

Non-Standard Interaction in Radiative Neutrino Mass Models

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Outline

- 1 Radiative ν Mass Models
- 2 Non-Standard Neutrino Interaction
- 3 Consistency with Neutrino Oscillation Data
- 4 Collider and Flavor Constraints
- 5 Numerical Results for NSI
- 6 Conclusion

ν mass generation

- In Standard Model $M_\nu = 0$. But, ν flavor mix. $\nu_{aL} \leftrightarrow \nu_{bL}$

$$|\nu_\alpha\rangle = \sum U_{\alpha i} |\nu_i\rangle \implies M_\nu \neq 0 \implies \text{New physics beyond SM}$$

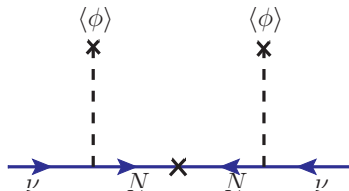
- Simplest possibility: Introduce ν_R to the SM allowing

$$\mathcal{L}_Y : y_\nu \bar{\psi}_L \phi \nu_R + h.c.$$

- $m_\nu \sim 0.1 eV$, this means yukawa coupling $y_\nu \sim 10^{-12}!!$
- Yukawa coupling likely to be **same order** as of quark and charged leptons.
But observation shows $m_\nu \ll m_q$ or m_l
- Schemes for neutrino masses and mixings:
 - Tree-level **Seesaw** mechanism
 - **Radiative** schemes

Seesaw Paradigm

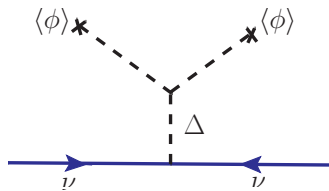
- Light neutrino mass is induced via Weingberg's dim-5 operator, $\frac{LL\phi\phi}{\Lambda}$.
- Large Majorana mass scale Λ to suppress the neutrino mass via $\frac{\langle\phi\rangle^2}{\Lambda}$.
- Different schemes:



Type I/ Type III:

ν -mass induced from **fermion exchange**:

$$N^1 \sim (1, 1, 0) \quad N^3 \sim (1, 3, 0)$$



Type II:

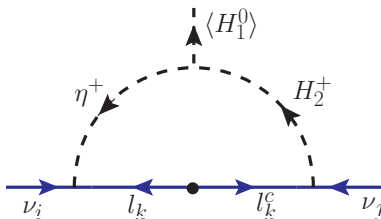
ν -mass induced from **scalar boson**

$$\text{exchange} \quad \Delta \sim (1, 3, 1)$$

- The scale of new physics can be **rather high**

Radiative ν mass generation

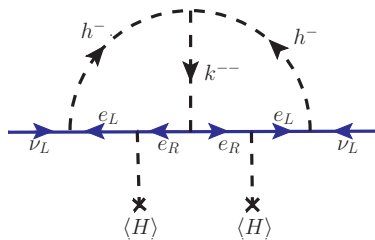
- Neutrino masses are **zero at tree level** as SM: ν_R may be absent.
- Small, finite Majorana masses are generated at the **quantum level**.
- Typically new heavy scalar fields introduced **violates lepton number**, gives rise to **neutrino flavor transitions**, and **lepton flavor violation**.
- Simple realization is the **Zee Model**, which has a second Higgs **doublet** and a charged **singlet**.



- Smallness of neutrino mass is explained via **loop** and **chiral suppression**.
- New physics in this framework may lie at the **TeV scale**.

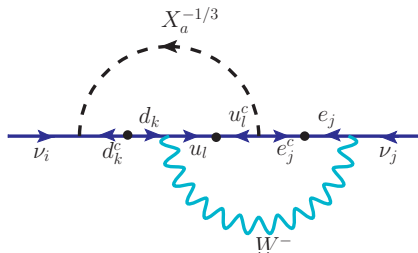
Type I radiative mechanism

- Obtained from effective $d = 7, 9, 11 \dots$ operators with $\Delta L = 2$ selection rule
- If the loop diagram has at least **one Standard Model particle**, this can be cut to generate such **effective operators**



$$\mathcal{O}_9 = L_i L_j L_k e^c L_l e^c \epsilon^{ij} \epsilon^{kl}$$

Zee, Babu



$$\mathcal{O}_8 = L_i \bar{e}^c \bar{u}^c d^c H_j \epsilon^{ij}$$

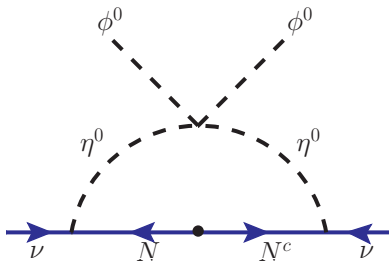
Babu, Julio (2010)

Classification: Babu, Leung (2001)

Cai, Herrero-Gracia, Schmidt, Vicente, Volkas (2017)

Type II radiative mechanism

- No Standard Model particle inside the loop
- Cannot be cut to generate $d = 7, 9, \dots$ operators
- Scotogenic model is an example



- Neutrino mass has **no chiral suppression**; new scale can be large
- Other considerations (**dark matter**) require TeV scale new physics

Ma (2006)

Nonstandard neutrino interactions

- **Unknown couplings** that involve neutrinos
- Many neutrino mass models naturally lead to NSI to some level
- New physics near **TeV scale** can generate **nonstandard neutrino interactions (NSI)**
- NSI effects happen in the neutrino **production**, ϵ^S , **propagation** through matter, ϵ^m , and the **detection** processes, ϵ^D .
- Most important effect of NSI is in neutrino **propagation in matter**
Wolfenstein (1978)
- Phenomenological, NSI can be described with an effective **four fermion Lagrangian**

$$\mathcal{L}_{\text{NSI}} = -2\sqrt{2}G_F \sum_{f,P,\alpha,\beta} \epsilon_{\alpha\beta}^{fP} (\bar{\nu}_\alpha \gamma^\mu P_L \nu_\beta) (\bar{f} \gamma_\mu P f)$$

