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# Neutrino Scattering and Nuclear Parton Distributions

What do the concepts of “Factorization” and “Universal” Parton  
Distributions mean in the Nuclear Environment

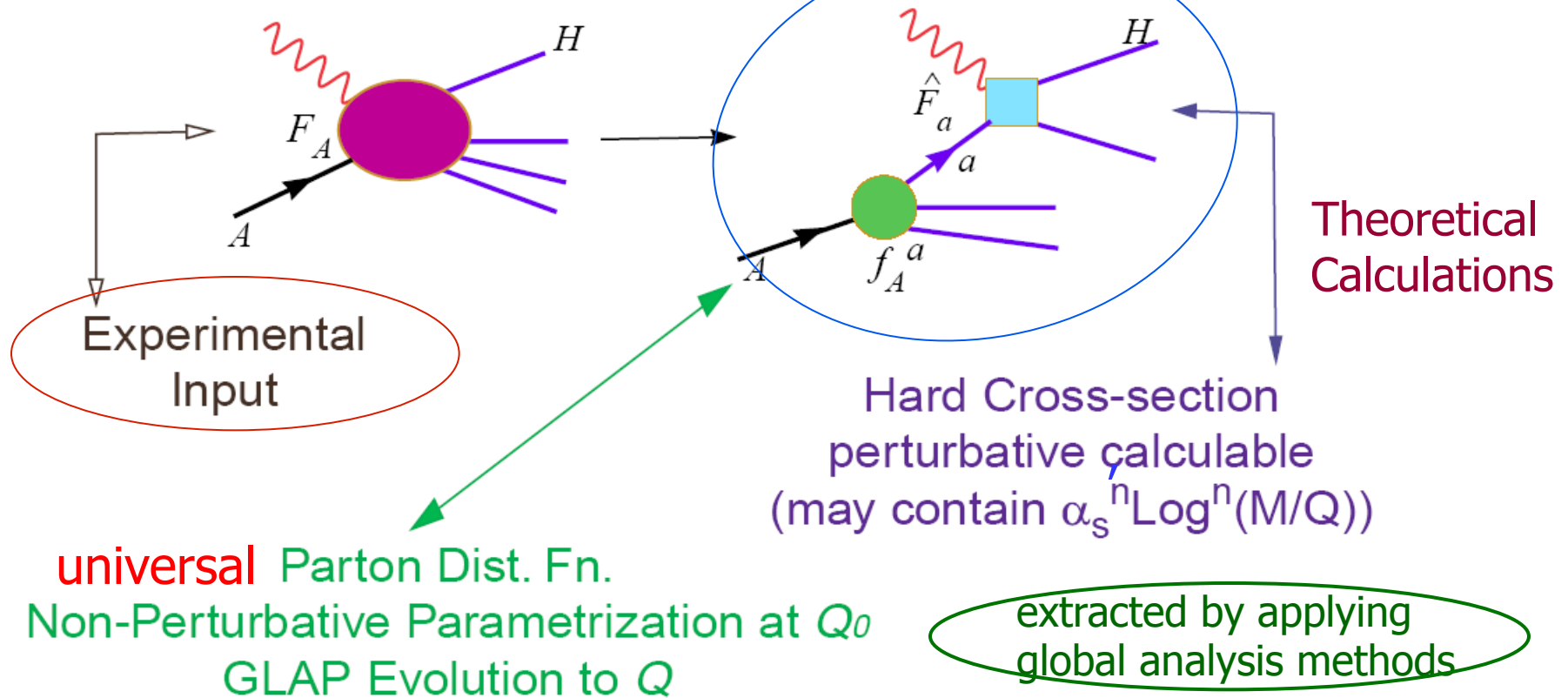
HEP2016 – Valparaiso, Chile  
January 2016

Jorge G. Morfin  
Fermilab

# Global QCD Analysis in a Nutshell

Master Equation for QCD Parton Model  
– the Factorization Theorem

$$F_A^\lambda(x, \frac{m}{Q}, \frac{M}{Q}) = \sum_a f_A^a(x, \frac{m}{\mu}) \otimes \hat{F}_a^\lambda(x, \frac{Q}{\mu}, \frac{M}{Q}) + \mathcal{O}((\frac{\Lambda}{Q})^2)$$



What do the concepts of "factorization" and "universal (nuclear) parton distributions" mean in the nuclear environment?

# The Nuclear Environment

## Nuclear Effects in lepton nucleus Interactions

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- ◆ Target nucleon in motion - spectral functions (Benhar et al.).
- ◆ Certain reactions prohibited - Pauli suppression.
- ◆ Form factors are modified within the nuclear environment. (Butkevich / Kulagin, Tsushima et al.).
- ◆ Interactions with correlated multi-nucleon initial states.
- ◆ Produced topologies are modified by final-state interactions modifying topologies and reducing detected energy.
  - ▼ Convolution of  $\delta\sigma(n\pi)$  formation zone uncertainties  $\pi$ -absorption uncertainties yield larger oscillation-parameter systematics.
- ◆ **Cross sections and structure functions are modified and parton distribution functions within a nucleus are different than in an isolated nucleon. Observations from an on-going CTEQ analysis of nuclear parton distributions.**

# Assumptions entering the nuclear PDF Analysis

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- ◆ **Factorization** & DGLAP evolution

- ▼ allow for definition of **universal** PDFs
- ▼ make the formalism predictive

- ◆ Isospin symmetry

- ▼ 
$$\begin{cases} u^{n/A}(x) = d^{p/A}(x) \\ d^{n/A}(x) = u^{p/A}(x) \end{cases}$$

- ◆  $x \in (0, 1)$  like in free-proton PDFs [instead of  $(0, A)$ ]

- ◆ The observables  $O^A$  can be calculated as:

$$O^A = Z O^{p/A} + (A-Z) O^{n/A}$$

- ◆ **With the above assumptions we can use the free proton framework to analyze nuclear data.**

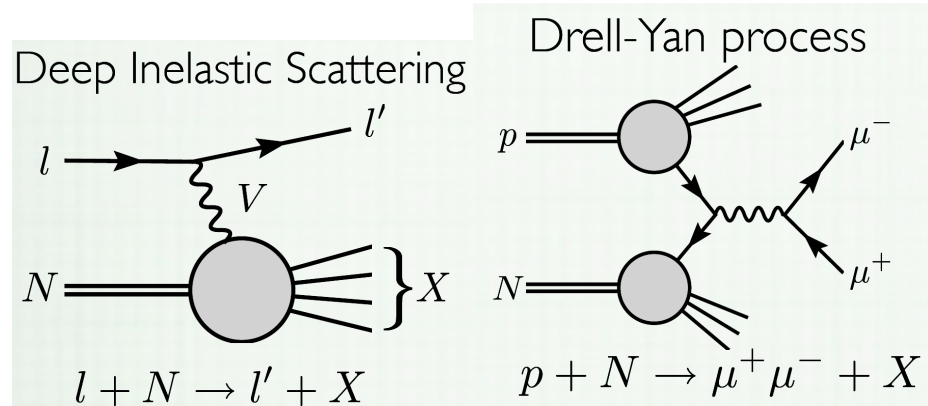
# First: nCTEQ Analysis based on Charged Lepton + D-Y

**No Neutrino Data Here**

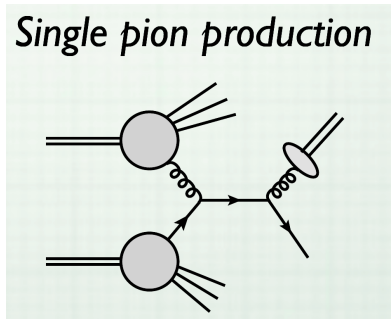
**Long publication describing details out shortly**

►  $L^\pm$  DIS & DY

- CERN BCDMS & EMC & NMC**  
N = (D, Al, Be, C, Ca, Cu, Fe, Li, Pb, Sn, W)
- FNAL E-665**  
N = (D, C, Ca, Pb, Xe)
- DESY Hermes**  
N = (D, He, N, Kr)
- SLAC E-139 & E-049**  
N = (D, Ag, Al, Au, Be, C, Ca, Fe, He)
- FNAL E-772 & E-886**  
N = (D, C, Ca, Fe, W)

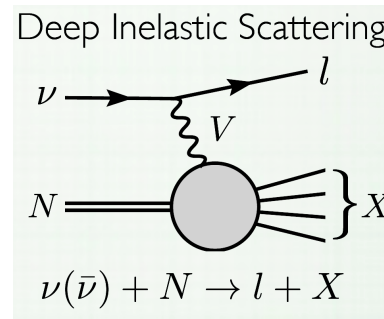


► Single pion production (new)



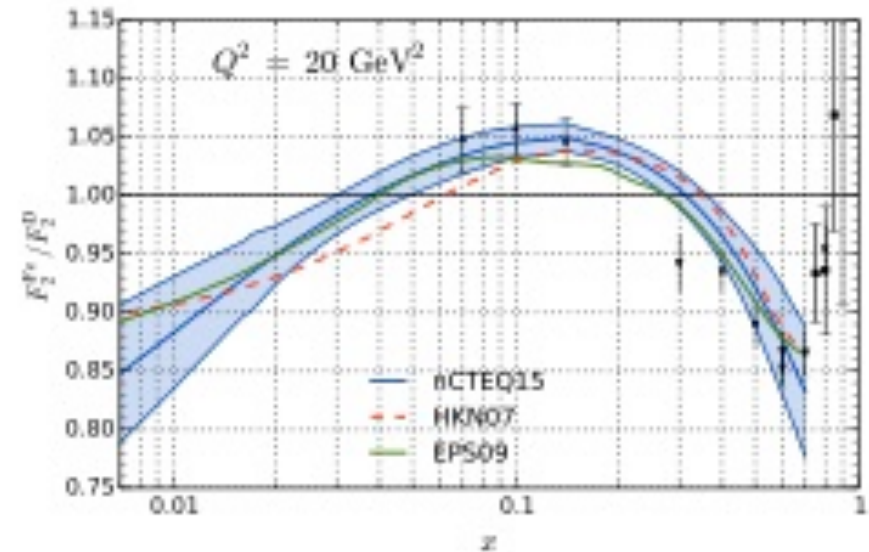
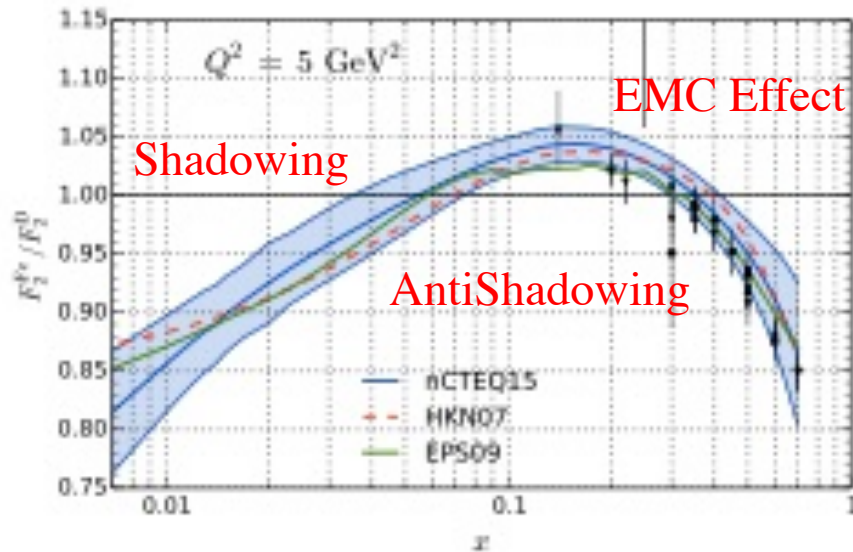
**RHIC - PHENIX & STAR**  
N = Au

► Neutrino (to be included later)



**CHORUS CCFR & NuTeV**  
N = Pb N = Fe

# nCTEQ results – charged lepton: $F_2$ ratios for Fe/D



## Now for Neutrinos

- ◆  $F_2$  / nucleon changes as a function of  $A$ . Measured in  $\mu/e - A$  not yet in  $\nu - A$
- ◆ Good reason to consider nuclear effects are DIFFERENT in  $\nu - A$ .
  - ▼ Presence of axial-vector current.
  - ▼ Different nuclear effects for valance and sea --> different shadowing for  $xF_3$  compared to  $F_2$ .
  - ▼ All flavor dependent nuclear effects will be different for  $\nu - A$ .

# Addressing the lack of $F_2^{\nu}$ Nuclear Effects Analyses

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## **Nuclear PDFs from neutrino deep inelastic scattering Using NuTeV $\nu$ -Fe and CHORUS $\nu$ -Pb Data**

**I. Schienbein (SMU & LPSC-Grenoble, J-Y. Yu (SMU)  
C. Keppel (Hampton & JeffersonLab) J.G.M. (Fermilab),  
F. Olness (SMU), J.F. Olness (Florida State U)**

Also analyses by:

K. Eskola, V. Kolhinen, Paukkunen and C. Salgado  
and

D. de Florian, R. Sassot, P. Zurita and M. Stratmann  
and

M.Hirai, S. Kumano and T.-H. Nagai

# CTEQ $\nu$ nuclear effects study

No high-statistics  $D_2$  data – “make it” from PDFs

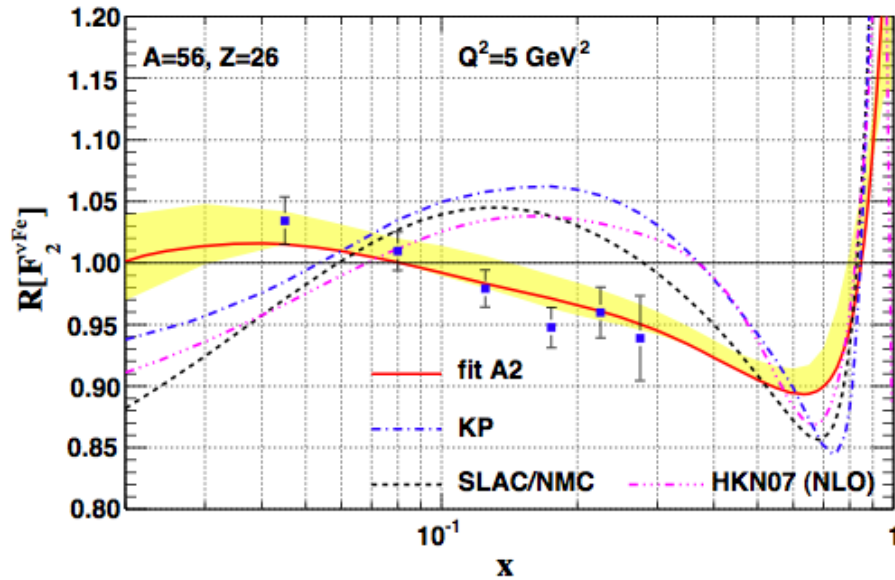
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- ◆ Form reference fit with nucleon (as opposed to nuclear  $A>2$ ) scattering results:
  - ▼ BCDMS results for  $F_2^p$  and  $F_2^d$
  - ▼ NMC results for  $F_2^p$  and  $F_2^d/F_2^p$
  - ▼ H1 and ZEUS results for  $F_2^p$
  - ▼ CDF and DØ result for inclusive jet production
  - ▼ CDF results for the W lepton asymmetry
  - ▼ E-866 results for the ratio of lepton pair cross sections for pd and pp interactions
  - ▼ E-605 results for dimuon production in pN interactions.
  
