



UNIVERSIDAD DE ANTIOQUIA
1803

Dark matter

in the light of the Λ CDM paradigm

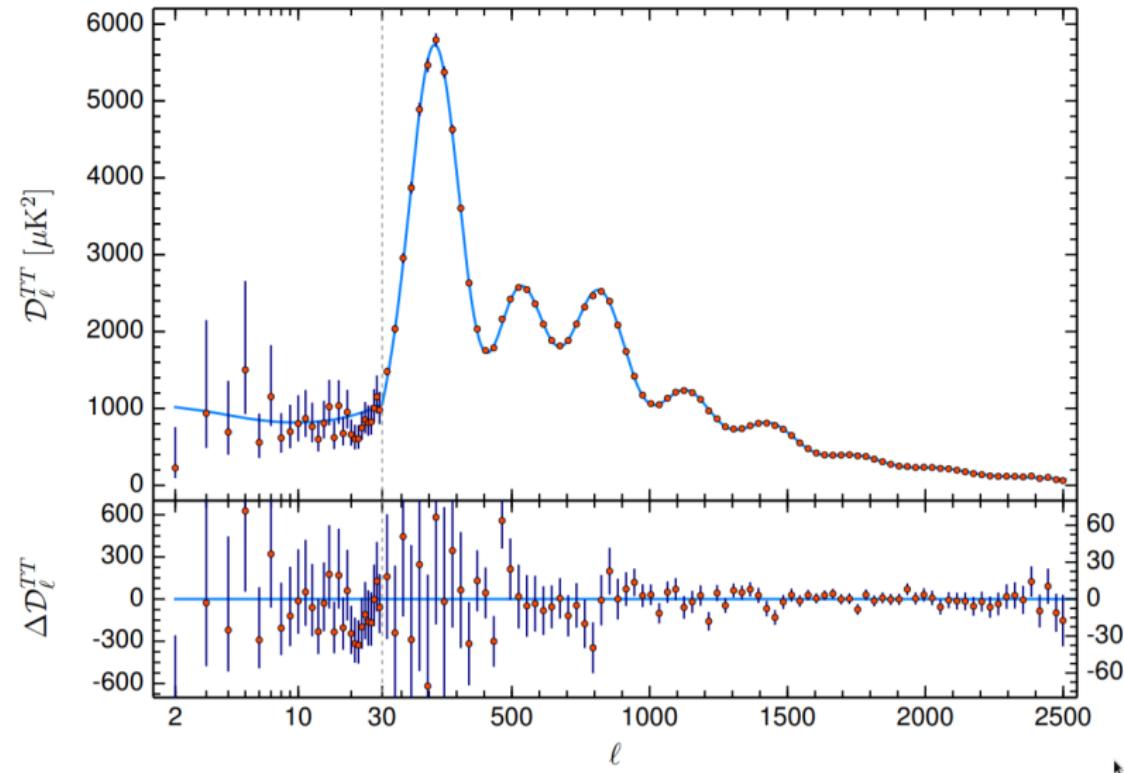
Diego Restrepo

Novembre 28, 2018

Instituto de Física
Universidad de Antioquia
Phenomenology Group
<http://gfif.udea.edu.co>



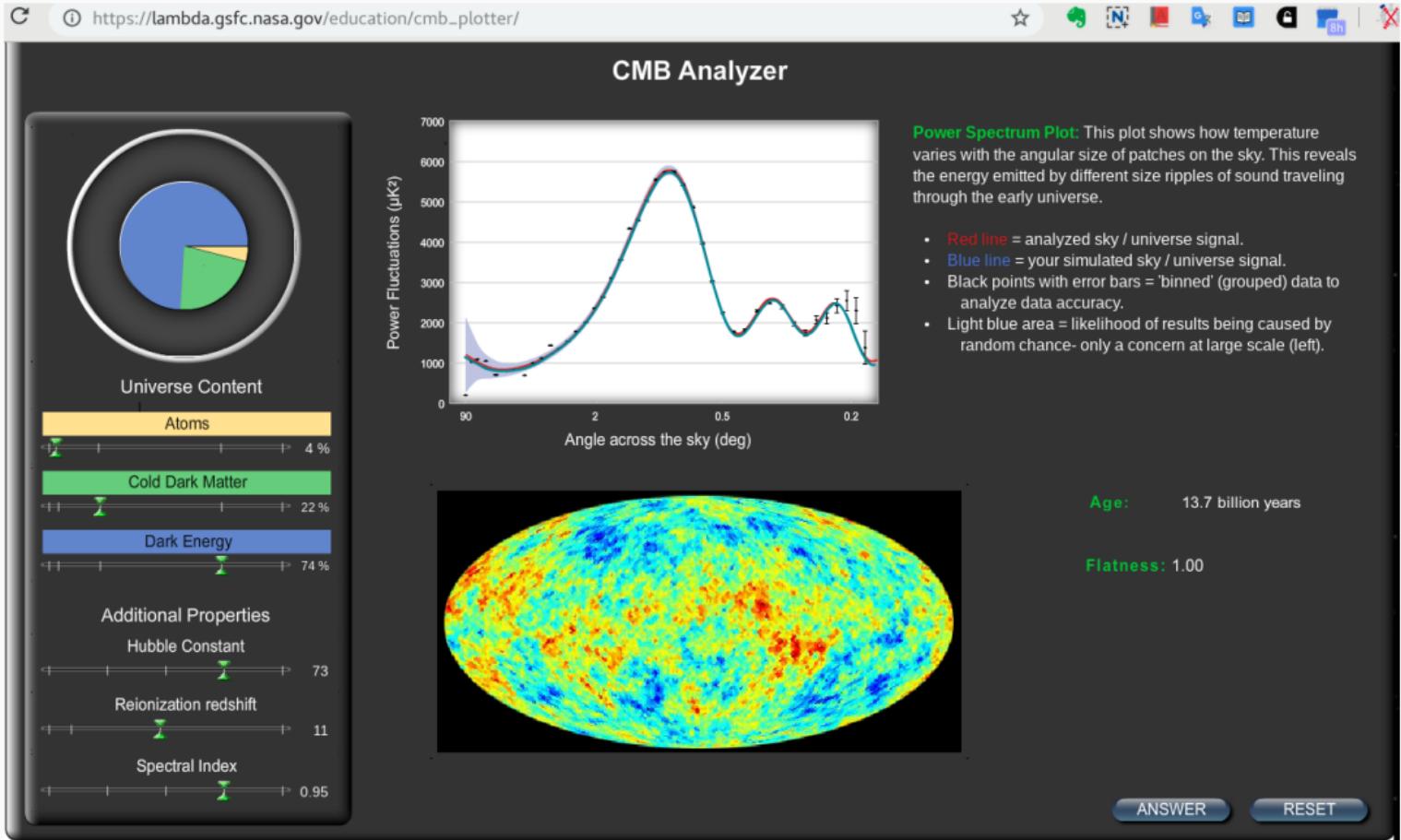
Λ CDM paradigm



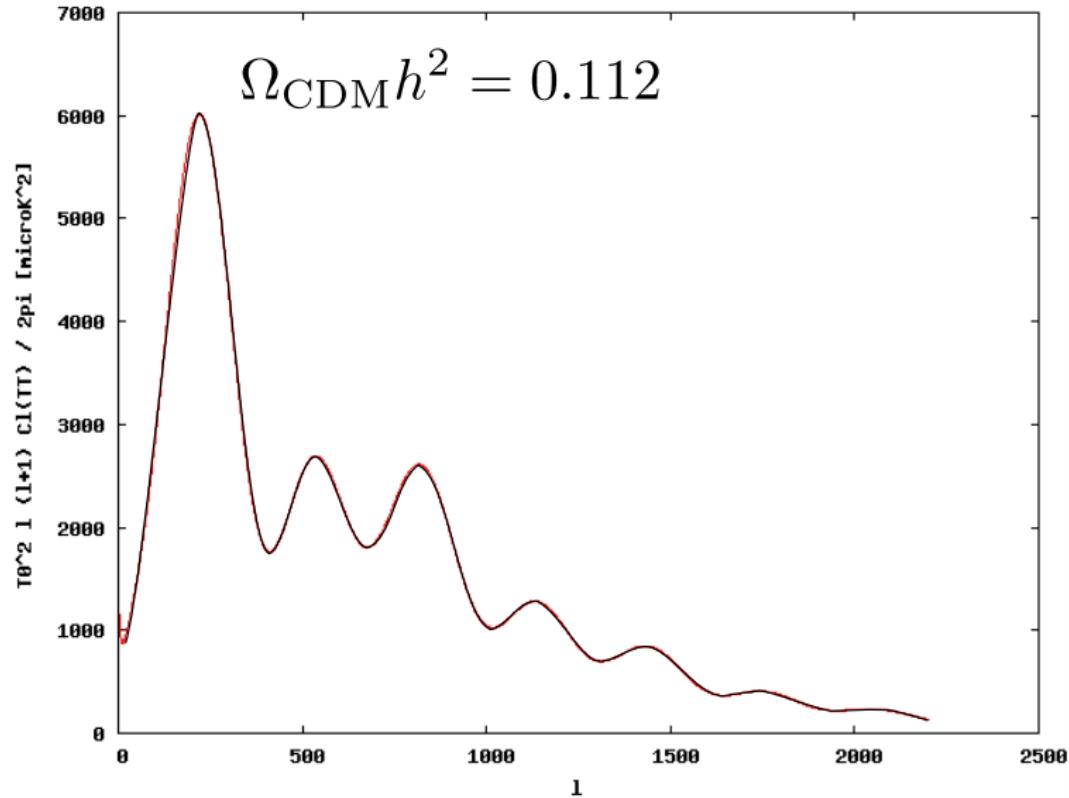
Credit: Planck 2018

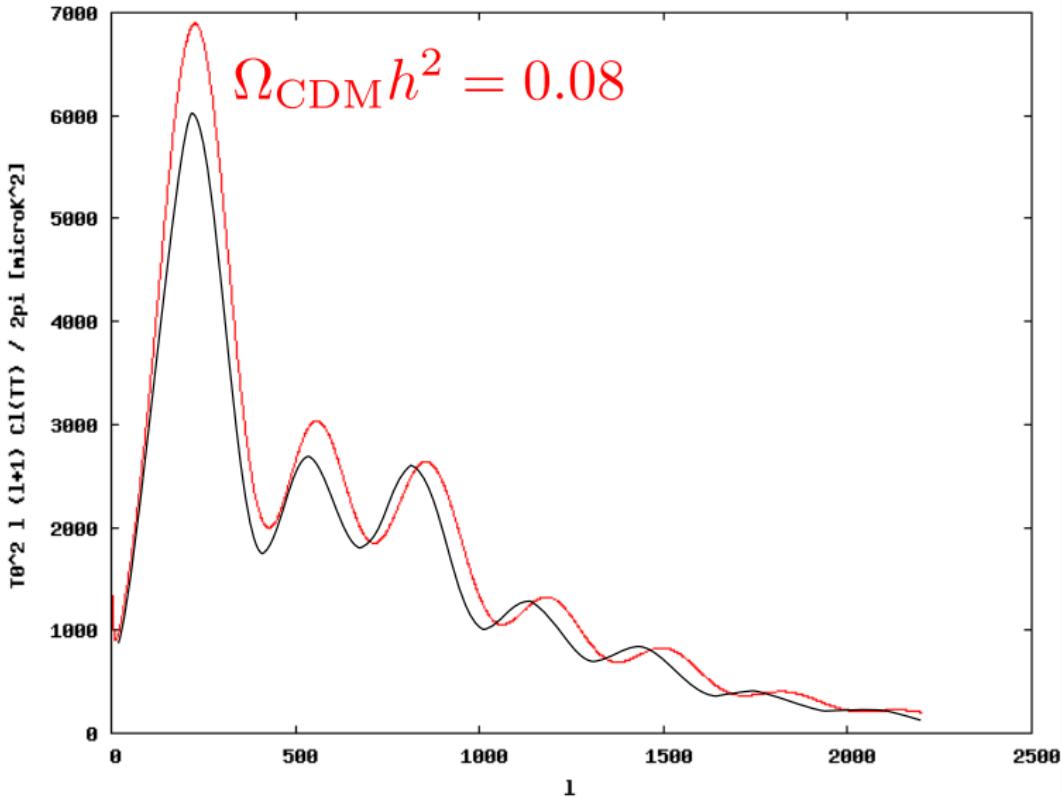
Why was the temperature of the CMB the same in all directions?

What was the origin of the small temperature fluctuations?



