

### DI-MUON PRODUCTION IN HEAVY-ION COLLISIONS: A SIGNAL FOR QUARK-GLUON DECONFINEMENT

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### Happy birthday Marcelo!!!

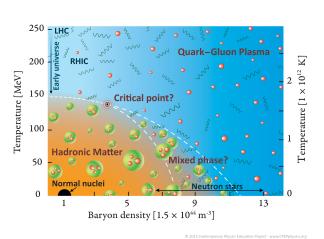






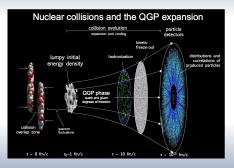


### Strongly interacting matter in extreme conditions.

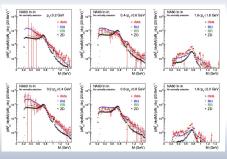




### Electromagnetic probes.



arXiv:0905.0174 by P. Sorensen



Eur. Phys. J. C 61, 711 (2009) by R. Arnaldi, et al.



### QCD Sum Rules.

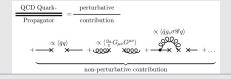
The QCD Sum Rules are an analytical formalism, they include non-perturbative and perturbative information of QCD.

#### Operator Product Expansion (OPE).

The correlation function of these currents is introduced and treated in the framework of the OPE.

$$\Pi_0^{\text{QCD}}(Q^2) = C_0 \,\hat{I} + \sum_{N=1} \frac{C_{2N}(Q^2, \mu^2)}{Q^{2N}} \langle \hat{\mathcal{O}}_{2N}(\mu^2) \rangle \;.$$

OPE includes the short- and long-distance quark-gluon interactions.





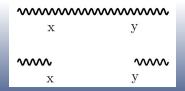
### QCD Sum Rules.

QCD information is then matched to a sum over hadronics states. where

$$\Pi(q^2) = i \int d^4x e^{iqx} \langle 0|T(J(x)J^{\dagger}(0))|0\rangle.$$

Correlation function in QFT.

$$\langle 0|T(J(y)J^{\dagger}(x))|0\rangle.$$



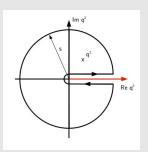




### QCD Sum Rules.

$$\Pi_0^{\rm QCD}(Q^2) \Leftrightarrow \Pi_0^{\rm HAD}(Q^2)$$
?

#### Cauchy's Theorem.



- The discontinuity across the real axis brings in the hadronic spectral function.
- Integration around the circle involves the QCD correlator.
- The radius of the circle (typically named s<sub>0</sub>) is the onset of pQCD.

Finite Energy QCD Sum Rules (FESR).



### FESR.

Time to join both sectors!!!

$$\int_{0}^{s_{0}} ds P(s) \frac{1}{\pi} \text{Im} \Pi(s) = -\oint_{C(|s_{0}|)} ds P(s) \Pi^{OPE}(s).$$

$$\int_{0}^{s_{0}} ds P(s) \frac{1}{\pi} \text{Im} \Pi(s) = -\oint_{C(|s_{0}|)} ds P(s) C_{0} \hat{I}$$

$$- \sum_{N=1} \oint_{C(|s_{0}|)} ds P(s) \frac{C_{2N}(Q^{2}, \mu^{2})}{Q^{2N}} \langle \hat{\mathcal{O}}_{2N}(\mu^{2}) \rangle.$$

$$(-1)^{N}C_{2N+2}\langle \widehat{O}_{2N+2}\rangle = \int_{0}^{s_{0}} ds \ s^{N} \frac{1}{\pi} \operatorname{Im} \Pi^{HAD}(s) + \frac{1}{2\pi i} \oint_{C(|s_{0}|)} ds \ s^{N} \Pi^{QCD}(s).$$



### FESR at finite temperature.

• We work with QFT at finite temperature.

$$S_{F}(T=0) = \frac{\cancel{k} + m}{k^{2} - m^{2} + i\epsilon},$$

$$S_{F}(T) = S_{F}(T=0) + 2\pi i \delta(k^{2} - m^{2})(\cancel{k} + m) n_{F}(|k_{0}|),$$

$$D_{B}(T=0) = \frac{i}{p^{2} - m^{2} + i\epsilon},$$

$$D_{B}(T) = D_{B}(T=0) + 2\pi \delta(p^{2} - m^{2}) n_{B}(|k_{0}|).$$

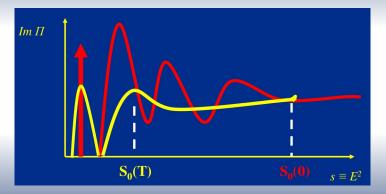
Wilson coefficients acquire explicitly the thermal behavior.

