



Compact Colliders Of Tomorrow: The Cool Copper Collider & The Muon Collider

Precision Electroweak to Discoveries at the Energy Frontier

*based on US Snowmass 2021-22 +
2023 Particle Physics Project Prioritization Panel (P5) discussions*

Report of the Snowmass 2021 e^+e^- -Collider Forum

Maria Chamizo Llatas, Sridhara Dasu, Ulrich Heintz,
Emilio Nanni, John Power, Stephen Wagner

<https://web.slac.stanford.edu/c3/>

Muon Collider Forum Report

Forum Conveners: K.M. Black¹, S. Jindariani², D. Li³, F. Maltoni^{4,5}, P. Meade⁶,
and D. Stratakis²

<https://www.muoncollider.us/>
<https://muoncollider.web.cern.ch/>

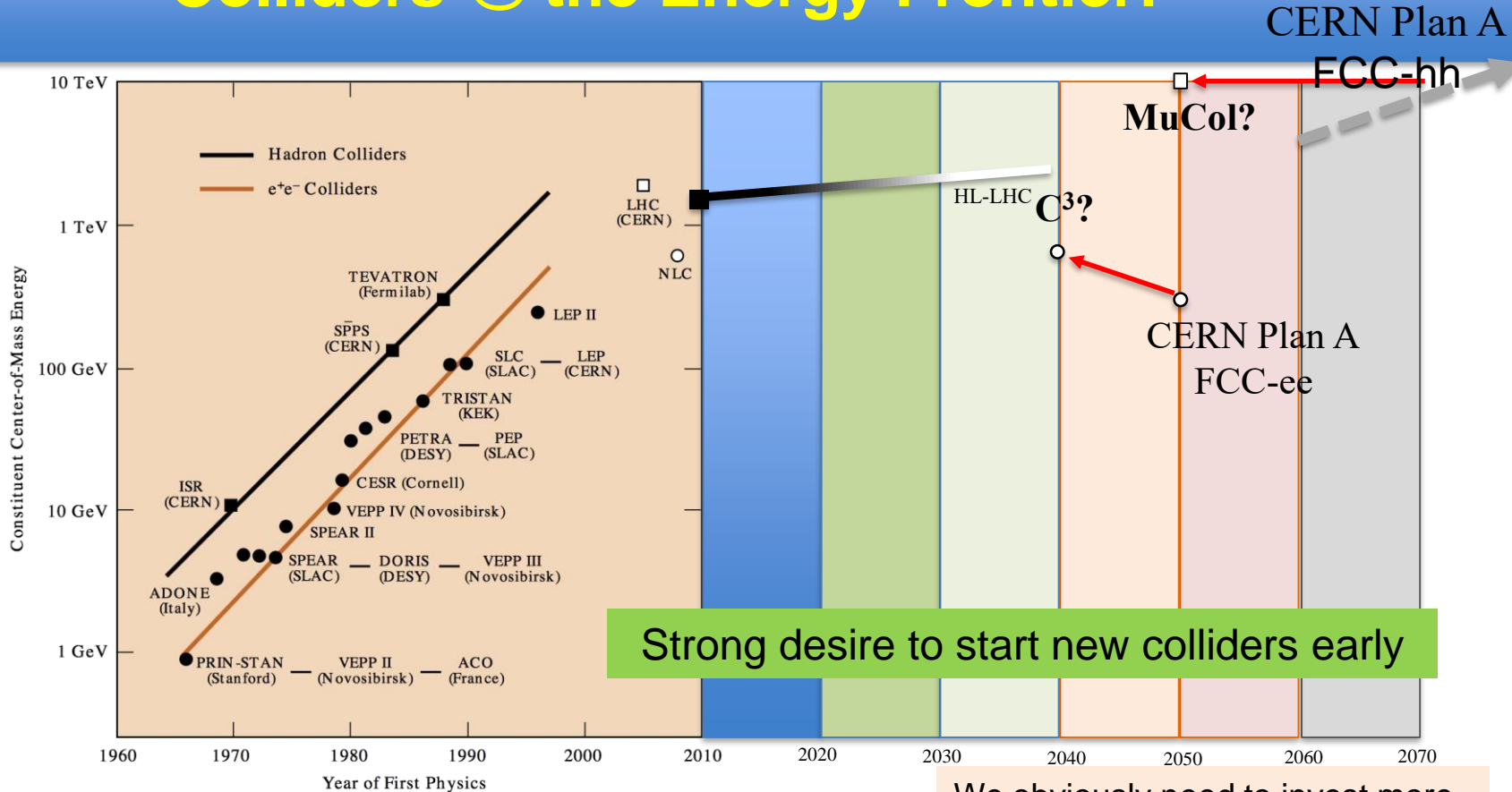
Report of the Snowmass'21
Collider Implementation Task Force

Thomas Roser (chair)¹, Reinhard Brinkmann², Sarah Cousineau³, Dmitri Denisov¹,
Spencer Gessner⁴, Steve Gourlay⁵, Philippe Lebrun⁶, Meenakshi Narain⁷, Katsunobu
Oide⁸, Tor Raubenheimer⁴, John Seeman⁴, Vladimir Shiltsev⁹, Jim Strait⁹, Marlene
Turner⁵, and Lian-Tao Wang¹⁰



Colliders @ the Energy Frontier!

<http://www.slac.stanford.edu/pubs/beamline/27/1/27-1-panofsky.pdf>



Strong desire to start new colliders early

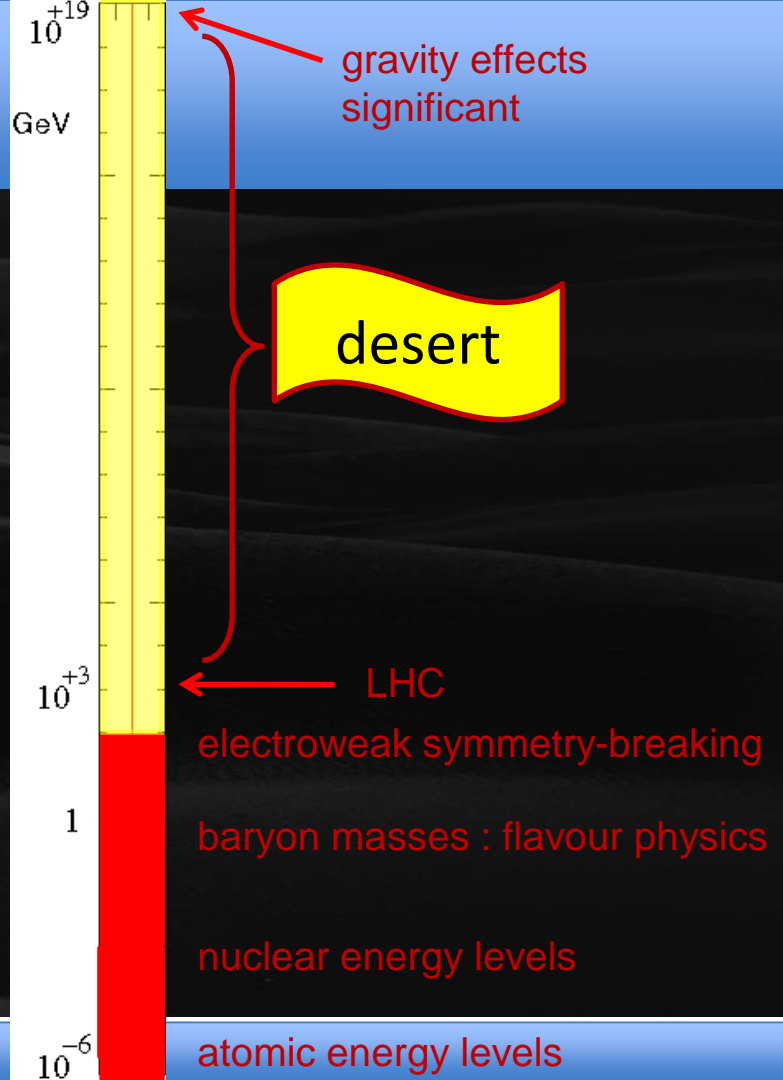
We obviously need to invest more in machine R&D; more people



Why go to new Colliders?

Standard model of particle physics works well at the LHC scales, although some key aspects of observed cosmological phenomena are left unexplained.

Yes, we are in the dark.

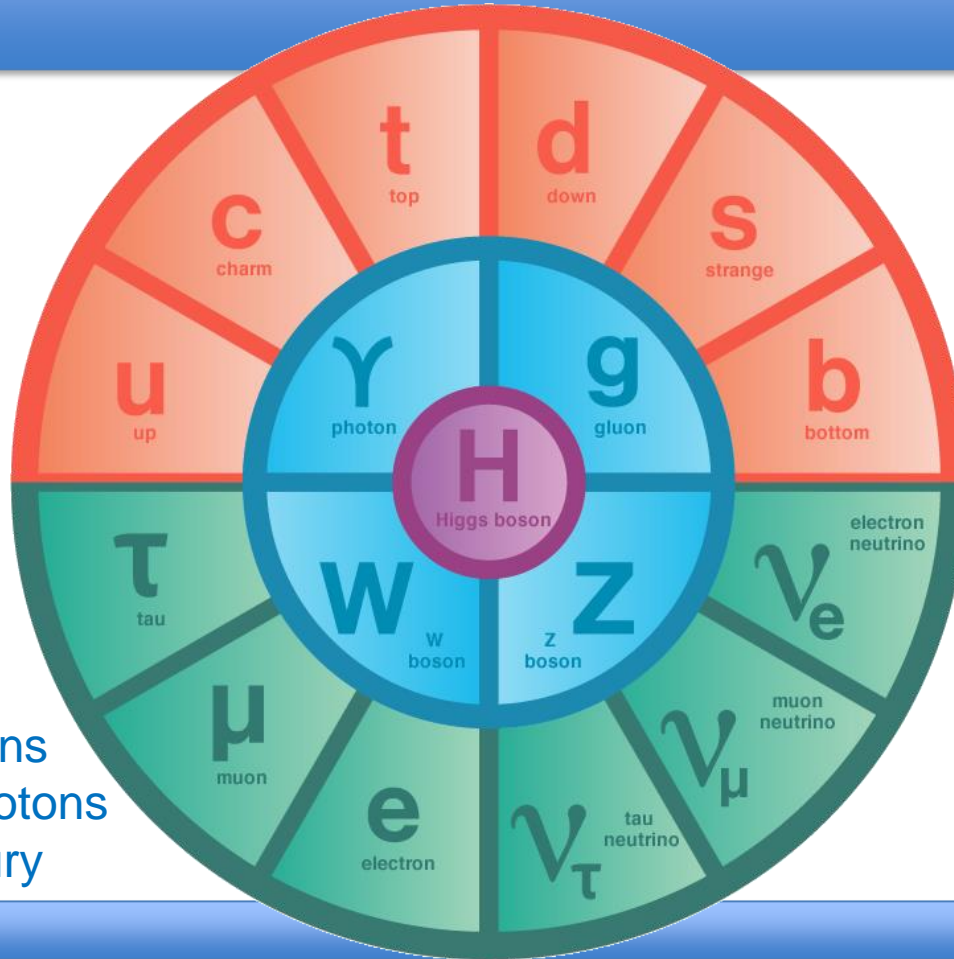




Higgs is Central

First Fermions discovered were electrons in 19th century

First Vector-bosons discovered were photons also in 19th century



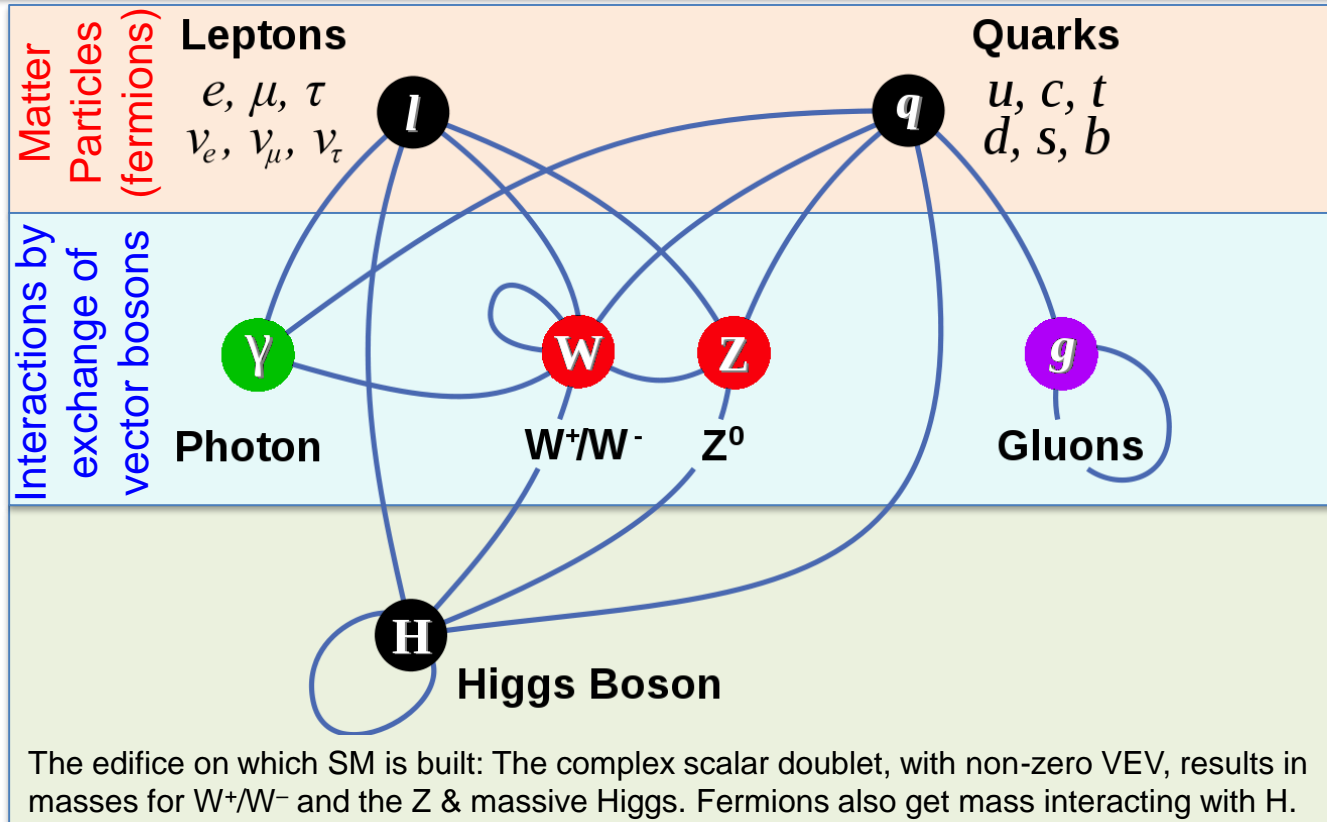
First Scalar boson discovered, the Higgs, was in 2012!