$\epsilon_{\alpha\beta}^{fP}$ is the parameter that describes the strength of the NSI

Nonstandard neutrino interactions

- Matter potential

$$H_{\text{mat}} = \sqrt{2}G_F N_e(x) \begin{pmatrix} 1 + \varepsilon_{ee}(x) & \varepsilon_{e\mu}(x) & \varepsilon_{e\tau}(x) \\ \varepsilon_{e\mu}^*(x) & \varepsilon_{\mu\mu}(x) & \varepsilon_{\mu\tau}(x) \\ \varepsilon_{e\tau}^*(x) & \varepsilon_{\mu\tau}^*(x) & \varepsilon_{\tau\tau}(x) \end{pmatrix}$$

- Note $\varepsilon_{\alpha\beta} \equiv \text{real}$ if $\alpha = \beta$

$$\varepsilon_{\alpha\beta}(x) \equiv \sum_{f=e,u,d} \varepsilon_{\alpha\beta}^f \frac{N_f(x)}{N_e(x)} \qquad \varepsilon_{\alpha\beta}^f = \varepsilon_{\alpha\beta}^{f,L} + \varepsilon_{\alpha\beta}^{f,R}$$

$$\begin{aligned} N_u &= 2N_p + N_n & N_d &= N_p + 2N_n \\ N_p &= N_e & & \\ \varepsilon_{\alpha\beta}^p &= 2\varepsilon_{\alpha\beta}^u + \varepsilon_{\alpha\beta}^d & \varepsilon_{\alpha\beta}^n &= \varepsilon_{\alpha\beta}^u + 2\varepsilon_{\alpha\beta}^d \end{aligned}$$

$$\begin{aligned} \varepsilon_{\alpha\beta}(x) &= \varepsilon_{\alpha\beta}^e + \varepsilon_{\alpha\beta}^p + y_n \varepsilon_{\alpha\beta}^n \\ y_n(x) &= \frac{N_n(x)}{N_p(x)} \end{aligned}$$

- In leptoquark models, one has $\varepsilon_{\alpha\beta}^{u,d}$ only
- Presence of ε_{ij} affect mass ordering and CP violation

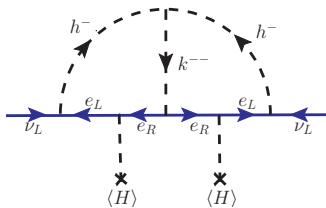
Esteban, Gonzalez-Garcia, Maltoni (2019)

NSI in Zee-Babu Model

- Two $SU(2)_L$ singlet Higgs fields, h^+ and k^{++} are introduced
- The corresponding Lagrangina reads:

$$\mathcal{L} = \mathcal{L}_{SM} + f_{ab} \overline{\Psi_{aL}^C} \Psi_{bL} h^+ + h_{ab} \overline{l_{aR}^C} l_{bR} k^{++} - \mu h^- h^- k^{++} + h.c. + V_H$$

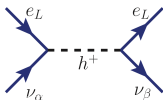
- Majorana neutrino masses are generated by 2-loop diagram:



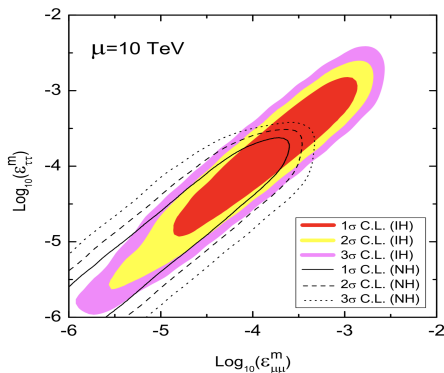
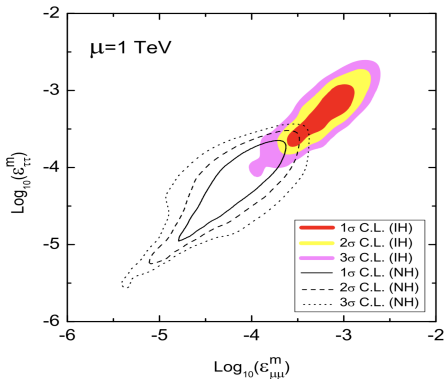
$$M_\nu \approx \frac{1}{(16\pi^2)^2} \frac{8\mu}{M^2} f_{ac} \tilde{h}_{cd} m_c m_d (f^\dagger)_{db} \tilde{I} \left(\frac{m_k^2}{m_h^2} \right)$$

NSI in Zee-Babu Model

The heavy singly charged scalar induces **nonstandard neutrino interactions**:



$$\epsilon_{\alpha\beta}^m = \epsilon_{\alpha\beta}^{ee} = \frac{f_{e\beta} f_{e\alpha}^*}{\sqrt{2} G_F m_h^2}$$



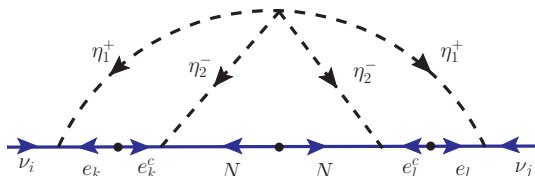
T. Ohlsson et al. (2009)

NSI in KNT Model

- Singlet fermion \mathbf{N} and two singlet scalars η_1^+ and η_2^+ are introduced

$$\mathcal{L}_Y = f LL\eta_1^+ + g e^c N \eta_2^- + \frac{1}{2} M_N N N$$

- η_2^+ and \mathbf{N} are odd under Z_2
- Majorana neutrino masses are generated via 3-loop diagram