• Hadronic parameters develop thermal behaviour (Masses, coupling constants, resonance's widths).



### FESR at finite temperature.

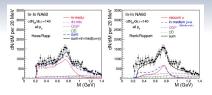
• The parameter  $s_0$  is thermal-dependent.

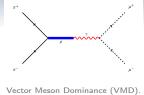


Cesareo A. Dominguez

Qualitative parameter of deconfinement.







Eur. Phys. J. C 61, 711 (2009) by R. Arnaldi, et al.

 $Im\Pi^{HAD}(s)$  is related with the hadronic spectral function and the latter is well approximated by the Breit-Wigner form

$$\frac{1}{\pi} \text{Im}\Pi^{\text{HAD}}(s) = \frac{1}{\pi} \frac{1}{f_{\rho}^{2}} \frac{M_{\rho}^{3} \Gamma_{\rho}}{(s - M_{\rho}^{2})^{2} + M_{\rho}^{2} \Gamma_{\rho}}$$

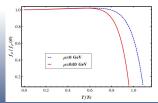
Finite Sum Rules at finite temperature.

$$(-1)^{N-1}C_{2N}\langle O_{2N}\rangle = 8\pi^2 \left[ \int_0^{s_0} ds \ s^{N-1} \frac{1}{\pi} |\mathsf{Im}\Pi^{\mathsf{HAD}}(s) - \frac{1}{2\pi i} \oint_{C(|s_0|)} ds \ s^{N-1}\Pi^{\mathsf{QCD}}(s) \right],$$

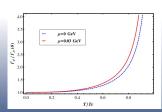


The solution from FESR for all hadronic parameters as a function of  ${\it T}$  are the following

$$\begin{split} \Gamma_{\rho}(T) &=& \Gamma_{\rho}(0)[1-(T/T_c)^3]^{-1}, \\ M_{\rho}(T) &=& M_{\rho}(0)[1-(T/T_M^*)^{10}], \\ f_{\rho}(T) &=& f_{\rho}(0)[1-0.3901(T/T_c)^{10.75} \\ &+& 0.04155(T/T_c)^{1.27}]. \end{split}$$



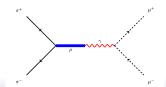
Temperature behaviour of  $f_o$ 



Temperature behaviour of  $\Gamma_{\alpha}$ 



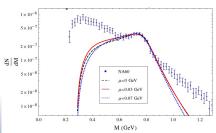
With the solution from the FESR, we proceed to compute the di-muon thermal rate in the hadronic phase originating from  $\rho$  decays. (We consider processes where pions annihilate into  $\rho$  which in turn decay into di-muon by means vector dominance.)



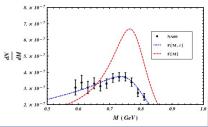
$$\frac{\frac{dN}{d^4 \times d^4 K}}{\frac{d^4 \times d^4 K}{d^4 \times d^4 K}} = \frac{\alpha^2}{48\pi^4} \left(1 + \frac{2m^2}{M^2}\right) \left(1 - \frac{4m_\pi^2}{M^2}\right) \times \sqrt{1 - \frac{4m^2}{M^2}} \, \mathrm{e}^{-K_0 / T} \mathcal{R}(K, T) \frac{|\mathsf{m} \mathsf{m}^\mathsf{res}_0(\mathsf{M}^2),}{\mathsf{m}^2}$$



Non-model dependence result but directly from the perturbative and non-perturbative QCD information.



Invariant di-muon mass distribution compared to NA60



(Linear scale) Invariant di-muon distribution around p-meson peak compared to NA60 data.

