

Dark photon superradiance: Electrodynamics and multimessenger signals

Cristina Mondino



Based on 2212.09772, with:

Nils Siemonsen, Daniel Egaña-Ugrinovic, Junwu Huang,
Masha Baryakhtar, and William E. East

Motivations

- New vector boson that may or may not be the dark matter,
- Ultra-low energies ($\sim 10^{-12}$ eV), macroscopical scales (km),
- Weakly coupled to the Standard Model (electromagnetism).

Outline

- Dark photon superradiance (with kinetic mixing)
- Plasma production
- Electrodynamics
- Electromagnetic emissions and signatures

Outline

- **Dark photon superradiance** (with kinetic mixing)
- Plasma production
- Electrodynamics
- Electromagnetic emissions and signatures

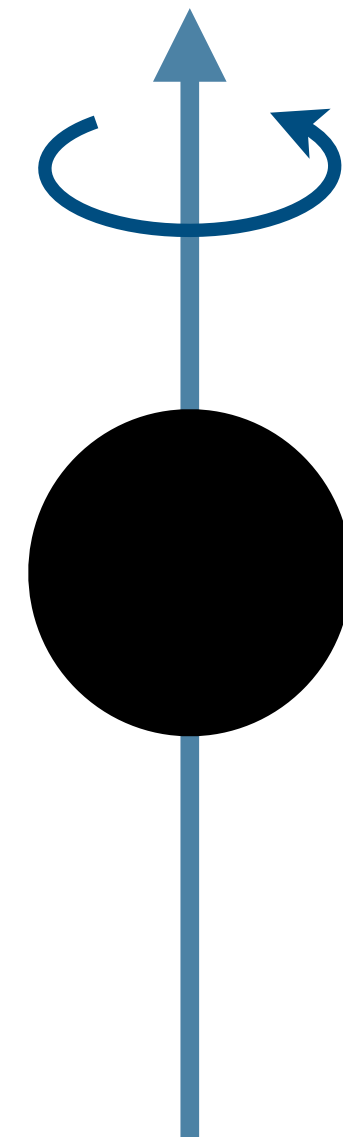
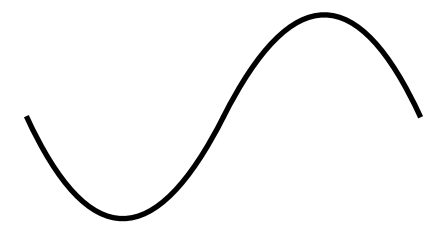
Dark photon superradiance

$$\mathcal{L} \supset -\frac{1}{4}F'_{\mu\nu}F'^{\mu\nu} - \frac{1}{2}\mu^2 A'^{\mu}A'_{\mu}$$

New massive vector boson

Boson's Compton wavelength $\frac{1}{\mu} \sim GM$ Black hole radius

Spinning back hole



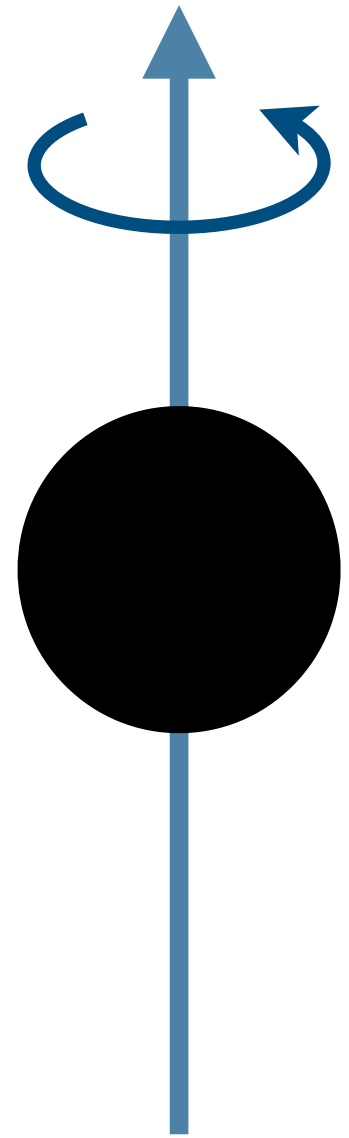
Dark photon superradiance

$$\mathcal{L} \supset -\frac{1}{4} F'_{\mu\nu} F'^{\mu\nu} - \frac{1}{2} \mu^2 A'^{\mu} A'_{\mu}$$

EOM in Kerr spacetime

$$D_{\mu} F'^{\mu\nu} = \mu^2 A'^{\nu}$$

- Hydrogen-like wave functions



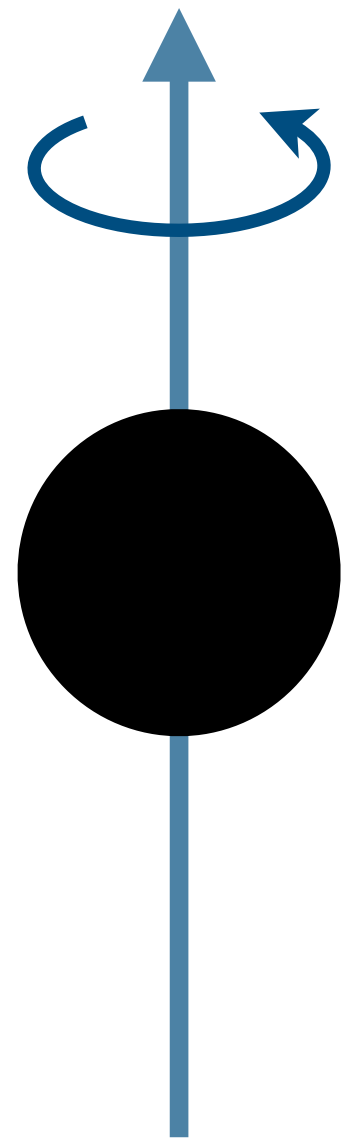
Dark photon superradiance

$$\mathcal{L} \supset -\frac{1}{4} F'_{\mu\nu} F'^{\mu\nu} - \frac{1}{2} \mu^2 A'^{\mu} A'_{\mu}$$

EOM in Kerr spacetime

$$D_{\mu} F'^{\mu\nu} = \mu^2 A'^{\nu}$$

- Hydrogen-like wave functions
- Energy with imaginary component



If $\frac{\mu}{m} \lesssim \Omega_{\text{H}}$

Orbital angular
momentum

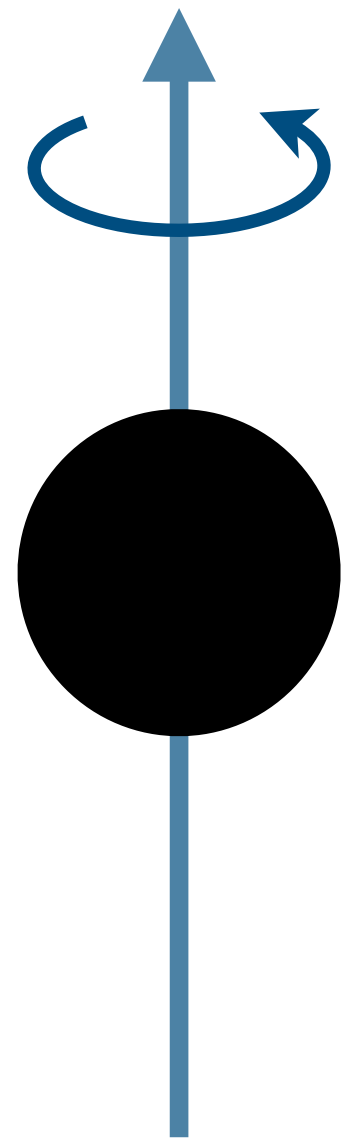
Angular velocity
of BH horizon

Dark photon superradiance

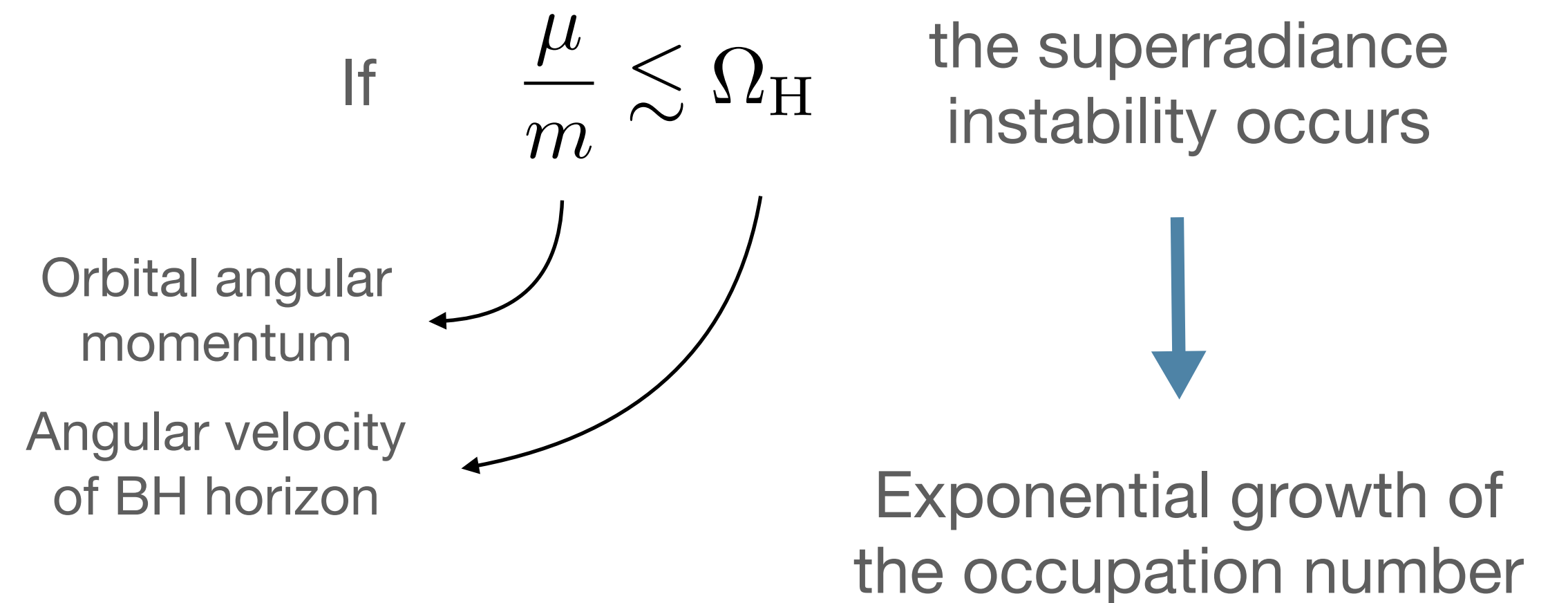
$$\mathcal{L} \supset -\frac{1}{4} F'_{\mu\nu} F'^{\mu\nu} - \frac{1}{2} \mu^2 A'^{\mu} A'_{\mu}$$

EOM in Kerr spacetime

$$D_{\mu} F'^{\mu\nu} = \mu^2 A'^{\nu}$$



- Hydrogen-like wave functions
- Energy with imaginary component



Dark photon superradiance

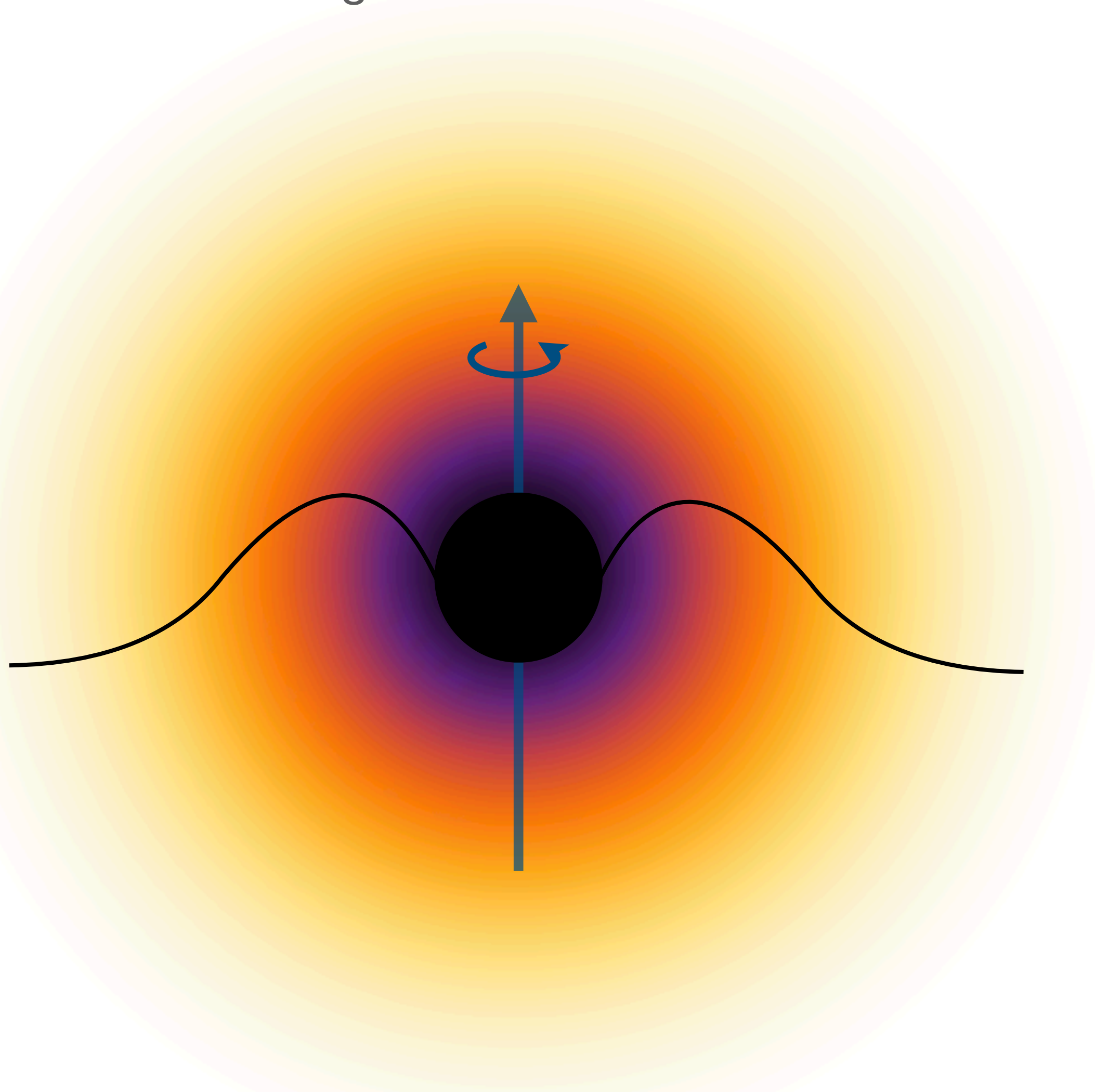
- For large enough BH spin
- Small enough vector boson mass

Gravitational coupling: $\alpha \equiv \mu GM$

For maximally spinning BH, superradiance occurs for:

$$\frac{\alpha}{m} \lesssim 0.5$$

The boson cloud extracts energy and angular momentum from the BH.



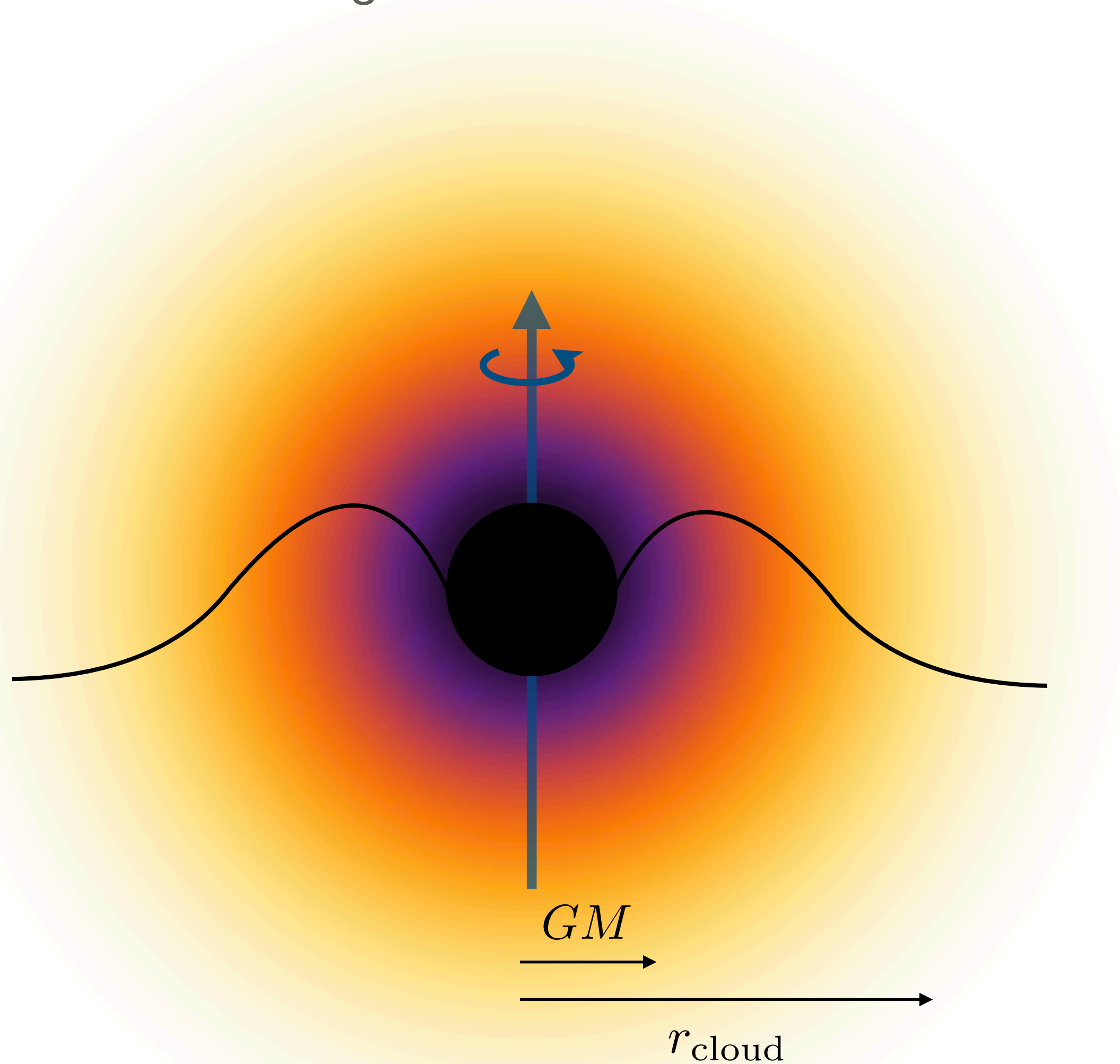
Dark photon superradiance

- For large enough BH spin
- Small enough vector boson mass

Gravitational coupling: $\alpha \equiv \mu GM$

Lowest energy level ($n=0, l=0, m=1$)
of the “gravitational atom”:

$$r_{\text{cloud}} \sim \frac{1}{\alpha\mu} = \frac{GM}{\alpha^2} \gg GM$$



Dark photon superradiance

- For large enough BH spin
- Small enough vector boson mass

Gravitational coupling: $\alpha \equiv \mu GM$

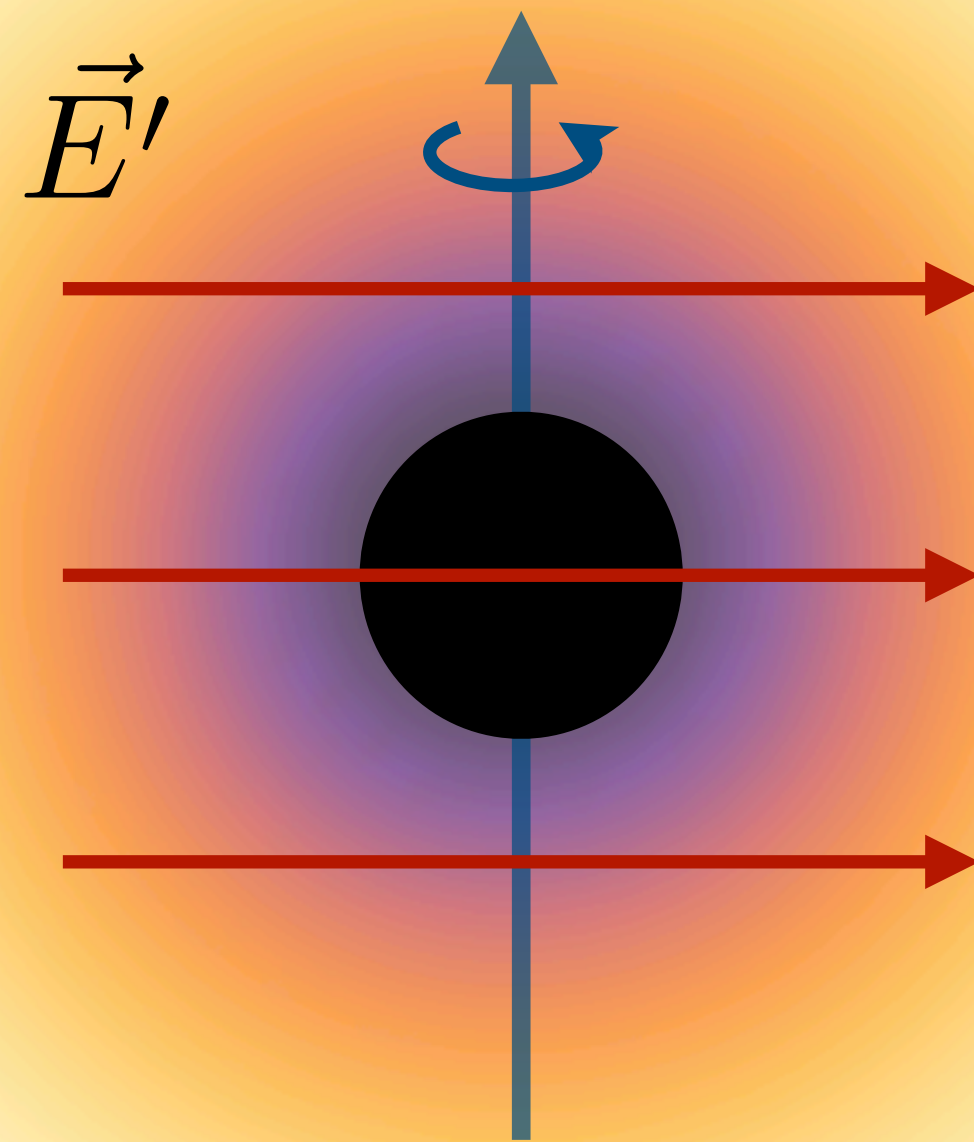
Large, rotating dark electric field

$$|\vec{E}'| \sim \alpha^{5/2} \mu M_{\text{pl}}$$

$$|\vec{B}'| \sim \alpha |\vec{E}'| \ll |\vec{E}'|$$

The rotational frequency is given
by the boson's energy

$$\omega \simeq \mu$$



Black hole superradiance

Y. B. Zeldovich, 1971

Can be used to probe ultralight bosons (axion, dark photon, etc.)

0905.4720, *String Axiverse*

A. Arvanitaki, S. Dimopoulos, S. Dubovsky, N. Kaloper, J. March–Russell

1004.3558, *Exploring the String Axiverse with Precision Black Hole Physics*

A. Arvanitaki, S. Dubovsky

1411.2263, *Discovering the QCD Axion with Black Holes and Gravitational Waves*

A. Arvanitaki, M. Baryakhtar, X. Huang

1704.04791, *Superradiant Instability and Backreaction of Massive Vector Fields around Kerr Black Holes*

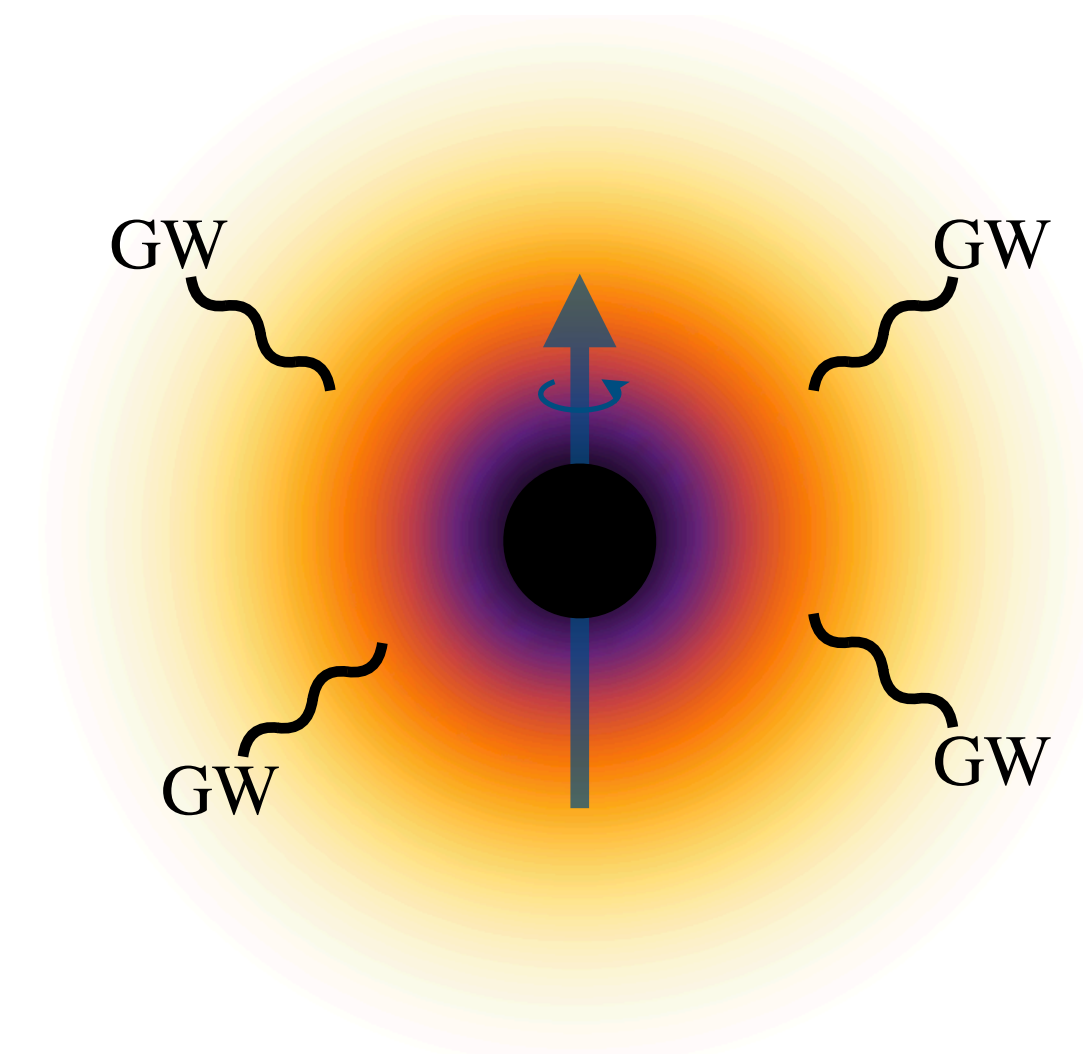
W. E. East, F. Pretorius

1801.01420, *Constraining the mass of dark photons and axion-like particles through black-hole superradiance*

V. Cardoso, O. J. C. Dias, G. S. Hartnett, M. Middleton, P. Pani, J. E. Santos

....

- Spin distribution of BH population.
- Continuous gravitational wave emissions (on going searches by Ligo-Virgo-Kagra).



Outline

- **Dark photon superradiance (with kinetic mixing)**
- Plasma production
- Electrodynamics
- Electromagnetic emissions and signatures

Dark photon kinetic mixing

$$\mathcal{L} \supset -\frac{1}{4}F'_{\mu\nu}F'^{\mu\nu} - \frac{1}{2}\mu^2 A'^{\mu}A'_{\mu} - \boxed{\frac{\varepsilon}{2}F_{\mu\nu}F'^{\mu\nu}}$$

Standard Model photon
↓

$$A_{\mu} \overset{\varepsilon \ll 1}{\sim} \text{X} \sim A'_{\mu}$$

Dark photon kinetic mixing

$$\mathcal{L} \supset -\frac{1}{4}F'_{\mu\nu}F'^{\mu\nu} - \frac{1}{2}\mu^2 A'^{\mu}A'_{\mu} - \boxed{\frac{\varepsilon}{2}F_{\mu\nu}F'^{\mu\nu}}$$

Standard Model photon
↓

$$A_{\mu} \overset{\varepsilon \ll 1}{\text{wavy}} \times \text{wavy} A'_{\mu}$$

$$\downarrow A_{\mu} \rightarrow A_{\mu} + \varepsilon A'_{\mu}$$

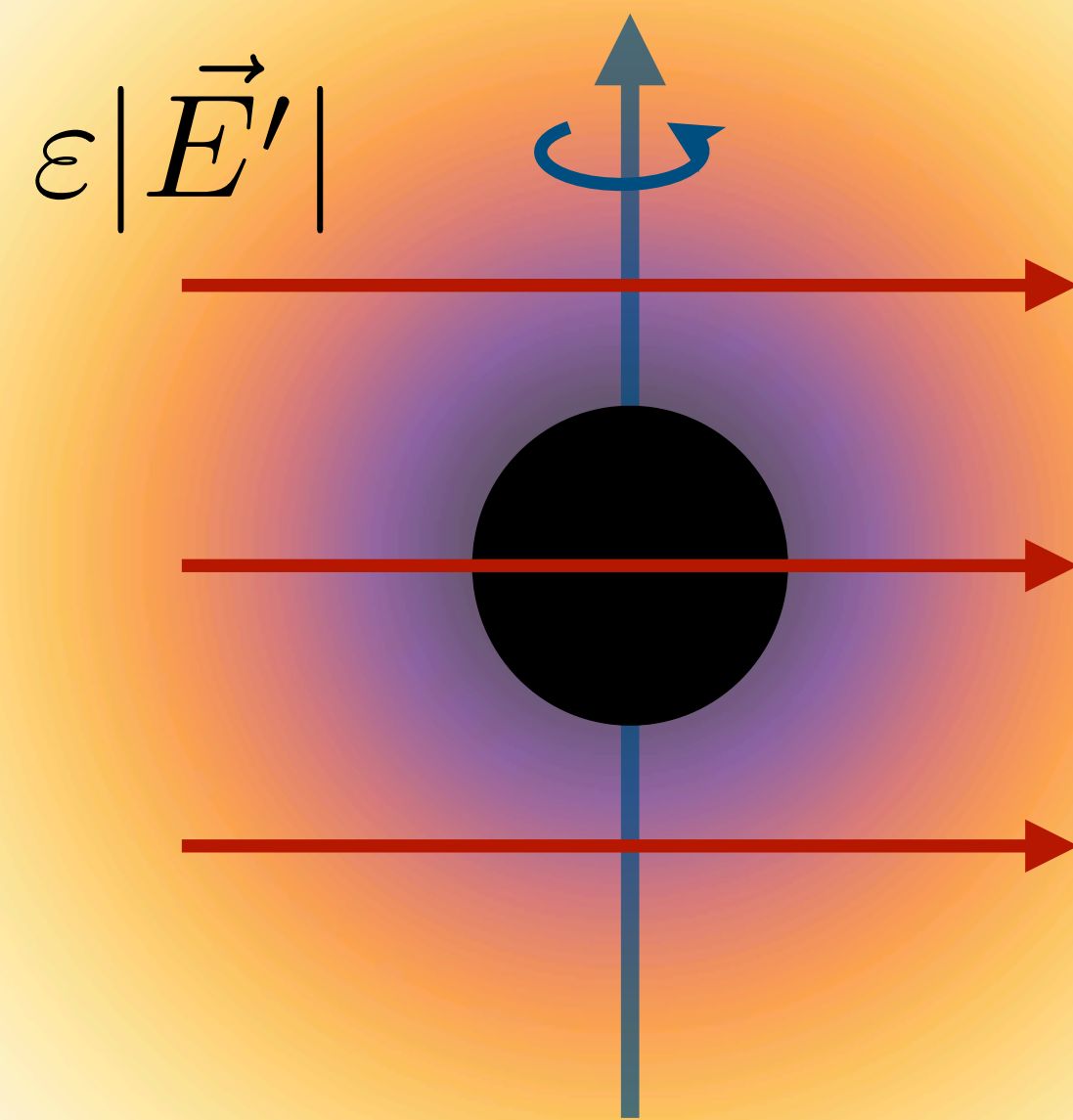
$$\mathcal{L} \supset -\frac{1}{4}F'_{\mu\nu}F'^{\mu\nu} - \frac{1}{2}\mu^2 A'^{\mu}A'_{\mu} + \boxed{J_{\text{EM}}^{\mu}(A_{\mu} + \varepsilon A'_{\mu})}$$

Coupling to SM charged particles $\propto e\varepsilon$

Dark photon kinetic mixing

$$\mathcal{L} \supset -\frac{1}{4}F'_{\mu\nu}F'^{\mu\nu} - \frac{1}{2}\mu^2 A'^{\mu}A'_{\mu} + J_{\text{EM}}^{\mu}(A_{\mu} + \varepsilon A'_{\mu})$$

Coupling to SM charged particles: $e\varepsilon$



Large, rotating electric field

$$|\vec{E}| = \varepsilon|\vec{E}'| \sim \varepsilon\alpha^{5/2}\mu M_{\text{pl}}$$

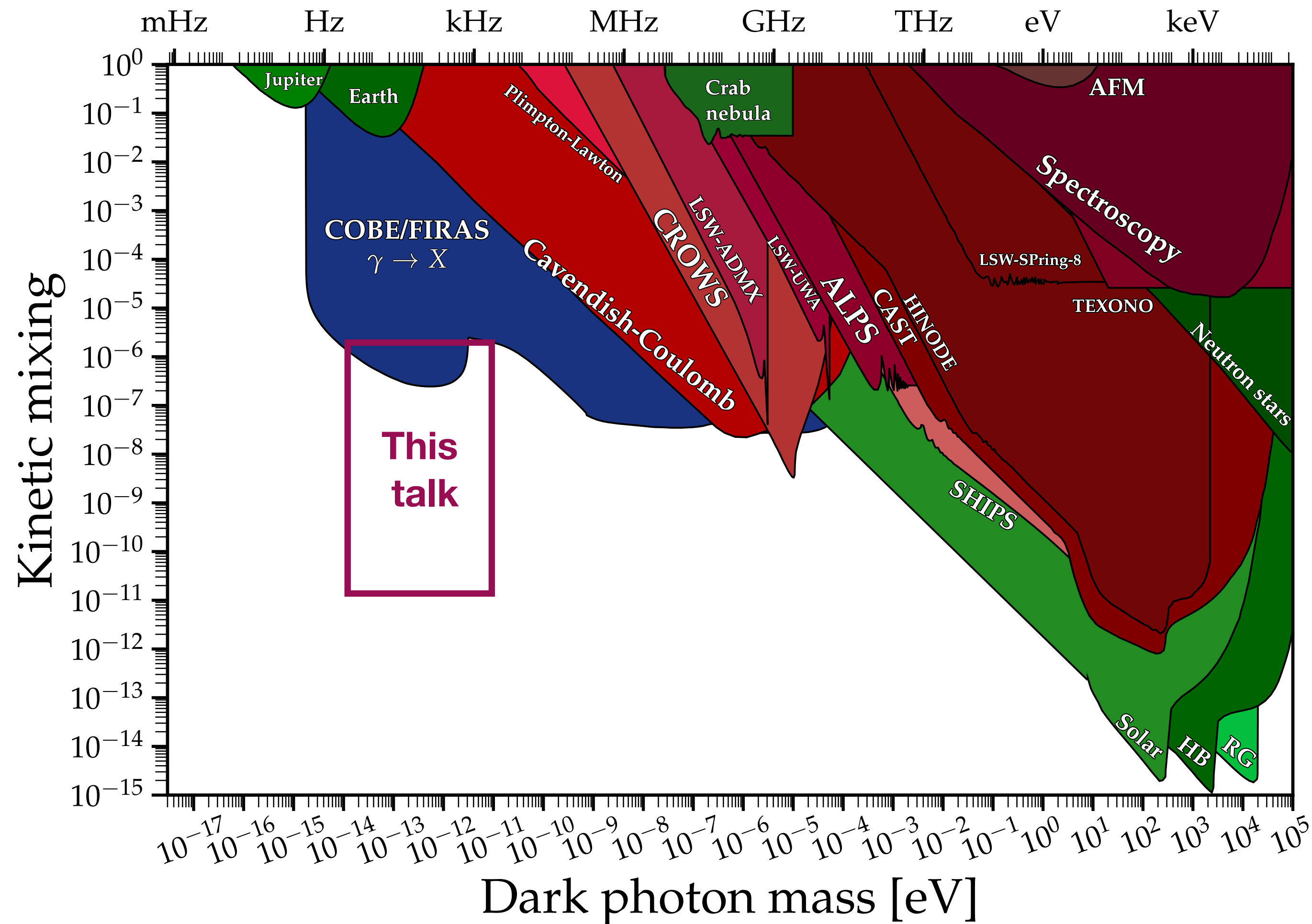
$$|\vec{E}| \sim 10^{13} \text{ V/m} \left(\frac{\varepsilon}{10^{-7}}\right) \left(\frac{\alpha}{0.1}\right)^{5/2} \left(\frac{\mu}{10^{-12} \text{ eV}}\right)$$

Dark photon parameter space

$$\mathcal{L} \supset -\frac{1}{4}F'_{\mu\nu}F'^{\mu\nu} - \frac{1}{2}\mu^2 A'^\mu A'_\mu + J_{\text{EM}}^\mu (A_\mu + \varepsilon A'_\mu)$$

Coupling to SM charged particles: $e\varepsilon$

Dark photons
that are NOT
the dark matter.



