

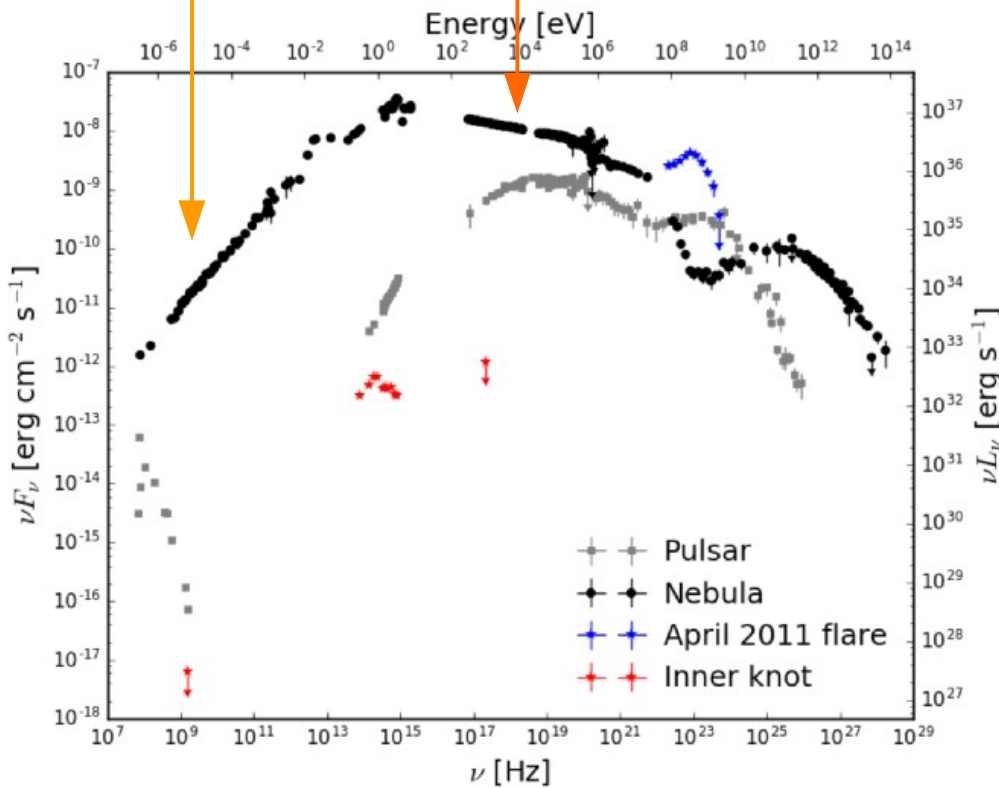
# **PARTICLE ACCELERATION AT PULSAR-WIND TERMINATION SHOCKS**

***Gwenael Giacinti (MPIK Heidelberg)  
& John G. Kirk (MPIK Heidelberg)***

**In Prep. (To be submitted soon)**

# Observations of the Crab nebula

**RADIO**      **X-RAYS**



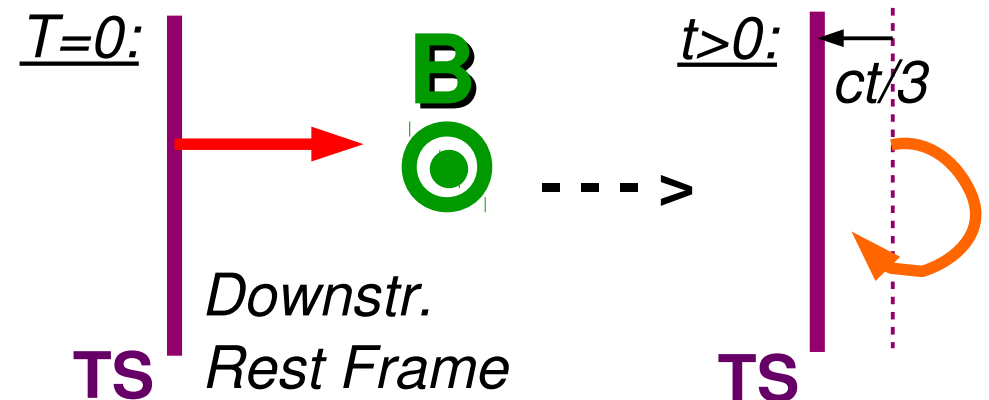
*Buehler & Blandford (2014)*

→ **X-ray spectral index :**  
 $d(\ln N_\gamma) / d(\ln \nu) = - 2.1$

→ **Predicted particle spectrum at ultra-relativistic shocks :**  
 $d(\ln N_e) / d(\ln \gamma) = - 2.2$

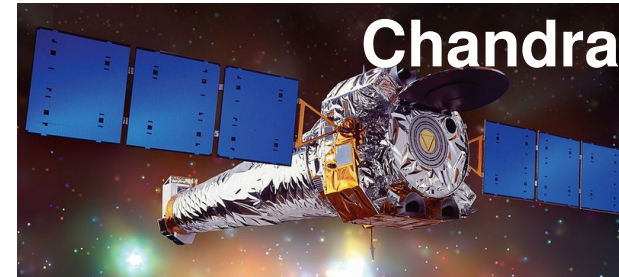
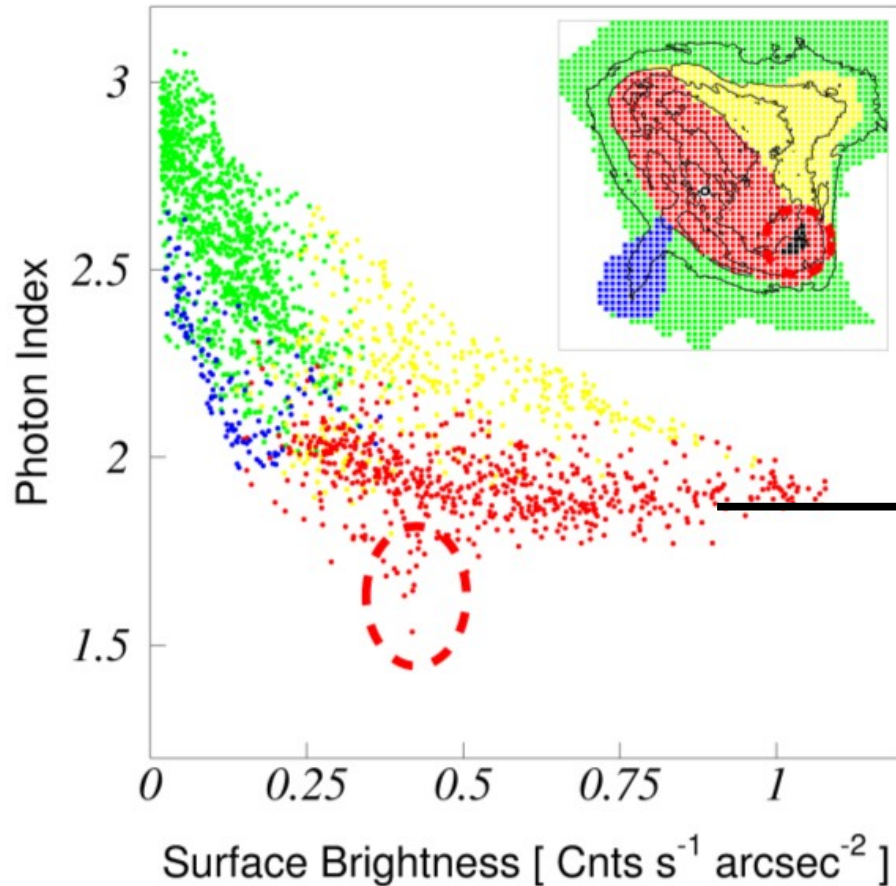
*Seems to be in perfect agreement*

**BUT... Perpendicular shock, so 1<sup>st</sup> order Fermi inoperative !**



# Observations of the Crab nebula

(1) Spectral index map - Mori *et al.*, ApJ (2004):



