

# Gravitational Wave Signals in Modified Cosmologies

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# Probing Non-Standard Cosmologies with the Stochastic GW Background

- What contributes to the stochastic GW background?
  - Astrophysical processes (e.g., BH & neutron star mergers)
  - Cosmology: inflation, cosmic strings, etc.
  - **GW are induced by curvature perturbations at second order!**

*K. Ananda, C. Clarkson, D. Wands, Phys.Rev.D 75 (2007) 123518*

- Key Questions:
  - What does this signal look like?
  - How does the cosmological history of the universe affect these?

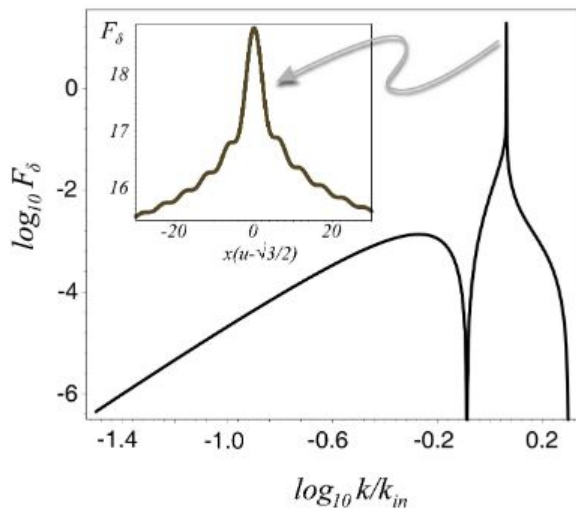


# Curvature-Induced Gravitational Waves

Why interesting? **Resonance-like enhancement!**

First pointed out in *K. Ananda, C. Clarkson, D. Wands, Phys Rev D 75 (2007) 123518*

Modified curvature power spectrum:  $\mathcal{P}_\zeta(k) \propto \delta(k - k_{\text{in}})$



Why? Oscillating gravitational potential  
 $\leftrightarrow$  oscillating sound wave  
resonantly produces GW

*Inomata et. al.*  
*Phys.Rev.D 101 (2020) 12,*  
*123533*

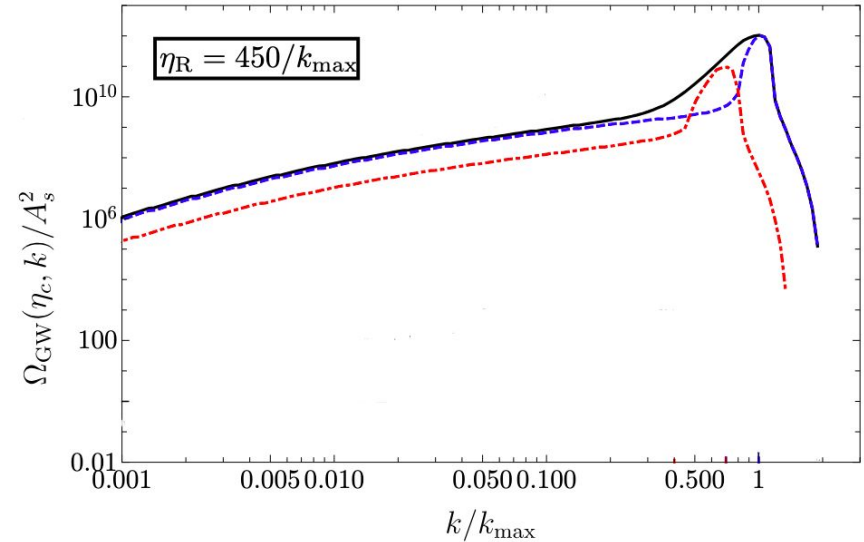
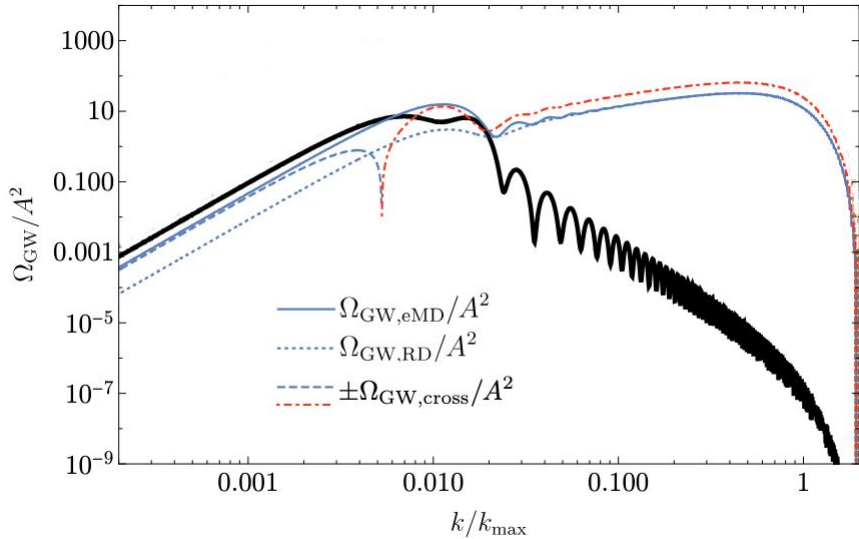
# Curvature-Induced Gravitational Waves

- Option 1: Modify  $\mathcal{P}_\zeta(k)$  like in Ananda et. al.  
(Will return to this later)
- Option 2: Use inflationary curvature spectrum-  
How does cosmological evolution affect it?
  - Consider an early matter dominated epoch