- ◆ Correct for deuteron nuclear effects

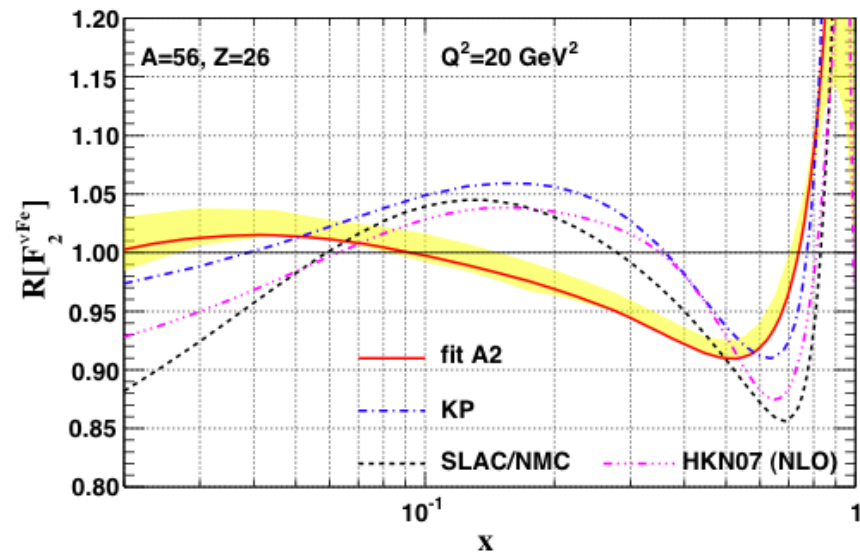


# $F_2$ Structure Function Ratios: $\nu$ -Iron

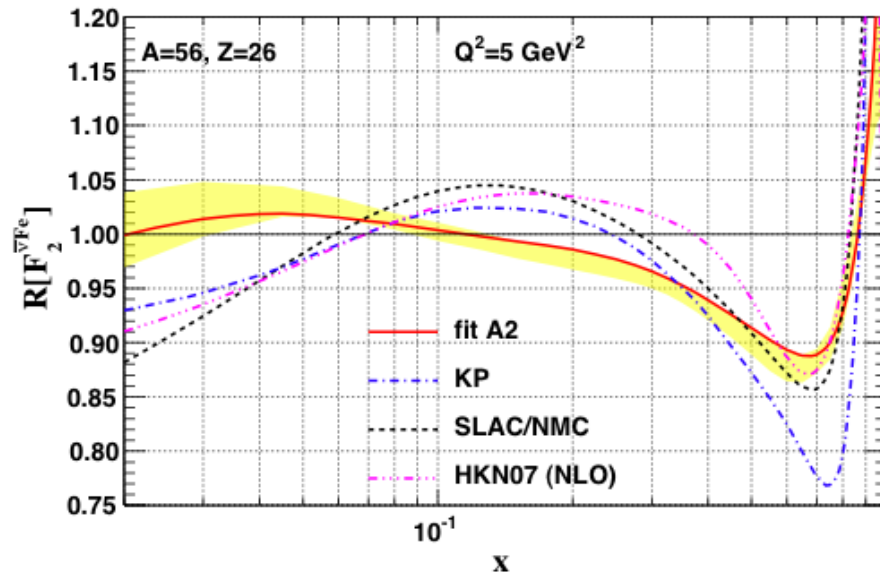
Using NuTeV  $\nu$ -Iron double differential cross sections



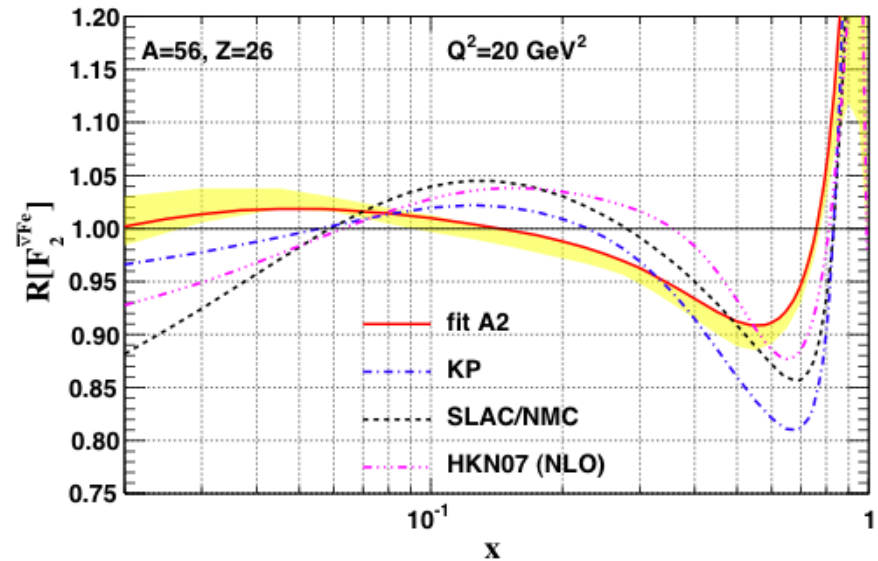
$$\frac{F_2(\nu + \text{Fe})}{F_2(\nu + [n+p])}$$



# $F_2$ Structure Function Ratios: $\bar{\nu}$ -Iron

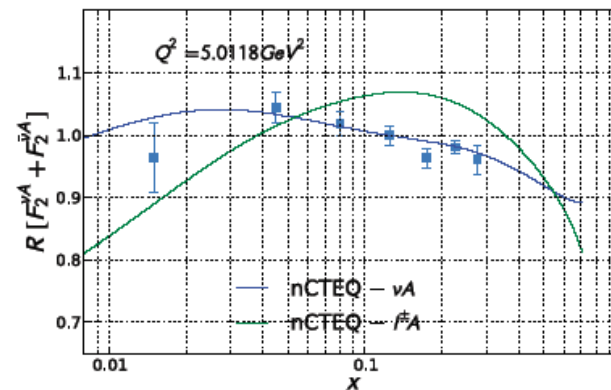
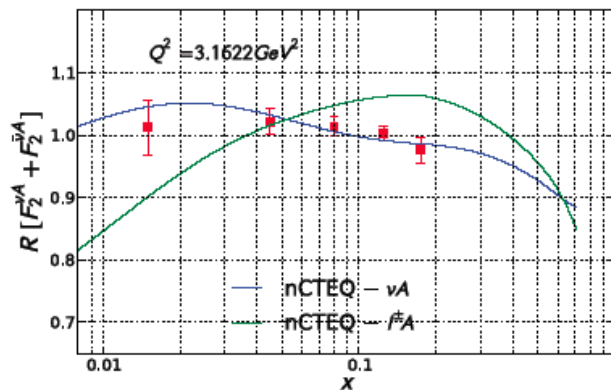
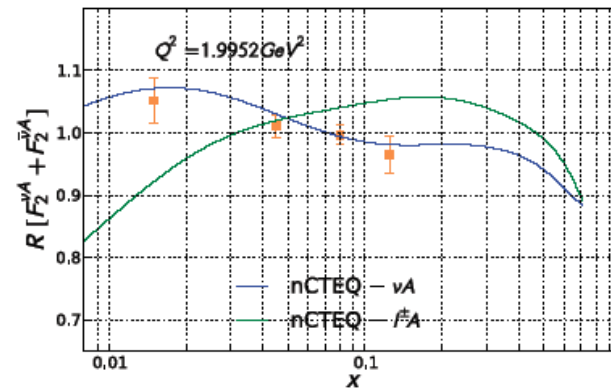
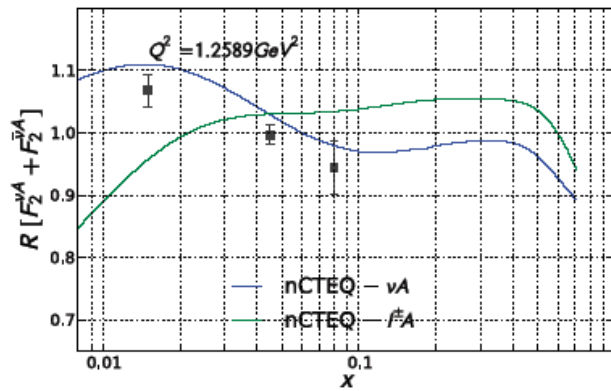


$$\frac{F_2(\bar{\nu} + \text{Fe})}{F_2(\bar{\nu} + [n+p])}$$



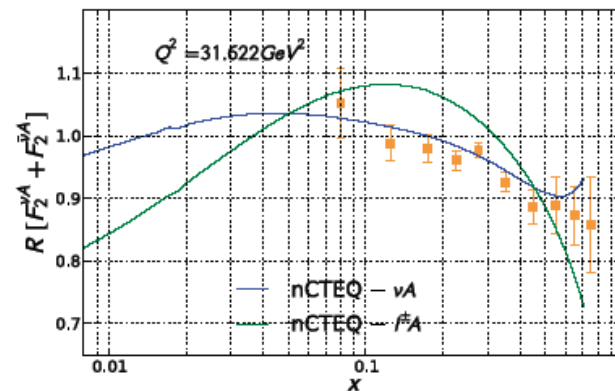
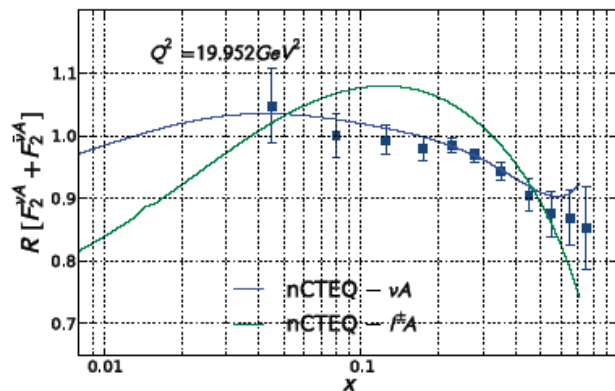
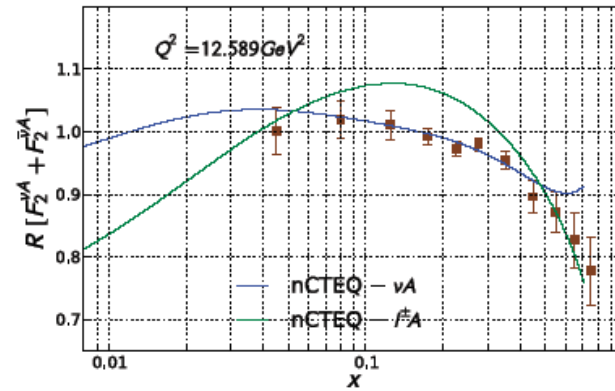
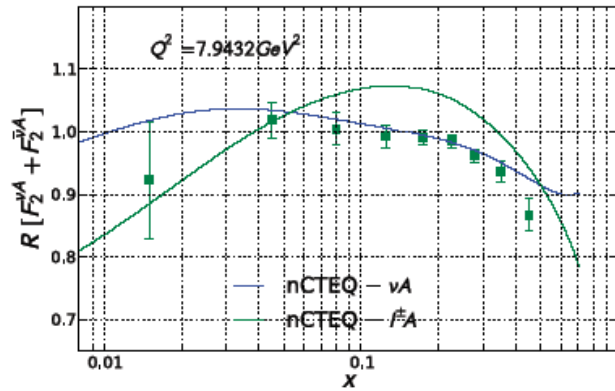
# A More-Detailed Look at Differences

- ◆ NLO QCD calculation of  $\frac{F_2^{\nu A} + F_2^{\bar{\nu} A}}{2}$  in the ACOT-VFN scheme
  - ▼ charge lepton fit undershoots low-x data & overshoots mid-x data
  - ▼ low- $Q^2$  and low-x data cause tension with the shadowing observed in charged lepton data



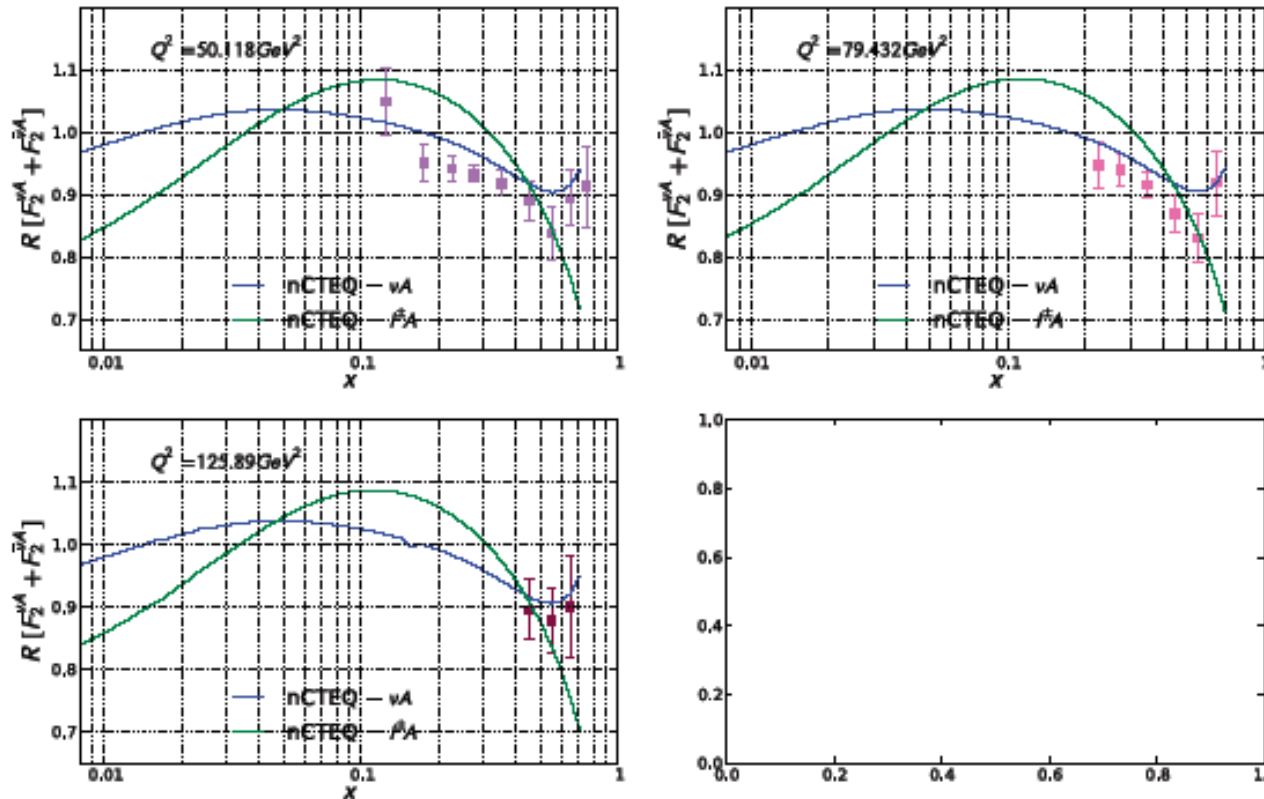
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# Can we get a reasonable **combined** fit of $\nu A$ , $\ell A$ and DY

**Kovarik**, Yu, Keppel, Morfin, Olness, Owens, **Schienbein**, Stavreva

- 
- ◆ Take the earlier analysis of  $\ell^\pm A$  data sets (built in A-dependence)
    - ▼ Schienbein, Yu, Kovarik, Keppel, Morfin, Olness, Owens,
    - ▼ PRD80 (2009) 094004
  - ◆ For  $\ell^\pm A$  take  $F_2(A) / F_2(D)$  and  $F_2(A) / F_2(A')$  and DY  $\sigma(pA) / \sigma(pA')$ 
    - ▼ 708 Data points with  $Q > 2$  and  $W > 3.5$
  - ◆ Use **8 Neutrino data sets**
    - ▼ NuTeV cross section data:  $\nu Fe, \bar{\nu} Fe$
    - ▼ NuTeV dimuon off Fe data
    - ▼ CHORUS cross section data:  $\nu Pb, \bar{\nu} Pb$
    - ▼ CCFR dimuon off Fe data
  - ◆ Initial problem, with standard CTEQ cuts of  $Q > 2$  and  $W > 3.5$   
**neutrino data points (3134) far outnumber  $\ell^\pm A$  (708)**. Multiply neutrino results by weight  $w$ .

# Quantitative $\chi^2$ Analysis of a Combined Fit:

## No combination satisfies tolerance requirement

- ◆ Up to now we are giving a qualitative analysis. Consider next quantitative criterion based on  $\chi^2$
- ◆ Introduce “tolerance” (T). Condition for compatibility of two fits:  
The 2nd fit  $\chi^2$  should be within the 90% C.L. region of the first fit  $\chi^2$
- ◆ Charged:  $638.9 \pm 45.6$  (best fit to charged lepton and DY data)
- ◆ Neutrino:  $4192 \pm 138$  (best fit to only neutrino data)

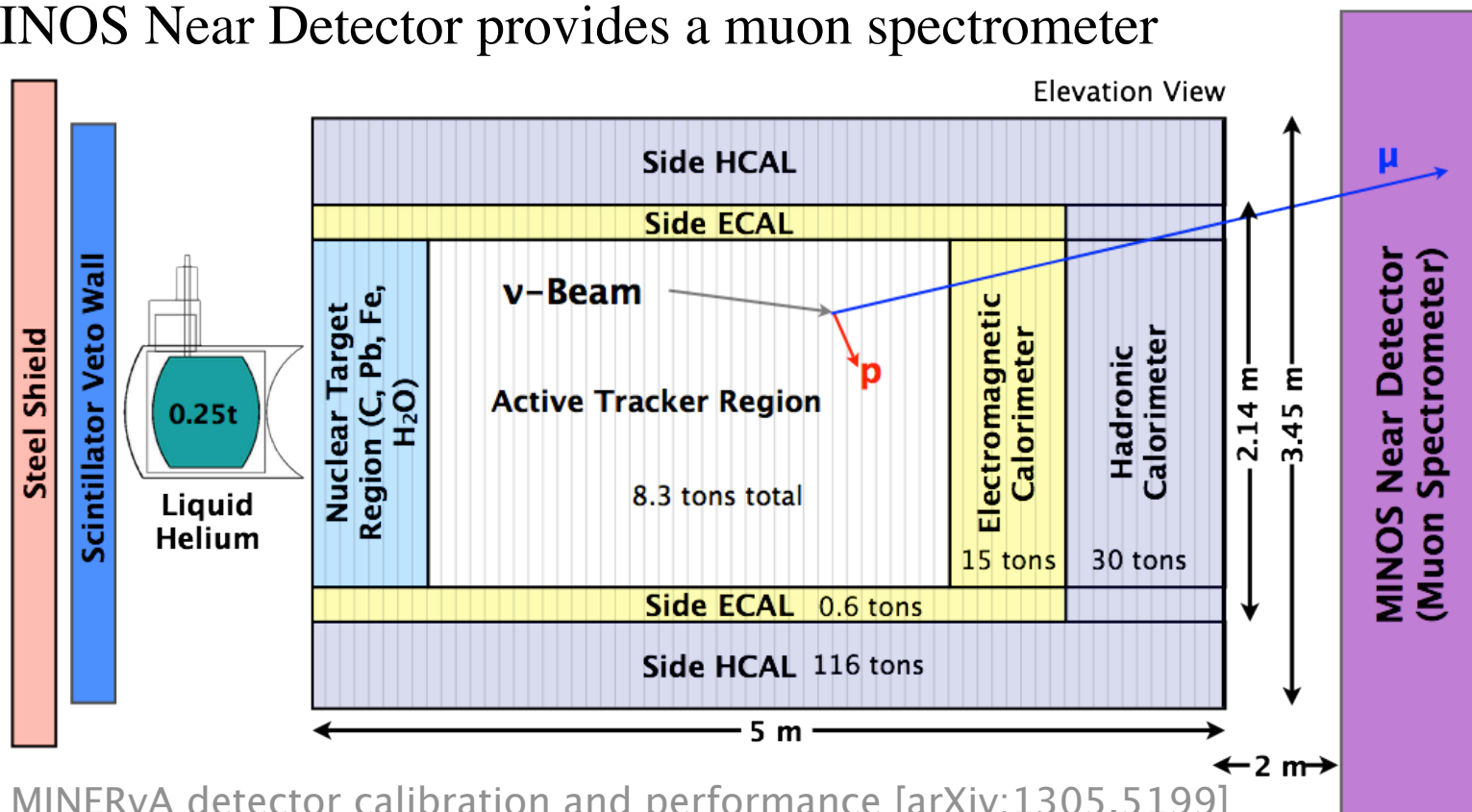
Weight	Fit name	$\ell$ data	$\chi^2$	$\nu$ data	$\chi^2$	total $\chi^2$ (/pt)
$w = 0$	decut3	708	639	-	nnnn <b>NO</b>	639 (0.90)
$w = 1/7$	glofac1a	708	645 <b>YES</b>	3134	4710 <b>NO</b>	5355 (1.39)
$w = 1/4$	glofac1c	708	654 <b>YES</b>	3134	4501 <b>NO</b>	5155 (1.34)
$w = 1/2$	<b>glofac1b</b>	708	680 <b>YES</b>	3134	4405 <b>NO***</b>	5085 (1.32)
$w = 1$	global2b	708	736 <b>NO</b>	3134	4277 <b>YES</b>	5014 (1.30)
$w = \infty$	nuanua1	-	nnn <b>NO</b>	3134	4192	4192 (1.33)

