

Heavy quarks within the electroweak multiplet

Jaime Besprosvany,

in collaboration with R. Romero

Instituto de Física

Universidad Nacional Autónoma de México

XII SILAFAE, Lima, Perú, November, 2018

J. Besprosvany and R. Romero, "Representation of quantum field theory in an extended spin space and fermion mass hierarchy " *Int. J. Mod. Phys. A* **29**, No. 29 1450144 (17 pp.) (2014), arXiv:1408.4066[hep-th].

Ricardo Romero and Jaime Besprosvany, "Quark horizontal flavor hierarchy and two-Higgs- doublet model in a (7+1)-dimensional extended spin space ", arXiv:1611.07446[hep-ph],

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Contents

- Standard model puzzle: independent Yukawa, scalar-vector sectors. Motivation: multiplet structure
- Spin-extended model, context, and features
- Spin space: states and operators; (7+1)-dimensional case; conventional and spin-extended bases' use
- Lagrangian representation of vector-fermion electroweak and scalar-vector terms
- Scalar-field uniqueness: scalar-vector and scalar-fermion terms comparison
- Quark-mass relation, and hierarchy argument
- Summary

Motivation: multiplet structure

Electroweak-related puzzles in the standard model:

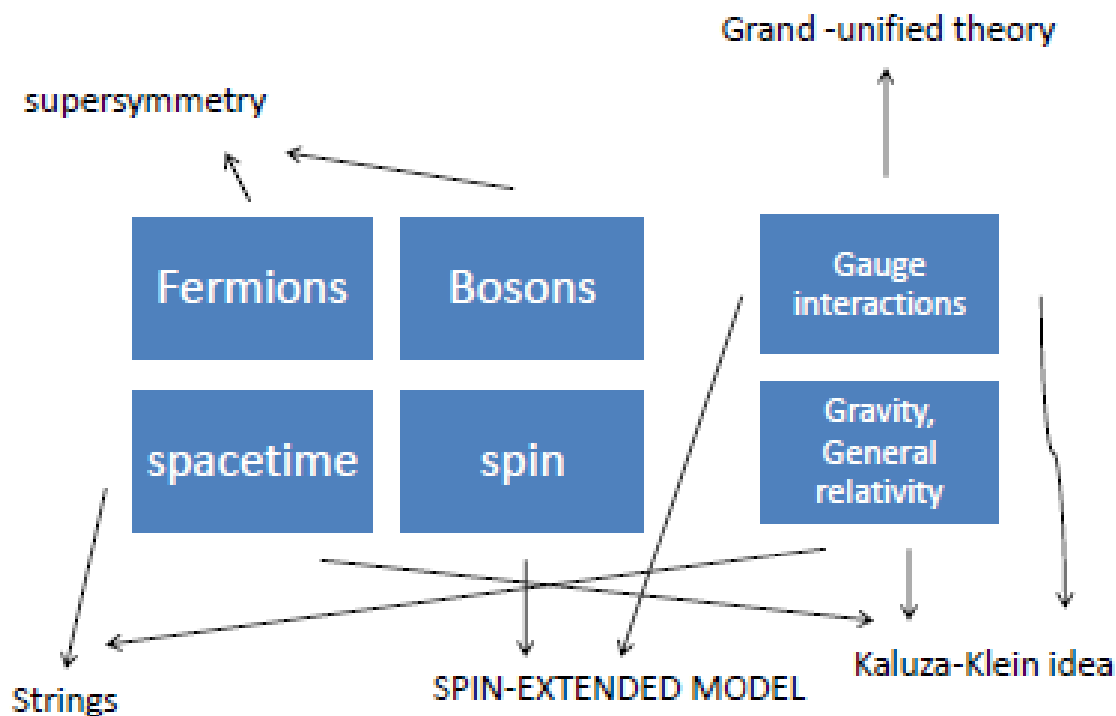
- Fermion-mass parameters; Yukawa sector independent of scalar-vector.
- Origin of electroweak symmetry breaking (Higgs mechanism).

