangle^2 = \left| \sum_i U_{ei}^2 m_{\nu i} \right|^2$$



Bands: unknown Majorana phases

Assume range for nuclear matrix elements from different nuclear calculations

Assuming current range for matrix elements, discovery @ ton-scale possible for **inverted spectrum** or **$m_{\text{lightest}} > 50 \text{ meV}$**

Diagnosing power

- High scale seesaw implies falsifiable correlation with other ν mass probes. Future data can unravel new LNV sources or physics beyond “ Λ CDM + m_ν ”

$$m_{\beta\beta} = \left| \sum_i U_{ei}^2 m_i \right|$$

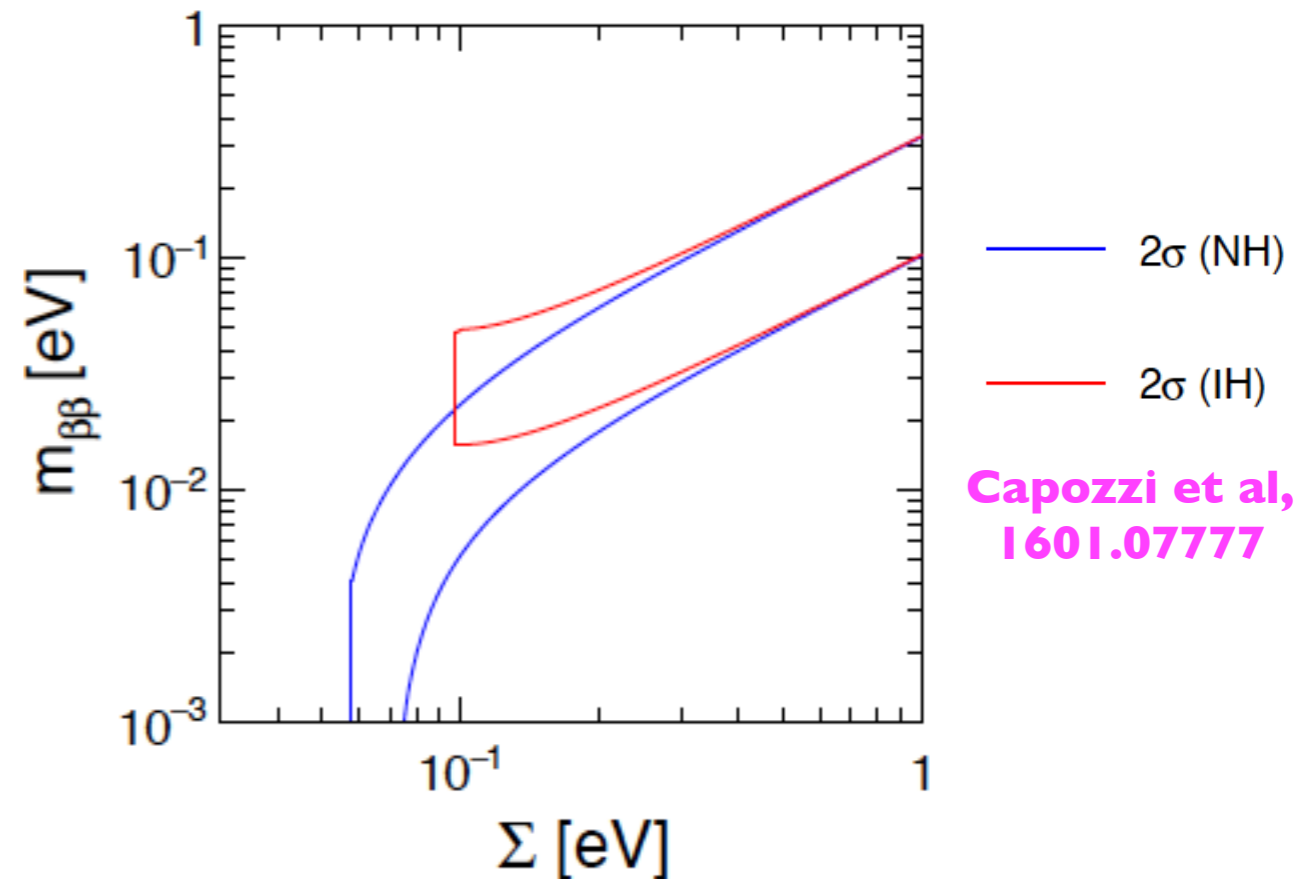
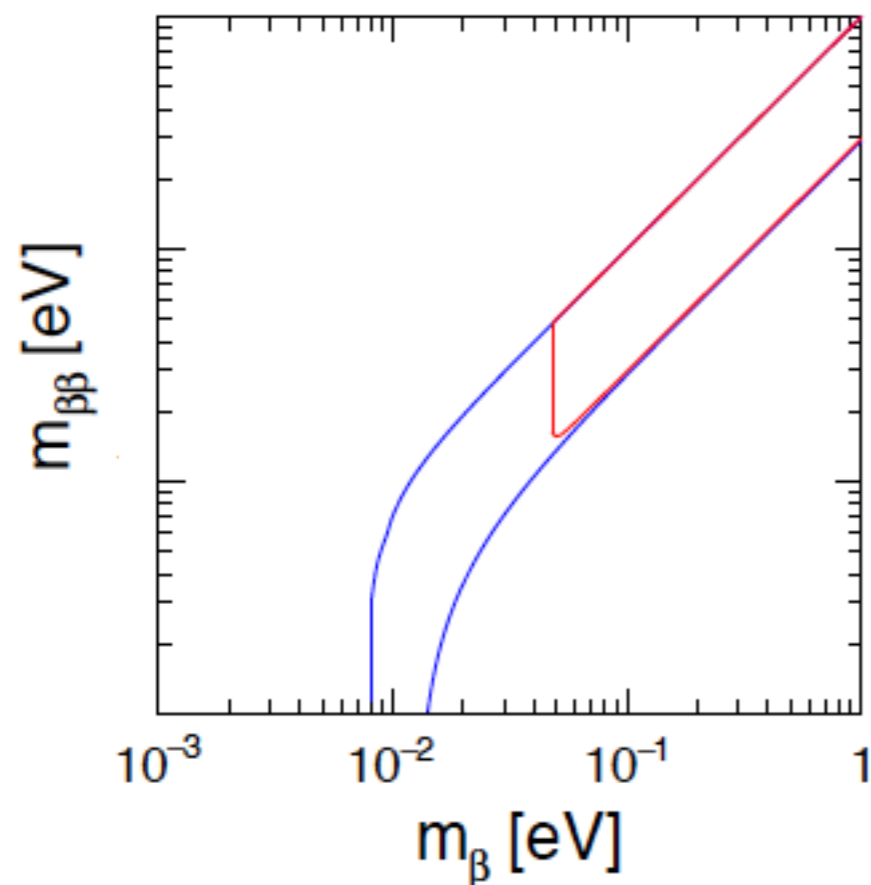
$0\nu\beta\beta$ decay

$$m_\beta = \sqrt{\sum_i |U_{ei}|^2 m_i^2}$$

Tritium β decay

$$\Sigma = \sum_i m_i$$

Cosmology



Capozzi et al,
1601.07777

Diagnosing power

- High scale seesaw implies falsifiable correlation with other ν mass probes. Future data can unravel new LNV sources or physics beyond “ Λ CDM + m_ν ”

$$m_{\beta\beta} = \left| \sum_i U_{ei}^2 m_i \right|$$

$0\nu\beta\beta$ decay

$$m_\beta = \sqrt{\sum_i |U_{ei}|^2 m_i^2}$$

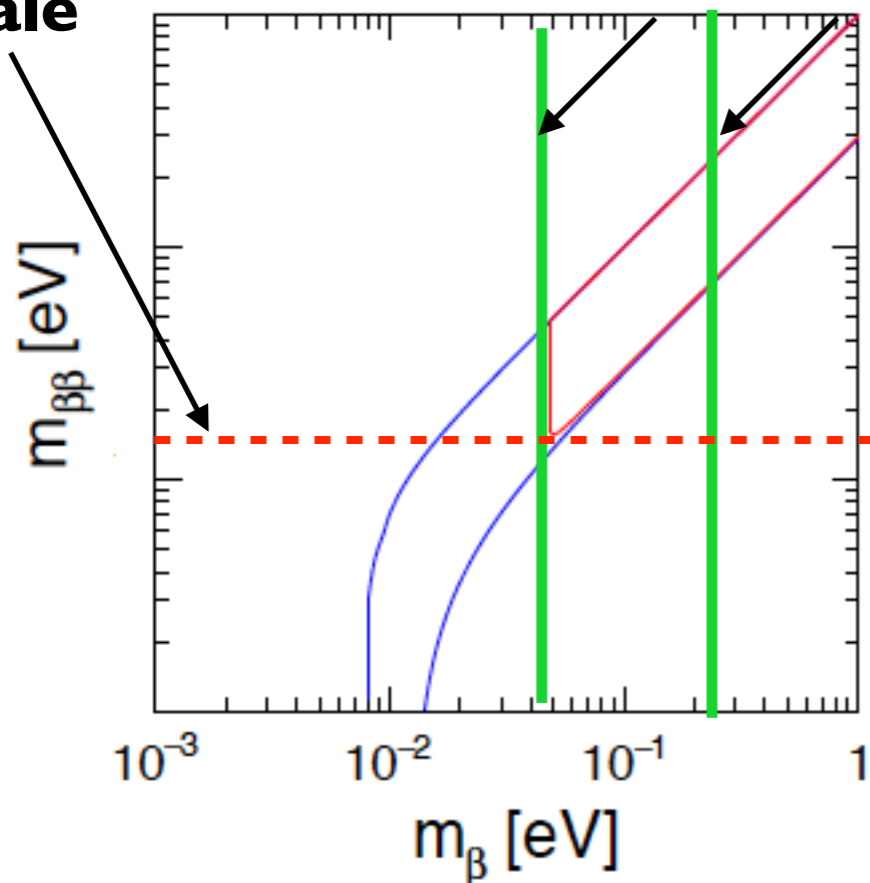
Tritium β decay

$$\Sigma = \sum_i m_i$$

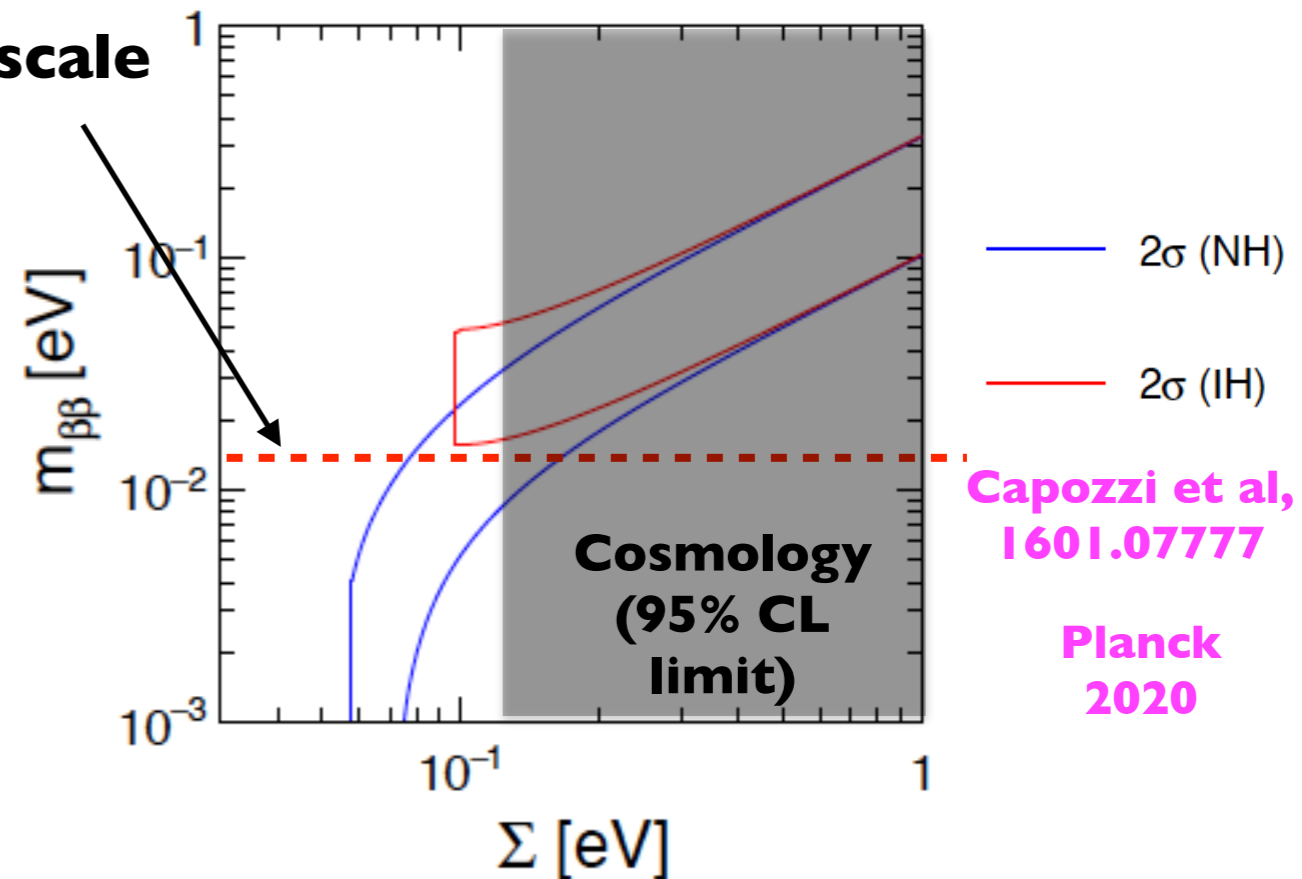
Cosmology

Project8 **KATRIN**

Ton scale



Ton scale



Diagnosing power

- High scale seesaw implies falsifiable correlation with other ν mass probes. Future data can unravel new LNV sources or physics beyond “ Λ CDM + m_ν ”

