



A renormalizable left-right symmetric model with low scale seesaw mechanisms

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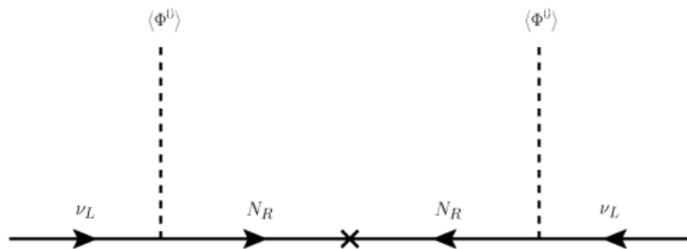
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Some reasons to extend the SM are:

- 1 SM charged fermion mass hierarchy.
- 2 Tiny masses of light active neutrinos.
- 3 CKM and PMNS matrices very close and very different to the identity matrix, respectively.
- 4 Dark matter.
- 5 Number of SM fermion families.
- 6 Lepton asymmetry of the Universe.
- 7 $(g - 2)_\mu$.
- 8 Tiny LFV signals several orders of magnitude below experimental sensitivity.



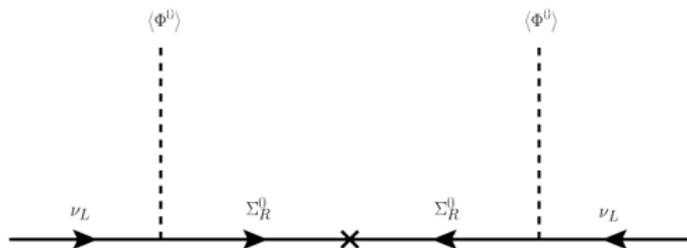
Type I seesaw

$$LHN \quad 2 \otimes 2 \otimes 1$$

Minkowski 1977, Gellman, Ramond, Slansky 1980

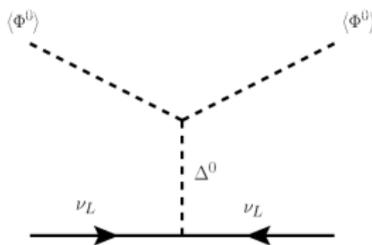
Glashow, Yanagida 1979, Mohapatra, Senjanovic 1980

Lazarides Shafi Weterrich 1981, Schechter-Valle 1980 and 1982



Type III seesaw

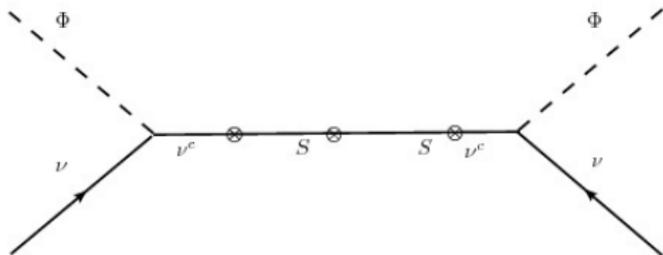
$$LH\Sigma \quad 2 \otimes 2 \otimes 3$$



Type II seesaw

$$L\Delta L \quad 2 \otimes 3 \otimes 2$$

Schechter-Valle 1980 and 1982



Inverse seesaw

$$-\mathcal{L}_{mass}^{(\nu)} = \frac{1}{2} \begin{pmatrix} \overline{\nu}_L^c & \overline{N}_R & \overline{S}_R \end{pmatrix} \mathbf{M}_\nu \begin{pmatrix} \nu_L \\ N_R^c \\ S_R^c \end{pmatrix} + H.c$$

$$\mathbf{M}_\nu = \begin{pmatrix} 0_{3 \times 3} & \mathbf{M}_1 & \mathbf{M}_L \\ \mathbf{M}_1^T & 0_{3 \times 3} & \mathbf{M}_2 \\ \mathbf{M}_L^T & \mathbf{M}_2^T & \mu \end{pmatrix}$$

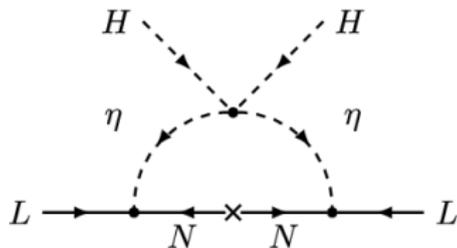
$$\mathbf{M}_L = 0_{3 \times 3}$$

$$Q_{\nu_L}^{U(1)_L} = Q_{S_R}^{U(1)_L} = -Q_{N_R}^{U(1)_L} = 1$$

$$\tilde{\mathbf{M}}_\nu = \mathbf{M}_1 (\mathbf{M}_2^T)^{-1} \mu \mathbf{M}_2^{-1} \mathbf{M}_1^T$$

$$\mathbf{M}_\nu^{(1)} = -\frac{1}{2} (\mathbf{M}_2 + \mathbf{M}_2^T) + \frac{1}{2} \mu$$

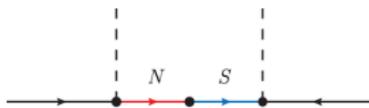
$$\mathbf{M}_\nu^{(2)} = \frac{1}{2} (\mathbf{M}_2 + \mathbf{M}_2^T) + \frac{1}{2} \mu$$



One loop Ma radiative seesaw model

η and N are odd under a preserved Z_2

$$L \tilde{\eta} N, \frac{\lambda_5}{2} (H^+ \cdot \eta)^2 + h.c$$



Linear seesaw:

$$\mu = 0_{3 \times 3}$$

$$\tilde{\mathbf{M}}_\nu = -\mathbf{M}_L \mathbf{M}_2^{-1} \mathbf{M}_1^T - \mathbf{M}_1 (\mathbf{M}_2^T)^{-1} \mathbf{M}_L^T$$

An extended left-right symmetric model.

The main features of the extended LR symmetric model are:

- 1 The top quark gets its mass from a renormalizable Yukawa interaction.
- 2 The bottom, strange and charm quarks, as well as for the tau and muon leptons acquire their masses from a tree level Universal Seesaw mechanism.
- 3 The first generation SM charged fermions acquire one loop level masses.
- 4 The tiny neutrino masses are generated from an inverse seesaw mechanism at one loop level.

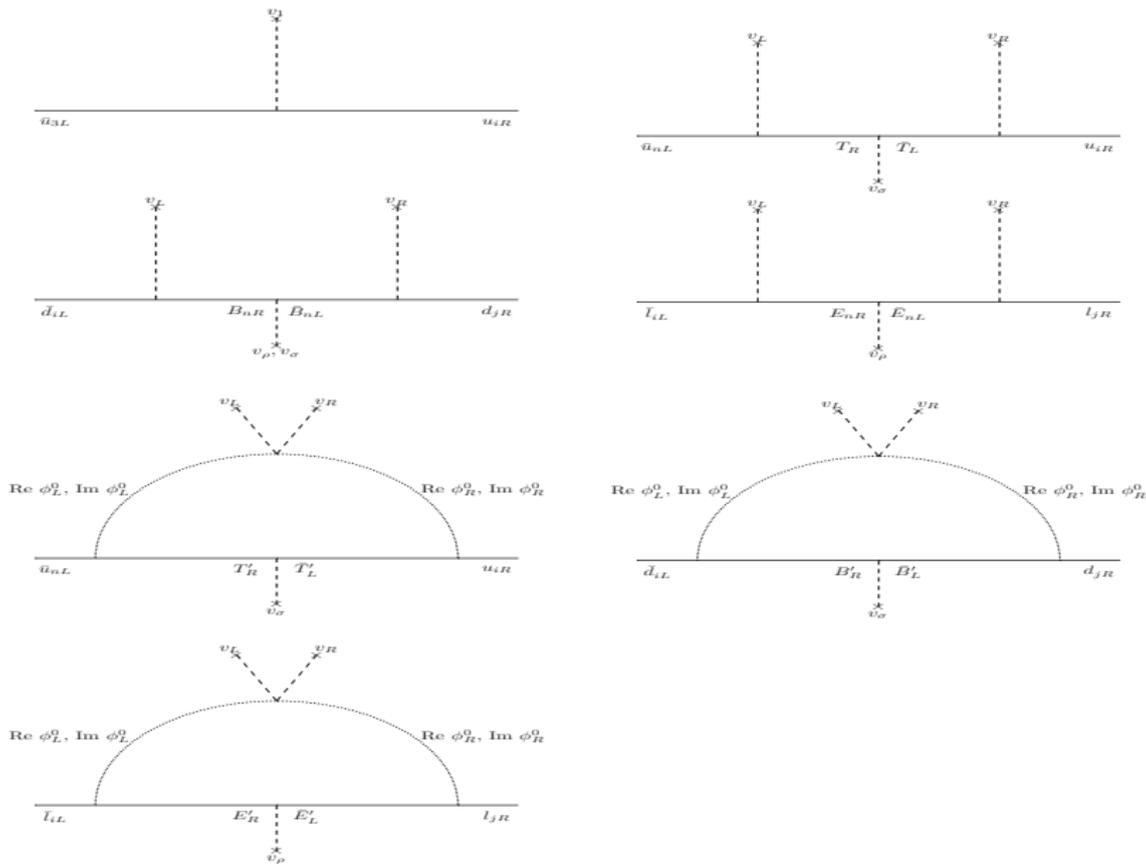


Figure: Feynman diagrams contributing to the entries of the SM charged fermion mass matrices. $n = 1, 2, i, j = 1, 2, 3$.

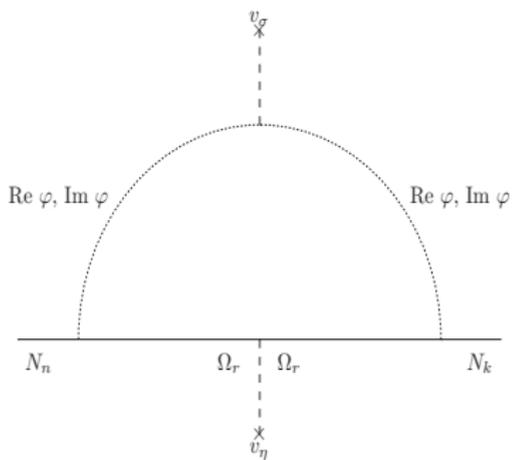


Figure: One-loop Feynman diagram contributing to the Majorana neutrino mass submatrix μ . Here, $n, k = 1, 2, 3$ and $r = 1, 2$.

$$\begin{aligned}
\mathcal{G} &= SU(3)_C \times SU(2)_L \times SU(2)_R \times U(1)_{B-L} \times Z_4^{(1)} \times Z_4^{(2)} \\
&\quad \Downarrow v_\sigma, v_\eta, v_\rho \gg v_R \\
&SU(3)_C \times SU(2)_L \times SU(2)_R \times U(1)_{B-L} \times Z_2 \\
&\quad \Downarrow v_R \sim \mathcal{O}(10) \text{ TeV} \\
&SU(3)_C \times SU(2)_L \times U(1)_Y \times Z_2 \\
&\quad \Downarrow v_1, v_L \\
&SU(3)_C \otimes U(1)_Q \times Z_2 \tag{1}
\end{aligned}$$

The $Z_4^{(1)}$ symmetry is completely broken, whereas the $Z_4^{(2)}$ symmetry is broken down to the preserved Z_2 symmetry.

