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Saha Theory Workshop: Cosmology at the interface

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Constraining $\mathcal{N} = 1$ supergravity inflationary framework with non-minimal Kähler operators

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ABSTRACT: In this paper we will illustrate how to constrain unavoidable Kähler corrections for $\mathcal{N} = 1$ supergravity (SUGRA) inflation from the recent Planck data. We will show that the non-renormalizable Kähler operators will induce in general a *minimal kinetic* term for the inflaton field, and two types of SUGRA corrections in the potential — the *Hubble-induced mass* (c_H), and the *Hubble-induced A-term* (a_H) correction. The entire SUGRA inflationary framework can now be constrained from (i) the *speed of sound*, c_s , and (ii) from the upper bound on the *tensor to scalar ratio*, r_* . We will illustrate this by considering a heavy scalar degree of freedom at a scale, M_s , and a light inflationary field which is responsible for a slow-roll inflation. We will compute the corrections to the kinetic term and the potential for the light field explicitly. As an example, we will consider a visible sector inflationary model of inflation where inflation occurs at the point of *inflection*, which can match the density perturbations for the cosmic microwave background radiation, and also explain why the universe is filled with the Standard Model degrees of freedom. We will scan the parameter space of the non-renormalizable Kähler operators, which we find them to be order $\mathcal{O}(1)$, consistent with physical arguments. While the scale of heavy physics is found to be bounded by the tensor-to scalar ratio, and the speed of sound, $\mathcal{O}(10^{11} \leq M_s \leq 10^{16})$ GeV, for $0.02 \leq c_s \leq 1$ and $10^{-22} \leq r_* \leq 0.12$.

KEYWORDS: Cosmology of Theories beyond the SM, Supersymmetric Effective Theories, Supergravity Models

ARXIV EPRINT: [1402.1227](https://arxiv.org/abs/1402.1227)

Constraining $\mathcal{N} = 1$ supergravity inflation with non-minimal Kähler operators using δN formalism

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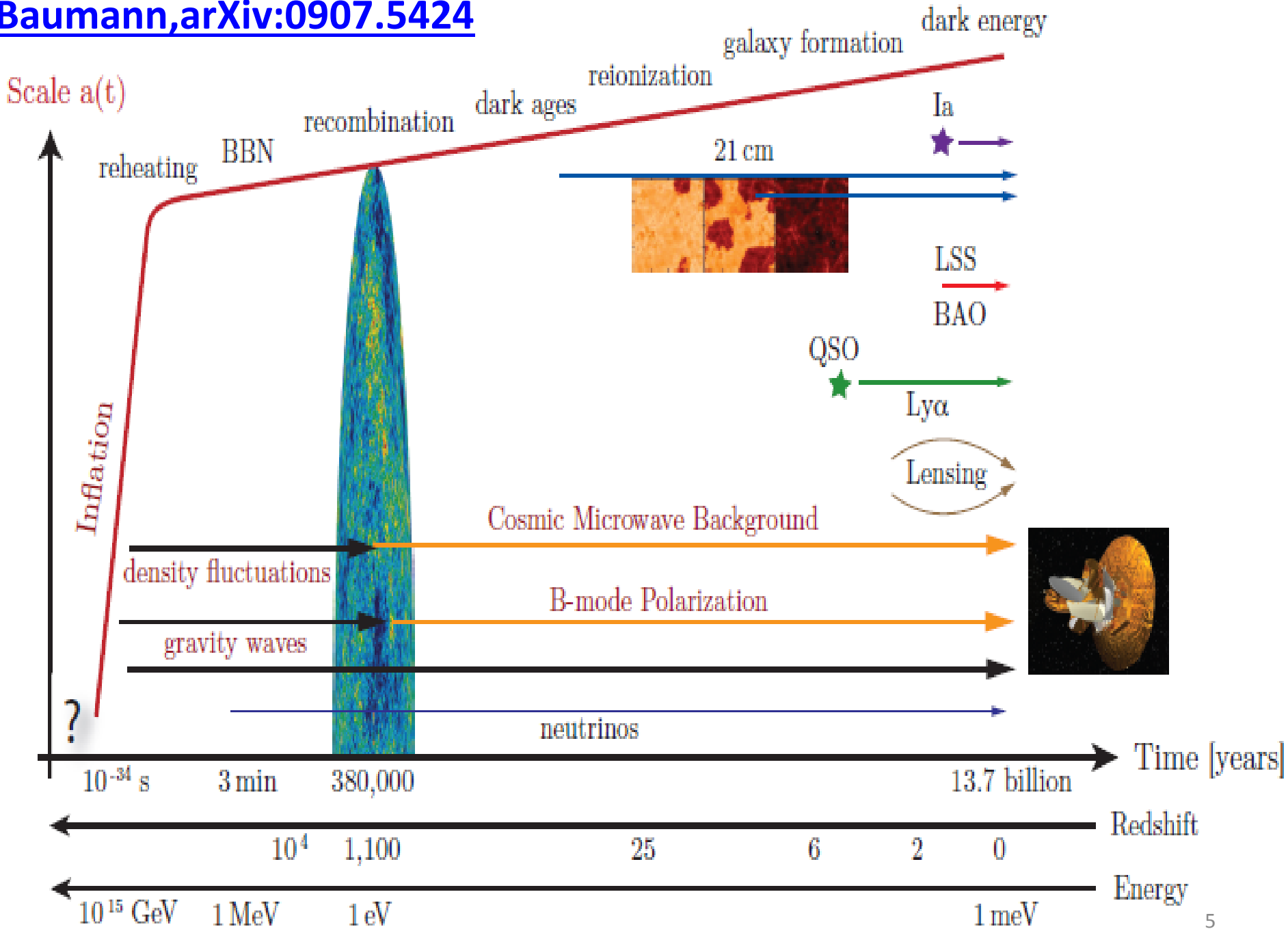
ABSTRACT: In this paper I provide a general framework based on δN formalism to study the features of unavoidable higher dimensional non-renormalizable Kähler operators for $\mathcal{N} = 1$ supergravity (SUGRA) during primordial inflation from the combined constraint on non-Gaussianity, sound speed and CMB dipolar asymmetry as obtained from the recent Planck data. In particular I study the nonlinear evolution of cosmological perturbations on large scales which enables us to compute the curvature perturbation, ζ , without solving the exact perturbed field equations. Further I compute the non-Gaussian parameters f_{NL} , τ_{NL} and g_{NL} for local type of non-Gaussianities and CMB dipolar asymmetry parameter, A_{CMB} , using the δN formalism for a generic class of sub-Planckian models induced by the Hubble-induced corrections for a minimal supersymmetric D-flat direction where inflation occurs at the point of inflection within the visible sector. Hence by using multi parameter scan I constrain the non-minimal couplings appearing in non-renormalizable Kähler operators within, $\mathcal{O}(1)$, for the speed of sound, $0.02 \leq c_s \leq 1$, and tensor to scalar, $10^{-22} \leq r_* \leq 0.12$. Finally applying all of these constraints I will fix the lower as well as the upper bound of the non-Gaussian parameters within, $\mathcal{O}(1 - 5) \leq f_{NL} \leq 8.5$, $\mathcal{O}(75 - 150) \leq \tau_{NL} \leq 2800$ and $\mathcal{O}(17.4 - 34.7) \leq g_{NL} \leq 648.2$, and CMB dipolar asymmetry parameter within the range, $0.05 \leq A_{CMB} \leq 0.09$.

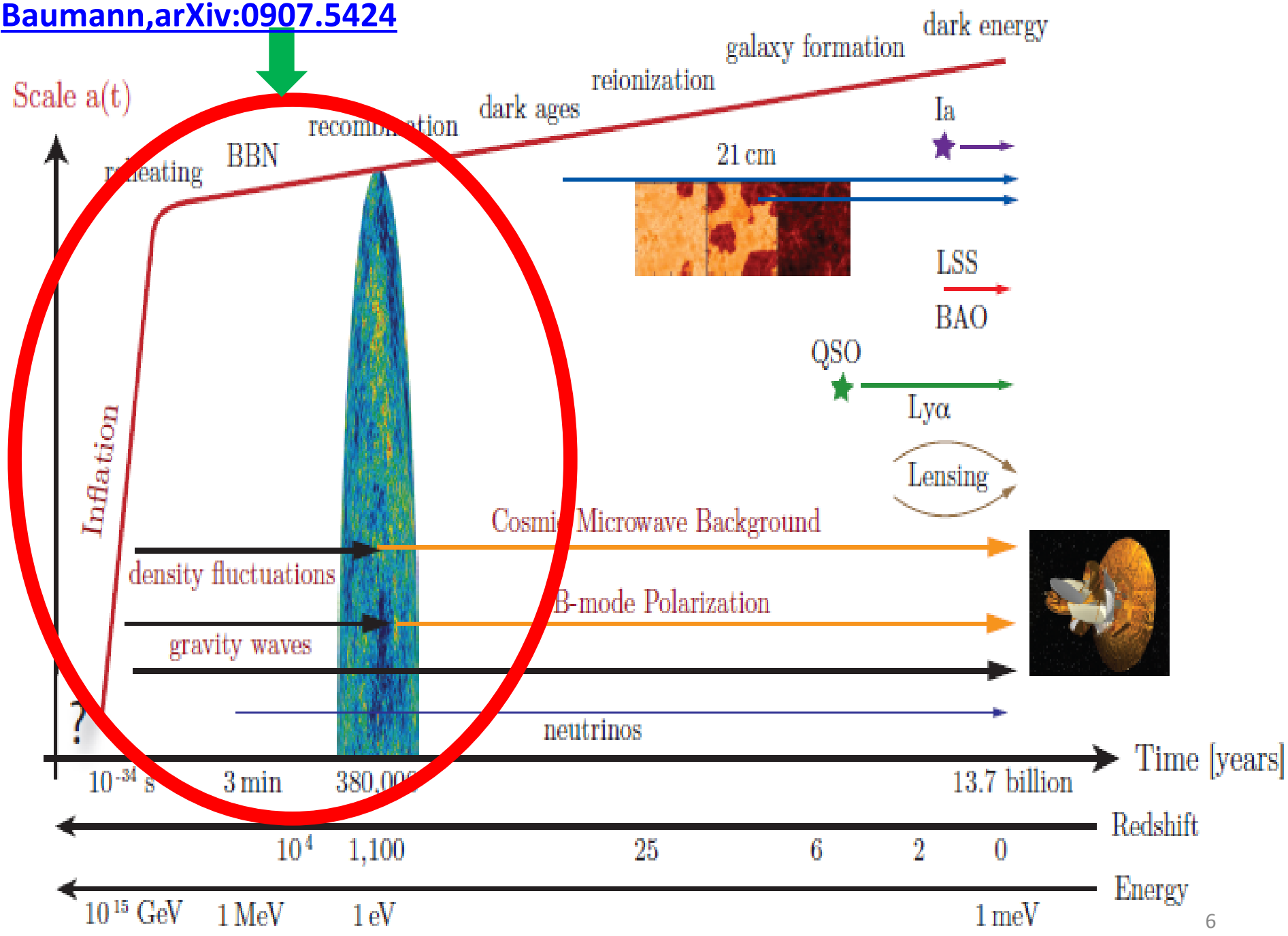
KEYWORDS: Cosmology of Theories beyond the SM, Supersymmetric Effective Theories, Supergravity Models

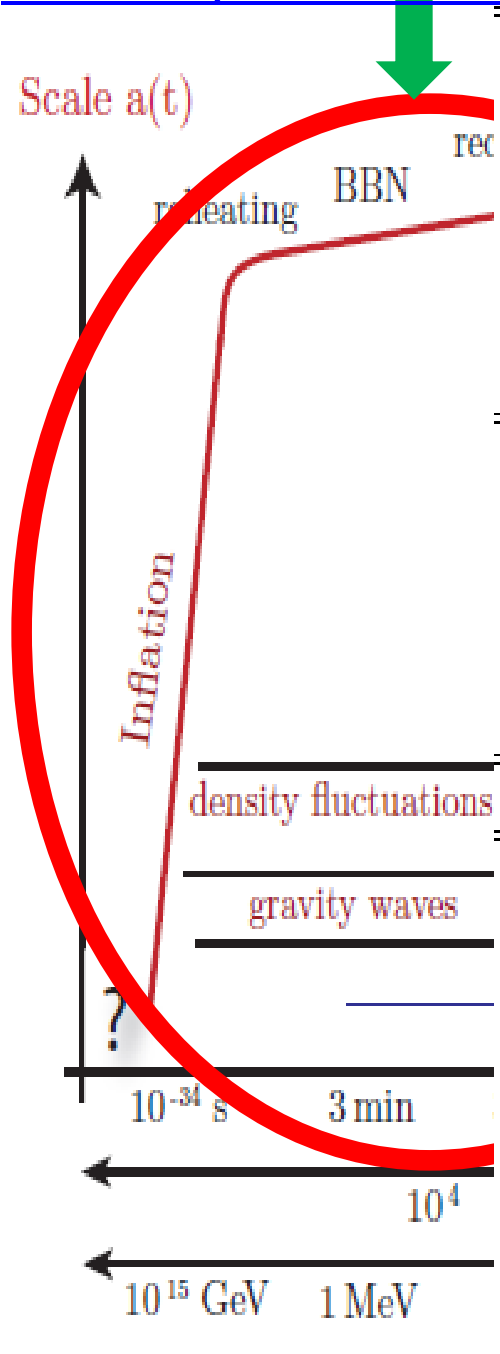
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Outline of talk

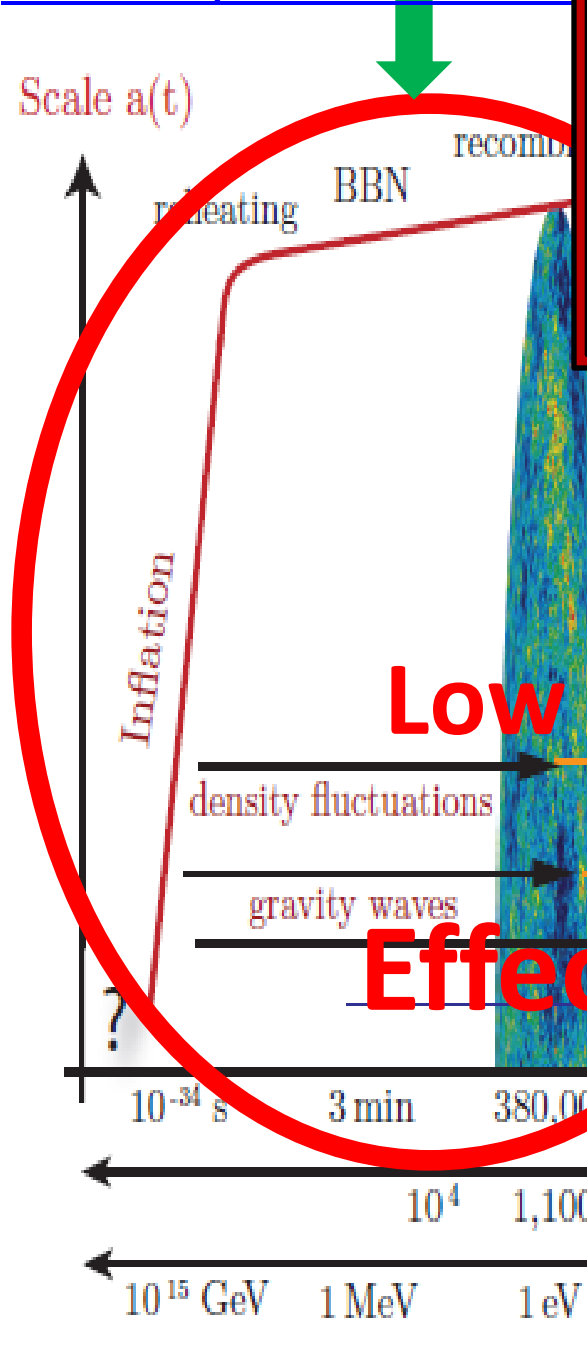
- EFT Redux.
- The EFT setup for N=1 SUGRA.
- Non-minimal interactions in N=1 SUGRA.
- Gauge invariant inflatons.
- Primordial non-Gaussianity using δN formalism.
- Model (MSSM) constraints.
- Bottom lines and future prospects.