**Hard spectrum** close to the shock, in the equatorial plane

Photon index  $s \sim 1.9$

$$\Rightarrow d(\ln N_{e^-}) / d(\ln \gamma) \sim -1.8 !$$

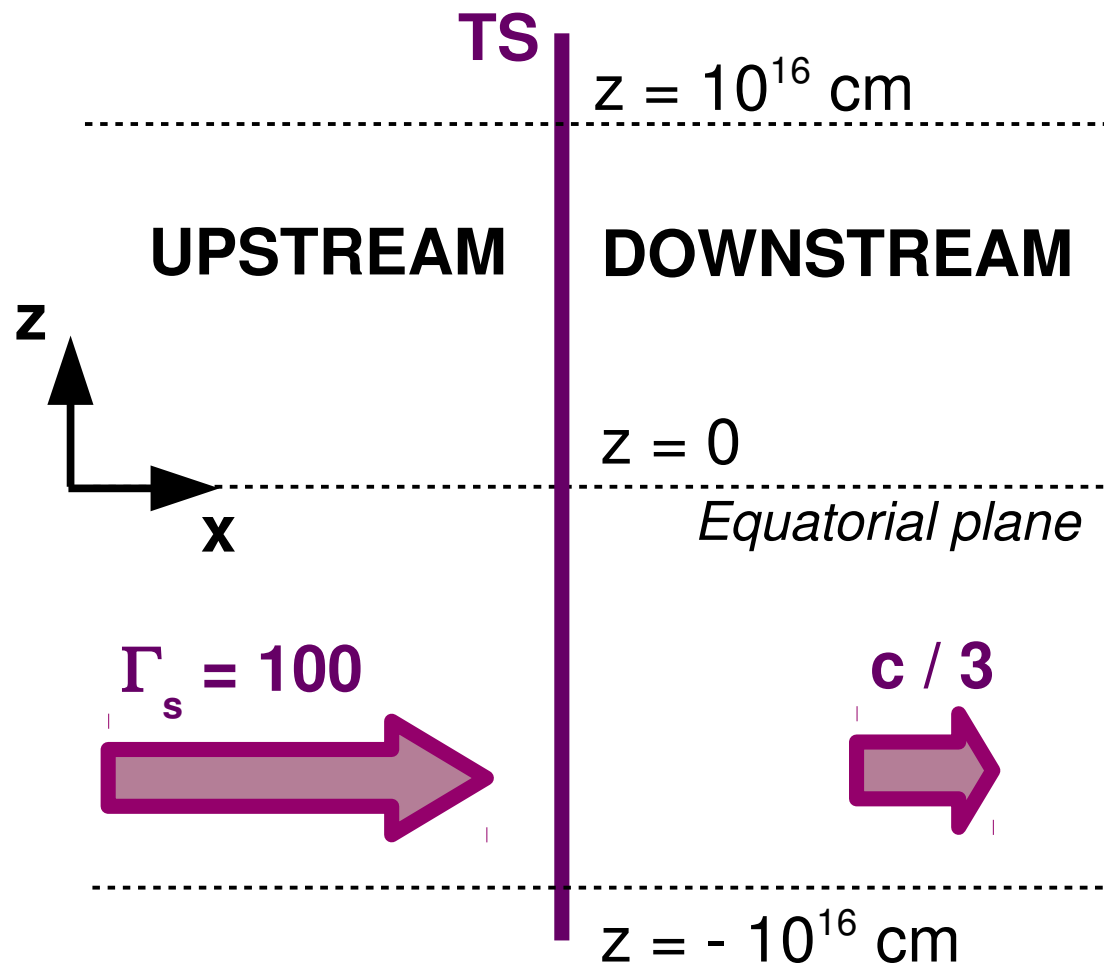
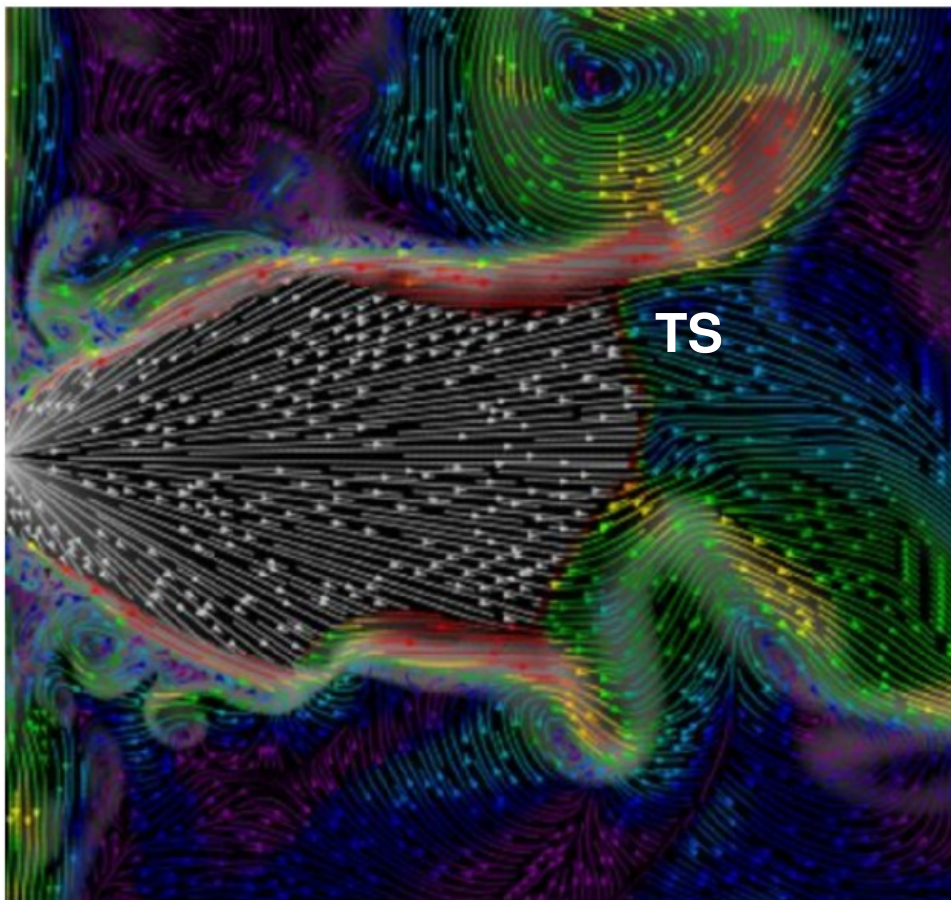
(2) How many X-ray emitting electrons ?

$N(e^- \text{ radio})/N(e^- \text{ X-rays}) \sim 10^4$  - e.g. Olmi *et al.*, J. Plasma Phys. (2016).

# Numerical simulations – Model

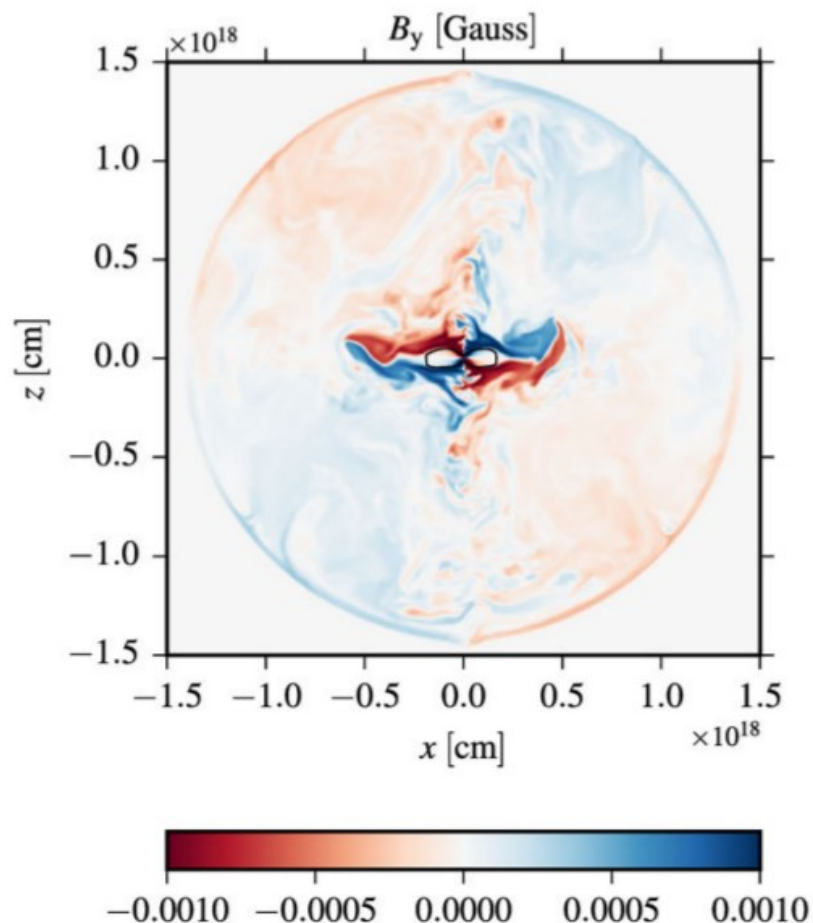
Simulations of  
Buehler & Giomi (2016) :

OUR MODEL (PLANAR 1D) :

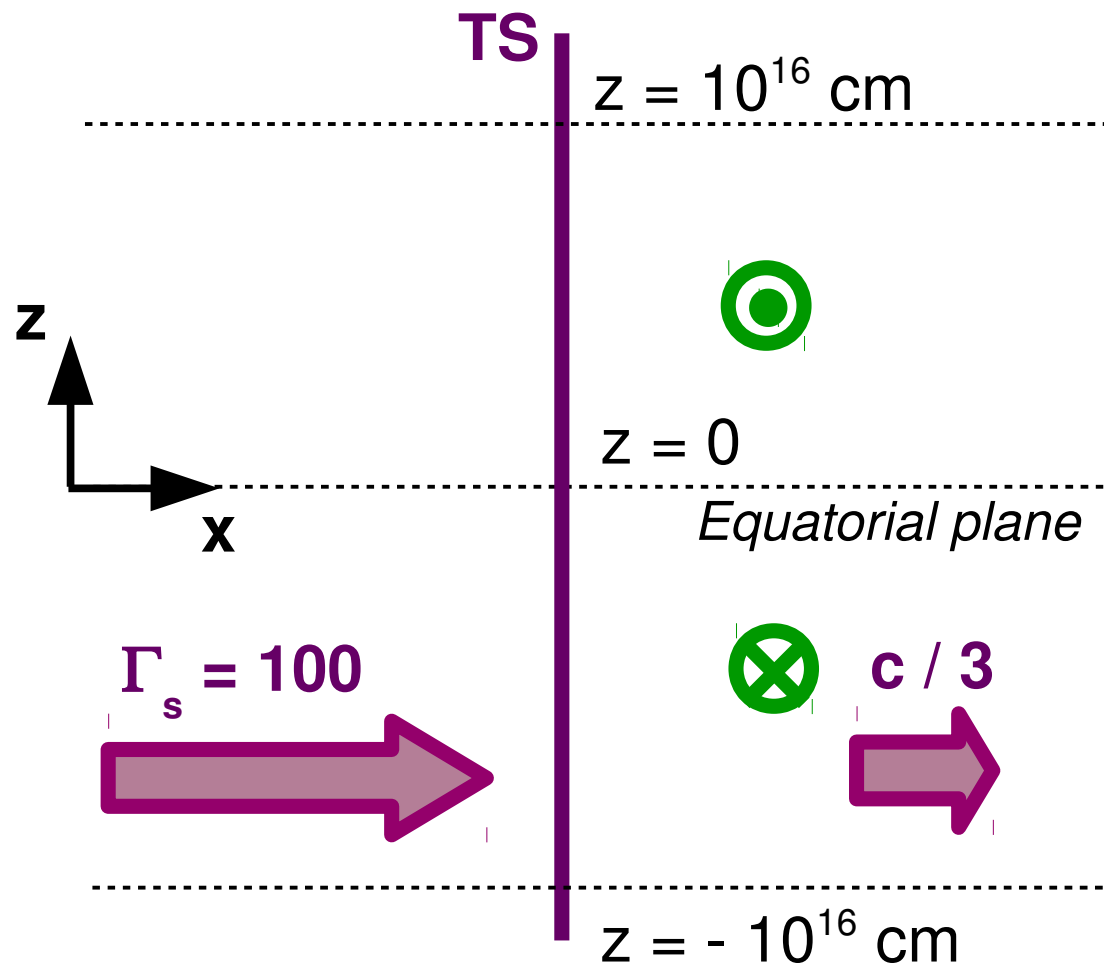


# Numerical simulations – Model

Simulations of Porth *et al.*  
(2014, 2016) – Crab nebula:



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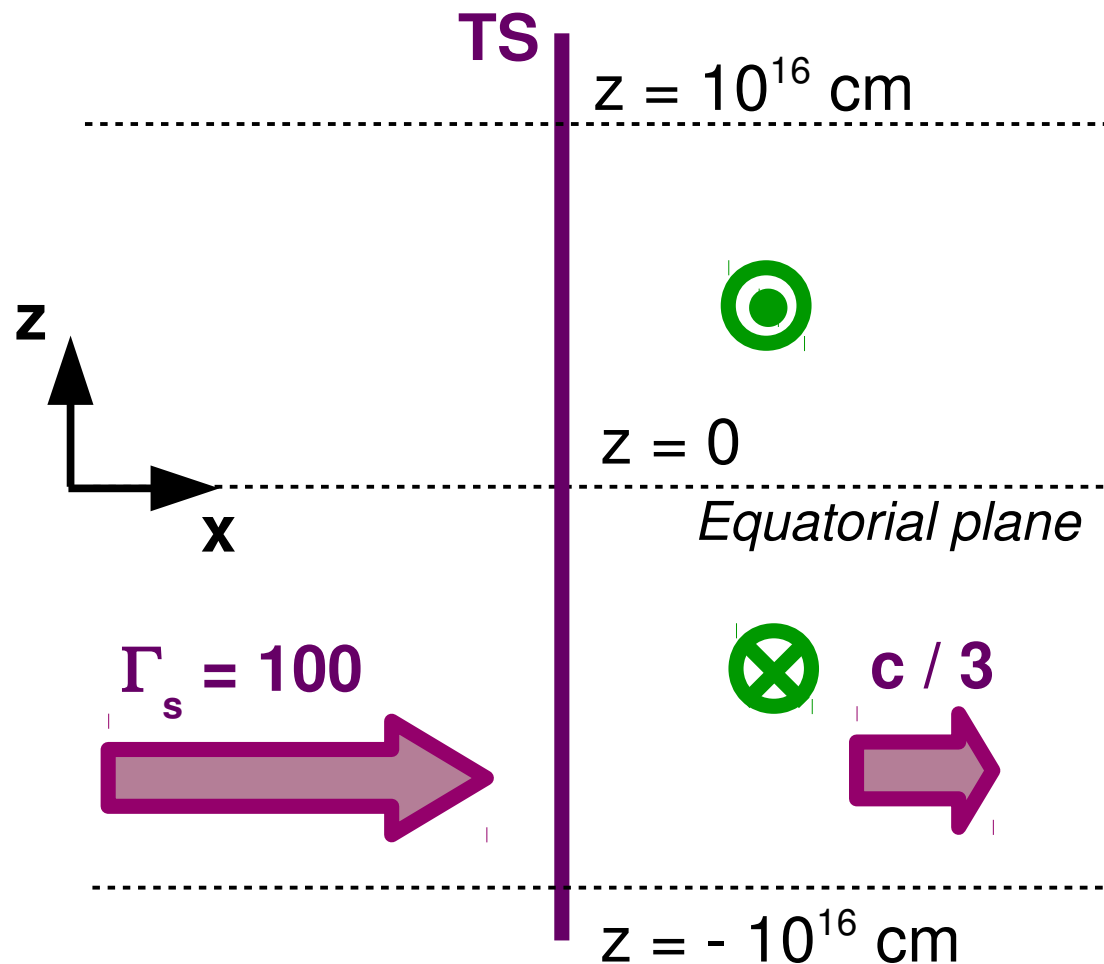
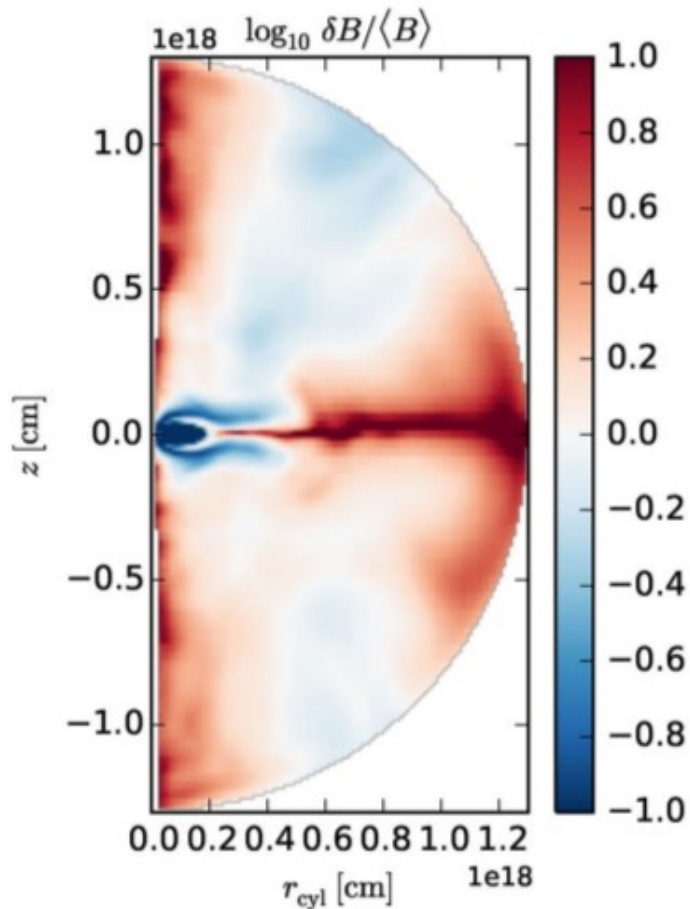
→  $\mathbf{B} \propto z \mathbf{u}_y$  for  $|z| < 10^{16}$  cm,

→ At  $z = \pm 10^{16}$  cm,  $B = \pm 1$  mG

# Numerical simulations – Model

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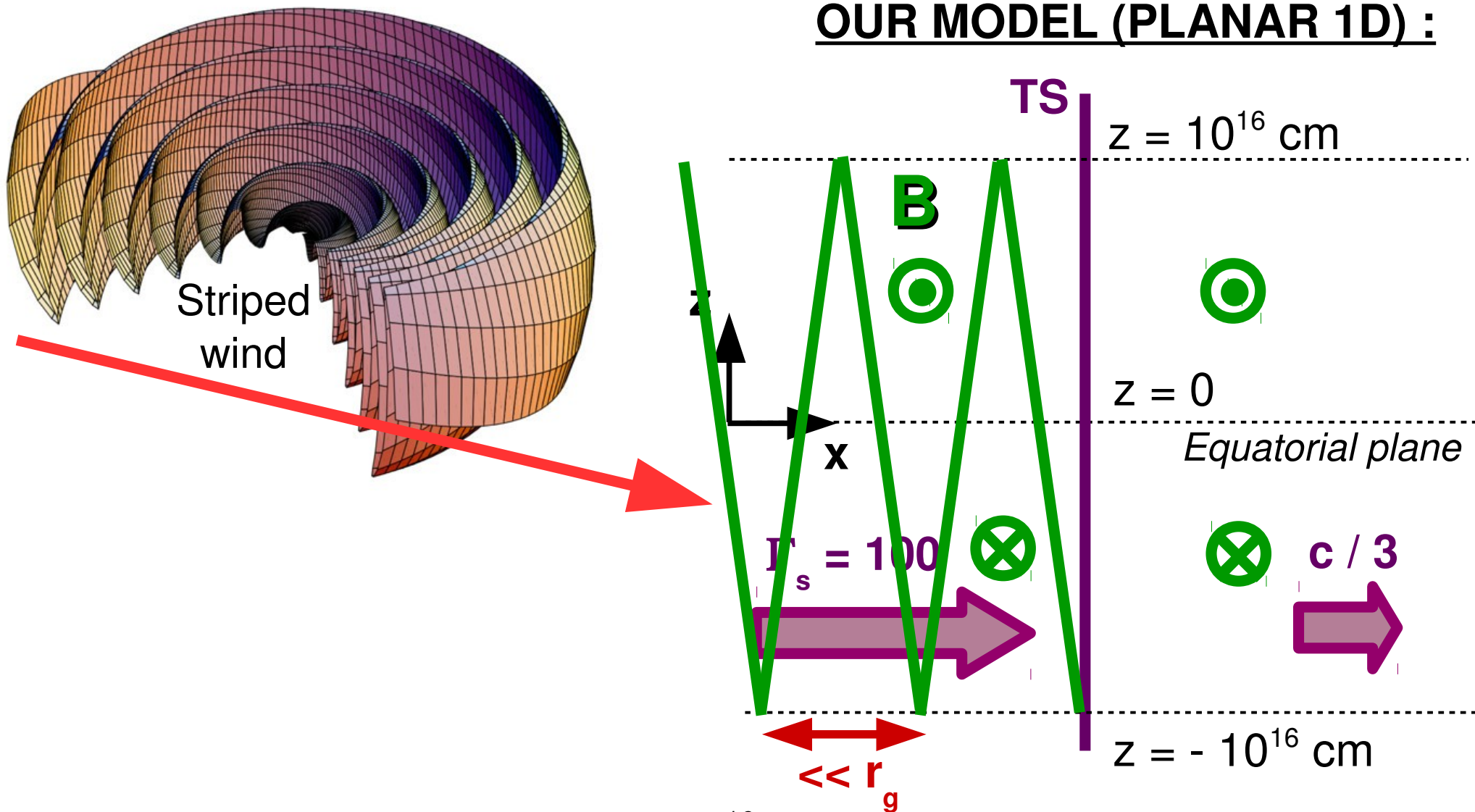


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→ At  $z = \pm 10^{16}$  cm,  $B = \pm 1$  mG,  $\delta B/B = 0.1$ , cst. of  $z$ , Bohm.