	Q_{nL}	Q_{3L}	Q_{iR}	L_{iL}	L_{iR}	T_L	T_R	T'_L	T'_R	B_{nL}	B_{1R}	B_{2R}	B'_L	B'_R	E_{nL}	E_{nR}	E'_L	E'_R	N_{iR}	Ω_{nR}
$SU(3)_C$	3	3	3	1	1	3	3	3	3	3	3	3	3	3	1	1	1	1	1	1
$SU(2)_L$	2	2	1	2	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
$SU(2)_R$	1	1	2	1	2	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
$U(1)_{B-L}$	$\frac{1}{3}$	$\frac{1}{3}$	$\frac{1}{3}$	-1	-1	$\frac{4}{3}$	$\frac{4}{3}$	$\frac{4}{3}$	$\frac{4}{3}$	$-\frac{2}{3}$	$-\frac{2}{3}$	$-\frac{2}{3}$	$-\frac{2}{3}$	$-\frac{2}{3}$	-2	-2	-2	-2	0	0
$Z_4^{(1)}$	-1	i	1	1	$-i$	1	1	1	1	1	$-i$	1	1	1	$-i$	-1	$-i$	-1	i	$-i$
$Z_4^{(2)}$	-1	-1	1	i	$-i$	1	-1	$-i$	i	1	-1	-1	i	$-i$	$-i$	i	1	-1	i	1

Table: Fermion assignments under

$SU(3)_C \times SU(2)_L \times SU(2)_R \times U(1)_{B-L} \times Z_4^{(1)} \times Z_4^{(2)}$. Here $i = 1, 2, 3$ and $n = 1, 2$

	Φ	χ_L	χ_R	ϕ_L	ϕ_R	φ	σ	η	ρ
$SU(3)_C$	1	1	1	1	1	1	1	1	1
$SU(2)_L$	2	2	1	2	1	1	1	1	1
$SU(2)_R$	2	1	2	1	2	1	1	1	1
$U(1)_{B-L}$	0	1	1	1	1	0	0	0	0
$Z_4^{(1)}$	i	-1	1	-1	1	1	1	-1	i
$Z_4^{(2)}$	-1	1	1	$-i$	$-i$	i	-1	1	-1

Table: Scalar assignments under

$SU(3)_C \times SU(2)_L \times SU(2)_R \times U(1)_{B-L} \times Z_4^{(1)} \times Z_4^{(2)}$.

The scalar dark matter candidate is the lightest among the $Re\varphi$, $Im\varphi$, $Re\phi_L^0$, $Re\phi_R^0$, $Im\phi_L^0$ and $Im\phi_R^0$ fields. The fermionic dark matter candidate is the lightest among the right handed Majorana neutrinos N_{iR} ($i = 1, 2, 3$).

The vacuum expectation values (VEVs) of the scalars Φ , χ_L and χ_R are:

$$\langle \Phi \rangle = \begin{pmatrix} v_1 & 0 \\ 0 & v_2 \end{pmatrix}, \quad \langle \chi_L \rangle = \begin{pmatrix} 0 \\ v_L \end{pmatrix}, \quad \langle \chi_R \rangle = \begin{pmatrix} 0 \\ v_R \end{pmatrix}, \quad (2)$$

We set $v_2 = 0$ to prevent a bottom quark mass arising from the Yukawa interaction involving the bidoublet scalar.

The bottom quark and tau lepton masses can be estimated as:

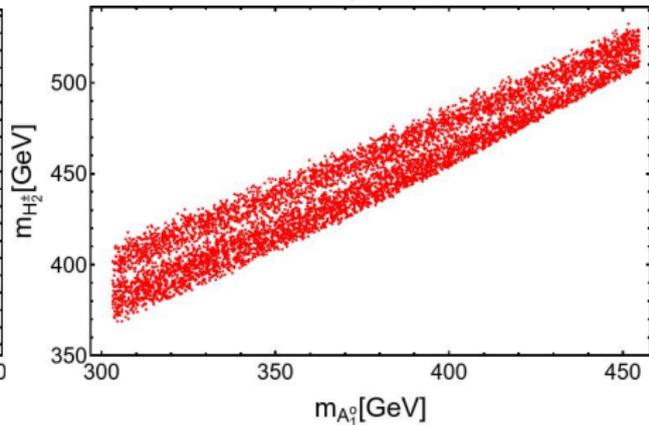
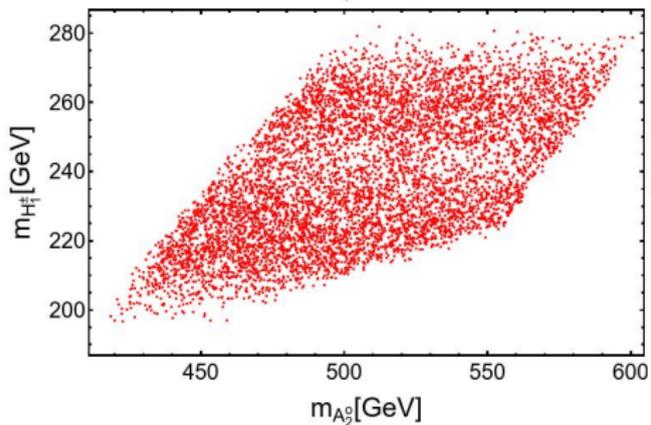
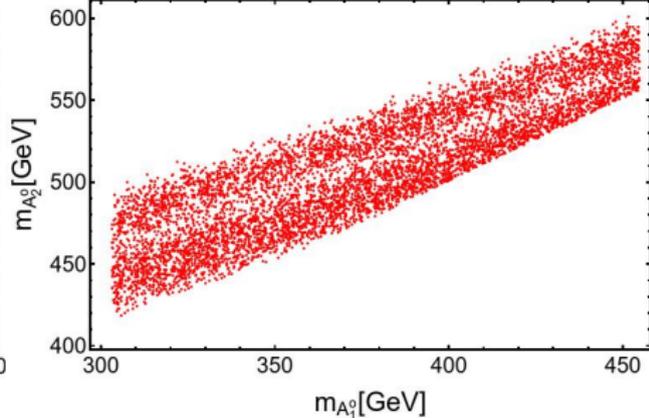
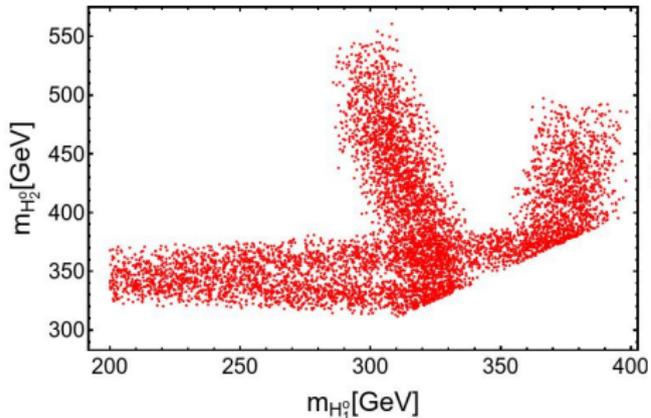
$$m_b \sim m_\tau \sim \frac{y^2 v_L v_R}{m_F} \quad (3)$$

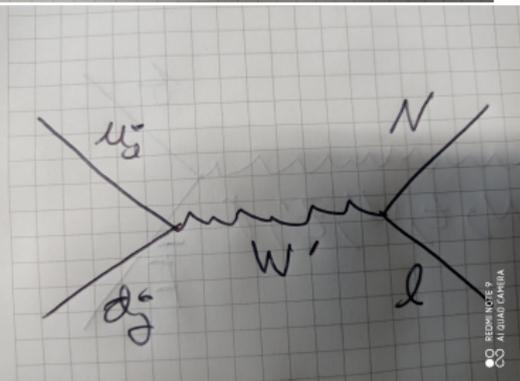
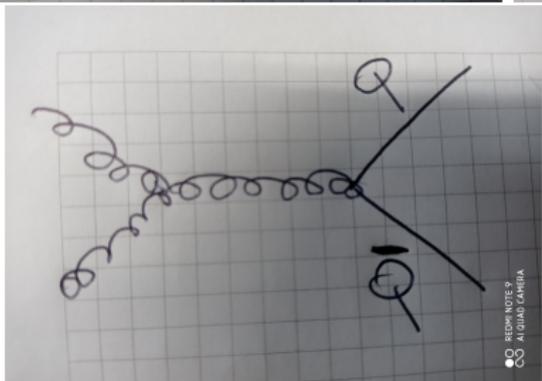
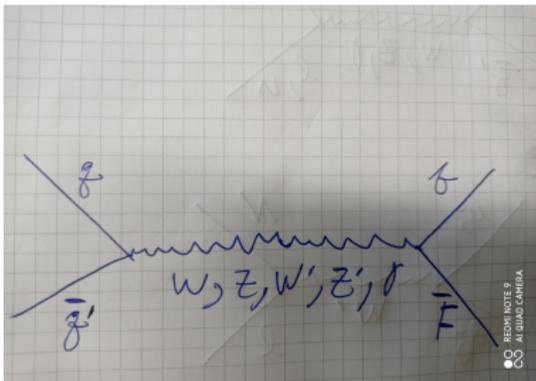
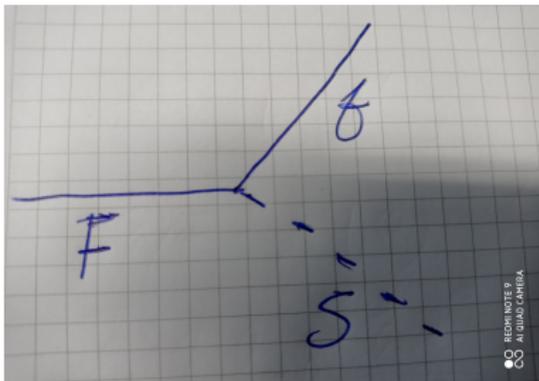
Taking $v_L \sim \mathcal{O}(100)$ GeV, $v_R \sim \mathcal{O}(10)$ TeV, $m_F \sim \mathcal{O}(100)$ TeV and $y \sim \mathcal{O}(0.4)$, it follows $m_b \sim m_\tau \sim \mathcal{O}(1)$ GeV.

The physical low energy scalar mass spectrum resulting from the scalar potential for the Φ , χ_L , ϕ_L , χ_R and ϕ_R scalars is composed of:

- 1 Physical electrically charged scalars H_1^\pm , H_2^\pm , $S_1^\pm = \phi_L^\pm$ and $S_2^\pm = \phi_R^\pm$.
- 2 Physical CP odd scalars A_1^0 , A_2^0 , P_1^0 , P_2^0 .
- 3 Physical CP even scalars h , H_1^0 , H_2^0 , H_3^0 , $S_1^0 = \phi_{1I}^0$, $S_2^0 = \phi_{2I}^0$.

Furthermore, the massless scalar eigenstates $Im\chi_L^0$, $Im\chi_R^0$, χ_L^\pm and χ_R^\pm are associated with the Goldstone bosons corresponding to the longitudinal components of the Z , Z' , W^\pm and W'^\pm gauge bosons, respectively.





