

# SINGLE AND DOUBLE SCATTERING PRODUCTION OF FOUR LEPTONS IN LEAD-LEAD UPC

MARIOLA KLUSEK-GAWENDA



THE HENRYK NIEWODNICZAŃSKI  
INSTITUTE OF NUCLEAR PHYSICS  
POLISH ACADEMY OF SCIENCES

MPI@LHC'17

FOUR LEPTONS IN  
Pb-Pb UPC

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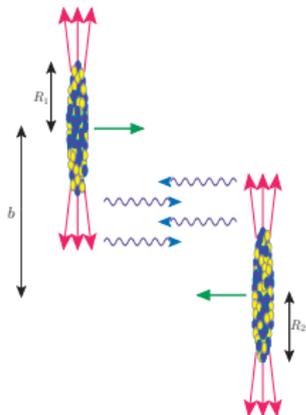
FOUR-LEPTON  
PRODUCTION

ELECTRONS

MUONS

CONCLUSION

EPA  
 FOUR-LEPTON PRODUCTION  
 CONCLUSION

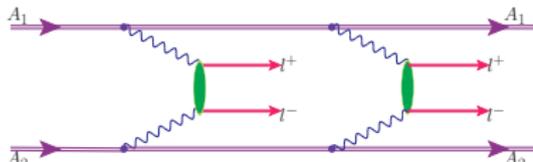


ULTRAPERIPHERAL COLLISIONS

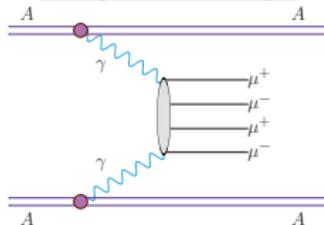
$$b > R_{min} = R_1 + R_2$$

1. M. K-G, A. Szczurek, Double scattering production of two positron–electron pairs in ultraperipheral heavy-ion collisions, Phys. Lett. **B763** (2016) 416,
2. A. van Hameren, M. K-G, A. Szczurek, From the Single- and double-scattering production of four muons in ultraperipheral PbPb collisions at the Large Hadron Collider, Phys. Lett. **B776** (2018) 84,

Double-scattering



Single-scattering



ALICE, ATLAS, CMS, LHCb ( $^{208}\text{Pb} + ^{208}\text{Pb}$  @  $\sqrt{s_{NN}} = 2.76, 3.5, 5.02, 5.5$  TeV)

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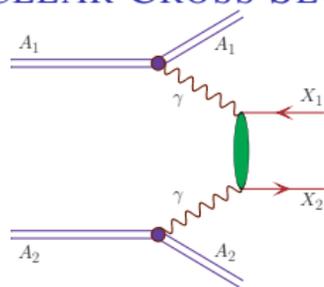
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# NUCLEAR CROSS SECTION



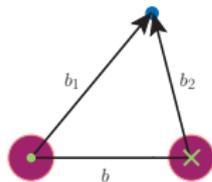
$$\sigma_{A_1 A_2 \rightarrow A_1 A_2 X_1 X_2} = \dots$$

$$\text{NAIVELY} \Rightarrow \dots = \int d\omega_1 d\omega_2 n(\omega_1) n(\omega_2) \\ \times \sigma_{\gamma\gamma \rightarrow X_1 X_2}(\omega_1, \omega_2)$$

$$n(\omega) = \int_{R_{min}}^{\infty} 2\pi b db N(\omega, b)$$

MORE

$$\text{CORRECTLY} \Rightarrow \dots = \int N(\omega_1, \mathbf{b}_1) N(\omega_2, \mathbf{b}_2) S_{abs}^2(\mathbf{b}) \\ \times \sigma_{\gamma\gamma \rightarrow X_1 X_2}(W_{\gamma\gamma}) \\ \times d^2b d\bar{b}_x d\bar{b}_y \frac{W_{\gamma\gamma}}{2} dW_{\gamma\gamma} dY_{X_1 X_2}$$