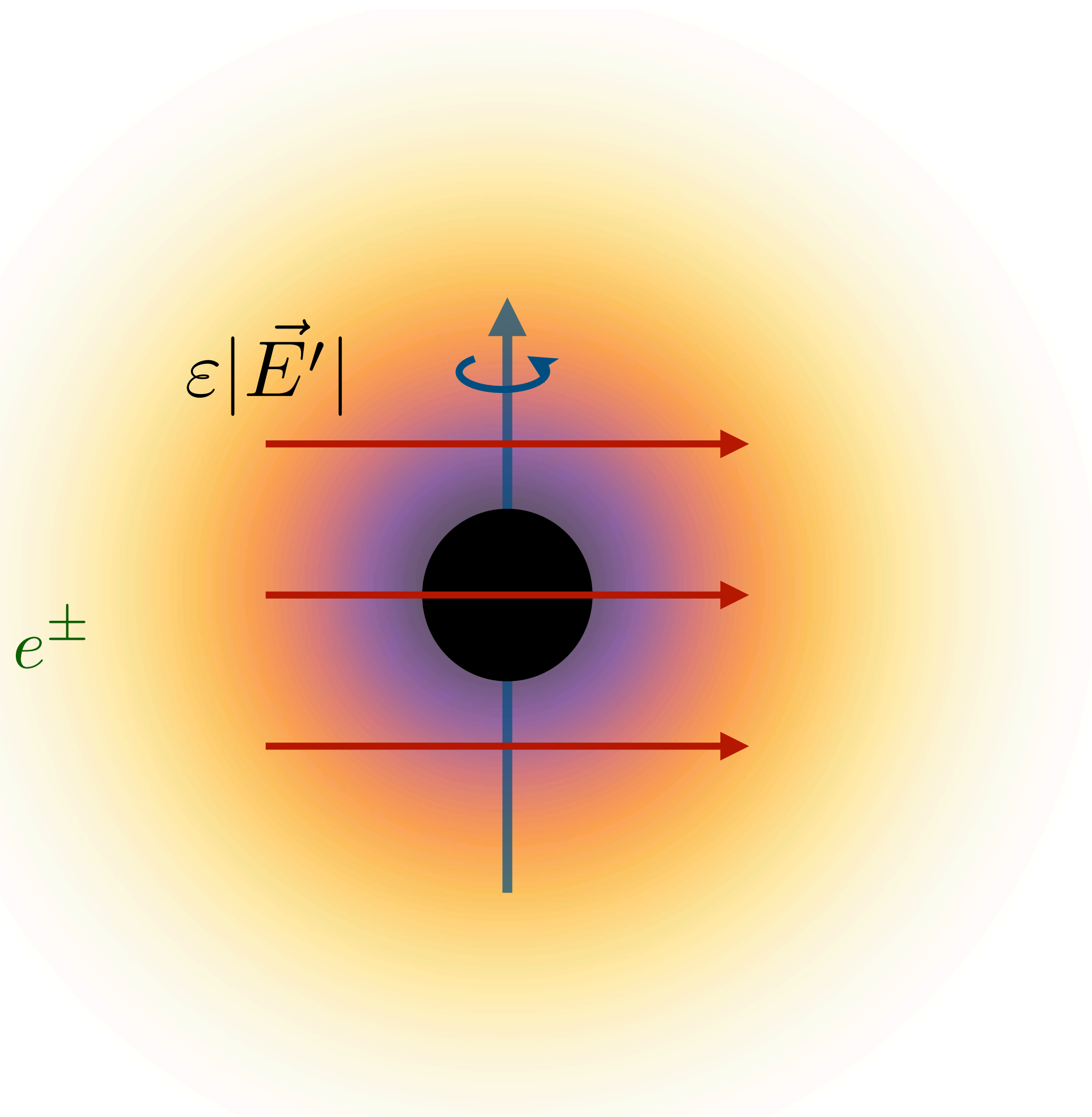
From 2105.04565, *Dark photon limits: a handbook*
A. Caputo, A. J. Millar, C. A. J. O'Hare, E. Vitagliano

Outline

- Dark photon superradiance (with kinetic mixing)
- **Plasma production**
- Electrodynamics
- Electromagnetic emissions and signatures

Plasma production

- Electron/positron highly accelerated in the electric field $\gamma_e \sim 10^{12}$
- Trajectory bends as the electric field rotates



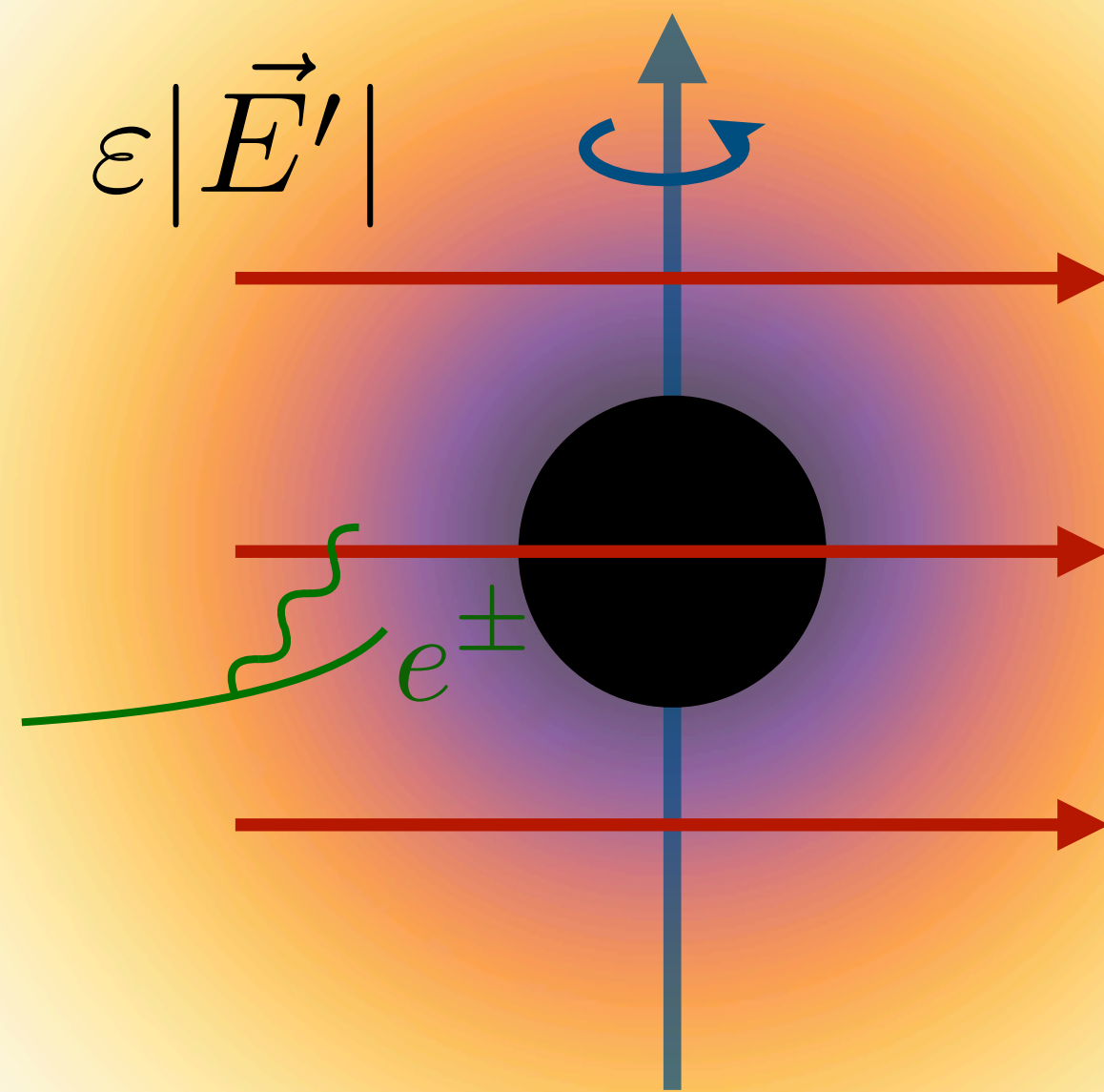
Plasma production

- Electron/positron highly accelerated in the electric field $\gamma_e \sim 10^{12}$
- Trajectory bends as the electric field rotates



Synchrotron emission of high energy photons

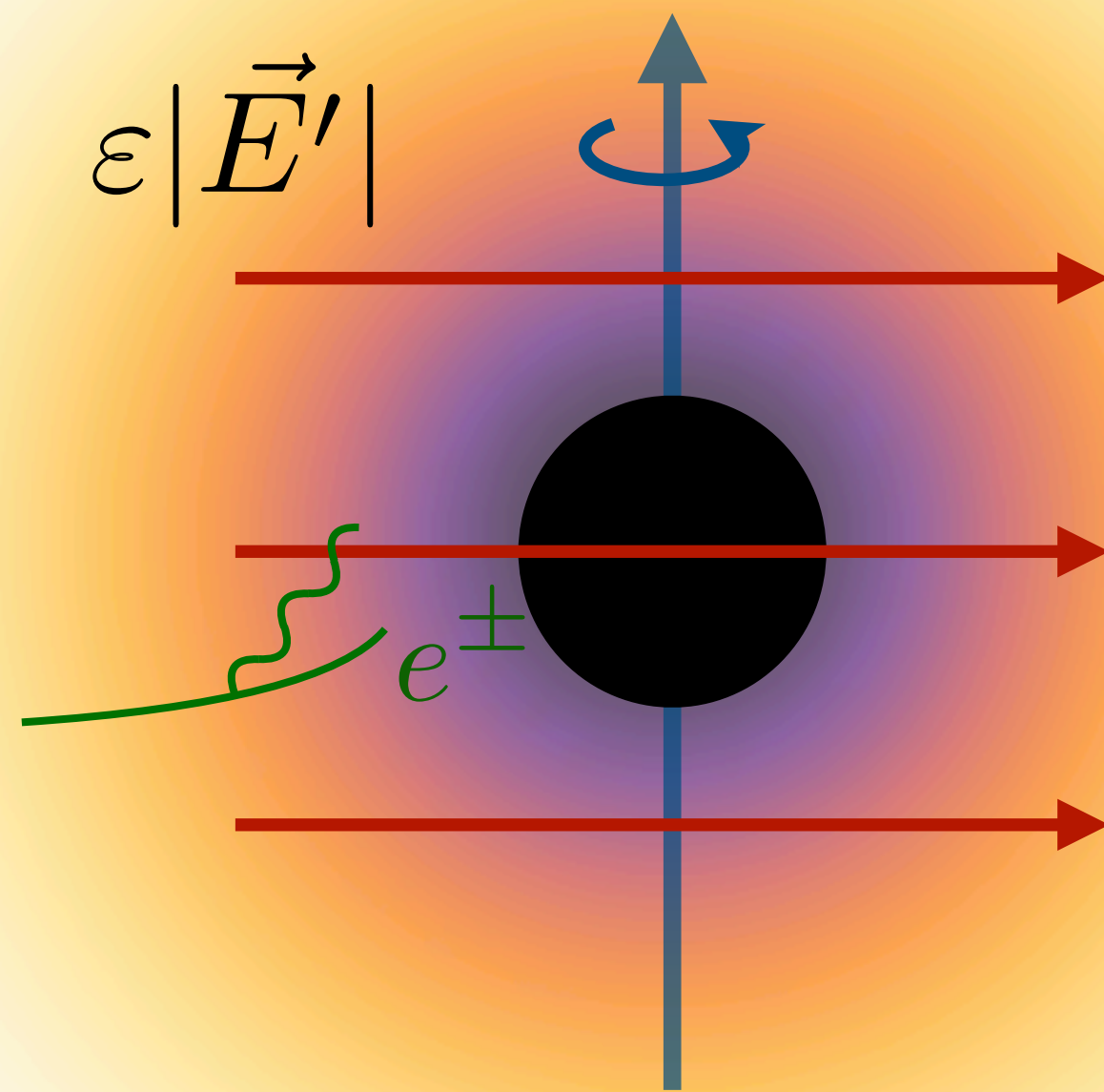
$$\omega_{\text{syn}} \simeq \gamma_e^3 \mu \gg m_e$$



Plasma production

Synchrotron emission of high energy photons

$$\omega_{\text{syn}} \simeq \gamma_e^3 \mu \gg m_e$$



Schwinger pair production:

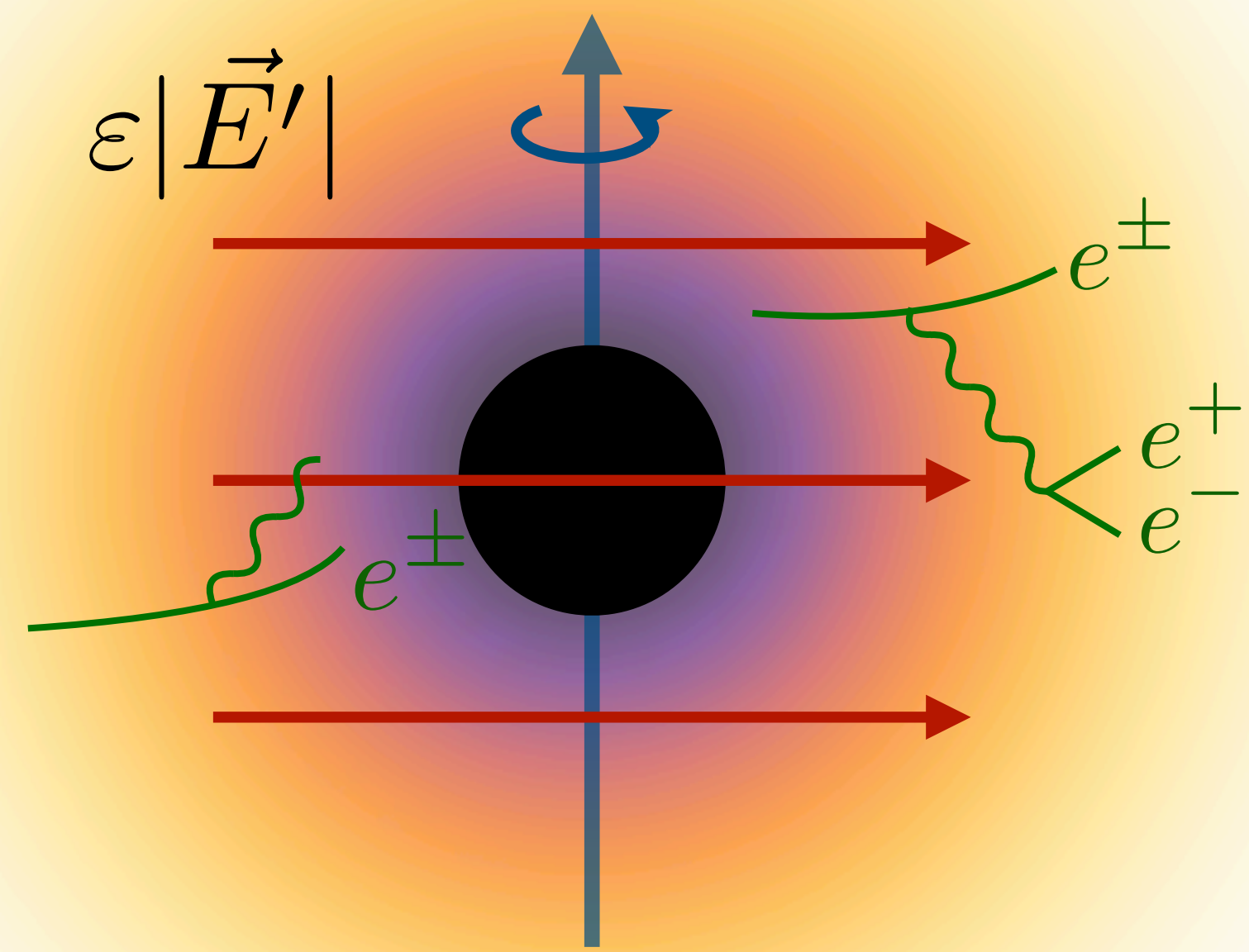
$$\Gamma_{e^\pm} \propto \exp\left(-\frac{\pi m_e^2}{e|\vec{E}|}\right)$$

$$|\vec{E}| \gtrsim 10^{18} \text{ V/m}$$

Plasma production

Synchrotron emission of high energy photons

$$\omega_{\text{syn}} \simeq \gamma_e^3 \mu \gg m_e$$



Schwinger pair production:

$$\Gamma_{e^\pm} \propto \exp\left(-\frac{\pi m_e^2}{e|\vec{E}|}\right)$$

$$|\vec{E}| \gtrsim 10^{18} \text{ V/m}$$

Photon-assisted Schwinger pair production:

$$\Gamma_{e^\pm} \propto \exp\left(-\frac{2m_e^2}{e|\vec{E}|} \frac{2m_e}{\omega_{\text{syn}}}\right)$$

Plasma production

Photon-assisted Schwinger pair production: $\Gamma_{e^\pm} = \frac{\alpha_{\text{EM}}}{2\pi} \frac{e\varepsilon |\vec{E}'|}{m_e} \exp\left(-\frac{4m_e^6 \mu^2}{(e\varepsilon |\vec{E}'|)^4}\right)$

Size of the superradiance cloud: $r_{\text{cloud}} = \frac{1}{\alpha\mu}$

Plasma production

Photon-assisted Schwinger pair production:

$$\Gamma_{e^\pm} = \frac{\alpha_{\text{EM}}}{2\pi} \frac{e\varepsilon |\vec{E}'|}{m_e} \exp\left(-\frac{4m_e^6 \mu^2}{(e\varepsilon |\vec{E}'|)^4}\right)$$

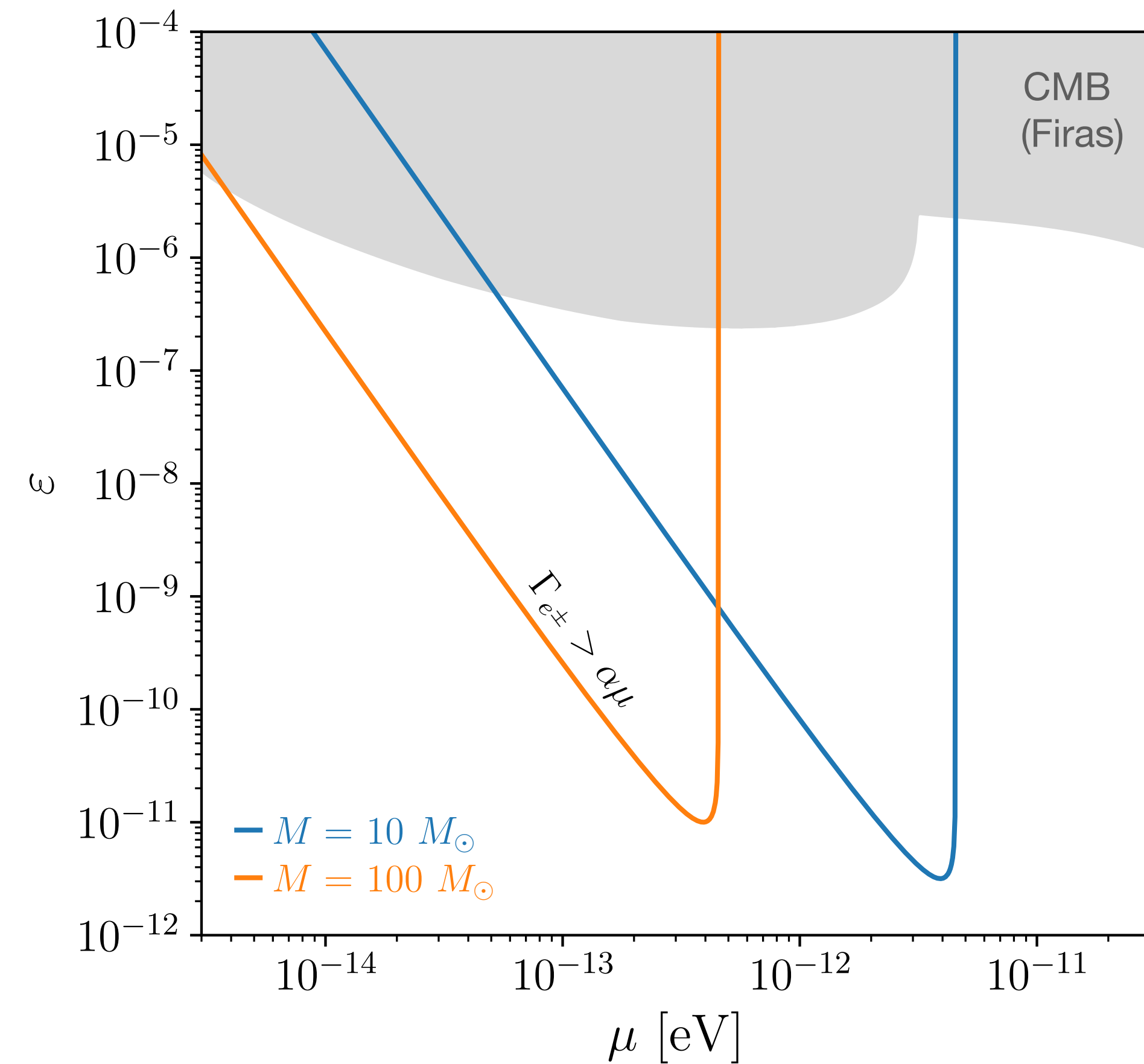
Size of the superradiance cloud:

$$r_{\text{cloud}} = \frac{1}{\alpha\mu}$$

Efficient pair production if

$$\Gamma_{e^\pm} \gg \alpha\mu$$

$$(\alpha \equiv \mu GM)$$



Plasma production

Photon-assisted Schwinger pair production:

$$\Gamma_{e^\pm} = \frac{\alpha_{\text{EM}}}{2\pi} \frac{e\varepsilon |\vec{E}'|}{m_e} \exp\left(-\frac{4m_e^6 \mu^2}{(e\varepsilon |\vec{E}'|)^4}\right)$$