The sterile neutrinos have the following decay modes $N_a^\pm \rightarrow l_i^\pm W^\mp$, $N_a^\pm \rightarrow \nu_i Z$ and $N_a^\pm \rightarrow \nu_i S$, $N_a^\pm \rightarrow l_i^+ l_j^- \nu_k$, $N_a^\pm \rightarrow l_i^- u_j \bar{d}_k$, $N_a^\pm \rightarrow b \bar{b} \nu_k$

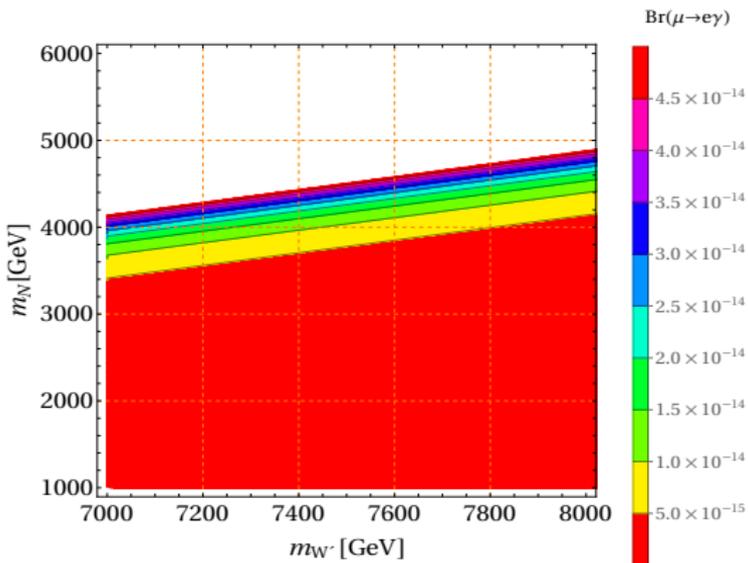


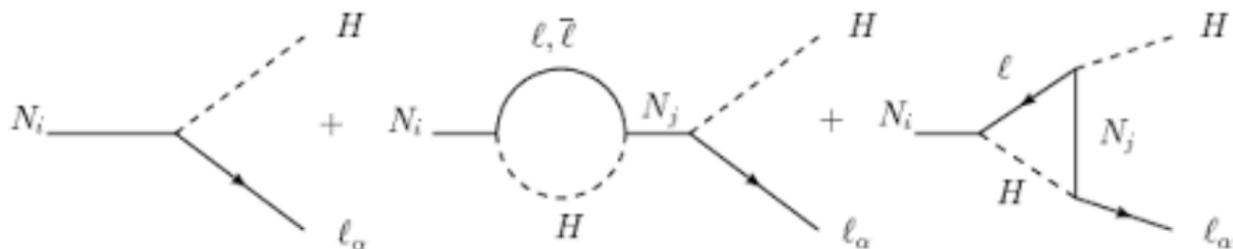
Figure: Allowed parameter space in the $m_{W'} - m_N$ plane consistent with the LFV constraints.

In the region of parameter space consistent with $\mu \rightarrow e\gamma$ decay rate constraints, the maximum obtained branching ratios for the $\tau \rightarrow \mu\gamma$ and $\tau \rightarrow e\gamma$ decays can reach values below their corresponding upper experimental bounds of 4.4×10^{-8} and 3.3×10^{-8} , respectively.

In our analysis of Leptogenesis we assume:

- ① The first generation of pseudo-Dirac fermions N_a^\pm , i.e. N_1^\pm will be much lighter than the second and third generation ones.
- ② The off-diagonal Dirac and Majorana neutrino mass submatrices are diagonal with 11 entries much smaller than the remaining ones.
- ③ The initial temperature is taken to be much larger than the mass m_{N^\pm} of the lightest pair of pseudo-Dirac fermions $N_1^\pm = N^\pm$.
- ④ The exotic leptonic fields E_{nR} , E' and Ω_{nR} ($n = 1, 2$) are heavier than the lightest pseudo-Dirac fermions $N_1^\pm = N^\pm$.

The lepton asymmetry parameter, is induced by decay process of N^\pm .



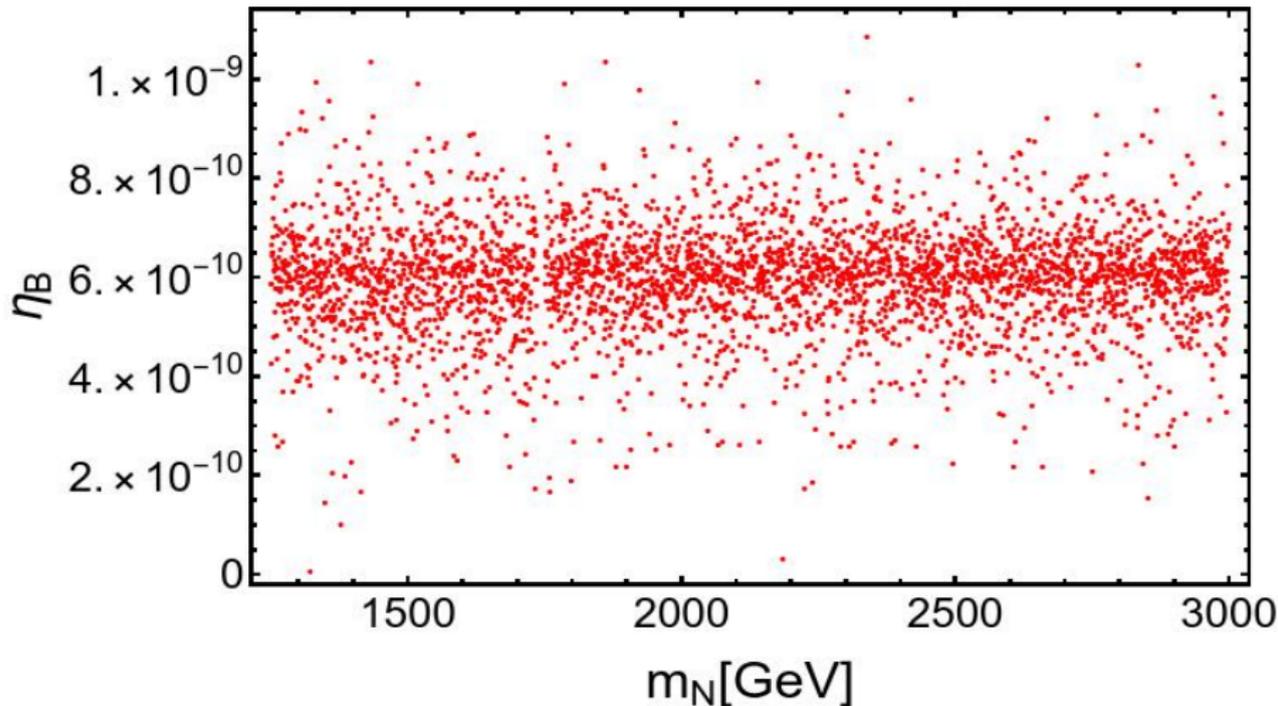
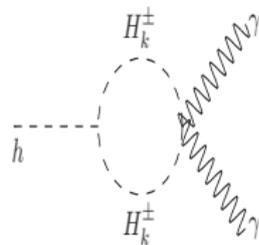
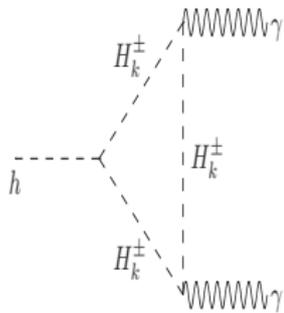
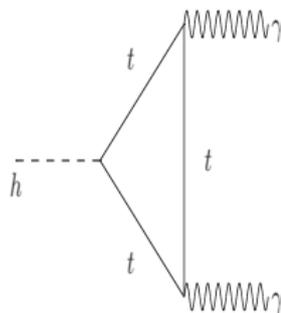
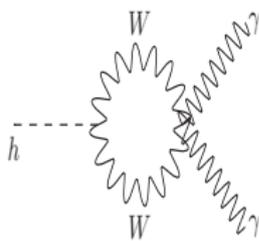
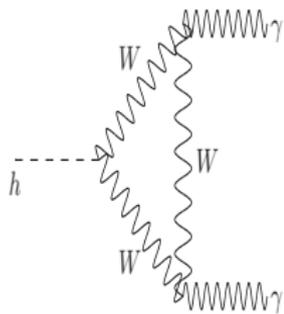


Figure: Correlation of the baryon asymmetry and the mass m_N of the lightest pair of pseudo-Dirac fermions $N_1^\pm = N^\pm$. Here we have set $v_R = 14$ TeV, $m_{W'} = 7$ TeV, $m_{Z'} = 7.2$ TeV, $m_{N_2^\pm} = 14$ TeV, $m_{N_3^\pm} = 28$ TeV and

$$\left| y_{22}^{(L)} \right| = \left| y_{33}^{(L)} \right| = \left| y_2^{(L)} \right|$$