	Time	Energy
Planck Epoch?	$< 10^{-43}$ s	10^{18} GeV
String Scale?	$\gtrsim 10^{-43}$ s	$\gtrsim 10^{18}$ GeV
Grand Unification?	$\sim 10^{-36}$ s	10^{15} GeV
Inflation?	$\gtrsim 10^{-34}$ s	$\gtrsim 10^{15}$ GeV
SUSY Breaking?	$< 10^{-10}$ s	> 1 TeV
Baryogenesis?	$< 10^{-10}$ s	> 1 TeV
Electroweak Unification	10^{-10} s	1 TeV
Quark-Hadron Transition	10^{-4} s	10^2 MeV
Nucleon Freeze-Out	0.01 s	10 MeV
Neutrino Decoupling	1 s	1 MeV
BBN	3 min	0.1 MeV
density fluctuations		
Matter-Radiation Equality	10^4 yrs	1 eV
Recombination	10^5 yrs	0.1 eV
Dark Ages	$10^5 - 10^8$ yrs	
Reionization	10^8 yrs	
Galaxy Formation	$\sim 6 \times 10^8$ yrs	
Dark Energy	$\sim 10^9$ yrs	
Solar System	8×10^9 yrs	
Albert Einstein born	14×10^9 yrs	1 meV^7



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Dark Energy	$\sim 10^9$ yrs	
Solar System	8×10^9 yrs	
Albert Einstein born	14×10^9 yrs	1 meV^8

Low Energy version of Superstring Theory

Effective Theory prescription of N=1 Supergravity

Constructing EFTs from the Top Down

“Integrating out”

EFT Redux



If the full theory is known (and computable), we can integrate out the heavy fields to get an effective theory for the light fields :

$$e^{iS_{\text{eff}}[\phi]} = \int \mathcal{D}\Psi e^{iS[\phi, \Psi]}$$

Let me illustrate this in a toy model:

$$\mathcal{L}[\phi, \Psi] = -\frac{1}{2}(\partial\phi)^2 - \frac{1}{2}m^2\phi^2 - \frac{1}{4!}\lambda\phi^4$$
$$-\frac{1}{2}(\partial\Psi)^2 - \frac{1}{2}M^2\Psi^2 - \frac{1}{4}g\phi^2\Psi^2$$

Light visible sector

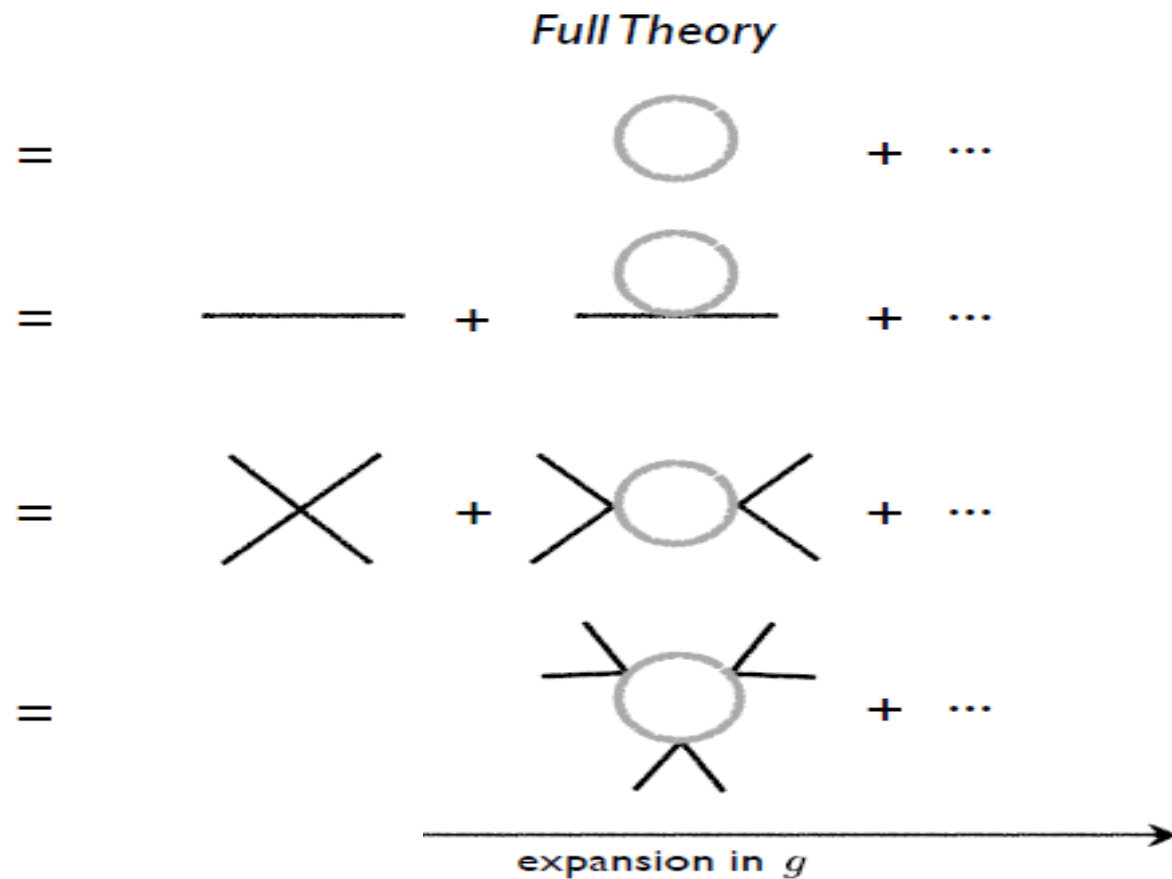
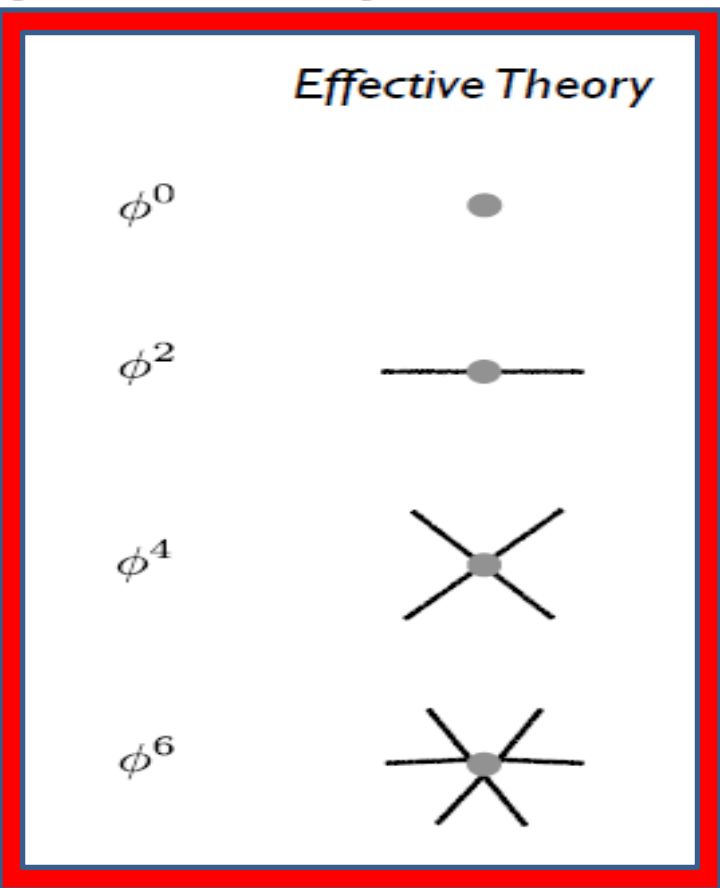
Heavy hidden sector

UV-coupling

Constructing EFTs from the Top Down

matching

EFT Redux



$$\Delta m^2 = \text{loop diagram} = \frac{g}{32\pi^2} \left(\Lambda^2 - M^2 \log \left(\frac{\Lambda^2}{\mu^2} \right) \right)$$

$$\Delta \lambda = \text{loop diagram} = -\frac{3g^2}{32\pi^2} \log \left(\frac{\Lambda^2}{\mu^2} \right)$$

↑ renormalization scale

Renormalization of IR couplings

$$\mathcal{L}_{\text{eff}}[\phi] = -\frac{1}{2}(\partial\phi)^2 - \frac{1}{2}m_{\text{R}}^2\phi^2 - \frac{1}{4!}\lambda_{\text{R}}\phi^4$$

renormalizable

$$- \sum_{i=1}^{\infty} \left(\frac{c_i}{M^{2i}}\phi^{4+2i} + \frac{d_i}{M^{2i}}(\partial\phi)^2\phi^{2i} + \dots \right)$$

non-renormalizable

expansion in $(E/M)^{2i}$

Only a finite number of operators are relevant to describe observations with finite precision.

EFT
Redux

renormalizable

Baumann & McAllister,
arXiv:1404.2601,1304.5226

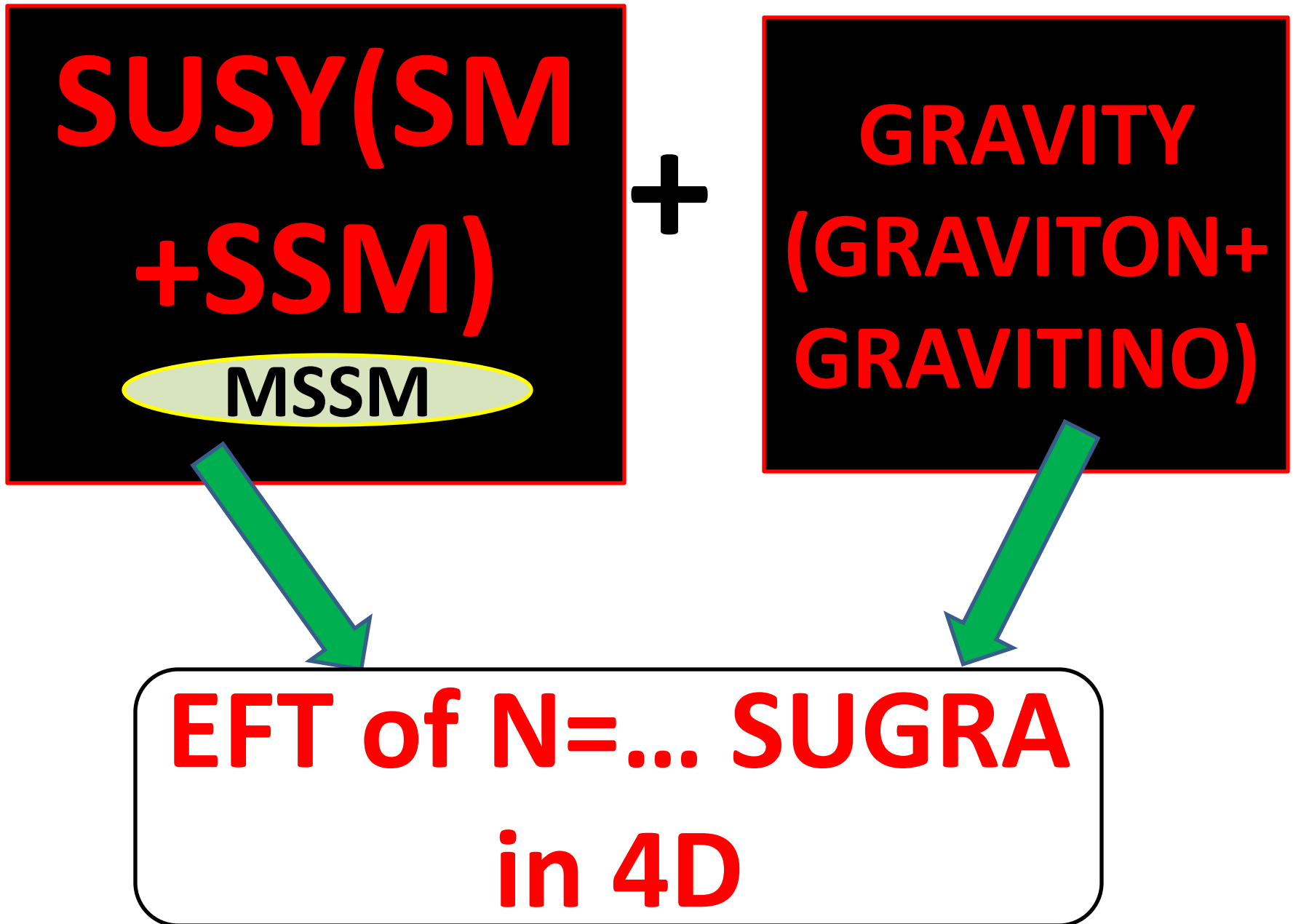
$$\mathcal{L}_{\text{eff}}[\phi] = \mathcal{L}_0[\phi] + \sum_i c_i \frac{\mathcal{O}_i[\phi]}{\Lambda^{\delta_i - 4}}$$