See also https://lambda.gsfc.nasa.gov/toolbox/tb_camb_form.cfm





Cosmic Miso Soup

- When matter and radiation were hotter than 3000 K, matter was completely ionised. The Universe was filled with plasma, which behaves just like a soup
- Think about a Miso soup (if you know what it is). Imagine throwing Tofus into a Miso soup, while changing the density of Miso
- And imagine watching how ripples are created and propagate throughout the soup

Credit: Komatsu, ICTP Summer School on Cosmology 2018¹

¹Video available

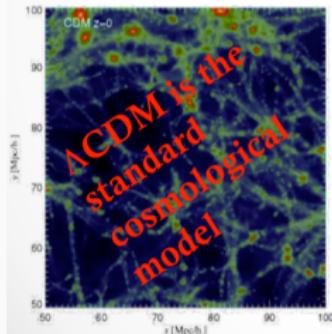


Credit: Komatsu, ICTP Summer School on Cosmology 2018¹

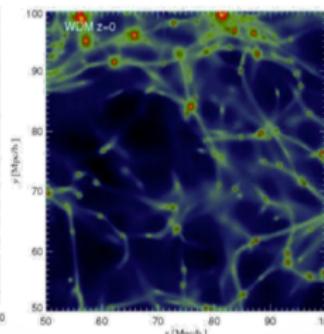
¹Video available

Dark matter simulations

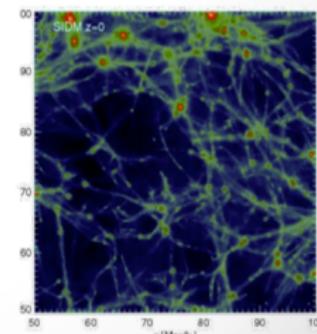
Cold Dark Matter
(Slow moving)
 $m \sim \text{GeV-TeV}$
Small structures form first, then merge



Warm Dark Matter
(Fast moving)
 $m \sim \text{keV}$
Small structures are erased

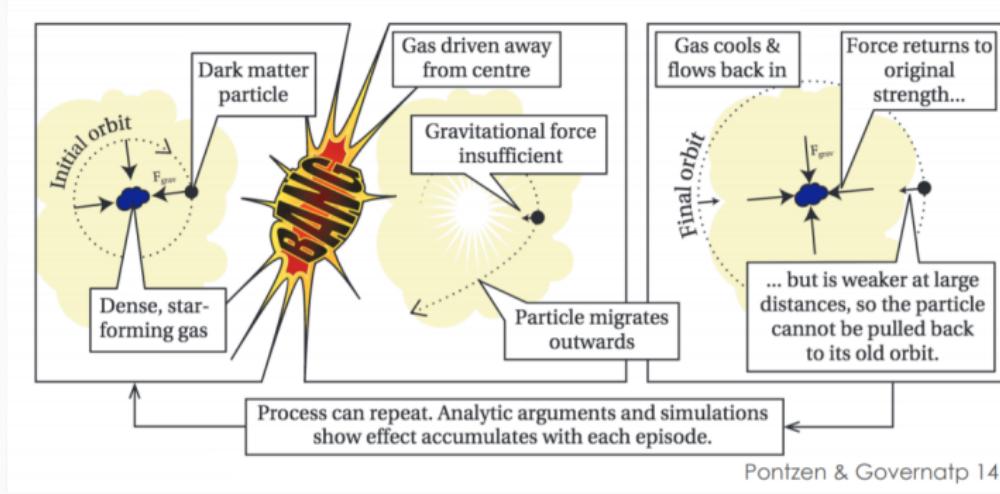


Self-Interacting Dark Matter
Strongly interact with itself
Large scale similar to CDM,
Small galaxies are different



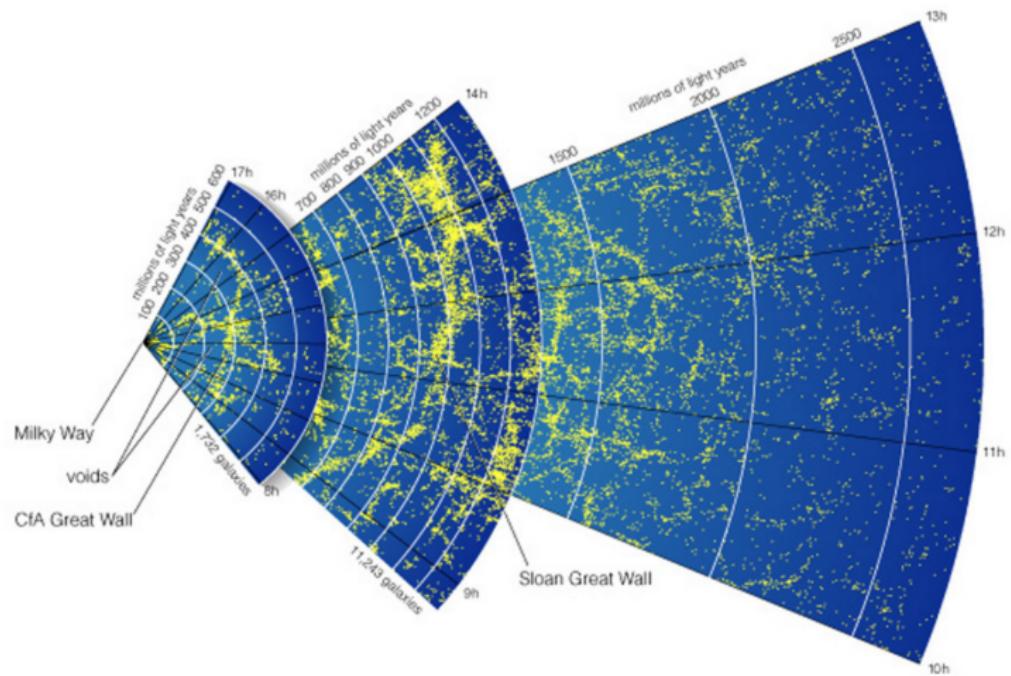
Credit: Arianna Di Cintio (Conference on Shedding Light on the Dark Universe with Extremely Large Telescopes, ICTP - 2018)

Baryonic effects



Once the effect of baryonic physics is included, it is hard to distinguish between WDM/SIDM/CDM

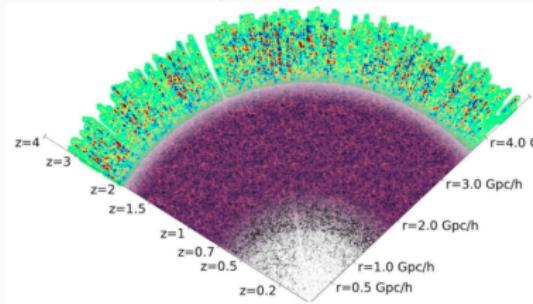
Goal



Maps of galaxy positions reveal extremely large structures: ***superclusters*** and ***voids***

© 2006 Pearson Education Inc, publishing as Addison-Wesley

The DESI experiment

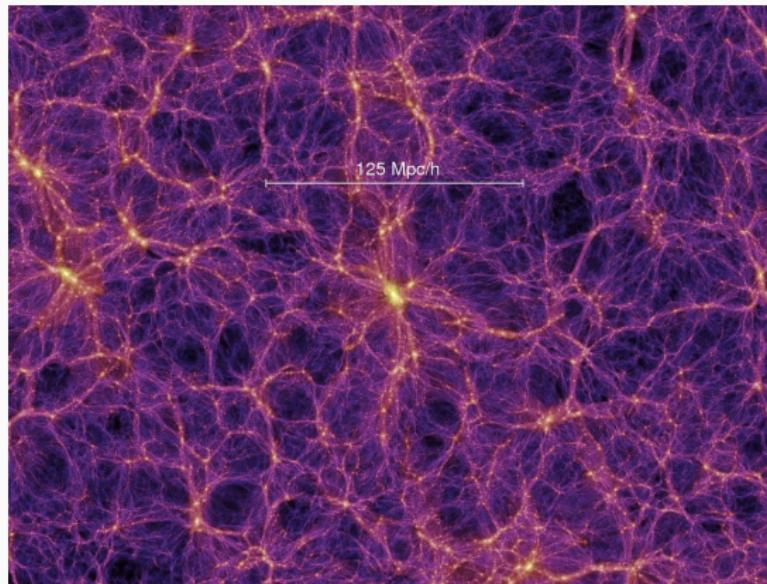


J. Forero <http://cosmology.univalle.edu.co/>

Cooking the soup: Cosmic web

Dark matter in the universe evolves through gravity to form a complex network of halos, filaments, sheets and voids, that is known as the cosmic web [arXiv:1801.09070]

An excess of a gas is observed between Milky Way and Andromeda



Cosmic Anatomy

Baryons

Missing Baryons

Dark Matter



Download from
Dreamstime.com
This image has been modified or cropped for publishing purposes only.



51423862
Digitalstormcinema | Dreamstime.com

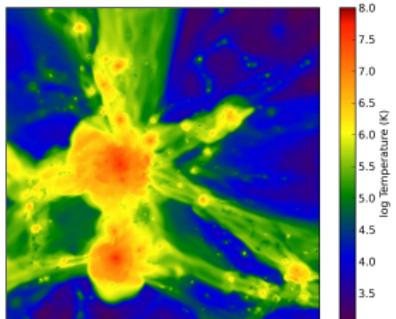
The muscles



Direct observations of filaments

Where are the Baryons? (Cen, Ostriker, astro-ph/9806281 [AJ])

Thus, not only is the universe dominated by dark matter, but more than one half of the normal matter is yet to be detected. (the muscles)



Warm-hot intergalactic medium (WHIM)
Density-weighted temperature projection of a portion of the refinement box of the C run of size $(18 h^{-1}\text{Mpc})^3$.
Low temperature WHIM confirmed by O VI line that peak at $T \sim 3 \times 10^5 \text{ K}$

Credit: Cen, arXiv:1112.4527 [AJ]



Hotter phases of the WHIM: Observations of the missing baryons in the warm-hot intergalactic medium (Nicastro, et al. arXiv:1806.08395 [Nature]).

The skeleton



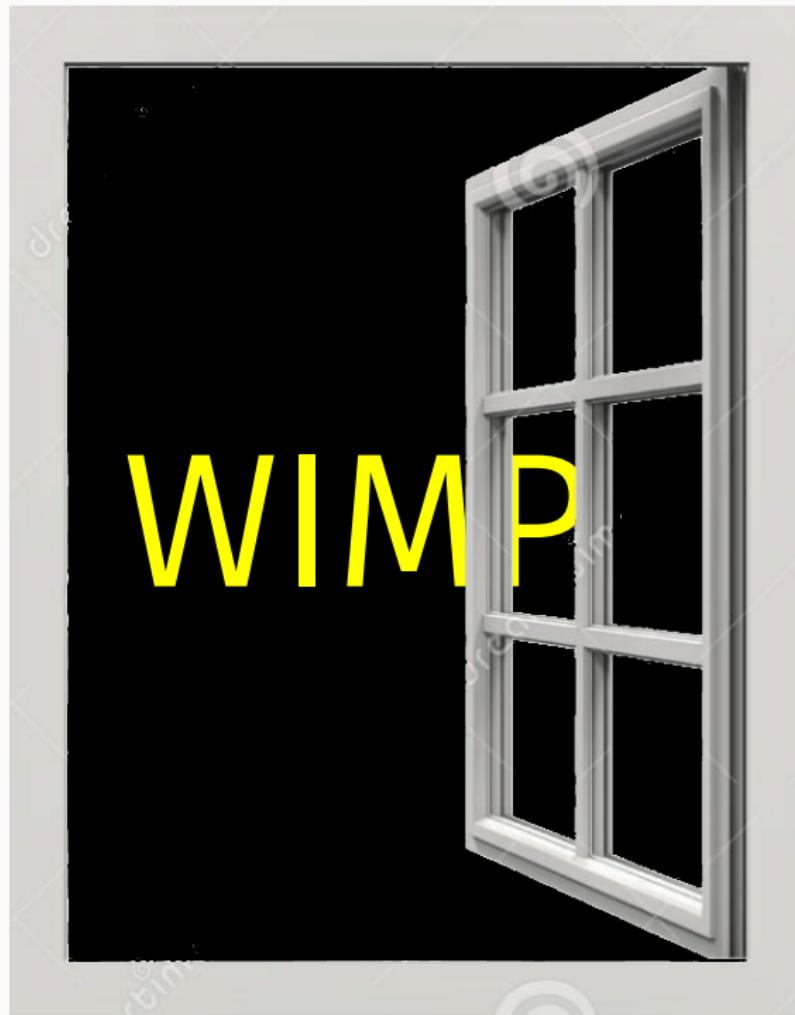
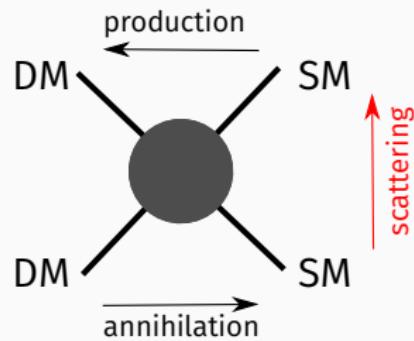
Credit: <https://www.disnola.com>