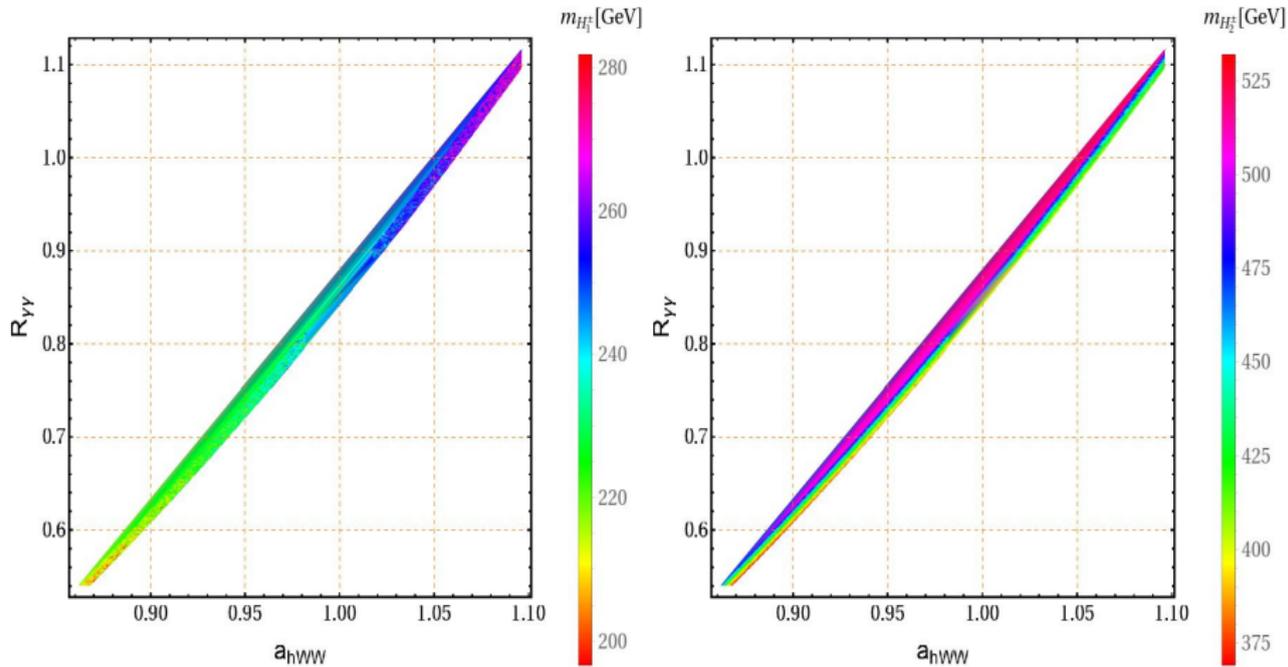
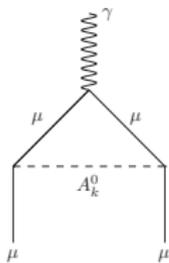
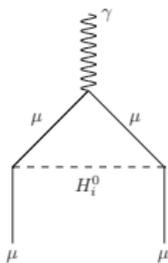
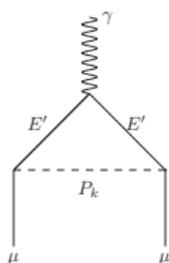
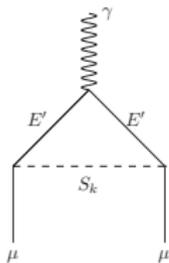
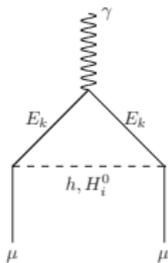
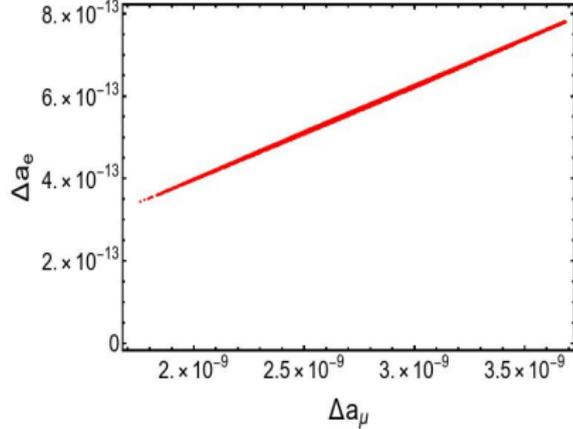
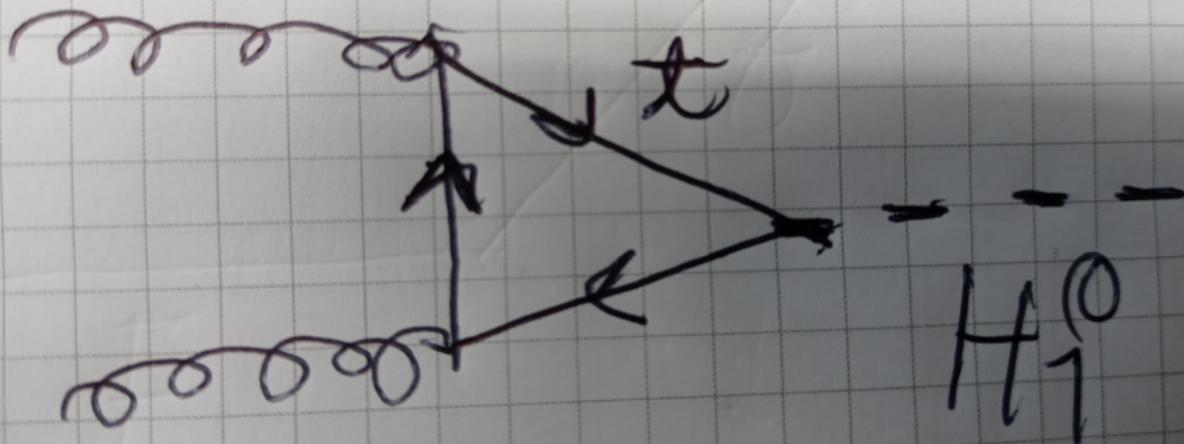


Figure: Correlation of the Higgs diphoton signal strength with the a_{hWW} deviation factor from the SM Higgs- W gauge boson coupling.







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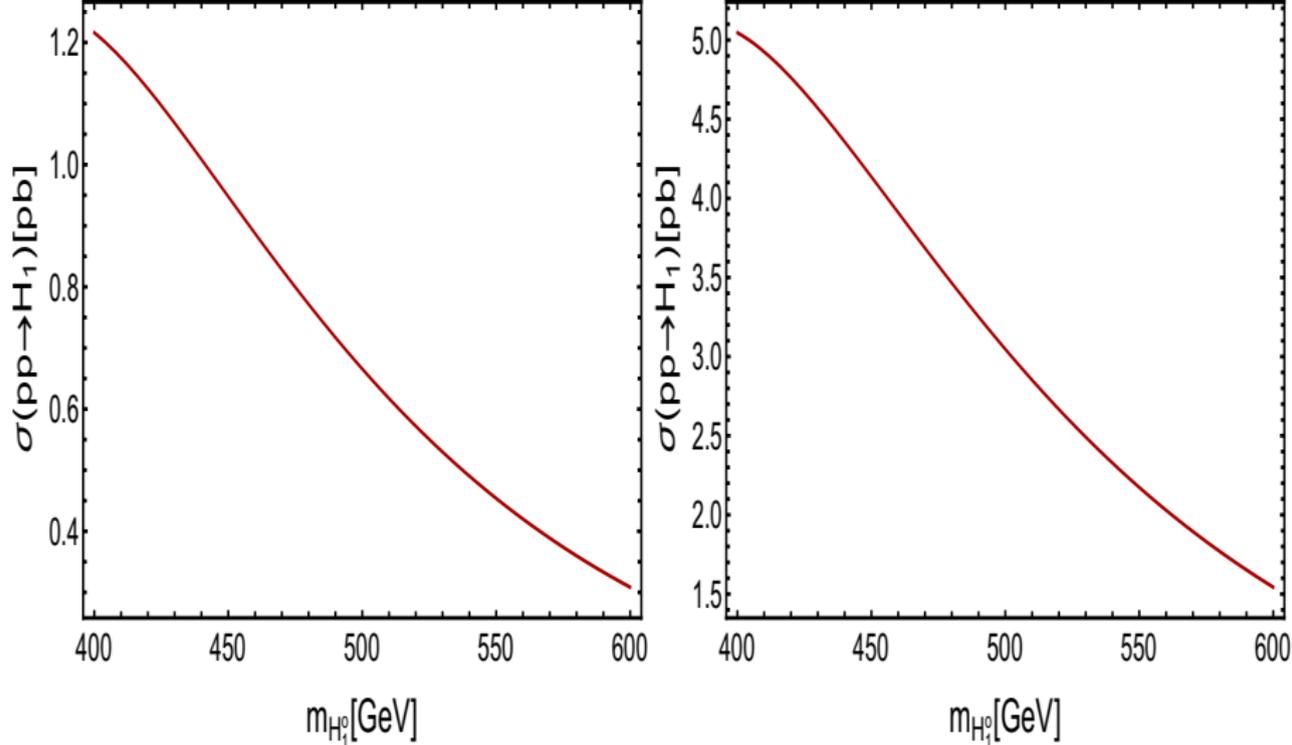
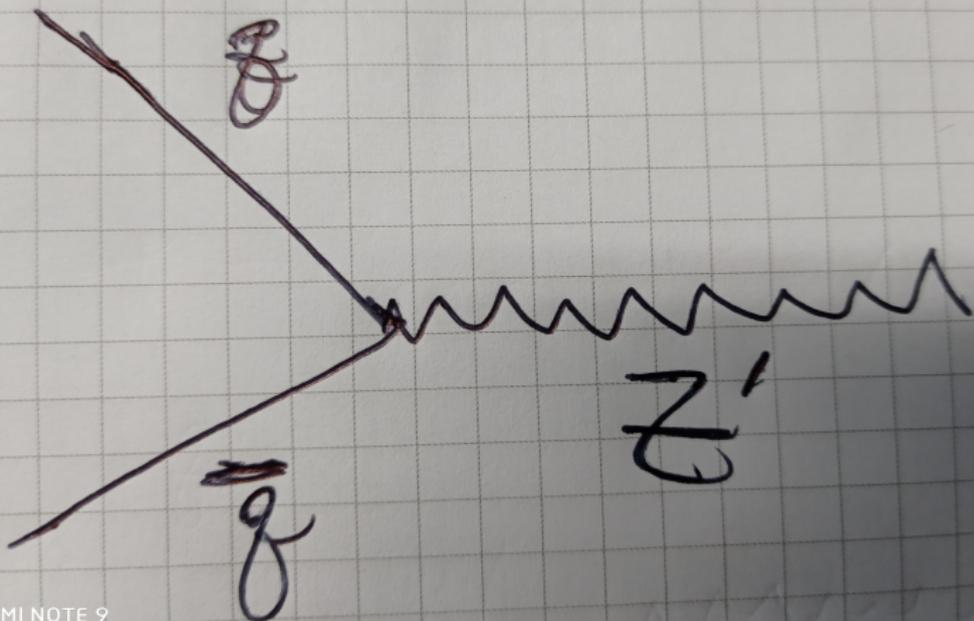


Figure: Total cross section for the H_1^0 production via gluon fusion mechanism at the LHC for $\sqrt{s} = 14$ TeV (left-panel) and $\sqrt{s} = 28$ (right-panel) TeV as a function of the heavy scalar mass $m_{H_1^0}$.



REDMI NOTE 9
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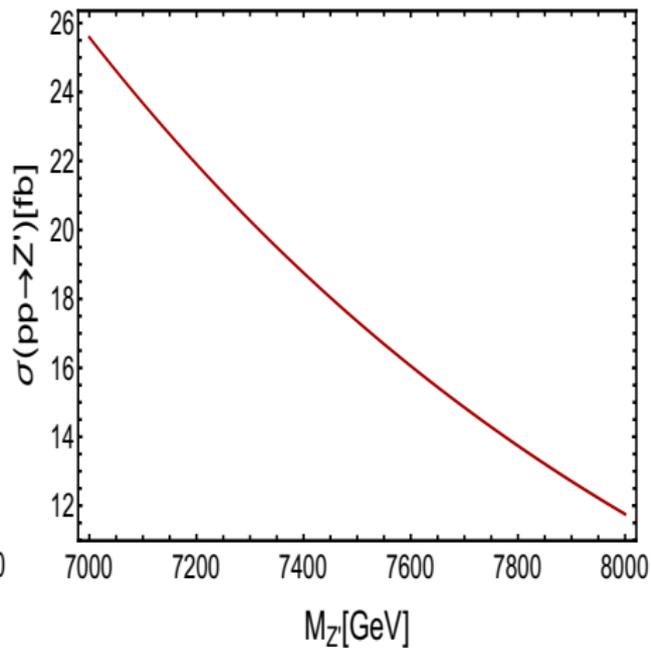
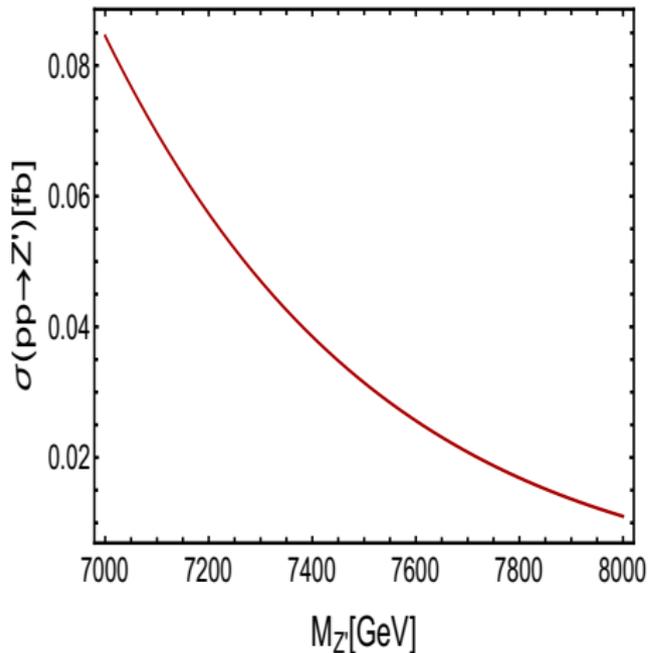


Figure: Total cross section for the Z' production via Drell-Yan mechanism at a proton-proton collider for $\sqrt{S} = 14$ TeV (left-panel) and $\sqrt{S} = 28$ TeV (right-panel) as a function of the Z' mass.