- Only NSI is from η_1^+

Zee Model

- Gauge symmetry is same as Standard Model
- Zee Model has a second Higgs doublet H_2 and a charged weak singlet η^+ scalars

$$H_1 = \begin{pmatrix} H_1^+ \\ \frac{1}{\sqrt{2}}(v + H_1^0 + iG^0) \end{pmatrix}, \quad H_2 = \begin{pmatrix} H_2^+ \\ \frac{1}{\sqrt{2}}(H_2^0 + iA) \end{pmatrix}$$

- The Yukawa lagrangian reads:

$$\mathcal{L}_Y = f^{ab}(\psi_{aL}^i C \psi_{bL}^j) \epsilon_{ij} \eta^+ + \bar{\psi}_L \tilde{Y} H_1 e_R + \bar{\psi}_L Y H_2 e_R + h.c.$$

$$V = \mu H_1^i H_2^j \eta^- + h.c. + \dots$$

- Mixing between η^+ and H_2^+ :

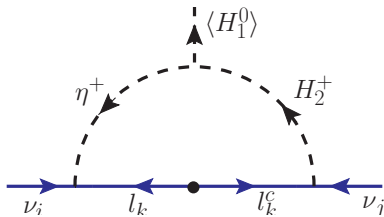
$$\begin{pmatrix} M_2^2 & -\mu v/\sqrt{2} \\ -\mu v/\sqrt{2} & M_3^2 \end{pmatrix}, \quad \sin 2\varphi = \frac{\sqrt{2}v\mu}{m_{h^+}^2 - m_{H^+}^2}$$

Neutrino masses in the Zee Model

- Yukawa coupling matrices:

$$f = \begin{pmatrix} 0 & f_{e\mu} & f_{e\tau} \\ -f_{e\mu} & 0 & f_{\mu\tau} \\ -f_{e\tau} & -f_{\mu\tau} & 0 \end{pmatrix}, \quad y = \begin{pmatrix} y_{ee} & y_{e\mu} & y_{e\tau} \\ y_{\mu e} & y_{\mu\mu} & y_{\mu\tau} \\ y_{\tau e} & y_{\tau\mu} & y_{\tau\tau} \end{pmatrix}$$

- Neutrino masses:



$$M_\nu = \kappa (f M_l y^T + y M_l f^T)$$

$$\kappa = \frac{1}{16\pi^2} \sin 2\varphi \log \frac{m_{h^+}^2}{m_{H^+}^2}$$

Neutrino masses in the Zee Model

- If $y \propto M_l$, which happens with a Z_2 , then model is ruled out
Wolfenstein (1980)
- In general, y is not proportional to M_l , and the model gives reasonable fit to oscillation data
- Charged current NSI arises via the exchange of h^\pm

Consistency with Neutrino Oscillation Data

$$M_l = \begin{pmatrix} m_e & 0 & 0 \\ 0 & m_\mu & 0 \\ 0 & 0 & m_\tau \end{pmatrix} \quad y = \begin{pmatrix} 0 & 0 & y_{e\tau} \\ 0 & y_{\mu\mu} & y_{\mu\tau} \\ y_{\tau e} & 0 & y_{\tau\tau} \end{pmatrix}$$

With the choice of parameters:

$$\frac{f_{e\mu}}{f_{\mu\tau}} = 0.42, \quad \frac{f_{e\tau}}{f_{\mu\tau}} = 4.34, \quad \frac{y_{e\tau}}{y_{\tau e}} = 0.003$$

$$\frac{y_{\mu\mu}}{y_{\tau e}} = 0.011, \quad \frac{y_{\mu\tau}}{y_{\tau e}} = -0.013, \quad \frac{y_{\tau\tau}}{y_{\tau e}} = 0.015$$

Parameters	3σ range	Benchmark Points
$\Delta m_{21}^2 (10^{-5})$	6.79 - 8.01	7.32
$\Delta m_{23}^2 (10^{-3})$	2.412 - 2.611	2.51
$\sin^2 \theta_{12}$	0.275 - 0.350	0.349
$\sin^2 \theta_{23}$	0.423 - 0.629	0.54
$\sin^2 \theta_{13}$	0.02068 - 0.02463	0.0236

Consistency with Neutrino Oscillation Data

$$y = \begin{pmatrix} y_{ee} & 0 & y_{e\tau} \\ 0 & y_{\mu\mu} & y_{\mu\tau} \\ 0 & 0 & y_{\tau\tau} \end{pmatrix}$$

With the choice of parameters:

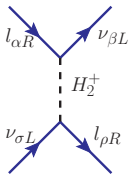
$$\frac{f_{e\mu}}{f_{\mu\tau}} = 4.55, \quad \frac{f_{e\tau}}{f_{\mu\tau}} = 1.79, \quad \frac{y_{e\tau}}{y_{ee}} = -0.049,$$

$$\frac{y_{\mu\mu}}{y_{ee}} = 0.99, \quad \frac{y_{\mu\tau}}{y_{ee}} = 0.046, \quad \frac{y_{\tau\tau}}{y_{ee}} = 0.21$$

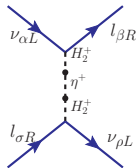
Parameters	3σ range	Benchmark Points
$\Delta m_{21}^2 (10^{-5})$	6.79 - 8.01	6.95
$\Delta m_{23}^2 (10^{-3})$	2.412 - 2.611	2.44
$\sin^2 \theta_{12}$	0.275 - 0.350	0.323
$\sin^2 \theta_{23}$	0.423 - 0.629	0.581
$\sin^2 \theta_{13}$	0.02068 - 0.02463	0.0208

NSI in Zee Model

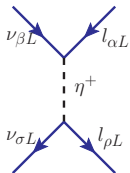
- The singly-charged scalars η^+ and H_2^+ induce NSI at tree level:



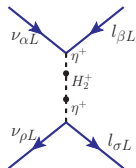
$$\sim \frac{\cos^2 \varphi}{m_{H^+}^2} y_{\alpha\beta} y_{\sigma\rho}^*$$



$$\sim \frac{\sin^2 \varphi}{m_{h^+}^2} y_{\alpha\beta} y_{\rho\sigma}^*$$



$$\sim \frac{\cos^2 \varphi}{m_{H^+}^2} f_{\alpha\beta} f_{\sigma\rho}^*$$



$$\sim \frac{\sin^2 \varphi}{m_{h^+}^2} f_{\alpha\beta} f_{\rho\sigma}^*$$

NSI in the Zee Model

- Considering, $y \sim \mathcal{O}(1)$, $m_\tau \sim 1.7 \text{ GeV}$ and $M_\nu \sim \mathcal{O}(10^{-1}) \text{ eV}$ demands $f \sim 10^{-8} \implies$ NSI effect from f is heavily suppressed
- The effective NSI is:

$$\varepsilon_{\alpha\beta}^m = -\frac{1}{4\sqrt{2}} \sin^2 \varphi \frac{y_{\alpha e}^* y_{\beta e}}{G_F m_{h^+}^2}$$

- The relevant Yukawas for NSI:

$$\begin{array}{ll} \varepsilon_{ee}^m \sim |y_{ee}|^2 & \varepsilon_{e\mu}^m \sim y_{ee}^* y_{\mu e} \\ \varepsilon_{\mu\mu}^m \sim |y_{\mu e}|^2 & \varepsilon_{\mu\tau}^m \sim y_{\mu e}^* y_{\tau e} \\ \varepsilon_{\tau\tau}^m \sim |y_{\tau e}|^2 & \varepsilon_{e\tau}^m \sim y_{ee}^* y_{\tau e} \end{array}$$

$$\begin{pmatrix} y_{ee} & y_{e\mu} & y_{e\tau} \\ y_{\mu e} & y_{\mu\mu} & y_{\mu\tau} \\ y_{\tau e} & y_{\tau\mu} & y_{\tau\tau} \end{pmatrix}$$

- Note: $\varepsilon_{\alpha\alpha} < 0$

NSI in Leptoquark: Colored Zee Model

- Two $SU(3)_C$ scalar fields, $\Omega \sim (3, 2, 1/6)$ and $\chi^{-1/3} \sim (3, 1, -1/3)$, are introduced

$$\Omega = \begin{pmatrix} \omega^{2/3} \\ \omega^{-1/3} \end{pmatrix} \quad \chi^{-1/3}$$

- The Yukawa lagrangian reads:

$$\mathcal{L}_Y = y_{ij} L_i d_j^c \Omega + y'_{ij} L_i Q_j \chi^* + h.c.$$

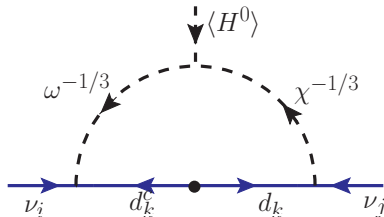
$$V = \mu \Omega \chi^* H^\dagger + h.c.$$

- Mixing between $\omega^{-1/3}$ and $\chi^{-1/3}$:

$$\begin{pmatrix} M_\omega^2 & \mu v \\ \mu v & M_\chi^{-1/3} \end{pmatrix}$$

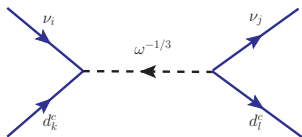
NSI in Leptoquark: Colored Zee Model

- Neutrino masses:



$$M_\nu = \frac{3 \sin 2\varphi}{32\pi^2} \log \frac{M_1^2}{M_2^2} (y M_d y'^T + y' M_d y^T)$$

- Choosing $y \cdot y' \approx 0 \implies y \sim \mathcal{O}(1)$ or $y' \sim \mathcal{O}(1)$



$$y \sim \mathcal{O}(1)$$

$$\varepsilon_{\alpha\beta}^d = \frac{1}{4\sqrt{2}} \frac{y_{\alpha 1}^* y_{\beta 1}}{G_F M_\omega^2}$$

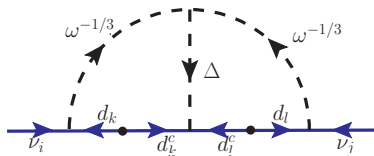
$$\text{For } \frac{N_n(x)}{N_p(x)} = 1 \implies \varepsilon_{\alpha\beta}(x) = 3\varepsilon_{\alpha\beta}^d$$

2-loop Leptoquark Model

- Same as before as it assumes $\Omega \sim (3, 2, 1/6)$ and $\chi^{-1/3} \sim (3, 1, -1/3)$
- $\chi^{-1/3}$ coupling is modified

$$\mathcal{L}_y = Y_{ij} L_i d_j^c \Omega + F_{ij} e_i^c u_j^c \chi^{-1/3} + h.c.$$

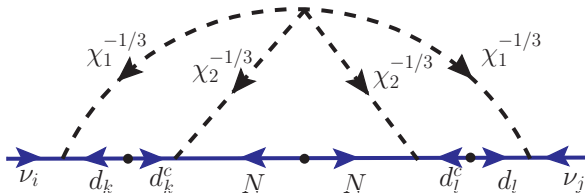
- Note F_{ij} do not lead to NSI.
- M_ν arises at 2-loops: Replace leptons by quarks in [Zee-Babu Model](#)



KNT Leptoquark Model

- Replace leptons by quarks

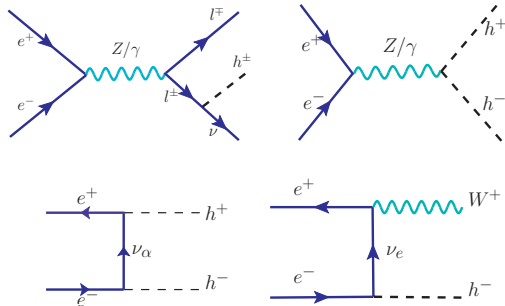
$$\mathcal{L}_y = fLQ\chi_1^{*1/3} + d^c N\chi_2^{-1/3} + \frac{1}{2}M_N N N$$



- $\chi_1^{-1/3}$ cause NSI.