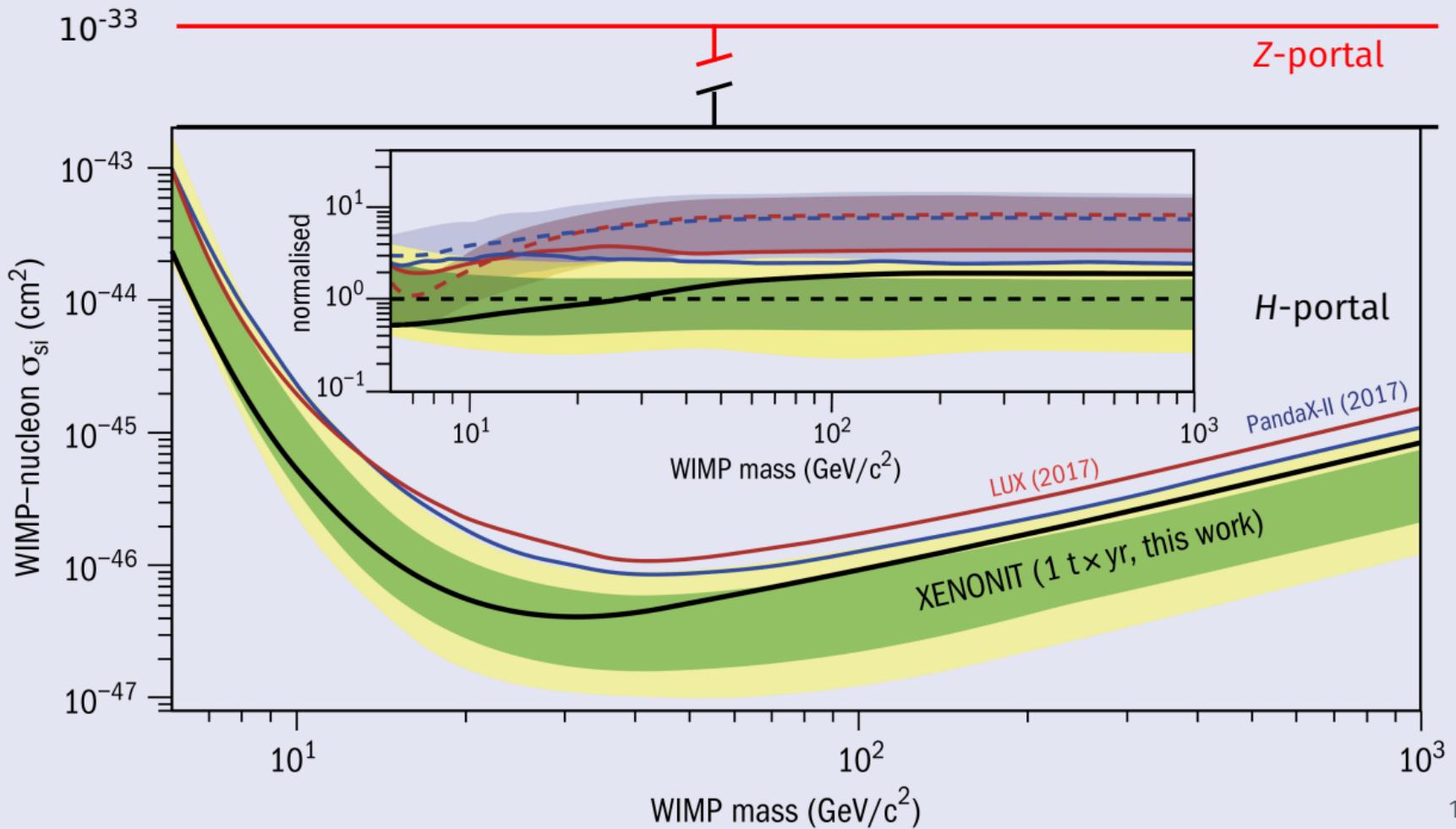
Dark matter interpretations

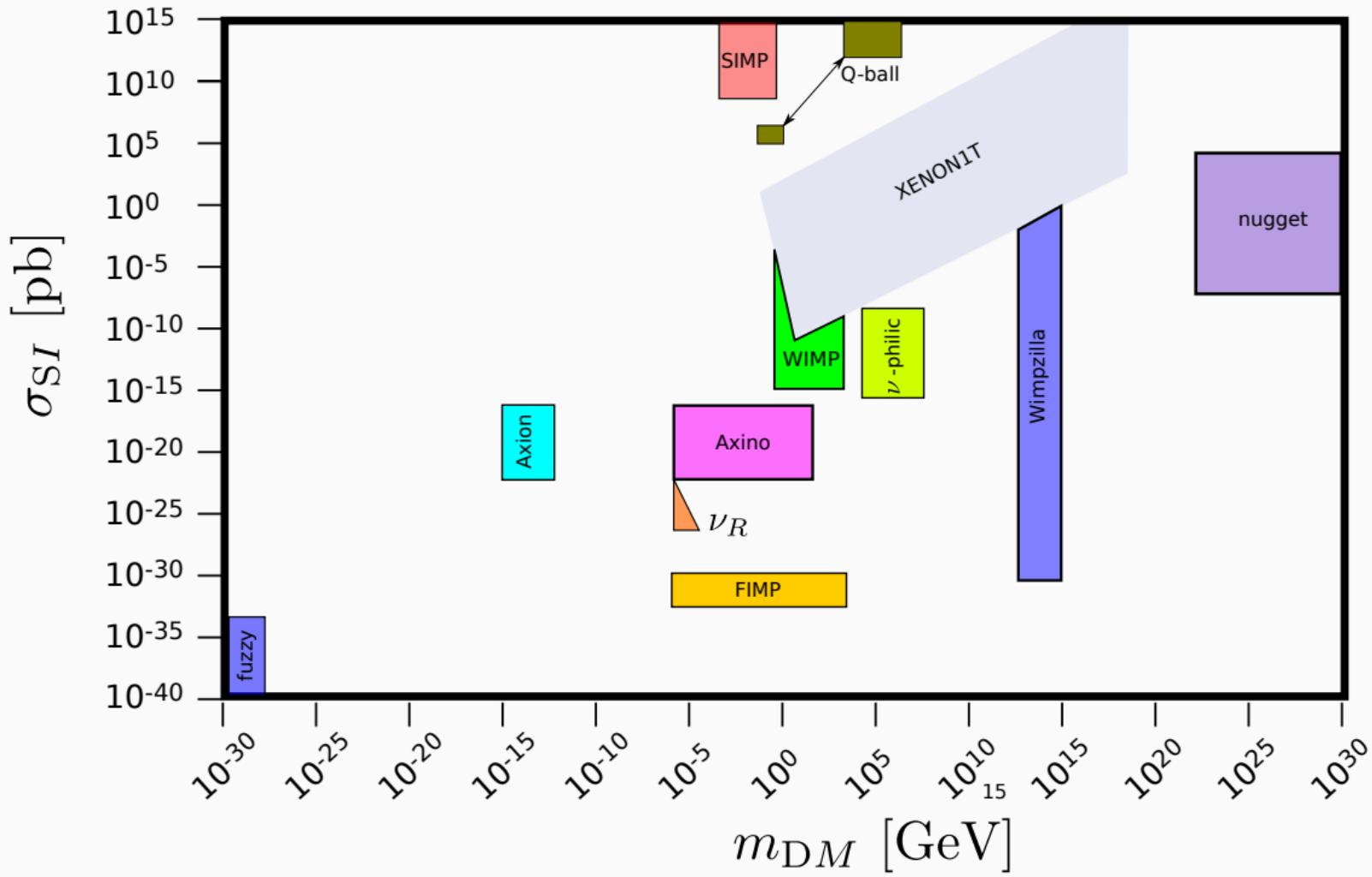
u	u	u	c	c	c	t	t	t
d	d	d	s	s	s	b	b	b
e^-	ν_e		μ^-	ν_μ		τ^-	ν_τ	
\bar{u}	\bar{u}	\bar{u}	\bar{c}	\bar{c}	\bar{c}	\bar{t}	\bar{t}	\bar{t}
\bar{d}	\bar{d}	\bar{d}	\bar{s}	\bar{s}	\bar{s}	\bar{b}	\bar{b}	\bar{b}
\bar{e}^+	$\bar{\nu}_e$		$\bar{\mu}^+$	$\bar{\nu}_\mu$		$\bar{\tau}^+$	$\bar{\nu}_\tau$	
g	g	g	g	g	g	γ	W^-	W^+
						Z^0	H	

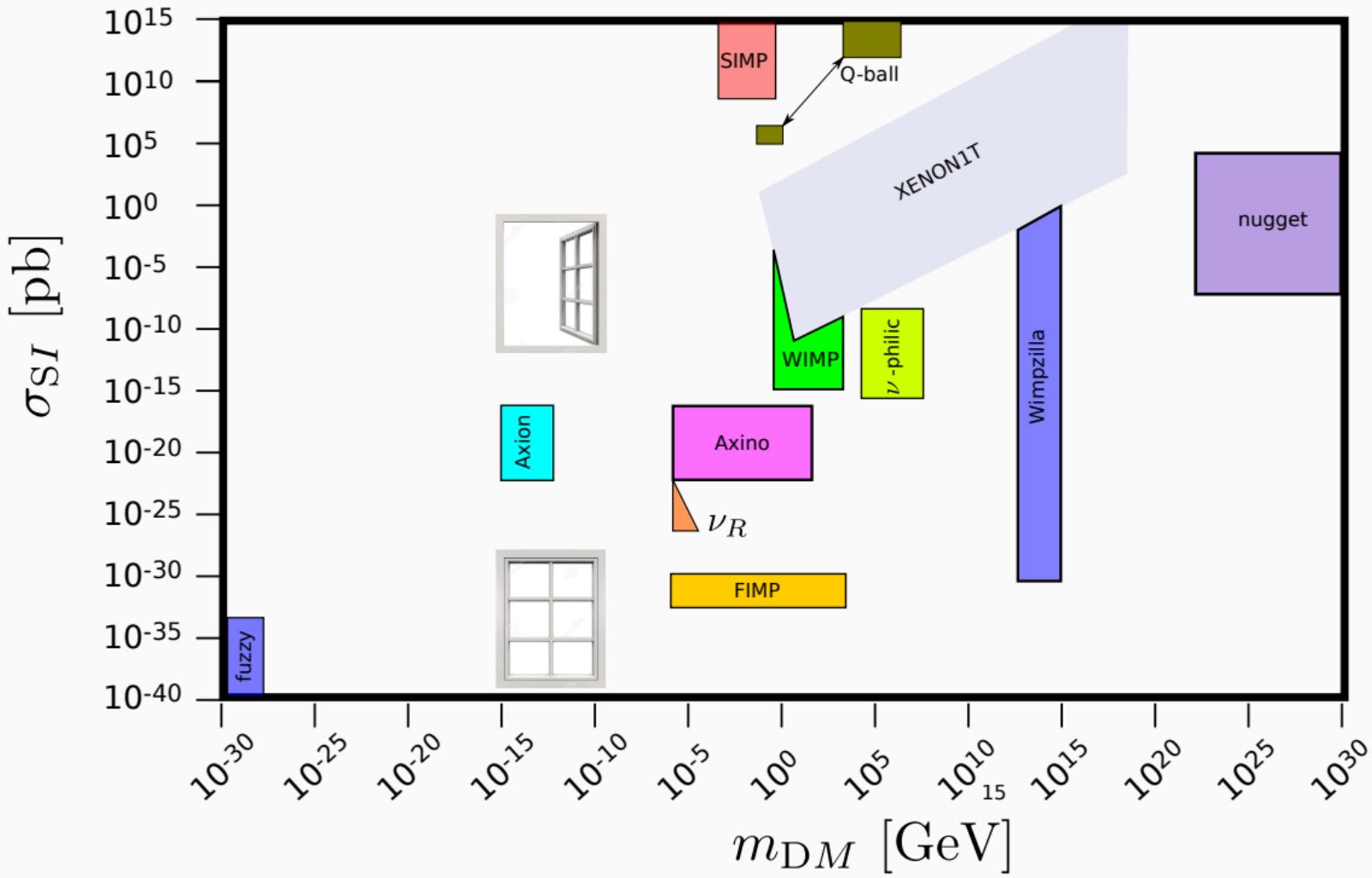


WIMP









Minimal number of fields:

SM (even) + Real Scalar singlet (odd)

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \frac{1}{2} \partial_\mu S \partial^\mu S - \lambda_{HS} H^\dagger H S^2 - M_S^2 S^2 - \lambda_S S^4.$$

S is stable and a dark matter particle

At some high temperature after reheating the scalar dark matter particle is in thermal equilibrium with the standard model plasma. With rather high yield. We need the Higgs portal interaction to exponential decrease the abundance until the correct relic density value. Freeze-out at $M_S/T \sim 20$

See <http://bit.ly/singletscalar>

requires $\lambda_{HS} \sim 0.1$ (weak-like annihilation cross sections)

```
[ ] %pylab inline
import numpy as np
from numpy import arange
from scipy.integrate import odeint
```



```
[ ] # parameters
```

<code>Ms = 100</code>	<small>#GeV Singlet Mass</small>
<code>Mp = 1.22e19</code>	<small>#GeV Planck Mass</small>
<code>g = 100</code>	<small># Degrees of freedom</small>
<code>gs = 106.75</code>	<small># Entropy degrees of freedom</small>
<code>H0 = 2.133*(0.7)*1e-42</code>	<small># GeV Hubble parameter (unused)</small>

▼ Boltzmann equation

The general expression for the thermal evolution of DM is as follows (see eq (5.26) Kolb and Turner):

$$\frac{x}{Y_{EQ}(x)} \frac{dY}{dx} = -\frac{n_{EQ}(x)\langle\sigma v\rangle}{H(x)} \left[\left(\frac{Y}{Y_{EQ}(x)} \right)^2 - 1 \right],$$

donde

$$n_{EQ}(x) = 2 \left(\frac{M^2}{2\pi x} \right)^{3/2} e^{-x}$$

and [] see (eq 5.16) Kolb & Turner]

$$H(x) = 1.67x^{-2}g_*^{1/2} \frac{M^2}{Mp}$$

▼ WIMP

The initial condition to solve the evolution equation is $Y(x_i) = Y_{EQ}$, where $x_i = 0.01$, such that $T_i = M/x_i = 10^4$ GeV.

```
[7] def Yeq(x):
    return 0.145*(g/gs)*(x)**(3/2)*np.exp(-x).

xi=1E-4
xe=1000
npts=3000
# For several order of magnitude:
x = np.linspace(0.01, 1000, 1000)
```

```
sigmav=[1.7475568196239999e-09,1.7475568196239999e-06]
def eqd(yl,x,Ms = 100,σv = sigmav[0]):
    """
    Ms   [GeV]      : Singlet Mass
    σv: [1/GeV^2]  : (σv)
    """

    Mp = 1.22e19
    g = 100          # Degrees of freedom
    gs = 106.75      # Entropy degrees of freedom

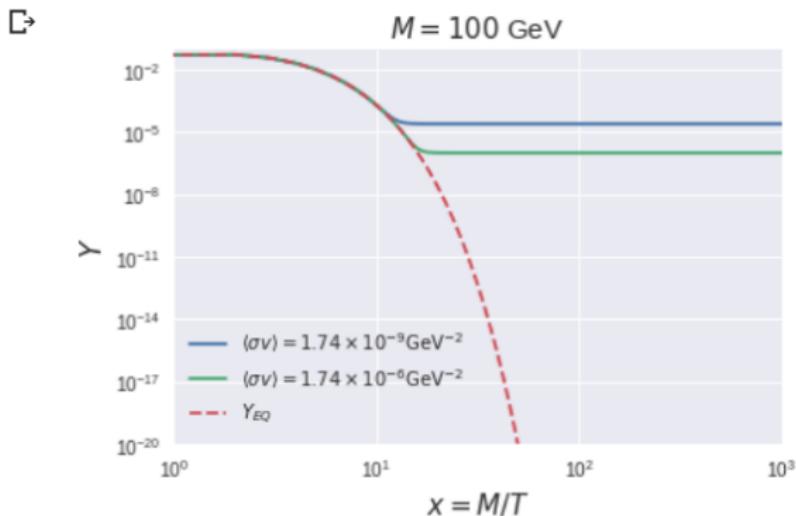
    H = 1.67*g**(1/2)*Ms**2/Mp

    dyl = -2*((Ms**2/(2*np.pi*x))**(3/2)*np.exp(-x))*σv/(x**(-2)*H*x))*(yl**2 - (0.145*(g/gs)*(x)**(3/2

    return dyl
```

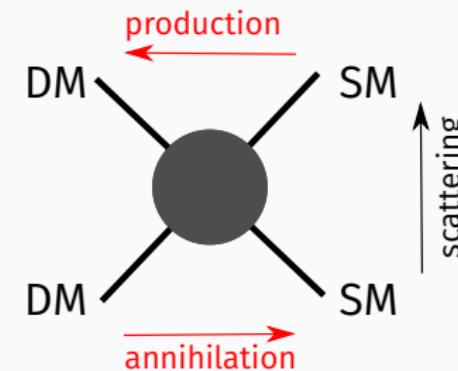
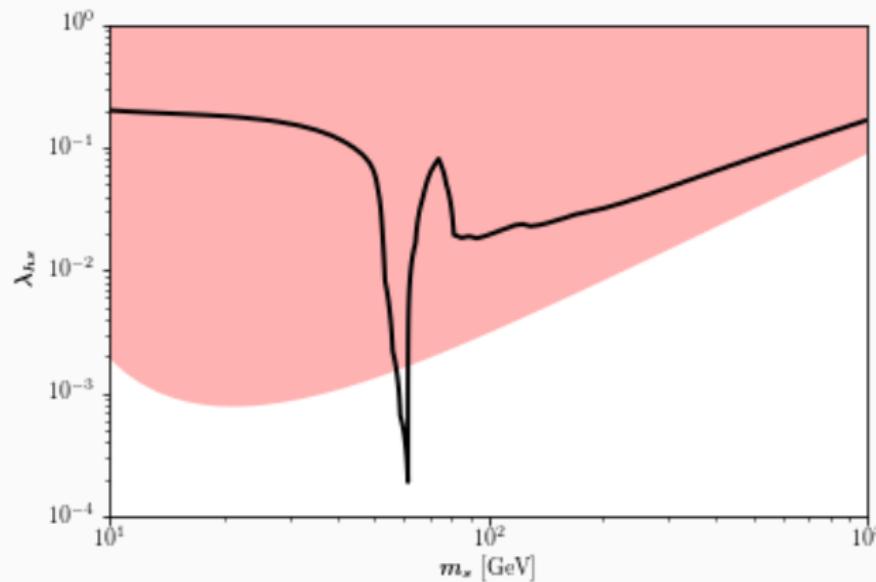
The following plot can be find in the reference book (Figure 3.1)

```
[10] plt.loglog(x,yl, label = r'$\langle \sigma v \rangle = 1.74 \times 10^{-9} \text{ GeV}^{-2}$')
    plt.loglog(x,yli, label = r'$\langle \sigma v \rangle = 1.74 \times 10^{-6} \text{ GeV}^{-2}$')
    plt.loglog(x,Yeq(x), '--', label = '$Y_{EQ}$')
    plt.ylim(ymax=0.1,ymin=1e-20)
    plt.xlim(xmax=1e3,xmin=1)
    plt.xlabel('$x = M/T$', size= 15)
    plt.ylabel('$Y$', size= 15)
    plt.title('$M = 100$ GeV', size= 15)
    plt.legend(loc='best',fontsize=10)
    plt.grid(True)
```



Full wimp parameter space

Restricted by direct detection cross section Xenon1T (arXiv:1805.12562)

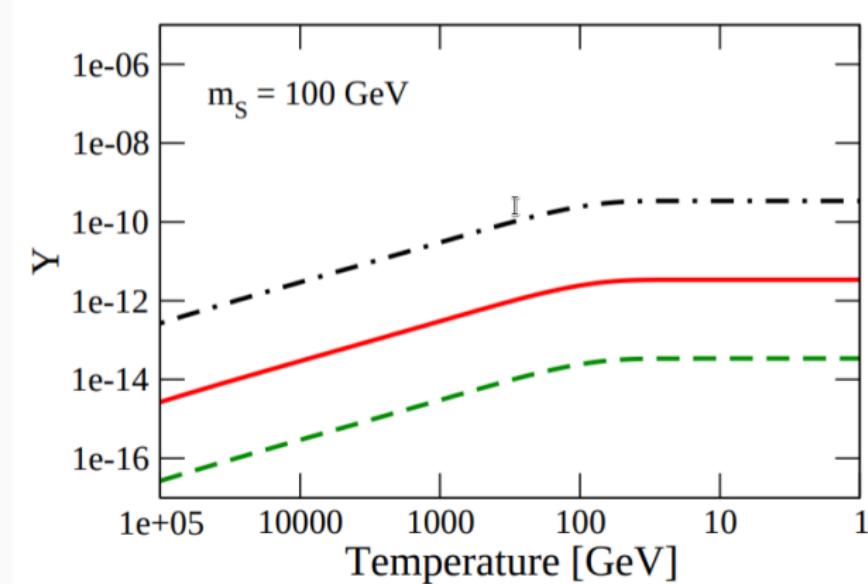


$$\Omega h^2 = 0.112$$

Hard To
KILL



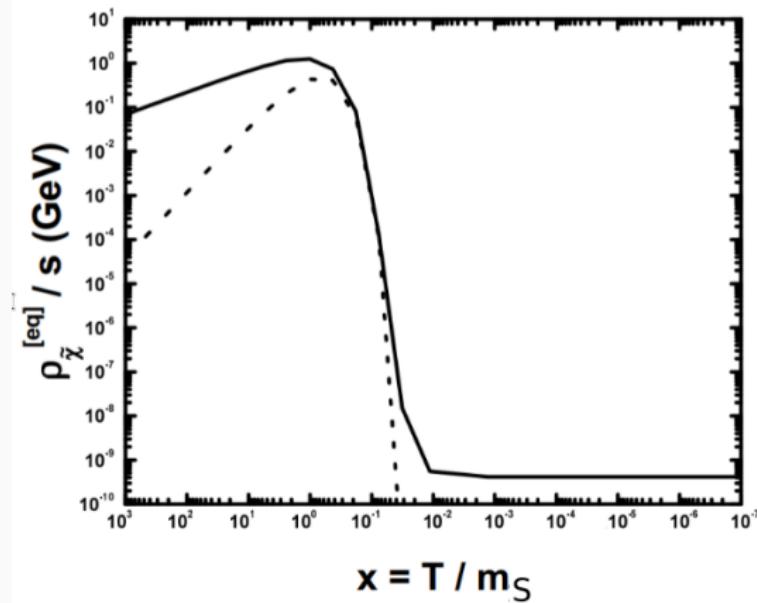
At some high temperature after reheating the abundance of scalar dark matter particle is zero. A feebly interaction allows the Higgs to produce dark matter particles until $M_S/T \sim 1$ where the freeze-in is reached. See C. Yaguna arXiv:1105.1654 [JHEP]



$\lambda_{HS} = 10^{-10}, 10^{-11}, 10^{-12}$. Not signals at all!

