

# Collinear Nucleon Structure at Large X

HEP-2023

Jan 9-13, 2023, at UTFSM, Valparaiso (Chile)



Sebastian Kuhn

*Old Dominion University, Norfolk (VA), USA*

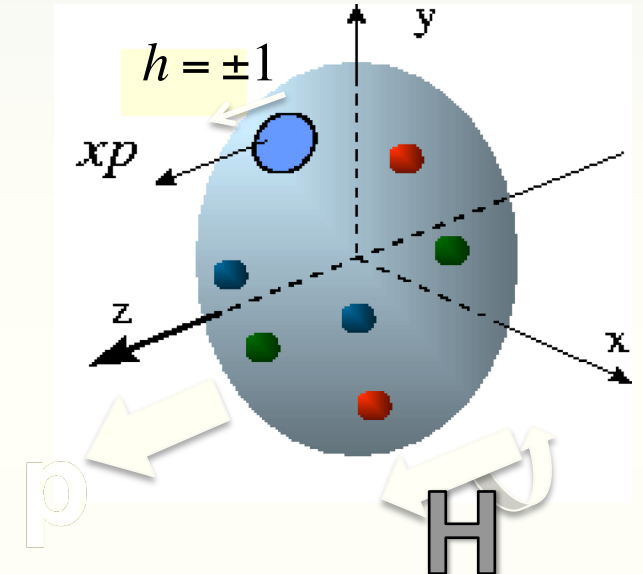
# Overview

- Longitudinal valence structure of the nucleon
  - Why do we care?
  - Where are we right now? What do we need?
- Unpolarized structure function of the neutron
  - The overall landscape
  - BONuS12 experiment at Jefferson Lab
- Spin structure at high  $x$ 
  - Existing world data
  - Recent results (Exp. and Theory)
  - Upcoming experiments
- The polarized EMC effect
- Future Facilities – what more can we do?
  - JLab at 20+ GeV?
  - EIC
- Conclusions



# Collinear Structure functions

- Understand origin of mass and spin of hadrons
- Important as limiting cases and constraints for TMDs, GPDs etc.
- Most stringent tests of pQCD, Lattice QCD and phenomenological models
  - NN...LO + DGLAP \*)
  - Sophisticated and mature PDF extractions
  - Well-established higher twist and target mass effects
  - Quark-hadron duality
- Important input for collider physics
- Input for investigations of modifications of quark distributions in nuclei



$$q(x; Q^2), \langle h \cdot H \rangle q(x; Q^2)$$

“1-D” Parton Distributions (PDFs)  
(integrated over all transverse variables)

$$\begin{aligned}
 *) \text{E.g., } g_1^p(x, Q^2) &= \frac{1}{2} \sum_q e_q^2 \Delta q_v(x, Q^2) \otimes \left( 1 + \frac{\alpha_s(Q^2)}{2\pi} \Delta C_q^{(1)} + \left( \frac{\alpha_s(Q^2)}{2\pi} \right)^2 \Delta C_{ns}^{(2)} \right) \\
 &+ e_q^2 (\Delta q_s + \Delta \bar{q}_s)(x, Q^2) \otimes \left( 1 + \frac{\alpha_s(Q^2)}{2\pi} \Delta C_q^{(1)} + \left( \frac{\alpha_s(Q^2)}{2\pi} \right)^2 \Delta C_s^{(2)} \right) \\
 &+ \frac{2}{9} \left( \frac{\alpha_s(Q^2)}{2\pi} \Delta C_g^{(1)} + \left( \frac{\alpha_s(Q^2)}{2\pi} \right)^2 \Delta C_g^{(2)} \right) \otimes \Delta g(x, Q^2)
 \end{aligned}$$

# Valence Region: Structure Functions for $x \rightarrow 1$

- Dominated by up and down valence quarks  $\rightarrow$  quantum numbers of the nucleon
- Important for higher power  $x^n$  moments  $\rightarrow$  Mellin Moments, LQCD
- Related to high- $Q^2$ , moderate  $x$  through DGLAP
- MANY predictions based on models, pQCD and Lattice QCD \*):

SU(6)-symmetric proton wave function in the “naïve” quark model:

$$|p\uparrow\rangle = \frac{1}{\sqrt{18}} (3u\uparrow[ud]_{S=0} + u\uparrow[ud]_{S=1} - \sqrt{2}u\downarrow[ud]_{S=1} - \sqrt{2}d\uparrow[uu]_{S=1} - 2d\downarrow[uu]_{S=1})$$

In this model:  $d/u = 1/2$ ,  $\Delta u/u = 2/3$ ,  $\Delta d/d = -1/3$  for all  $x$

Hyperfine structure effect in QM:  $S=1$  suppressed  $\Rightarrow d/u = 0$ ,  $\Delta u/u = 1$ ,  $\Delta d/d = -1/3$   
for  $x \rightarrow 1$

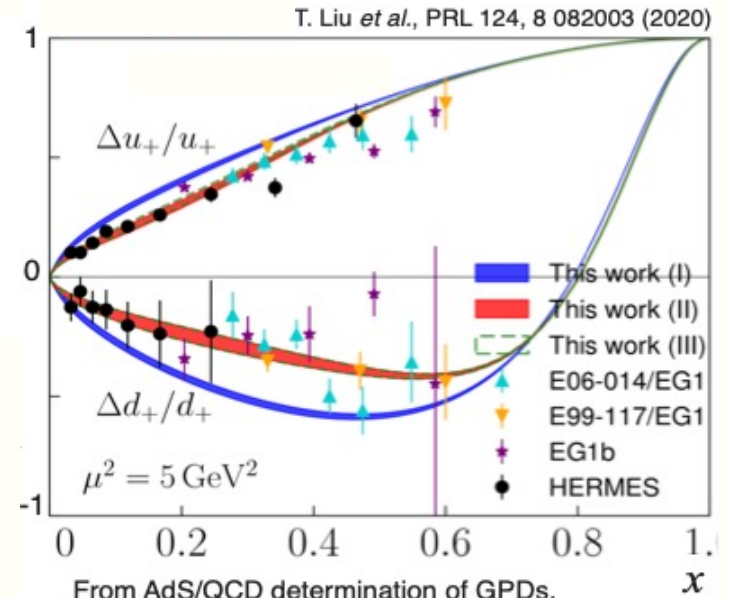
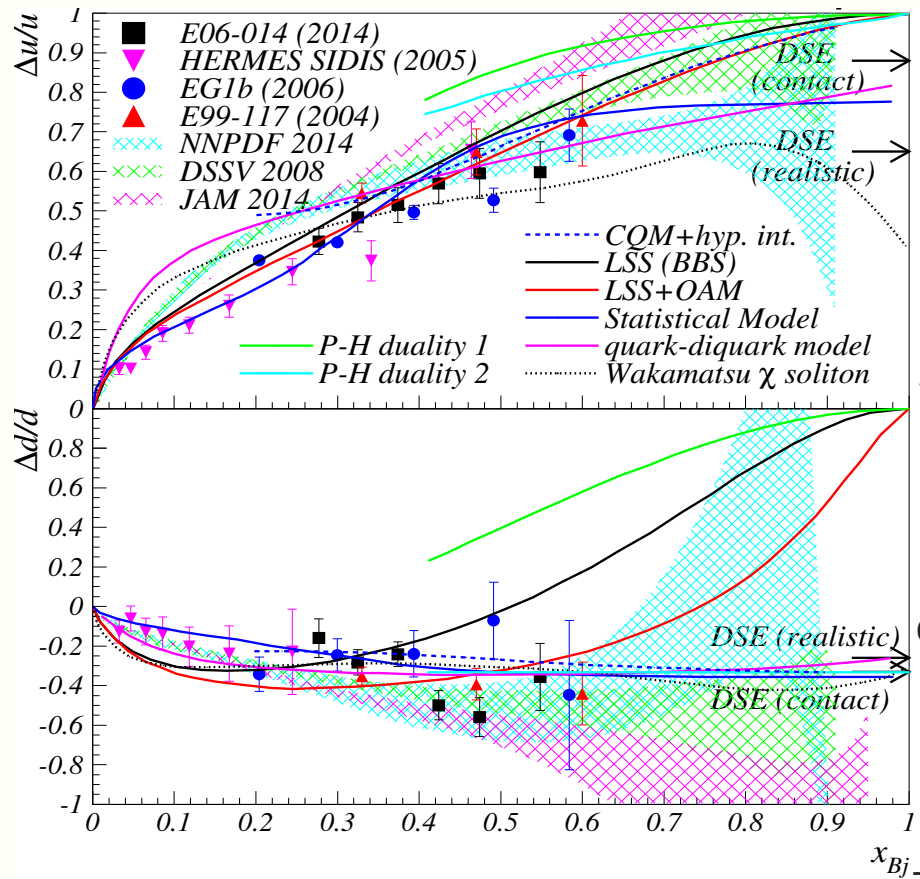
pQCD: helicity conservation ( $q\uparrow\uparrow p$ )  $\Rightarrow d/u \rightarrow 2/(9+1) = 1/5$ ,  $\Delta u/u \rightarrow 1$ ,  $\Delta d/d \rightarrow 1$  for  $x \rightarrow 1$

Other approaches: Dyson-Schwinger Equation, statistical models, pQCD + orbital angular momentum, AdS (Light-front holographic QCD)

\*) Moments, quasi-PDFs, pseudo-PDFs



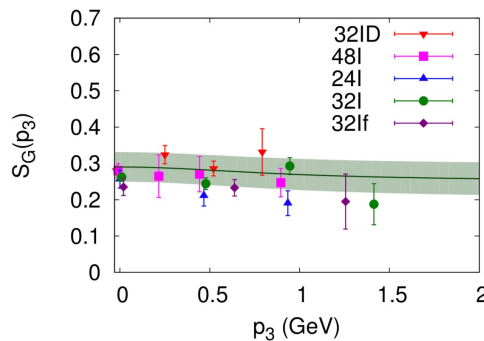
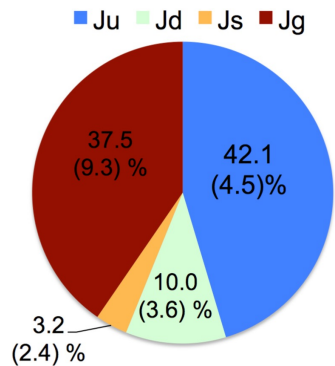
# Recent theoretical predictions



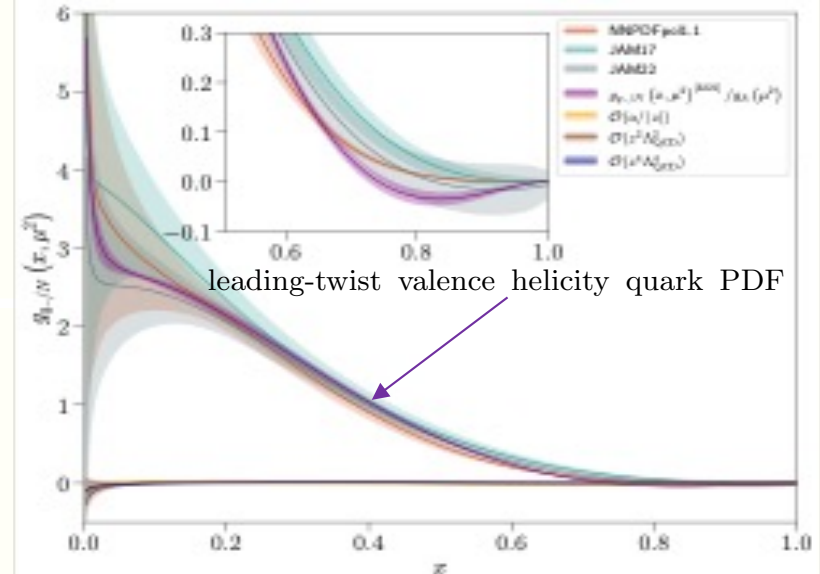
From AdS/QCD determination of GPDs.  
**No free parameters.**  
 Predicts  $\Delta d/d$  changes sign near  $x=0.8$ .  
 Reproduces QCD counting rules used for BBS/LSS.

R.G. Edwards et al. JLAB-THY-22-3751 arXiv:2211.04434v1  
 Non-singlet quark helicity PDFs of the nucleon from pseudo-distributions

Ji, Yuan and Zhao: arXiv2009.01291 [hep-ph]



LATTICE QCD



# High-x PDFs: Input for Collider experiments

## Ex.: High-Precision Measurement of the W Boson Mass with the CDF II Detector

Ashutosh Kotwal, Duke University

Jefferson Lab Users Meeting June 14, 2022

### Parton Distribution Functions

- Affect W boson kinematic line-shapes through acceptance cuts
- We use NNPDF3.1 as the default NNLO PDFs
- Use ensemble of 25 'uncertainty' PDFs => 3.9 MeV
- Central values from NNLO PDF sets CT18, MMHT2014 and NNPDF3.1 agree within 2.1 MeV of their midpoint
- As an additional check, central values from NLO PDF sets ABMP16, CJ15, MMHT2014 and NNPDF3.1 agree within 3 MeV of their midpoint

“For example, the cj15 set includes all Tevatron data on the W -charge asymmetry, as well as the lepton- charge asymmetry from W boson decays and quasi-free neutron scattering data from the Jefferson Lab BONuS experiment [95, 96] “



Science  
AAAS

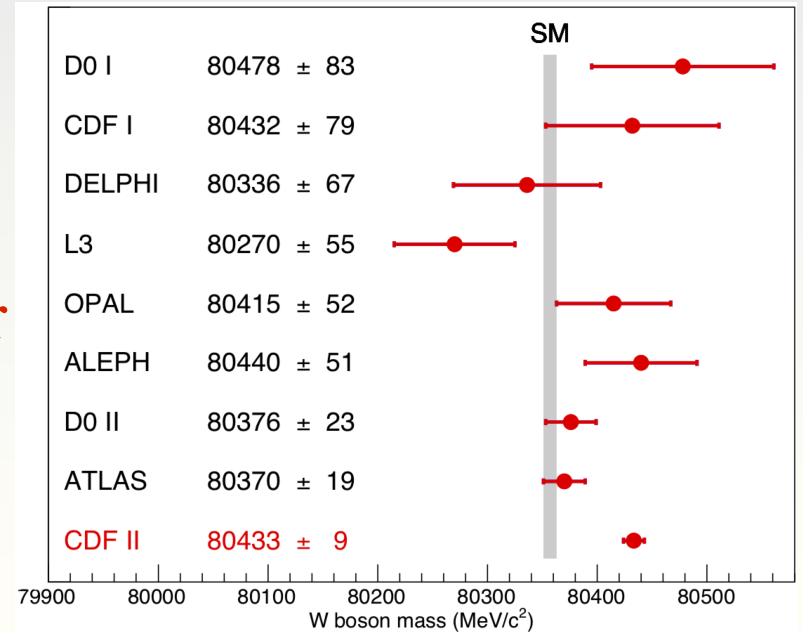
Supplementary Materials for

High-precision measurement of the W boson mass with the CDF II detector

CDF Collaboration

Corresponding author: A. V. Kotwal, ashutosh.kotwal@duke.edu

Science 376, 170 (2022)  
DOI: 10.1126/science.abk1781



CDF Collaboration *et al.*, *Science* **376**, 170–176 (2022)

95. N. Baillie, S. Tkachenko, J. Zhang, P. Bosted, S. Bültmann, M. E. Christy, H. Fenker, K. A. Griffioen, C. E. Keppel, S. E. Kuhn, W. Melnitchouk, V. Tvaskis, K. P. Adhikari, D. ... Measurement of the neutron  $F_2$  structure function via spectator tagging with CLAS. *Phys. Rev. Lett.* **108**, 142001 (2012). [doi:10.1103/PhysRevLett.108.142001](https://doi.org/10.1103/PhysRevLett.108.142001) [Medline](#)

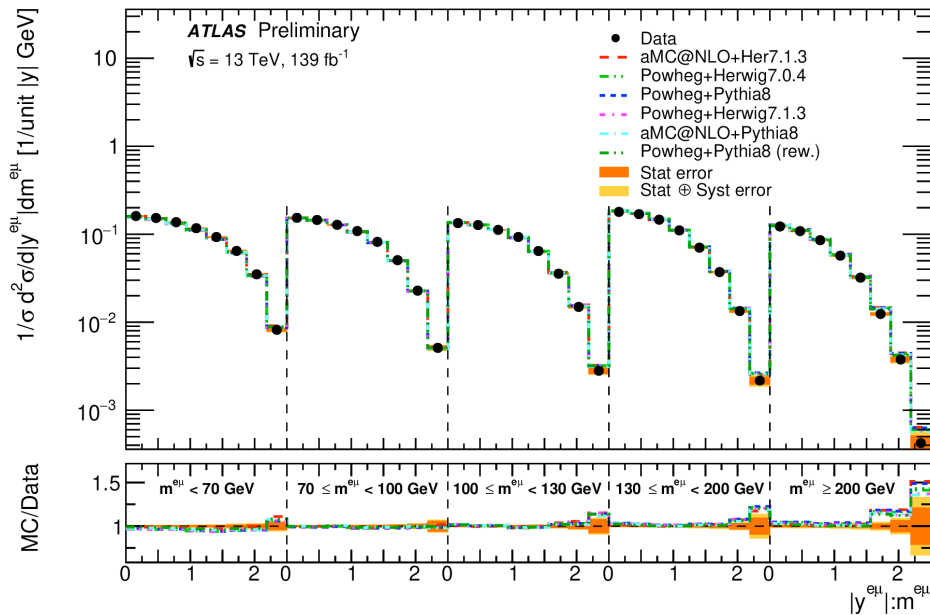
96. S. Tkachenko, N. Baillie, S. E. Kuhn, ...

D. Watts, X. Wei, L. B. Weinstein, M. H. Wood, L. Zana, I. Zonta, Measurement of the structure function of the nearly free neutron using spectator tagging in inelastic  $^2\text{H}(e,e'p_s)X$  scattering with CLAS. *Phys. Rev. C* **89**, 045206 (2014).