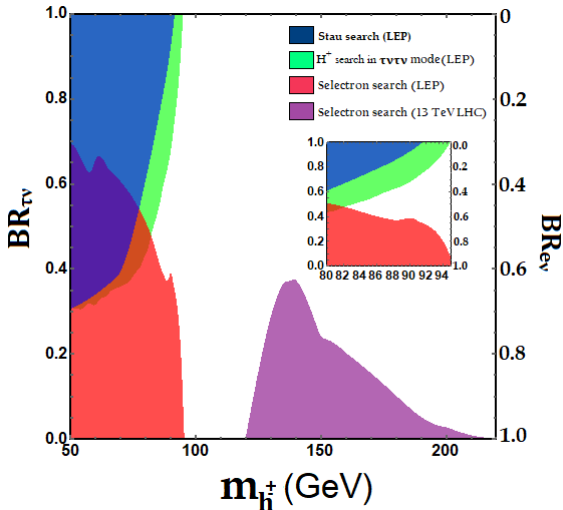
Collider constraints on h^\pm mass

- New Physics at sub-TeV scale is highly constrained from direct prompt searches as well as indirect searches.
- Direct searches: we can put bound on h^+ mass by looking at the final state (leptons + missing energy)
 - Some supersymmetric searches (Stau, Selectron) exactly mimics the charged higgs searches.
 - Dominant production mechanisms in LEP are:



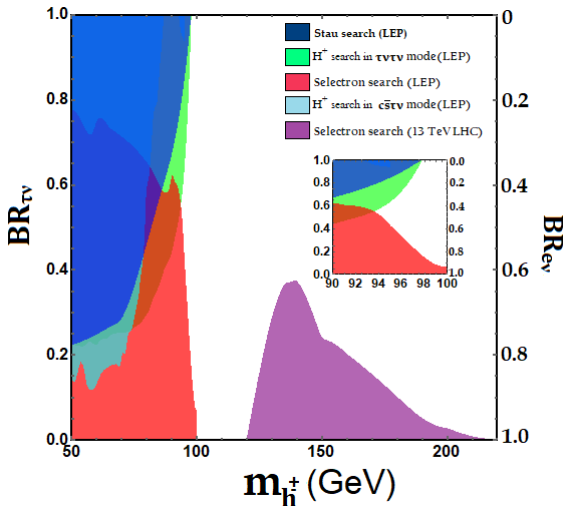
Constraints on Light Charged Scalar

- The lowest charged higgs allowed is 82 GeV with $y_{ee} = 0$.

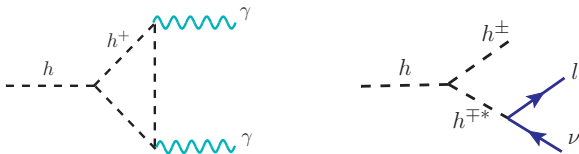


Contd.

- The lowest charged higgs allowed is 94 GeV with $y_{ae} = 1$.



Constraints from SM Higgs Observables



- The signal strength is expressed as:

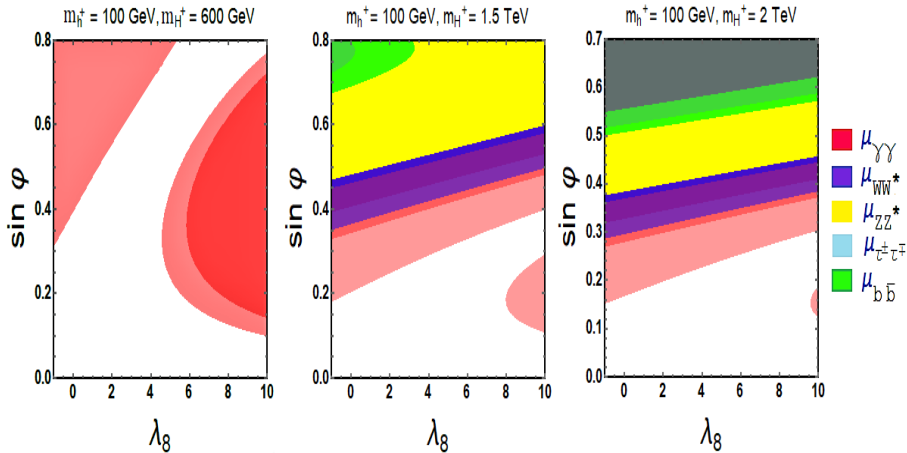
$$\mu_f^i = \frac{\sigma^i \cdot BR_f}{(\sigma^i)_{SM} \cdot (BR_f)_{SM}} = \mu^i \cdot \mu_f$$

- The effective coupling $\mu_{eff}(hh^\pm h^\mp)$ parameterized as:

$$\mu_{eff} = -\sqrt{2}\mu \sin \varphi \cos \varphi + \lambda_3 v \sin^2 \varphi + \lambda_8 v \cos^2 \varphi$$

- λ_3 term is suppressed by $\sin^2 \varphi$

Constraints from SM Higgs Observables



Contact Interaction Constraints on Neutral Higgs

- At LEP experiment, e^+e^- collision above the Z boson mass imposes significant constraints on contact interactions involving e^+e^- and fermion pair.
- An effective Lagrangian has the form:

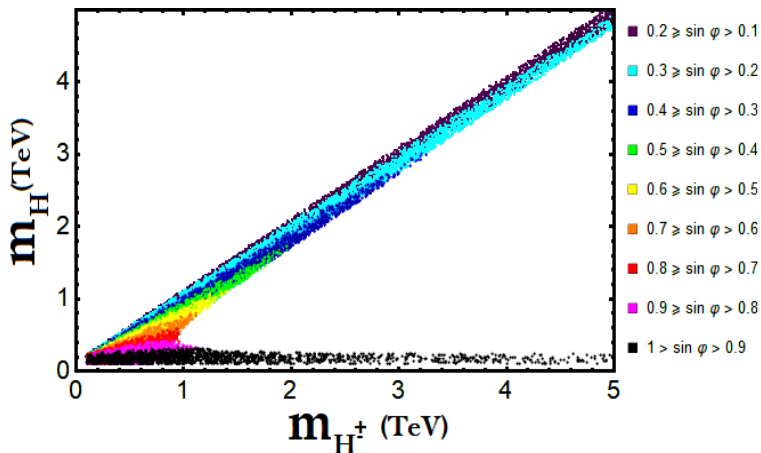
$$\mathcal{L}_{eff} = \frac{4\pi}{\Lambda^2(1 + \delta_{ef})} \sum_{i,j=L,R} \eta_{ij}^f (\bar{e}_i \gamma^\mu e_i) (\bar{f}_j \gamma_\mu f_j)$$

$$\frac{m_H}{|y_{e\mu}| \cos \varphi} > 1.577 \text{ TeV},$$

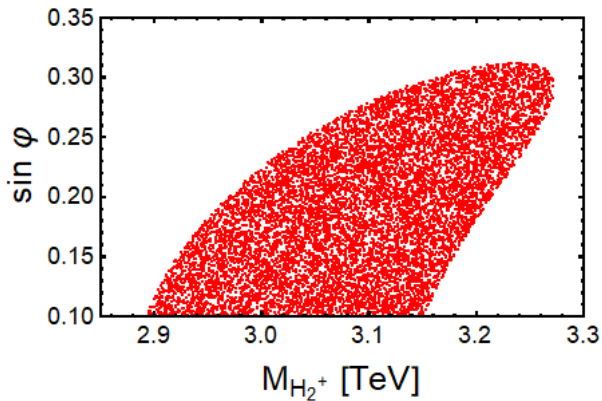
$$\frac{m_H}{|y_{e\tau}| \cos \varphi} > 438.9 \text{ GeV},$$

$$\frac{m_H}{|y_{ee}| \cos \varphi} > 1.994 \text{ TeV}$$

Bound from EW Precision Constraints



Bound from EW Precision Constraints



Lepton Flavor Violation

- Lepton number(L) is an accidental discrete or Abelian symmetry of the standard model (SM)
- Lepton flavor violation (LFV) is transition between e, μ, τ sectors that violates lepton family number.
- Detection of LFV signals \implies clear evidence for BSM

LFV Constraints in Zee Model

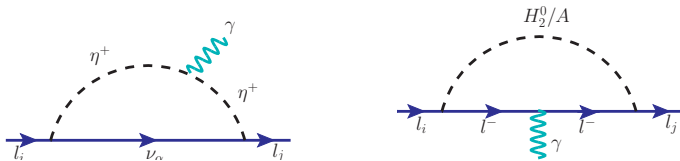
- The presence of the second Higgs doublet gives rise to **tree-level** **trilepton decays** $l_i \rightarrow l_j l_k l_l$

Process	Exp. bound	Constraint
$\mu^- \rightarrow e^+ e^- e^-$	$\text{Br.} < 1.0 \times 10^{-12}$	$\frac{ y_{\mu e}^* y_{ee} }{m_H^2} < 6.6 \times 10^{-11} \text{ GeV}^{-2}$
$\tau^- \rightarrow e^+ e^- e^-$	$\text{Br.} < 2.7 \times 10^{-8}$	$\frac{ y_{\tau e}^* y_{ee} }{m_H^2} < 2.4 \times 10^{-9} \text{ GeV}^{-2}$
$\tau^- \rightarrow e^+ \mu^- \mu^-$	$\text{Br.} < 1.7 \times 10^{-8}$	$\frac{ y_{\tau \mu}^* y_{\mu e} }{m_H^2} < 2.04 \times 10^{-9} \text{ GeV}^{-2}$
$\tau^- \rightarrow e^+ e^- \mu^-$	$\text{Br.} < 1.8 \times 10^{-8}$	$\frac{ y_{\tau \mu}^* y_{ee} }{m_H^2} < 2.12 \times 10^{-9} \text{ GeV}^{-2}$
$\tau^- \rightarrow \mu^+ e^- e^-$	$\text{Br.} < 1.5 \times 10^{-8}$	$\frac{ y_{\tau e}^* y_{e\mu} }{m_H^2} < 1.8 \times 10^{-9} \text{ GeV}^{-2}$
$\tau^- \rightarrow \mu^+ \mu^- \mu^-$	$\text{Br.} < 2.1 \times 10^{-8}$	$\frac{ y_{\tau \mu}^* y_{\mu \mu} }{m_H^2} < 2.21 \times 10^{-9} \text{ GeV}^{-2}$
$\tau^- \rightarrow \mu^+ e^- \mu^-$	$\text{Br.} < 2.7 \times 10^{-8}$	$\frac{ y_{\tau \mu}^* y_{e\mu} }{m_H^2} < 3 \times 10^{-9} \text{ GeV}^{-2}$

- These tree-level processes do not restrict the parameter space as much as $l_i \rightarrow l_j \gamma$

LFV Constraints in Zee Model

- One of the most constrained **cLFV** process is the **radiative process**
 $l_i \rightarrow l_j \gamma$
- This process always arises at **loop level**

