

# Inclusive Higgs Rate with Forward Detection at High Energy Muon Collider

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- Inclusive Higgs rate from ZZ fusion ( $\sqrt{s} = 10 \text{ TeV}$ )
  - Motivation
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- Conclusion

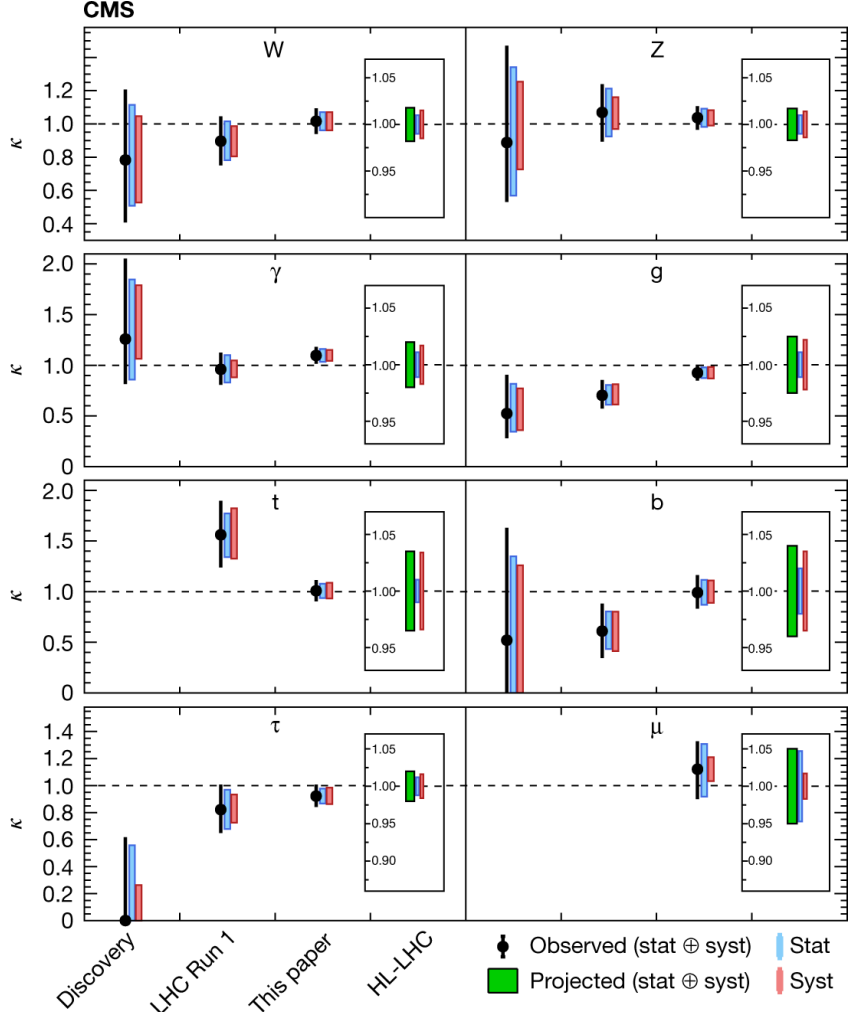
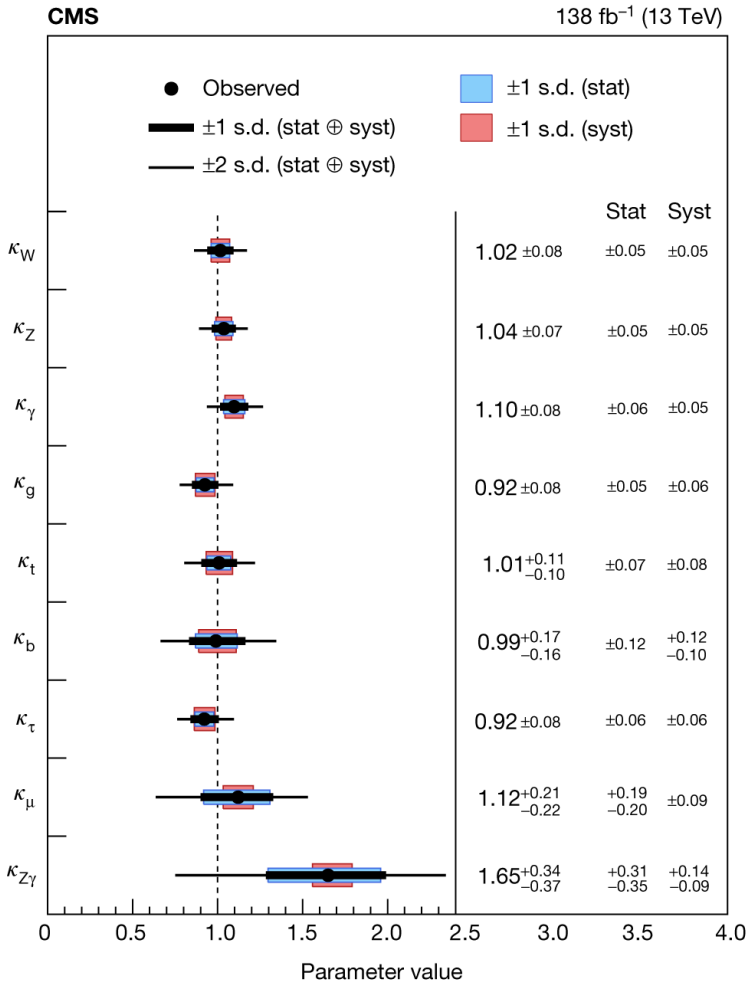
# Motivation

Nature volume 607, 60–68 (2022)

Higgs boson has been discovered over ten years ago.

Higgs is still the central player of many mysteries and puzzles.

We need to have deeper understanding of the Higgs properties.



