

# ***The Daya Bay Reactor Neutrino Experiment***

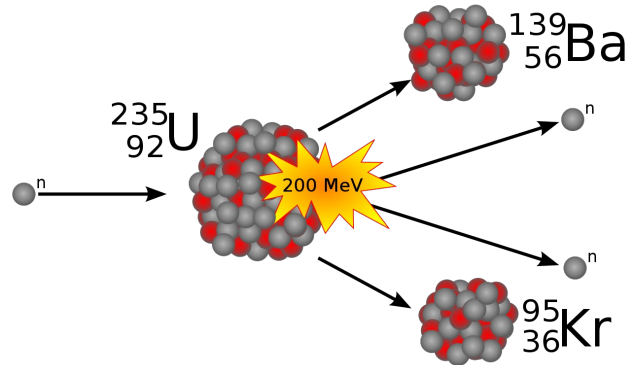
*Wei Wang, Sun Yat-sen University  
On Behalf of the Daya Bay Collaboration  
HEP2023, Valparaiso, Jan 12, 2023*



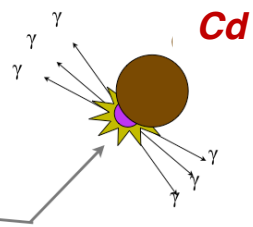
- Neutrino Oscillation: A Brief Review*
- Design and Running of Daya Bay*
- Highlights of Selected Daya Bay Results*
- Summary and Conclusion*

# Reines&Cowan Detected Reactor Neutrinos in 1956

➤ Cowan and Reines at the Savannah River Power Plant (1956-1959)

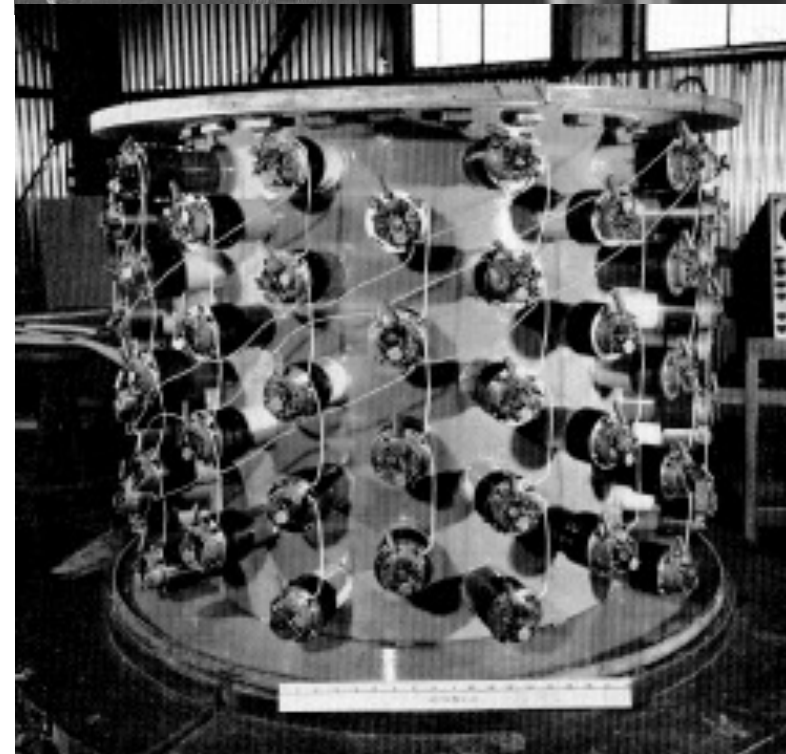


$\beta$  decay :  $N \rightarrow N' + e + \nu$   
Creation



Inversed  $\beta$  decay

Detection:  $p + \nu \rightarrow e^+ + n$



# Neutrino Mixing & Oscillation Proposed



- Bruno Pontecorvo in 1957:

**Interaction Eigenstates  $\neq$  Mass Eigenstates**  
**→ Neutrino Mixing and Oscillation**

*Бруно Понтекорво*

- Extended to 3 flavor mixing by Maki, Nakagawa and Sakata, after muon neutrino was discovered at BNL in 1962



Courtesy of Sakata Memorial Archival Library

S. Sakata  
1911-1970

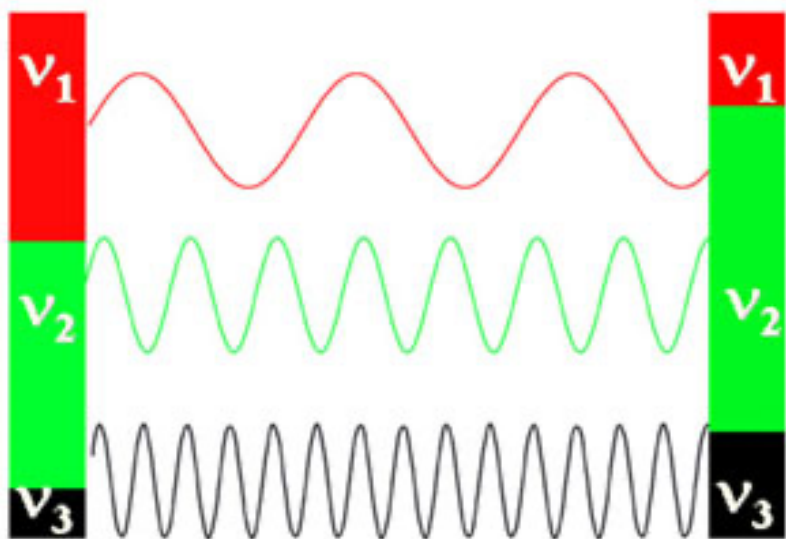
Z. Maki  
1929-2005

M. Nakagawa  
1932-2001

# Neutrino Mixing & Oscillation

➤ Pontecorvo-Maki-Nakagawa-Sakata (PMNS) mixing matrix,

$$U_{PMNS} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & \cos \theta_{23} & \sin \theta_{23} \\ 0 & -\sin \theta_{23} & \cos \theta_{23} \end{pmatrix} \begin{pmatrix} \cos \theta_{13} & 0 & e^{-i\delta_{CP}} \sin \theta_{13} \\ 0 & 1 & 0 \\ -e^{i\delta_{CP}} \sin \theta_{13} & 0 & \cos \theta_{13} \end{pmatrix} \begin{pmatrix} \cos \theta_{12} & \sin \theta_{12} & 0 \\ -\sin \theta_{12} & \cos \theta_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$



$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \begin{pmatrix} V_{e1} & V_{e2} & V_{e3} \\ V_{\mu1} & V_{\mu2} & V_{\mu3} \\ V_{\tau1} & V_{\tau2} & V_{\tau3} \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$

⇒ Oscillation Probability:

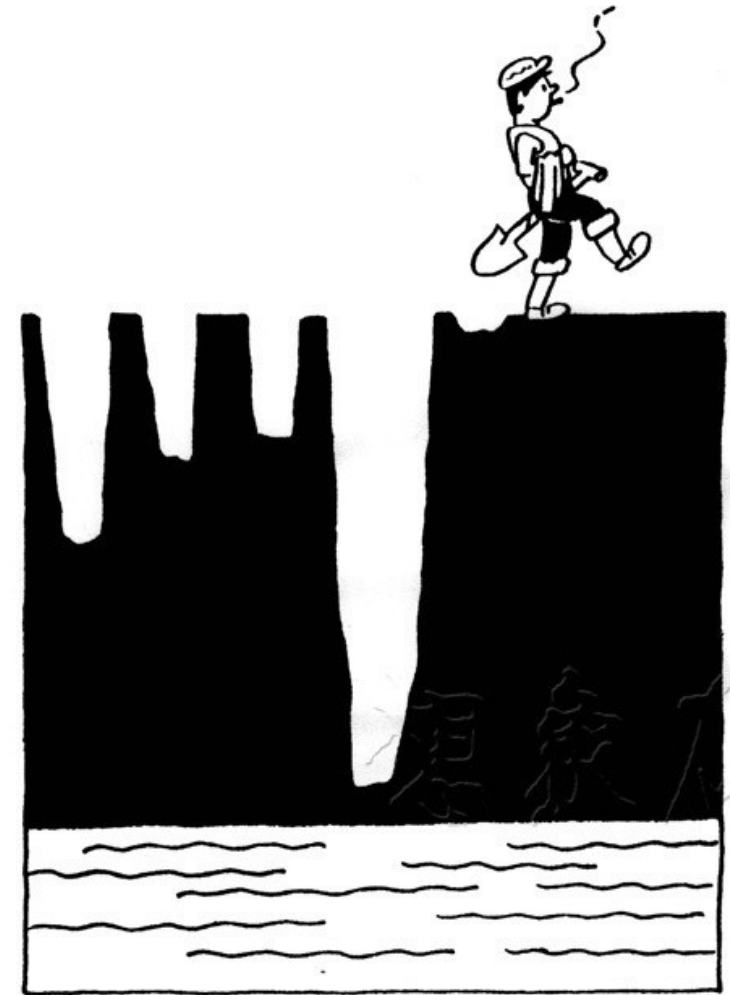
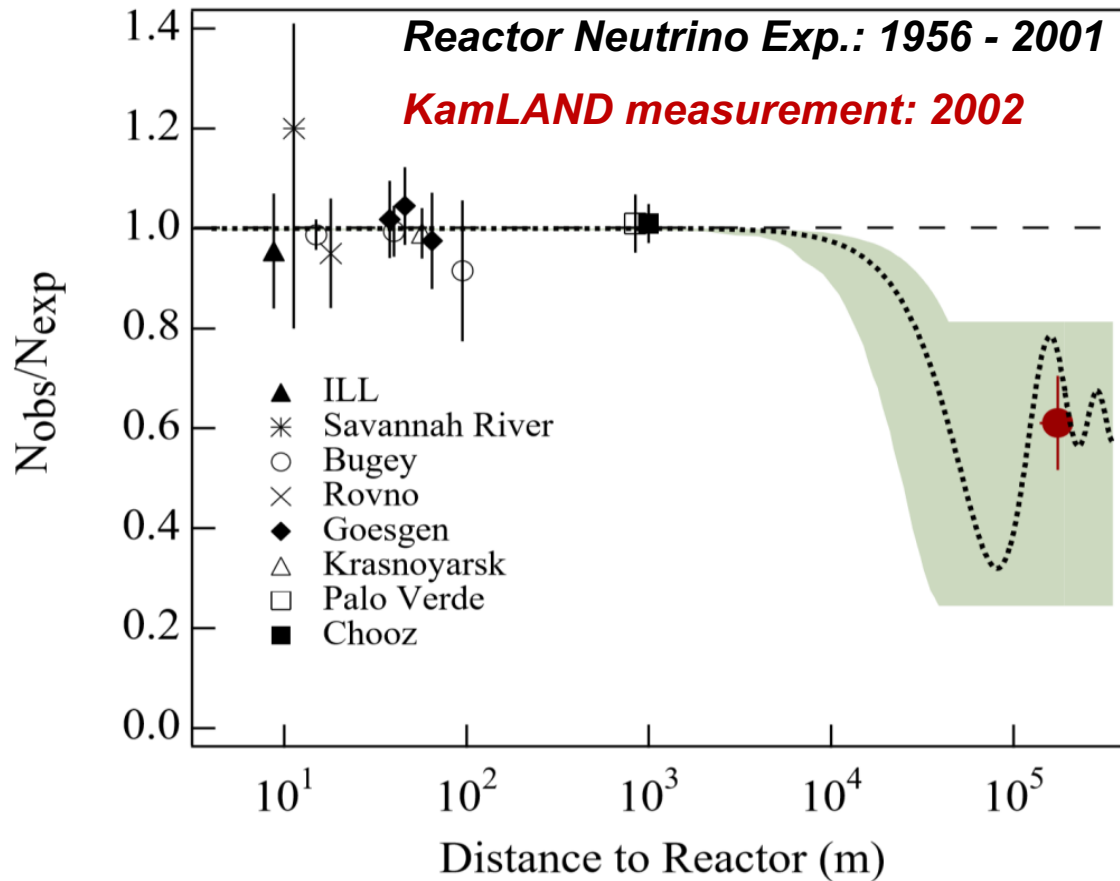
$$P_{\nu_\alpha \rightarrow \nu_\beta} = 1 - 4 \sum_{i < j} |V_{\alpha j}|^2 |V_{\beta i}|^2 \sin^2 \frac{\Delta m_{ji}^2 L}{4E}$$

**Amplitude  $\propto \sin^2 2\theta$**

**Frequency  $\propto \Delta m^2 L/E$**



# The Search for Neutrino Oscillation 1957-1997



—这下面没有水，再换个地方挖

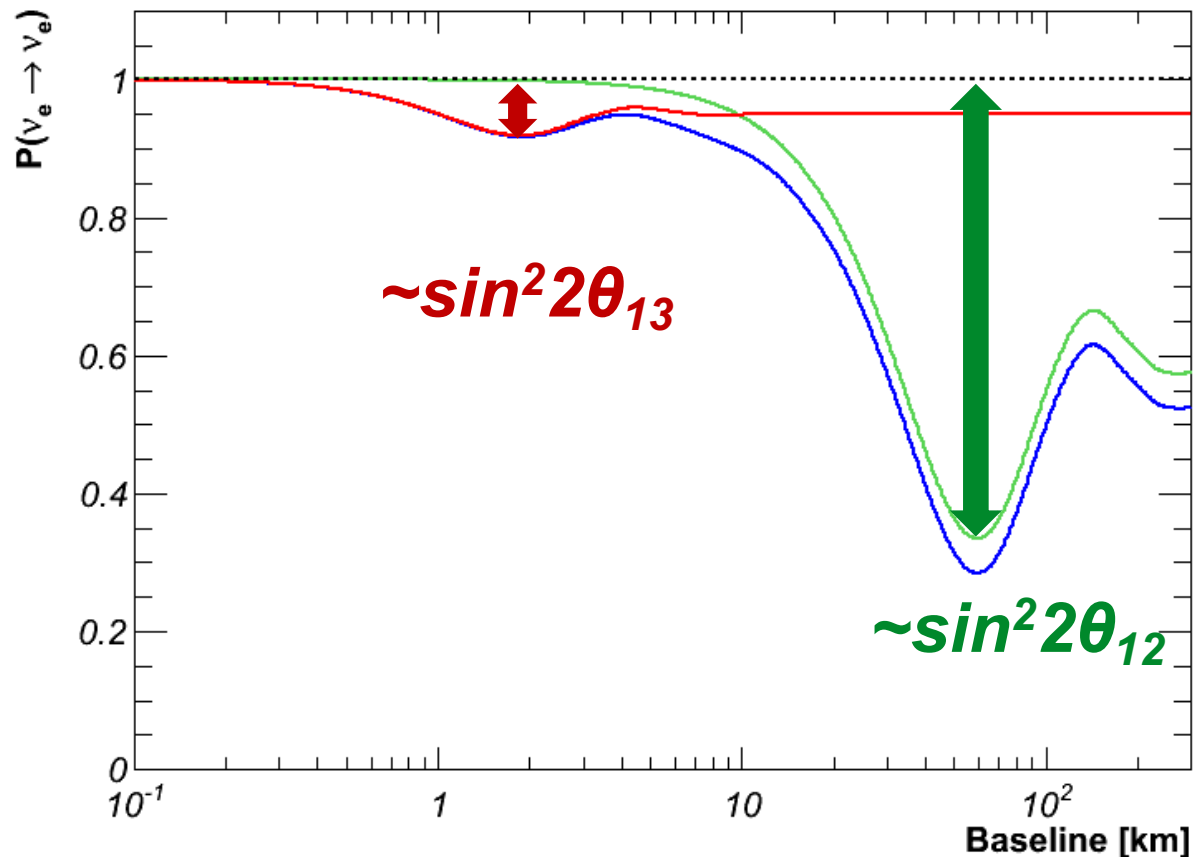
张新华画

# What Reactor Neutrinos Can Measure

$$P(\bar{\nu}_e \rightarrow \bar{\nu}_e) \approx 1 - \boxed{\sin^2 2\theta_{13} \sin^2 \left( \frac{\Delta m_{ee}^2 L}{4E} \right)} - \boxed{\cos^4 \theta_{13} \sin^2 2\theta_{12} \sin^2 \left( \frac{\Delta m_{21}^2 L}{4E} \right)}$$

$\sin^2 \left( \Delta m_{ee}^2 \frac{L}{4E} \right) \equiv \cos^2 \theta_{12} \sin^2 \left( \Delta m_{31}^2 \frac{L}{4E} \right) + \sin^2 \theta_{12} \sin^2 \left( \Delta m_{32}^2 \frac{L}{4E} \right)$

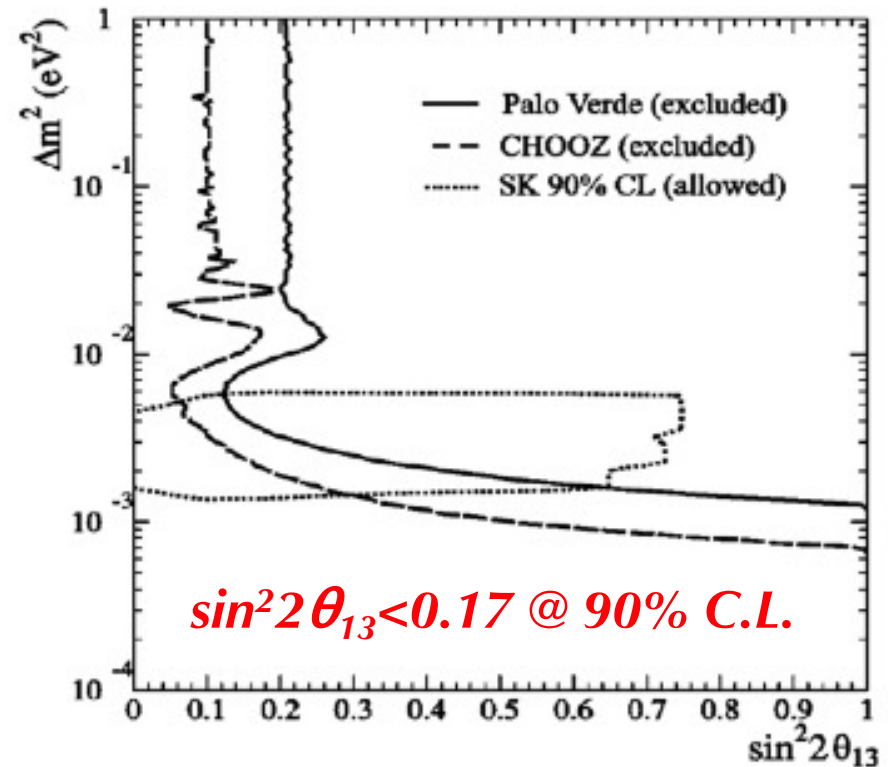
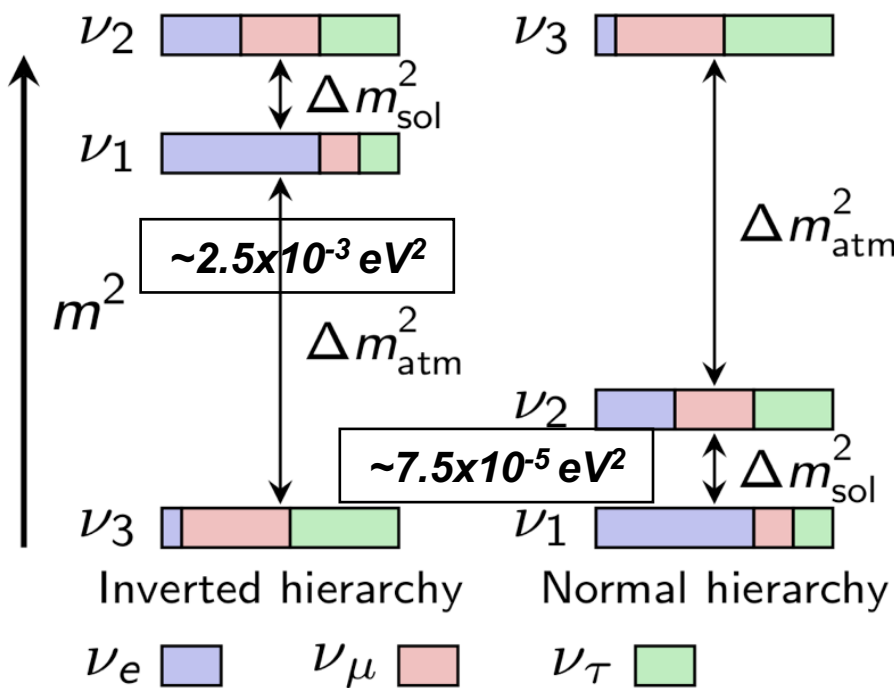
- At different distances, the survival rate is dominated by different mixing angles
- To measure  $\theta_{13}$ , a baseline of  $\sim 2$  km is optimal