# Cross sections

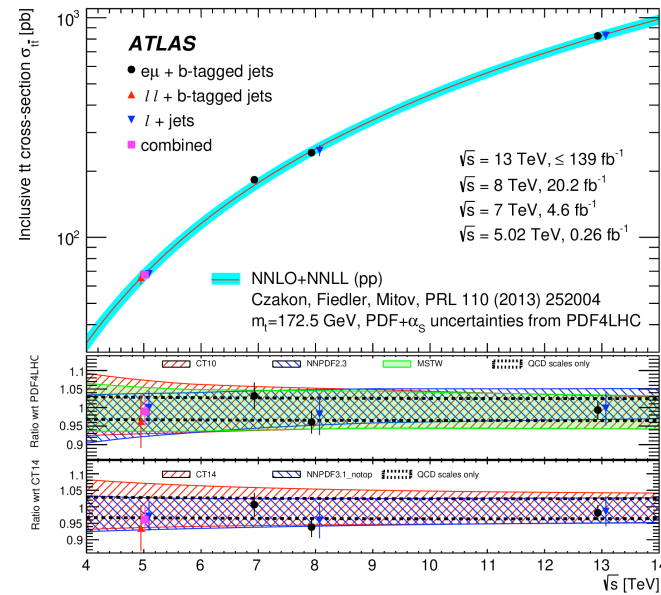
ATLAS-CONF-2022-061



- **Differential and double differential distributions**
- Full Run-2,  $e\mu$  final state
- Inclusive production cross section
  - $\sigma_{tt} = 836 \pm 1(\text{stat}) \pm 12(\text{syst}) \pm 16(\text{lumi}) \pm 2(\text{beam}) \text{pb}$

arXiv:2207.01354

TOPQ-2018-40



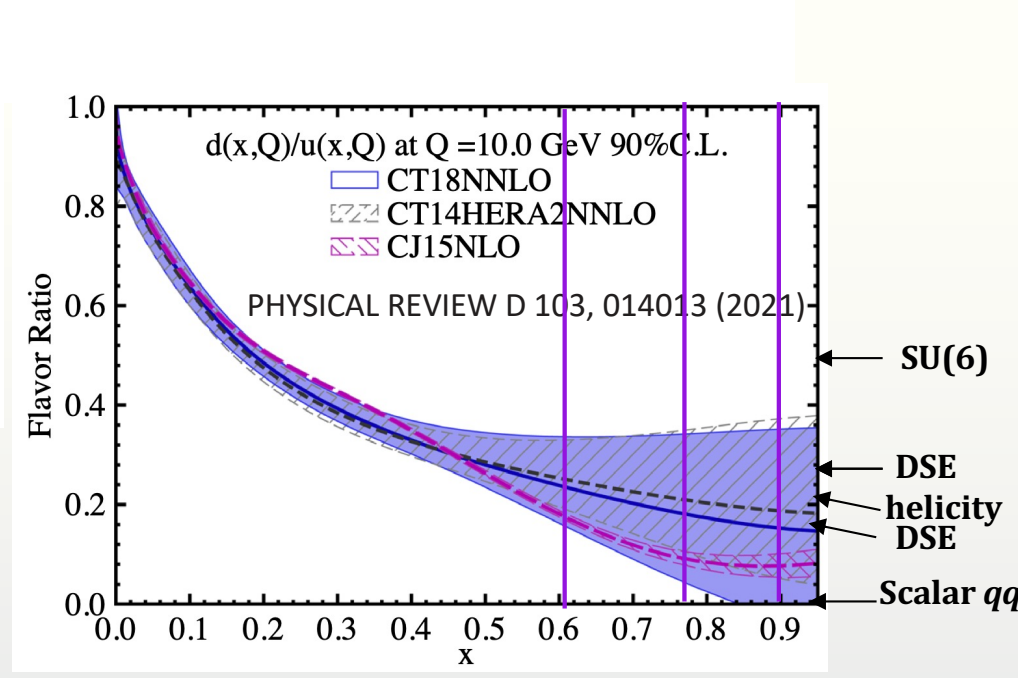
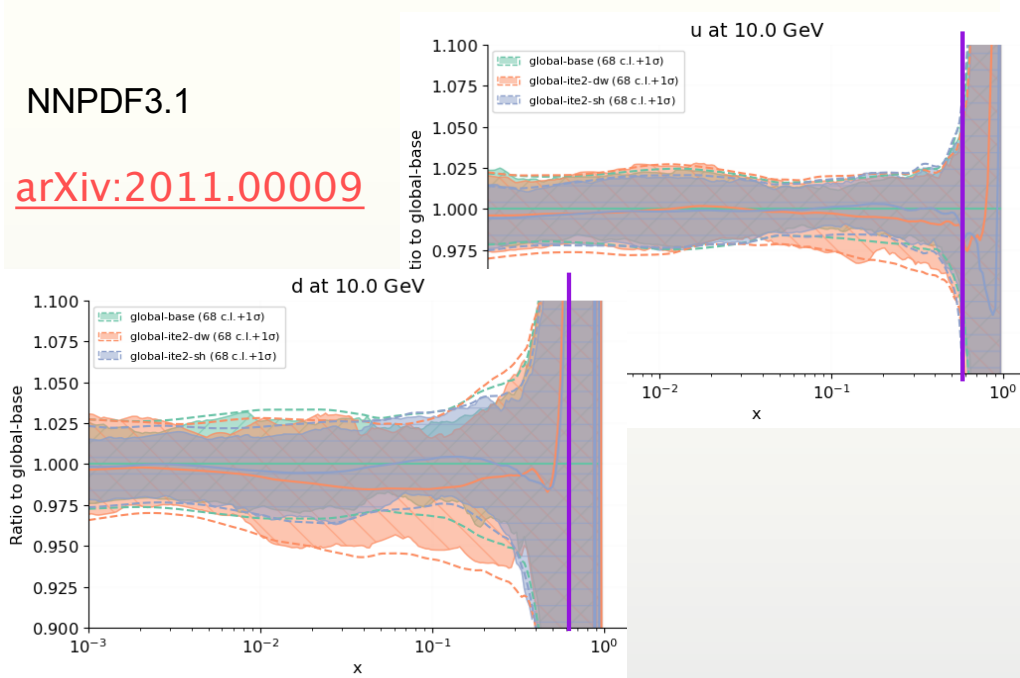
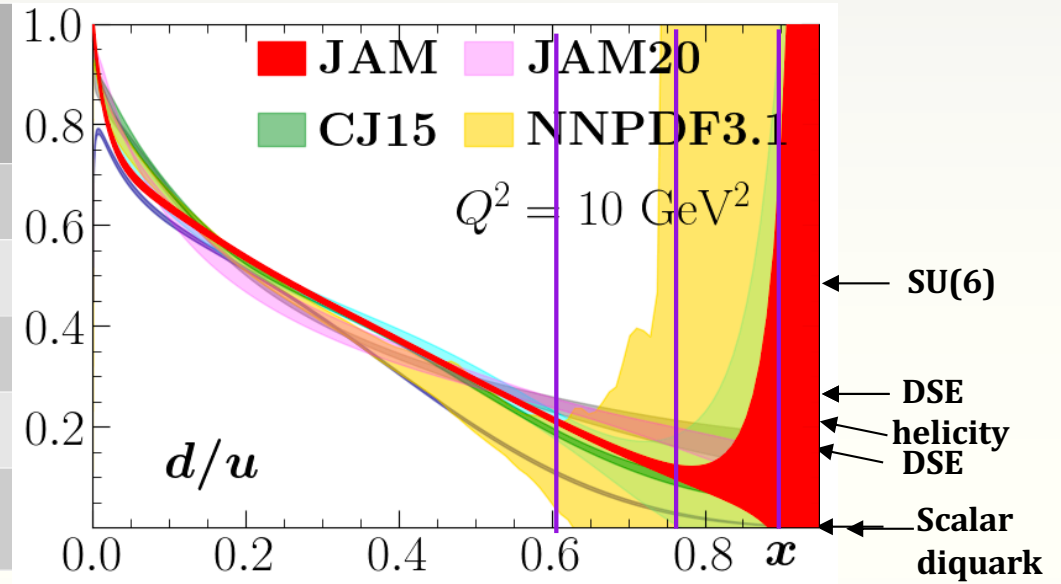
- **5.02 TeV**
- dilepton and single-lepton
- $\sigma_{tt} = 67.5 \pm 0.9(\text{stat.}) \pm 2.3(\text{syst.}) \pm 1.1(\text{lumi.}) \pm 0.2(\text{beam}) \text{pb}$
- Relative uncertainty  $\sim 3.9\%$
- In agreement with theoretical QCD calculations at NNLO
- **Constrains proton parton distribution functions at large Bjorken-x**

- **Run-1, 7 TeV  $l$ -jets**
- Multidimensional event classifier based on [support vector machines](#)
- $\sigma_{tt} = 168.5 \pm 0.7(\text{stat.}) + 6.2 - 5.9(\text{syst.}) + 3.4 - 3.2(\text{lumi.}) \text{pb}$

TOPQ-2017-08  
arXiv:2212.00571

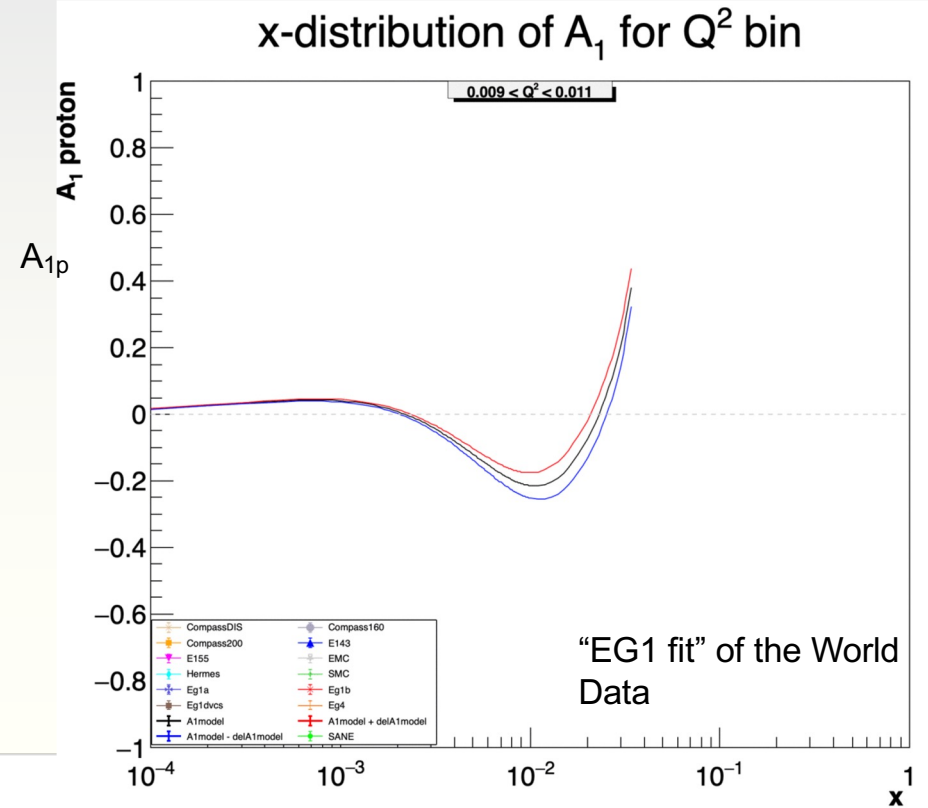
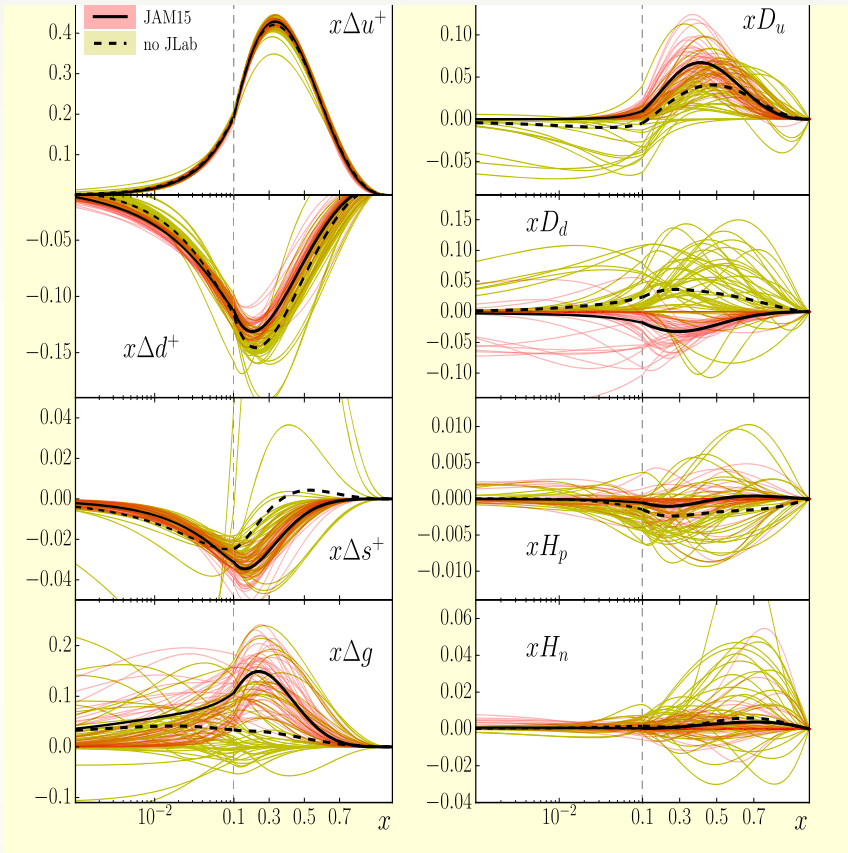
# Unpolarized PDFs— high $x$

Nucleon Model	$F_2^n/F_2^p$ $X \rightarrow 1$	$d/u$ $X \rightarrow 1$
SU(6) Symmetry	2/3	0.5
Scalar diquark dominance	1/4	0
DSE contact interaction	0.41	0.18
DSE realistic interaction	0.49	0.28
PQCD (helicity conservation)	3/7	0.2

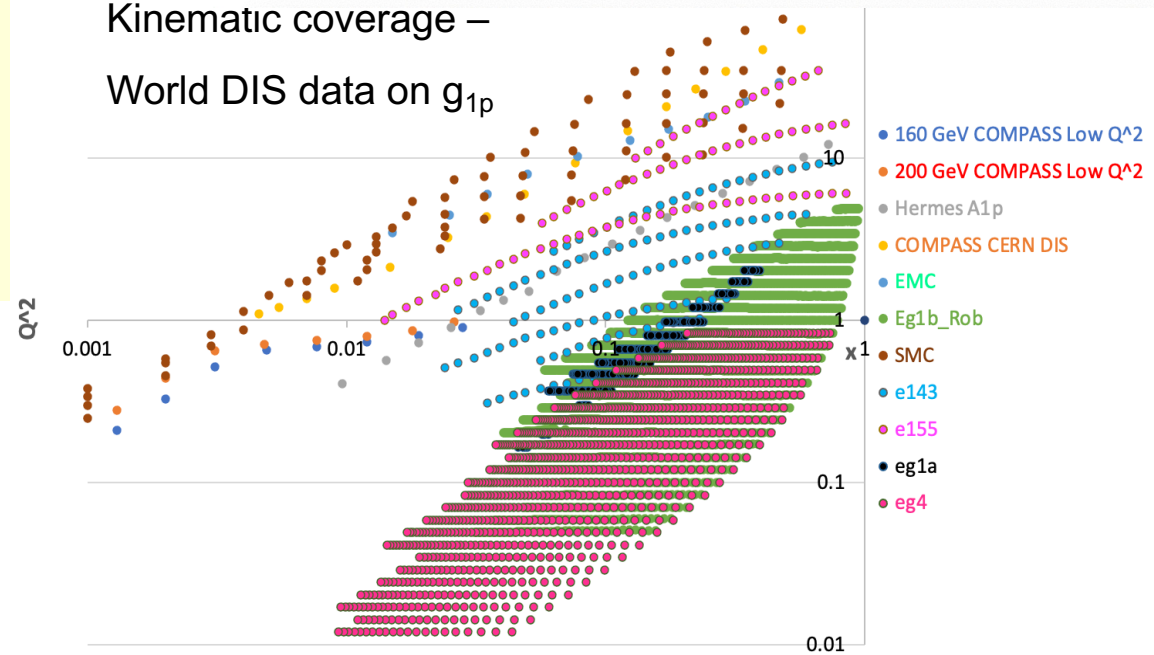




# Spin Structure Functions in the last 40 years



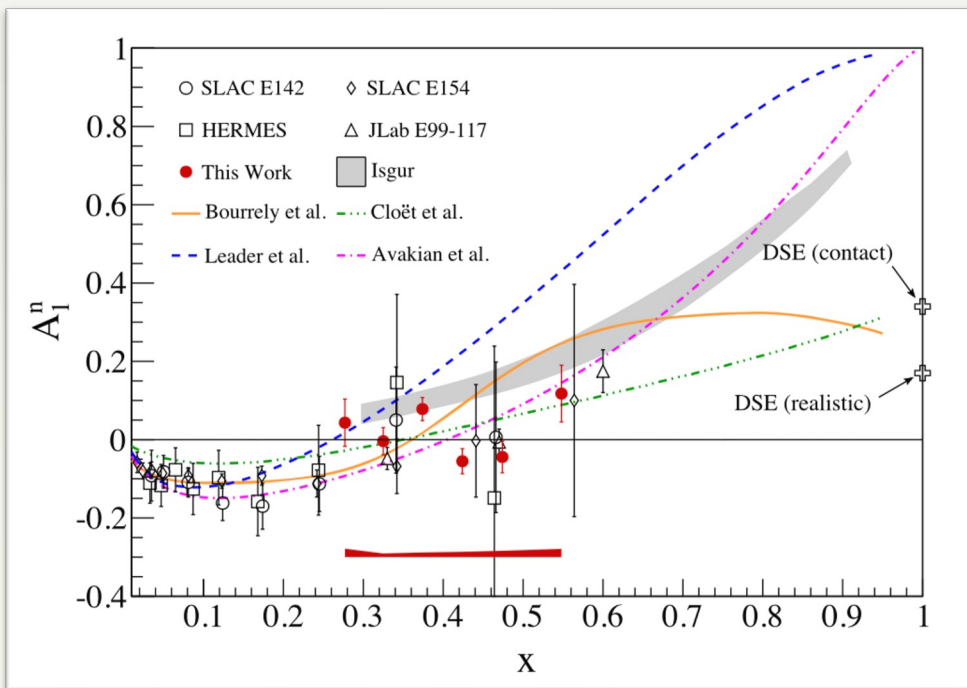
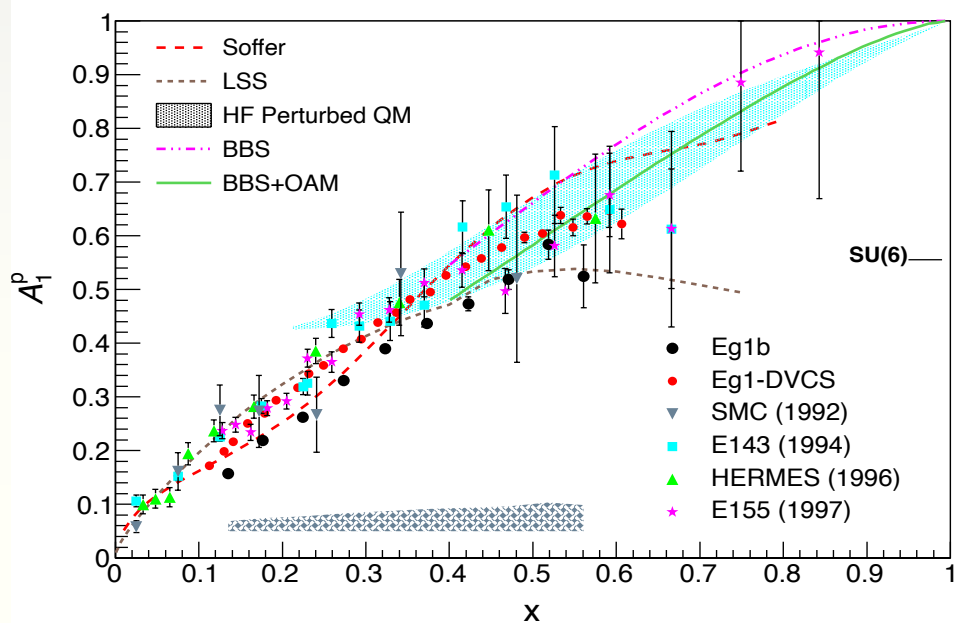
Kinematic coverage –  
World DIS data on  $g_{1p}$