Wilson coefficient cutoff dimension

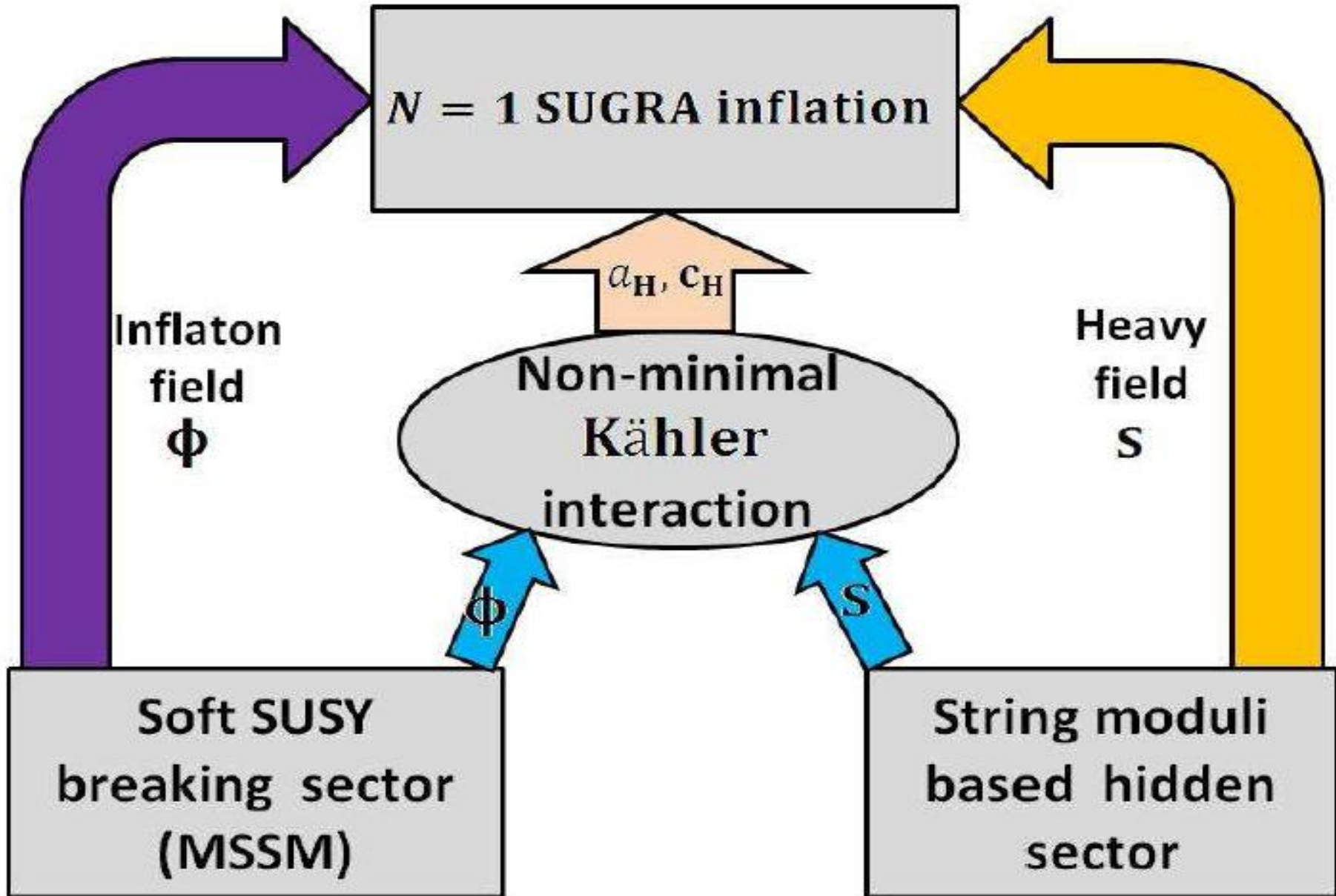
operator

Welcome to SUPER-WORLD

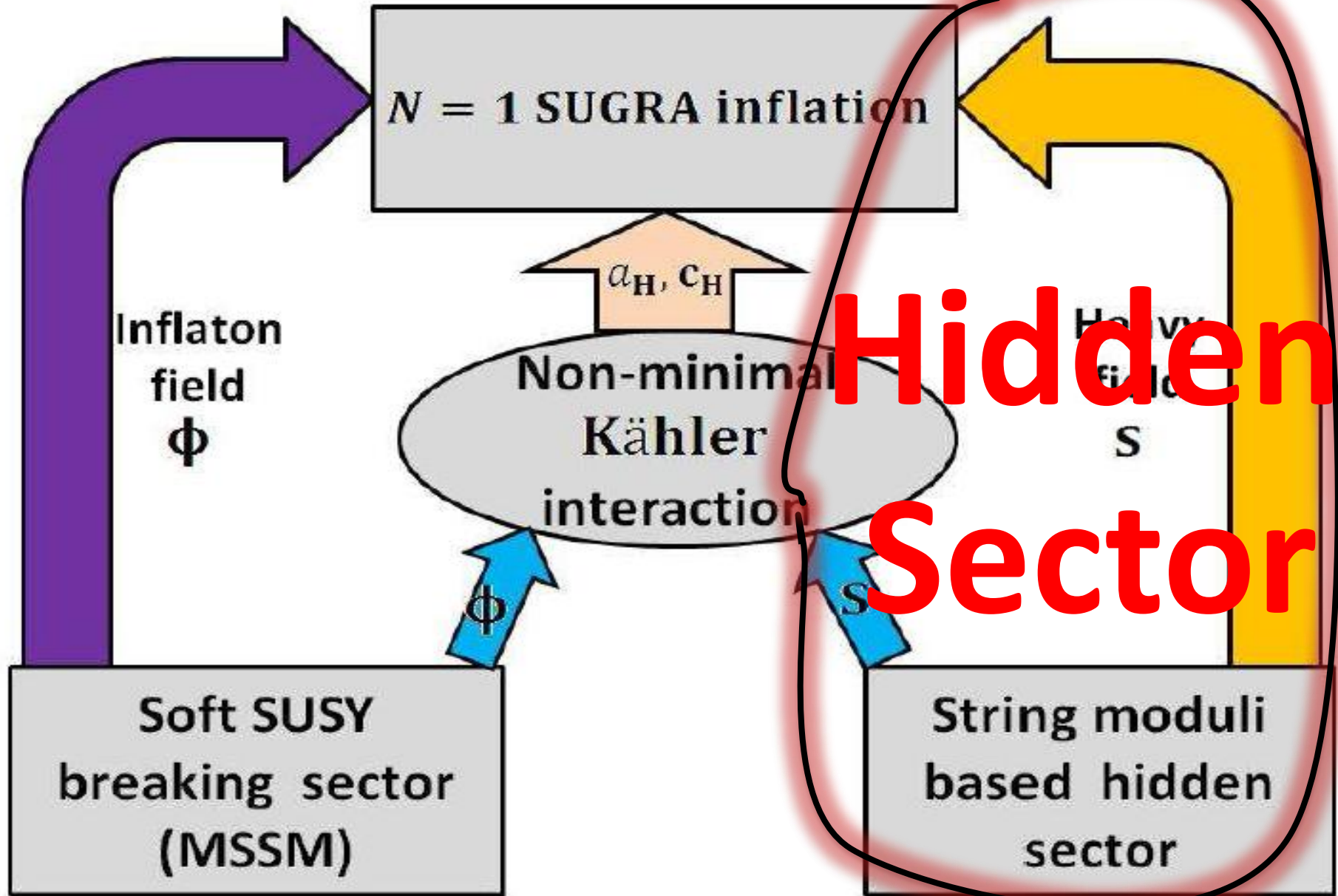




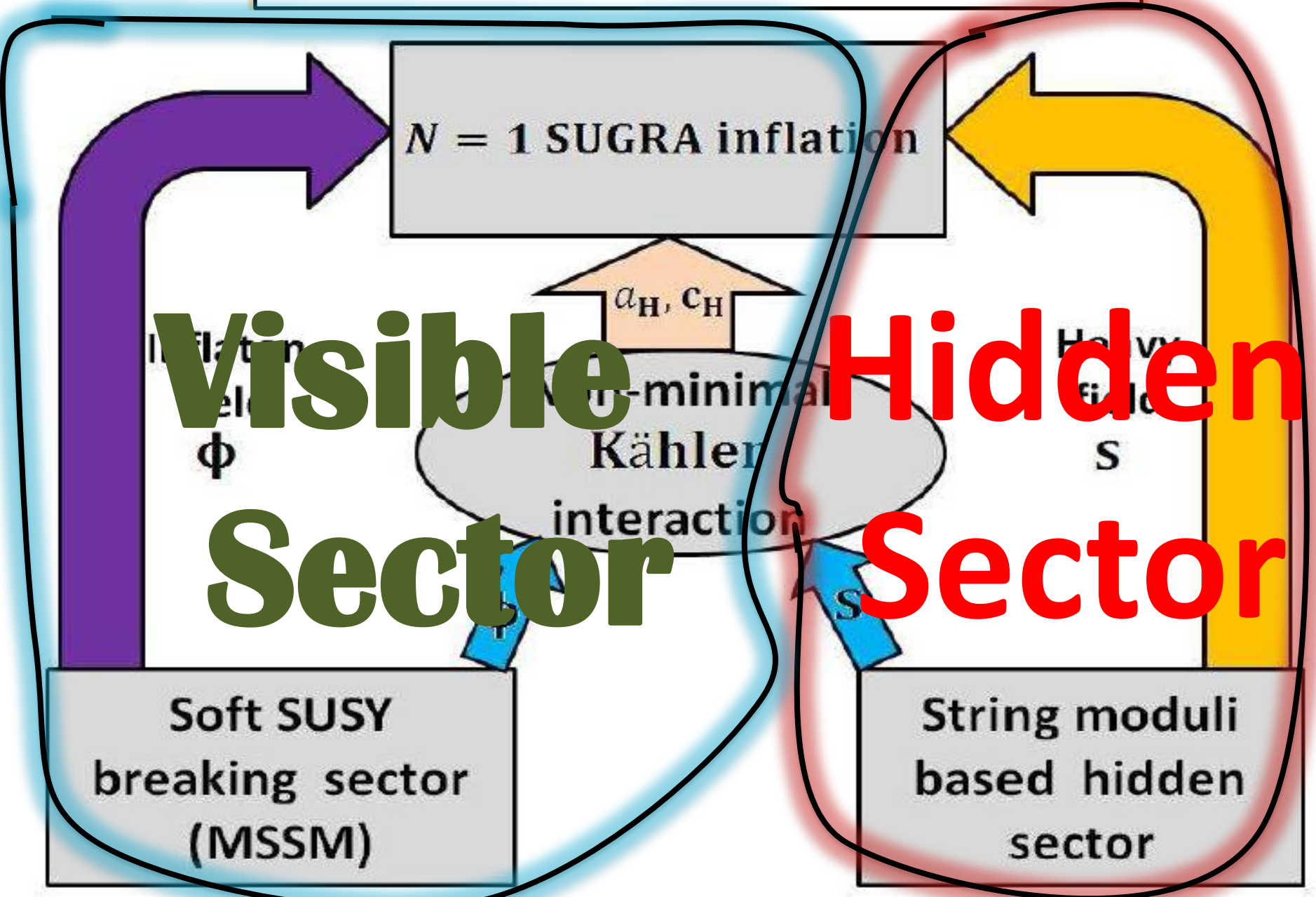
The EFT setup for N=1 SUGRA



The EFT setup for N=1 SUGRA



The EFT setup for N=1 SUGRA



The EFT setup for N=1 SUGRA

Visible Sector

Soft SUSY
breaking sector
(MSSM)

$N = 1$ SUGRA inflation

a_H, c_H

Kähler interaction

VEV from
hidden sector
heavy field
 $\langle \mathcal{S} \rangle = M_s < M_p$
 $\langle V(\mathcal{S}) \rangle = V_0$

The EFT setup for N=1 SUGRA

*Theory from
visible sector
in N=1 SUGRA:*

$$V_{vis} = V_m + V_H$$

MSSM flat

Direction contents

*(udd, lLe, NH_u L
.....)*

*VEV from
hidden sector
heavy field*

$$\langle S \rangle = M_s < M_p$$

$$\langle V(S) \rangle = V_0$$

The EFT setup for N=1 SUGRA

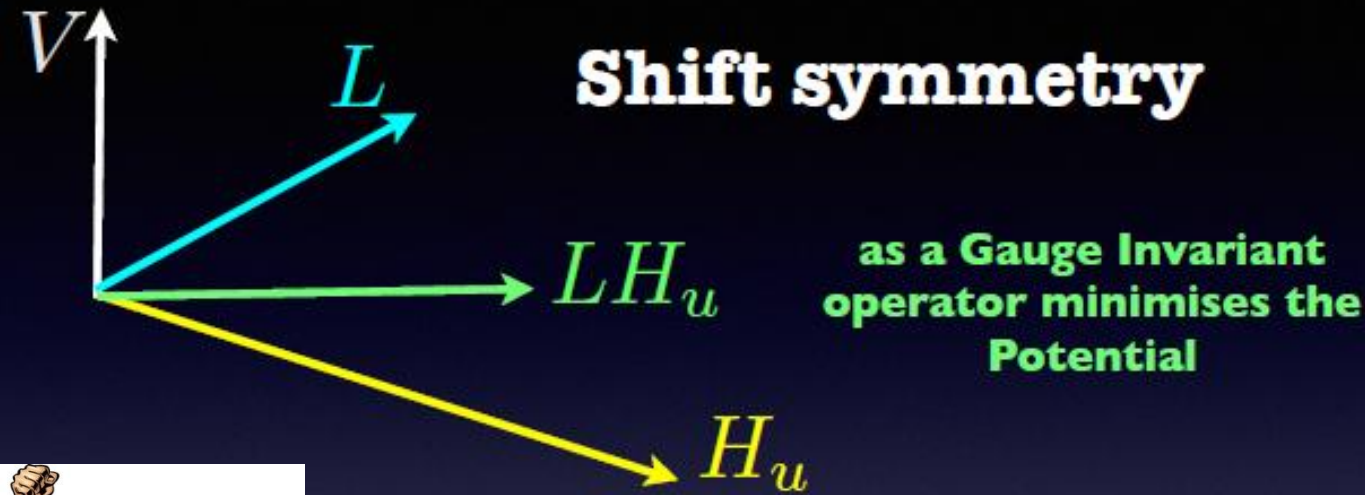
*Theory from
visible sector*

Effective Theory of N=1 SUGRA

$$V_{\text{EFT}} = V_{\text{vis}} + V_{\text{0}} = V_m + V_H + V_{\text{0}}$$

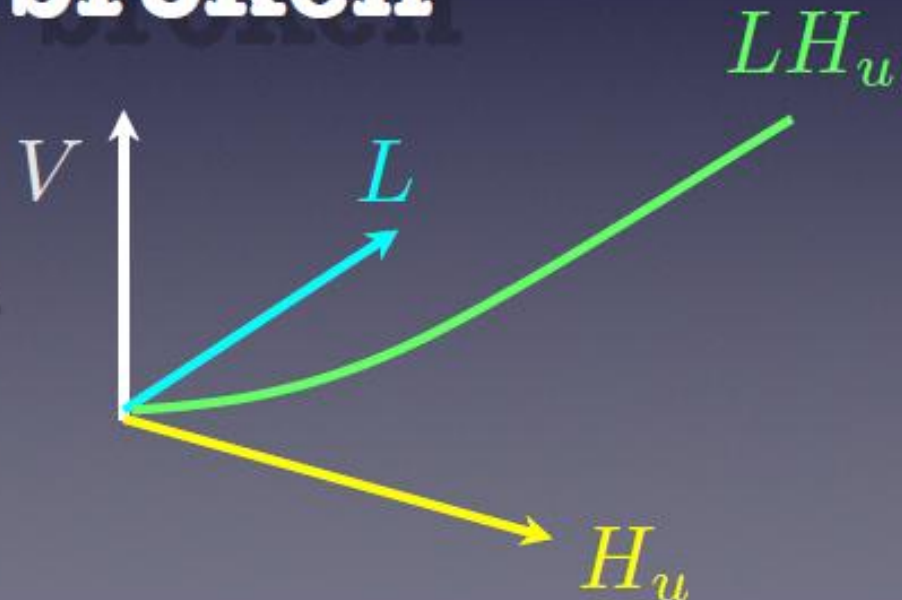
$$V(\phi) = V(s) + (m_\phi^2 + c_H H(t)^2) |\phi|^2 + \left(A \frac{\lambda \phi^n}{n M_p^{n-3}} + a_H H(t) \frac{\lambda \phi^n}{n M_p^{n-3}} + h.c. \right) + \lambda^2 \frac{|\phi|^{2(n-1)}}{M_p^{2(n-3)}}$$

SUSY Flat directions



SUSY is broken

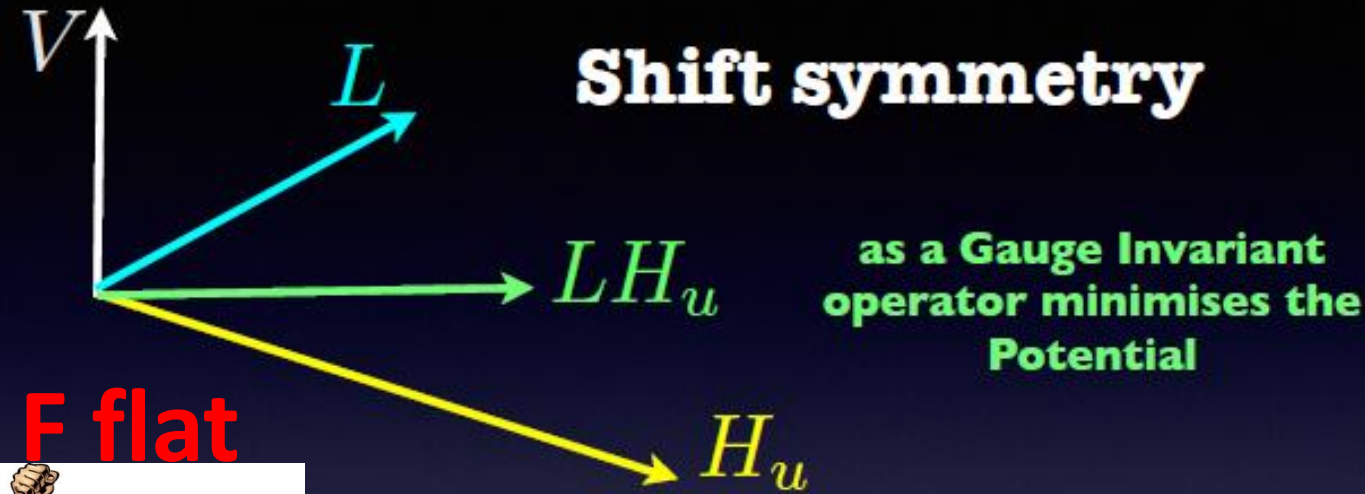
Shift symmetry is broken



SUSY Flat directions



D flat

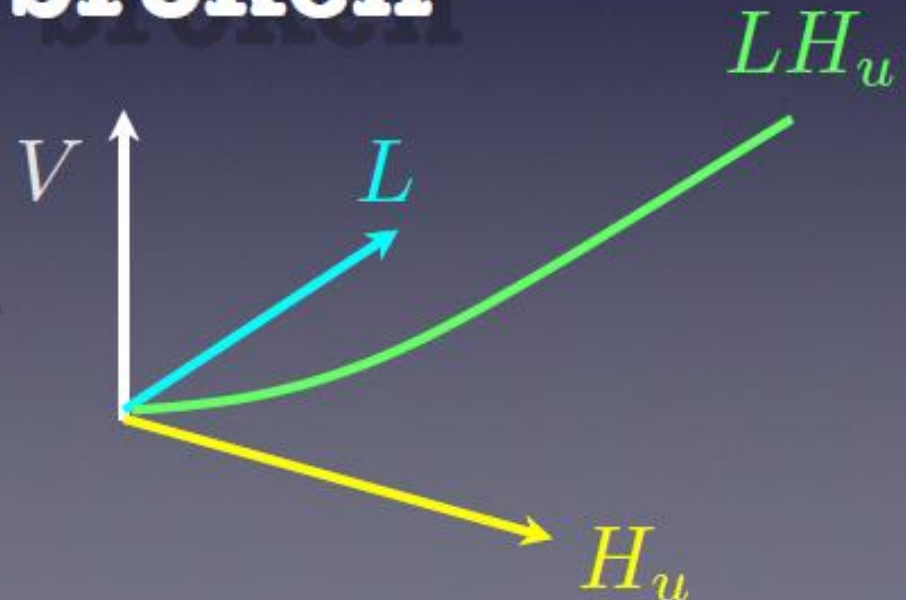


F flat



SUSY is broken

Shift symmetry is broken



Flat directions in the scalar potential of the supersymmetric standard model

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¹*Randall Physics Laboratory, University of Michigan, Ann Arbor MI 48109*

²*School of Natural Sciences, Institute for Advanced Study, Princeton NJ 08540*

ABSTRACT: The scalar potential of the Minimal Supersymmetric Standard Model (MSSM) is nearly flat along many directions in field space. We provide a catalog of the flat directions of the renormalizable and supersymmetry-preserving part of the scalar potential of the MSSM, along with a correspondence between flat directions and gauge-invariant polynomials of chiral superfields. We then study how these flat directions are lifted by non-renormalizable terms in the superpotential, with special attention given to the subtleties associated with the family index structure. Several flat directions are lifted only by supersymmetry-breaking effects and by supersymmetric terms in the scalar potential of surprisingly high dimensionality.