Currently we can measure the higgs coupling to above 5%

# Measurements to be interpreted

Observables at the colliders are the cross sections, a convolution of PDF, hard scattering, parton shower, detector response ...

$$\kappa_i = \frac{g_i}{g_i^{\text{SM}}}, \kappa_\Gamma = \frac{\Gamma_{\text{tot}}}{\Gamma_{\text{tot}}^{\text{SM}}}$$

For the hard scattering under the narrow width approximation:

$$\sigma(a \rightarrow H \rightarrow b) \propto \frac{\Gamma_a \Gamma_b}{\Gamma_{\text{tot}}} \propto \frac{\kappa_a^2 \kappa_b^2}{\kappa_\Gamma} = \mu_a^b \quad \kappa_\Gamma = \frac{\sum_i \kappa_i^2 \text{Br}_{i,\text{SM}}}{1 - \text{Br}_{\text{exo}}}$$

All onshell channels can be parametrized this way, simple extension possible for more channels/observables.

# Higgs Fit Degeneracy

Under the rescaling  $\kappa_{a/b} \rightarrow t \kappa_{a/b}$ ,  
 $\mu_a^b$  would be invariant if  $\kappa_\Gamma \rightarrow t^4 \kappa_\Gamma$

- For  $t < 1$

$$t^4 \kappa_\Gamma = \frac{\sum_i \kappa_i^2 \text{Br}_{i,\text{SM}}}{1 - \text{Br}_{\text{exo}}} \quad \begin{matrix} t^2 \\ t^{-2} \end{matrix}$$

No exotic branching ratio can satisfy, so degeneracy is broken

- For  $t > 1$

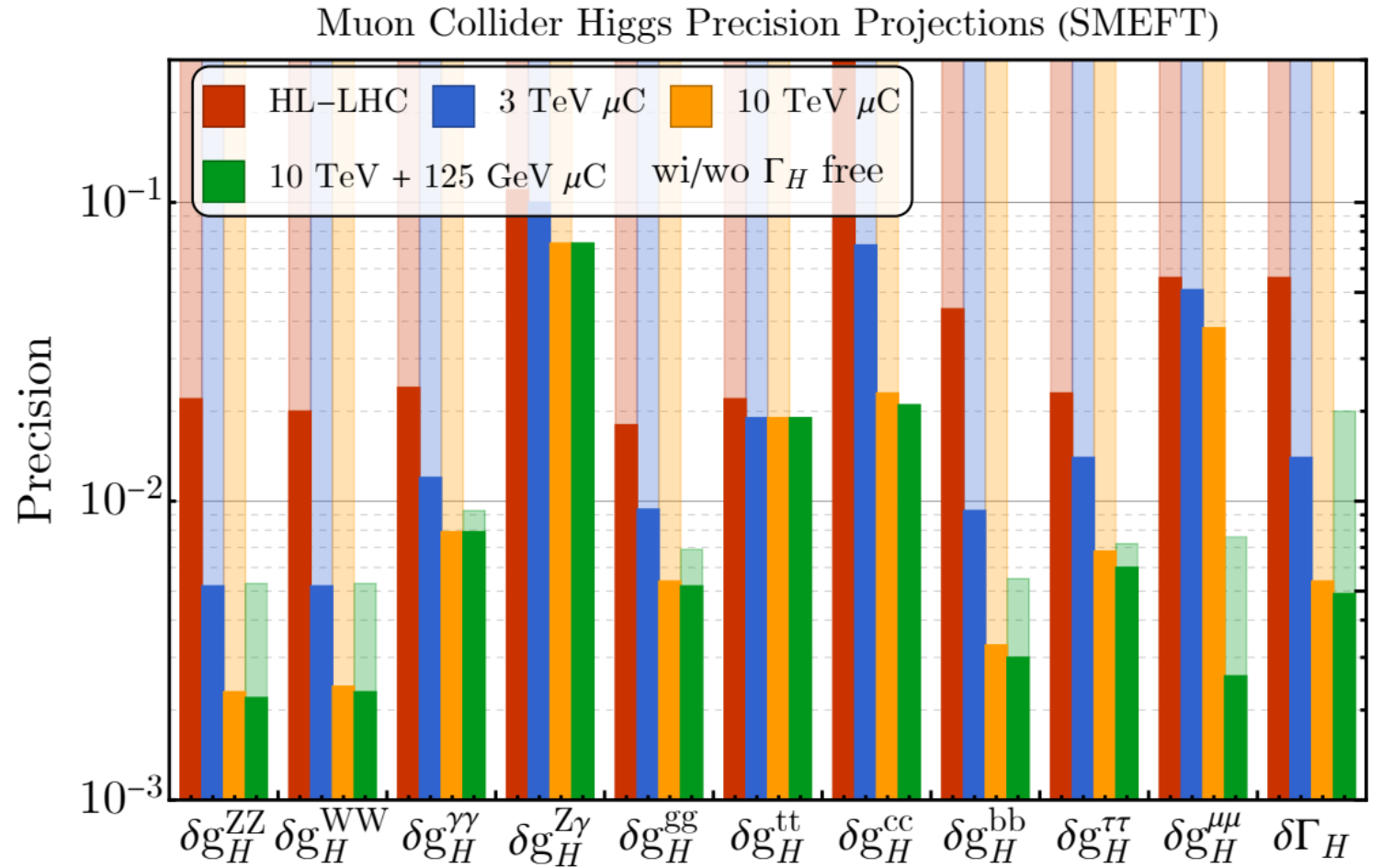
$$t^4 \kappa_\Gamma = \frac{\sum_i \kappa_i^2 \text{Br}_{i,\text{SM}}}{1 - \text{Br}_{\text{exo}}} \quad \begin{matrix} t^2 \\ t^{-2} \end{matrix}$$

Certain exotic branching ratio can always satisfy, we cannot break the degeneracy.