# Numerical simulations – Model

## OUR MODEL (PLANAR 1D) :

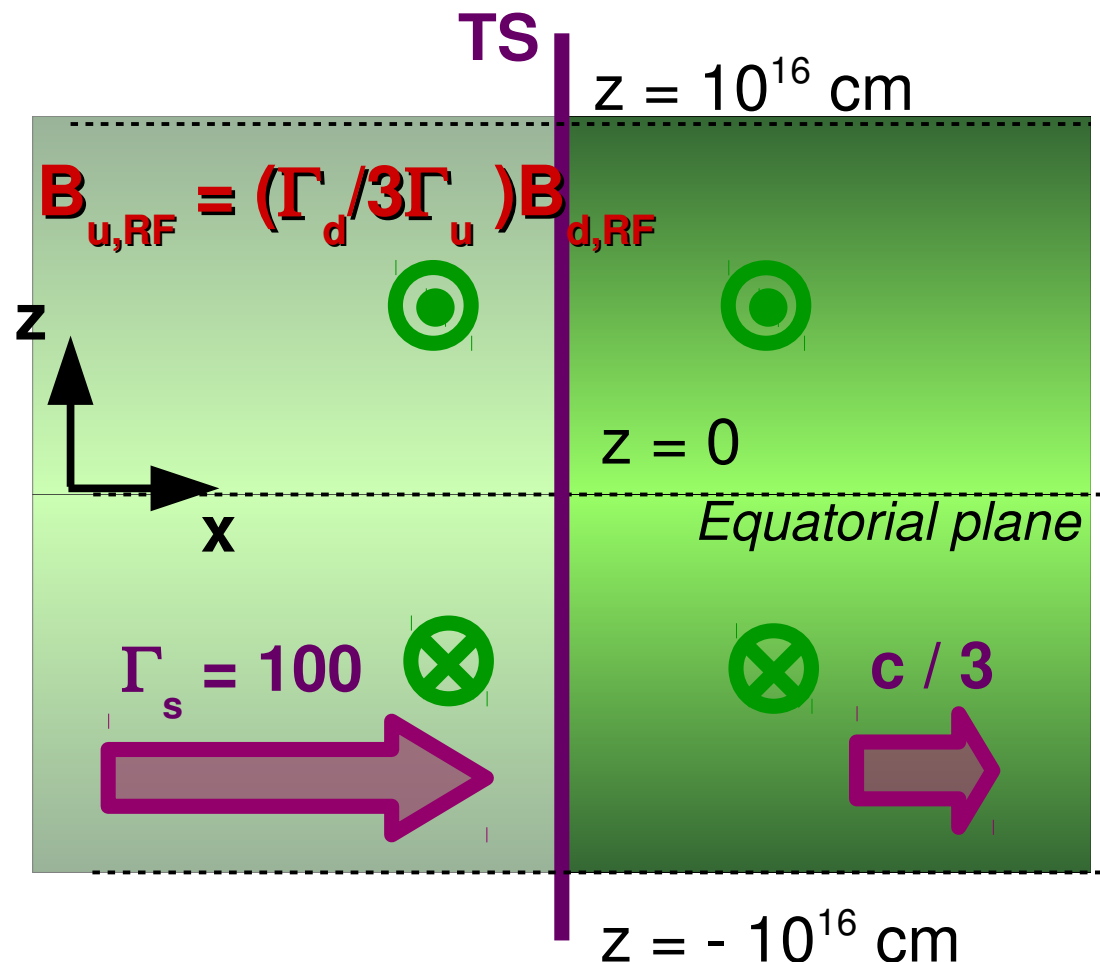


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# Numerical simulations – Model

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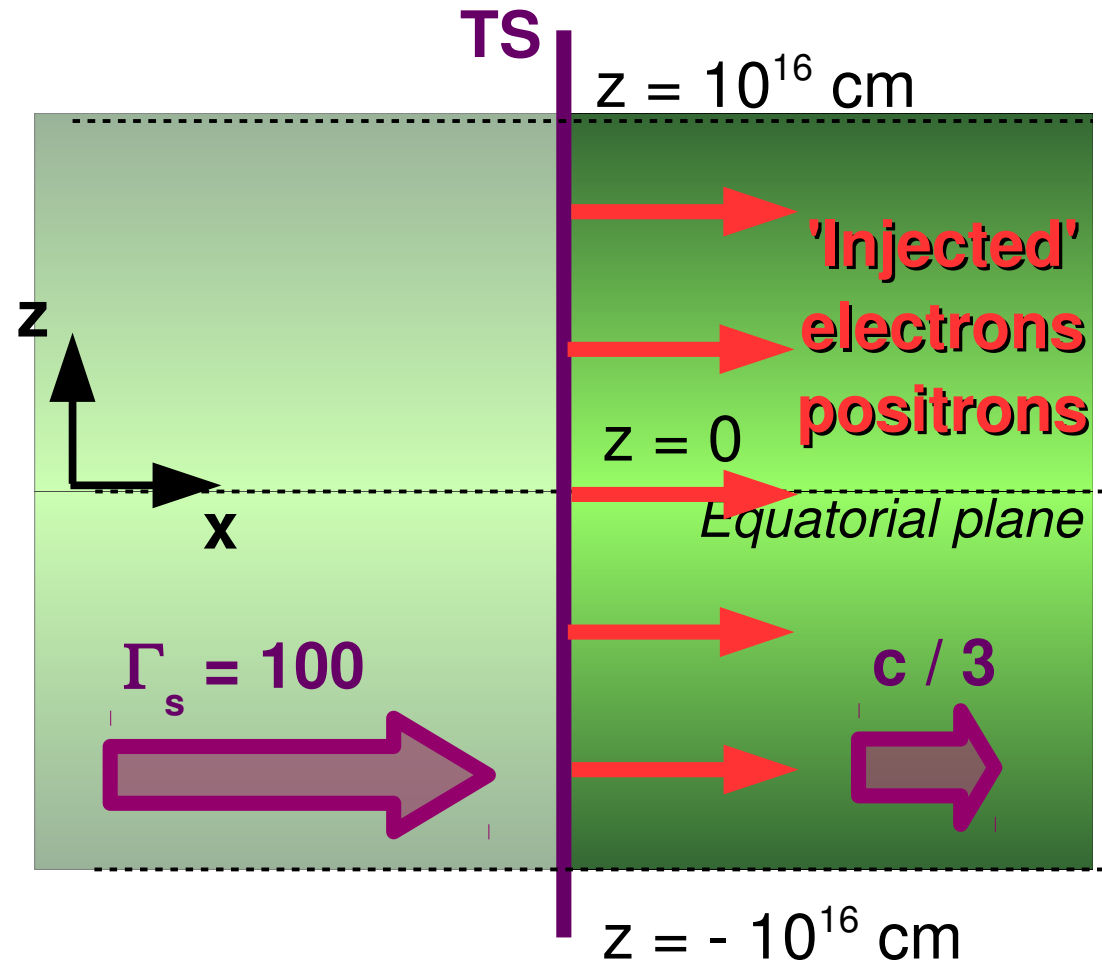
→ At  $z = \pm 10^{16}$  cm,  $B = \pm 1$  mG,  $\delta B/B = 0.1$ , cst. of  $z$ , Bohm.



# Numerical simulations – Model

## OUR MODEL (PLANAR 1D) :

- Integrate trajectories of individual particles in 3D (test particle limit),
- Use 3D realizations of turbulent B fields,
- Integrate in Downstream or Upstream rest frame ( $E=0$ ) ;  
If shock crossing: Do the Lorentz transfo.  $(X_d, t_d) \leftrightarrow (X_u, t_u)$ ,
- Obs. Fr.  $\sim$  Shock Fr.  $\leftrightarrow (X_s, t_s)$ .



# Numerical simulations – Model

## OUR MODEL (PLANAR 1D) :

Wave period 33 ms, low density wind  $\Rightarrow$  MHD invalid.