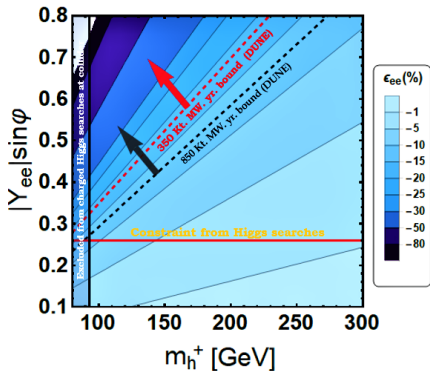


Process	Exp. bound	Constraint
$e \rightarrow e\gamma$	$\delta(g-2)_e < 1.34 \times 10^{-12}$	$\frac{\sin^2 \varphi}{m_{h^+}^2} (y_{ee} ^2 + y_{\mu e} ^2 + y_{\tau e} ^2) < \frac{5.092 \times 10^{-3}}{\text{GeV}^2}$
$\mu \rightarrow \mu\gamma$	$\delta(g-2)_\mu < 3.64 \times 10^{-9}$	$\frac{\sin^2 \varphi}{m_{h^+}^2} (y_{e\mu} ^2 + y_{\mu\mu} ^2 + y_{\tau\mu} ^2) < \frac{3.155 \times 10^{-5}}{\text{GeV}^2}$
$\mu \rightarrow e\gamma$	Br. < 4.2×10^{-13}	$\frac{\sin^4 \varphi}{m_{h^+}^4} (y_{ee}^* y_{e\mu} ^2 + y_{\mu e}^* y_{\mu\mu} ^2 + y_{\tau e}^* y_{\tau\mu} ^2) < \frac{9.52 \times 10^{-18}}{\text{GeV}^4}$
$\tau \rightarrow e\gamma$	Br. < 3.3×10^{-8}	$\frac{\sin^4 \varphi}{m_{h^+}^4} (y_{e\mu}^* y_{e\tau} ^2 + y_{\mu e}^* y_{\mu\tau} ^2 + y_{\tau e}^* y_{\tau\tau} ^2) < \frac{3.91 \times 10^{-12}}{\text{GeV}^4}$
$\tau \rightarrow \mu\gamma$	Br. < 4.4×10^{-8}	$\frac{\sin^4 \varphi}{m_{h^+}^4} (y_{e\mu}^* y_{e\tau} ^2 + y_{\mu\mu}^* y_{\mu\tau} ^2 + y_{\tau\mu}^* y_{\tau\tau} ^2) < \frac{5.25 \times 10^{-12}}{\text{GeV}^4}$

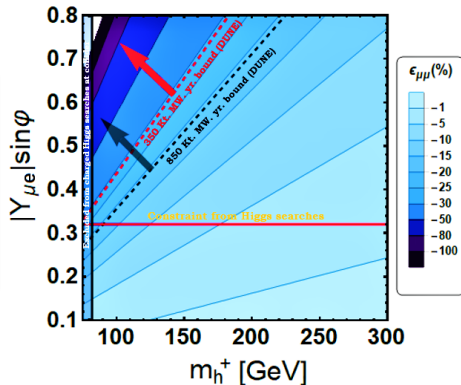
Numerical results for NSI

$$\epsilon_{ee}^m = -\frac{1}{4\sqrt{2}} \sin^2 \varphi \frac{|y_{ee}|^2}{G_F m_{h^+}^2}$$

$$\epsilon_{\mu\mu}^m = -\frac{1}{4\sqrt{2}} \sin^2 \varphi \frac{|y_{\mu e}|^2}{G_F m_{h^+}^2}$$



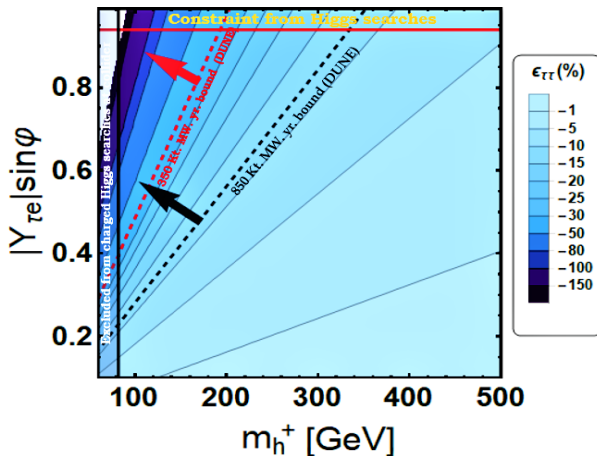
$$\epsilon_{ee}^{\max} \approx 11\%$$



$$\epsilon_{\mu\mu}^{\max} \approx 20\%$$

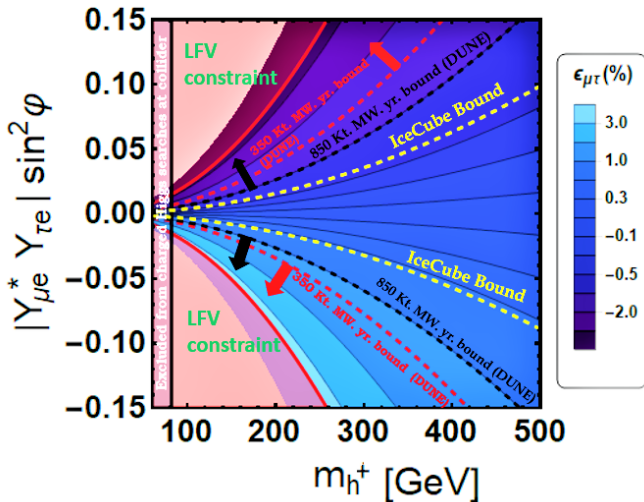
Contd.

$$\epsilon_{\tau\tau}^m = -\frac{1}{4\sqrt{2}} \sin^2 \varphi \frac{|y_{\tau e}|^2}{G_F m_{h^+}^2}$$



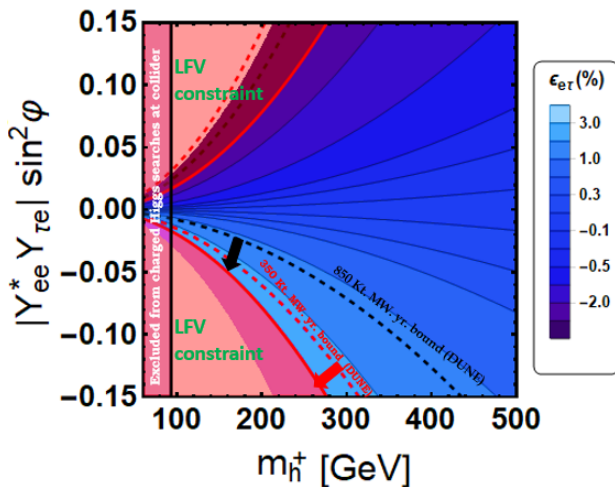
$$\epsilon_{\tau\tau}^{\max} \approx 150\%$$

Contd.



