

Jožef Stefan Institute

Probing Heavy Neutrino Magnetic Moments at the LHC Using Non-Pointing Photon Signatures

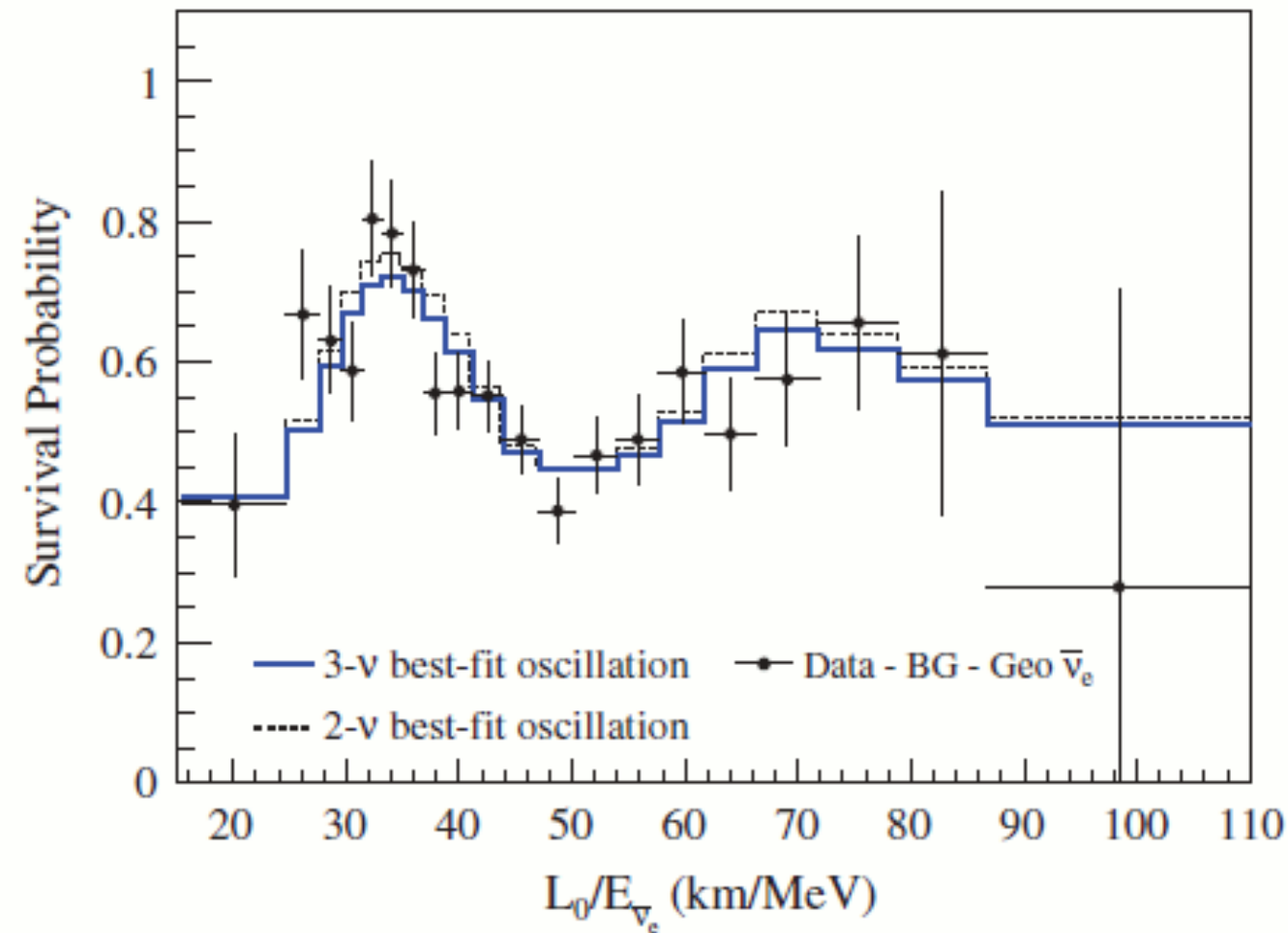
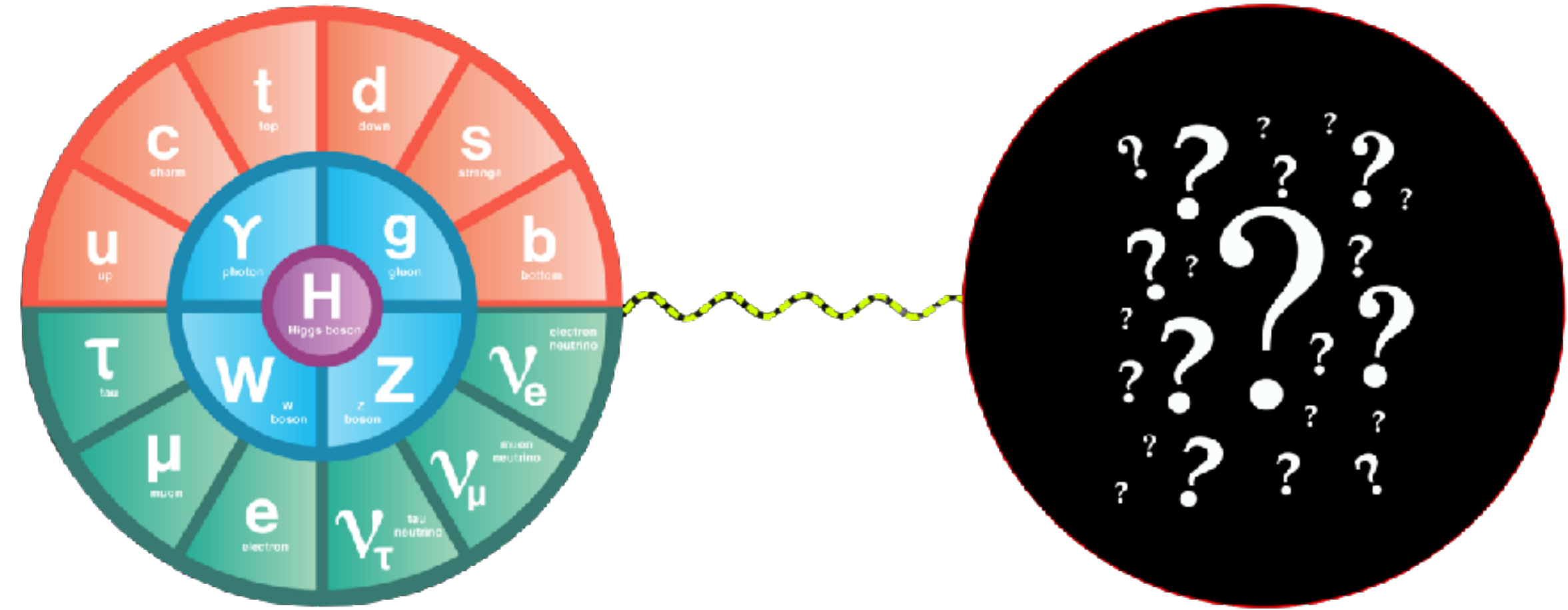
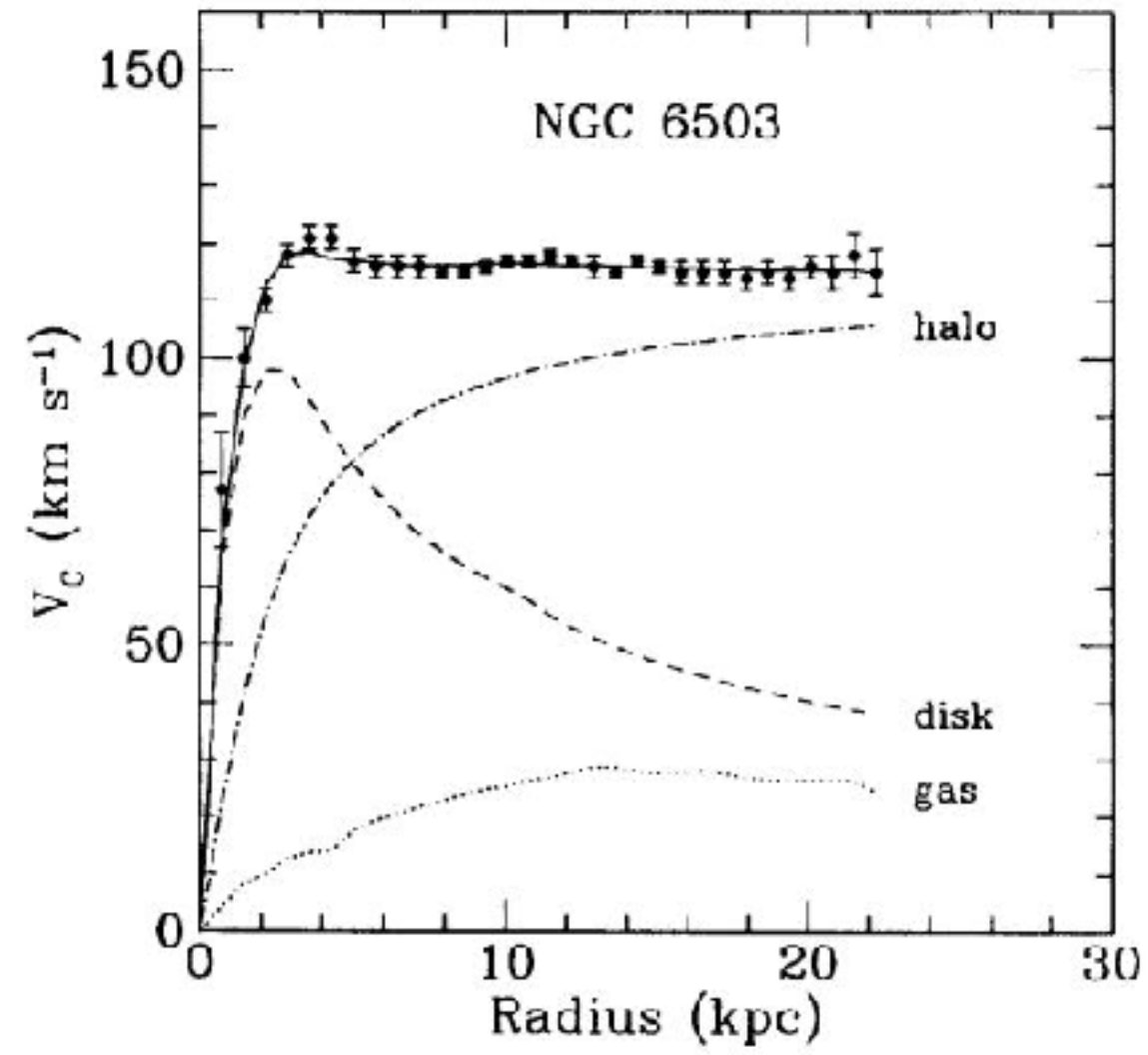
Patrick D. Bolton (Jožef Stefan Institute, Ljubljana)

In collaboration with: Rebeca Beltrán (IFIC), Frank Deppisch (UCL),
Chandan Hati (IFIC) and Martin Hirsch (IFIC)

See: [arXiv:2405.08877](https://arxiv.org/abs/2405.08877)

Heavy Neutral Leptons - where and why?

Unsolved Problems



~~Dark Matter
 Neutrino Masses
 Baryon Asymmetry~~

?
 =

Hidden sector

Right-Handed Neutrinos

Consider N_R (SM gauge singlet), only $U(1)_L$ forbids a mass term:

$$\mathcal{L}_{\text{SM}+N_R} \supset \mathcal{L}_{\text{SM}} + i\bar{N}_R \not{\partial} N_R - \left[\bar{L} Y_\nu N_R \tilde{H} + \frac{1}{2} \bar{N}_R^c M_R N_R + \text{h.c.} \right]$$

Extended neutrino mass matrix:

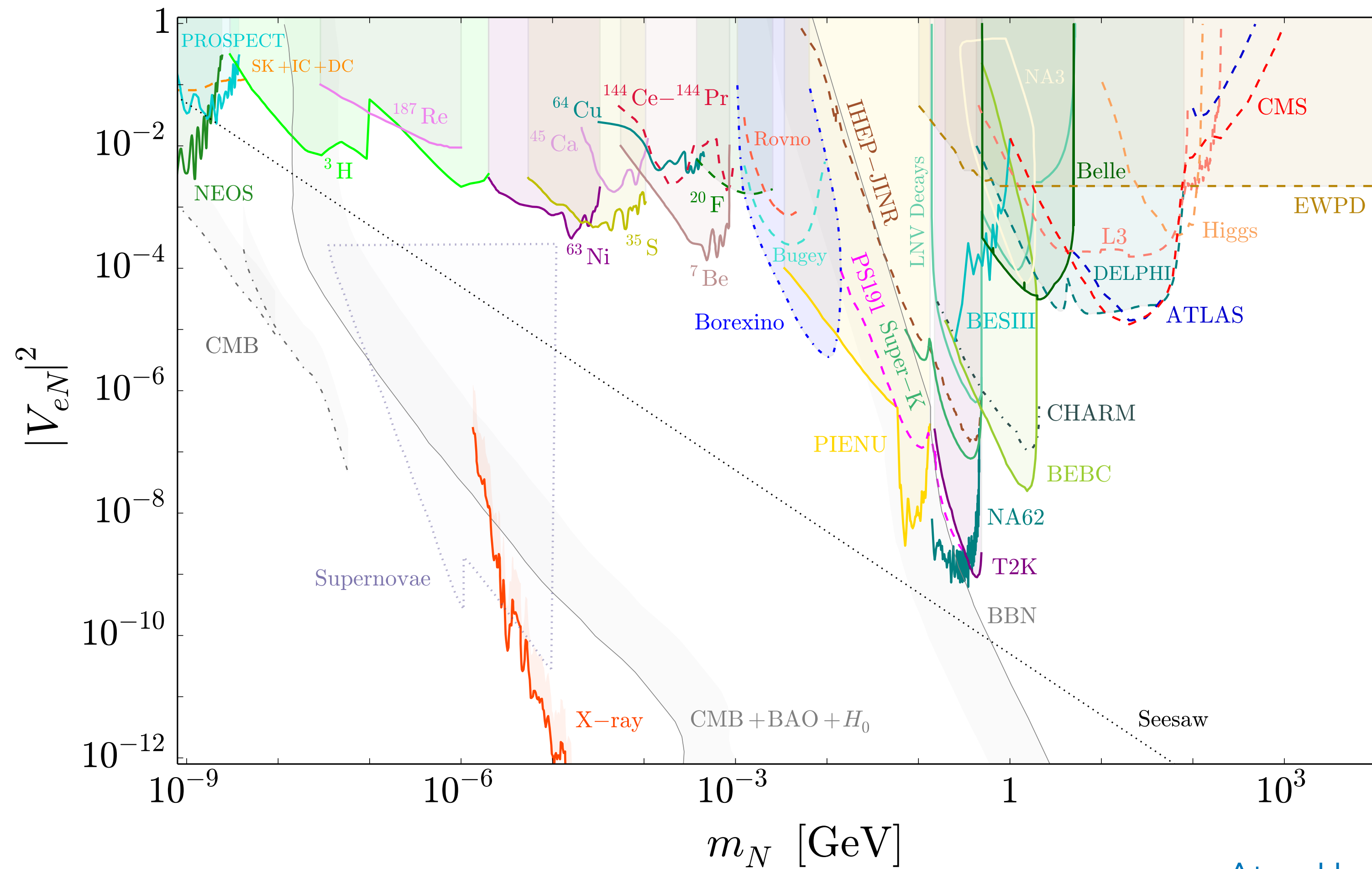
$$-\frac{1}{2} \begin{pmatrix} \bar{\nu}_L & \bar{N}_R^c \end{pmatrix} \begin{pmatrix} 0 & M_D \\ M_D^T & M_R \end{pmatrix} \begin{pmatrix} \nu_L^c \\ N_R \end{pmatrix} + \text{h.c.}, \quad M_D = \frac{v}{\sqrt{2}} Y_\nu$$

Diagonalise: Light neutrino masses if $M_D \ll M_R$ or $U(1)_L$ is approximately conserved

$$[M_\nu]_{\alpha\beta} = U_{\alpha i} U_{\beta i} m_i \approx -[M_D M_R^{-1} M_D^T]_{\alpha\beta} \quad V_{\alpha N_i} = i U_{\alpha j} \mathcal{R}_{ji} \sqrt{\frac{m_j}{m_{N_i}}}$$

Resulting heavy states: **Majorana** (Type-I seesaw) or **pseudo-Dirac** (inverse seesaw) fermions

Active-Sterile Mixing Phenomenology



$$\mathcal{L} \supset \left[-\frac{g}{\sqrt{2}} V_{\alpha N_i} \bar{\ell}_\alpha \not{W} P_L N_i + \text{h.c.} \right] - \frac{g}{2c_W} \left[V_{\alpha N_i} \bar{\nu}_\alpha \not{Z} P_L N_i + V_{\alpha N_i}^* V_{\alpha N_j} \bar{N}_i \not{Z} P_L N_j \right]$$

Atre, Han, Pascoli, Zhang, 0901.3589

Bondarenko et al., 1805.08567

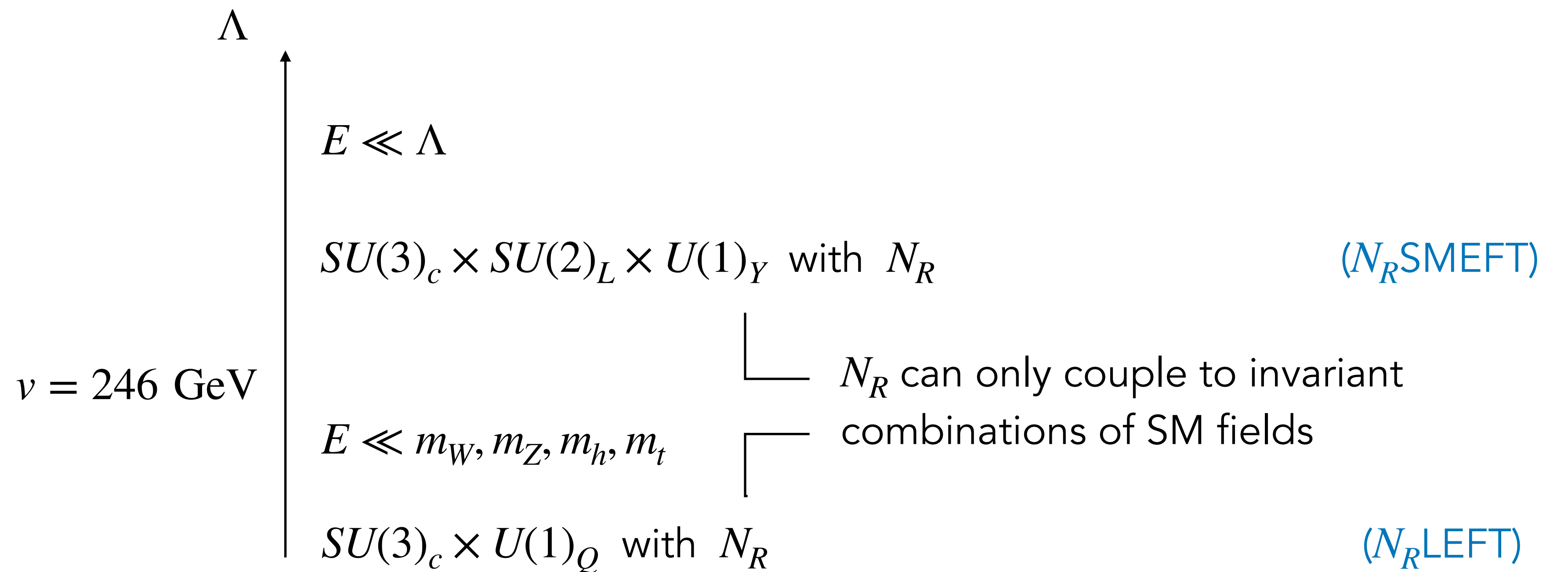
PDB, Deppisch, Dev, 1912.03058

Coloma et al., 2007.03701

Beyond the Renormalisable: SMEFT + N_R

If N_R is coupled to some heavy new physics at the scale Λ :

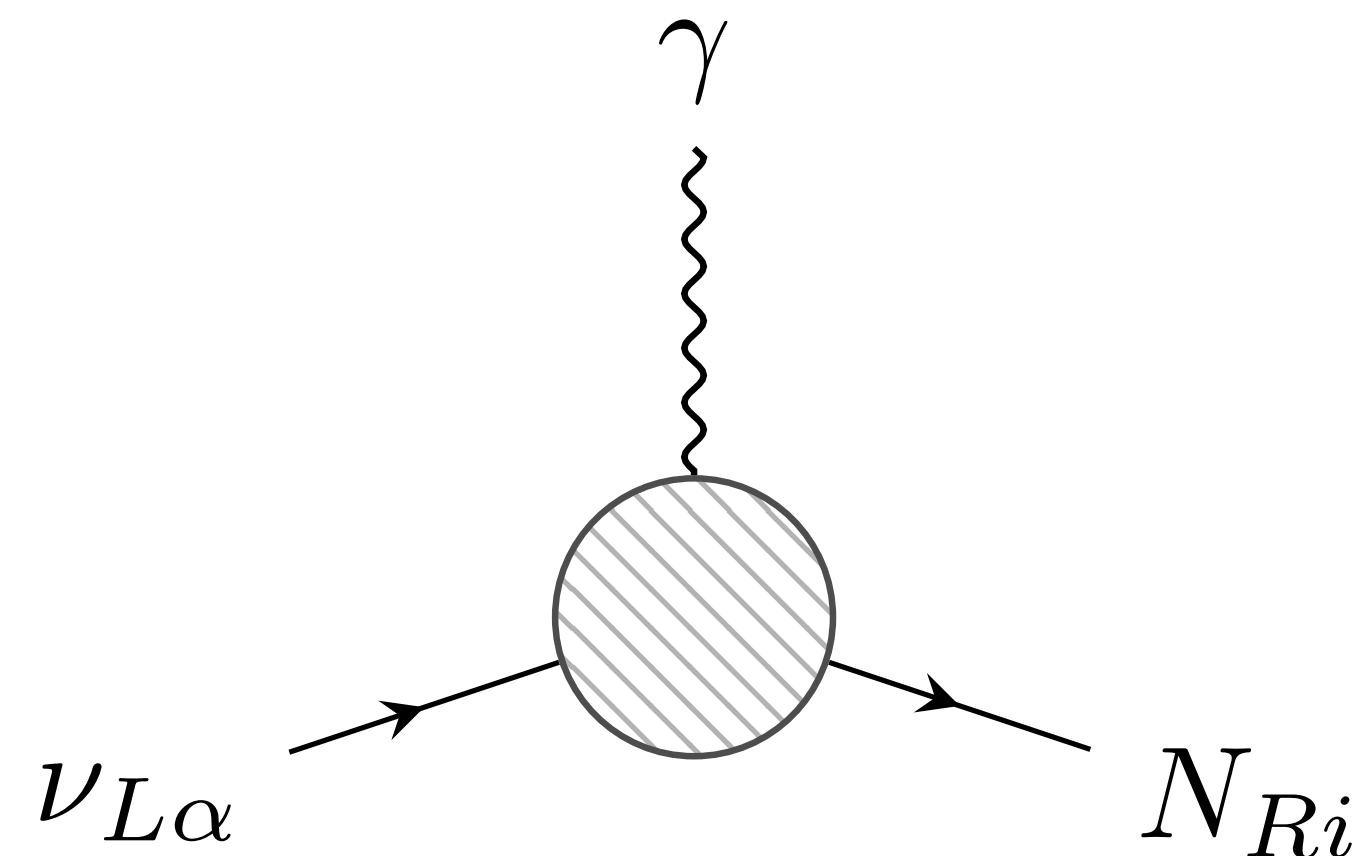
$$\mathcal{L} = \mathcal{L}_{\text{SM}+N_R} + \sum_i C_i^{(d)} \mathcal{O}_i^{(d)} \quad C_i^{(d)} \propto \Lambda^{4-d}$$



