

# The Structure of Something Strange

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# Why Hadrons?

## Difficult to describe

- Spin
- Mass
- Size
- **Structure ← Our focus**

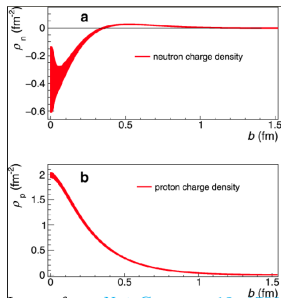
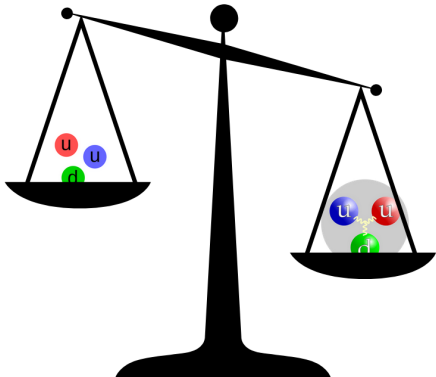


Image from [Nat Commun 12, 1759 \(2021\)](#).

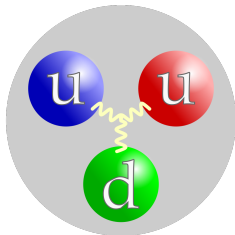
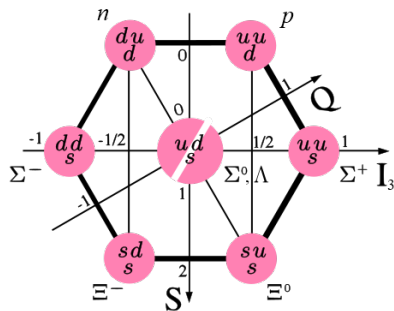


Image credit: [Jacek Rybak](#)

## Hyperons: What are they and why study them?

- Baryons with strangeness  $\geq 1$
- Complementary to nucleons, relatively unexplored



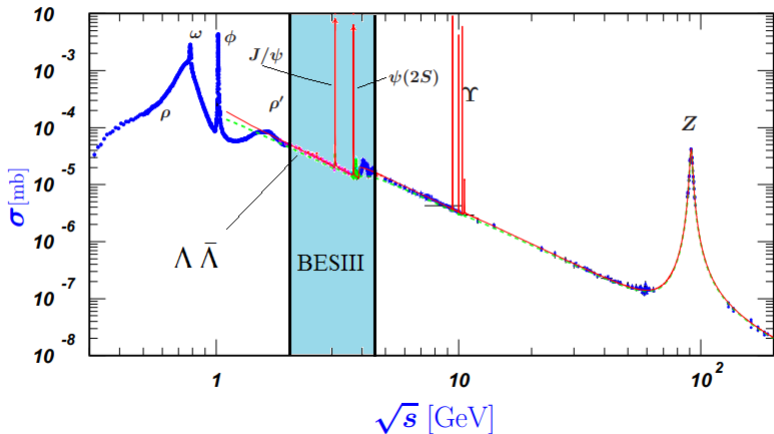
| Hyperon    | Mass [GeV/c <sup>2</sup> ] | Decay (BF)   |
|------------|----------------------------|--|
| $\Lambda$  | 1.116                      | $p\pi^-$ (63.9%)<br>$n\pi^0$ (35.8%)                                 |
| $\Sigma^-$ | 1.197                      | $n\pi^-$ (99.8%)   |
| $\Sigma^+$ | 1.189                      | $p\pi^0$ (51.6%)<br>$n\pi^+$ (48.3%)                                 |
| $\Xi^0$    | 1.315                      | $\Lambda\pi^0$ (99.5%)   |
| $\Xi^-$    | 1.321                      | $\Lambda\pi^-$ (99.8%)   |
| $\Omega$   | 1.672                      | $\Lambda K^-$ (67.8%)<br>$\Xi^0\pi^-$ (23.6%)<br>$\Xi^-\pi^0$ (8.6%) |

+  $\Omega^- (sss)$  Spin 3/2

### $\Lambda$ Hyperon:

- Two dominating decay modes:  $\Lambda \rightarrow p\pi$  (63.9%) and  $\rightarrow n\pi^0$  (35.8%)
- Decays weakly  $\rightarrow$  long-lived. Travels measurable distance before decaying.