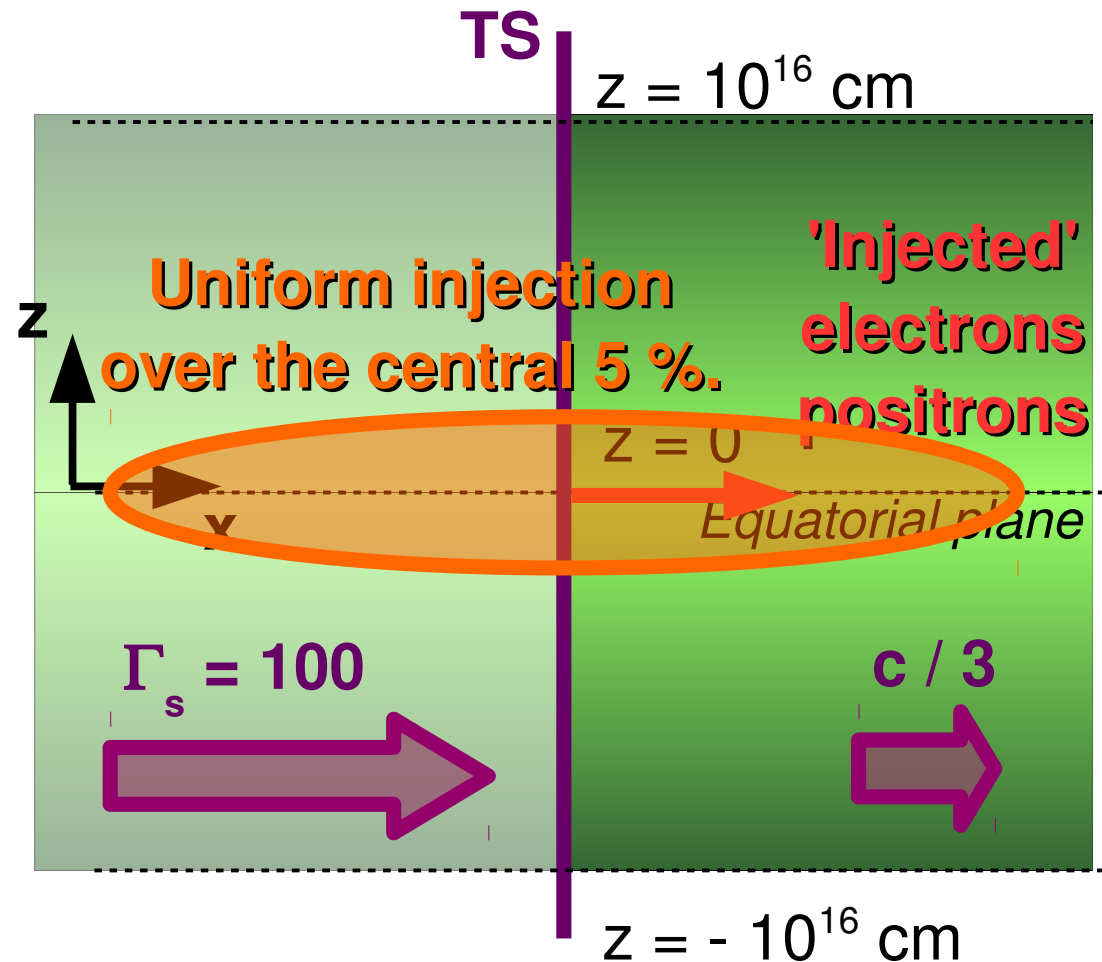
**Amano & Kirk (2013):**

Two fluid simulations of a shock front in a Poynting-flux-dominated relativistic flow.

**Giacchè & Kirk (2017):**

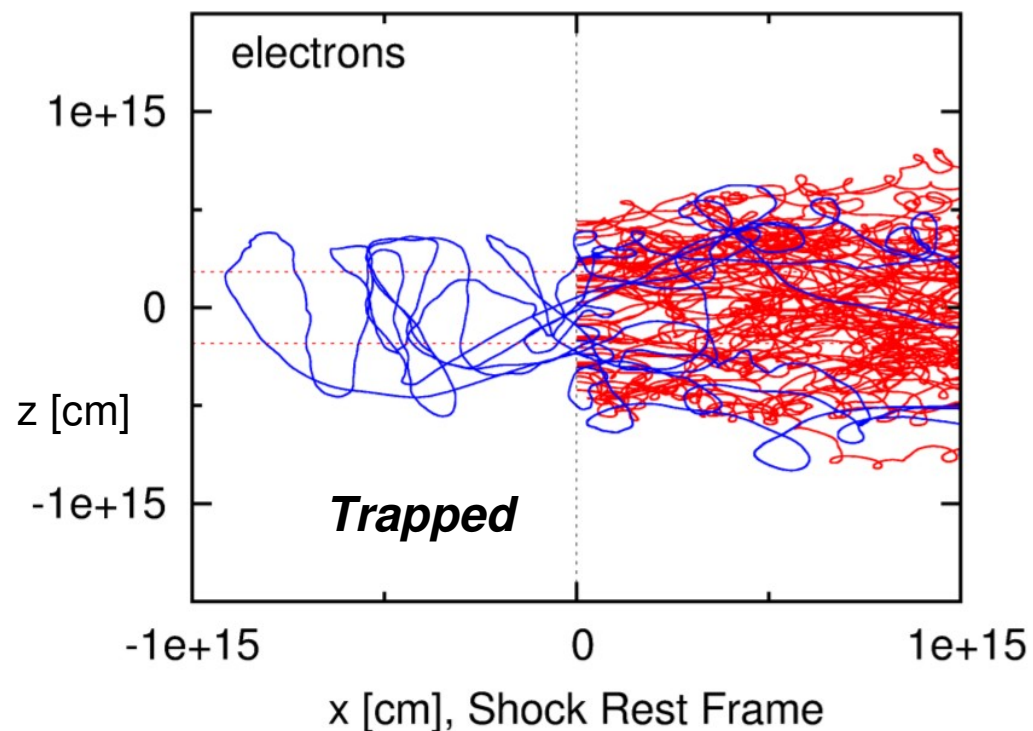
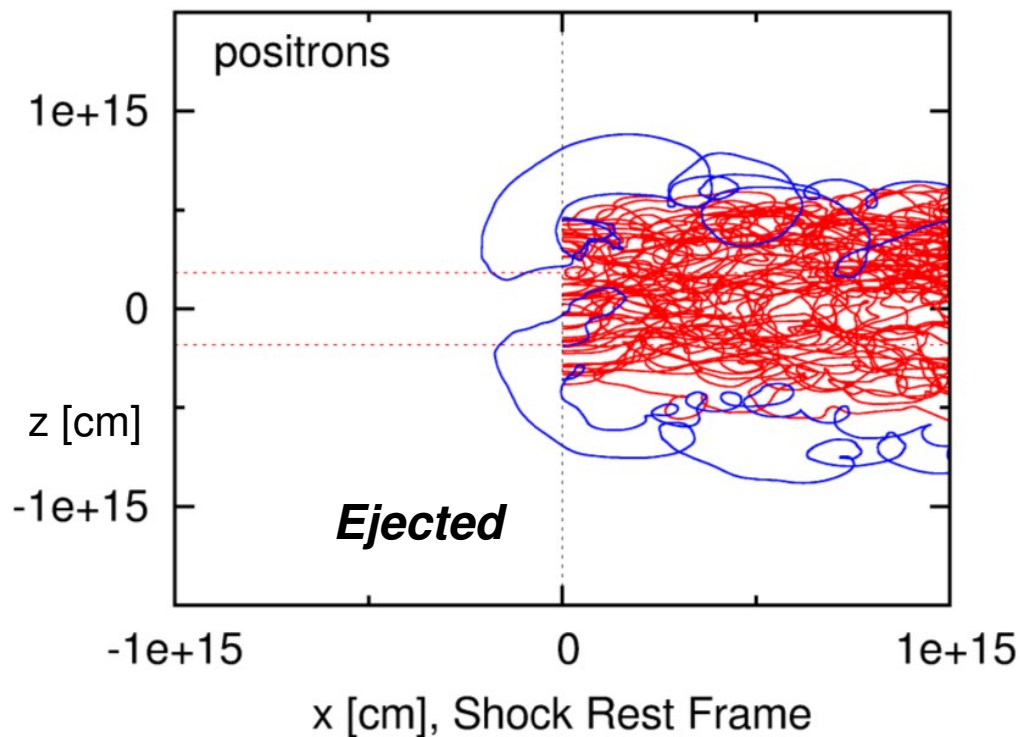
Propagate individual  $e^\pm$ .

$\gamma_{inj} \sim 10^{4-6} \Rightarrow$  **TeV electrons.**



# Numerical simulations

In the equatorial current sheet :