### Thank you!!!

#### For more information and details:

- A. Ayala and C. A. Dominguez and L. A. Hernandez and M. Loewe and M. J. Mizher, Phys. Rev. D88, 114028, (2013)
- A. Ayala and C. A. Dominguez and M. Loewe and Y. Zhang, Phys. Rev. D86, 114036, (2012)



- QCD Sum Rules was developed more than 30 years ago by Shifman, Vainshtein and Zakharov (SVZ).
- light-quark vector current correlator, which at T=0 can be written as

$$\Pi_{\mu\nu}(q^2) = i \int d^4x e^{iq\cdot x} \langle 0|T \left[ \mathcal{V}_{\mu}(x) \mathcal{V}^{\dagger}_{\nu}(0) \right] |0\rangle$$
$$= \left( -g_{\mu\nu} + q_{\mu}q_{\nu} \right) \Pi_1(q^2),$$

where  $V_{\mu}(x)=(1/2)[:\bar{u}(x)\gamma_{\mu}u(x)-\bar{d}(x)\gamma_{\mu}d(x):]$  is the conserved vector current and  $q_{\mu}$  is the four-momentum transfer.

• In the thermal perturbative QCD sector, only one-loop contributions can be taken into account, since the problem of the appearance of two scales, i.e. the short-distance QCD scale and the critical temperature  $T_c$ , remains unsolved.



- ullet  $\Gamma_
  ho(0)=0.145$  GeV,  $M_
  ho(0)=0.776$  GeV,  $T_c=0.197$  GeV and  $f_
  ho(0)=5$
- In order to extend this analysis to finite chemical potential we first incorporate the  $\mu$  dependence into the pQCD sector, which involves a quark loop. This modifies the corresponding Fermi-Dirac distribution, splitting it into particle-antiparticle contributions. And we incorporate the  $\mu$  dependence of the critical temperature  $T_c$ . For this, we use a Schwinger-Dyson approach, a parametrization for the crossover transition line between chiral-symmetry-restored and -broken phases.

$$T_c(\mu) = T_c(\mu = 0) - 0.218\mu - 0.139\mu$$



The rate is given by

$$\frac{dN}{d^4 \times d^4 K} = \frac{\alpha^2}{48 \pi^4} \left(1 + \frac{2m^2}{M^2}\right) \left(1 - \frac{4m_\pi^2}{M^2}\right) \times \sqrt{1 - \frac{4m^2}{M^2}} e^{-K_0/T} \mathcal{R}(K, T) \mathsf{Im} \Pi_0^{\mathsf{res}}(M^2),$$

where N is the number of muon pairs per unit of infinitesimal space-time and energy-momentum volume, with  $x^{\mu}$  the space-time coordinate and  $K^{\mu}$  the four-momentum of the muon pairs,  $\alpha$  is the electromagnetic coupling, m is the muon mass,  $m_{\pi}$  is the pion mass and M is the di-muon invariant mass. And

$$\begin{split} \mathcal{R} &= \frac{T/K}{1 - e^{-K_0/T}} \\ &\times & \ln \left[ \left( \frac{e^{-E_{\max}/T} - 1}{e^{-E_{\min}/T} - 1} \right) \left( \frac{e^{E_{\min}/T} - e^{-K_0/T}}{e^{E_{\max}/T} - e^{-K_0/T}} \right) \right], \end{split}$$



with

$$E_{\text{max}} = \frac{1}{2} \left[ K_0 + K \sqrt{1 - 4m_{\pi}^2/M^2} \right]$$

$$E_{\text{min}} = \frac{1}{2} \left[ K_0 - K \sqrt{1 - 4m_{\pi}^2/M^2} \right].$$

In order to integrate the di-moun thermal rate, we use

$$d^{4}K = \frac{1}{2}dM^{2}d^{2}K_{\perp}dy$$
$$d^{4}X = \tau d\tau d\eta d^{2}X_{\perp},$$

where y and  $\eta$  are the momentum-space and coordinate-space rapidities, respectively and  $\tau = \sqrt{t^2 - z^2}$ . To relate the temperature change to the time evolution of the system, we neglect a possible small transverse expansion, assume it entirely longitudinal, and use the cooling law

$$T = T_0 \left(\frac{\tau_0}{\tau}\right)^{v_s^2},$$



where  $v_s^2=1/3$  is the square of the sound velocity for an ideal hadron gas. The evolution is taken down to a freeze-out temperature  $T_f$ . Also, we consider perfect correlation between  $\eta$  and y ( $\eta=y$ ). The invariant mass distribution becomes

$$\frac{dN}{dMdy} = \Delta y M \int_{\tau_0}^{\tau_f} \tau d\tau \int d^2 K_{\perp} \int d^2 x_{\perp} \frac{dN}{d^4 x d^4 K}.$$