- ◆ **We need a fresh look with direct measurements of nuclear target ratios in a neutrino experiment!**

# A new direct look at $\nu$ A scattering Then MINER $\nu$ A Experiment

See Chris Marshall's talk tomorrow for details

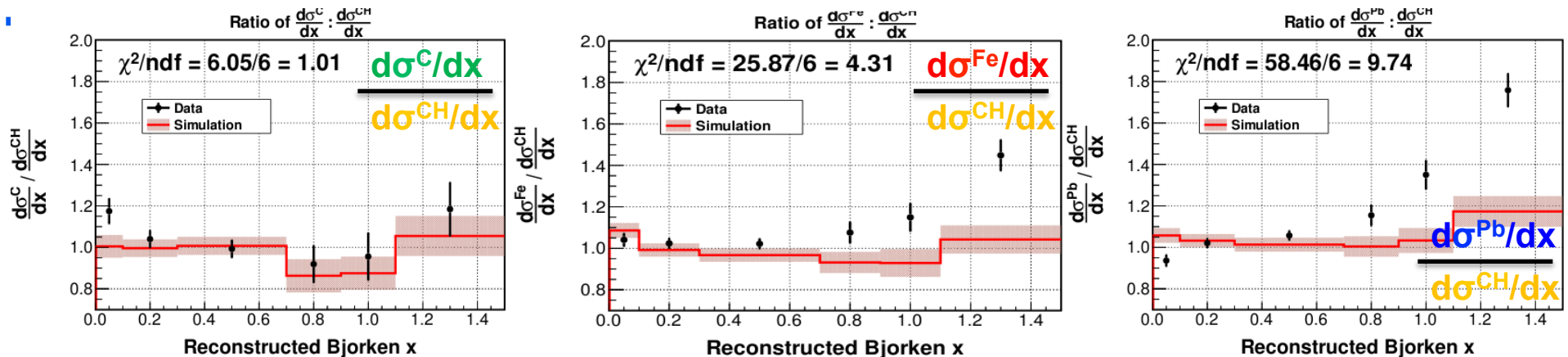
- ◆ 120 modules for tracking and calorimetry (~32k channels)
  - ▼ Active element is polystyrene (extruded plastic scintillator)
- ◆ Fully commissioned in Spring 2010
- ◆ MINOS Near Detector provides a muon spectrometer



The MINER $\nu$ A detector calibration and performance [arXiv:1305.5199]



# Inclusive Cross Section Ratios – $d\sigma / dx_{Bj}$ Compared to the GENIE Event Generator Predictions



Reconstructed  $x$  (no correction for detector smearing)

Tice et al., PRL 112 (2014) 231801

Taking ratios removes uncertainties due to the neutrino flux, acceptance, ...

*At low  $x$* ,  $x < 0.1$ , observe a *deficit* that increases with the size of the nucleus (possibly additional nuclear shadowing in  $\nu$  scattering, *study more directly in DIS*)

*At high  $x$* ,  $x > 0.7$ , observe an *excess* that grows with the size of the nucleus (events are dominated by CCQE and resonances)

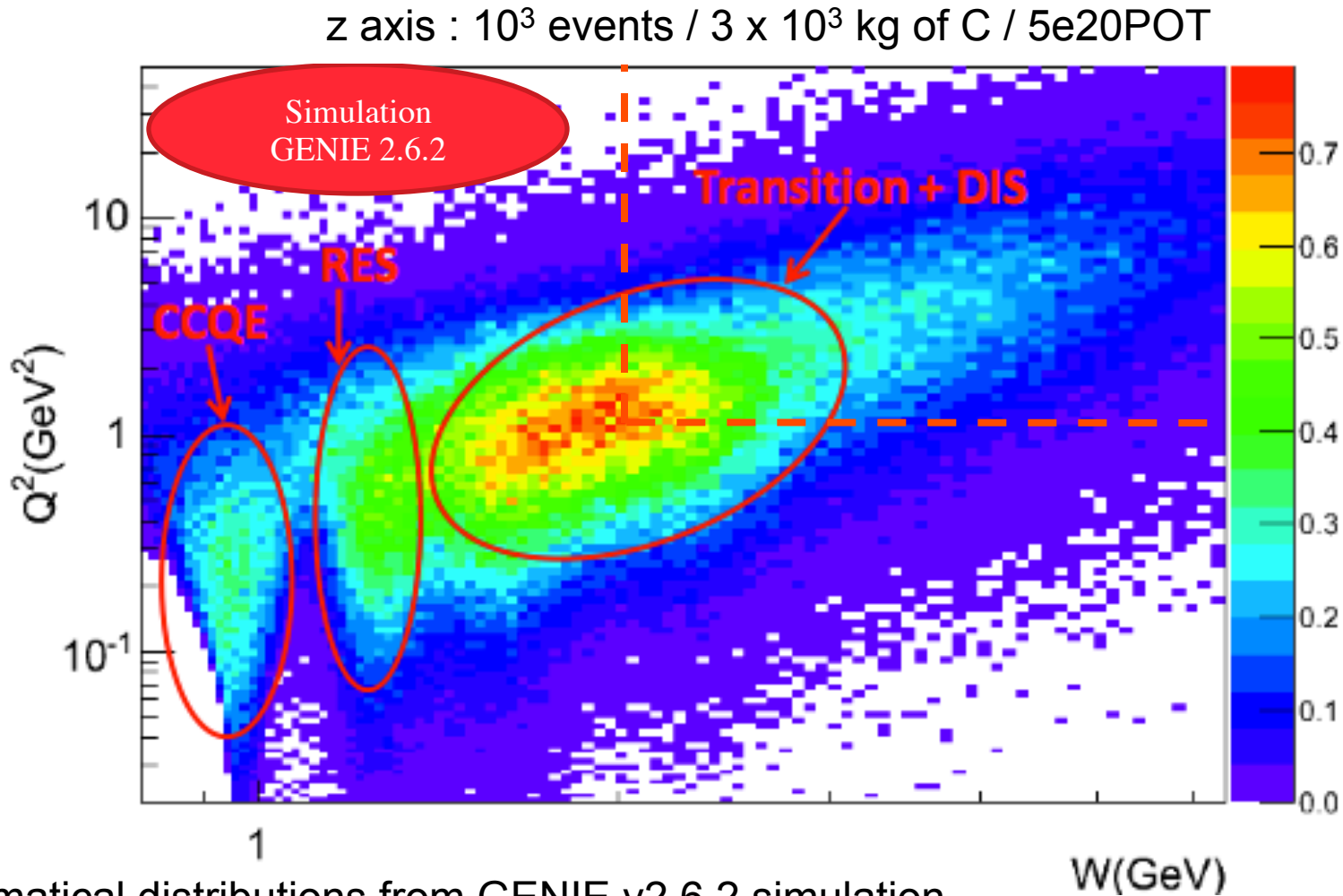
These effects are not reproduced by current neutrino interaction models

GENIE assumes an  $x$  dependent effect from charged lepton scattering on nuclei but  $\nu$  sensitive to  $xF_3$  and also to the axial part of  $F_2$

When studied as a function of  $E_\nu$ :

no evidence of tension between MINERvA data and GENIE 2.6.2 simulations

W – Q<sup>2</sup> Kinematical Region in LE Beam  
Select **DIS** sample by requiring Q<sup>2</sup> > 1.0 GeV<sup>2</sup> and W > 2.0 GeV  
Extend E<sub>ν</sub> to 50 GeV : 5 < E<sub>ν</sub> < 50 GeV

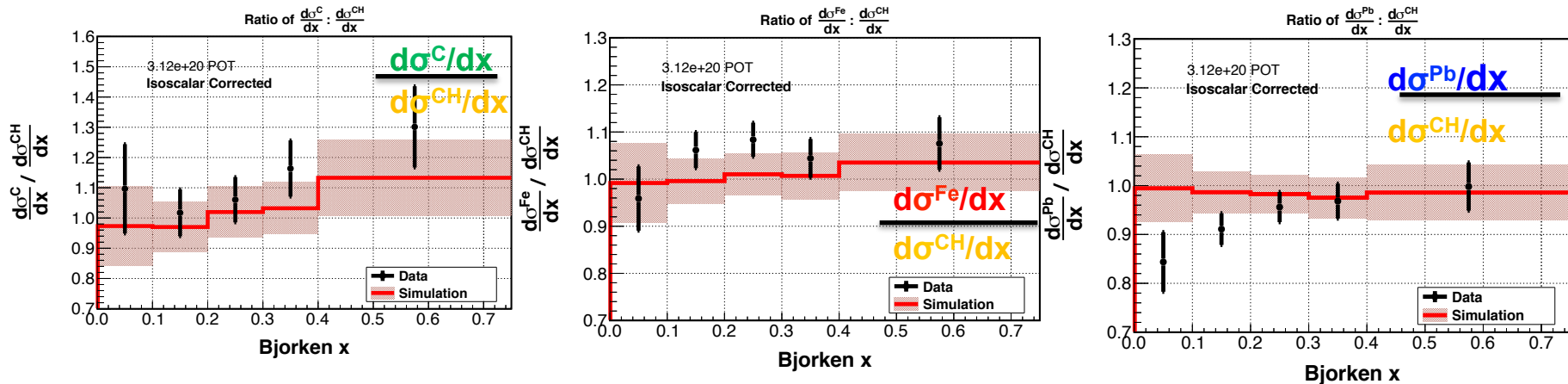


kinematical distributions from GENIE v2.6.2 simulation  
events shown have muon tracked in MINOS

# We Now Have A New DIS Player - What does MINERvA see?

## DIS Cross Section Ratios – $d\sigma / dx_{Bj}$

J. Mousseau, PhD thesis



Unfolded  $x$  (detector smearing)

$$x_{Bj} = \frac{Q^2}{2ME_{had}}$$

DIS: interpret data at partonic level

$x$  dependent ratios directly translates to  $x$  dependent nuclear effects

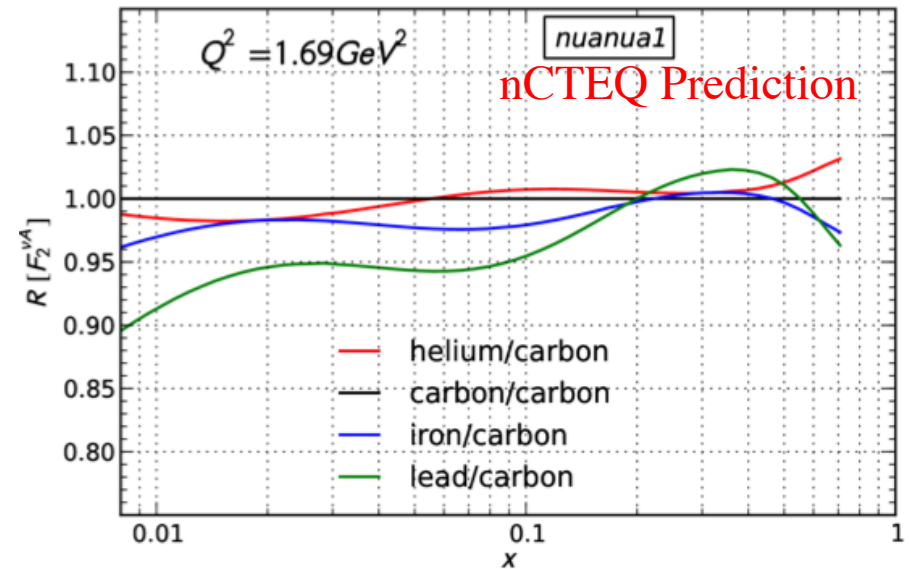
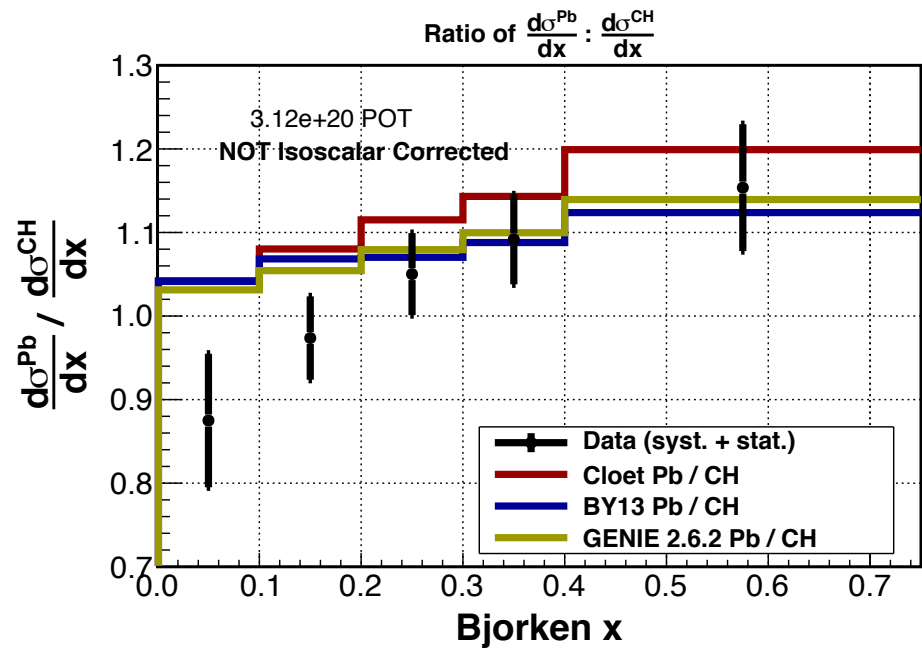
(cannot reach the high- $x$  with LE data sample)

MINERvA data suggests additional nuclear shadowing in the lowest  $x$  bin

( $\langle x \rangle = 0.07$ ,  $\langle Q^2 \rangle = 2 \text{ GeV}^2$ )

In EMC region ( $0.3 < x < 0.7$ ) agreement between data and models

# Shadowing in Neutrino Interactions: Pb / CH



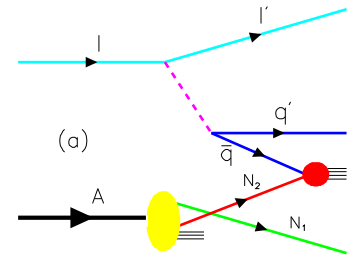
- ◆ Although not yet statistically significant the trend is certainly suggestive of something interesting happening in the low-x region of Pb/CH.
- ◆ **The data is consistent with nuclear shadowing at an  $\langle x \rangle$  (0.07) &  $\langle Q^2 \rangle$  (2 GeV<sup>2</sup>) where negligible shadowing is expected with  $l^\pm$ .**

# Shadowing in Neutrino Interactions

## Difference expected compared to $l^\pm$ A

Nuclear Shadowing in Electro-Weak Interactions - Kopeliovich, JGM and Schmidt arXiv:1208.6541

