

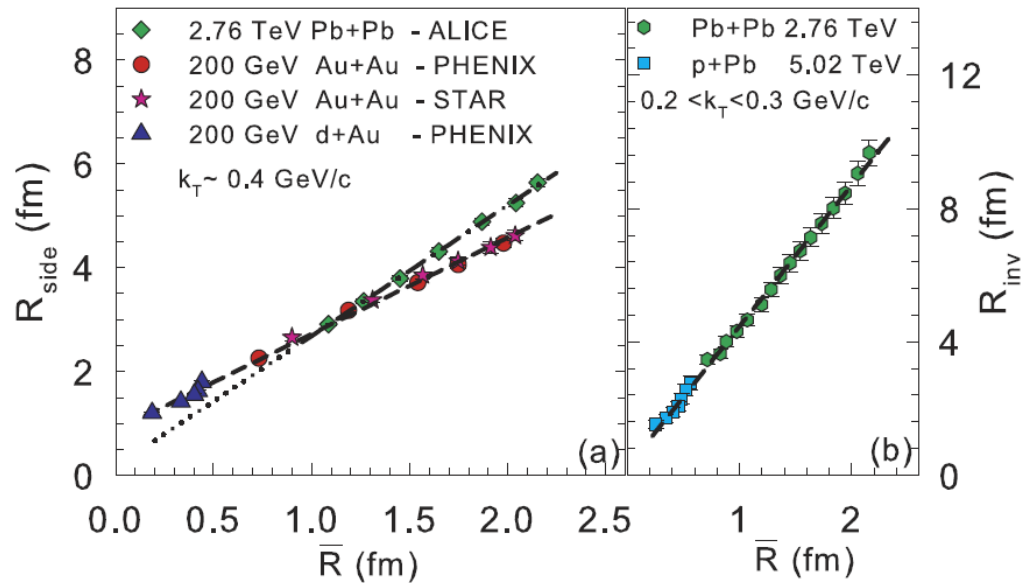
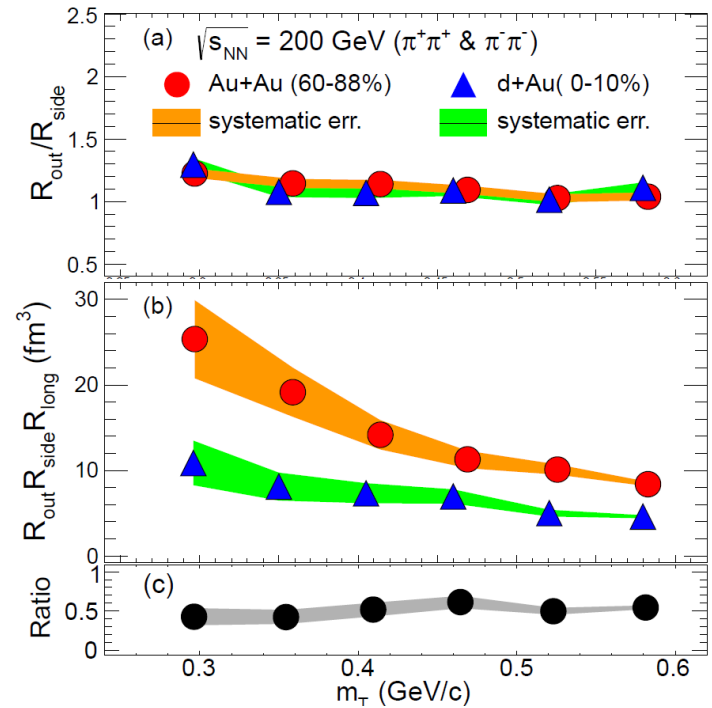
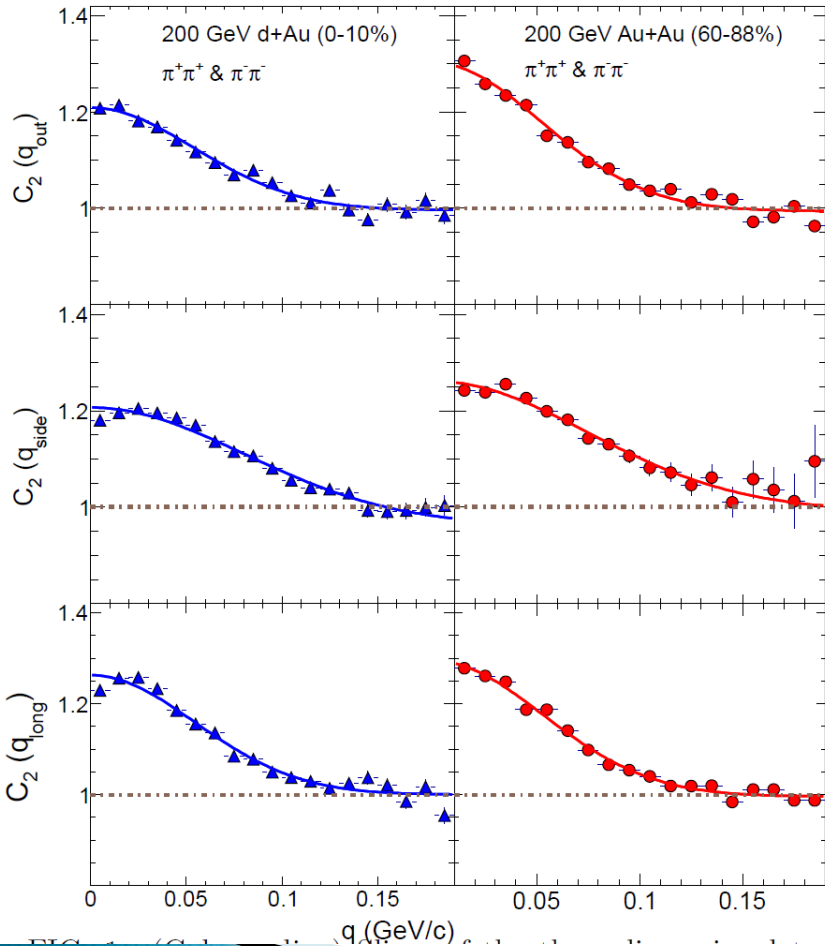
# How to discern between initial-state-driven (CGC-EFT) and final-state-driven (Flow) azimuthal anisotropy

*Roy A. Lacey*  
*Stony Brook University*

# Response to HBT request

Comparison of the space-time extent of the emission source in  $d+Au$  and  $Au+Au$  collisions at  $\sqrt{s_{NN}} = 200$  GeV

PHENIX Collaboration Author List (Brant will insert later)  
(Dated: April 12, 2014)

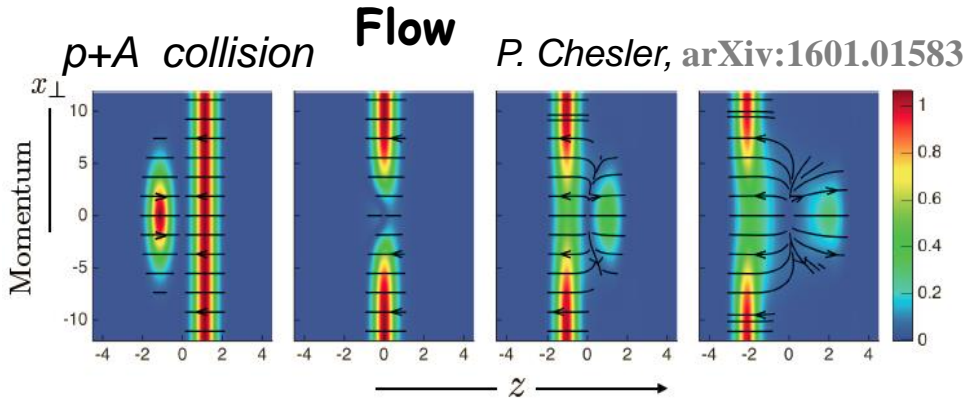


# How to discern between initial-state-driven (CGC-EFT) and final-state-driven (Flow) azimuthal anisotropy

*Roy A. Lacey  
Stony Brook University*

- I. *Backdrop to the strategy*
- II. *Anatomy of a few key variables*
- III. *Results focusing on the discerning role of:*
  - ✓  $N_{chg}$ ,  $\varepsilon_n$  and  $\frac{\eta}{s}$
  - ✓ *Fluctuations*
  - ✓ *Anti/Correlations*
- IV. *Summary & Conclusions*