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# PHOTON FLUX & FORM FACTOR

$\chi$  charge distribution in nucleus

$$N(\omega, b) = \frac{Z^2 \alpha_{em}}{\pi^2 \beta^2} \frac{1}{\omega} \frac{1}{b^2} \times \left| \int d\chi \chi^2 \frac{F\left(\frac{\chi^2 + u^2}{b^2}\right)}{\chi^2 + u^2} J_1(\chi) \right|^2$$

$$\beta = \frac{p}{E}, \gamma = \frac{1}{\sqrt{1-\beta^2}}, u = \frac{\omega b}{\gamma \beta}, \chi = k_{\perp} b$$

► realistic charge distribution

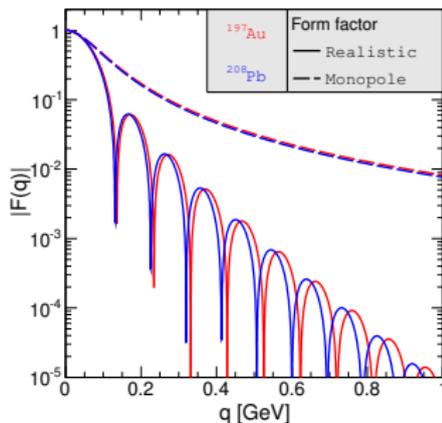
$$F(\mathbf{q}^2) = \frac{4\pi}{|\mathbf{q}|} \int \rho(r) \sin(|\mathbf{q}| r) r dr$$

► point-like  $F(\mathbf{q}^2) = 1$

$$N(\omega, b) = \frac{Z^2 \alpha_{em}}{\pi^2 \beta^2} \frac{1}{\omega} \frac{1}{b^2} \times u^2 \left[ K_1^2(u) + \frac{1}{\gamma^2} K_0^2(u) \right]$$

► monopole  $F(\mathbf{q}^2) = \frac{\Lambda^2}{\Lambda^2 + |\mathbf{q}|^2}$

$$\sqrt{\langle r^2 \rangle} = \sqrt{\frac{6}{\Lambda^2}} = 1 \text{ fm } A^{1/3}$$



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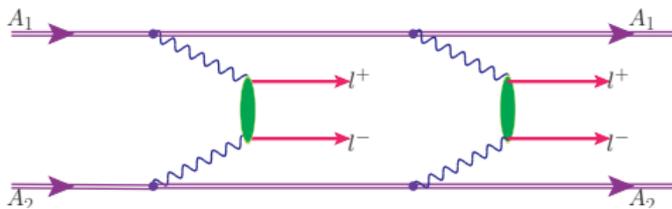
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## FOUR-LEPTON PRODUCTION



$$\begin{aligned}
 P_{AA \rightarrow AA l^+ l^-}^{\gamma\gamma}(b; y_{l^+}, y_{l^-}, p_{t,l}) &= \int N(\omega_1, \mathbf{b}_1) N(\omega_2, \mathbf{b}_2) S_{abs}^2(\mathbf{b}) \\
 &\times \frac{d\sigma_{\gamma\gamma \rightarrow l^+ l^-}(W_{\gamma\gamma})}{dz} d\bar{b}_x d\bar{b}_y \frac{W_{\gamma\gamma}}{2} dW_{\gamma\gamma} dY_{l^+ l^-} \\
 \frac{d\sigma_{A_1 A_2 \rightarrow A_1 A_2 l^+ l^-}}{dy_{l^+} dy_{l^-} dp_{t,l} dy_{l^+} dy_{l^-} dp_{t,l}} &= \frac{1}{2} \int \frac{dP^I}{dy_{l^+} dy_{l^-} dp_{t,l}} \frac{d\sigma_{AA \rightarrow AA l^+ l^-}^{\gamma\gamma}(b; y_{l^+}, y_{l^-}, p_{t,l})}{dy_{l^+} dy_{l^-} dp_{t,l}} \\
 &\times \frac{dP^{II}}{dy_{l^+} dy_{l^-} dp_{t,l}} \frac{d\sigma_{AA \rightarrow AA l^+ l^-}^{\gamma\gamma}(b; y_{l^+}, y_{l^-}, p_{t,l})}{dy_{l^+} dy_{l^-} dp_{t,l}} d^2b \\
 \sigma_{A_1 A_2 \rightarrow A_1 A_2 l^+ l^-} &= \int \frac{dP}{dy_{l^+} dy_{l^-} dp_{t,l}} \frac{d\sigma_{AA \rightarrow AA l^+ l^-}^{\gamma\gamma}(b; y_{l^+}, y_{l^-}, p_{t,l})}{dy_{l^+} dy_{l^-} dp_{t,l}} d^2b \\
 &\times dy_{l^+} dy_{l^-} dp_{t,l}
 \end{aligned}$$