$$m_{\beta\beta} = \left| \sum_i U_{ei}^2 m_i \right|$$

$0\nu\beta\beta$ decay

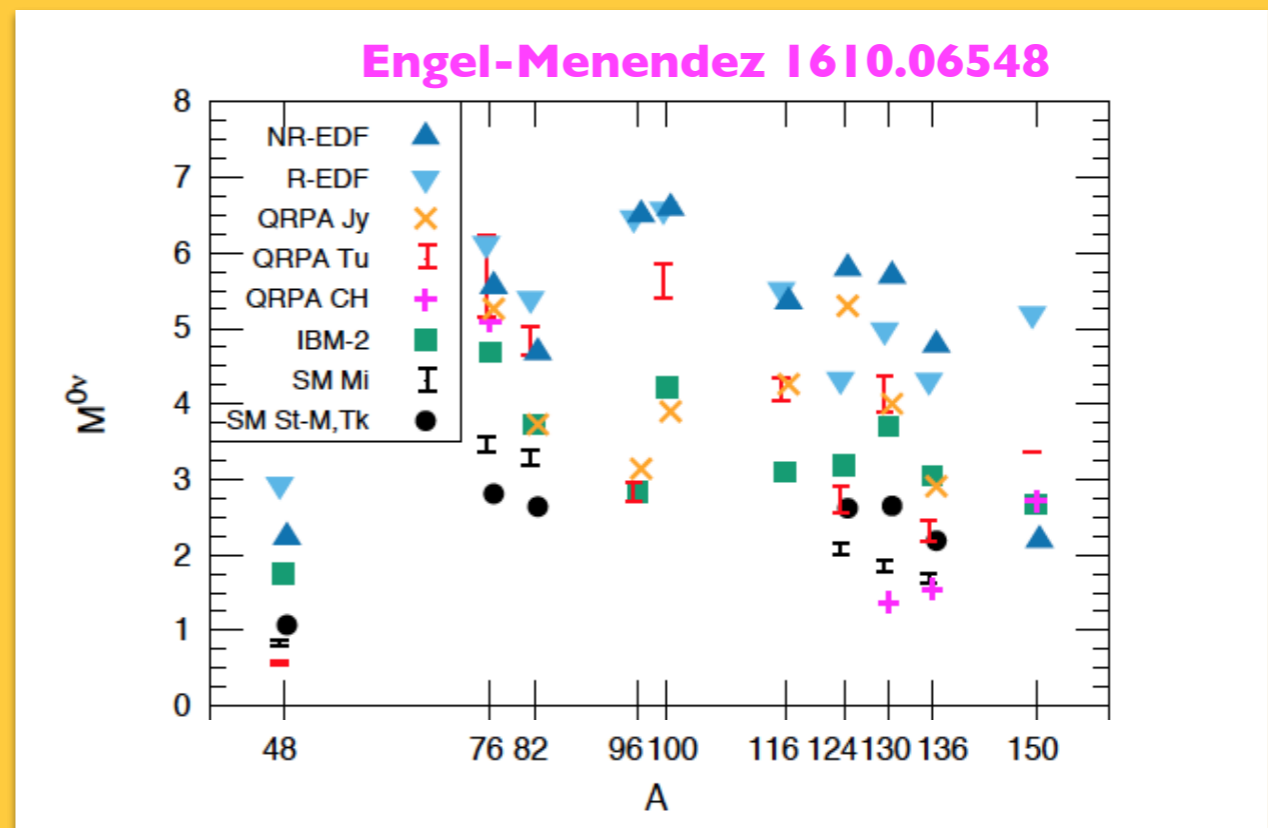
$$m_\beta = \sqrt{\sum_i |U_{ei}|^2 m_i^2}$$

Tritium β decay

$$\Sigma = \sum_i m_i$$

Cosmology

But these important *quantitative* connections require knowing nuclear matrix elements and their uncertainties!



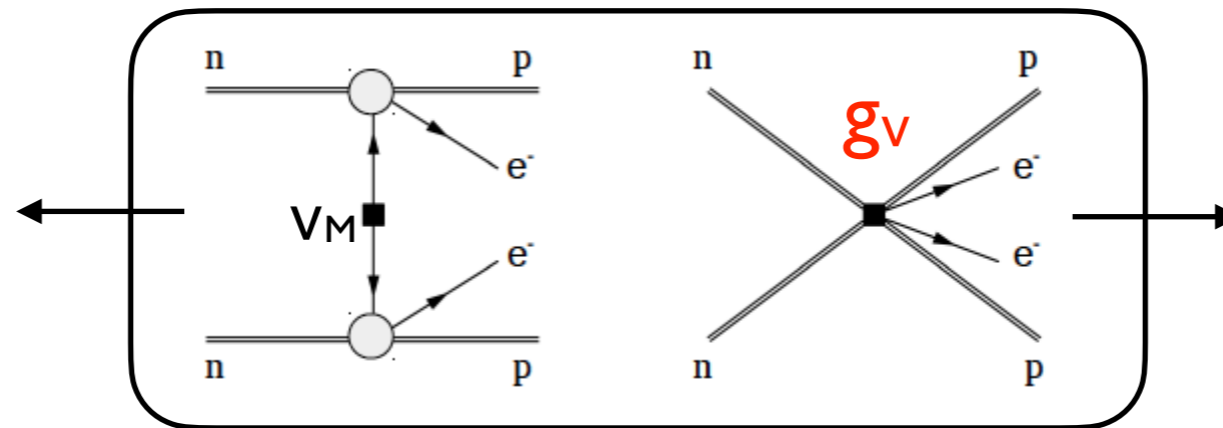
New insights from EFT

VC, W. Dekens, E. Mereghetti, A. Walker-Loud, 1710.01729

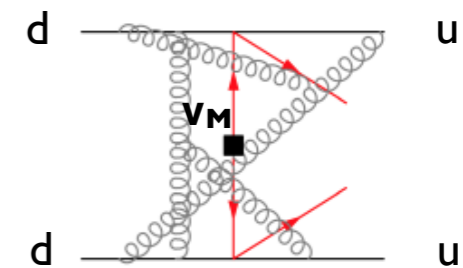
VC, W. Dekens, J. de Vries, M. Graesser, E. Mereghetti, S. Pastore, U. van Kolck 1802.10097

- Transition operator to leading order in Q/Λ_χ ($Q \sim k_F \sim m_\pi$, $\Lambda_\chi \sim \text{GeV}$)

'Usual' V_M exchange
 $\sim 1/k_F^2 \sim 1/Q^2$
 Coulomb-like potential



'New': short-range
 coupling $g_v \sim 1/Q^2$



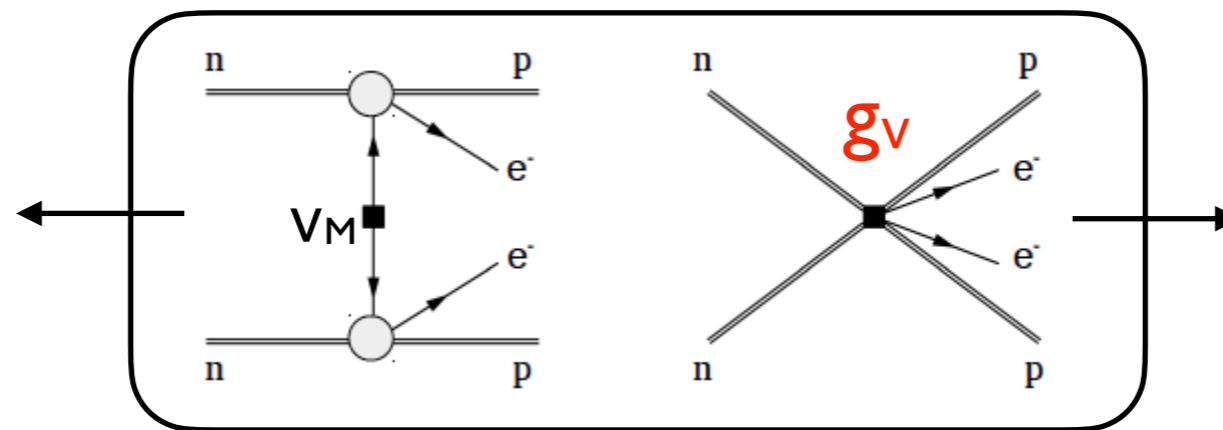
New insights from EFT

VC, W. Dekens, E. Mereghetti, A. Walker-Loud, 1710.01729

VC, W. Dekens, J. de Vries, M. Graesser, E. Mereghetti, S. Pastore, U. van Kolck 1802.10097

- Transition operator to leading order in Q/Λ_χ ($Q \sim k_F \sim m_\pi$, $\Lambda_\chi \sim \text{GeV}$)

'Usual' V_M exchange
 $\sim 1/k_F^2 \sim 1/Q^2$
 Coulomb-like potential

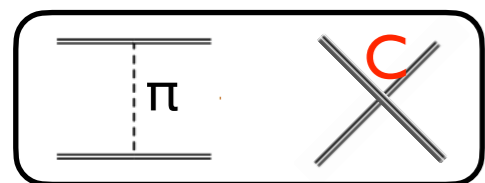


'New': short-range
 coupling $g_V \sim 1/Q^2$

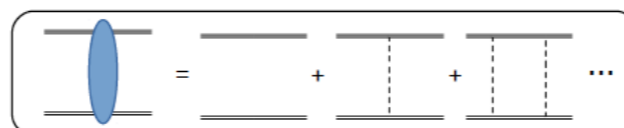
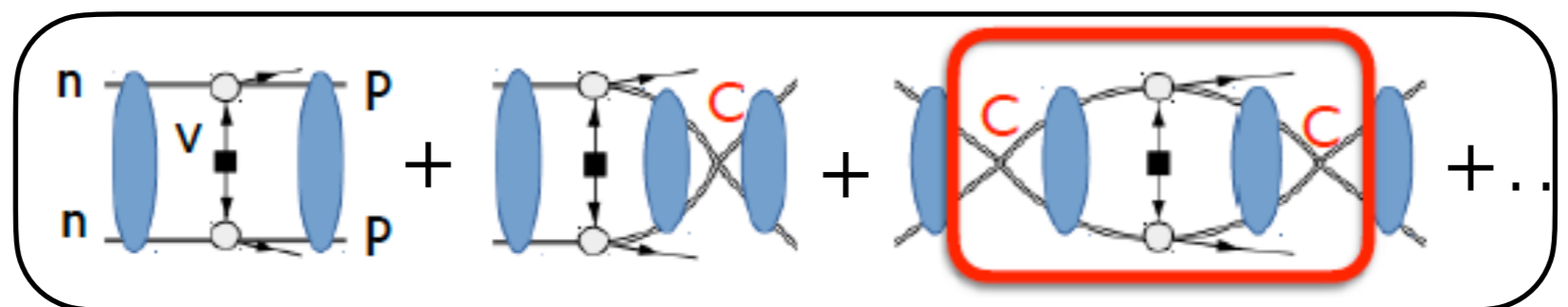
- Required by renormalization of $nn \rightarrow pp$ amplitude in presence of strong interactions

UV divergence $\propto (m_N C / 4\pi)^2 \sim 1/Q^2$

LO strong potential

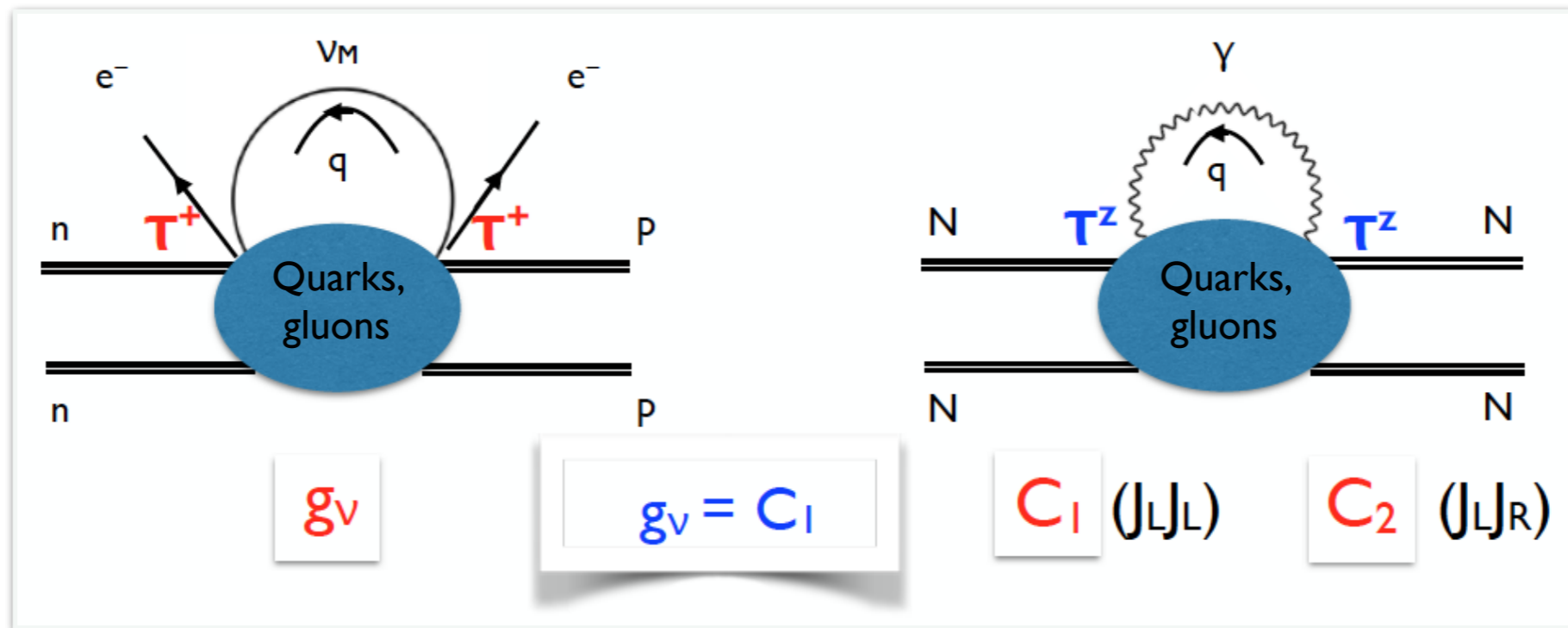


$C \sim 4\pi / (m_N Q)$



Connection with data?