People typically assume  $|\kappa_V| < 1$  or  $\text{Br}_{\text{exo}} = 0$  which means  $\kappa_\Gamma$  is not a free parameter

We need to introduce new types of observables. One possibility is just  $\kappa_V^2$  from the inclusive measurement.

- Previous Higgs studies, at 3/10 TeV MuC alone do not have constraint on Higgs total width.
- Our study will be directly sensitive to  $g_H^{ZZ}$ . Combining with other channels will be able to constraint  $\Gamma_H$



[2209.01318] Muon Collider Forum Report

# Inclusive Higgs rate from ZZ fusion ( $\sqrt{s} = 10 \text{ TeV}$ )

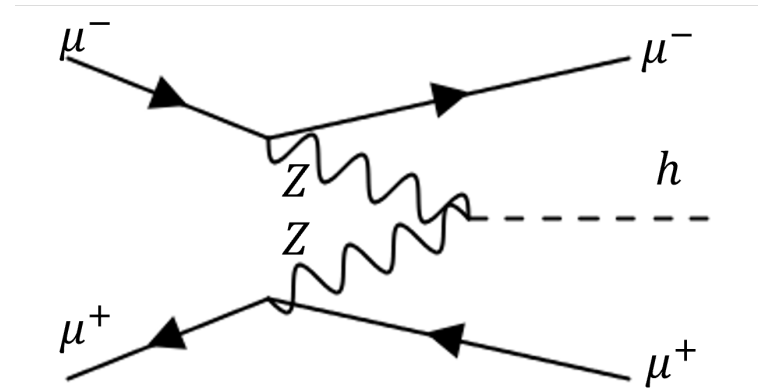
Forward muon detector:  $2.5 < \eta(\mu) < 4, 6, 8$

Ultra-energetic muons would penetrate the shielding nozzles

$$p_h = (\sqrt{s}, 0, 0, 0) - p_{\mu^+} - p_{\mu^-}$$

$$m_h^2 = [(\sqrt{s}, 0, 0, 0) - p_{\mu^+} - p_{\mu^-}]^2$$

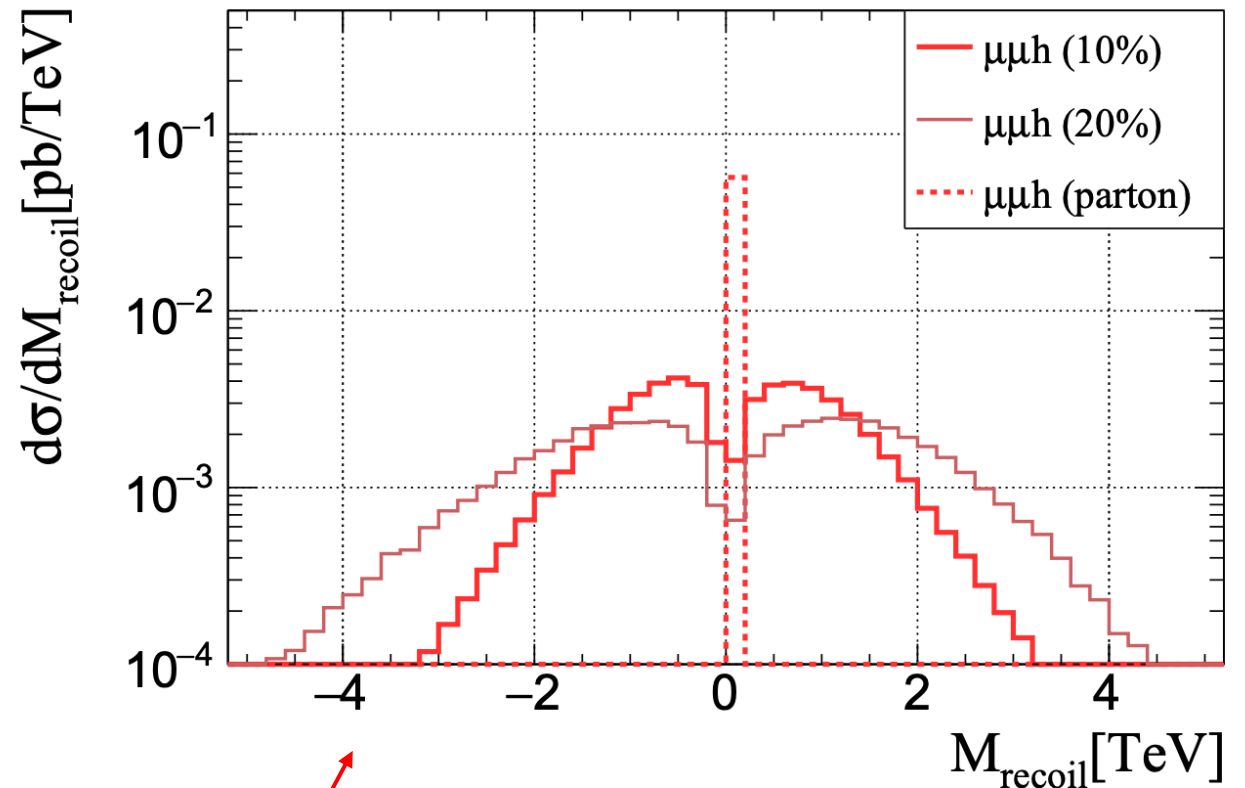
Recoil mass of dimuon



**Does not rely on the detection of Higgs decay product.**

# Inclusive Higgs rate from ZZ fusion ( $\sqrt{s} = 10$ TeV)

Due to the uncertainty of high energy measurement, the smearing effect will distort the recoil mass distribution.