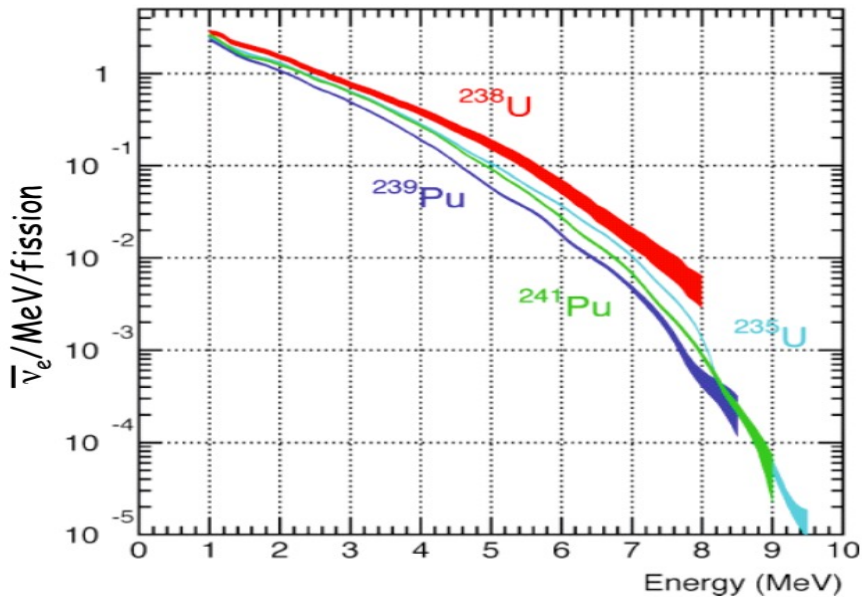
# Between the Breakthroughs (2002-2012)

$$U_{PMNS} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & \cos \theta_{23} & \sin \theta_{23} \\ 0 & -\sin \theta_{23} & \cos \theta_{23} \end{pmatrix} \begin{pmatrix} \cos \theta_{13} & 0 & e^{-i\delta_{CP}} \sin \theta_{13} \\ 0 & 1 & 0 \\ -e^{i\delta_{CP}} \sin \theta_{13} & ? & \cos \theta_{13} \end{pmatrix} \begin{pmatrix} \cos \theta_{12} & \sin \theta_{12} & 0 \\ -\sin \theta_{12} & \cos \theta_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

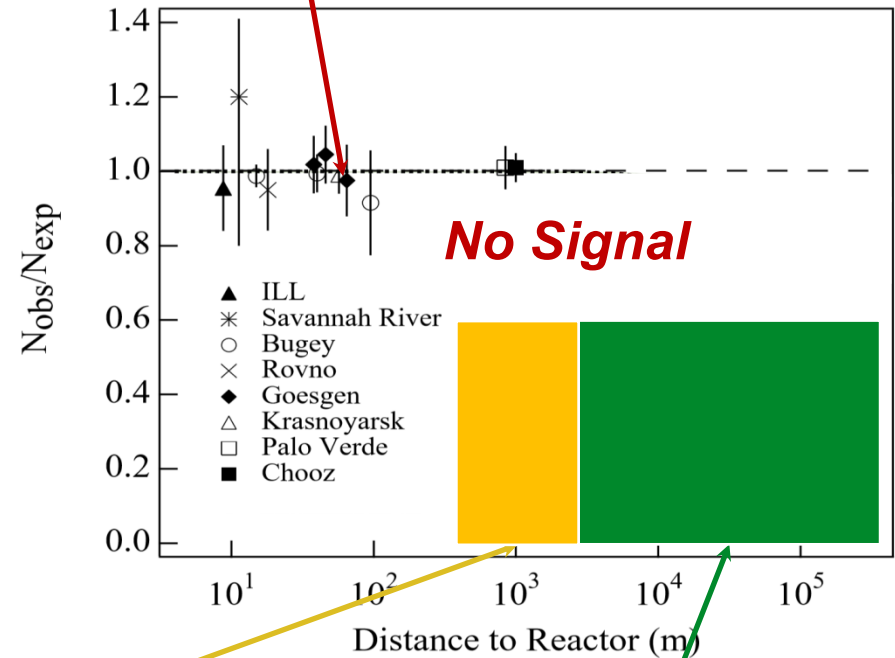
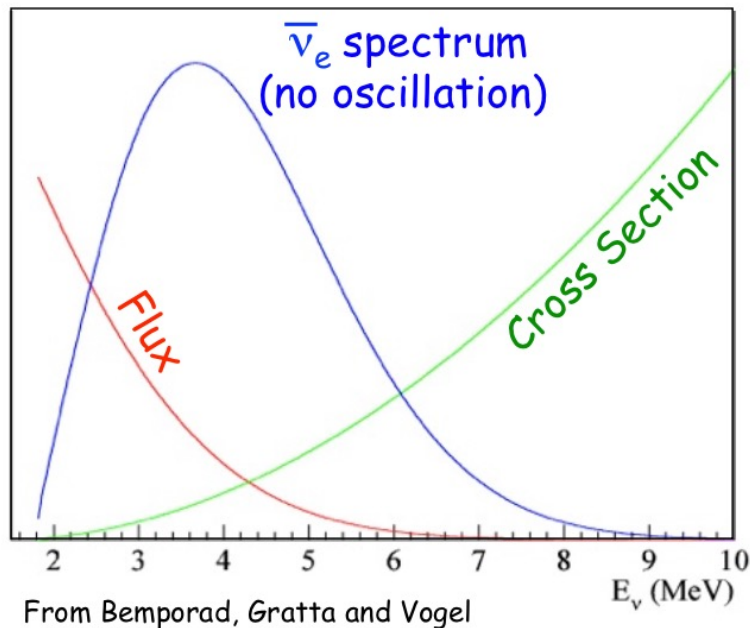
**Atmospheric Sector:**  
SK, K2K, T2K, MINOS, etc
**Reactor Sector:**  
CHOOZ, Palo Verde
**Solar Sector:**  
SNO, SK, KamLAND etc



# Reactor Neutrinos for Theta13: Challenges



**Six antineutrinos/fission:  
~2-8MeV, ~5% accuracy**



$\theta_{13}$   
Dominated

$\theta_{12}$   
Dominated



# Daya Bay: A Powerful Neutrino Source at an Ideal Location



Mountains shield detectors from cosmic ray background

Daya Bay NPP  
 $2 \times 2.9 \text{ GW}_{\text{th}}$

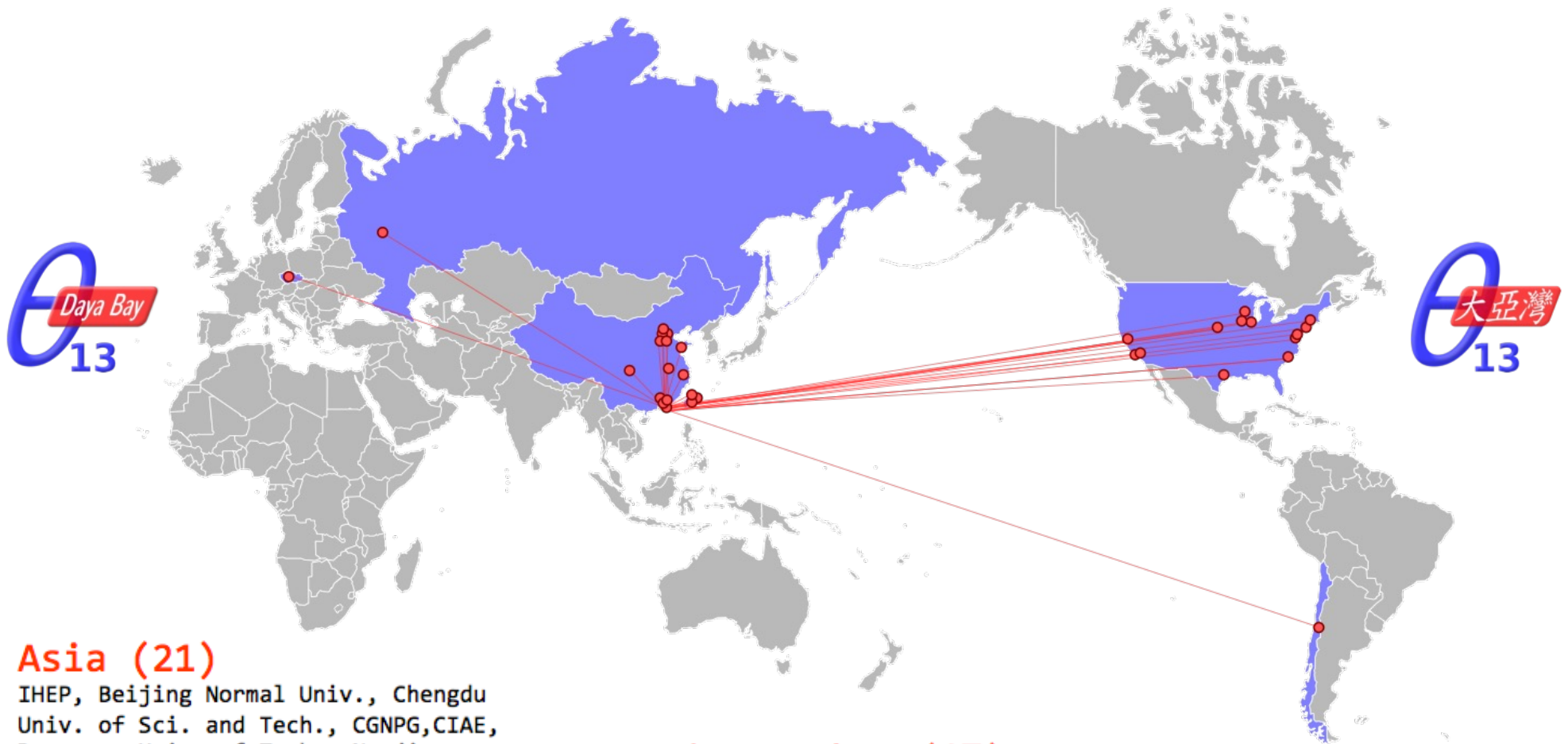
Ling Ao I NPP  
 $2 \times 2.9 \text{ GW}_{\text{th}}$

Ling Ao II NPP  
 $2 \times 2.9 \text{ GW}_{\text{th}}$

Entrance to Daya Bay experiment tunnels

Among the top 5 most powerful reactor complexes in the world, 6 cores produce  $17.4 \text{ GW}_{\text{th}}$  power,  $35 \times 10^{20}$  neutrinos per second

# The Daya Bay International Collaboration



## Asia (21)

IHEP, Beijing Normal Univ., Chengdu Univ. of Sci. and Tech., CGNPG, CIAE, Dongguan Univ. of Tech., Nanjing Univ., Nankai Univ., NCEPU, Shandong Univ., Shanghai Jiao tong Univ., Shenzhen Univ., Tsinghua Univ., USTC, Xi'an Jiaotong Univ., **Sun Yat-sen Univ.**, Univ. of Hong Kong, Chinese Univ. of Hong Kong, National Taiwan Univ., National Chiao Tung Univ., National United Univ.

## North America (17)

BNL, LBNL, Iowa State Univ., RPI, Illinois Inst. Tech., Princeton, UC-Berkeley, UCLA, Univ. of Cincinnati, Univ. of Houston, Univ. of Wisconsin, William & Mary, Virginia Tech., Univ. of Illinois-Urbana-Champaign, Siena, Temple Univ, Yale

## Europe (2)

JINR, Dubna, Russia; Charles University, Czech Republic

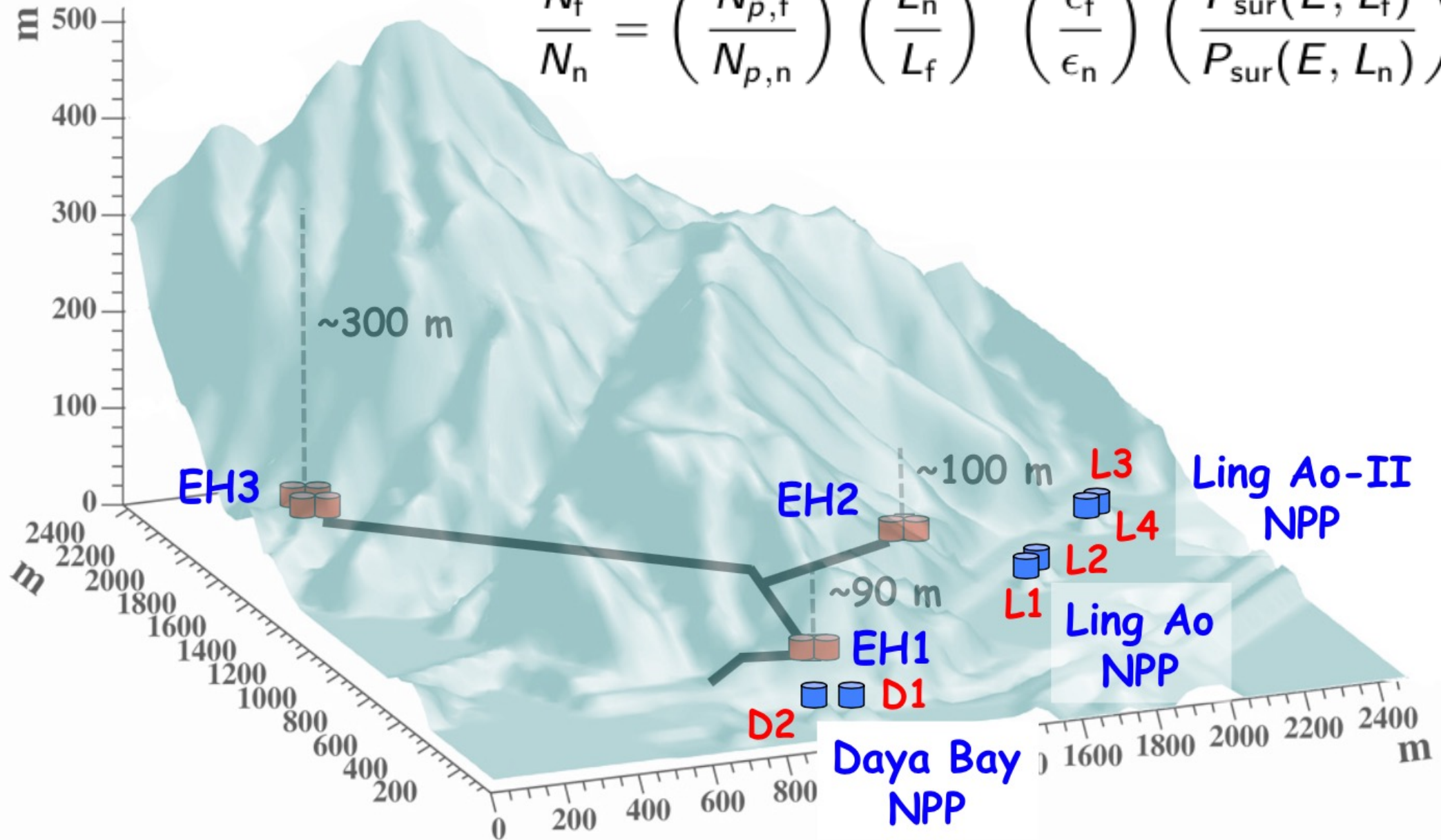
## South America (1)

**Catholic Univ. of Chile (2014-2019)**



# Multi-Baseline and Multi-Detector Design of Daya Bay

$$\frac{N_f}{N_n} = \left( \frac{N_{p,f}}{N_{p,n}} \right) \left( \frac{L_n}{L_f} \right)^2 \left( \frac{\epsilon_f}{\epsilon_n} \right) \left( \frac{P_{\text{sur}}(E, L_f)}{P_{\text{sur}}(E, L_n)} \right)$$