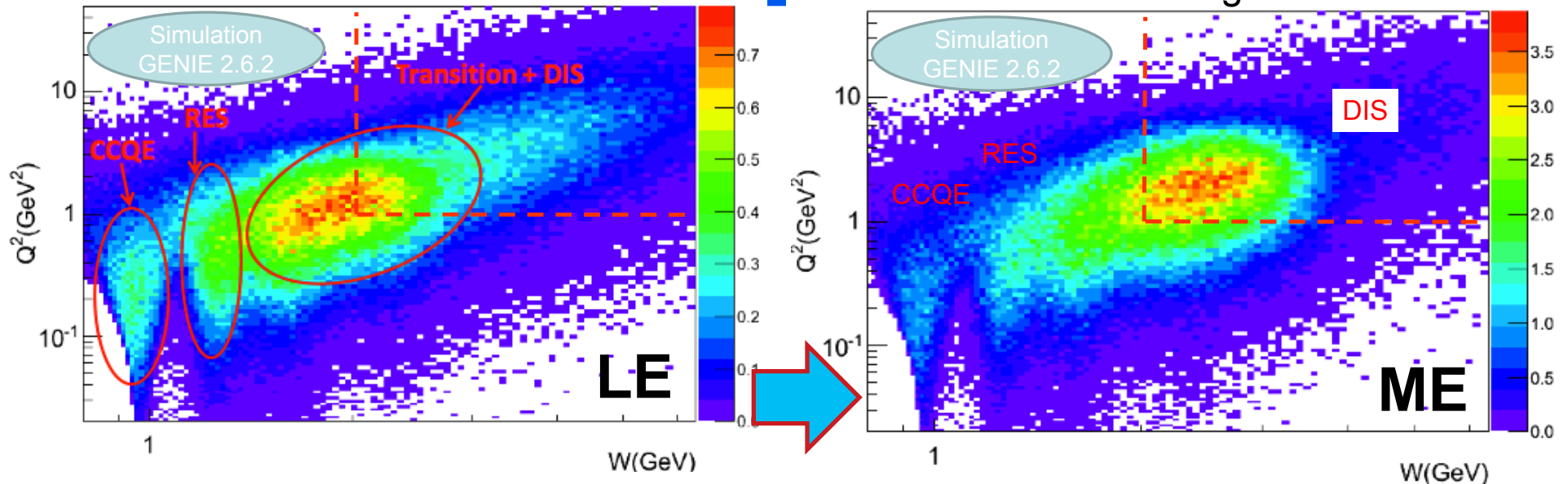
- ◆ Most successful theoretical models of shadowing are based on hadronic fluctuations of the  $\gamma$  (or  $W/Z$  for neutrinos)
- ◆ These fluctuations then undergo multiple diffractive scattering off leading nucleons in the nucleus.
- ◆ The lifetime  $t_c$  of the hadronic fluctuation has to be sufficient to allow for these multiple diffractive scatters.
- ◆ For a given  $Q^2$  need large  $E_{\text{had}}$  to yield sufficient  $t_c$  which implies small  $x$ .
- ◆ For a given  $Q^2$  you need more  $E_{\text{had}}$  for the vector current than the axial vector current to have sufficient  $t_c$ .
- ◆ **This implies you can have shadowing at higher  $x$  with neutrinos than with charged leptons**



# Need Higher Statistics: Prospects for DIS with ME Beams

W – Q<sup>2</sup> Kinematical Region in LE and ME

z axis : 10<sup>3</sup> events / 3 x 10<sup>3</sup> kg of C / 5e20 POT



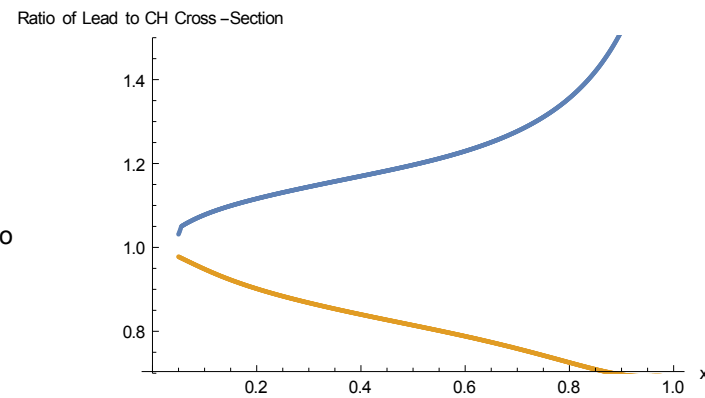
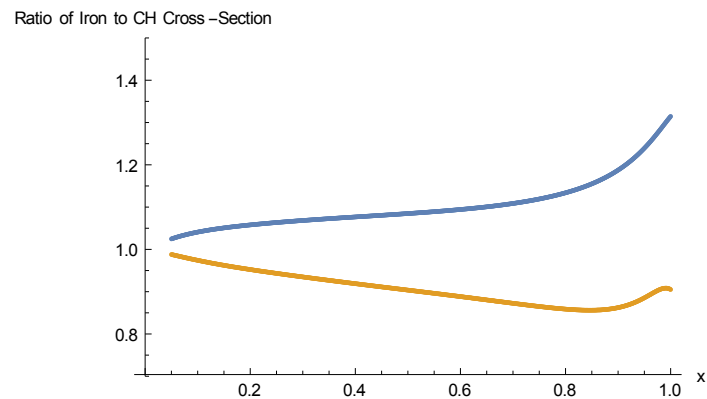
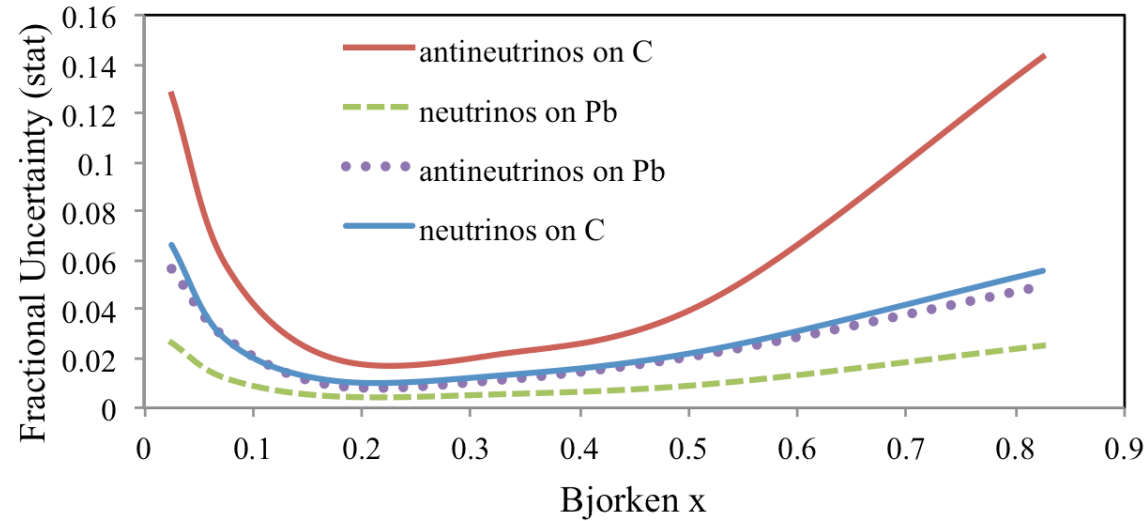
Many more neutrino interactions in DIS regime

- higher beam energy
- increased statistics (beam intensity, energy) and kinematic reach
- improve on systematical uncertainties
- structure function measurements on different nuclei
- probe quark flavor dependence of nuclear effects

Requested 10 x 10<sup>20</sup> POT in neutrino and  
12 x 10<sup>20</sup> POT in antineutrino mode

# ME Physics Reach on Nuclear Effects

Assume  $10 \times 10^{20}$  POT in neutrino mode,  $12 \times 10^{20}$  POT in antineutrino mode



Prediction from Cloet model described in PRL 109, 182301

## Summary and Conclusions

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- ◆ There are indications from the nCTEQ analysis of **one** experiment using **one** nucleus that  **$\nu$ -induced parton-level nuclear effects are quite different** than  $\ell^\pm$ -nuclear effects.
- ◆ MINER $\nu$ A has performed a systematic study of nuclear medium modifications of hadronic structure using different nuclear targets in the same detector exposed to the same neutrino beam. **First measurement of ratios of neutrino cross sections on nuclei in the DIS regime.**
- ◆ **In the lowest  $x$  bin MINER $\nu$ A data suggests nuclear shadowing at an  $\langle x \rangle$  (0.07) &  $\langle Q^2 \rangle$  (2 GeV<sup>2</sup>) where negligible shadowing is expected with  $\ell^\pm$ . This is consistent with axial-vector expectations but different than nCTEQ claims.**
- ◆ Need systematic high-statistics **experimental** study of  **$\nu$ -induced nuclear effects in A (and D<sub>2</sub>) such as MINER $\nu$ A in the ME Beam.**
- ◆ **SO WHAT ABOUT THE CONCEPTS OF FACTORIZATION AND UNIVERSAL PDFS IN THE NUCLEAR ENVIRONMENT**



# Additional Details

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## Fit Details

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- ◆ Fit @ NLO with  $Q_0 = 1.3 \text{ GeV}$
- ◆ Using ACOT heavy quark scheme
- ◆ Kinematic cuts:
  - ▼  $Q > 2 \text{ GeV}, W > 3.5 \text{ GeV}$
  - ▼  $p_T > 1.7 \text{ GeV}$
- ◆ 708 (DIS & DY) + 32 (single  $\pi^0$ ) = 740 data points after cuts
- ◆ 16 free parameters
  - ▼ 7 gluon, 7 valence and 2 sea
- ◆  $\chi^2 = 611$ , giving  $\chi^2/\text{dof} = 0.85$
- ◆ Error analysis – use Hessian method

# Extraction of Nuclear PDFs and Nuclear Correction Factors from $\nu$ -A Scattering

- ◆ PDF Parameterized at  $Q_0 = 1.3$  GeV as

$$xf_i(x, Q_0) = \begin{cases} A_0 x^{A_1} (1-x)^{A_2} e^{A_3 x} (1+e^{A_4 x})^{A_5} & : i = u_v, d_v, g, \bar{u} + \bar{d}, s, \bar{s}, \\ A_0 x^{A_1} (1-x)^{A_2} + (1+A_3 x)(1-x)^{A_4} & : i = \bar{d}/\bar{u}, \end{cases}$$

- ◆ PDFs for a nucleus are constructed as:

$$f_i^A(x, Q) = \frac{Z}{A} f_i^{p/A}(x, Q) + \frac{(A-Z)}{A} f_i^{n/A}(x, Q)$$

- ◆ Resulting in nuclear structure functions:

$$F_i^A(x, Q) = \frac{Z}{A} F_i^{p/A}(x, Q) + \frac{(A-Z)}{A} F_i^{n/A}(x, Q)$$

- ◆ The differential cross sections for CC scattering off a nucleus::

$$\frac{d^2\sigma}{dx dy} {}^{(\bar{\nu})A} = \frac{G^2 ME}{\pi} \left[ \left(1 - y - \frac{Mxy}{2E}\right) F_2 {}^{(\bar{\nu})A} + \frac{y^2}{2} 2xF_1 {}^{(\bar{\nu})A} \pm y\left(1 - \frac{y}{2}\right) xF_3 {}^{(\bar{\nu})A} \right]$$

# Available nuclear PDF sets

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## ◆ Multiplicative nuclear correction factors

$$f_i^{p/A}(x_N, \mu_0) = R_i(x_N, \mu_0, A) f_i^{\text{free proton}}(x_N, \mu_0)$$

- ▼ Hirai, Kumano, Nagai [PRC 76, 065207 (2007), arXiv:0709.3038]
- ▼ Eskola, Paukkunen, Salgado [JHEP 04 (2009) 065, arXiv:0902.4154]
- ▼ de Florian, Sassot, Stratmann, Zurita [PRD 85, 074028 (2012), arXiv:1112.6324]

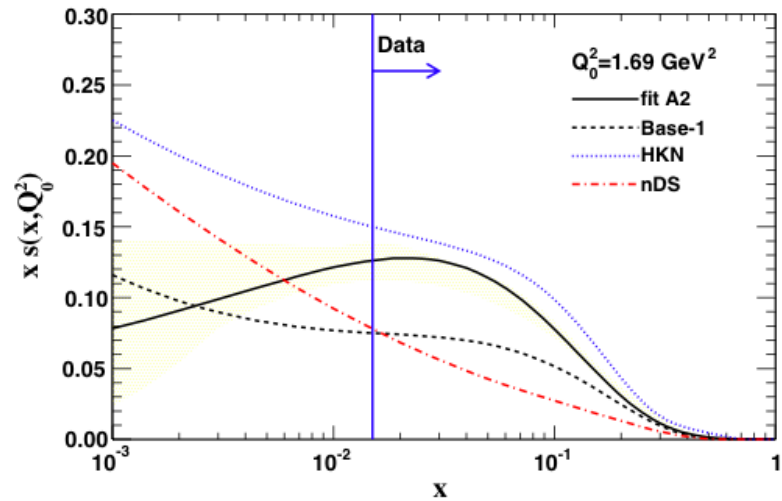
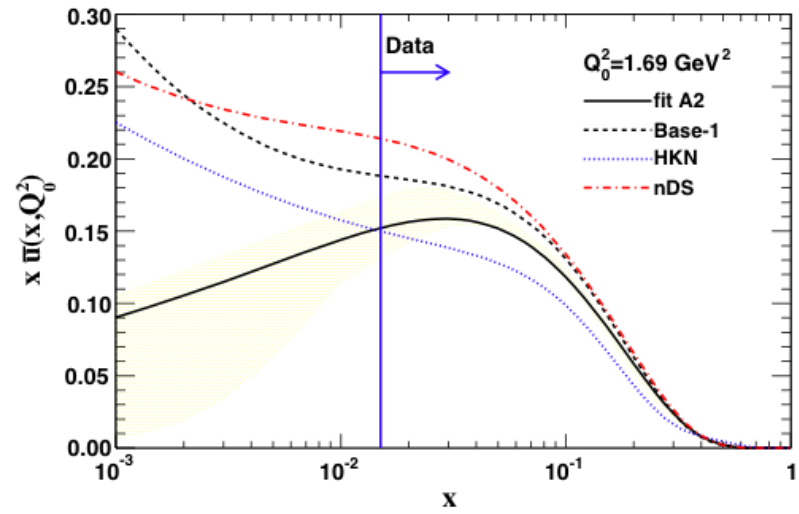
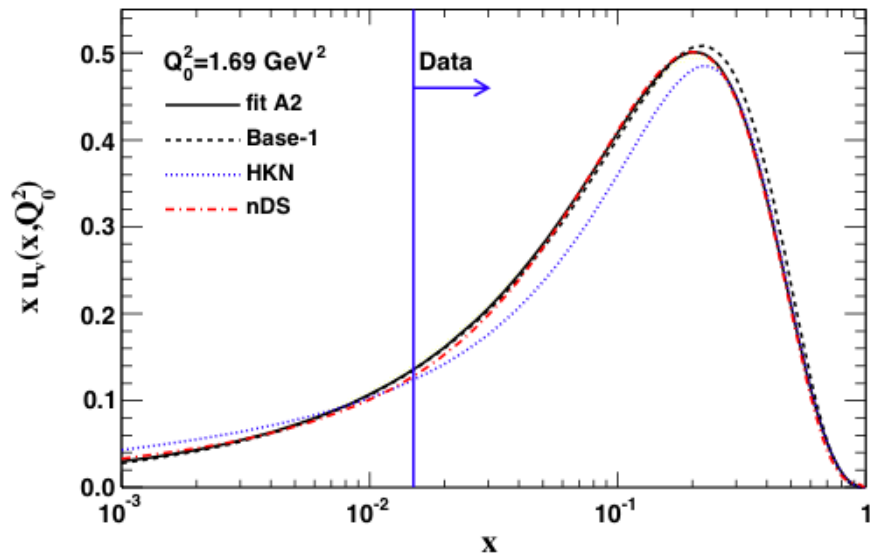
## ◆ Native nuclear PDFs

- ▼ nCTEQ [PRD 80, 094004 (2009), arXiv:0907.2357]

$$f_i^{p/A}(x_N, \mu_0) = f_i(x_N, A, \mu_0)$$

$$f_i(x_N, A = 1, \mu_0) \equiv f_i^{\text{free proton}}(x_N, \mu_0)$$

# Iron PDFs



# Kulagin-Petti Model of Nuclear Effects

hep-ph/0412425

- ◆ Global Approach -aiming to obtain quantitative calculations covering the complete range of  $x$  and  $Q^2$  available with thorough physics basis for fit to data.