Fast detector simulation using Delphes.

$$[(\sqrt{s}, 0, 0, 0) - p_{\mu^+} - p_{\mu^-}]^2 < 0$$



# Signal vs. Background ( $\sqrt{s} = 10 \text{ TeV}$ )

## Only tag 2 forward muons

Do not have any requirements on other detection.

Type	Scattering process	cross section $\sigma$ (pb)
VBF	$\mu^+\mu^- \rightarrow \mu^+\mu^-h$	0.0867
<i>t</i> -channel	$\mu^+\mu^- \rightarrow \mu^+\mu^-$	$1.12 \times 10^4$
<i>t</i> -channel	$\mu^+\mu^- \rightarrow \mu^+\mu^-\gamma$	754.8
VBS	$\mu^+\mu^- \rightarrow \mu^+\mu^-\ell^+\ell^-$	3.96
VBS	$\mu^+\mu^- \rightarrow \mu^+\mu^-jj$	2.06
VBS	$\mu^+\mu^- \rightarrow \mu^+\mu^-\nu_\ell\bar{\nu}_\ell$	1.68
VBS	$\mu^+\mu^- \rightarrow \mu^+\mu^-W^+W^-$	0.939

Cross section for both signal and background after parton-level pre-selection.

Pre-selection at parton-level:

$$p_T(l, j) > 5 \text{ GeV},$$

$$p_T(\gamma) > 1 \text{ GeV},$$

$$|\eta(l)| < 10,$$

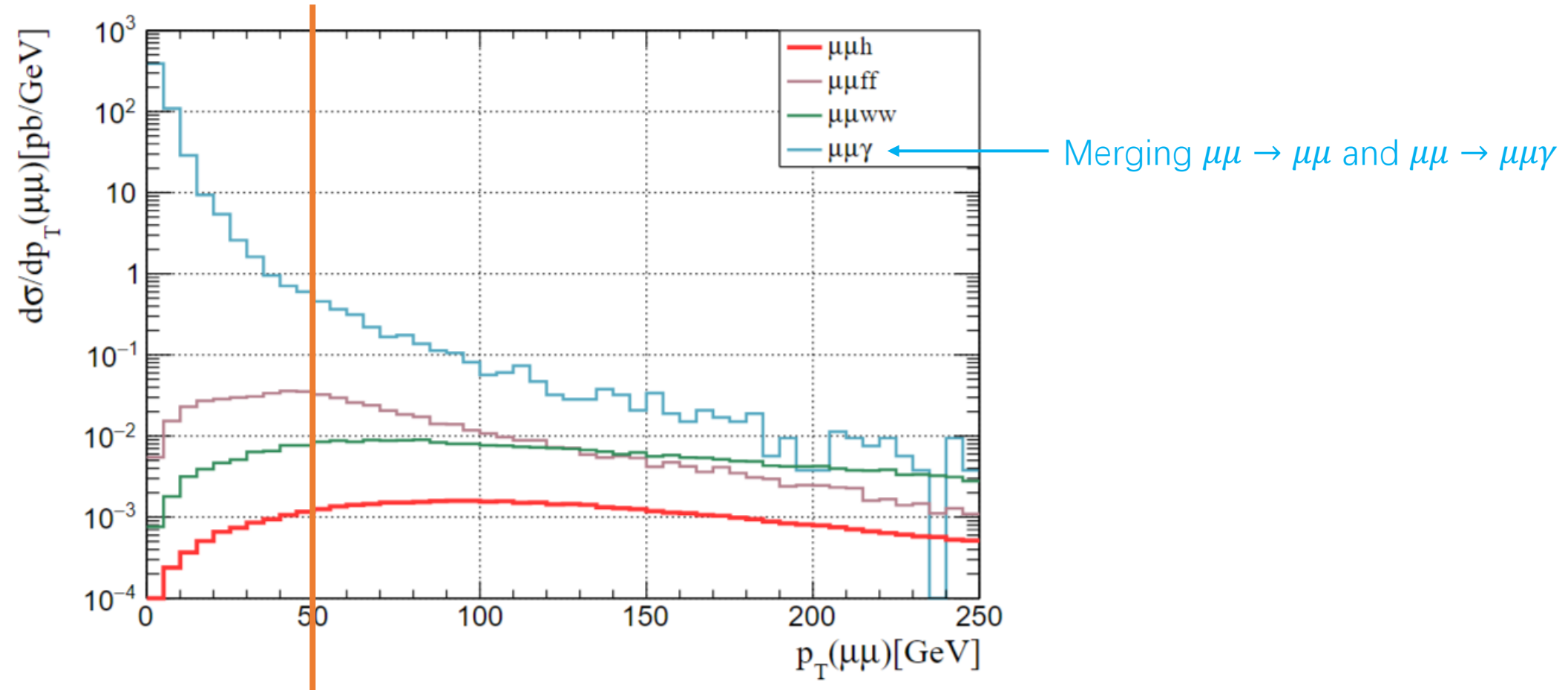
$$\Delta R(ll, lj, jj) > 0.2$$

3 types of background

- $\mu\mu \rightarrow \mu\mu(\gamma)$
- $\mu\mu \rightarrow \mu\mu + ff$
- $\mu\mu \rightarrow \mu\mu + WW$