# Backdrop – How to discern between models



**Hydrodynamic expansion dynamics works for sizes as small as  $RT \sim 1$**

Flow is acoustic

$$v_n = \varepsilon_n e^{-n \left[ n \left( \frac{4\eta}{3s} + \frac{\xi}{s} \right) + \kappa p_T^2 \right] \frac{1}{RT}}, RT \propto \langle N_{\text{chg}} \rangle^{1/3}$$

**Specific respective influence from:**

$$\varepsilon_n, \delta\varepsilon_n, C_r(\varepsilon_n, \varepsilon_m), n^2, \left( \frac{4\eta}{3s} + \frac{\xi}{s} \right), p_T^2, \langle N_{\text{chg}} \rangle^{1/3}$$

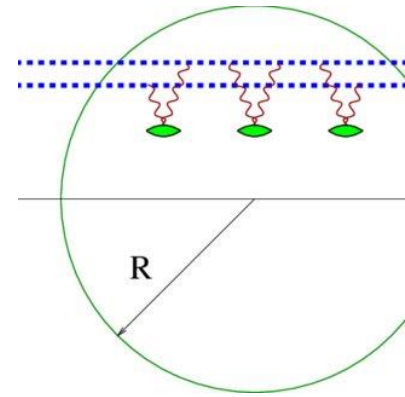
$\varepsilon_n$  & its fluctuations

correlations *visc. attenu.*

$$\varepsilon_n \left( + \delta\varepsilon_n + C_r(\varepsilon_n, \varepsilon_m) \right), n^2, \left( \frac{4\eta}{3s} + \frac{\xi}{s} \right), p_T^2, \langle N_{\text{chg}} \rangle^{1/3}$$

**➤ There are several specific contrasting dependencies which can be leveraged to discern between these final- and initial-state models**

**CGC-EFT**  
arXiv:1807.00825



**Eikonal-like scattering of quarks off of a gluon dense nuclear target**

**Controlling influence from:**

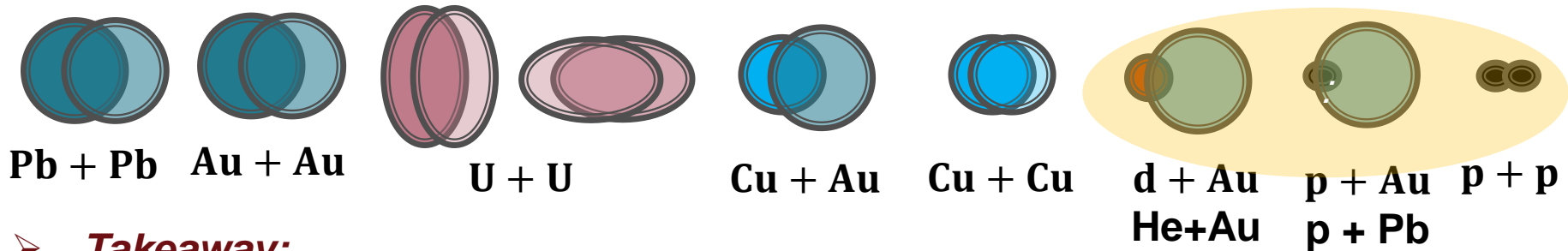
$$Q_{s,T} \ll p_T^{\text{max}}, Q_{s,p}(B_p)$$

$$v_{2n}\{2\} \propto N_{\text{chg}}^0, v_{2n+1}\{2\} \propto N_{\text{chg}}^{1/2}, \delta(v_n), C_r(n, m)$$

# Commentary -1

- The azimuthal anisotropy in systems spanning the broadest range of  $\sqrt{s_{NN}}$ , collision-system sizes, shapes and asymmetries should be employed for any meaningful distinction between Flow and CGC-EFT models.

✓ [arXiv:1901.08155](https://arxiv.org/abs/1901.08155), [arXiv:1804.04618](https://arxiv.org/abs/1804.04618), [arXiv:1802.06595](https://arxiv.org/abs/1802.06595) (recent examples)



## ➤ Takeaway:

- The dimensionless size  $RT \propto \langle N_{chg} \rangle^{1/3}$ , is the size metric and small systems are created irrespective of colliding species – not just in  $p+A$ ,  $d+A$ , etc.

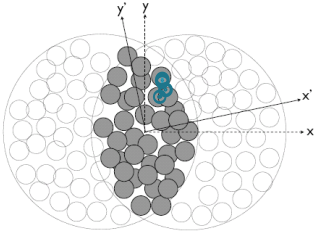
$$\left( \frac{dN_{chg}}{d\eta} \right)_{|\eta|=0.5} = N_{qpp} \left[ b_{AA} + m_{AA} \ln(\sqrt{s_{NN}}) \right]^3$$

$$b_{AA} = 0.5303 \pm 0.008, \quad m_{AA} = 0.1131 \pm 0.002$$

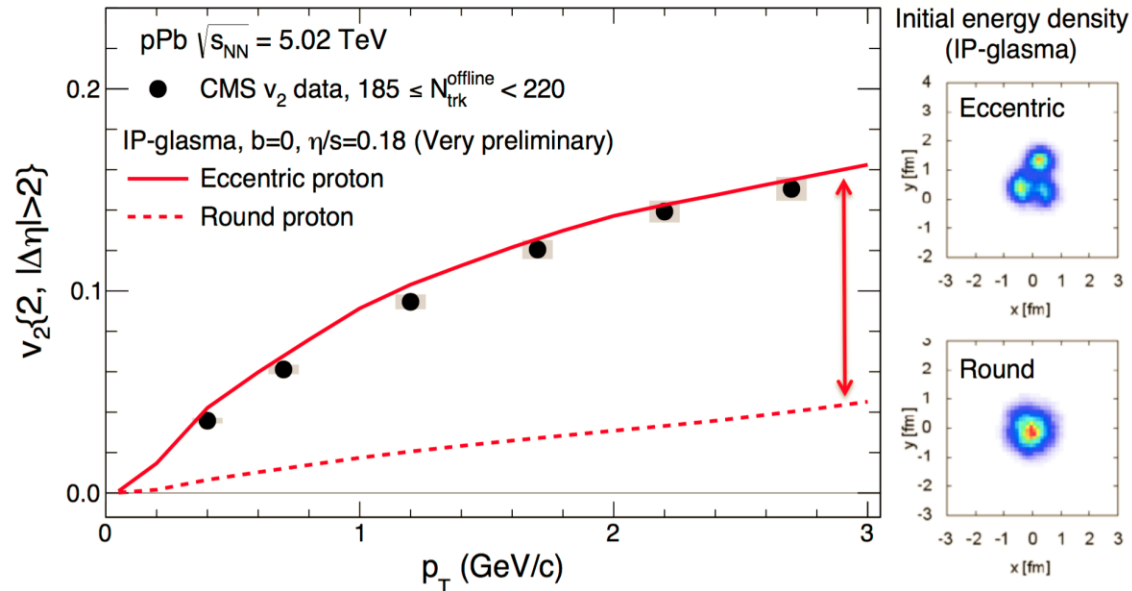
Universe 4 (2018) no.1, 22 [arXiv:1601.06001](https://arxiv.org/abs/1601.06001)

**There are many ways to vary dimensionless size, shape, viscous attenuation, fluctuations,  $v_n$ -correlations., etc.**