Higgs is Edifice on which the Standard Model is built.

Higgs Will Likely Play a Central Role in guiding us out of this Darkness



Particles & Interactions of The Standard Model





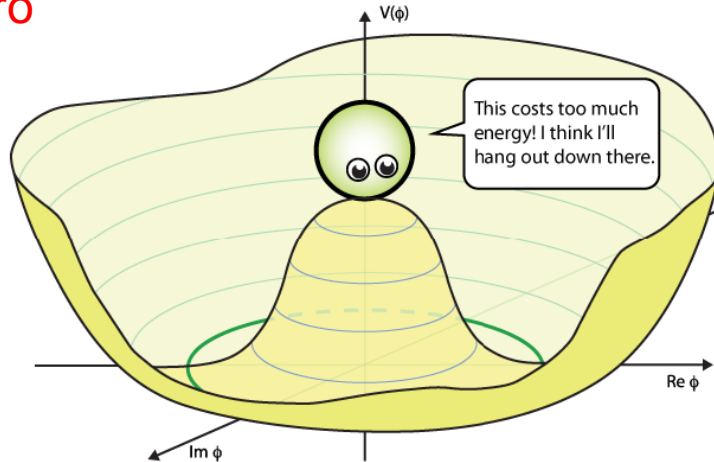
Higgs Field is Special

Electro-Weak Symmetry Breaking

50 years ago, gauge theory unified electro-weak interactions, but could not accommodate non-zero masses for W^\pm & Z

Introduction of a doublet of complex scalar fields with **peculiar** potential provided masses for W^\pm & Z and left γ massless!

Coupling to Higgs field provides masses to matter particles!!



$$\phi = \begin{pmatrix} \phi_1 + i\phi_2 \\ \phi_3 + i\phi_4 \end{pmatrix}$$

The remnant fourth field degree of freedom is the Higgs Boson discovered in 2012

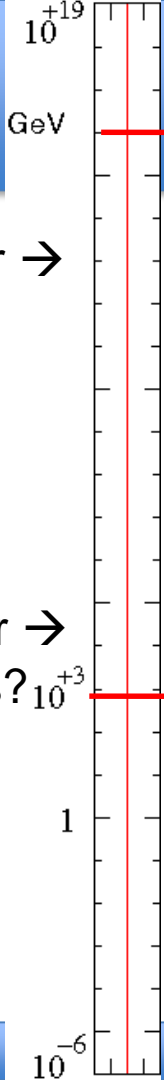
Confirming the form of the potential requires measuring di-higgs production

$$\mathcal{L} = |D_\mu \phi|^2 - \mu^2 \phi^2 - \lambda \phi^4$$

$$\text{For } \mu^2 < 0, \text{ minimum } v = \sqrt{-\frac{\mu^2}{2\lambda}}$$



Sneak Peek into the Desert

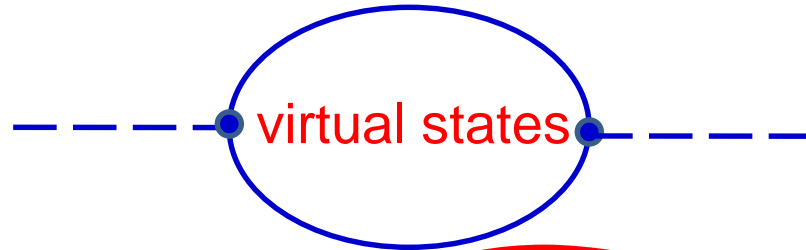


Flavor sector →
new physics

Higgs sector →
new physics?

LHC

In the language of quantum field theory...



$$m \rightarrow m + \delta m(Q^2)$$

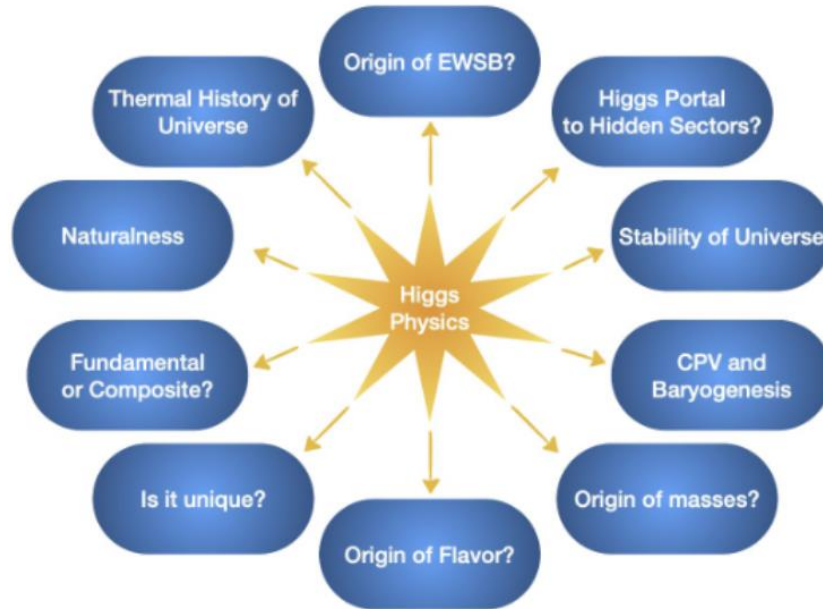
$$g \rightarrow g + \delta g(Q^2)$$

...our window into the desert

Scalar Higgs boson mass corrections would be very large with only the particle content of the Standard Model



Higgs Central to Many Fundamental Topics



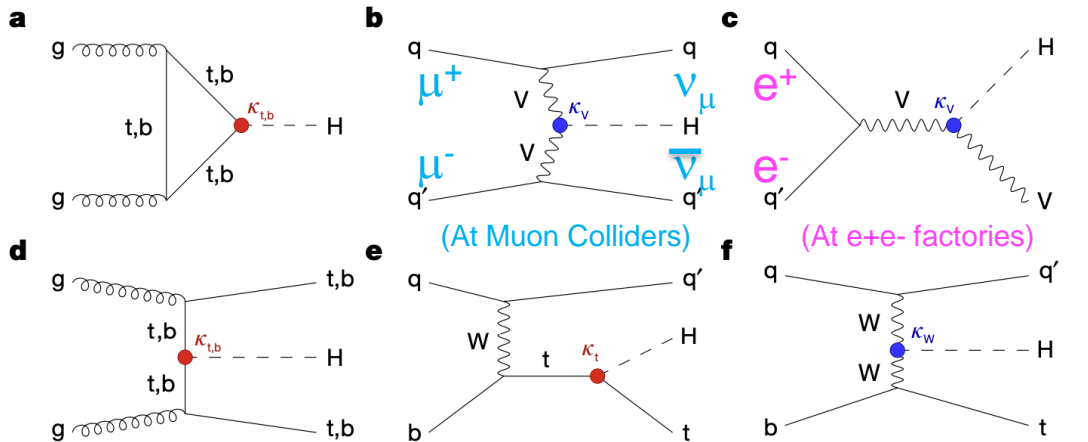
Percent level Higgs couplings deviations from SM values → BSM physics at 10 TeV

$e^+ e^-$ Higgs Factory → Energy Frontier (10 TeV) Muon Collider

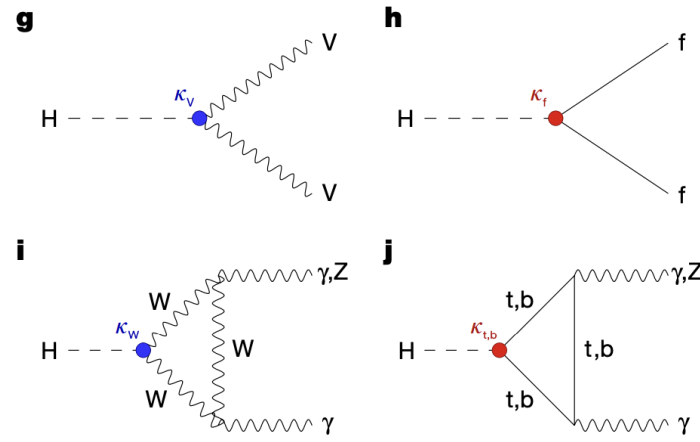


Higgs Boson Couplings, Production and Decays

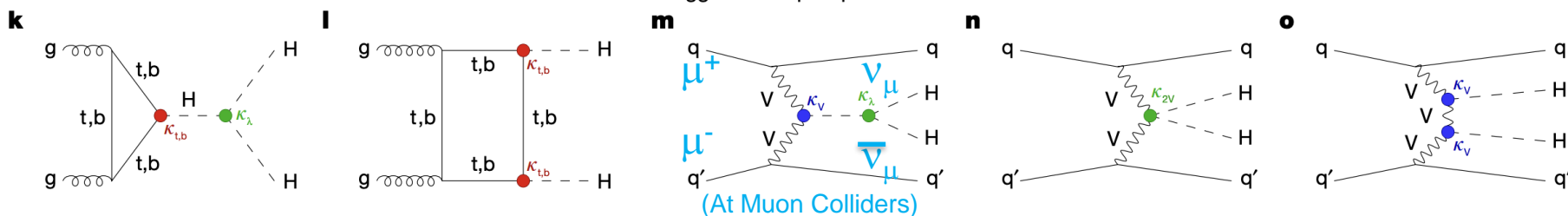
Higgs boson production modes (At the LHC)



Higgs boson decay channels



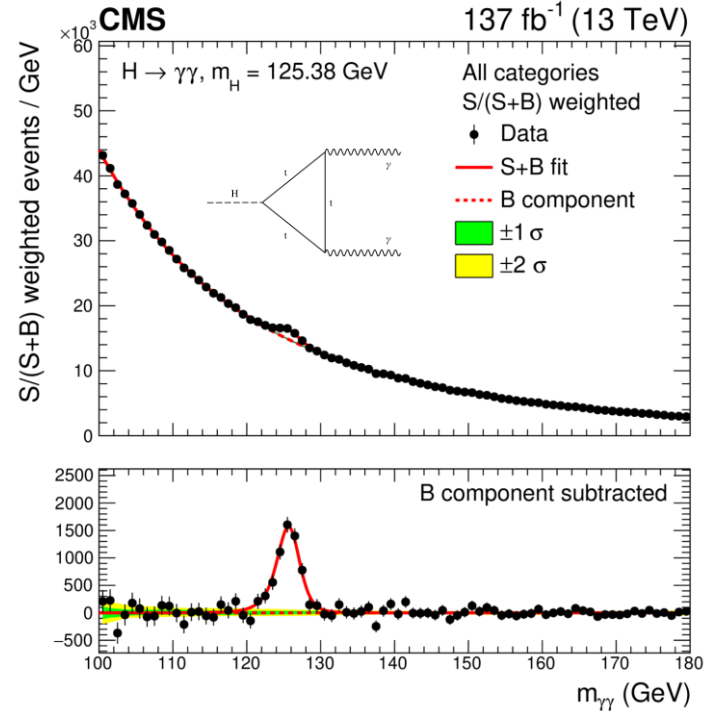
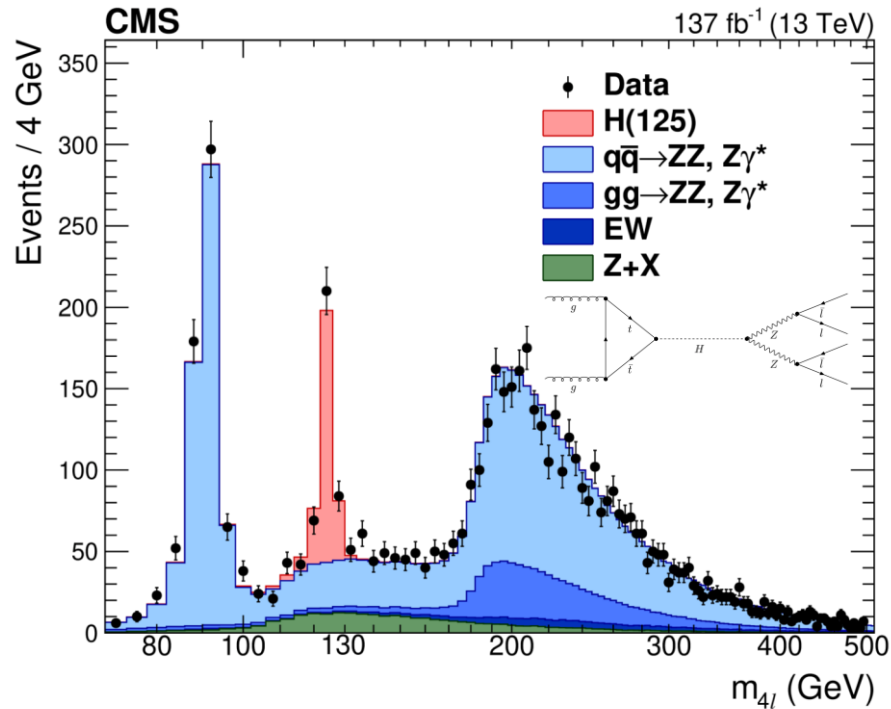
Higgs boson pair production