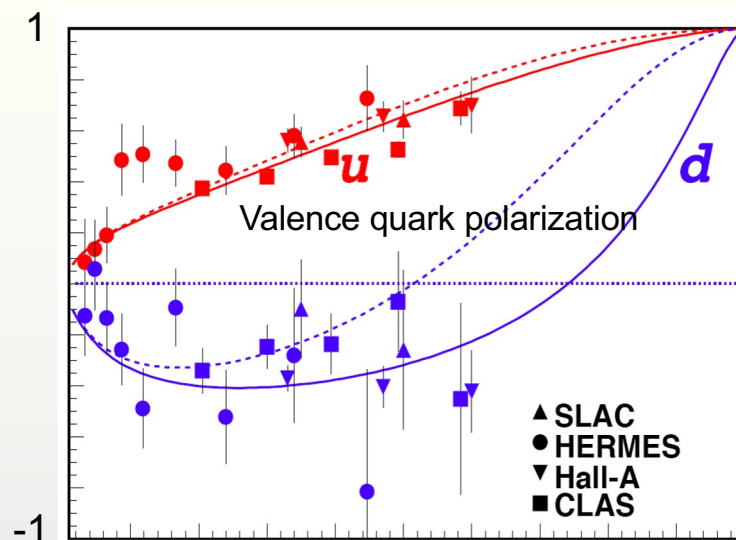
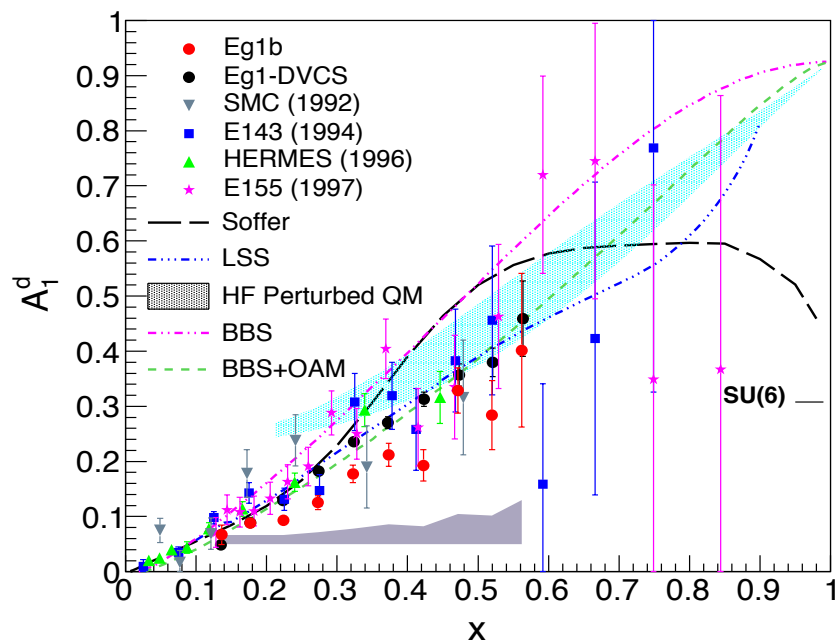
Nobuo Sato, W. Melnitchouk, S. E. Kuhn, J. J. Ethier, and A. Accardi: "Iterative Monte Carlo analysis of spin-dependent parton distributions", Phys. Rev. D **93**, 074005 (5 April 2016).

A. Deur, Y. Prok, V. Burkert, D. Crabb, F.-X. Girod, K. A. Griffioen, N. Guler, S. E. Kuhn, and N. Kvaltine: "High precision determination of the  $Q^2$  evolution of the Bjorken sum", Phys. Rev. C **90**, 012009 (July 2014).

# Existing Spin Structure Functions at high $x$



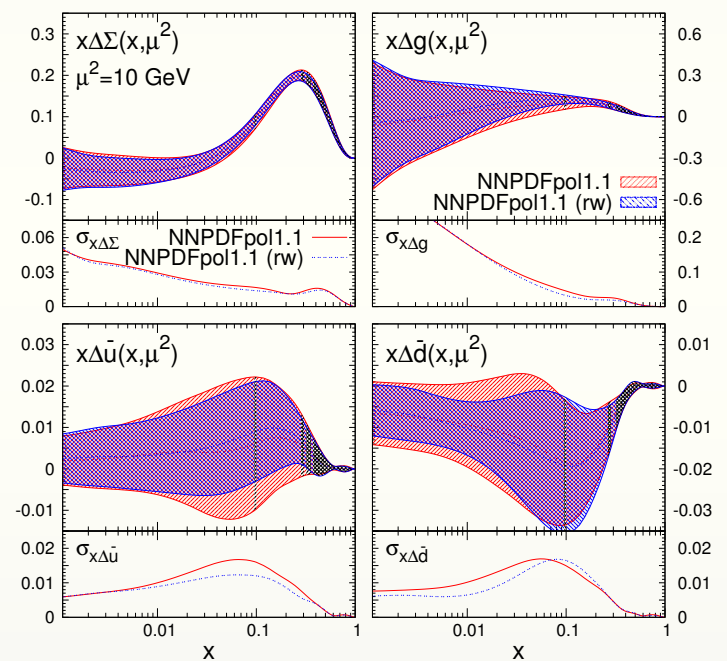
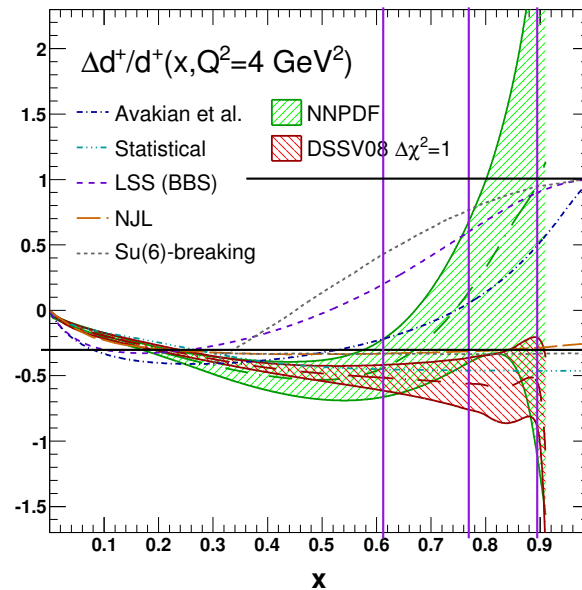
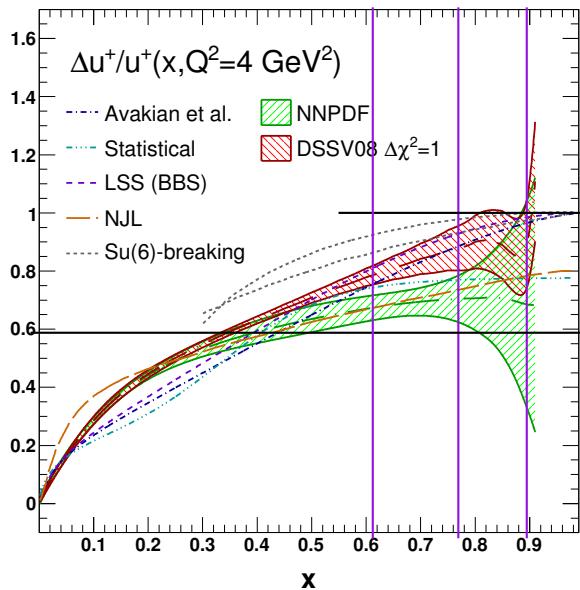
Parno et al., *Phy Let B* DOI: 10.1016/j.physletb.2015.03.067  
 X. Zheng et al., *PRL* 92, 012004 (2004); *PRC* 70, 065207 (2004)





# Present Status on polarized PDFs

- NNPDFpol1.1+RHIC W data analysis



arXiv:1410.7290v2 [hep-ph] 23 Jan 2015

arXiv:1702.05077v1 [hep-ph] 16 Feb 2017

# Present Status on polarized PDFs

- Newest JAM analysis including RHIC and COMPASS data

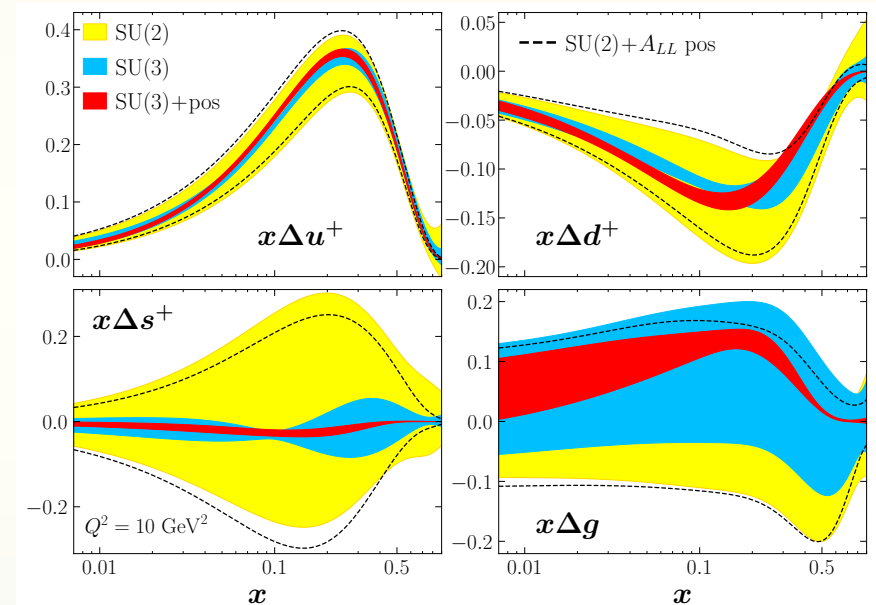
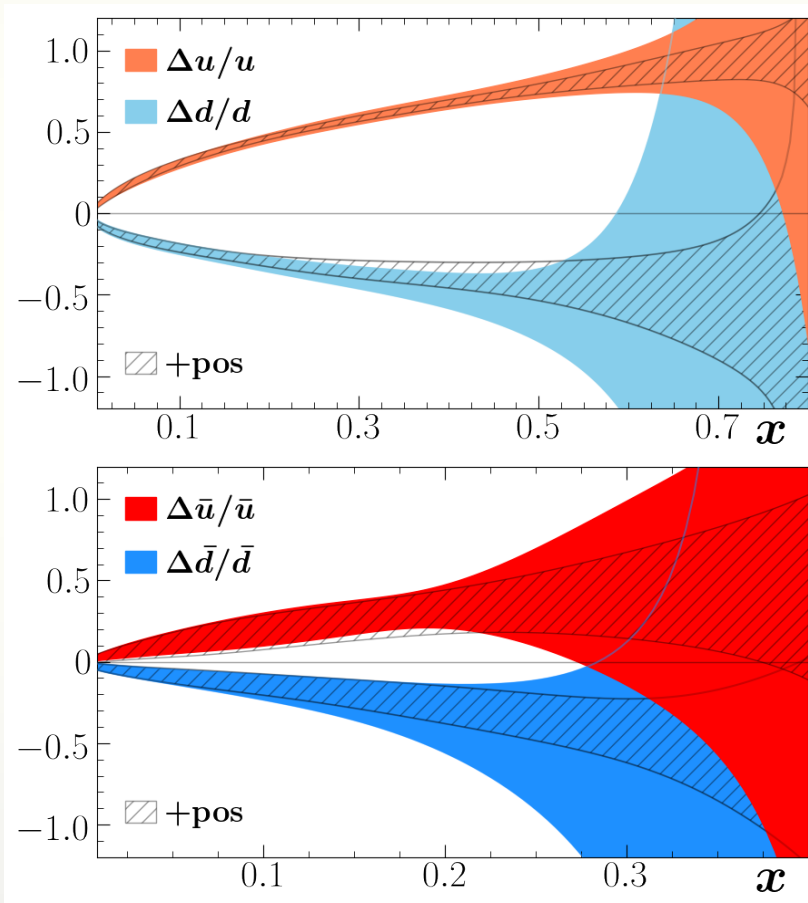
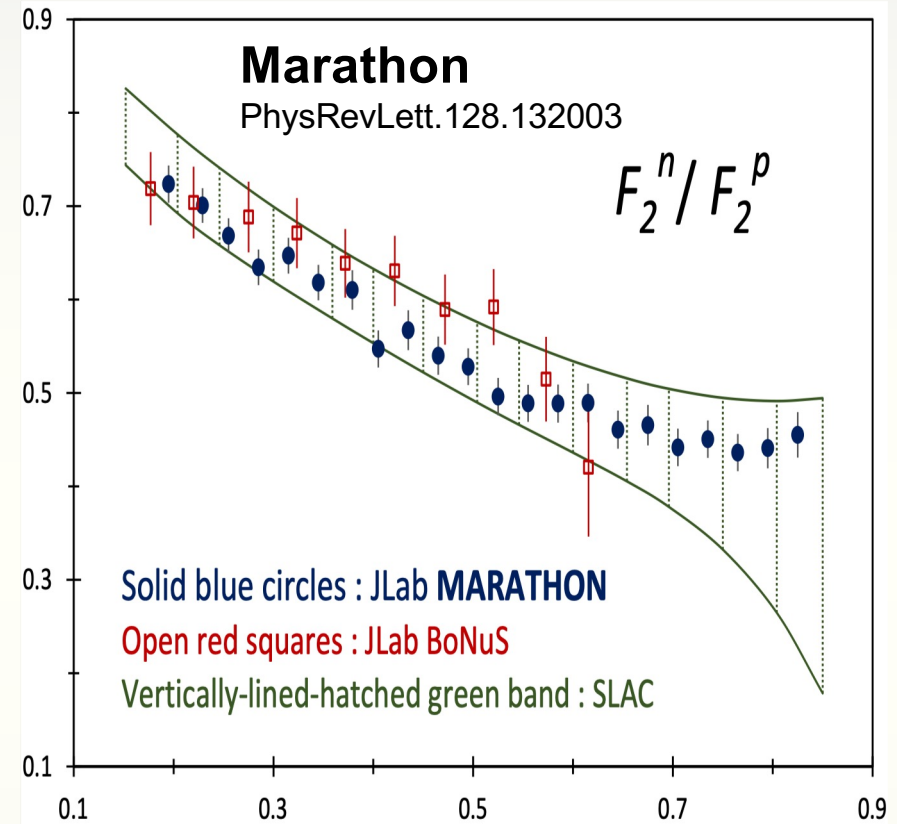
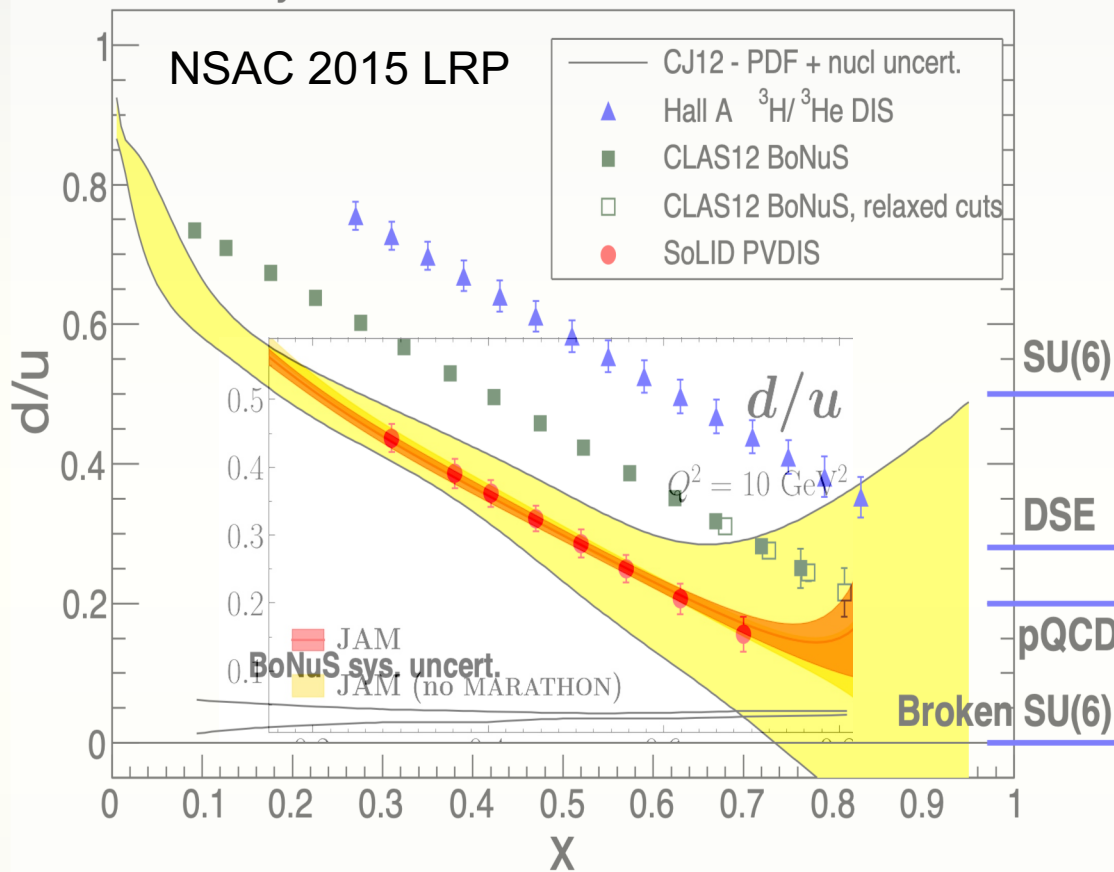


FIG. 6. Expectations values for spin-dependent  $\Delta u^+$ ,  $\Delta d^+$ ,  $\Delta s^+$ , and  $\Delta g$  PDFs at  $Q^2 = 10 \text{ GeV}^2$  fitted under various theory assumptions according to the SU(2) (yellow  $1\sigma$  bands), SU(3) (blue  $1\sigma$  bands) and SU(3)+positivity (red  $1\sigma$  bands) scenarios, as well as with the SU(2) scenario but filtered to ensure  $A_{LL}$  positivity at large  $x$  (dashed lines).