## MC-quarkGlauber



**A quarkGlauber model is used to characterize the nucleonic sub-structure across collision-systems**



## Valence quarks substructure

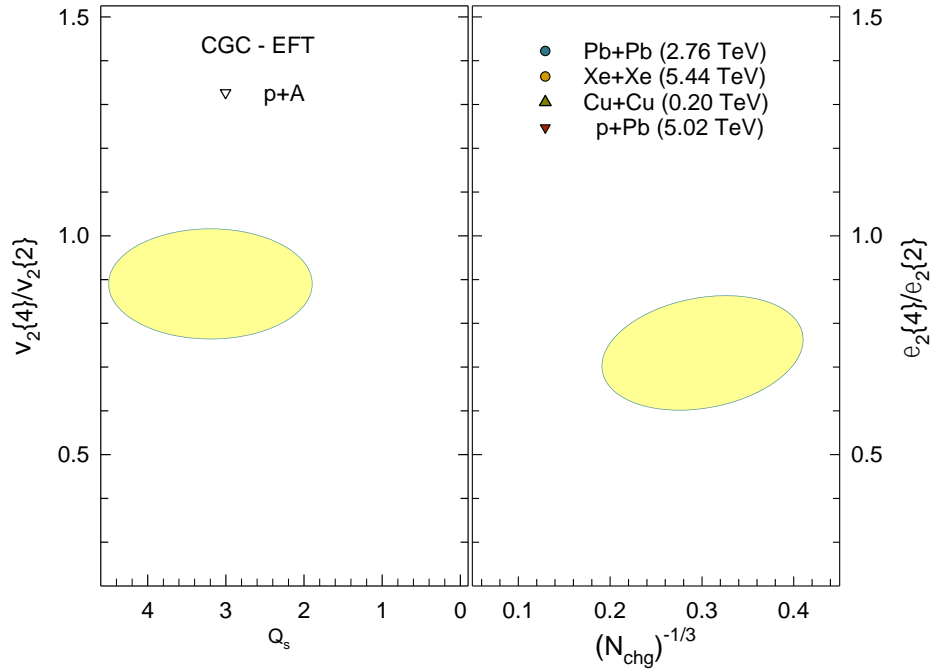
- $q$ - $q$  cross section adjusted to reproduce  $n$ - $n$  inelastic cross section
- quarks in each nucleon selected from charge distribution
- $q$ - $q$  profile constrained with elastic scattering measurements rms radius

$$\begin{aligned} \epsilon_n &= \sqrt{\langle |\mathcal{E}_n|^2 \rangle}, & \epsilon_{4,(2,2)}^{mc} &= \sqrt{\langle \epsilon_2^4 \rangle}, \\ \epsilon_{5,(2,3)}^{mc} &= \sqrt{\langle \epsilon_2^2 \epsilon_3^2 \rangle}, & \epsilon_{6,(3,3)}^{mc} &= \sqrt{\langle \epsilon_3^4 \rangle}, \\ \epsilon_{6,(2,2,2)}^{mc} &= \sqrt{\langle \epsilon_2^6 \rangle}, & \epsilon_{7,(2,2,3)}^{mc} &= \sqrt{\langle \epsilon_2^4 \epsilon_3^2 \rangle}. \end{aligned}$$

- **Geometric consistency across collision-systems**  
 ✓ Important constraint for  $\epsilon_n$ -fluctuations

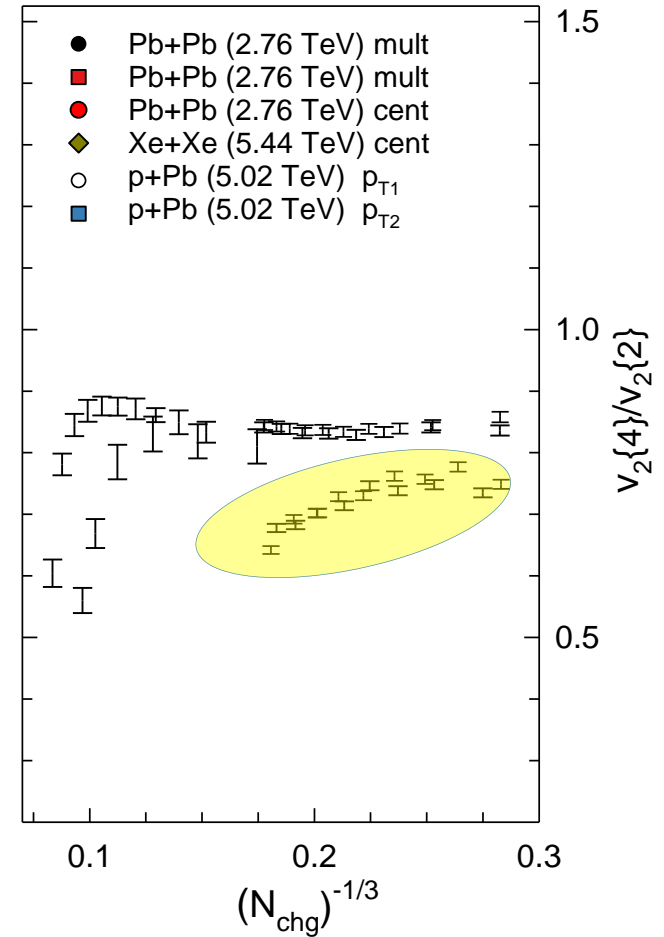
# Flow Fluctuations are discerning

## ➤ Model discerning character of flow fluctuations



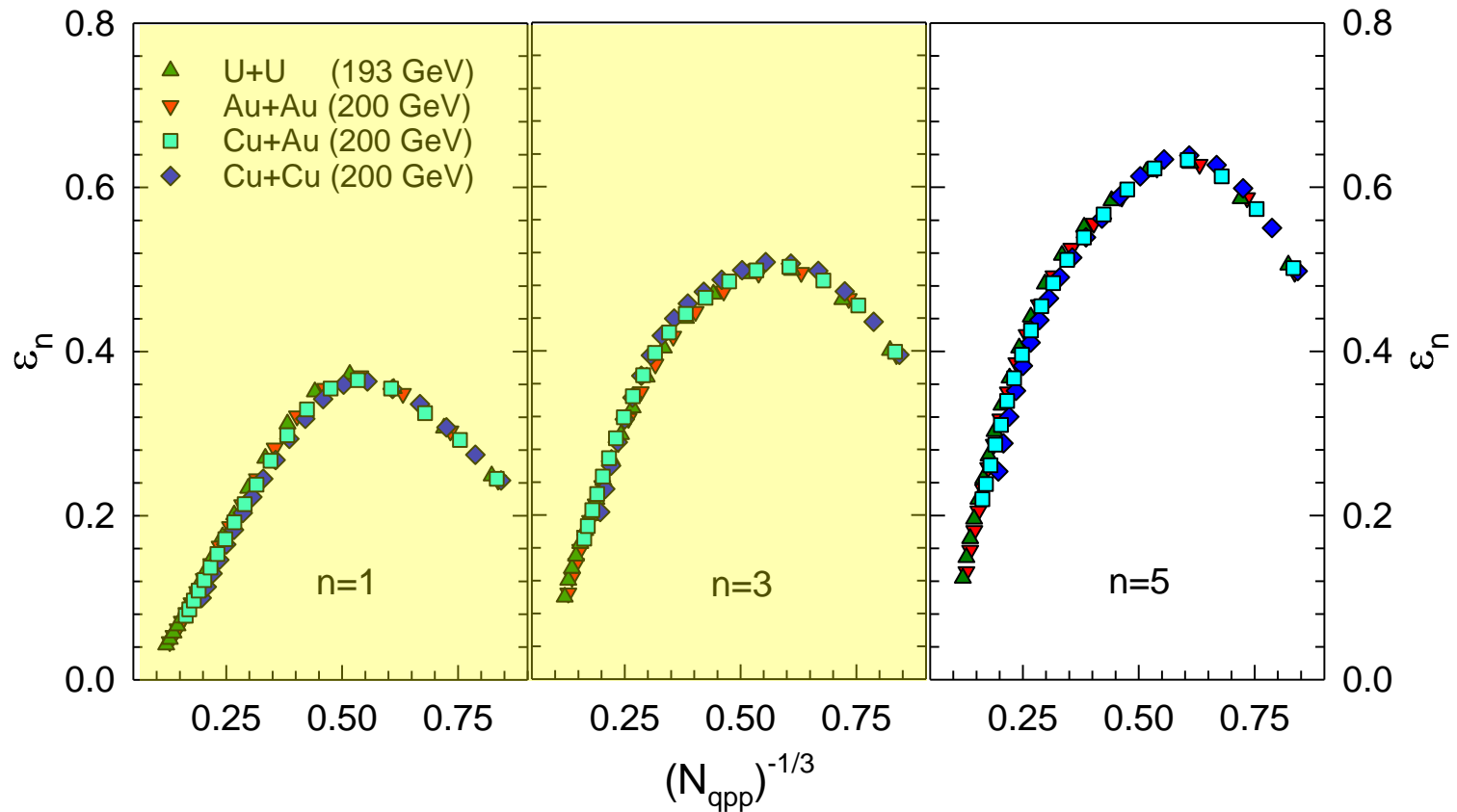
**Eccentricity fluctuations dominate flow fluctuations**