Size of the superradiance cloud:

$$r_{\text{cloud}} = \frac{1}{\alpha\mu}$$

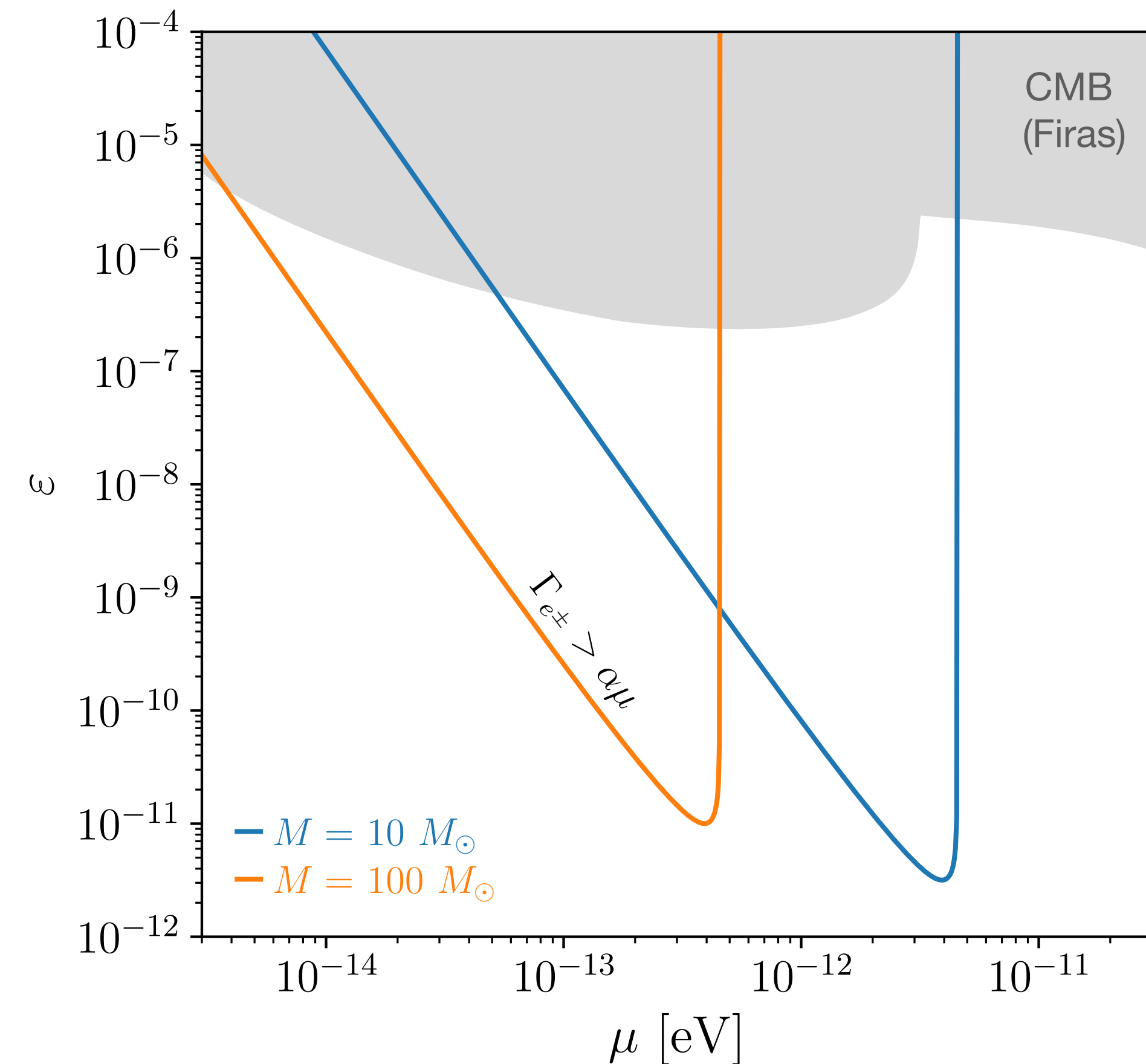
Efficient pair production if

$$\Gamma_{e^\pm} \gg \alpha\mu$$

$$(\alpha \equiv \mu GM)$$

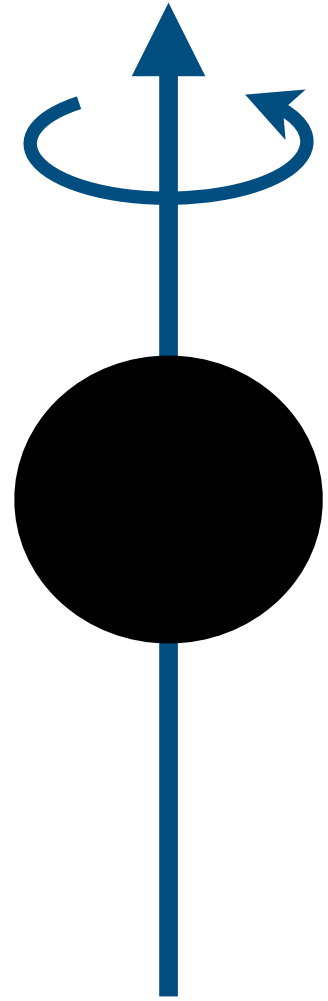
→ Cascade production of charged particles until the electric field is screened

$$en_e \simeq \varepsilon \nabla \cdot \vec{E}'$$



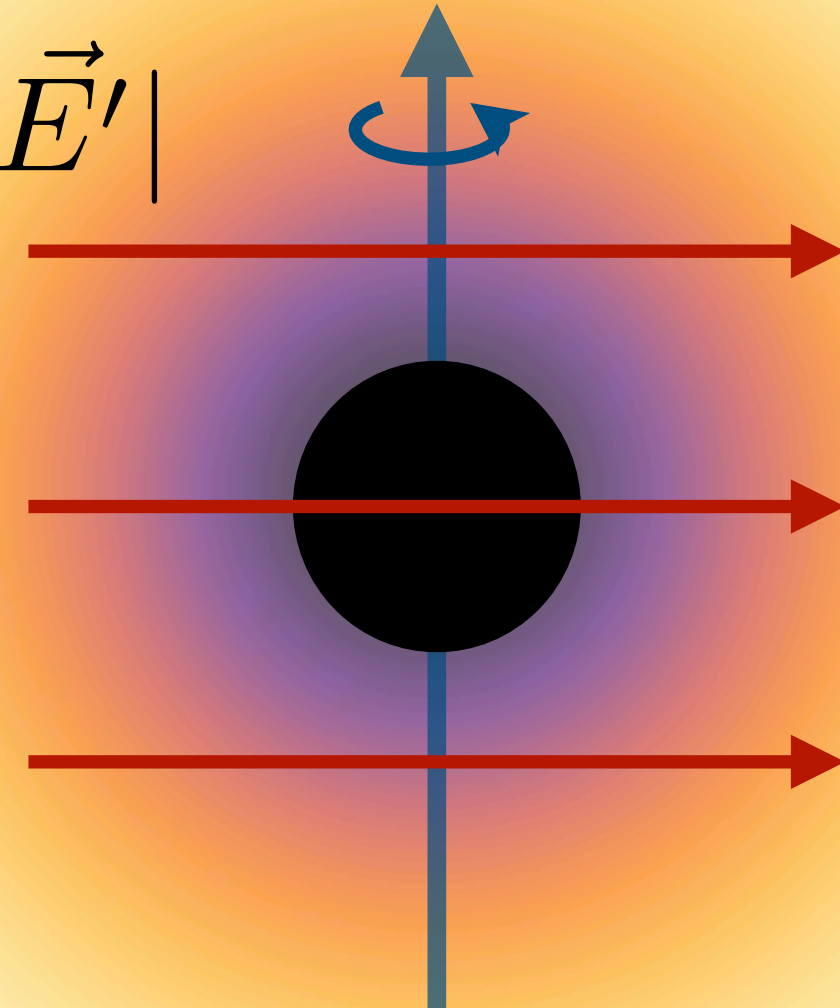
Important timescales

Exponential growth of
the dark photon cloud



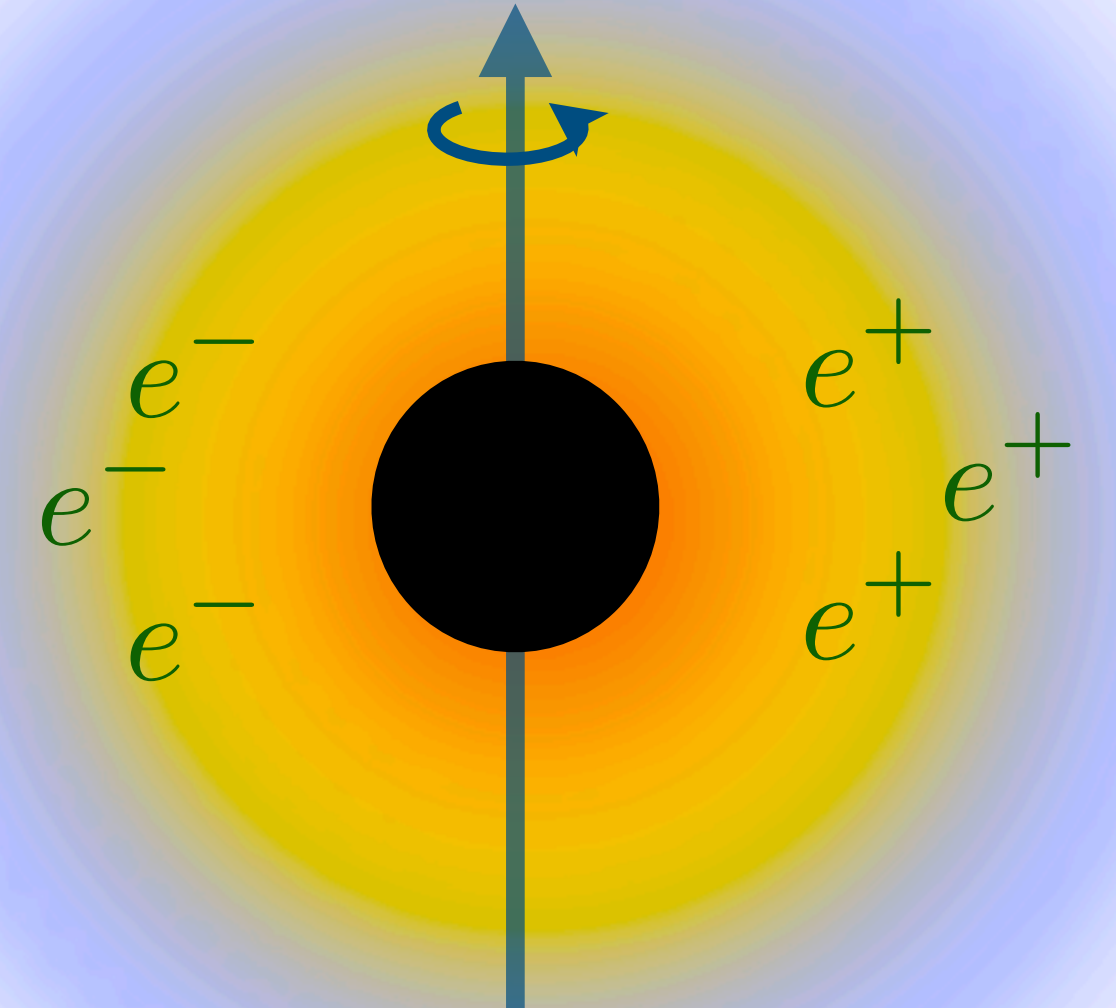
τ_{SR}

$\epsilon |\vec{E}'|$



Exponential growth of
the plasma

τ_{plasma}



$$\tau_{\text{SR}} \simeq \frac{1}{4a_* \alpha^6 \mu}$$

$$\tau_{\text{plasma}} \simeq \frac{1}{\Gamma_{e^\pm}}$$

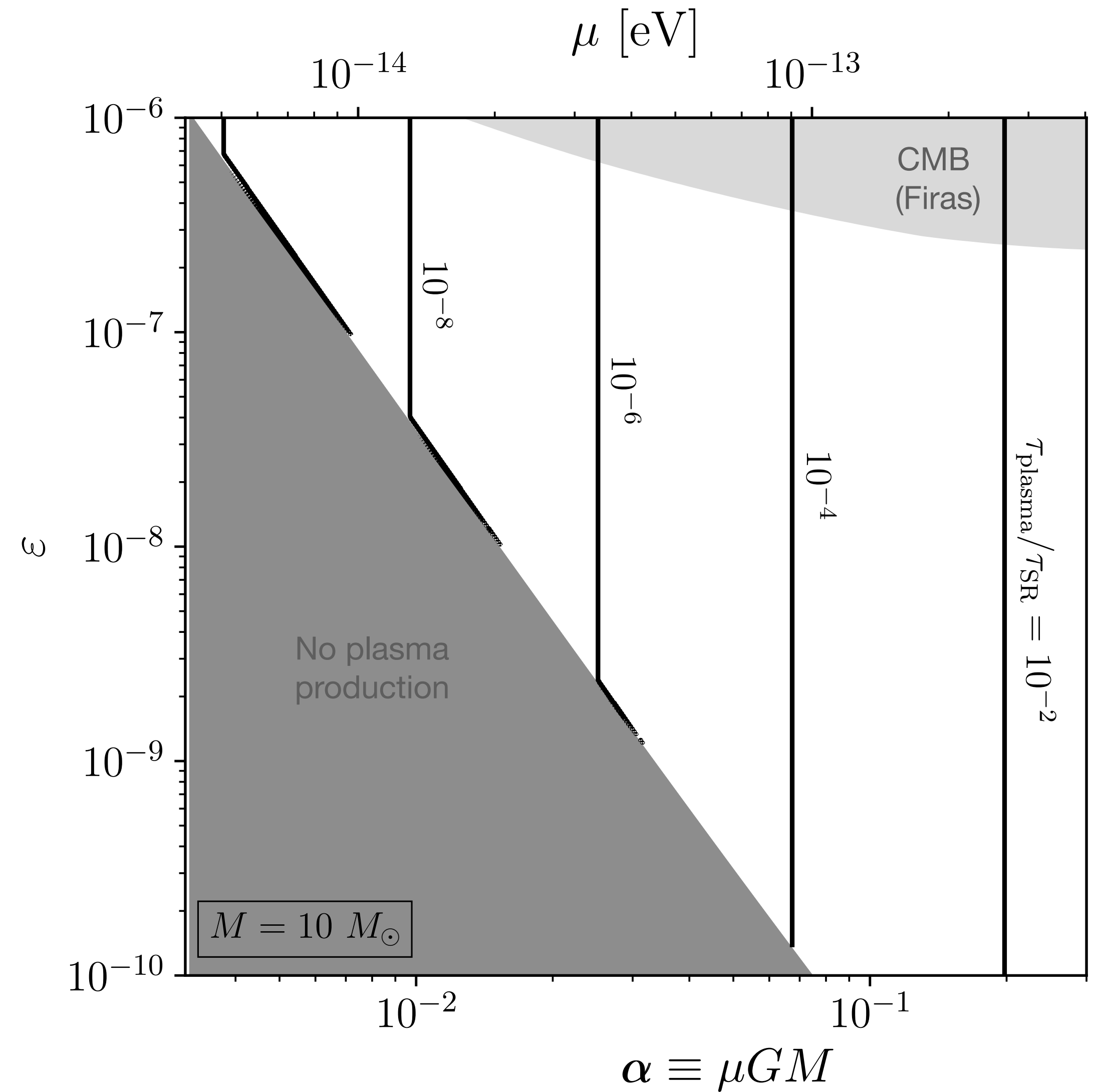
$$\tau_{\text{plasma}} \ll \tau_{\text{SR}}$$

Important timescales

$$\tau_{\text{SR}} \simeq \frac{1}{4a_* \alpha^6 \mu}$$

$$\tau_{\text{plasma}} \simeq \frac{1}{\Gamma_{e^\pm}}$$

$$\tau_{\text{plasma}} \ll \tau_{\text{SR}}$$



Outline

- Dark photon superradiance (with kinetic mixing)
- Plasma production
- **Electrodynamics**
- Electromagnetic emissions and signatures

Electrodynamics: modeling the plasma

Ohm's law $\vec{J} = \sigma(\vec{E} + \vec{v} \times \vec{B})$



Conductivity



We can solve numerically
Maxwell's equation for the E
and B fields

encodes microscopic particle physics of the plasma

- $\sigma \rightarrow \infty$: perfect conductivity, fields are perfectly screened and the plasma is “force-free”
- Finite σ : resistive plasma, fields are not perfectly screened, dissipative effects are important