# The Daya Bay Antineutrino Detector (AD)

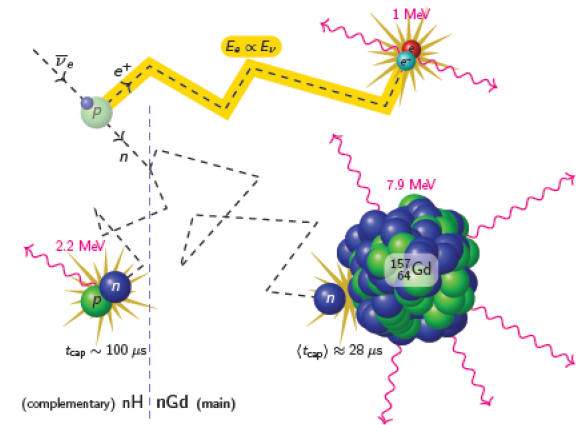
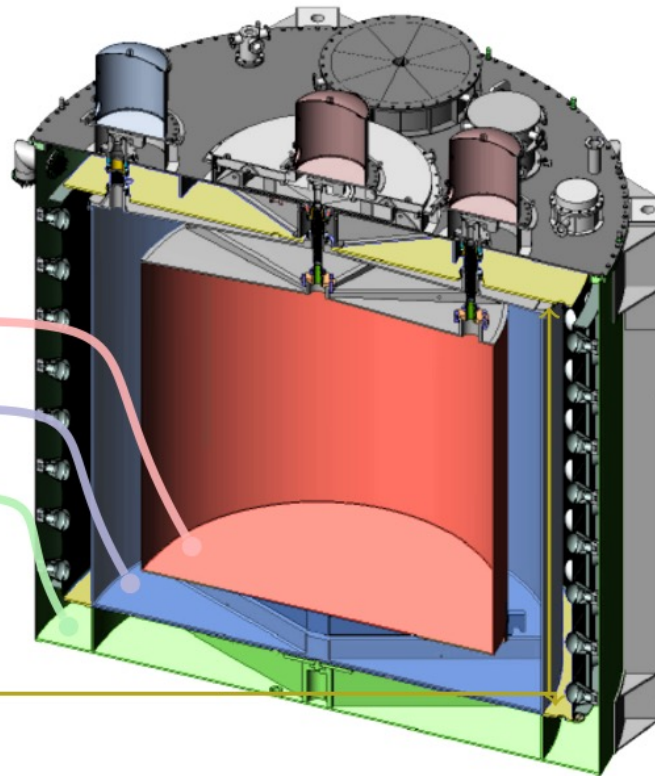
8 functionally identical detectors  
reduce systematic uncertainties

### 3 zone cylindrical vessels

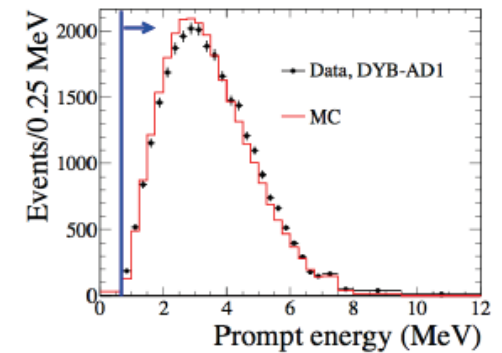
	Liquid	Mass	Function
Inner acrylic	Gd-doped liquid scint.	20 t	Antineutrino target
Outer acrylic	Liquid scintillator	20 t	Gamma catcher
Stainless steel	Mineral oil	40 t	Radiation shielding

192 8 inch PMTs in each detector

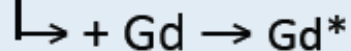
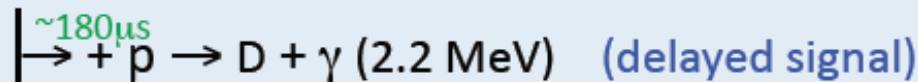
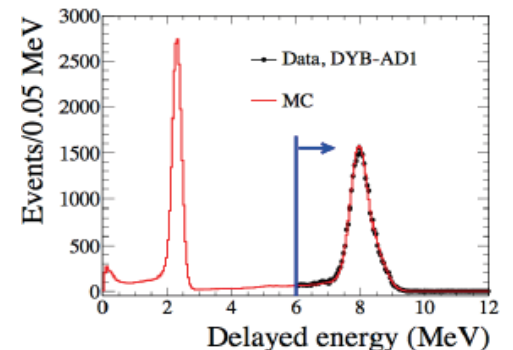
Top and bottom reflectors increase light yield  
and flatten detector response



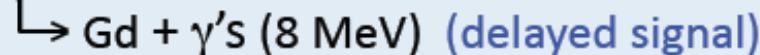
### Prompt Energy Signal



### Delayed Energy Signal

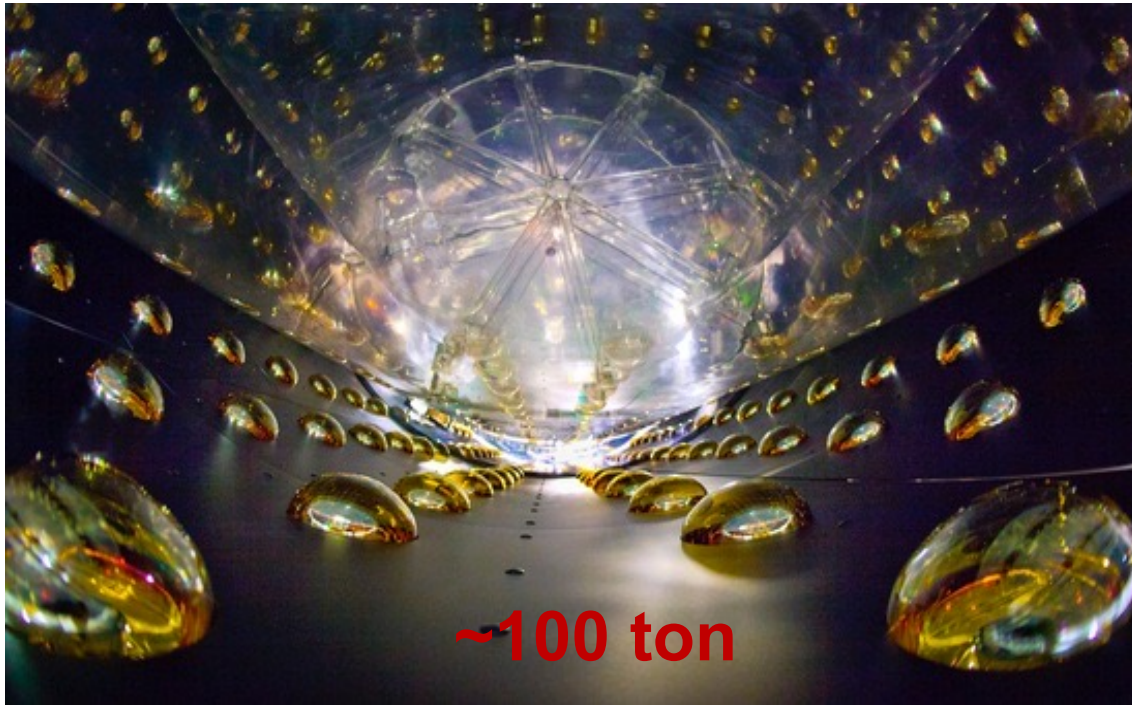


$\sim 30 \mu s$   
for 0.1% Gd

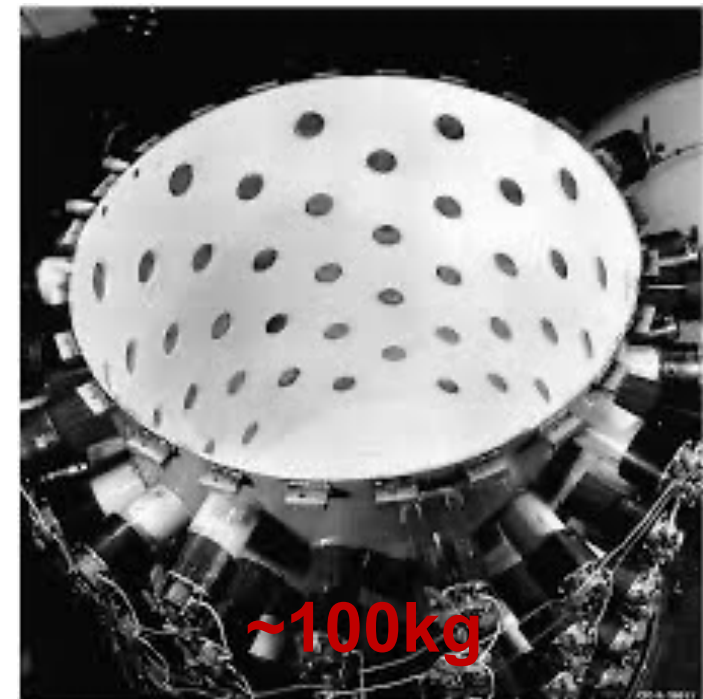




# The Daya Bay Detector and the Reines&Cowan Design



***“Standing on the shoulder of giants”***





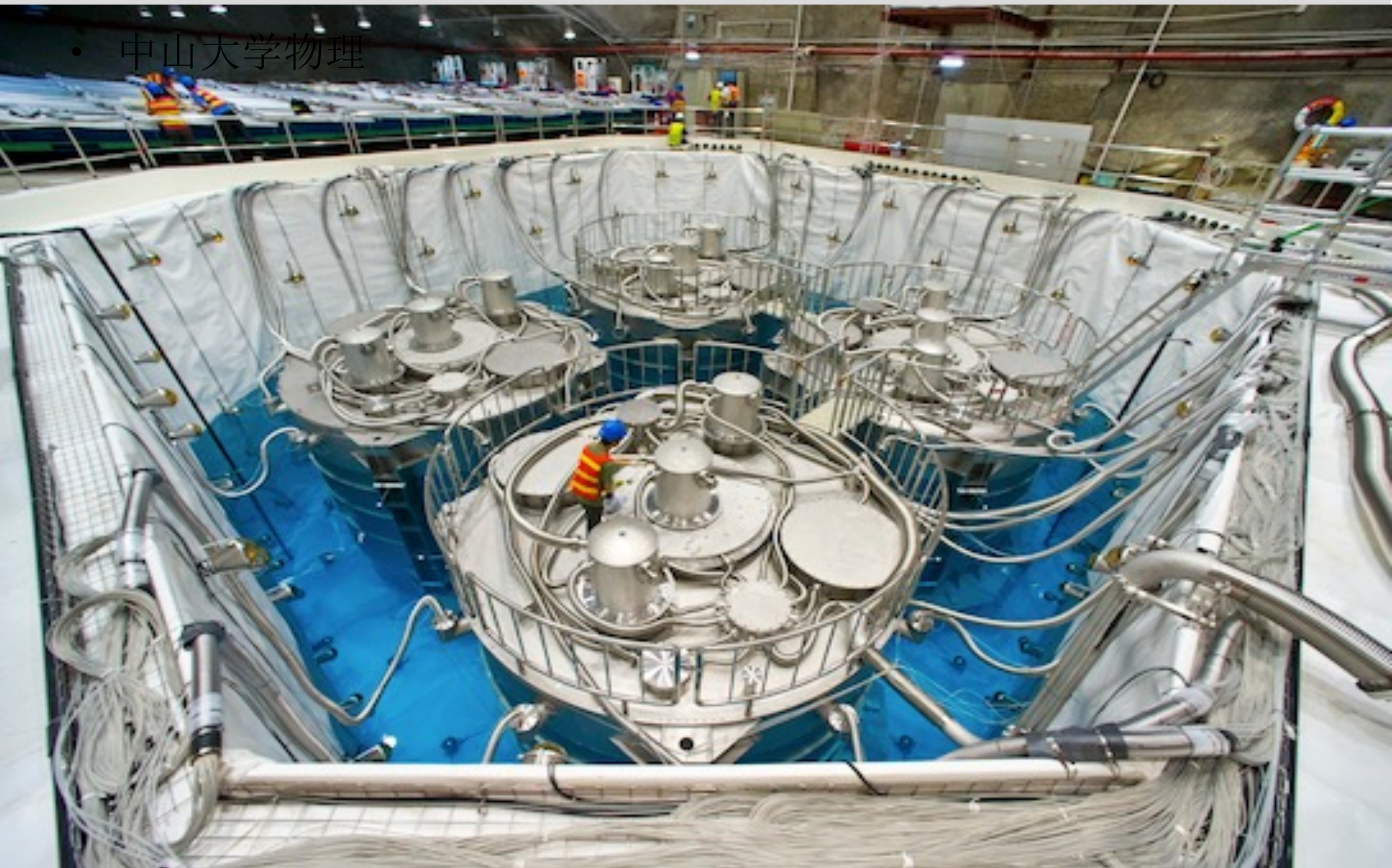
# A Small Big Science Project





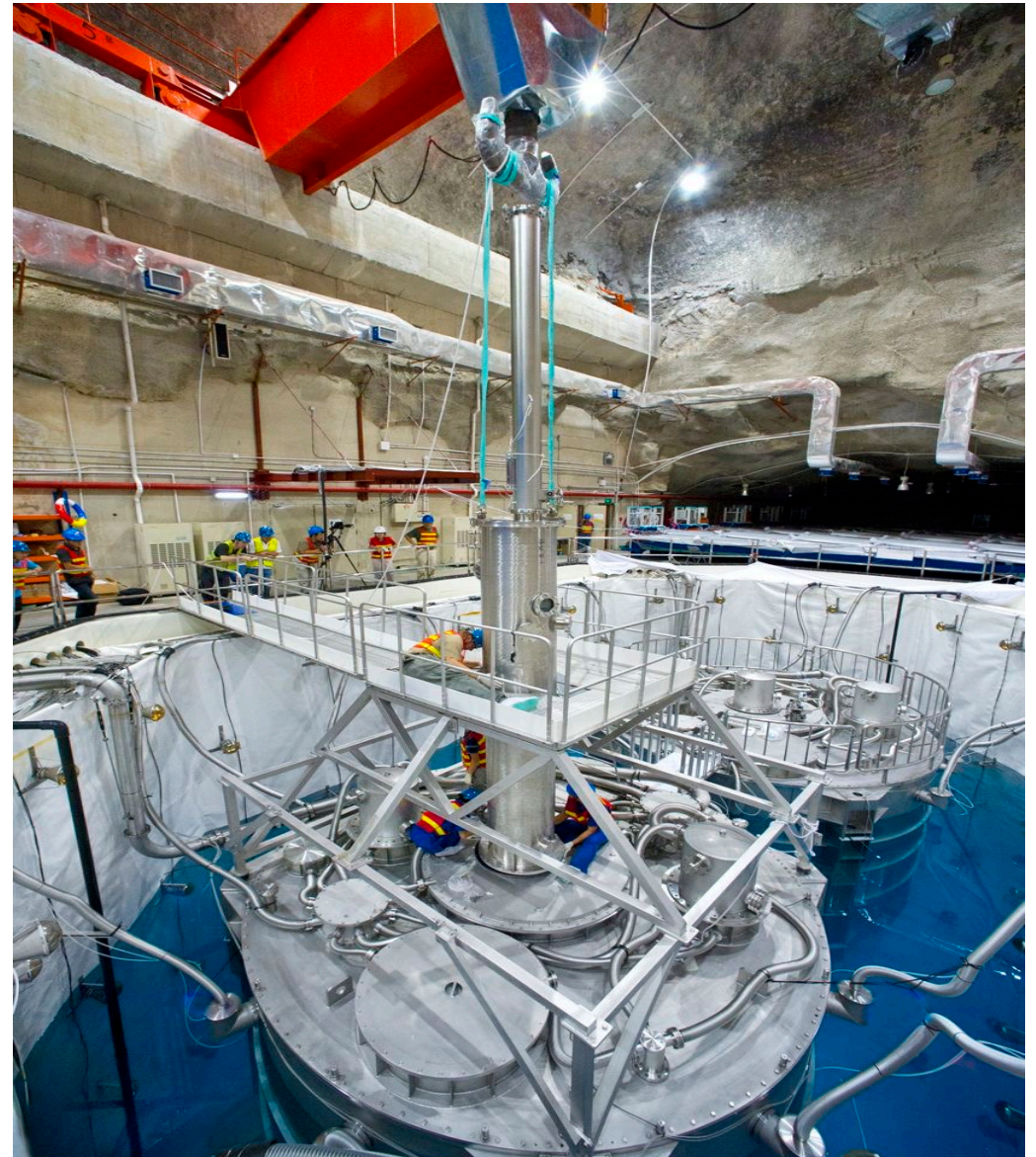
# A Small Big Science Project

- 中山大学物理





# Daya Bay Calibration Systems



- Automatic Calibration Units (ACUs)
- Manual calibration by CIAE



# The Daya Bay Running & Data Taking



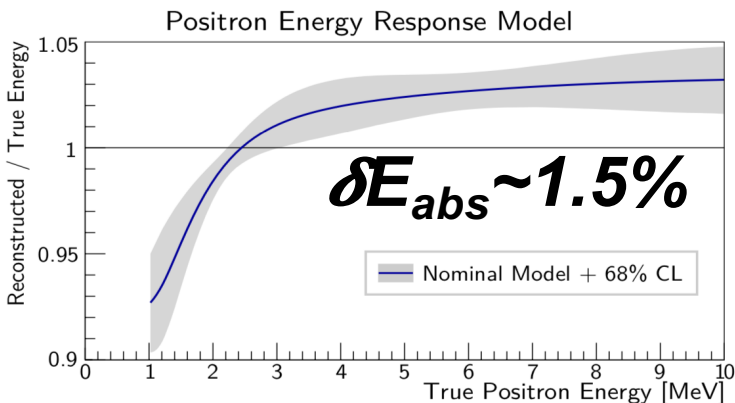
Date	Operation	Duration
<b>Dec 24, 2011</b>	<b>Data taking with 6 ADs</b> EH1: 2 ADs EH2: 1 AD EH3: 3 ADs	217 Days
Jul 28 – Oct 19, 2012	Special calibration runs; Installation of the last 2 ADs	
Oct 19, 2012	<b>Data taking with 8 ADs</b>	1,524 Days
Dec 20, 2016 – Jan 26, 2017	Special calibration runs <b>EH1 AD1 used for JUNO LS studies</b>	
Jan 26, 2017	<b>Data taking with 7 ADs</b> EH1: 1 ADs EH2: 2 AD EH3: 4 ADs	1,417 Days
<b>Dec 12, 2020</b>	<b>Shutdown; Decommissioning started</b>	/

# Understanding the Detector to *Extreme*

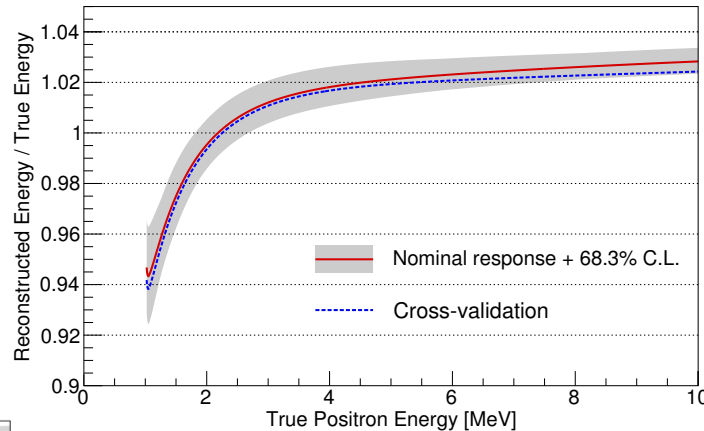
## 2012

Detector			
	Efficiency	Correlated	Uncorrelated
Target Protons		0.47%	0.03%
Flasher cut	99.98%	0.01%	0.01%
Delayed energy cut	90.9%	0.6%	0.12%
Prompt energy cut	99.88%	0.10%	0.01%
Multiplicity cut		0.02%	<0.01%
Capture time cut	98.6%	0.12%	0.01%
Gd capture ratio	83.8%	0.8%	<0.1%
Spill-in	105.0%	1.5%	0.02%
Livetime	100.0%	0.002%	<0.01%
Combined	78.8%	1.9%	0.2%