✓ **A characteristic model-dependent difference in the  $N_{\text{chg}}$  dependence of fluctuations is expected**

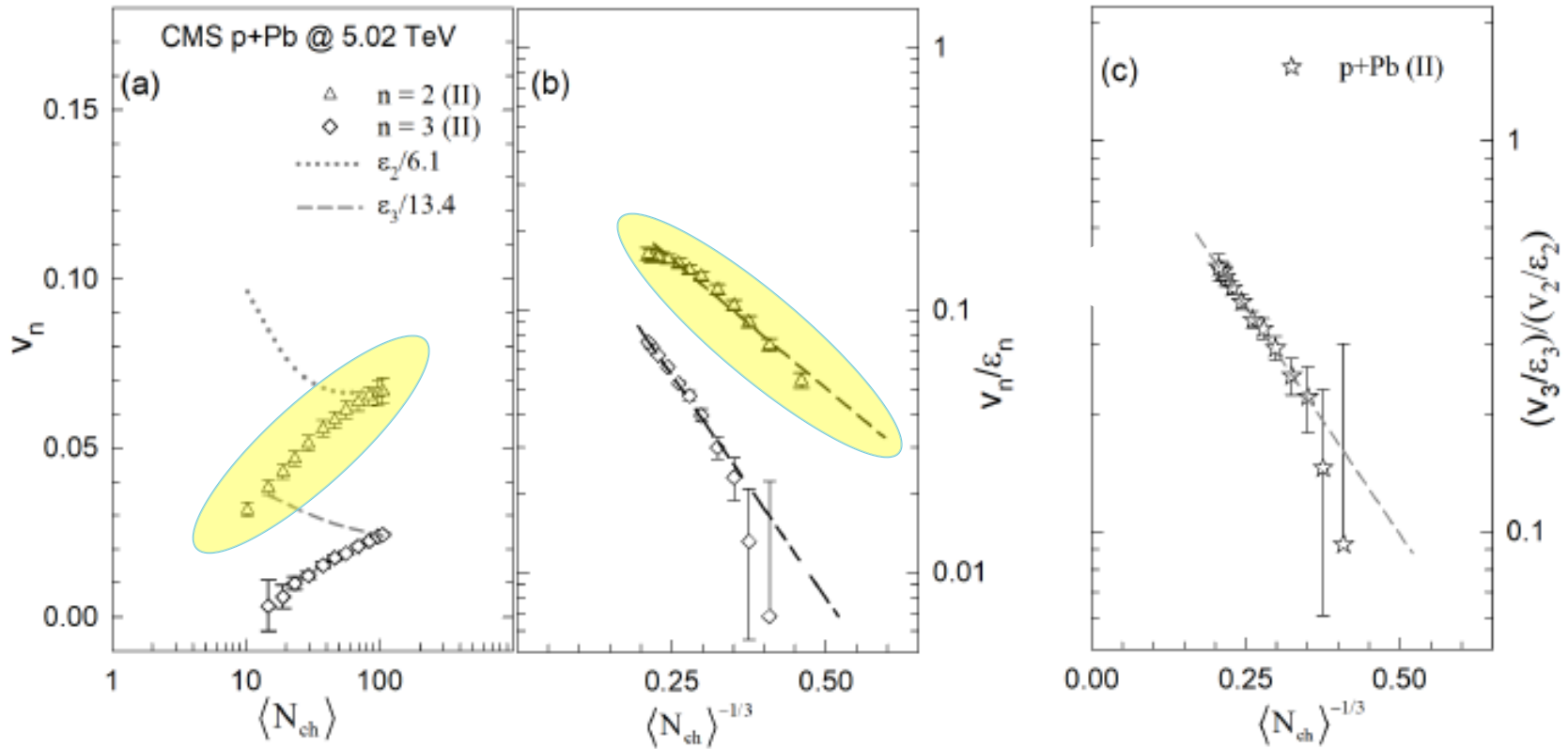


**These dependencies pose a challenge to CGC-EFT models**

# Collision-system dependent shape response - $\varepsilon_n$



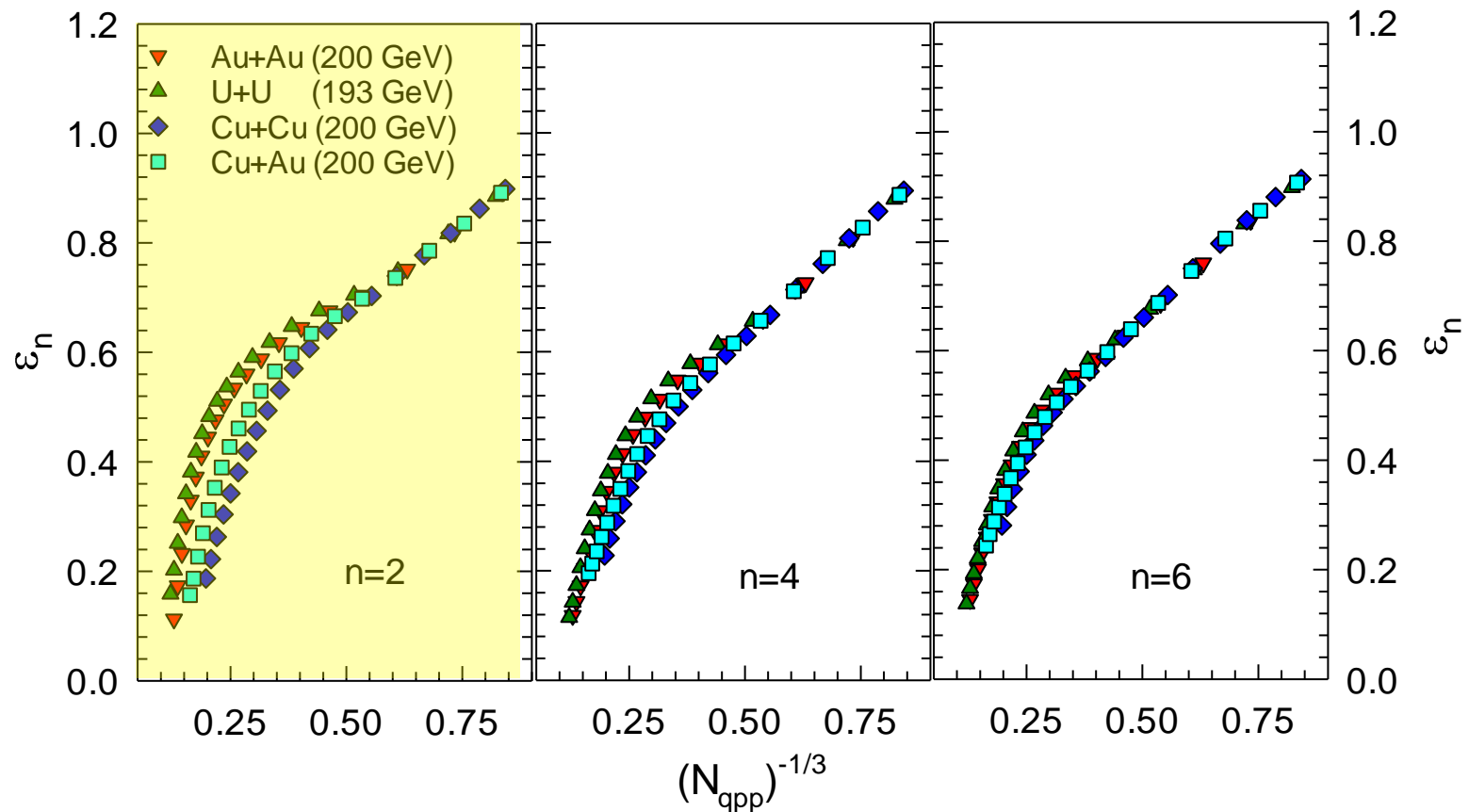
- **Odd eccentricity moments are fluctuations driven**
  - ✓ **Little, if any, system dependence for A+A(B) collisions for similar dimensionless size**