# JLab@12 GeV d/u



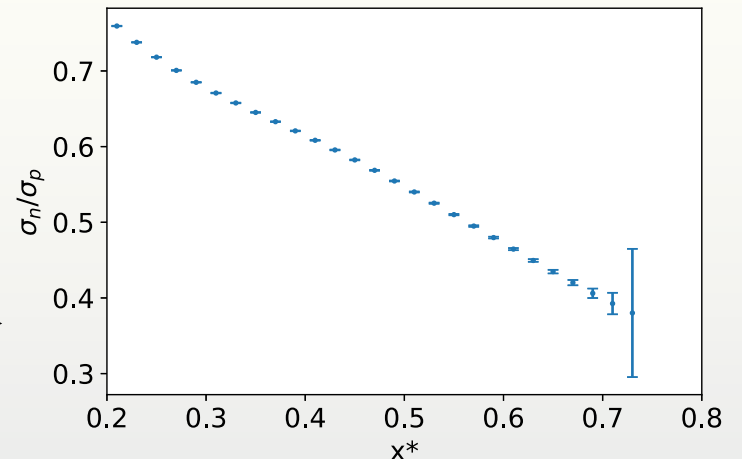
BONuS12:

**Dark Symbols:**  $W^* > 2 \text{ GeV}$  ( $x^*$  up to 0.8, bin centered  $x^* = 0.76$ )

**Open Symbols:** "Relaxed cut"  $W^* > 1.8 \text{ GeV}$  ( $x^*$  up to 0.83)

...also: Additional data from ALERT and TDIS →

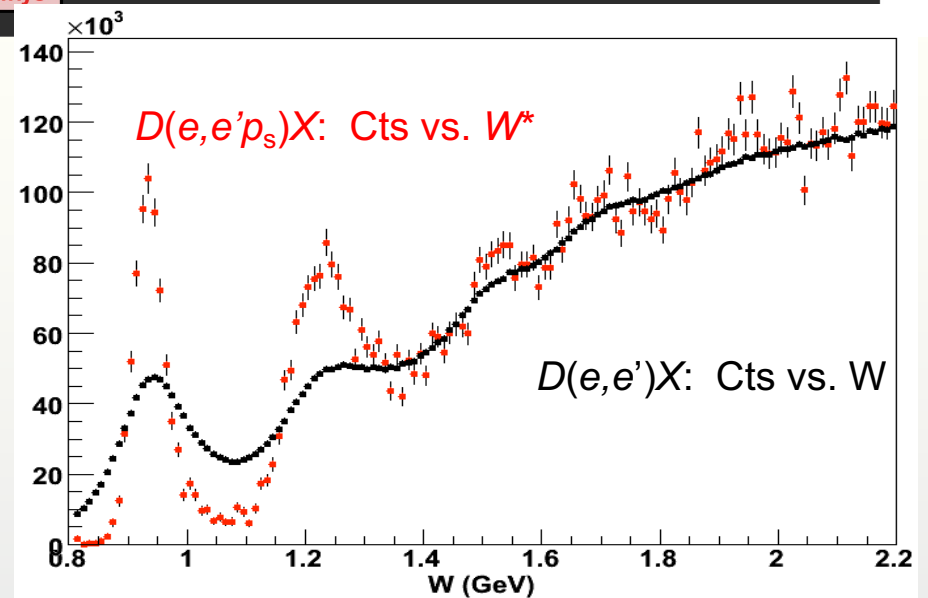
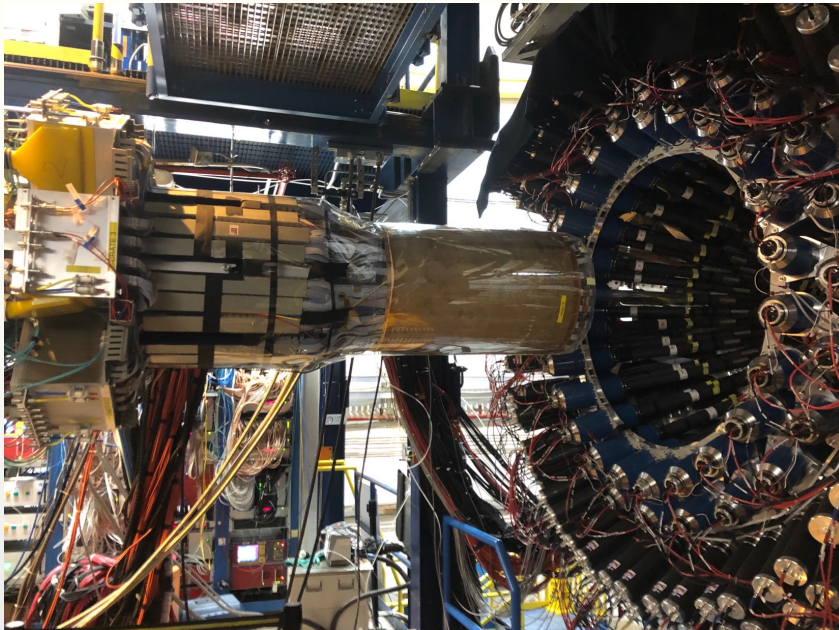
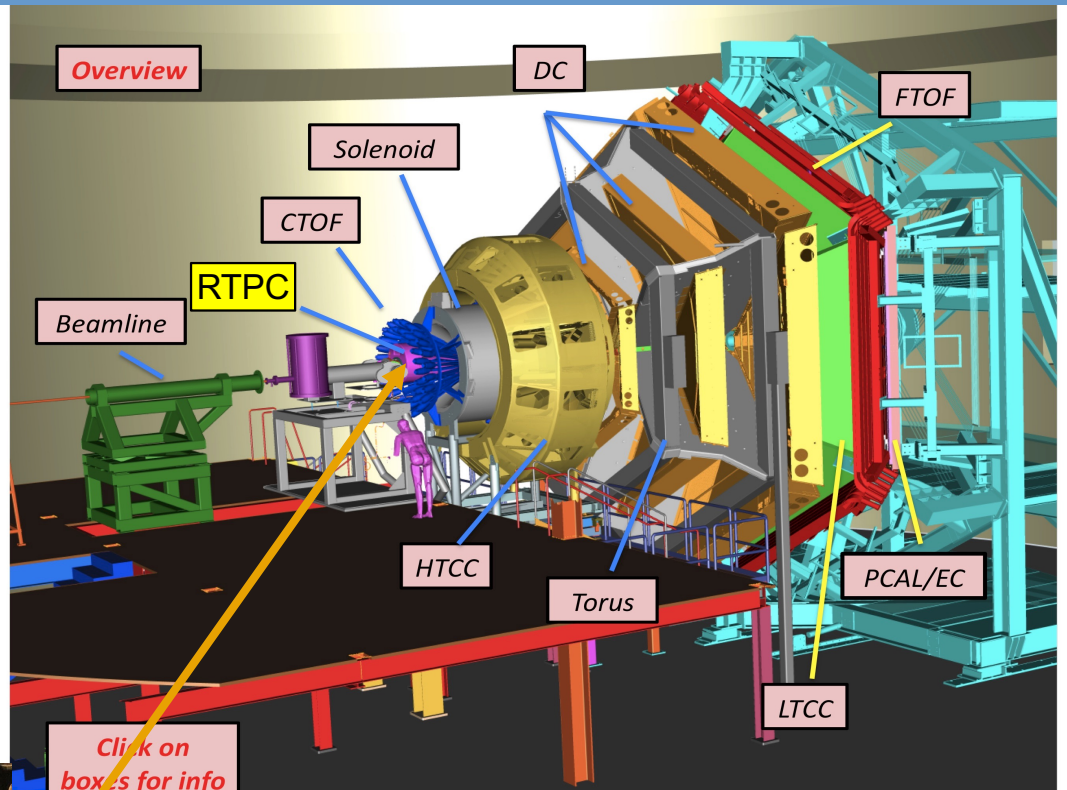
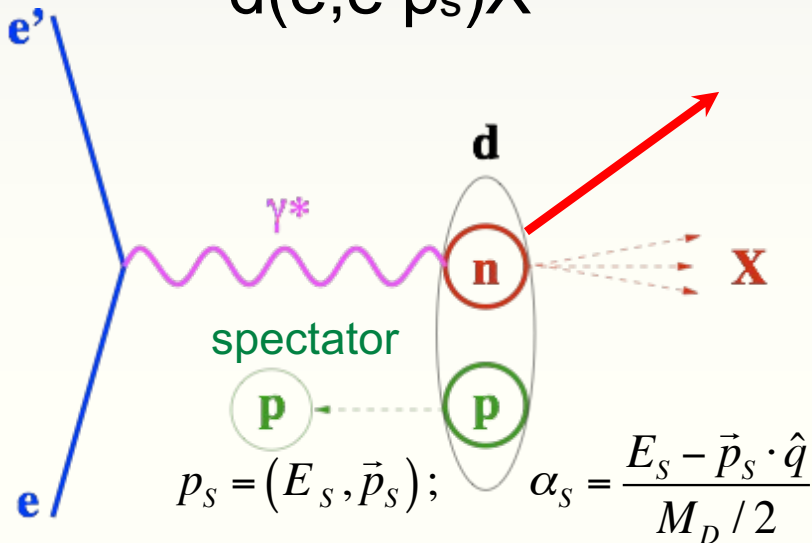
Courtesy Arun Tadepalli



# BONuS12 with CLAS12 (Run Group F in 2020)

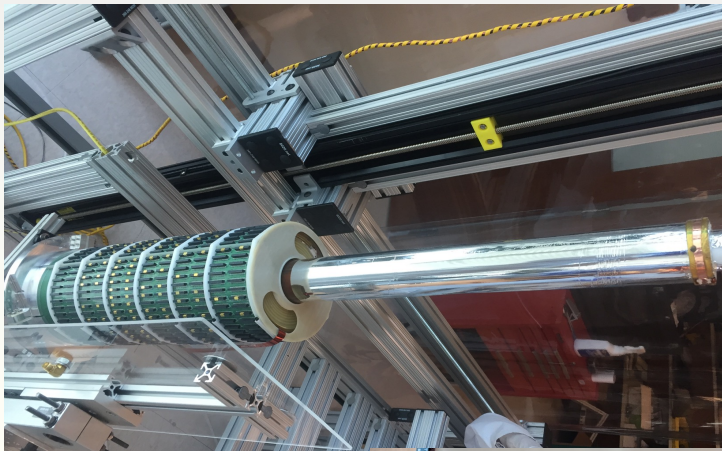
$F_{2n}/F_{2p}$  through spectator tagging

$d(e, e' p_s) X$

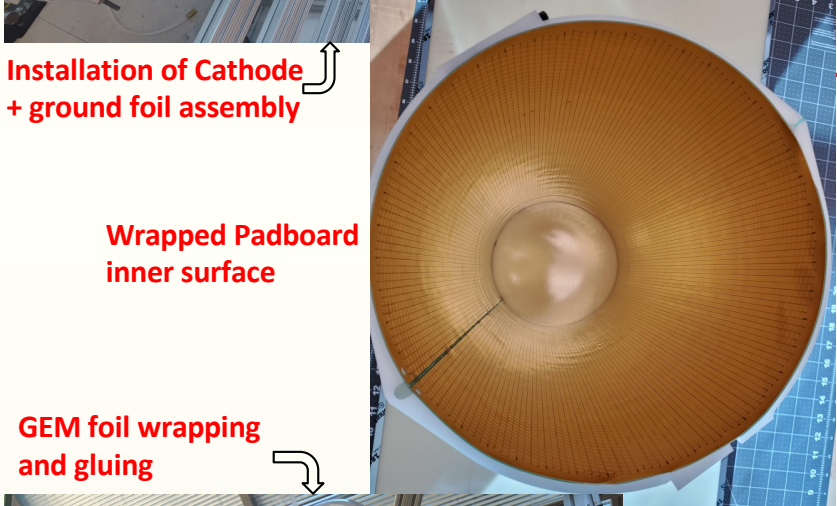




# BONuS12 Radial Time Projection Chamber

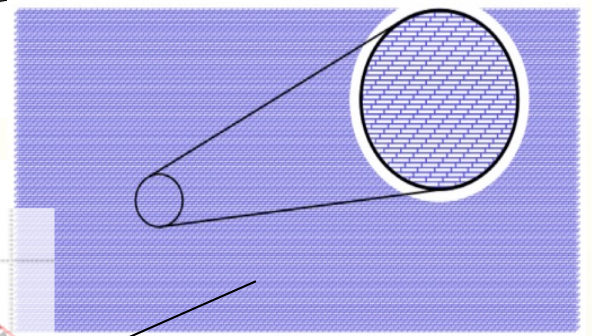
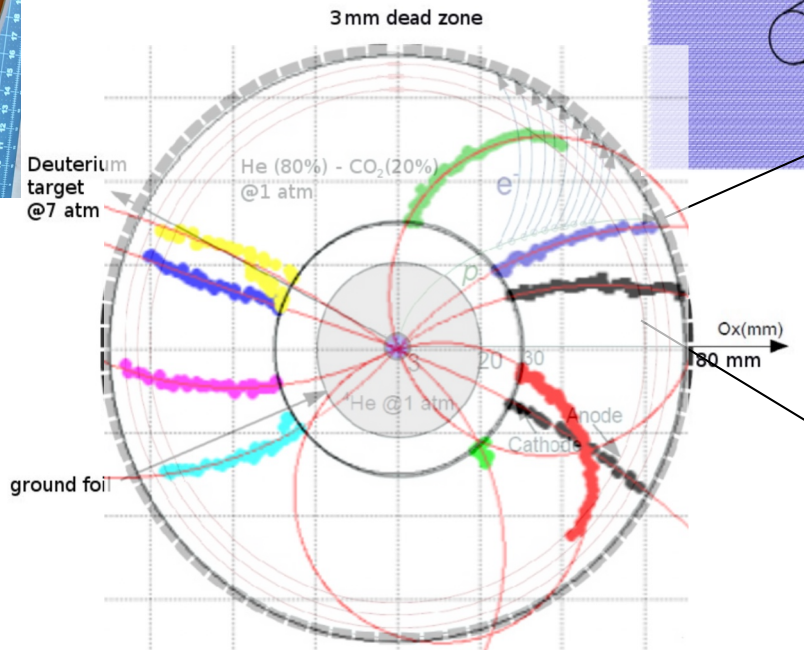
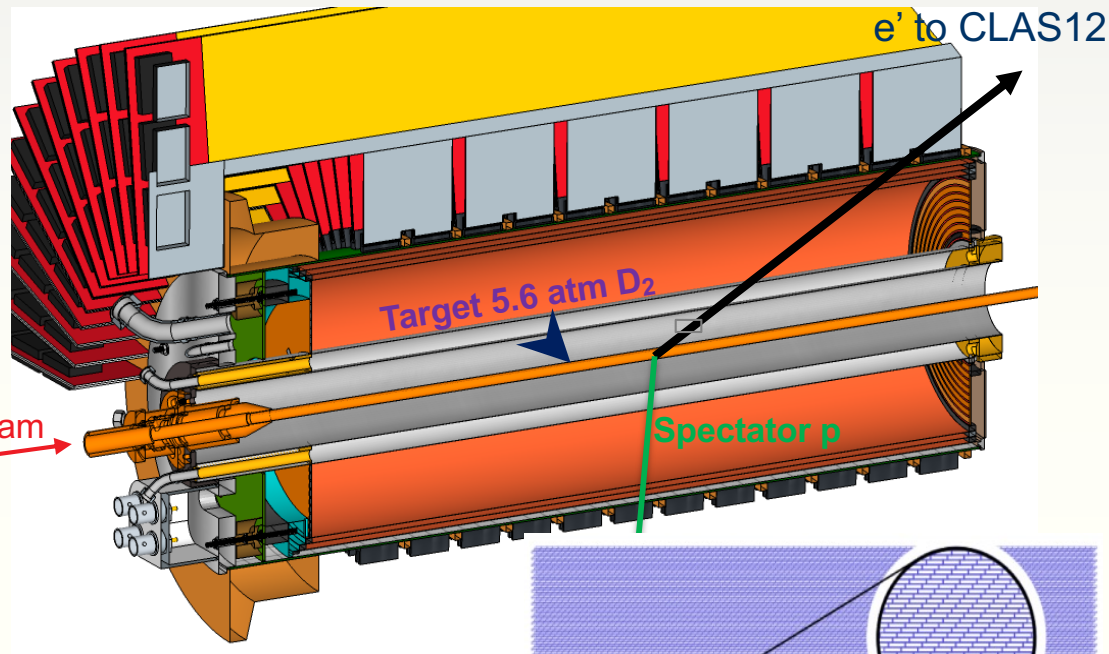
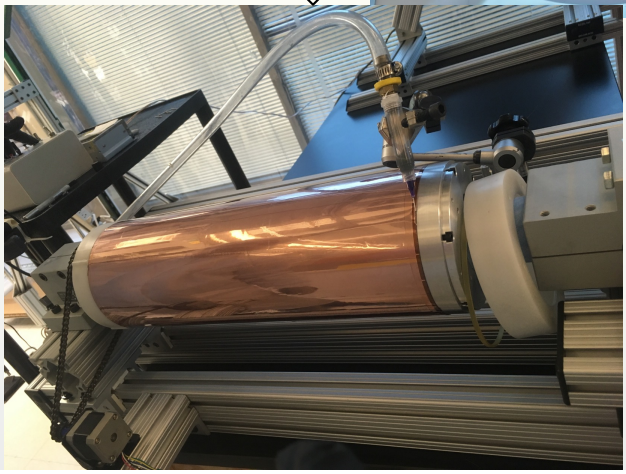