# Induced GW with Early Matter Dominated Epoch

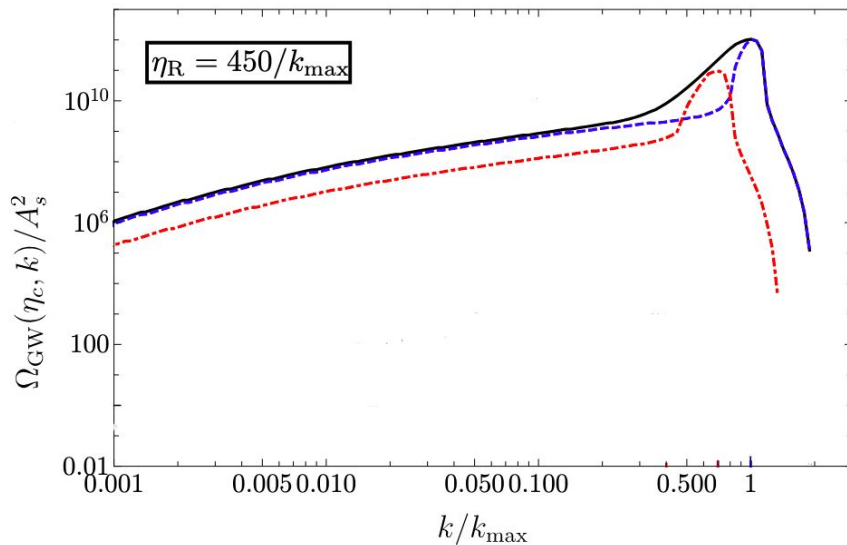
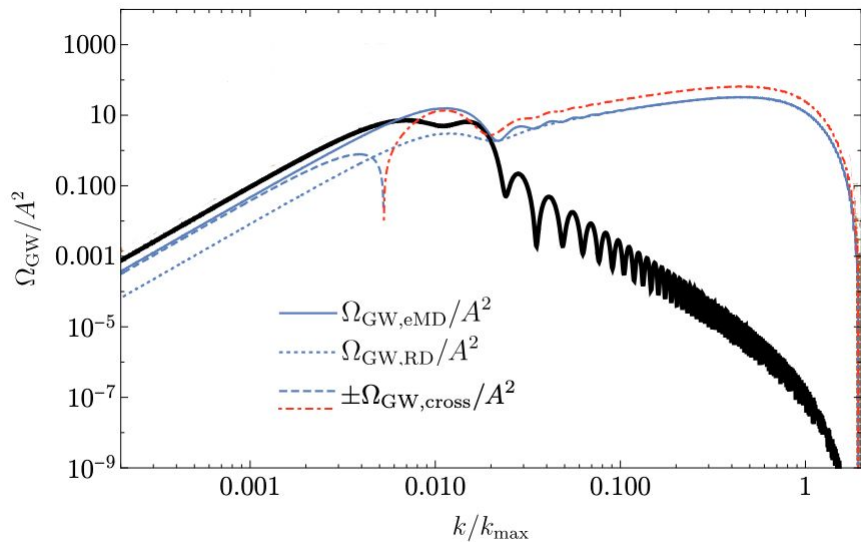
Depends sensitively on how the eMD epoch **ENDS**



Left: Slow end-signal is suppressed because of a cancellation between modes that enter in MD & RD

# Induced GW with Early Matter Dominated Epoch

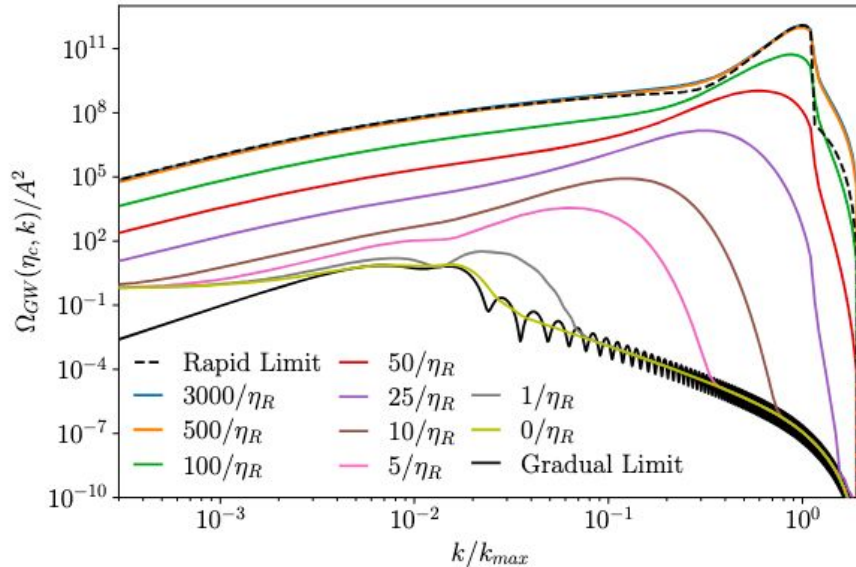
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Right: Instantaneous end-Resonance-like enhancement!