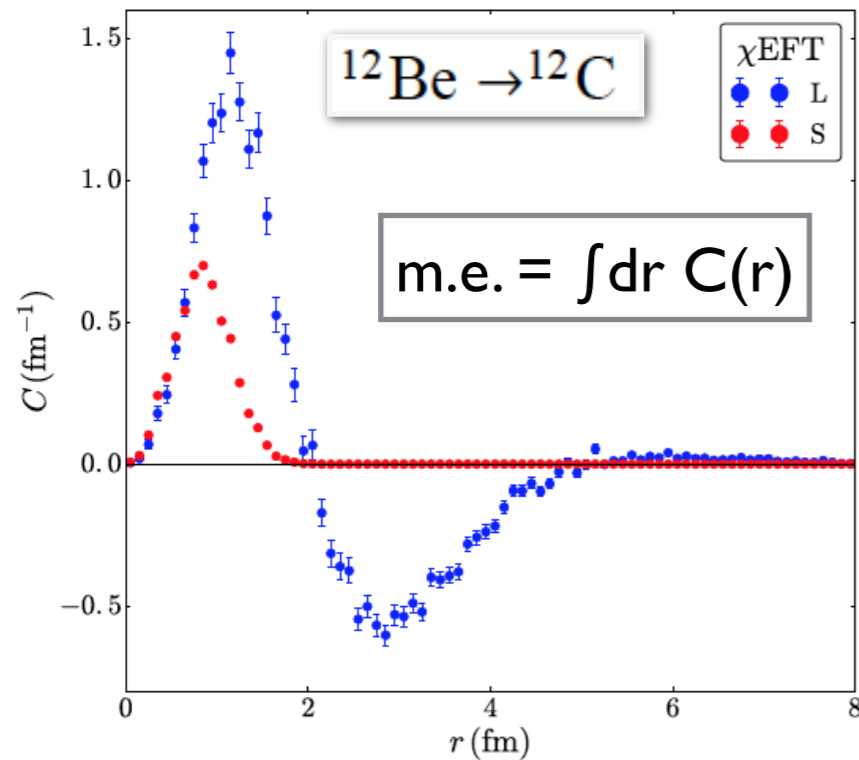
- Isospin symmetry relates g_v to one of two $I=2$ e.m. couplings (hard γ 's & ν 's)



- NN data ($a_{nn} + a_{pp} - 2a_{np}$) determine $C_1 + C_2$, confirming LO scaling!

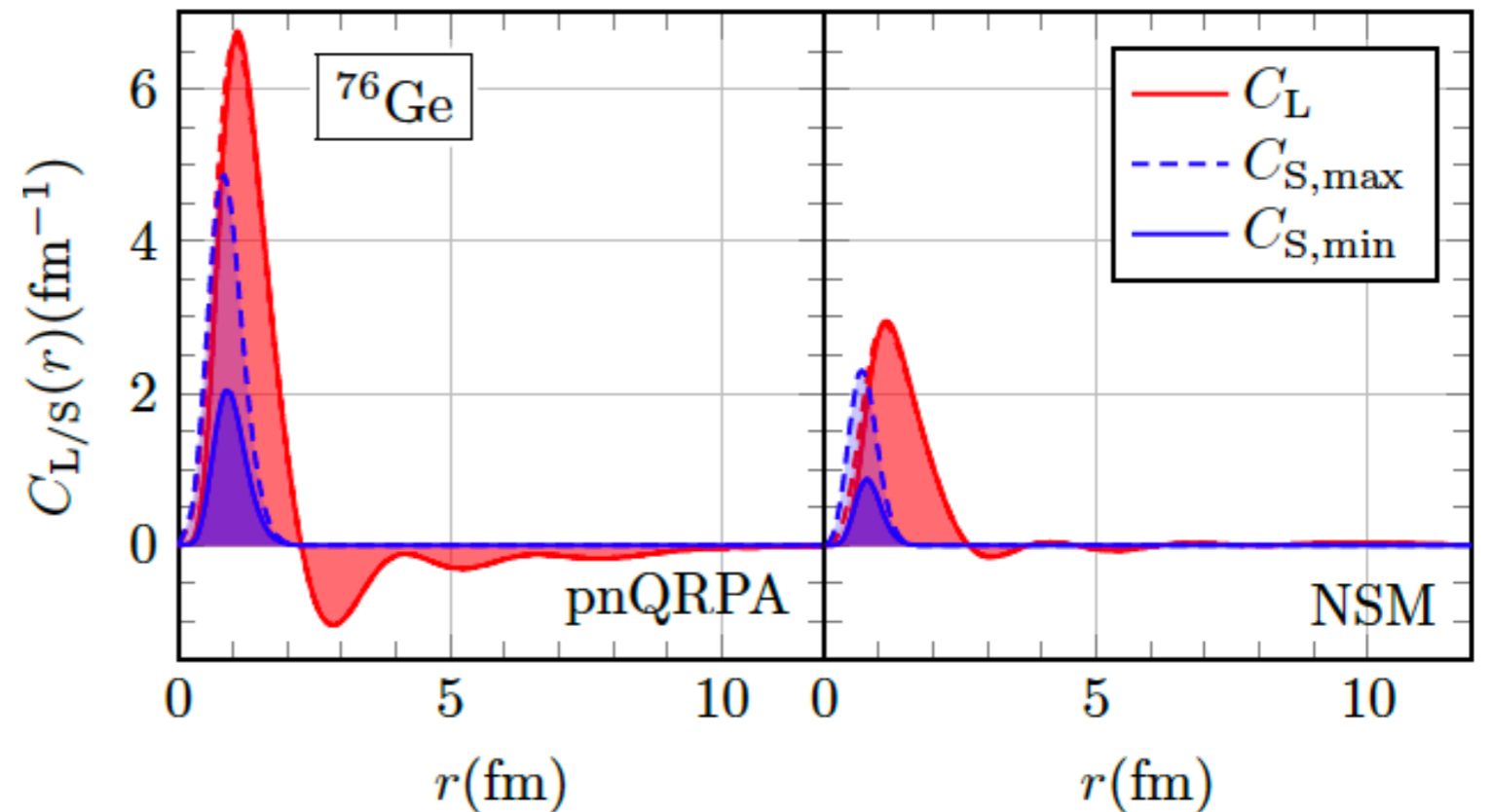
Impact on nuclear matrix elements

- Assuming $g_v \sim (C_1 + C_2)/2 \rightarrow O(1)$ impact on m.e. and $m_{\beta\beta}$ extraction



70% effect in ^{12}Be transition, using Variational Monte Carlo methods + Norfolk chiral potential [1606.06335]

VC, W. Dekens, J. de Vries, M. Graesser, E. Mereghetti, S. Pastore, M. Piarulli, U. van Kolck, R. Wiringa, 1907.11254

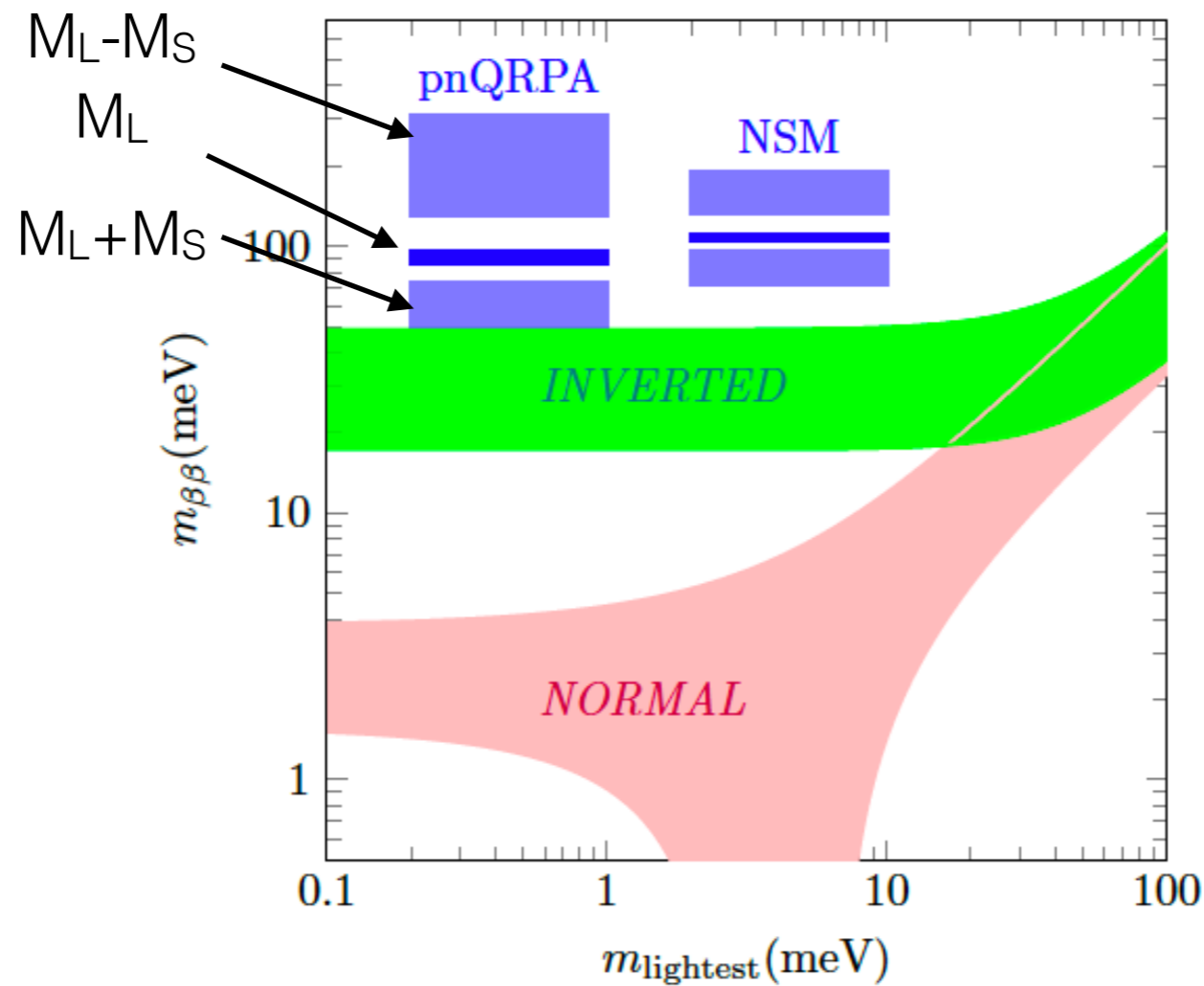


30-70% effect in QRPA and 15-45% in NSM. Similar or larger in other isotopes

Jokiniemi-Soriano-Menendez, 2107.13354

Impact on nuclear matrix elements

- Assuming $g_v \sim (C_1 + C_2)/2 \rightarrow O(1)$ impact on m.e. and $m_{\beta\beta}$ extraction



Key question:
is the interference
constructive or
destructive?

Jokiniemi-Soriano-Menendez, 2107.13354

Towards determining of g_V

- Large- N_c arguments point to $g_V \sim (C_1 + C_2)/2$

Richardson, Shindler, Pastore, Springer, 2102.02814

- Lattice QCD

- $\pi^- \rightarrow \pi^+ e^- e^-$ precisely known
- Formalism for NN developed

Tuo et al. 1909.13525;
Detmold, Murphy 2004.07404

Davoudi, Kadam, 2012.02083

- Analytic approach inspired by Cottingham formula for $\delta m_{p,n}$ (EM)

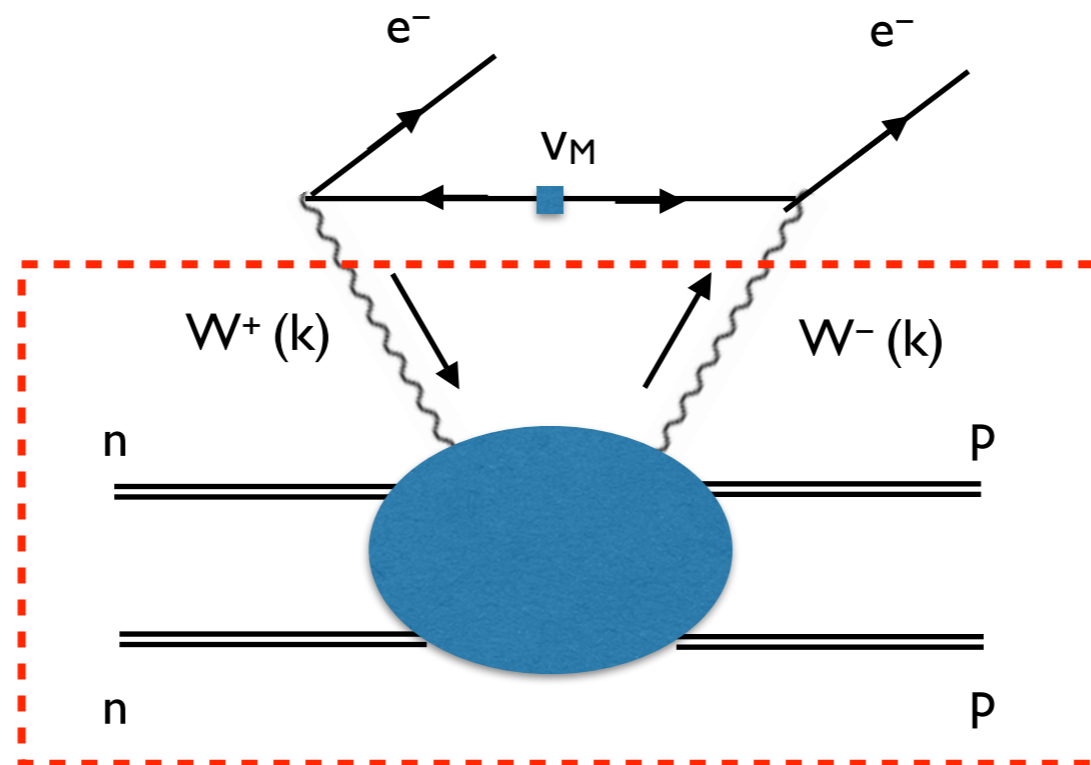
VC, Dekens, deVries, Hoferichter, Mereghetti, 2012.11602, 2102.03371