We take into account the constraint $\frac{M_{Z'}}{g_R} > 7$ TeV arising from LEP I and II measurements of $e^+e^- \rightarrow l^+l^-$, which is also consistent with LHC bounds.

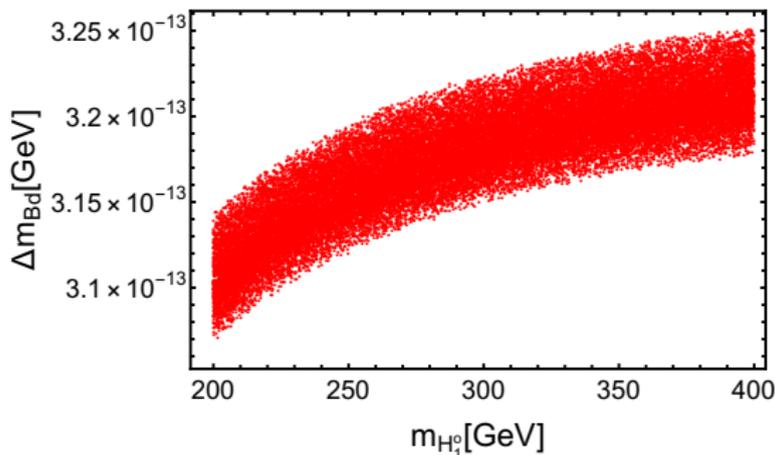


Figure: Correlation between the Δm_{B_d} mass splitting and the heavy CP even scalar mass $m_{H_1^0}$. The couplings of the flavor changing neutral Yukawa interactions that produce the $B_d^0 - \bar{B}_d^0$ oscillations have been set to be equal to 10^{-4} . We have also fixed $m_{H_3^0} = 10$ TeV and considered the ranges $200 \text{ GeV} \leq m_{H_1^0} \leq 400 \text{ GeV}$, $350 \text{ GeV} \leq m_{H_2^0} \leq 550 \text{ GeV}$ and $300 \text{ GeV} \leq m_{A_1^0} \leq 450 \text{ GeV}$, whereas we have also set $m_{A_2^0} = m_{A_1^0} + 150 \text{ GeV}$.

$B_s^0 - \bar{B}_s^0$ and $K^0 - \bar{K}^0$ are consistent with the experimental data for flavor violating Yukawa couplings equal to 2.5×10^{-4} and 10^{-6} , respectively.

Conclusions

- In the extended LR model, the top and exotic fermions get tree level masses whereas the masses of the bottom, charm and strange quarks, tau and muon leptons are generated from a tree level. The masses of the first generation of SM charged fermions arise at one loop level.
- Neutrino masses can be generated via one-loop inverse seesaw.
- Fermion masses and mixings, DM, meson oscillations, CLFV, $(g - 2)_{e,\mu}$ anomalies, lepton and baryon asymmetries can be accounted for.
- Dark matter stability can arise from a residual parity symmetry.

Acknowledgements

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Extra Slides

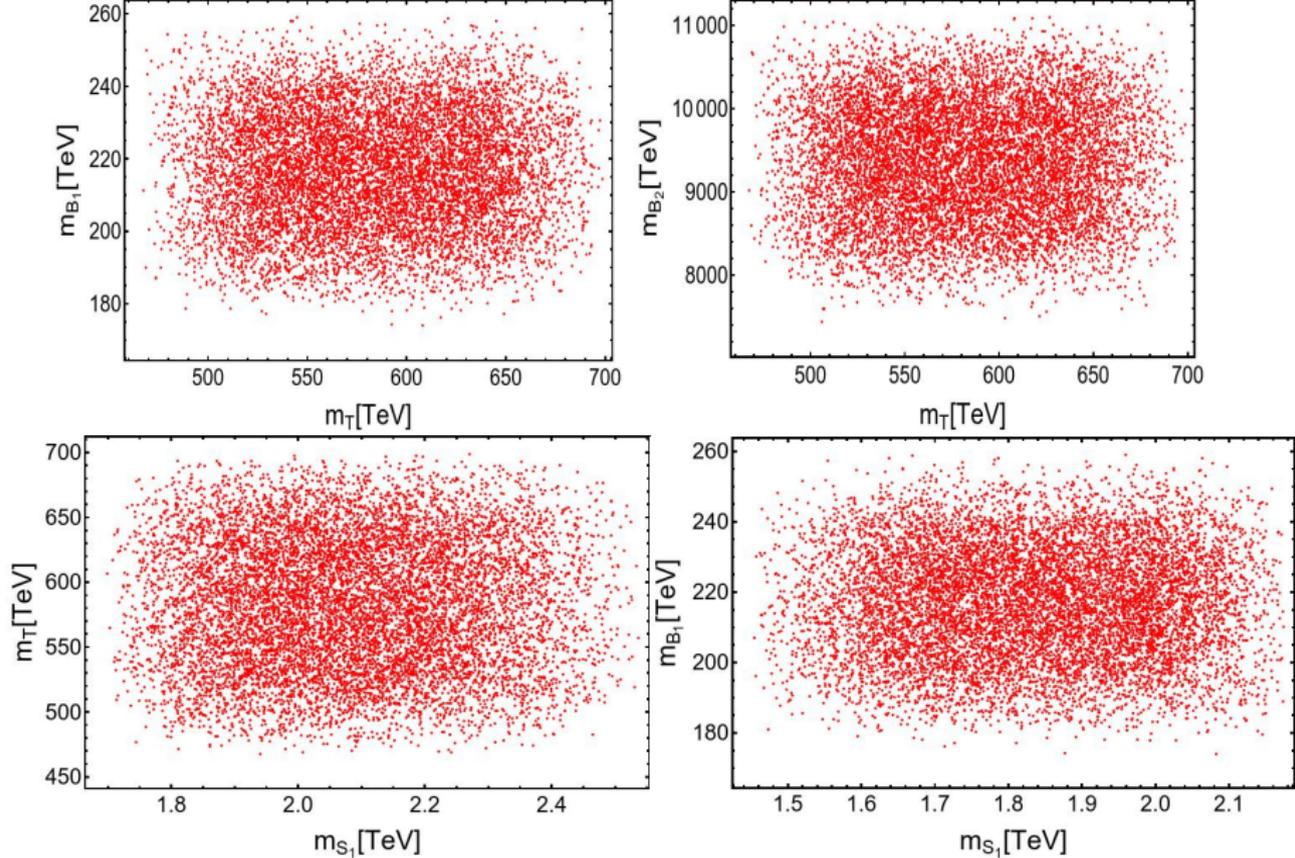


Figure: Correlations between the heavy exotic quark masses.

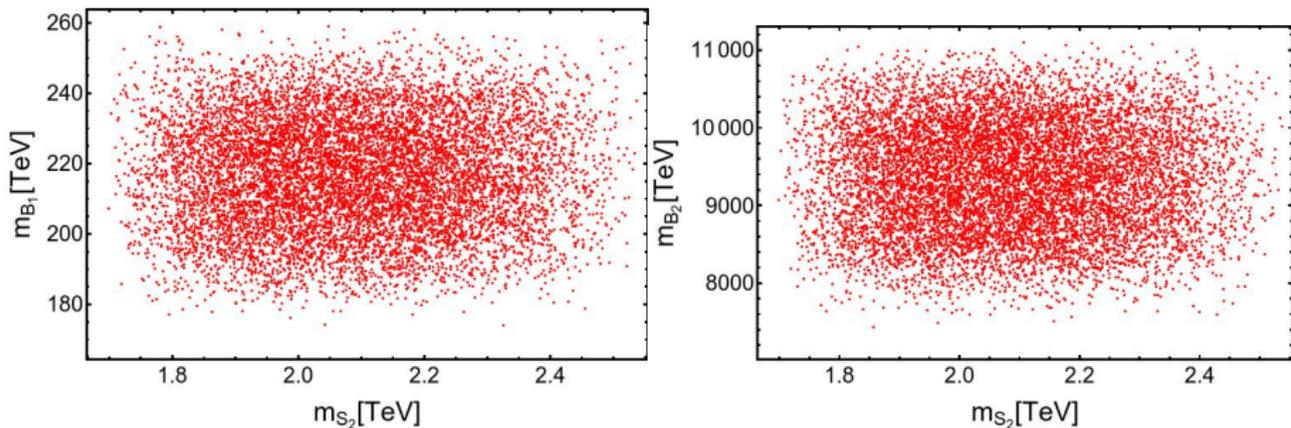


Figure: Correlations between the exotic quark masses and the masses m_{S_1} and m_{S_2} of the inert scalars S_1 and S_2 , respectively.