- ◆ Different effects on structure functions (SF) are taken into account:

$$F_i^A = F_i^{p/A} + F_i^{n/A} + F_i^{\pi/A} + \delta F_i^{\text{coh}}$$

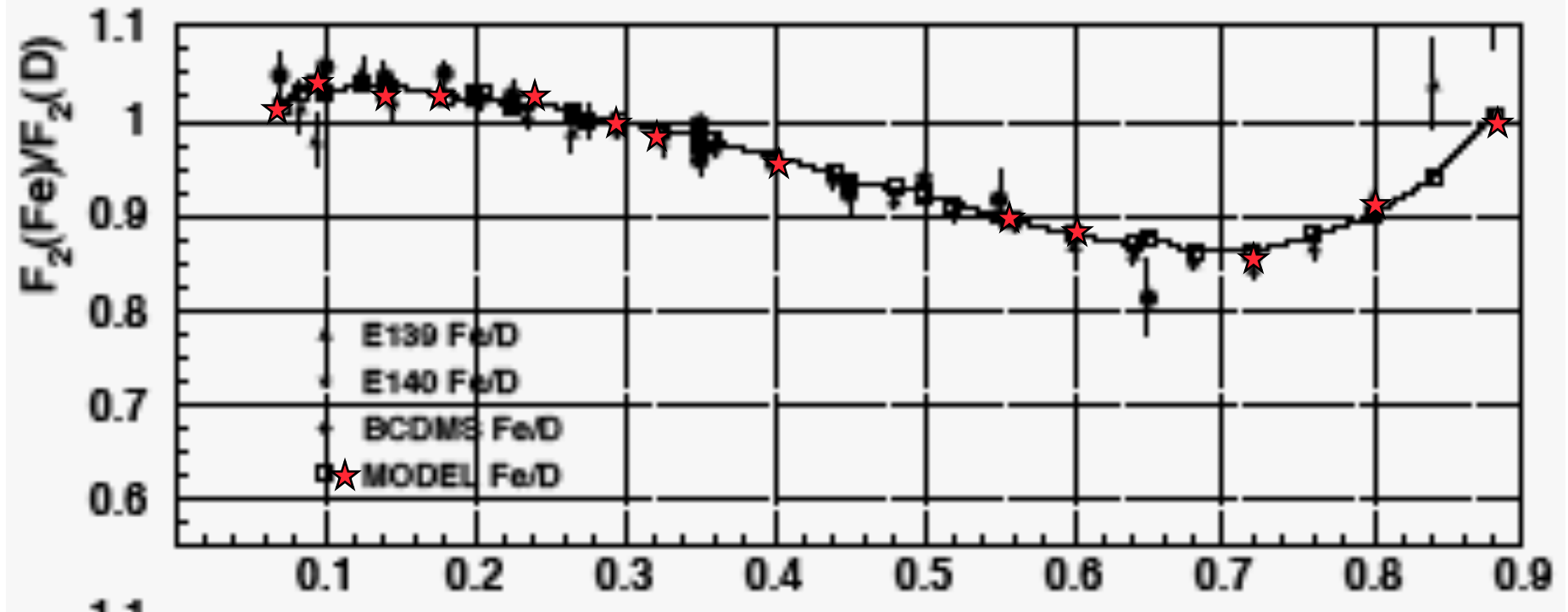
- $F_i^{p(n)/A}$  bound proton(neutron) SF with *Fermi Motion, Binding (FMB) and Off-Shell effect (OS)*
  - $F_i^{\pi/A}$  *nuclear Pion excess correction (PI)*
  - $\delta F_i^{\text{coh}}$  *contribution from coherent nuclear interactions: Nuclear Shadowing (NS)*
- ◆ **Fermi Motion** and **Binding** in nuclear structure functions is calculated from the convolution of nuclear spectral function and (bound) nucleon SFs:
  - ◆ Since bound nucleons are off-mass shell there appears dependence on the nucleon virtuality  $\kappa^2 = (M + \varepsilon)^2 - k^2$  where we have introduced an **off-shell structure function  $\delta f_2(x)$**

$$F_2(x, Q^2, k^2) = F_2(x, Q^2) \left( 1 + \delta f_2(x) (k^2 - M^2) / M^2 \right)$$

- ◆ Leptons can scatter off mesons which mediate interactions among bound nucleons yielding a **nuclear pion correction**

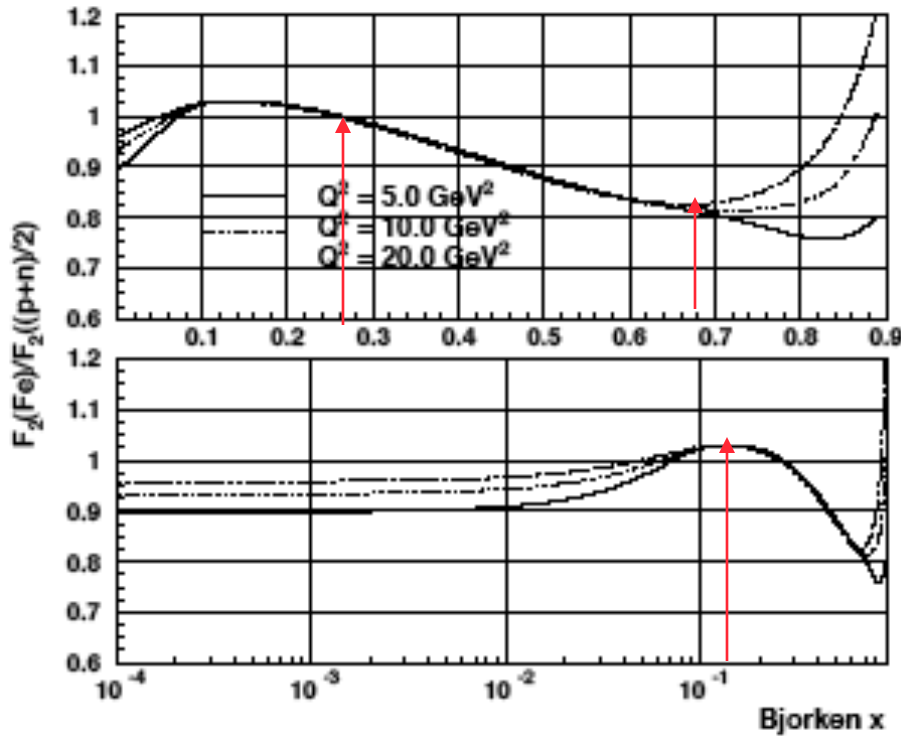
# Kulagin-Petti compared to e/ $\mu$ +Fe data

$$F_2(e/\mu+Fe) / F_2(e/\mu+D)$$

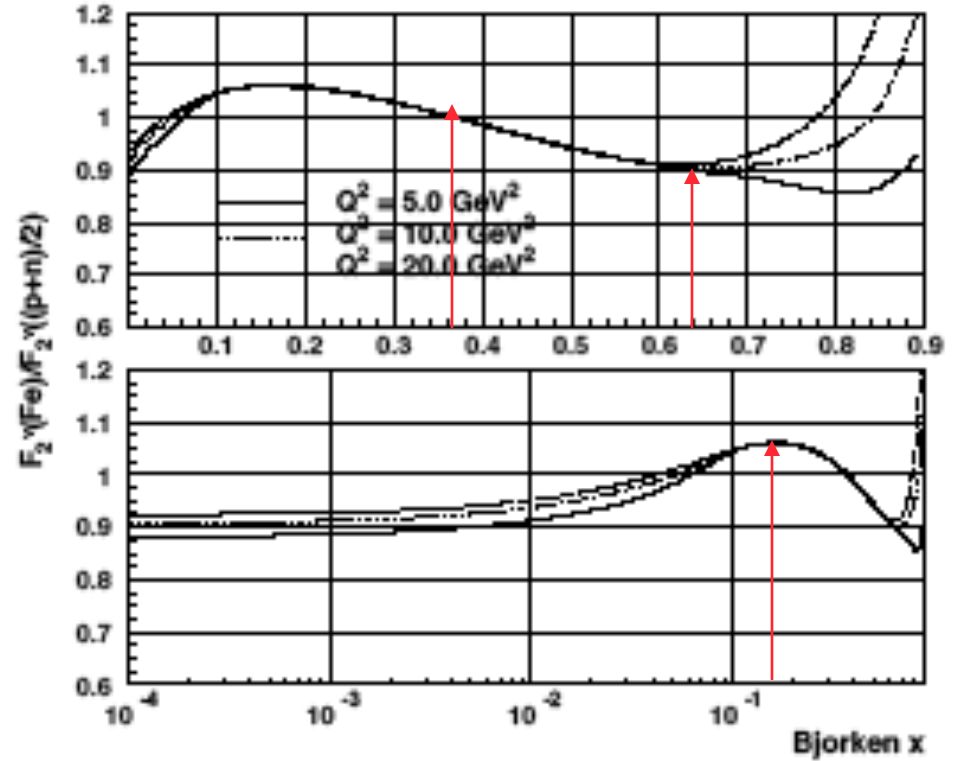


Charged Lepton

# $F_2(\mu+Fe) / F_2(\mu+N)$ compared to $F_2(\nu+Fe) / F_2(\nu+N)$



Charged Lepton

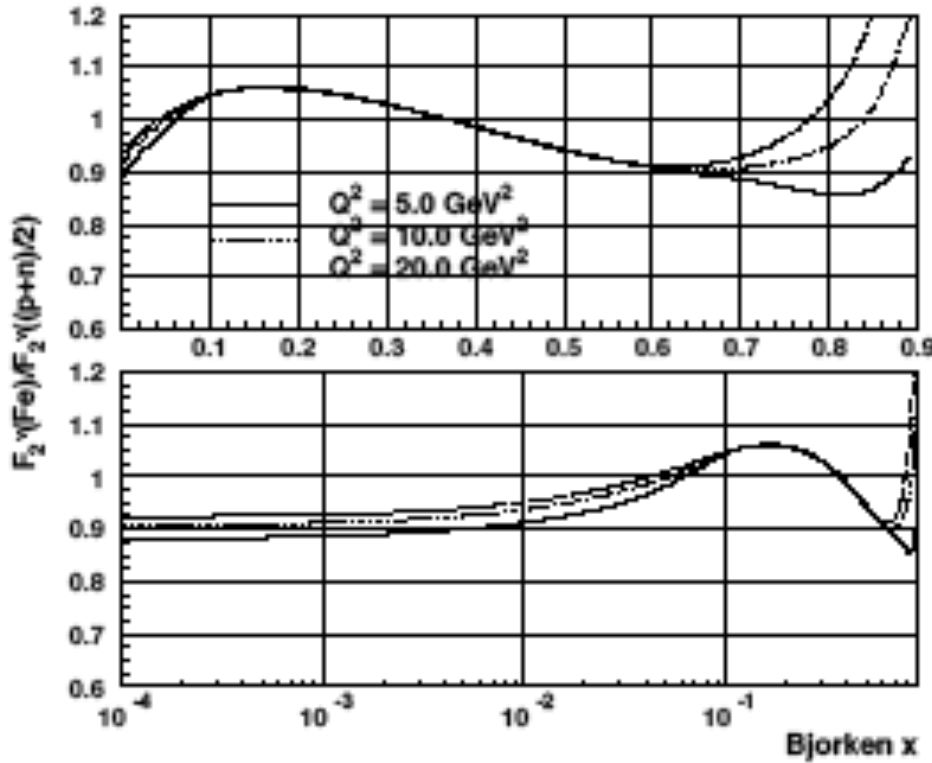


Neutrino

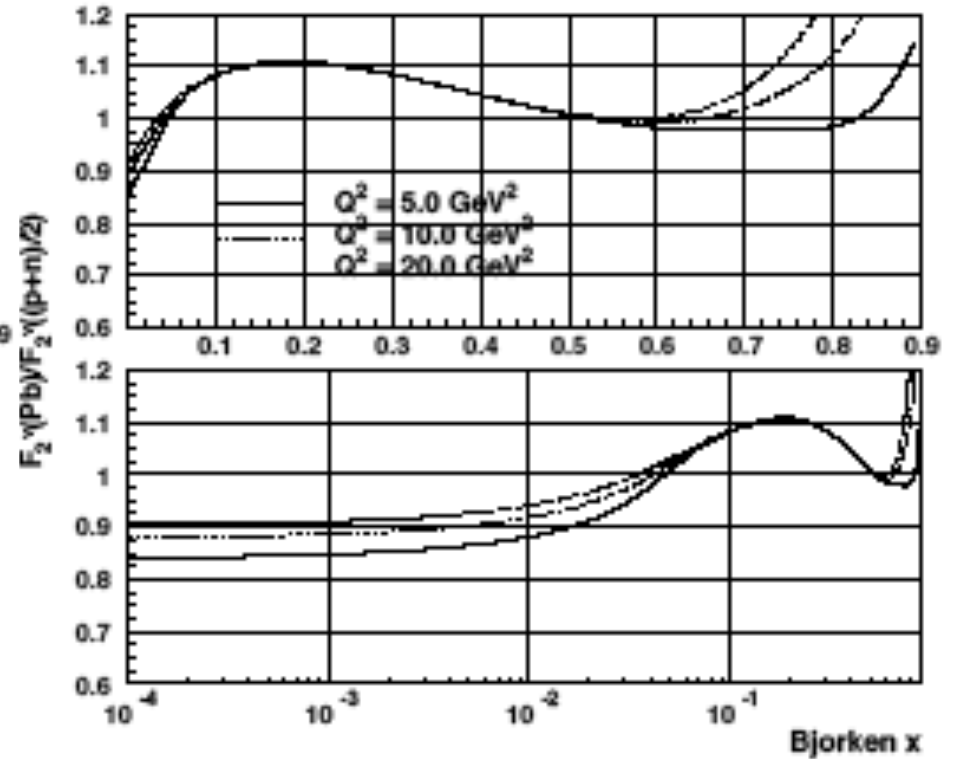


$$F_2(\nu+A) / F_2(\nu+N)$$

(n excess included in effect)

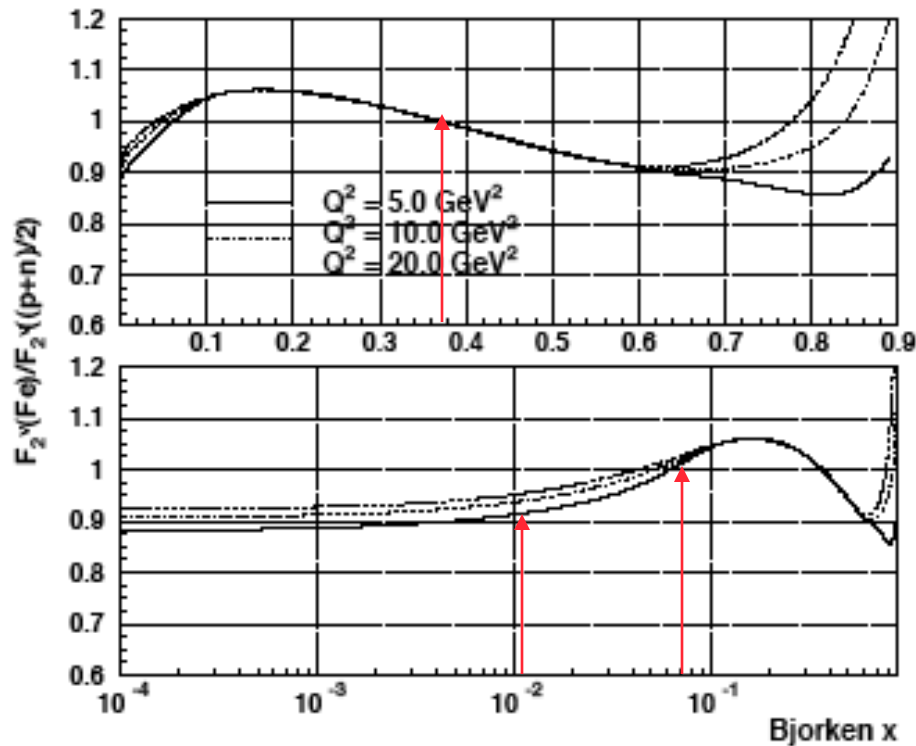


Fe

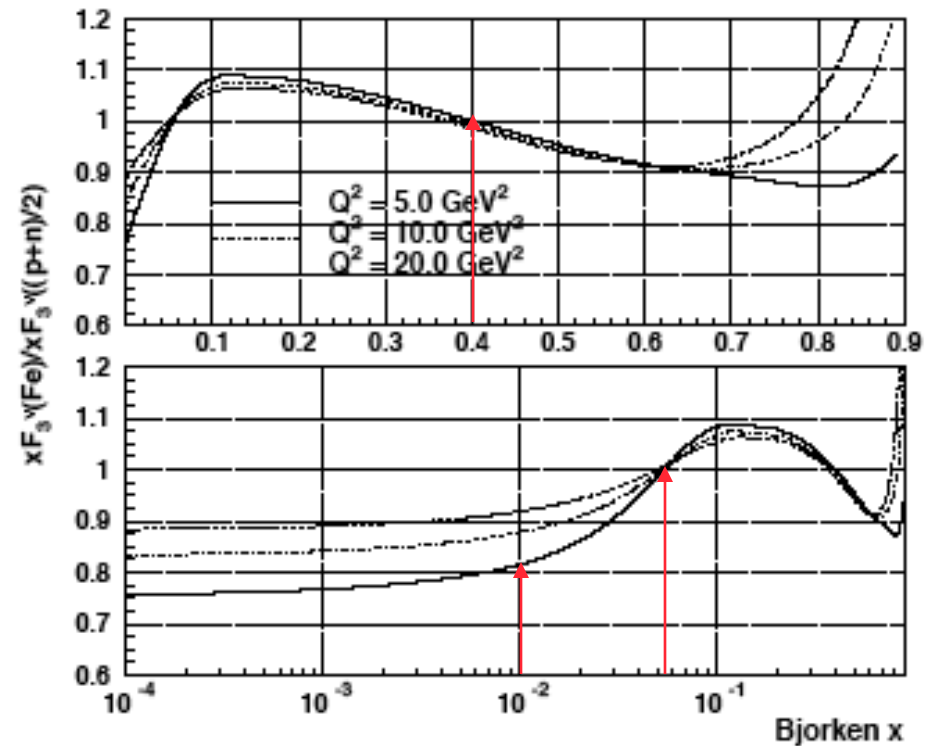


Pb

# Kulagin-Petti: $\nu$ -Fe Nuclear Effects



$F_2$

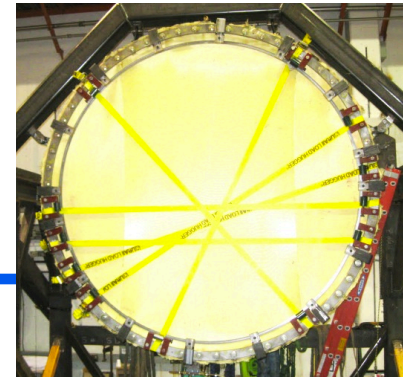


$x F_3$

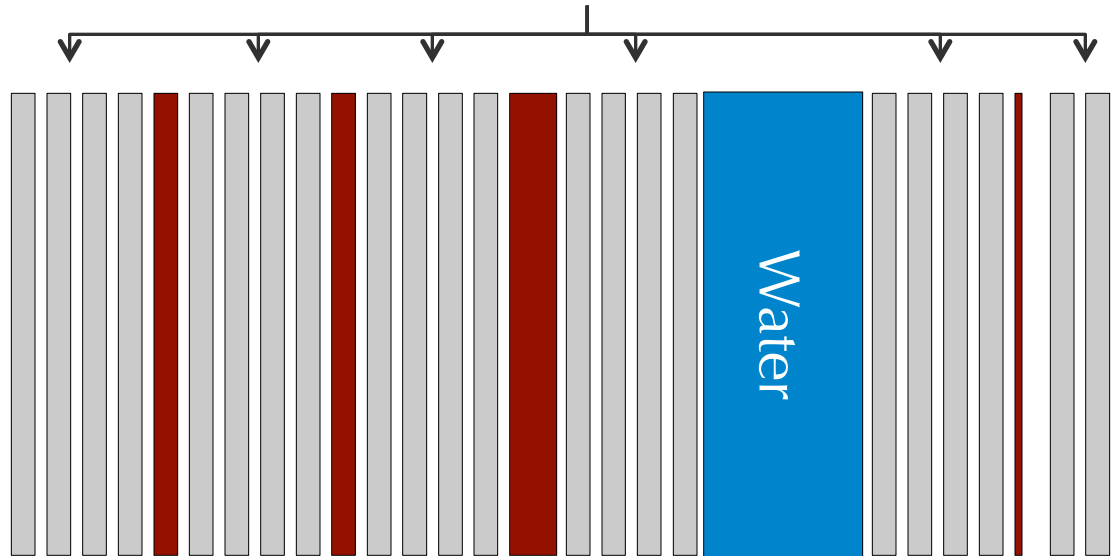
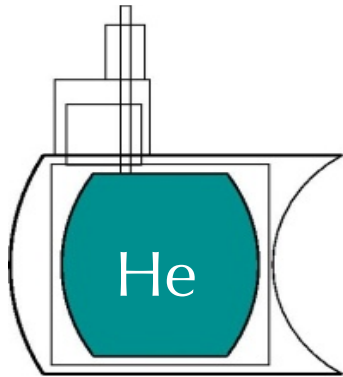