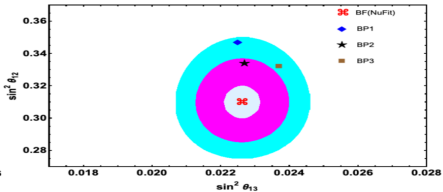
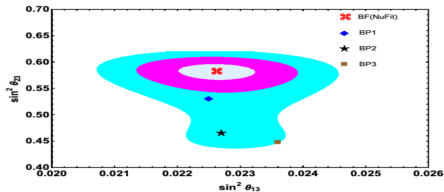
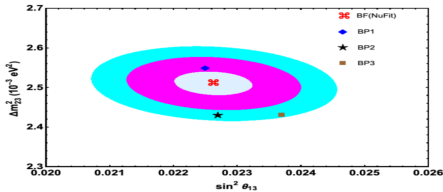
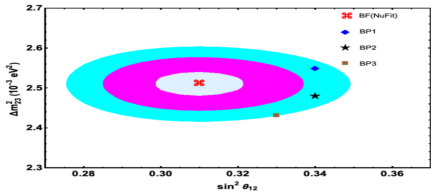
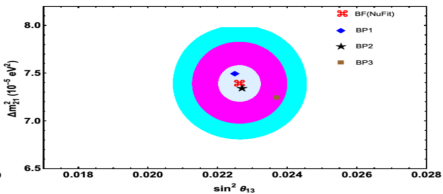
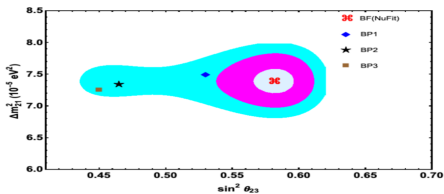
$$\epsilon_{\mu\tau}^{\max} \approx 2.5\%$$

Contd.



$$\epsilon_{e\tau}^{\max} \approx 2.5\%$$

Consistency with Neutrino Oscillation Data



Numerical results for Leptoquark Colored Zee Model

- Considering the pair-production channel, the current CMS limits on leptoquark masses are 1.43 TeV for first generation, 1.25 TeV for second generation, and 1.02 TeV for third generation.
- Constraints on Yukawa $y_{\alpha i}$

- $\mu \rightarrow e\gamma$: No significant constraints due to cancellations. This suppresses amplitude by $\frac{m_b^2}{m_\omega^2} \ll 1$

- $\mu \rightarrow 3e$

$$|y_{13}y_{23}| < 7.6 \times 10^{-3} \quad M_\omega = 1\text{TeV}$$

- $\mu - e$ conversion

$$|y_{11}y_{21}| < 3.3 \times 10^{-7} \quad M_\omega = 1\text{TeV}$$

- $\tau^- \rightarrow e^- \eta$ and $\tau^- \rightarrow \mu^- \eta$

$$|y_{12}y_{32}| < 1.2 \times 10^{-2} \left(\frac{M_\omega}{300\text{GeV}}\right)^2 \quad |y_{22}y_{32}| < 1.0 \times 10^{-2} \left(\frac{M_\omega}{300\text{GeV}}\right)^2$$

- Atomic Parity Violation constraints:

$$y_{11} < 0.03 \frac{M_\omega^{2/3}}{100 \text{ GeV}} \quad y'_{11} < 0.03 \frac{M_\chi}{100 \text{ GeV}}$$

- ϵ_{ee} , $\epsilon_{e\mu}$, and $\epsilon_{e\tau}$ cannot be too large as one y_{e1} factor is order 0.3 for 1 TeV Leptoquark mass

$$\begin{aligned} \epsilon_{ee} &\approx 0.33\% & \epsilon_{e\mu} &= 2.2\% & \epsilon_{e\tau} &= 2.2\% \\ \epsilon_{\mu\mu} &= 14.7\% & \epsilon_{\mu\tau} &\approx 14.7\% & \epsilon_{\tau\tau} &\approx 14.7\% \end{aligned}$$

Conclusion

- Matter NSI in the radiative mass models has been studied.
- Mass as low as 82 GeV for the charged scalar is shown to be consistent with direct and indirect limits from LEP and LHC.
- Diagonal NSI in Zee Model are allowed to be as large as (11 % , 20 % , 150 %) for $(\varepsilon_{ee}, \varepsilon_{\mu\mu}, \varepsilon_{\tau\tau})$, while off-diagonal NSIs are allowed to be (-, 2.5 % , 2.5 %) for $(\varepsilon_{e\mu}, \varepsilon_{e\tau}, \varepsilon_{\mu\tau})$.
- NSI in leptoquark models are studied.
- Radiative neutrino mass model allows parameters which are in good agreement with the neutrino oscillation experiments

Thank You

Dune Projected Limits

NSI Parameter	300 Kt.MW.yr bound ($\leq 90\%$)	850 Kt.MW.yr bound ($\leq 90\%$)
$\varepsilon_{e\mu}$	-0.025 \rightarrow +0.052	-0.017 \rightarrow +0.04
$\varepsilon_{e\tau}$	-0.055 \rightarrow +0.023	-0.042 \rightarrow +0.012
$\varepsilon_{\mu\tau}$	-0.015 \rightarrow +0.013	-0.01 \rightarrow +0.01
ε_{ee}	-0.185 \rightarrow +0.38	-0.13 \rightarrow +0.185
$\varepsilon_{\mu\mu}$	-0.29 \rightarrow +0.39	-0.192 \rightarrow +0.24
$\varepsilon_{\tau\tau}$	-0.36 \rightarrow +0.145	-0.12 \rightarrow +0.095