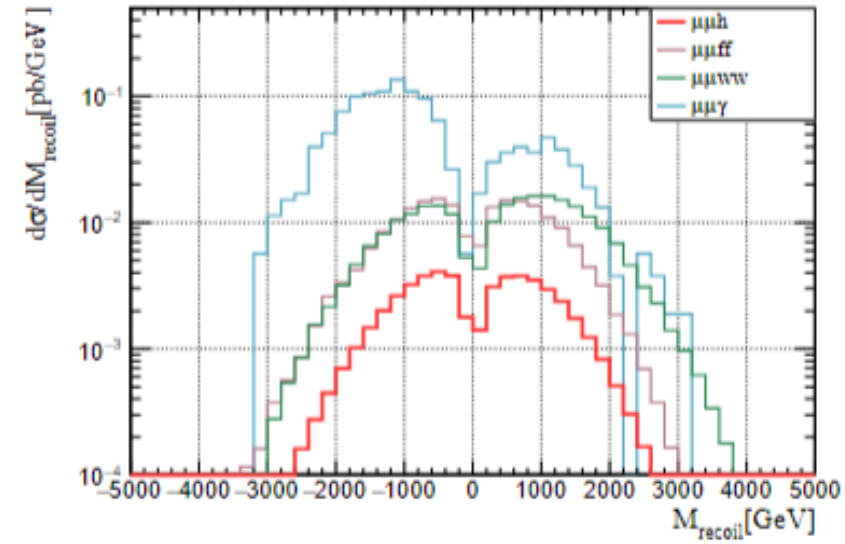
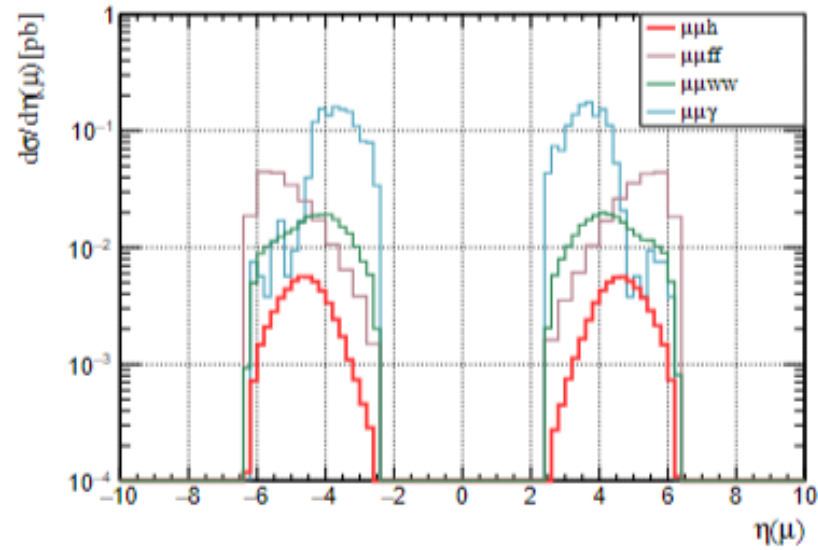
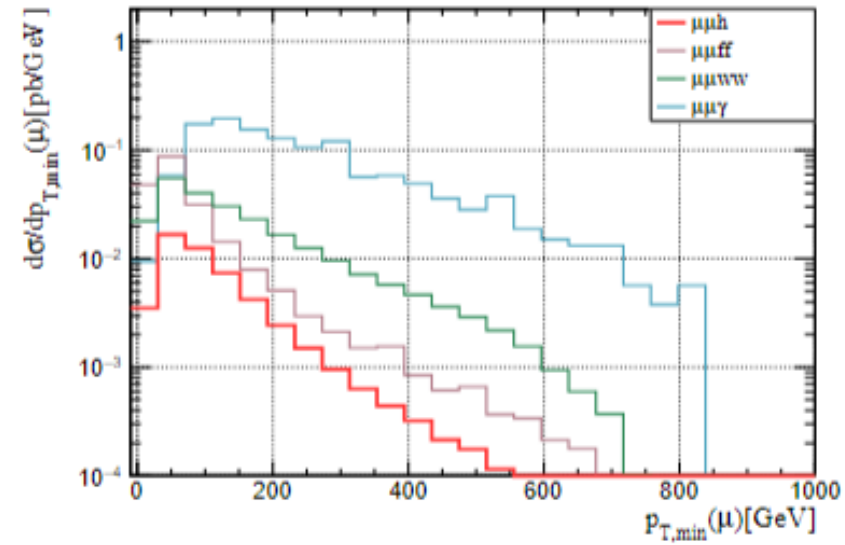
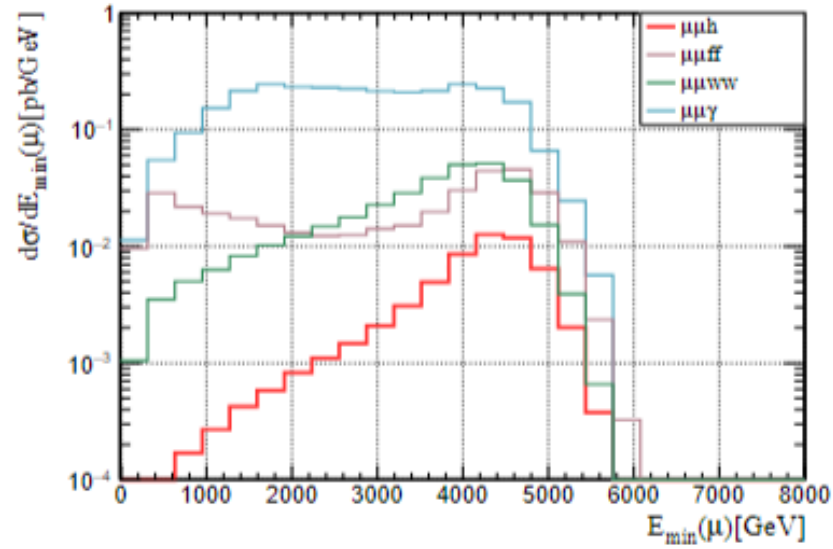
# Signal vs. Background ( $\sqrt{s} = 10 \text{ TeV}$ )