250 kg  
Liquid He

500kg  
Water



### Active scintillator modules



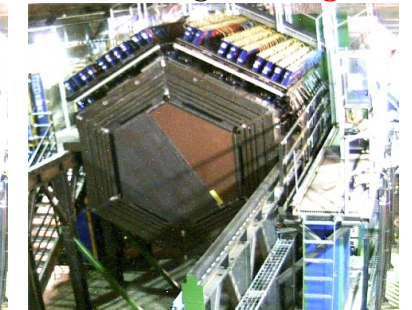
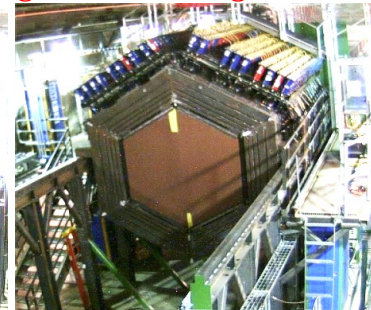
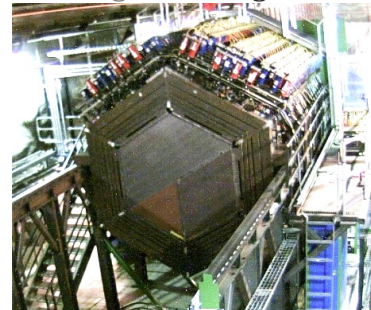
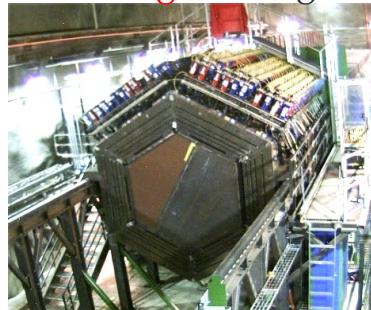
1" Fe / 1" Pb  
323kg / 264kg

1" Pb / 1" Fe  
266kg / 323kg

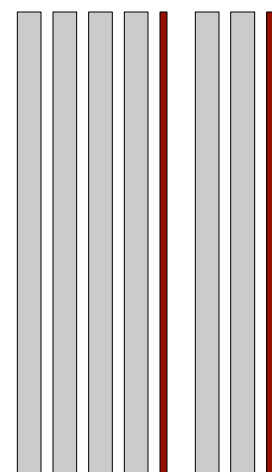
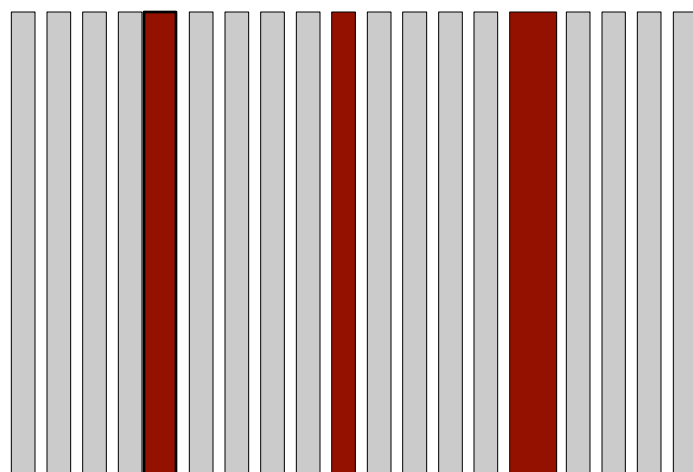
3" C / 1" Fe / 1" Pb  
166kg / 169kg / 121kg

0.3" Pb  
228kg

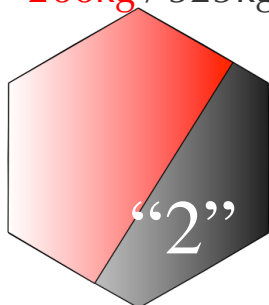
.5" Fe / .5" Pb  
161kg / 135kg



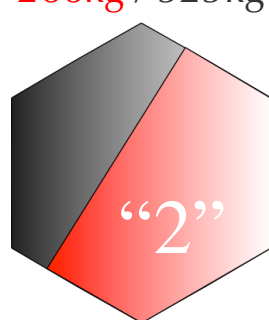
# Targets used for these results



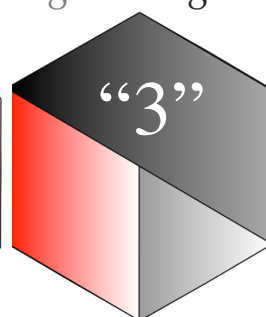
1" Pb / 1" Fe  
266kg / 323kg



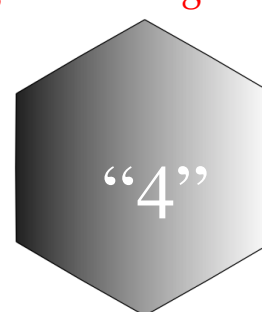
1" Pb / 1" Fe  
266kg / 323kg



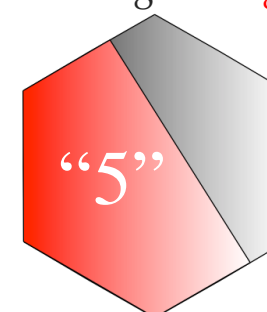
3" C / 1" Fe / 1" Pb  
166kg / 169kg / 121kg



0.3" Pb  
228kg

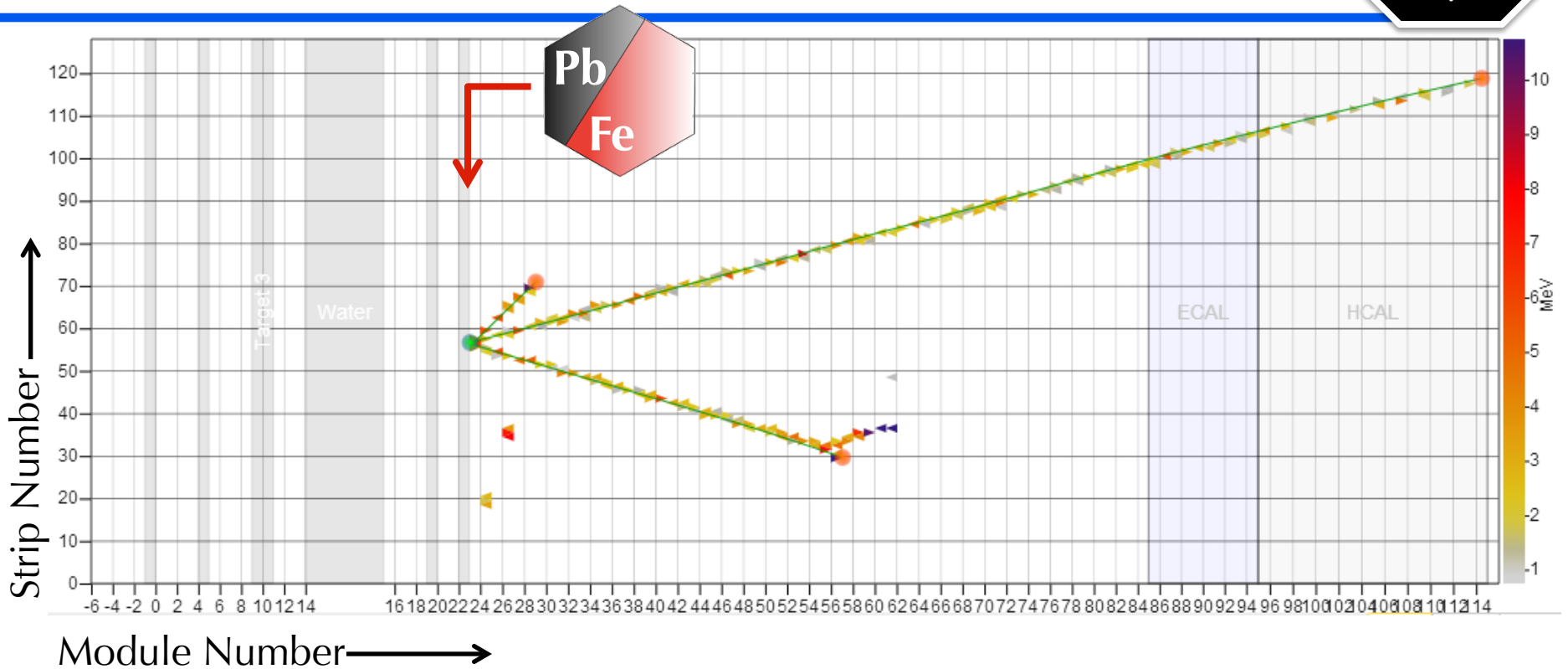


.5" Fe / .5" Pb  
161kg / 135kg



# Event selection (1)

Thanks  
MINOS  
!



## Event topology

Muon must be matched to a muon in MINOS

## Resulting kinematic region

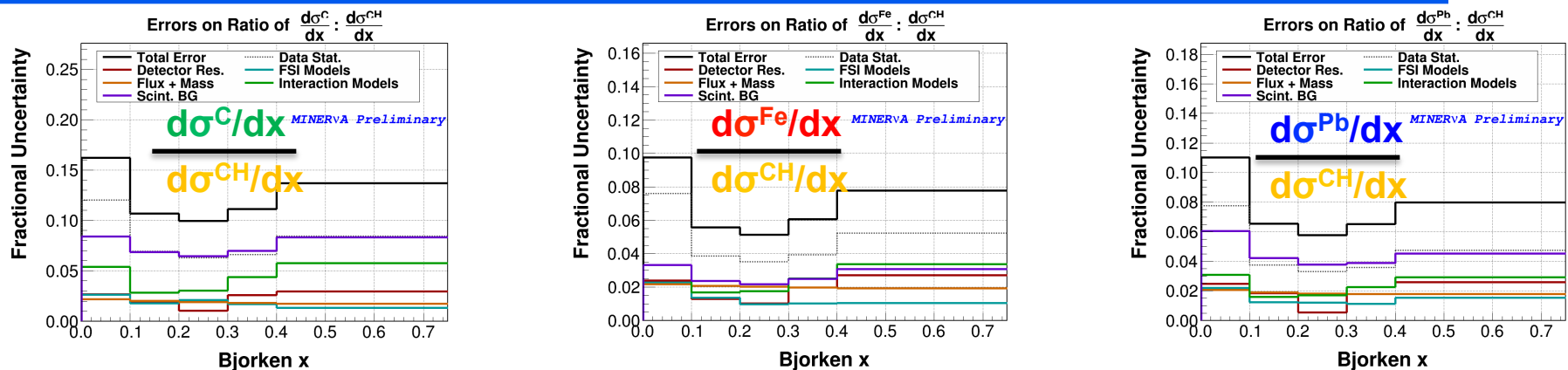
$2 < \text{Neutrino Energy} < 20 \text{ GeV}$

$0 < \text{Muon Angle} < 17^\circ$

## Nuclear target sample

Vertex must be in passive target or an adjacent downstream scintillator plane

# Cross Section Ratios Uncertainties ( $x_{Bj}$ )



Taking ratios removes large uncertainties due to the neutrino flux

Uncertainties similar across different targets, all targets in same beam

→ flux largely cancels

→ similar acceptance and reconstruction

(however efficiency correction introduces cross section model uncertainties)

Most of the uncertainty stems from data statistics

(higher intensity, higher energy ME beam will improve this substantially)

“Plastic” background subtraction introduces a larger uncertainty in  $x$  (not in  $E_\nu$ )

# Fit Details

- ◆ Fit @NLO with  $Q_0 = 1.3 \text{ GeV}$

- ◆ Using ACOT heavy quark

- ◆ Kinematic cuts:

  - ▼  $Q > 2 \text{ GeV}$ ,  $W > 3.5 \text{ GeV}$

  - ▼  $p_T > 1.7 \text{ GeV}$

## Kinematic cuts

nCTEQ:

$$\begin{cases} Q > 2 \text{ GeV} \\ W > 3.5 \text{ GeV} \end{cases}$$

EPS:  $Q > 1.3 \text{ GeV}$

HKN:  $Q > 1 \text{ GeV}$

DSSZ:  $Q > 1 \text{ GeV}$

- ◆ 708 (DIS & DY) + 32 (single  $\pi^0$ ) = 740 data points after cuts

- ◆ 16 free parameters

  - ▼ 7 gluon, 7 valence and 2 sea

- ◆  $\chi^2 = 611$ , giving  $\chi^2/\text{dof} = 0.85$

- ◆ Error analysis – use Hessian method

# Fit Details

◆ Fit @NLO with  $Q_0 = 1.3\text{GeV}$

◆ Using ACOT heavy quark

◆ Kinematic cuts:

▼  $Q > 2\text{ GeV}$ ,  $W > 3.5\text{ GeV}$

▼  $p_T > 1.7\text{ GeV}$

Kinematic cuts

<u>nCTEQ</u> :	<u>EPS</u> : $Q > 1.3\text{ GeV}$
$\begin{cases} Q > 2\text{ GeV} \\ W > 3.5\text{ GeV} \end{cases}$	<u>HKN</u> : $Q > 1\text{ GeV}$
	<u>DSSZ</u> : $Q > 1\text{ GeV}$

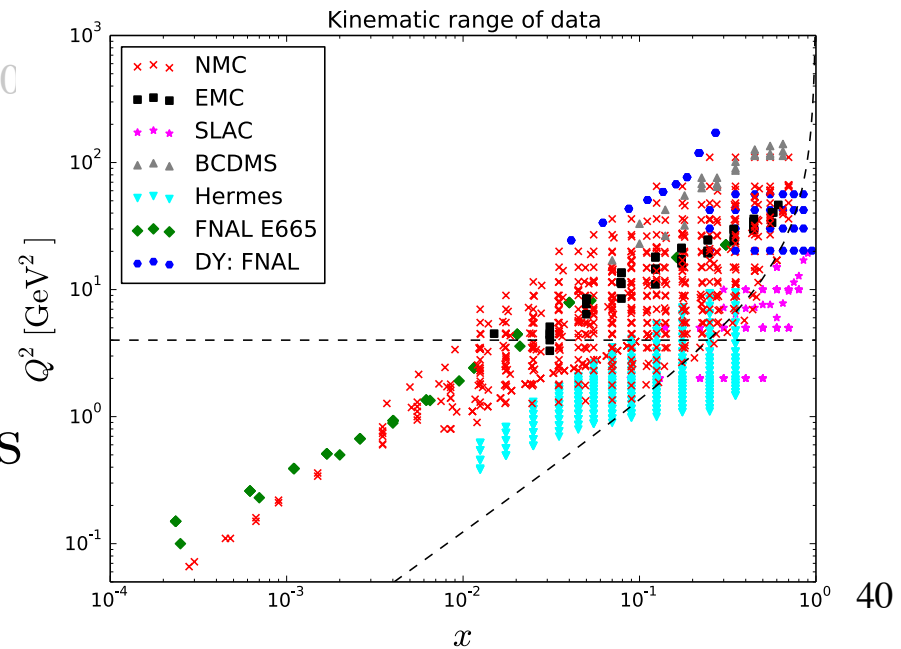
◆ 708 (DIS & DY) + 32 (single  $\pi^0$ )