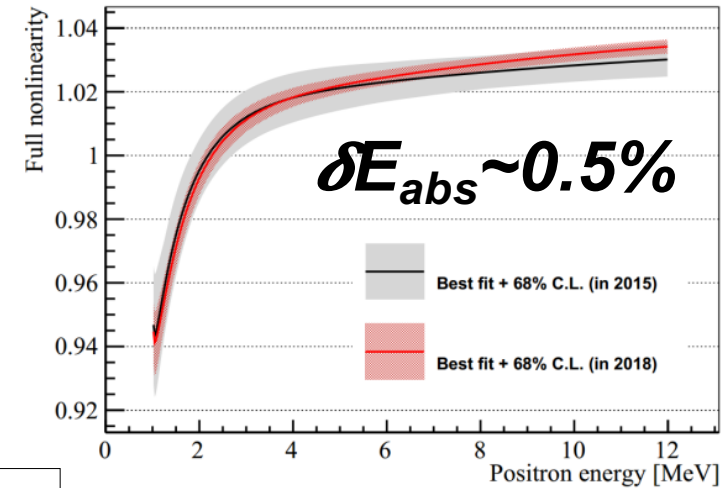
Reactor			
	Correlated	Uncorrelated	
Energy/fission	0.2%	Power	0.5%
$\bar{\nu}_e$ /fission	3%	Fission fraction	0.6%
		Spent fuel	0.3%
Combined	3%	Combined	0.8%



## 2015



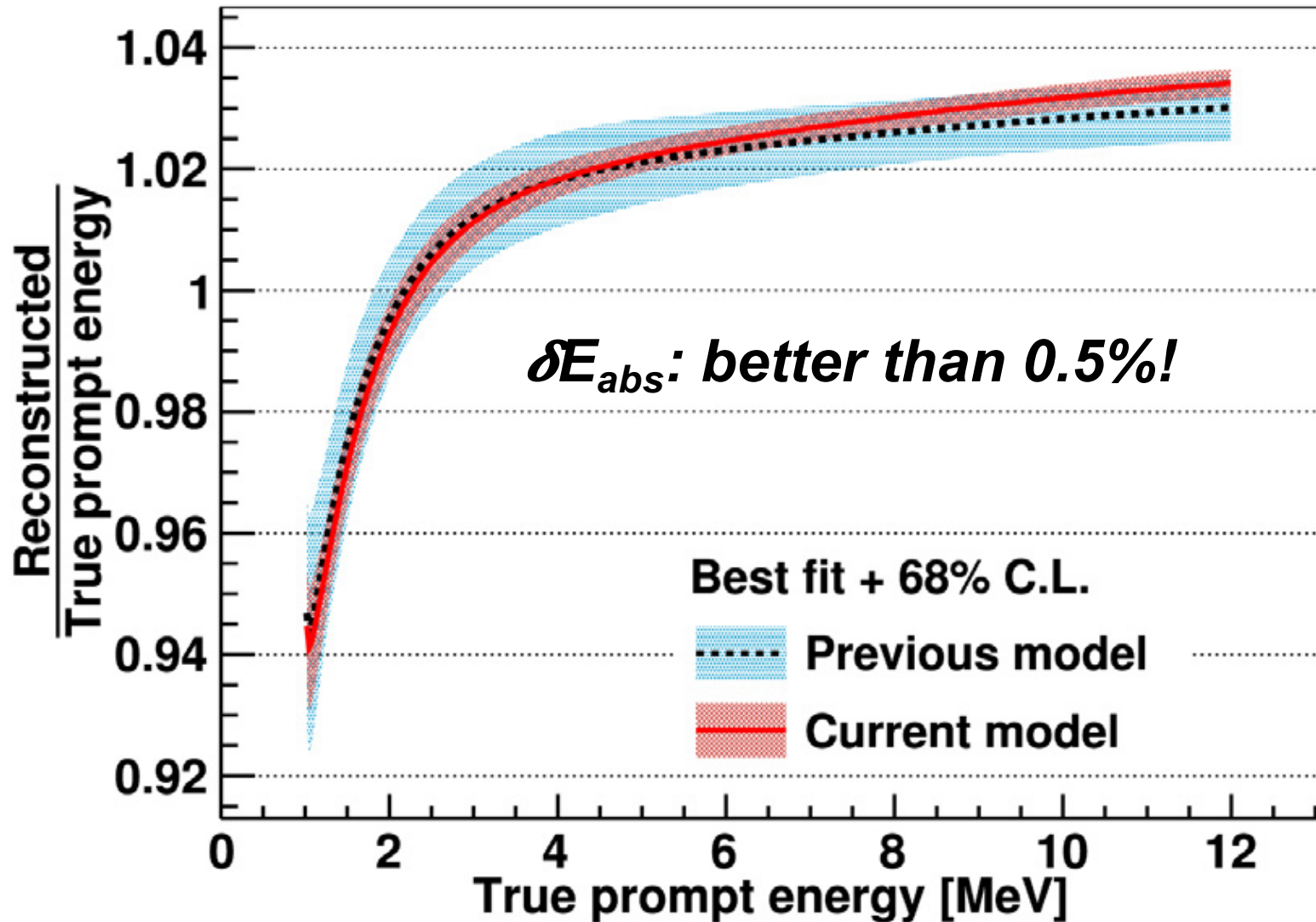
## 2018



	Efficiency	Uncertainty	
		Correlated	Uncorrelated
Target protons	-	0.92%	0.03%
Flasher cut	99.98%	0.01%	0.01%
Prompt Energy cut	99.8%	0.10%	0.01%
Multiplicity cut	-	0.02%	0.01%
Capture time cut	98.7%	0.12%	0.01%
Delayed neutron cut	81.48%	0.74%	0.13%
Live time	-	0.002%	0.01%
Combined	80.2%	1.2%	0.13%

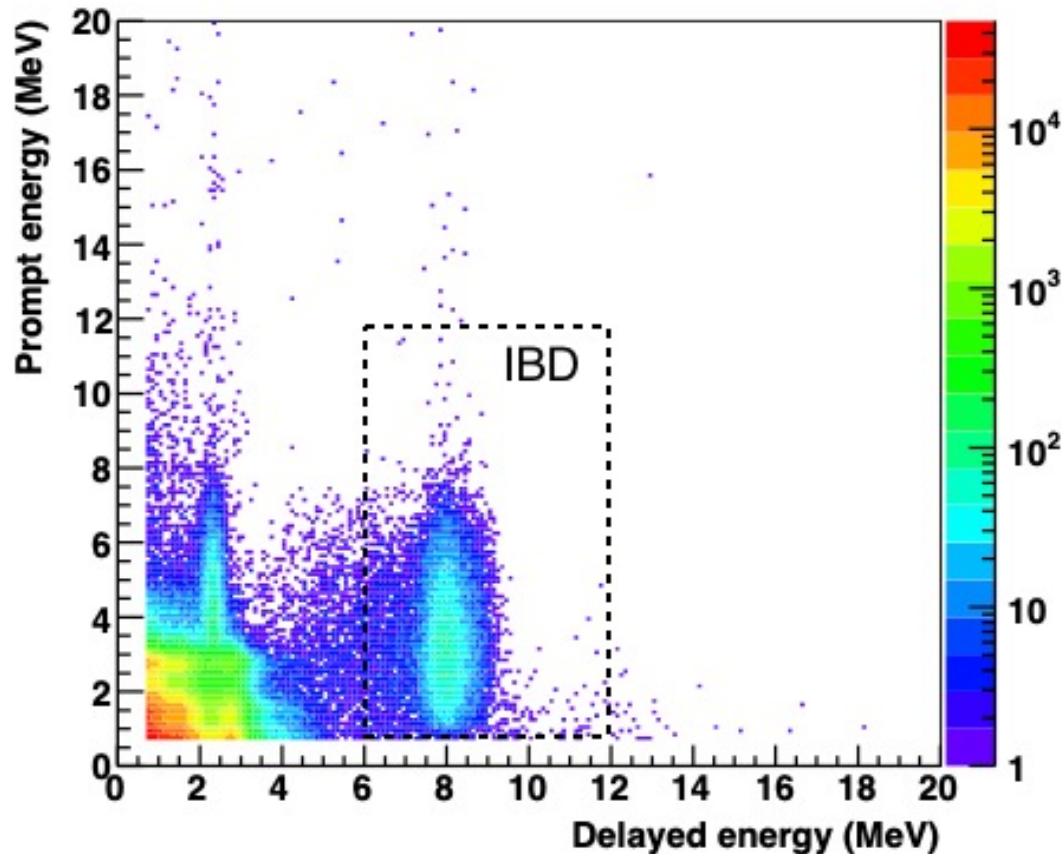
# The Best Understood LS Reactor Neutrino Detector

2019



For Details: *Nuclear Inst. and Methods in Physics Research, A 940 (2019) 230–242*

# How to Select Antineutrino Events



- First apply flasher cuts to clean up the data
- Muon veto to get rid of cosmogenic products
- IBD cuts
  - Prompt energy cut: (0.7, 12) MeV
  - **Delayed energy cut: (6, 12) MeV**
  - **Time correlation (Multiplicity) cut** to pick up IBD pairs

*Daya Bay Collaboration, PRD95 (2017) 072006*

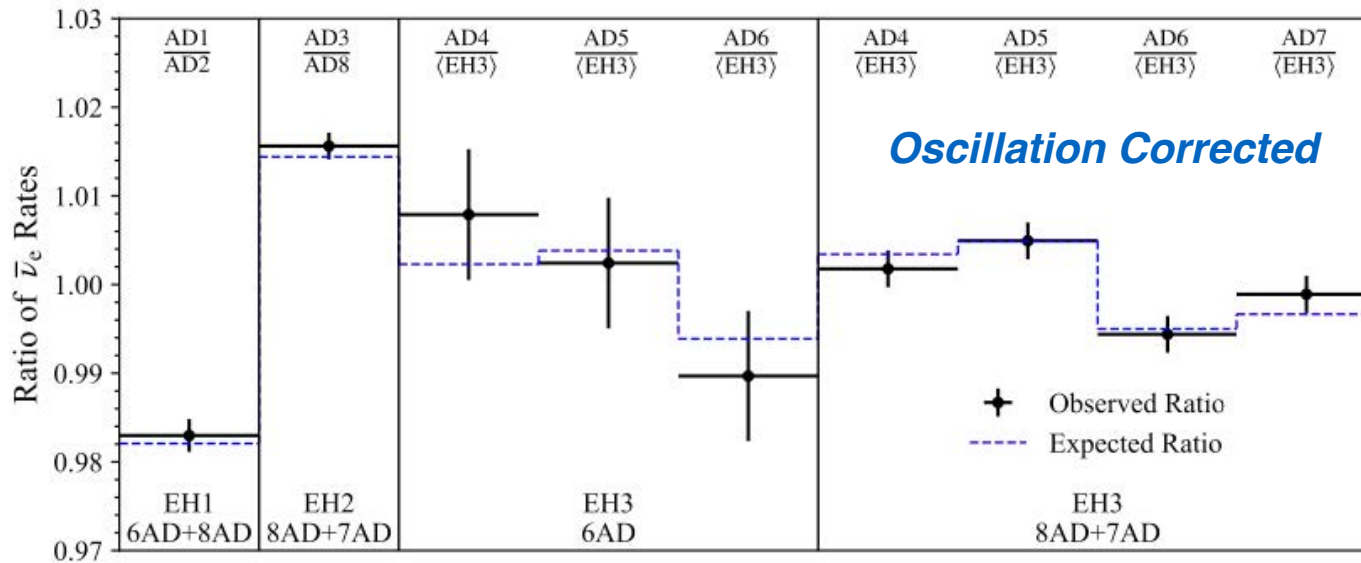
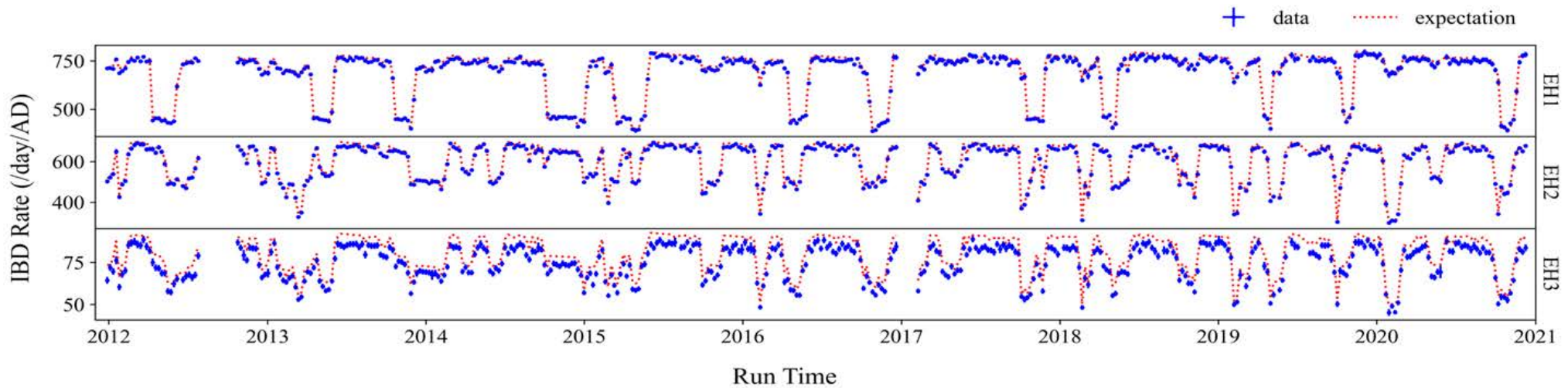


# Inversed Beta Decay Like Background Events



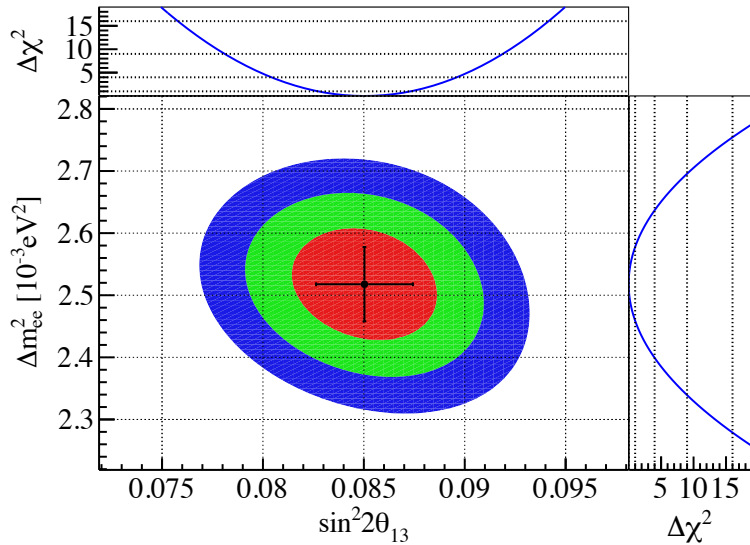
- Uncorrelated background: accidental pairs
- Correlated backgrounds:
  - Fast neutron: cosmogenic outside  $\rightarrow$  AD
  - ${}^9\text{Li}/{}^8\text{He}$ : cosmogenic from spallation products of cosmic-ray muons
  - ${}^{241}\text{Am}-{}^{13}\text{C}$ : ACU neutron calibration sources
  - ${}^{13}\text{C}(\alpha, n){}^{16}\text{O}$ :  $\alpha$  decay of natural radioactive isotopes
  - New backgrounds: Residual PMT flasher & Muon-x

# Event Rates at Daya Bay Detectors



- Daya Bay uses a combined Huber-Muller model to predict reactor neutrino fluxes --- the HM model

# The Latest Daya Bay Oscillation Results



$$\sin^2 2\theta_{13} = 0.0852 \pm 0.0024$$

$$|\Delta m_{ee}^2| = (2.519 \pm 0.060) \times 10^{-3} \text{ eV}^2$$

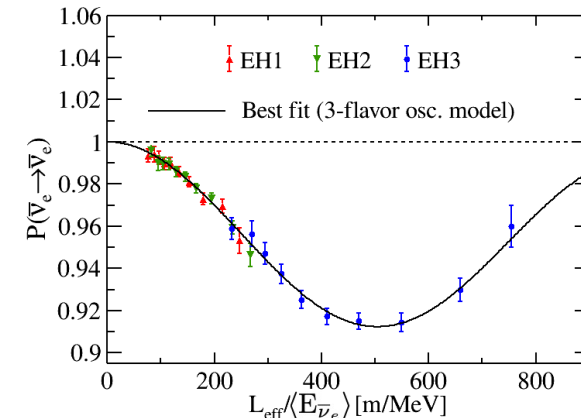
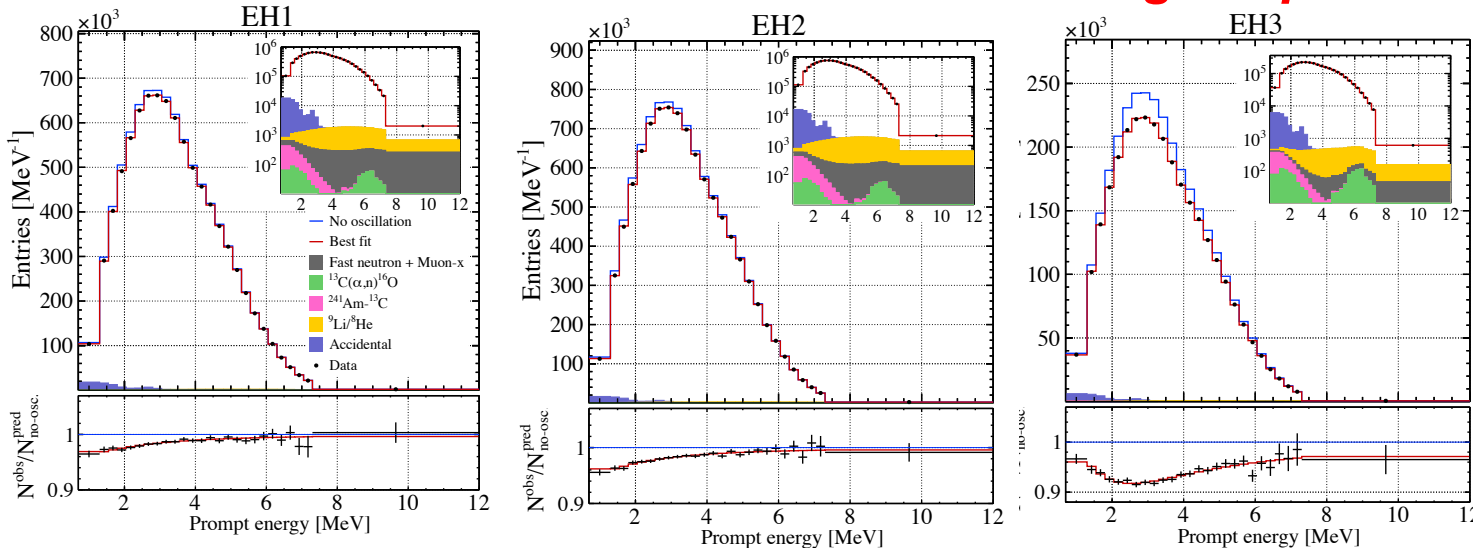
$$\Delta m_{32}^2 = (2.466 \pm 0.060) \times 10^{-3} \text{ eV}^2$$

$$\Delta m_{32}^2 = -(2.571 \pm 0.060) \times 10^{-3} \text{ eV}^2$$

❖  $\theta_{13}$  measured to a precision of 2.8%, currently the best known mixing angle