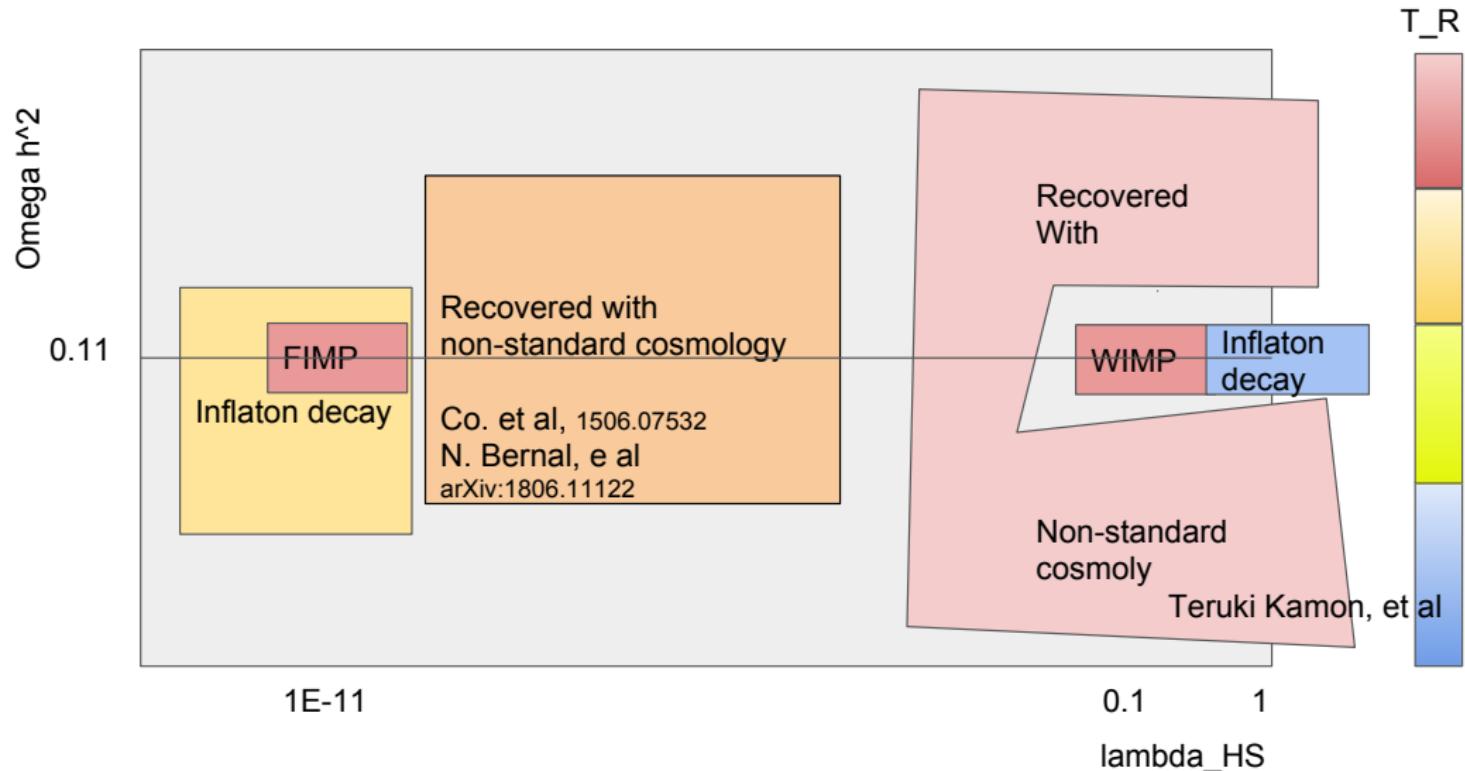
WIMP during reheating

The freeze-out occurs at $M/T_{\text{RH}} \sim 10^3$. Very slow reheating for $M \sim 1\text{TeV}$ - After reheating the dark matter particle not longer thermalize and the freeze out is kept. See C. Pallis hep-ph/0402033 [APP]



$M_\phi = 10^6 \text{ GeV}$, $M_S = 350 \text{ GeV}$, $T_{\text{RH}} = 5 \text{ GeV}$, $N_S^i = 1.4 \times 10^{-7}$. λ_{HS} fixed to be compatible with direct detection constraints

Recovered parameter space



Alternative WIMP portals

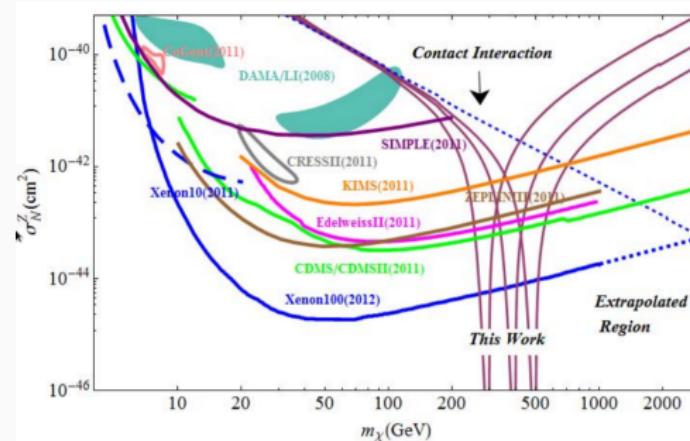
- One-loop direct cross-section
- Z' -portal (Dirac fermion dark matter)
- :

Isosinglet dark matter candidate

ψ as a isosinglet Dirac dark matter fermion charged under a local $U(1)_X$ (SM) couples to a SM-singlet vector mediator X as

$$\mathcal{L}_{\text{int}} = -g_\psi \bar{\psi} \gamma^\mu \psi X_\mu - \sum_f g_f \bar{f} \gamma^\mu f X_\mu,$$

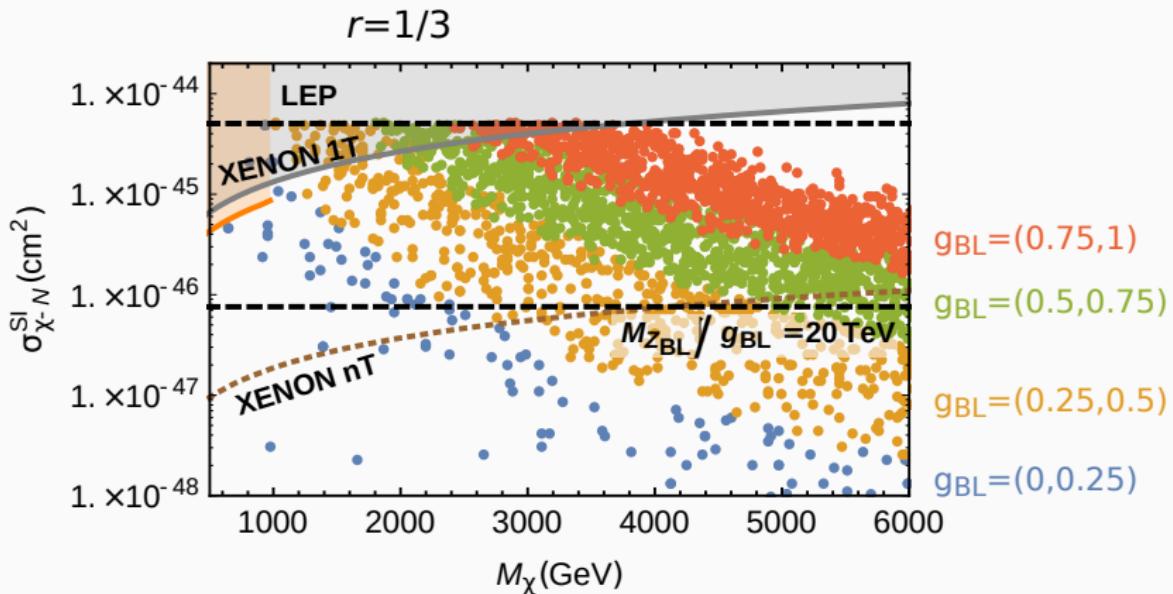
where f are the Standard Model fermions



Isosinglet Dirac fermion dark matter model

Left Field	$U(1)_{B-L}$
$(\nu_{R_1})^\dagger$	+1
$(\nu_{R_2})^\dagger$	+1
$(\nu_{R_2})^\dagger$	+1
ψ_L	-r
$(\psi_R)^\dagger$	r
ϕ	2

$$\chi = \begin{pmatrix} \psi_L \\ \psi_R \end{pmatrix}$$

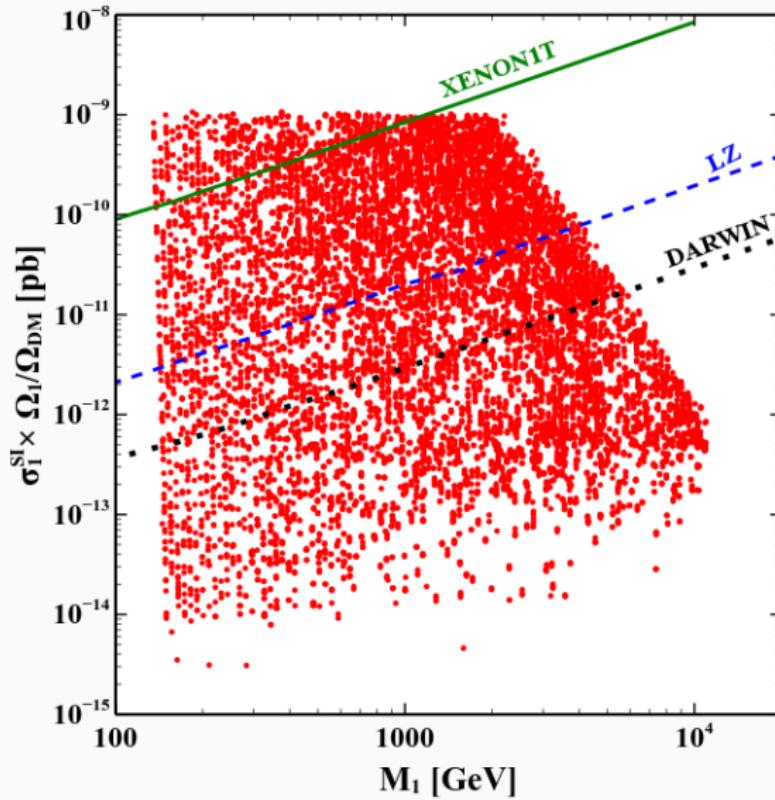


Duerr et al: 1803.07462 [PRD]

Two component Dirac fermion dark matter model

Field	$U(1)_{B-L}$
$(\nu_{R_1})^\dagger$	+1
$(\nu_{R_2})^\dagger$	+1
ξ_1	$10/7$
η_1	$4/7$
ξ_2	$-9/7$
η_2	$2/7$
ϕ_1	2
ϕ_1	1

$$U(1)_{B-L} \rightarrow Z_7.$$



Colored Dirac fermion dark matter



Colored Dirac fermion dark matter

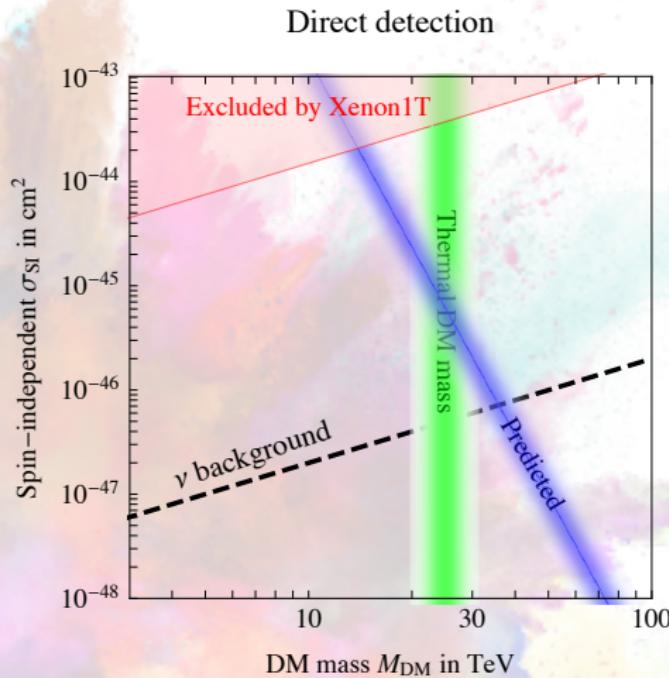
SU(3) _C = 8	
Field	U(1) _Q
\mathcal{Q}_L	r
$(\mathcal{Q}_R)^\dagger$	$-r$