Nils Siemonsen

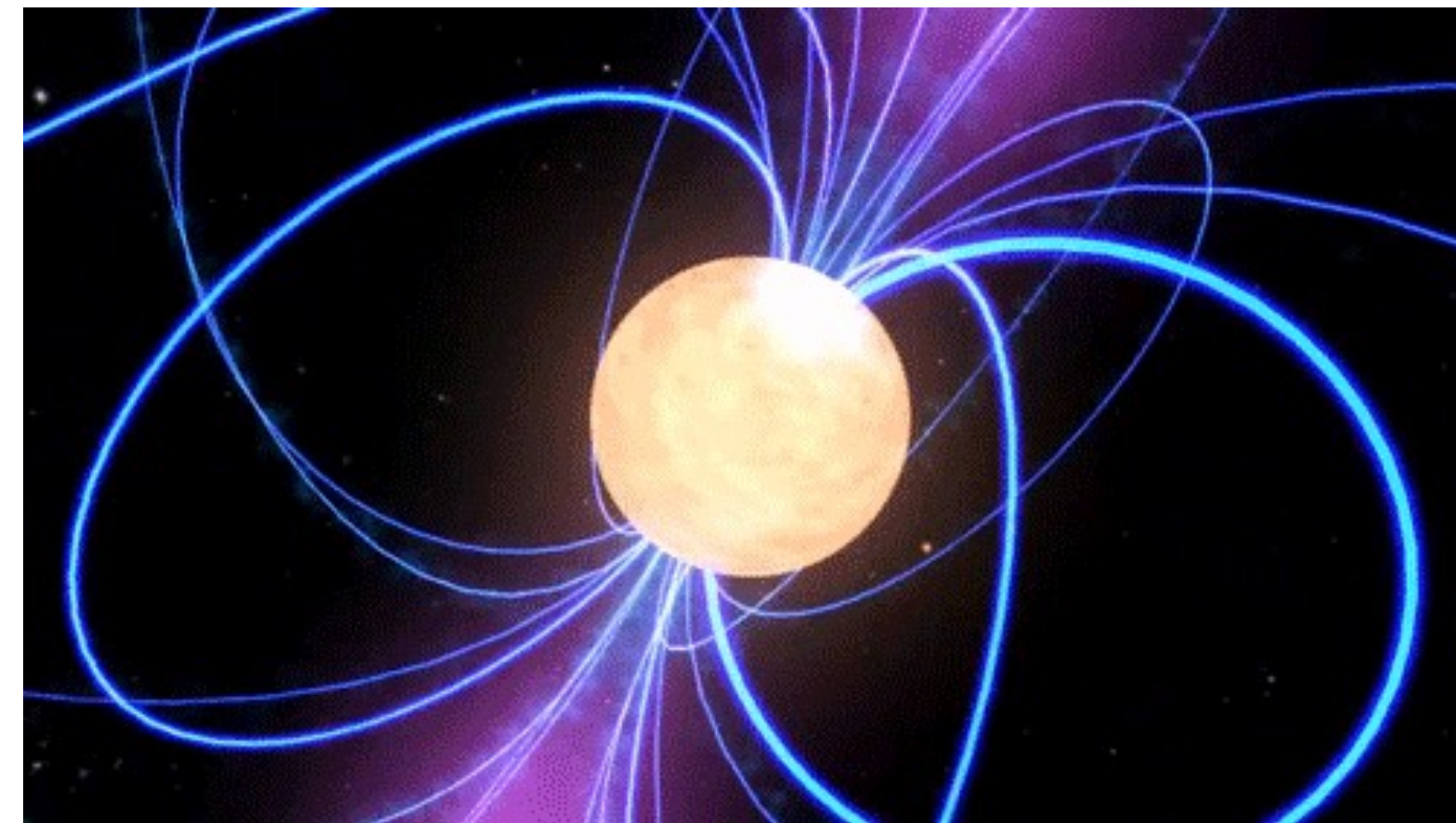


Electrodynamics: modeling the plasma

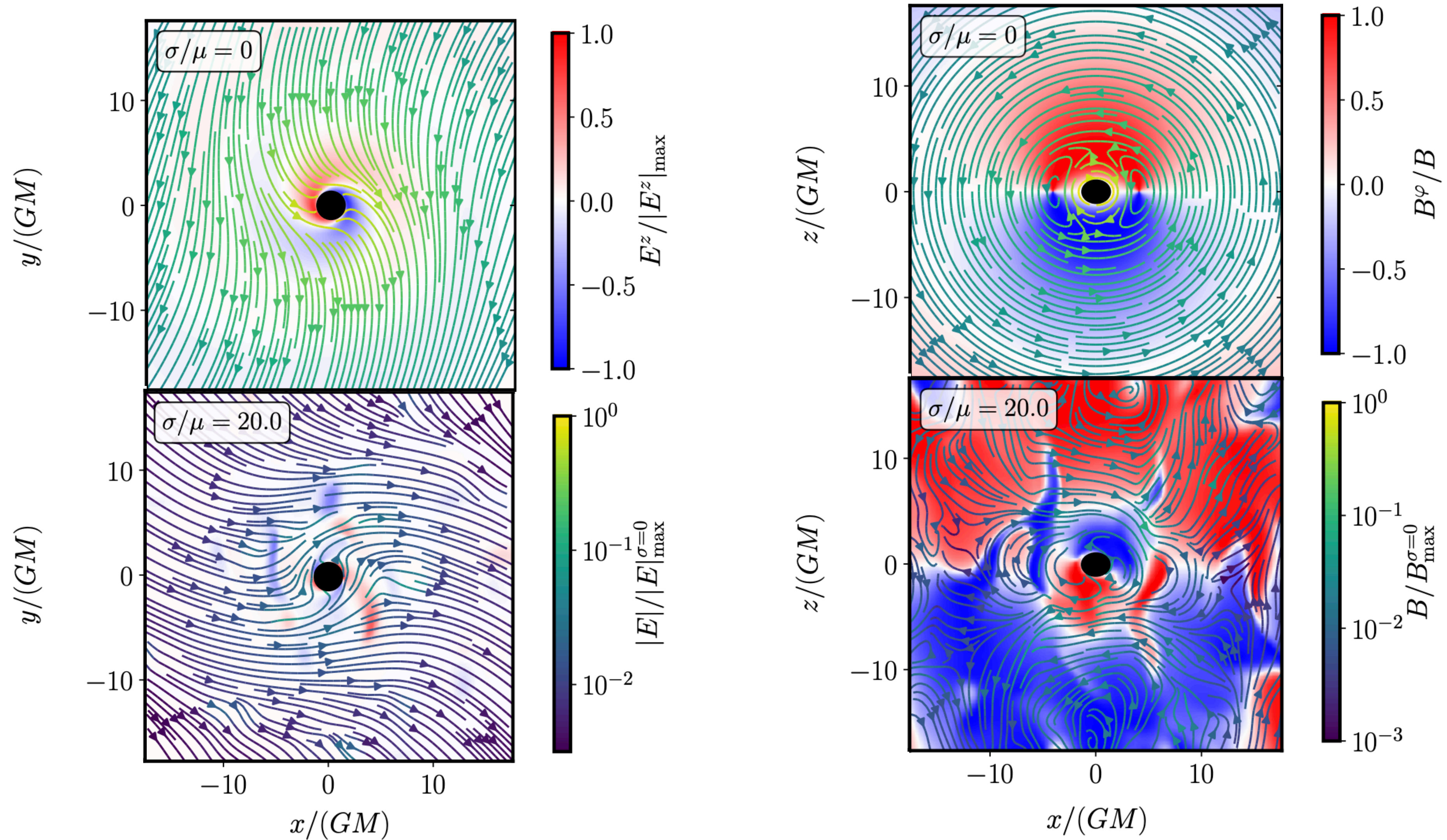
Ohm's law $\vec{J} = \sigma(\vec{E} + \vec{v} \times \vec{B})$

- $\sigma \rightarrow \infty$: perfect conductivity, fields are perfectly screened and the plasma is “force-free”

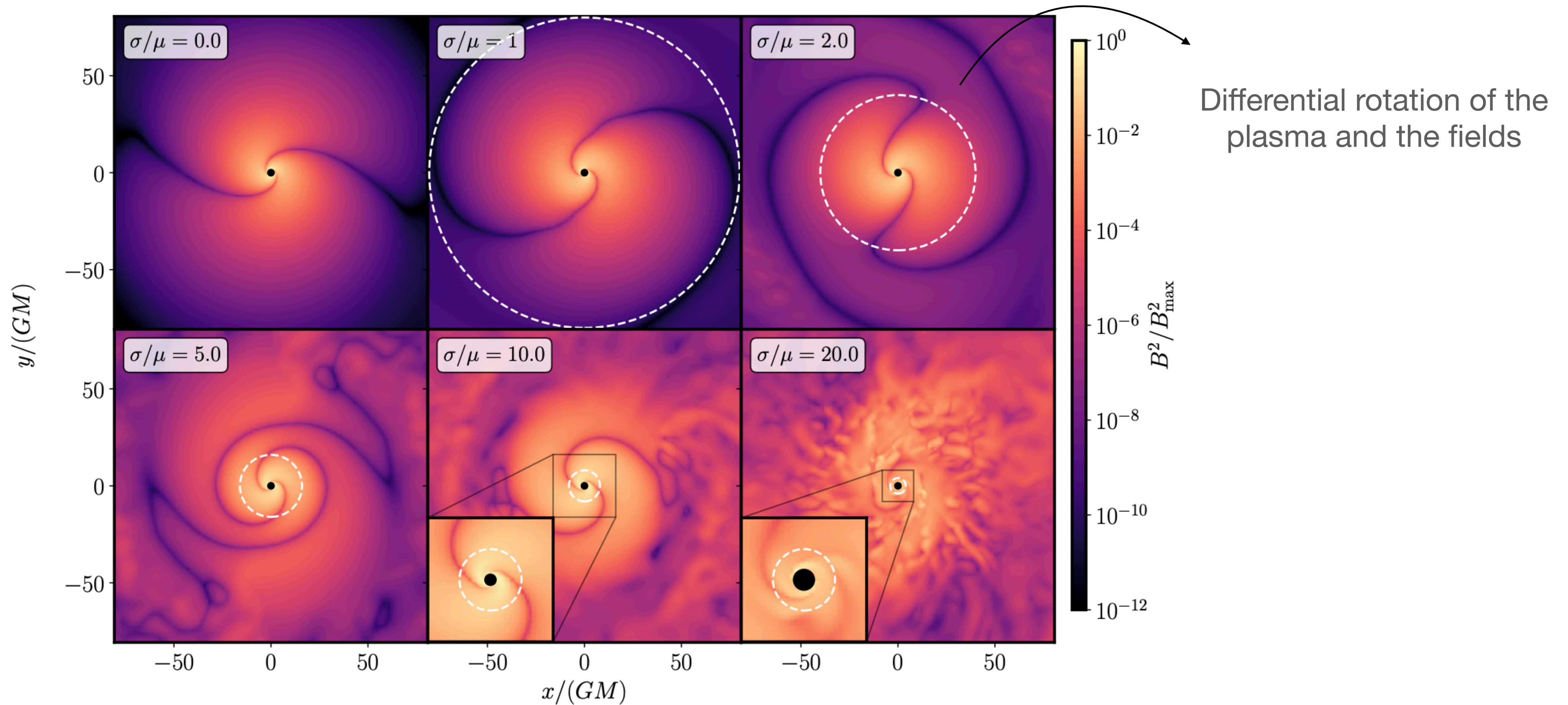
In a **neutron star pulsars** the magnetosphere is modeled as a force-free plasma