$e^+e^- \rightarrow$  Hyperons



Two possible approaches for studying energy-dependent phenomena:

- Initial state radiation (ISR)
- Energy scan ← **Chosen here**

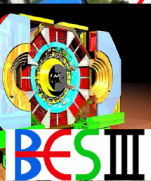
# Beijing Electron-Positron Collider (BEPCII)

CMS Energy: 2-4.95 GeV

Design luminosity:  $10^{33} \text{ cm}^{-2} \text{ s}^{-1}$

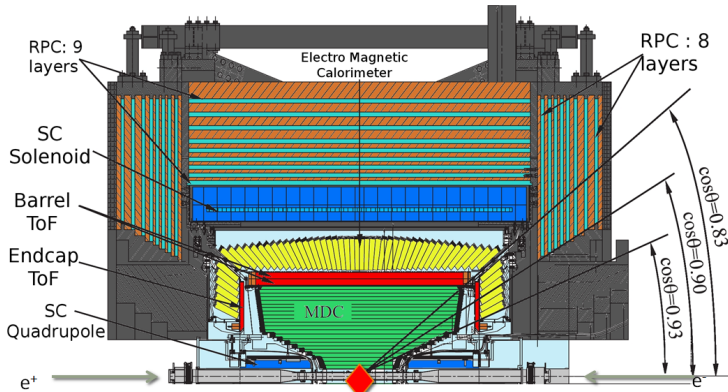
Linac

BEPCII



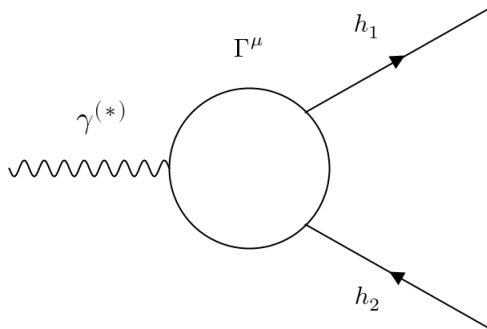
# Beijing Spectrometer (BESIII)

- Near  $4\pi$  coverage
- Helium-gas drift chamber
- CsI(Tl) crystal calorimeter
- Plastic scintillator TOF-system
- 1 T super-conducting solenoid
- RPC-based muon chamber



# Electromagnetic Form Factors

- Depends on complex internal structure
- Form factors quantify deviation from pointlike nature
- Scalar functions of momentum transfer  $q^2$
- Elastic/transition ( $h_1 = h_2/h_1 \neq h_2$ )
- Spacelike/Timelike ( $q^2 < 0/q^2 > 0$ )



# Electromagnetic Form Factors of Hyperons

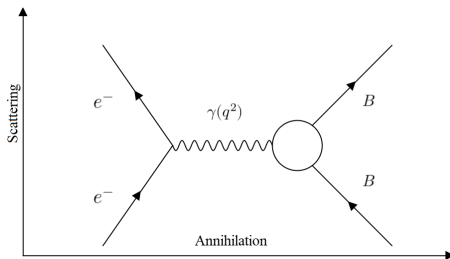
**Spin 1/2:** Two independent form factors  $G_E$ ,  $G_M$

**SL FFs** ( $q^2 < 0$ )

- Can be studied in elastic lepton scattering  
**Hyperons are unstable**  
→ **Difficult!**
- Real-valued functions of  $q^2$ .

**TL FFs** ( $q^2 > 0$ )

- Can be studied in lepton-antilepton annihilation  
**Hyperon FFs experimentally accessible!**
- Complex functions of  $q^2$ :  
 $G_M(q^2) = |G_M(q^2)|e^{i\Phi_M}$   
 $G_E(q^2) = |G_E(q^2)|e^{i\Phi_E}$
- Observables  $R = |G_E/G_M|$ ,  
 $\Delta\Phi = \Phi_E - \Phi_M$





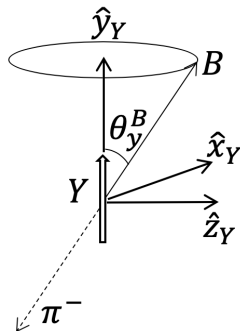
## What is the significance of $\Delta\Phi$ ?

