

Exotic Compact Objects

(Frontiers in Particle Physics 2024, CHEP, IISc. Bangalore)

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- Unusual astrophysical objects

Dark stars powered by self-interacting dark matter

Youjia Wu, Sebastian Baum, Katherine Freese, Luca Visinelli, and Hai-Bo Yu
 Phys. Rev. D **106**, 043028 – Published 29 August 2022



Physics Reports

Volume 1052, 12 February 2024, Pages 1-48



Supermassive Dark Star candidates seen by JWST

Cosmin Ilie , Jillian Paulin , and Katherine Freese [Authors Info & Affiliations](#)

Contributed by Katherine Freese; received April 10, 2023; accepted June 2, 2023; reviewed by Marc P. Kamionkowski and Laura Baudis

This contribution is part of the special series of Inaugural Articles by members of the National Academy of Sciences elected in 2020.

July 11, 2023 | 120 (30) e2305762120 | <https://doi.org/10.1073/pnas.2305762120>

- Topological solitonic objects

Q-monopole-ball: a topological and nontopological soliton

Yang Bai,^a Sida Lu^b and Nicholas Orlofsky^c

Comments on magnetic black holes

Juan Maldacena

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- Non-topological solitonic objects

Solitonic boson stars: Numerical solutions beyond the thin-wall approximation

Lucas G. Collodel and Daniela D. Doneva
 Phys. Rev. D **106**, 084057 – Published 28 October 2022

Tidal Love numbers and approximate universal relations for fermion soliton stars

Emanuele Berti, Valerio De Luca, Loris Del Grosso, and Paolo Pani
 Phys. Rev. D **109**, 124008 – Published 4 June 2024

Living Reviews in Relativity (2019) 22:4
<https://doi.org/10.1007/s41114-019-0020-4>

REVIEW ARTICLE

Testing the nature of dark compact objects: a status report

Vitor Cardoso^{1,2} · Paolo Pani³



Characteristic sizes and masses of Boson stars

$$mv \sim \frac{1}{2R} \Rightarrow K \sim \frac{1}{8mR^2}$$

$$V_{total} \sim -\frac{3G_N M^2}{5R}$$

$$N \sim M/m$$

$$E_{total} = K_{total} + V_{total} \sim \frac{N}{8mR^2} - \frac{3G_N M^2}{5R}$$

$$\frac{\partial E_{total}}{\partial R} = 0 \rightarrow \boxed{R_* \sim \frac{5}{12G_N m^2 M}}$$

$$2M < R_*$$

$$M_{max.} \sim \sqrt{\frac{5}{24}} \frac{1}{G_N m}$$

(Kaup mass limit)



[Dall-E]

How different?

$$ds^2 = -e^{2\alpha(r)} dt^2 + e^{2\beta(r)} dr^2 + r^2 d\Omega^2.$$



$$T_{\mu\nu} = (\rho + p)U_\mu U_\nu + p g_{\mu\nu}. \quad T_{\mu\nu} = \begin{pmatrix} e^{2\alpha}\rho & & & \\ & e^{2\beta}p & & \\ & & r^2 p & \\ & & & r^2(\sin^2\theta)p \end{pmatrix}.$$

$$\frac{dp}{dr} = -\frac{(\rho + p)[Gm(r) + 4\pi Gr^3 p]}{r[r - 2Gm(r)]}.$$

(Tolman-Oppenheimer-Volkoff equation)

$$T_{\phi}^{\mu\nu} = \frac{2}{\sqrt{-g}} \frac{\partial(\sqrt{-g} \mathcal{L}_{\phi})}{\partial g_{\mu\nu}} \longrightarrow T_{\mu\nu} = \nabla_{\mu}\phi^{*}\nabla_{\nu}\phi + \nabla_{\mu}\phi\nabla_{\nu}\phi^{*} - g_{\mu\nu} (g^{\alpha\beta}\nabla_{\alpha}\phi^{*}\nabla_{\beta}\phi + V(\phi^{*}\phi))$$