# This Resonance...

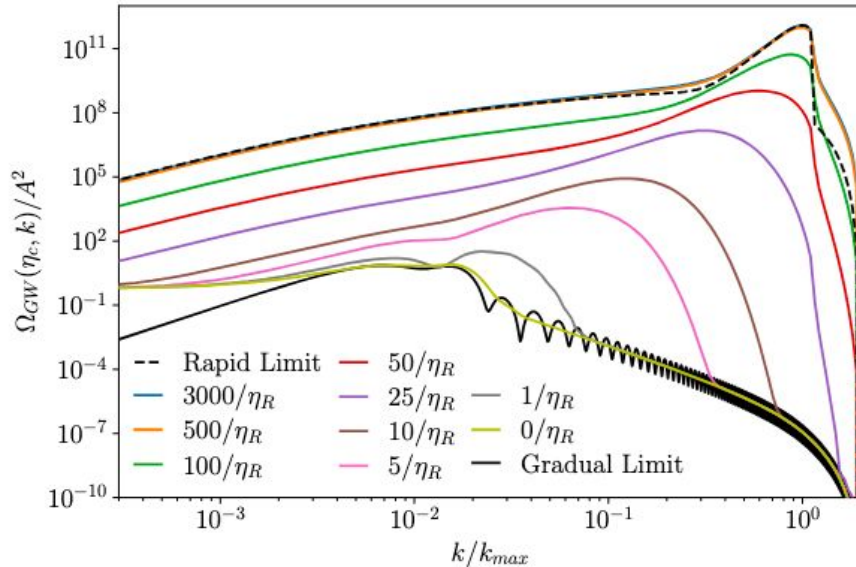
- My question:  
Instantaneous  $\rightarrow$  infinite slope  $\rightarrow$  signal depends on  $\Phi'$   
How sure are we that this is real???



Used tanh profile for matter decay rate  
*M. Pearce, L. Pearce, G. White, C. Balazs,*  
*JCAP 06 (2024) 021*

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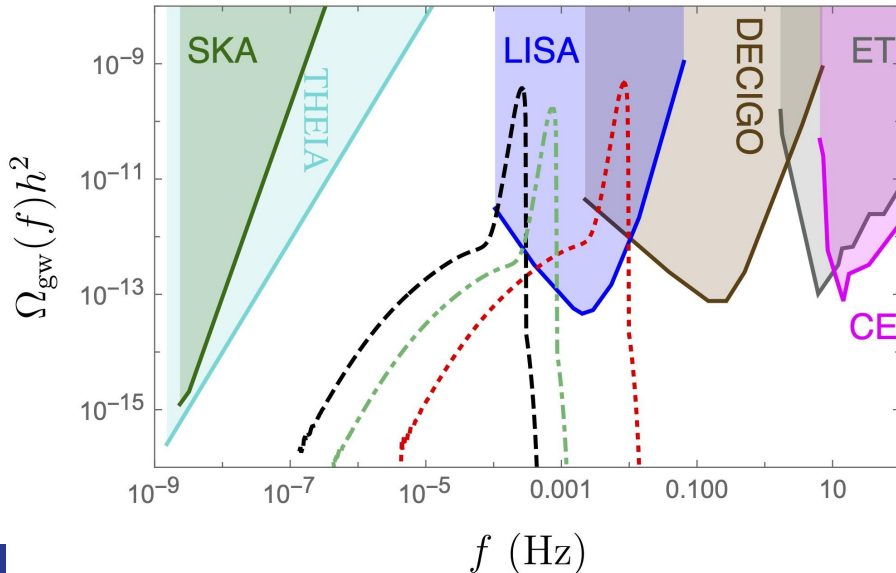
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Cause: Sudden decay leads to oscillating  
sound waves in radiation bath  
Resonantly produce GW  
*K. Inomata et. al.*  
*Phy.Rev.D 101 (2020) 12, 123533*



# How Can We Get a “Fast” Phase Transition?

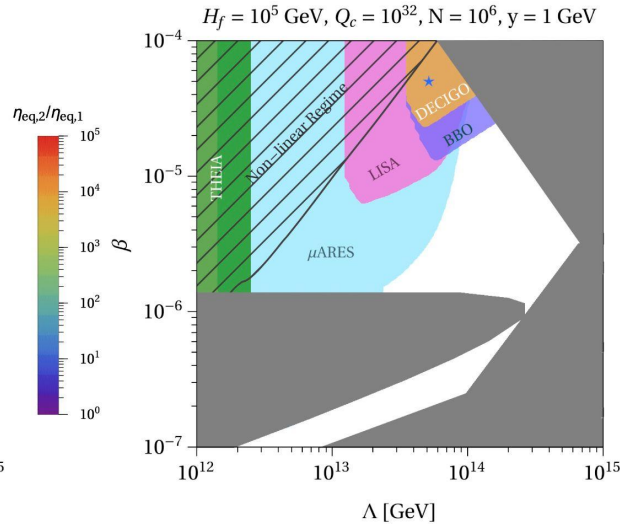
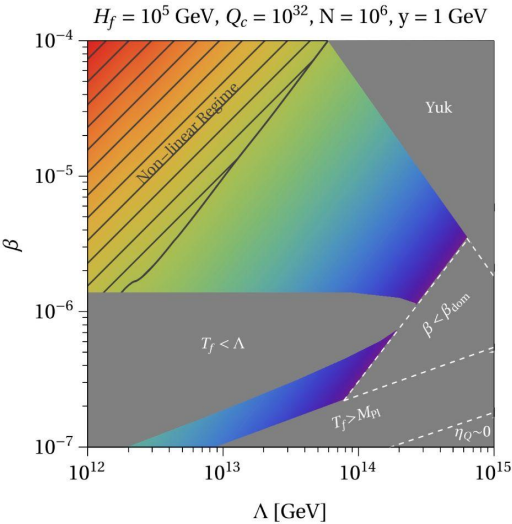
- Need heavy objects whose decays speed up:
  - PBHs: *K. Inomata et. al. Phys.Rev.D 101 (2020) 12, 123533*
  - Q-balls: *G. White., L. Pearce, D. Vagie, A. Kusenko PRL 127 (2021) 18, 181601*



Temp scales: eMD starts around  $10^4$  GeV, ends around  $10^2$  GeV.