**Tool for computing SUSY flat
directions**

Gauge invariant Inflatons

	B-L	Always lifted by W_{GUTS} ?
LH_u	-1	
$H_u H_d$	0	
udd	-1	
LLe	-1	
$Q_u L$	-1	
$Q_u H_u$	0	✓
$Q_d H_d$	0	✓
LH_{ge}	0	✓
$QQQL$	0	
$Q_u Q_d$	0	
$Q_u Le$	0	
uude	0	
$QQQH_d$	1	✓
$Q_u H_{ge}$	1	✓
dddLL	-3	
uuuee	1	
$Q_u Q_u e$	1	
$QQQQ_u$	1	
dddLH_d	-2	✓
uudQ_d H_u	-1	✓
$(QQQ)_4 LLH_u$	-1	✓
$(QQQ)_4 LH_u H_d$	0	✓
$(QQQ)_4 H_u H_d H_d$	1	✓
$(QQQ)_4 LLe$	-1	
uudQ_d Q_d	-1	
$(QQQ)_4 LLH_{de}$	0	✓
$(QQQ)_4 LH_d H_{de}$	1	✓
$(QQQ)_4 H_d H_d H_{de}$	2	✓

$$\underline{SU(3) \times SU(2)_l \times U(1)_Y}$$

$$\underline{u_1 d_2 d_3} \quad d_2^\beta = \frac{1}{\sqrt{3}} \phi \quad u_1^\alpha = \frac{1}{\sqrt{3}} \phi \quad d_3^\gamma = \frac{1}{\sqrt{3}} \phi$$

$$\underline{L_1 L_2 e_3} \quad L_1^a = \frac{1}{\sqrt{3}} \begin{pmatrix} 0 \\ \phi \end{pmatrix} \quad L_2^b = \frac{1}{\sqrt{3}} \begin{pmatrix} \phi \\ 0 \end{pmatrix} \quad e_3 = \frac{1}{\sqrt{3}} \phi$$

$$\underline{H_u H_d} \quad H_u = \frac{1}{\sqrt{2}} \begin{pmatrix} \phi \\ 0 \end{pmatrix} \quad H_d = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ \phi \end{pmatrix}$$

$$\underline{SU(3) \times SU(2)_l \times U(1)_Y \times U(1)_{B-L}}$$

$$\underline{N H_u L} \quad N = \frac{1}{\sqrt{3}} \phi \quad H_u = \frac{1}{\sqrt{3}} \begin{pmatrix} 0 \\ \phi \end{pmatrix} \quad L = \frac{1}{\sqrt{3}} \begin{pmatrix} \phi \\ 0 \end{pmatrix}$$

Gauge invariant Inflatons

	B-L	Always lifted by W_{GUT} ?
LL_u	-1	
$H_u H_d$	0	
udd	-1	
LL_e	-1	
$Q_u L$	-1	
$Q_u H_u$	0	✓
$Q_d H_d$	0	✓
$Q_u L$	0	✓
$Q_u L$	0	
$Q_u L_e$	0	
$uude$	0	
$QQQH_d$	1	✓
$Q_u H_d e$	1	✓
$dddL$	-2	
$uuee$	1	
$Q_u L$	1	
$QQQQ_u$	1	
$dddLH_d$	-2	✓
$uudQ_d H_u$	-1	✓
$(QQQ)_4 LLH_u$	-1	✓
$(QQQ)_4 LH_u H_d$	0	✓
$(QQQ)_4 H_u H_d H_d$	1	✓
$(QQQ)_4 LLL_e$	-1	
$uudQ_d Q_d$	-1	
$(QQQ)_4 LLH_d e$	0	✓
$(QQQ)_4 LH_d H_d e$	1	✓
$(QQQ)_4 H_d H_d H_d e$	2	✓

300 such combinations.....

$$SU(3) \times SU(2)_l \times U(1)_Y$$

$$u_1 d_2 d_3 \quad d_2^\beta = \frac{1}{\sqrt{3}} \phi \quad u_1^\alpha = \frac{1}{\sqrt{3}} \phi \quad d_3^\gamma = \frac{1}{\sqrt{3}} \phi$$

$$L_1 L_2 e_3 \quad L_1^a = \frac{1}{\sqrt{3}} \begin{pmatrix} 0 \\ \phi \end{pmatrix} \quad L_2^b = \frac{1}{\sqrt{3}} \begin{pmatrix} \phi \\ 0 \end{pmatrix} \quad e_3 = \frac{1}{\sqrt{3}} \phi$$

$$H_u H_d \quad H_u = \frac{1}{\sqrt{2}} \begin{pmatrix} \phi \\ 0 \end{pmatrix} \quad H_d = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ \phi \end{pmatrix}$$

$$SU(3) \times SU(2)_l \times U(1)_Y \times U(1)_{B-L}$$

$$NH_u L \quad N = \frac{1}{\sqrt{3}} \phi \quad H_u = \frac{1}{\sqrt{3}} \begin{pmatrix} 0 \\ \phi \end{pmatrix} \quad L = \frac{1}{\sqrt{3}} \begin{pmatrix} \phi \\ 0 \end{pmatrix}$$

Allahverdi, Engvist, Bellido, AM, (PRL, 2006), (JCAP, 2007), Allahverdi, Kusenko, AM, JCAP (2007), Allahverdi, Dutta, AM (PRL 2007), Chatterjee, AM, JCAP (2011)

Non-minimal interactions in N=1 SUGRA

NON-MINIMAL INTERACTIONS IN N=1 SUGRA

$$e^{K(\phi, \phi^\dagger)/M_p^2} V(s)$$

$$(D_S W(s)) K^{s\bar{s}} (D_{\bar{S}} W^*(s^\dagger))$$

$$W_\phi K^{\phi\bar{\phi}} K_{\bar{\phi}} \frac{W^*(s^\dagger)}{M_p^2} + h.c.$$

$$-\frac{3}{M_p^2} W^*(s^\dagger) W(\phi) + h.c.$$

$$K_\phi K^{\phi\bar{\phi}} K_{\bar{\phi}} \frac{|W(s)|^2}{M_p^4}$$

$$K_s \frac{W(\phi)}{M_p^2} K^{s\bar{s}} (D_{\bar{S}} W^*(s^\dagger)) + h.c.$$

$$K_\phi K^{\phi\bar{s}} D_{\bar{s}} W^*(s^\dagger) \frac{W(s)}{M_p^2} + h.c.$$

$$W_\phi K^{\phi\bar{s}} (D_{\bar{S}} W^*(s^\dagger)) + h.c.$$

Gauge invariant Inflatons

$$W = W(\Phi) + W(S), \quad \Phi = \text{Light}, \quad S = \text{Heavy}$$

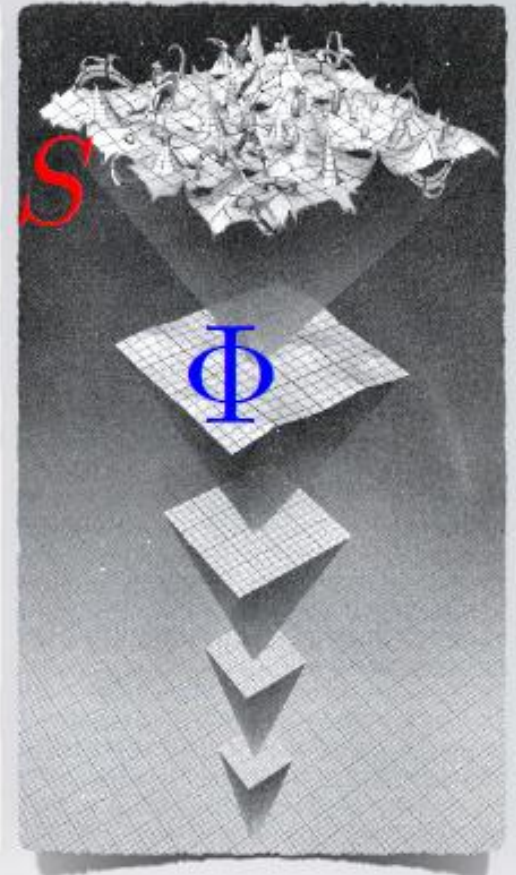
$$= \frac{\lambda \Phi^n}{n M_p^{n-3}} + \frac{M_s}{2} S^2, \quad \phi = \frac{\tilde{u} + \tilde{d} + \bar{\tilde{d}}}{\sqrt{3}}, \quad \phi = \frac{\tilde{L} + \bar{\tilde{L}} + \tilde{e}}{\sqrt{3}}$$

$$K = s^\dagger s + \phi^\dagger \phi + \delta K,$$

where *gauge invariant* Kähler corrections:

$$\delta K = f(\phi^\dagger \phi, s^\dagger s), \quad f(s^\dagger \phi \phi), \quad f(s^\dagger s^\dagger \phi \phi), \quad f(s \phi^\dagger \phi)$$

$$V = e^{K(\Phi^\dagger, \Phi)/M_p^2} \left[(D_{\Phi_i} W(\Phi)) K^{\Phi_i \bar{\Phi}_j} (D_{\bar{\Phi}_j} W^*(\Phi^\dagger)) - 3 \frac{|W(\Phi)|^2}{M_p^2} \right]$$



$$V_{total} = M_s^4 + c_H H^2 |\phi|^2 + \left(a_H H \frac{\lambda \phi^n}{n M_p^{n-3}} + h.c. \right) + \lambda^2 \frac{|\phi|^{2(n-1)}}{M_p^{2(n-3)}}$$

EFT potential structure (for MSSM) in N=1 SUGRA.

$$\mathcal{L}_{\text{Kin}} = \left(1 + \frac{a|s|^2}{M_p^2}\right) (\partial_\mu \phi) (\partial^\mu \phi^\dagger) + \frac{a}{M_p^2} \left\{ \phi^\dagger s (\partial_\mu \phi) (\partial^\mu s^\dagger) + \phi s^\dagger (\partial_\mu s) (\partial^\mu \phi^\dagger) \right\} + \left(1 + \frac{a|\phi|^2}{M_p^2}\right) (\partial_\mu s) (\partial^\mu s^\dagger)$$

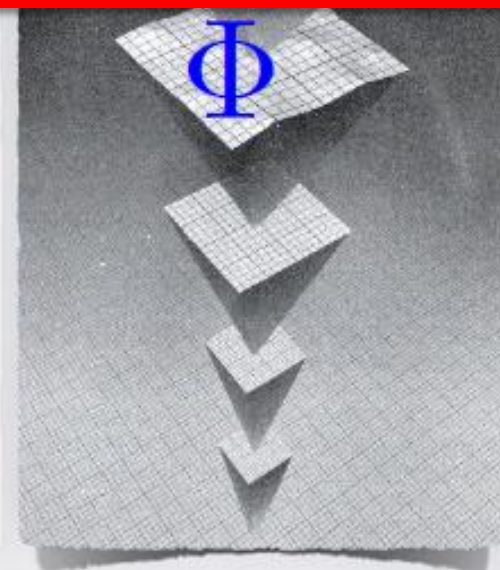
$$V(s) + \left(m_\phi^2 + 3(1-a)H^2\right) |\phi|^2 - \frac{A\phi^n}{nM_p^{n-3}} - \left(1 + a\frac{|s|^2}{M_p^2}\right) \left(1 - \frac{3}{n}\right) \frac{s^2}{M_p^2} \frac{\lambda M_s \phi^n}{M_p^{n-3}} - \left(1 - a\frac{|s|^2}{M_p^2}\right) \left(a - \frac{1}{n}\right) \frac{(s^\dagger)^2}{M_p^2} \frac{\lambda M_s \phi^n}{M_p^{n-3}} + \lambda^2 \frac{|\phi|^{2(n-1)}}{M_p^{2(n-3)}} + \text{h.c.}$$

$$K = s^\dagger s + \phi^\dagger \phi + \delta K,$$

where *gauge invariant* Kähler corrections:

$$\delta K = f(\phi^\dagger \phi, s^\dagger s), f(s^\dagger \phi \phi), f(s^\dagger s^\dagger \phi \phi), f(s \phi^\dagger \phi)$$

$$V = e^{K(\Phi_i^\dagger, \Phi_i)/M_p^2} \left[(D_{\Phi_i} W(\Phi)) K^{\Phi_i, \bar{\Phi}_j} (D_{\bar{\Phi}_j} W^*(\Phi^\dagger)) - 3 \frac{|W(\Phi)|^2}{M_p^2} \right],$$



$$V_{\text{total}} = M_s^4 + c_H H^2 |\phi|^2 + \left(a_H H \frac{\lambda \phi^n}{n M_p^{n-3}} + \text{h.c.} \right) + \lambda^2 \frac{|\phi|^{2(n-1)}}{M_p^{2(n-3)}}$$

EFT potential structure (for MSSM) in N=1 SUGRA.

$$\begin{aligned} \mathcal{L}_{\text{Kin}} = & (\partial_\mu \phi)(\partial^\mu \phi^\dagger) + (\partial_\mu s)(\partial^\mu s^\dagger) \\ & + \frac{b\phi}{2M_p} (\partial_\mu \phi)(\partial^\mu s^\dagger) \\ & + \frac{b\phi^\dagger}{2M_p} (\partial_\mu s)(\partial^\mu \phi^\dagger) \end{aligned}$$

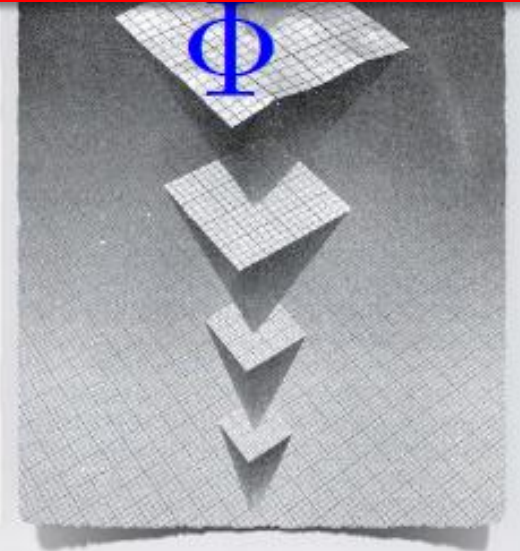
$$\begin{aligned} V(s) + & \left(m_\phi^2 + 3(1+b^2)H^2 \right) |\phi|^2 - A \frac{\phi^n}{nM_p^{n-3}} \\ & - \left\{ \left(1 - \frac{3}{n} \right) \phi + \frac{b\phi^\dagger s}{nM_p} \right\} \frac{\lambda \phi^{n-1} M_s s^2}{M_p^{n-1}} \\ & - \left(\frac{s^\dagger \phi}{M_p} - bn\phi^\dagger \right) \frac{2M_s \lambda \phi^{n-1} s^\dagger}{nM_p^{n-2}} \\ & - \frac{bM_s s^2}{2M_p^2} \left(\frac{2M_s s}{M_p} - \frac{M_s s^2 s^\dagger}{M_p^3} \right) \phi \phi \\ & - \frac{4M_s^2 b |s|^2 s^\dagger}{M_p^3} \phi \phi + \lambda^2 \frac{|\phi|^{2(n-1)}}{M_p^{2(n-3)}} + \text{h.c.} \end{aligned}$$

$$K = s^\dagger s + \phi^\dagger \phi + \delta K,$$

where *gauge invariant* Kähler corrections

$$\delta K = f(\phi^\dagger \phi, s^\dagger s), f(s^\dagger \phi \phi), f(s^\dagger s^\dagger \phi \phi), f(s \phi^\dagger \phi)$$

$$V = e^{K(\Phi_i^\dagger, \Phi_i)/M_p^2} \left[(D_{\Phi_i} W(\Phi)) K^{\Phi_i \bar{\Phi}_j} (D_{\bar{\Phi}_j} W^*(\Phi^\dagger)) - 3 \frac{|W(\Phi)|^2}{M_p^2} \right],$$



$$V_{\text{total}} = M_s^4 + c_H H^2 |\phi|^2 + \left(a_H H \frac{\lambda \phi^n}{nM_p^{n-3}} + \text{h.c.} \right) + \lambda^2 \frac{|\phi|^{2(n-1)}}{M_p^{2(n-3)}}$$