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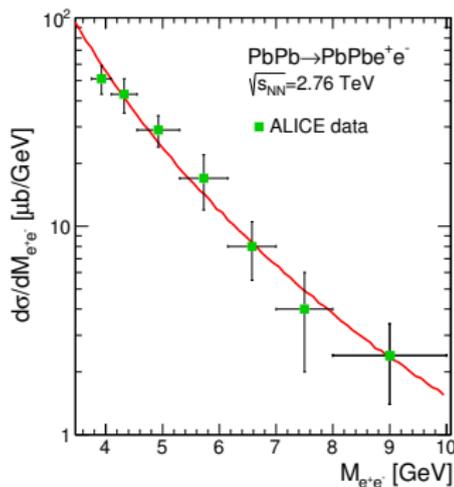
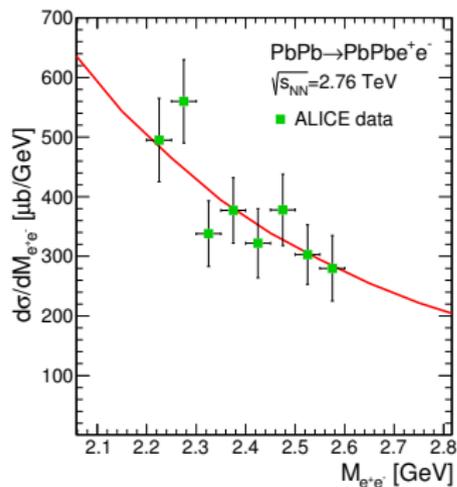
# $AA \rightarrow AAe^+e^-$ - CALCULATIONS VS. DATA

- ALICE Collaboration (Abbas, E. et al.),  
*Charmonium and  $e^+e^-$  pair photoproduction at mid-rapidity in ultra-peripheral Pb-Pb collisions at  $\sqrt{s_{NN}} = 2.76$  TeV*,  
Eur. Phys. J. **C73** (2013) 2617

$2.2 \text{ GeV} < M_{ee} < 2.6 \text{ GeV}$

$|y_e| < 0.9$

$3.7 \text{ GeV} < M_{ee} < 10 \text{ GeV}$



Good description of single pair production  $\Rightarrow$  two  $e^+e^-$  pair production

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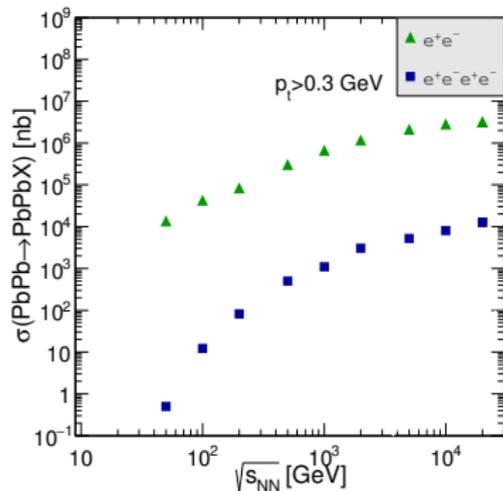
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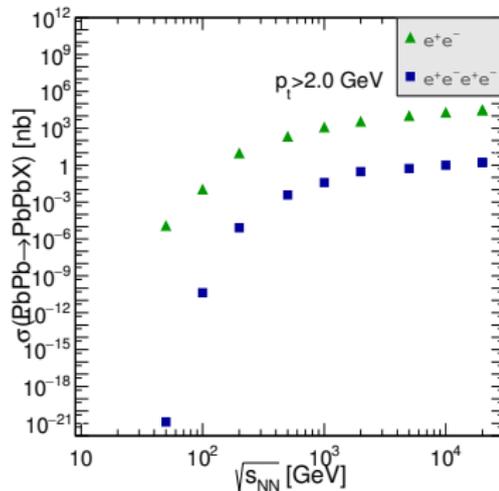
CONCLUSION