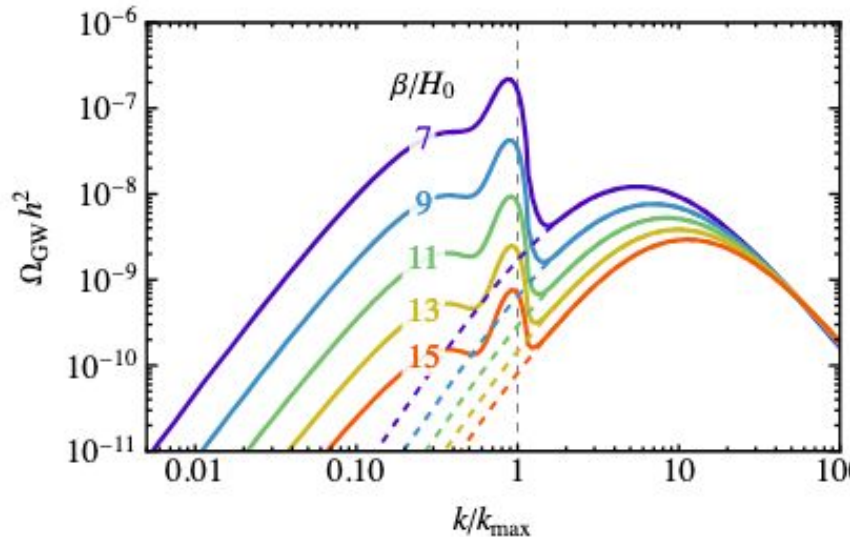
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  - Q-balls: *G. White., L. Pearce, D. Vagie, A. Kusenko PRL 127 (2021) 18, 181601*
    - Can be embedded in e.g., high scale SUSY  
*M. Flores et. al. Phys.Rev.D 108 (2023) 12, 123002*



# What About Modifying Curvature Power Spectrum?

- Need to modify curvature power spectrum on superhorizon scales
- Phase transitions give  $\mathcal{P}_\zeta \propto k^3$ 
  - *M. Lewicki, P. Toczek, and V. Vaskonen, arXiv:2402.04158*

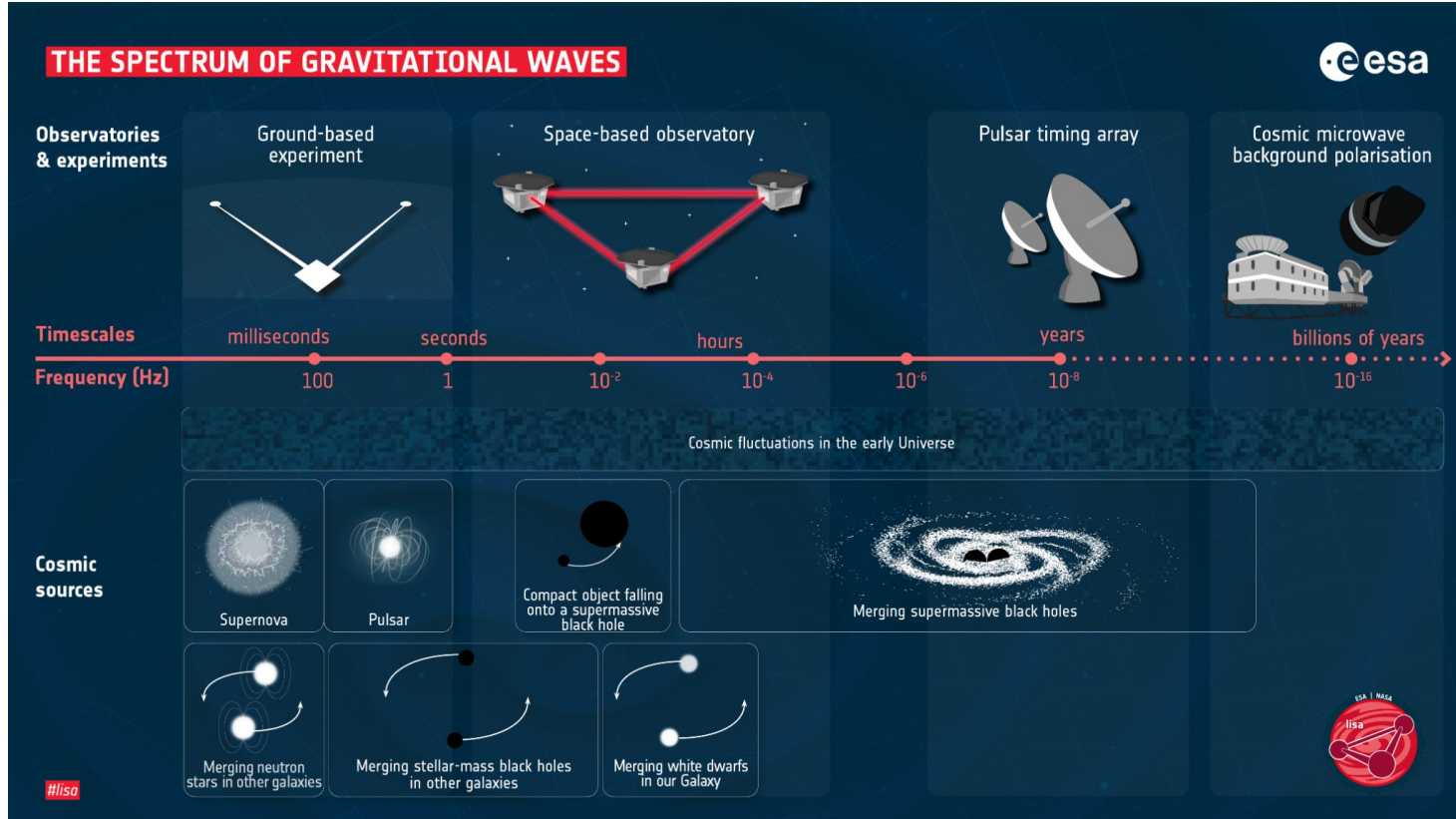


# What Else?

- Work has also been done with kination instead of early matter domination
  - *G. Domenech, S. Pi, M. Sasaki, JCAP 08 (2020) 017*
- Connects to pulsar timing arrays
  - *E.g., K. Harigaya, K. Inomata, T. Terada Phys Rev D 108 (2023) 12, 123538*