◆ 16 free parameters

▼ 7 gluon, 7 valence and 2 sea

◆ **nCTEQ: 740 data points**

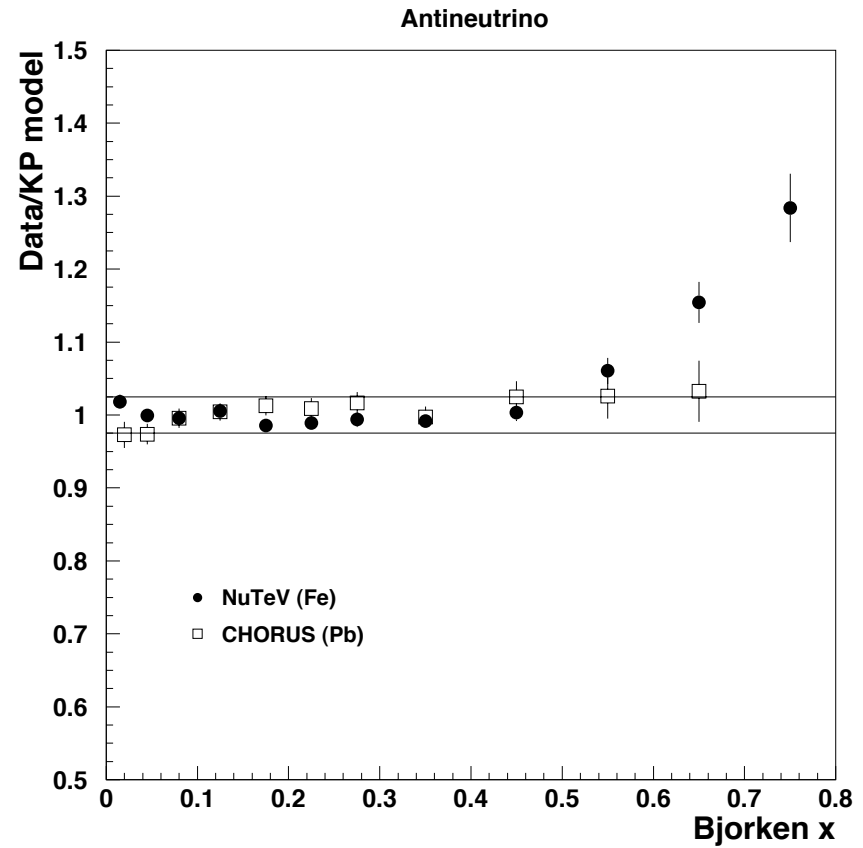
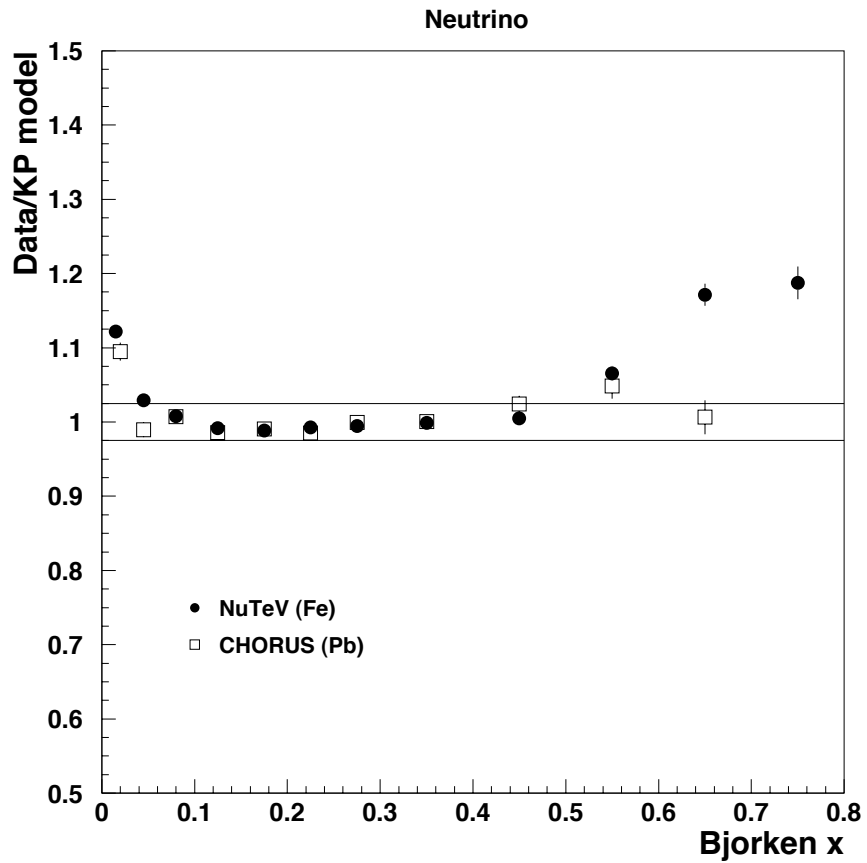
◆ **EPS09: 929 data points**





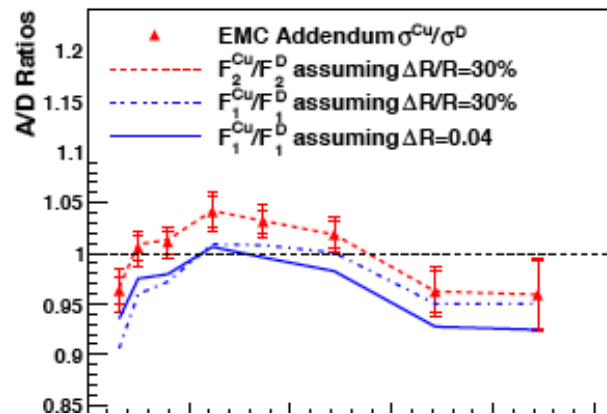
# Comparison of Data to the Kulagin-Petti Model

thanks to Roberto Petti



## If Difference between both $I^{\pm}$ -A and $\nu$ -A persists?

- ◆ In neutrino scattering, low- $Q^2$  is dominated by the (PCAC) part of the axial-vector contribution of the longitudinal structure function  $F_L$ .
- ◆ Shadowing is led by  $F_T$  and the shadowing of  $F_L$  lags at lower  $x$ .



V. Guzey et al. arXiv 1207.0131

- ▼  $F_1$  (Blue) is purely transverse and  $F_2$  (Red) is a sum of  $F_T$  ( $F_1$ ) and  $F_L$
- ▼ This could be a contributing factor to such a difference.
- ◆ Another idea also from Guzey and colleagues is the observation that

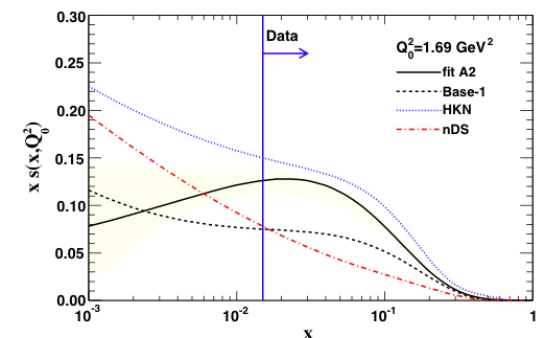
# If Difference between both $l^\pm$ -A and $\nu$ -A persists?

- ◆ Another idea also from Guzey and colleagues is the observation that (in leading order):

$$\frac{d\sigma^{\nu A}}{dx dy} = \frac{G_F^2 M_W^4}{(Q^2 + M_W^2)^2} \frac{ME}{\pi} 2x [d^A + s^A + (1-y)^2(\bar{u}^A + \bar{c}^A)]$$

$$\frac{d\sigma^{\bar{\nu} A}}{dx dy} = \frac{G_F^2 M_W^4}{(Q^2 + M_W^2)^2} \frac{ME}{\pi} 2x [d^{\bar{A}} + s^{\bar{A}} + (1-y)^2(u^A + c^A)]$$

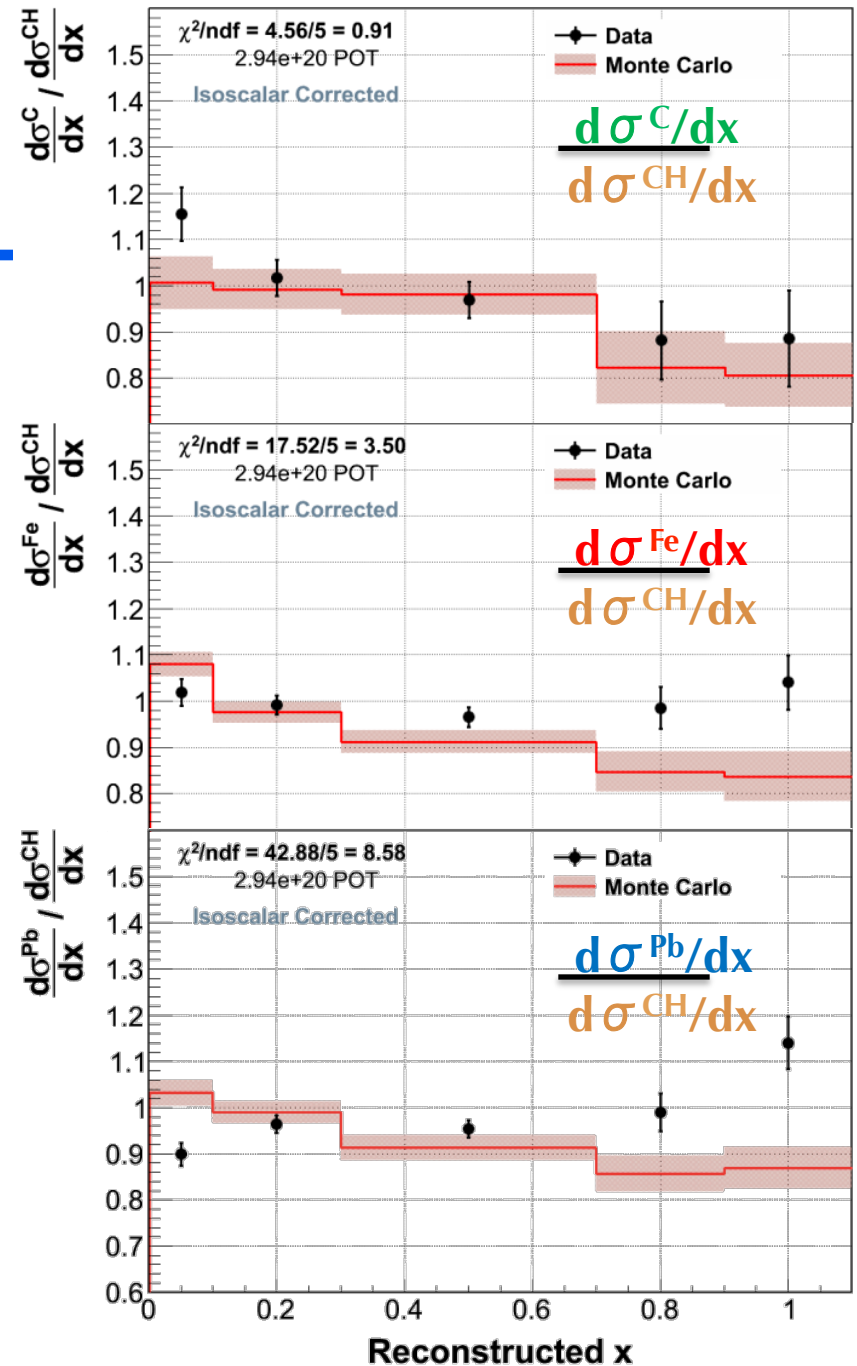
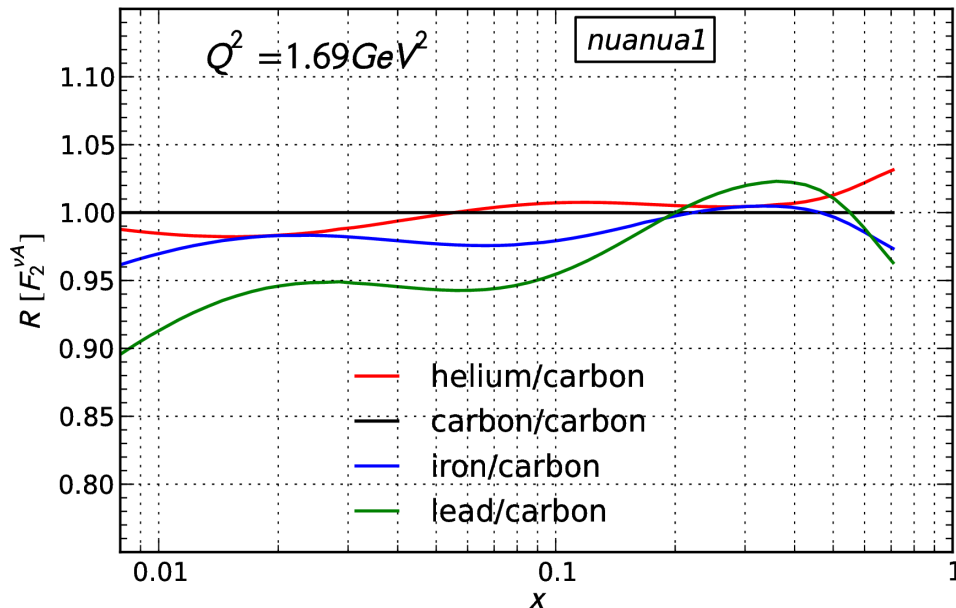
- ▼ In the shadowing region at low- $x$ ,  $y$  is large and the  $\sigma$  are primarily probing the d- and s-quarks.
- ◆ This is very different from  $l^\pm$  scattering where the d- and s-quarks are reduced by a factor of 4 compared to the u- and c-quarks.
  - ▼ If shadowing of the d- or s-quarks is negligible this would explain the NuTeV result.
  - ▼ Diminished shadowing of the nuclear s-quark is suggested by early extraction of nPDFs by nCTEQ.



# High x summary

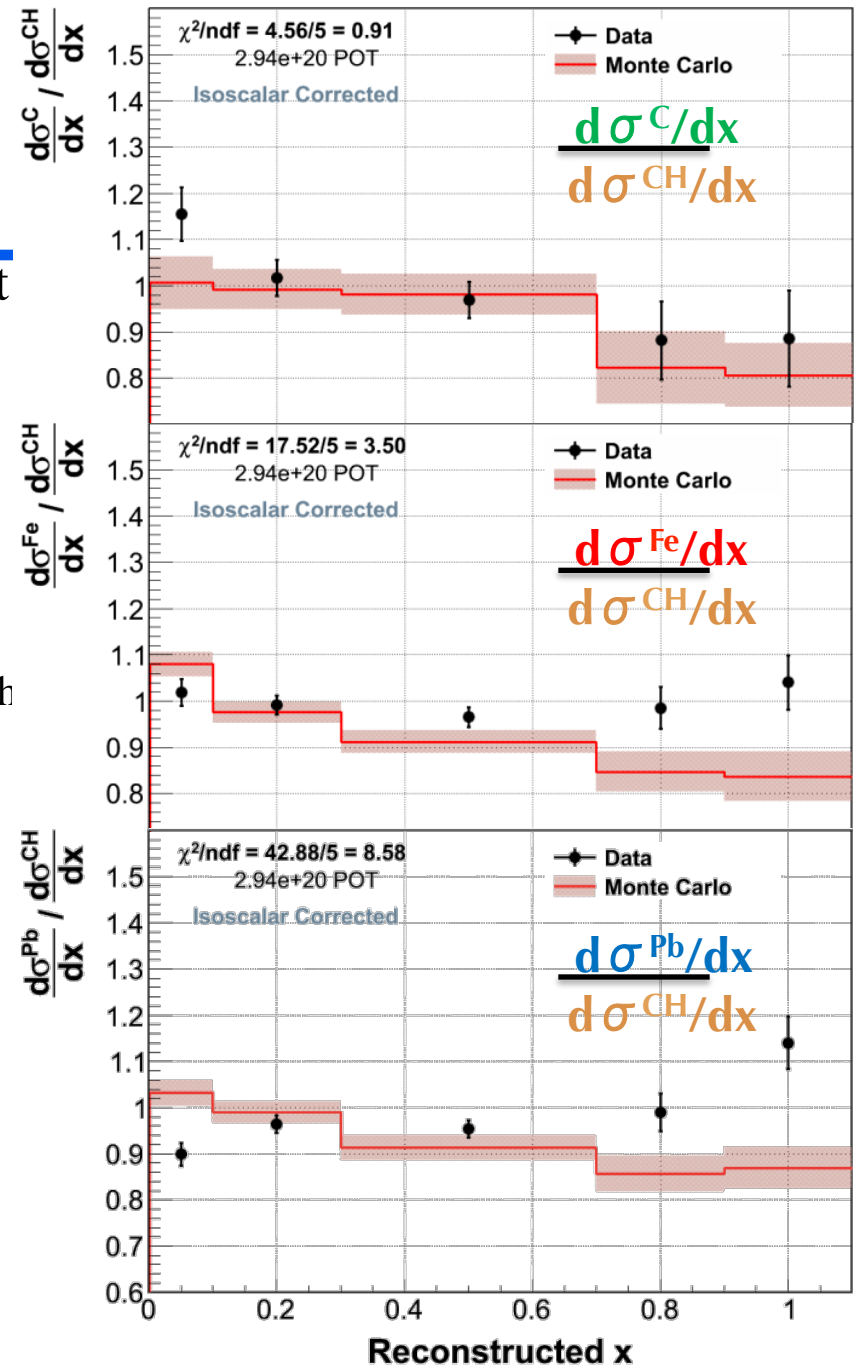
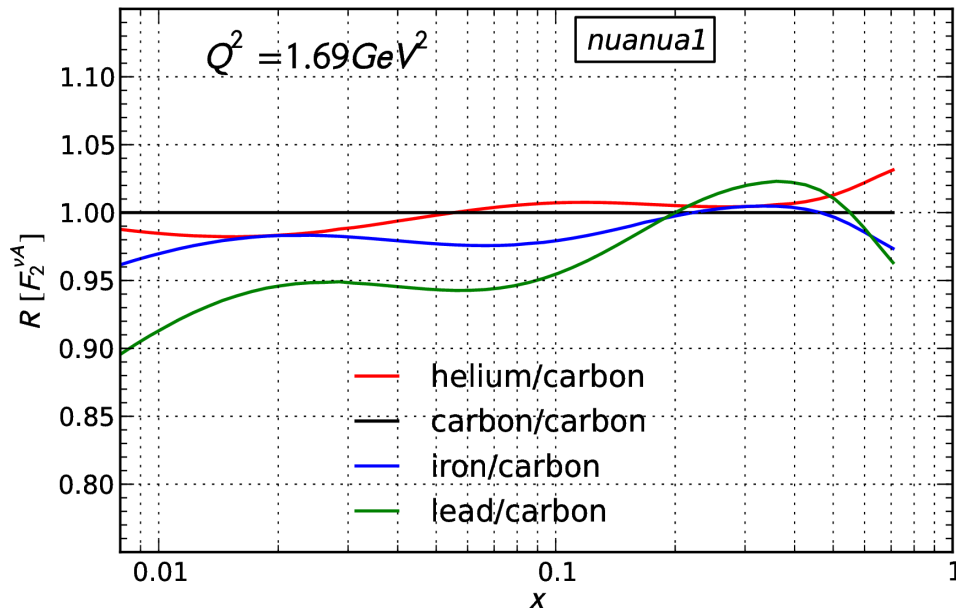
## INCLUSIVE RATIOS