Estimating the contact term (I)

VC, Dekens, deVries, Hoferichter, Mereghetti, 2012.11602, 2102.03371

- Useful representation of the amplitude

$$\mathcal{A}_\nu \propto \int \frac{d^4 k}{(2\pi)^4} \frac{g_{\alpha\beta}}{k^2 + i\epsilon} \int d^4 x e^{ik \cdot x} \langle pp | T \{ j_W^\alpha(x) j_W^\beta(0) \} | nn \rangle$$



Forward “Compton” amplitude

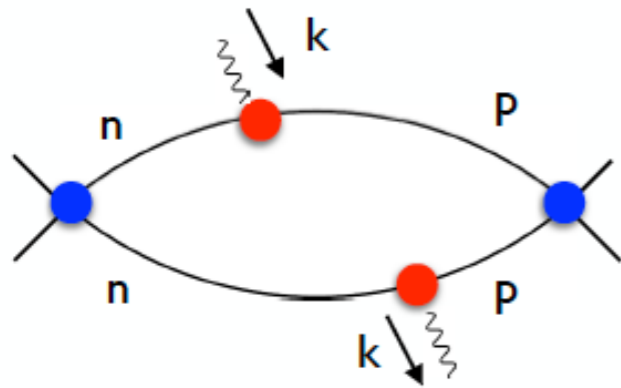
Estimating the contact term (I)

VC, Dekens, deVries, Hoferichter, Mereghetti, 2012.11602, 2102.03371

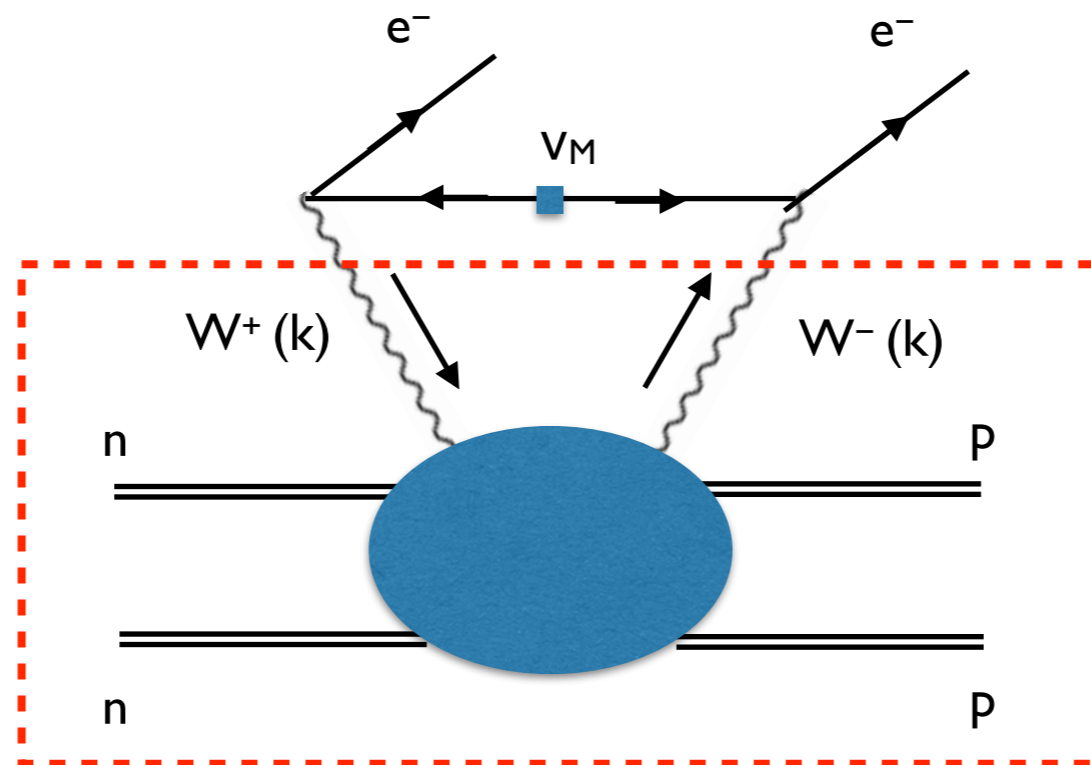
- Useful representation of the amplitude

$$\mathcal{A}_\nu \propto \int \frac{d^4 k}{(2\pi)^4} \frac{g_{\alpha\beta}}{k^2 + i\epsilon} \int d^4 x e^{ik \cdot x} \langle pp | T \{ j_W^\alpha(x) j_W^\beta(0) \} | nn \rangle$$

Low k: chiral EFT to NLO

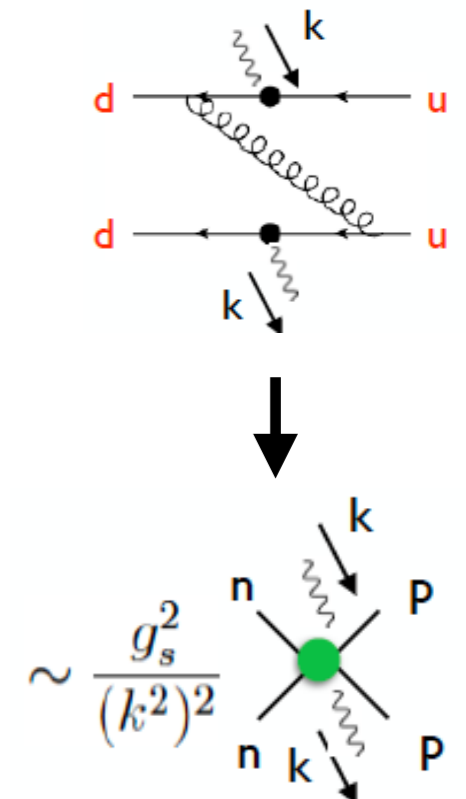


Intermediate k: resonance contributions in πNN intermediate state, ...



Forward "Compton" amplitude

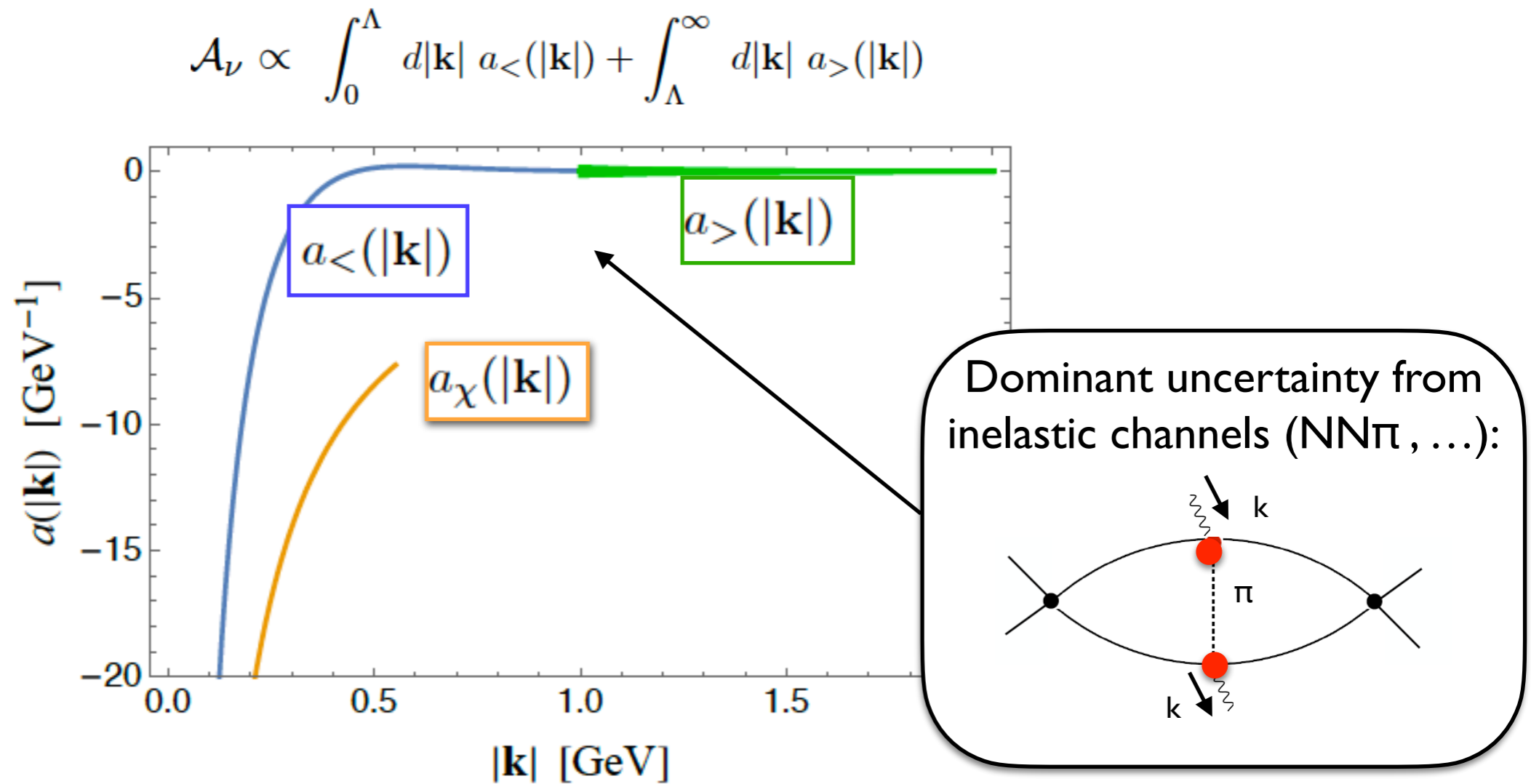
High k: QCD OPE



Estimating the contact term (2)

VC, Dekens, deVries, Hoferichter, Mereghetti, 2012.11602, 2102.03371

- Determine $C_{1,2}$ with $\sim 30\%$ uncertainty (dominated by intermediate k)



Estimating the contact term (2)

VC, Dekens, deVries, Hoferichter, Mereghetti, 2012.11602, 2102.03371

- Determine $C_{1,2}$ with $\sim 30\%$ uncertainty (dominated by intermediate k)
- Validation: $C_1 + C_2 \Rightarrow (a_{nn} + a_{pp})/2 - a_{np} = 15.5(4.5)$ fm versus $10.4(2)$ fm (exp)
- Provided 'synthetic data' for the $nn \rightarrow pp$ amplitude at threshold
- First calculation of $^{48}\text{Ca} \rightarrow ^{48}\text{Ti}$ with contact fitted to synthetic data \Rightarrow contact term enhances nuclear matrix element by $(43 \pm 7)\%$

Wirth, Yao, Hergert, 2105.05415

Estimating the contact term (2)

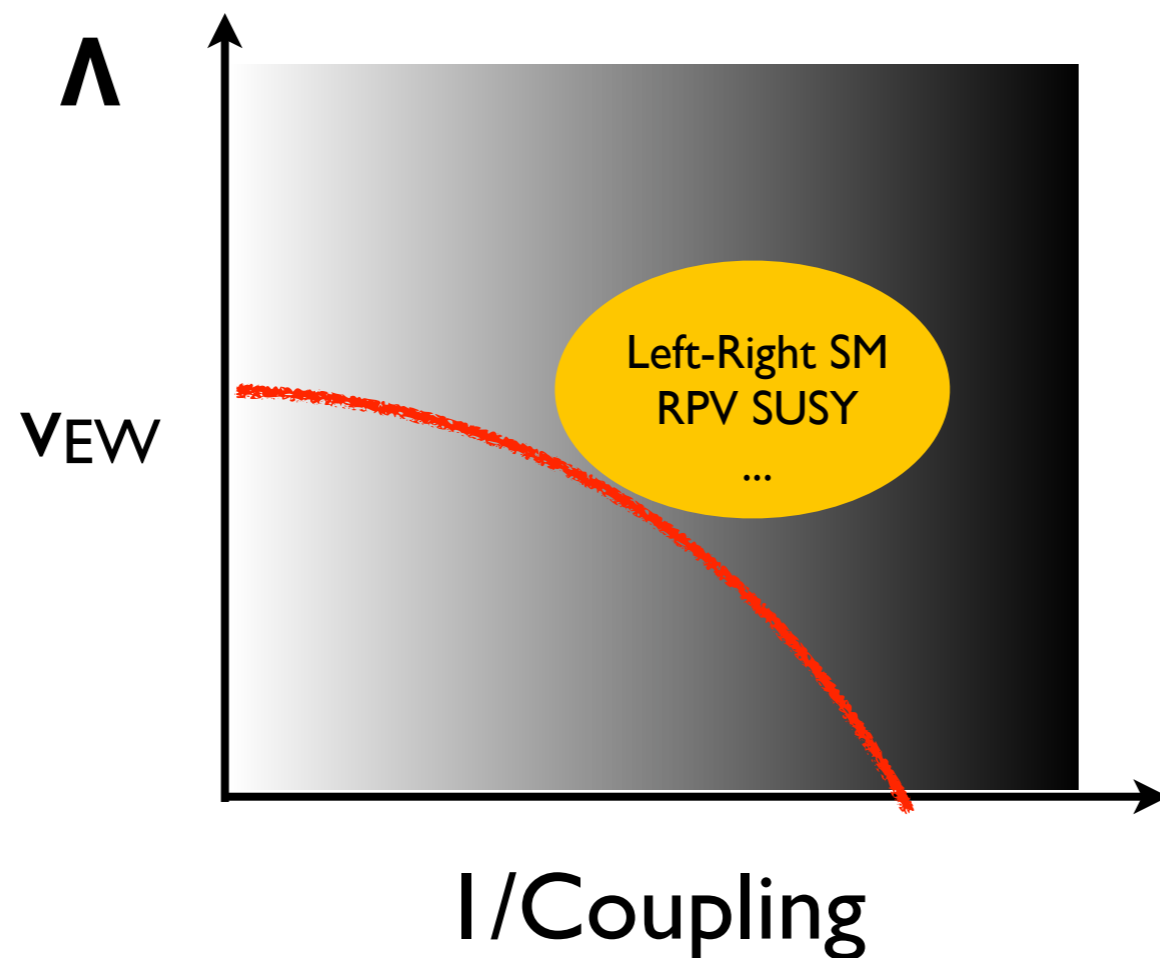
VC, Dekens, deVries, Hoferichter, Mereghetti, 2012.11602, 2102.03371