Installation of Cathode + ground foil assembly

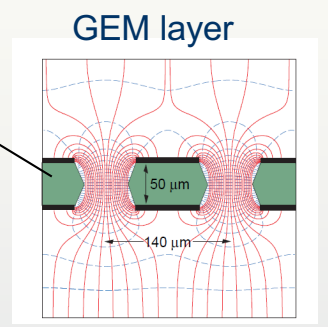


Wrapped Padboard inner surface

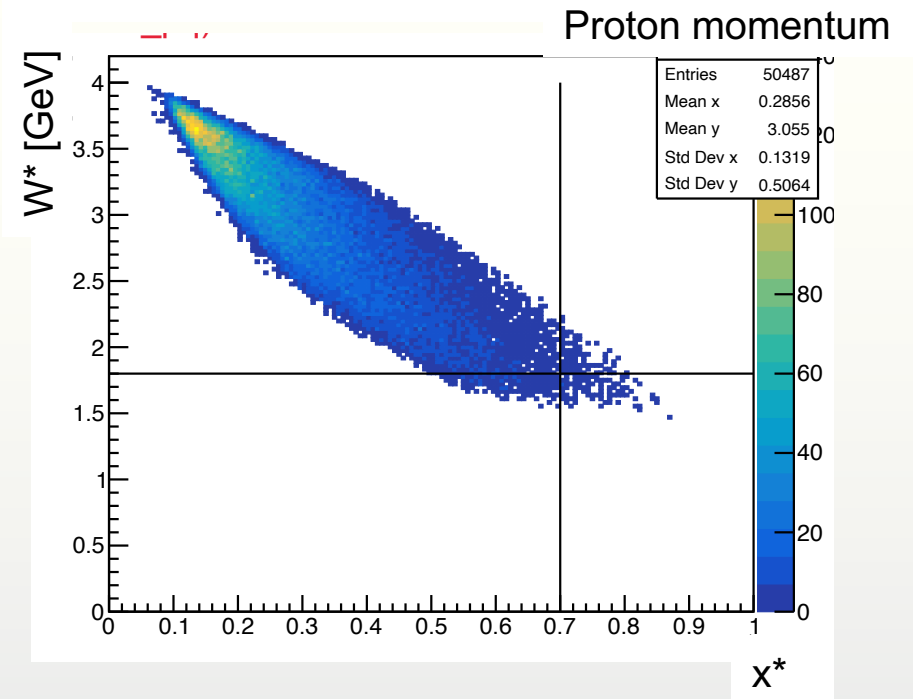
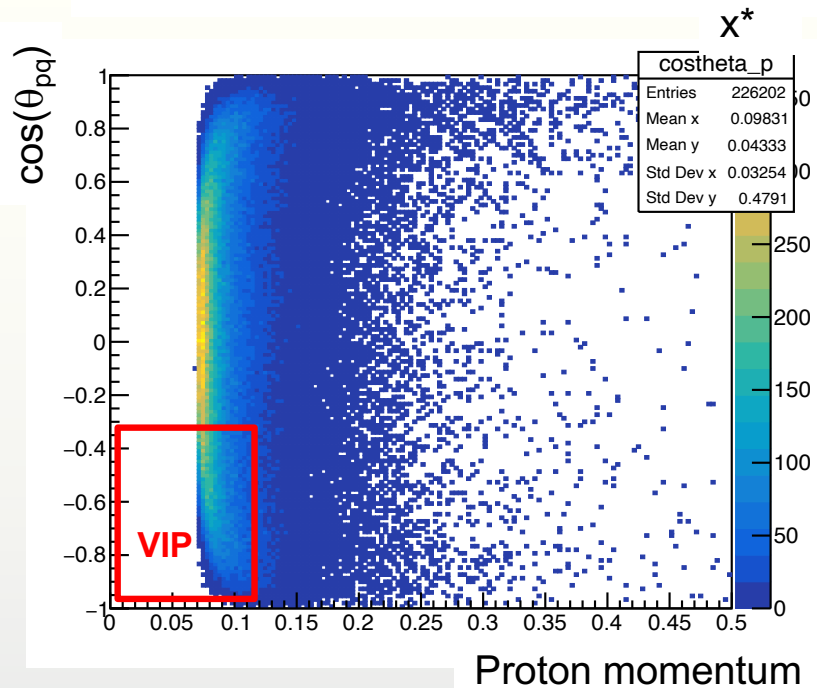
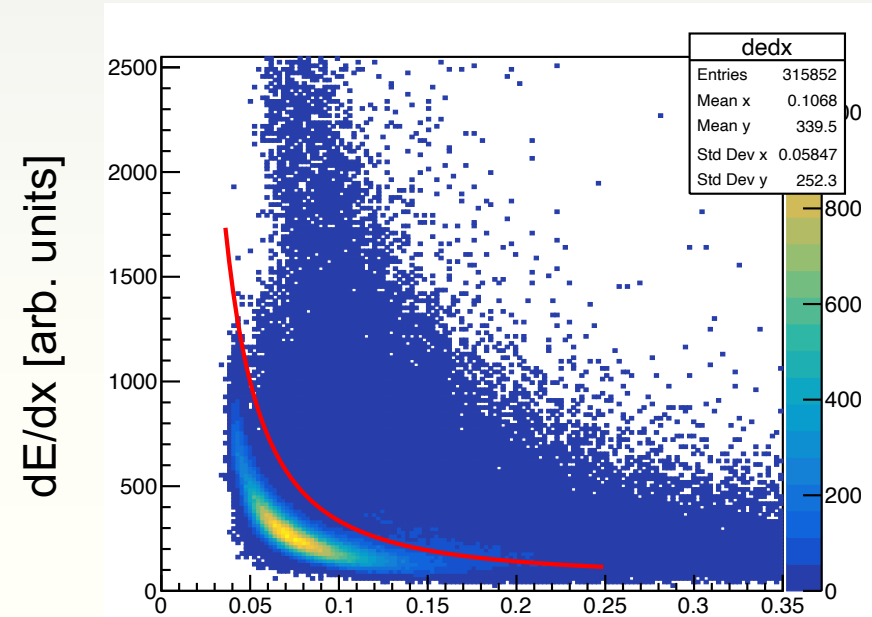
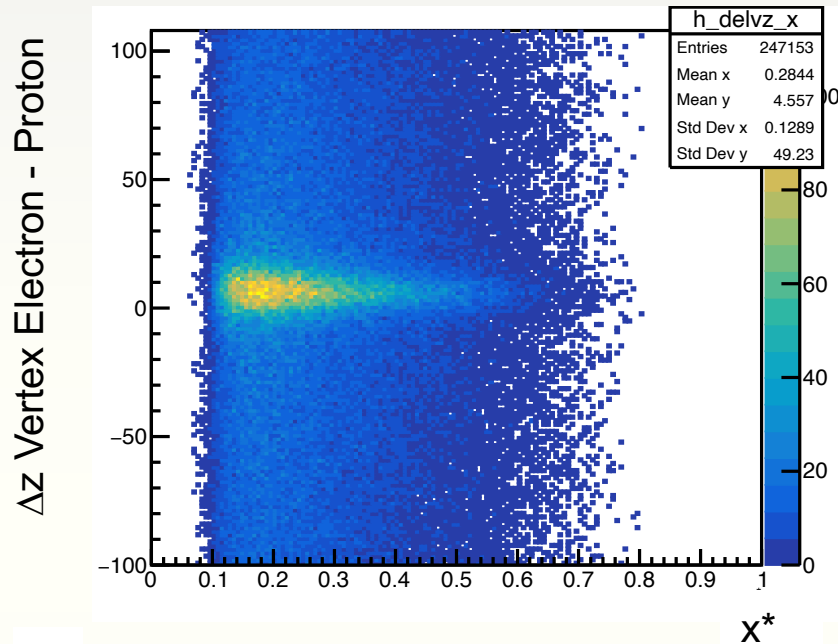
GEM foil wrapping and gluing



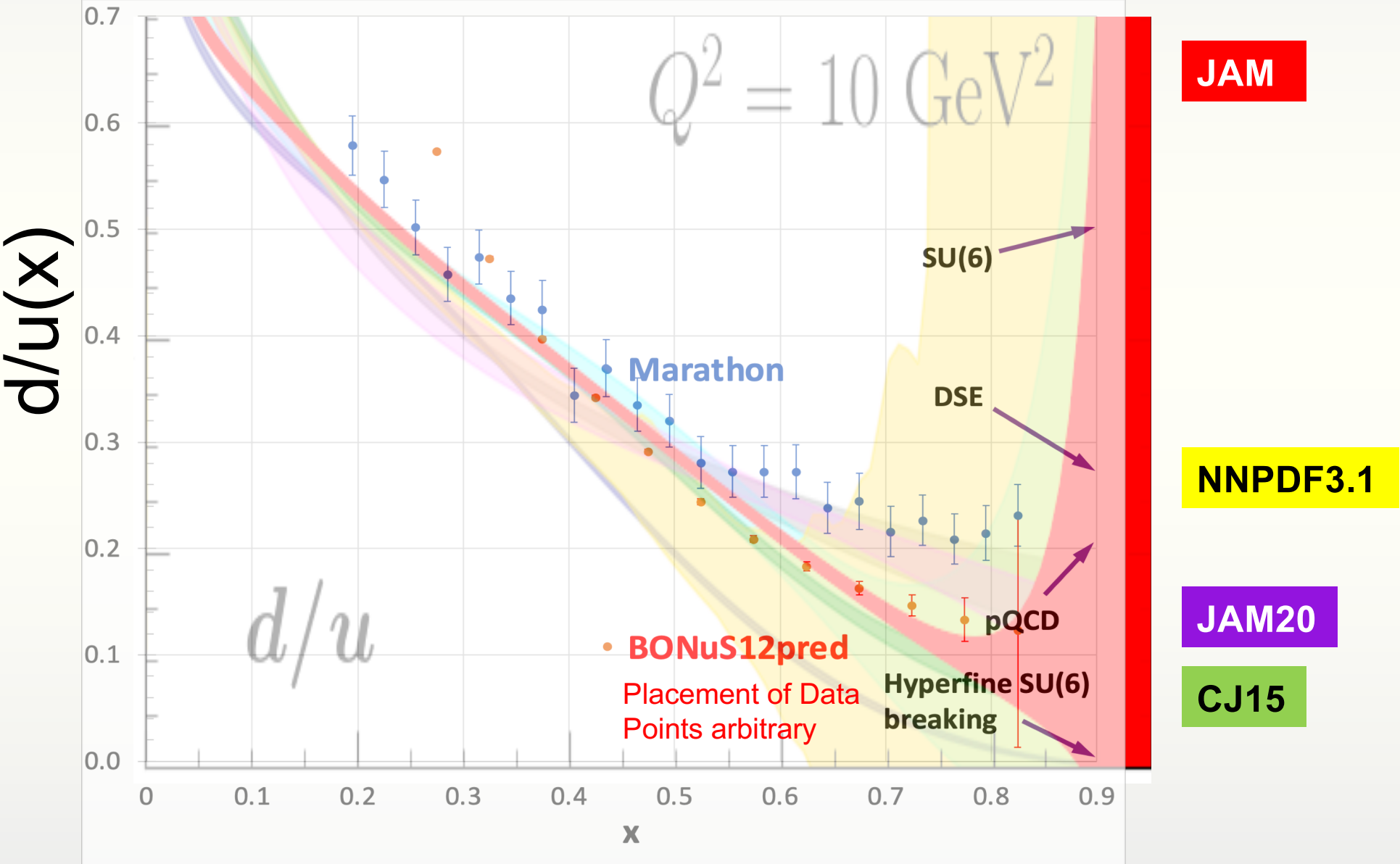
Readout Pads



# Preliminary BONuS12 Results



# BONuS12 Expected Uncertainties

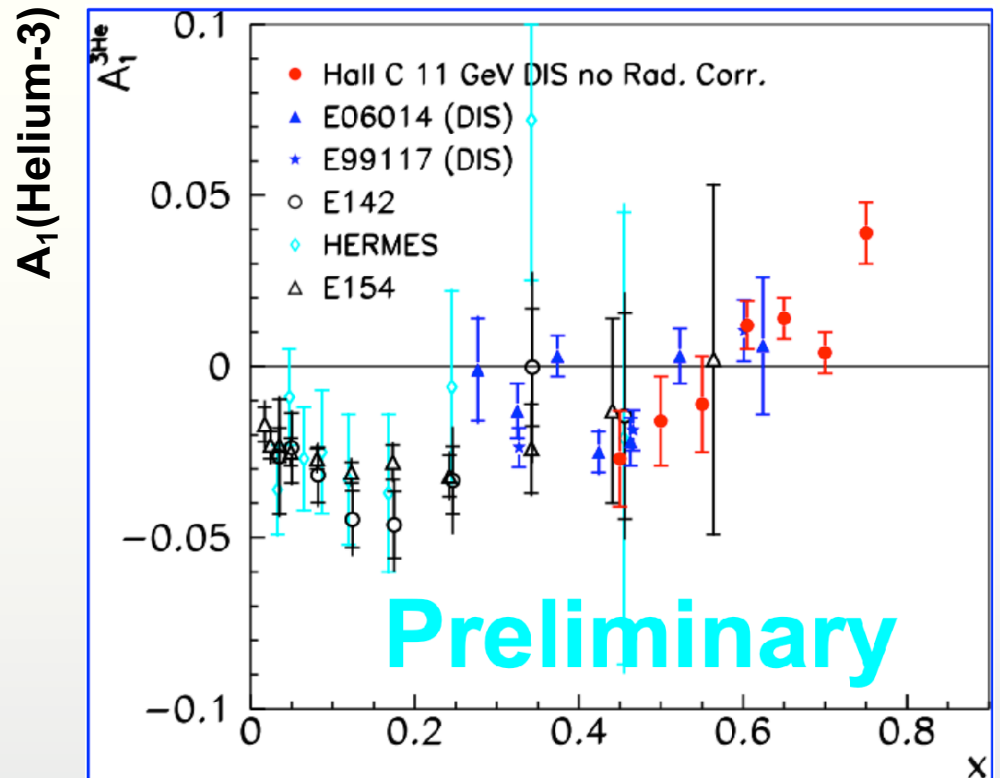
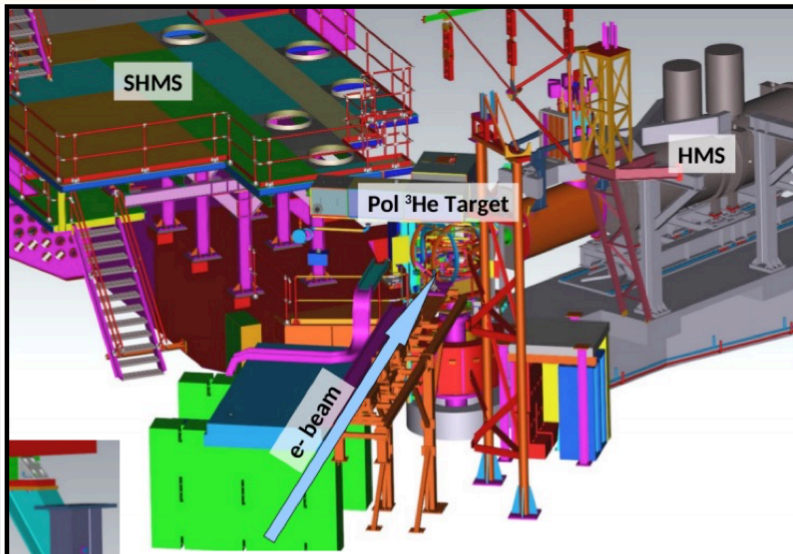
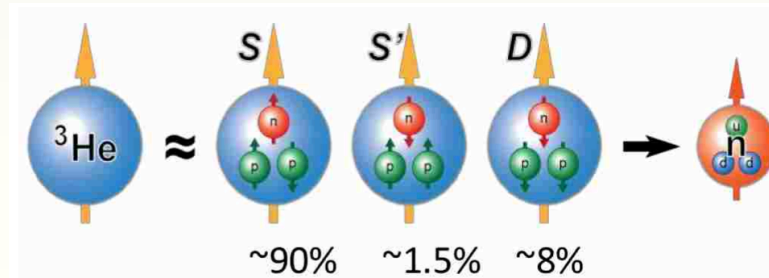
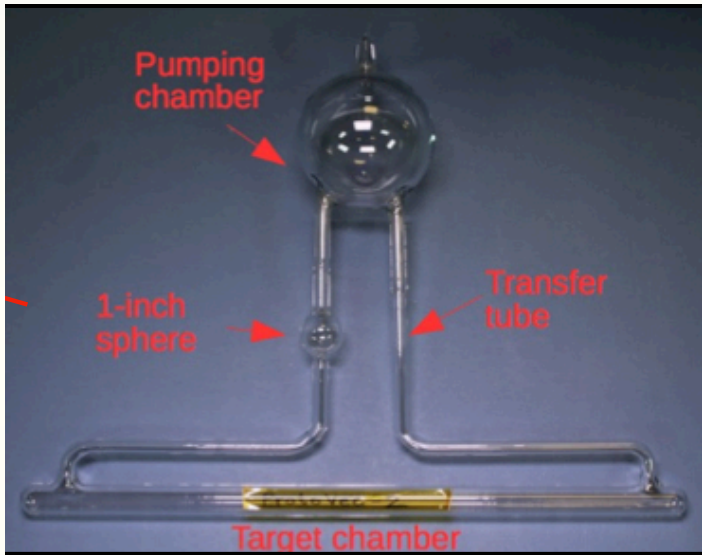