$$AA \rightarrow AAe^+e^- \text{ \& \ } AA \rightarrow AAe^+e^-e^+e^-$$

$p_t > 0.3 \text{ GeV}$



$p_t > 2.0 \text{ GeV}$



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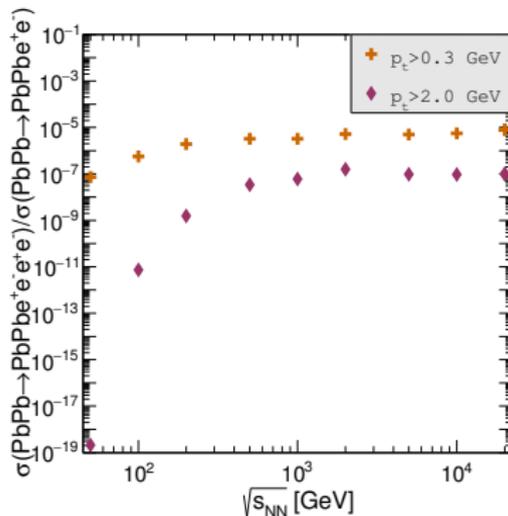
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$$AA \rightarrow AAe^+e^- \text{ \& \ } AA \rightarrow AAe^+e^-e^+e^-$$

$$\frac{\sigma_{AA \rightarrow AAe^+e^-e^+e^-}}{\sigma_{AA \rightarrow AAe^+e^-}}$$



Ratio depends on  $\sqrt{s_{NN}}$  and  $p_{t,min}$

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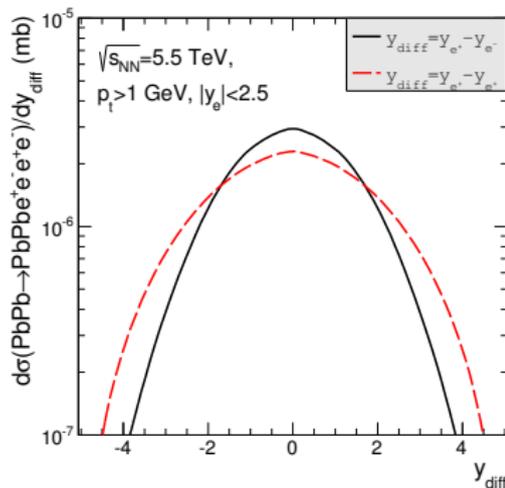
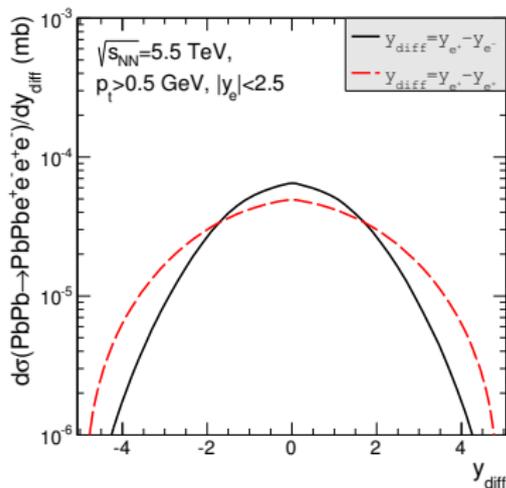
CONCLUSION