$$\mathcal{Q} = \begin{pmatrix} \mathcal{Q}_L \\ \mathcal{Q}_R \end{pmatrix}$$

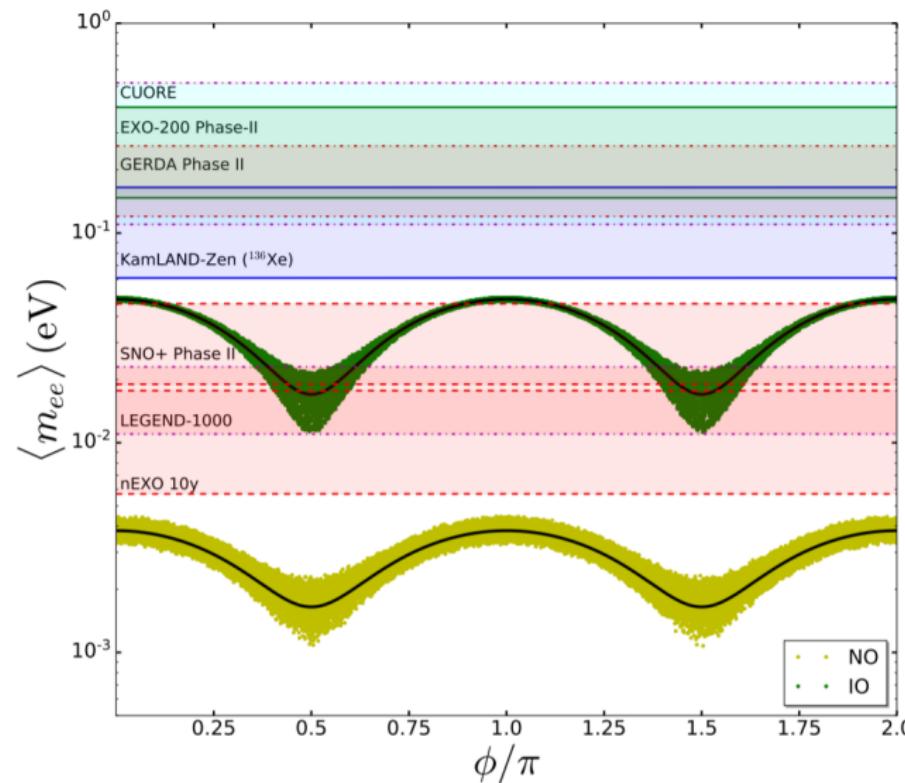
$$\mathcal{L} = i\bar{\mathcal{Q}}\gamma^\mu \mathcal{D}_\mu \mathcal{Q} - M_{\mathcal{Q}}\bar{\mathcal{Q}}\mathcal{Q}.$$

$$\chi = |\mathcal{Q}\mathcal{Q}\rangle, \quad \bar{\chi} = |\overline{\mathcal{Q}\mathcal{Q}}\rangle$$

$$M_{\text{DM}} \approx 2M_{\mathcal{Q}}$$



Dirac neutrino masses



Small Dirac neutrino masses

$$\text{SM} \times \text{U}(1)_{B-L} \xrightarrow[\langle S \rangle]{} \text{SM} + Z_N .$$

- Avoids tree-level mass (TL) term ($Y(H) = +1/2$)

$$\begin{aligned}\mathcal{L}_{\text{T.L.}} &= h_D \epsilon_{ab} (\nu_R)^\dagger L^a H^b + \text{h.c} \\ &= h_D (\nu_R)^\dagger L H + \text{h.c}\end{aligned}$$

Small Dirac neutrino masses

$$\text{SM} \times \text{U}(1)_{B-L} \xrightarrow[\langle S \rangle]{} \text{SM} + Z_N .$$

- Avoids tree-level mass (TL) term ($Y(H) = +1/2$)

$$\begin{aligned}\mathcal{L}_{\text{T.L.}} &= h_D \epsilon_{ab} (\nu_R)^\dagger L^a H^b + \text{h.c} \\ &= h_D (\nu_R)^\dagger L H + \text{h.c}\end{aligned}$$

- Forbids Majorana term: $\nu_R \nu_R$

Small Dirac neutrino masses

$$\text{SM} \times \text{U}(1)_{B-L} \xrightarrow{\langle S \rangle} \text{SM} + Z_N .$$

- Avoids tree-level mass (TL) term ($Y(H) = +1/2$)

$$\begin{aligned}\mathcal{L}_{\text{T.L.}} &= h_D \epsilon_{ab} (\nu_R)^\dagger L^a H^b + \text{h.c} \\ &= h_D (\nu_R)^\dagger L H + \text{h.c}\end{aligned}$$

- Forbids Majorana term: $\nu_R \nu_R$
- Realization of the 5-D operator which conserves **total** lepton number in $\text{SU}(3)_c \times \text{SU}(2)_L \times \text{U}(1)_Y \times \text{U}(1)_{B-L}$:

$$\mathcal{L}_{5-D} = \frac{h_\nu}{\Lambda} (\nu_R)^\dagger L H \textcolor{red}{S} + \text{h.c}$$

Small Dirac neutrino masses

$$\text{SM} \times \text{U}(1)_{B-L} \xrightarrow[\langle S \rangle]{} \text{SM} + Z_N .$$

- Avoids tree-level mass (TL) term ($Y(H) = +1/2$)

$$\begin{aligned}\mathcal{L}_{\text{T.L.}} &= h_D \epsilon_{ab} (\nu_R)^\dagger L^a H^b + \text{h.c} \\ &= h_D (\nu_R)^\dagger L H + \text{h.c}\end{aligned}$$

- Forbids Majorana term: $\nu_R \nu_R$
- Realization of the 5-D operator which conserves **total** lepton number in $\text{SU}(3)_c \times \text{SU}(2)_L \times \text{U}(1)_Y \times \text{U}(1)_{B-L}$:

$$\mathcal{L}_{5-D} = \frac{h_\nu}{\Lambda} (\nu_R)^\dagger L H \cancel{S} + \text{h.c}$$

- Prediction of extra relativistic degrees of freedom N_{eff}

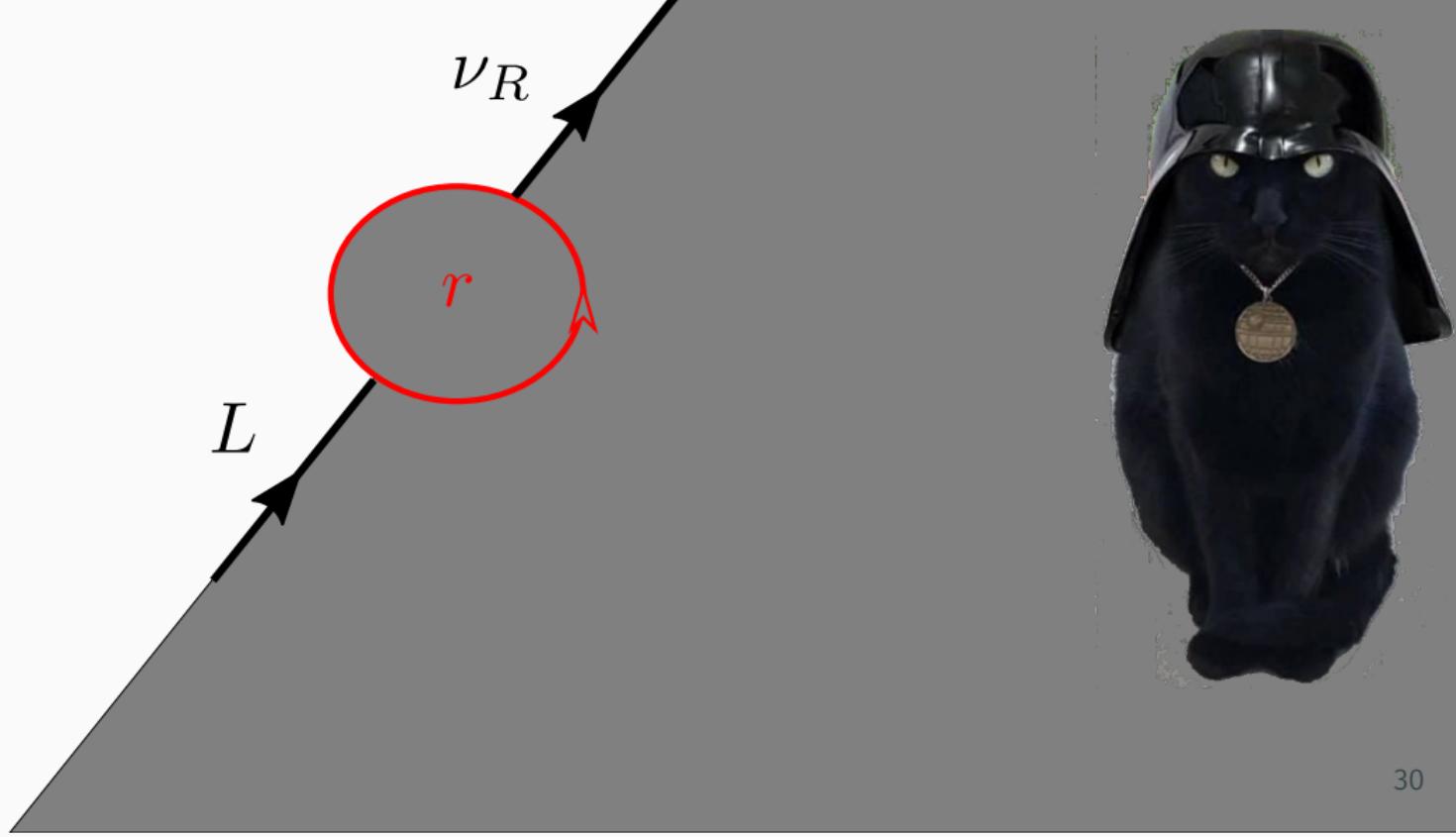
One-loop realization of \mathcal{L}_{5-D} with
total L