# $A_{1n}$ in Jefferson Lab's Hall C

E12-06-110 in Hall C: 1/12/2020 – 3/13/2020; 10.4 GeV polarized electrons on polarized  $^3\text{He}$

William Henry 2022 Jefferson Lab Users Organization Annual Meeting

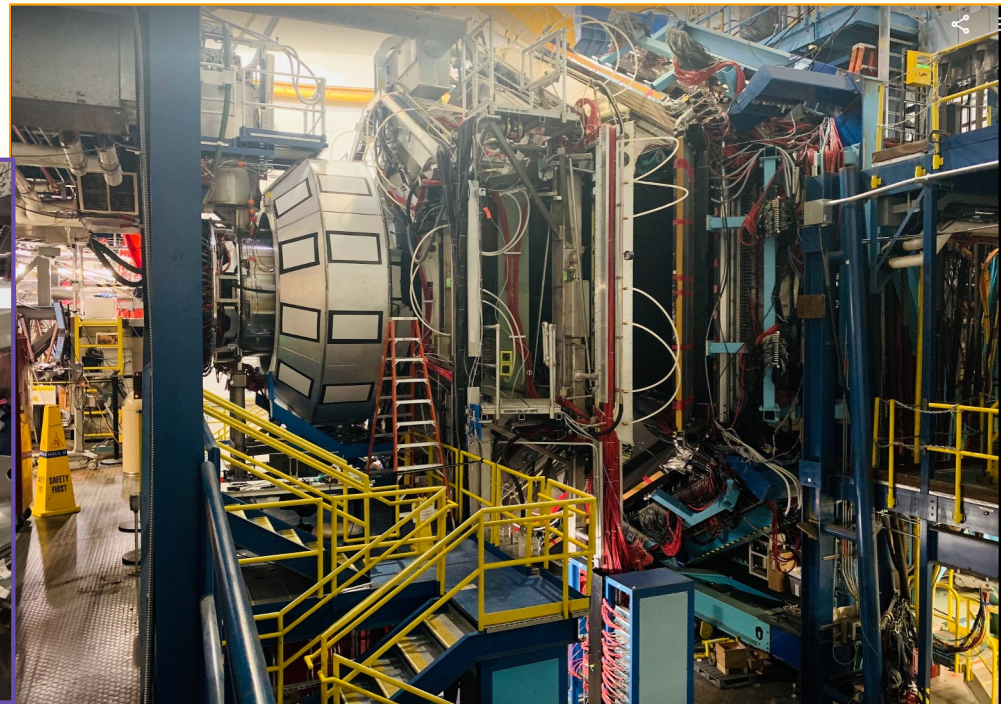




# RG-C with CLAS12

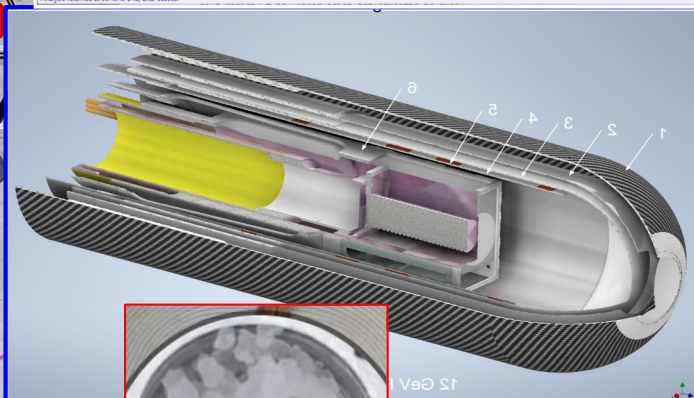
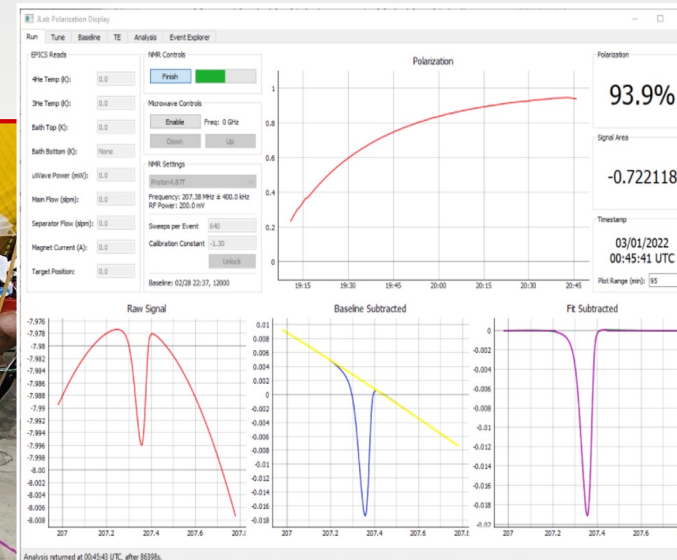
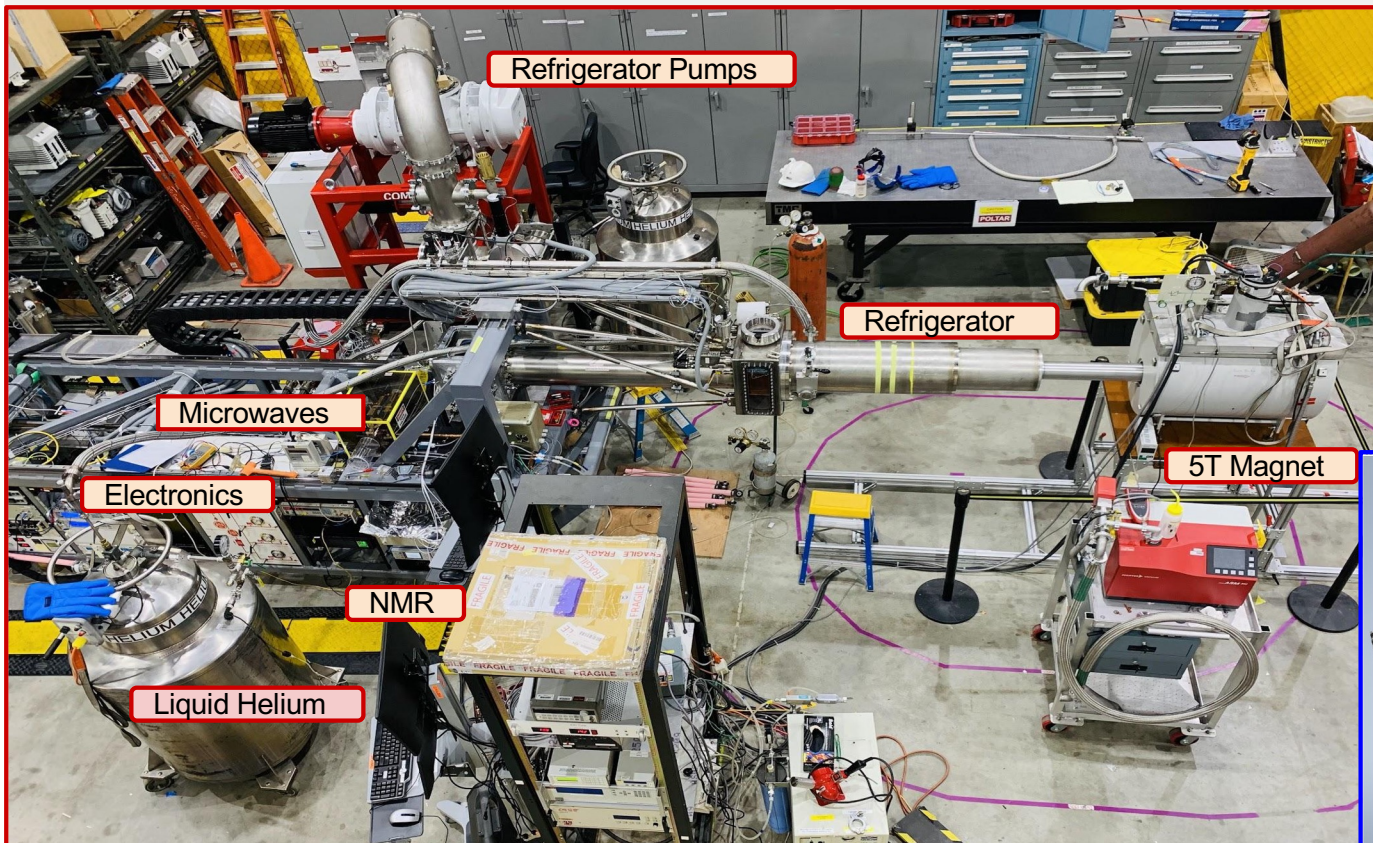
- ❑ Measure DIS inclusive spin structure functions ( $A_1, g_1$ ) of the proton and deuteron.
  - ❑ Include tagging with  $\pi, K$  SIDIS to extract flavor-separated  $\Delta q$
- ❑ Measure spin- and transverse momentum-dependent (TMD) PDFs (SIDIS).
- ❑ Deeply Virtual Compton Scattering (DVCS) to access Generalized Parton Distributions (GPDs) - Measure target single and beam/target double spin asymmetries in proton and neutron DVCS.
  - Scheduled from June 2022 through March 2023 (240 Calendar Days)
  - 10.6 GeV, 10 nA polarized electrons on 3 g/cm<sup>2</sup> polarized NH<sub>3</sub> / ND<sub>3</sub> ( $\mathcal{L} = 10^{35}$ )
  - Dynamic Nuclear Polarization at 1 K, 5 T with 140 GHz  $\mu$ wave on irradiated ammonia

*Polarized target "APOLLO"*





# Longitudinally Polarized Target for CLAS12



# First (VERY preliminary) data

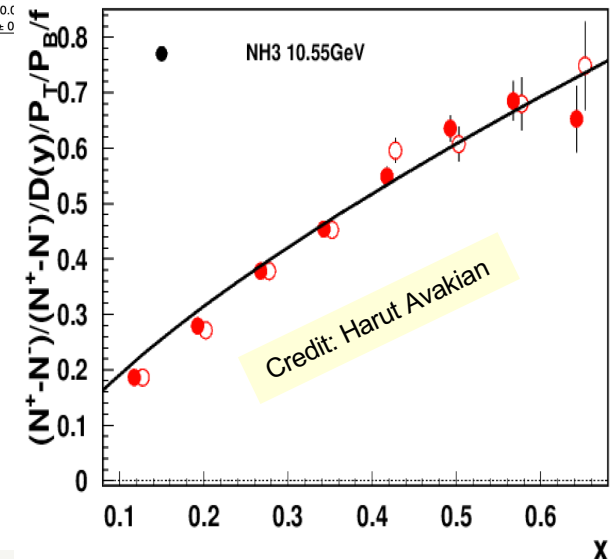
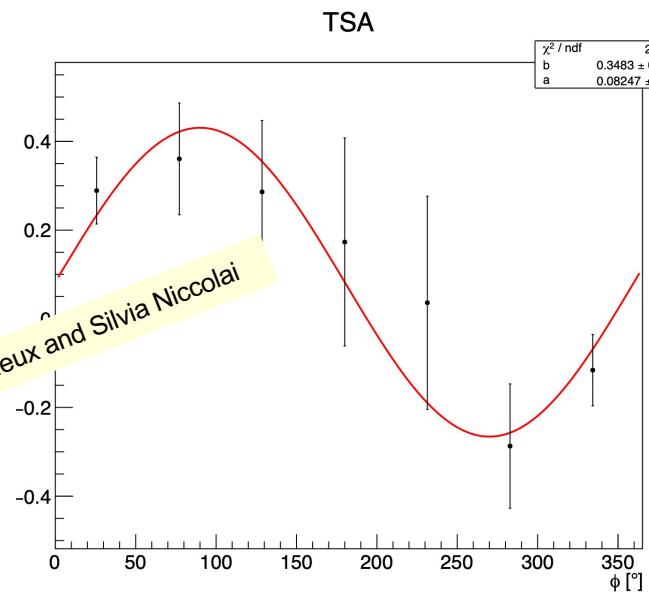
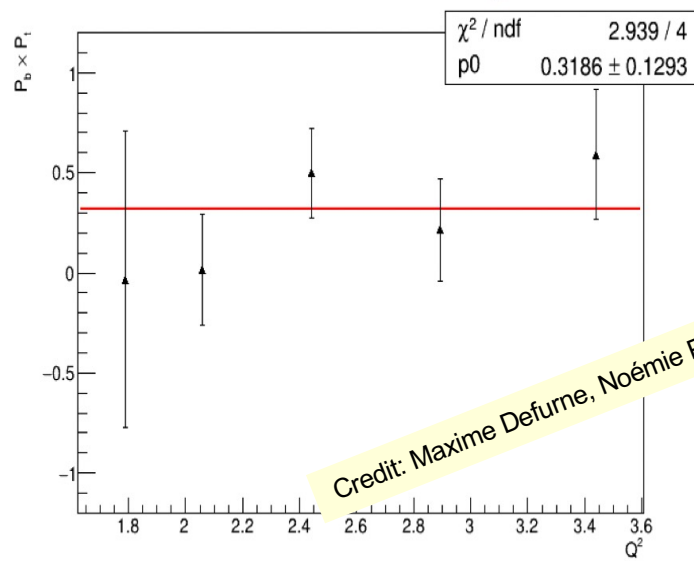
Based on a few % of data set collected so far; near-online analysis

ND<sub>3</sub> target polarization from quasi-elastic scattering

Proton DVCS from FTON period

A<sub>||</sub> in DIS on proton

$\langle Q^2 \rangle = 2.231$ ,  $\langle x_B \rangle = 0.1801$ ,  $\langle -t \rangle = 0.4061$



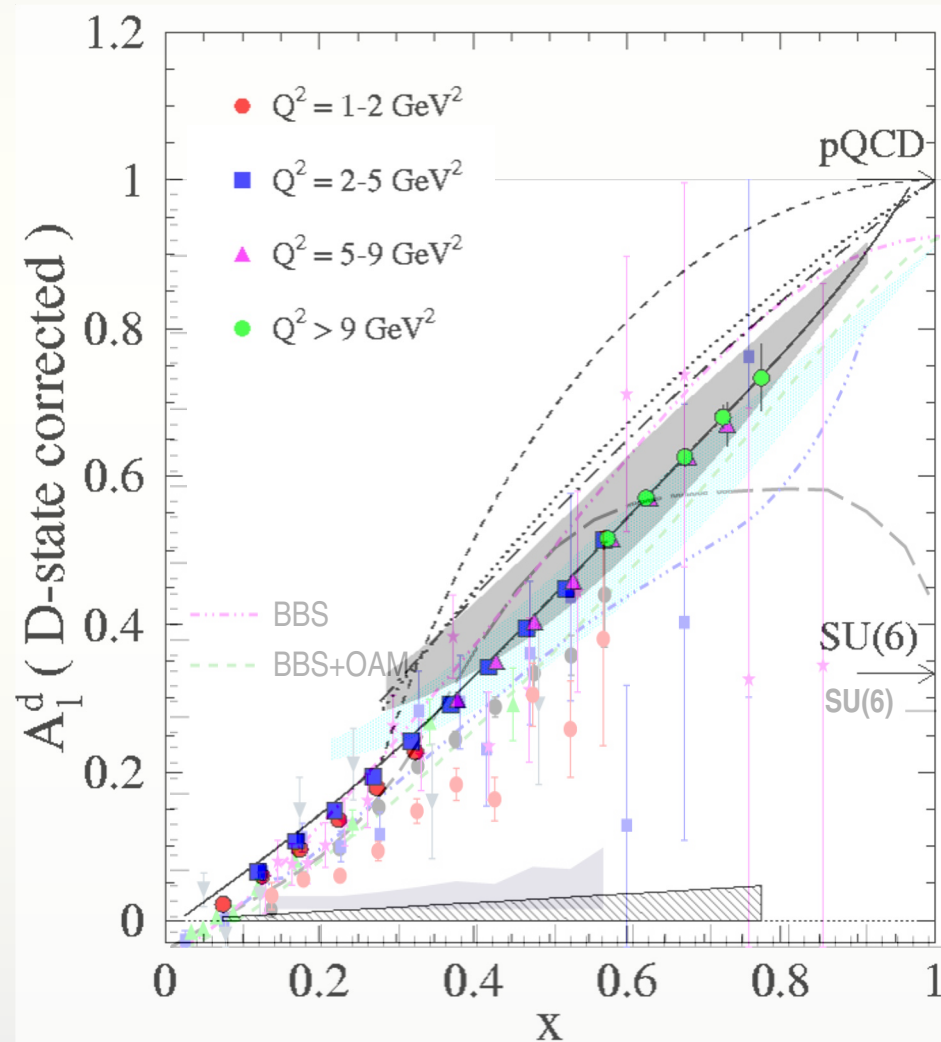
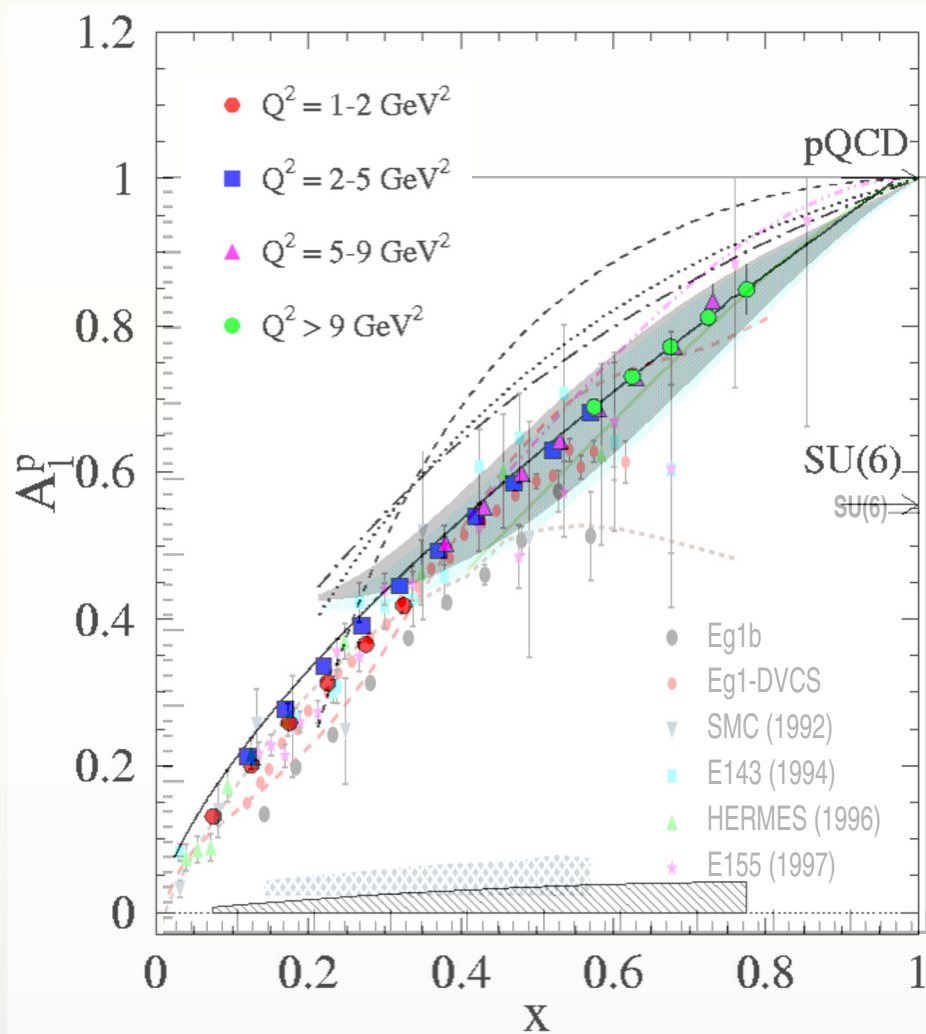