- SL and TL FFs related by dispersion relations.
  - As  $|q^2| \rightarrow \infty$ : **SL**  $\rightarrow$  **TL**  $\implies \Delta\Phi = n \cdot \pi$
  - Oscillations of  $\Delta\Phi$  reveal zero-crossings  
Phys. Rev. D 104, 116016 (2021)
- Provides constraints for unmeasurable SL FFs

## How to measure it?

- If  $\sin \Delta\Phi \neq 0$   $B/\bar{B}$  can be polarized
- Experimental access to polarization in self-analyzing weak decays of hyperons!
- Utilized by BESIII to measure the  $\Lambda$  FFs

Phys. Rev. Lett. **123** (2019) 12, 122003



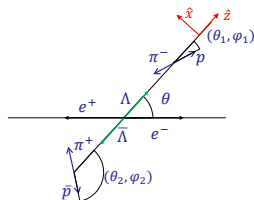
**Next step:** What is the  $q^2$  dependence of  $\Delta\Phi$ ?

**We look at**  $e^+e^- \rightarrow \Lambda\bar{\Lambda}, \Lambda/\bar{\Lambda} \rightarrow p\pi$

# Formalism for the Process $e^+e^- \rightarrow \Lambda\bar{\Lambda} \rightarrow p\pi^-\bar{p}\pi^+$

Full reaction described by:  $\xi = (\theta, \theta_1, \phi_1, \theta_2, \phi_2) = (\theta, \Omega_1, \Omega_2)$

Fäldt, Kupsc, Phys.Lett.B 772 (2017) 16-20



$$d\Gamma \propto \mathcal{W}(\xi) = \mathcal{F}_0(\xi) + \eta \mathcal{F}_5(\xi)$$

$$- \alpha_{\Lambda}^2 \left( \mathcal{F}_1(\xi) + \sqrt{1 - \eta^2} \cos(\Delta\Phi) \mathcal{F}_2(\xi) + \eta \mathcal{F}_6(\xi) \right)$$

Spin correlations

$$+ \alpha_{\Lambda} \sqrt{1 - \eta^2} \sin(\Delta\Phi) (\mathcal{F}_3(\xi) - \mathcal{F}_4(\xi))$$

Polarization

- $\mathcal{F}_i$  are known functions of the angles
- R can be extracted as  $R = \sqrt{\tau} \sqrt{\frac{1-\eta}{1+\eta}}$ ,  $\tau = \frac{q^2}{4m_{\Lambda}^2}$
- $\alpha_{\Lambda}$ :  $\Lambda$  decay asymmetry parameter  $\leftarrow$  **CP-tests** e.g. BESIII, Nature 606, 64–69 (2022)

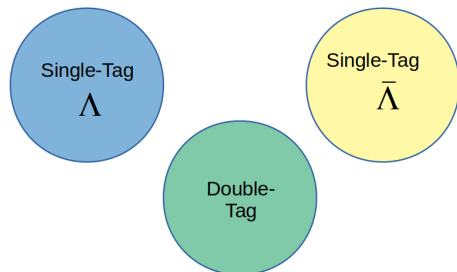
When only  $\Lambda/\bar{\Lambda}$  is measured two angles  $\xi = (\theta, \theta_p)$  are sufficient.

$$\mathcal{W}_{\Lambda/\bar{\Lambda}}(\xi) = 1 + \eta \cos^2 \theta + \alpha_{\Lambda/\bar{\Lambda}} \sqrt{1 - \eta^2} \sin(\Delta\Phi) \sin \theta \cos \theta \cos \theta_p$$

Polarization

Two possible ways of selecting  $e^+e^- \rightarrow \Lambda\bar{\Lambda}$  events:

- Double-Tag: Reconstruct **both**  $\Lambda$  and  $\bar{\Lambda}$
- Single-Tag: Reconstruct **either**  $\Lambda$  or  $\bar{\Lambda}$



| $E_{cm}$ [GeV] | $\mathcal{L}$ [ $\text{pb}^{-1}$ ] |
|----------------|------------------------------------|
| 2.3864         | $22.59 \pm 0.01 \pm 0.17$          |
| 2.3960         | $66.89 \pm 0.02 \pm 0.46$          |
| 2.6444         | $33.65 \pm 0.01 \pm 0.21$          |
| 2.6464         | $34.06 \pm 0.01 \pm 0.28$          |
| 2.9000         | $105.53 \pm 0.03 \pm 0.90$         |
| 3.0800         | $126.21 \pm 0.03 \pm 0.90$         |

Three statistically independent samples at each energy.