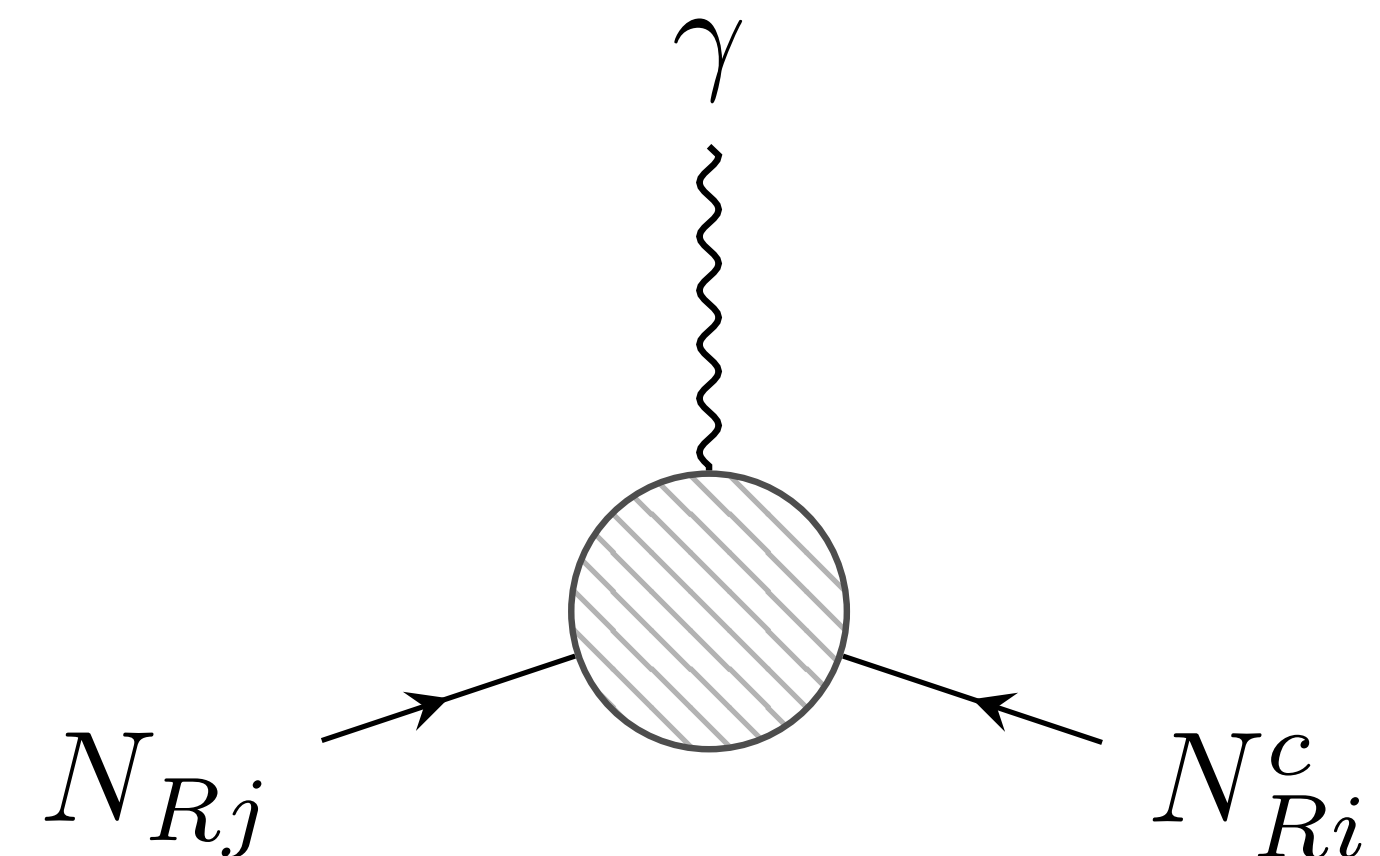
Active-to-Sterile and Sterile-to-Sterile Neutrino Magnetic Moments

In the N_R LEFT, magnetic moments of RH fields are described by the operators:

$$\mathcal{O}_{\nu N\gamma} = (\bar{\nu}_L \sigma_{\mu\nu} N_R) F^{\mu\nu}$$



$$\mathcal{O}_{NN\gamma} = (\bar{N}_R^c \sigma_{\mu\nu} N_R) F^{\mu\nu}$$



Phenomenology:

- Neutrino upscattering (solar ν , CE ν NS)
- Meson Decays (Dalitz-like)
- Supernova cooling (SN1987A)
- Monophoton + E_T^{miss} , Γ_Z^{inv} at LEP, LHC

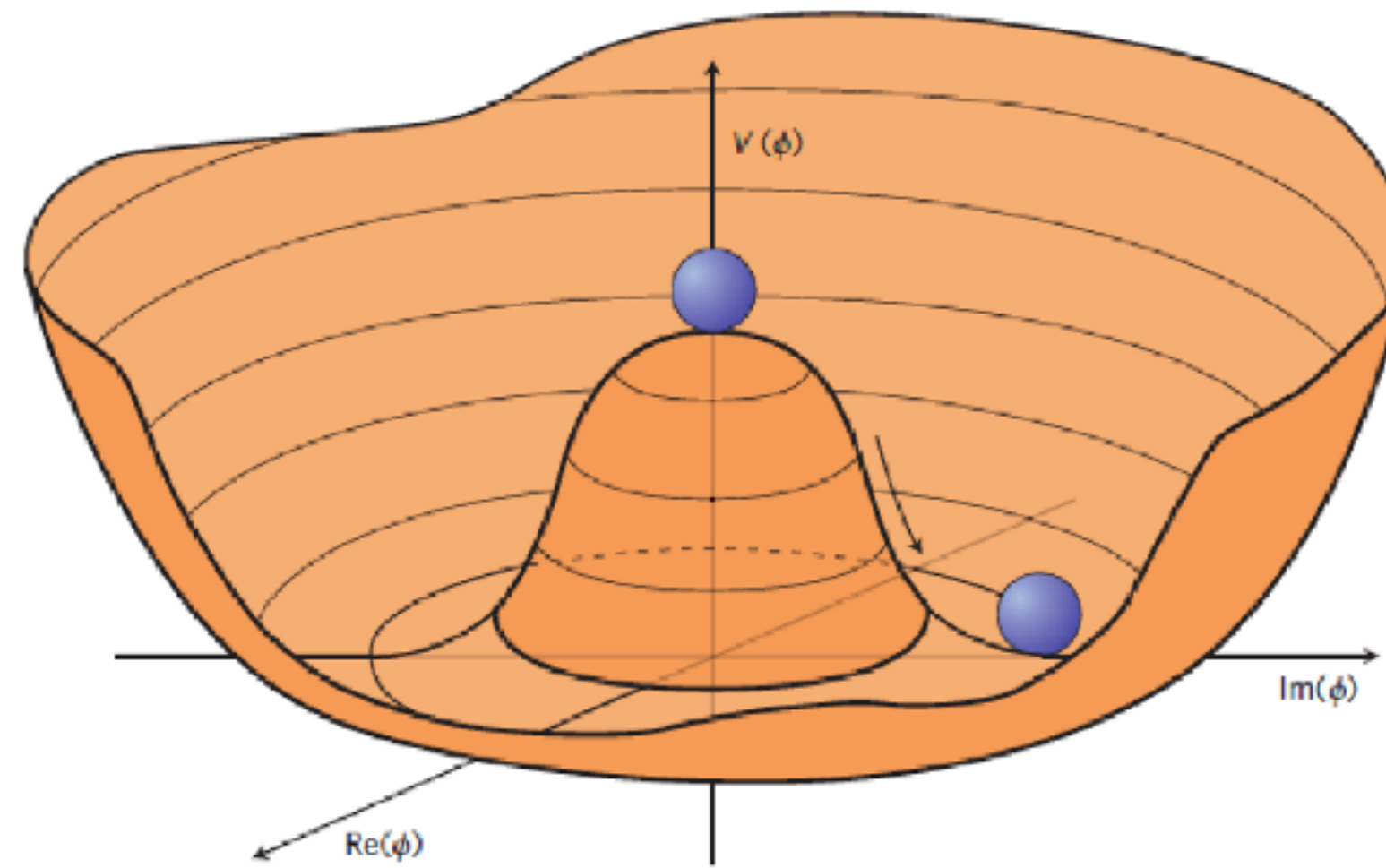
- Meson Decays (Dalitz-like)
- Supernova cooling (SN1987A)
- Monophoton + E_T^{miss} , Γ_Z^{inv} , at LEP, LHC

From the SMEFT

These are induced by the N_R SMEFT operators:

$$\mathcal{O}_{NNB}^{(5)} = (\bar{N}_R^c \sigma_{\mu\nu} N_R) B^{\mu\nu}$$

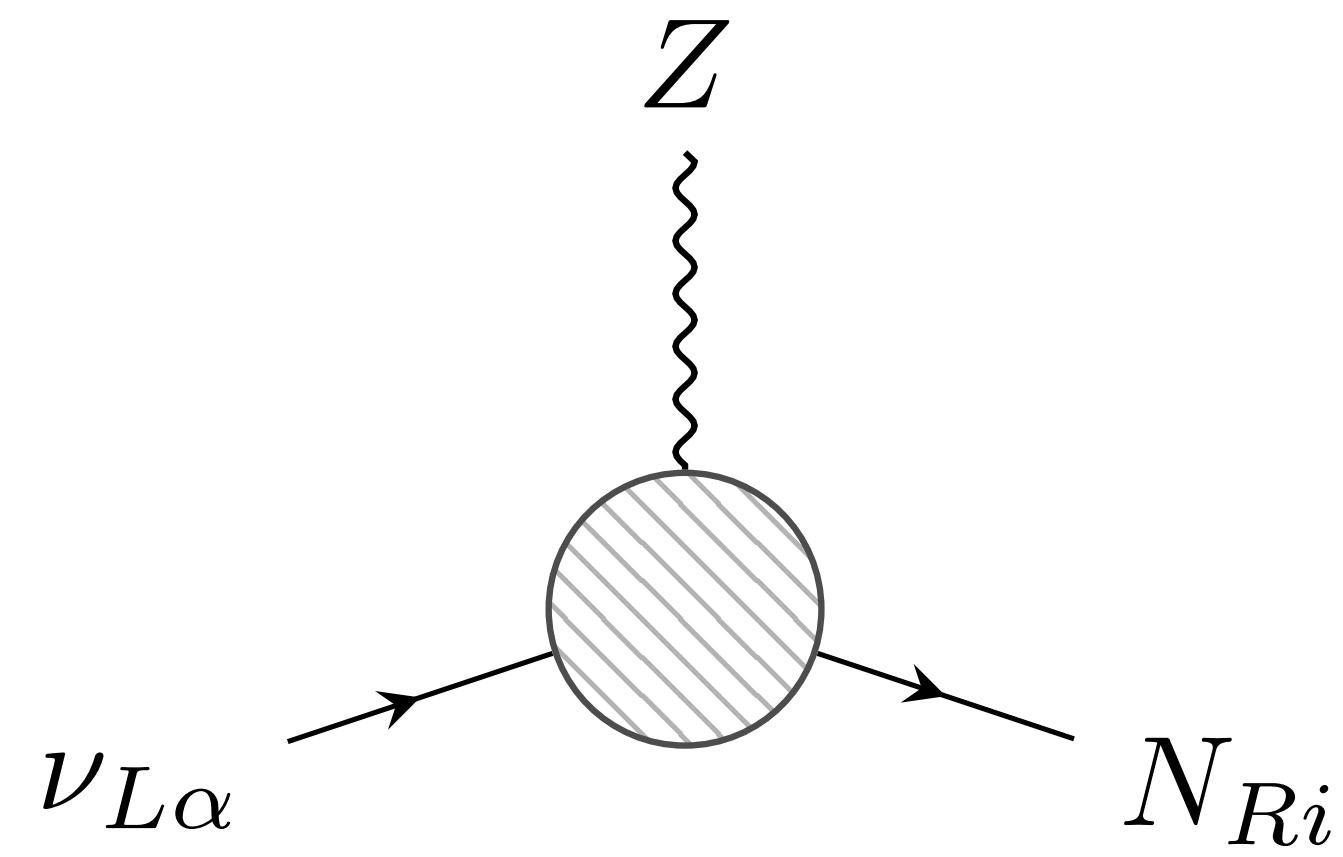
$$\mathcal{O}_{NB}^{(6)} = (\bar{L} \sigma_{\mu\nu} N_R) \tilde{H} B^{\mu\nu} \quad \mathcal{O}_{NW}^{(6)} = (\bar{L} \sigma_{\mu\nu} N_R) \tau^I \tilde{H} W^{I\mu\nu}$$



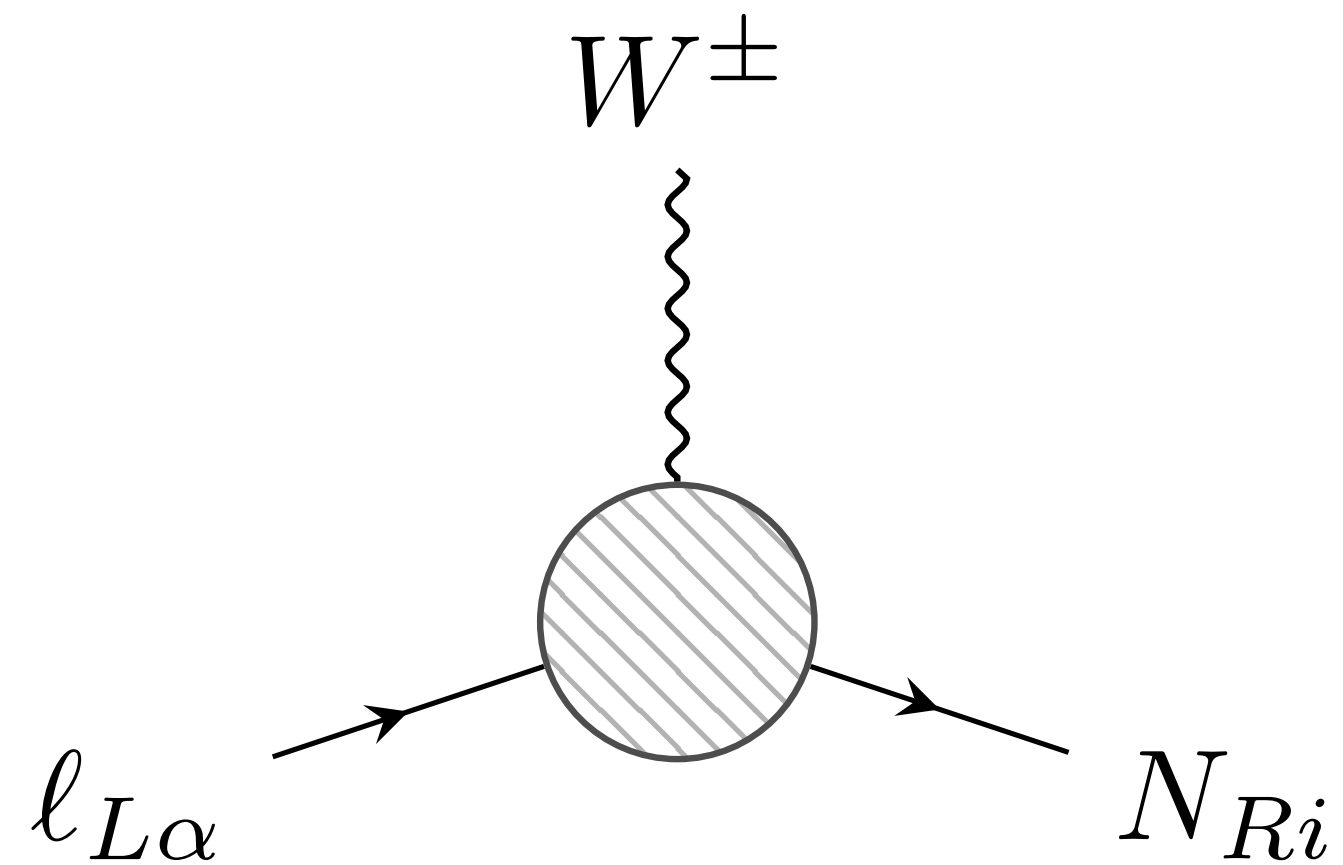
$$H = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v + h \end{pmatrix} \longrightarrow d_{NN\gamma}^{ij} = c_w C_{NNB}^{(5)ij} \quad d_{\nu N\gamma}^{\alpha i} = \frac{v}{\sqrt{2}} \left(c_w C_{NB}^{(6)\alpha i} + \frac{s_w}{2} C_{NW}^{(6)\alpha i} \right)$$

Electroweak Dipole Moments

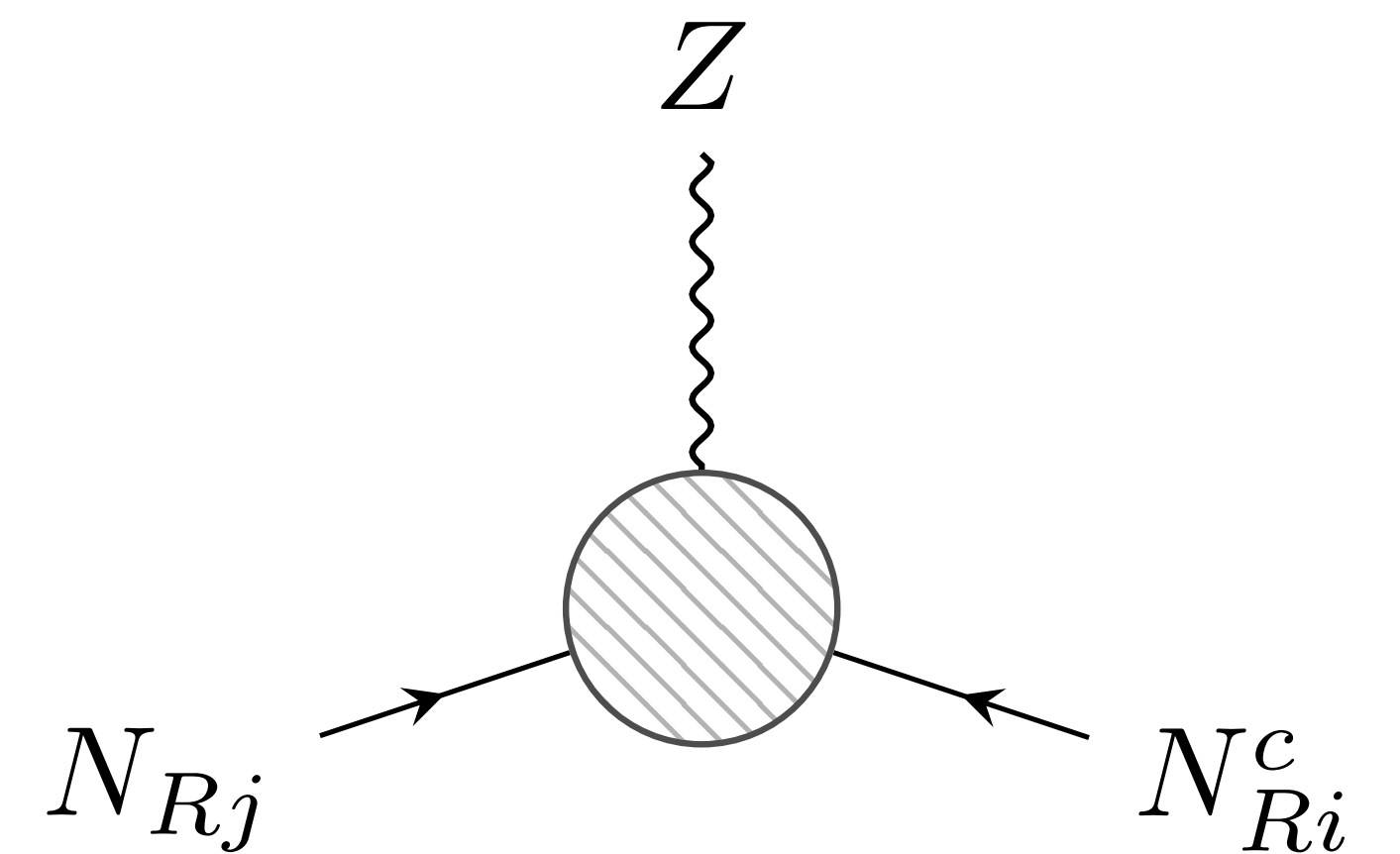
For high-energy collider processes, also relevant are