# Predicted Data from CLAS12 - DIS

Proton

$W > 2; Q^2 > 1$

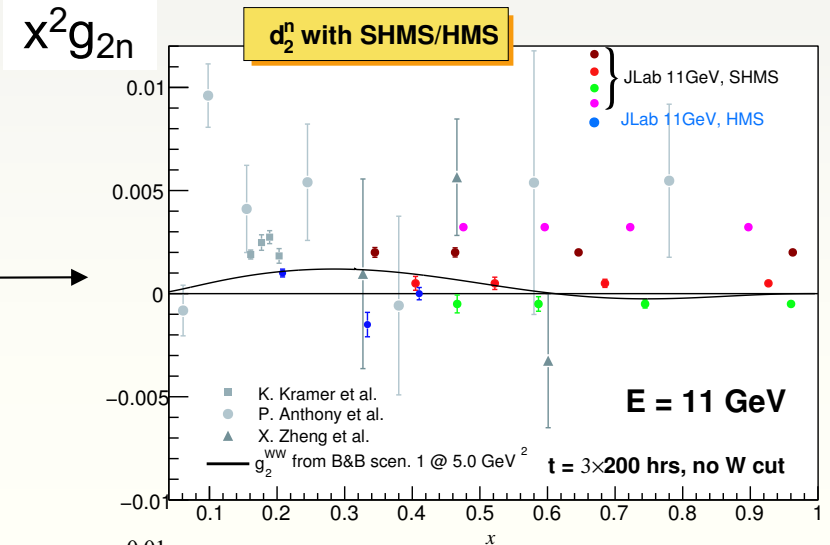
Deuteron



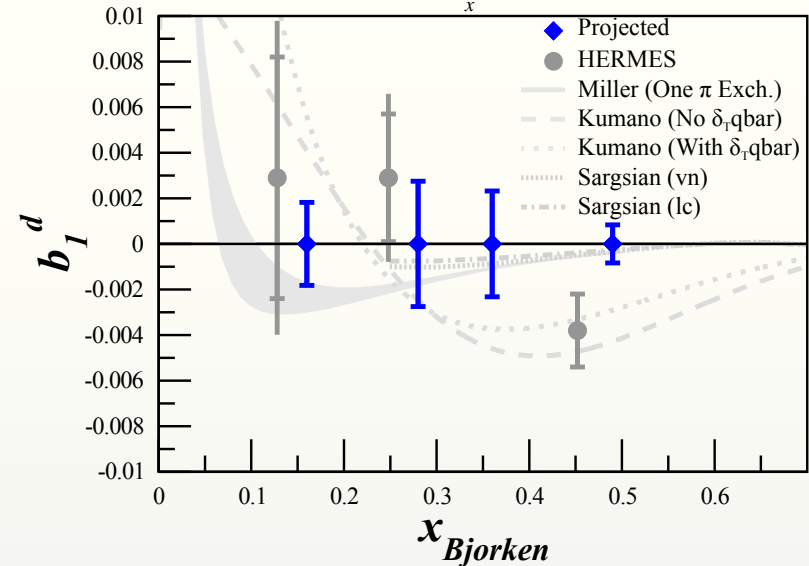


# Other SF experiments

- $g_2$  on proton and neutron (E12-06-121)



- Tensor structure function  $b_1$  (E12-11-110)



- Unpolarized structure function  $F_{2N}$ , R; PVDIS, ...

# EMC effect

- Fundamental question: How does nuclear binding modify the high- $x$  structure function of the nucleon?
- Relevant for the extraction of neutron structure functions from experimental data on  $d$ ,  ${}^3\text{He}$ ,  ${}^3\text{H}$
- Many models: mean field, Short range correlations (SRC), Light-Front Holography (LFHQCD), ...

C. Cocuzza et al., PHYSICAL REVIEW LETTERS 127, 242001 (2021)

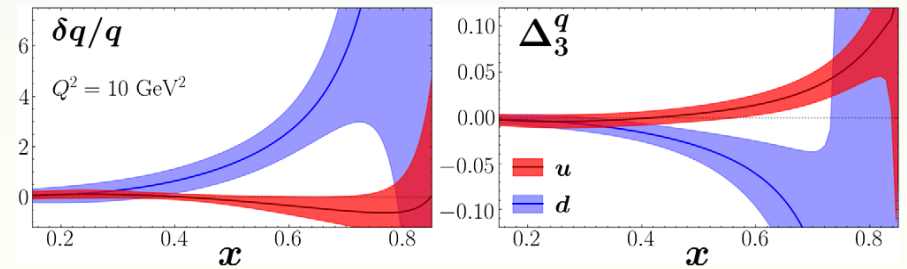
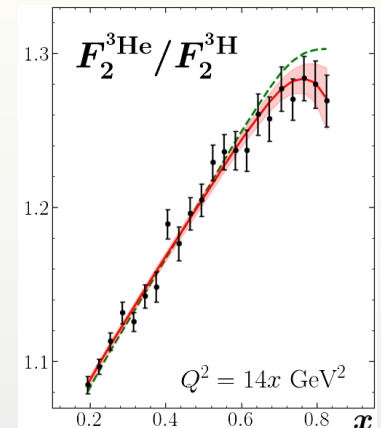
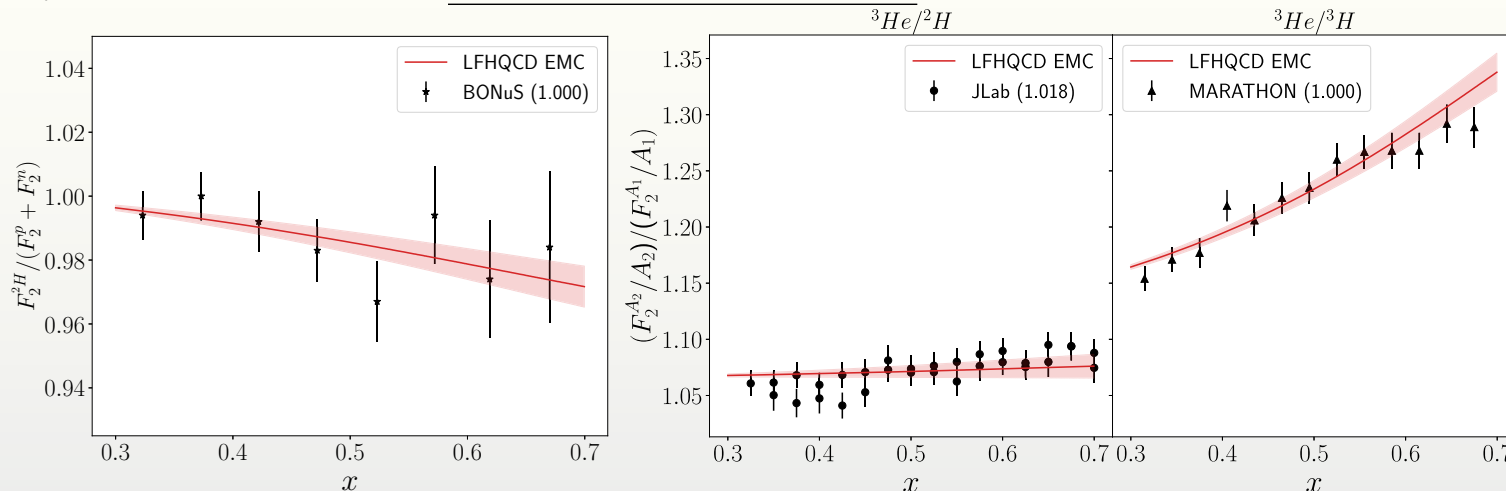


FIG. 3. Ratio of off-shell to on-shell PDFs  $\delta q/q$  (left) and the difference between proton valence quarks in  ${}^3\text{He}$  and  ${}^3\text{H}$  normalized to the sum,  $\Delta_3^q$  (right), for valence  $u$  (red bands) and  $d$  (blue bands) quarks, at  $Q^2 = 10 \text{ GeV}^2$ .

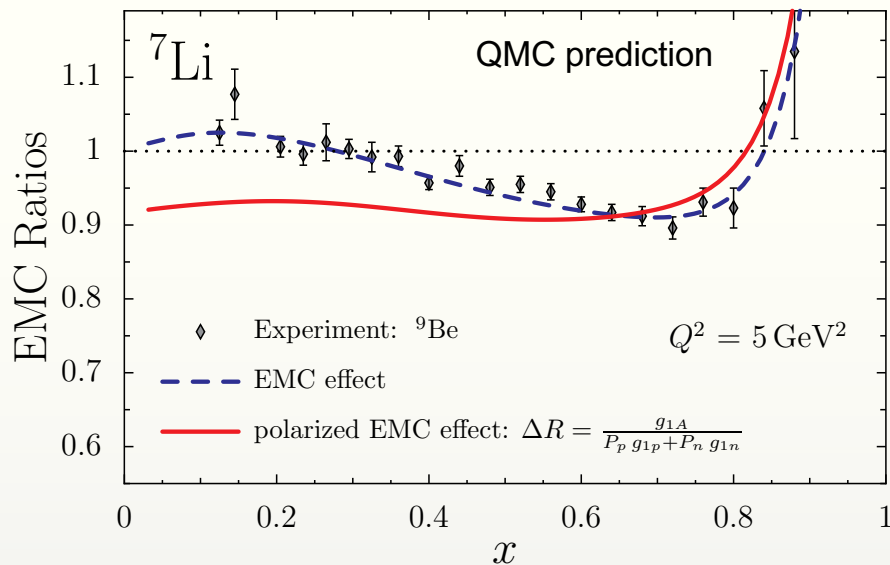
Dmitriy N. Kim and Gerald A. Miller PHYSICAL REVIEW C 106, 055202 (2022)



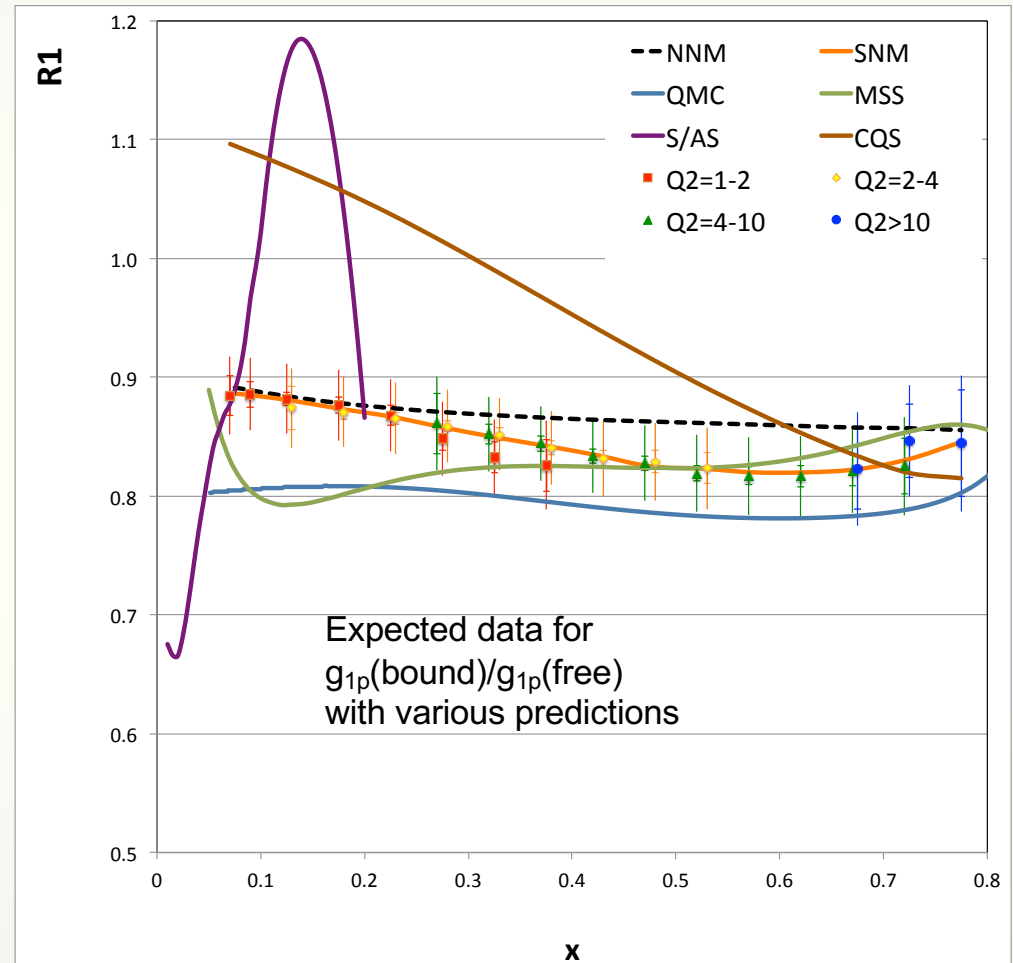
# Polarized EMC effect

(Approved Experiment RG-G with CLAS12 at Jefferson Lab)

- A large number of experiments is studying modifications of bound nucleon structure function  $F_2$  on a wide range of nuclei – data average over ALL nucleons!
- Unique test of EMC models: Measure modification of **polarized** structure function  $g_{1p}$  on a single valence nucleon!