EFT potential structure (for MSSM) in N=1 SUGRA.

$$\mathcal{L}_{\text{Kin}} = (\partial_\mu \phi) (\partial^\mu \phi^\dagger) + (\partial_\mu s) (\partial^\mu s^\dagger) + \frac{cs^\dagger \phi}{4M_p^2} (\partial_\mu \phi) (\partial^\mu s^\dagger) + \frac{cs\phi^\dagger}{4M_p^2} (\partial_\mu s) (\partial^\mu \phi^\dagger)$$

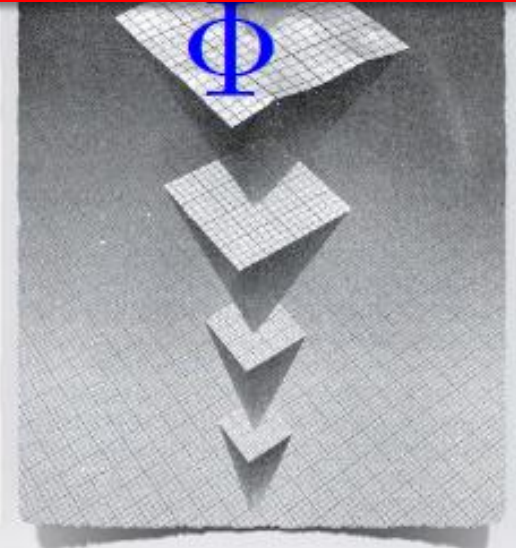
$$V(s) + \left(m_\phi^2 + 3H^2\right) |\phi|^2 - A \frac{\phi^n}{nM_p^{n-3}} - \left\{ \left(1 - \frac{3}{n}\right) \phi + \frac{c\phi^\dagger s s}{2M_p^2} \right\} \frac{\lambda \phi^{n-1} M_s s^2}{M_p^{n-1}} + \frac{cM_s^2 s^2 s^\dagger s \phi \phi}{M_p^4} - \frac{M_s^2 c |s|^2 s^\dagger s^\dagger}{M_p^4} \phi \phi + \lambda^2 \frac{|\phi|^{2(n-1)}}{M_p^{2(n-3)}} - \left(\frac{s^\dagger \phi}{M_p} - \frac{cn\phi^\dagger s}{M_p} \right) \frac{2M_s \lambda \phi^{n-1} s^\dagger}{nM_p^{n-2}} + \text{h.c.}$$

$$K = s^\dagger s + \phi^\dagger \phi + \delta K,$$

where *gauge invariant* Kähler corrections:

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$$V_{\text{total}} = M_s^4 + c_H H^2 |\phi|^2 + \left(a_H H \frac{\lambda \phi^n}{nM_p^{n-3}} + \text{h.c.} \right) + \lambda^2 \frac{|\phi|^{2(n-1)}}{M_p^{2(n-3)}}$$

EFT potential structure (for MSSM) in N=1 SUGRA.

$$\mathcal{L}_{\text{Kin}} = \left(\frac{ds}{M_p} + \frac{ds^\dagger}{M_p} + 1 \right) (\partial_\mu \phi) (\partial^\mu \phi^\dagger) + (\partial_\mu s) (\partial^\mu s^\dagger) + \frac{d\phi^\dagger}{M_p} (\partial_\mu \phi) (\partial^\mu s^\dagger) + \frac{d\phi}{M_p} (\partial_\mu s) (\partial^\mu \phi^\dagger)$$

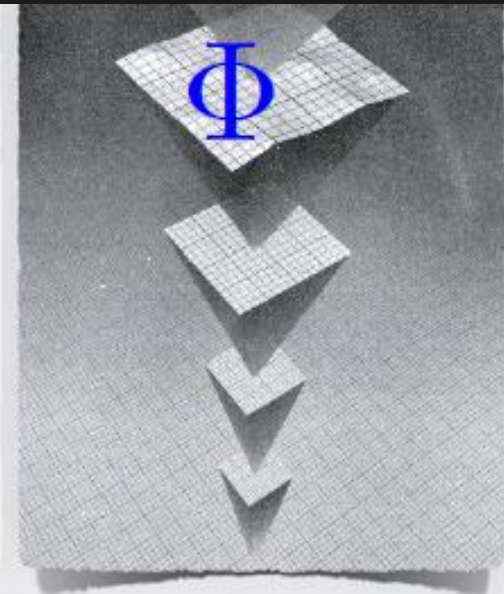
$$V(s) + \left(m_\phi^2 + 3(1+d^2)H^2 \right) |\phi|^2 - A \frac{\phi^n}{nM_p^{n-3}} - \left(1 - \frac{3}{n} \right) \frac{\lambda \phi^n M_s s^2}{M_p^{n-1}} - \left(\frac{s^\dagger}{M_p} - d \right) \frac{2M_s \lambda \phi^n s^\dagger}{nM_p^{n-2}} + \lambda^2 \frac{|\phi|^{2(n-1)}}{M_p^{2(n-3)}} + \text{h.c.}$$

$$K = s^\dagger s + \phi^\dagger \phi + \delta K,$$

where *gauge invariant* Kähler corrections:

$$\delta K = f(\phi^\dagger \phi, s^\dagger s), f(s^\dagger \phi \phi), f(s^\dagger s^\dagger \phi \phi), f(s \phi^\dagger \phi)$$

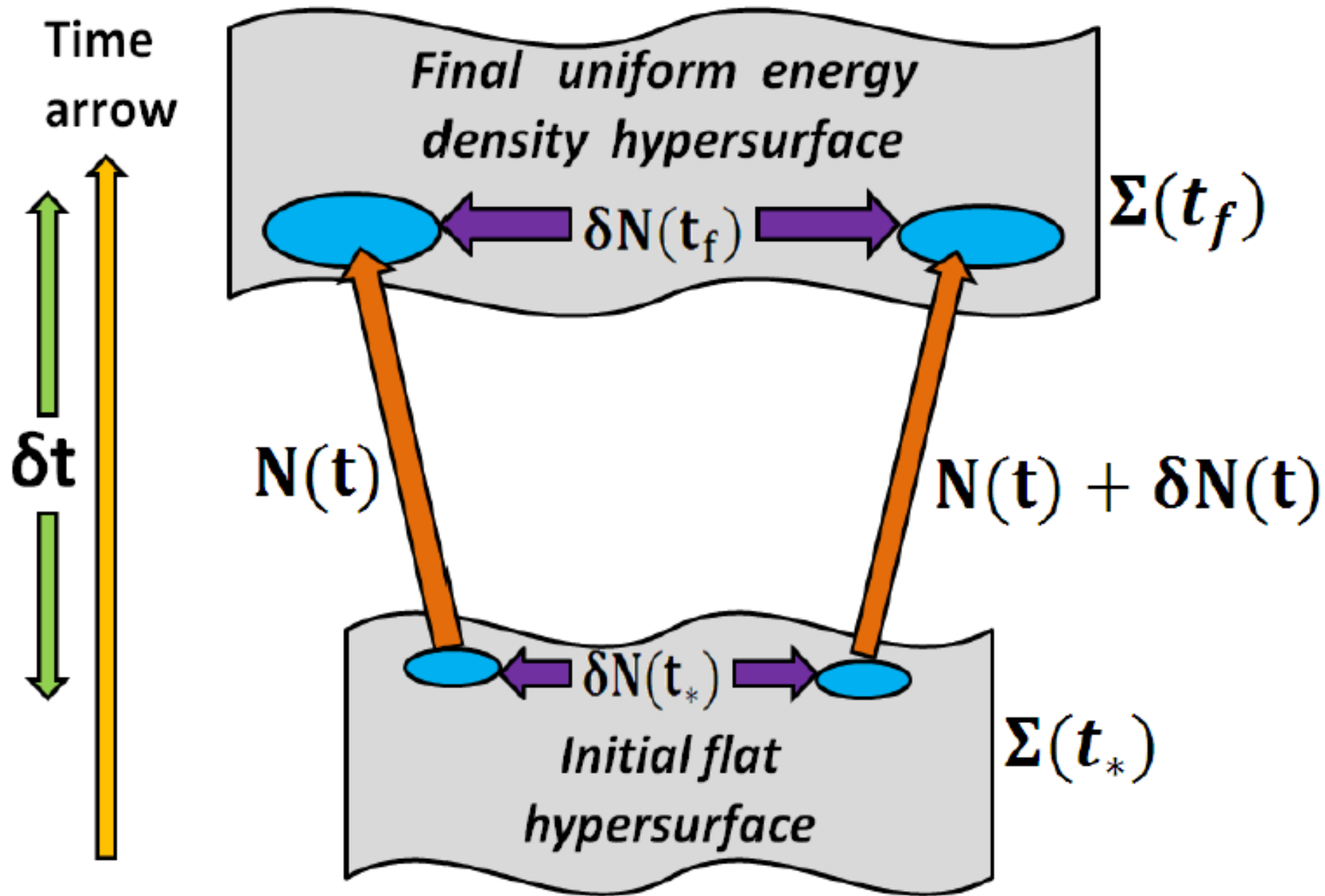
$$V = e^{K(\Phi_i^\dagger, \Phi_i)/M_p^2} \left[(D_{\Phi_i} W(\Phi)) K^{\Phi_i, \bar{\Phi}_j} (D_{\bar{\Phi}_j} W^*(\Phi^\dagger)) - 3 \frac{|W(\Phi)|^2}{M_p^2} \right]$$



$$V_{\text{total}} = M_s^4 + c_H H^2 |\phi|^2 + \left(a_H H \frac{\lambda \phi^n}{nM_p^{n-3}} + \text{h.c.} \right) + \lambda^2 \frac{|\phi|^{2(n-1)}}{M_p^{2(n-3)}}$$

EFT potential structure (for MSSM) in N=1 SUGRA.

Primordial non-Gaussianity using δN formalism



Primordial non-Gaussianity using δN formalism

Time
axis

δN?

- ➔ δN is a well accepted tool for computing PNG in classical regime via non linear evolution of cosmological perturbations on large scales.
- ➔ Provides fruitful technique to compute the expression for curvature perturbation without explicitly solving the perturbed field equations.
- ➔ Independent of any intrinsic NG generated at the scale of horizon crossing.



Primordial non-Gaussianity using δN formalism

$$\zeta = \delta N = N_{,\phi}\delta\phi + \frac{1}{2}N_{,\phi\phi}\delta\phi^2 + \frac{1}{6}N_{,\phi\phi\phi}\delta\phi^3 + \dots$$

3 point correlation

$$\langle \zeta_{k_1} \zeta_{k_2} \zeta_{k_3} \rangle = (2\pi)^7 \delta^3(\mathbf{k}_1 + \mathbf{k}_2 + \mathbf{k}_3) \left[\frac{3f_{NL}^{\text{local}}}{10k_1^3 k_2^3} P_s(k_1) P_s(k_2) + (k_2 \leftrightarrow k_3) + (k_1 \leftrightarrow k_3) \right]$$

4 point correlation

$$\langle \zeta_{k_1} \zeta_{k_2} \zeta_{k_3} \zeta_{k_4} \rangle = (2\pi)^9 \delta^4(\mathbf{k}_1 + \mathbf{k}_2 + \mathbf{k}_3 + \mathbf{k}_4) \left[\frac{27g_{NL}^{\text{local}}}{100} \sum_{i < j < p=1}^3 \frac{P_s(k_i) P_s(k_j) P_s(k_p)}{(k_i k_j k_p)^3} + \frac{\tau_{NL}^{\text{local}}}{8} \sum_{j < p, i \neq j, p=1}^{11} \frac{P_s(k_{ij}) P_s(k_j) P_s(k_p)}{(k_{ij} k_j k_p)^3} \right]$$

Primordial non-Gaussianity using δN formalism

$$f_{NL}^{\text{local}} = \frac{5}{6} \frac{N_{,\phi\phi}}{N_{,\phi}^2} + \dots = \frac{5\vartheta}{6} + \dots$$

$$\tau_{NL}^{\text{local}} = \frac{N_{,\phi\phi}^2}{N_{,\phi}^4} + \dots = \vartheta^2 + \dots$$

$$g_{NL}^{\text{local}} = \frac{25}{54} \frac{N_{,\phi\phi\phi}}{N_{,\phi}^3} + \dots = \frac{25\vartheta^2}{108} + \dots$$

misprint on LHS

$$\vartheta \approx \left[\eta_V \left(1 + \frac{1}{c_s^2} \right)^2 + \epsilon_V \left(1 - \frac{1}{c_s^4} \right) \right]$$

$$\mathcal{P}_S = \frac{V_\star}{24\pi^2 M_p^4 c_s \epsilon_V}$$

$$\mathcal{P}_T = \frac{2V_\star}{3\pi^2 M_p^4} c_s^{\frac{2\epsilon_V}{1-\epsilon_V}}$$

$$n_S - 1 = 2\eta_V - 6\epsilon_V - s$$

$$n_T = -2\epsilon_V$$

$$r_\star = 16\epsilon_V c_s^{\frac{1+\epsilon_V}{1-\epsilon_V}} = -8n_T c_s^{\frac{1-\frac{n_T}{2}}{1+\frac{n_T}{2}}}$$

$$\epsilon_V = \frac{M_p^2}{2} \left(\frac{V'}{V} \right)^2, \quad \eta_V = M_p^2 \left(\frac{V''}{V} \right)$$

$$s = \frac{\dot{c}_s}{H c_s} = \sqrt{\frac{3}{V}} \frac{\dot{c}_s}{c_s} M_p$$

Scale of visible sector (inflation) and hidden sector

$$H \leq 9.241 \times 10^{13} \times \sqrt{\frac{r_*}{0.12}} c_s^{\frac{\epsilon_V}{\epsilon_V - 1}} \text{ GeV},$$

$$\sqrt[4]{V_*} \leq 1.96 \times 10^{16} \times \sqrt[4]{\frac{r_*}{0.12}} c_s^{\frac{\epsilon_V}{2(\epsilon_V - 1)}} \text{ GeV},$$

$$M_s \leq 1.77 \times 10^{16} \times \sqrt[4]{\frac{r_*}{0.12}} c_s^{\frac{\epsilon_V}{2(\epsilon_V - 1)}} \text{ GeV}.$$

Field excursion in MSSM within N=1 SUGRA

$$\frac{|\Delta\phi|}{M_p} \approx \frac{3}{25\sqrt{c_s}} \sqrt{\frac{r_*}{0.12}} \left| \left\{ \frac{3}{400} \left(\frac{r_*}{0.12} \right) - \frac{\eta_V(k_*)}{2} - \frac{1}{2} \right\} \right|$$