- **Eccentricity change alone is not sufficient**
  - ✓ Same pattern as in peripheral Pb+Pb

- ✓ **Characteristic  $1/(RT)$  viscous damping similar to that for p+Pb collisions of similar “size”**
- ✓ **Viscous damping supersedes the influence of eccentricity**
  - ✓ **Important constraint for  $\eta/s$  &  $\zeta/s$**

# Collision-system dependent shape response - $\varepsilon_n$



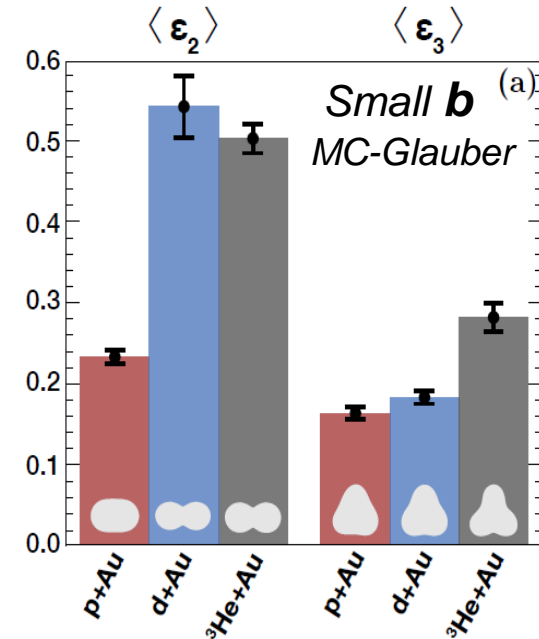
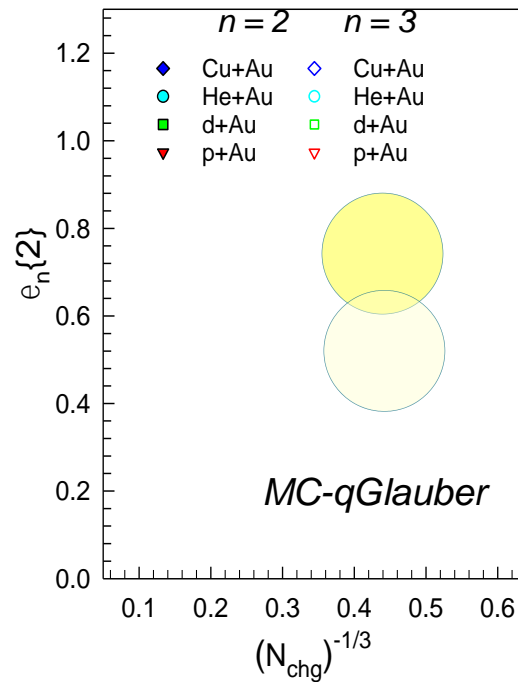
- **Even eccentricity moments are shape driven**
- ✓ **Sizeable system dependence for A+A(B) collisions in central & mid-central collisions**
- ✓ **System independence in peripheral collisions**

# Shape response

➤ **Similar eccentricity patterns observed for small and large collision-systems for the same dimensionless size.**

✓ **Small shape ( $\epsilon_2$  and  $\epsilon_3$ ) dependence on collision-system for similar dimensionless size.**

✓ **Sub-nucleonic degrees of freedom are especially important for small collision-systems**



**Circular, elliptical & triangular droplets ??**

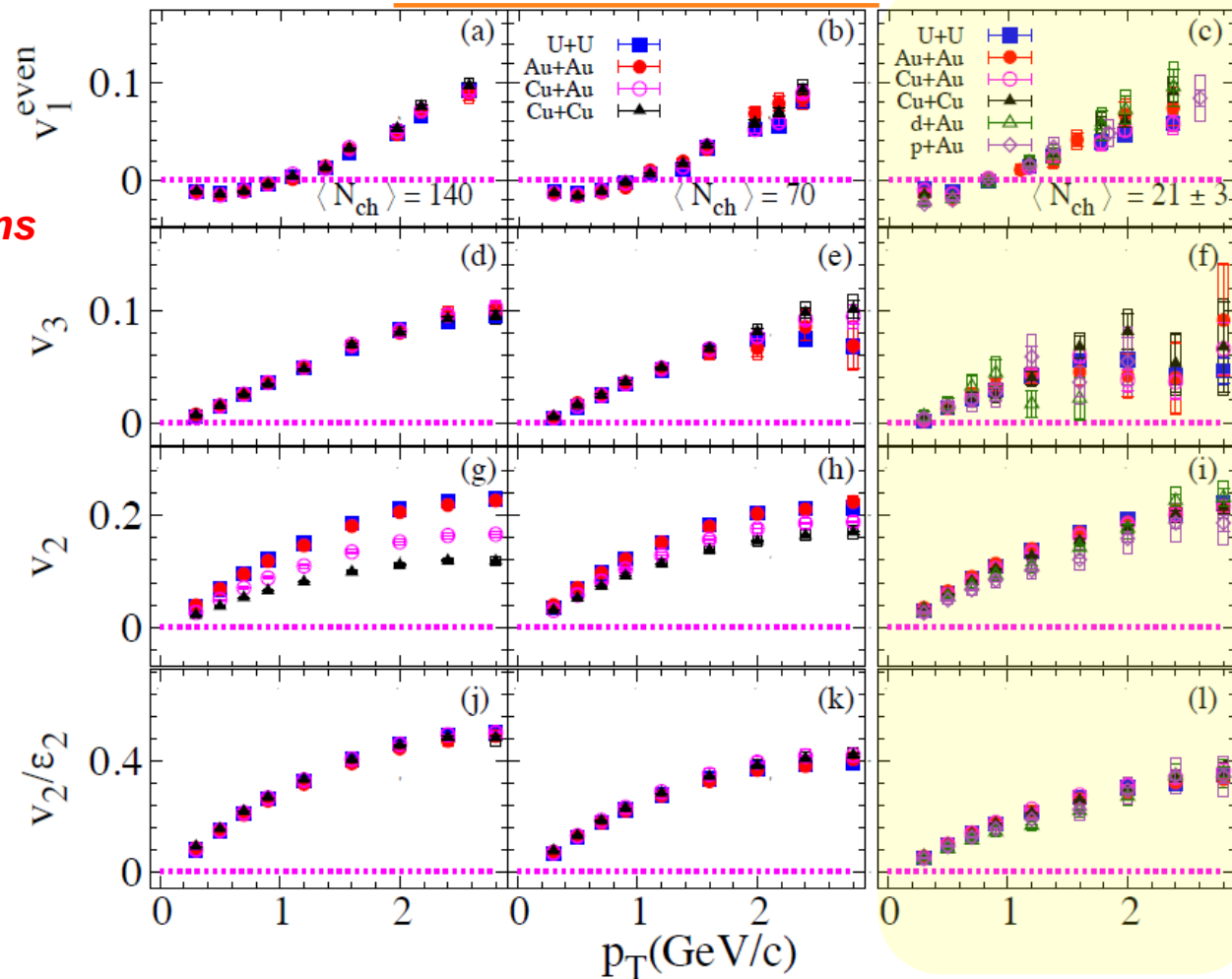
- **Key consequence**
- ✓ **Similar  $v_{2,3}$  patterns expected for small and large collision-systems, for the same dimensionless size  $RT \propto \langle N_{chg} \rangle^{1/3}$ .**
- ✓ **Little difference between collision-systems**

# Shape Response

Comparison of collision-systems at  $\sim$  similar  $\sqrt{s_{NN}}$  and  $\langle N_{ch} \rangle$

✓ Collision-system dependence of  $v_n(p_T)$  for fixed values of  $\langle N_{ch} \rangle$

Challenge to CGC-EFT models?