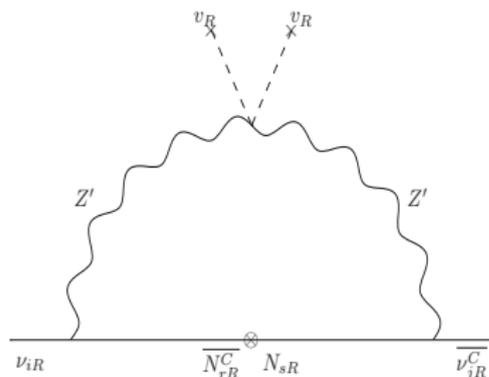
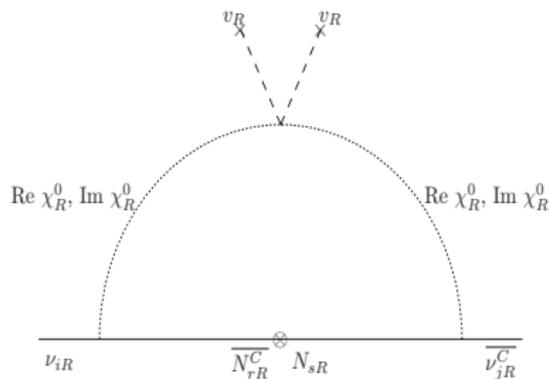
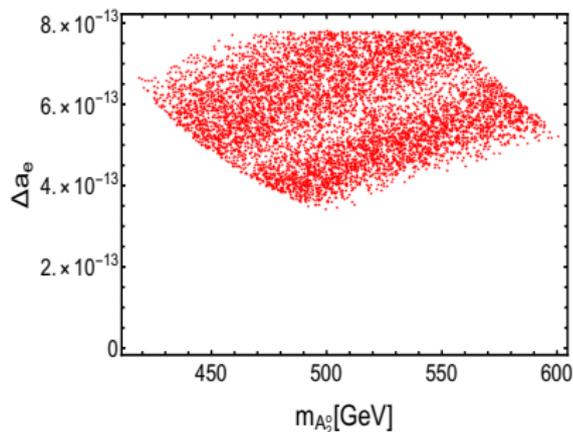
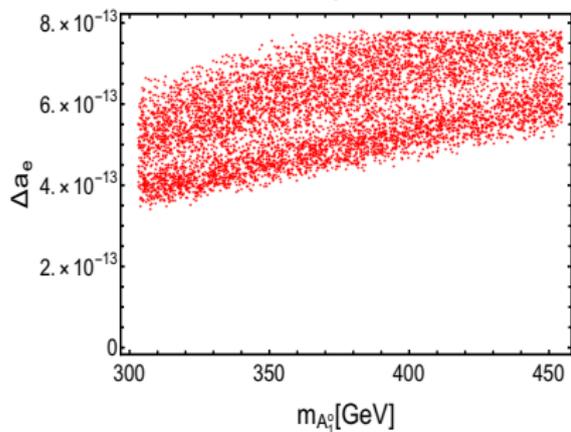
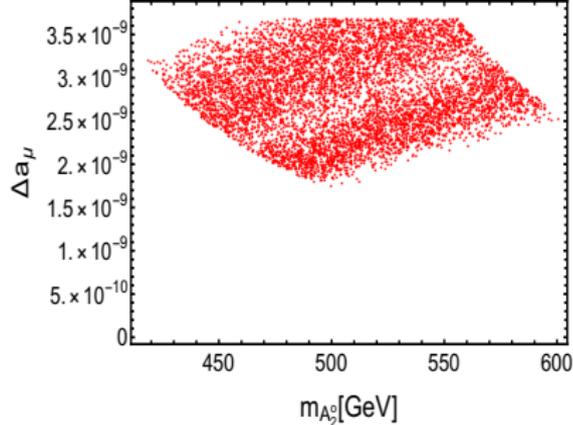
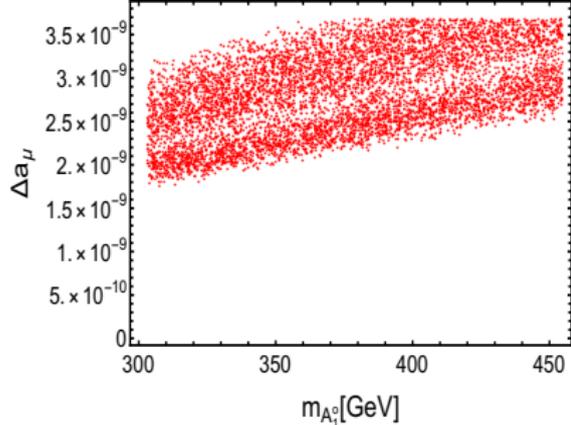


Figure: Feynman diagram contributing to the Majorana neutrino mass submatrix $\tilde{\mu}$. Here, $i, j, r, s = 1, 2, 3$ and the cross mark \otimes in the internal lines corresponds to the one loop level induced Majorana mass term.



For the case of two heavy seesaw mediators, one has:

$$M = \begin{pmatrix} F_1 G_1 + X_1 Y_1 & F_1 G_2 + X_1 Y_2 & F_1 G_3 + X_1 Y_3 \\ F_2 G_1 + X_2 Y_1 & F_2 G_2 + X_2 Y_2 & F_2 G_3 + X_2 Y_3 \\ F_3 G_1 + X_3 Y_1 & F_3 G_2 + X_3 Y_2 & F_3 G_3 + X_3 Y_3 \end{pmatrix}, \quad (4)$$

$$M_{ij} = M_j^i = F_i G_j + X_i Y_j = F^i G_j + X^i Y_j \quad (5)$$

$$F^i = F_i, \quad X^i = X_i \quad (6)$$

$$\det(M_j^i) = \frac{1}{3!} \varepsilon_{j_1 j_2 j_3} \varepsilon^{i_1 i_2 i_3} M_{i_1}^{j_1} M_{i_2}^{j_2} M_{i_3}^{j_3}, \quad M_j^i = M_{ij} \quad (7)$$

$$\begin{aligned} \det(M_j^i) &= \frac{1}{3!} \varepsilon_{j_1 j_2 j_3} \varepsilon^{i_1 i_2 i_3} (F^{j_1} G_{i_1} + X^{j_1} Y_{i_1}) \\ &\times (F^{j_2} G_{i_2} + X^{j_2} Y_{i_2}) (F^{j_3} G_{i_3} + X^{j_3} Y_{i_3}) = 0 \end{aligned} \quad (8)$$

For the case of three fermionic seesaw mediators, one has:

$$M_{ij} = M_j^i = F_i G_j + X_i Y_j + R_i S_j = F^i G_j + X^i Y_j + R^i S_j \quad (9)$$

Then, it follows that:

$$\det(M_j^i) = \varepsilon_{j_1 j_2 j_3} \varepsilon^{i_1 i_2 i_3} F^{j_1} G_{i_1} X^{j_2} Y_{i_2} R^{j_3} S_{i_3} \neq 0 \quad (10)$$

provided that:

$$G_{i_1} \neq Y_{i_2} \neq S_{i_3}, \quad F^{j_1} \neq X^{j_2} \neq R^{j_3} \quad (11)$$

Therefore, we have shown that in order to generate the masses of three fermion families via a seesaw mechanism, there should be at least three fermionic seesaw mediators. Furthermore, the number of the massless states obtained in a mass matrix resulting from a seesaw mechanism is $3 - n$, where n is the number of fermionic seesaw mediators.

In the analysis of Leptogenesis, the following processes are considered:

- 1 Decays $N_1^\pm \rightarrow l_i H_r^+$ ($r = 1, 2$), $N_1^\pm \rightarrow \nu_i h$ ($i = 1, 2, 3$ and $N_1^\pm \rightarrow l_i^- u_j \bar{d}_k$ ($i, j, k = 1, 2, 3$).
- 2 Z' mediated scattering processes $N_1^\pm N_1^\pm \longleftrightarrow l_i \bar{l}_j$ ($i, j = 1, 2, 3$), $N_1^\pm N_1^\pm \longleftrightarrow u_i \bar{u}_j$ and $N_1^\pm N_1^\pm \longleftrightarrow d_i \bar{d}_j$.
- 3 W' mediated processes $N_1^\pm l_{iR} \longleftrightarrow \bar{u}_{jR} d_{kR}$, $N_1^\pm \bar{u}_{iR} \longleftrightarrow l_{jR} \bar{d}_{kR}$, $N_1^\pm d_{iR} \longleftrightarrow l_{jR} u_{kR}$ ($i, j, k = 1, 2, 3$).
- 4 Inverse two and three body decays of N_1^\pm .

The Boltzmann equations take the form:

$$\begin{aligned}\frac{dN_{N_1^\pm}(z)}{dz} &= -[D(z) + S(z)] \left[N_{N_1^\pm}(z) - N_{N_1^\pm}^{eq}(z) \right], \\ \frac{dN_{N_{B-L}}(z)}{dz} &= -\varepsilon_\pm D(z) \left[N_{N_1^\pm}(z) - N_{N_1^\pm}^{eq}(z) \right] - W(z) N_{N_{B-L}}(z),\end{aligned}$$

where $z = \frac{m_{N_1^\pm}}{T}$, whereas $N_{N_1^\pm}$ and $N_{N_{B-L}}$ are the number density and the amount of $B - L$ asymmetry, respectively. Here ε_\pm reads:

$$\begin{aligned}\varepsilon_\pm &= \sum_{i=1}^3 \sum_{r=1}^2 \frac{[\Gamma(N_\pm \rightarrow l_i H_r^+) - \Gamma(N_\pm \rightarrow \bar{l}_i H_r^-)]}{[\Gamma(N_\pm \rightarrow l_i H_r^+) + \Gamma(N_\pm \rightarrow \bar{l}_i H_r^-)]} \\ &+ \sum_{i=1}^3 \frac{[\Gamma(N_\pm \rightarrow h\nu_i) - \Gamma(N_\pm \rightarrow h\nu_i)]}{[\Gamma(N_\pm \rightarrow h\nu_i) + \Gamma(N_\pm \rightarrow h\nu_i)]} \\ &\approx \frac{\Im \left\{ \left(\left[(y_{N_+})^\dagger (y_{N_-}) \right]_{11}^2 \right) \right\}}{8\pi A_\pm} \frac{r}{r^2 + \frac{\Gamma_\pm^2}{m_{N_\pm}^2}},\end{aligned}\tag{12}$$

with:

$$\begin{aligned} r &= \frac{m_{N_+}^2 - m_{N_-}^2}{m_{N_+} m_{N_-}}, \quad A_{\pm} = \left[(y_{N_{\pm}})^{\dagger} y_{N_{\pm}} \right]_{11}, \quad \Gamma_{\pm} = \frac{A_{\pm} m_{N_{\pm}}}{8\pi}, \\ y_{N_{\pm}} &= \frac{y^{(L)}}{\sqrt{2}} (1 \mp S) = \frac{y^{(L)}}{\sqrt{2}} \left[1 \pm \frac{1}{4} M^{-1} (\mu + \tilde{\mu}) \right], \end{aligned} \quad (13)$$

The baryon to photon ratio is:

$$\eta_B = \frac{n_B}{n_{\gamma}} = \frac{3}{4} a_{sph} N_{B-L}, \quad a_{sph} = \frac{8n_f + 4n_H}{22n_f + 13n_H}, \quad (14)$$

where a_{sph} is the L to B sphaleron conversion rate. Furthermore, n_f is the number of fermion families and n_H is the number of Higgs doublets.

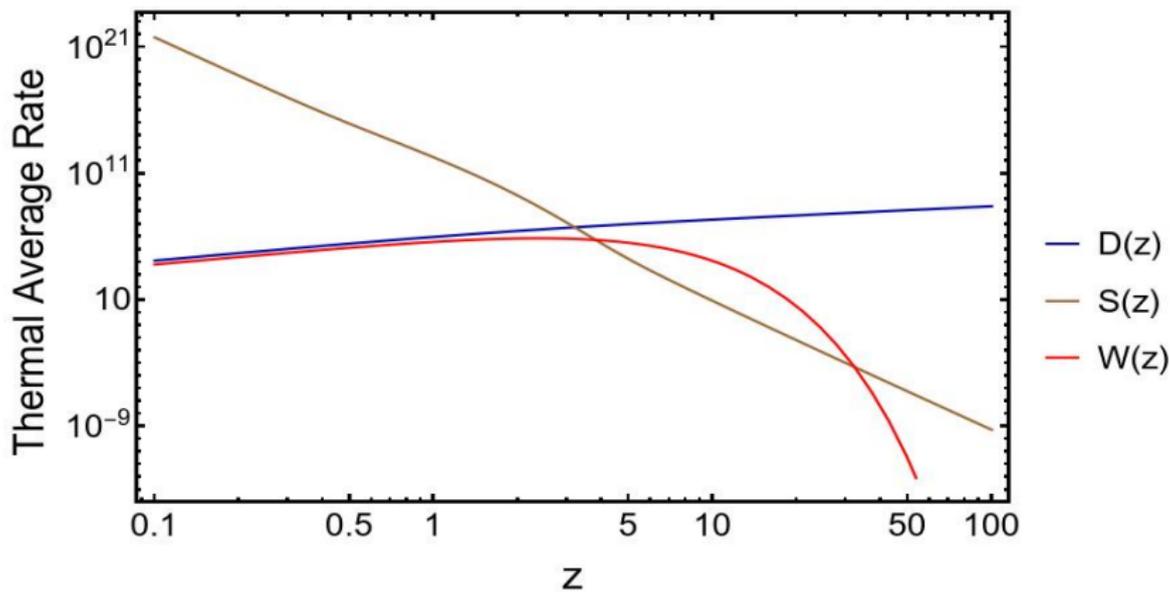


Figure: Thermally averaged scattering rates $D(z)$, $S(z)$ and $W(z)$ as functions of $z = \frac{m_N}{T}$, with m_N the mass of the lightest pair of pseudo-Dirac fermions $N_1^\pm = N^\pm$ and T the temperature. Here we have set $v_R = 14$ TeV, $m_{W'} = 7$ TeV and $m_{Z'} = 7.2$ TeV.