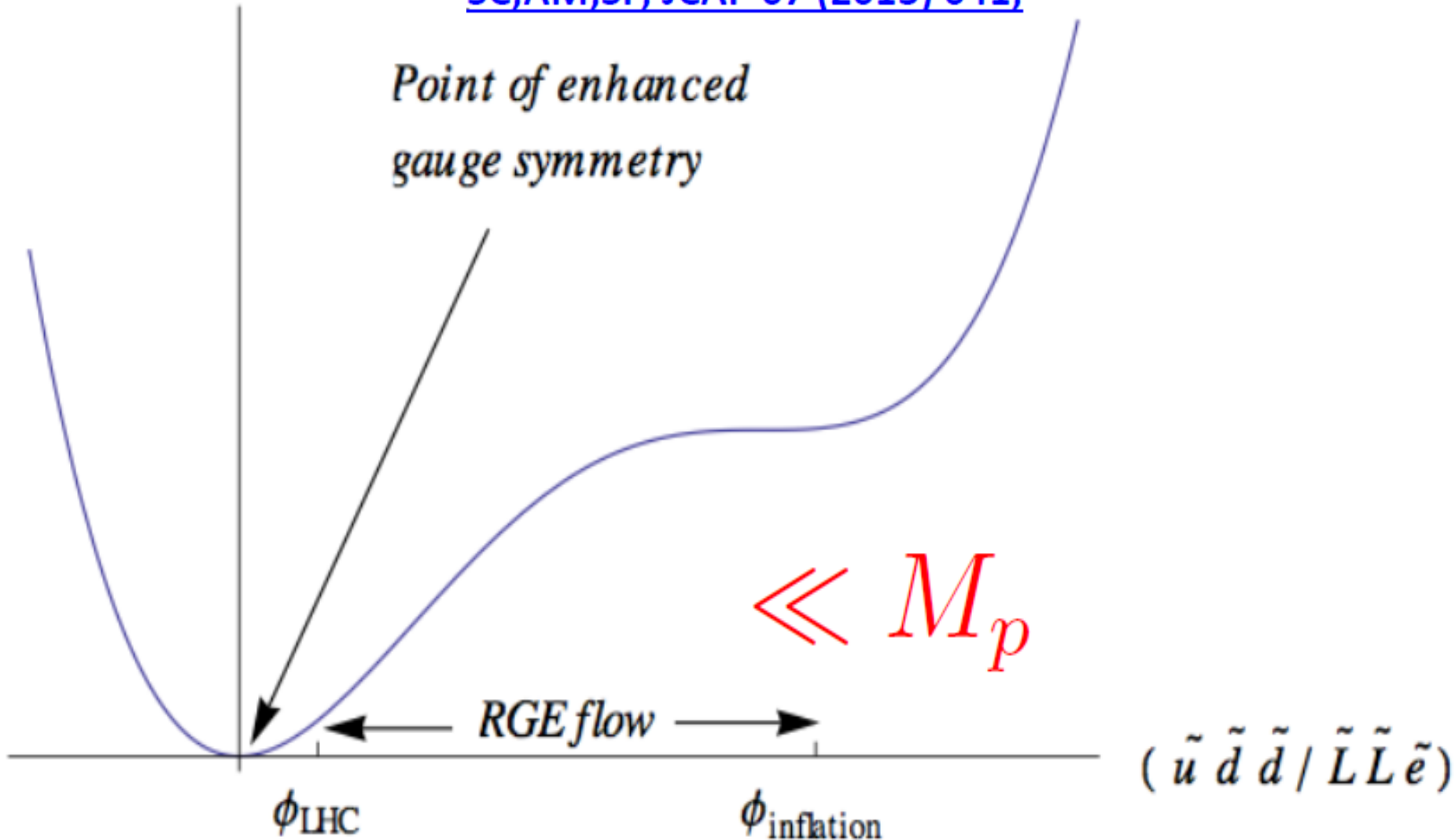
Reheating temperature

$$T_{rh} = \left(\frac{30}{\pi^2 g_*} \right)^{\frac{1}{4}} \sqrt[4]{V_*} \leq 6.654 \times 10^{15} \sqrt[4]{\frac{r_*}{0.12}} c_s^{\frac{\epsilon_V}{2(\epsilon_V - 1)}} \text{ GeV}$$

Model (MSSM) constraints

$V(\tilde{u}, \tilde{d}, \tilde{L}, \tilde{e})$ [SC, JHEP 04 \(2014\) 105,](#)
[SC, AM, EP, JHEP 04 \(2014\) 077,](#)
[SC, AM, SP, JCAP 07 \(2013\) 041,](#)

*Point of enhanced
gauge symmetry*



Model (MSSM) constraints

$$V(\phi) = \alpha + \beta(\phi - \phi_0) + \gamma(\phi - \phi_0)^3 + \kappa(\phi - \phi_0)^4 + \dots$$

Point of inflection

$$V''(\phi_0) = 0$$

$$\alpha = V(\phi_0) = V(s) + \left(\frac{(n-2)^2}{n(n-1)} + \frac{(n-2)^2}{n} \delta^2 \right) c_H H^2 \phi_0^2 + \mathcal{O}(\delta^4),$$

$$\beta = V'(\phi_0) = 2 \left(\frac{n-2}{2} \right)^2 \delta^2 c_H H^2 \phi_0 + \mathcal{O}(\delta^4),$$

$$\gamma = \frac{V'''(\phi_0)}{3!} = \frac{c_H H^2}{\phi_0} \left(4(n-2)^2 - \frac{(n-1)(n-2)^3}{2} \delta^2 \right) + \mathcal{O}(\delta^4),$$

$$\kappa = \frac{V''''(\phi_0)}{4!} = \frac{c_H H^2}{\phi_0^2} \left(12(n-2)^3 - \frac{(n-1)(n-2)(n-3)(7n^2 - 27n + 26)}{2} \delta^2 \right)$$

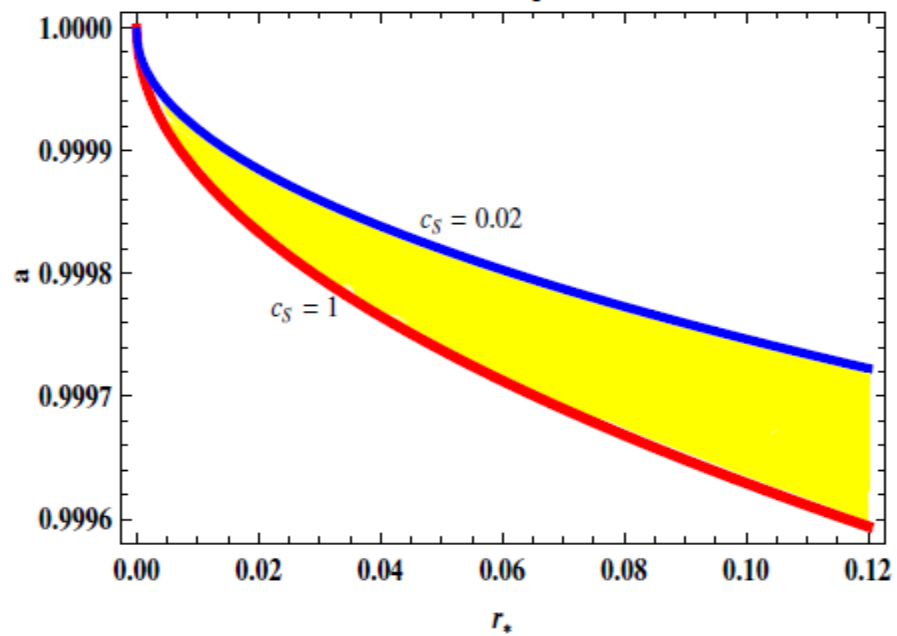
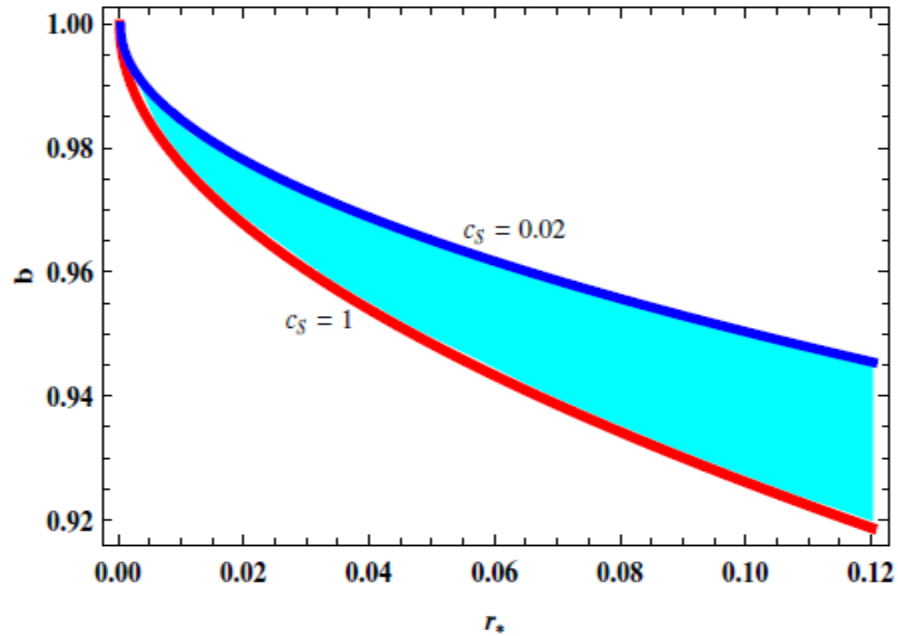
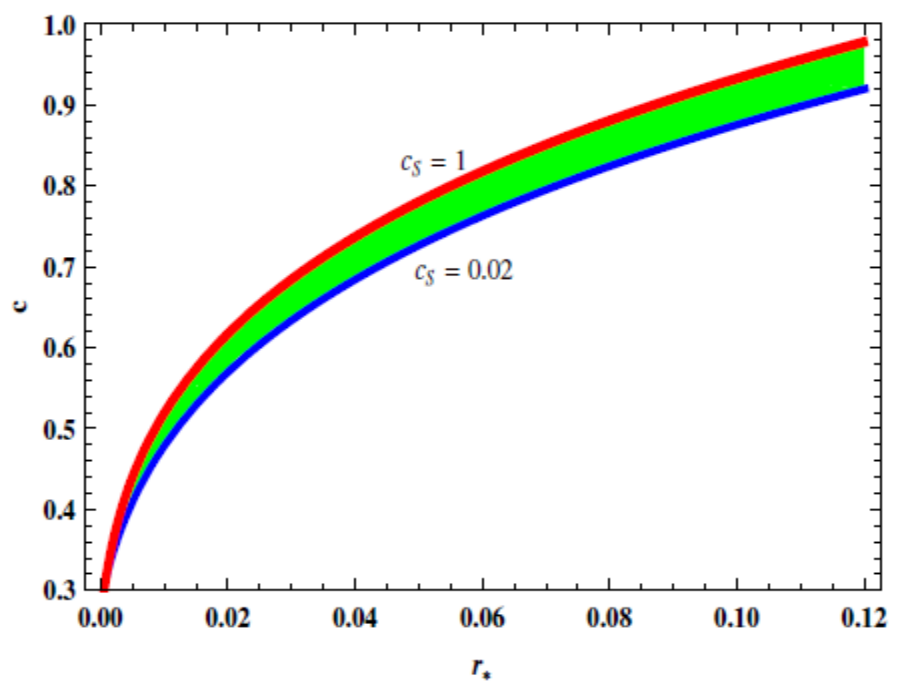
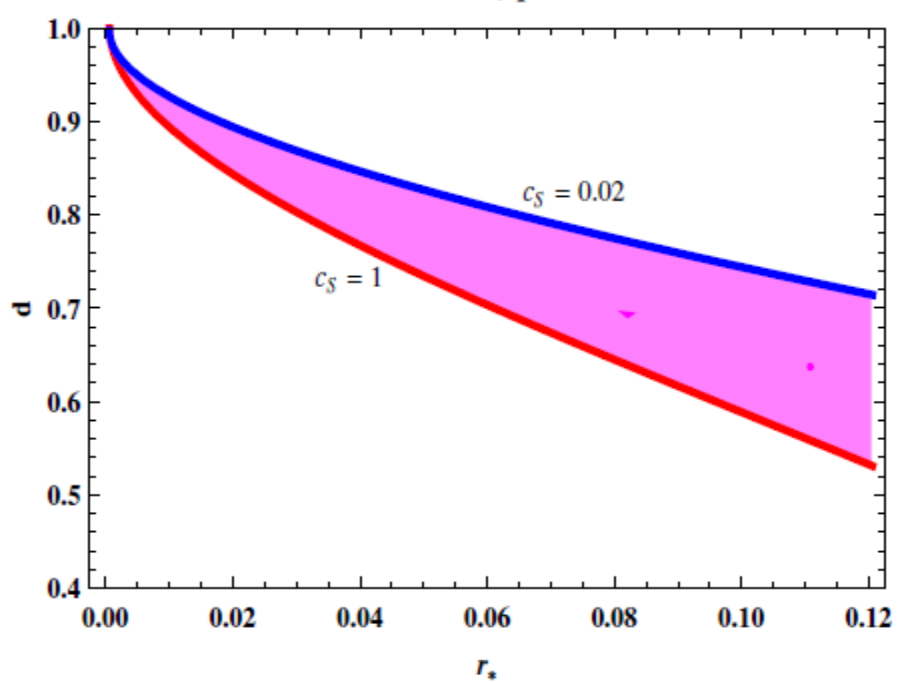
$$\frac{a_H^2}{8(n-1)c_H} = 1 - \left(\frac{n-2}{2} \right)^2 \delta^2 \quad \phi_0 = \left(\sqrt{\frac{c_H}{(n-1)}} H M_p^{n-3} \right)^{1/n-2} + \mathcal{O}(\delta^2)$$

Model (MSSM) constraints

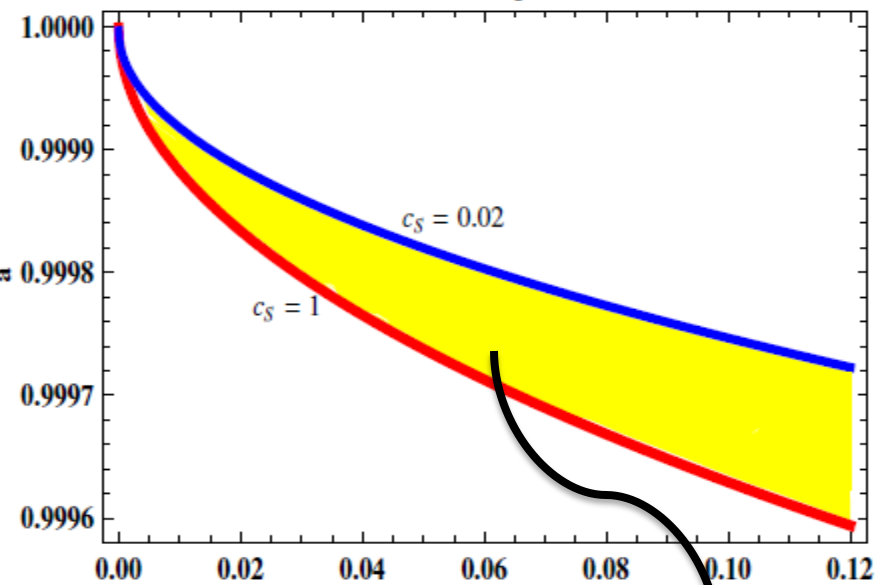
$$\left. \begin{aligned} c_H &\sim \mathcal{O}(10 - 10^{-6}) & a &\sim \mathcal{O}(1 - 0.99), \\ a_H &\sim \mathcal{O}(30 - 10^{-3}) & b &\sim \mathcal{O}(1 - 0.92), \\ \phi_0 &\sim \mathcal{O}(10^{14} - 10^{17}) \text{ GeV} & c &\sim \mathcal{O}(0.3 - 1), \\ M_s &\sim \mathcal{O}(9.50 \times 10^{10} - 1.77 \times 10^{16}) \text{ GeV} & d &\sim \mathcal{O}(1 - 0.5). \end{aligned} \right\} \begin{array}{l} \text{Model} \\ \text{(MSSM)} \\ \text{parameters} \end{array}$$