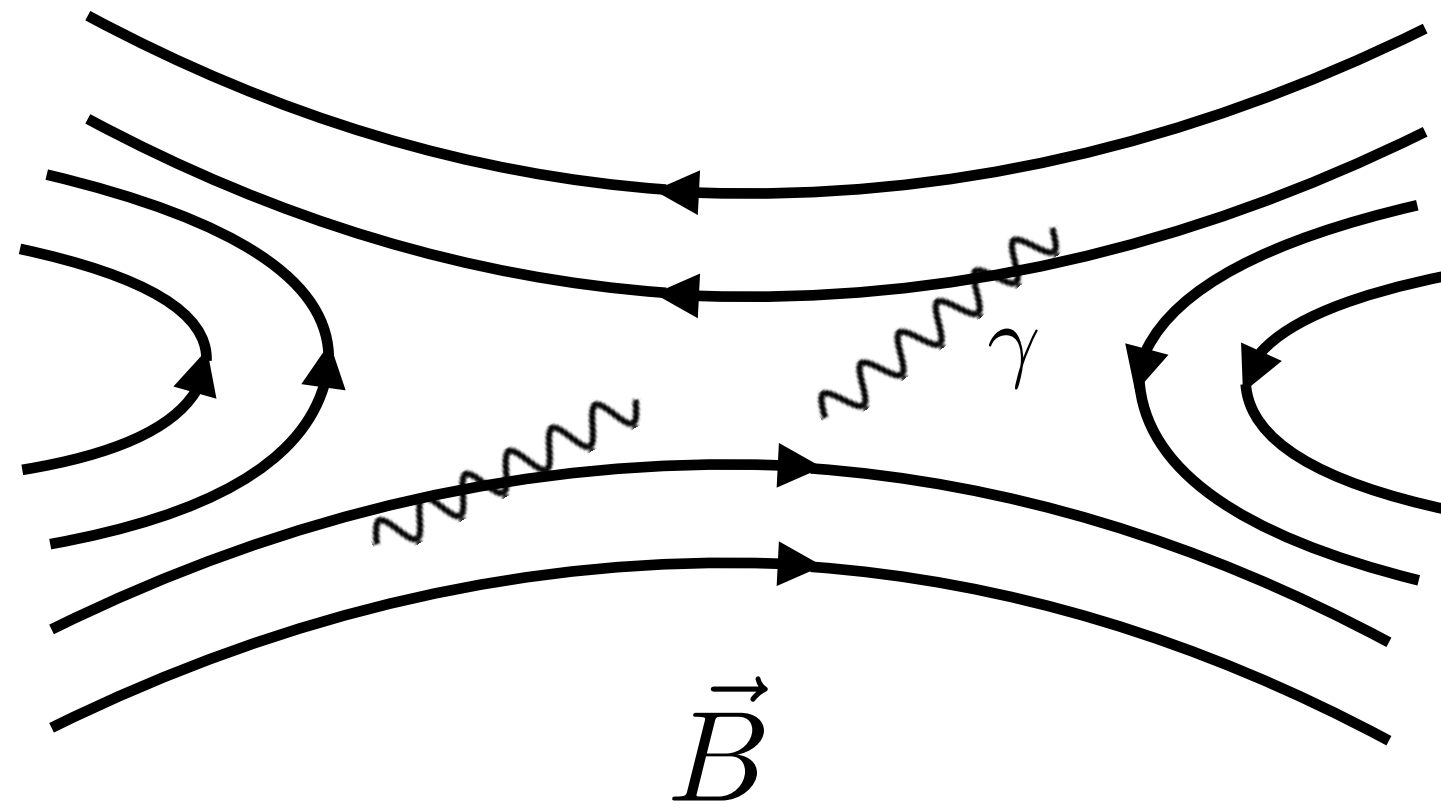
Electrodynamics: field solutions



Electrodynamics: field solutions

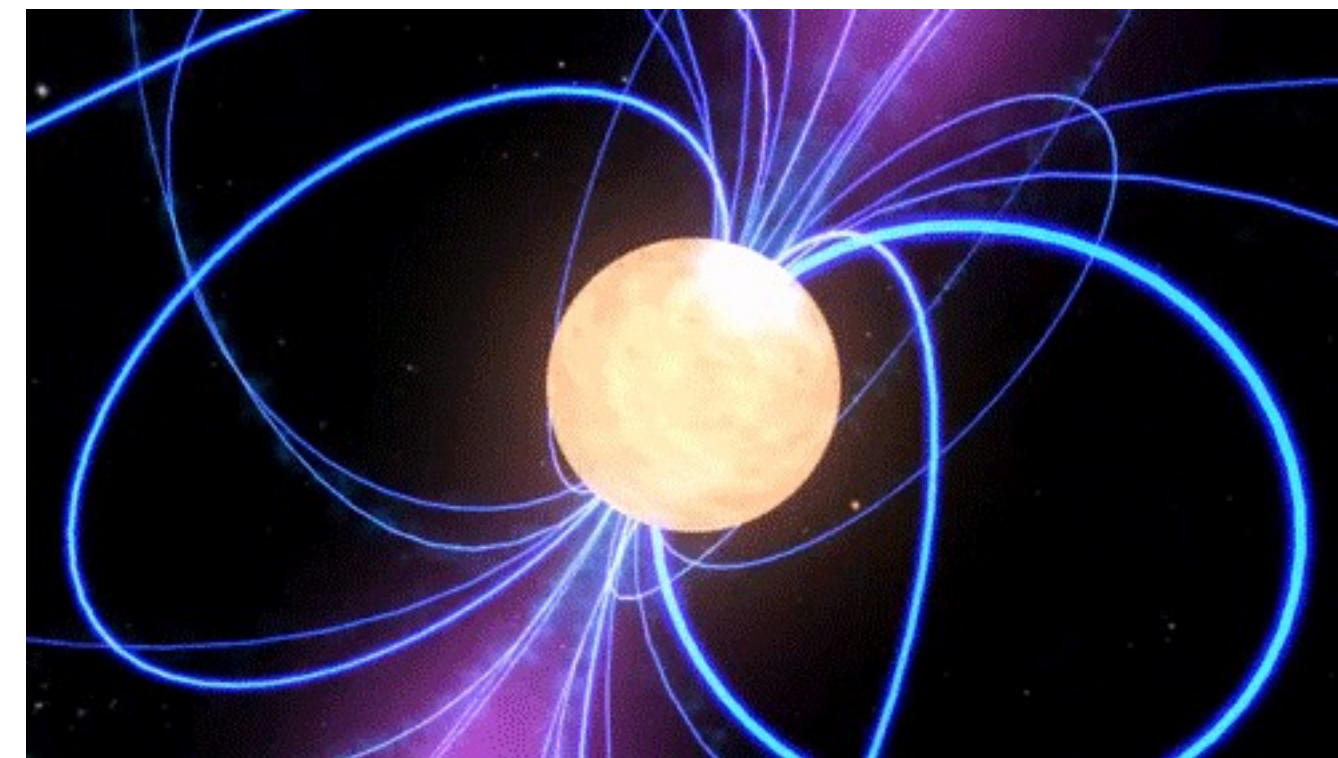


Magnetic reconnection

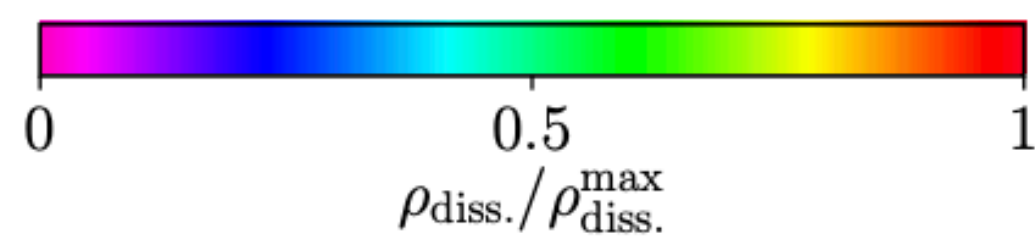
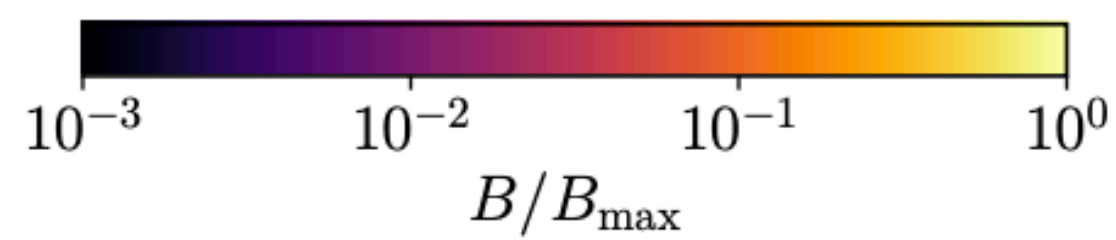
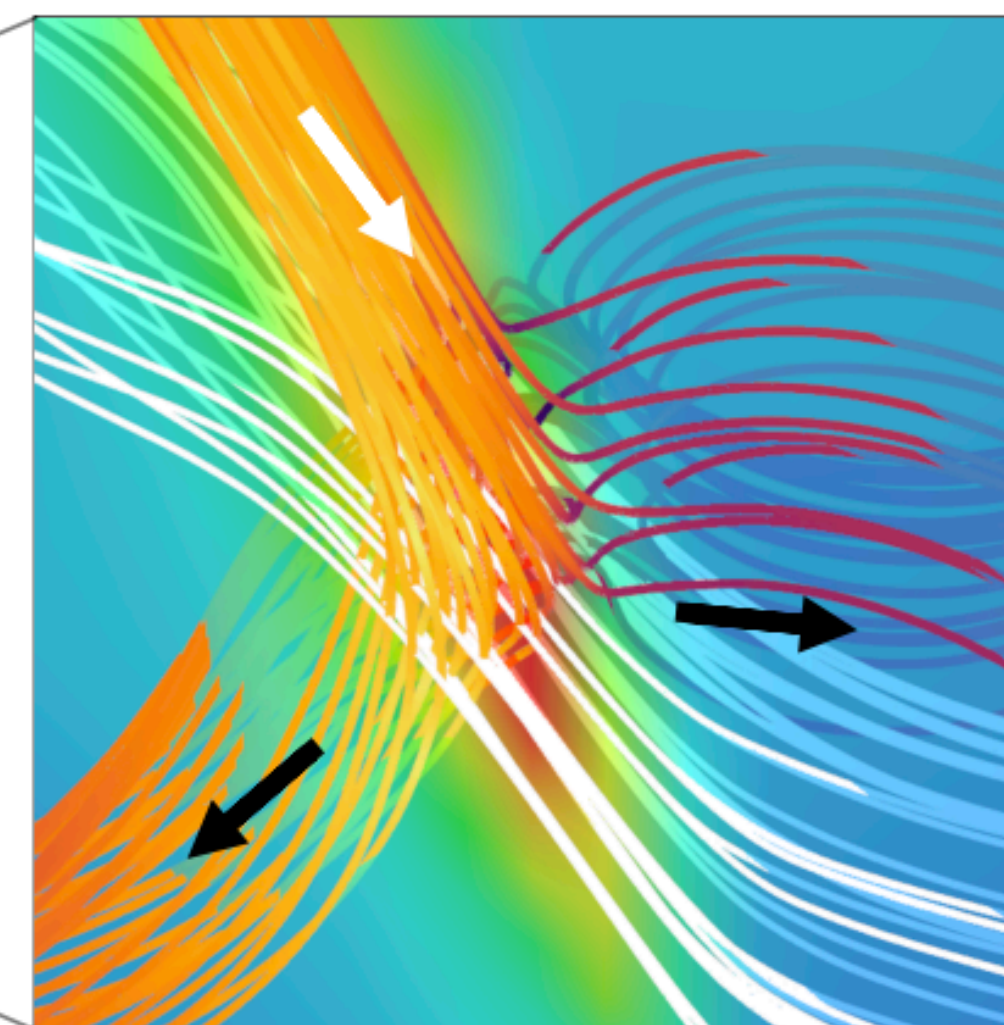
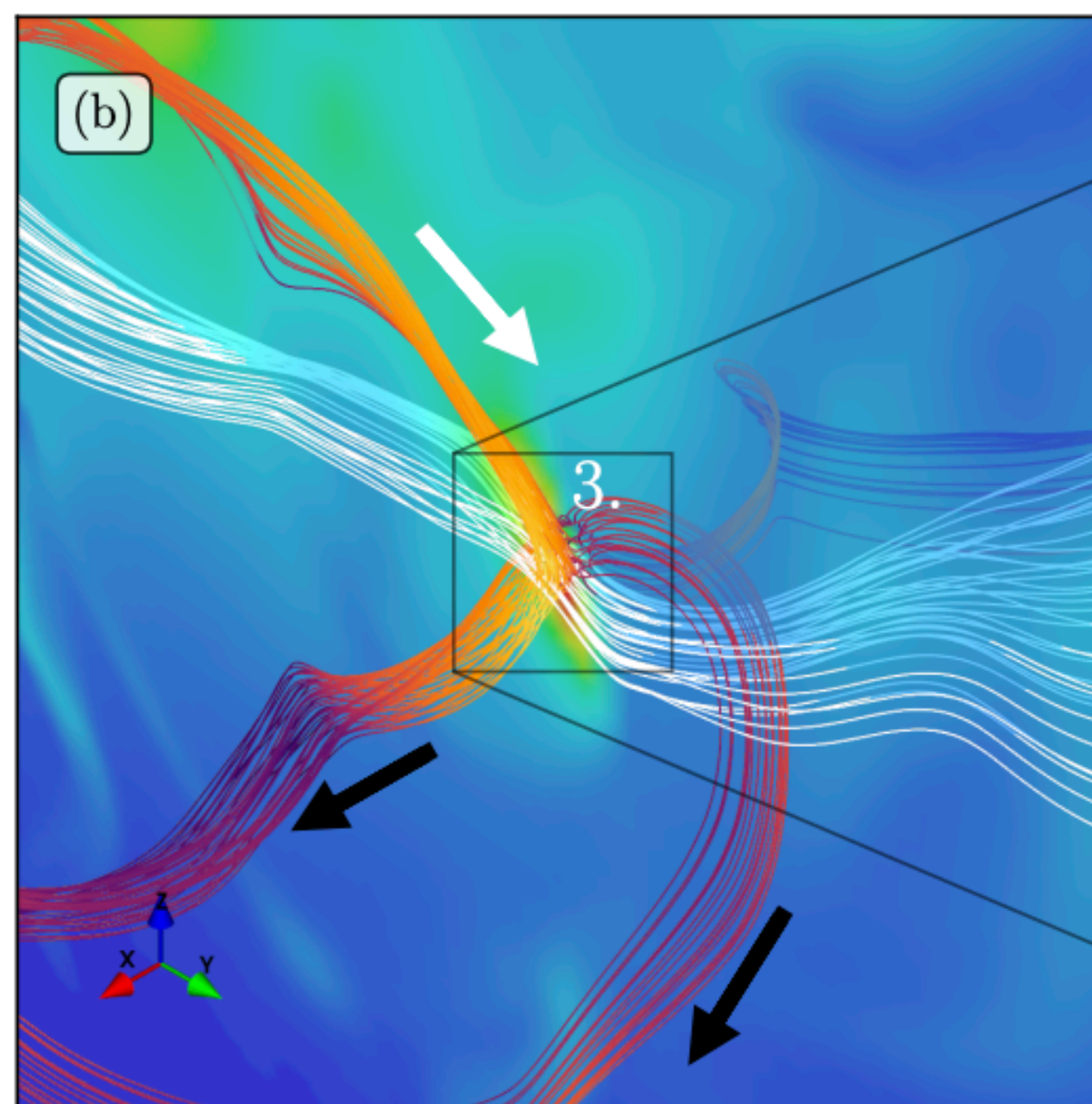
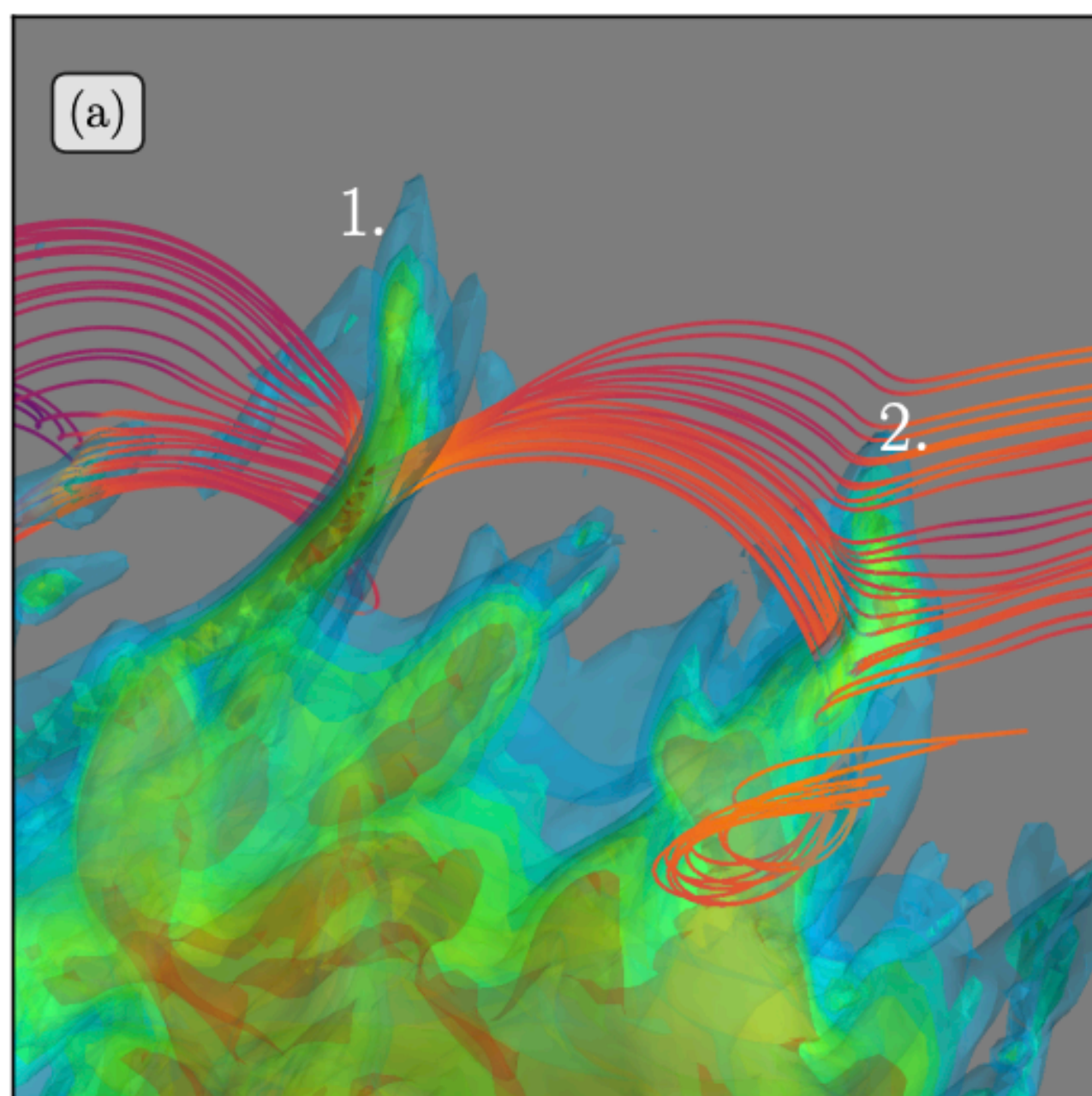
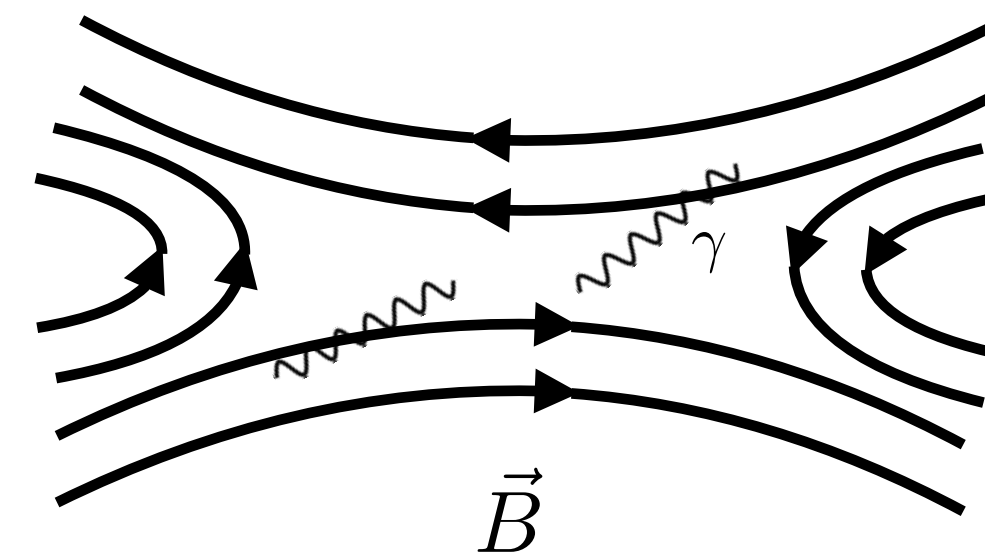


Field energy dissipated into particle acceleration and EM emissions

In a **neutron star pulsars** magnetic reconnection happens in the current sheets

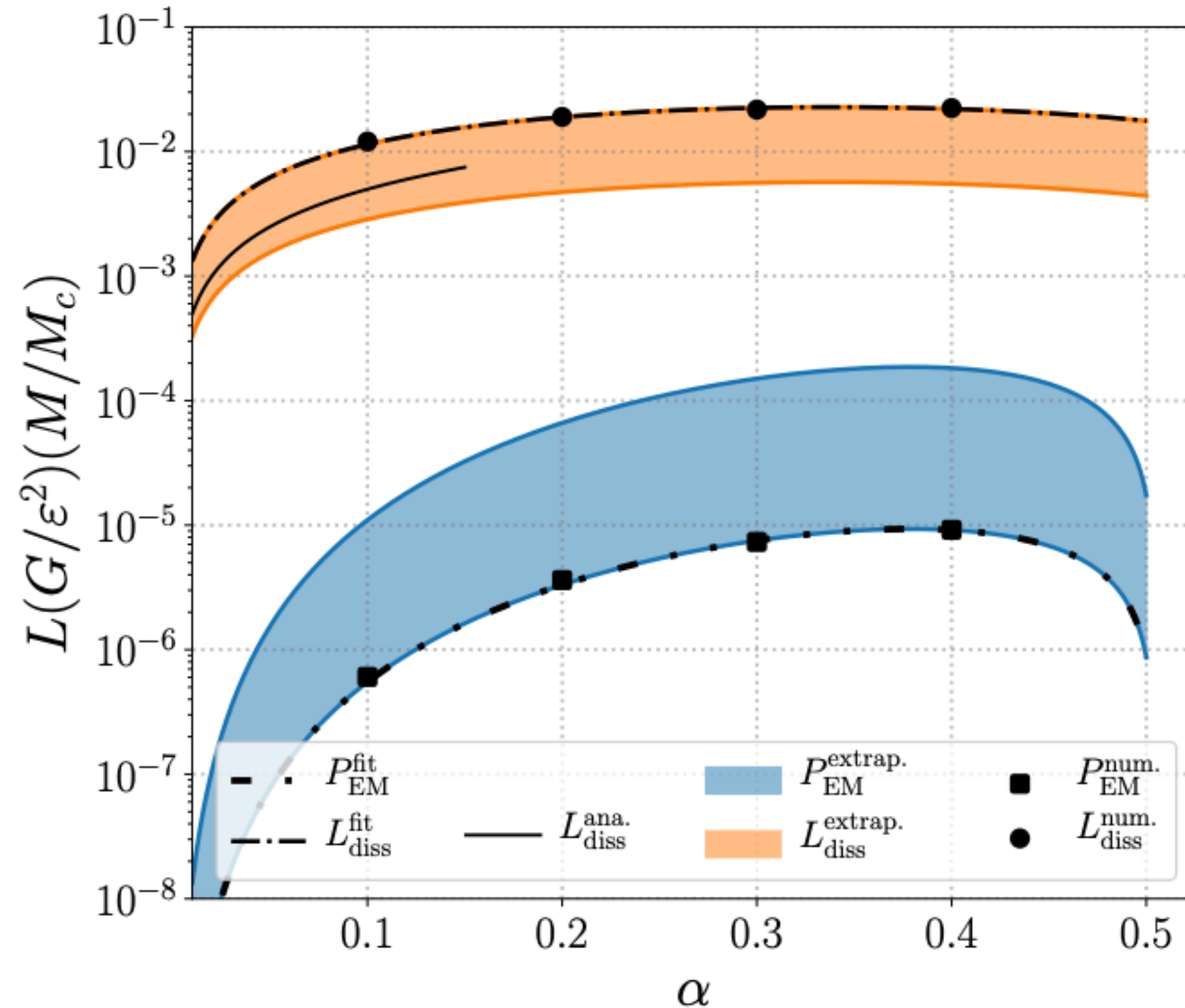


Magnetic reconnection



Electrodynamics: power output

Numerical solutions and fit



Power emitted:

- Poynting flux

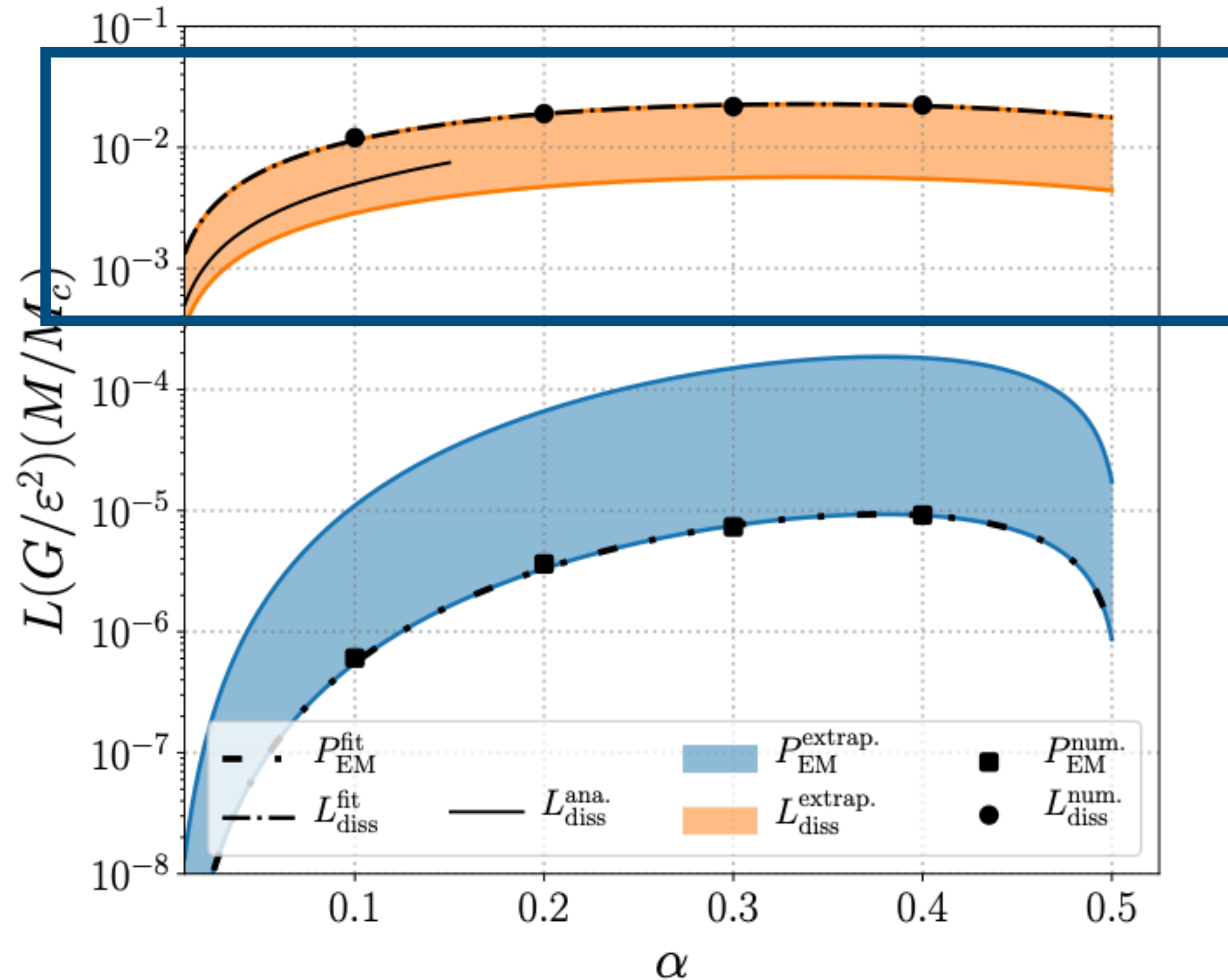
$$P_{\text{EM}} = \oint dS \vec{r} \cdot (\vec{E} \times \vec{B})$$

- Dissipative losses

$$L_{\text{diss}} = \int dV \vec{E} \cdot \vec{J}$$

Electrodynamics: power output

Numerical solutions and fit



Power emitted:

- Poynting flux

$$P_{EM} = \oint dS \vec{r} \cdot (\vec{E} \times \vec{B})$$

- Dissipative losses

$$L_{diss} = \int dV \rho_{diss}$$

$$L_{fit} = \epsilon^2 F(\alpha) \frac{M_c}{GM}$$

Outline

- Dark photon superradiance (with kinetic mixing)
- Plasma production
- Electrodynamics
- **Electromagnetic emissions and signatures**