❖ Also the most precise  $\Delta m_{atm}^2$

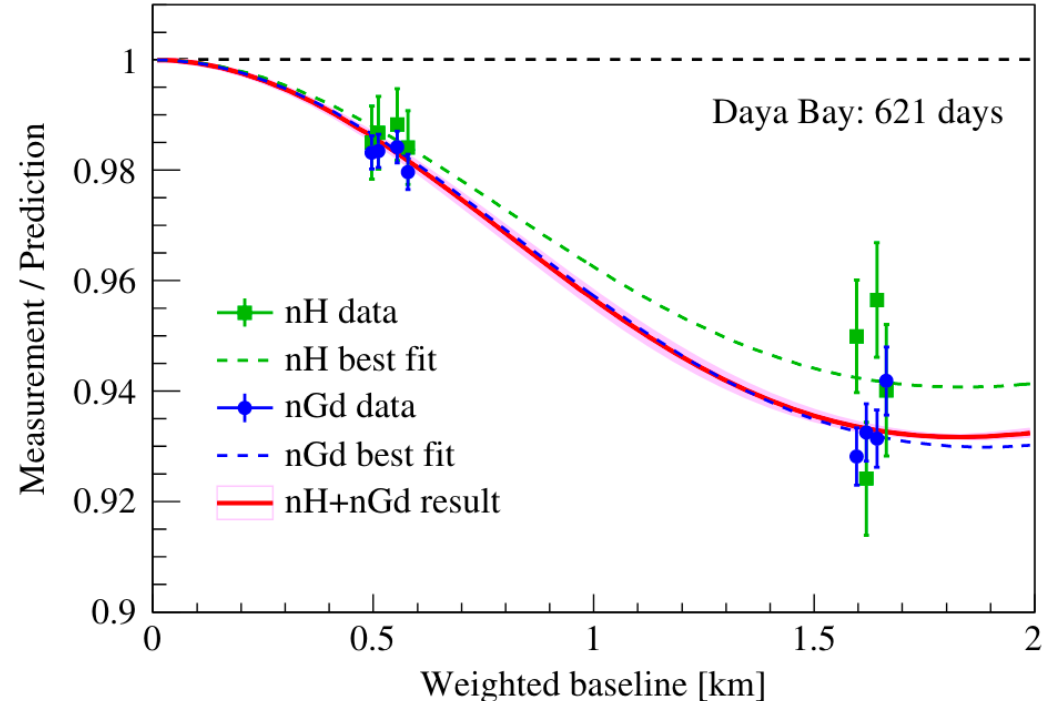
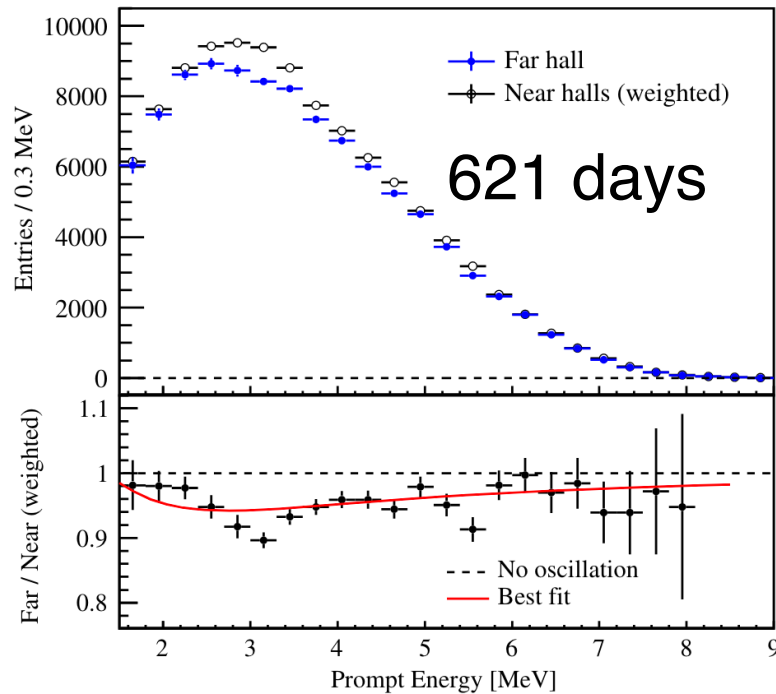
➤ *Kam-Biu will offer more details during his parallel talk this afternoon*



# $\sin^2 2\theta_{13}$ from nH-IBD analysis

- Independent  $\sin^2 2\theta_{13}$  measurement
- Challenging: much more low-energy backgrounds
  - Signal to background ratio is about 1:1 at the far hall
- Rate-only analysis result:  $\sin^2 2\theta_{13} = 0.071 \pm 0.011$
- Improved measurement is coming soon

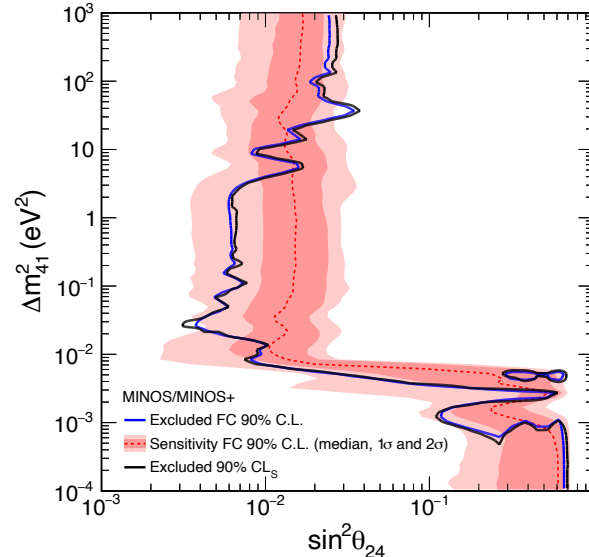
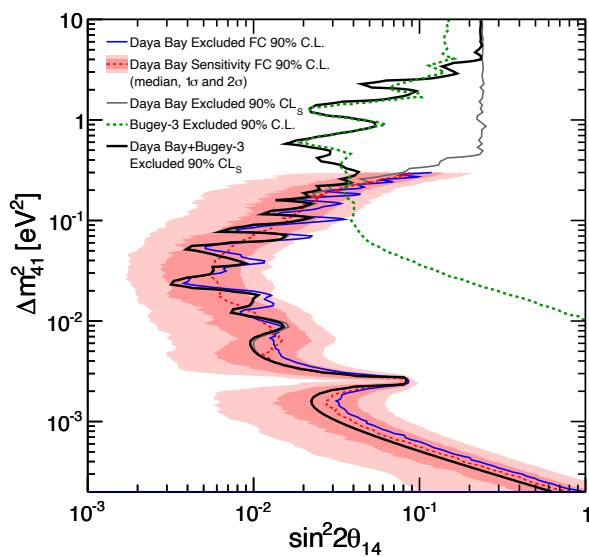
*PRD 93 072011 (2016)*







# Sterile Neutrino Searches at Daya Bay (and Combined with MINOS/MINOS+ & Bugey-3)



- Daya Bay has multiple baselines
- Daya Bay and MINOS are sensitive to  $\sim 0.1 \text{ eV}^2$  but different flavors
- Together, better sensitivity to the LSND result

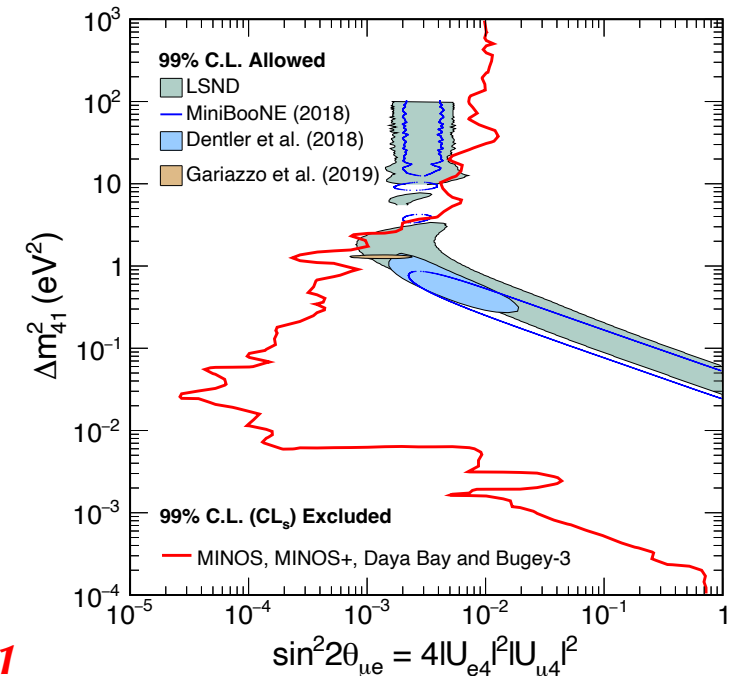
Appearance probability:

$$4|U_{e4}|^2|U_{\mu4}|^2 \sin^2 \left( \frac{\Delta m_{41}^2 L}{4E} \right)$$

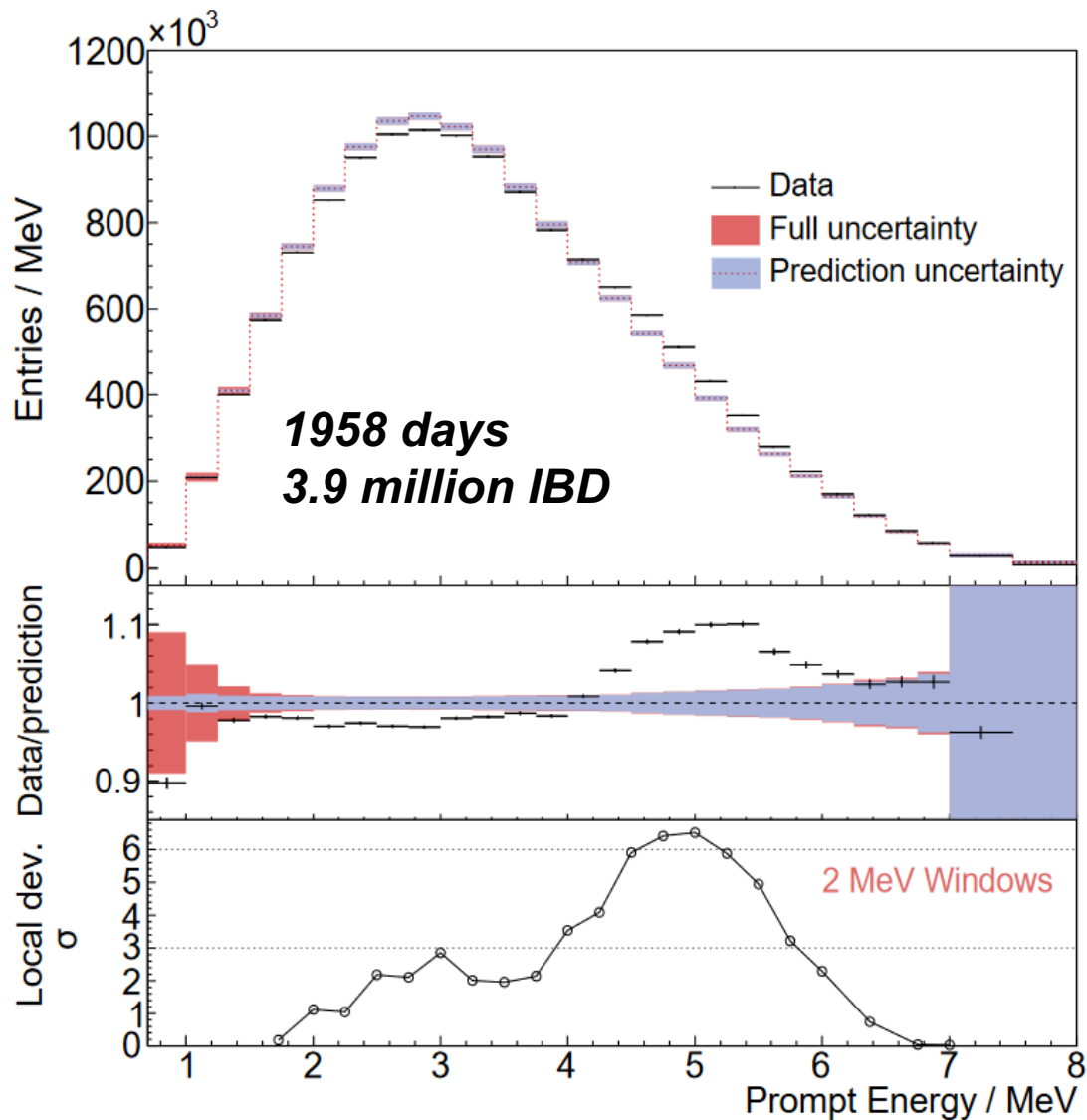
Where:

$$4|U_{e4}|^2|U_{\mu4}|^2 = \sin^2 2\theta_{14} \sin^2 \theta_{24} \equiv \sin^2 2\theta_{\mu e}$$

**For details, see *Daya Bay*, PRL125 (2020) 7, 071801  
PRL113 (2014) 141802, PRL117 (2016), PRL117 (2016) 15, 151801**



# Measuring the Reactor Antineutrinos Spectrum



- With 1958 days of data, Daya Bay has confirmed the discrepancy between 4-6 MeV (visible energy) with a  $\sim 6\sigma$  significance
- This discrepancy, the “Bump”, is not correlated with burn-up, i.e. the operation of reactors, or the operations of the Daya Bay detectors

• *For details, see PRL 123 (2019) 111801, PRL 116 (2016) 061801*

# Fuel Evolution and Responsible Fuel Components



- See *PRL 118 (2017) no.25, 251801* and *CPC, 2017, 41(1)* for details

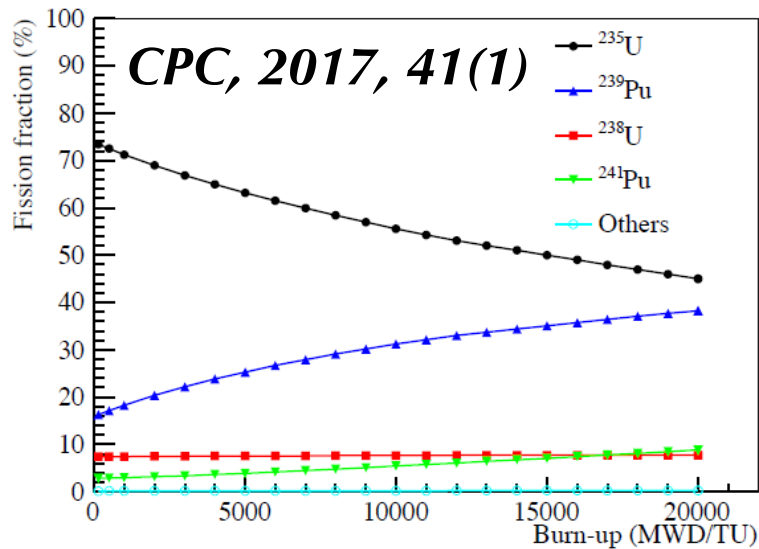
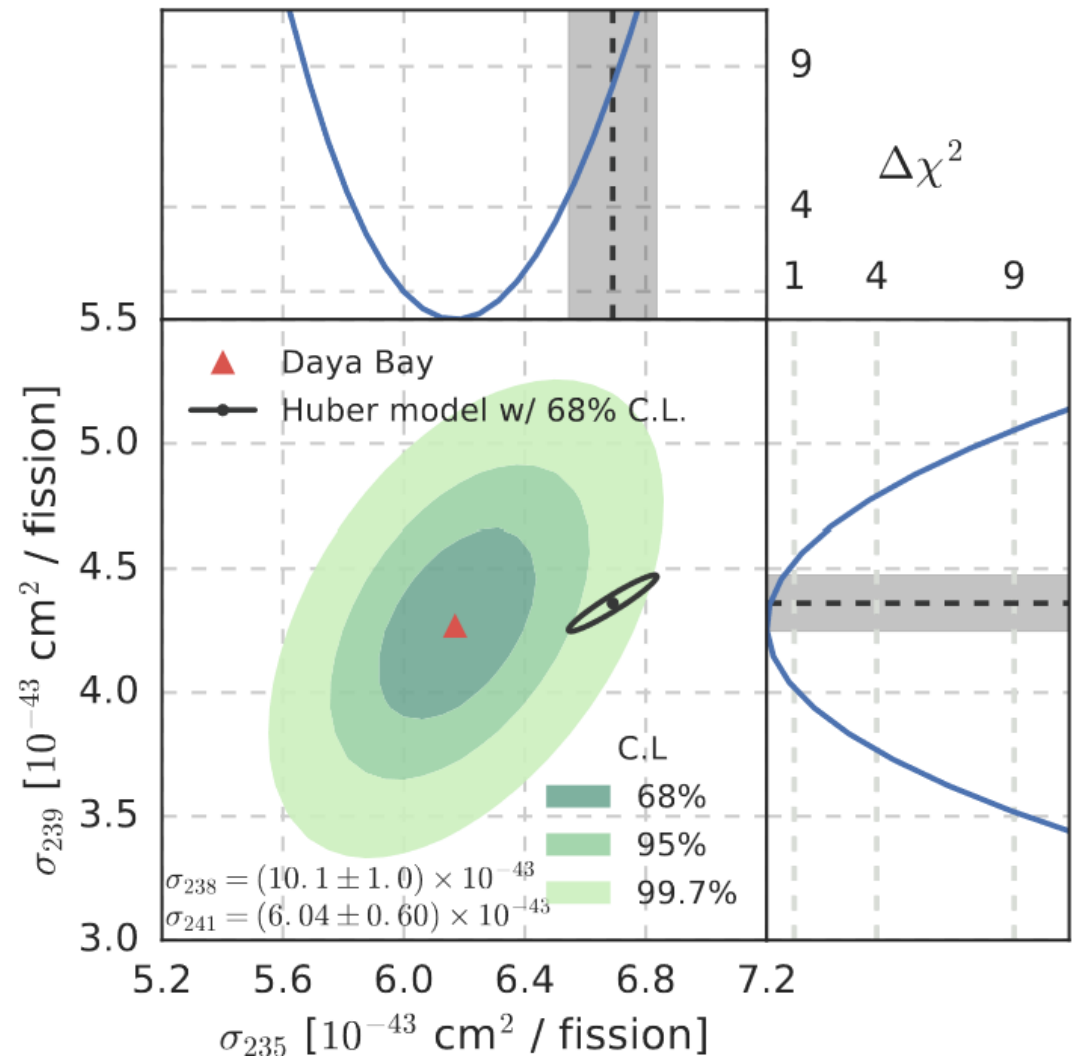
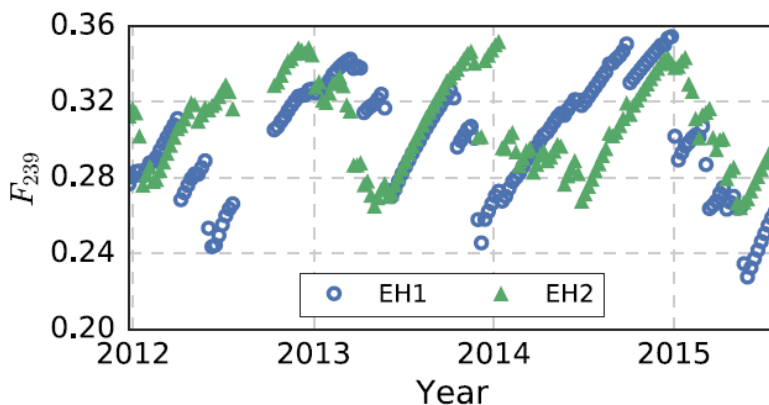