↓

$$p_r^{\phi} \neq p_T^{\phi}$$

$$\frac{1}{\sqrt{-g}} \partial_{\mu} (\sqrt{-g} g^{\mu\nu} \partial_{\nu} \phi) - m^2 \phi = -\frac{dV}{d\phi}.$$

$$R_{\mu\nu} - \frac{1}{2} g_{\mu\nu} R = 8\pi G T_{\mu\nu}.$$

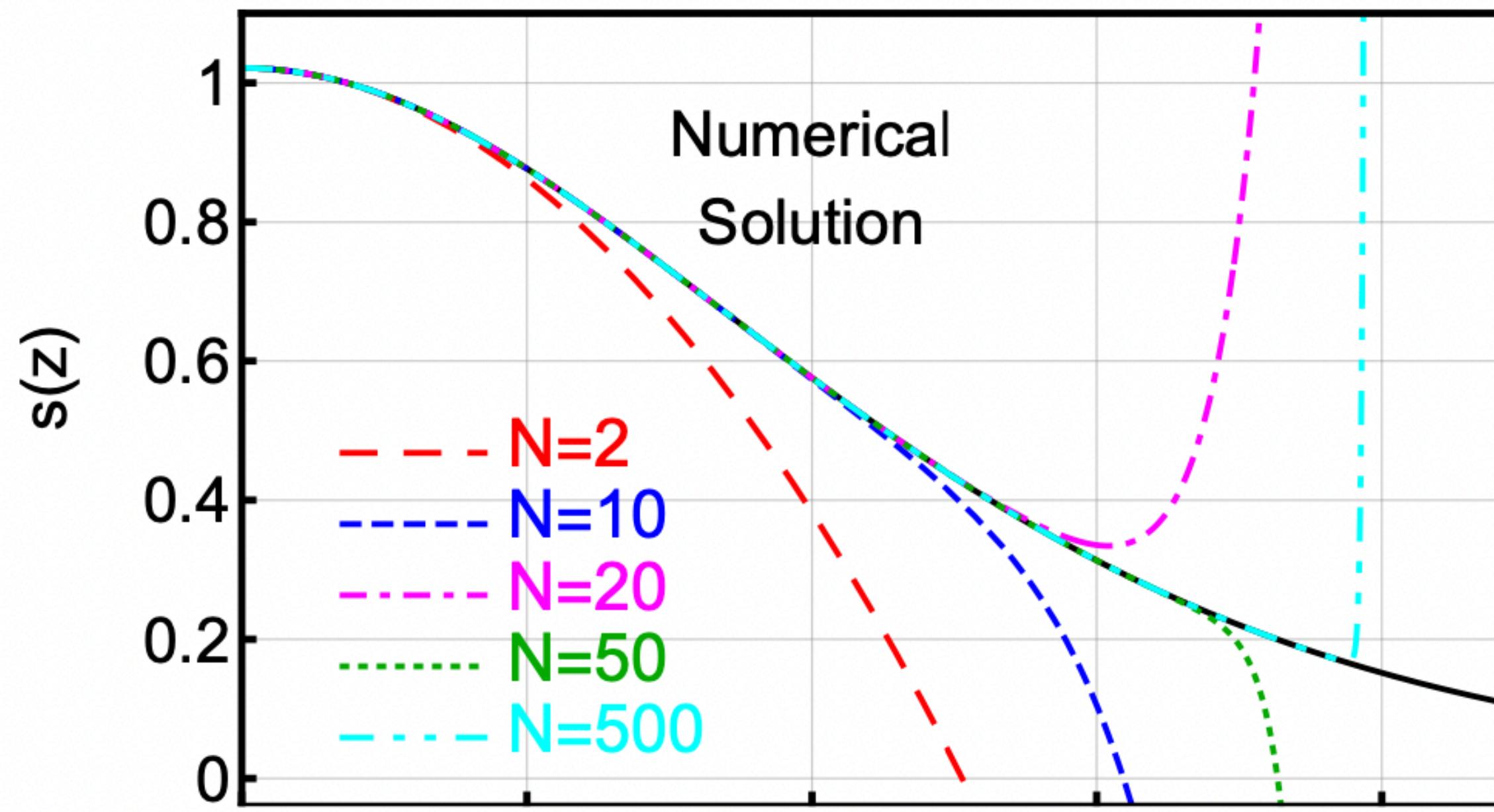
Need to usually solve the full Einstein Klein-Gordon system of equations

$$e\psi = -\frac{1}{2m}\nabla^2\psi + m\Phi\psi + \frac{N\lambda}{4m^2}\psi^3.$$



$$\nabla^2 V = -S^2 \quad \text{and} \quad \nabla^2 S = -VS + \Lambda S^3.$$

$$\nabla^2\Phi = 4\pi G N m \psi^2$$



Towards an analytic construction of the wavefunction of boson stars

Felix Kling and Arvind Rajaraman
Phys. Rev. D **96**, 044039 – Published 28 August 2017