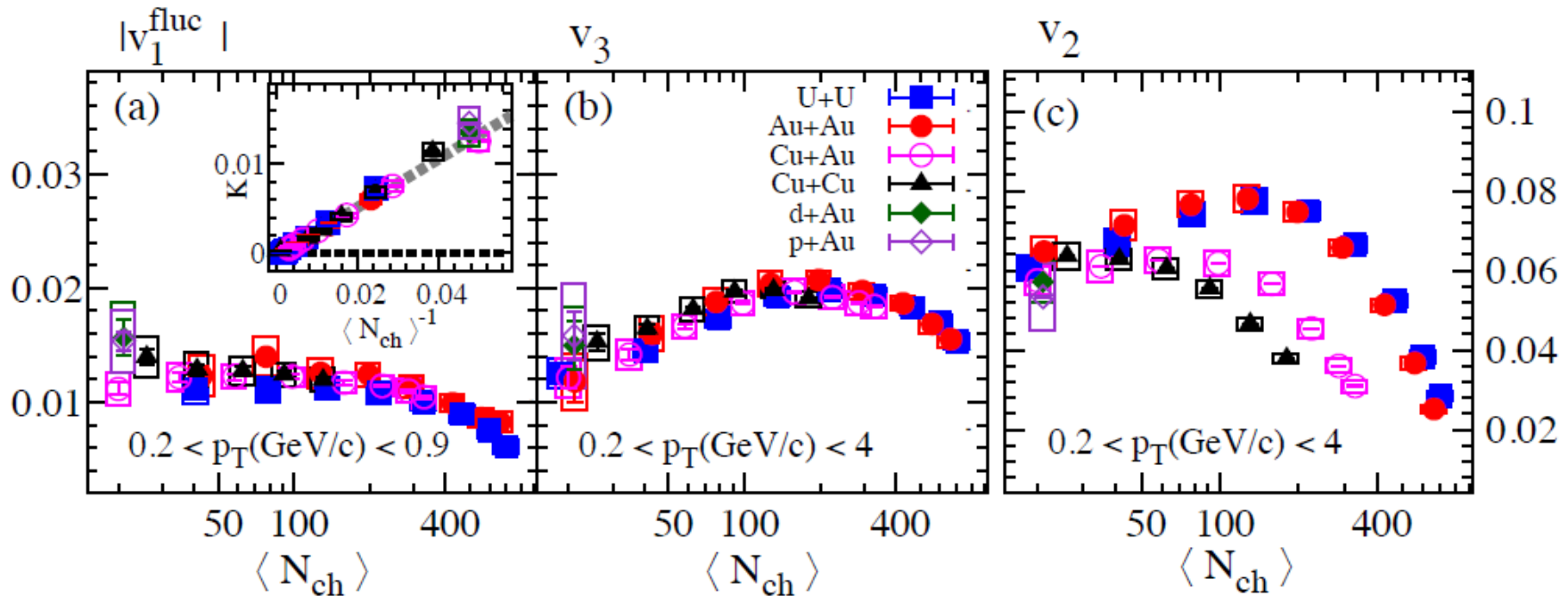


- For a given  $n$ ,  $v_n(p_T)$  shows the predicted trends for all collision-systems.
  - ✓  $v_1^{even}$  and  $v_3$  are system independent.
  - ✓  $v_2$  is system dependent for sizeable  $\langle N_{ch} \rangle$ , but system-independent for small  $\langle N_{ch} \rangle$ .
    - ✓ The eccentricity-scaled  $v_2$  is system independent