# Landscape of GW Observations




# Stochastic GW Background (low frequency)

## Sources:

- Population of unresolved supermassive black hole binaries
- Early Universe physics (e.g., inflation, phase transitions, topological defects, enhanced scalar perturbations)

## Observations:

- Current: evidence from pulsar timing array (PTA) experiments
  - Upcoming: LISA will probe higher frequencies
- 

# PTAs

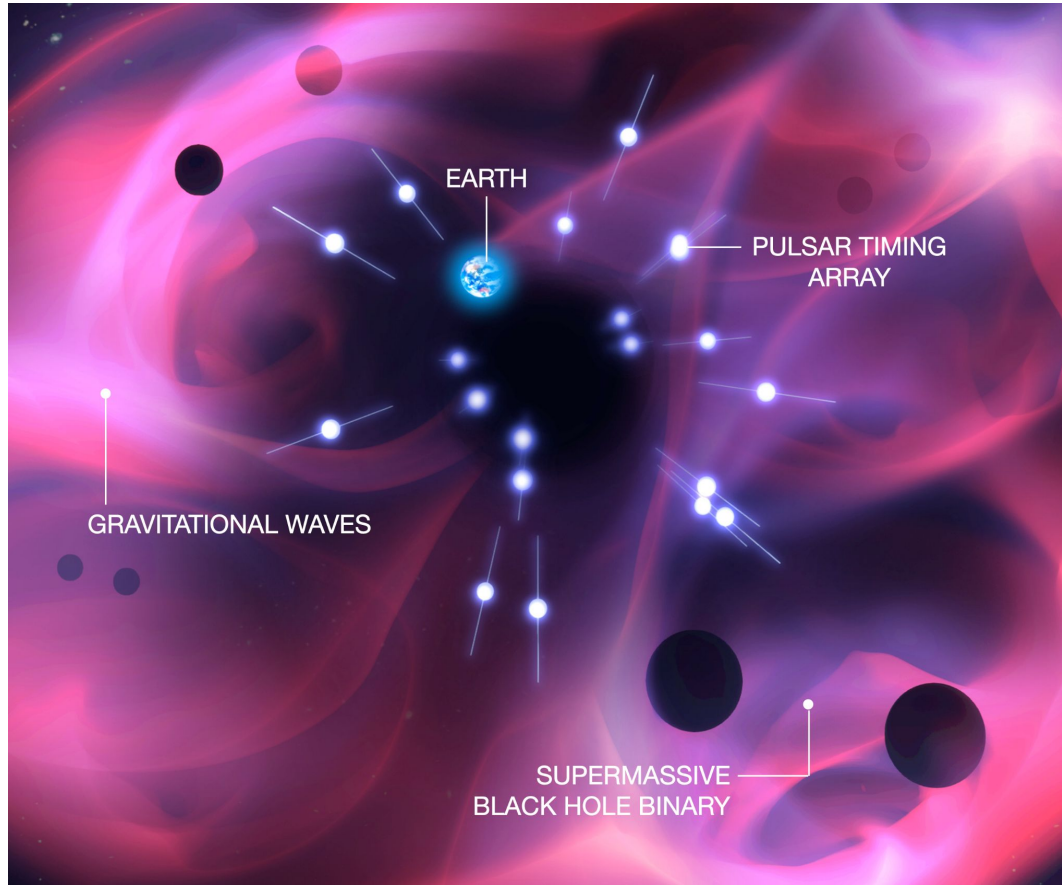
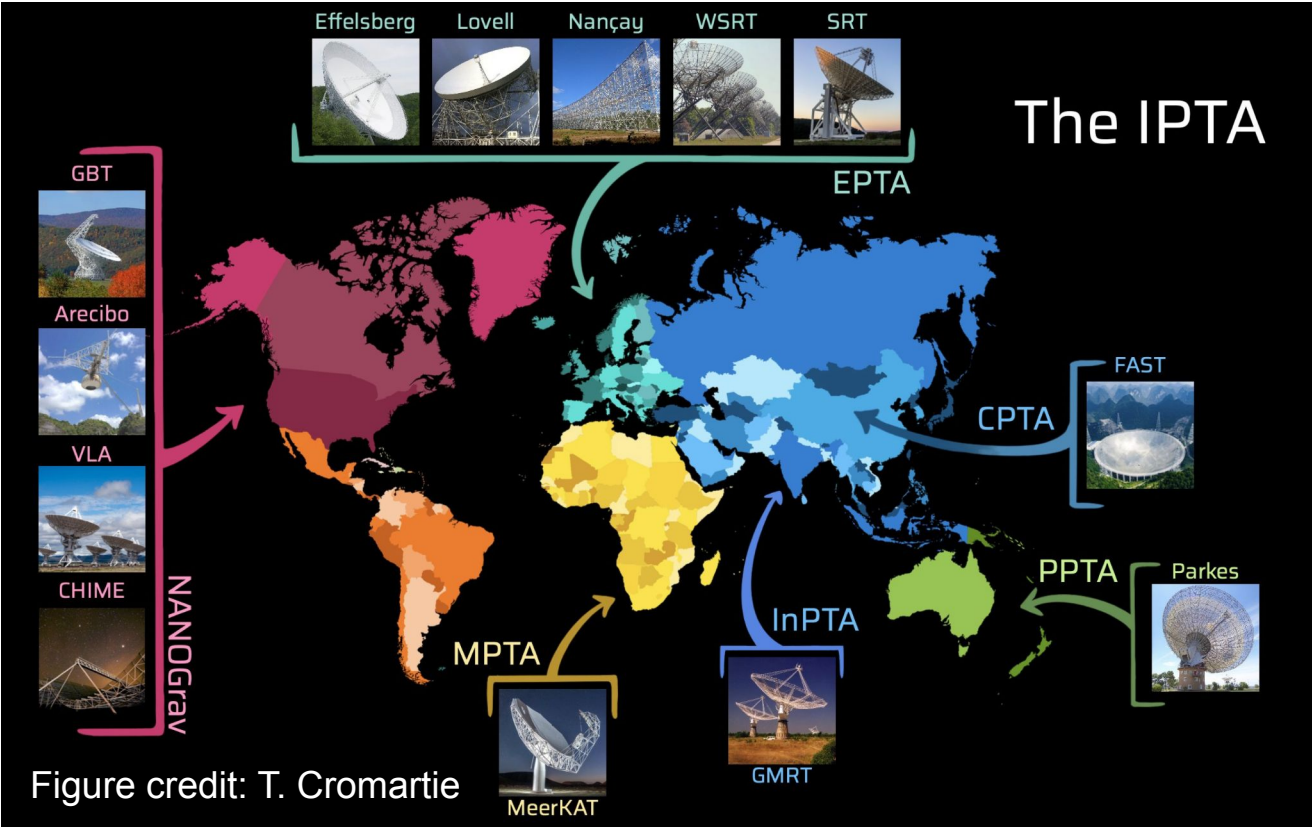