Combine to determine:

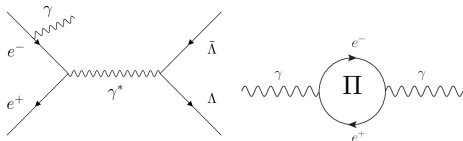
- $\sigma_{Born}$  as inverse-variance weighted mean
- $R$ ,  $\Delta\Phi$  through simultaneous fit

Data at 2.396 GeV used to illustrate event selection procedure

# Determination of the Born Cross Section

To determine  $\sigma_{Born}$ , correct for

- Initial state radiation (ISR)
- Vacuum polarization (VP)



$$\sigma_{obs.} = \frac{N}{\mathcal{L}\mathcal{B}(\Lambda \rightarrow p\pi^-) [\epsilon_1\mathcal{B}(\Lambda \rightarrow p\pi^-) + \epsilon_2\mathcal{B}(\Lambda \rightarrow n\pi^0)]}$$

$$\sigma_{Born} = \frac{\sigma_{obs.}}{(1 + \delta)_{ISR+VP}}$$

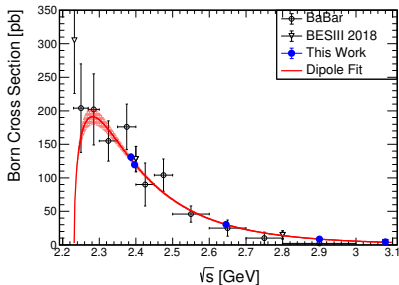
Need energy dependence of Born cross section to estimate correction factor.

**Dipole approximation:**

$$\sigma_{Born}(q^2) = \frac{1}{q^2} \frac{c_0 \cdot \beta}{(q^2 - c_1^2)^4},$$

$c_1 = 1.77 \pm 0.01$  GeV indicates mix of  $\phi(1680)$  and  $\phi(2170)$  in line with Chin. Phys.

Lett. 39 011201



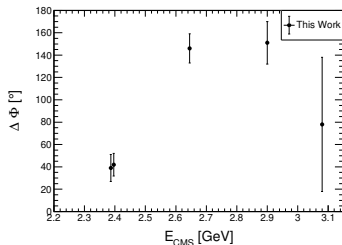
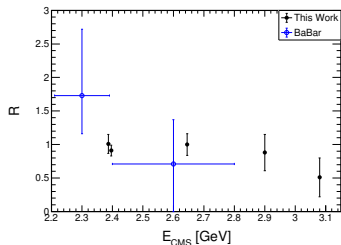
# Form Factor Measurement

Parameters  $R$ ,  $\Delta\Phi$  determined by unbinned MLL fit.

$\Lambda$  decay asymmetry parameter fixed  $\alpha_\Lambda = 0.754$  (BESIII, Nature Phys. 15 (2019) 631)

$$-\ln \mathcal{L} = -\sum_{i=1}^N \ln \frac{\mathcal{W}(\xi_i; \eta, \Delta\Phi)}{\mathcal{N}(\eta, \Delta\Phi)} - \sum_{i=1}^N \ln \epsilon(\xi_i), \quad \mathcal{N}(\eta, \Delta\Phi) = \int \mathcal{W}(\xi; \eta, \Delta\Phi) \epsilon(\xi) d\xi$$
$$-\ln \mathcal{L}_{tot.} = -\ln \mathcal{L}_{\Lambda\bar{\Lambda}} - \ln \mathcal{L}_{\bar{\Lambda}} - \ln \mathcal{L}_{\Lambda}$$

## Results:



Note that  $\Delta\Phi$  moves from first to second quadrant between 2.396 and 2.64 GeV!

## What has been done:

- Combination of full and partial reconstruction
- $R$ ,  $\Delta\Phi$ ,  $\sigma_{Born}$  measured at five energies from 2.3864 GeV to 3.08 GeV
  - First measurement of energy dependence of  $\Delta\Phi$

## To be done:

- Study unexpected behavior of  $\Delta\Phi$ 
  - Related to method/size of data samples?
  - If true, due to resonance, rescattering?
- Interpretation of result in terms of  $\Lambda$  charge radius  
Phys. Rev. D 104, 116016
- Cross section measurement at additional data points.