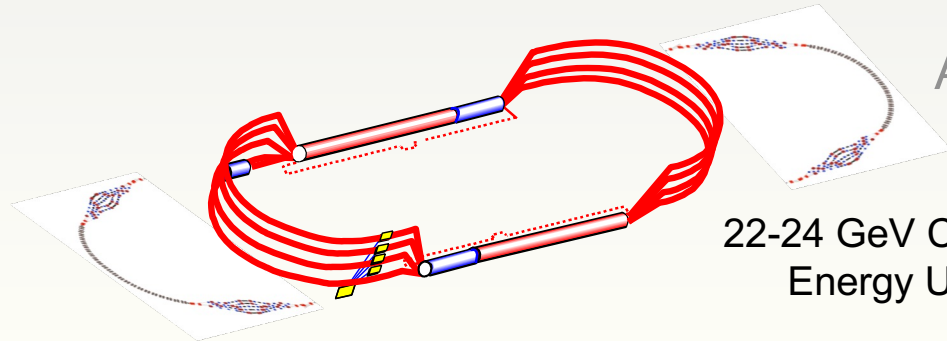


$$\Delta\sigma \text{ Ratio} \propto [N^+-N^-]({}^7\text{Li}) / [N^+-N^-](p)$$



NNM = Shell model prediction (p 87% pol.) SNM = Standard Nuclear Model (convolution w/out change in medium; equiv. to SRC model) QMC = Mean Field (Quark-Meson Coupling) MSS (rescaling/modified sea scheme) S/AS = Shadowing/Antishadowing (Guzey/Strikman) CQS = Chiral Quark Soliton (Smith/Miller)

# Future: JLab at 20+ GeV?



Alex Bogacz

J-FUTURE Workshop

Jefferson Lab / Messina University

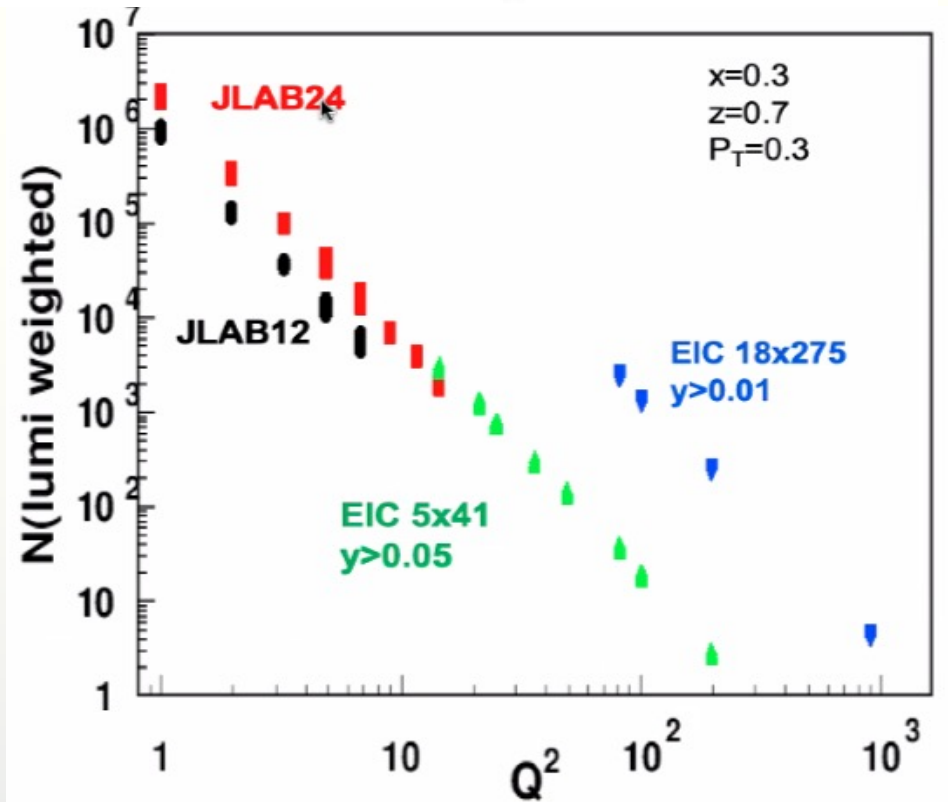
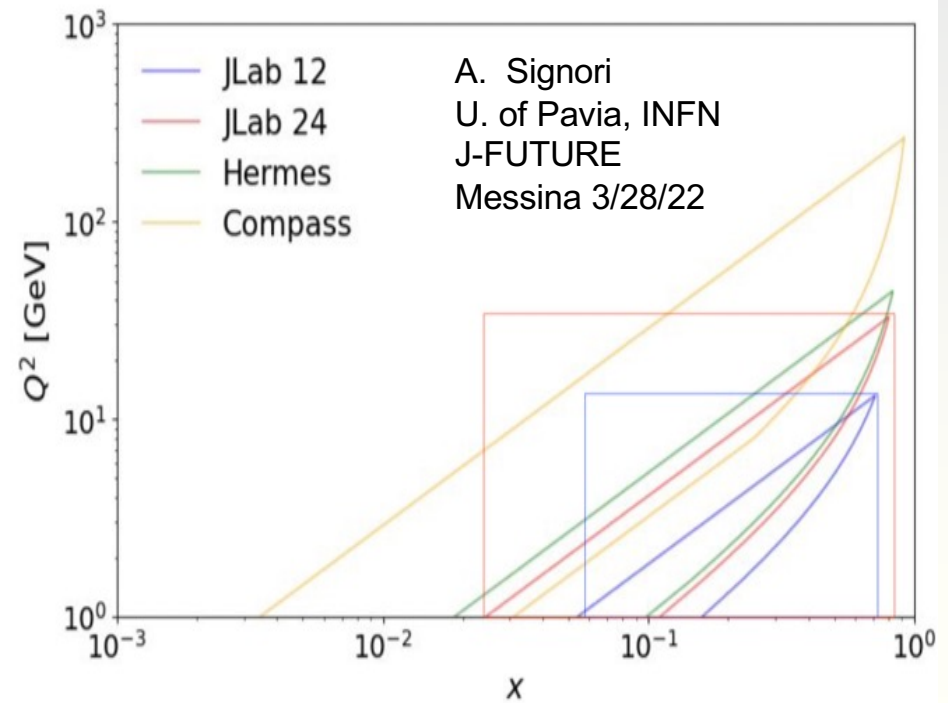
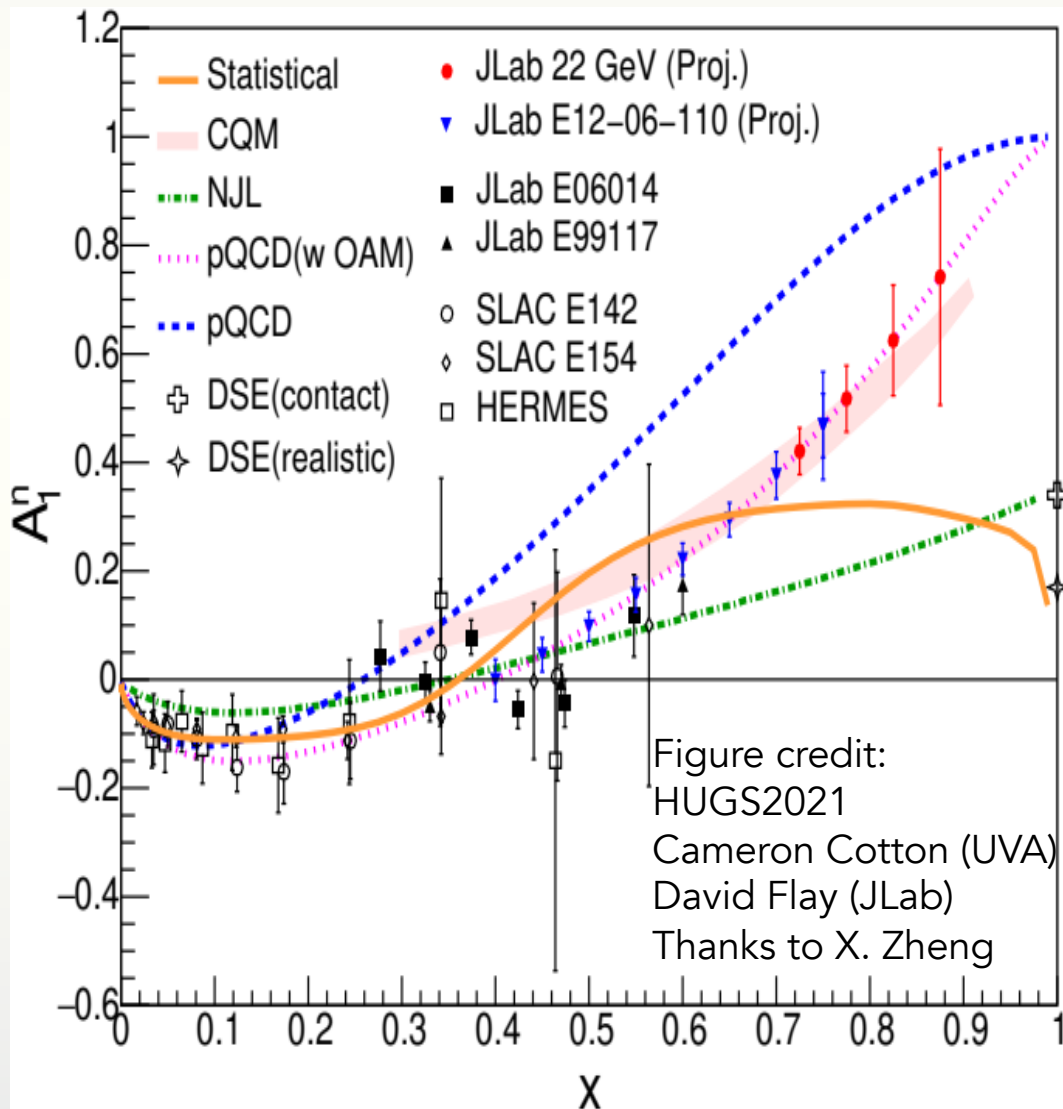
22-24 GeV CEBAF FFA  
Energy Upgrade

- Halve distance to  $x = 1$ , higher  $Q^2$ : Definite determination of asymptotic limit... \*)
- ...AND to  $x = 0 \Rightarrow$  Study “valence” sea quarks (pion cloud)
- Increase  $Q^2$  range for all  $x \rightarrow$  DGLAP  $\Rightarrow$  Study “valence” gluon helicity
- Even for same  $x$ ,  $Q^2$ : higher energy  $\rightarrow$  higher rates  $\rightarrow$  better statistics
- (*Super*)*Rosenbluth* – expand range in  $\varepsilon$  for fixed  $x$ ,  $Q^2 \Rightarrow R, g_2, A_2$
- Extend flavor tagging with SIDIS to higher  $x$ ,  $Q^2$ :
- Issues: Still need to deal with nuclear uncertainties.

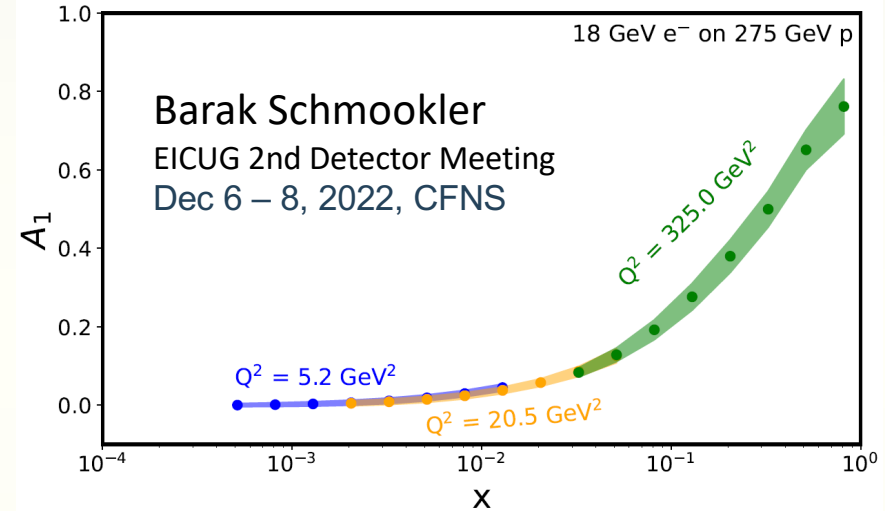
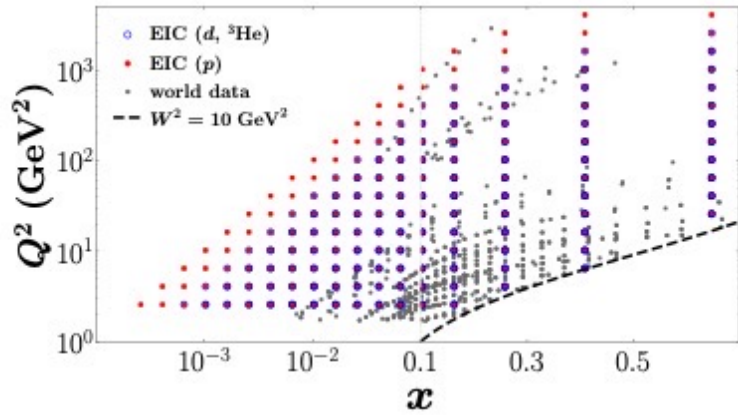
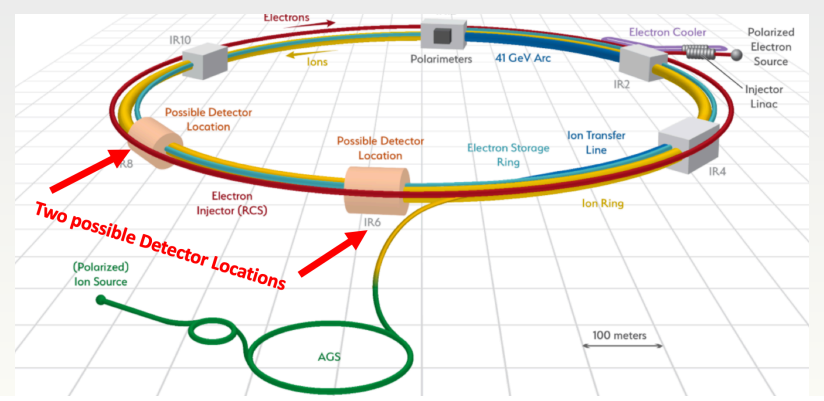
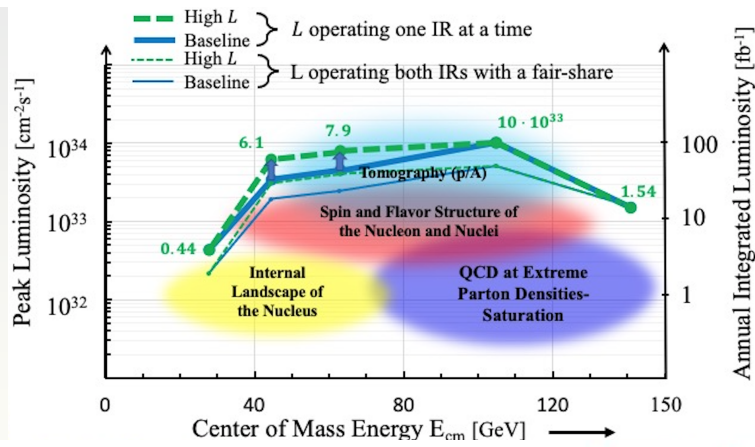
\*) Higher  $Q^2$ : Suppress higher twist, study logarithmic resummation



# From 12 to 24 GeV

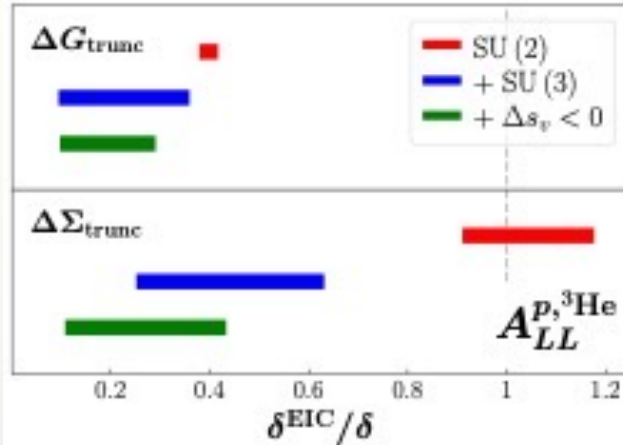
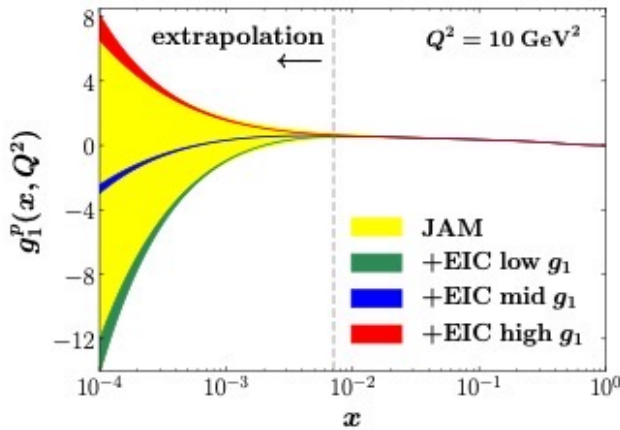


# EIC



Y. Zhou et al., Phys. Rev. D **104**(2021)034028 arXiv:2105.04434v1

Expected reduction of present SSF uncertainties from EIC



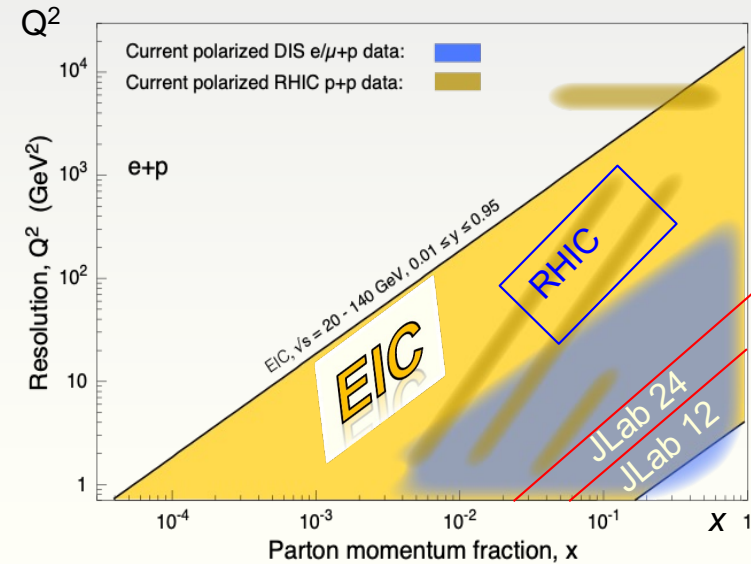
Inclusive p A<sub>LL</sub>, enforce SU(3)

Gluon and quark singlet moments from EIC

- Missing piece to solve the proton spin puzzle: Low-x extrapolation, gluon contribution
- Include weak IA for flavor separation
- Extend spectator tagging to **all** nucleon momenta in the nuclear rest frame => Extrapolate to the free nucleon pole

# SUMMARY: COMPLETING THE COLLINEAR PICTURE

Enormous Progress on understanding Collinear PDFs fueled by large new data sets and sophisticated phenomenology. Still, some questions remain:



➤ **d/u,  $\Delta u/u$  and  $\Delta d/d$  at highest x ?**

➤ **Nuclear effects on nucleon structure**

➤ **Understanding the sea –  $\Delta s$ ,  $\bar{u} - \bar{d}$ ,  $\Delta \bar{u} - \Delta \bar{d}$**

➤ **Axial and Tensor charges of the nucleon**

➤ **Gluon helicity distribution at large x AND at small x?**

**What is the integral  $\Delta G$ ?**

**Total contribution of parton helicity to proton spin?**

➤ **What happens at really small x  $\ll 0.01$ ?**

JLab @ 12 -> 24 GeV

JLab, FNAL, RHIC, AMBER, LHC

COMPASS, JLab

JLab + DGLAP,  
RHIC, COMPASS



# Conclusions

- Structure functions in the valence region remain of high theoretical interest and provide crucial input to precision collider experiments
- Jefferson Lab at 12 GeV is starting to have significant impact on our understanding of this region
- Jefferson Lab at 24 GeV can expand the coverage in  $x$  from 0.75 to 0.9 and more than double the range in  $Q^2$ , thereby minimizing the extrapolation to  $x \rightarrow 1$ .
- Jefferson Lab and EIC together cover the entire kinematic region necessary to complete the “spin puzzle”.
- Essential ingredient: Extract neutron (polarized) structure functions from measurements on nuclei (d,  $^3\text{He}$ )  $\Rightarrow$  we must understand the EMC effect in detail.