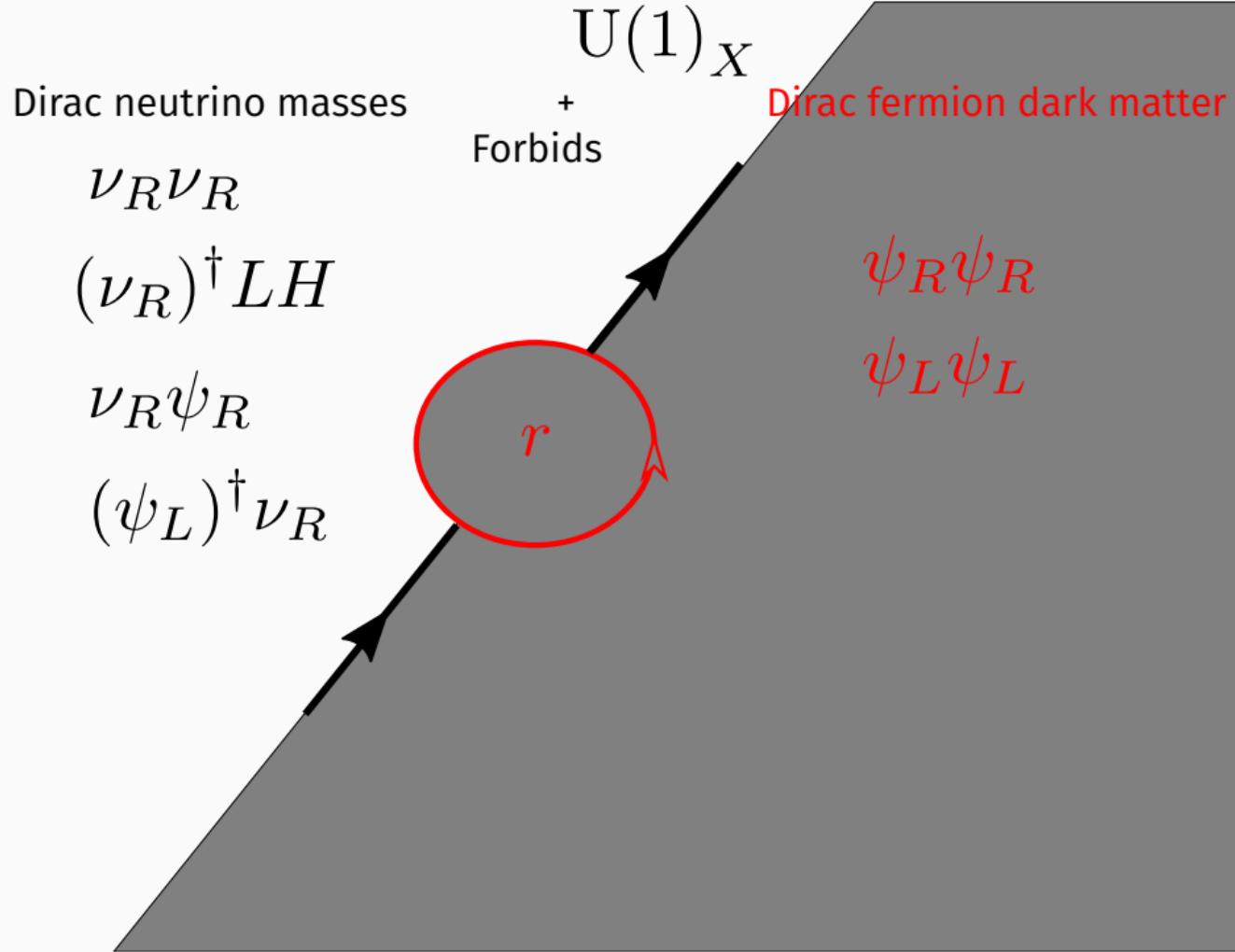
$U(1)_X$

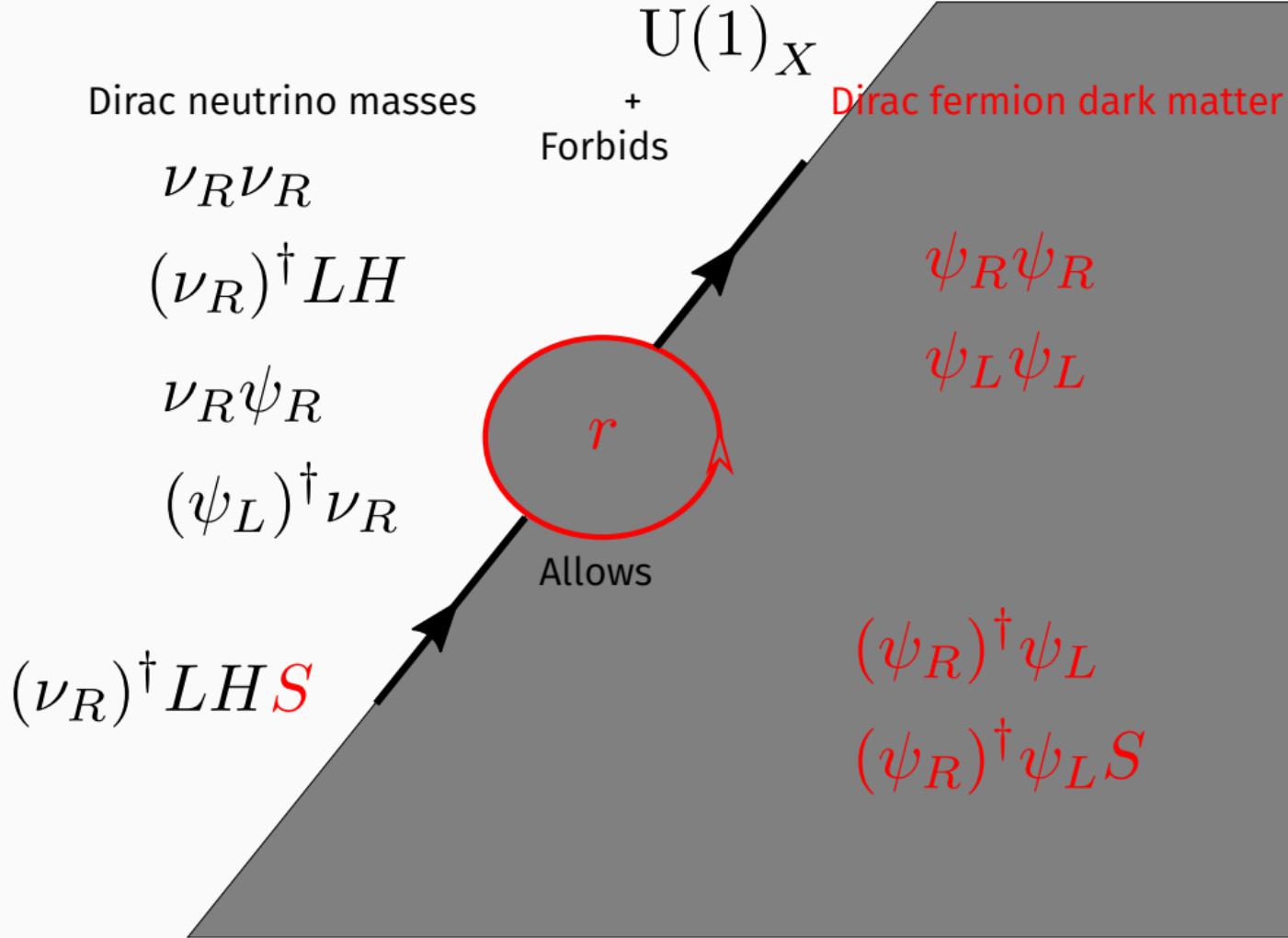
Dirac neutrino masses

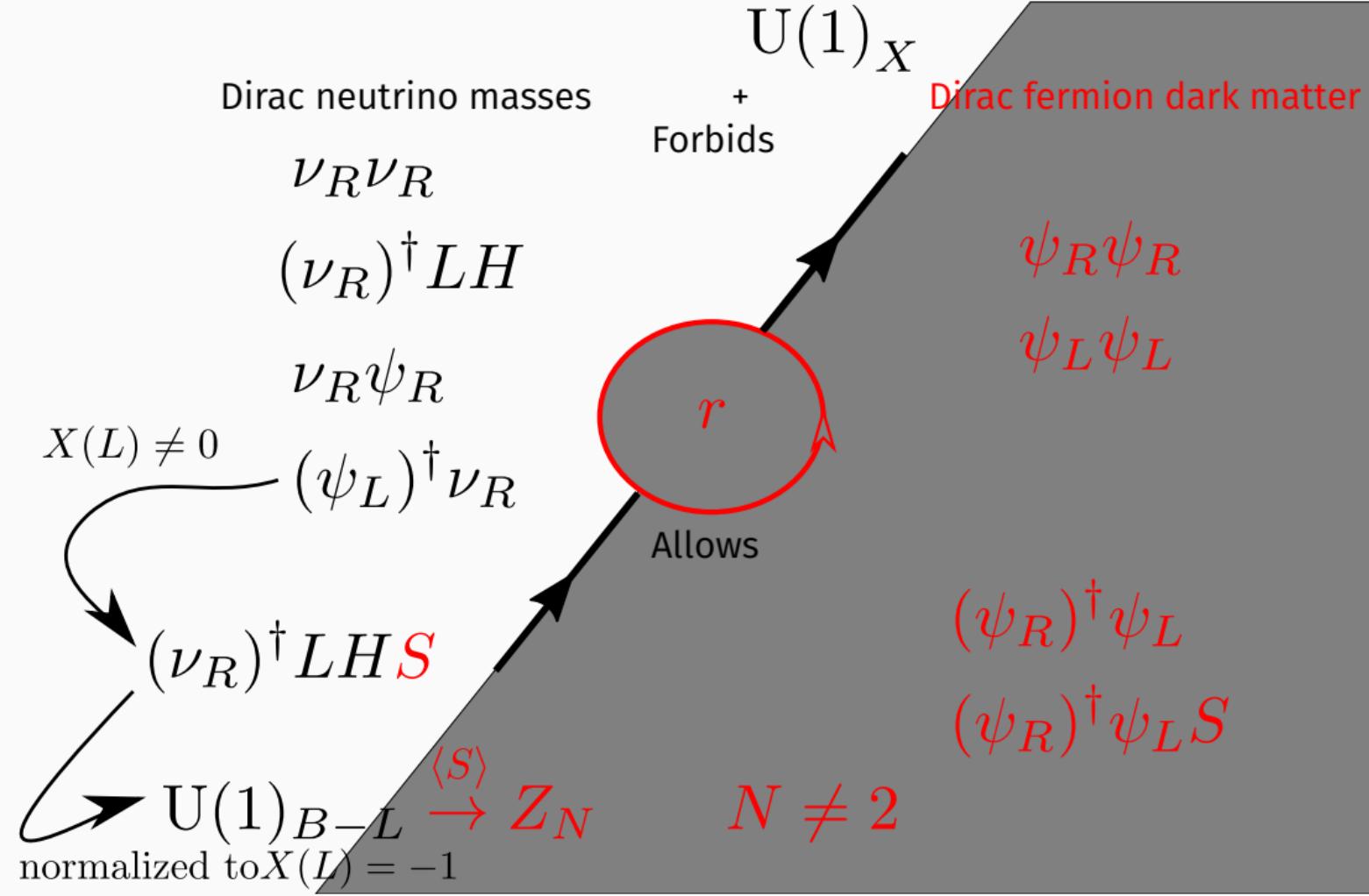
+

Dirac fermion dark matter

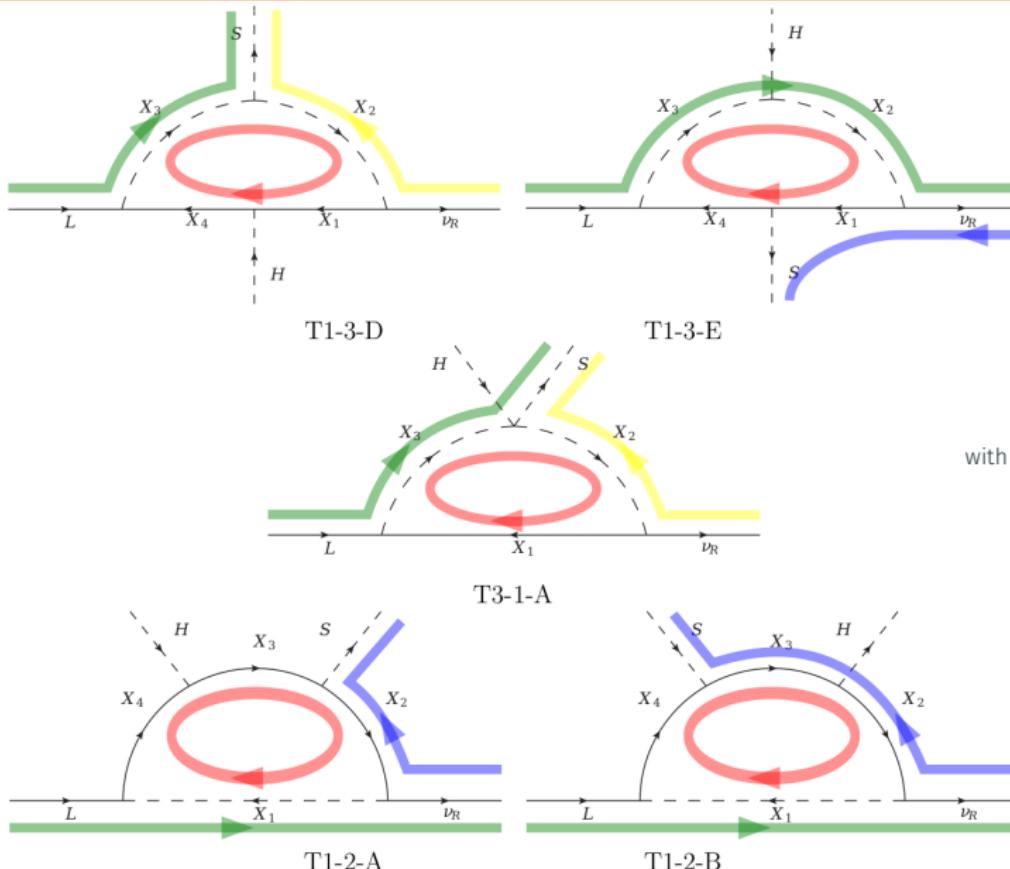




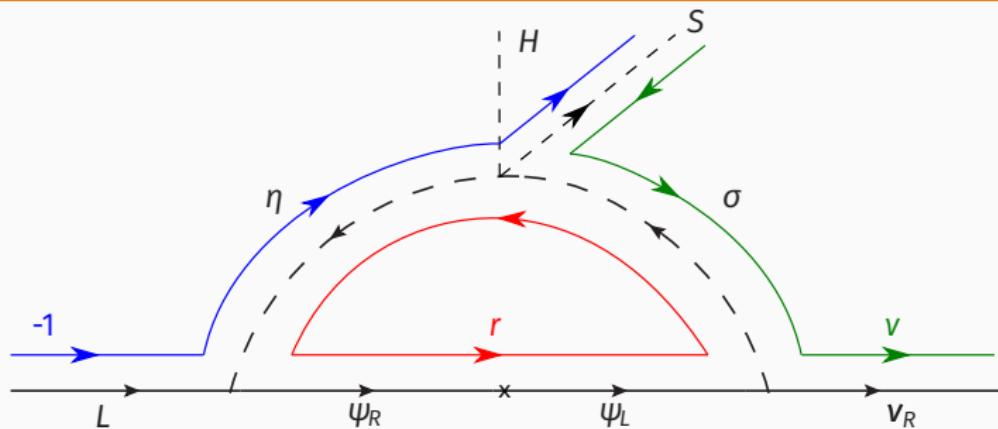




One loop topologies



with J. Calle, C. Yaguna, and O. Zapata, arXiv:1811.XXXXX

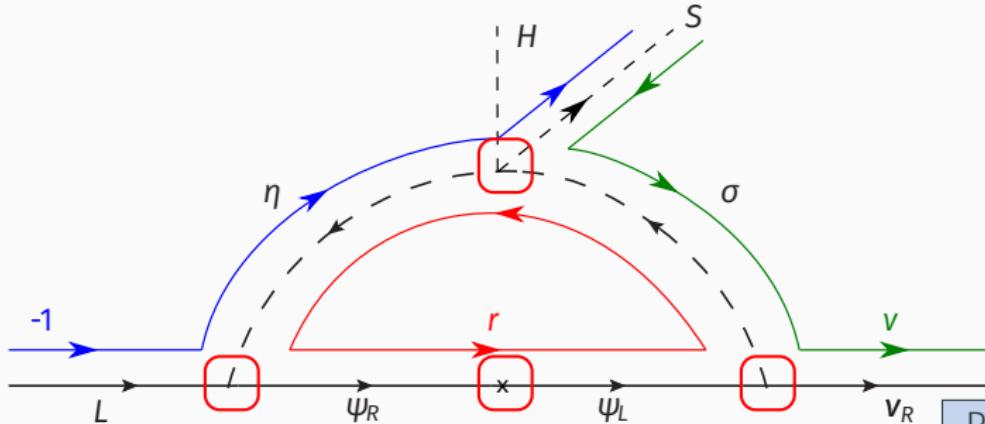


Soft breaking term induced:

$$\mathcal{L} \supset \kappa \sigma \eta^\dagger H,$$

where $\kappa = \lambda \langle S \rangle$.