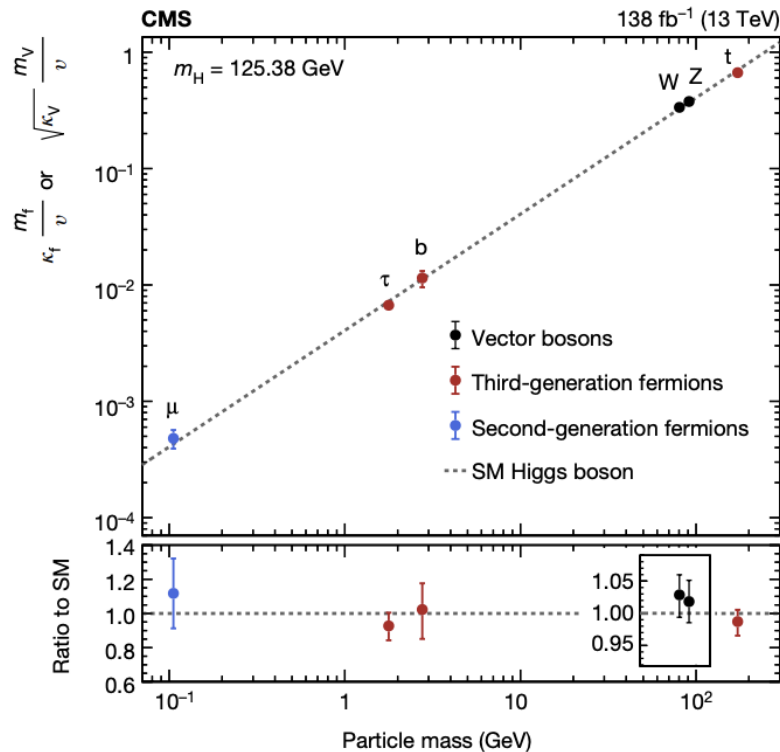
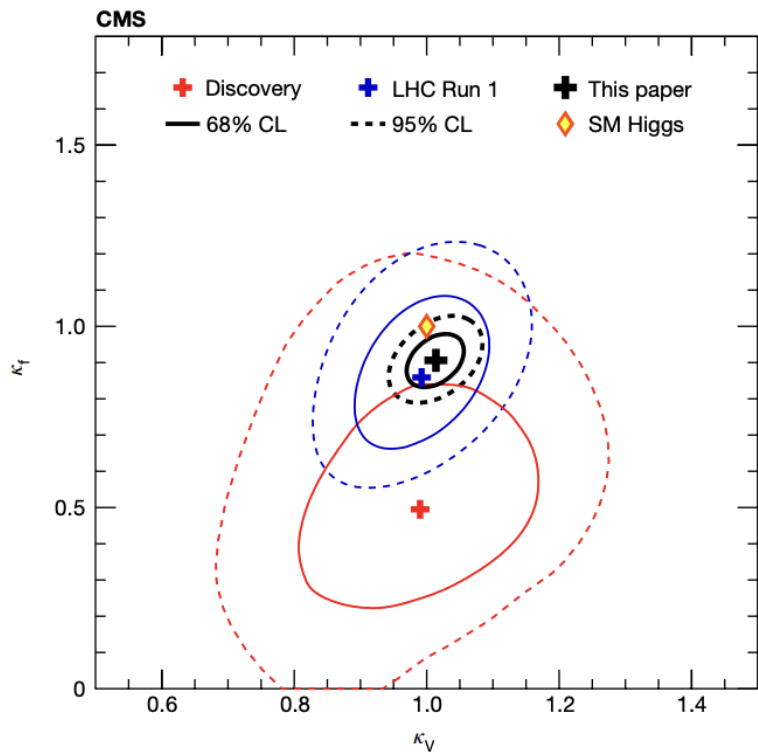
Current Status of Golden Channels @ LHC

Our Higgs boson data sets are enabling detailed studies of the SM





Current Status of Higgs Couplings



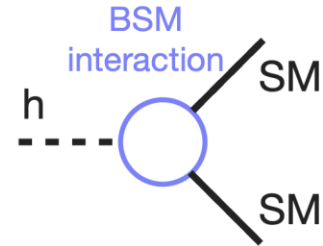
Discrepancies at this level if any would imply <1 TeV scale new physics – we did not see either



What's Next?

Sub-percent Level Higgs Couplings → 10 TeV BSM

Can we use precision measurements to indirectly probe new physics at higher energies?
 Are higgs couplings to SM particles modified?

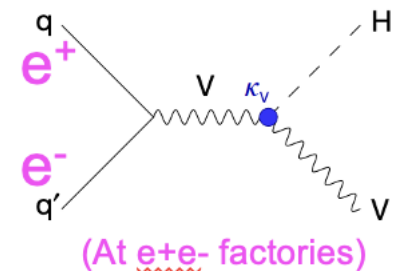
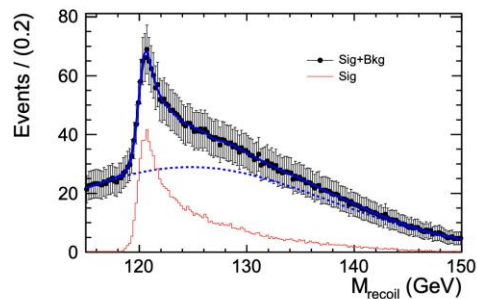
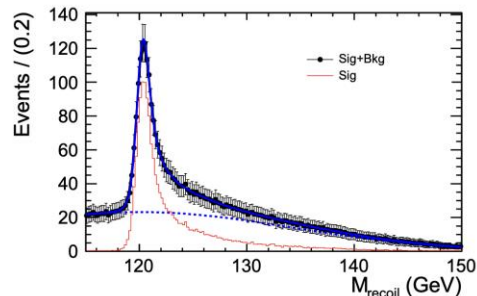
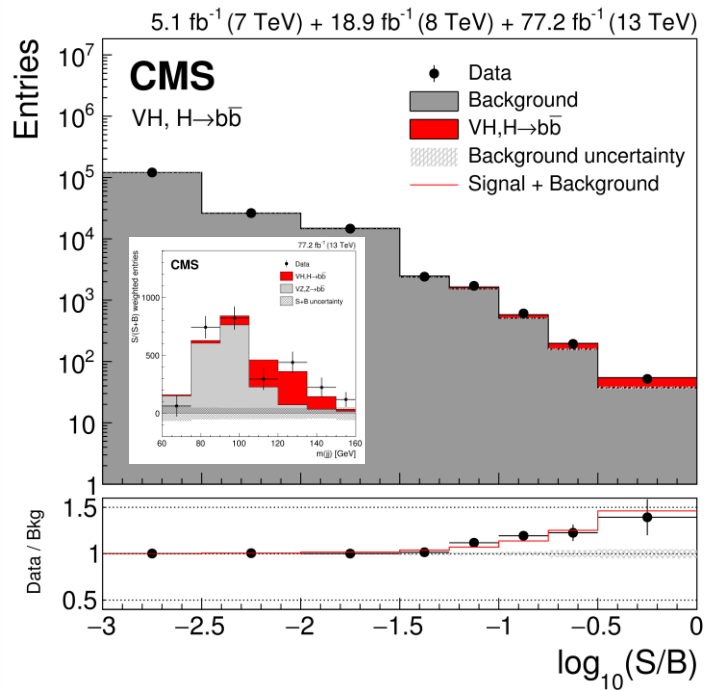


		HL-LHC few%	Higgs Factory 0.1%
Tree-level	$\sim \frac{v^2}{M^2}$	$\sim 1 \text{ TeV}$	$\sim \text{few TeV}$
Loop-level	$\sim \frac{1}{4\pi^2} \frac{v^2}{M^2}$	$\sim 100 \text{ GeV}$	$\sim 1 \text{ TeV}$

Couplings Deviations found at
 C^3 e⁺e⁻-Higgs Factory
 →
 BSM @ 10 TeV Muon Collider



Why an electron-positron collider?



Recoil mass at electron positron collider

Higgs to anything over background

Figure 24: Reconstructed Higgs mass spectrum together with the sum of underlying background for the $\mu\mu X$ -channel (top) and eeX -channel (bottom). The polarisation mode is $e_L^+e_L^-$. The lines show the fits using the Simplified Kernel Estimation fitting formula to the signal and a polynomial of second order to the background as explained in the text.



Colliders Of Tomorrow

Many Opportunities at the Energy Frontier

FCC-pp, SPPS	100 km	100 TeV ~ $E_{qq} \sim 15$ TeV	500 - 3000 fb ⁻¹ sy ⁻¹
FCC-ee, CEPC	100 km	240, 365 GeV	850, 155 fb ⁻¹ sy ⁻¹
CLIC-ee	50 km	0.38, 1.5, 3 TeV	150, 370, 590 fb ⁻¹ sy ⁻¹
ILC-ee	31 km	250, 500 GeV	75, 180 fb ⁻¹ sy ⁻¹
C ³ -ee	7 km	250, 550 GeV	100, 200 fb ⁻¹ sy ⁻¹
HL-LHC	27 km	14 TeV ~ $E_{qq} \sim 2$ TeV	200 - 500 fb ⁻¹ y ⁻¹
μ Col ~27 km		10, 15 TeV	1000 - 2000 fb ⁻¹ sy ⁻¹
μ Col 6 km		3, 6, 10 TeV	200, 500 fb ⁻¹ sy ⁻¹





Implementation Task Force Evaluated Collider Types

Circular Colliders e^+e^-

- From $\sqrt{s} = M_Z \rightarrow M_{WW} \rightarrow M_{Z+H} \rightarrow M_{tt}$
- Tera-Z, millions of H – very high luminosity
- "Upgrade" to pp-machine for high energy

Proton Colliders (FCC-hh, SPPS/China ~ 100 TeV, $10s \text{ ab}^{-1}$)

Linear Colliders e^+e^-

- Polarization, Energy Reach
- From $\sqrt{s} = M_Z \rightarrow M_{WW} \rightarrow M_{Z+H} \rightarrow 550$ GeV
- Upgraded / Expanded facilities: $\sqrt{s} \rightarrow 3$ TeV
- Advanced technologies: $\sqrt{s} \rightarrow 15$ TeV (much R&D needed)

Muon Colliders (10 TeV, 10 ab^{-1})

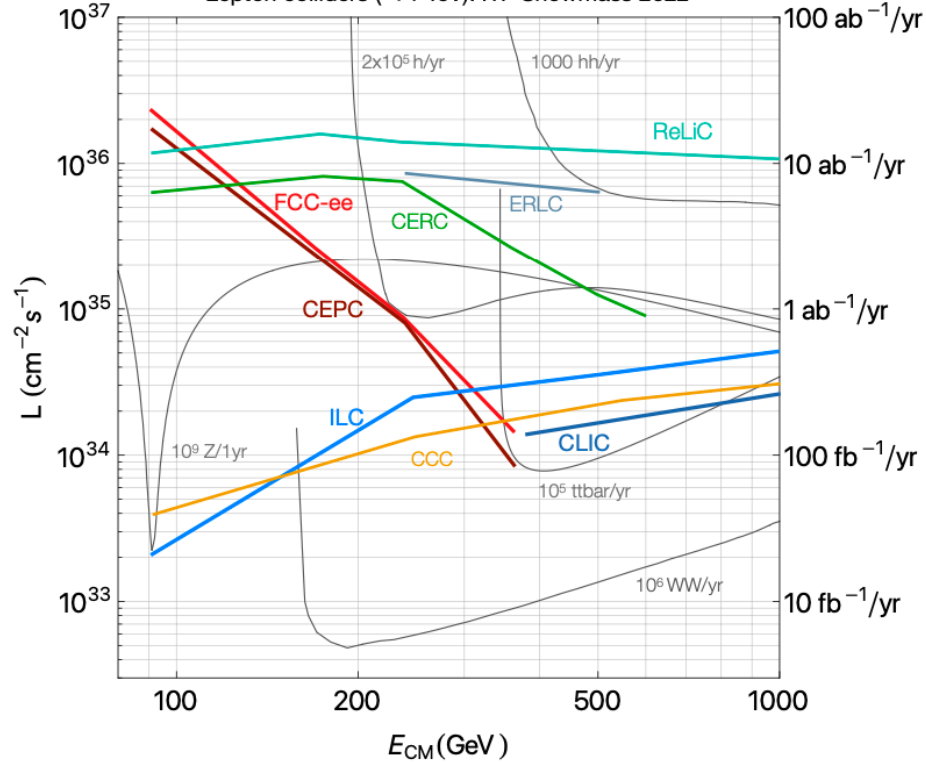
- Revived interest in high-energy option due to recent advances