Require  $p_T(\mu\mu) > 50 \text{ GeV}$



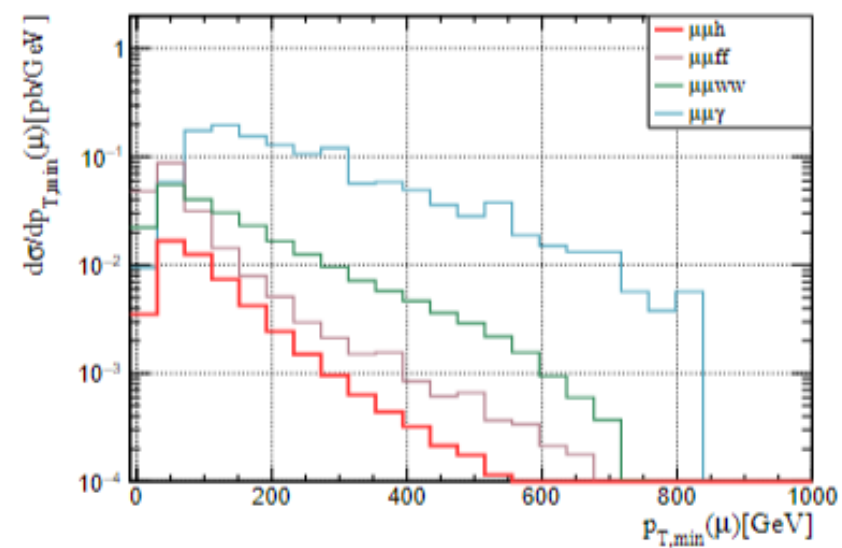
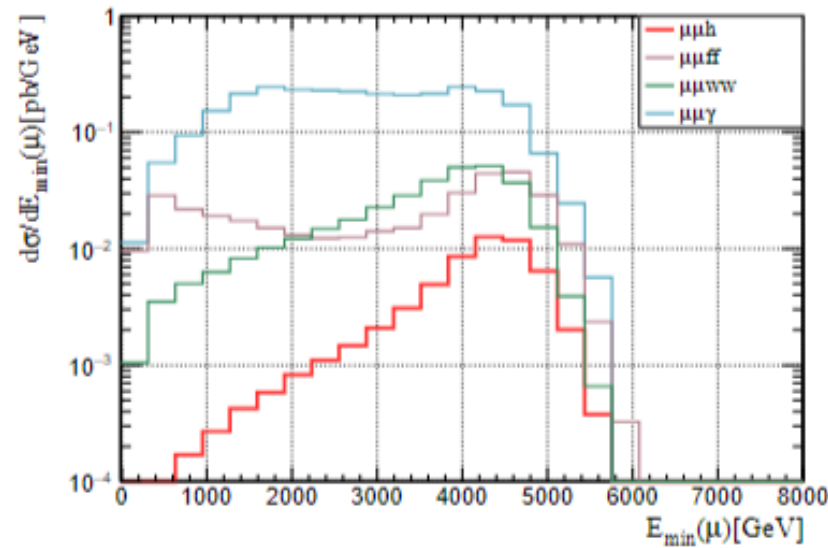
# Cutflow analysis

Checking other kinematics and applying a few cuts.



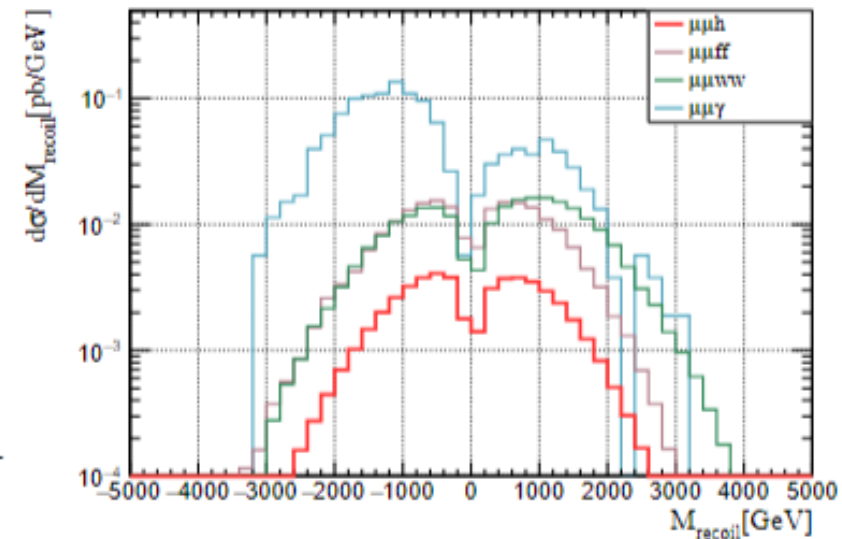
# Cutflow analysis

Checking other kinematics and applying a few cuts.



Process	Pre-selection	$p_T(\mu\mu) > 50$ GeV	$E(\mu) > 3000$ GeV & $p_{T,min}(\mu) < 300$ GeV
$\mu^+\mu^- \rightarrow \mu^+\mu^-h$	73.3%	65.7%	56.4% (0.0489 pb)
$\mu^+\mu^- \rightarrow \mu^+\mu^-\gamma$	13.1%	0.38%	0.12% (0.906 pb)
$\mu^+\mu^- \rightarrow \mu^+\mu^-f\bar{f}$	8.13%	4.69%	2.58% (0.199 pb)
$\mu^+\mu^- \rightarrow \mu^+\mu^-W^+W^-$	40.0%	34.9%	22.0% (0.207 pb)

TABLE II. Cutflow table for both signal and background events. All processes before the pre-selection cuts are set to 100%.



- Only two visible muons in forward region ( $2.5 < \eta(\mu) < 8.0$ ).