- Determine $C_{1,2}$ with $\sim 30\%$ uncertainty (dominated by intermediate k)
- Validation: $C_1 + C_2 \Rightarrow (a_{nn} + a_{pp})/2 - a_{np} = 15.5(4.5)$ fm versus $10.4(2)$ fm (exp)
- Provided 'synthetic data' for the $nn \rightarrow pp$ amplitude at threshold
- First calculation of $^{48}\text{Ca} \rightarrow ^{48}\text{Ti}$ with contact fitted to synthetic data \Rightarrow contact term enhances nuclear matrix element by $(43 \pm 7)\%$

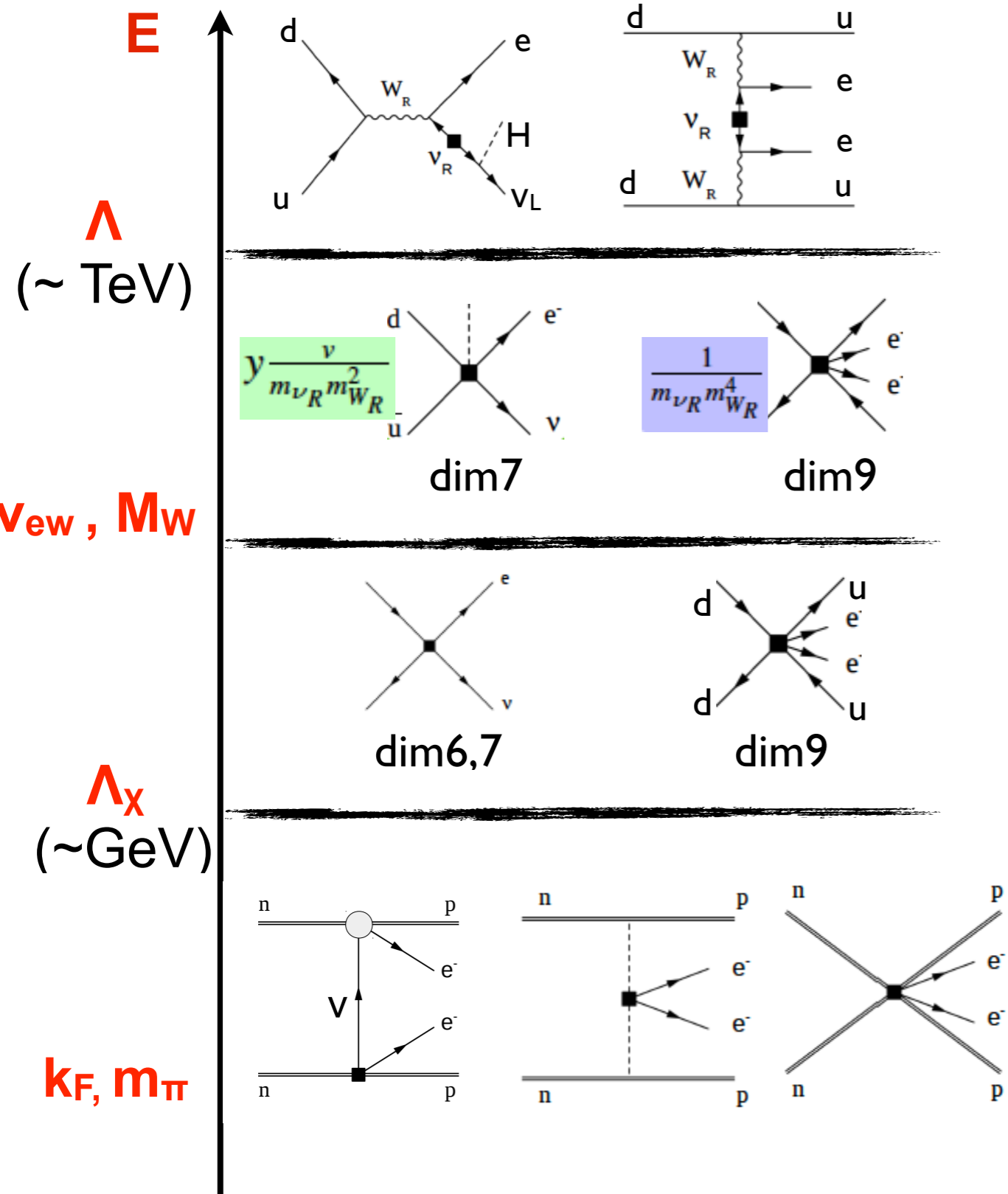
Wirth, Yao, Hergert, 2105.05415

Good news, while we wait for lattice results

$0\nu\beta\beta$ from multi-TeV scale dynamics (dim-7, 9, ... operators)



~TeV-scale LNV



- Higher dim operators arise in well motivated models

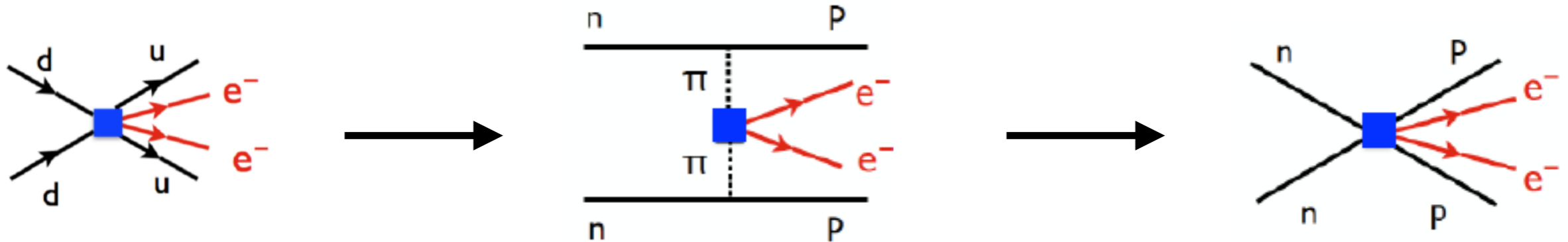
See talks by Babu, Fileviez Perez., ...

- 31 operators up to dimension 9

- New mechanisms at the hadronic scale: need appropriate chiral EFT treatment. **Not including pion range effects leads to factor $\sim (Q/\Lambda_\chi)^2 \sim 1/100$ reduction in sensitivity to short-distance couplings!**

Hadronic theory developments

- Leading order hadronic realization of dim-9 operators:



In Weinberg's counting, pion-exchange contribution dominates

Prezeau, Ramsey-Musolf, Vogel
hep-ph/0303205

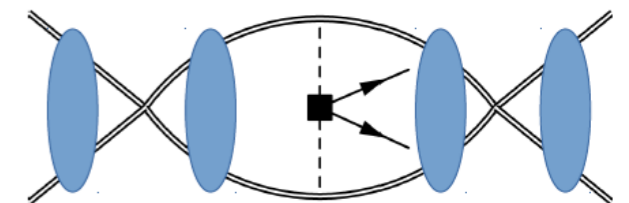
Vergados 1982,

Faessler, Kovalenko, Simkovic, Schweiger 1996

$\pi\pi$ matrix element known from Lattice QCD at <10%

Nicholson et al (CaLat),
1805.02634

Renormalization requires a contact at the same order!



VC, W. Dekens, J. de Vries, M. Graesser,
E. Mereghetti [1806.02780]

- Several unknown LO NN contact couplings! Opportunity for LQCD

Phenomenological interest

- TeV-scale LNV induces contributions to $0\nu\beta\beta$ *not directly related to the exchange of light neutrinos*, within reach of current experiments

New contributions can add incoherently *or interfere with* $m_{\beta\beta}$, significantly affecting the interpretation of experimental results

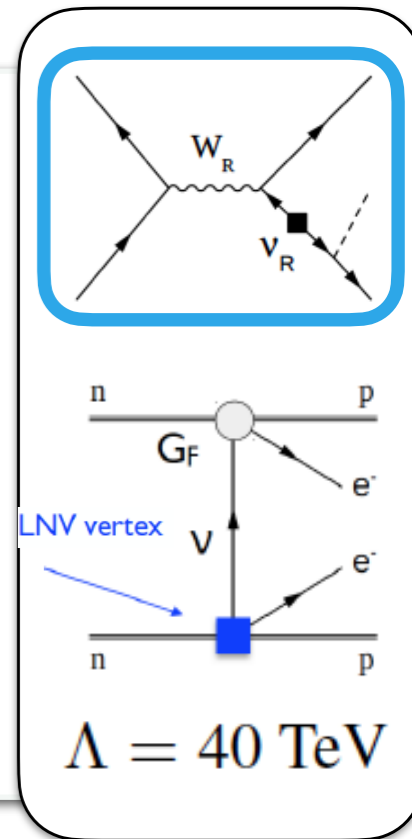
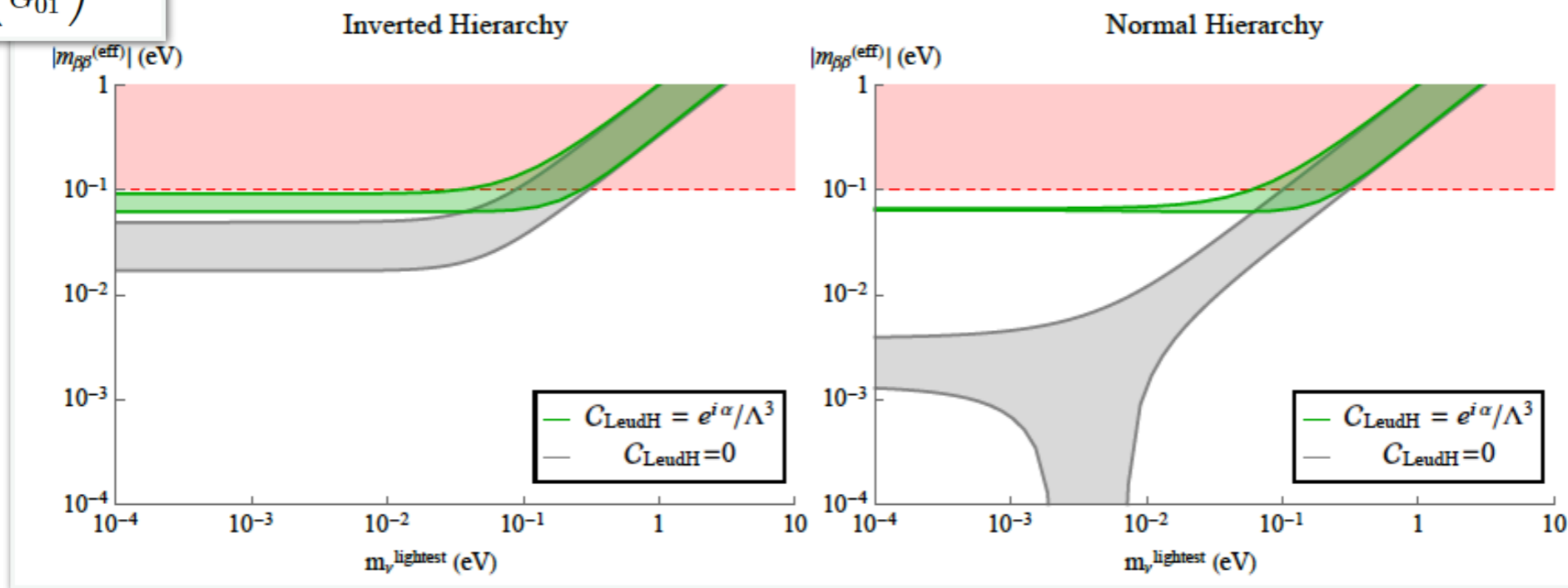
Phenomenological interest

- TeV-scale LNV induces contributions to $0\nu\beta\beta$ *not directly related to the exchange of light neutrinos*, within reach of current experiments

New contributions can add incoherently or interfere with $m_{\beta\beta}$, significantly affecting the interpretation of experimental results

$$m_{\beta\beta}^{(\text{eff})} = \frac{m_e}{g_A^2 M_\nu} \left(\frac{T_{1/2}^{0\nu}}{G_{01}} \right)^{-1/2}$$

$$C_{\text{LeudH}} \epsilon_{ij} (\bar{d}\gamma^\mu u) (L_m^T C \gamma_\mu e) H_j$$