$$AA \rightarrow AAe^+e^-e^+e^-$$

 $y_{diff}$ 
 $p_{t,e} > 0.5 \text{ GeV}$ 

$$\Rightarrow y_{e^+} - y_{e^-}$$

$$\Rightarrow y_{e^+} - y_{e^+}$$

 $p_{t,e} > 1.0 \text{ GeV}$ 


Can be measured...  $\Rightarrow$  First verification of the DS

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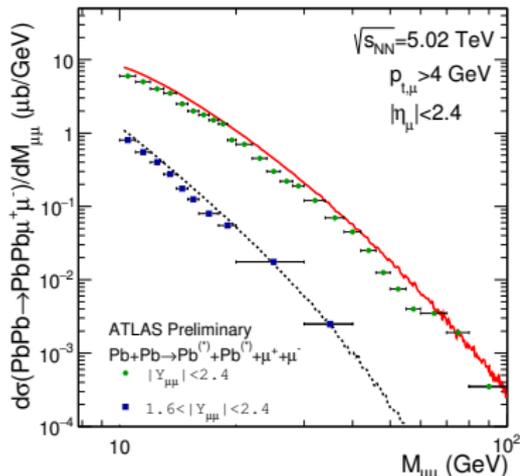
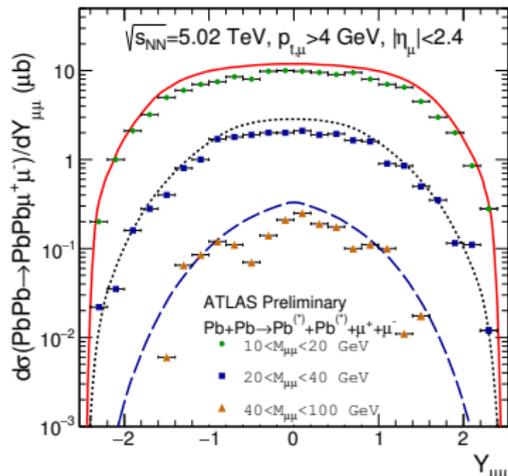
# AA $\rightarrow$ AA $\mu^+\mu^-$ - CALCULATIONS VS. DATA

- ATLAS Collaboration,  
*Measurement of high-mass dimuon pairs from ultraperipheral lead-lead collisions at  $\sqrt{s_{NN}} = 5.02$  TeV with the ATLAS detector at the LHC, ATLAS-CONF-2016-025*

$$\frac{d\sigma}{dY_{\mu^+\mu^-}}$$

$$p_{t,\mu} > 4 \text{ GeV}, |\eta_e| < 0.9$$

$$\frac{d\sigma}{dM_{\mu^+\mu^-}}$$



"Overwriting" of single  $\mu^+\mu^-$  pair production vs. preliminary data

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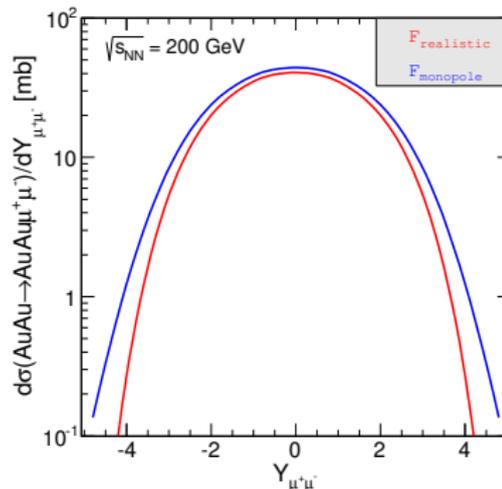
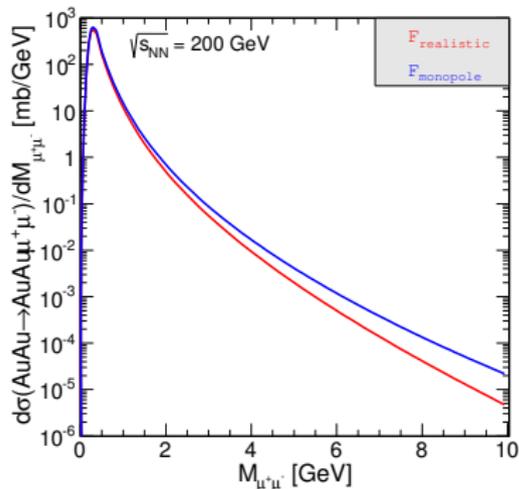
# AA → AAμ<sup>+</sup>μ<sup>-</sup> - FORM FACTOR