Profiles of boson stars with self-interactions

Felix Kling and Arvind Rajaraman
Phys. Rev. D **97**, 063012 – Published 20 March 2018

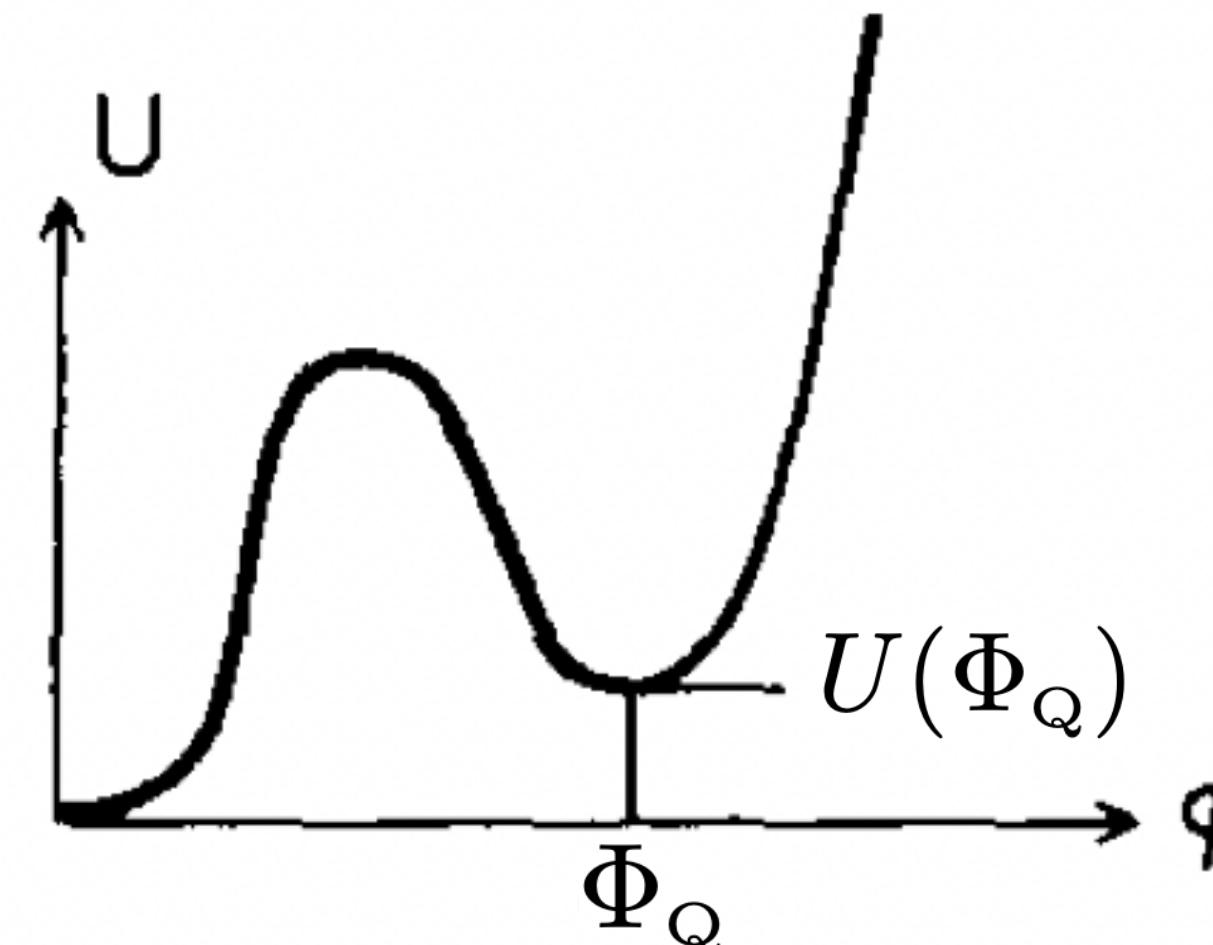
Q-balls

$$\mathcal{L} = \partial_\mu \Phi \partial^\mu \Phi^\dagger - U(\Phi^\dagger \Phi) .$$