$$d(\ln N) / d(\ln \gamma) \approx -6 \dots -5 < -2.2$$

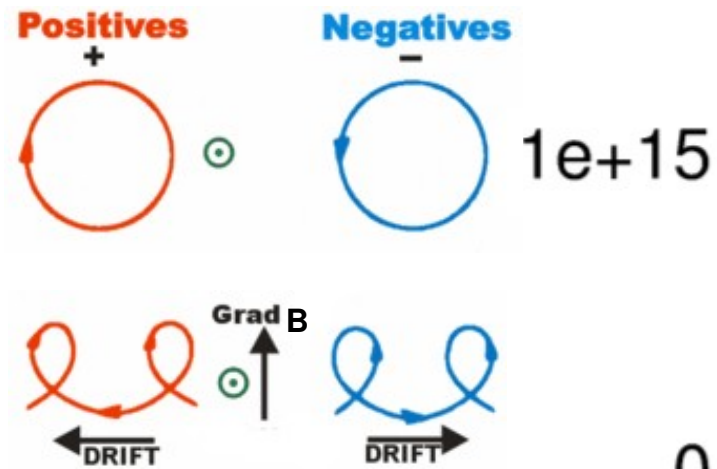
**VERY SOFT**

$$d(\ln N) / d(\ln \gamma) \approx -1.8 > -2.2 !$$

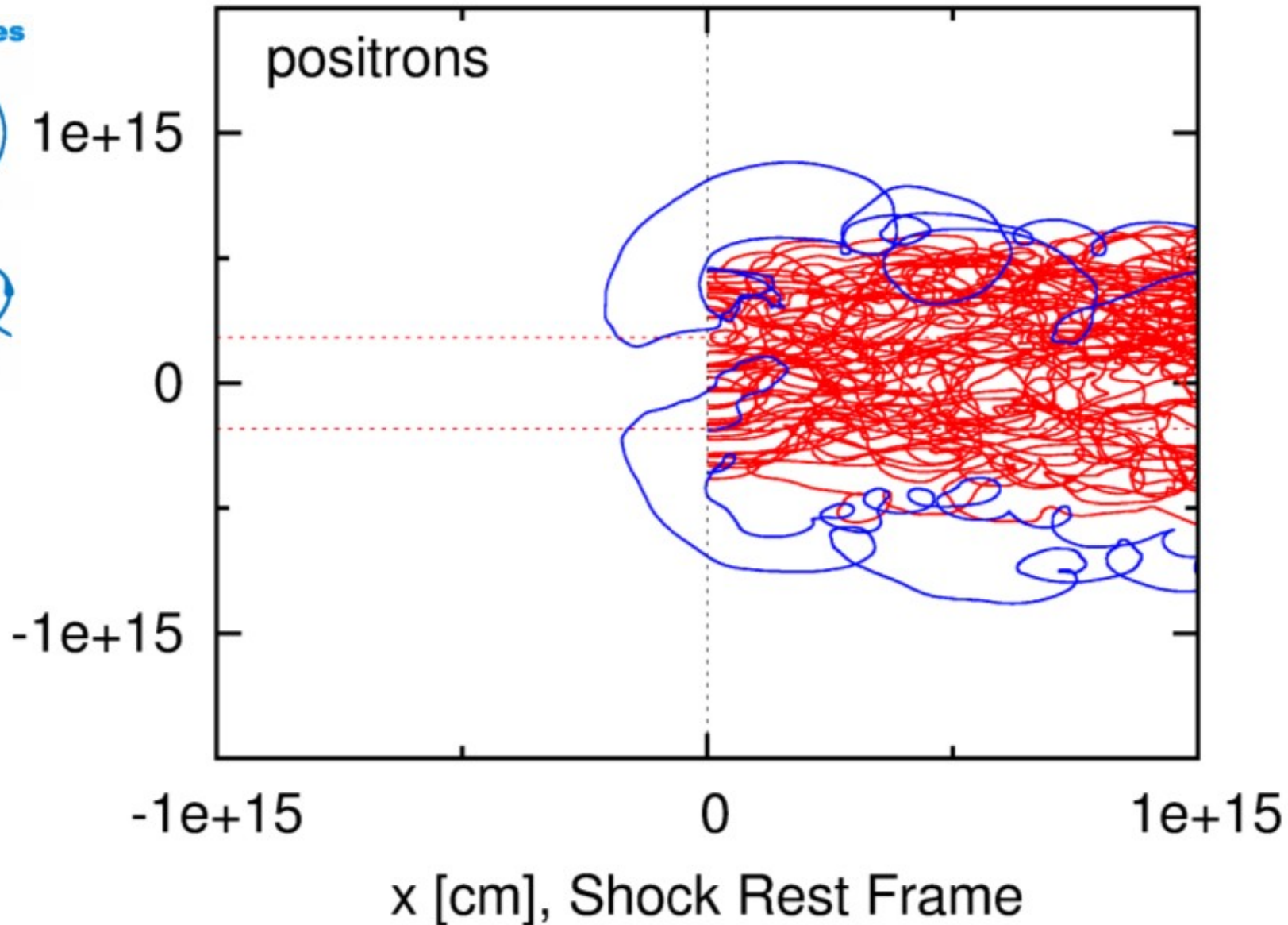
**HARD**

# Positrons

(... or electrons - depends on polarity)