⇒ realistic

⇒ monopole

$$M_{\mu^+\mu^-}$$

$$Y_{\mu^+\mu^-}$$



$\frac{\sigma_{\text{monopole}}}{\sigma_{\text{realistic}}}$  ↗ for larger values of kinematic variables

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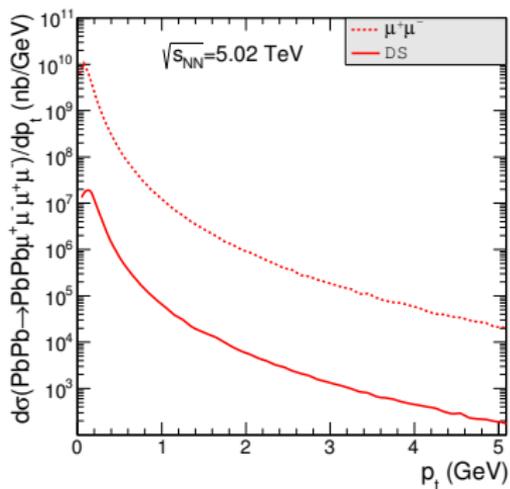
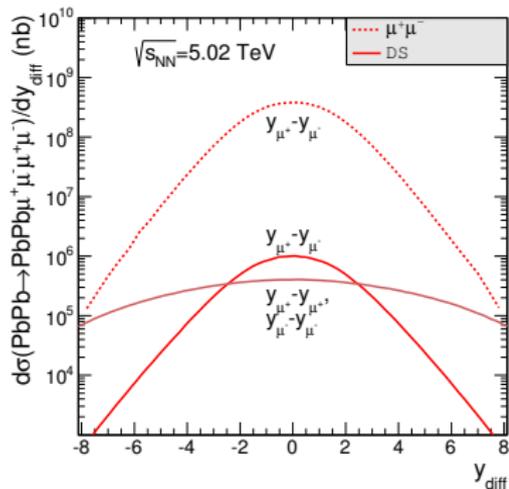
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$$AA \rightarrow AA\mu^+\mu^- \text{ \& \ } AA \rightarrow AA\mu^+\mu^-\mu^+\mu^-$$

 $p_{t,\mu}$ 

 $y_{diff}$ 


Similar like for electron-positron production:  $\sigma_{\mu^+\mu^-} \simeq 1000 \times \sigma_{\mu^+\mu^-\mu^+\mu^-}$

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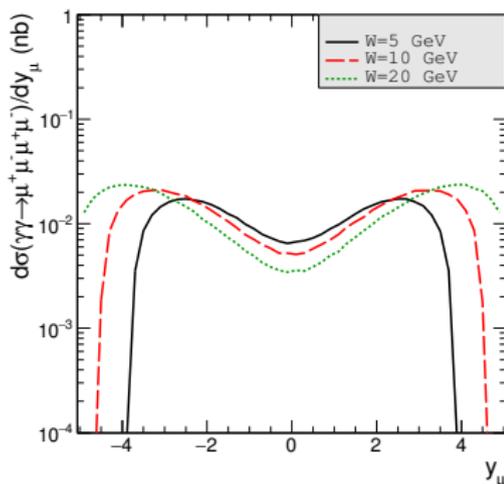
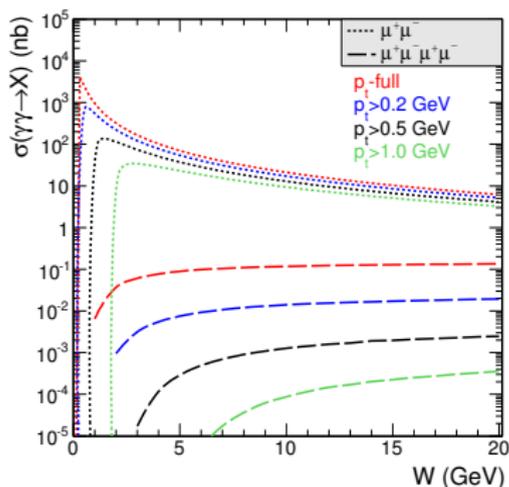
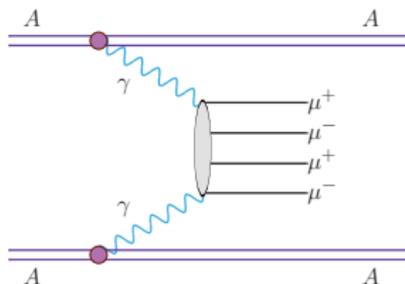
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# $\gamma\gamma \rightarrow \mu^+\mu^-\mu^+\mu^-$ - SINGLE SCATTERING