$$0 \leq \frac{U(\Phi_Q)}{\Phi_Q^2} \equiv \omega_Q^2 < m^2 .$$

$$E = \omega Q + \frac{8\pi}{3} \int dr r^2 \phi'^2 .$$

$$U(\phi) = m^2 \phi^2 + \lambda \phi^4 + \zeta \phi^6 .$$



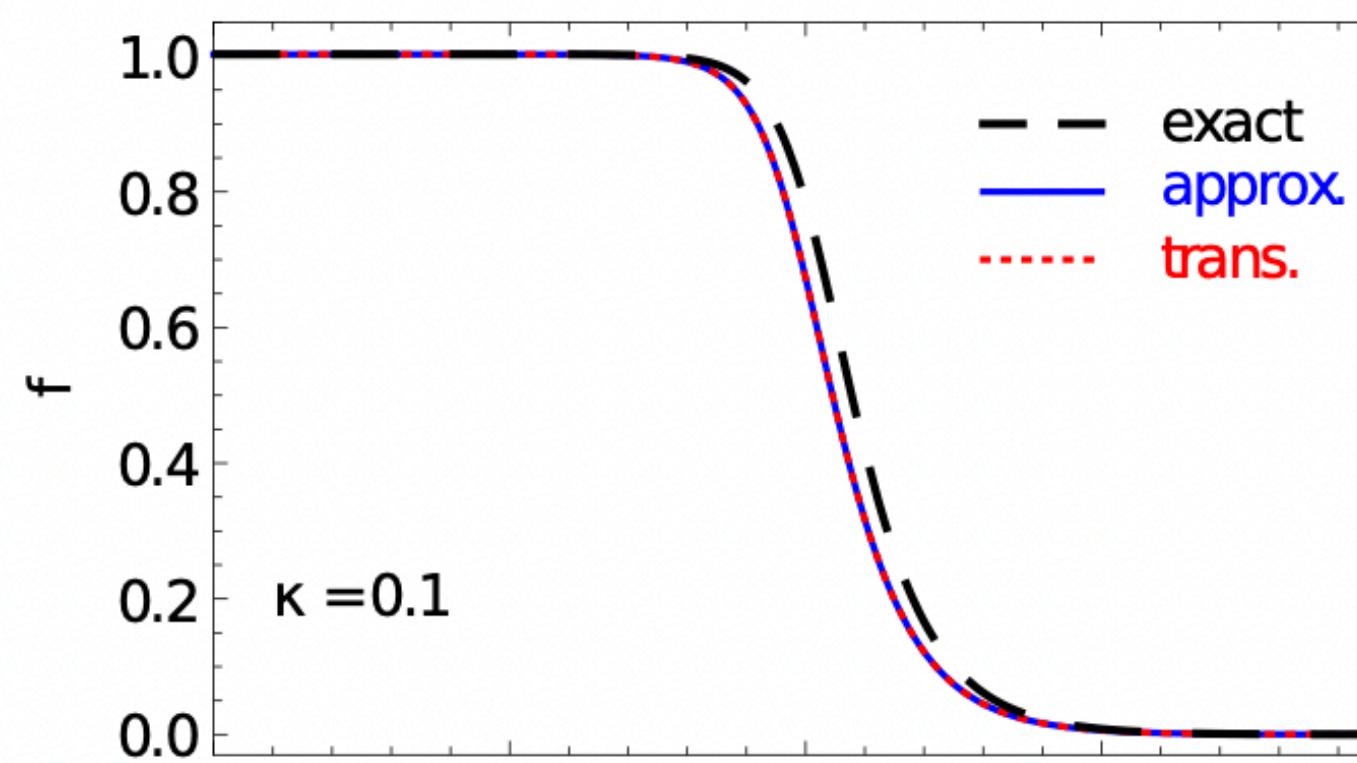
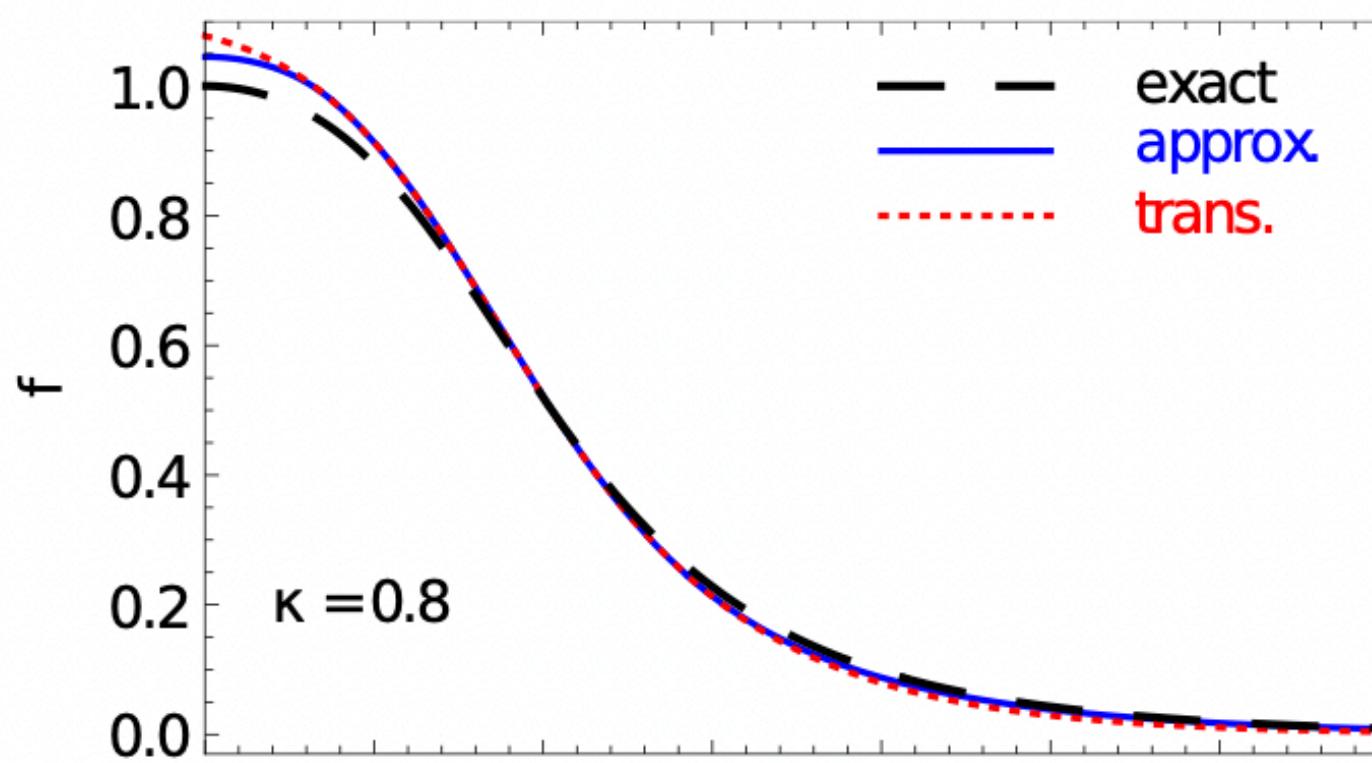
Q-BALLS*