Collider	Type
FCC-ee (0.24 TeV)	Circular
CEPC (0.24 TeV)	Circular
CERC (0.24 TeV)	Circular
ILC (0.25 TeV)	Linear
CLIC (0.38 TeV)	Linear
CLIC (3 TeV)	Linear
C ³ (0.25 TeV)	Linear
ReLiC (0.24 TeV)	Linear
ERLC (0.24 TeV)	Linear
ILC (3 TeV)	Linear
C ³ (3 TeV)	Linear
ReLiC (3 TeV)	Linear
WFA (3 TeV)	Linear
WFA-flat (15 TeV)	Linear
WFA-round (15 TeV)	Linear

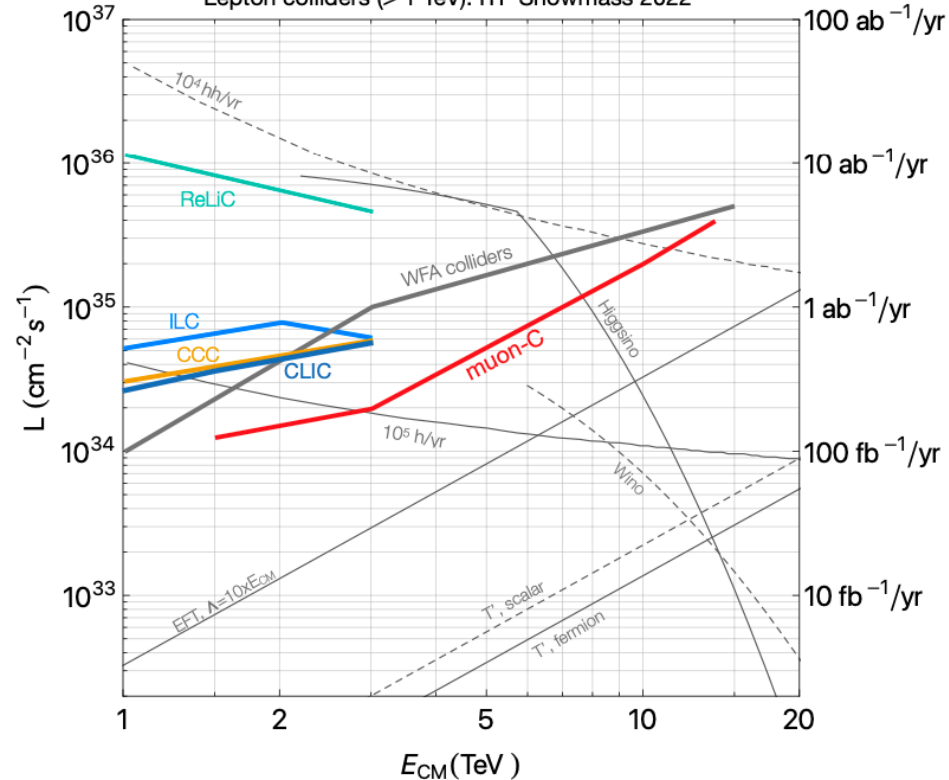


Lepton collider Luminosity vs \sqrt{s} Landscape

Lepton colliders (< 1 TeV). ITF Snowmass 2022



Lepton colliders (> 1 TeV). ITF Snowmass 2022

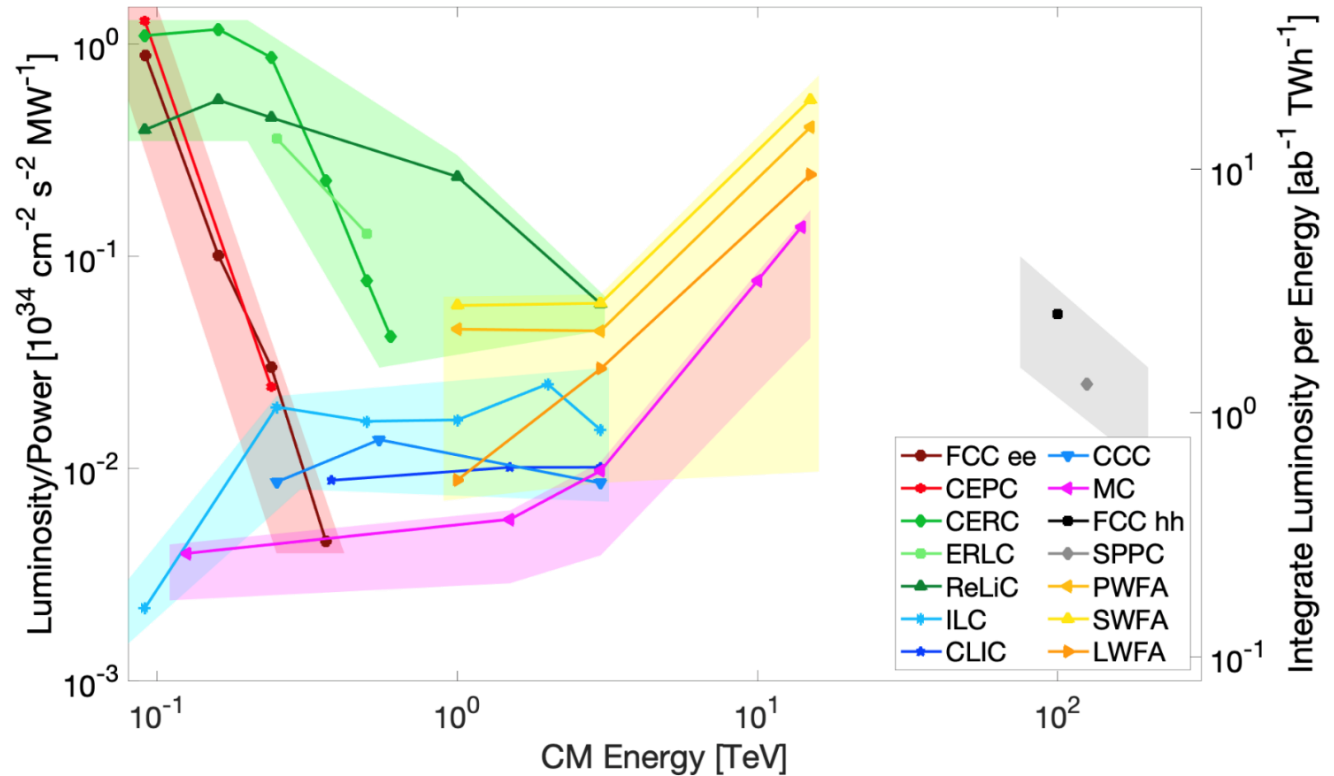




Luminosity / Power vs Energy from ITF

Points computed from
proponent submitted
parameters table

Uncertainty band is
ITF judgement based
on many
considerations:
technical design
status, risk
assessment, ...





Higgs Factories

With 5 y R&D could
get physics rolling by
2040 for ~\$10B

Proposal Name	CM energy nom. (range) [TeV]	Lum./IP @ nom. CME [$10^{34} \text{ cm}^{-2} \text{ s}^{-1}$]	Years of pre-project R&D	Years to first physics	Construction cost range [2021 B\$]	Est. operating electric power [MW]
FCC-ee ^{1,2}	0.24 (0.09-0.37)	7.7 (28.9)	0-2	13-18	12-18	290
CEPC ^{1,2}	0.24 (0.09-0.37)	8.3 (16.6)	0-2	13-18	12-18	340
ILC ³ - Higgs factory	0.25 (0.09-1)	2.7	0-2	<12	7-12	140
CLIC ³ - Higgs factory	0.38 (0.09-1)	2.3	0-2	13-18	7-12	110
CCC ³ (Cool Copper Collider)	0.25 (0.25-0.55)	1.3	3-5	13-18	7-12	150
CERC ³ (Circular ERL Collider)	0.24 (0.09-0.6)	78	5-10	19-24	12-30	90
ReLiC ^{1,3} (Recycling Linear Collider)	0.24 (0.25-1)	165 (330)	5-10	>25	7-18	315
ERLC ³ (ERL linear collider)	0.24 (0.25-0.5)	90	5-10	>25	12-18	250
XCC (FEL-based $\gamma\gamma$ collider)	0.125 (0.125-0.14)	0.1	5-10	19-24	4-7	90
Muon Collider Higgs Factory ³	0.13	0.01	>10	19-24	4-7	200



Energy Frontier Machines

With 10 y R&D could
get physics rolling by
2050 for ~\$18B

Proposal Name	CM energy nom. (range) [TeV]	Lum./IP @ nom. CME [$10^{34} \text{ cm}^{-2}\text{s}^{-1}$]	Years of pre-project R&D	Years to first physics	Construction cost range [2021 B\$]	Est. operating electric power [MW]
Muon Collider	10 (1.5-14)	20 (40)	>10	>25	12-18	~300
LWFA - LC (Laser-driven)	15 (1-15)	50	>10	>25	18-80	~1030
PWFA - LC (Beam-driven)	15 (1-15)	50	>10	>25	18-50	~620
Structure WFA (Beam-driven)	15 (1-15)	50	>10	>25	18-50	~450
FCC-hh	100	30 (60)	>10	>25	30-50	~560
SPPS	125 (75-125)	13 (26)	>10	>25	30-80	~400



Higgs Factory Physics Timeline vis-à-vis Integrated Luminosity

Caveat – run plans are adjustable; start of physics times are different

- **Technically feasible times:** ILC < 12y, FCC-ee, CLIC, CEPC, C3 : 13-18y
- ILC “shovel ready” + C3 Short R&D –potential for earliest start
- FCC-ee, CLIC – post HL-LHC
- Circular colliders have shorter runs, higher luminosity
- Linear collider runs have access to polarization and higher energy
- Both provide good precision on Higgs Couplings & EWK

time	T0		T+5		T+10		T+15		T+20		T+25		T+30
FCC-ee		150/ab Mz	10/ab 2Mw	5/ab 240 GeV		1.7/ab 2mtop	mH						
CEPC	100/ab Mz	6/ab 2Mw		10/ab 240GeV			1/ab-1 2mtop						
ILC (and C3)			2/ab 240 GeV		0.1/ab MZ	0.1/ab 2mtop		4/ab 500 GeV				8/ab 1 TeV	
CLIC		1.1/ab 380 GeV				3.5/ab 1.5 TeV			5.6/ab 3 TeV				

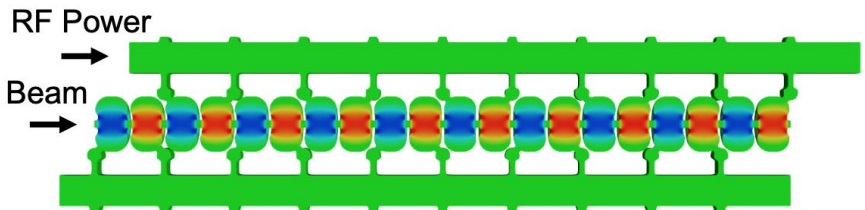


C3 – Cool Copper Collider – New Option

Breakthrough in the Performance of RF Accelerators

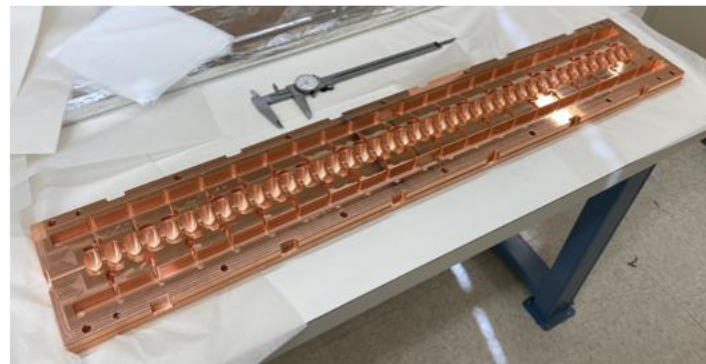


- RF power coupled to each cell – no on-axis coupling
- Full system design requires modern virtual prototyping



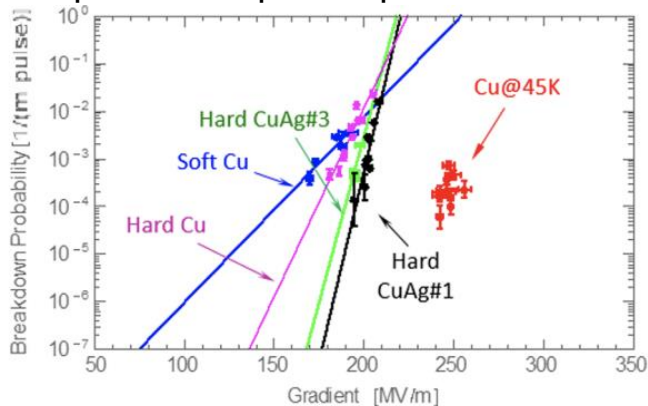
Electric field magnitude produced when RF manifold feeds alternating cells equally