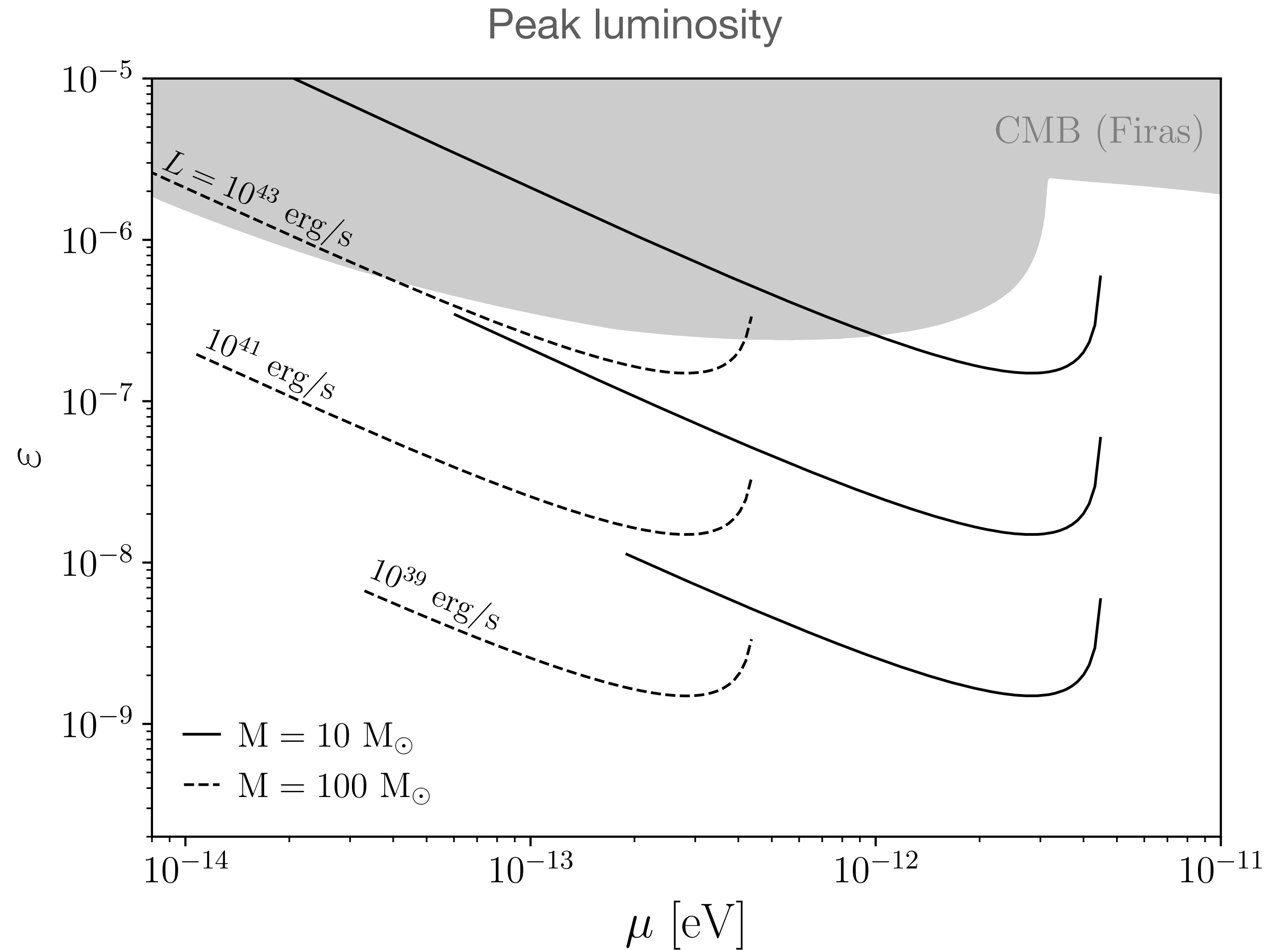
EM emissions

Luminosity of the dark photon
superradiance cloud

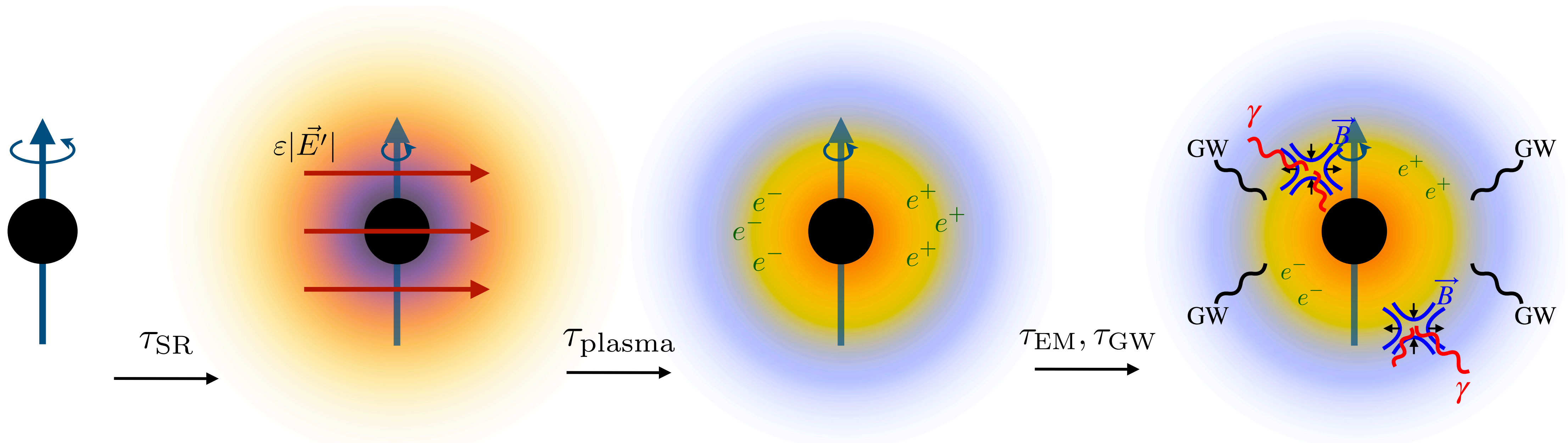
$$L_{\text{fit}} = \varepsilon^2 F(\alpha) \frac{M_c}{GM}$$

Crab pulsar $L_{\text{crab}} \simeq 10^{38}$ erg/s

Supernova $L_{\text{SN}} \simeq 10^{43} - 10^{45}$ erg/s



Evolution of the system

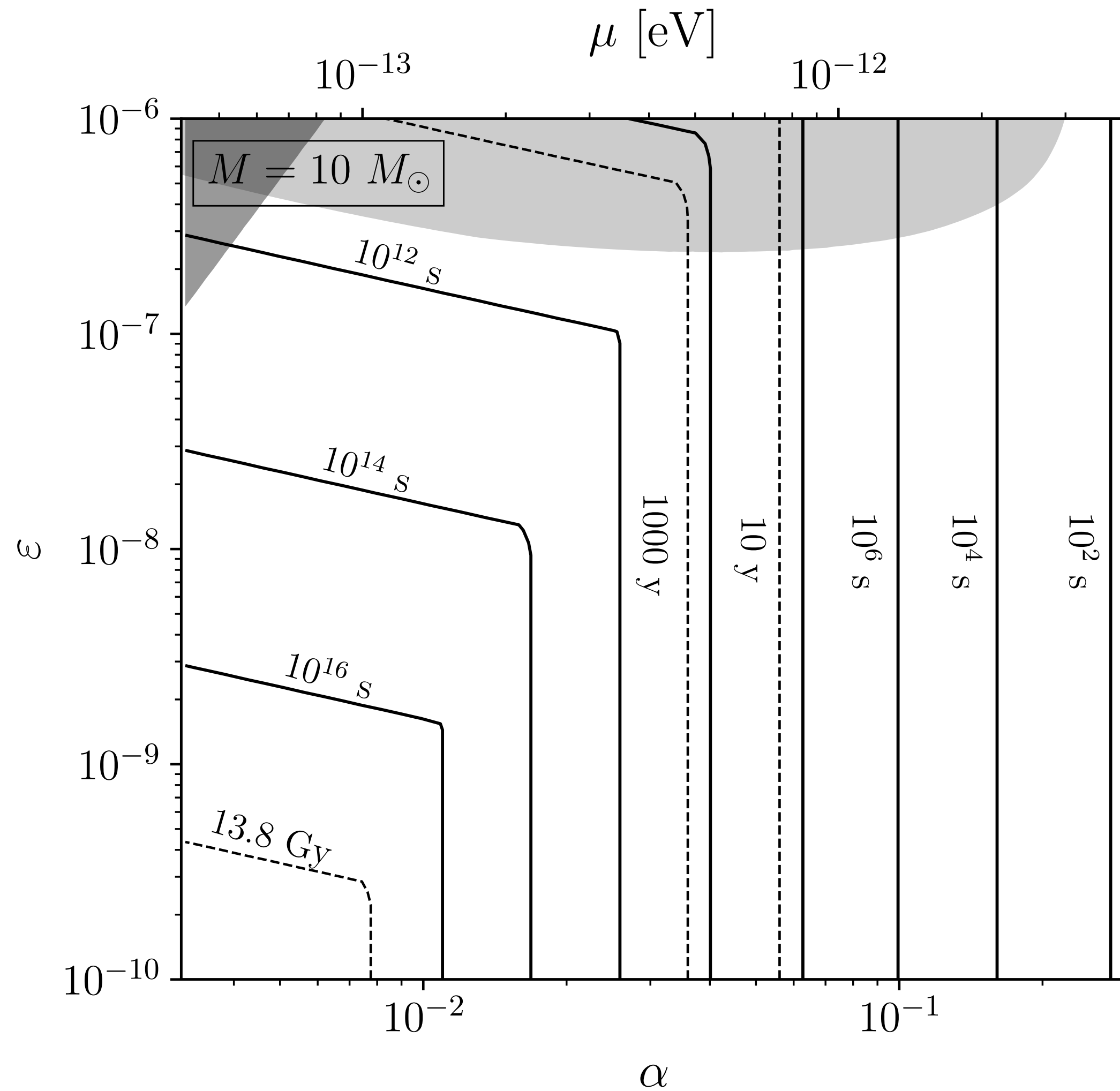


Decay of the superradiance cloud through gravitational wave and EM emissions.

Lifetime of the system

$$\tau_{\text{GW}} \approx \frac{GM}{17\alpha^{11} \Delta a_*}$$

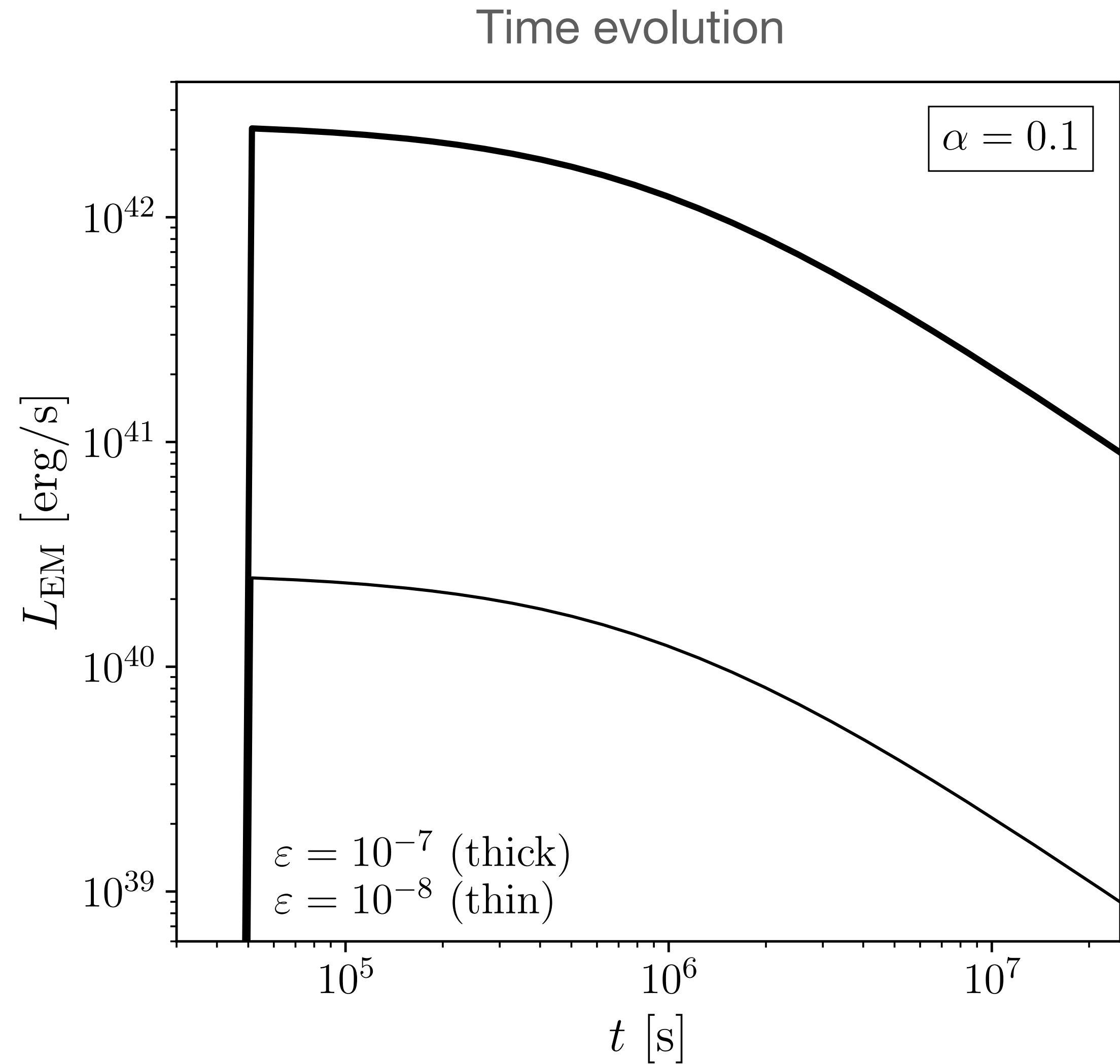
$$\tau_{\text{EM}} \approx \frac{GM \ln 2}{\varepsilon^2 F(\alpha)}$$



EM emissions

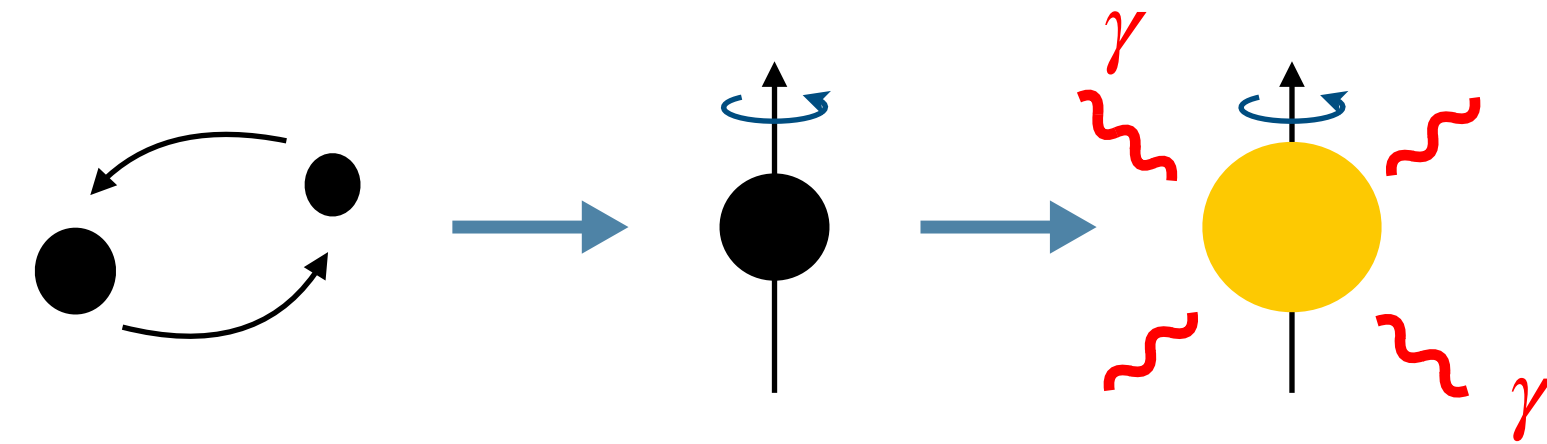
Luminosity of the dark photon
superradiance cloud