Exotic $(\nu_R)^\dagger$ with $\nu \neq -1$, and vector-like Dirac fermion with $r \neq 1$



Soft breaking term induced:

$$\mathcal{L} \supset \kappa \sigma \eta^\dagger H,$$

where $\kappa = \lambda \langle S \rangle$.

$$-1 + \eta = -r$$

$$-r = -r$$

$$-r = -\nu + \sigma$$

$$\sigma = \eta + s$$

$$N_c = 1.$$

Particles	$U(1)_{B-L}$	$(SU(3)_c, SU(2)_L)_Y$
L_i	-1	$(1, 2)_{-1/2}$
H	0	$(1, 2)_{1/2}$
$(\nu_{Ri})^\dagger$	ν	$(1, 1)_0$
ψ_L	-r	$(N_c, 1)_0$
$(\psi_R)^\dagger$	r	$(N_c, 1)_0$
σ_a	$\nu - r$	$(N_c, 1)_0$
η_a	$1 - r$	$(N_c, 2)_{1/2}$
S	$\nu - 1$	$(N_c, 2)_{1/2}$

Neutrino masses and mixings

- ν_i are free parameter and could be fixed if we impose $U(1)_{B-L}$ to be local

$$r \neq 1,$$

$$\sum_i \nu_i = 3,$$

$$\sum_i \nu_i^3 = 3$$

	$(\nu_R)_1^\dagger$	$(\nu_R)_2^\dagger$	$(\nu_R)_3^\dagger$
$U(1)_{B-L}$	+4	+4	-5
$U(1)_{B-L}$	-6	$+\frac{10}{3}$	$+\frac{17}{3}$

Neutrino masses and mixings

- ν_i are free parameter and could be fixed if we impose $U(1)_{B-L}$ to be local

$$r \neq 1,$$

$$\sum_i \nu_i = 3,$$

$$\sum_i \nu_i^3 = 3$$

	$(\nu_R)_1^\dagger$	$(\nu_R)_2^\dagger$	$(\nu_R)_3^\dagger$
$U(1)_{B-L}$	+4	+4	-5
$U(1)_{B-L}$	-6	$+\frac{10}{3}$	$+\frac{17}{3}$

- To have at least a rank 2 neutrino mass matrix we need either:
 - At least two heavy Dirac fermions Ψ_a , $a = 1, 2, \dots$
 - At least two sets of scalars η_a , σ_a

Neutrino masses and mixings

- ν_i are free parameter and could be fixed if we impose $U(1)_{B-L}$ to be local

$$r \neq 1,$$

$$\sum_i \nu_i = 3,$$

$$\sum_i \nu_i^3 = 3$$

	$(\nu_R)_1^\dagger$	$(\nu_R)_2^\dagger$	$(\nu_R)_3^\dagger$
$U(1)_{B-L}$	+4	+4	-5
$U(1)_{B-L}$	-6	$+\frac{10}{3}$	$+\frac{17}{3}$

- To have at least a rank 2 neutrino mass matrix we need either:
 - At least two heavy Dirac fermions Ψ_a , $a = 1, 2, \dots$
 - **At least two sets of scalars η_a, σ_a**

Neutrino masses and mixings

- ν_i are free parameter and could be fixed if we impose $U(1)_{B-L}$ to be local

$$r \neq 1,$$

$$\sum_i \nu_i = 3,$$

$$\sum_i \nu_i^3 = 3$$

	$(\nu_R)_1^\dagger$	$(\nu_R)_2^\dagger$	$(\nu_R)_3^\dagger$
$U(1)_{B-L}$	+4	+4	-5
$U(1)_{B-L}$	-6	$+\frac{10}{3}$	$+\frac{17}{3}$

- To have at least a rank 2 neutrino mass matrix we need either:
 - At least two heavy Dirac fermions Ψ_a , $a = 1, 2, \dots$
 - **At least two sets of scalars η_a, σ_a**
-

$$\mathcal{L} \supset \left[M_\Psi (\psi_R)^\dagger \psi_L + h_i^a (\psi_R)^\dagger \tilde{\eta}_a^\dagger L_i + y_i^a \bar{\nu}_{Ri} \sigma_a^* \psi_L + \text{h.c.} \right] + \kappa^{ab} \sigma_a \eta_b^\dagger H + \dots$$

$$(\mathcal{M}_\nu)_{ij} = N_c \frac{M_\Psi}{64\pi^2} \sum_{a=1}^2 h_i^a y_j^a \frac{\sqrt{2}\kappa_{aa}\nu}{m_{S_{2R}^a}^2 - m_{S_{1R}^a}^2} \left[F\left(\frac{m_{S_{2R}^a}^2}{M_\Psi^2}\right) - F\left(\frac{m_{S_{1R}^a}^2}{M_\Psi^2}\right) \right] + (R \rightarrow I) \quad (1)$$

where $F(m_{S_\beta}^2/M_\Psi^2) = m_{S_\beta}^2 \log(m_{S_\beta}^2/M_\Psi^2)/(m_{S_\beta}^2 - M_\Psi^2)$. The four CP-even mass eigenstates are denoted as $S_{1R}^1, S_{2R}^1, S_{1R}^2, S_{2R}^2$, with a similar notation for the CP-odd ones.

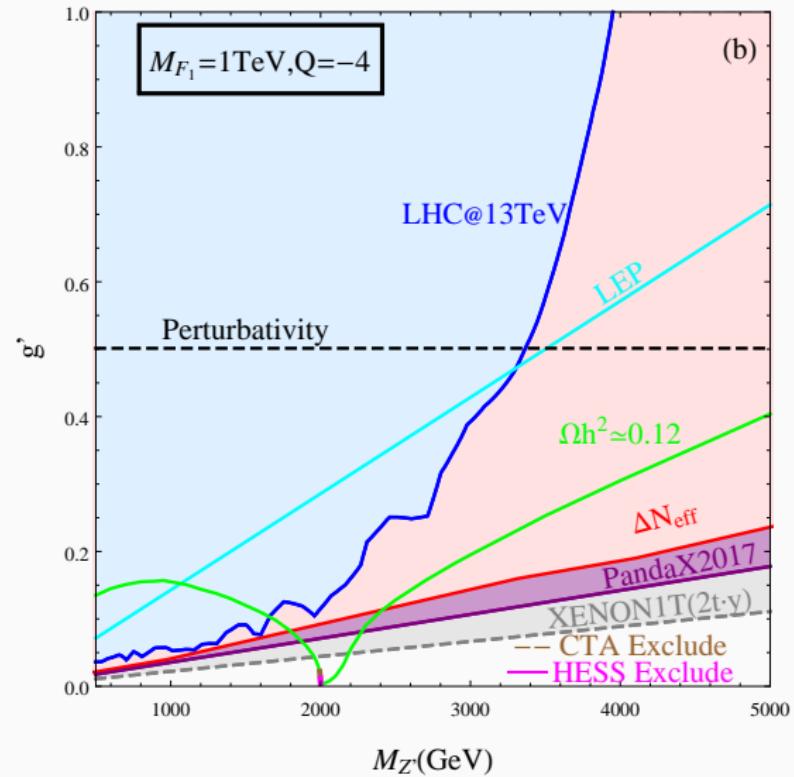
T3-1-A with only $U(1)_{B-L}$

Field	$U(1)_{B-L}$
$(\nu_{R_i})^\dagger$	+4
$(\nu_{R_j})^\dagger$	+4
$(\nu_{R_k})^\dagger$	-5
ψ_L	-r
$(\psi_R)^\dagger$	r
η_a	r-4
σ_a	r-1
S	-3

$a = 1, 2, i \neq j \neq k$.

$m = 0$: ν_{L_k} , and $\nu_{R_k} \rightarrow N_{\text{eff}}$

$$F_1 = \begin{pmatrix} \psi_L \\ \psi_R \end{pmatrix}$$



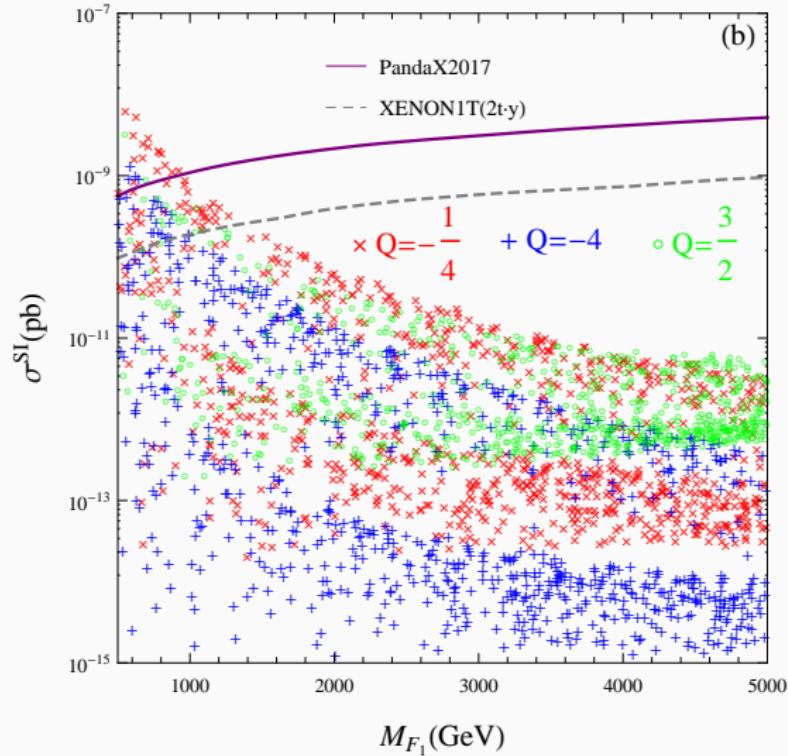
T3-1-A with only $U(1)_{B-L}$

Field	$U(1)_{B-L}$
$(\nu_{R_i})^\dagger$	+4
$(\nu_{R_j})^\dagger$	+4
$(\nu_{R_k})^\dagger$	-5
ψ_L	$-r$
$(\psi_R)^\dagger$	r
η_a	$r-4$
σ_a	$r-1$
S	-3

$a = 1, 2, i \neq j \neq k.$

$m = 0: \nu_{L_k}, \text{ and } \nu_{R_k} \rightarrow N_{\text{eff}}$

$$F_1 = \begin{pmatrix} \psi_L \\ \psi_R \end{pmatrix}$$



Extra Z_2 : Han, Wang, 1808.03352 [EJPC]

Conclusions

Only gravitational evidence of dark matter so far which is fully compatible with the Λ CDM-paradigm without simulation problems (~~-cusps vs core, etc~~)

Not convincing signal at all

- ~~Galactic center excess~~
- ~~KeV lines~~
- ~~Positron excess~~
- ~~DAMA oscillation signal~~

Direct detection and LHC null results suggest to look

- Other (CDM) windows (Axion, FIMP, SIMP, ...)
- Non-standard cosmology
- Other portals ...

Z'-portal: A single $U(1)$ symmetry to explain both the smallness of Dirac neutrino masses and the stability of Dirac fermion dark matter

Thanks!