Detector level pre-selection:

- Back-to-back muons:  $\eta(\mu^-) \cdot \eta(\mu^+) < 0$ .
- Sufficient transverse momentum:  $p_T(\mu) > 20$  GeV.

# Sensitivity

3 TeV

Benchmark	$\eta(\mu) < 4$	$\eta(\mu) < 6$	$\eta(\mu) < 8$
$\Delta\sigma/\sigma$	6.2%	3.94%	3.94%

TABLE V. The 68% projected sensitivity on the Higgs inclusive rate from  $ZZ$  fusion at 3 TeV muon collider.

10 TeV

Benchmark	$\eta(\mu) < 4$	$\eta(\mu) < 6$	$\eta(\mu) < 8$
$\Delta\sigma/\sigma$	15.2%	0.75%	0.74%

TABLE III. The 68% projected sensitivity on the Higgs inclusive rate from  $ZZ$  fusion at 10 TeV muon collider.

# Higgs coupling global fit

We perform the chi square analysis via combining

- (1) All kinds of on-shell channels,
- (2) Indirect search for top yukawa,
- (3) Invisible decay branching ratio using forward muon
- (4) Our inclusive ZZ fusion measurement at 3/10 TeV Muon Collider

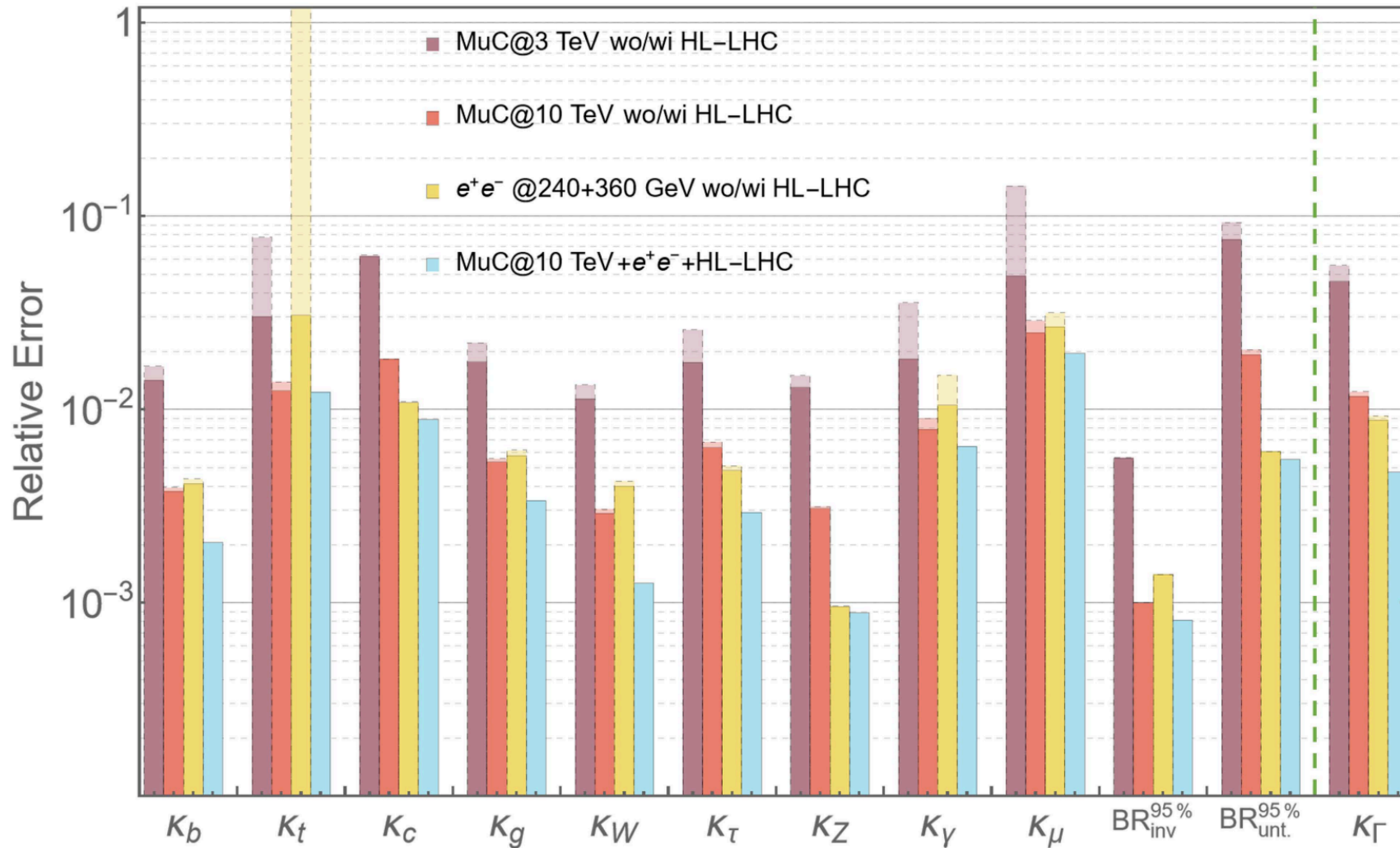
We further combine with HL-LHC and CEPC.

1. Matthew Forslund and Patrick Meade. [\[2203.09425\] High Precision Higgs from High Energy Muon Colliders](#)
2. Zhen Liu, Kun-Feng Lyu, Ishmam Mahbub, Lian-Tao Wang. [\[2308.06323\] Top Yukawa Coupling Determination at High Energy Muon Collider](#)
3. M. Ruhdorfer, E. Salvioni, A. Wulzer. [\[2303.14202\] Invisible Higgs from forward muons at a muon collider](#)
4. Our inclusive Higgs rate result.