Sidney COLEMAN

Lyman Laboratory of Physics, Harvard University, Cambridge, Massachusetts 02138, USA

Understanding Q-balls beyond the thin-wall limit

Julian Heeck, Arvind Rajaraman, Rebecca Riley, and Christopher B. Verhaaren
Phys. Rev. D **103**, 045008 – Published 9 February 2021



Eur. Phys. J. C (2024) 84:364
<https://doi.org/10.1140/epjc/s10052-024-12712-x>

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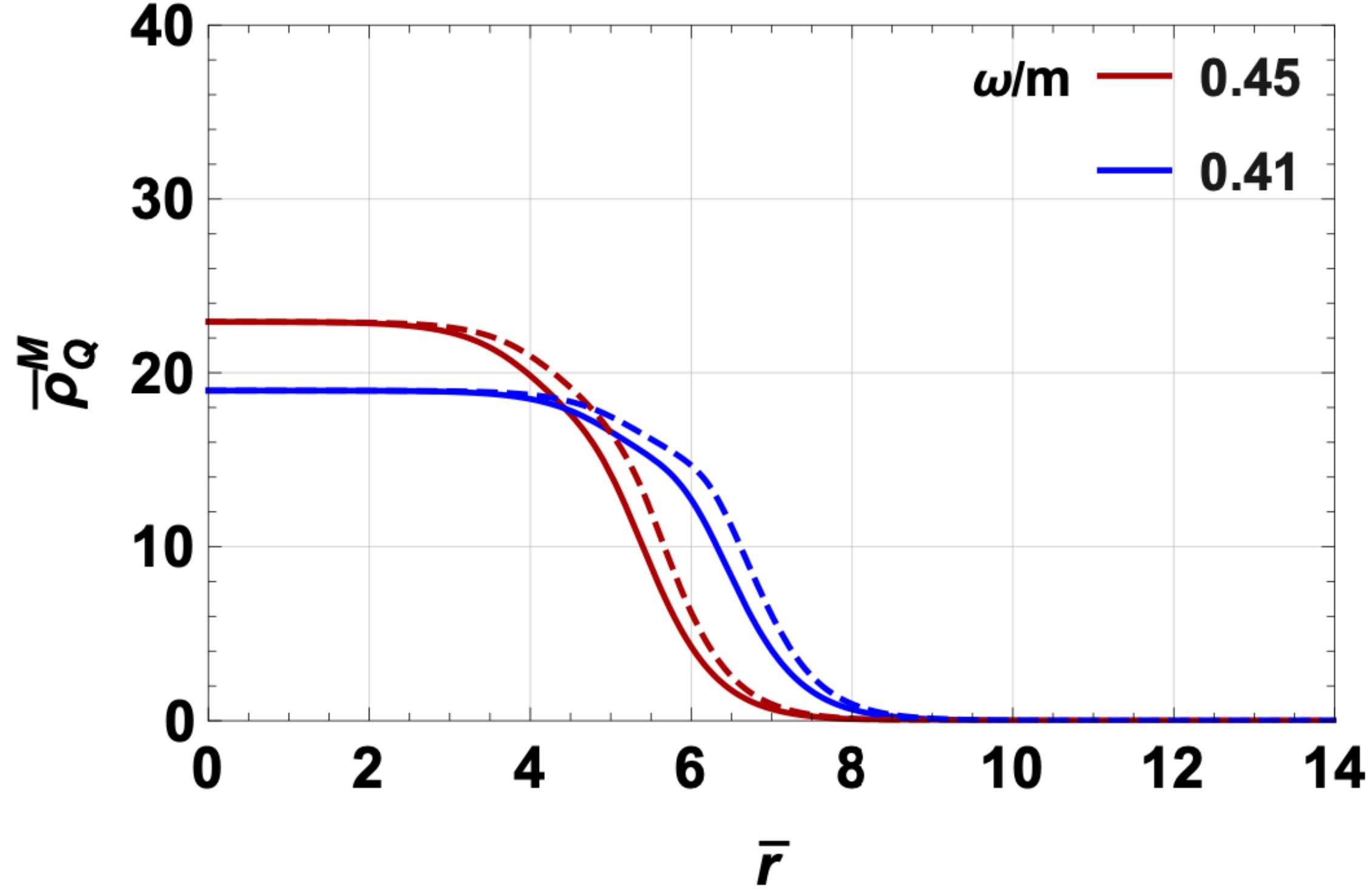
Regular Article - Theoretical Physics

Slowly rotating Q-balls

Yahya Almumin^{1,2,a}, Julian Heeck^{3,b}, Arvind Rajaraman^{1,c}, Christopher B. Verhaaren^{4,d}