$$L_{\text{fit}} = \varepsilon^2 F(\alpha) \frac{M_c}{GM}$$

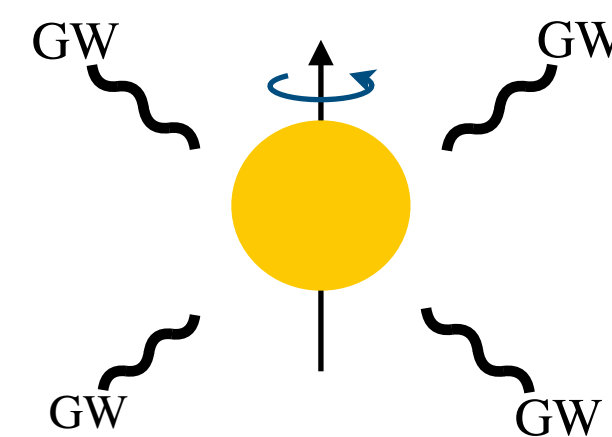


Observational strategies

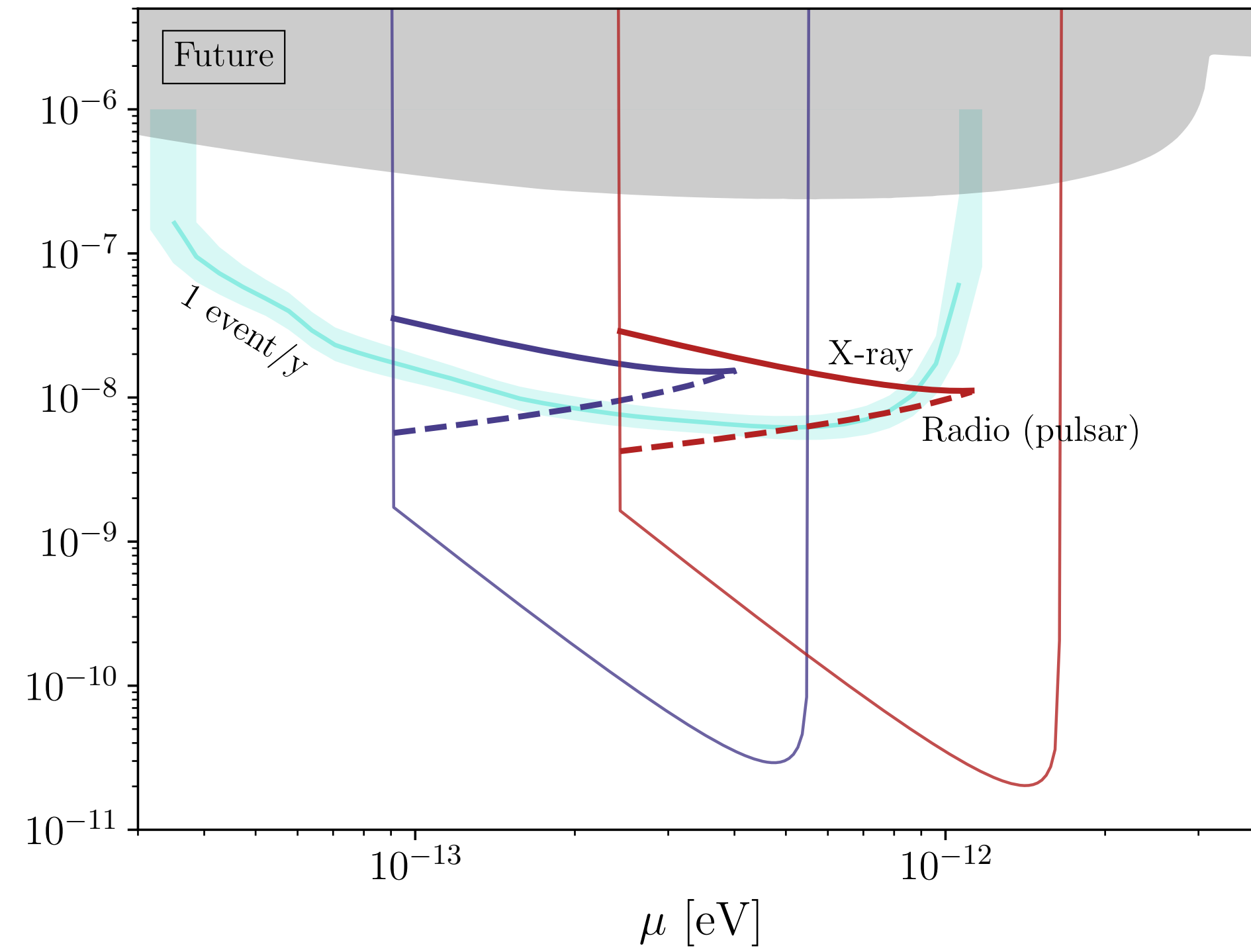
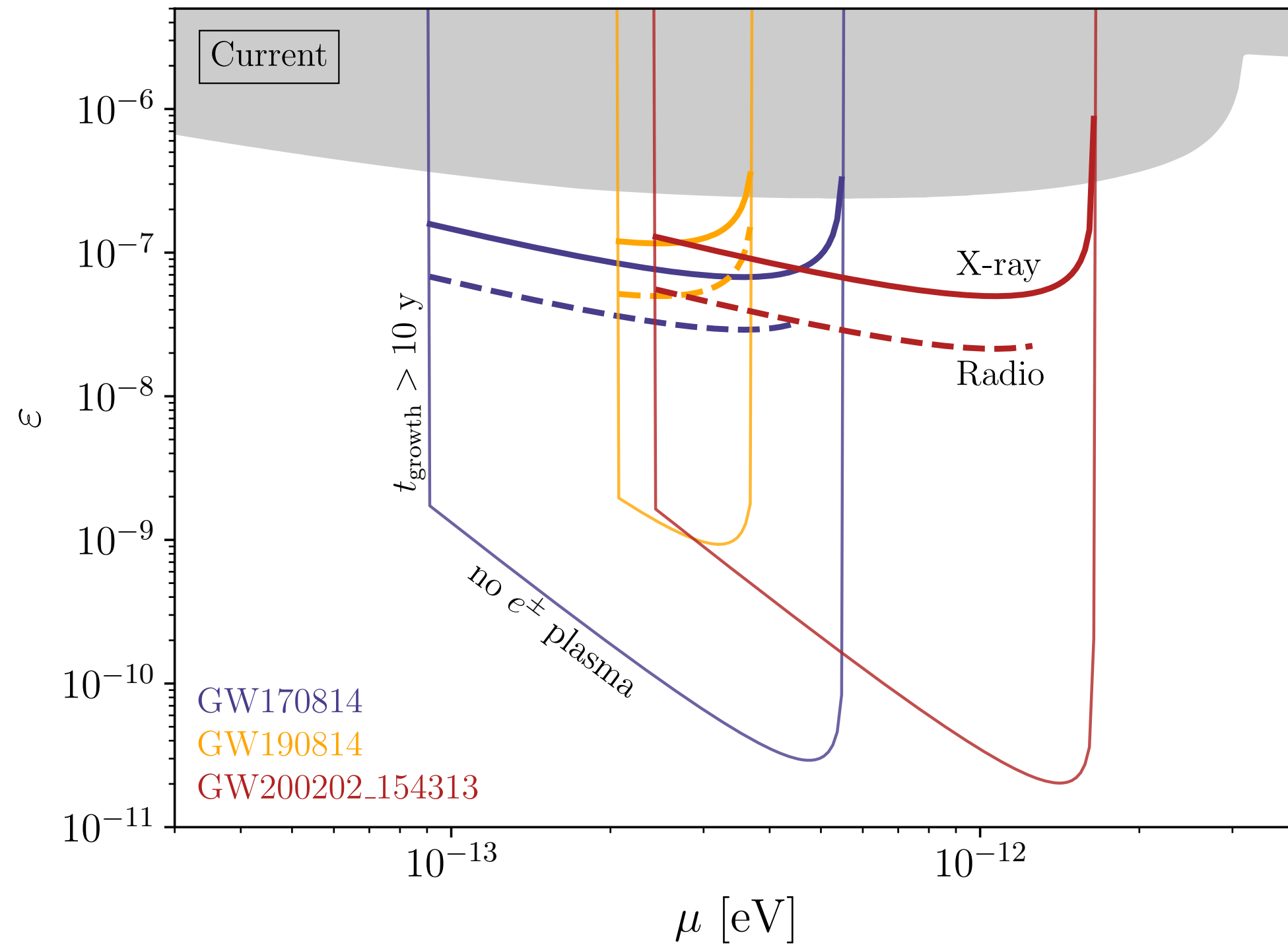
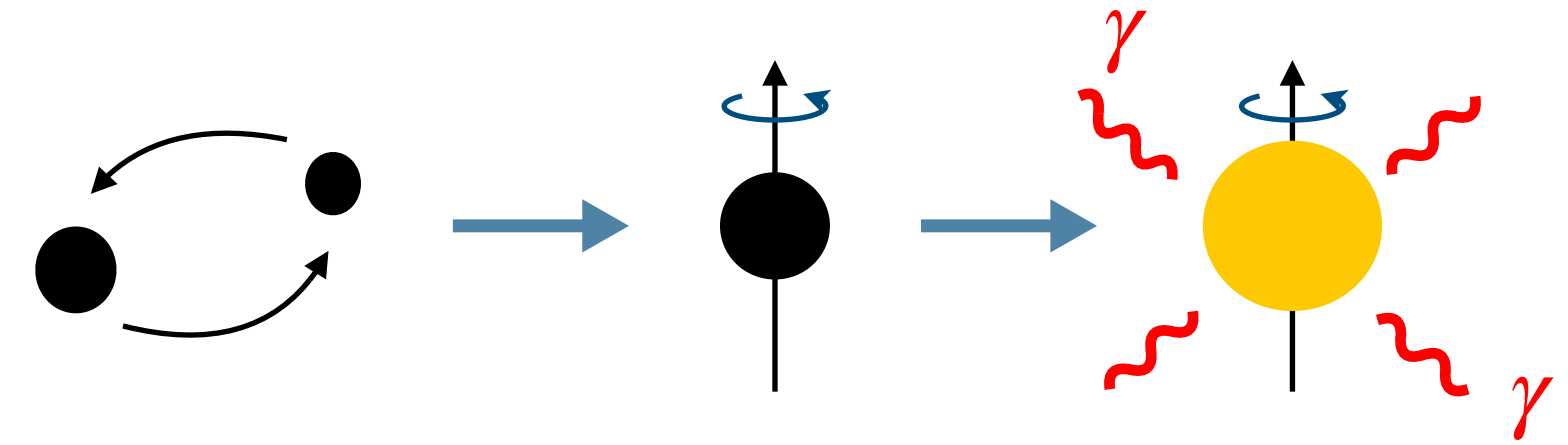
1. EM follow-ups of compact binary mergers
(large α)



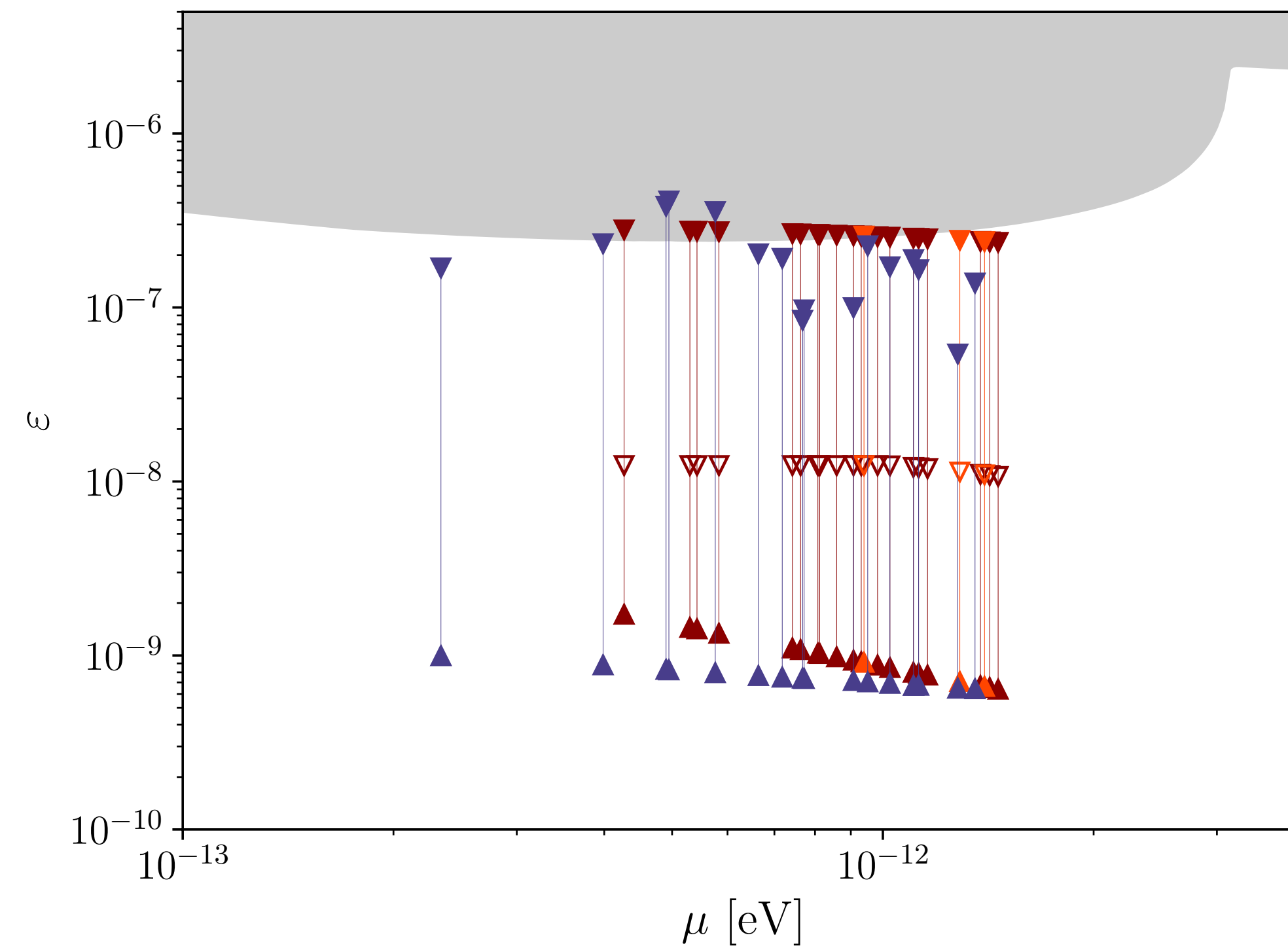
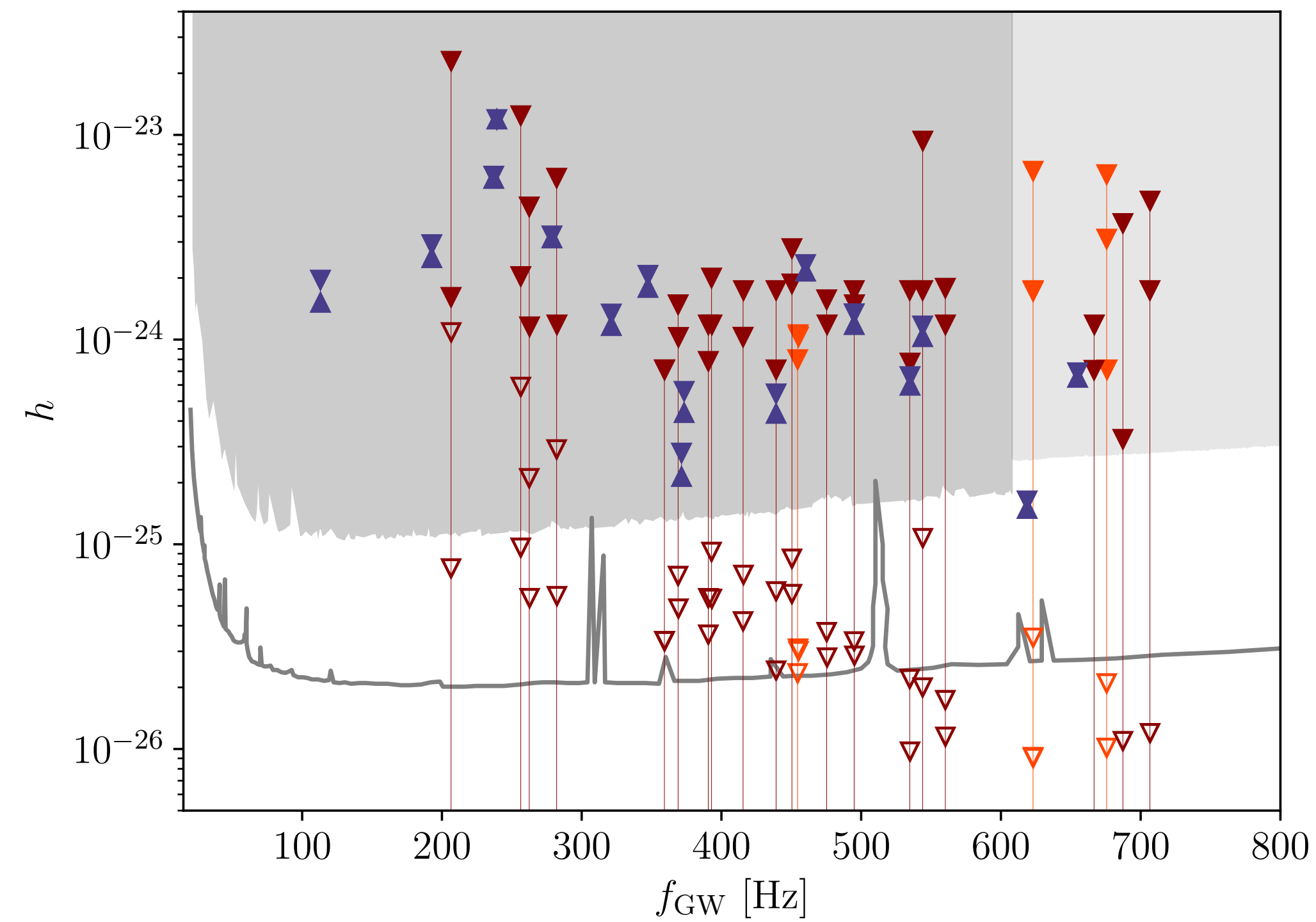
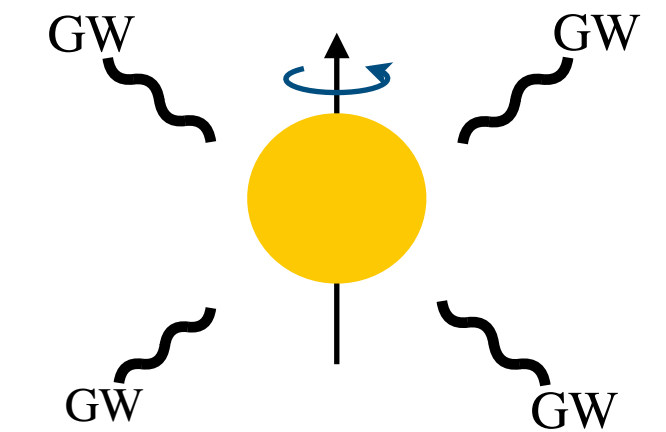
2. GW follow-ups of anomalous pulsars
(small α)



EM follow-up of BH mergers



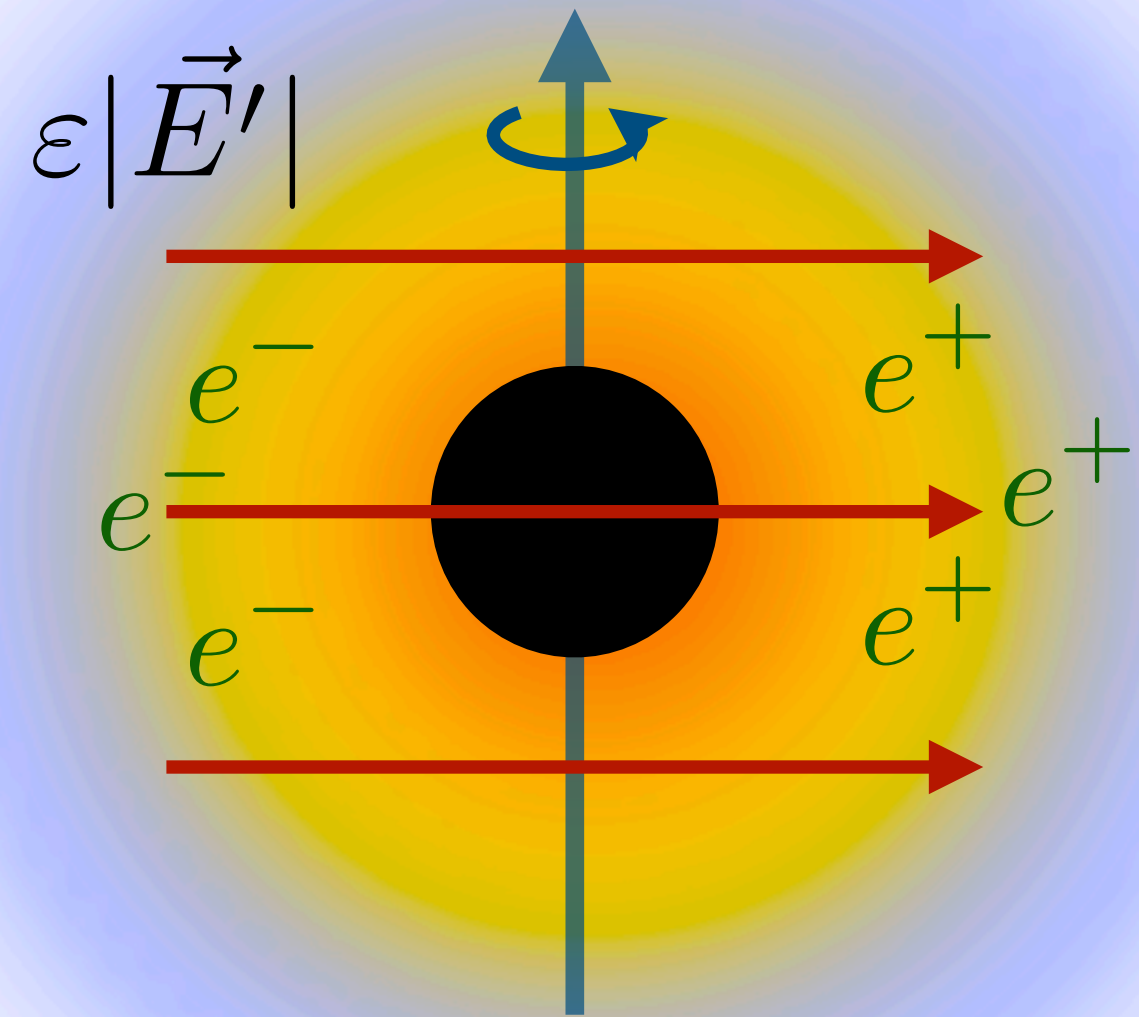
GW follow-up of anomalous pulsars



Summary

Black hole superradiance can probe ultralight dark photons with small kinetic mixing.

- The superradiance cloud is filled with a plasma of charged particles.
- The electrodynamics of the plasma + fields can be modeled in analogy to a pulsar.
- Large electromagnetic emissions are released.



Future directions:

- More robust predictions for the emission spectra and the periodicity.
- Ultraluminous X-ray sources or FRB.
- Supermassive BH.