Production	Decay	$\Delta\sigma/\sigma$ (%)	
		3 TeV	10 TeV
WW-fusion	$bb$	0.84	0.24
	$cc$	14	4.4
	$gg$	4.2	1.2
	$\tau^+\tau^-$	4.5	1.3
	$WW^*(jj\ell\nu)$	1.8	0.50
	$WW^*(4j)$	5.7	1.4
	$ZZ^*(4\ell)$	48	13
	$ZZ^*(jj\ell\ell)$	12	3.5
	$ZZ^*(4j)$	67	16
	$\gamma\gamma$	7.7	2.1
	$Z(jj)\gamma$	73	20
ZZ-fusion	$\mu^+\mu^-$	43	11
	$bb$	7.9	2.2
	$bb, (N_\mu \geq 2)$	2.6	0.77
	$WW^*(4j)$	49	12
$tth$	$WW^*(4j), (N_\mu \geq 2)$	17	4.3
	$bb$	61	53

# Higgs coupling global fit

Precision of Higgs coupling measurement ("model-independent" fit)



- With forwarded detection  $2.5 < \eta(\mu) < 6$ , the cross-section precision is  $\sim 0.75\%$
- Combining with other studies, we can constraint on  $\Gamma_H \sim 2\%$  and Higgs couplings in 0.5% level.

# Conclusion

- We study the  $ZZ \rightarrow h$  inclusive rate channel only using forward muon detection.
- Only sensitive to  $\kappa_Z$
- With forward detection  $2.5 < \eta(\mu) < 6$ , the cross-section precision is  $\sim 0.75\%$ .
- This measurement can break the degeneracy relation and constrain the Higgs total decay width.



Backup

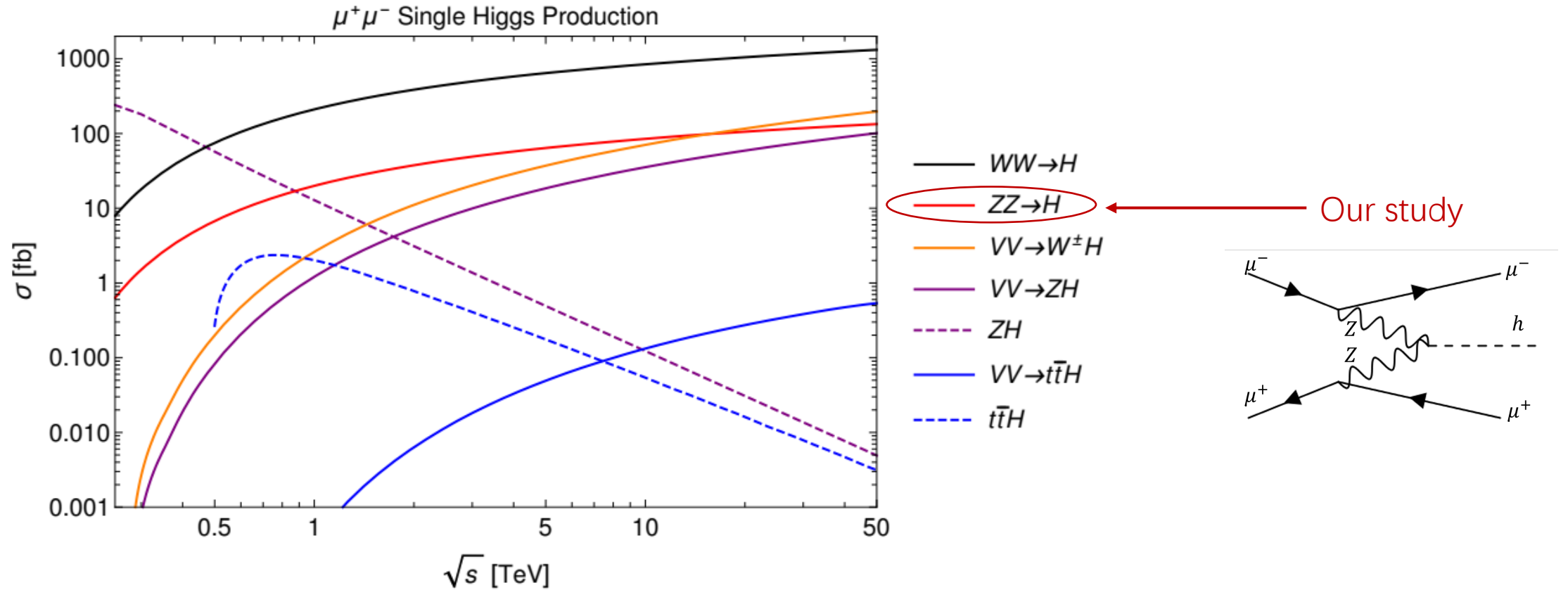
# Kappa Basis Choice

$$\text{Br}_{\text{exo}} = \text{Br}_{\text{inv}}^{\text{BSM}} + \text{Br}_{\text{unt}}^{\text{BSM}}$$

$$(\text{Br}_{\text{inv}}^{\text{BSM}}, \text{Br}_{\text{unt}}^{\text{BSM}})$$

(%)	Postive	Negative
$\kappa_b$	+0.557	-0.232
$\kappa_t$	+1.42	-1.36
$\kappa_c$	+1.83	-1.82
$\kappa_g$	+0.665	-0.450
$\kappa_W$	+0.509	-0.102
$\kappa_\tau$	+0.762	-0.595
$\kappa_Z$	+0.374	-0.254
$\kappa_\gamma$	+0.974	-0.824
$\kappa_\mu$	+2.86	-2.90
$\text{Br}_{\text{inv}}^{95\%}$	+1.0	0
$\text{Br}_{\text{unt}}^{95\%}$	+2.02	0

# Higgs productions at Muon Collider



Matthew Forsslund, Patrick Meade, [\[2203.09425\]](#)