	Masses (GeV)	Spin	Weak I^2	Hypercharge Y
• $W^{+/-}$	80.4	1	1	0
• Z	91.2	1	0	0
• H	126	0	$\frac{1}{2}$	1
• t	173	$\frac{1}{2}$	$\frac{1}{2}, 0$	$\frac{1}{3}, \frac{4}{3}$
• b	4	$\frac{1}{2}$	$\frac{1}{2}, 0$	$\frac{1}{3}, -\frac{2}{3}$

Composite multiplet structure suggested

Spin-extended model within standard-model extensions

Unification examples



Spin-space structure, at each dimension

- Finite number of partitions at each d , consistent with Lorentz symmetry
- Operators: **gauge** and **flavor** (only act on **fermions**)
- States: **fermions** and **bosons**
- Chiral components

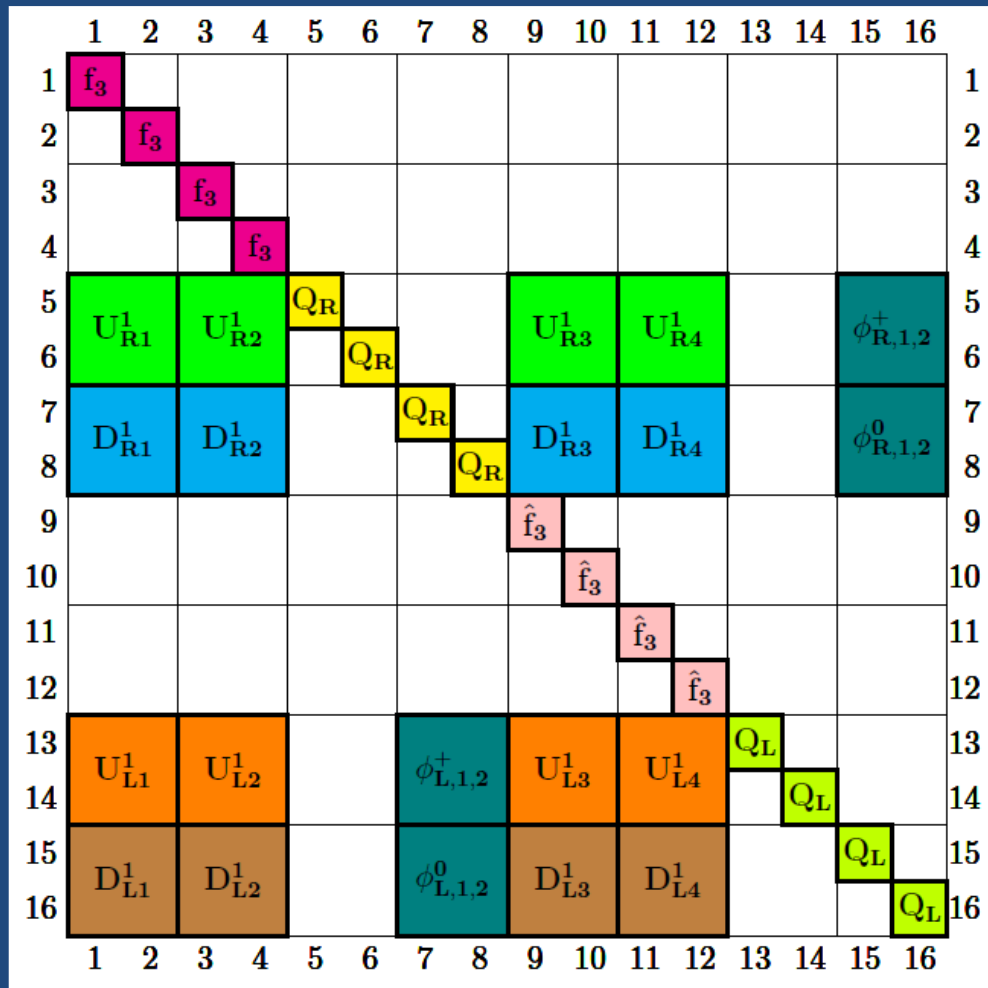
Operators

$1 - \mathcal{P}$		
	$\mathcal{I}'_{(N-4)R} \otimes \mathcal{C}_4$	
		$\mathcal{I}'_{(N-4)L} \otimes \mathcal{C}_4$

States

$1 - \mathcal{P}$	\bar{F}	\bar{F}
F	V	S, A
F	S, A	V

States in (7+1)-dimensional space



Use of conventional and spin bases

spin basis  conventional basis

- Finite number of possible partitions, consistent with 4-d Lorentz symmetry.
- Constrain representations and interactions at given dimension.

spin basis  conventional basis

Reinterpretation of fields:

- Standard-model projection.
- **SV**: scalar operator acting over vectors
- **SF**: scalar operator acting over fermions