$$\mathcal{O}_{\nu NZ} = (\bar{\nu}_L \sigma_{\mu\nu} N_R) Z^{\mu\nu}$$



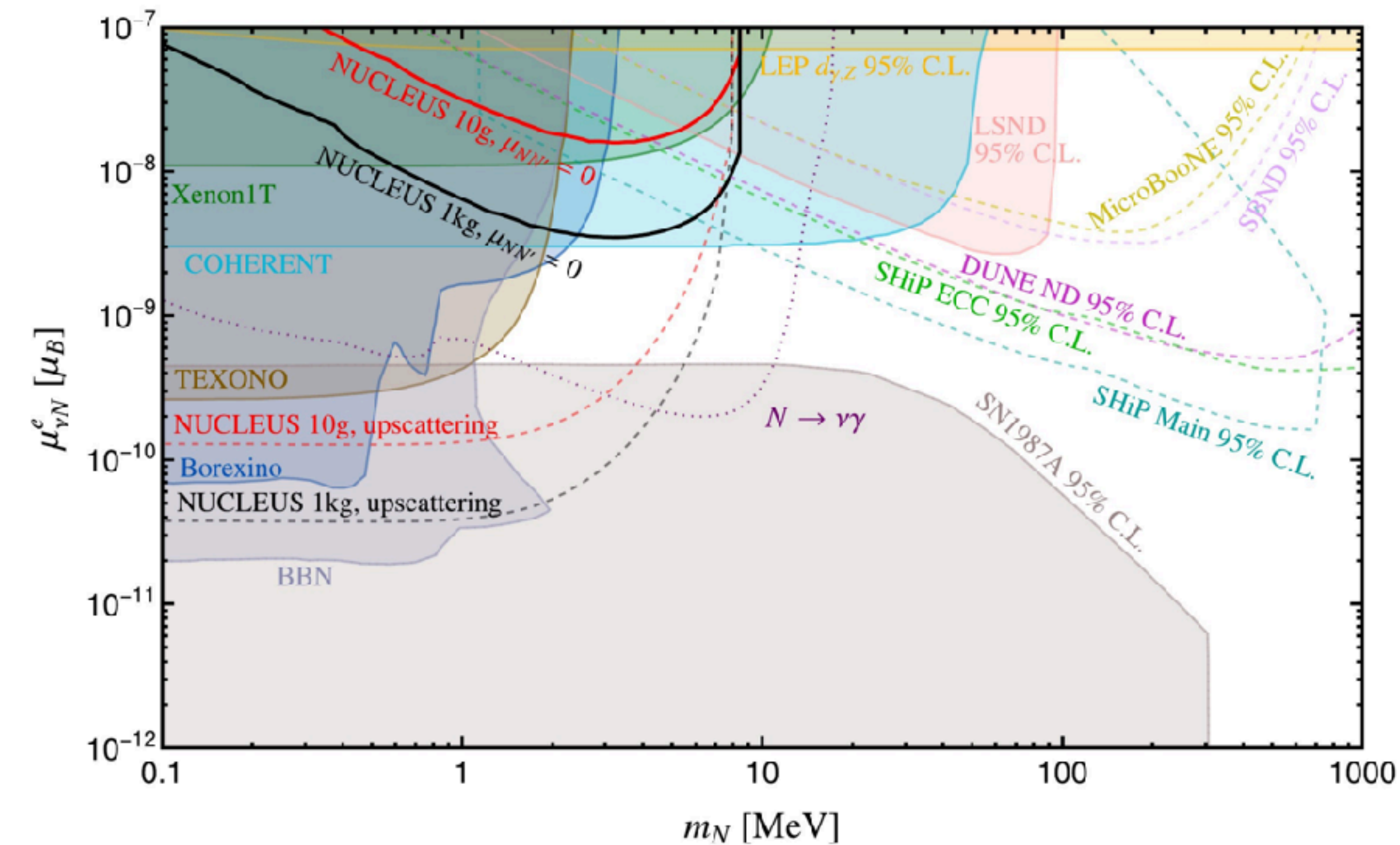
$$\mathcal{O}_{\ell NW} = (\bar{\ell}_L \sigma_{\mu\nu} N_R) W^{\mu\nu}$$



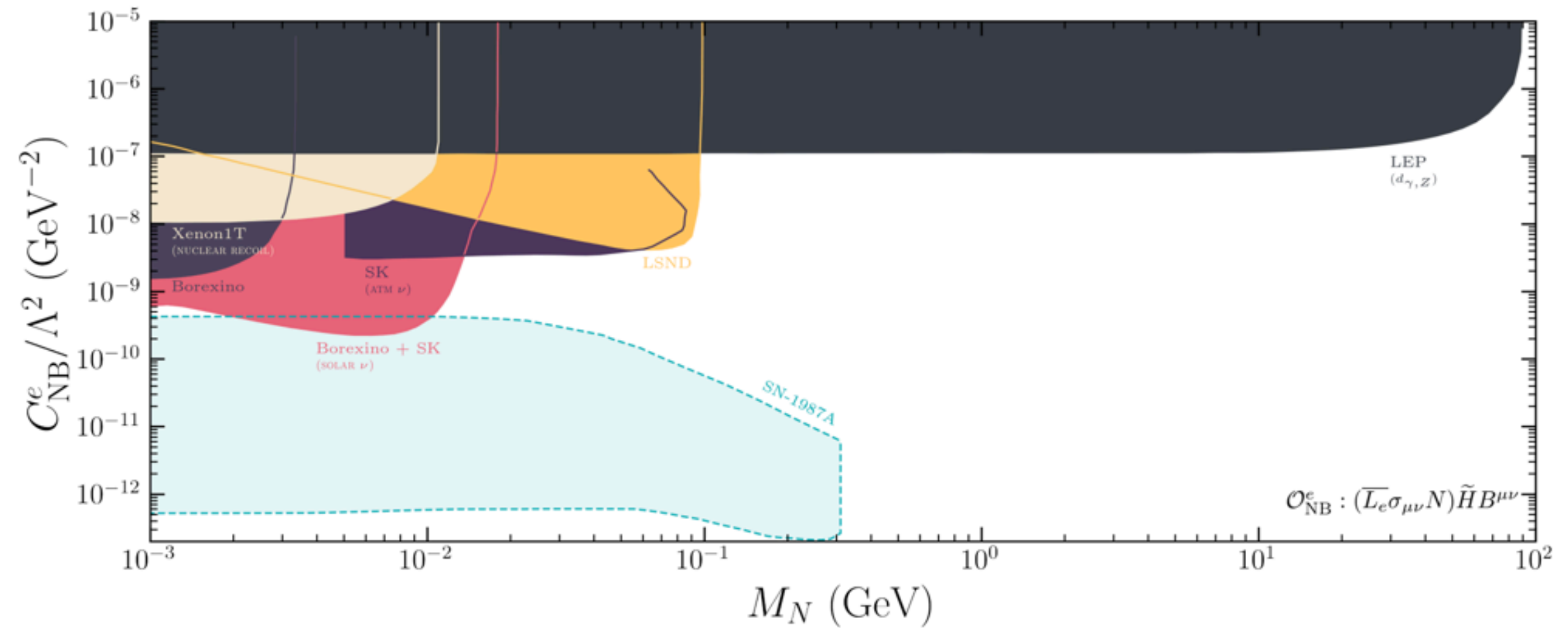
$$\mathcal{O}_{NNZ} = (\bar{N}_R^c \sigma_{\mu\nu} N_R) Z^{\mu\nu}$$

Current Bounds: Active-Sterile Dipole Moments

PDB, Deppisch, Fridell, Harz, Hati, Kulkarni, 2110.02233



Fernández-Martínez et al., 2304.06772



- Neutrino upscattering (solar ν , $CE\nu NS$)
- Meson Decays (Dalitz-like)
- Supernova cooling (SN1987A)
- Monophoton + E_T^{miss} , Γ_Z^{inv} at LEP, LHC

Patrick D. Bolton, IJS, PPC 2024

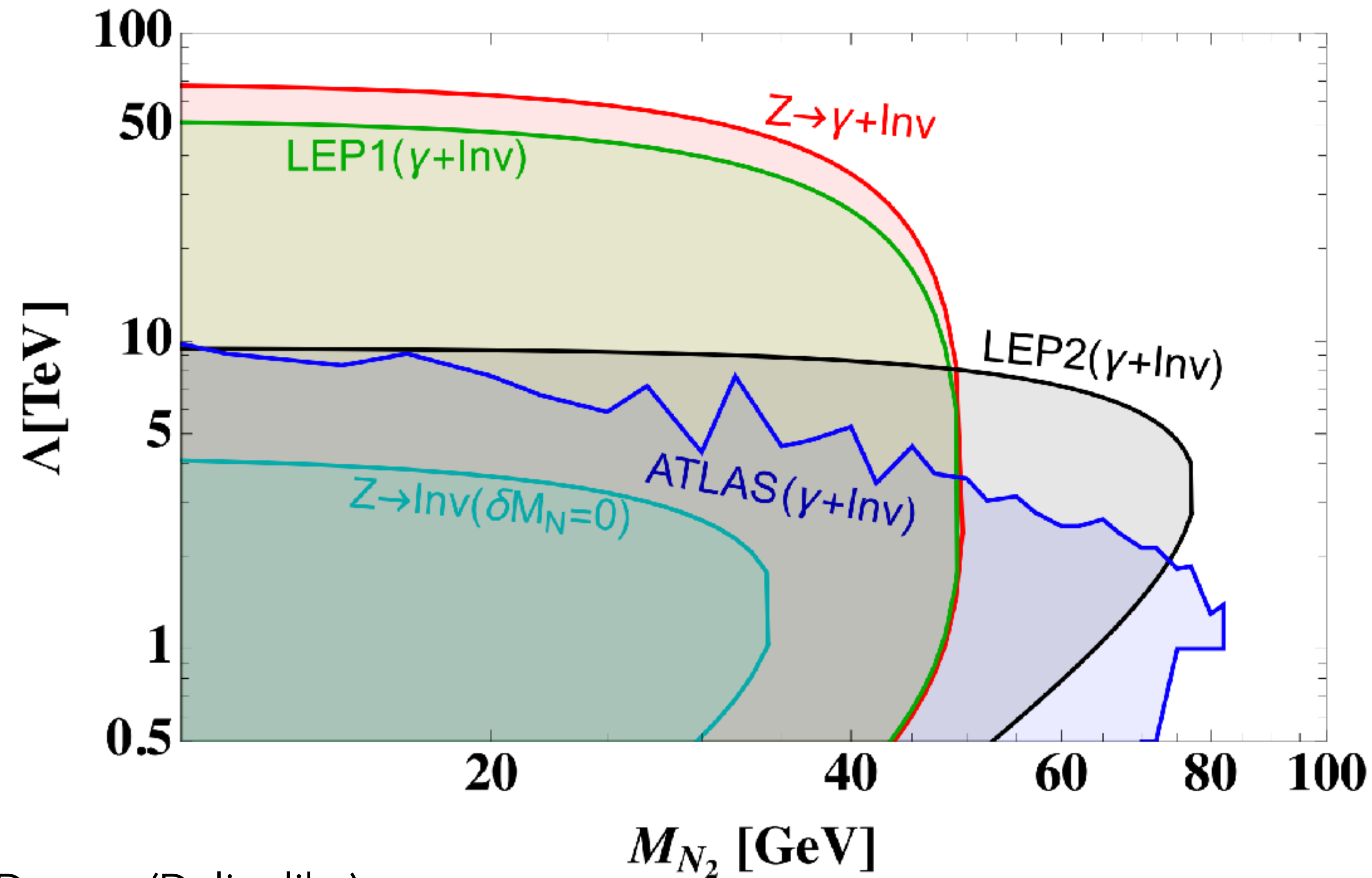
Magill, Plestid, Pospelov, Tsai, 1803.03262

Brdar, Greljo, Kopp, Opferkuch, 2007.15563

Schwetz, Zhou, Zhu, 2105.09699

Barducci, Liu, Titov, Wang, Zhang, 2308.16608

Current Bounds: Sterile-Sterile Dipole Moments



$$C_{NNB}^{(5)} = \frac{1}{\Lambda}$$

Bounds depend on $m_{N_2} - m_{N_1}$

- Meson Decays (Dalitz-like)
- Supernova cooling (SN1987A)
- Monophoton + E_T^{miss} , Γ_Z^{inv} , at LEP, LHC

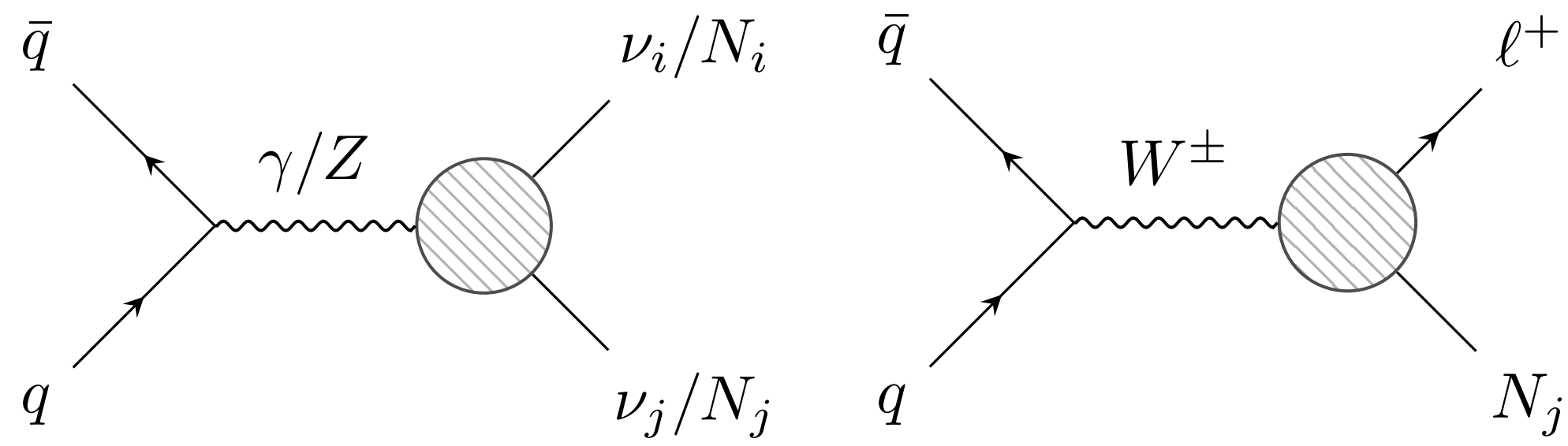
Delgado, Duarte, Jones-Pérez, Manrique-Chavil, Pēna, 2205.13550

Barducci, Bertuzzo, Taoso, Toni, 2209.13469

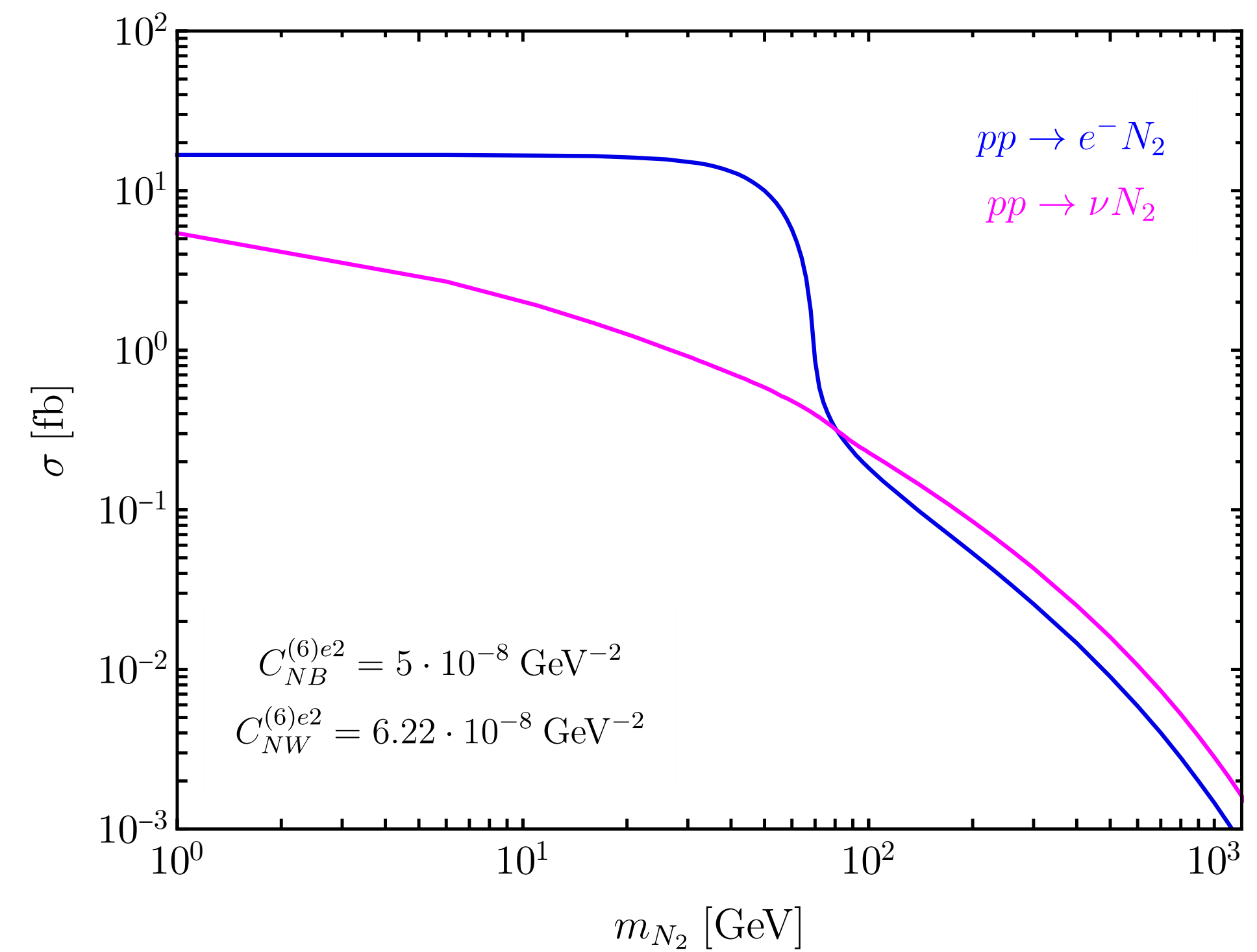
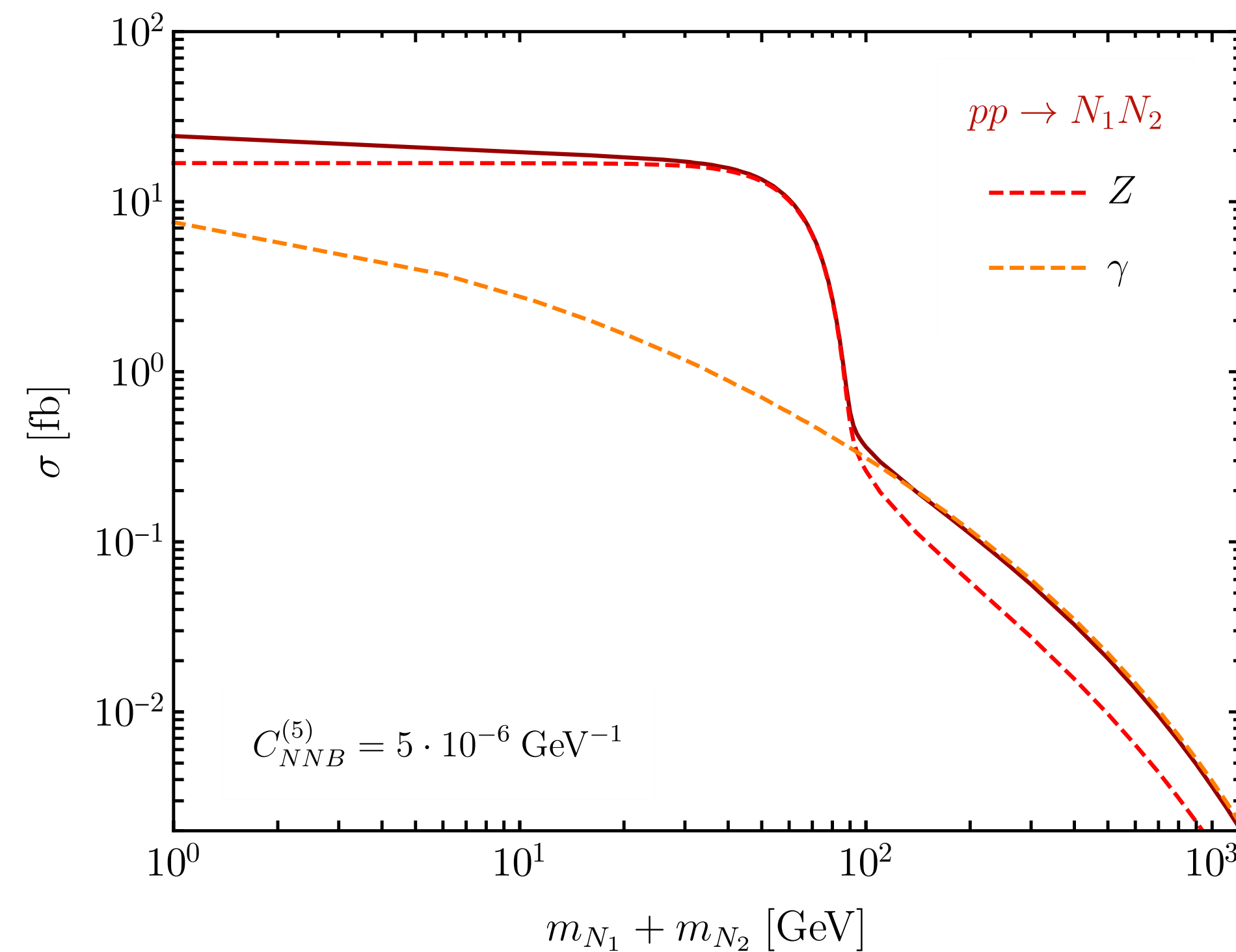
Chun, Mandal, Padhan, 2401.05174