# Shape Response

## Comparison of collision-systems at $\sim$ similar $\sqrt{s_{NN}}$ and $\langle N_{ch} \rangle$

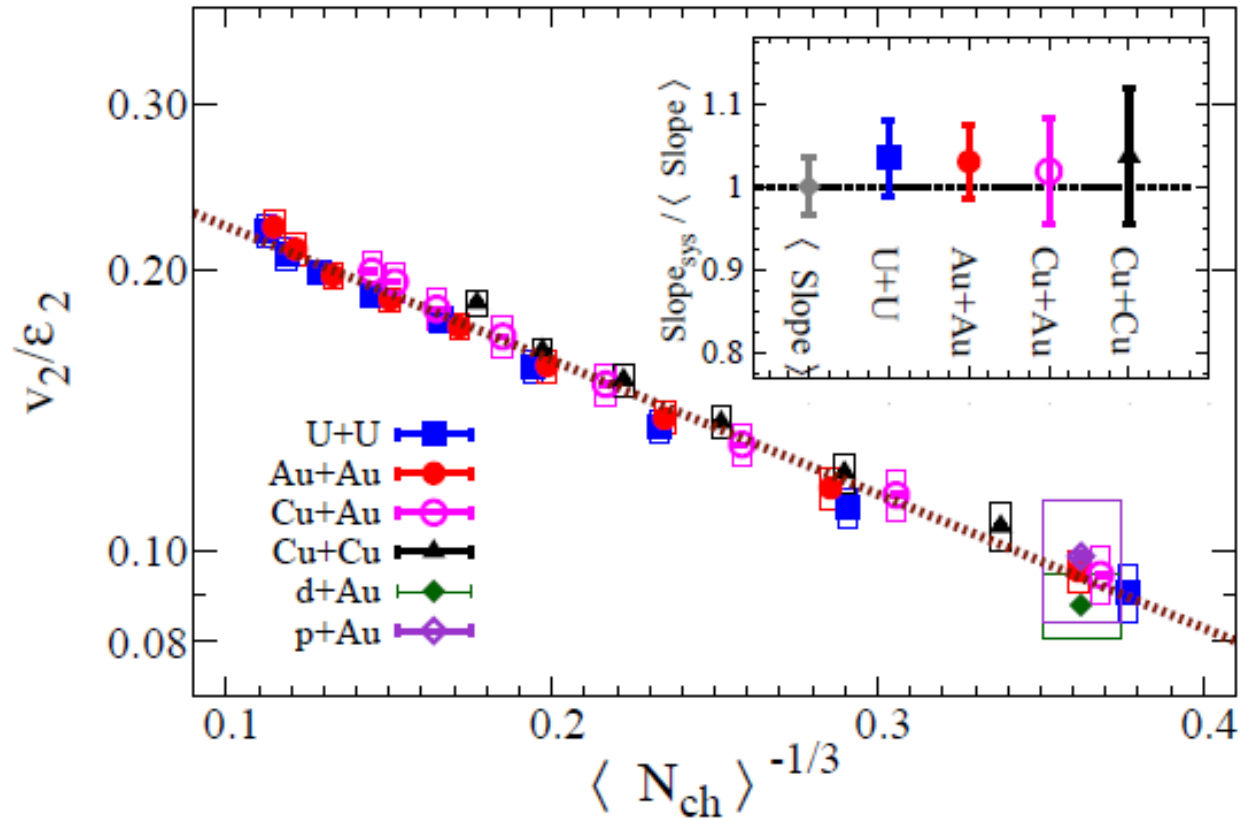
STAR - arXiv:1901.08155



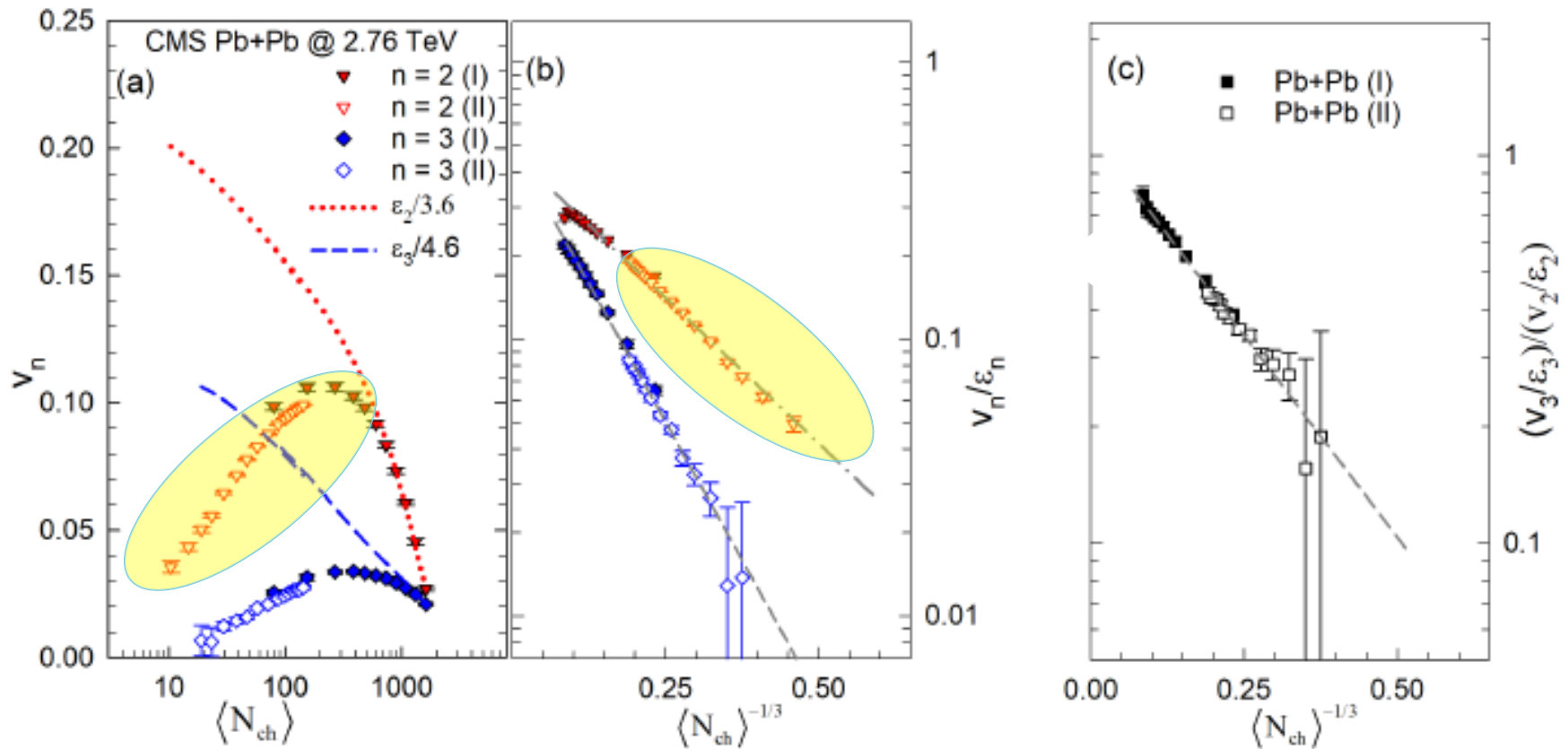
- *For a given  $n$ ,  $v_n(N_{ch})$  show the expected trends for all systems.*
  - ✓  $v_1^{even}$  and  $v_3$  are  $\sim$  system independent.
  - ✓  $v_2$  is system dependent for sizeable  $\langle N_{ch} \rangle$ , but system-independent for small  $\langle N_{ch} \rangle$ .

**Challenge to  
CGC-EFT models?**

$\langle N_{ch} \rangle$  dependence of  $\frac{v_2}{\varepsilon_2}$  for several systems



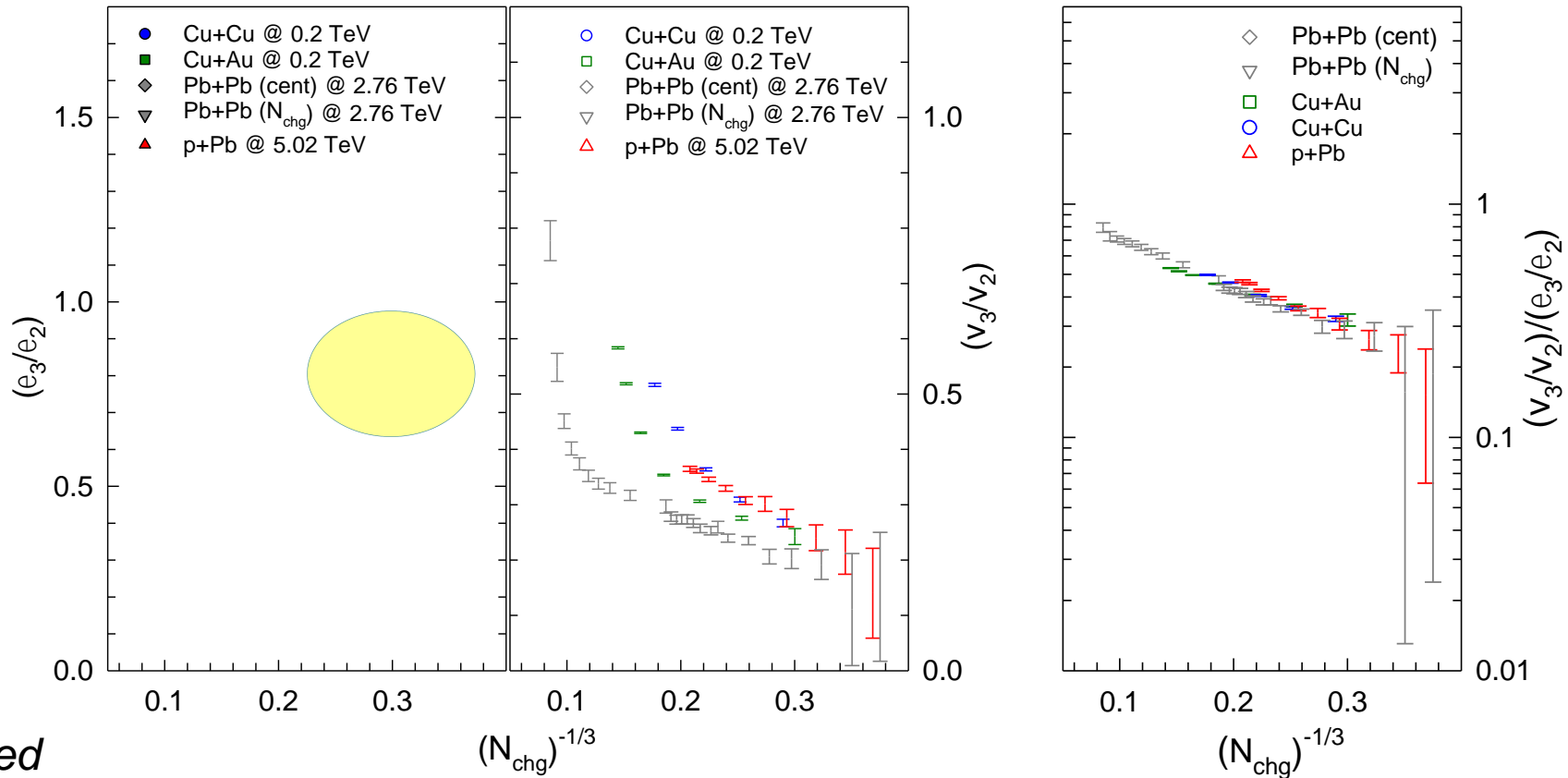
- ✓ Characteristic  $1/(RT)$  viscous damping validated
- ✓ Viscous damping very important for small dimensionless sizes.
- ✓ Similar slopes imply similar  $\frac{\eta}{s}$ .



➤ **Eccentricity considerations alone not sufficient**

- ✓ **Characteristic  $1/(RT)$  viscous damping validated across dimensionless size**
- ✓ **Viscous damping supersedes the influence of eccentricity for “small” systems**
  - ✓ **Important constraint for  $\eta/s$  &  $\zeta/s$**