Conventional and spin-extended bases, Lagrangian equivalence: fermion-vector

conventional basis

spin-extended basis

Field formulation:

$$A_\mu(x) = g_\mu{}^\nu A_\nu(x)$$

$$A_\mu(x) \gamma_0 \gamma^\mu$$

$$\mathcal{L}_{FV} = \bar{\mathbf{q}}_L(x) [i\partial_\mu + \frac{1}{2} g \tau^a W_\mu^a(x) + \frac{1}{6} g' B_\mu(x)] \gamma^\mu \mathbf{q}_L(x) +$$

$$\bar{t}_R(x) [i\partial_\mu + \frac{2}{3} g' B_\mu(x)] \gamma^\mu t_R(x) + \bar{b}_R(x) [i\partial_\mu - \frac{1}{3} g' B_\mu(x)] \gamma^\mu b_R(x)$$

$$\mathbf{q}_L(x) = \begin{pmatrix} t_L(x) \\ b_L(x) \end{pmatrix}$$

$$t_L(x) = \begin{pmatrix} \psi_{tL}^1(x) \\ \psi_{tL}^2(x) \end{pmatrix}$$

$$\mathcal{L}_{FV} = \text{tr} \{ \Psi_{qL}^\dagger(x) [i\partial_\mu + g I^a W_\mu^a(x) + \frac{1}{2} g' Y_o B_\mu(x)] \gamma^0 \gamma^\mu \Psi_{qL}(x) +$$

$$\Psi_{tR}^\dagger(x) [i\partial_\mu + \frac{1}{2} g' Y_o B_\mu(x)] \gamma^0 \gamma^\mu \Psi_{tR}(x) + \Psi_{bR}^\dagger(x) [i\partial_\mu + \frac{1}{2} g' Y_o B_\mu(x)] \gamma^0 \gamma^\mu \Psi_{bR}(x) \} P_f$$

$$\Psi_{qL}(x) = \sum_\alpha \psi_{tL}^\alpha(x) T_L^\alpha + \psi_{bL}^\alpha(x) B_L^\alpha$$

SV Lagrangian and scalar t-b spin representation

Scalar correspondence

$$\mathbf{H}(\mathbf{x}) \rightarrow \phi_1(\mathbf{x}) - \phi_2(\mathbf{x})$$

$$\tilde{\mathbf{H}}^\dagger(\mathbf{x}) \rightarrow \phi_1(\mathbf{x}) + \phi_2(\mathbf{x}).$$

$$\mathbf{H}_t(\mathbf{x}) = \phi_1(\mathbf{x}) + \phi_2(\mathbf{x}), \quad \mathbf{H}_b(\mathbf{x}) = \phi_1(\mathbf{x}) - \phi_2(\mathbf{x})$$

$$\mathbf{H}_{af}(\mathbf{x}) = a\phi_1(\mathbf{x}) + f\phi_2(\mathbf{x}).$$

$$R_5 = \frac{1}{2}(1 + \tilde{\gamma}_5), \text{ e. g., } R_5 \mathbf{H}_t(\mathbf{x}) L_5 = \mathbf{H}_t(\mathbf{x})$$

$$L_5 \mathbf{H}_t(\mathbf{x}) R_5 = 0, \quad R_5 \mathbf{H}_b(\mathbf{x}) L_5 = 0$$

$$\mathbf{H}_{af}(\mathbf{x}) = \frac{1}{\sqrt{2}}(\chi_t \mathbf{H}_t(\mathbf{x}) + \chi_b \mathbf{H}_b(\mathbf{x}))$$

$$\chi_t = \frac{1}{\sqrt{2}}(a + f), \quad \chi_b = \frac{1}{\sqrt{2}}(a - f)$$

SV spin representation

$$\mathbf{F}''(\mathbf{x}) = [i\partial_\mu + gW_\mu^i(\mathbf{x})I^i + \frac{1}{2}g'B_\mu(\mathbf{x})Y_o]\gamma_0\gamma^\mu$$

$$\mathcal{L}_{SV} = \text{tr}\{[\mathbf{F}''(\mathbf{x}), \mathbf{H}_{af}(\mathbf{x})]_\pm^\dagger [\mathbf{F}''(\mathbf{x}), \mathbf{H}_{af}(\mathbf{x})]_\pm\}_{\text{sym}}$$