Displaced Vertex Searches with Non-Pointing Photons at LHC

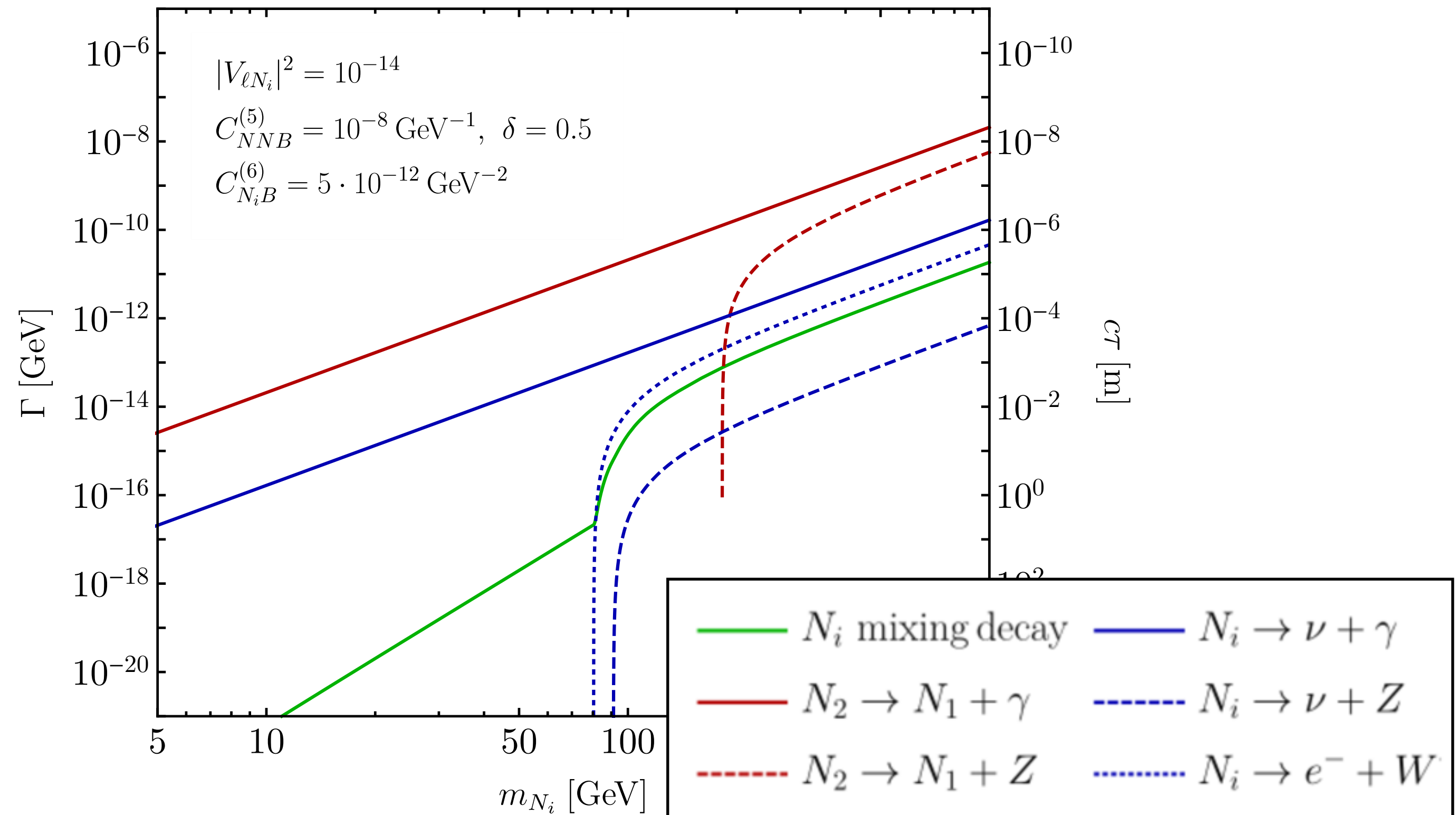
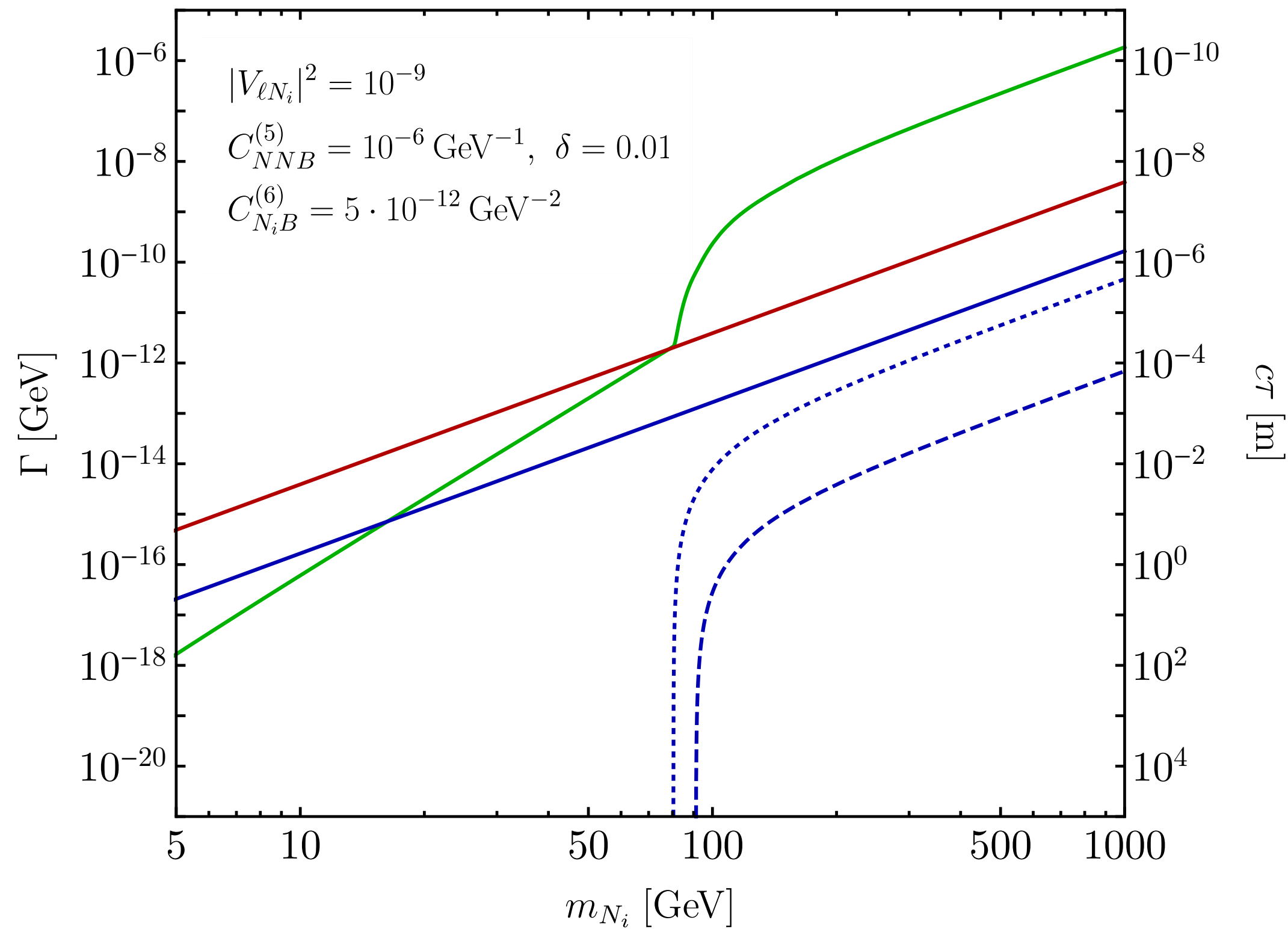
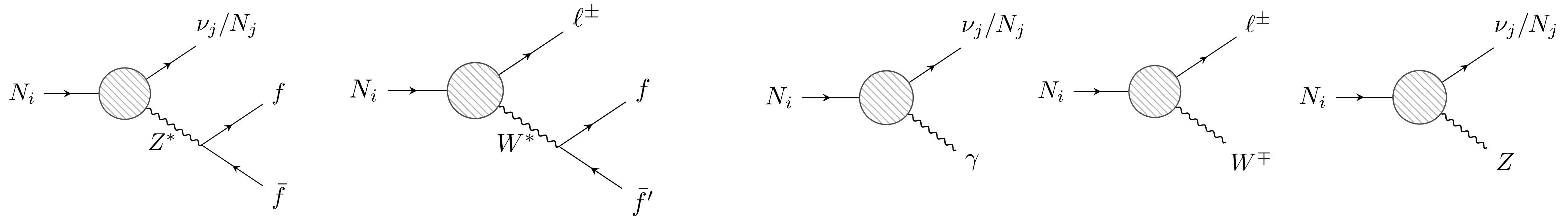
HNL Production



$$d\sigma(pp \rightarrow N_i N_j X) = \sum_q \int_0^1 dx_1 \int_0^1 dx_2 (f_q(x_1, \hat{s}) f_{\bar{q}}(x_2, \hat{s}) + q \leftrightarrow \bar{q}) d\hat{\sigma}(q\bar{q} \rightarrow N_1 N_2)$$



HNL Decays



Possible Scenarios

With active-sterile mixing ($V_{\alpha N}$), active-to-sterile dipole moments ($C_{NB}^{(6)}$) and sterile-to-sterile moments ($C_{NNB}^{(5)}$)

↳ Each coupling can dominate production and decay (limiting cases are taken as 9 benchmarks)

Prod. \ Dec.	$C_{NNB}^{(5)}$	$C_{NB}^{(6)}, C_{NW}^{(6)}$	V_{eN}
$C_{NNB}^{(5)}$	(B1)	(B2)	(B3)
$C_{NB}^{(6)}, C_{NW}^{(6)}$	(B4)	(B5)	(B6)
V_{eN}	(B7)	(B8)	Minimal scenario

Production and decay via mixing $V_{\alpha N}$

Displaced Vertex Signatures: Non-Pointing Photons

Non-pointing photons can be emitted in the decay of LLP N

- └─> Occur at secondary vertex, displaced from **primary vertex** (PV)
- └─> Motivation: Significantly reduce SM backgrounds

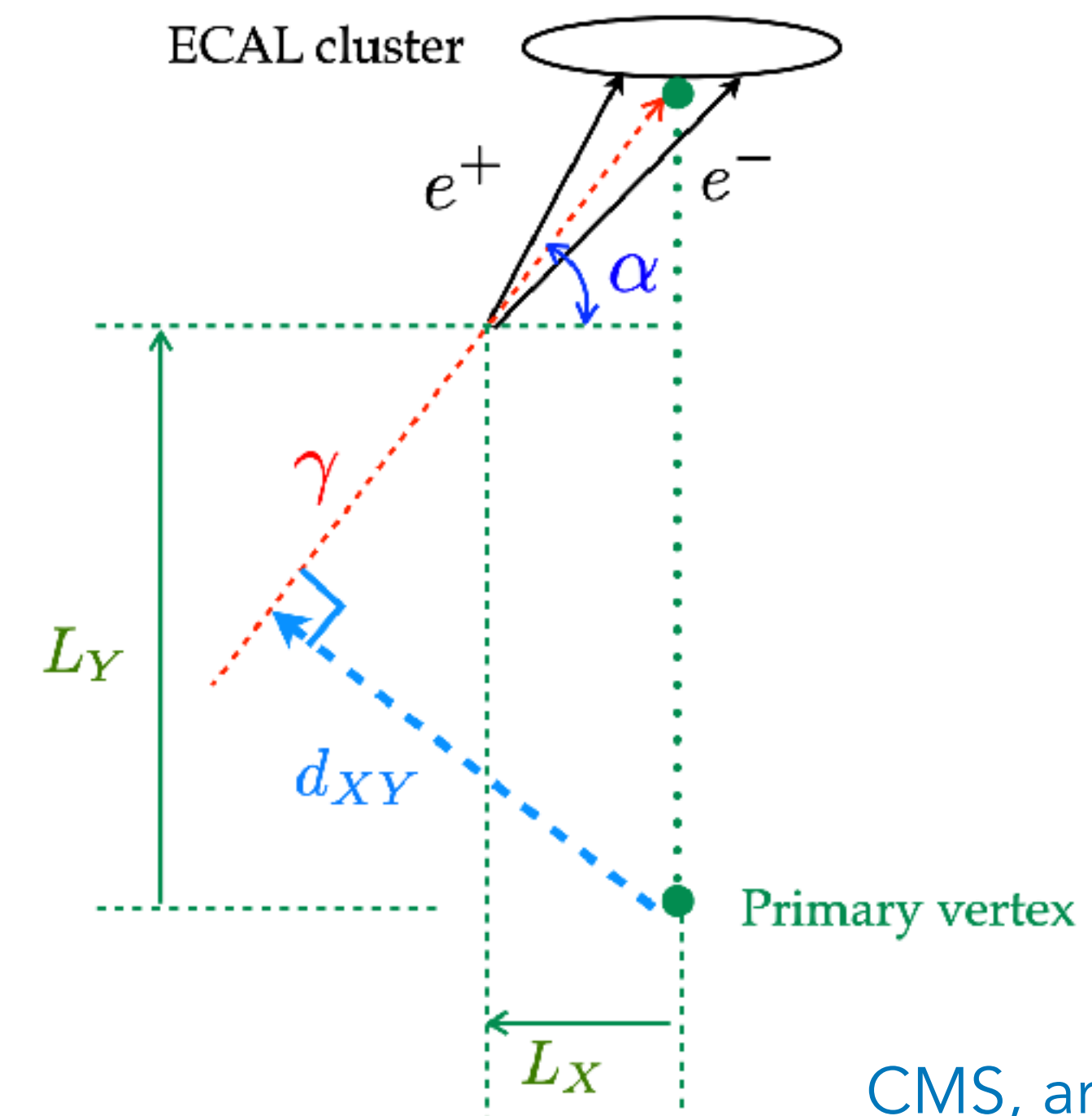
ATLAS and CMS ECals reconstruct trajectory of photons \longrightarrow Displacement via **impact parameter** (IP)

$$d_{XY} = x_{LLP} \frac{p_Y}{p_T} - y_{LLP} \frac{p_X}{p_T} \quad d_Z = \frac{z_{LLP} - (\vec{r} \cdot \vec{p}) p_Z / |\vec{p}|^2}{1 - p_Z^2 / |\vec{p}|^2}$$

$$\vec{r} = \{x_{LLP}, y_{LLP}, z_{LLP}\}$$

Impact parameter: Minimal distance from from γ to PV

In practice: Measuring d_Z difficult (several PVs, no ℓ^\pm). Use only d_{XY}



Possible Scenarios

9 Scenarios: Where is the non-pointing photon signature viable?

Dec. / Prod.	$C_{NNB}^{(5)}$	$C_{NB}^{(6)}, C_{NW}^{(6)}$	V_{eN}
$C_{NNB}^{(5)}$	<p>(B1)</p>	<p>(B2)</p>	<p>(B3)</p>
$C_{NB}^{(6)}, C_{NW}^{(6)}$	<p>(B4)</p>	<p>(B5)</p>	<p>(B6)</p>
V_{eN}	<p>(B7)</p>	<p>(B8)</p>	Minimal scenario

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Possible Scenarios

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Prod. \ Dec.	$C_{NNB}^{(5)}$	$C_{NB}^{(6)}, C_{NW}^{(6)}$	V_{eN}
$C_{NNB}^{(5)}$			
$C_{NB}^{(6)}, C_{NW}^{(6)}$			
V_{eN}			Minimal scenario

B1-B2: (> 1) non-pointing photons from N_1 and N_2 decays



Possible Scenarios

9 Scenarios: Where is the non-pointing photon signature viable?

Dec. / Prod.	$C_{NNB}^{(5)}$	$C_{NB}^{(6)}, C_{NW}^{(6)}$	V_{eN}
$C_{NNB}^{(5)}$	(B1)	(B2)	(B3)
$C_{NB}^{(6)}, C_{NW}^{(6)}$	(B4)	(B5)	(B6)
V_{eN}	(B7)	(B8)	Minimal scenario

B3: No non-pointing photons but DVs (j) + prompt photon still possible



Simulation

To determine the sensitivity reach of ATLAS, performed numerical study:

- Dipole operators up to $d = 6$ implements in FeynRules, UFO output
- For each benchmark, 10^5 events in MadGraph5 at $\sqrt{s} = 14$ TeV covering the parameter space $(m_{LLP}, c_{\text{decay}})$
- Remaining parameter(s) fixed
- Decays handled by MadSpin, Pythia8 showering \Rightarrow estimate efficiencies

Scenario	Model parameters		Simulated decay
	Scan	Fixed	
B1	$m_{N_2}, C_{NNB}^{(5)}$	δ	$N_2 \rightarrow N_1 \gamma$
B2	$m_{N_1}, C_{N_1 X}^{(6)}$	$m_{N_2}, C_{NNB}^{(5)}$	$N_2 \rightarrow N_1 \gamma$ $N_1 \rightarrow \nu \gamma$
B3	$m_{N_1}, V_{eN_1} ^2$	$m_{N_2}, C_{NNB}^{(5)}$	$N_2 \rightarrow N_1 \gamma$ $N_1 \rightarrow e j j$

Selection Cuts and Events

Trigger: $|p_T^\gamma|$ and $|\eta^\gamma|$ (B1 and B2)
 $|p_T^e|$ and $|\eta^e|$ (B3)

B1 and **B2**: LLP in ECal (cut on d_{XY}^γ)

B3: LLP in inner detector (cut on d_0, m_{DV})

Scenario	Signature	Selection cuts
B1	Non-pointing γ	$ p_T^\gamma > 10 \text{ GeV}$, $ \eta^\gamma < 2.47$
B2	Non-pointing γ ($\times 2$) (+ prompt γ)	$r_{DV} < 1450 \text{ mm}$, $ z_{DV} < 3450 \text{ mm}$ $ d_{XY}^\gamma > 6 \text{ mm}$
B3	Displaced Vertex ($\times 2$) (+ prompt γ)	$ p_T^e > 120 \text{ GeV}$, $ \eta^e < 2.47$ $4 \text{ mm} < r_{DV} < 300 \text{ mm}$, $ z_{DV} < 300 \text{ mm}$ 4 tracks with $ d_0 > 2 \text{ mm}$ $m_{DV} > 5 \text{ GeV}$

CMS, 1207.0627

ATLAS, 2209.01029

Number of non-pointing photon events:

$$N_{\text{sig.}}^{\text{B1}} = \sigma \cdot \mathcal{L} \cdot \mathcal{B}(N_2 \rightarrow N_1 \gamma) \cdot \epsilon_{\text{sel}}^{\text{B1}}$$

$$N_{\text{sig.}}^{\text{B2}} = \sigma \cdot \mathcal{L} \cdot \mathcal{B}(N_2 \rightarrow N_1 \gamma) \cdot 2 \cdot \mathcal{B}(N_1 \rightarrow \nu \gamma) \cdot \epsilon_{\text{sel}}^{\text{B2}}$$

$$N_{\text{sig.}}^{\text{B3}} = \sigma \cdot \mathcal{L} \cdot \mathcal{B}(N_2 \rightarrow N_1 \gamma) \cdot 2 \cdot \mathcal{B}(N_1 \rightarrow e j j) \cdot \epsilon_{\text{sel}}^{\text{B3}}$$

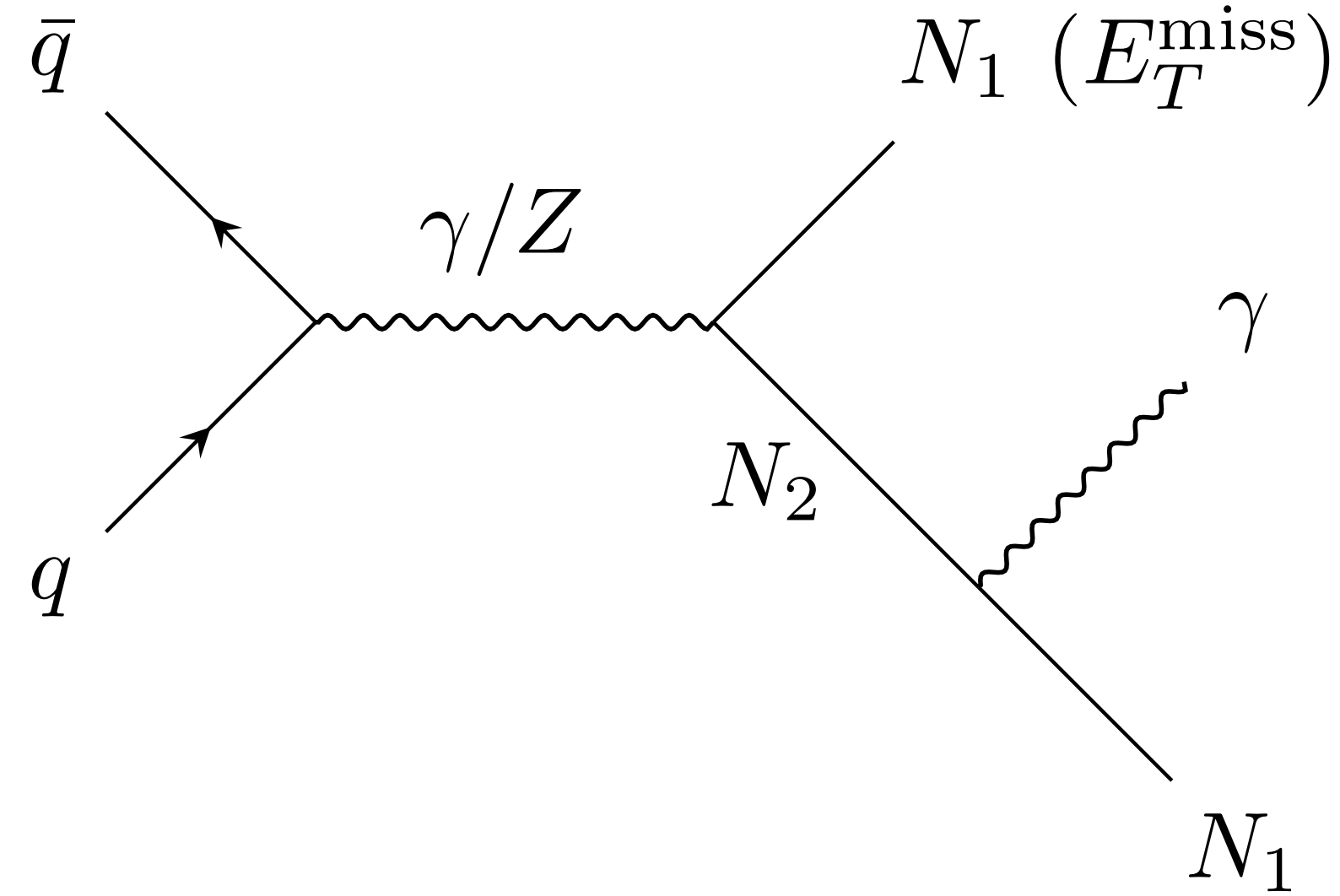
Bounds from Displaced Vertex Searches at LHC