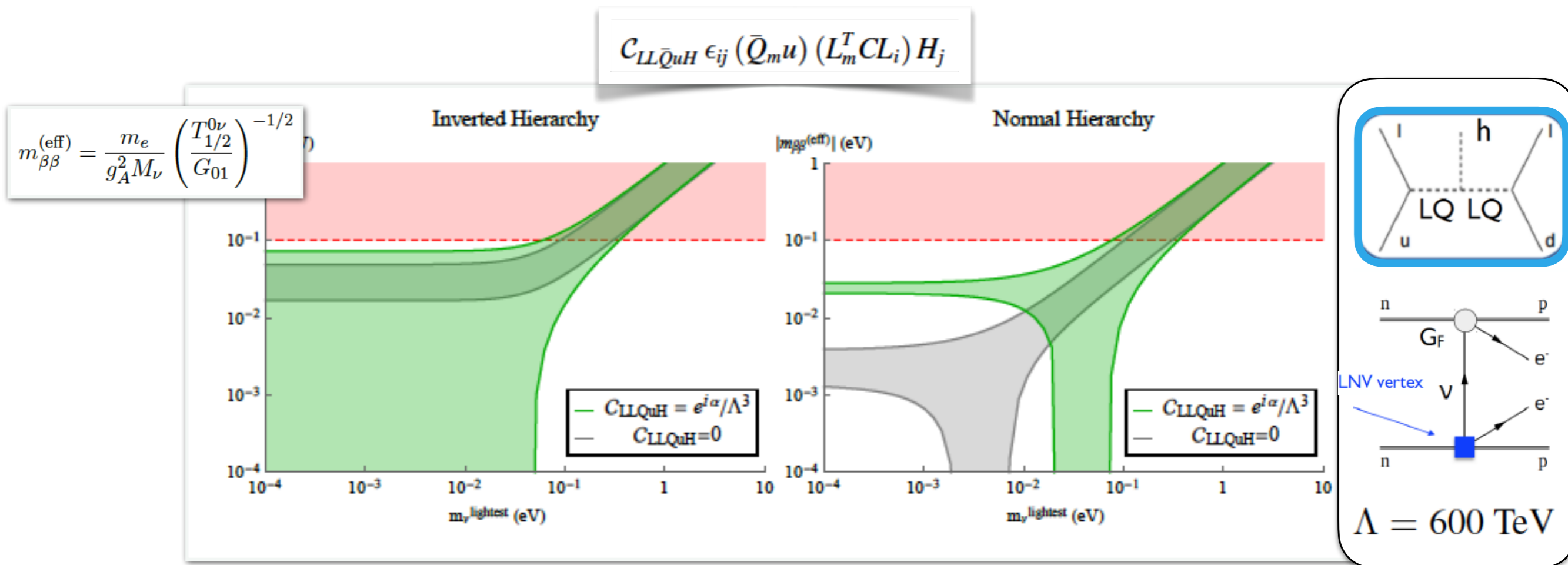


VC, W. Dekens, J. de Vries, M. Graesser, E. Mereghetti, 1708.09390

Phenomenological interest

- TeV-scale LNV induces contributions to $0\nu\beta\beta$ *not directly related to the exchange of light neutrinos*, within reach of current experiments

New contributions can add incoherently or interfere with $m_{\beta\beta}$, significantly affecting the interpretation of experimental results



VC, W. Dekens, J. de Vries, M. Graesser, E. Mereghetti, 1708.09390

Phenomenological interest

- TeV-scale LNV induces contributions to $0\nu\beta\beta$ *not directly related to the exchange of light neutrinos*, within reach of current experiments
- May lead to correlated (or precursor!) signal at LHC: $pp \rightarrow ee jj$

Keung-Senjanovic '83

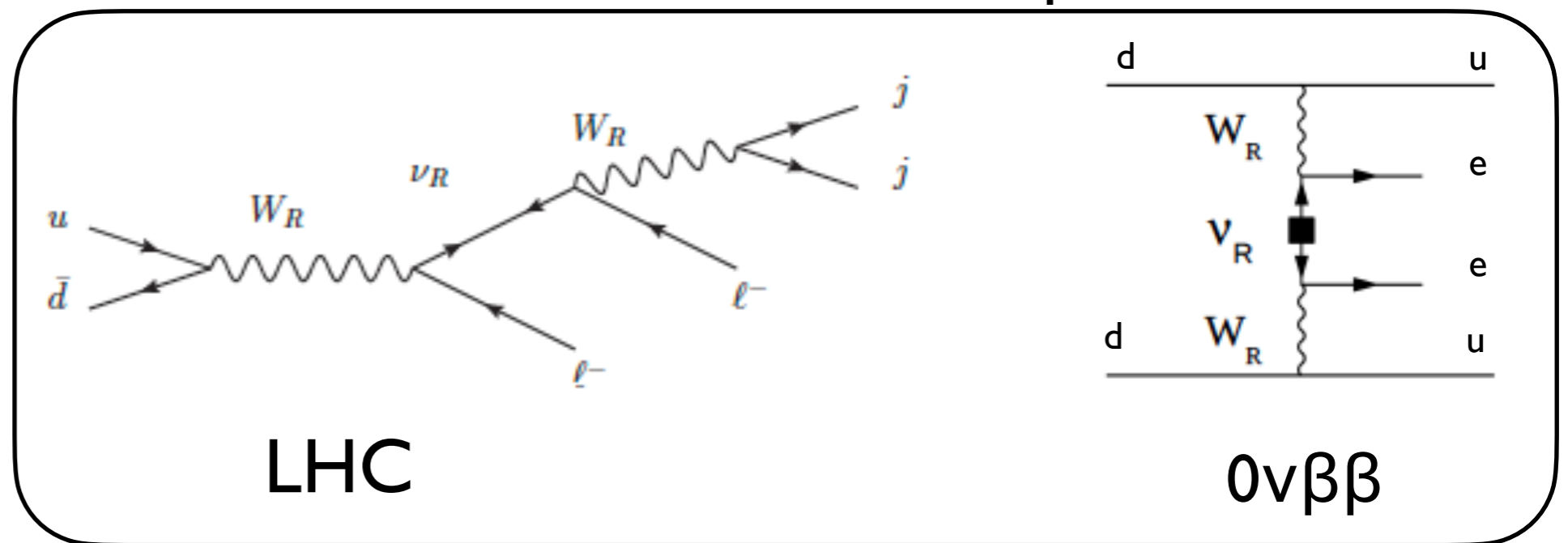
Maiezza-Nemevesek-
Nesti- Senjanovic
1005.5160

Helo-Kovalenko-Hirsch-
Pas 1303.0899, 1307.4849

Cai, Han, Li, Ruiz
1711.02180

...

Classic LRSM example



Phenomenological interest

- TeV-scale LNV induces contributions to $0\nu\beta\beta$ *not directly related to the exchange of light neutrinos*, within reach of current experiments
- May lead to correlated (or precursor!) signal at LHC: $pp \rightarrow ee jj$

Keung-Senjanovic '83

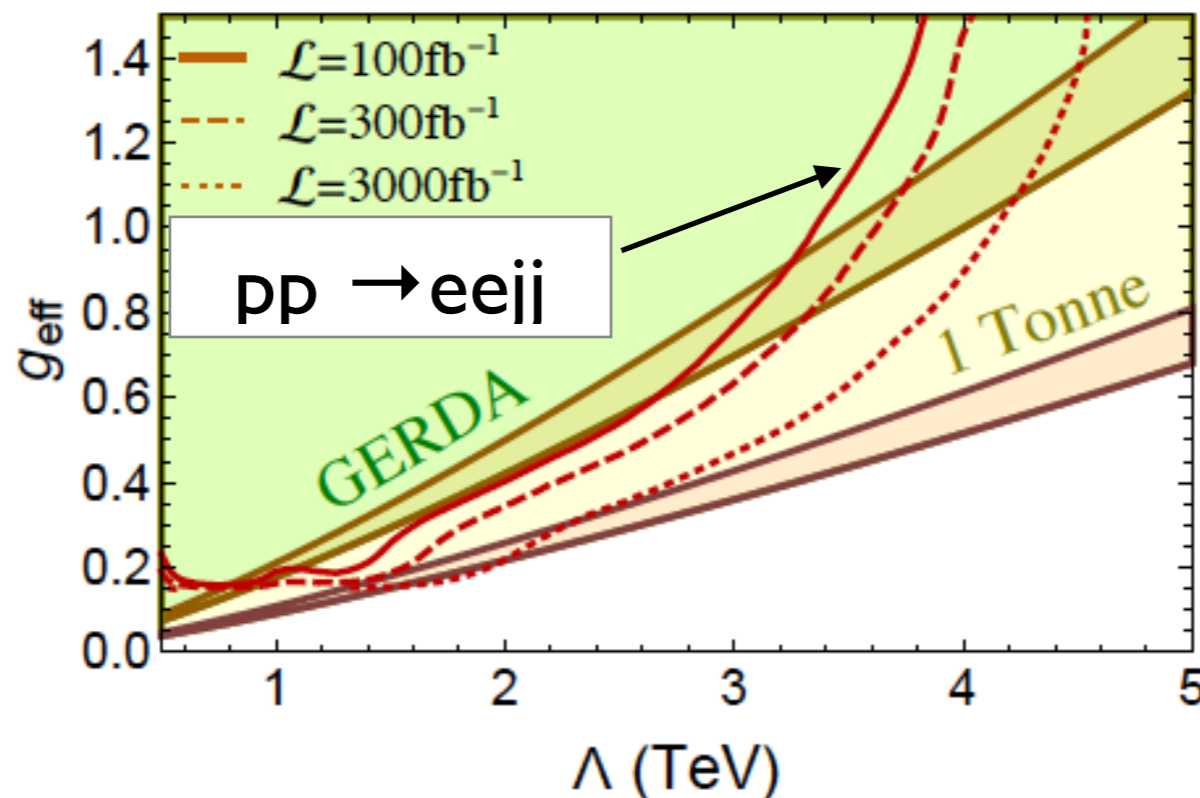
Maiezza-Nemevesek-
Nesti- Senjanovic
1005.5160

Helo-Kovalenko-Hirsch-
Pas 1303.0899, 1307.4849

Cai, Han, Li, Ruiz
1711.02180

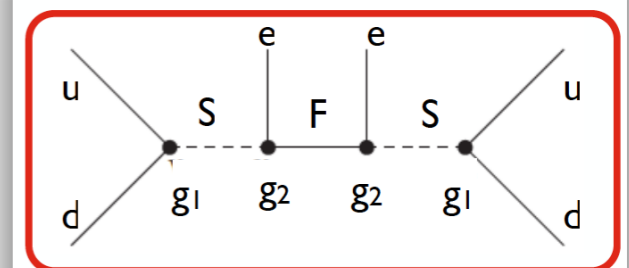
Peng, Ramsey-Musolf,
Winslow, 1508.0444

...



Simplified model

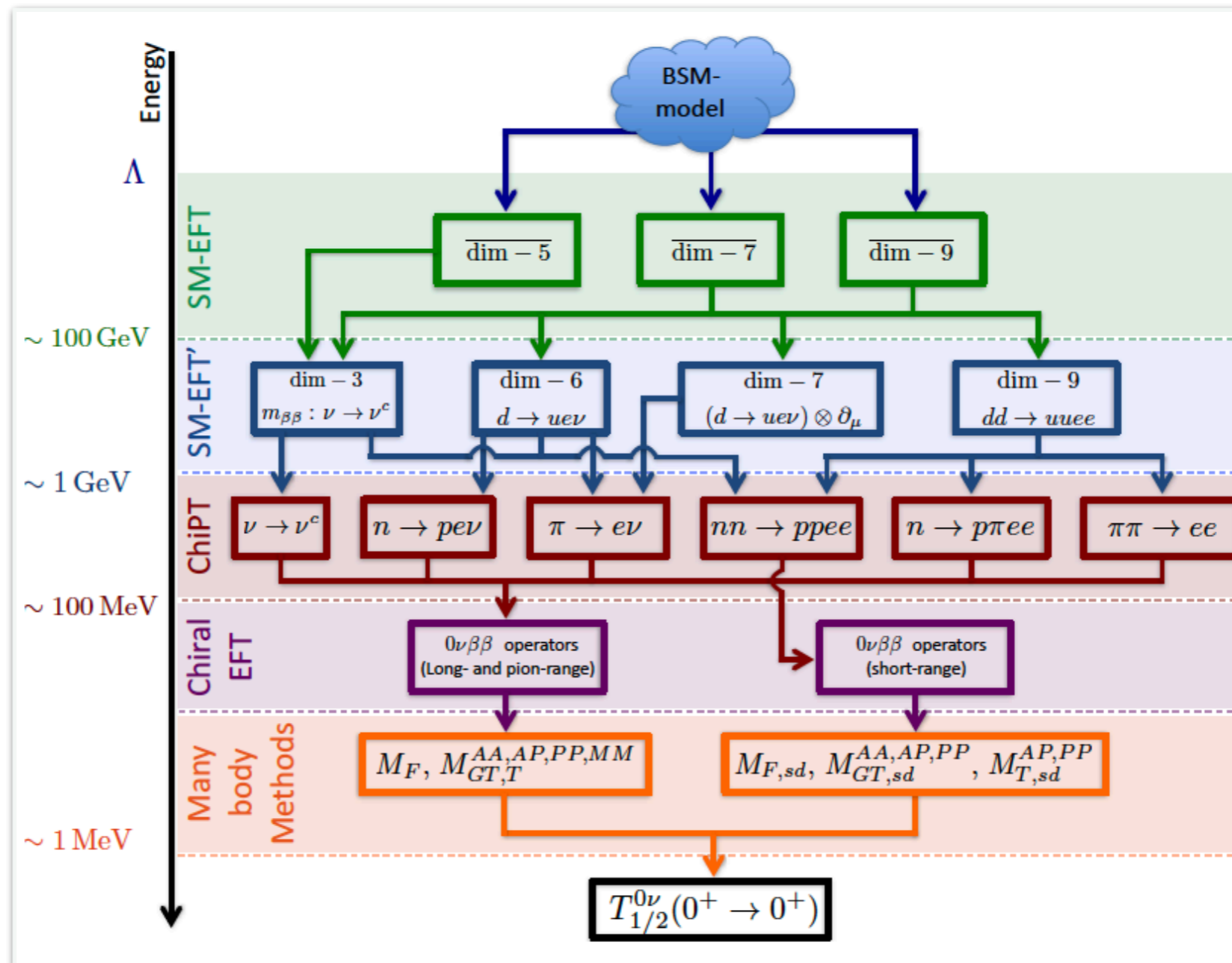
$$M_S = M_F = M_{\text{eff}} \quad (g_{\text{eff}})^4 = g_1^2 g_2^2$$



$$A_{0\nu\beta\beta} \sim (g_{\text{eff}})^4 / (M_{\text{eff}})^5$$

Summary: EFT-based master formula

- Framework to interpret $0\nu\beta\beta$ searches in terms of any high-scale model and possibly unravel the underlying mechanism in case of discovery