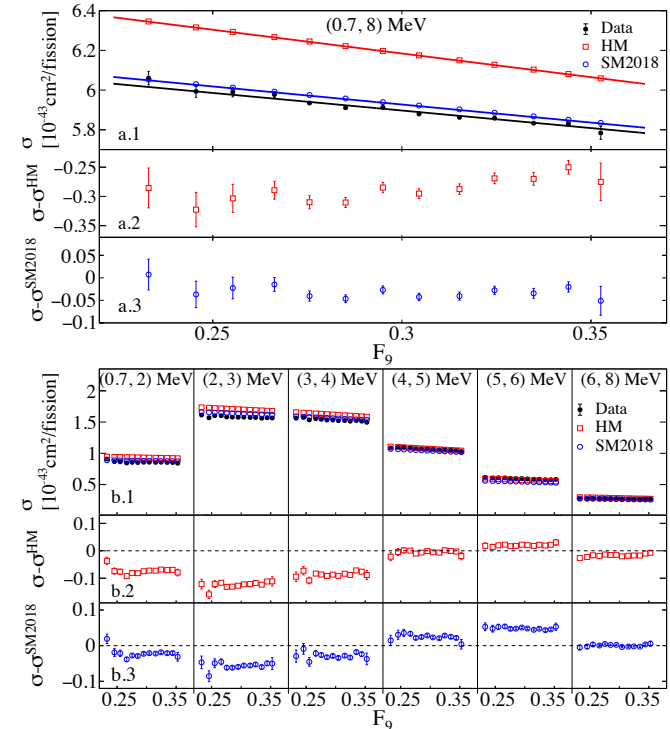
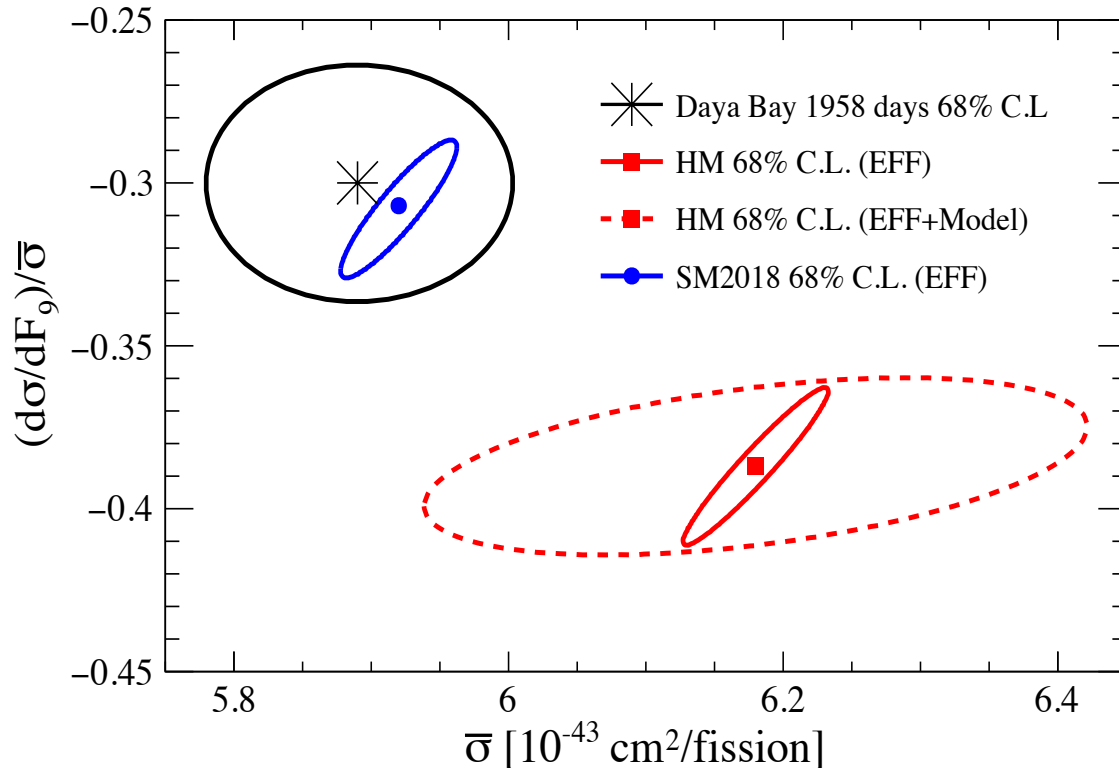
Fig. 4. Fission fractions of isotopes in reactor core D1 as a function of cycle burn-up from a simulation of a complete refueling cycle. Other isotopes contribute less than 0.3%.



*PRL 118 (2017) no.25, 251801*

# The Lates Fuel Evolution Analysis

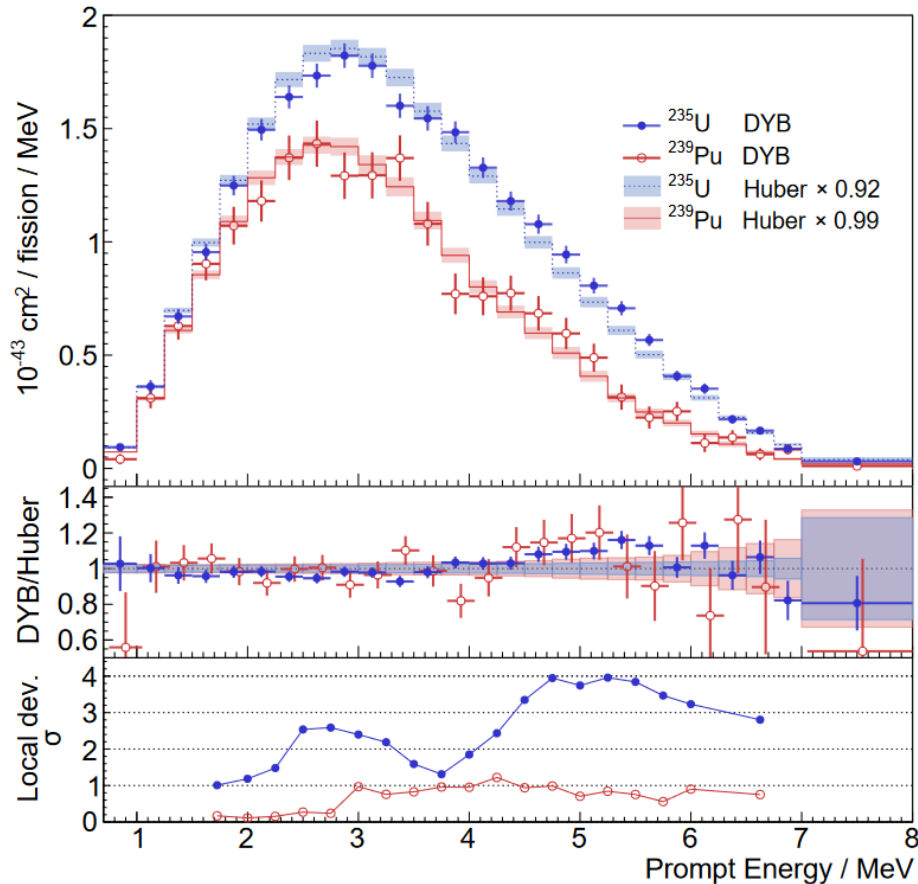
- **An improved analysis on fuel evolution by the Daya Bay Collaboration just released, see [arXiv:2210.01068](https://arxiv.org/abs/2210.01068)**



Analysis Improvements besides more statistics (1230 days  $\rightarrow$  1958 days)

- SM2018: a new summation method by M. Estienne *et al.*, PRL123, 022502 (2019)
- Better correlated and uncorrelated detector uncertainties
- Improved reactor related uncertainties
- Checking two characteristic variables: average neutrino yields and their evolution slope wrt.  $F_9$ , the  $^{239}\text{Pu}$  fraction bred within the reactor

# Decomposing Reactor Antineutrino Components



- The very first measurement of the  $^{235}\text{U}$  and  $^{239}\text{Pu}$  spectra at commercial reactors
- An excess, data over prediction, around 4-6 MeV for  $^{235}\text{U}$  is more pronounced but the  $^{239}\text{Pu}$  one is consistent with null bump

**$^{235}\text{U}$ : a  $4\sigma$  effect;  $^{239}\text{Pu}$ : a  $1.2\sigma$  effect**

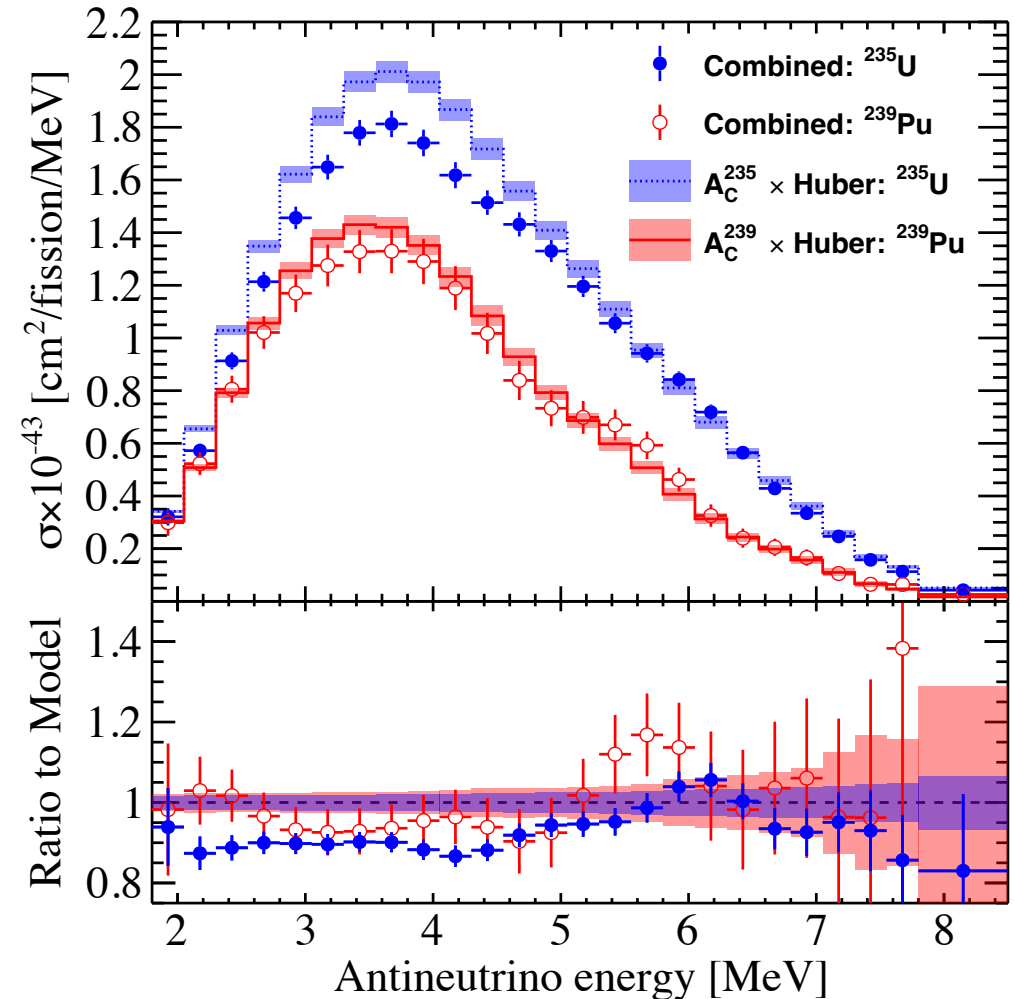
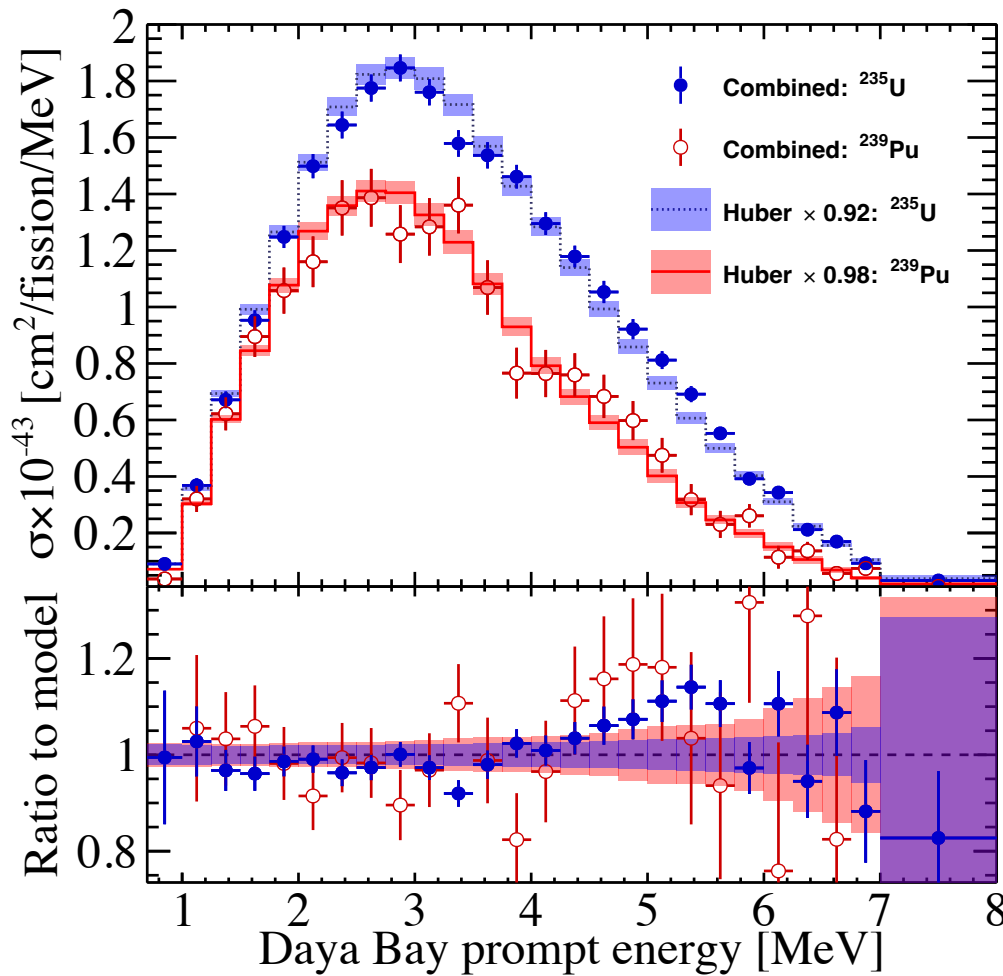
- *For details of the isotope decomposition analysis, see PRL 123 (2019) no.11, 111801*