First C³ structure at SLAC



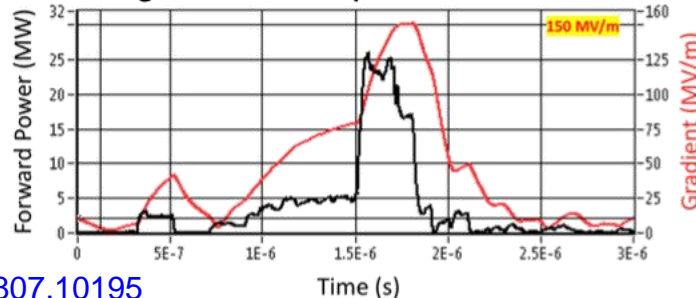
Cryogenic operation improves performance

Cahill et al.
PRAB 21.10 (2018): 102002



Bane et al, arXiv 1807.10195

High Gradient Operation at 150 MV/m



X-band Prototype

Ithara Dasu (dasu@hep.wisc.edu)



Synergies With X-Ray Photon Sources

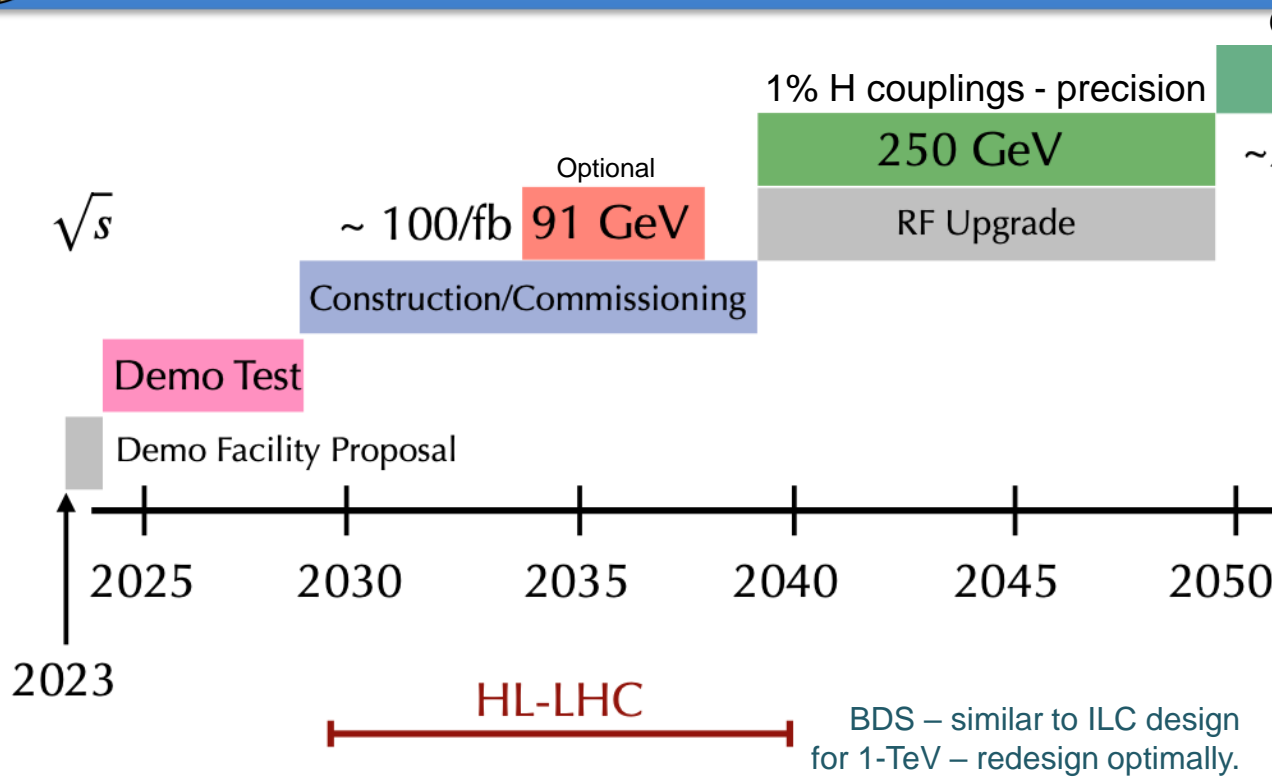
The vast majority of ~30,000 currently operating accelerators globally are electron accelerators.

Electron accelerator R&D ranges from industrial applications to the cutting-edge development of ultimate storage rings and linear accelerator based XFELs.

This fortunate situation allows e^+e^- colliders to leverage these global efforts to provide a viable path to a collider reducing the R&D costs to the HEP budget.



C³ – $\sqrt{s} = 250 - 550$ GeV – Potential Coordinates

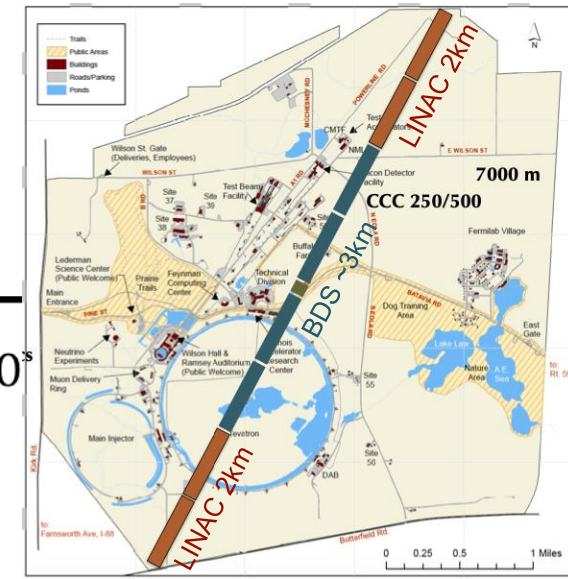


O(10)% Higgs Self Coupling

550 GeV

~3-4/ab

~2/ab



Can fit in FNAL site with BDS improvements



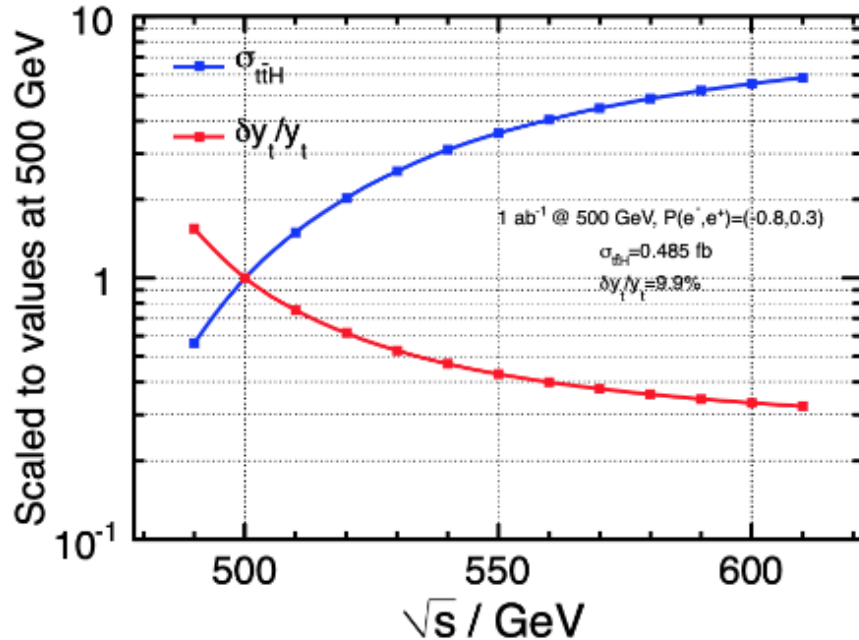
Higgs Couplings from Factories

Higgs Coupling (%)	HL-LHC	ILC250 + HL-LHC	ILC500 +HL-LHC	ILC1000 + HL-LHC	FCC-ee + HL-LHC	CEPC240 + HL-LHC	CEPC360 +HL-LHC	CLIC380 + HL-LHC	CLIC3000 +HL-LHC
hZZ	1.5	.22	.17	.16	.17	.074	.072	.34	.22
hWW	1.7	.98	.20	.13	.41	.73	.41	.62	1
$hb\bar{b}$	3.7	1.06	.50	.41	.64	.73	.44	.98	.36
$h\tau^+\tau^-$	3.4	1.03	.58	.48	.66	.77	.49	1.26	.74
hgg	2.5	1.32	.82	.59	.89	.86	.61	1.36	.78
$hc\bar{c}$	-	1.95	1.22	.87	1.3	1.3	1.1	3.95	1.37
$h\gamma\gamma$	1.8	1.36	1.22	1.07	1.3	1.68	1.5	1.37	1.13
$h\gamma Z$	9.8	10.2	10.2	10.2	10	4.28	4.17	10.26	5.67
$h\mu^+\mu^-$	4.3	4.14	3.9	3.53	3.9	3.3	3.2	4.36	3.47
$ht\bar{t}$	3.4	3.12	2.82	1.4	3.1	3.1	3.1	3.14	2.01
Γ_{tot}	5.3	1.8	.63	.45	1.1	1.65	1.1	1.44	.41



Top-Yukawa and Higgs Self-Coupling

Advantages of Energy Reach



Double Higgs production

E_{CM} (TeV)	Precision of λ_{HHH}
HL-LHC	50%
ILC 0.5, C3 0.55	20%
CLIC 1.5	36%
CLIC 3	9%
μ C10, FCC-hh	4%



Electroweak Observables

GigaZ is a big improvement over current status

FCC-ee TeraZ suggests even bigger leap forward in precision

Quantity	current	ILC250	ILC-GigaZ	FCC-ee	CEPC	CLIC380
$\Delta\alpha(m_Z)^{-1} (\times 10^3)$	17.8*	17.8*		3.8 (1.2)	17.8*	
Δm_W (MeV)	12*	0.5 (2.4)		0.25 (0.3)	0.35 (0.3)	
Δm_Z (MeV)	2.1*	0.7 (0.2)	0.2	0.004 (0.1)	0.005 (0.1)	2.1*
Δm_H (MeV)	170*	14		2.5 (2)	5.9	78
$\Delta\Gamma_W$ (MeV)	42*	2		1.2 (0.3)	1.8 (0.9)	
$\Delta\Gamma_Z$ (MeV)	2.3*	1.5 (0.2)	0.12	0.004 (0.025)	0.005 (0.025)	2.3*
$\Delta A_e (\times 10^5)$	190*	14 (4.5)	1.5 (8)	0.7 (2)	1.5 (2)	64
$\Delta A_\mu (\times 10^5)$	1500*	82 (4.5)	3 (8)	2.3 (2.2)	3.0 (1.8)	400
$\Delta A_\tau (\times 10^5)$	400*	86 (4.5)	3 (8)	0.5 (20)	1.2 (20)	570
$\Delta A_b (\times 10^5)$	2000*	53 (35)	9 (50)	2.4 (21)	3 (21)	380
$\Delta A_c (\times 10^5)$	2700*	140 (25)	20 (37)	20 (15)	6 (30)	200
$\Delta\sigma_{\text{had}}^0$ (pb)	37*			0.035 (4)	0.05 (2)	37*
$\delta R_e (\times 10^3)$	2.4*	0.5 (1.0)	0.2 (0.5)	0.004 (0.3)	0.003 (0.2)	2.7
$\delta R_\mu (\times 10^3)$	1.6*	0.5 (1.0)	0.2 (0.2)	0.003 (0.05)	0.003 (0.1)	2.7
$\delta R_\tau (\times 10^3)$	2.2*	0.6 (1.0)	0.2 (0.4)	0.003 (0.1)	0.003 (0.1)	6
$\delta R_b (\times 10^3)$	3.1*	0.4 (1.0)	0.04 (0.7)	0.0014 (< 0.3)	0.005 (0.2)	1.8
$\delta R_c (\times 10^3)$	17*	0.6 (5.0)	0.2 (3.0)	0.015 (1.5)	0.02 (1)	5.6



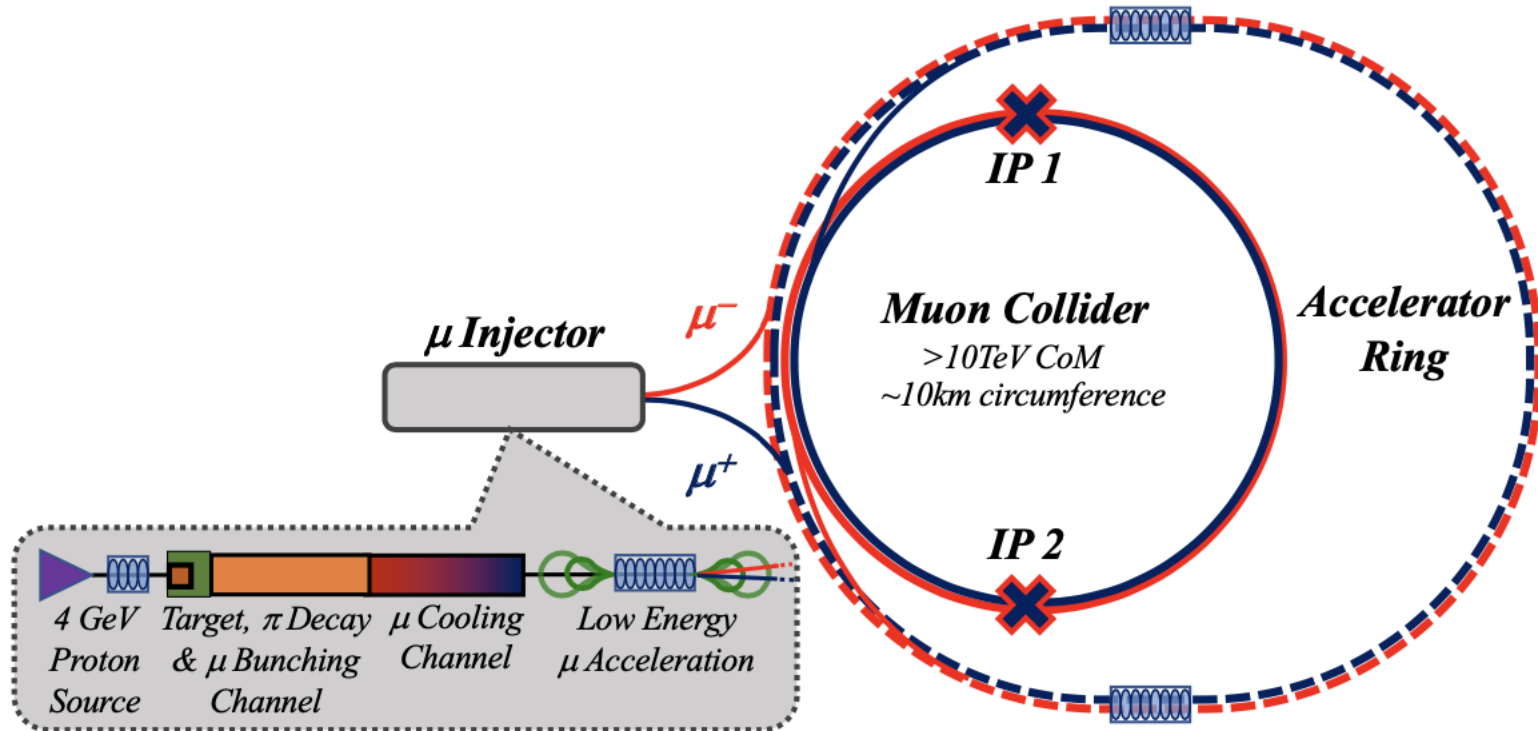
Oh! Lord of Rings!!
Can't we get to 10 TeV in one swoop?