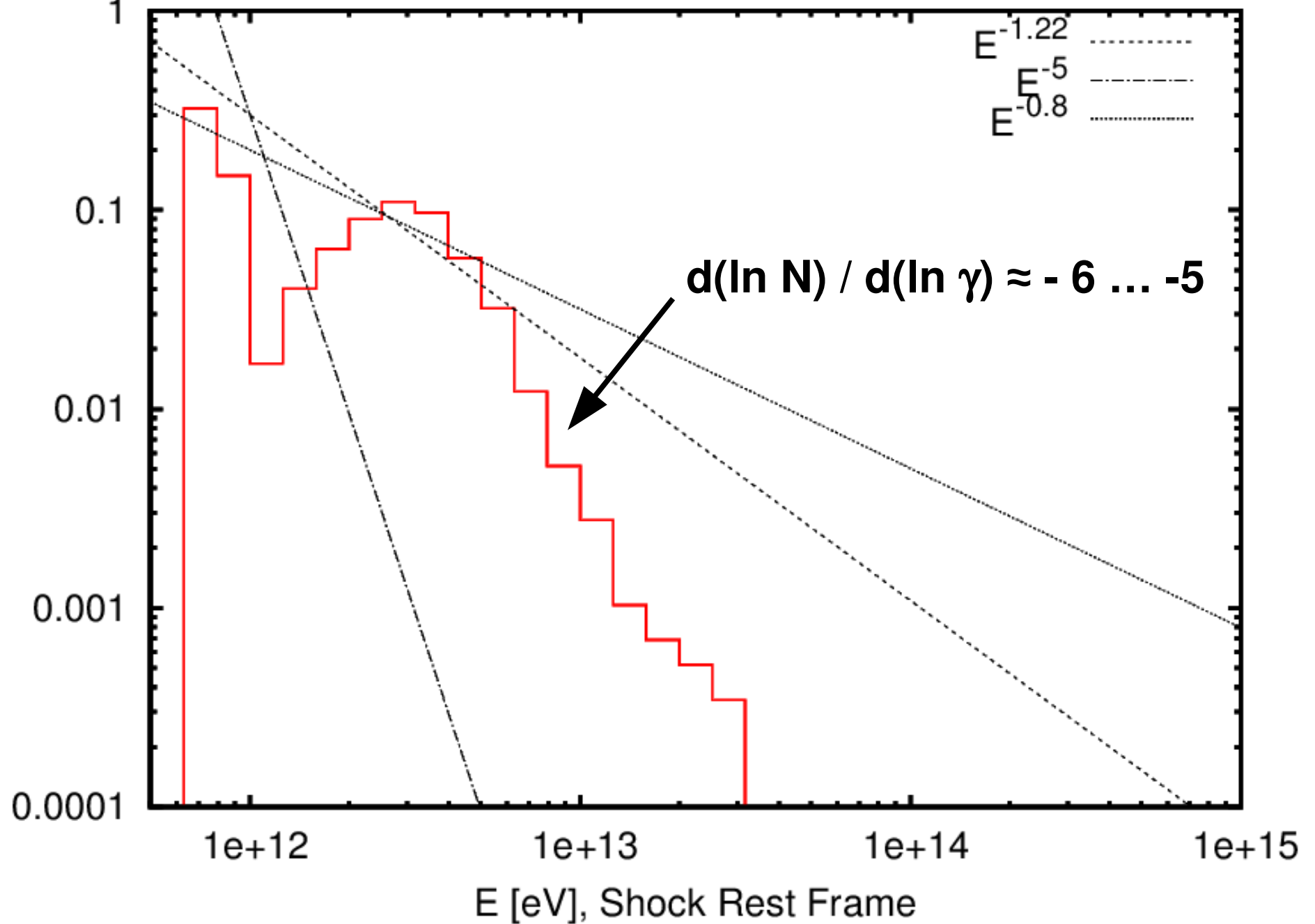


**Grad-B drift**  
can beat the  
advection at  
 $c/3$  in small  
regions close  
to  $z=0$  (on  
both sides).

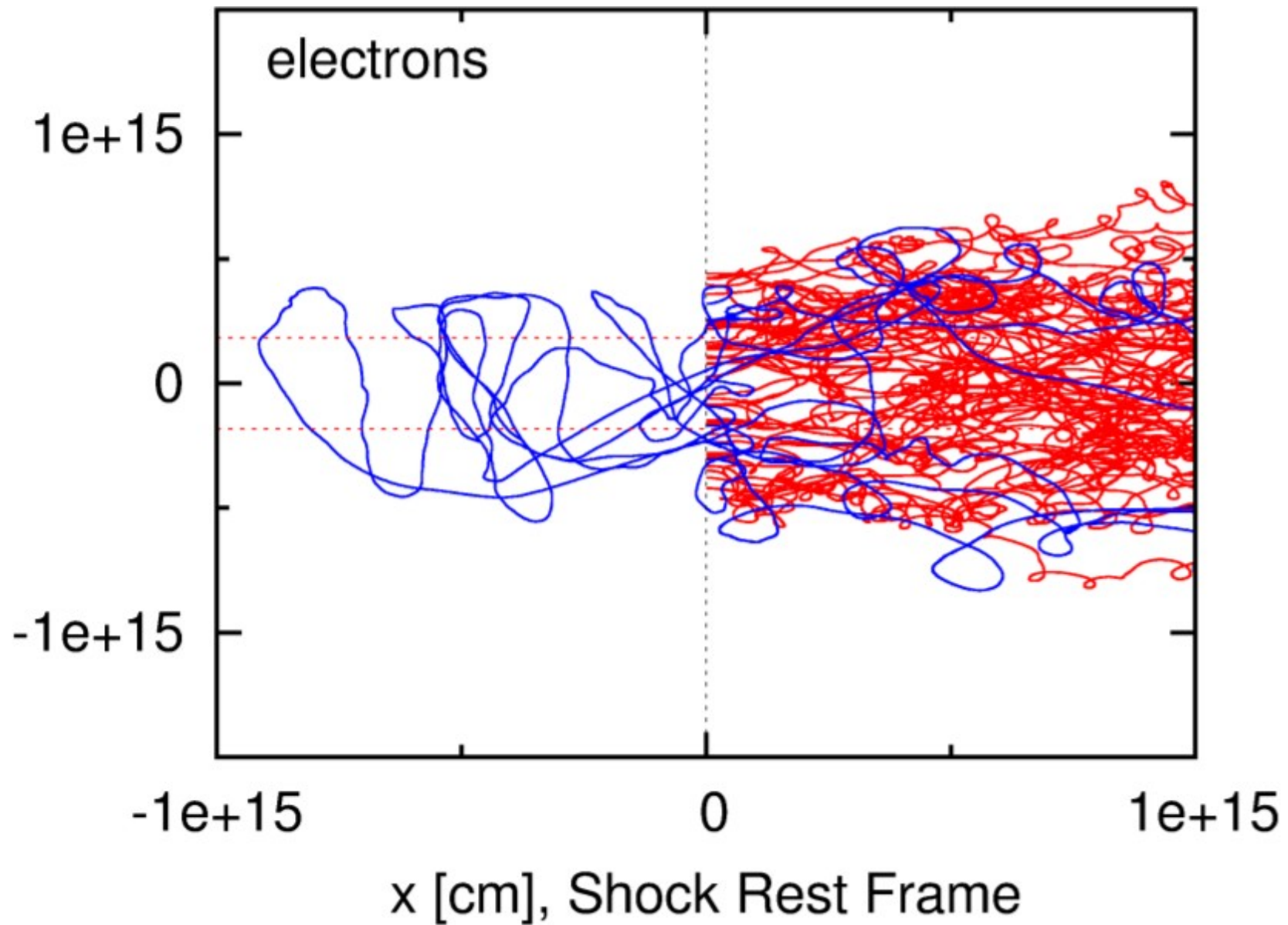


# Positrons

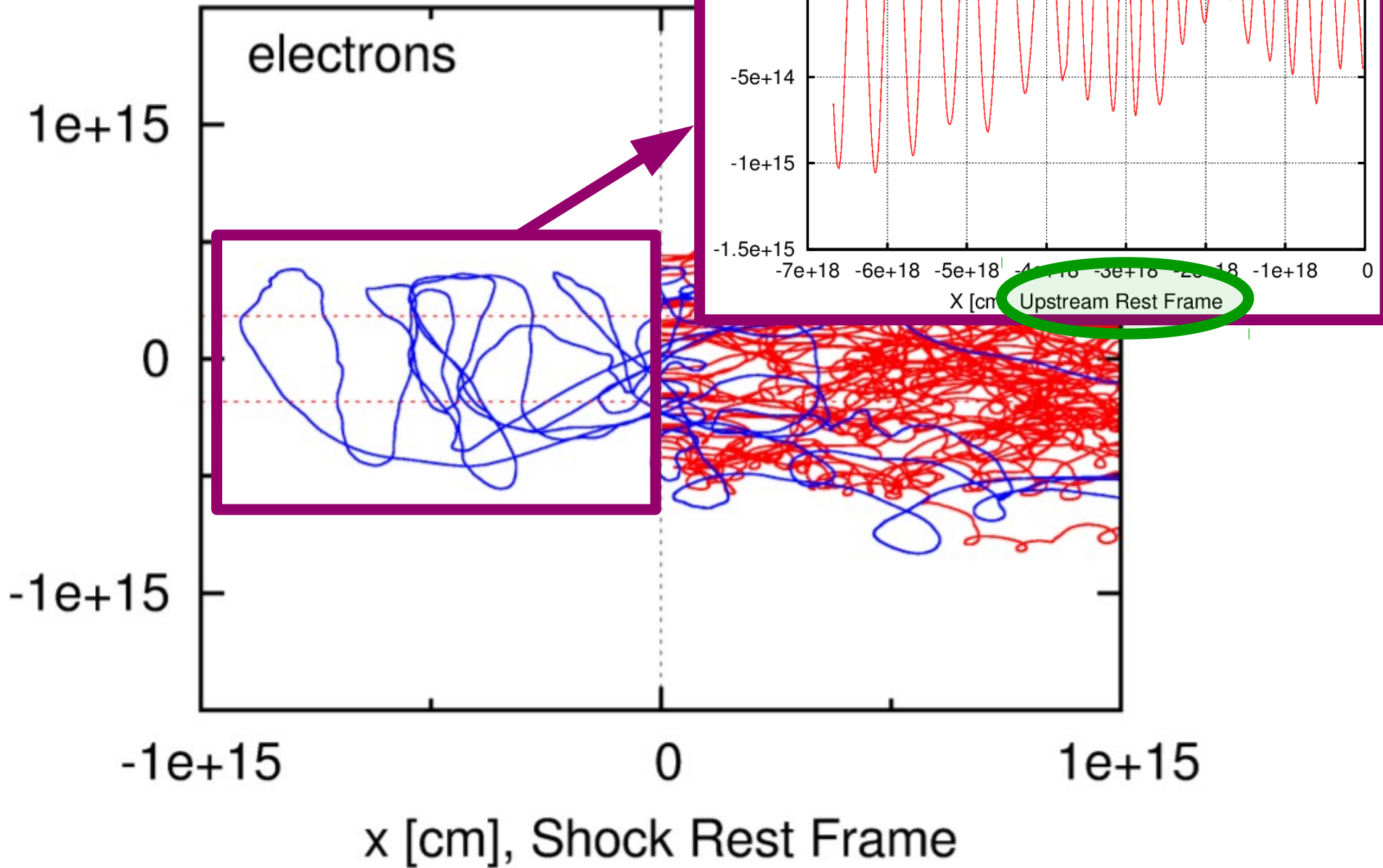
$\sim E \cdot dN/dE$



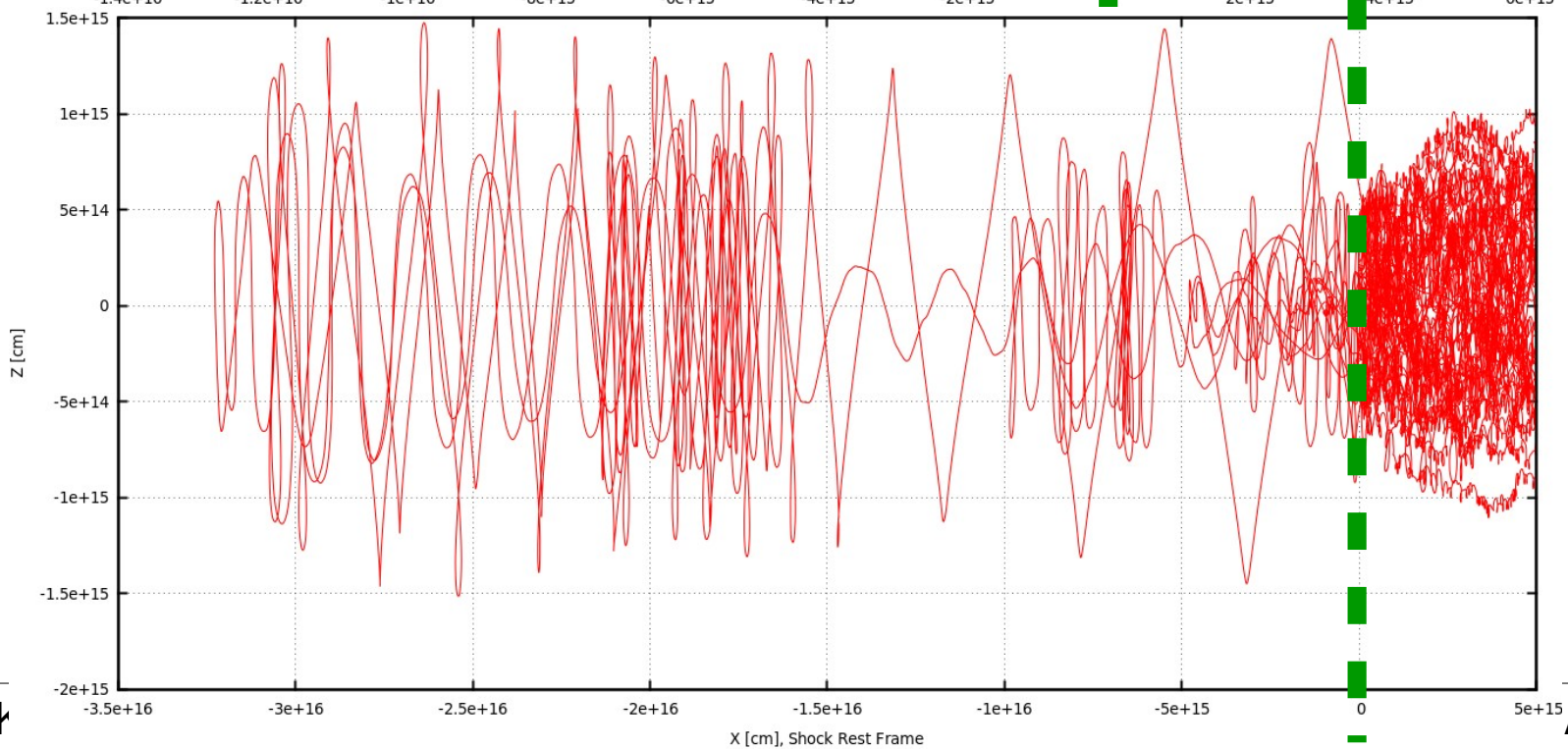
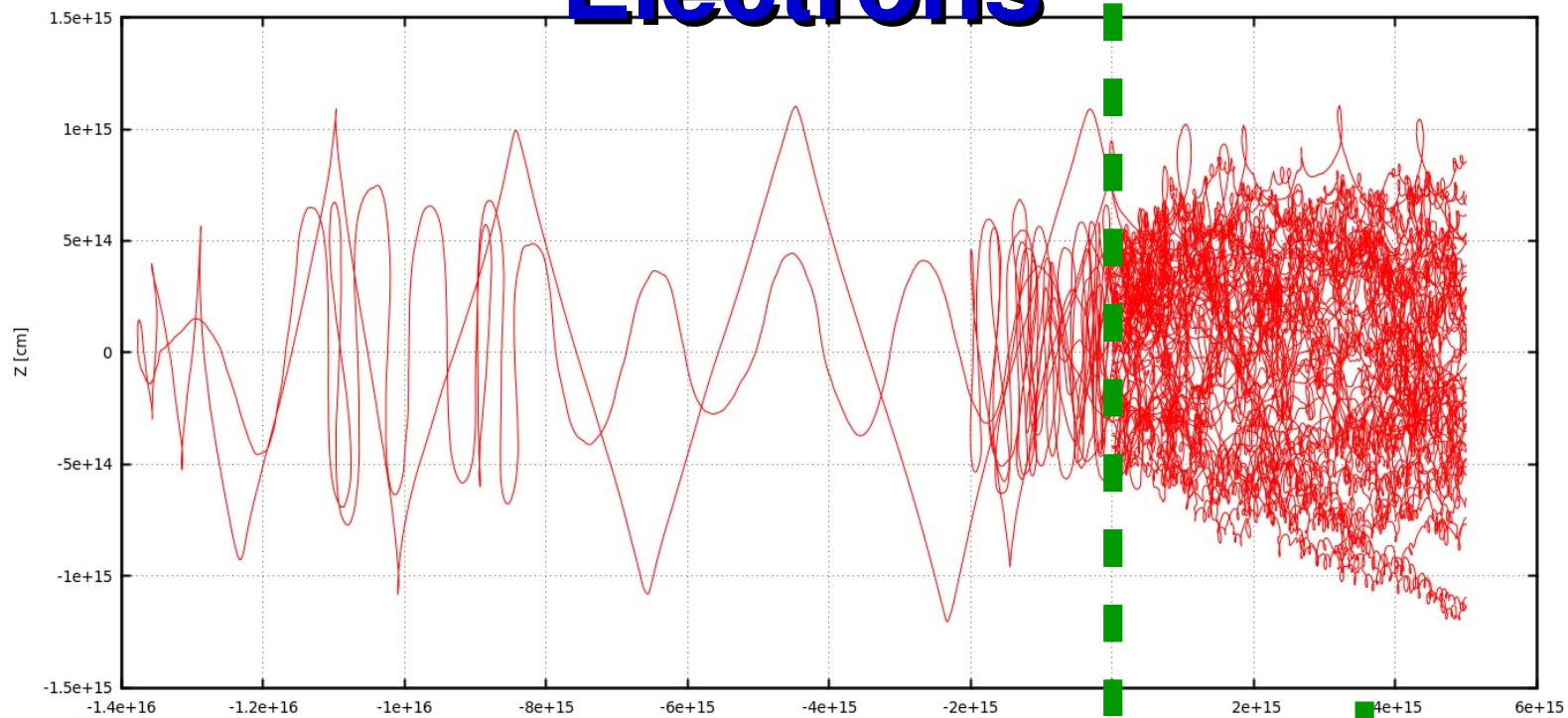
# Electrons