Conclusions & Outlook

- Ton-scale $0\nu\beta\beta$ searches have **significant discovery potential** — we simply don't know the origin of m_ν and the scale Λ associated with LNV
- EFT approach provides a general framework to:
 1. **Relate $0\nu\beta\beta$ to underlying LNV dynamics (and collider & cosmology)**
 - Master formula for $0\nu\beta\beta$ up dim-9 operators
 2. **Organize contributions to hadronic and nuclear matrix elements**
 - Identified new leading order short-range contributions

Improving the theory uncertainty is challenging, but there are exciting prospects thanks to advances in **EFT**, **lattice QCD**, and **nuclear structure**

Backup

LNv@dim5: What about higher orders?

- N2LO

- πN loops + new contact

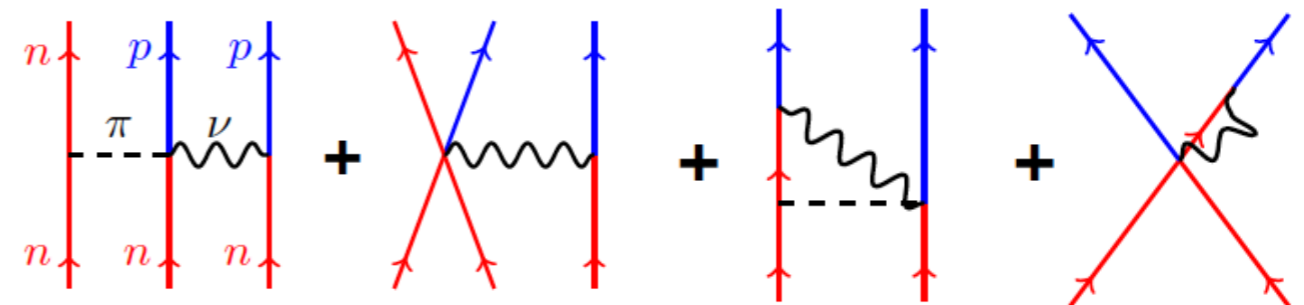
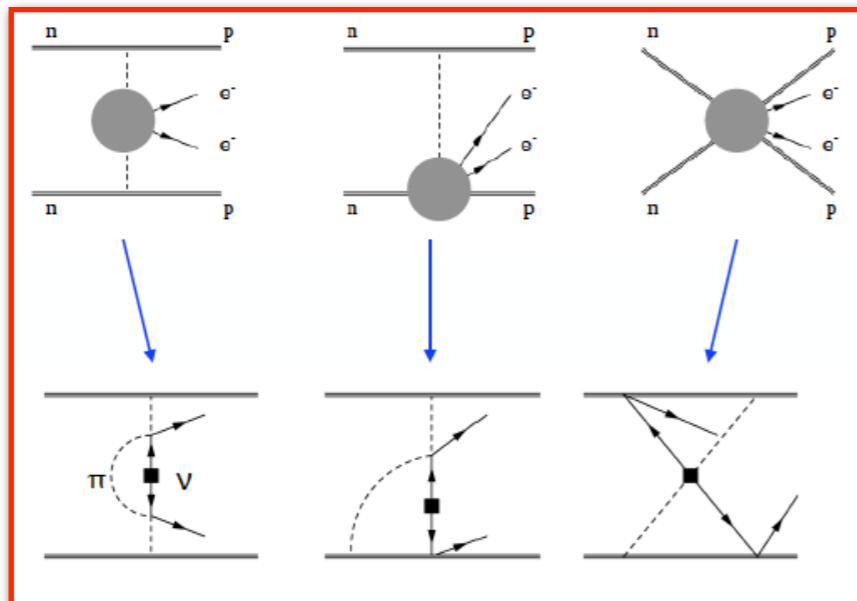
VC, W. Dekens, E. Mereghetti, A. Walker-Loud, 1710.01729

- 2-body \times 1-body current (and a new contact)

Wang-Engel-Yao 1805.10276

- Neglecting contact terms, calculations in light and heavy nuclei find $O(10\%)$ corrections: encouraging!

S. Pastore, J. Carlson, V.C., W. Dekens, E. Mereghetti, R. Wiringa 1710.05026
 J. Engel, private communication



LVN@dim5: What about higher orders?

- N2LO

- πN loops + new contact

VC, W. Dekens, E. Mereghetti, A. Walker-Loud, 1710.01729

- 2-body \times 1-body current (and a new contact)

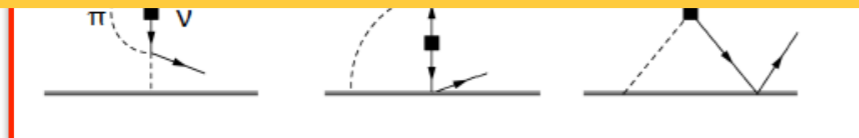
Wang-Engel-Yao 1805.10276

- Neglecting contact terms, calculations in light and heavy nuclei find $O(10\%)$ corrections: encouraging!

S. Pastore, J. Carlson, V.C., W. Dekens, E. Mereghetti, R. Wiringa 1710.05026
J. Engel, private communication

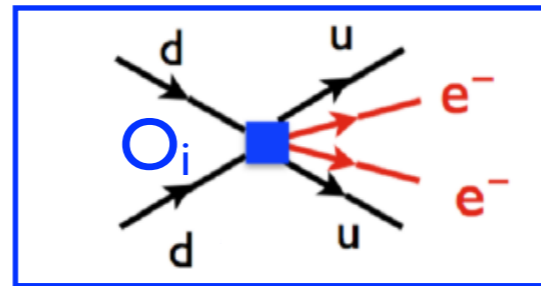


Full analysis beyond leading order requires again matching to Lattice QCD and dedicated many body calculations — long term goal

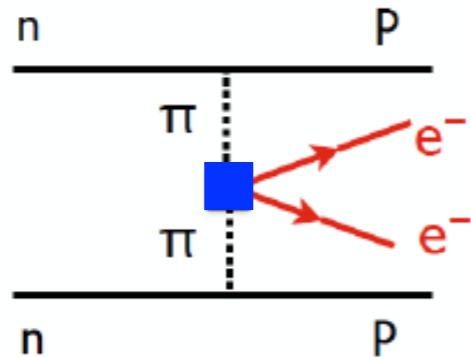


TeV-scale LNV: hadronic theory developments

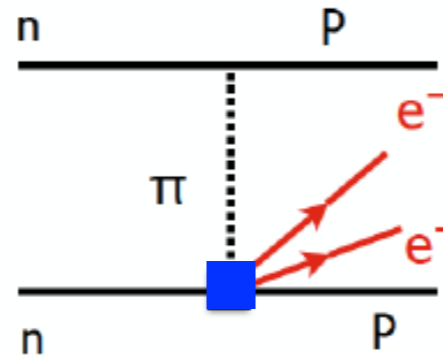
Pion-range effects



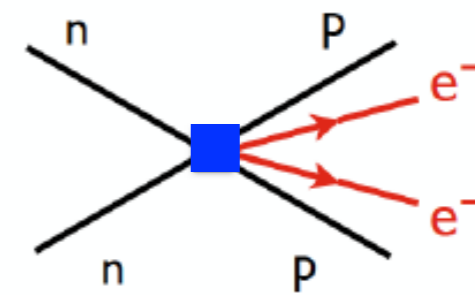
Short-range effects



Q^{-2}



Q^0



Q^0

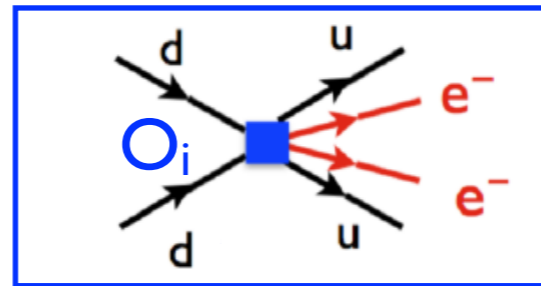
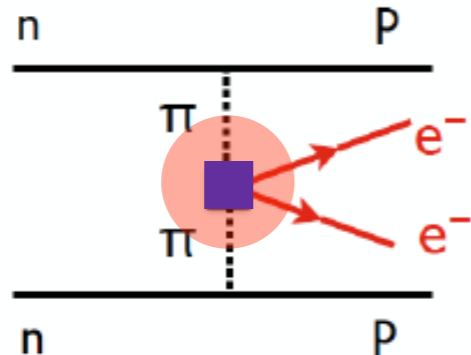
Hadronic realization of dim-9 operators in chiral EFT

Weinberg's counting (NDA for NN contact) $\rightarrow V_{\pi\pi}$ dominates

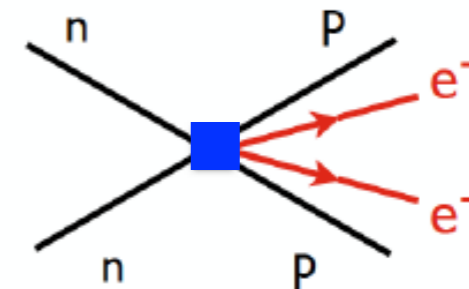
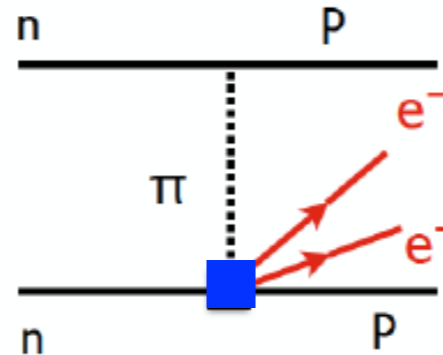
Prezeau, Ramsey-Musolf, Vogel [hep-ph/0303205](https://arxiv.org/abs/hep-ph/0303205)

TeV-scale LNV: hadronic theory developments

Pion-range effects

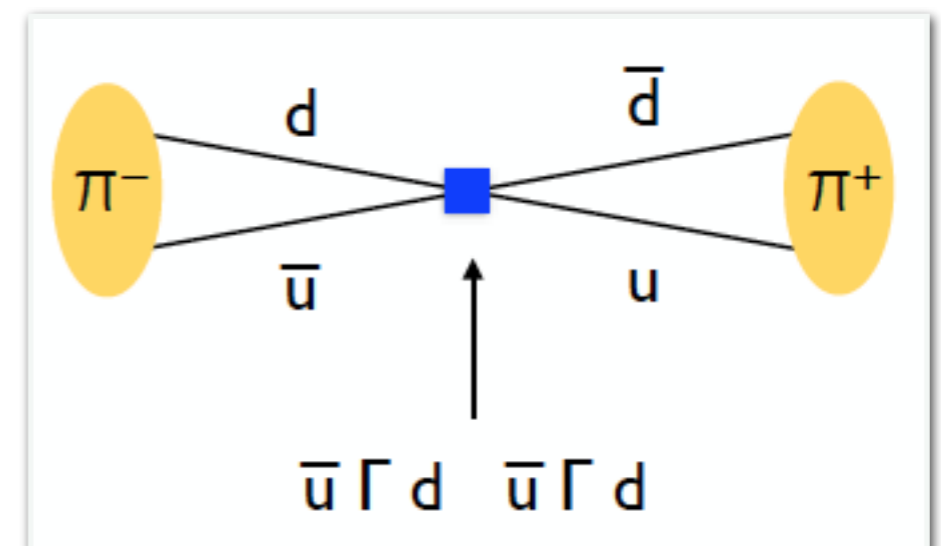


Short-range effects



- Two recent developments:

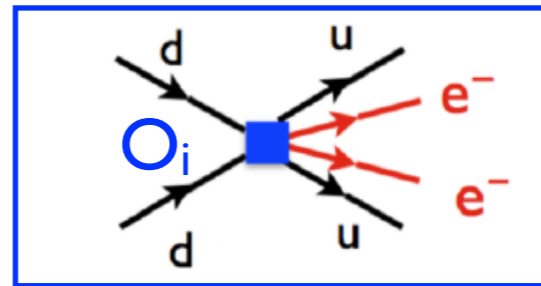
- $\pi\pi$ matrix elements now precisely calculated in lattice QCD ($\sim 10\%$ or better)