Figure credit: Andreas Freise

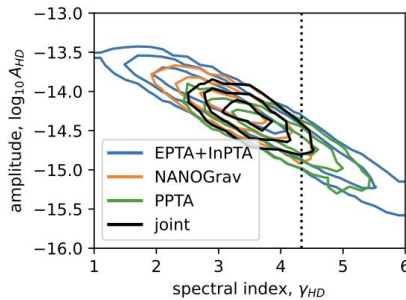
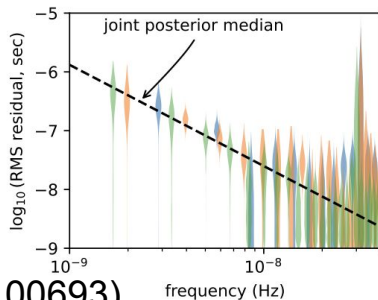
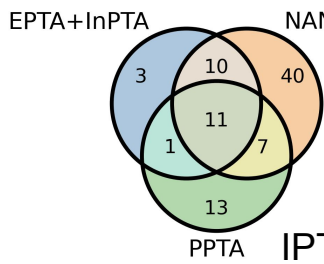
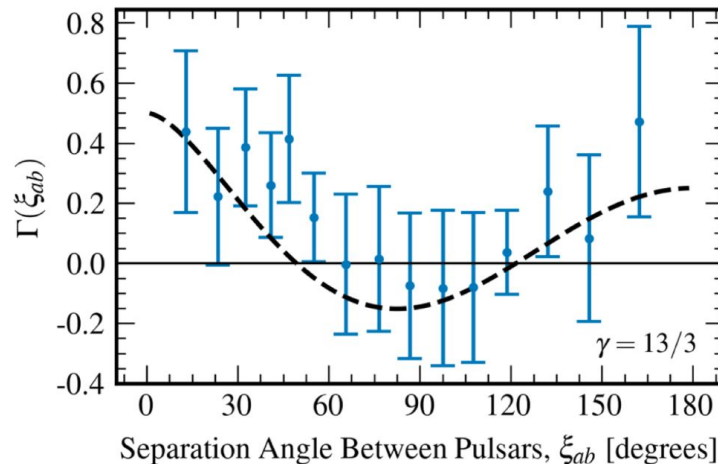
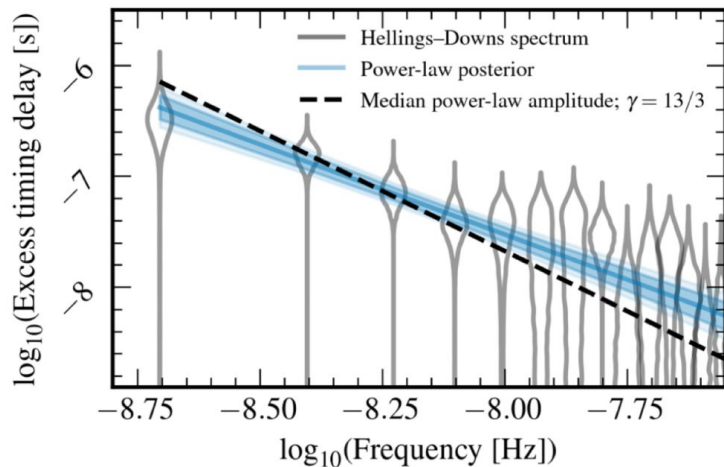
# PTA Experiments