KATIE- an event generator that is specially designed to deal with initial states that have an explicit transverse momentum dependence, but can also deal with on-shell initial states. KATIE is a parton-level generator for hadron scattering, but requires only a few adjustments to deal with photon scattering.



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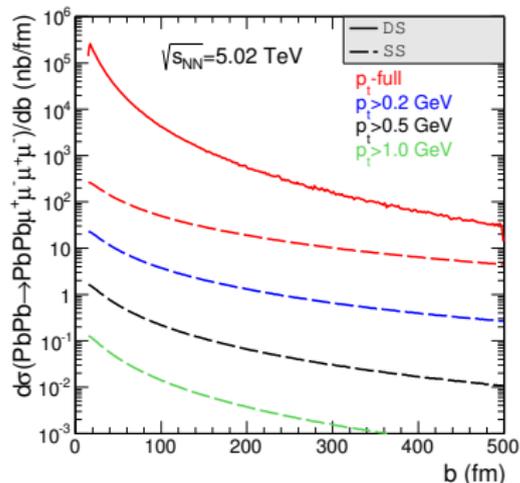
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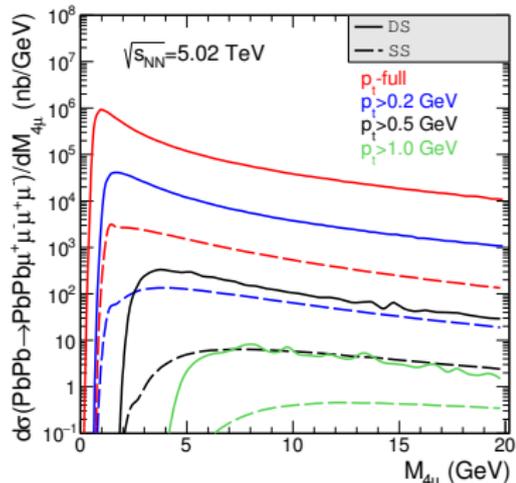
$$AA \rightarrow AA \mu^+ \mu^- \mu^+ \mu^-$$

impact parameter



↑ purely theoretical distribution

$W_{\gamma\gamma} = M_{4\mu}$



↑ DS dominates

It is difficult to isolate range of SS domination

- \*DS - double-scattering mechanism
- \*SS - a NEW single-scattering mechanism

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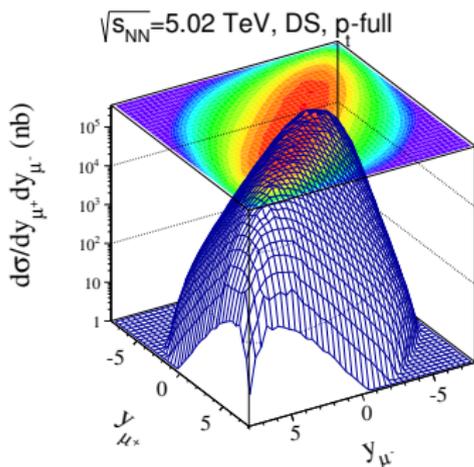
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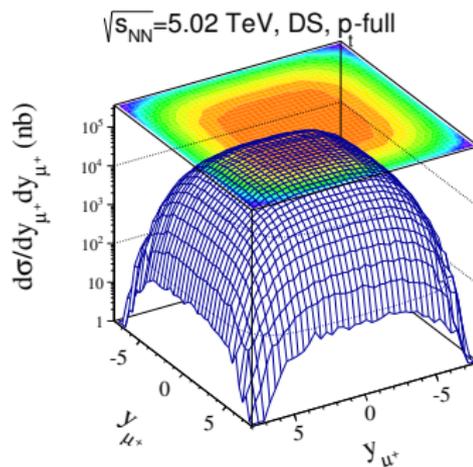
CONCLUSION