**Inflationary
Observables
from MSSM**

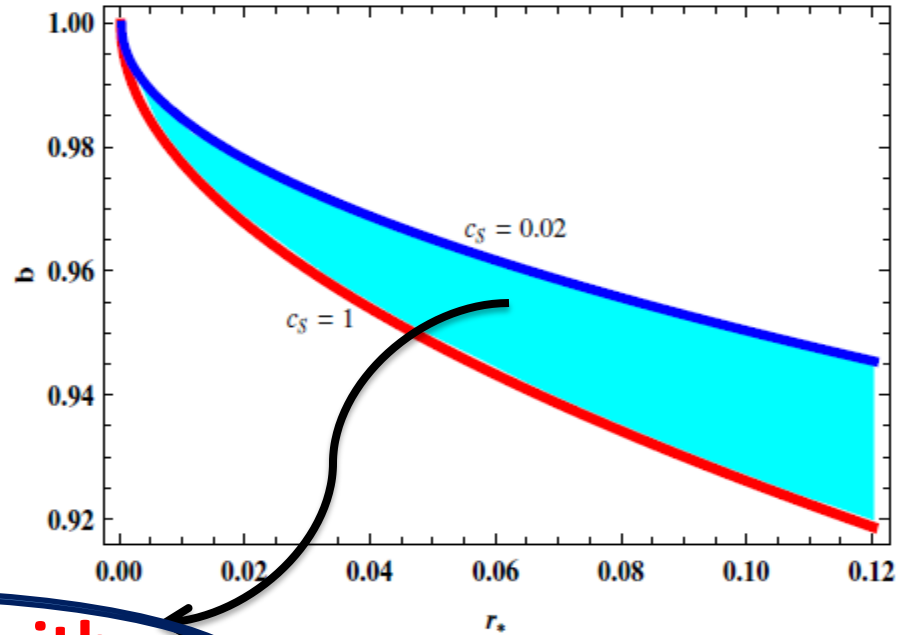
$$\left. \begin{aligned} 2.092 \times 10^{-9} &< P_S < 2.297 \times 10^{-9} \\ 0.02 &\leq c_s \leq 1 & 0.958 &< n_S < 0.963 \\ & & 10^{-22} &< r_* < 0.12 \\ & & \mathcal{O}(1 - 5) &\leq f_{NL} \leq 8.5 \\ & & \mathcal{O}(75 - 150) &\leq \tau_{NL} \leq 2800 \\ & & \mathcal{O}(17.4 - 34.7) &\leq g_{NL} \leq 648.2 \end{aligned} \right\}$$