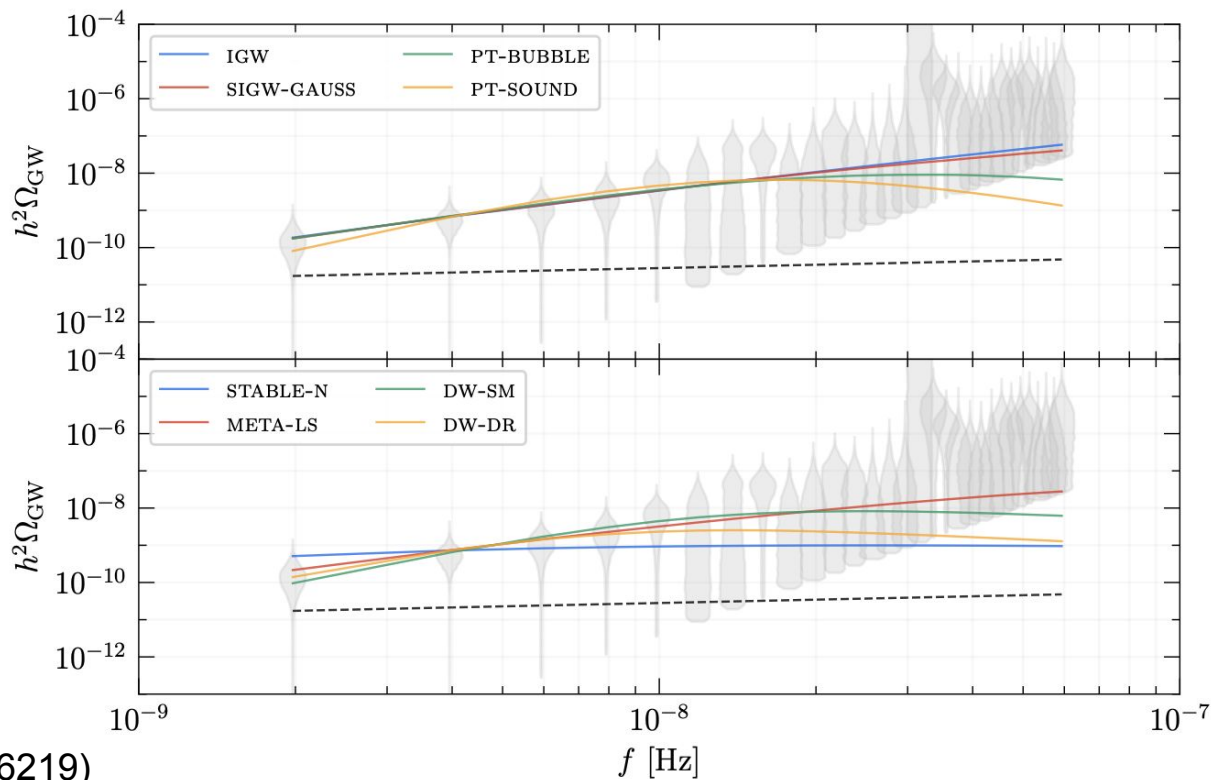


# Evidence for SGWB

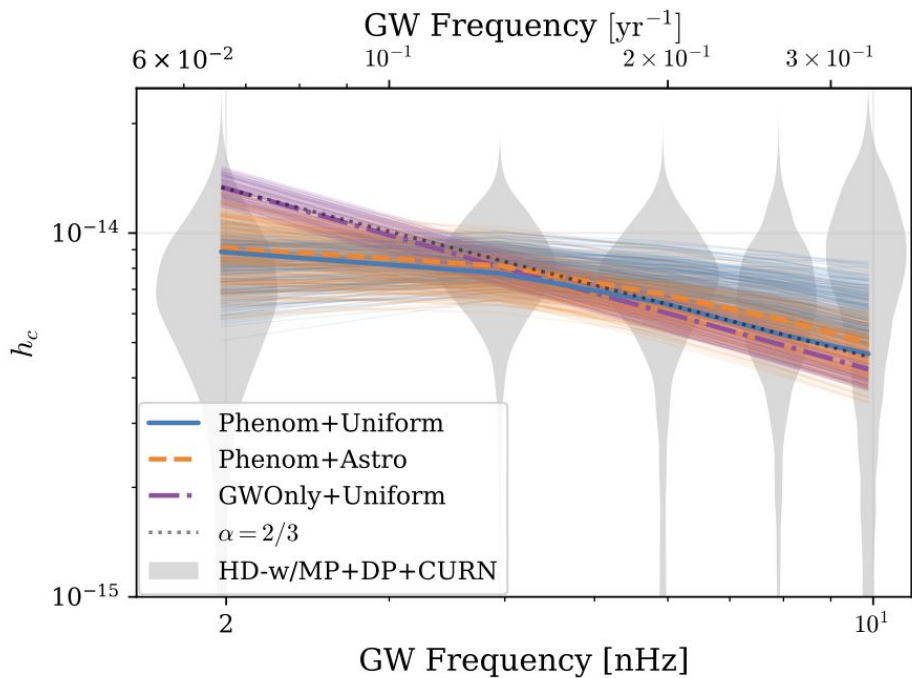
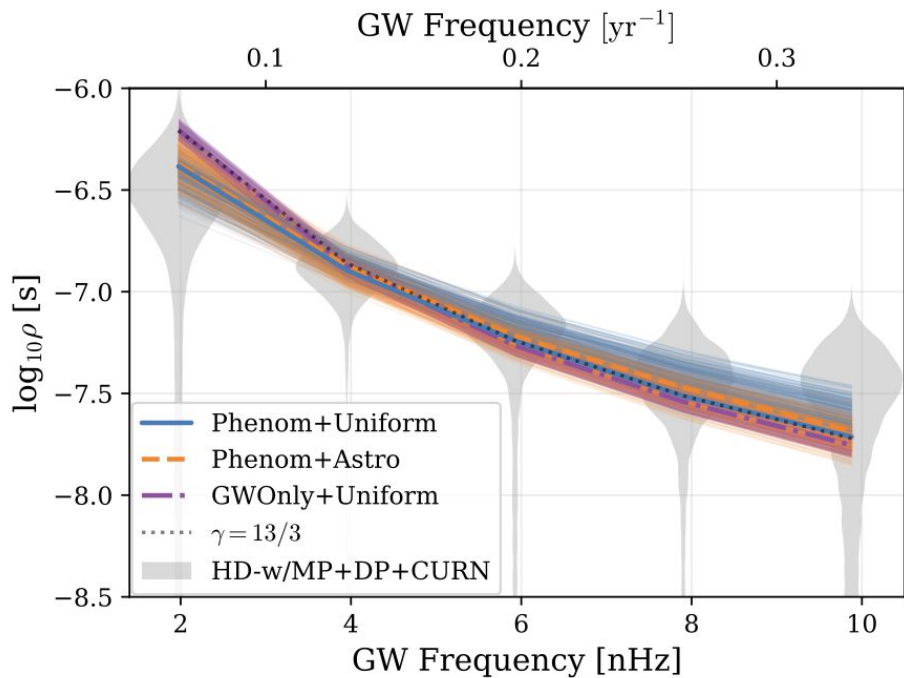
NANOGrav (2306.16213)