Scenario B1

$$pp \rightarrow N_1 N_2 (d_{NN\gamma})$$

$$N_1 (E_T^{\text{miss}})$$

$$N_2 \rightarrow (N_1 \gamma)^{\text{LLP}} (d_{NN\gamma})$$



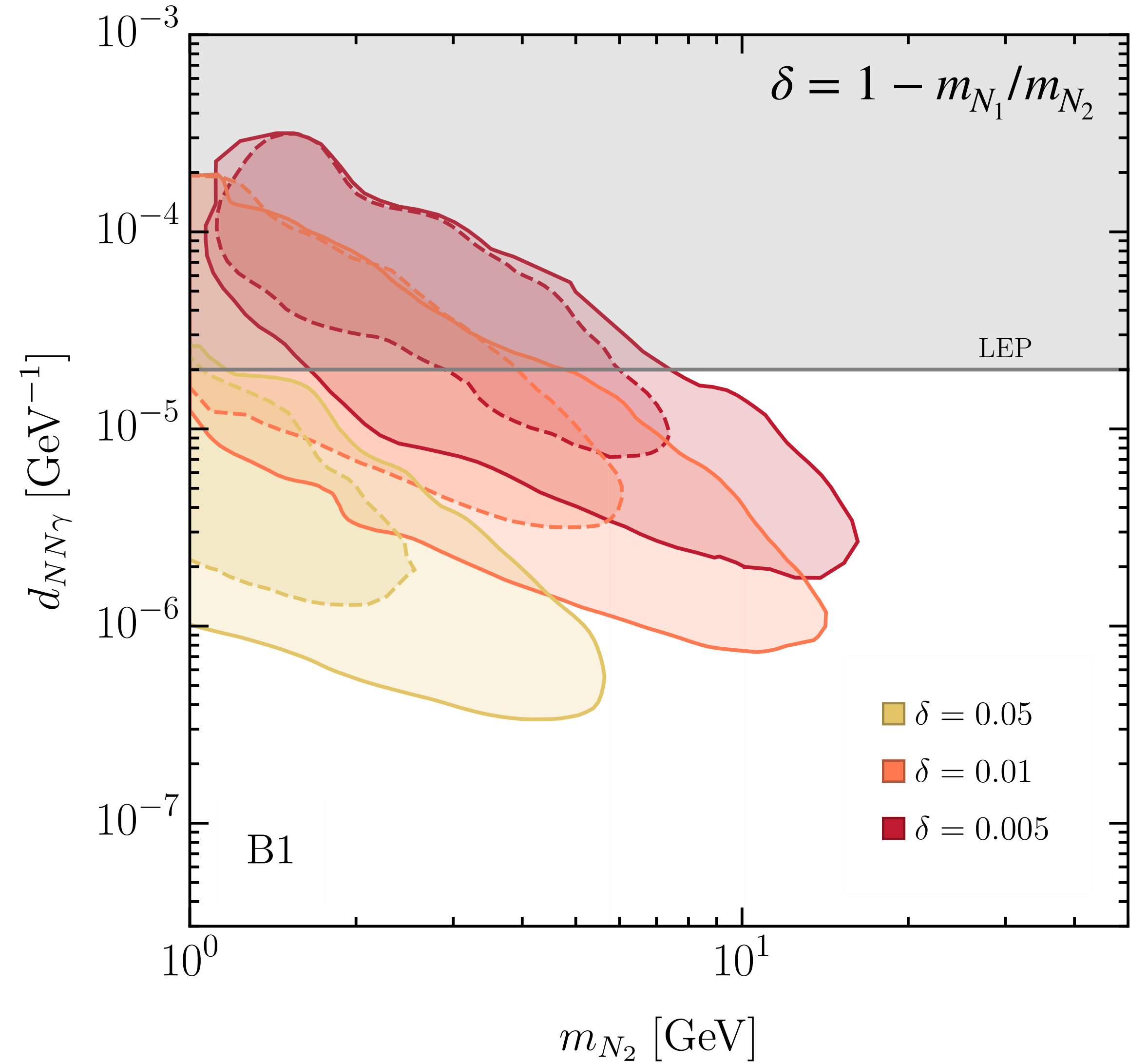
$$N_{\text{sig.}}^{\text{B1}} = \sigma \cdot \mathcal{L} \cdot \mathcal{B}(N_2 \rightarrow N_1 \gamma) \cdot \epsilon_{\text{sel}}^{\text{B1}}$$

Solid: 3 events (95% C.L.)

Dashed: 30 events

$$\sqrt{s} = 14 \text{ TeV}$$

$$\mathcal{L} = 3 \text{ ab}^{-1}$$

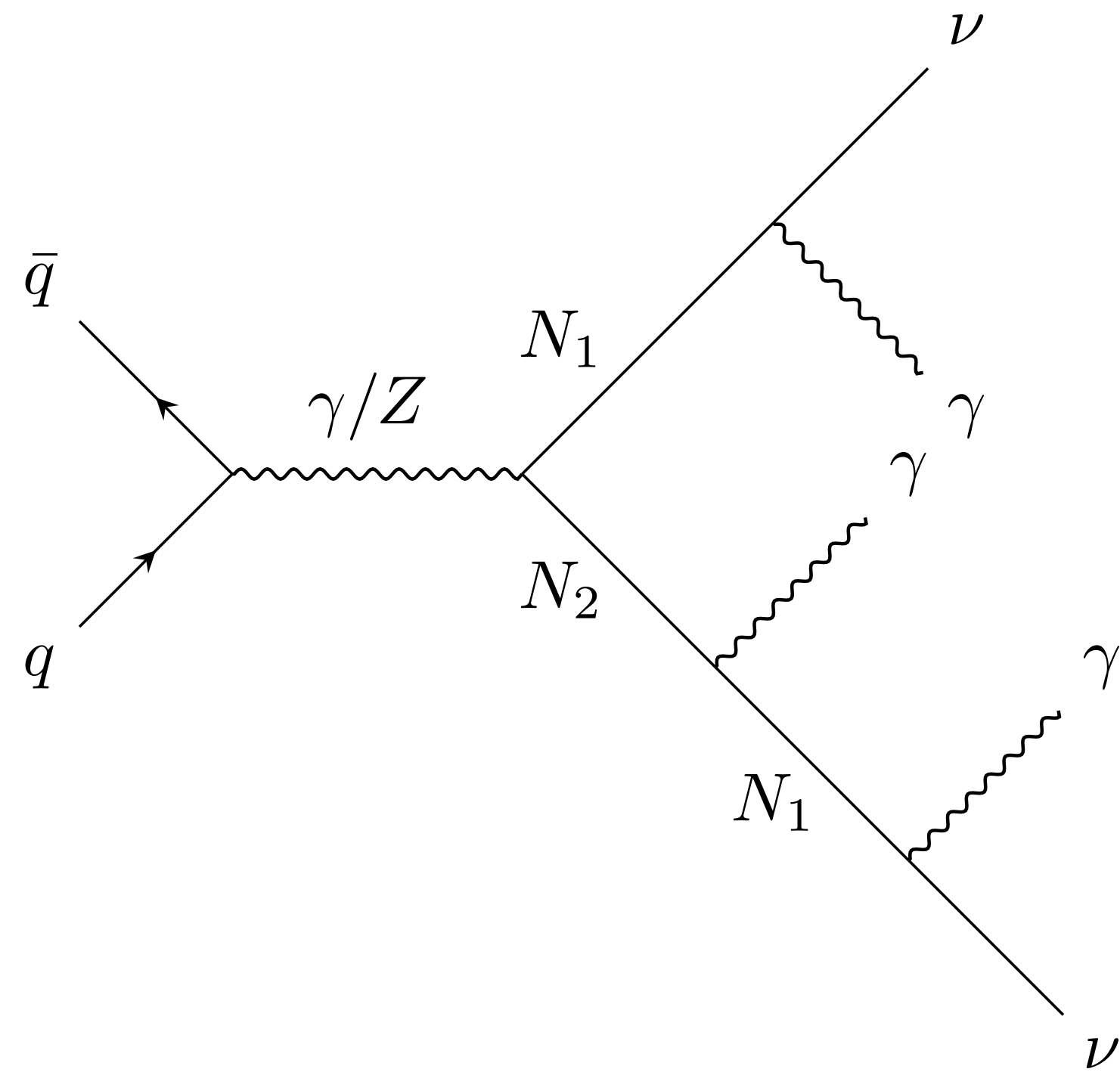


Scenario B2

$$pp \rightarrow N_1 N_2 \quad (d_{NN\gamma})$$

$$N_1 \rightarrow (\nu\gamma)^{\text{LLP}} \quad (d_{\nu N\gamma})$$

$$N_2 \rightarrow N_1 \gamma \rightarrow (\nu\gamma)^{\text{LLP}} \gamma \quad (d_{\nu N\gamma}, d_{NN\gamma})$$

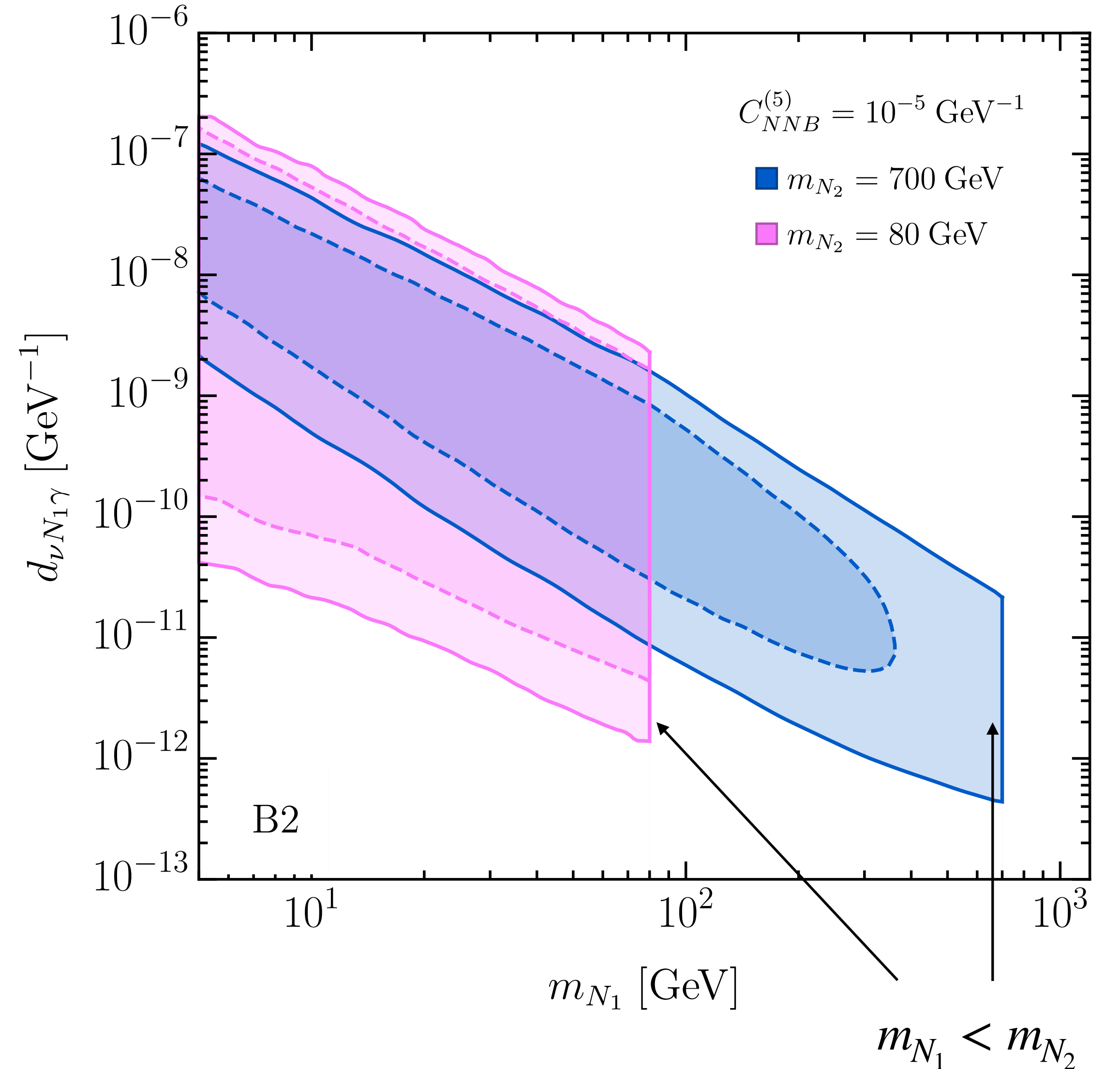


Solid: 3 events (95% C.L.)

Dashed: 30 events

$\sqrt{s} = 14 \text{ TeV}$

$\mathcal{L} = 3 \text{ ab}^{-1}$



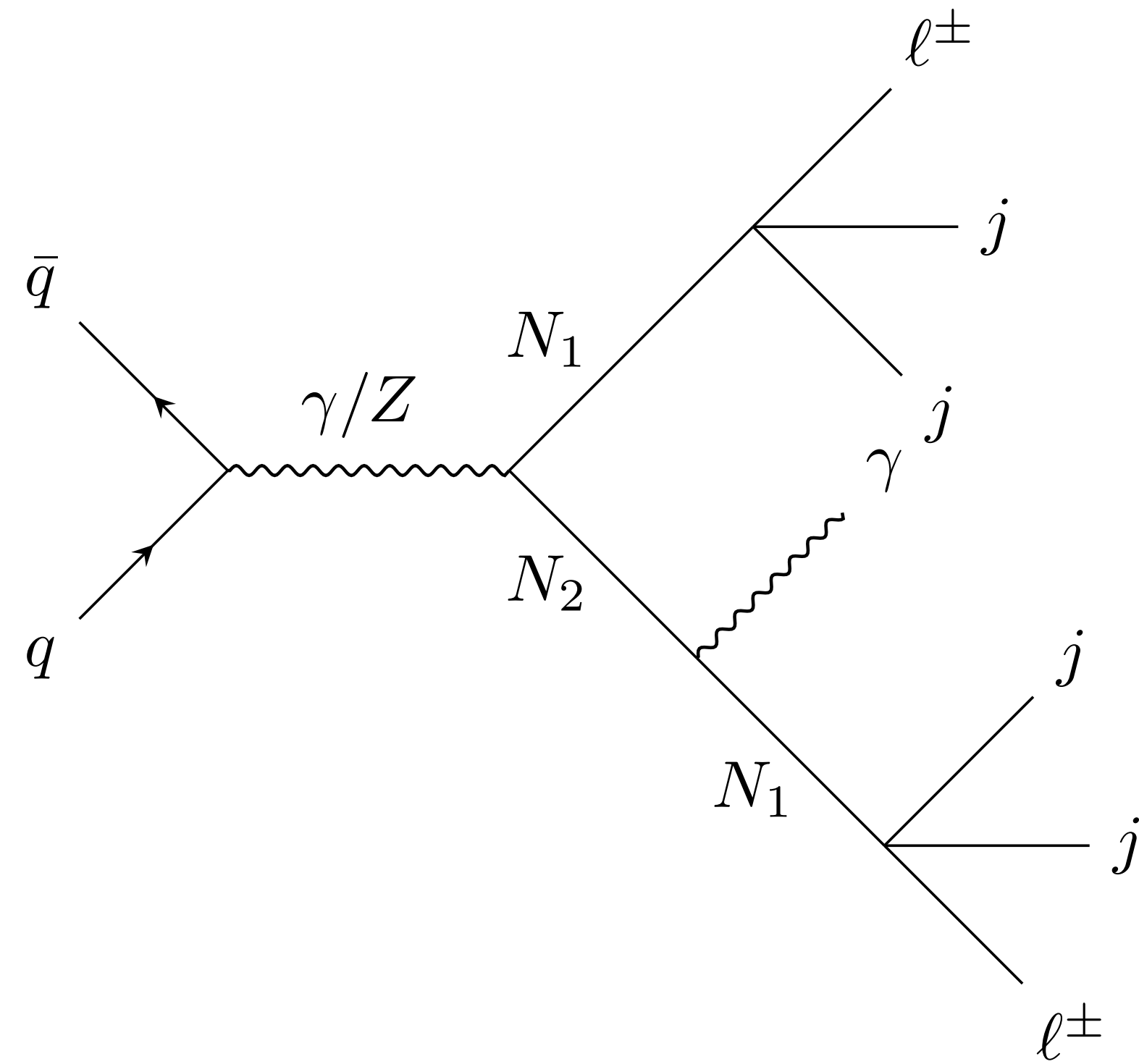
$$N_{\text{sig.}}^{\text{B2}} = \sigma \cdot \mathcal{L} \cdot \mathcal{B}(N_2 \rightarrow N_1 \gamma) \cdot 2 \cdot \mathcal{B}(N_1 \rightarrow \nu \gamma) \cdot \epsilon_{\text{sel}}^{\text{B2}}$$

Scenario B3

$$pp \rightarrow N_1 N_2 (d_{NN\gamma}),$$

$$N_1 \rightarrow (ejj)^{\text{LLP}} (V_{eN})$$

$$N_2 \rightarrow N_1 \gamma \rightarrow (ejj)^{\text{LLP}} \gamma (d_{NN\gamma}, V_{eN})$$



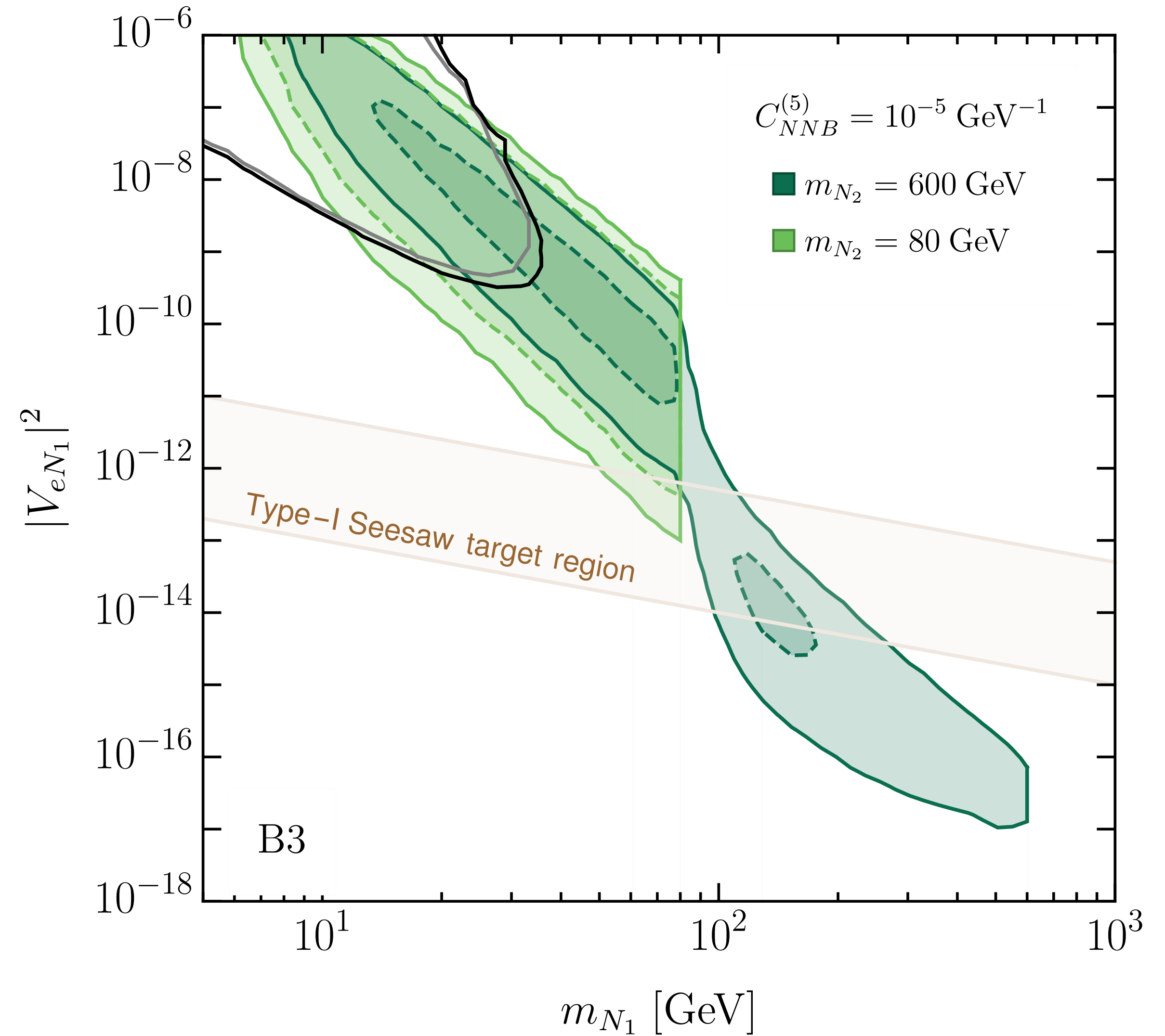
$$N_{\text{sig.}}^{\text{B3}} = \sigma \cdot \mathcal{L} \cdot \mathcal{B}(N_2 \rightarrow N_1 \gamma) \cdot 2 \cdot \mathcal{B}(N_1 \rightarrow ejj) \cdot \epsilon_{\text{sel}}^{\text{B3}}$$

Solid: 3 events (95% C.L.)