$$AA \rightarrow AA \mu^+ \mu^- \mu^+ \mu^-$$

$$y_{\mu^+}, y_{\mu^-}$$



$$y_{\mu^\pm}, y_{\mu^\pm}$$



$p_{t,\mu^+} \simeq p_{t,\mu^-} \Rightarrow$  construction of similar distributions by ALICE or CMS?

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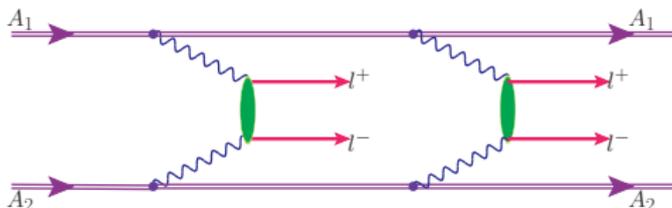
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The number of counts for  $L_{int} = 1 \text{ nb}^{-1}$

$(4\mu), \sqrt{s_{NN}} = 5.02 \text{ TeV}$		$(4e), \sqrt{s_{NN}} = 5.5 \text{ TeV}$	
experimental cuts	N	experimental cuts	N
$ y_i  < 2.5, p_t > 0.5 \text{ GeV}$	815	$ y_i  < 2.5, p_t > 0.5 \text{ GeV}$	235
$ y_i  < 2.5, p_t > 1.0 \text{ GeV}$	53	$ y_i  < 2.5, p_t > 1.0 \text{ GeV}$	10
$ y_i  < 0.9, p_t > 0.5 \text{ GeV}$	31	$ y_i  < 1.0, p_t > 0.2 \text{ GeV}$	649
$ y_i  < 0.9, p_t > 1.0 \text{ GeV}$	2	$ y_i  < 1.0, p_t > 1.0 \text{ GeV}$	1
$ y_i  < 2.4, p_t > 4.0 \text{ GeV}$	$\ll 1$		

CMS and ALICE  $\Rightarrow p_{t,cut} = 1 \text{ GeV}$

ALICE  $\Rightarrow p_{t,cut} = 0.2 \text{ GeV}$

ATLAS  $\Rightarrow p_{t,cut} = 4 \text{ GeV}$  **Potential background**

$\downarrow \sqrt{s_{NN}} = 5.5 \text{ TeV}, |y| < 4.9$

Reaction	$p_{t,min} = 0.3 \text{ GeV}$	$p_{t,min} = 0.5 \text{ GeV}$
$PbPb \rightarrow PbPb\pi^+\pi^-\pi^+\pi^-$	2.954 mb	8.862 $\mu\text{b}$
$PbPb \rightarrow PbPbe^+e^-e^+e^-$	7.447 $\mu\text{b}$	0.704 $\mu\text{b}$

# CONCLUSION

- EPA in the impact parameter space
- Realistic charge distribution
- Description of the
  - ▶ ALICE data for  $Pb\ Pb \rightarrow Pb\ Pb\ e^+ e^-$  and
  - ▶ ATLAS data for  $Pb\ Pb \rightarrow Pb\ Pb\ \mu^+ \mu^-$
- $Pb\ Pb \rightarrow Pb\ Pb\ \mu^+ \mu^- \mu^+ \mu^- \Rightarrow \sigma_{SS}^{NEW} < \sigma_{DS}$
- Difficult to isolate a region where SS dominates
- $\sigma_{PbPb \rightarrow PbPb l^+ l^-} \cong 1000 \times \sigma_{PbPb \rightarrow PbPb l^+ l^- l^+ l^-}$
- The cross sections for four-lepton production strongly depend on the  $p_{t,min}$  and  $y_l$
- Triple scattering production  $\rightarrow$  smaller cross section

Thank you