The contributions arising from the scattering processes, as well as from the inverse decays, are subdominant for temperatures sufficiently lower than the mass m_N , i.e., $z \gg 1$.

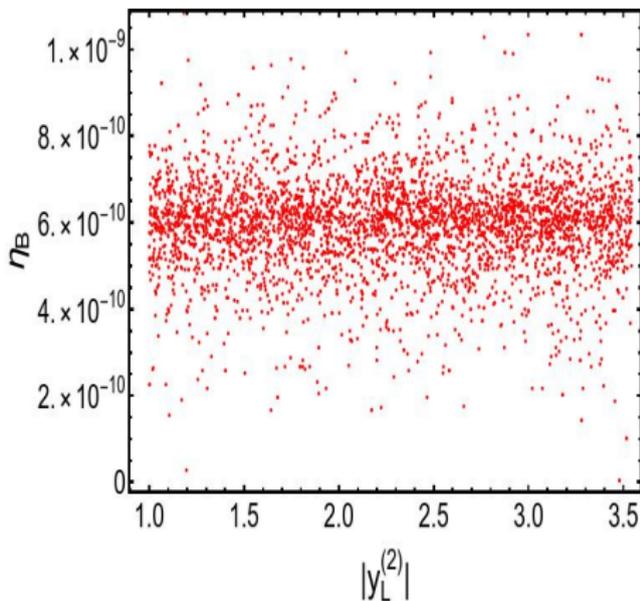
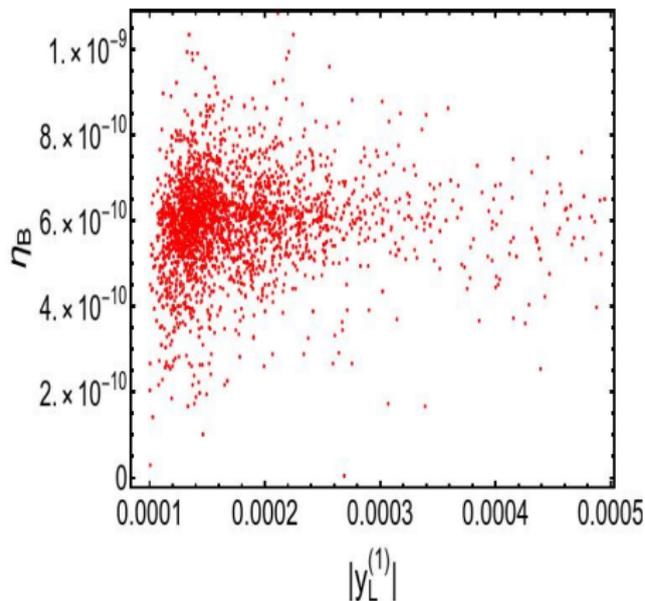
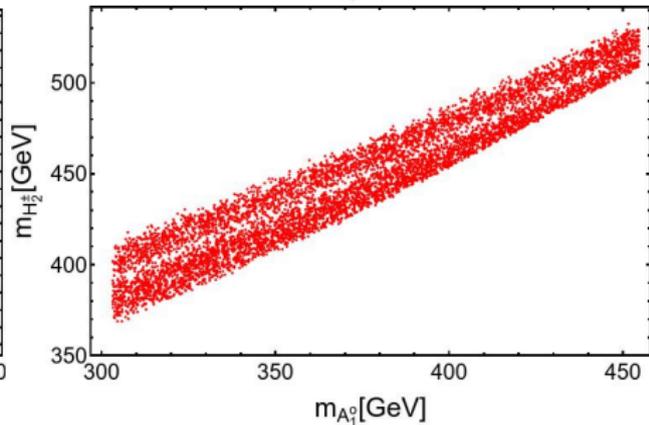
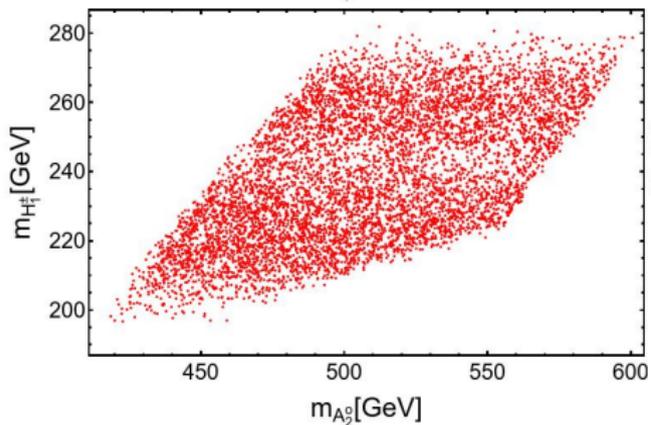
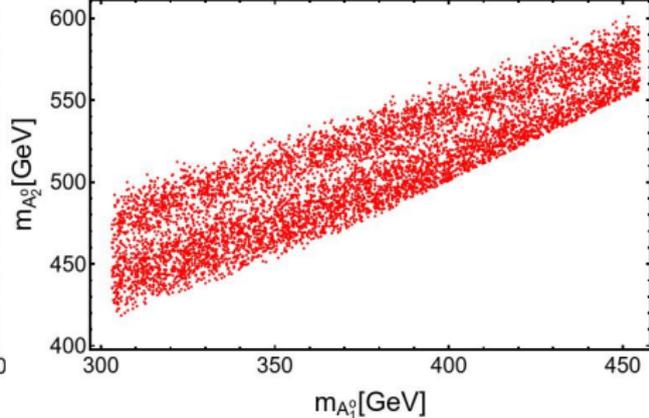
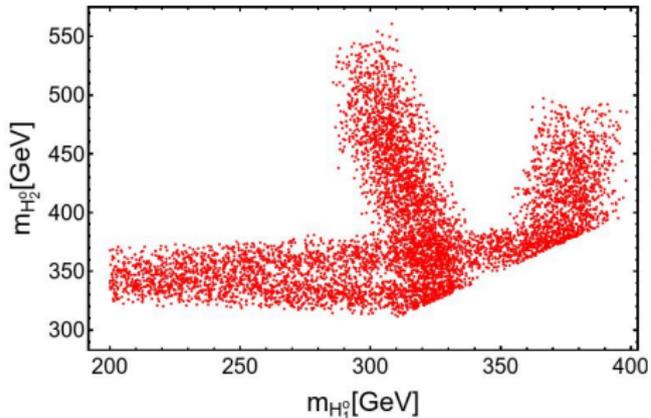


Figure: Correlation of the baryon asymmetry and the magnitude of the Dirac neutrino Yukawa couplings $y_{11}^{(L)}$ and $y_{22}^{(L)}$. Here we have set $v_R = 14$ TeV, $m_{W'} = 7$ TeV, $m_{Z'} = 7.2$ TeV, $m_{N_2^\pm} = 14$ TeV, $m_{N_3^\pm} = 28$ TeV and $|y_{22}^{(L)}| = |y_{33}^{(L)}| = |y_2^{(L)}|$.



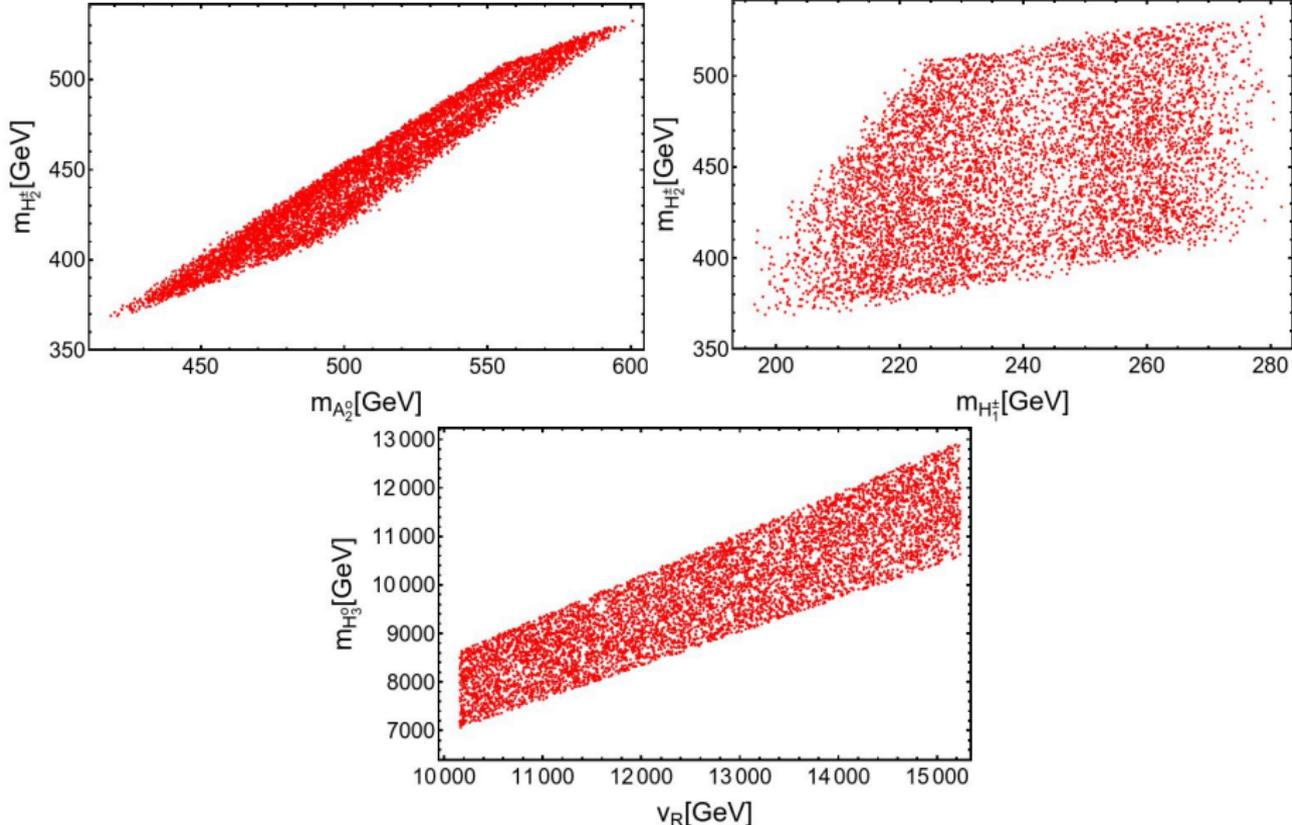


Figure: Correlations between the non SM scalar masses (top plots). Correlation between the mass of the CP even neutral scalar H_3^0 and the scale v_R of breaking of the left-right symmetry.