Dashed: 10 events

$\sqrt{s} = 14 \text{ TeV}$

$\mathcal{L} = 3 \text{ ab}^{-1}$



Solid black: DV + prompt ℓ

Constraints on Specific UV Model

UV Model for Neutrino Magnetic Moments

To generate active (sterile)-to-sterile magnetic moments for N_R , we introduce two additional fields:

Field(s)	Irrep	Couplings
N_R	$(\mathbf{1}, \mathbf{1})_0$	Y_ν
E	$(\mathbf{1}, \mathbf{1})_{-1}$	Y_E
ϕ	$(\mathbf{1}, \mathbf{1})_{-1}$	$f, \lambda_{\phi H}$

[Aparici, Kim, Santamaria, Wudka, 0904.3244](#)

[Aparici, Santamaria, Wudka, 0911.4103](#)

Introducing the vector-like lepton $E = E_L + E_R$:

$$\mathcal{L} \supset \bar{E} (i\not{D} - m_E) E - \left[\bar{L} Y_E H E_R + \text{h.c.} \right] \quad Y_E = \begin{pmatrix} Y_E^e \\ Y_E^\mu \\ Y_E^\tau \end{pmatrix}$$

Introducing the scalar ϕ :

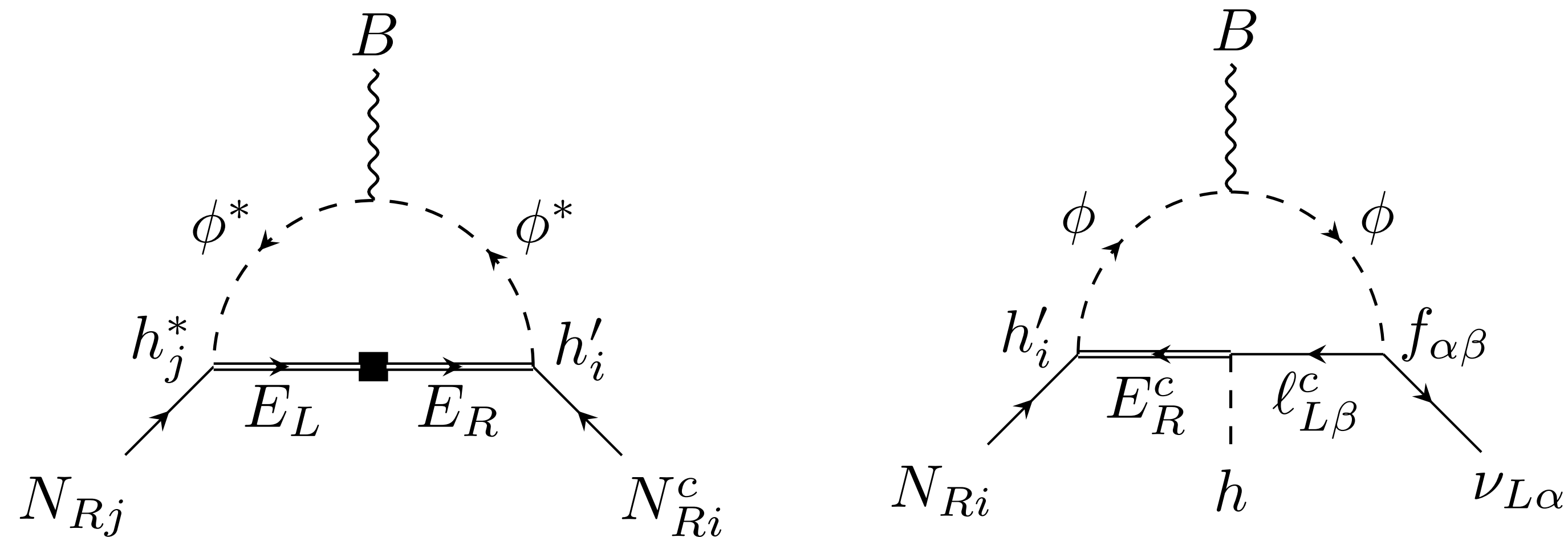
$$\mathcal{L} \supset (D_\mu \phi)^* (D^\mu \phi) - V(\phi) - \left[\bar{L} f \tilde{L} \phi + \bar{N}_R^c f' \ell_R \phi^* + \text{h.c.} \right] \quad f = \begin{pmatrix} 0 & f_{e\mu} & f_{e\tau} \\ -f_{e\mu} & 0 & f_{\mu\tau} \\ -f_{e\tau} & -f_{\mu\tau} & 0 \end{pmatrix}$$

When both E and ϕ are Present

When both the vector-like lepton and singly-charged scalar are present, we can write

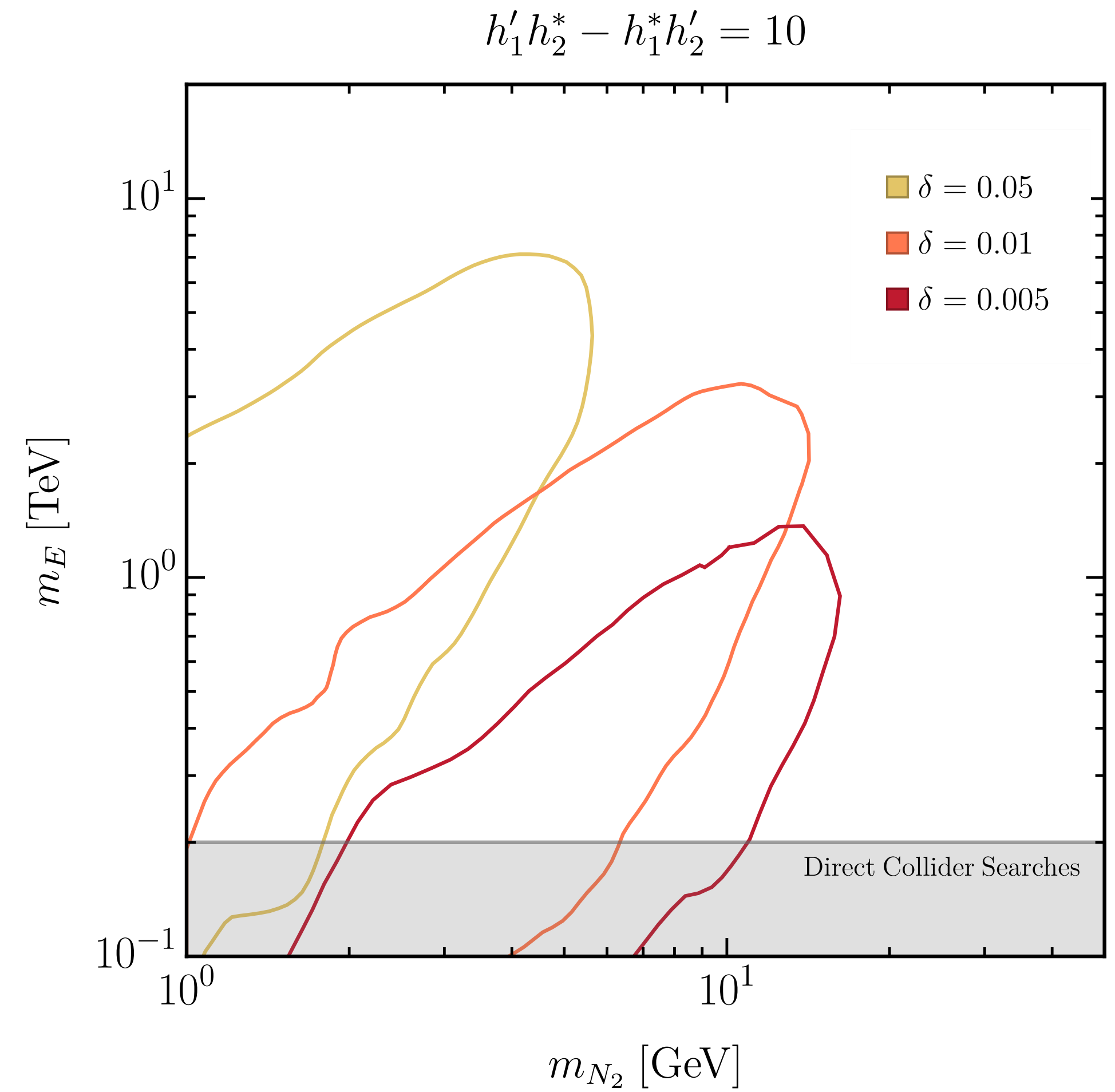
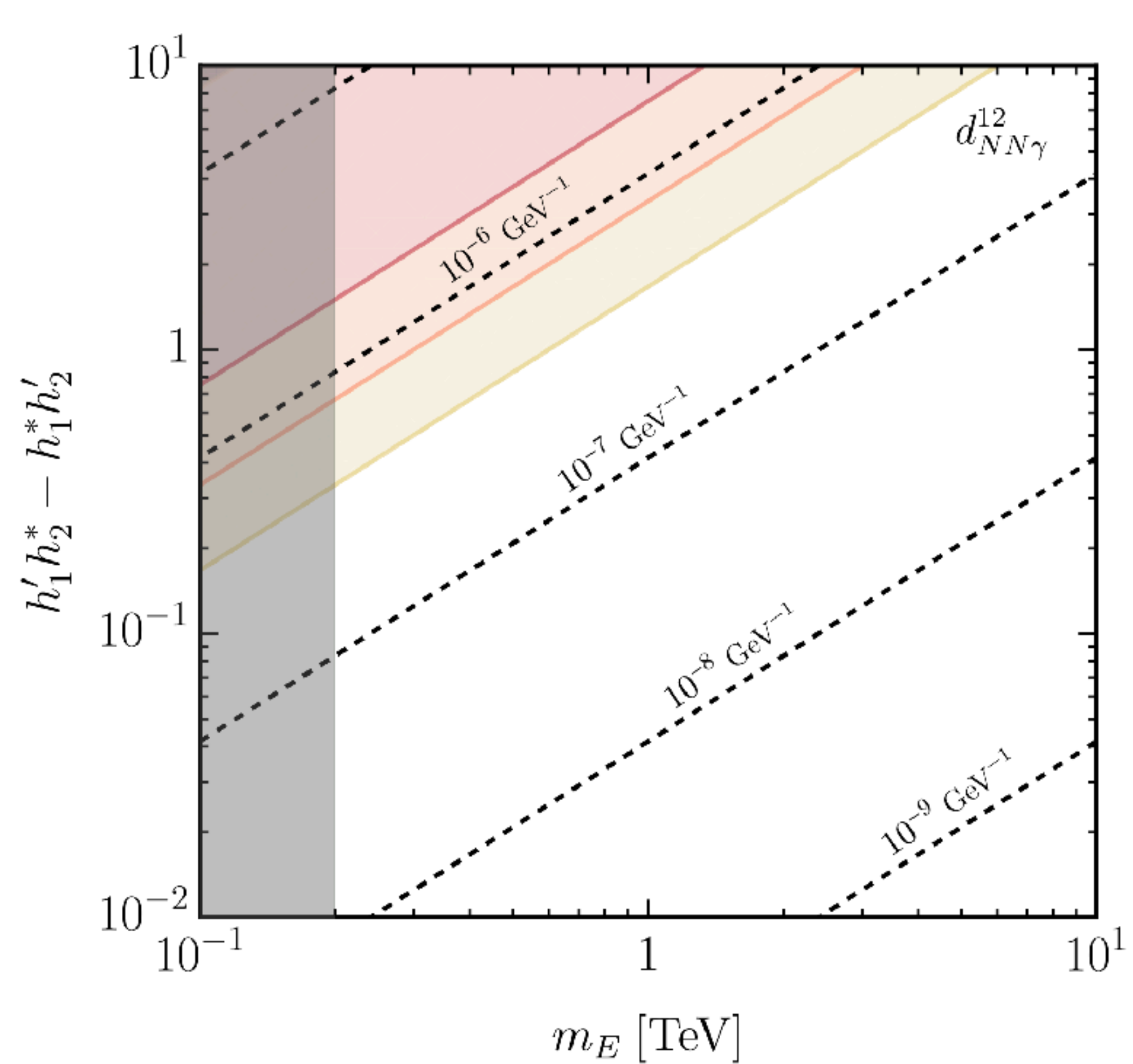
$$\mathcal{L} \supset \bar{N}_R h E_L \phi^* + \bar{N}_R^c h' E_R \phi^* + \text{h.c.},$$

If $E \rightarrow -E$ and $\phi \rightarrow -\phi$ under Z_2 , these are the only possible new interactions















UV Model Bounds from Benchmark 1

$$d_{NN\gamma}^{ij} = c_w C_{NNB}^{(5)ij} \quad C_{NNB}^{(5)ij} = \frac{1}{16\pi^2} \frac{g'(h'_i h_j^* - h_i^* h'_j)}{4m_E} f(r)$$



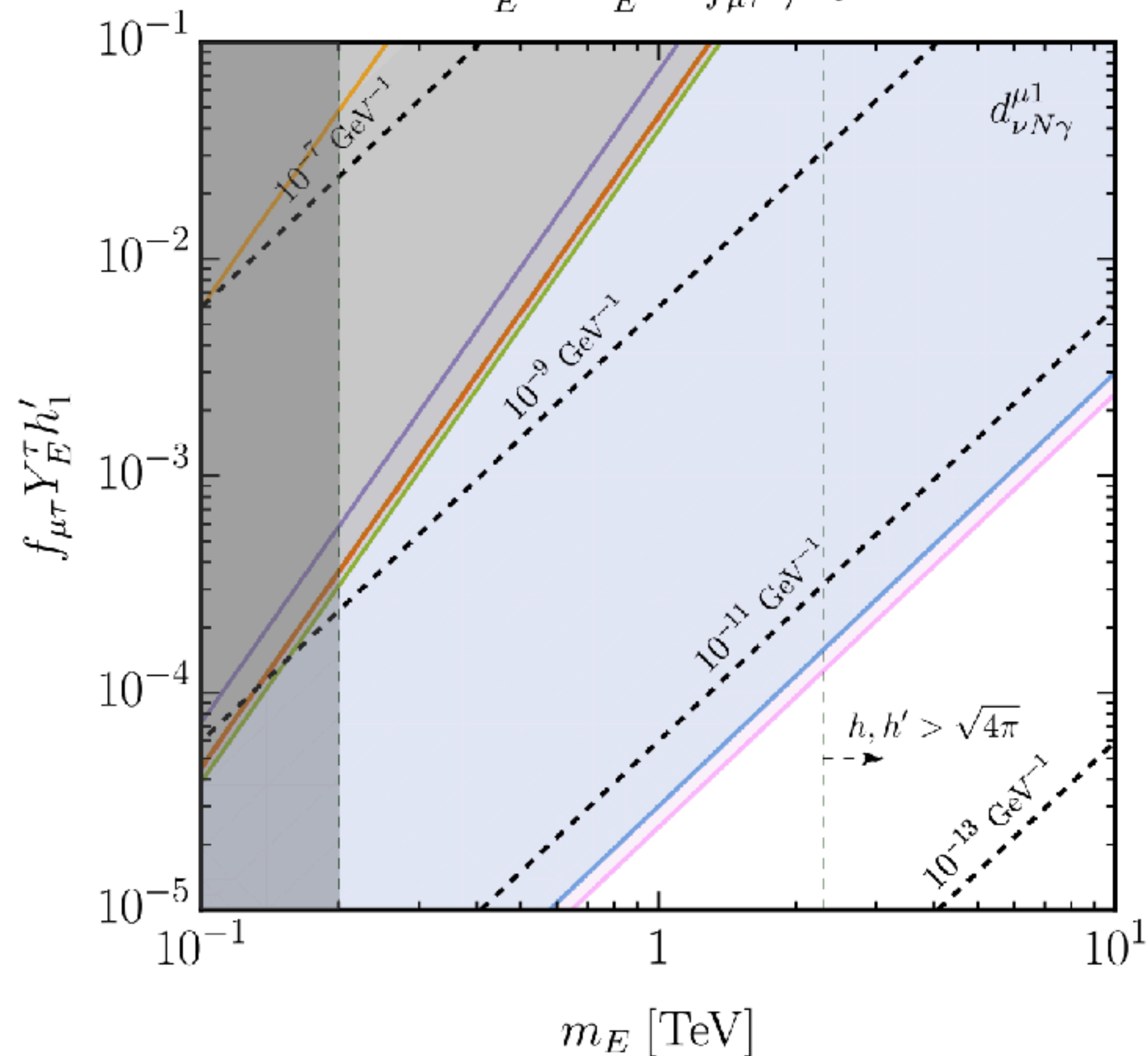
Active-to-Sterile Bounds

$$C_{NB}^{(6)\alpha i} = \frac{1}{16\pi^2} \frac{3g'_{\alpha\beta} Y_E^{\beta*} h'_i}{4m_E^2} f(r)$$

Constraints case 1: $\mu - \tau$		Constraints case 2: only τ	
	$\tau \rightarrow \mu\gamma$ (BaBar)		$\mu \rightarrow e\gamma$ (MEG)
	$\tau \rightarrow 3\mu$ (Belle)		$\mu \rightarrow 3e$ (SINDRUM)
	$\tau \rightarrow \mu ee$ (Belle)		$\mu - e$ conversion (Au, SINDRUM)
	LFU, g_μ/g_e (HFLAV)		LFU, g_τ/g_μ (HFLAV)
	EWPD (LEP)		EWPD (LEP)
	DirectColliderSearches		Direct Collider Searches

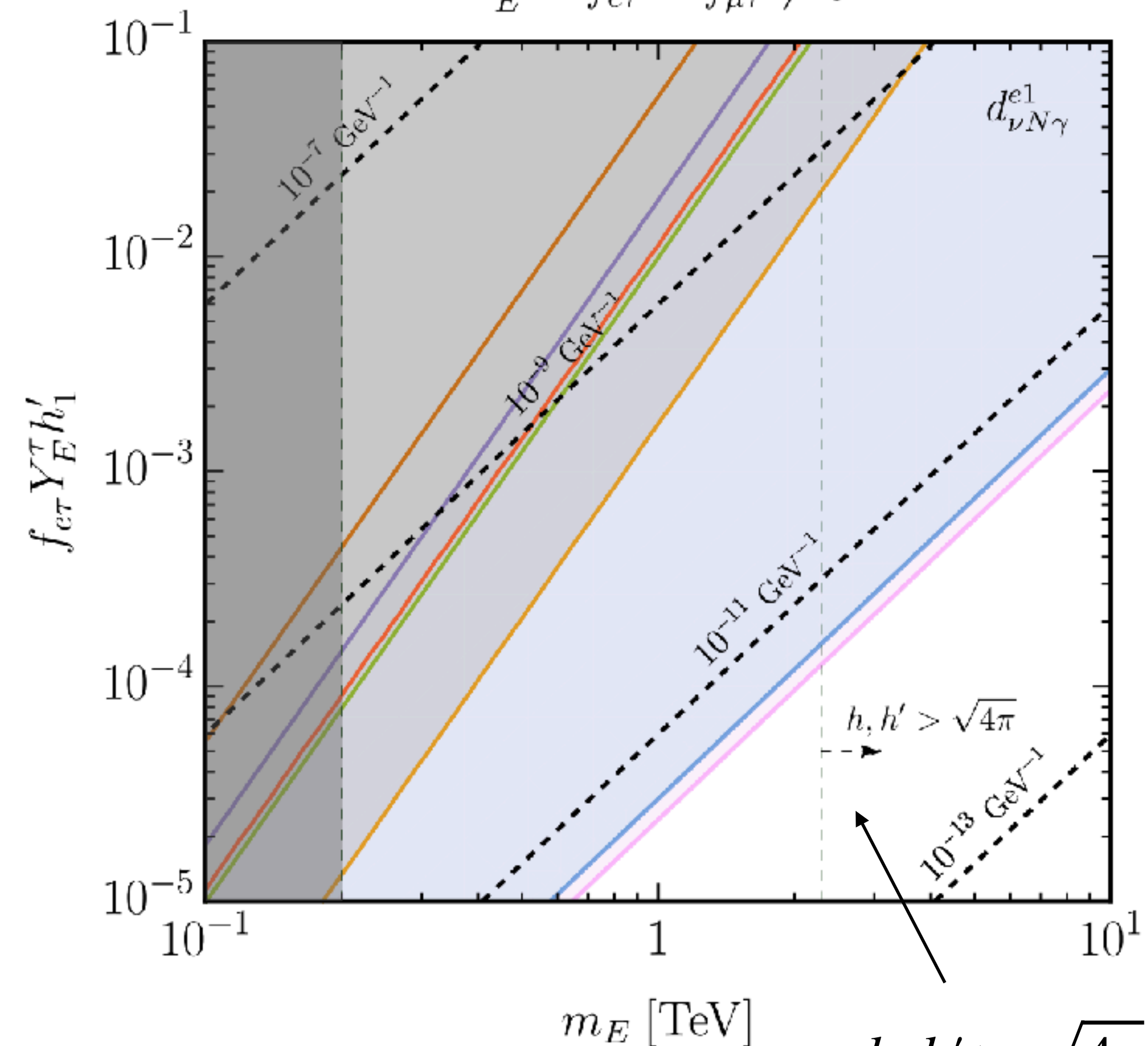
'No e ' couplings

$$Y_E^\mu = Y_E^\tau = f_{\mu\tau} \neq 0$$



' τ only' couplings

$$Y_E^\tau = f_{e\tau} = f_{\mu\tau} \neq 0$$



$h, h' > \sqrt{4\pi}$ to obtain $C_{NNB}^{(5)}$

Summary and Conclusions

Study: Phenomenology of **heavy sterile neutrinos** with **magnetic moments** at the LHC

EFT analysis with the N_R SMEFT operators $\mathcal{O}_{NNB}^{(5)}$, $\mathcal{O}_{NB}^{(6)}$ and $\mathcal{O}_{NW}^{(6)}$:

- Examined future sensitivity of LHC experiments using displaced **non-pointing photons**
- Excluded regions in 3 of 9 limiting benchmark cases

Toy **UV model** to generate $C_{NNB}^{(5)}$, $C_{NB}^{(6)}$ and $C_{NW}^{(6)}$ at one-loop

- Single vector-like lepton E and singly-charged scalar ϕ
- Additional constraints from EWPT, cLFV and LFU violating observables

Conclusions:

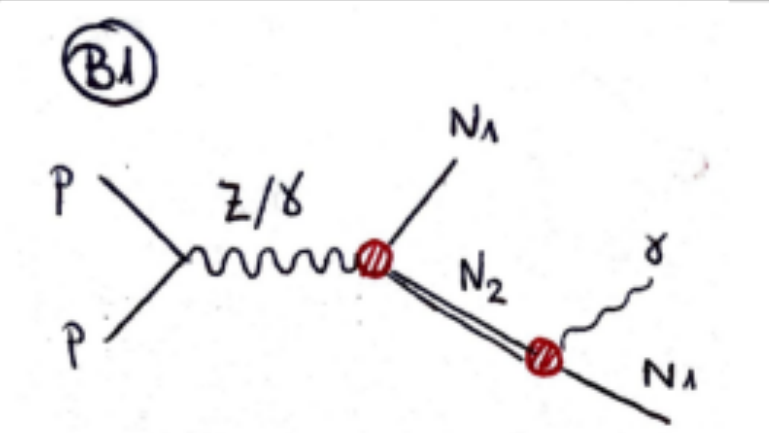
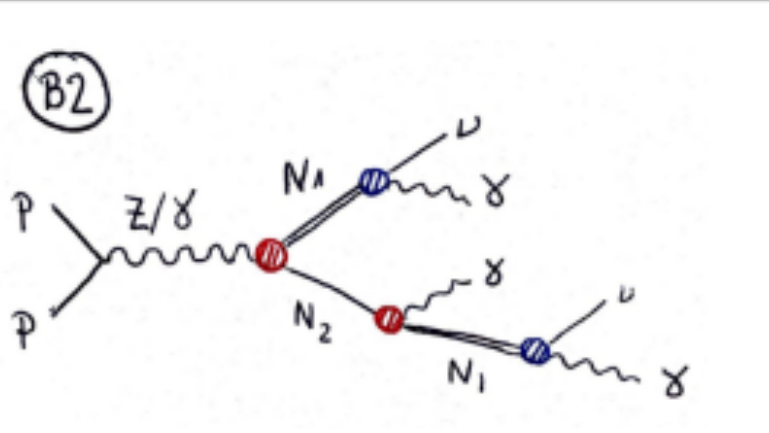
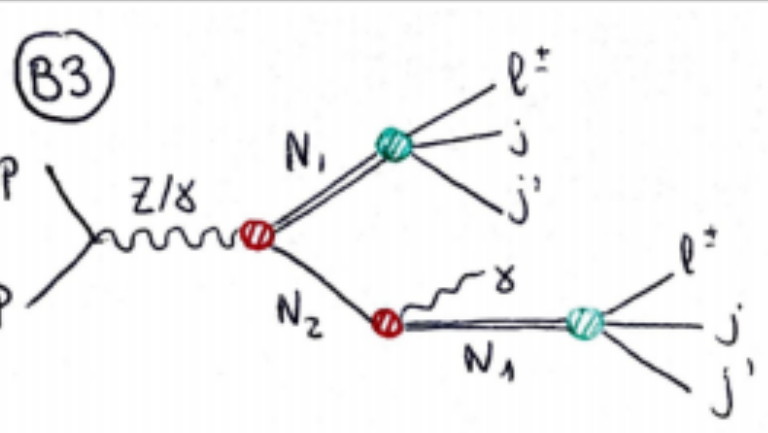
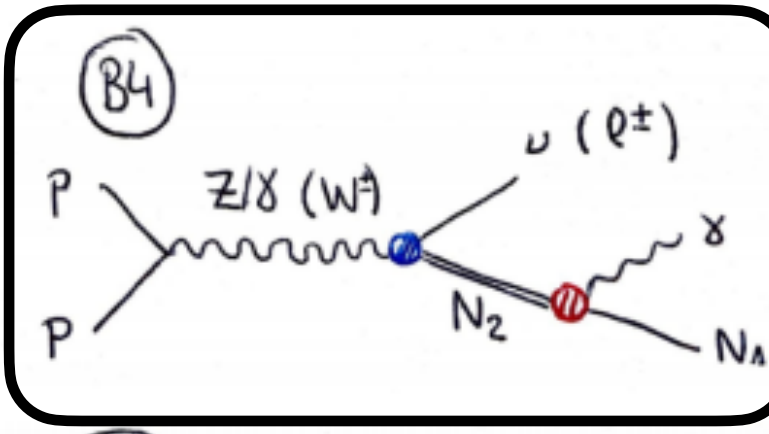
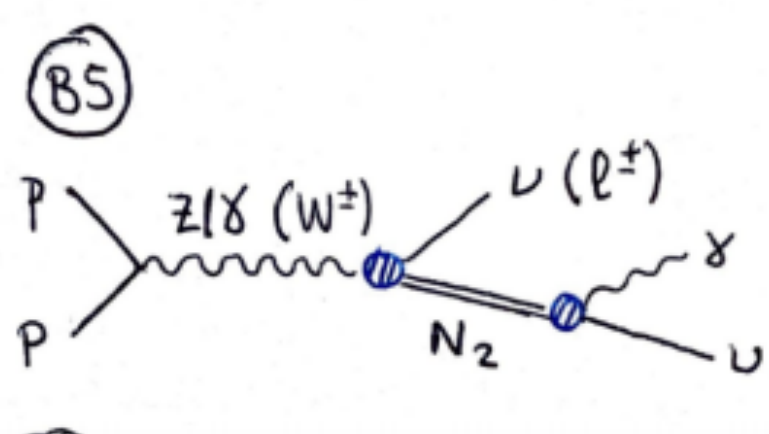
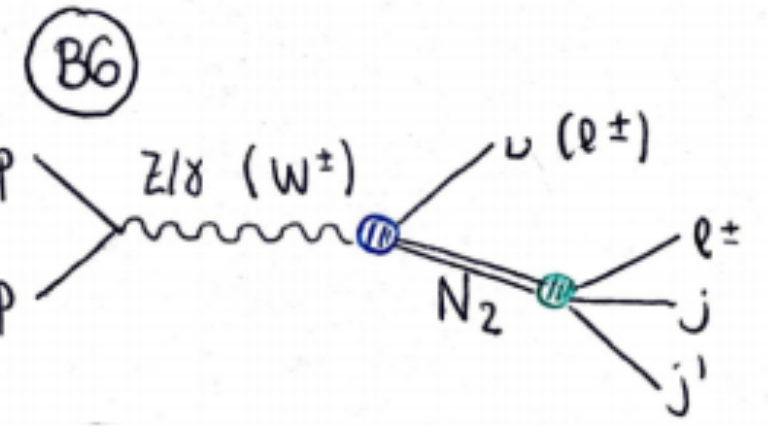
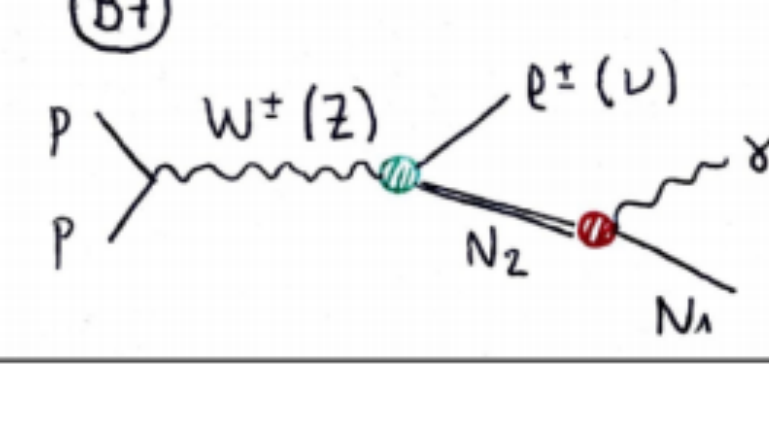
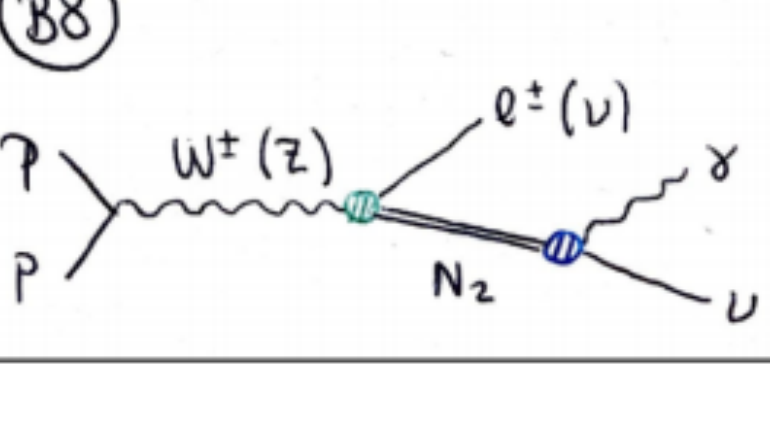
- Non-pointing photons can explore new regions of EFT parameter space for $d_{NN\gamma}$, $d_{\nu N\gamma}$ and $V_{\alpha N}$
- In specific model, complementarity with EWPT, cLFV

Thank you for your attention!

Bonus Slides

Possible Scenarios

9 Scenarios: Where is the non-pointing photon signature viable?

Prod. \ Dec.	$C_{NNB}^{(5)}$	$C_{NB}^{(6)}, C_{NW}^{(6)}$	V_{eN}
$C_{NNB}^{(5)}$	(B1) 	(B2) 	(B3) 
$C_{NB}^{(6)}, C_{NW}^{(6)}$	(B4) 	(B5) 	(B6) 
V_{eN}	(B7) 	(B8) 	Minimal scenario

B4: $C_{NNB}^{(5)}$ large enough to dominate the decay of N_2 would also dominate $\sigma(pp \rightarrow X)$



Possible Scenarios

9 Scenarios: Where is the non-pointing photon signature viable?

Prod. \ Dec.	$C_{NNB}^{(5)}$	$C_{NB}^{(6)}, C_{NW}^{(6)}$	V_{eN}
$C_{NNB}^{(5)}$			
$C_{NB}^{(6)}, C_{NW}^{(6)}$			
V_{eN}			Minimal scenario

B5 and **B6**: Difficult to realise displaced vertex (decay prompt if $C_{NB}^{(6)}$ dominates σ)



Possible Scenarios

9 Scenarios: Where is the non-pointing photon signature viable?

Dec. / Prod.	$C_{NNB}^{(5)}$	$C_{NB}^{(6)}, C_{NW}^{(6)}$	V_{eN}
$C_{NNB}^{(5)}$	(B1)	(B2)	(B3)
$C_{NB}^{(6)}, C_{NW}^{(6)}$	(B4)	(B5)	(B6)
V_{eN}	(B7)	(B8)	Minimal scenario

B7: Can only be realised in a narrow region of parameter space



Possible Scenarios

9 Scenarios: Where is the non-pointing photon signature viable?

Prod. \ Dec.	$C_{NNB}^{(5)}$	$C_{NB}^{(6)}, C_{NW}^{(6)}$	V_{eN}
$C_{NNB}^{(5)}$			
$C_{NB}^{(6)}, C_{NW}^{(6)}$			
V_{eN}			Minimal scenario

B8: Prompt ℓ^\pm plus photon (prompt or displaced depending on $C_{NB}^{(6)}$)



UV Model for Neutrino Magnetic Moments

Vector-Like Lepton

Extended charged lepton mass term including vector-like lepton

$$\mathcal{L} \supset - (\bar{\ell}_L \ \bar{E}_L) \mathcal{M}_E \begin{pmatrix} \ell_R \\ E_R \end{pmatrix} + \text{h.c.}; \quad \mathcal{M}_E = \begin{pmatrix} \frac{vY_e}{\sqrt{2}} & \frac{vY_E}{\sqrt{2}} \\ 0 & m_E \end{pmatrix}$$

Diagonalise:

$$\begin{pmatrix} \ell_{L\alpha} \\ E_L \end{pmatrix} = \begin{pmatrix} V_{\alpha\beta}^L & V_{\alpha E}^L \\ V_{E\beta}^L & V_{EE}^L \end{pmatrix} P_L \begin{pmatrix} \ell'_\beta \\ E' \end{pmatrix}, \quad \begin{pmatrix} \ell_{R\alpha} \\ E_R \end{pmatrix} = \begin{pmatrix} V_{\alpha\beta}^R & V_{\alpha E}^R \\ V_{E\beta}^R & V_{EE}^R \end{pmatrix} P_R \begin{pmatrix} \ell'_\beta \\ E' \end{pmatrix},$$

In the limit $m_\ell \ll m_E$, seesaw-like mixing

$$V_{\alpha E}^L = -V_{E\alpha}^{L*} \approx \frac{vY_E^\alpha}{\sqrt{2}m_E}, \quad V_{\alpha E}^R = -V_{E\alpha}^{R*} \approx \frac{v^2[Y_e]_{\alpha\gamma}^* Y_E^\gamma}{2m_E^2}$$

$\Rightarrow V^{L,R}$ enters SM charged and neutral currents

Vector-Like Lepton

Equivalently, for $m_\ell \ll m_E$, the vector-like lepton can be integrated out. At tree-level:

$$\mathcal{O}_{Hl}^{(1)} = (H^\dagger i \overleftrightarrow{D}_\mu H) (\bar{L} \gamma^\mu L) \quad \mathcal{O}_{Hl}^{(3)} = (H^\dagger i \overleftrightarrow{D}_\mu^I H) (\bar{L} \tau^I \gamma^\mu L) \quad \mathcal{O}_{eH} = (H^\dagger H) \bar{L} H \ell_R$$

With matching conditions:

$$C_{Hl}^{(1)\alpha\beta} = C_{Hl}^{(3)\alpha\beta} = -\frac{Y_E^\alpha Y_E^{\beta*}}{4m_E^2} \quad C_{eH}^{\alpha\beta} = \frac{Y_E^\alpha Y_E^{\gamma*} [Y_e]_{\gamma\beta}}{2m_E^2}$$

del Aguila, de Blas, Perez-Victoria, arXiv:0803.4008

Give off-diagonal Z , Higgs couplings or flavour-changing neutral currents (FCNCs)

↳ Bounds from electroweak precision tests (EWPT) and charged-lepton flavour violation (cLFV)

Singly-Charged Scalar

For the singly-charged scalar, we can write

$$\mathcal{L} \supset - (\bar{\nu}_L \bar{\ell}_L) f \begin{pmatrix} \ell_L^c \\ -\nu_L^c \end{pmatrix} \phi + \text{h.c.} = -2\bar{\nu}_L f \ell_L^c \phi + \text{h.c.},$$

Similarly, for $m_\ell \ll m_\phi$, we obtain from f and f' couplings:

$$\mathcal{O}_{ll} = (\bar{L}\gamma_\mu L)(\bar{L}\gamma^\mu L) \quad \mathcal{O}_{lNle} = (\bar{L}N_R)\epsilon(\bar{L}\ell_R) \quad \mathcal{O}_{eN} = (\bar{\ell}_R\gamma_\mu\ell_R)(\bar{N}_R\gamma^\mu N_R)$$

With tree-level matching conditions:

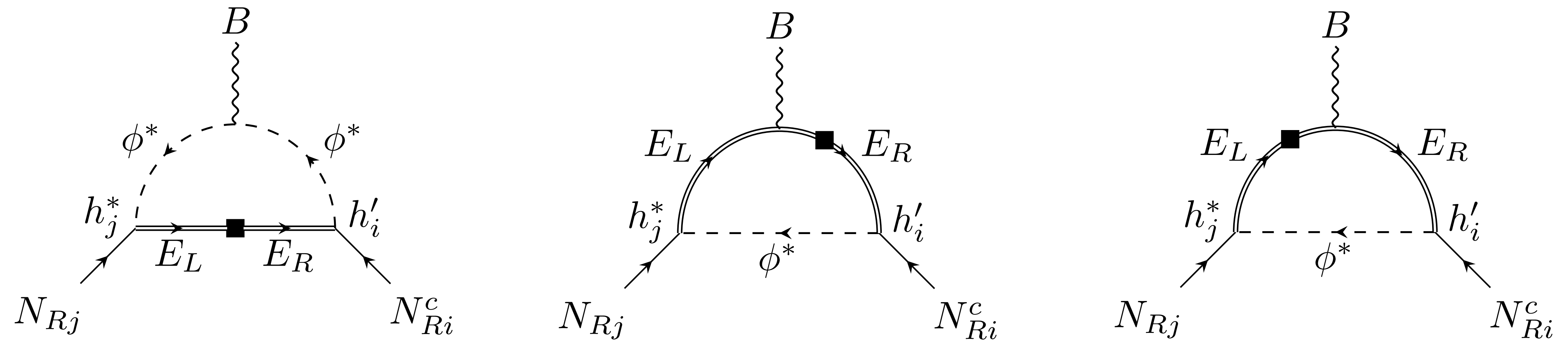
$$C_{ll}^{\alpha\beta\gamma\delta} = \frac{f_{\alpha\gamma}f_{\delta\beta}^*}{m_\phi^2} \quad C_{lNle}^{\alpha i\beta\gamma} = \frac{2f_{\alpha\beta}f'_{i\gamma}}{m_\phi^2} \quad C_{eN}^{\alpha\beta ij} = \frac{f'_{i\alpha}f'_{j\beta}}{2m_\phi^2}$$

Exotic lepton interactions

↳ Bounds from lepton flavour universality (LFU) and charged lepton flavour violating probes

Sterile-to-Sterile Neutrino Magnetic Moments

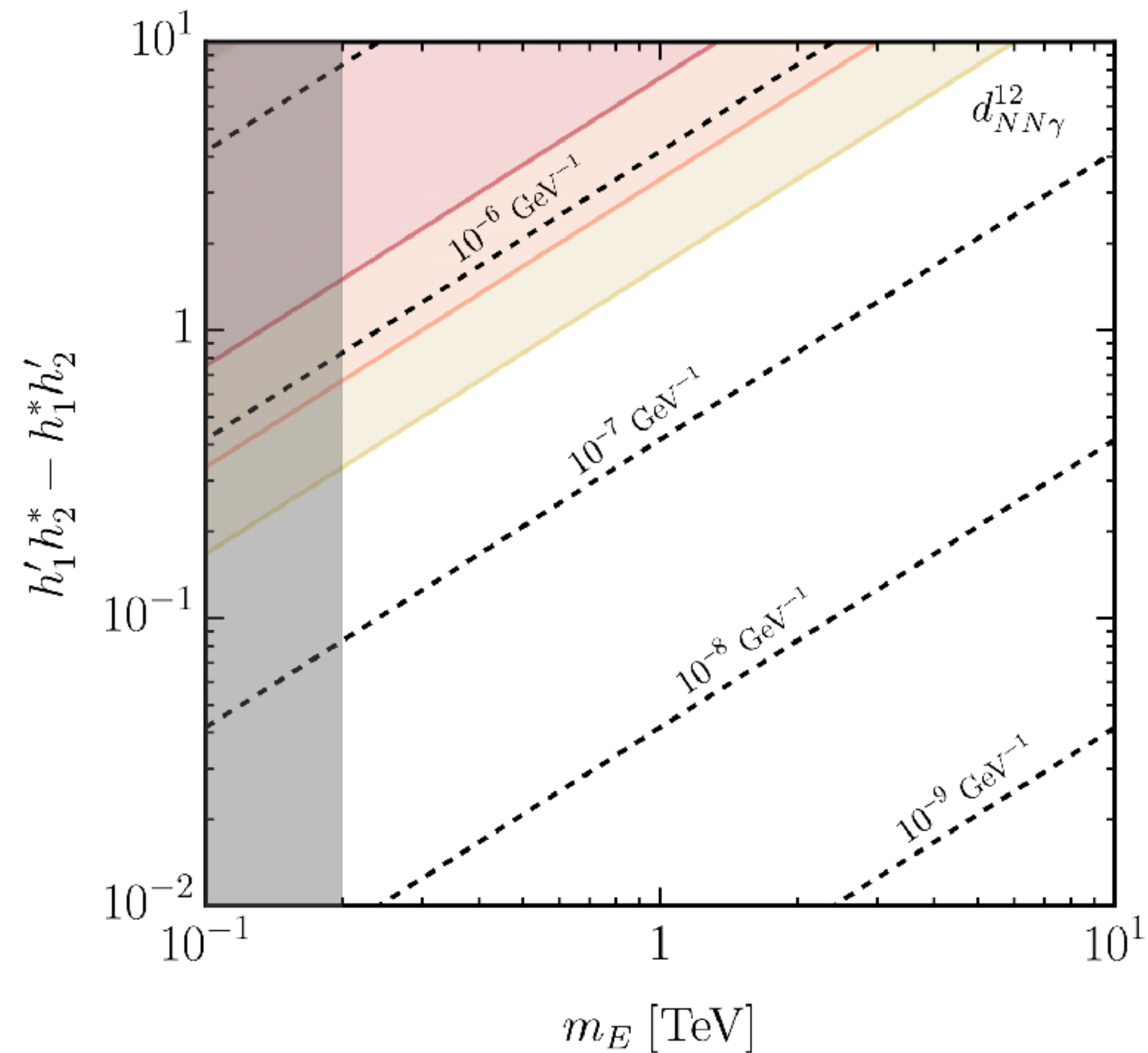
At one-loop in the UV model:



One-loop matching:

$$C_{NNB}^{(5)ij} = \frac{1}{16\pi^2} \frac{g'(h'_i h_j^* - h_i^* h'_j)}{4m_E} f(r) \quad f(r) = \frac{1}{1-r} + \frac{r \log r}{(1-r)^2}$$