Scalar-vector scalar-fermion comparison

$$\langle \eta_3(x) \rangle = v, \quad \langle \mathbf{H}(x) \rangle = \frac{v}{\sqrt{2}} \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

scalar-vector symmetry

Z-vector mass

Higgs mechanism

$$\langle \mathbf{H}_{af}(x) \rangle = H_n = \frac{v}{2} (\chi_t H_t^0 + \chi_b H_b^0),$$

$$\begin{aligned} \mathcal{L}_{SZm0} &= \text{tr}[H_n, W_0^3(x)gI^3 + B_0(x)\frac{1}{2}g'Y_o]^\dagger [H_n, W_0^3(x)gI^3 + B_0(x)\frac{1}{2}g'Y_o] \quad (11) \\ &= Z_0^2(x) \frac{1}{g^2 + g'^2} \text{tr}[H_n, g^2I^3 - \frac{1}{2}g'^2Y_o]^\dagger [H_n, g^2I^3 - \frac{1}{2}g'^2Y_o] = \frac{1}{2}Z_0^2(x)m_Z^2, \end{aligned}$$

Top-quark mass

Higgs mechanism

$$H_m = \langle \mathbf{H}_m(x) \rangle = m_t H_t^0 + m_b H_b^0$$

$$H_m^h T_M^1 = m_t T_M^1, \quad H_m^h T_M^{c1} = -m_t T_M^{c1},$$

$$H_m^h B_M^1 = m_b B_M^1, \quad H_m^h B_M^{c1} = -m_b B_M^{c1}, \quad (13)$$

where $H_m^h = H_m + H_m^\dagger$, and T_M^{c1}, B_M^{c1} correspond to negative-energy solution states

Spin-space connection: vector and fermion masses

vector

$$m_Z = v\sqrt{g^2 + g'^2}/2$$

fermion

massive quarks	H_m^h	Q	$\frac{3i}{2}B\gamma^1\gamma^2$
$T_M^1 = \frac{1}{\sqrt{2}}(T_L^1 + T_R^1)$	m_t	$2/3$	$1/2$
$B_M^1 = \frac{1}{\sqrt{2}}(B_L^1 - B_R^1)$	m_b	$-1/3$	$1/2$
$T_M^{c1} = \frac{1}{\sqrt{2}}(T_L^1 - T_R^1)$	$-m_t$	$2/3$	$1/2$
$B_M^{c1} = \frac{1}{\sqrt{2}}(B_L^1 + B_R^1)$	$-m_b$	$-1/3$	$1/2$

Table 3: Massive quark eigenstates of H_m^h



$$\sqrt{2}H_n = H_m$$

Quark-mass relation

Higgs mechanism

$$\langle \mathbf{H}_{af}^\dagger(x) \mathbf{H}_{af}(x) \rangle = (|a|^2 + |f|^2)v^2/2 = (|\chi_t|^2 + |\chi_b|^2)v^2/2 = v^2/2$$

$$(|a|^2 + |f|^2)v^2/2 = |m_t|^2 + |m_b|^2 = v^2/2$$



$$m_t = \sqrt{v^2/2 - m_b^2} \simeq 173.90 \text{ GeV}$$

$$v = 246 \text{ GeV}$$

$$m_b = 4 \text{ GeV}$$


Top-quark mass from hierarchy argument

$$\mathbf{H}_{af}(x) = a\phi_1(x) + f\phi_2(x)$$

$$\chi_t = \frac{1}{\sqrt{2}}(a + f), \chi_b = \frac{1}{\sqrt{2}}(a - f)$$

$$\mathbf{H}_{af}(x) = \frac{1}{\sqrt{2}}(\chi_t \mathbf{H}_t(x) + \chi_b \mathbf{H}_b(x))$$

$$(|a|^2 + |f|^2)v^2/2 = |m_t|^2 + |m_b|^2 = v^2/2$$



$O(a) \simeq O(f)$, ($m_b \ll m_t$) we get $\frac{1}{\sqrt{2}}v \simeq 173.95$, for $v = 246$ GeV

The “punchline:”

$$|\langle Z | \sqrt{2} H_n | Z \rangle|^2 = m_Z^2 \text{ and } \langle t | H_m + H_m^\dagger | t \rangle = m_t$$

Higgs mechanism

Argument summary

- Electroweak **conventional** fields and their Lagrangian can be written in a **spin**-extended space.
- **Scalar-vector** term, invariant under **scalar and conjugate** parametrization.
- **Same scalar** field within **SV** and **SF** terms connects **V** and **F**; after the **Higgs** mechanism, it constrains **quark** masses.
- **Multiplet** structure suggested for **heavy** standard-model particles.