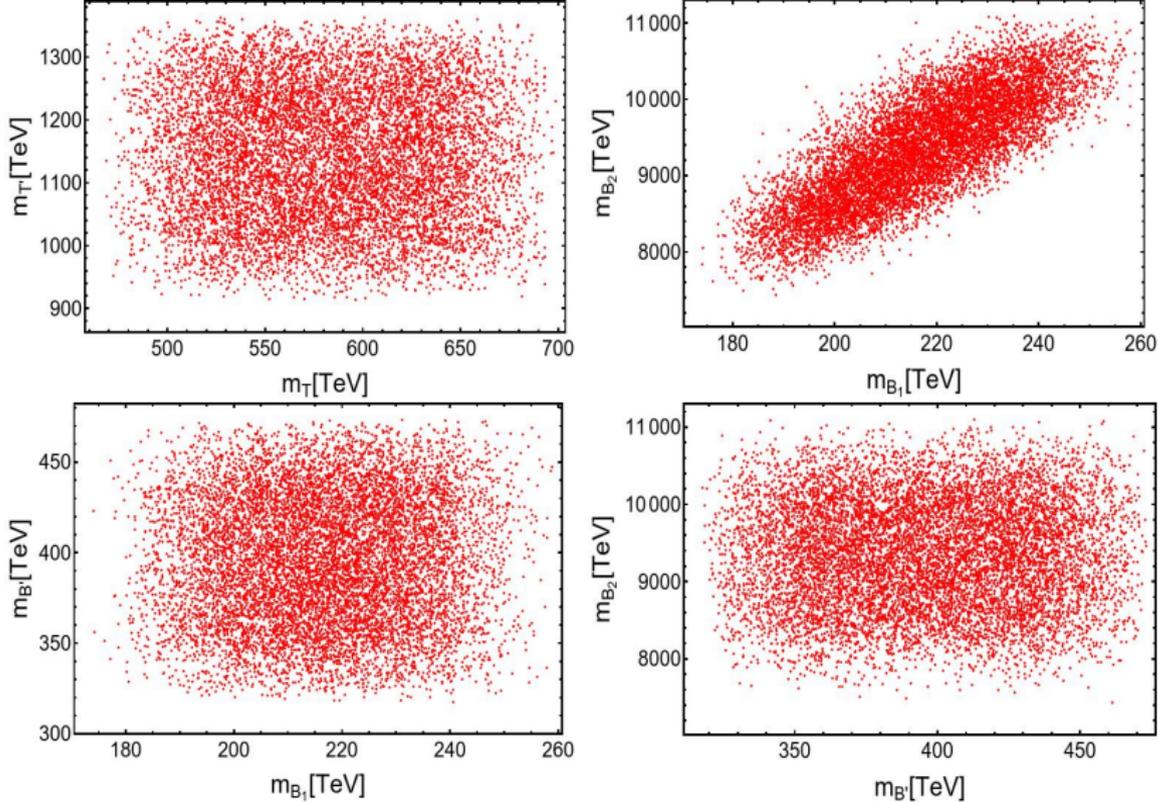


Figure: Correlations between the heavy exotic quark masses.

$$\begin{aligned}
m_u^{\text{exp}}(M_Z) &= 1.24 \pm 0.22 \text{ MeV}, \\
m_c^{\text{exp}}(M_Z) &= 0.626 \pm 0.020 \text{ GeV}, \\
m_t^{\text{exp}}(M_Z) &= 172.9 \pm 0.04 \text{ GeV}, \\
m_d^{\text{exp}}(M_Z) &= 2.69 \pm 0.19 \text{ MeV}, \\
m_s^{\text{exp}}(M_Z) &= 53.5 \pm 4.6 \text{ MeV}, \\
m_b^{\text{exp}}(M_Z) &= 2.86 \pm 0.03 \text{ GeV},
\end{aligned}$$

and the CKM parameters are [19]

$$\begin{aligned}
|\mathbf{V}_{12}^{\text{exp}}| &= 0.22452 \pm 0.00044, \\
|\mathbf{V}_{23}^{\text{exp}}| &= 0.04214 \pm 0.00076, \\
|\mathbf{V}_{13}^{\text{exp}}| &= 0.00365 \pm 0.00012, \\
J_q^{\text{exp}} &= (3.18 \pm 0.15) \times 10^{-5}.
\end{aligned}$$

The magnitudes of the quark Yukawa couplings are randomly varied in the range [0.1, 1.5], whereas their complex phases are ranged between 0 and 2π . Furthermore, we have fixed $v_L = 100 \text{ GeV}$ and $v_R = 10 \text{ TeV}$ and randomly varied $\theta = \theta_S = -\theta_P$ in a small range around $\frac{\pi}{3}$. The masses of the vector like quarks and inert scalar mediators are varied in the ranges:

$$\begin{aligned}
0.5 \text{ TeV} \leq m_{S_1} = m_{P_1} \leq 10 \text{ TeV}, & \quad 1.01 m_{S_1} \leq m_{S_2} = m_{P_2} \leq 1.03 m_{S_1}, \\
1 \text{ TeV} \leq m_{T'}, m_{B'} \leq 10^3 \text{ TeV}, & \quad 10^2 \text{ TeV} \leq m_{B_1} \leq 2 \times 10^2 \text{ TeV}, \\
10^2 \frac{m_b}{m_c} \text{ TeV} \leq m_T \leq 2 \times 10^2 \frac{m_b}{m_c} \text{ TeV}, & \quad 10^2 \frac{m_b}{m_s} \text{ TeV} \leq m_{B_2} \leq 2 \times 10^2 \frac{m_b}{m_s} \text{ TeV},
\end{aligned}$$

In the above described range of parameters, we find that the minimization of the χ^2 function yields the following benchmark point, consistent with the experimental values of the SM quark masses and CKM parameters:

$$\begin{aligned}
\theta &\simeq 85.9^\circ, & m_{S_1} = m_{P_1} &\simeq 1.9 \text{ TeV}, & m_{S_2} = m_{P_2} &\simeq 2.1 \text{ TeV}, \\
v_L &\simeq 100 \text{ GeV}, & v_R &\simeq 10 \text{ TeV}, \\
m_T &\simeq 583 \text{ TeV}, & m_{T'} &\simeq 1.1 \times 10^3 \text{ TeV}, & m_{B_1} &\simeq 216 \text{ TeV}, \\
m_{B_2} &\simeq 9.3 \times 10^3 \text{ TeV}, & m_{B'} &\simeq 396 \text{ TeV}, \\
x_1^{(T)} &\simeq 0.24 - 0.02i, & x_2^{(T)} &\simeq 0.96 - 0.06i, & z_1^{(T)} = z_2^{(T)} &\simeq -0.16 + 0.08i, \\
x_{12}^{(B)} &\simeq -0.05 - 0.03i, & x_{22}^{(B)} &\simeq -0.62 - 0.06i, & x_3^{(B)} &\simeq 0.07 - 0.62i, \\
z_{11}^{(B)} &\simeq 0.25, & z_{12}^{(B)} &\simeq 0.49, & z_{13}^{(B)} &\simeq -0.44, \\
z_{21}^{(B)} &\simeq -1.17i, & z_{22}^{(B)} &\simeq 0.95i, & z_{23}^{(B)} &\simeq 0.80i, \\
w_1^{(T)} &\simeq -0.39 + 0.197i, & w_2^{(T)} &\simeq -0.58 + 0.29i, \\
r_1^{(T)} &\simeq -0.154 + 0.084i, & r_2^{(T)} &\simeq -0.875 + 0.48i, & r_3^{(T)} &\simeq 0.30 - 0.16i, \\
w_1^{(B')} &\simeq 0.12 - 0.087i, & w_2^{(B')} &\simeq 0.44 + 0.74i, \\
r_1^{(B')} &\simeq -0.17 - 0.98i, & r_2^{(B')} &\simeq -1.22, & r_3^{(B')} &\simeq 1.299 + 0.698i.
\end{aligned} \tag{26}$$

With the above particle content, the following relevant Yukawa terms arise:

$$\begin{aligned}
-\mathcal{L}_Y = & \sum_{i=1}^3 \alpha_i \bar{Q}_{3L} \Phi Q_{iR} + \sum_{n=1}^2 x_n^{(T)} \bar{Q}_{nL} \tilde{\chi}_L T_R + \sum_{i=1}^3 z_i^{(T)} \bar{T}_L \tilde{\chi}_R^\dagger Q_{iR} \\
& + \sum_{n=1}^2 w_n^{(T')} \bar{Q}_{nL} \tilde{\phi}_L T'_R + \sum_{i=1}^3 r_i^{(T')} \bar{T}'_L \tilde{\phi}_R^\dagger Q_{iR} \\
& + x_3^{(B)} \bar{Q}_{3L} \chi_L B_{1R} + \sum_{n=1}^2 x_{n2}^{(B)} \bar{Q}_{nL} \chi_L B_{2R} + \sum_{n=1}^2 \sum_{i=1}^3 z_{ni}^{(B)} \bar{B}_{nL} \chi_R^\dagger Q_{iR} \\
& + \sum_{n=1}^2 w_n^{(B')} \bar{Q}_{nL} \phi_L B'_R + \sum_{i=1}^3 r_i^{(B')} \bar{B}'_L \phi_R^\dagger Q_{iR} \\
& + y_T \bar{T}_L \sigma T_R + y_{T'} \bar{T}'_L \sigma T'_R + y_{B_1} \bar{B}_{1L} \rho B_{1R} + y_{B_2} \bar{B}_{2L} \sigma B_{2R} + y_{B'} \bar{B}'_L \sigma B'_R \\
& + \sum_{n=1}^2 y_{E_n} \bar{E}_{nL} \rho E_{nR} + y_{E'} \bar{E}'_L \rho E'_R + \sum_{i=1}^3 \sum_{n=1}^2 x_{in}^{(E)} \bar{L}_{iL} \chi_L E_{nR} \\
& + \sum_{n=1}^2 \sum_{i=1}^3 z_{nj}^{(E)} \bar{E}_{nL} \chi_R^\dagger L_{jR} + \sum_{i=1}^3 w_i^{(E')} \bar{L}_{iL} \phi_L E'_R + \sum_{i=1}^3 r_i^{(E')} \bar{E}'_L \phi_R^\dagger L_{iR} \\
& + \sum_{i=1}^3 \sum_{j=1}^3 y_{ij}^{(L)} \bar{L}_{iL} \Phi L_{jR} + \sum_{i=1}^3 \sum_{j=1}^3 x_{ij}^{(N)} \bar{N}_{iR}^C \tilde{\chi}_R^\dagger L_{jR} + \sum_{n=1}^2 (y_{\Omega_n}) \bar{\Omega}_{nR} \Omega_{nR}^C \eta \\
& + \sum_{i=1}^3 \sum_{k=1}^2 x_{ik}^{(S)} \bar{N}_{iR} \Omega_{kR}^C \varphi + H.c.
\end{aligned} \tag{12}$$