Sterile-to-Sterile Neutrino Magnetic Moments

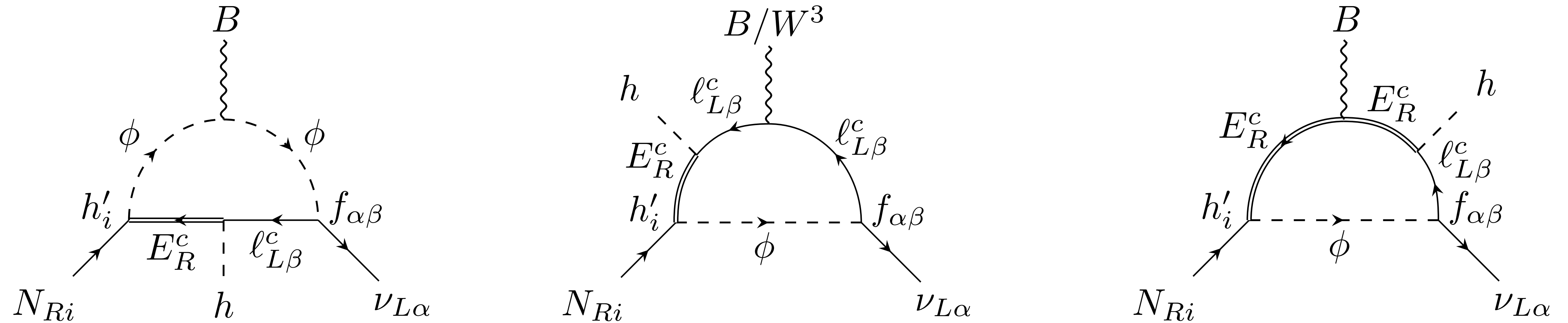


$$d_{NN\gamma}^{ij} = c_w C_{NNB}^{(5)ij} \approx 2.4 \times 10^{-6} \text{ GeV}^{-1} \left(\frac{h'_i h_j^* - h_i^* h'_j}{10} \right) \left(\frac{1 \text{ TeV}}{m_E} \right)$$

$$h_i, h'_i < \sqrt{4\pi}$$

Active-to-Sterile Neutrino Magnetic Moments

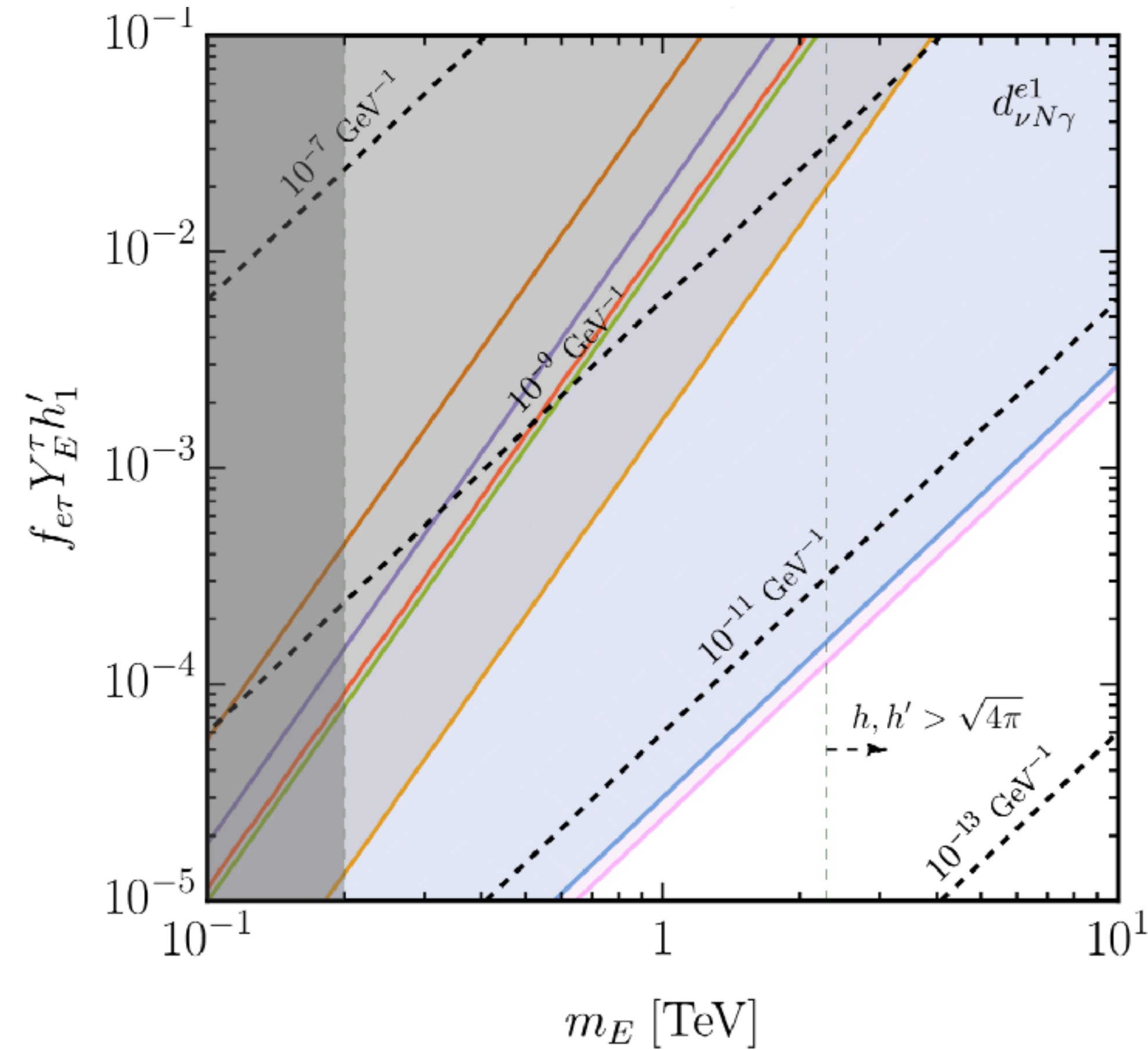
Without Z_2 , at one-loop in the UV model:



Matching:
$$C_{NB}^{(6)\alpha i} = \frac{1}{16\pi^2} \frac{3g'_{\alpha\beta} Y_E^{\beta*} h'_i}{4m_E^2} f(r) \quad C_{NW}^{(6)\alpha i} = \frac{1}{16\pi^2} \frac{g f_{\alpha\beta} Y_E^{\beta*} h'_i}{2m_E^2} f(r).$$

The UV model therefore predicts $a = \frac{g'}{g} \frac{C_{NW}^{(6)\alpha i}}{C_{NB}^{(6)\alpha i}} = \frac{2}{3}$ which narrows down the phenomenology

Active-to-Sterile Neutrino Magnetic Moments



$$d_{\nu N \gamma}^{\alpha i} = \frac{4vc_w}{3\sqrt{2}} C_{NB}^{(6)\alpha i} \approx 1.7 \times 10^{-9} \text{ GeV}^{-1} \left(\frac{f_{\alpha\beta} Y_E^{\beta*} h'_i}{10^{-2}} \right) \left(\frac{1 \text{ TeV}}{m_E} \right)^2$$

Other Constraints on UV Scenario

Charged Lepton Flavour Violation Bounds

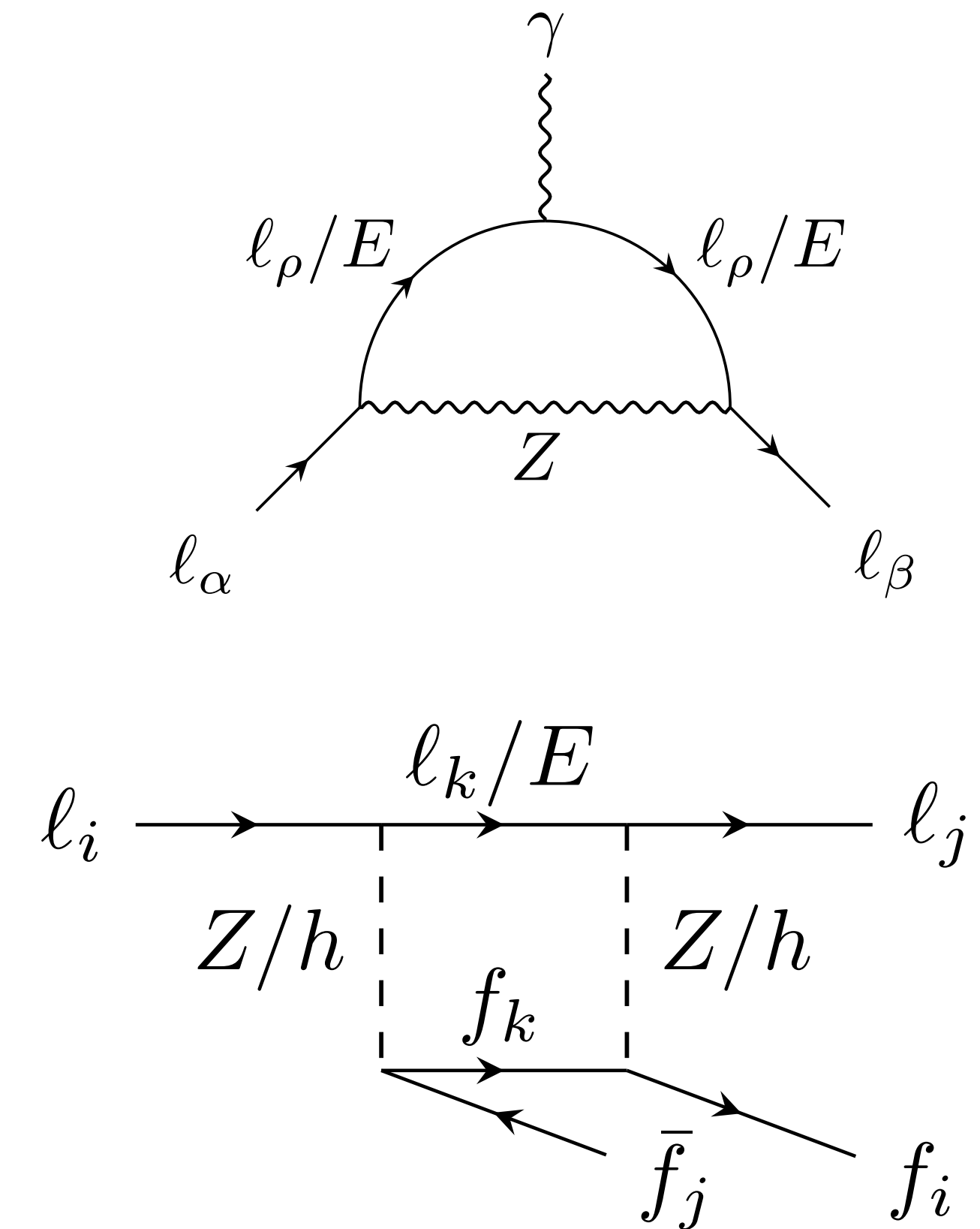
cLFV processes via the general couplings Y_E^α and $f_{\alpha\beta}$ can also be used to constrain the model:

Tree-level

- $\mu \rightarrow 3e, \tau \rightarrow 3e, \tau \rightarrow 3\mu$ (SINDRUM, Belle)
- $\mu \rightarrow e$ conversion in nuclei (SINDRUM)
- LFU violation in charged-currents
- Flavour-violating Z and Higgs decays (ATLAS, CMS)

One-loop

- $\mu \rightarrow e\gamma, \tau \rightarrow e\gamma, \tau \rightarrow \mu\gamma$ (MEG, BaBar)



Direct Production Bounds

The vector-like lepton E and singly-charged scalar ϕ can also be produced directly at the LHC

- Drell-Yan production: $pp \rightarrow \gamma/Z \rightarrow E^+E^-$, $pp \rightarrow \gamma/Z \rightarrow \phi^+\phi^-$
- Decays: $\phi^\pm \rightarrow \ell^\pm\nu$, $E^\pm(\rightarrow N\phi^\pm) \rightarrow \ell^\pm\nu N$

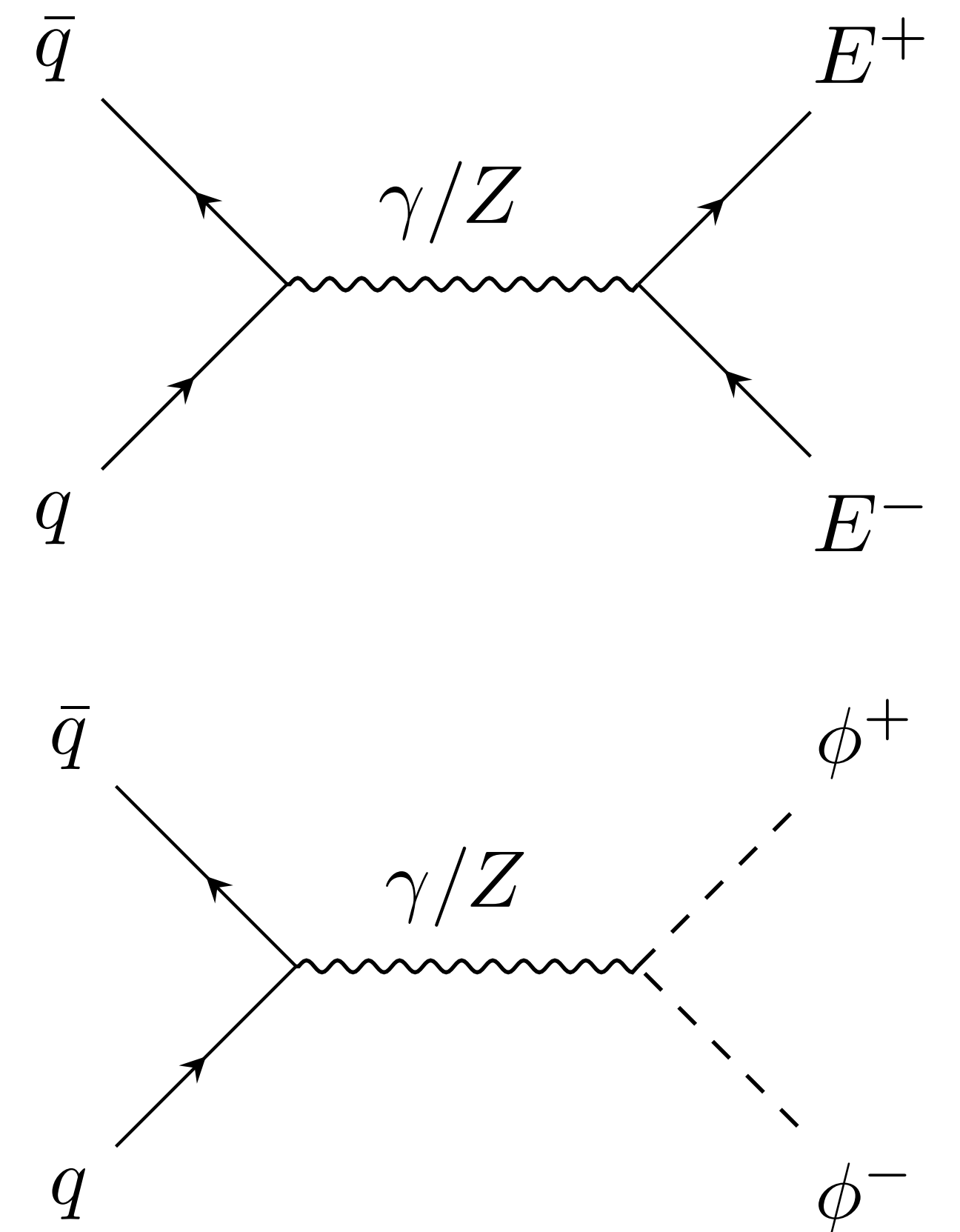
Recast:

- Slepton ATLAS search using oppositely-charged e and μ pairs

$$m_E, m_\phi \gtrsim 200 \text{ GeV}$$

- Dark matter LEP monophoton bounds

$$m_\phi / |f_{e\mu}|^2 \gtrsim 350 \text{ GeV}$$



Benchmark Flavour Scenarios

1) **Flavour universal** couplings: $Y_E^e = Y_E^\mu = Y_E^\tau = f_{e\mu} = f_{e\tau} = f_{\mu\tau}$

└ Strongest bounds from $\mu \rightarrow 3e$ and $\mu \rightarrow e$ conversion (tree-level)

2) **'Tau-only'** couplings: $Y_E^e = Y_E^\mu = f_{e\mu} = 0$, $Y_E^\tau = f_{e\tau} = f_{\mu\tau} \neq 0$

└ Strongest bounds from $\mu \rightarrow e\gamma$ and $\mu \rightarrow 3e$ (one-loop)

3) **'No electron' or $\mu - \tau$** couplings: $Y_E^e = f_{e\mu} = f_{e\tau} = 0$, $Y_E^\mu = Y_E^\tau = f_{\mu\tau} \neq 0$

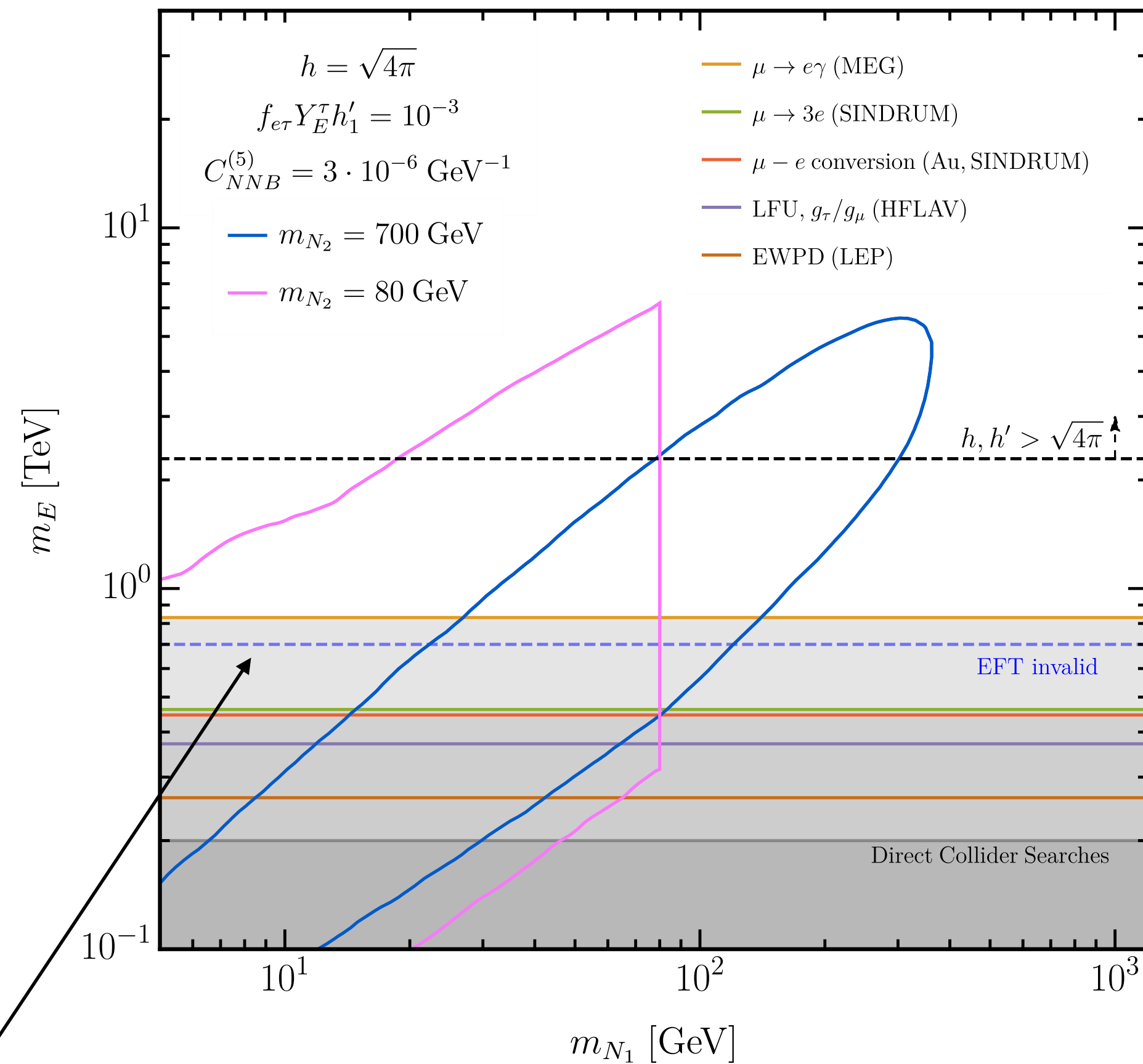
└ Strongest bounds from $\tau \rightarrow 3\mu$ and $\tau \rightarrow \mu ee$ (tree-level)

Active-to-Sterile Bounds

$$h, h' > \sqrt{4\pi} \text{ to obtain } C_{NNB}^{(5)}$$

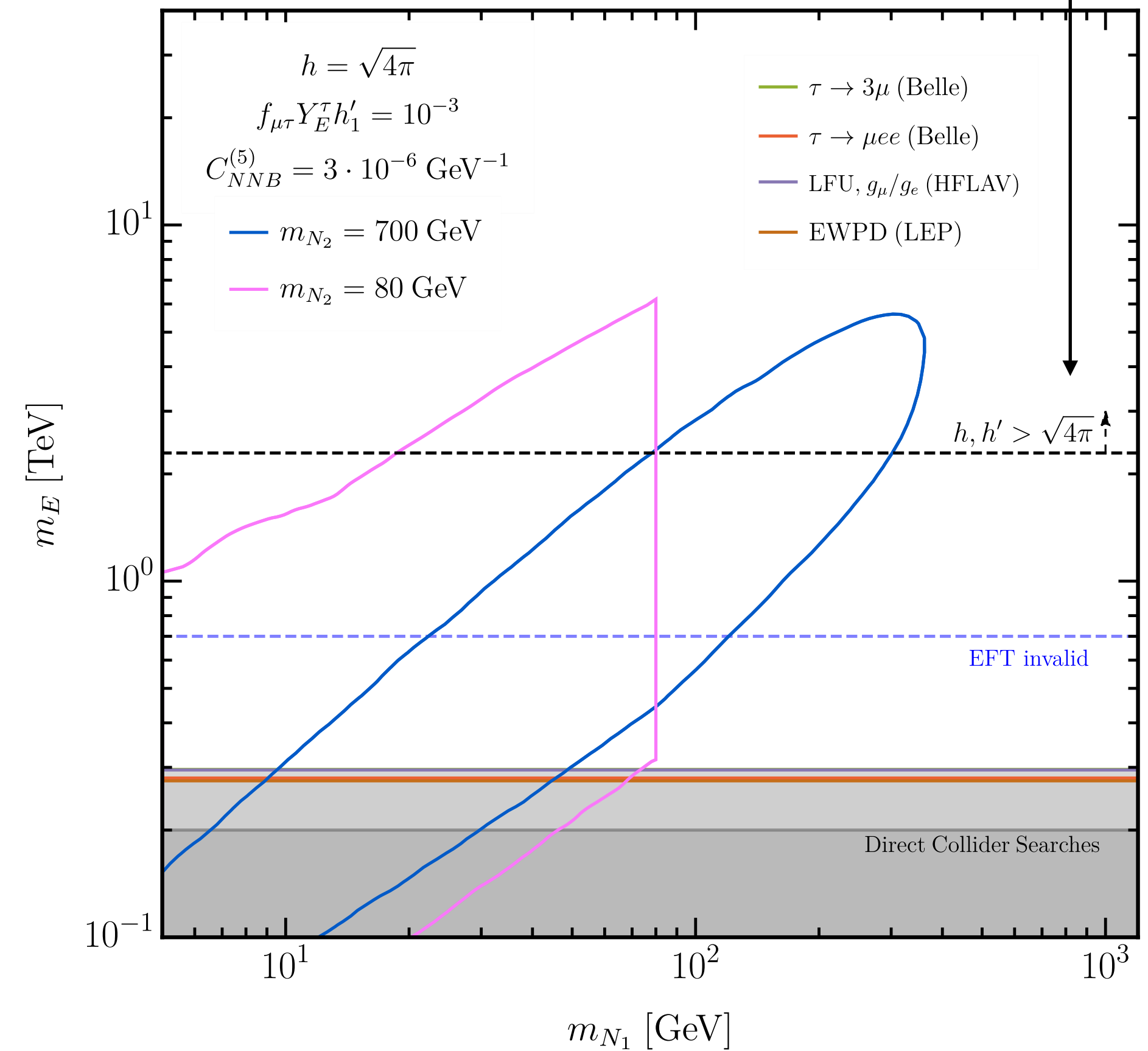
'No e ' couplings

$$Y_E^\tau = f_{e\tau} = f_{\mu\tau} \neq 0$$



' τ only' couplings

$$Y_E^\mu = Y_E^\tau = f_{\mu\tau} \neq 0$$



EFT invalid for $m_E < m_{N_2} = 700 \text{ GeV}$