Innovative Muon Collider Concepts

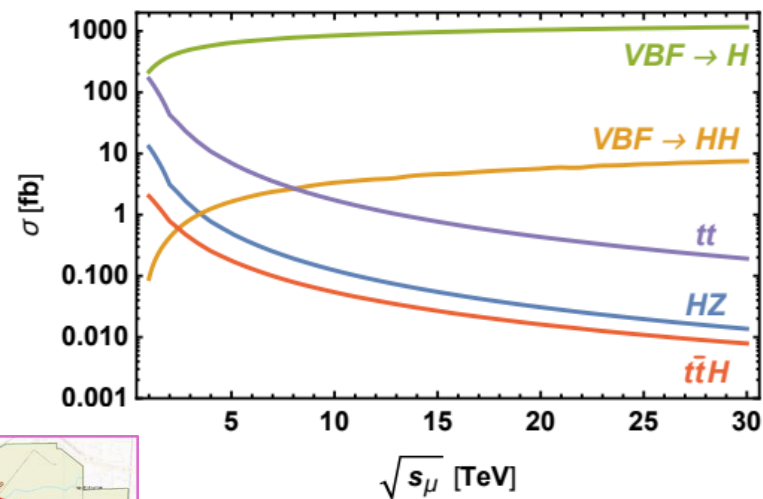
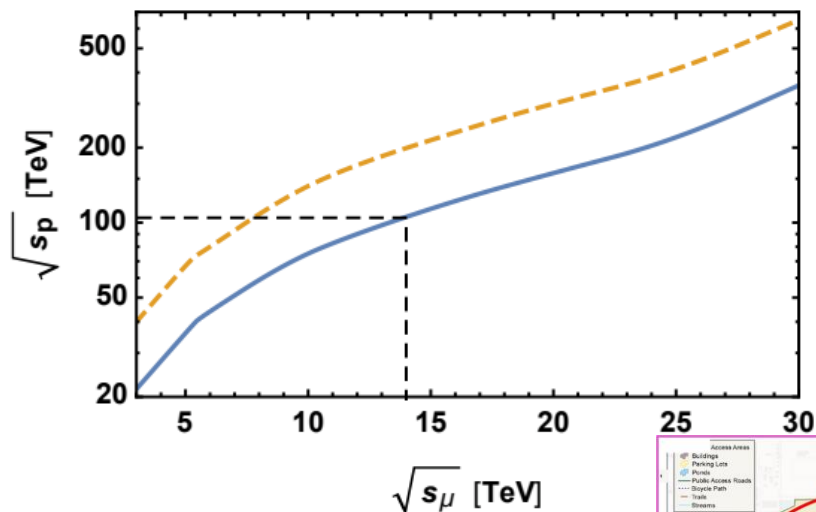
Energy Efficient Path to O(10)-TeV Colliders





Muon Collider Advantages

arxiv:1901.06150

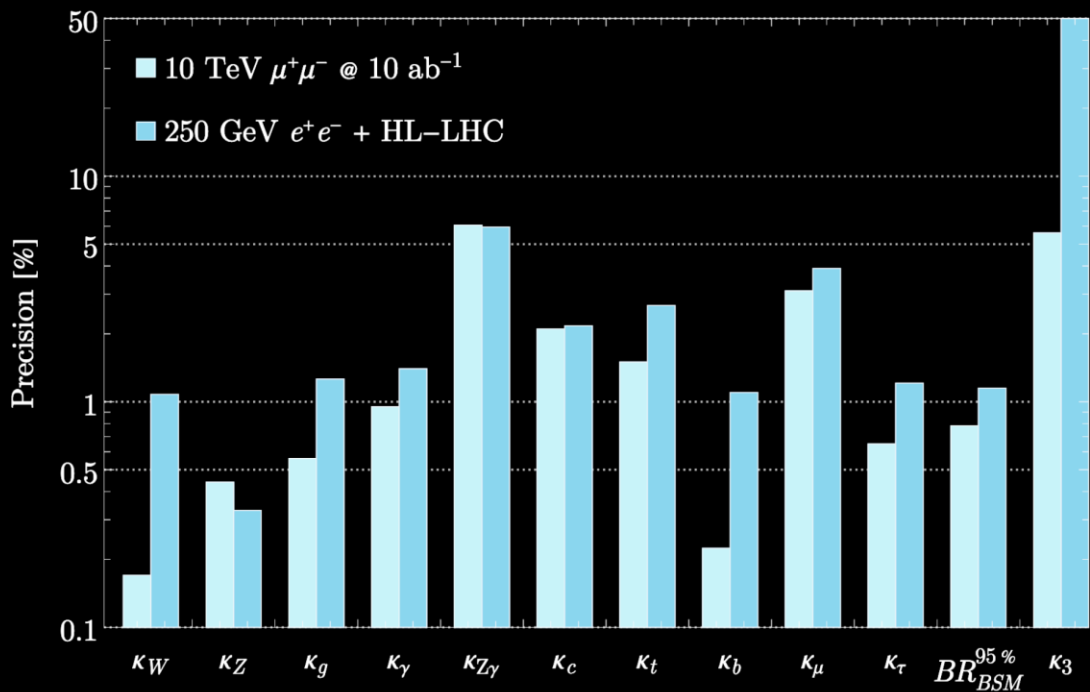


6-10 TeV muon collider can fit on FNAL site
Accelerator ring would be a FNAL site filler

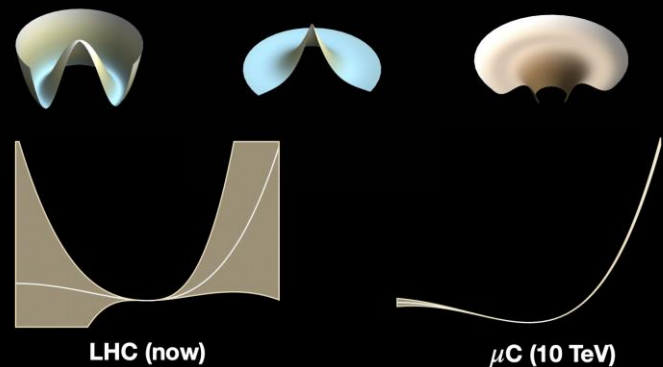
Reduced civil engineering costs compared to pp-machines



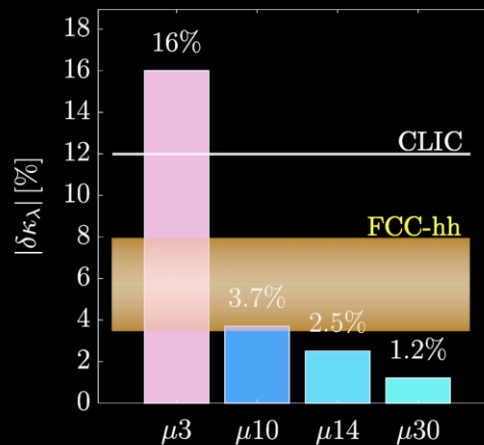
Higgs Precision & Di-Higgs Potential



[Forslund & Meade, 2308.02633]



[Accettura et al. 2303.08533]



Sub-percent deviations of Higgs couplings will be observable at muon collider too



Muon Collider Prospects: Heavy Scalar Singlet

Higgs Smashers Guide, arXiv: 2103.14043

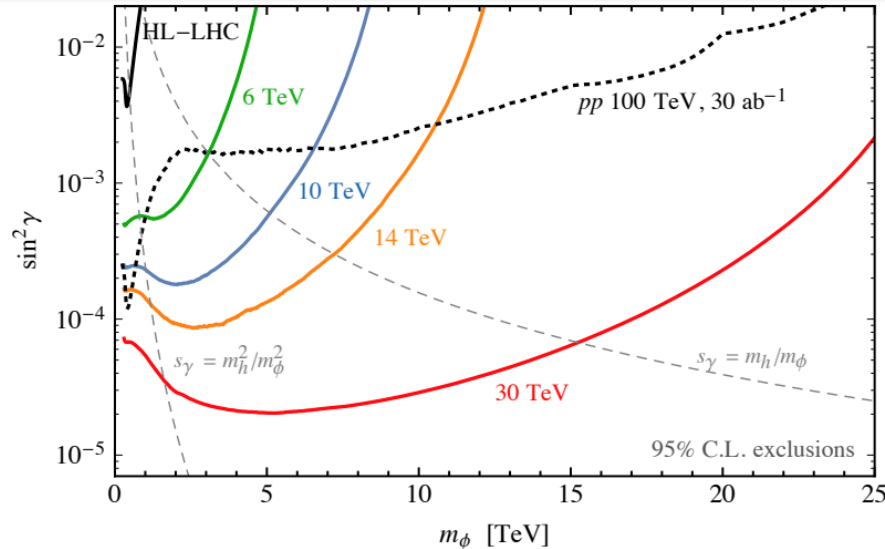


Figure 14: Exclusions on the mixing angle of a generic scalar singlet, $\sin^2 \gamma = \kappa_V - 1$, as a function of the singlet mass m_ϕ for the various collider benchmarks (colored lines). The expected limits at HL-LHC (solid) and a FCC-hh (dashed) are shown as black lines for comparison. The thin dashed lines indicate the two possible scalings of the mixing angle with m_ϕ in realistic models with fixed coupling.