a vs r_* plot**b vs r_* plot****c vs r_* plot****d vs r_* plot**

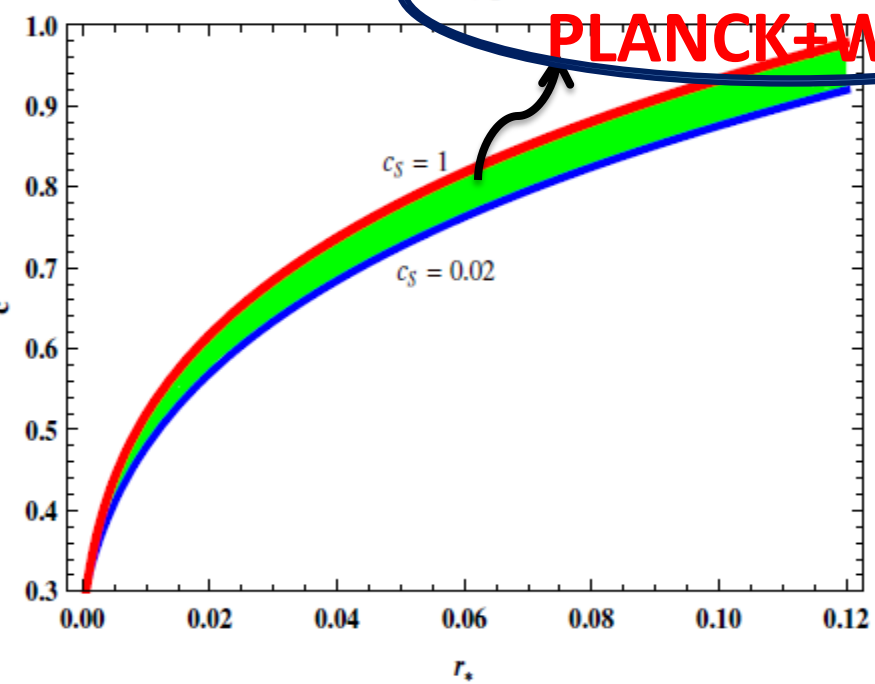
a vs r_* plot



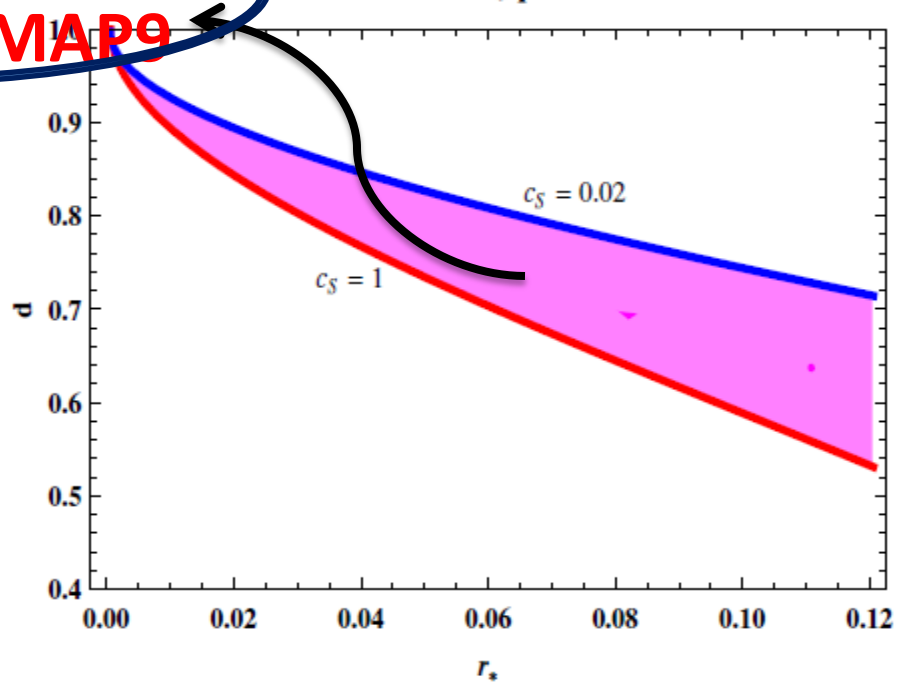
b vs r_* plot



c vs r_* plot

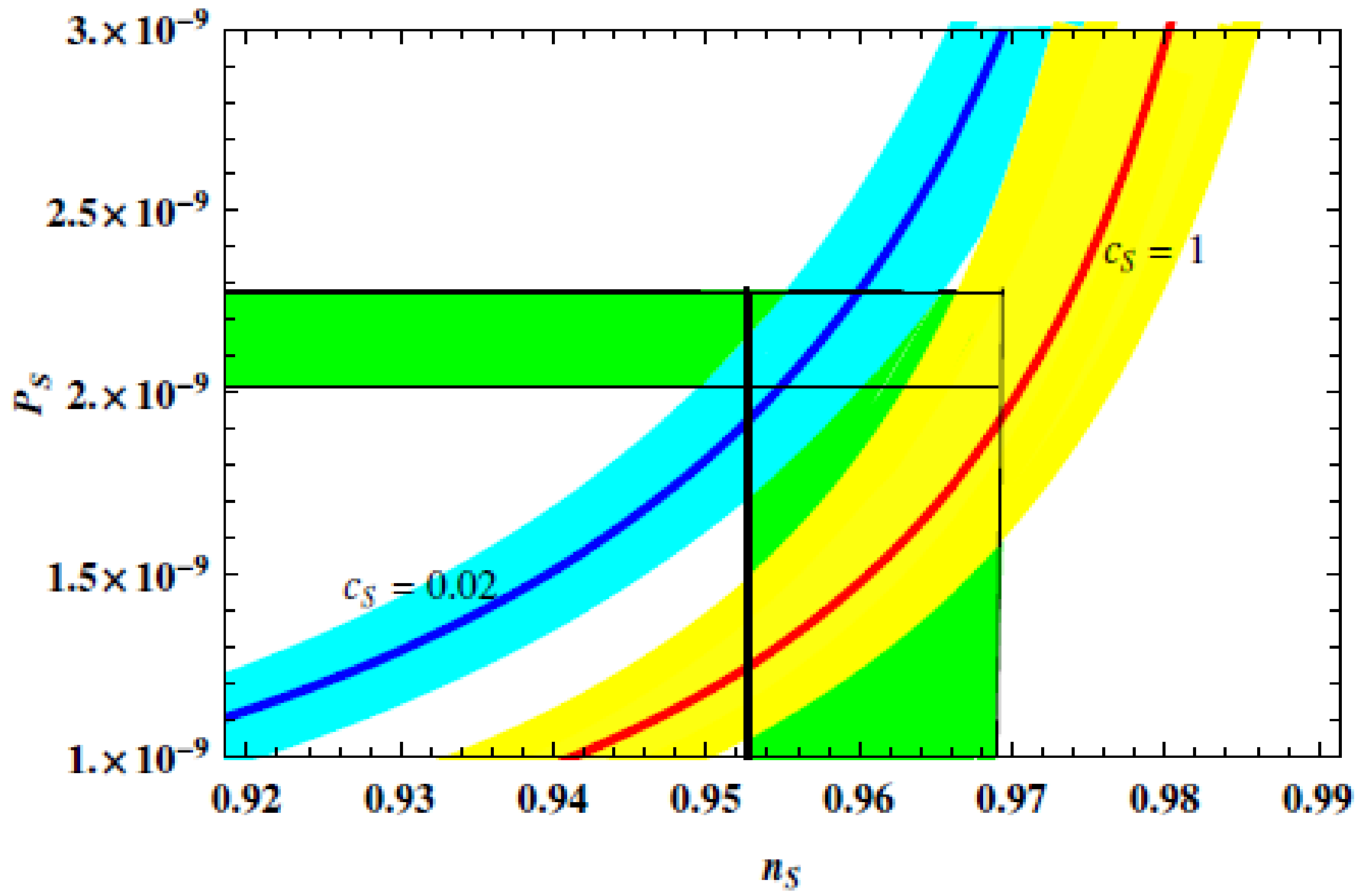


d vs r_* plot

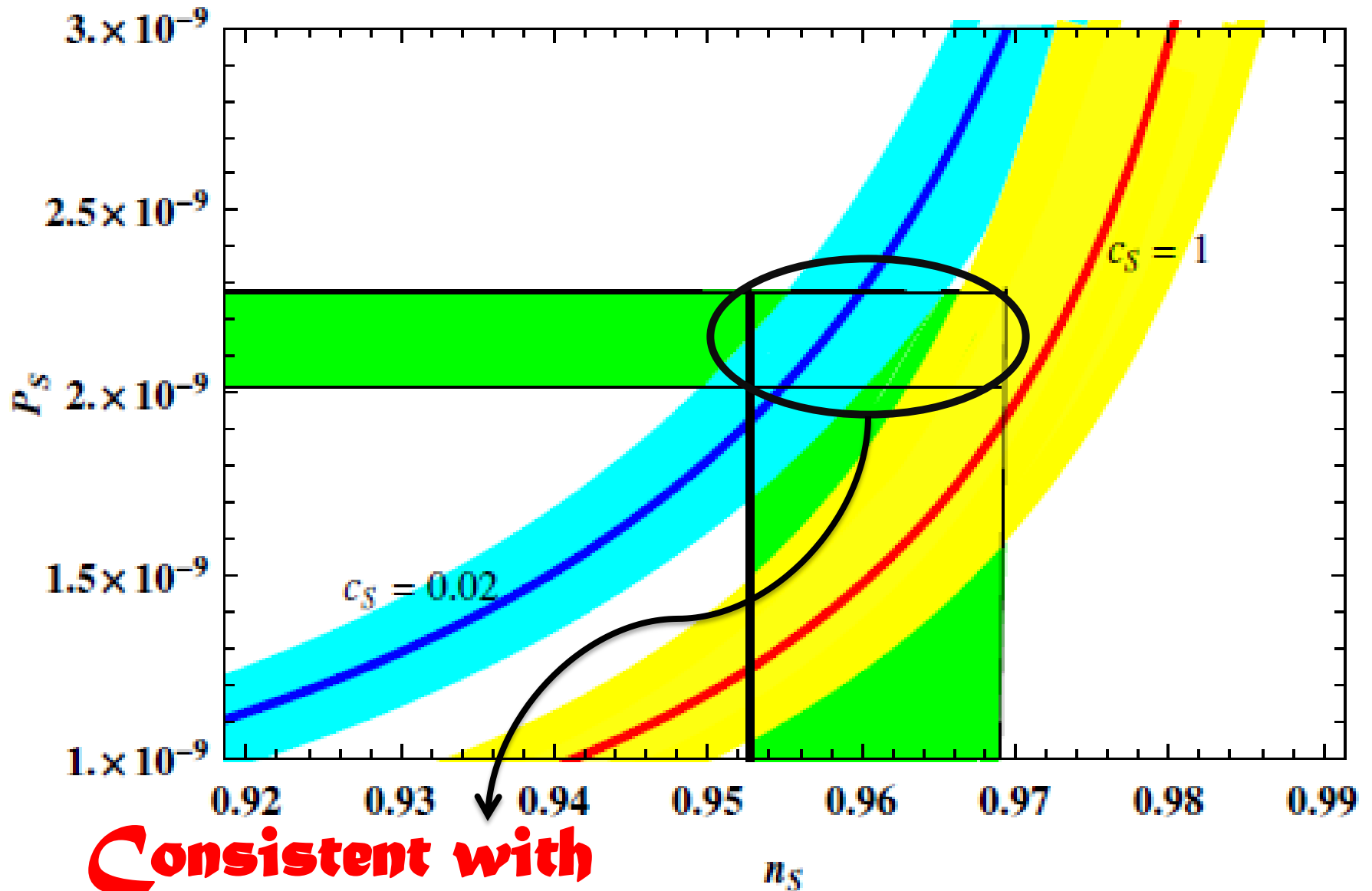


Consistent with
PLANCK+WMAP9

P_S vs n_S plot

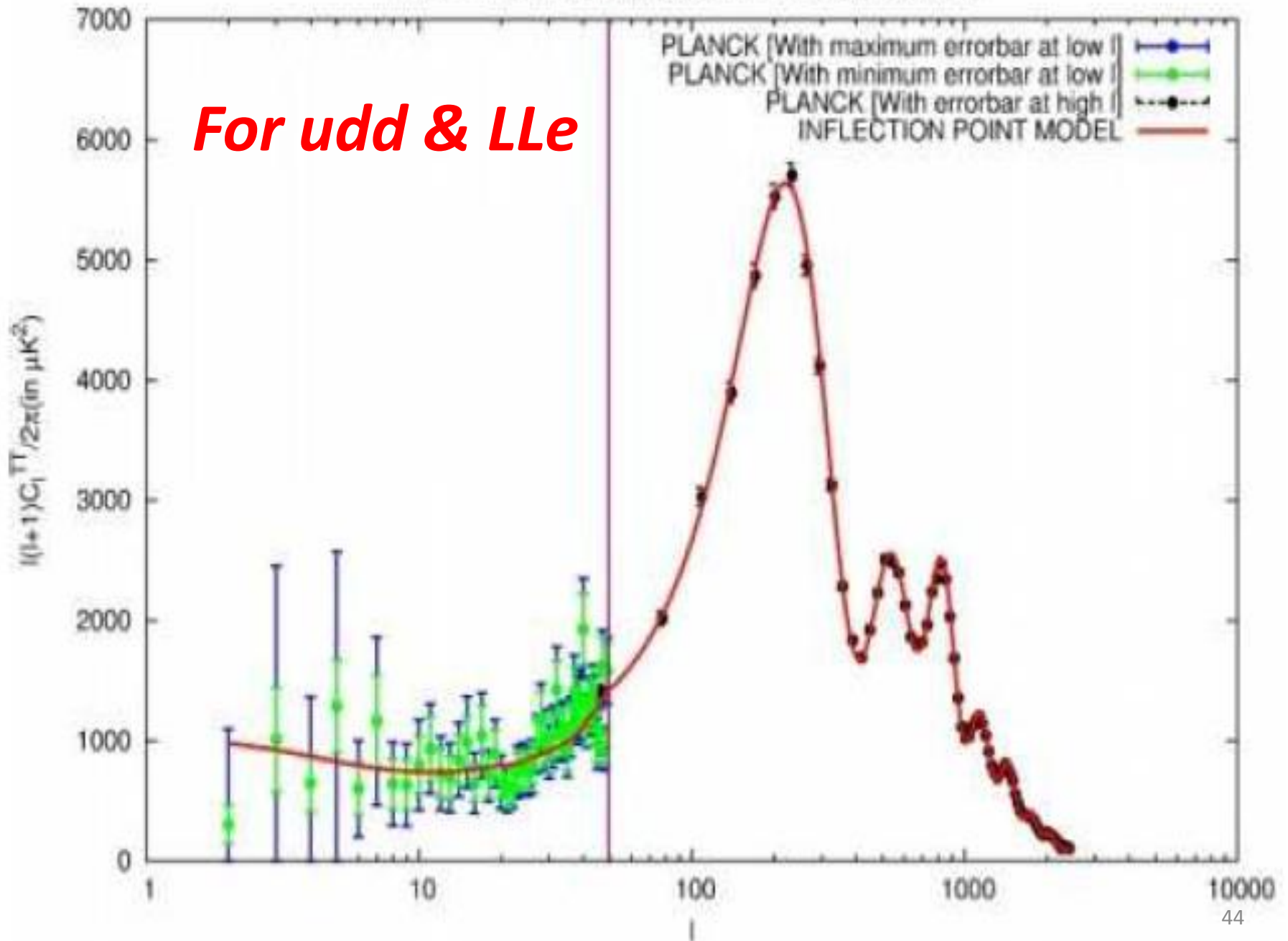


P_S vs n_S plot

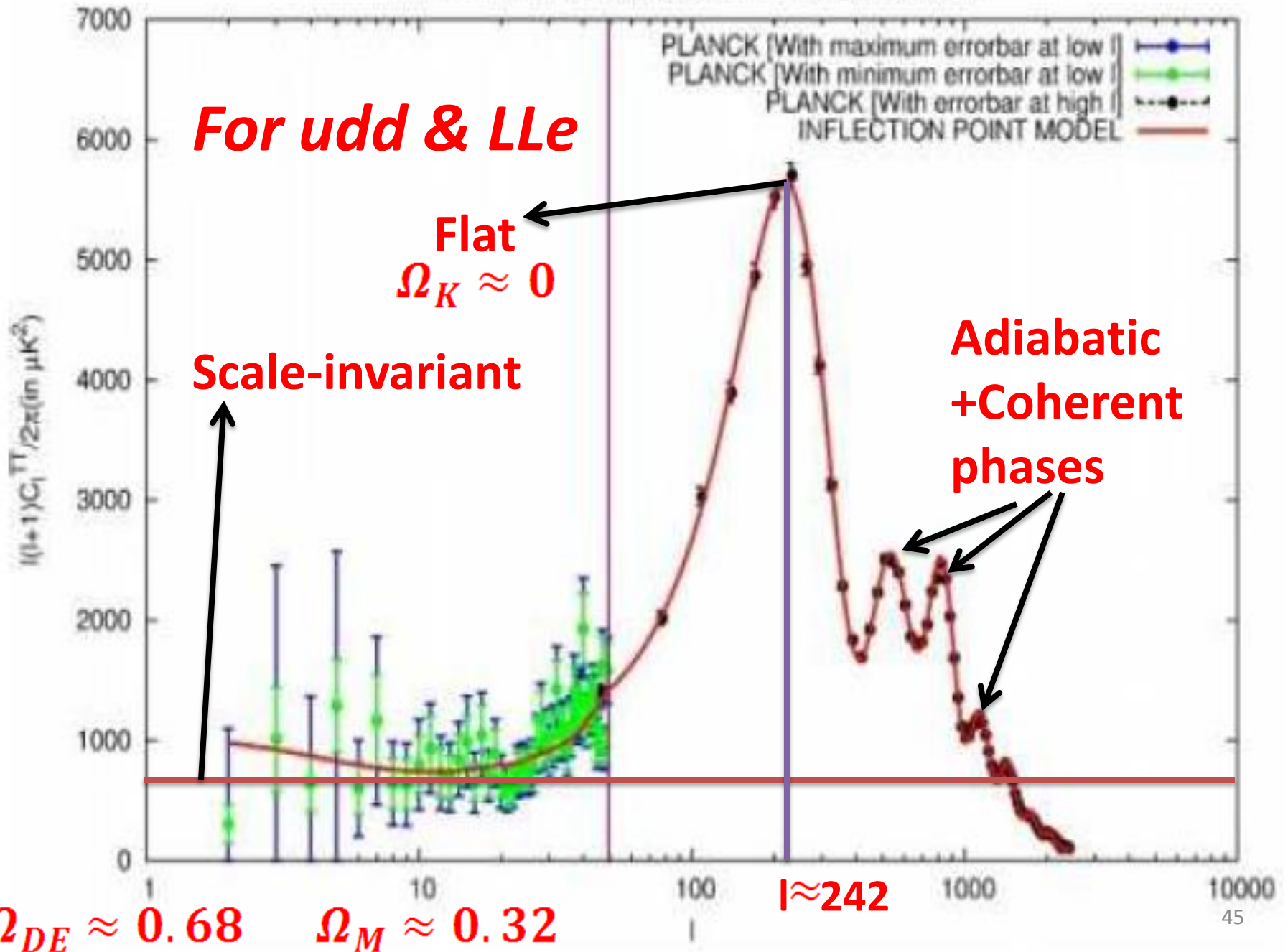


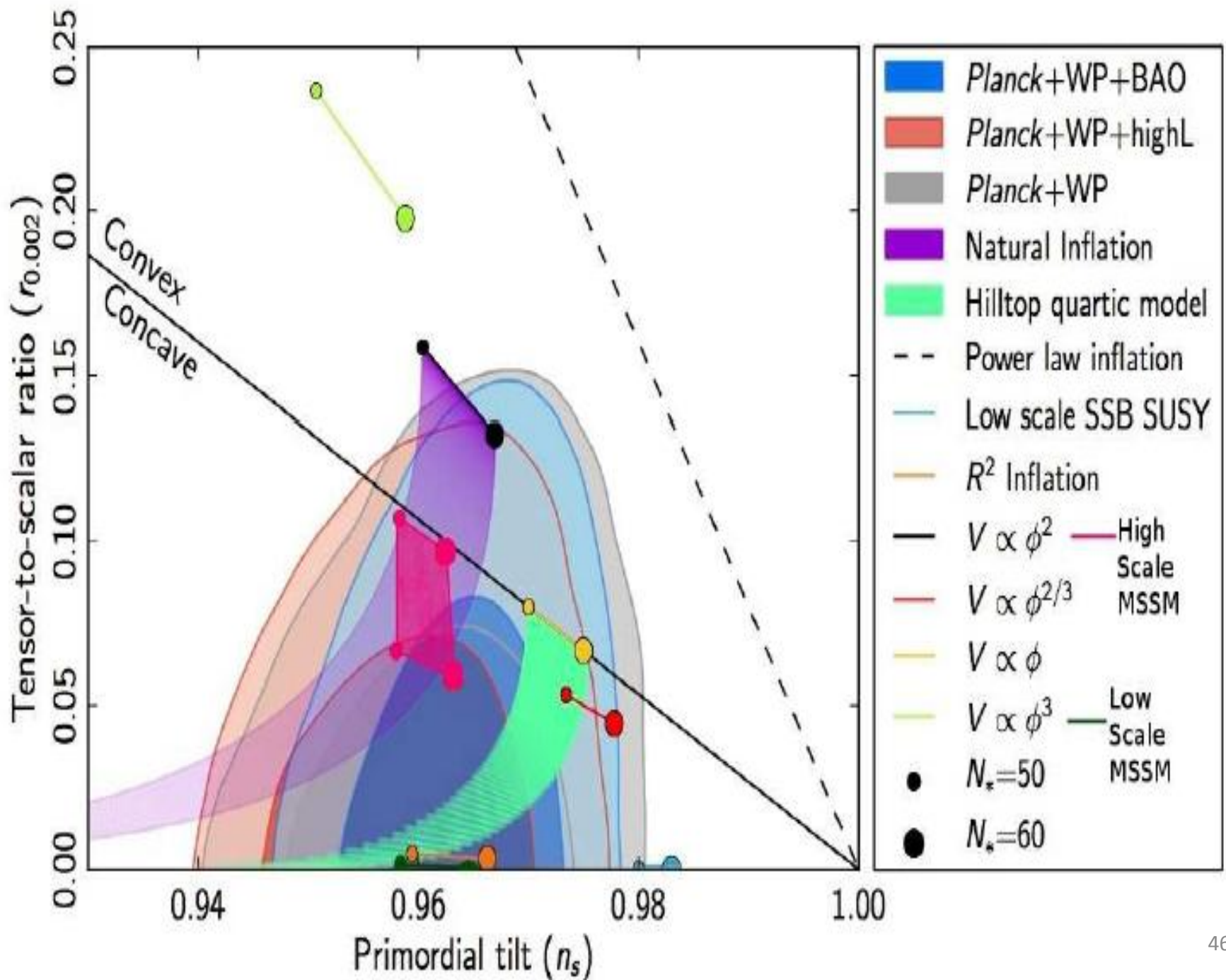
**Consistent with
PLANCK+WAP9**

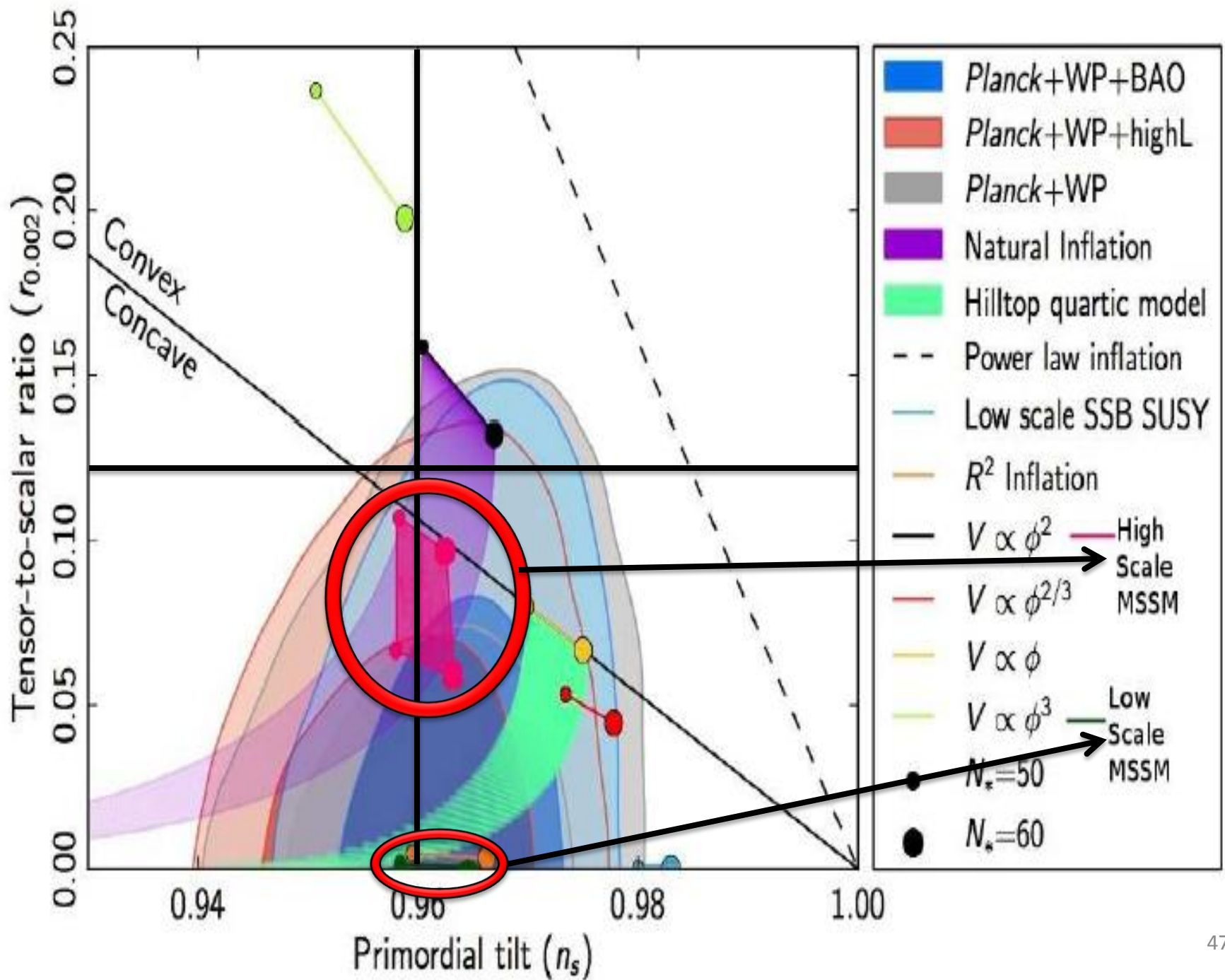
CMB TT Angular Power Spectrum (Survey over all l)



CMB TT Angular Power Spectrum (Survey over all l)

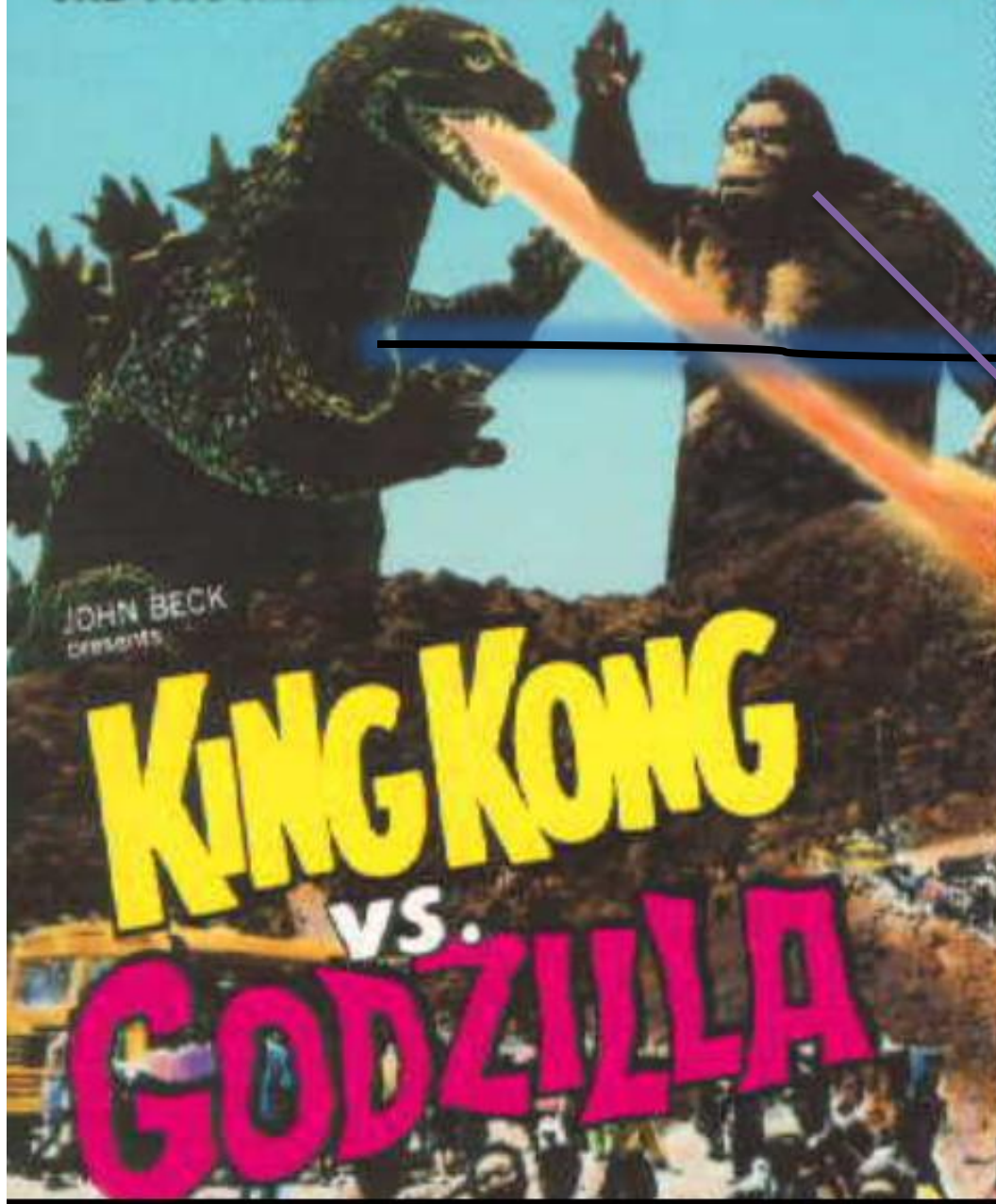






How to obtain Large 'r'

THE TWO MIGHTIEST MONSTERS OF ALL TIME!



Super

VS

Sub

**Planckian
Inflation ?**

In MSSM with

Non-minimal PSO

Sub-Planckian Inflation

Journal of **Cosmology and Astroparticle Physics**
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Observable gravitational waves from inflation with small field excursions

Low & high scale MSSM inflation, gravitational waves and constraints from Planck

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Bound on largest $r \lesssim 0.1$ from sub-Planckian excursions of inflaton

An accurate bound on tensor-to-scalar ratio and the scale of inflation

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Received 10 December 2013; accepted 11 March 2014

$$V = V_0 + A\phi^2 - B\phi^6 + C\phi^{10}$$

15 Sep 2014

Sub-Planckian Inflation

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10.1016/j.nucphysb.2014.09.015

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$$V = V_0 + A\phi^2 - B\phi^6 + C\phi^{10}$$

$$\Delta \phi \leq M_p$$



**Super
vs
Sub
Planckian
Inflation ?**

Checked for udd,
LLe, NHuL, HuHd.

Sub



**EFT
works well
for
(v)MSSM**

Checked for udd,
LLe, NH_uL, H_uH_d.

Sub

Bottom lines

- **High scale models of MSSM inflation within N=1 SUGRA are favoured after Planck.**
- **Validity of EFT prescription in N=1 SUGRA within MSSM requires non-minimal kahler interactions.**
- **Sub-Planckian VEV and field excursion can be generated in presence of PSO for $u d d, L L e, H_u H_d, N H_u L$ flat directions for MSSM.**
- **Non-minimal setup put stringent constraint on PNG parameters.**
- **Also put constraint on Reheating temperature .**

Future prospects

- **Dark matter +baryogenesis in presence of non-minimal PSO???**
- **Reconstruction of EFT within N=1 SUGRA sector using observed data (Planck)???**
- **(UV-IR) behaviour of MSSM in presence of higher curvature corrections???**
- **Origin of non-minimal corrections in N=1 SUGRA???**
- **Source of hidden sector and its uniqueness???**
Only stringy origin???
- **Embedding of MSSM within N=1 SUGRA from superstring theory ???**
- **Sensitivity of EFT couplings at UV end???**

MSSM collaborators.....

Anupam Mazumdar

Supratik Pal

Ernestas Pukartas

Lingfei Wang

Thanks for your time.....