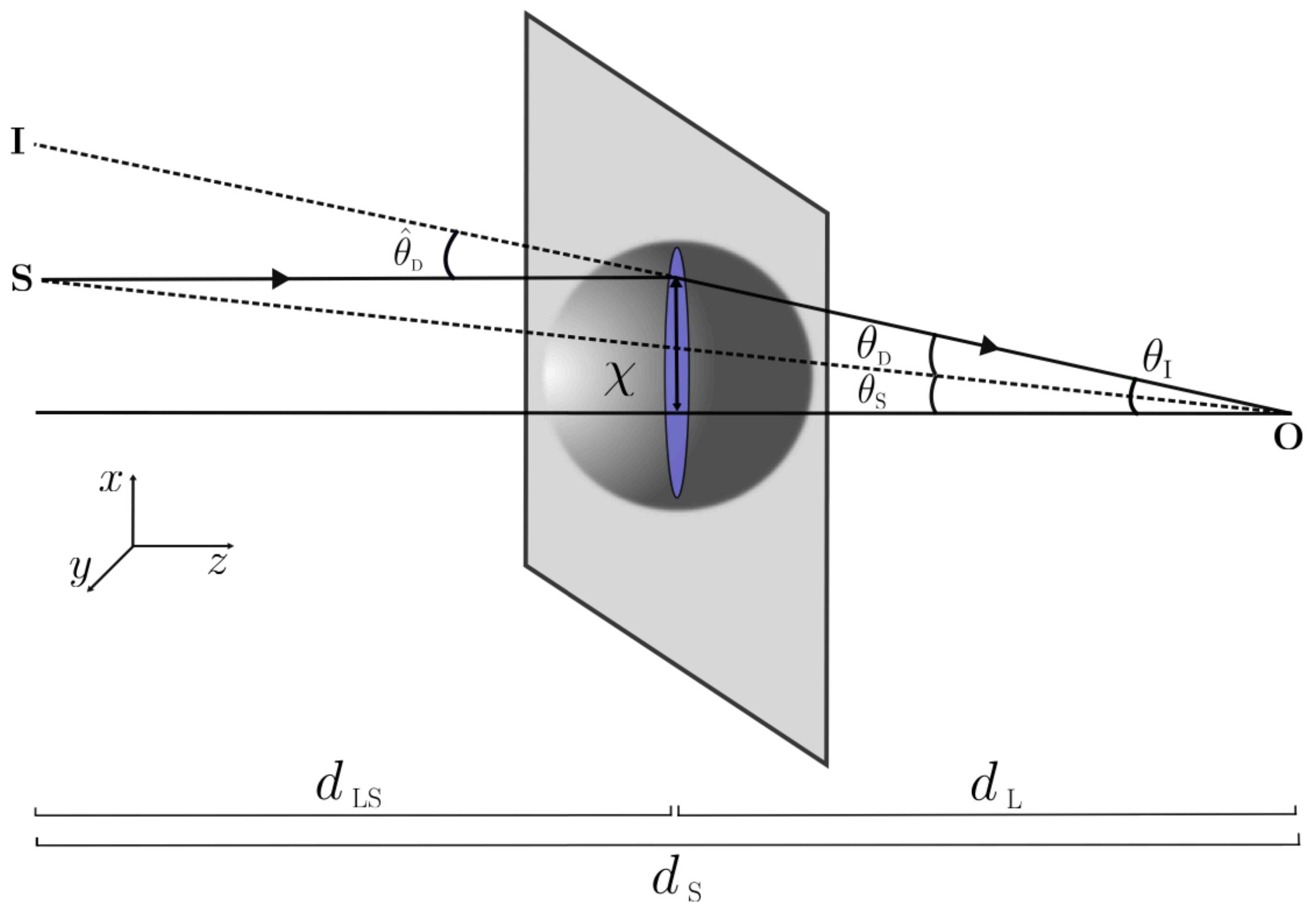
Energy Extraction from Q-balls and Other Fundamental Solitons

Vitor Cardoso, Rodrigo Vicente, and Zhen Zhong
Phys. Rev. Lett. **131**, 111602 – Published 11 September 2023



$$\phi(r) = \frac{\phi_*}{\sqrt{1 + 2 \exp [2\sqrt{m^2 - \omega_Q^2} (r - R_Q)]}} ,$$

$$\phi_*^2 = \frac{\phi_Q^2}{3} \left[2 + \sqrt{1 + 3 \left(\frac{\omega^2 - \omega_Q^2}{m^2 - \omega_Q^2} \right)} \right]$$



Thank you