Higgs Compositeness & Minimal Z' – Another place where Muon Collider Shines

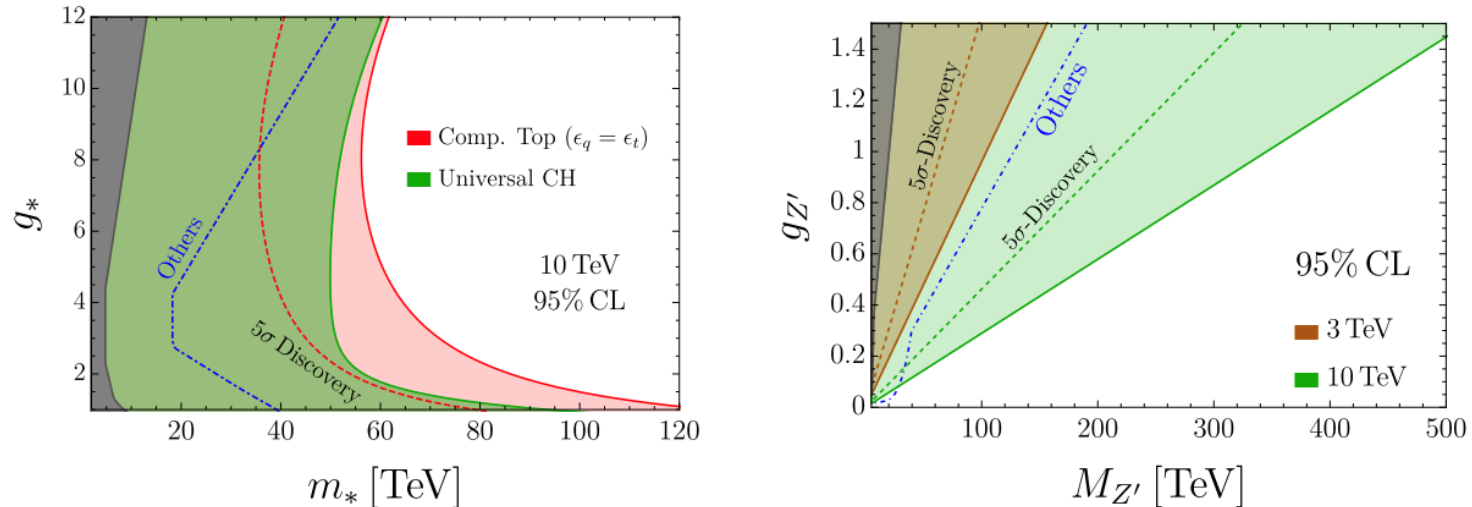


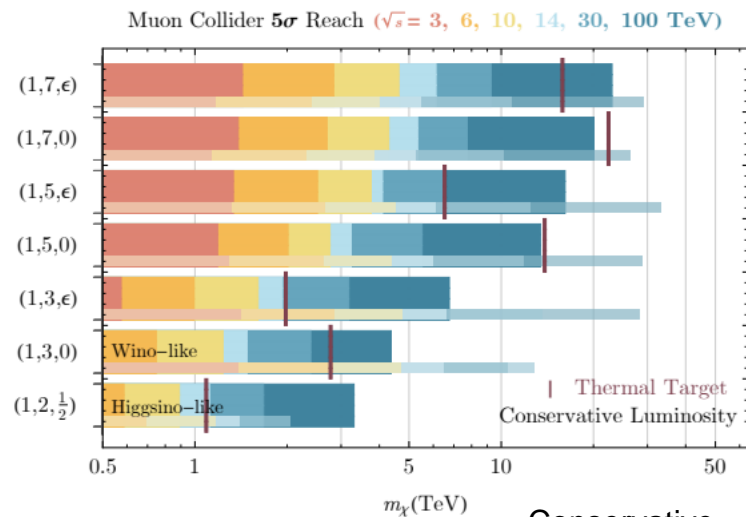
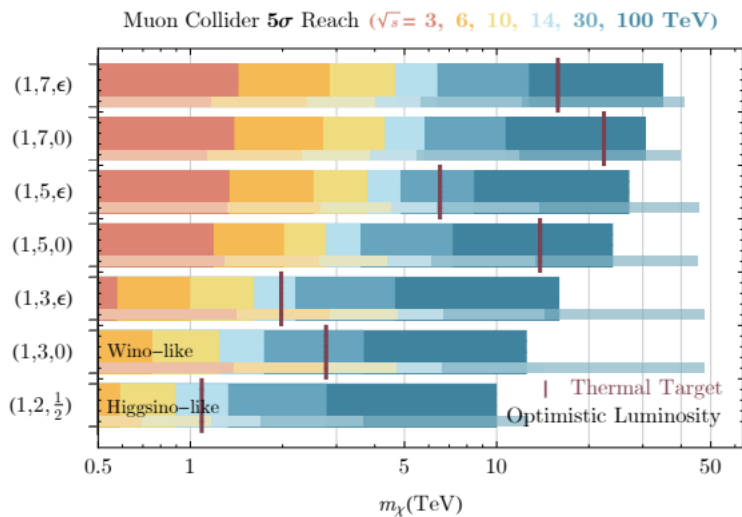
Fig. 6: Left panel: 95% reach on the Composite Higgs scenario from high-energy measurements in di-boson and di-fermion final states [26]. The green contour display the sensitivity from “Universal” effects related with the composite nature of the Higgs boson and not of the top quark. The red contour includes the effects of top compositeness. Right panel: sensitivity to a minimal Z' [26]. Discovery contours at 5σ are also reported in both panels.



Dark Matter Reach

Higgs Smashers Guide, arXiv: 2103.14043

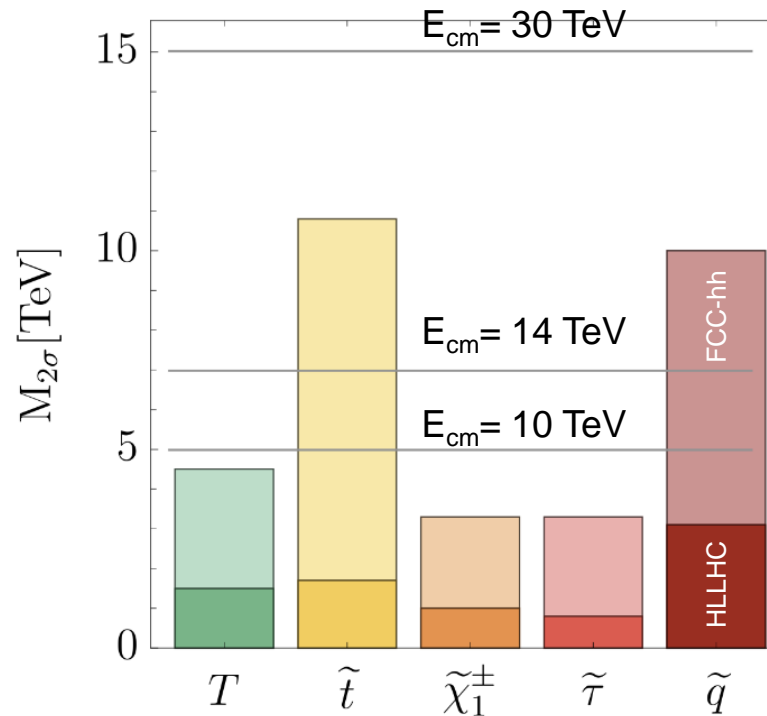
Discovery potential for 10-TeV scale WIMPs for a variety of color/ew/hypercharge multiplets



Conservative == 10ab^{-1}



SUSY sparticle Searches



Of course, FCC-hh wins in colored particle case over 10 TeV μCol



Towards Muon Collider

Critical concepts to demonstrate

- **Target Solenoid**
 - Similar Low Temp Superconductor parameters to ITER Central Solenoid
 - Performance can be improved with a radiation resistant HTS or Cu insert
- **Muon 6D Cooling**
 - MICE Demonstration of Emittance Cooling
 - High gradient demonstration of RF operating in Tesla-class magnetic fields
 - Cooling channel concepts and detailed simulation consistent with operational targets
- **Muon Final Cooling**
 - Advances in HTS conductor/cable/magnet technology
 - High Field User Magnet program operationally demonstrating magnet parameters that are rapidly approaching the MC requirements



Towards Muon Collider ...

Critical concepts to demonstrate

– Muon Acceleration

- Significant recent advancement in HTS-based fast-ramping magnets
- Focused effort on studying the integrated magnet/power supply efficiency issues for TeV-scale acceleration

– Collider and Detector

- Detailed studies of backgrounds that may impact physics
- Detector performance studies now demonstrate the ability to successfully measure key processes
- Concepts in development to manage off-site neutrino radiation issues

See dedicated JINST Volume for key references:

[Muon Accelerators for Particle Physics \(MUON\)](#)

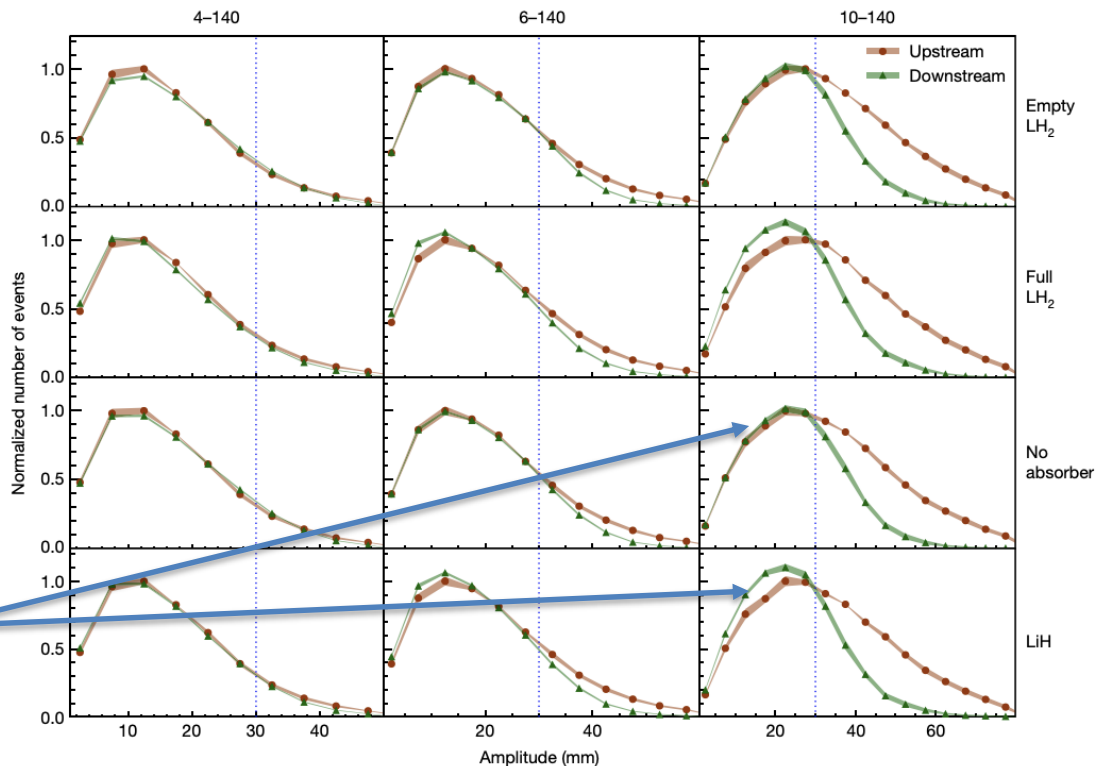
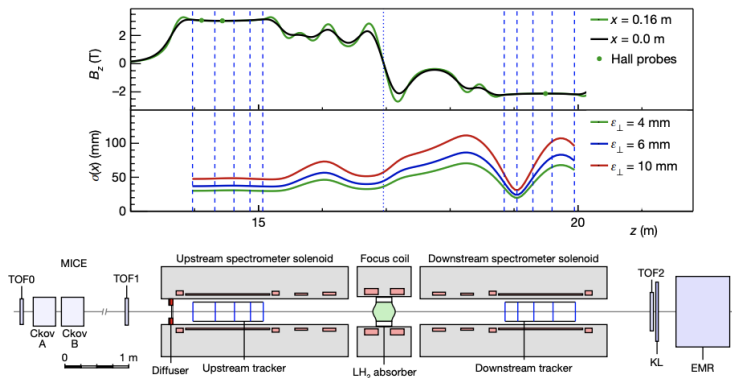


Muon Collider Accelerator Challenges

Beam Production : Demonstration of Ionization Cooling

[Nature, Vol 578, P53](#)

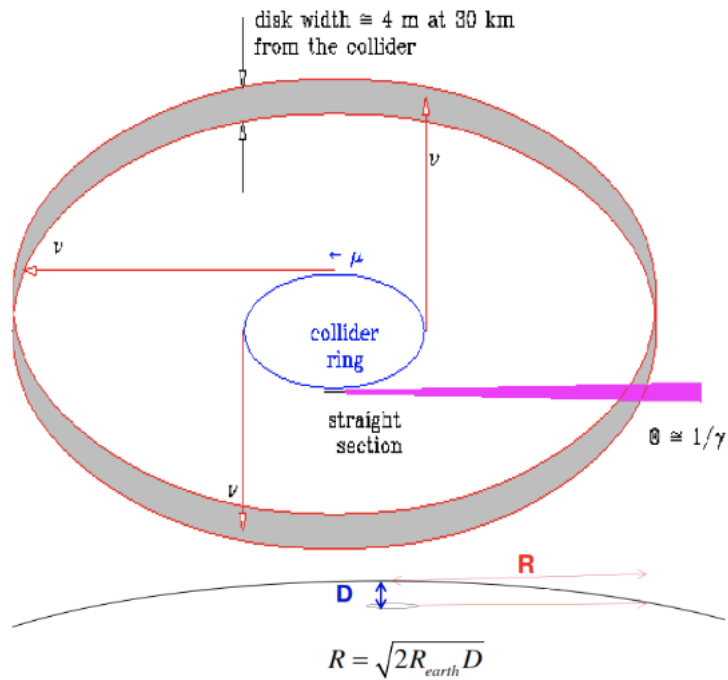
MICE



Increase in particle counts at smaller amplitude with low-Z absorber in place



Neutrino Background?





Muon Collider Accelerator Challenges

Neutrino Radiation Mitigation

Mokhov & Van Ginneken

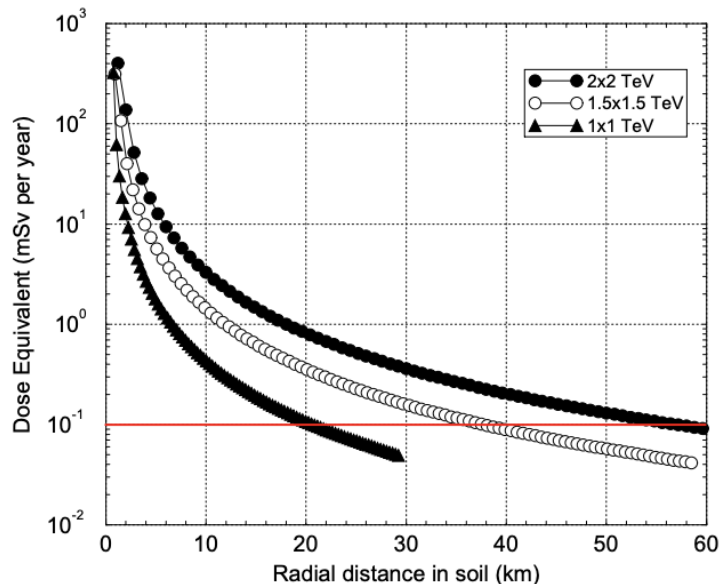


Figure 4: Maximum dose equivalent in TEP embedded in soil in high-energy muon collider orbit plane with 1.2×10^{21} decays per year vs distance from ring center.