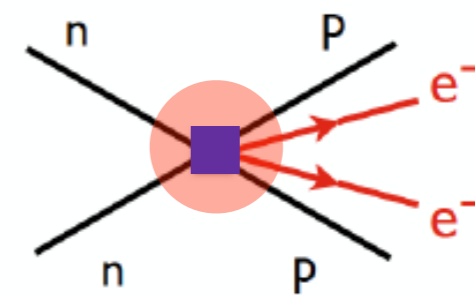
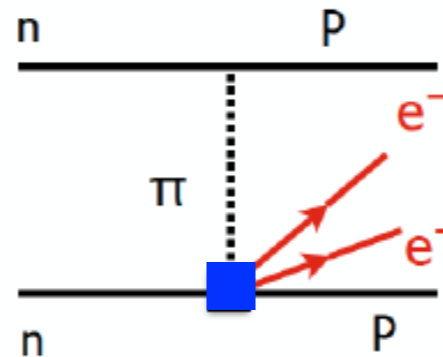
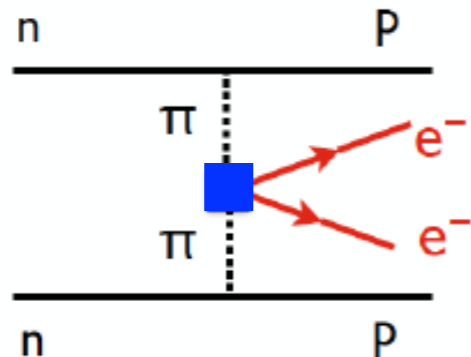
Nicholson et al (Callat), 1805.02634, PRL

TeV-scale LNV: hadronic theory developments

Pion-range effects

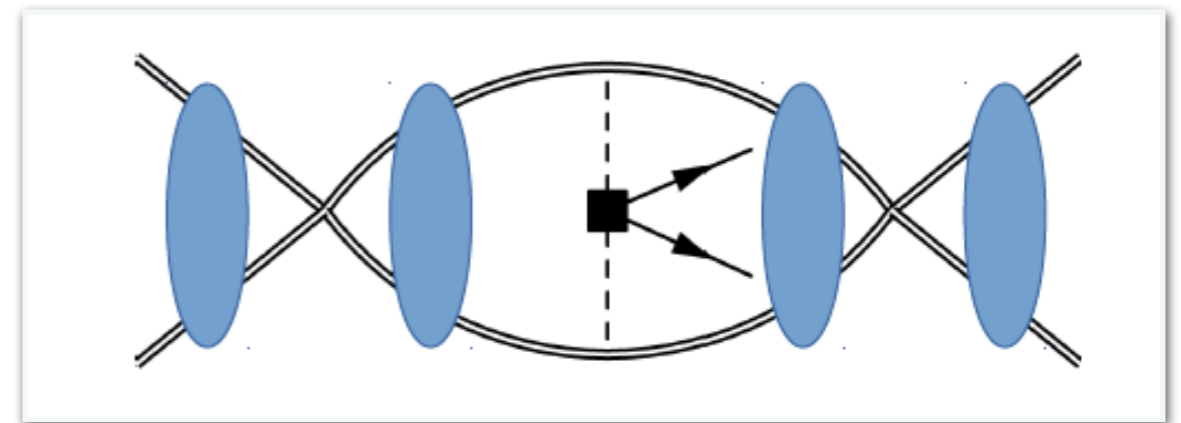


Short-range effects



- Two recent developments:

2. Renormalization $\rightarrow V_{\pi\pi}$ and V_{NN} are both leading order



V.C, W. Dekens, J. de Vries, M. Graesser, E. Mereghetti [1806.02780]

Dimension 6 and 7 operators

$$\mathcal{L}_{\Delta L=2}^{(6)} = \frac{2G_F}{\sqrt{2}} \left(C_{\text{VL},ij}^{(6)} \bar{u}_L \gamma^\mu d_L \bar{e}_{R,i} \gamma_\mu C \bar{\nu}_{L,j}^T + C_{\text{VR},ij}^{(6)} \bar{u}_R \gamma^\mu d_R \bar{e}_{R,i} \gamma_\mu C \bar{\nu}_{L,j}^T \right. \\ \left. + C_{\text{SR},ij}^{(6)} \bar{u}_L d_R \bar{e}_{L,i} C \bar{\nu}_{L,j}^T + C_{\text{SL},ij}^{(6)} \bar{u}_R d_L \bar{e}_{L,i} C \bar{\nu}_{L,j}^T + C_{\text{T},ij}^{(6)} \bar{u}_L \sigma^{\mu\nu} d_R \bar{e}_{L,i} \sigma_{\mu\nu} C \bar{\nu}_{L,j}^T \right) + \text{h.c.}$$

$$\mathcal{L}_{\Delta L=2}^{(7)} = \frac{2G_F}{\sqrt{2}v} \left(C_{\text{VL},ij}^{(7)} \bar{u}_L \gamma^\mu d_L \bar{e}_{L,i} C i \overleftrightarrow{\partial}_\mu \bar{\nu}_{L,j}^T + C_{\text{VR},ij}^{(7)} \bar{u}_R \gamma^\mu d_R \bar{e}_{L,i} C i \overleftrightarrow{\partial}_\mu \bar{\nu}_{L,j}^T \right) + \text{h.c.}$$

Dimension 9 operators

$$\mathcal{L}_{\Delta L=2}^{(9)} = \frac{1}{v^5} \sum_i \left[\left(C_{iR}^{(9)} \bar{e}_R C \bar{e}_R^T + C_{iL}^{(9)} \bar{e}_L C \bar{e}_L^T \right) O_i + C_i^{(9)} \bar{e} \gamma_\mu \gamma_5 C \bar{e}^T O_i^\mu \right]$$

$$\begin{aligned} O_1 &= \bar{q}_L^\alpha \gamma_\mu \tau^+ q_L^\alpha \bar{q}_L^\beta \gamma^\mu \tau^+ q_L^\beta, & O'_1 &= \bar{q}_R^\alpha \gamma_\mu \tau^+ q_R^\alpha \bar{q}_R^\beta \gamma^\mu \tau^+ q_R^\beta \\ O_2 &= \bar{q}_R^\alpha \tau^+ q_L^\alpha \bar{q}_R^\beta \tau^+ q_L^\beta, & O'_2 &= \bar{q}_L^\alpha \tau^+ q_R^\alpha \bar{q}_L^\beta \tau^+ q_R^\beta, \\ O_3 &= \bar{q}_R^\alpha \tau^+ q_L^\beta \bar{q}_R^\beta \tau^+ q_L^\alpha, & O'_3 &= \bar{q}_L^\alpha \tau^+ q_R^\beta \bar{q}_L^\beta \tau^+ q_R^\alpha, \\ O_4 &= \bar{q}_L^\alpha \gamma_\mu \tau^+ q_L^\alpha \bar{q}_R^\beta \gamma^\mu \tau^+ q_R^\beta, \\ O_5 &= \bar{q}_L^\alpha \gamma_\mu \tau^+ q_L^\beta \bar{q}_R^\beta \gamma^\mu \tau^+ q_R^\alpha, \end{aligned}$$

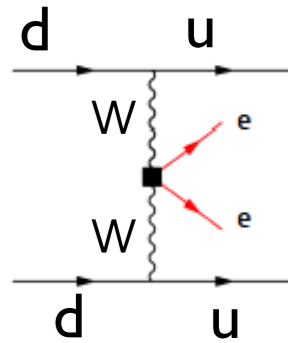
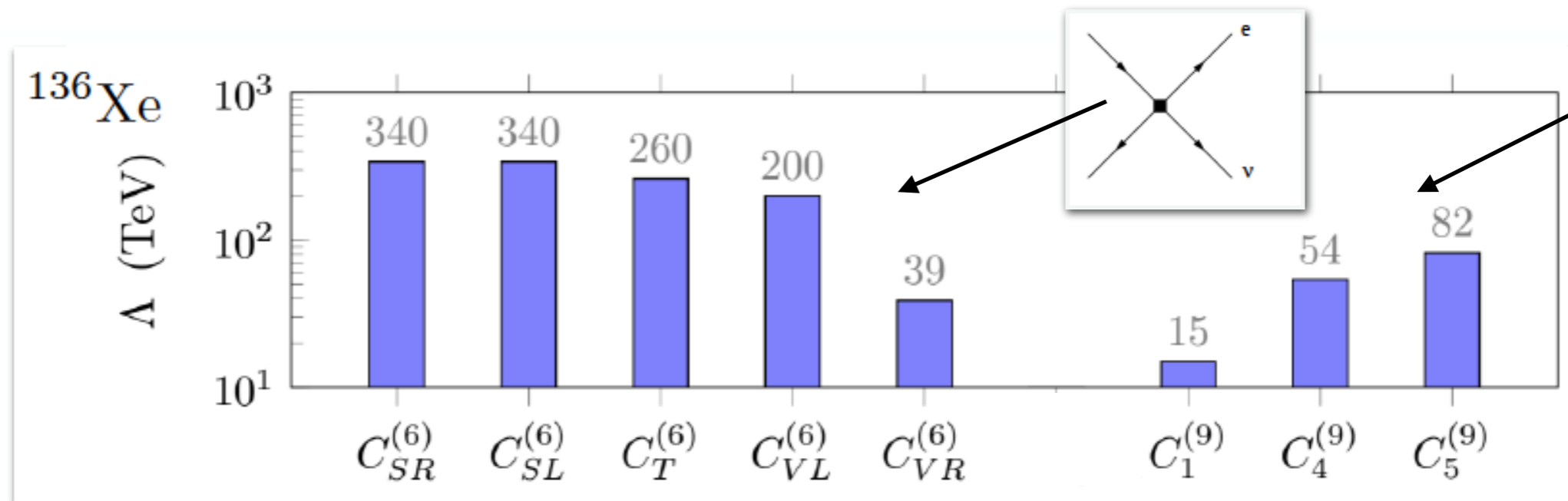
$$\begin{aligned} O_6^\mu &= (\bar{q}_L \tau^+ \gamma^\mu q_L) (\bar{q}_L \tau^+ q_R), & O_6^{\mu'} &= (\bar{q}_R \tau^+ \gamma^\mu q_R) (\bar{q}_R \tau^+ q_L), \\ O_7^\mu &= (\bar{q}_L t^a \tau^+ \gamma^\mu q_L) (\bar{q}_L t^a \tau^+ q_R), & O_7^{\mu'} &= (\bar{q}_R t^a \tau^+ \gamma^\mu q_R) (\bar{q}_R t^a \tau^+ q_L), \\ O_8^\mu &= (\bar{q}_L \tau^+ \gamma^\mu q_L) (\bar{q}_R \tau^+ q_L), & O_8^{\mu'} &= (\bar{q}_R \tau^+ \gamma^\mu q_R) (\bar{q}_L \tau^+ q_R), \\ O_9^\mu &= (\bar{q}_L t^a \tau^+ \gamma^\mu q_L) (\bar{q}_R t^a \tau^+ q_L), & O_9^{\mu'} &= (\bar{q}_R t^a \tau^+ \gamma^\mu q_R) (\bar{q}_L t^a \tau^+ q_R), \end{aligned}$$

What scales are we probing?

VC, W. Dekens, J. de Vries, M. Graesser, E. Mereghetti, 1806.02780

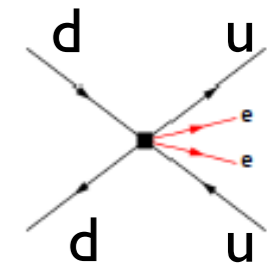
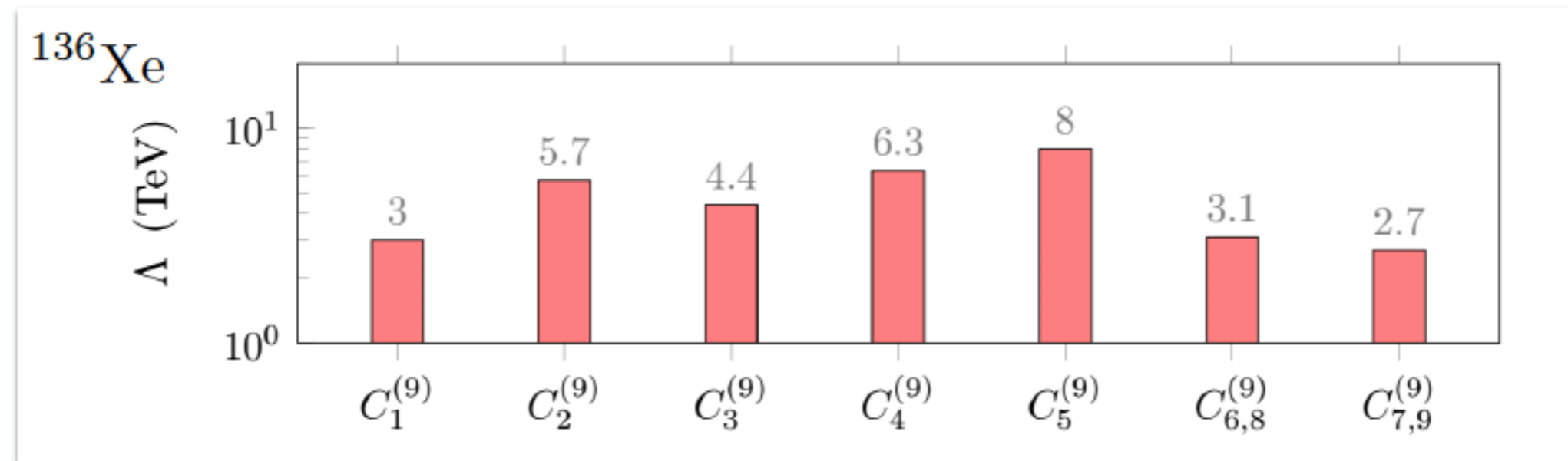
Dim 7 in
SM-EFT

$(\nu/\Lambda)^3$



Dim 9 in
SM-EFT

$(\nu/\Lambda)^5$



Bounds reflect dependence on Λ_χ / Λ and Q / Λ_χ