# New-Physics Interpretation



# Astrophysics interpretation





Discuss!

# Back-Up Slides (Lauren)



# Formalism (1)

Conformal Newtonian Gauge (using conformal time  $\eta$ ):

$$ds^2 = -a^2 (1 + 2\Phi) d\eta^2 + a^2 \left( (1 - 2\Psi) \delta_{ij} + \frac{1}{2} h_{ij} \right) dx^i dx^j$$

Fourier components of tensor modes satisfy equation of motion:

$$h''_{\vec{k}}(\eta) + 2\mathcal{H}h'_{\vec{k}}(\eta) + k^2 h_{\vec{k}}(\eta) = 4S_{\vec{k}}(\eta)$$

with the source expressed in terms of the gravitational potential:

$$S_{\vec{k}} = \int \frac{d^3q}{(2\pi)^{3/2}} e_{ij}(\vec{k}) q_i q_j \left( 2\Phi_{\vec{q}} \Phi_{\vec{k}-\vec{q}} + \frac{4}{3(1+w)} (\mathcal{H}^{-1} \Phi'_{\vec{q}} + \Phi_{\vec{q}}) (\mathcal{H}^{-1} \Phi'_{\vec{k}-\vec{q}} + \Phi_{\vec{k}-\vec{q}}) \right)$$

GWs are a **second order** effect

## Formalism (2)

Solve via Green's function approach:  $a(\eta)h_{\vec{k}}(\eta) = 4 \int^{\eta} d\bar{\eta} G_{\vec{k}}(\eta, \bar{\eta})a(\bar{\eta})S_{\vec{k}}(\bar{\eta})$

Green's function solves:  $G_{\vec{k}}''(\eta, \bar{\eta}) + \left(k^2 - \frac{a''(\eta)}{a(\eta)}\right) G_{\vec{k}}(\eta, \bar{\eta}) = \delta(\eta - \bar{\eta})$

Gravitational potential obeys:  $\Phi_{\vec{k}}''(\eta) + \frac{6(1+w)}{(1+3w)\eta} \Phi_{\vec{k}}'(\eta) + wk^2 \Phi_{\vec{k}}(\eta) = 0$

Express in terms of transfer function  $\Phi_{\vec{k}} = \Phi(k\eta)\phi_{\vec{k}}$

which is normalized to 1 at early times and

$$\langle \phi_{\vec{k}} \phi_{\vec{k}'} \rangle = \delta(\vec{k} + \vec{k}') \cdot \frac{2\pi^2}{k^3} \left( \frac{3+3w}{5+3w} \right)^2 \mathcal{P}_{\zeta}(k)$$

## Formalism (3)

Putting it all together, the GW power spectrum is:

$$\mathcal{P}_h(\eta, k) = 4 \int_0^\infty dv \int_{|1-v|}^{1+v} du \left( \frac{4v^2 - (1 + v^2 - u^2)^2}{4vu} \right)^2 I^2(v, u, x) \mathcal{P}_\zeta(kv) \mathcal{P}_\zeta(ku)$$

where  $I(v, u, x) = \int_0^x d\bar{x} \frac{a(\bar{\eta})}{a(\eta)} k G_k(\eta, \bar{\eta}) f(v, u, \bar{x})$

and the source is

$$f(v, u, \bar{x}) = \frac{6(w+1)}{3w+5} \Phi(v\bar{x}) \Phi(u\bar{x}) + \frac{6(1+3w)(w+1)}{(3w+5)^2} (\bar{x} \partial_{\bar{\eta}} \Phi(v\bar{x}) \Phi(u\bar{x}) + \bar{x} \partial_{\bar{\eta}} \Phi(u\bar{x}) \Phi(v\bar{x})) \\ + \frac{3(1+3w)^2(1+w)}{(3w+5)^2} \bar{x}^2 \partial_{\bar{\eta}} \Phi(v\bar{x}) \partial_{\bar{\eta}} \Phi(u\bar{x})$$