# Combined Flux Analysis of Daya Bay and PROSPECT



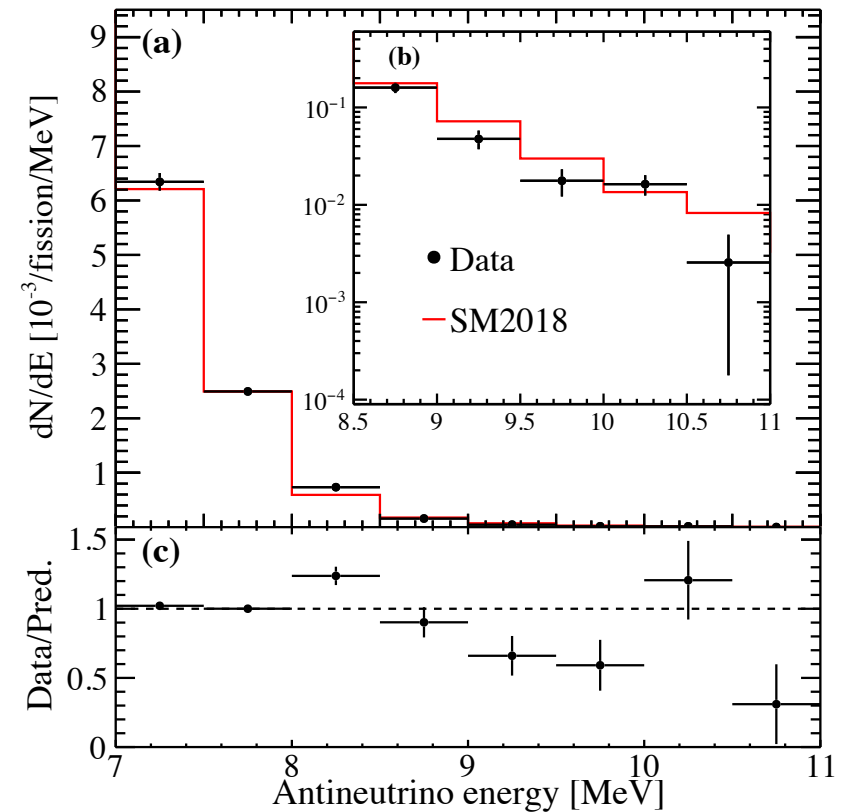
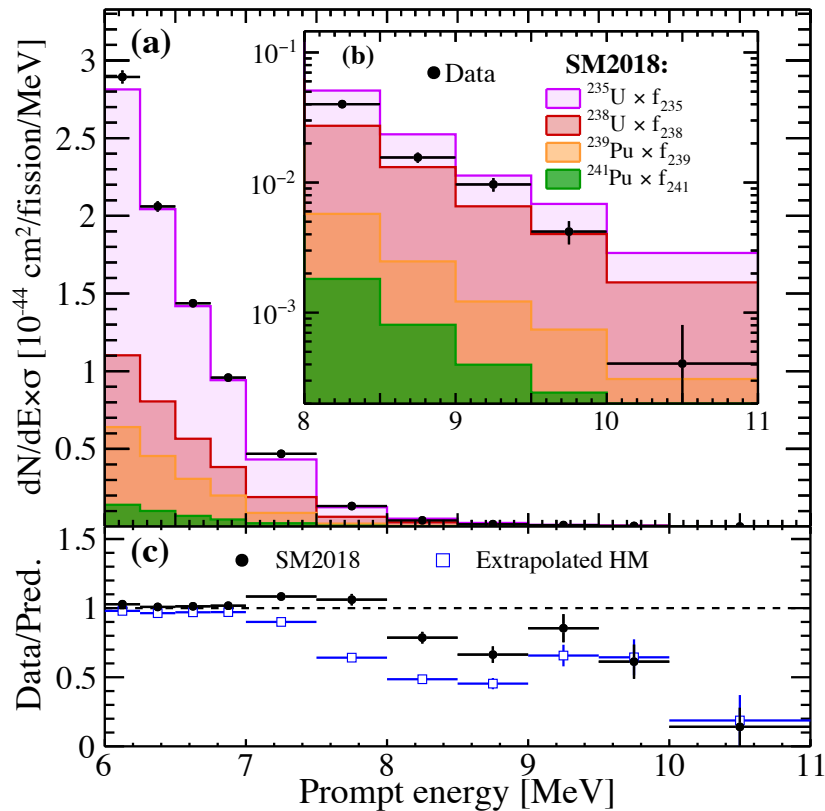
• *Daya Bay + PROSPECT Collaborations, see PRL 128 (2022) 8, 081801*



- First ever results: A HEU reactor + LEU reactors (commercial PWR reactors)
- $^{235}\text{U}$  flux improved to 3%; Degeneracy between U and Pu contributions reduced

# First Evidence of High-Energy Reactor Neutrinos

- Daya Bay discovers reactor neutrinos above 10MeV with a  $6.2\sigma$  significance for the first time
- A deficit of 29% in the high-E region (8-11MeV) is observed compared with the SM2018 ab-initio prediction
- The first direct observation of antineutrinos from several high- $Q_\beta$  isotopes in commercial reactors

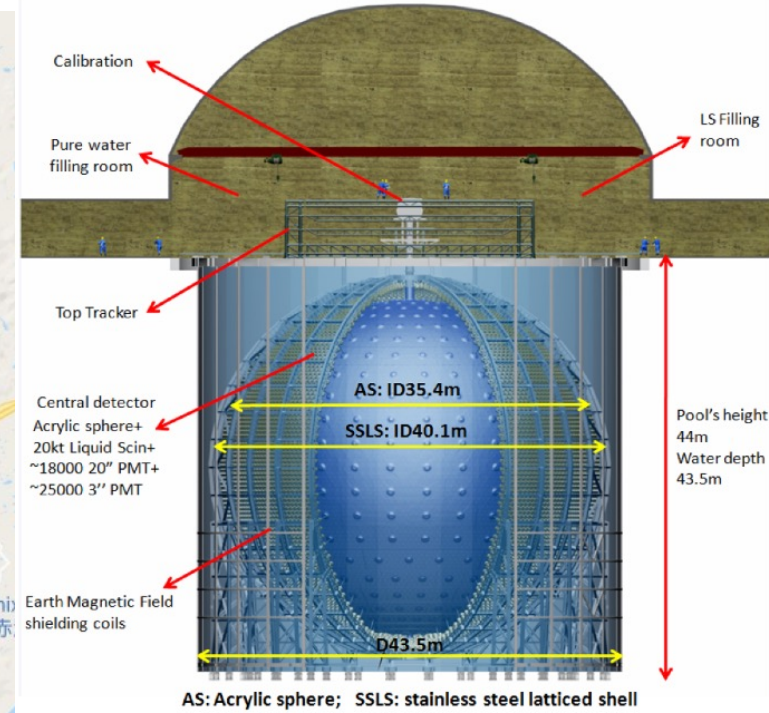
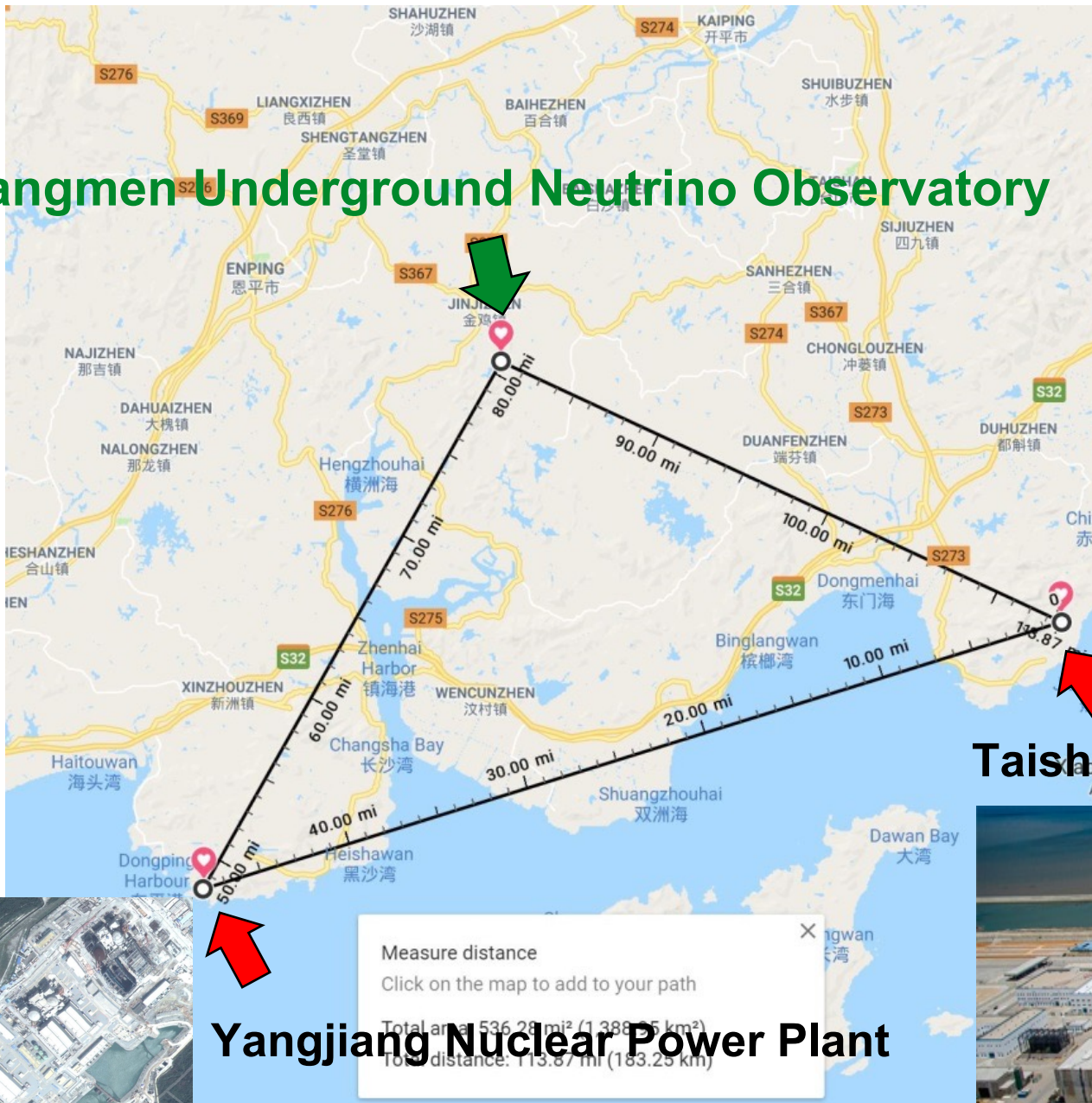


- **For details, see *PRL 129 (2022) 4, 041801***

# Future Reactor Neutrino: JUNO for Neutrino Mass Ordering



## Jiangmen Underground Neutrino Observatory



## Taishan Nuclear Power Plant



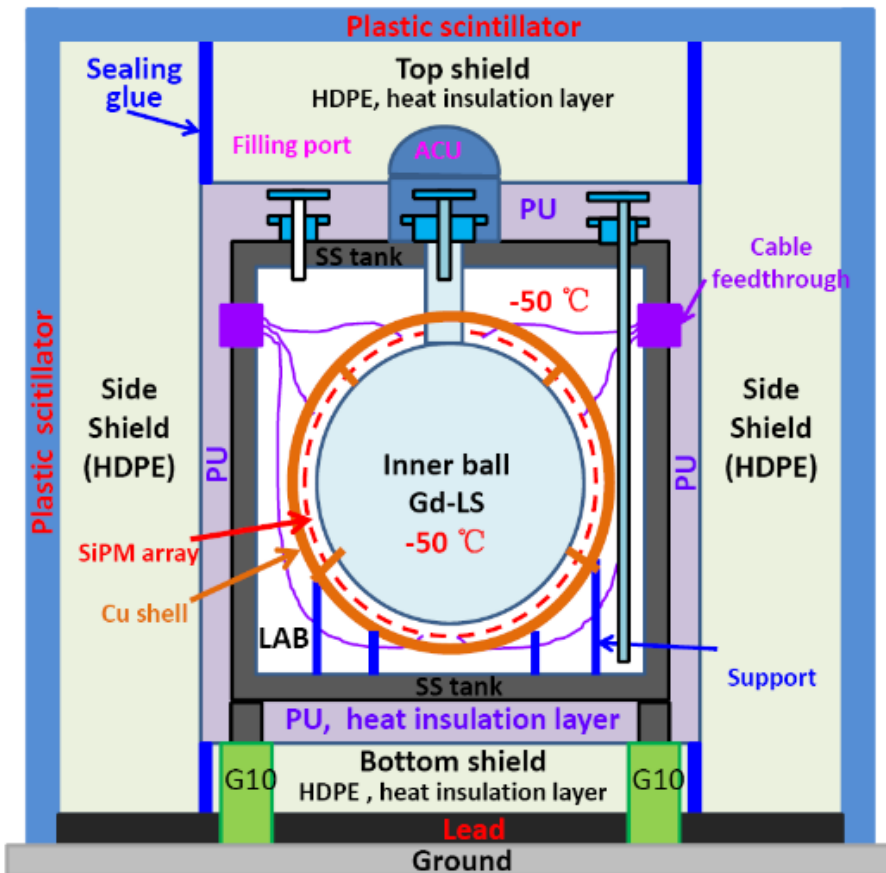
## Yangjiang Nuclear Power Plant





# JUNO-TAO: A Satellite Experiment of JUNO

- Taishan Antineutrino Observatory (TAO), a ton-level, high energy resolution LS detector, at 30-35 m from a 4.6 GW<sub>th</sub> core, a satellite exp. of JUNO
- 2.6 ton Gd\_LS | acrylic vessel | SiPM and Cu shell| Cryogenic vessel| water or HDPE



- ◆ TAO will be used to measure reactor neutrino spectrum
- ◆ Full coverage of SiPM with PDE > 50%  
Operate at -50 °C (lower SiPM dark noise)
  - 4500 p.e./MeV →  $1.5\% \sqrt{E(\text{MeV})}$
- ◆ Taishan Nuclear Power Plant  
2000 IBD/day (4000)

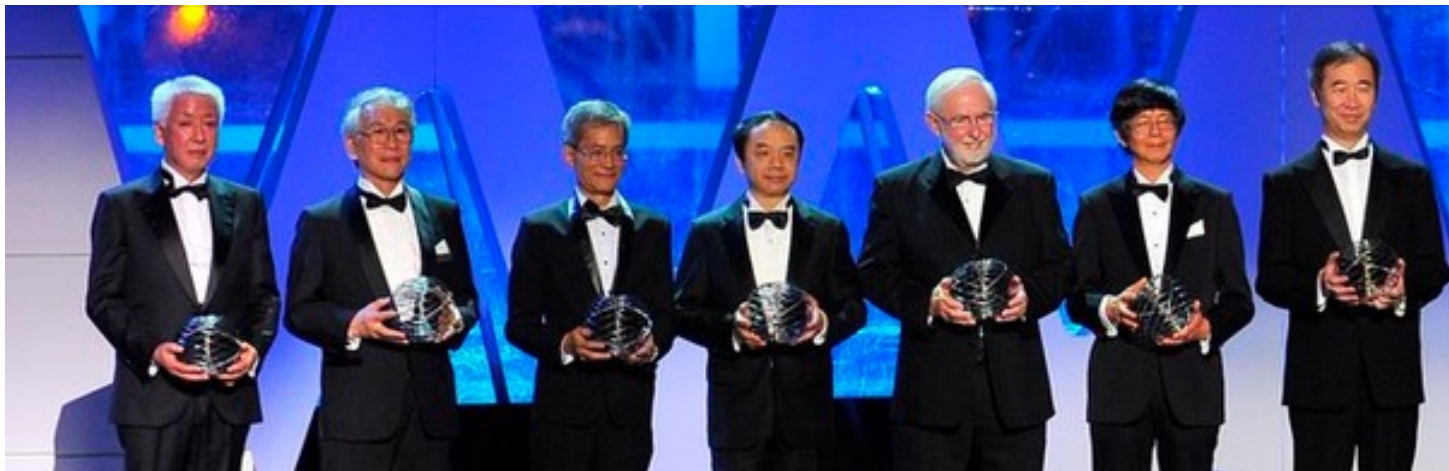




# Summary and Conclusion

- **Reactor neutrino has played irreplaceable roles in neutrino studies**
- **Daya Bay has made the most precise measurement of  $\sin^2 2\theta_{13}$ , which makes**
  - **mass ordering resolution possible using reactor antineutrinos; CP phase measurement possible**
- **Daya Bay has made precise measurements of reactor antineutrino flux, its spectrum and contributions of the 2 major fission isotopes**
  - **Confirms Reactor Antineutrino Anomaly and the spectrum discrepancy**
  - **Both direct search (combined) and fuel evolution analysis disfavor sterile neutrino assumptions**
  - **Provide the best flux measurements of commercial reactors for future reactor neutrino experiments such as JUNO**
  - **“Repaying” the nuclear energy community: a different perspective for nuclear data studies relevant to reactor physics**
- **Daya Bay data will be open to the scientific community: proposals welcome!**

***Thanks for your Attention!***





- ❖ SYSU was founded in 1924 by Dr. Sun Yat-sen
- ❖ One of the top 10 comprehensive universities



- 5 campuses in the 3 most important cities in Guangdong province: Guangzhou, Shenzhen, Zhuhai
- Well connected by air, land and water - -- <2 hours to any of the 5 international airports.



# Welcome to Sun Yat-sen University (Zhuhai Campus) for **Weak Interactions and Neutrinos 2023: July 3-8**



Guangzhou South Campus



Guangzhou East Campus



Guangzhou North Campus



Shenzhen Campus

**Wushunde Academic Center and  
Multiple Auditoriums (Venue of ~300  
plenary and multiple parallel sessions)**



**Zhuhai Campus**





# The Latest Daya Bay Reactor Neutrino Data Set

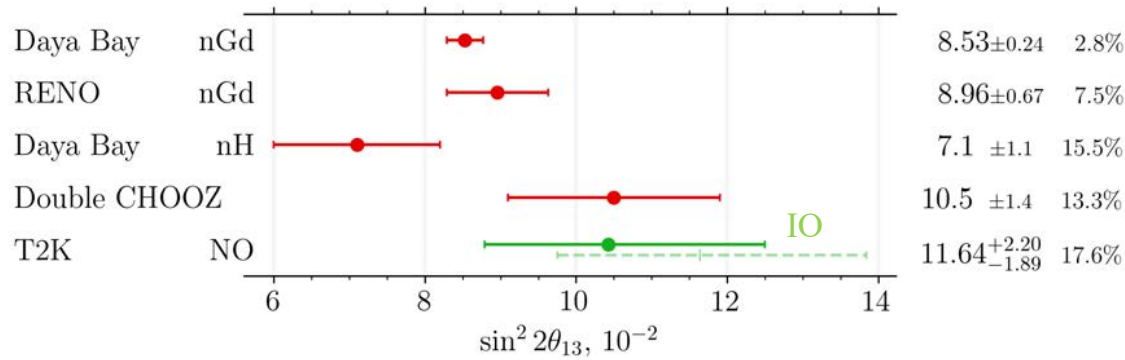
- Summary of the Daya Bay data sample:

TABLE I. Summary of IBD signal and background. Rates are corrected for the muon veto and multiplicity selection efficiencies  $\varepsilon_\mu \times \varepsilon_m$ . The sum of the fast neutron and muon-x background rates is reported as “Fast n + muon-x”. The AD numbering scheme reflects the time order of AD fabrication and deployment.