# Electro



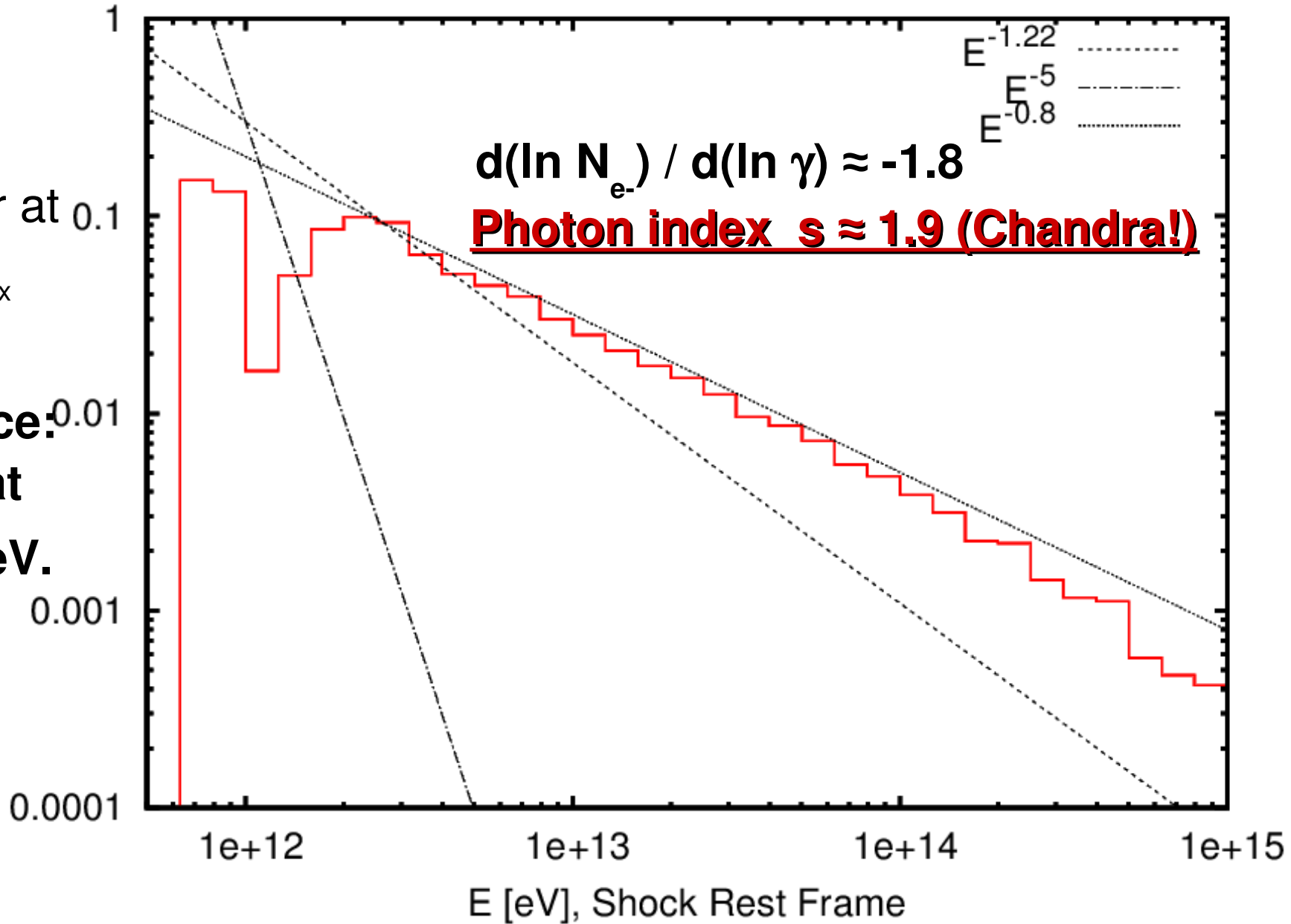
# Electrons





# Electrons

$\sim E \cdot dN/dE$



→ Turnover at 0.1  
high-E :  $L_{\max}$   
from turb.

→ **In practice:**  
 $t_{\text{synch}} \sim t_{\text{gyr}}$  at  
**E ~ 1-10 PeV.**

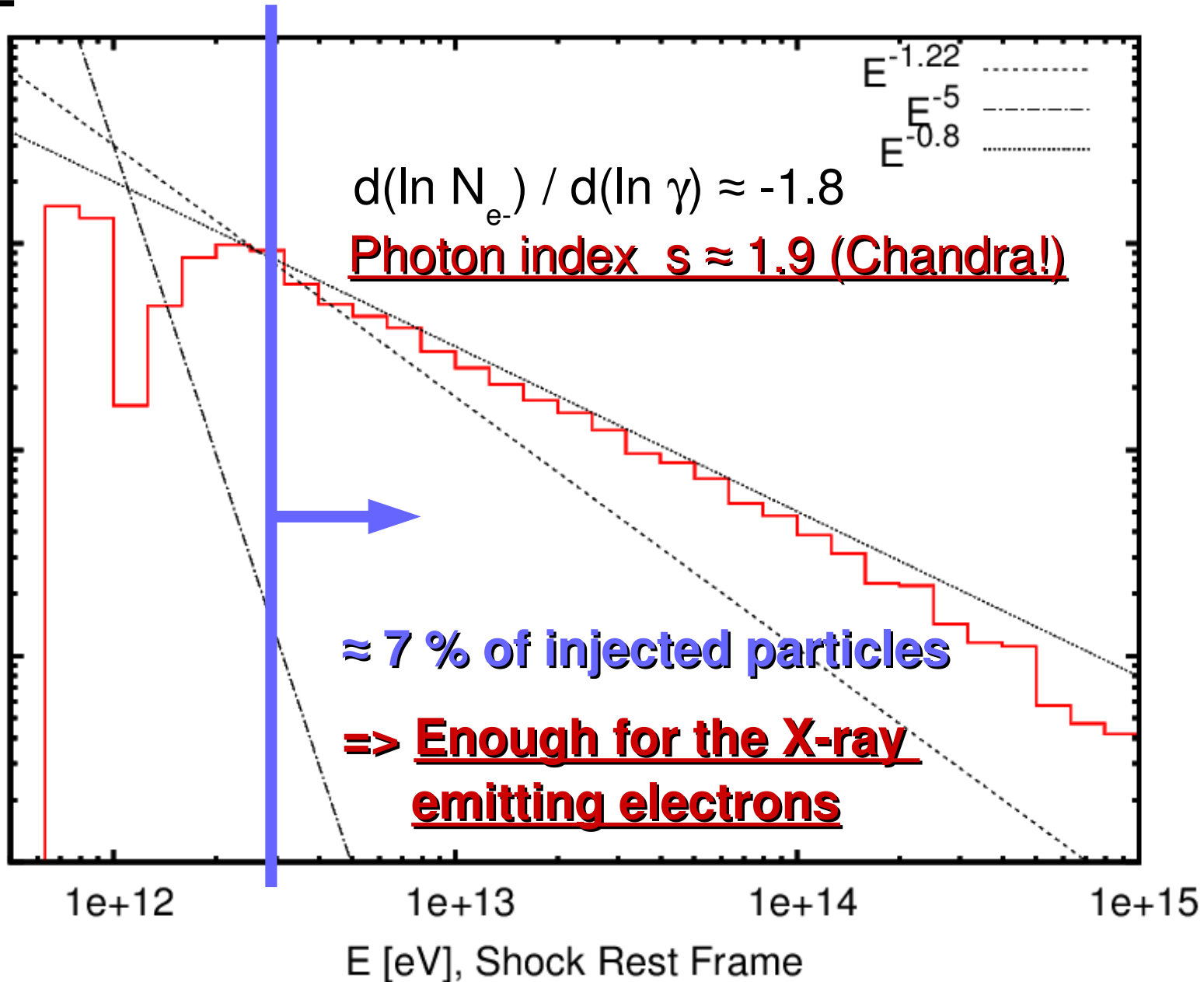
# Electrons

$\sim E \cdot dN/dE$

→ Turnover at 0.1  
high-E :  $L_{\max}$   
from turb.

→ In practice: 0.01  
 $t_{\text{synch}} \sim t_{\text{gyr}}$  at  
 $E \sim 1-10$  PeV.

→ **Outside**  
**this  $\pm 5\%$**   
**region :**  
**No/Very little**  
**acceleration.**



# Conclusions

- **X-ray emitting particles in the Crab Nebula can be accelerated at the termination shock by 1<sup>st</sup> order Fermi,**
- Grad B-drift does not help (particles advected after  $\sim 1$  cycle),
- On the contrary, **shock-drift helps: Multiple shock crossings, hard electron (or positron) spectrum,**
- Spectral hardening (photon index  $\sim -1.9$ ) results from the drift of  $e^-$  (or  $e^+$ ) along the shock and into the current sheet,

## **- - - > Chandra observations**

- Enough particles are accelerated to explain radio/X-ray obs.
- ( → Reconnection probably relevant only for radio electrons. )