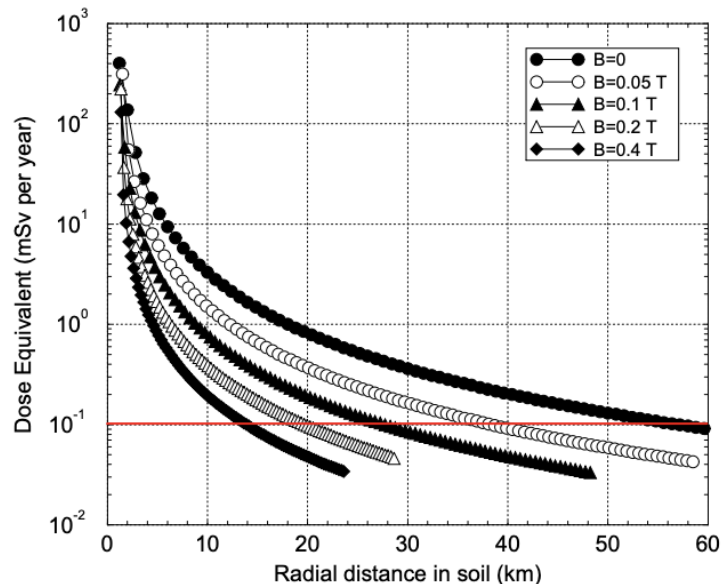


Figure 5: Average dose in TEP located in orbit plane vs distance from ring center in soil around a $2+2$ TeV muon collider with 1.2×10^{21} decays per year for five values of vertical wave field.

Higher the collider energy the deeper the ring needs to be.

Magnetic field to dither the orbit also helps.

LHC Tunnel is 100m deep.



Muon Collider Challenges – Beam Induced Background

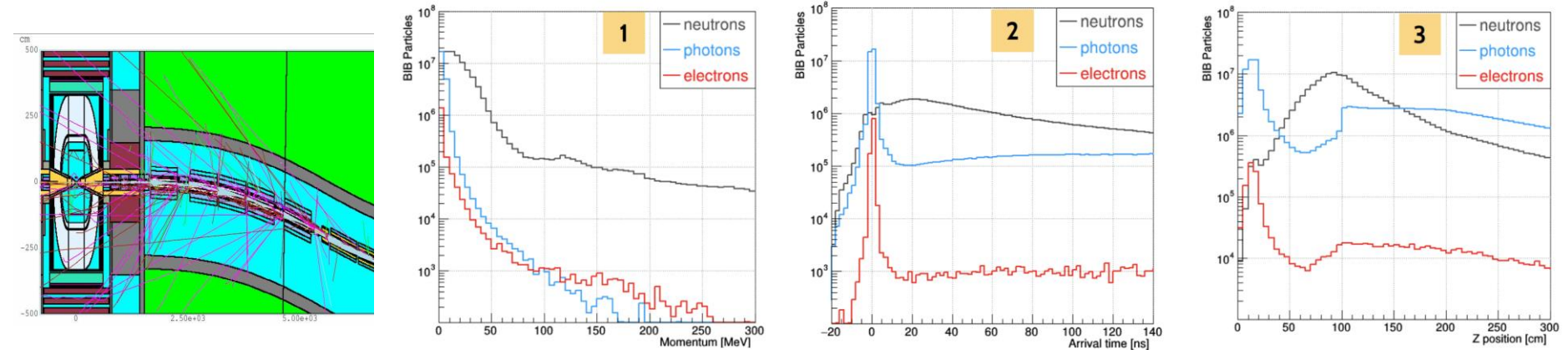


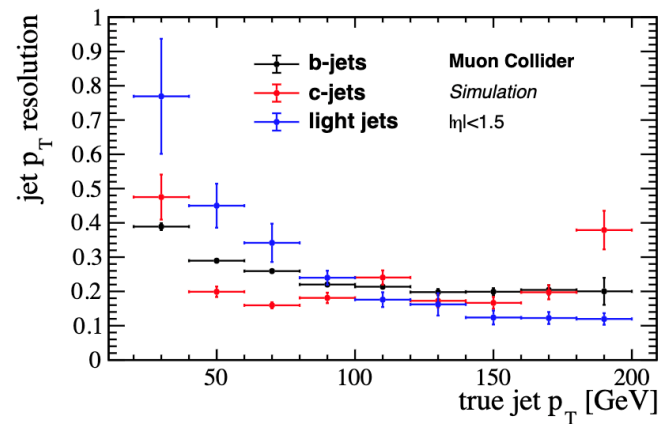
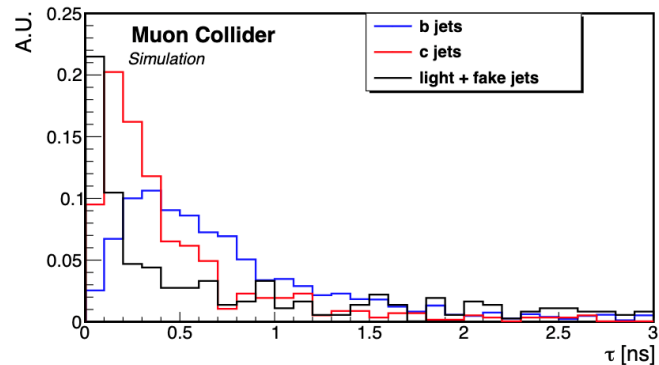
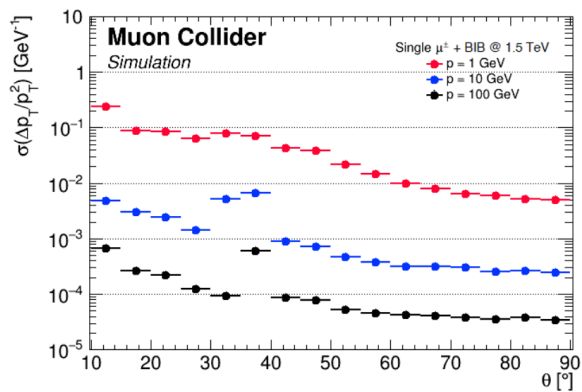
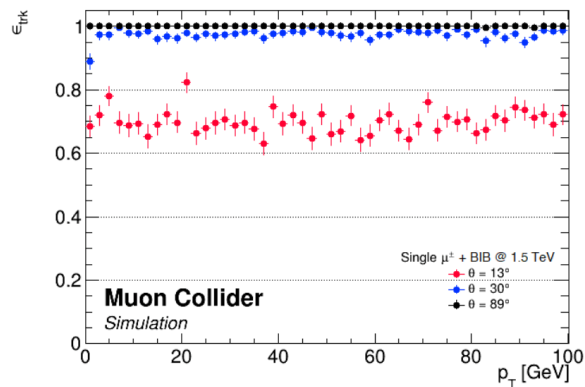
Figure: by N.Bartosik

Mitigation Strategies needed in spite of the optimized conical absorber

- Highly segmented detectors
- Timing cuts and energy cuts
- Doublet tracker design a la CMS tracker



Can we reconstruct stuff?





Muon Collider Challenges

Increased Accelerator R&D is the Key

10+ TeV is NEW Territory \Rightarrow Key Areas of Investigation:

Evaluation of physics potential (including detector technology)

- Impacts of beam induced background

Neutrino Flux Mitigation

- Straight accelerator sections produce intense ν beam - safety

High Energy Systems

- Acceleration sections can impact the energy reach due to cost, power, technical risk, and impact on beam quality
- 10+ TeV Collider designs must be developed and fully evaluated

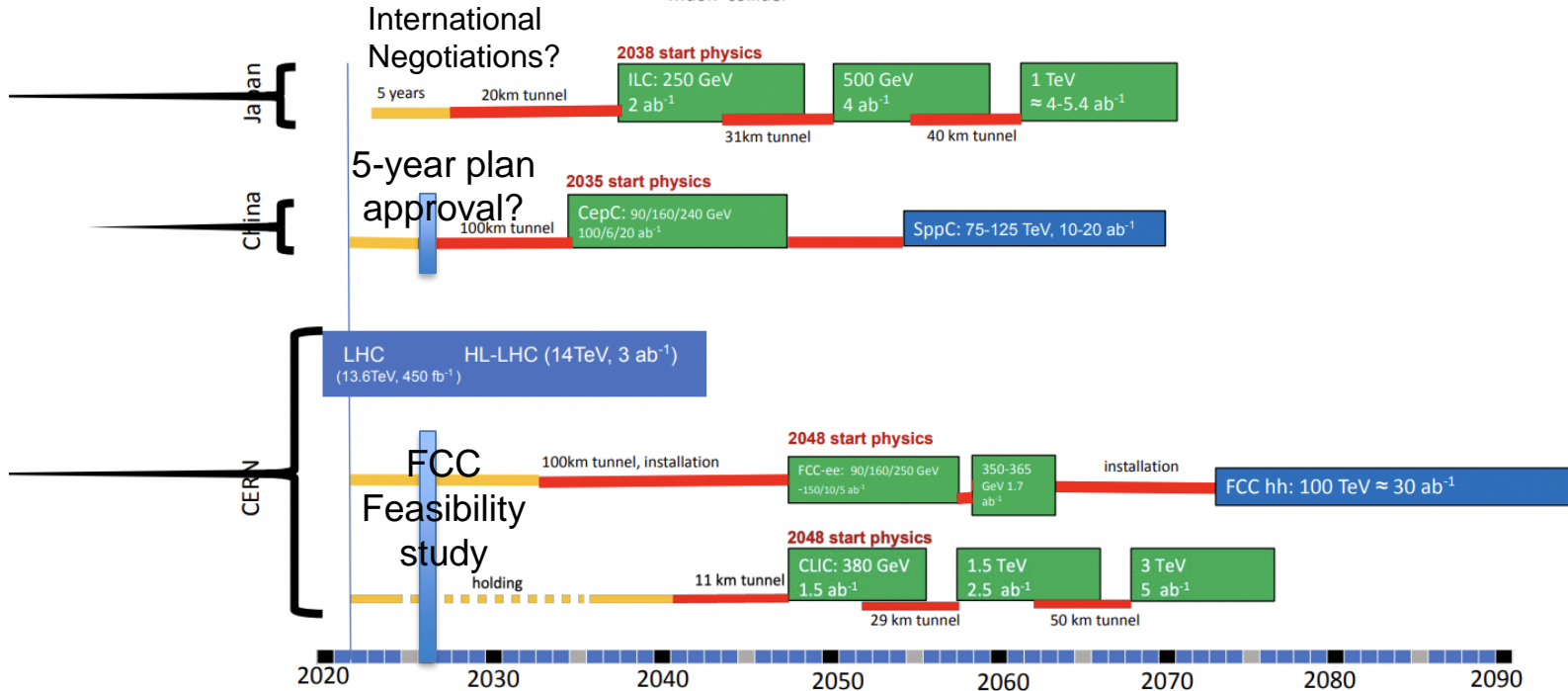
Cooling string demonstration to verify high brightness μ beam delivery



Summary – Asia & Europe

Original from ESG 2020 by UB
Updated July 25, 2022 by MN

- Proton collider
- Electron collider
- Muon collider
- Construction/Transformation
- Preparation / R&D



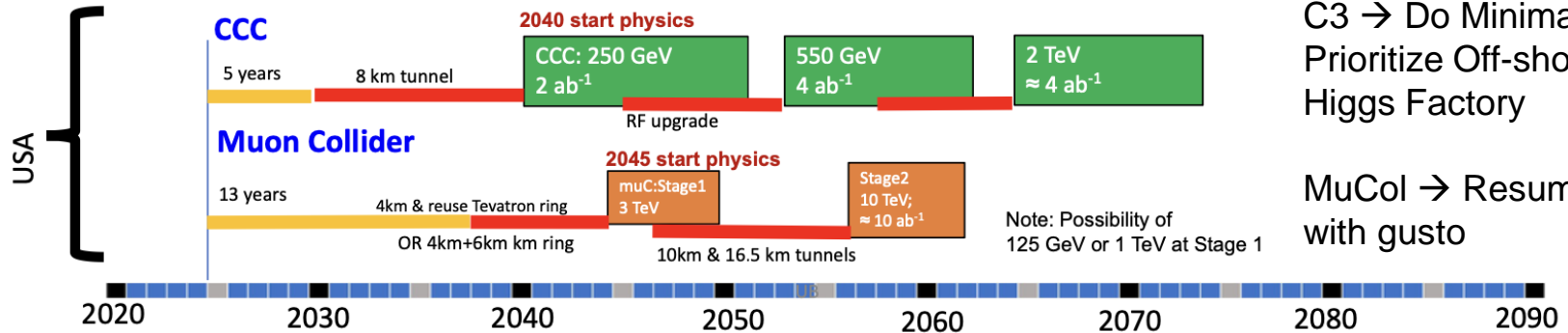


Summary + Invitation



P5

Proposals emerging from Snowmass 2021 for a US based collider



C3 → Do Minimal R&D
Prioritize Off-shore
Higgs Factory

MuCol → Resume R&D
with gusto

Welcome *your* participation in studies – starting with simulations
Accelerators, detector technologies, machine-detector interface ...

Biggest need is accelerator workforce – ideal place for our young to start



Another Invitation!



Lepton Photon 2025, Madison, Wisconsin, USA

Aug 25 – 29, 2025
Monona Convention Center
America/Chicago timezone



<https://agenda.hep.wisc.edu/event/2188/>

Please ask for US Visa letter ~now if you need one