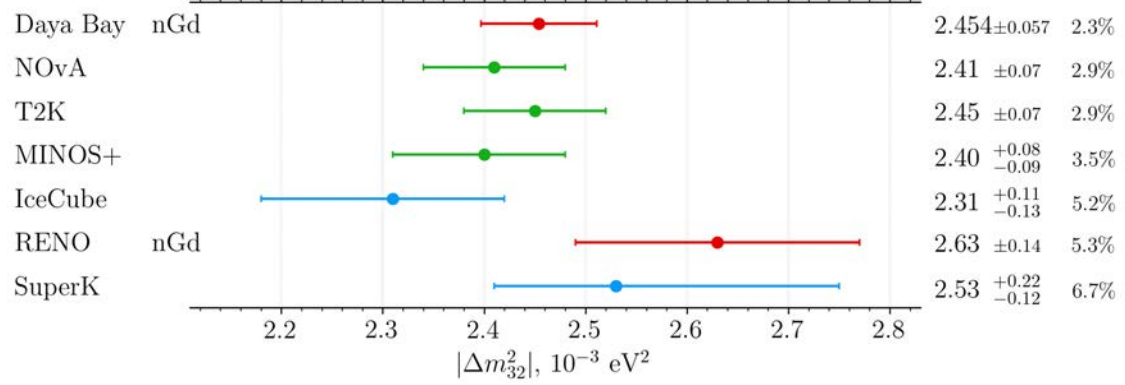
	EH1		EH2		EH3			
	AD1	AD2	AD3	AD8	AD4	AD5	AD6	AD7
$\bar{\nu}_e$ candidates	794335	1442475	1328301	1216593	194949	195369	193334	180762
DAQ live time [days]	1535.111	2686.110	2689.880	2502.816	2689.156	2689.156	2689.156	2501.531
$\varepsilon_\mu \times \varepsilon_m$	0.7743	0.7716	0.8127	0.8105	0.9513	0.9514	0.9512	0.9513
Accidentals [ $\text{day}^{-1}$ ]	$7.11 \pm 0.01$	$6.76 \pm 0.01$	$5.00 \pm 0.00$	$4.85 \pm 0.01$	$0.80 \pm 0.00$	$0.77 \pm 0.00$	$0.79 \pm 0.00$	$0.66 \pm 0.00$
Fast n + muon-x [ $\text{day}^{-1}$ ]	$0.83 \pm 0.17$	$0.96 \pm 0.19$	$0.56 \pm 0.11$	$0.56 \pm 0.11$	$0.05 \pm 0.01$	$0.05 \pm 0.01$	$0.05 \pm 0.01$	$0.05 \pm 0.01$
${}^9\text{Li}/{}^8\text{He}$ [ $\text{AD}^{-1} \text{ day}^{-1}$ ]	$2.92 \pm 0.78$		$2.45 \pm 0.57$		$0.26 \pm 0.04$			
${}^{241}\text{Am}-{}^{13}\text{C}$ [ $\text{day}^{-1}$ ]	$0.16 \pm 0.07$	$0.13 \pm 0.06$	$0.12 \pm 0.05$	$0.11 \pm 0.05$	$0.04 \pm 0.02$	$0.04 \pm 0.02$	$0.04 \pm 0.02$	$0.03 \pm 0.01$
${}^{13}\text{C}(\alpha, n){}^{16}\text{O}$ [ $\text{day}^{-1}$ ]	$0.08 \pm 0.04$	$0.06 \pm 0.03$	$0.04 \pm 0.02$	$0.06 \pm 0.03$	$0.04 \pm 0.02$	$0.04 \pm 0.02$	$0.03 \pm 0.02$	$0.04 \pm 0.02$
$\bar{\nu}_e$ rate [ $\text{day}^{-1}$ ]	$657.16 \pm 1.10$	$685.13 \pm 1.00$	$599.47 \pm 0.78$	$591.71 \pm 0.79$	$75.02 \pm 0.18$	$75.21 \pm 0.18$	$74.41 \pm 0.18$	$74.93 \pm 0.18$

- Largest Reactor Neutrino Data Ever:
  - More than **5.5 million IBDs (~0.7 million at far site)**

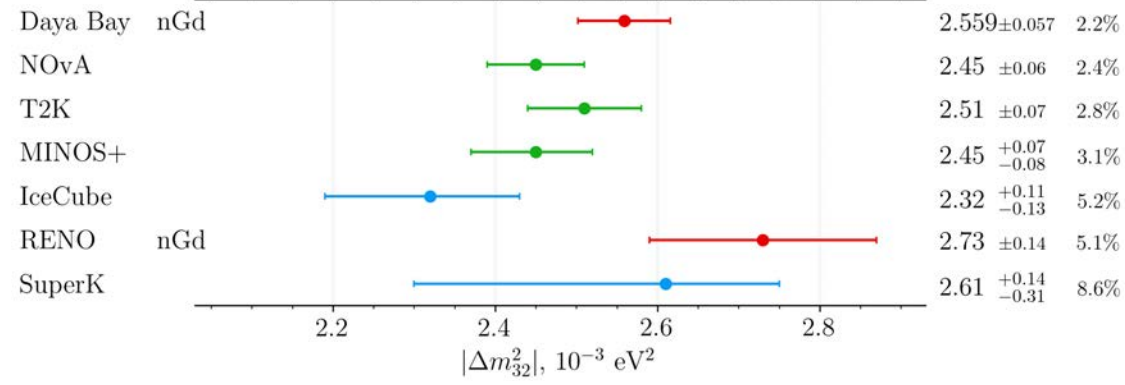
# Daya Bay Oscillation Results and Global Comparison



Normal mass ordering

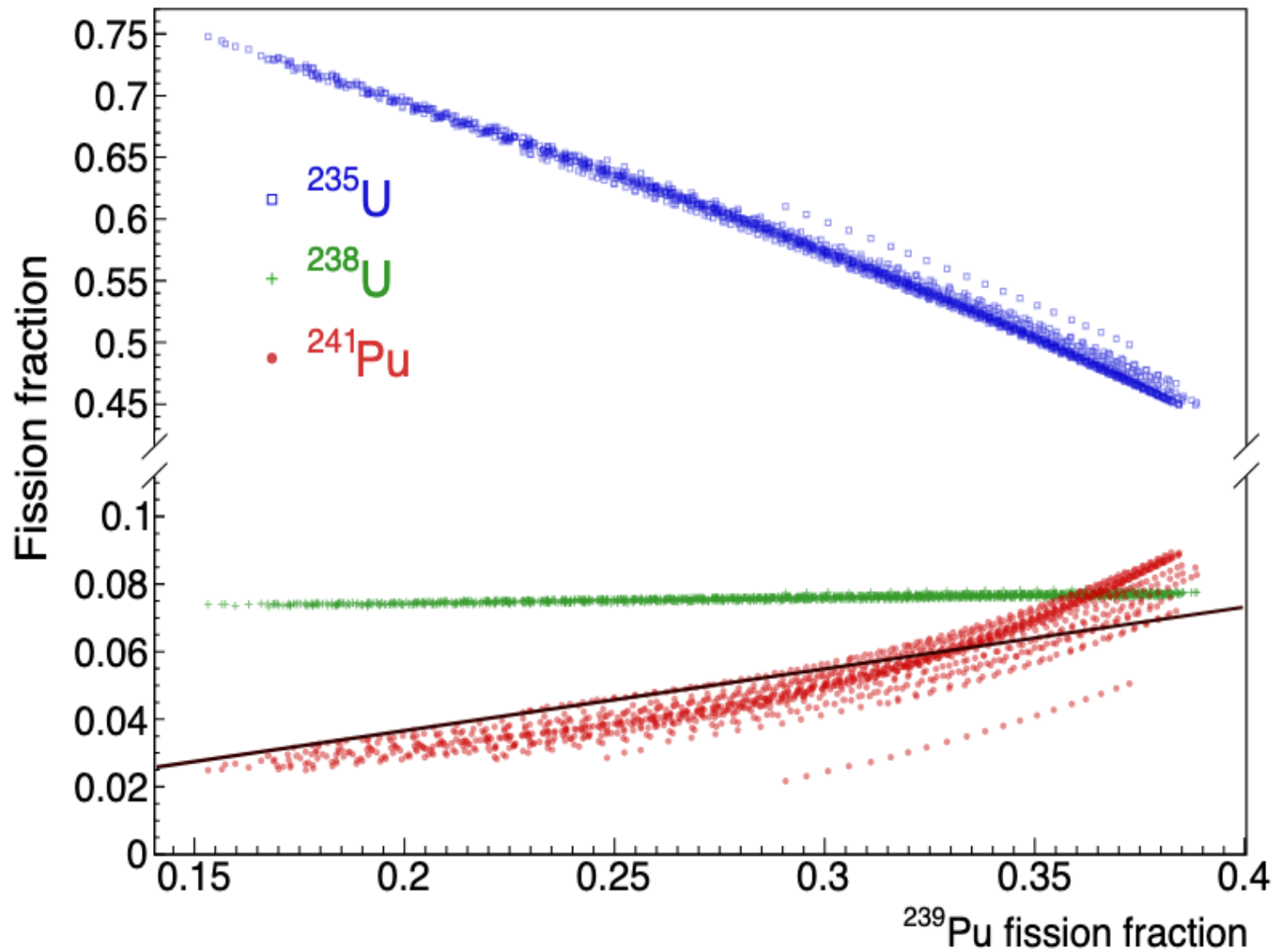


Inverted mass ordering





# Fission Fraction Evolution



# Sterile Neutrino Search Advantages of Daya Bay

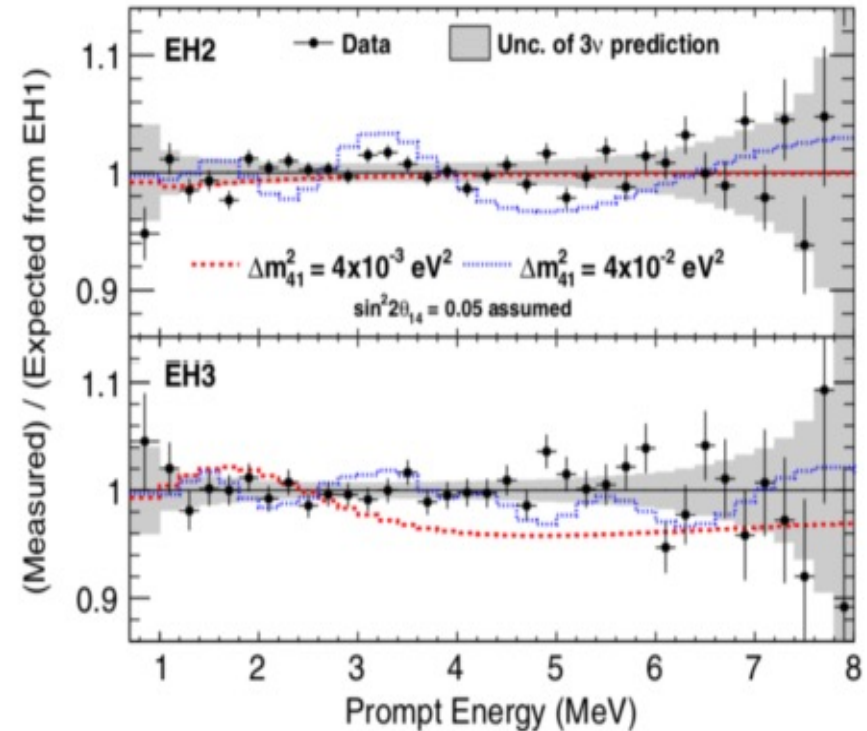
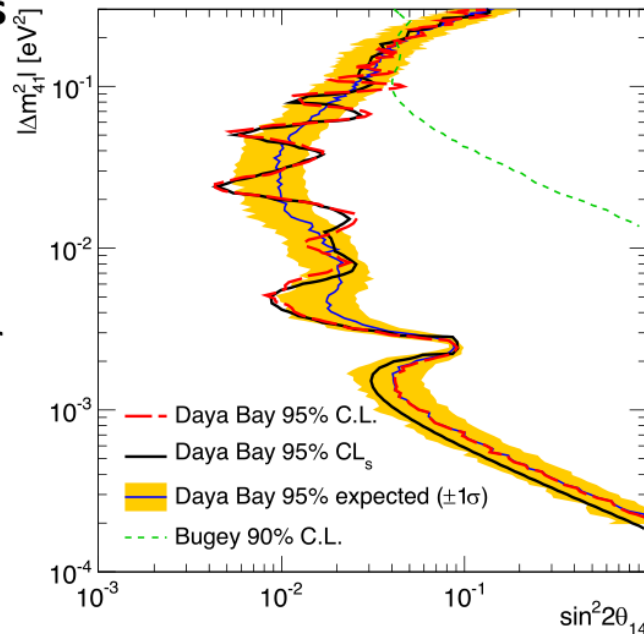
- Unique multi-baseline opportunity

## Exclusion Contours

- Two-hypothesis test for  $3\nu$  and  $3+1-\nu$
- Gaussian CLs<sup>[4]</sup> approach to set exclusion contour

$$CL_s = \frac{1 - p_1}{1 - p_0}$$

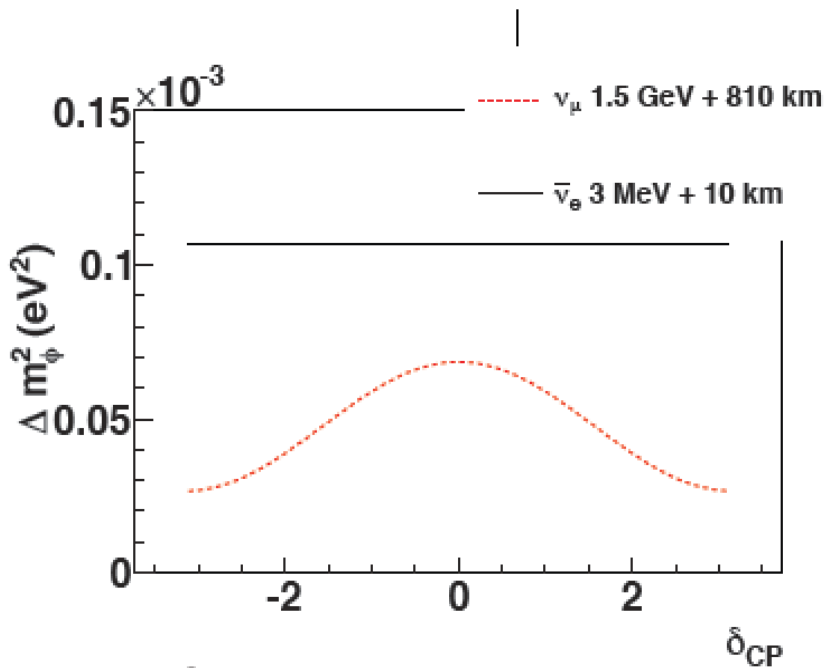
$$p_0: 3\nu \quad p_1: 3+1-\nu$$



# e- / $\mu$ -Flavor “Senses” Mass Ordering Differently

A fair question to ask: Why care  $|\Delta m_{ee}^2|$  from reactor experiments?

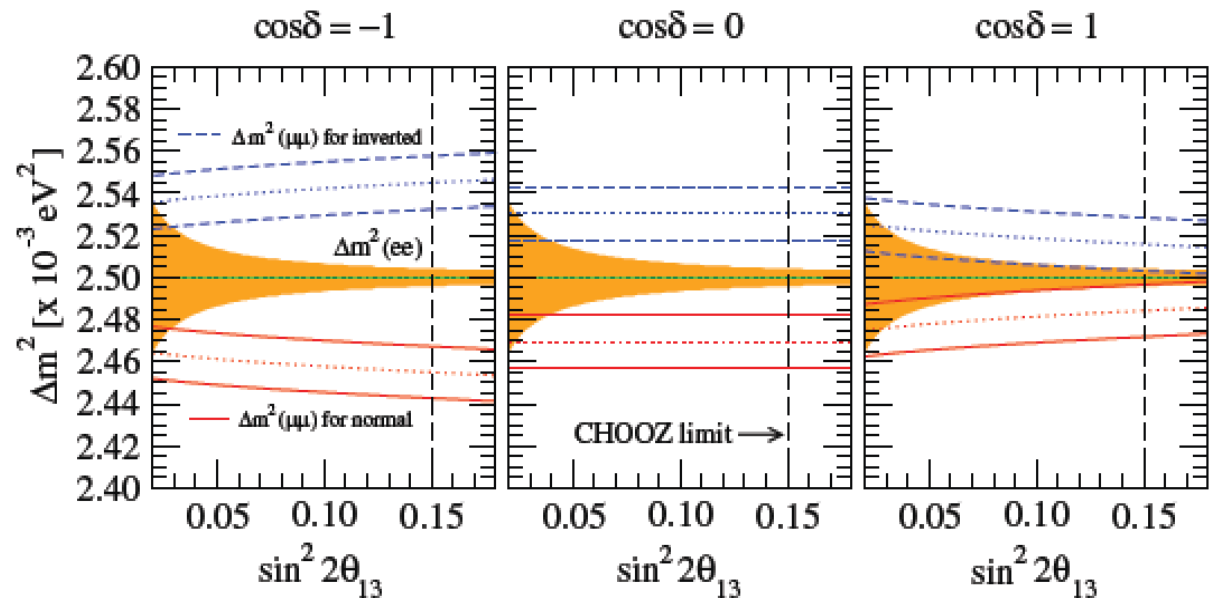
$$P_{\nu_\mu \rightarrow \nu_\mu} = 1 - P_{21}^\mu - \cos^2 \theta_{13} \sin^2 2\theta_{23} \sin^2 \frac{(\Delta m_{32}^2 \pm \phi)L}{4E}$$



*Qian et al, PRD87(2013)3, 033005*

FIG. 6: The dependence of effective mass-squared difference  $\Delta m_{ee\phi}^2$  (solid line) and  $\Delta m_{\mu\mu\phi}^2$  (dotted line) w.r.t. the value of  $\delta_{CP}$  for  $\bar{\nu}_e$  and  $\nu_\mu$  disappearance measurements, respectively.

**Impractical: Need 1% accuracy!**



*Minakata et al PRD74(2006), 053008*

**Also See: Zhang&Ma, arXiv:1310.4443/  
Mod. Phys. Lett. A29 (2014) 1450096**



# Global Efforts Resolving $\nu$ Mass Hierarchy



Source / Principle	Matter Effect	Interference of Solar&Atm Osc. Terms	Collective Oscillation	Constraining Total Mass or Effective Mass
Atmospheric $\nu$	Super-K, Hyper-K, IceCube PINGU, ICAL/INO, ORCA, DUNE	Atm $\nu_\mu$ + JUNO		
Beam $\nu_\mu$	T2K, NOvA, T2HKK, DUNE	Beam $\nu_\mu$ + JUNO		
Reactor $\nu_e$		JUNO, JUNO+Beam $\nu_\mu$		
Supernova Burst $\nu$			Super-K, Hyper-K, IceCube PINGU, ORCA, DUNE, JUNO	
Interplay of Measurements				Cosmo. Data, KATRIN, Proj-8, $0\nu\beta\beta$

# Known $\theta_{13}$ Enables Neutrino Mass Hierarchy at Reactors

$$P_{\bar{\nu}_e \rightarrow \bar{\nu}_e} = 1 - \cos^4 \theta_{13} \sin^2 2\theta_{12} \sin^2 \Delta_{21}$$

$$- \sin^2 2\theta_{13} (\cos^2 \theta_{12} \sin^2 \Delta_{31} + \sin^2 \theta_{12} \sin^2 \Delta_{32})$$

*Petcov&Piai, Phys. Lett. B533 (2002) 94-106*