- ◆ At  $x = [0.7, 1.1]$ , we observe an **excess** that grows with the size of the nucleus
- ◆ This effect is not modeled in simulation



# Low x summary INCLUSIVE RATIOS

- ◆ At  $x = [0.0, 0.1]$ , we observe a **deficit** that increases with the size of the nucleus
- ◆ This effect is not modeled in simulation
- ◆ Expected Neutrino Differences
  - ▼ Neutrino sensitive to  $x F_3$
  - ▼ Axial-vector current different coherence length

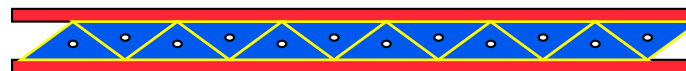
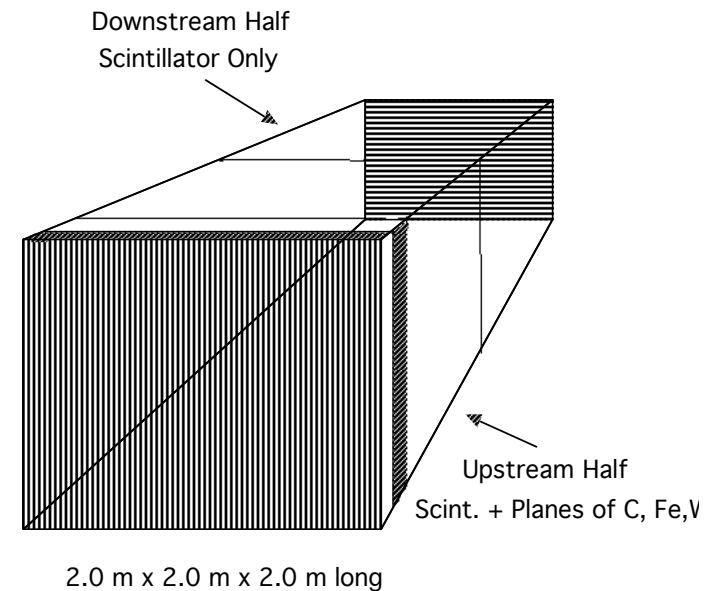


# Before MINERvA there was MIDIS and a High-energy Configuration of NuMI

## MIDIS: Central Detector, Conceptual Design

ANL: John Arrington, Roy Holt, Dave Potterveld and Paul Reimer - FNAL: JGM  
Fermilab Bright Booster Study - Spring 2001

- ◆ 2m x 2 cm x 2cm scintillator (CH) strips with fiber readout.
- ◆ **Fiducial volume:**  $r = .8\text{m}$   $L = 1.5$ :  
**3 tons of scintillator**
- ◆ Downstream half: pure scintillator
- ◆ Upstream half: scintillator plus 2 cm thick planes of C, Fe and W.
  - ▼ 11 planes C = 1.0 ton (+Scintillator)
  - ▼ 3 planes Fe = 1.0 ton (+MINOS)
  - ▼ 2 planes Pb = 1.0 ton
- ◆ Readout: mainly VLPC, perhaps also multi-anode PMT for TOF.
- ◆ Use MINOS near detector as muon identifier / spectrometer.



Triangles: 1 cm base and transverse segmentation.  
Yields about 1 mm position resolution for mips

From D0 pre-shower test data

## Shadowing - continued

---

- ◆ Why low  $x$ ?
- ◆ The lifetime of the hadronic fluctuation has to be sufficient to allow for these multiple diffractive scatters:

$$t_c \approx 2E_{\text{had}} / (Q^2 + m^2)$$

- ◆ For a given  $Q^2$  need large  $E_{\text{had}}$  to yield sufficient  $t_c$  which implies small  $x$ .
- ◆  $m$  is larger for the vector current than the axial vector current  $\rightarrow$  for a given  $Q^2$  you need more  $E_{\text{had}}$  for the vector current than the axial vector current to have sufficient  $t_c$ .
- ◆ This implies you can have shadowing at higher  $x$  with neutrinos than with charged leptons

# Conclusions

---

MINER $\nu$ A performs a systematic study of nuclear medium modifications of hadronic structure using different nuclear targets in the same detector exposed to the same neutrino beam

**First measurement of ratios of neutrino cross sections on nuclei in the DIS regime**

**Observe no significant  $E_\nu$  dependences compared to theory**

These measurements may be interpreted directly as  $x$  dependent nuclear effects  
(GENIE assumes an  $x$  dependent effect from charged lepton scattering on nuclei)

- \*\* In the EMC region ( $0.3 < x < 0.7$ ) good agreement between data and models within errors**
- \*\* In the lowest  $x$  bin ( $x < 0.1$ ) MINER $\nu$ A data suggests nuclear shadowing at an  $\langle x \rangle$  (0.07) &  $\langle Q^2 \rangle$  (2 GeV<sup>2</sup>) where negligible shadowing is expected with  $l^\pm$ .**

Data taking with a “Medium Energy”  $\nu$  beam started in fall 2013

$E_\nu$  peak  $\sim 6$  GeV, already more POT ( $6 \times 10^{20}$ ) than LE data taking

The higher neutrino beam energy allow us to access the DIS region and study quark distributions over a broad  $x_{Bj}$  range

Increased statistics gives nuclear target ratios for all interactions

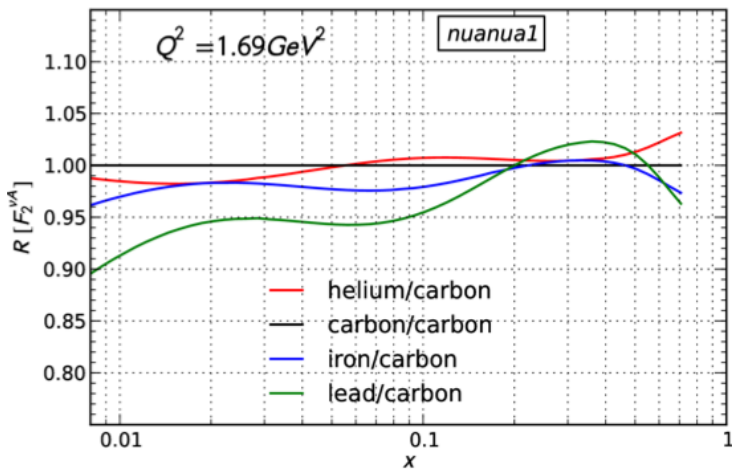
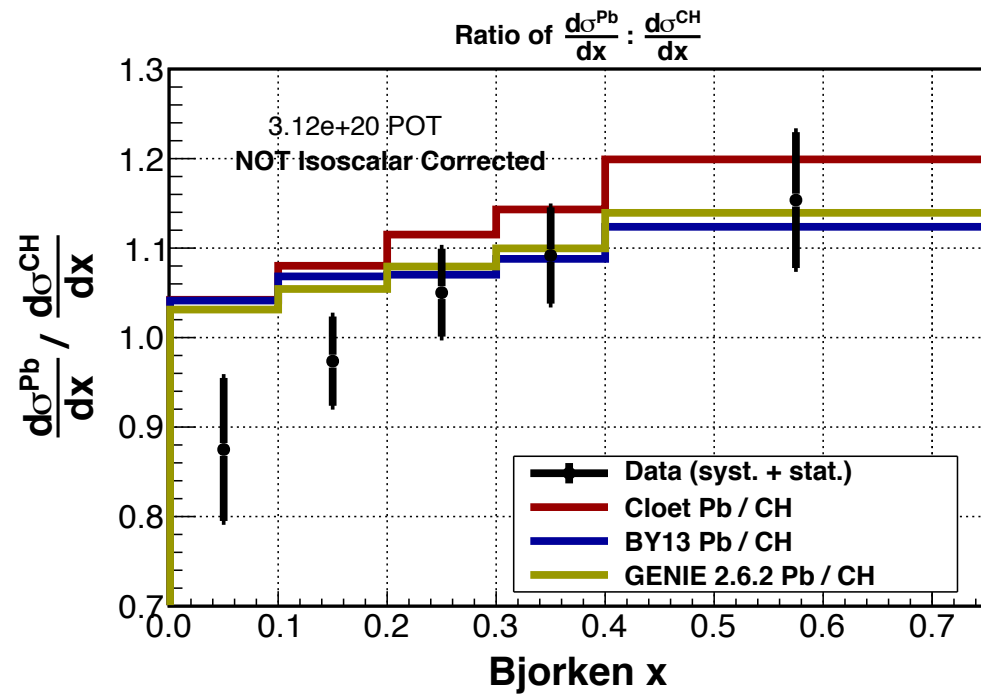
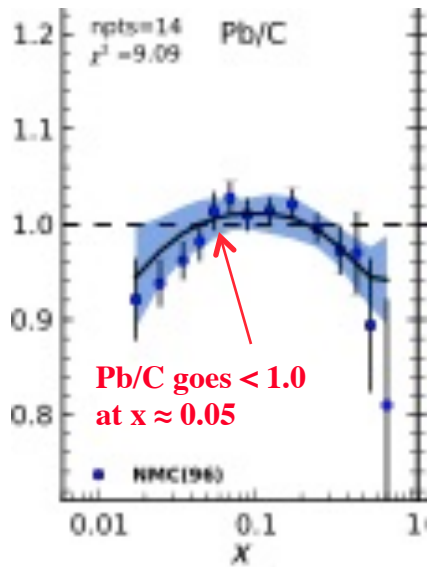


## Others Do NOT Find this Difference between $l^\pm$ and $\nu$

---

- ◆ The analyses of K. Eskola et al. and D. de Florian et al. do not find this difference between  $l^\pm$ -A and  $\nu$ -A scattering.
- ◆ They do not use the full covariant error matrix rather adding statistical and systematic errors in quadrature.
- ◆ They do not use the full double differential cross section rather they use the extracted structure functions which involve assumptions:
  - ▼ Assume a value for  $\Delta x F_3$  ( $= F_3^{\nu} - F_3^{l^\pm}$ ) from theory.
  - ▼ Assume a value for  $R = F_L / F_T$ .
- ◆ If nCTEQ makes these same assumptions, than a combined solution of  $l^\pm$ -A and  $\nu$ -A scattering can be found.
- ◆ **What's next?**

# Charged lepton $F_2$ Pb/C ratio & nCTEQ Prediction



# nCTEQ Framework

[PRD 80, 094004 (2009), arXiv:0907.2357]

---

- ◆ Functional form of the bound proton PDF same as for the free proton ( $\sim$ CTEQ6.1 [hep-ph/0702159],  $x$  restricted to  $0 < x < 1$ )

$$x f_i^{p/A}(x, Q_0) = x^{c_1} (1-x)^{c_2} e^{c_3 x} (1 + e^{c_4 x})^{c_5}, \quad i = u_v, d_v, g, \dots$$
$$\bar{d}(x, Q_0)/\bar{u}(x, Q_0) = x^{c_1} (1-x)^{c_2} + (1 + c_3 x)(1-x)^{c_4}$$

- ◆ A-dependent fit parameters (reduces to free proton for  $A = 1$ )

$$c_k \rightarrow c_k(A) \equiv c_{k,0} + c_{k,1} (1 - A^{-c_{k,2}}), \quad k = \{1, \dots, 5\}$$

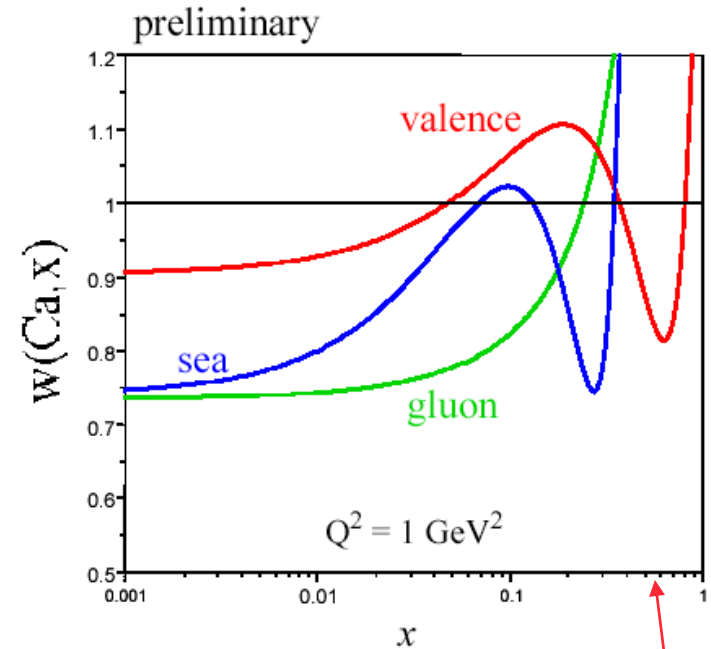
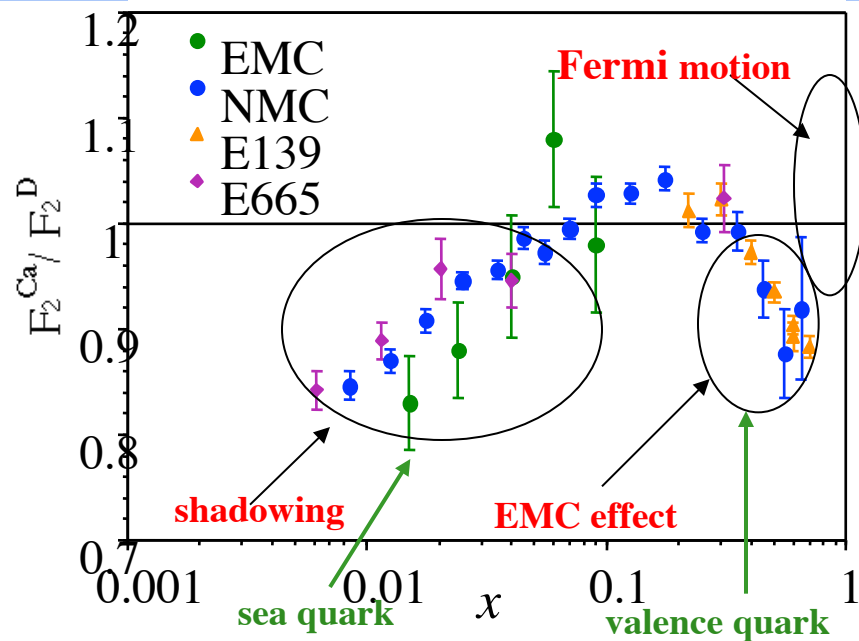
- ◆ PDFs for nucleus ( $A, Z$ )

$$f_i^{(A,Z)}(x, Q) = \frac{Z}{A} f_i^{p/A}(x, Q) + \frac{A-Z}{A} f_i^{n/A}(x, Q)$$

- ▼ Bound neutron PDFs  $f_i^{n/A}$  by isospin symmetry

## Now for Neutrinos

Experimental Studies of (Parton-level) Nuclear Effects with Neutrinos:  
limited to early Bubble Chamber studies and, now, MINERvA



- ◆  $F_2$  / nucleon changes as a function of A. Measured in  $\mu/e - A$  **not yet in  $\nu - A$**
- ◆ **Good reason to consider nuclear effects are DIFFERENT in  $\nu - A$ .**
  - ▼ Presence of axial-vector current.
  - ▼ Different nuclear effects for valence and sea --> different shadowing for  $x F_3$  compared to  $F_2$ .
  - ▼ All flavor dependent nuclear effects will be different for  $\nu - A$ .

# charged lepton $F_2$ ratios: continued