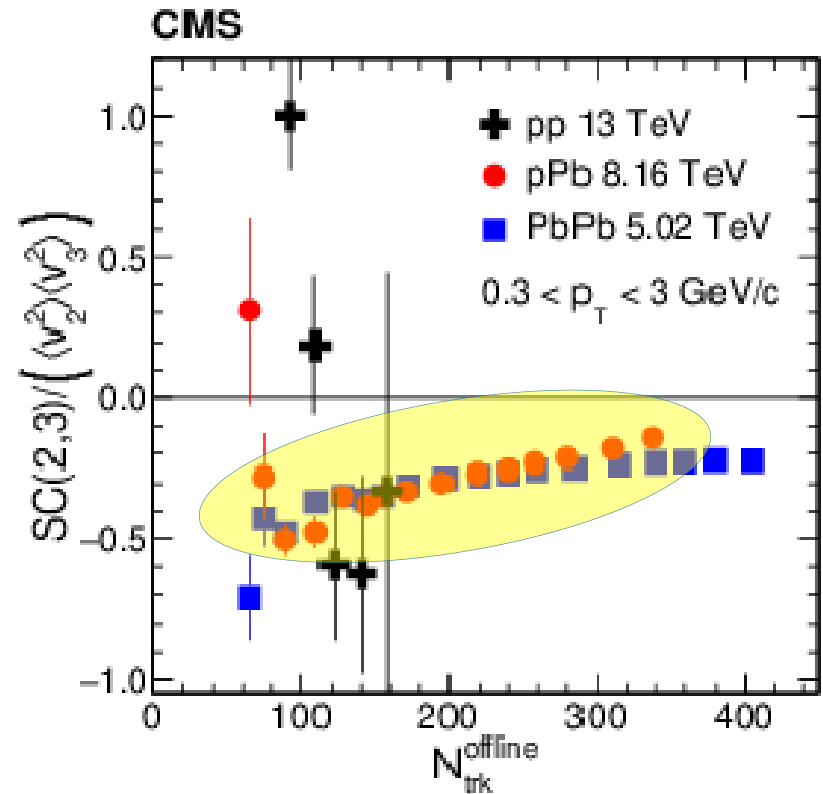
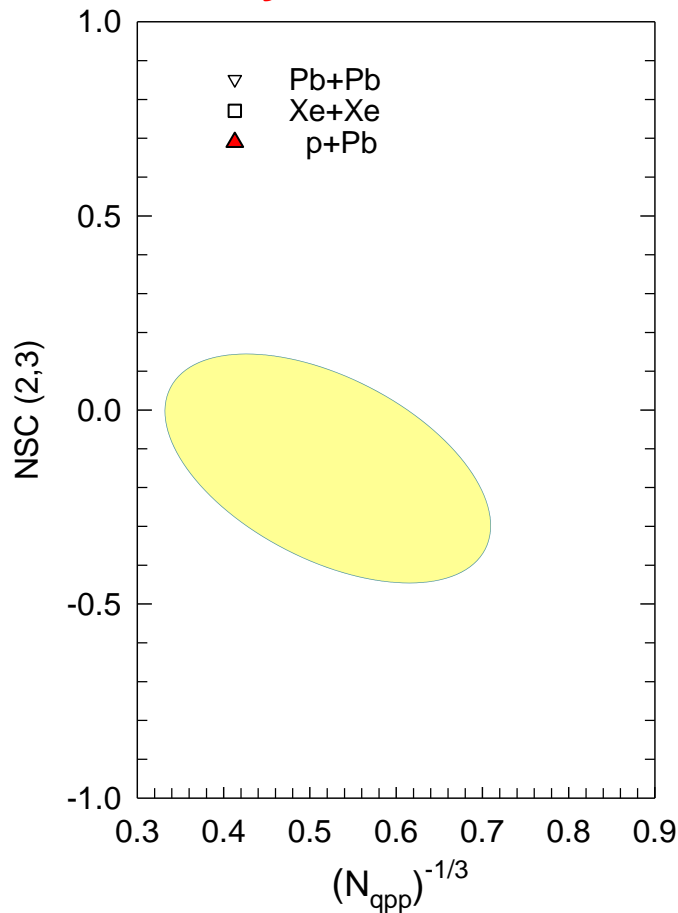
# Acoustic Scaling – System size



Submitted  
for  
Publication

- ✓ **Characteristic  $1/(RT)$  viscous damping validated**
- ✓ **Viscous damping comparable for different collision-systems with similar dimensionless sizes**
  - ✓ **Important constraint for  $\eta/s(T)$  &  $\zeta/s(T)$**

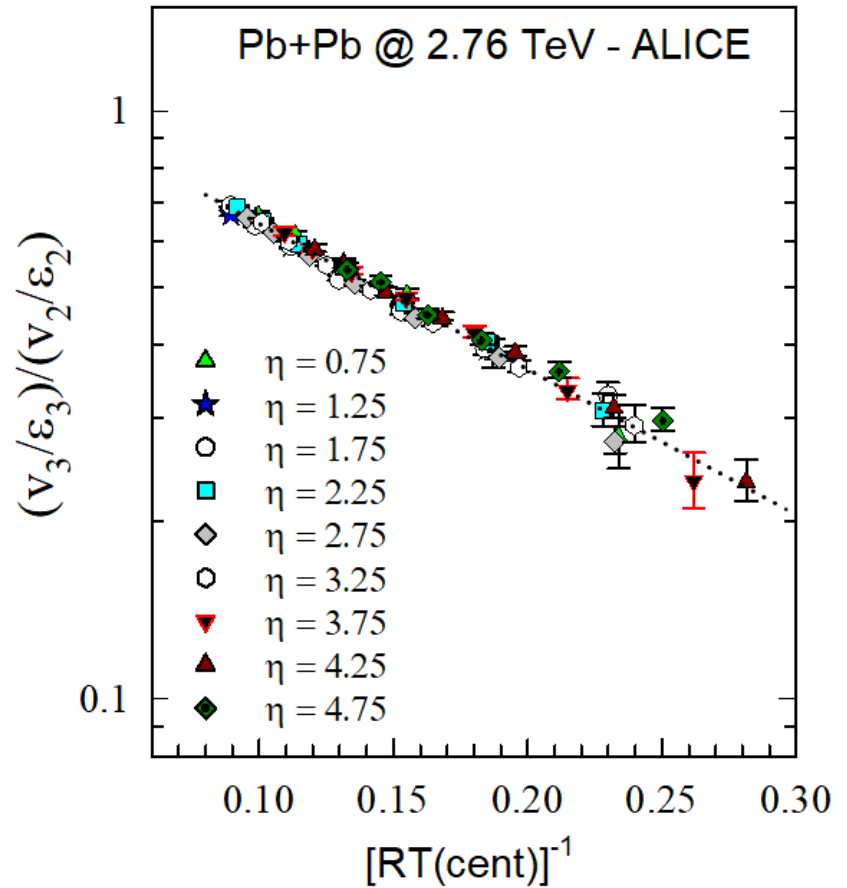
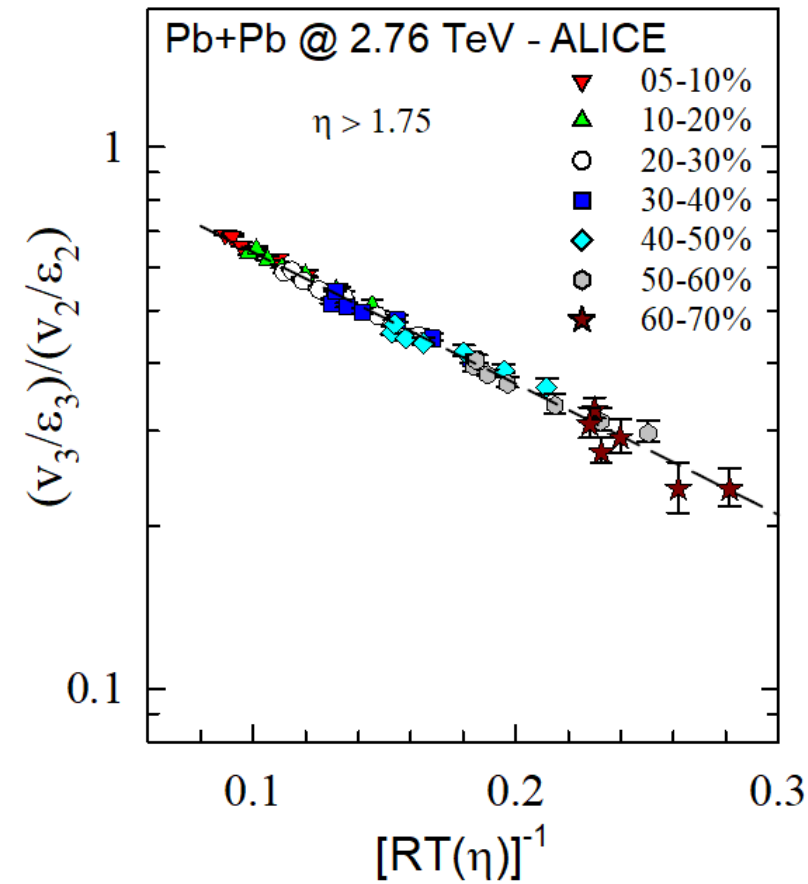
➤ **Model discerning character of normalized symmetric cumulants**



✓ **Characteristic collision-system independent eccentricity anti-correlation**

***This dependency poses a challenge for CGC-EFT models***

## Acoustic Scaling - eta dependence



➤ *The full data set scales*

✓ *Implications for the temperature dependence of  $\dot{\eta}/s$  (high  $T$ )!*

*End*