



A new channel for supermassive black hole formation

Carlos R. Argüelles

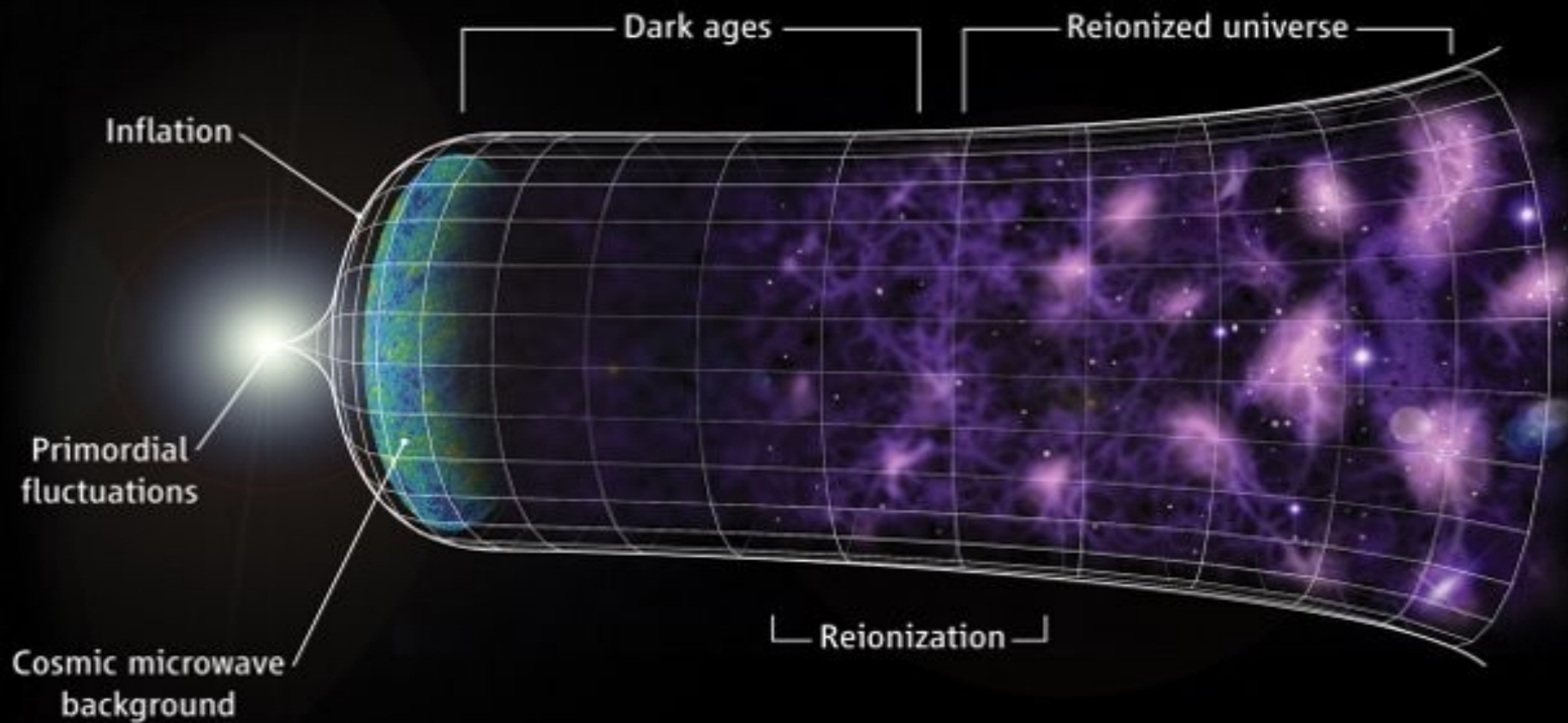
Collaborators: R. Ruffini, J. A. Rueda, A. Krut, E. A. Becerra-Vergara, M. Díaz, R. Yunis, M. Mestre, V. Crespi, K. Boshkayev, J. Uribe-Suárez, P.-H. Chavanis

- **Cosmology 2023 in Miramare– August 28-September 2, SISSA, Italy**

- **BASED ON: Argüelles, Boshkayev, Krut, et al. MNRAS (2023) [arXiv:2305.02430](#)**

Argüelles et al. PDU (2018,2019) [arXiv:1606.07040](#); [arXiv:1810.00405](#) & MNRAS (2021) [2012.11709](#)

Becerra-Vergara, Argüelles, et al. A&A (2020) [arXiv:2007.11478](#) & MNRAS Lett (2021) [2105.06301](#)



DM halo formation from a statistical mechanics approach

DM halo formation: collisionless relaxation & coarse-grained Entropy maximum

- DM as a collisionless particle system described by a mean-field **Vlasov-Poisson** equation

$$f = f(\mathbf{x}, \mathbf{v}, t) \quad \text{mass density of particles in phase-space } (\mathbf{x}, \mathbf{v})$$

$$\bar{f}: \text{coarse-grained}; \tilde{f}: \text{fine-grained fluctuations}$$

$$\frac{df}{dt} \equiv \frac{\partial f}{\partial t} + \mathbf{v} \frac{\partial f}{\partial \mathbf{r}} + \mathbf{F} \frac{\partial f}{\partial \mathbf{v}} = 0, \quad \longrightarrow \quad \frac{\partial \bar{f}}{\partial t} + \mathbf{v} \frac{\partial \bar{f}}{\partial \mathbf{r}} + \bar{\mathbf{F}} \frac{\partial \bar{f}}{\partial \mathbf{v}} = - \frac{\partial \mathbf{J}}{\partial \mathbf{v}} \quad (1)$$

$$\Delta \Phi = 4\pi G n, \quad n(\mathbf{r}, t) = \int f(\mathbf{r}, \mathbf{v}, t) d^3 \mathbf{v}$$

- $f = \bar{f} + \tilde{f}$
- Take local average of V-P

$$\mathbf{J} = \tilde{f} \bar{\mathbf{F}}$$

$$\mathbf{F} = -\nabla \Phi$$

Diffusion current

Maximum Entropy production

Ple. Chavanis, MNRAS (1998)

Chavanis, (2006)

$$\dot{S} \geq 0$$

$$\xrightarrow{\text{J=cte}} \bar{f} = \eta_0 \frac{1 - e^{\beta(\epsilon - \epsilon_m)}}{1 + e^{\beta\epsilon + \alpha}}$$

stationary solution of Fermi-Dirac type including for evaporation: generalization of Lynden-Bell DF

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$$\Delta \Phi = 4\pi G n, \quad n(\mathbf{r}, t) = \int f(\mathbf{r}, \mathbf{v}, t) d^3 \mathbf{v}$$

- 1) $f = \bar{f} + \tilde{f}$
 2) Take local average of V-P

$$\mathbf{J} = \overline{\tilde{f} \tilde{\mathbf{F}}}$$

$$\mathbf{F} = -\nabla \Phi$$

Diffusion current

- For **fermions**, the maximum accessible value of the DF is fixed by the **Pauli principle**

$$\eta_0 = gm^4 / h^3$$

DM halos as equilibrium systems of self-gravitating fermions

- **Fermions** under self-gravity DO ADMIT a **perfect fluid approximation**
Ruffini & Bonazzola, Phys. Rev. (1969) - by solving Einstein Dirac equations -
- We solve Einstein equilibrium equations for Fermi Gas at finite T in hydrostatic equilibrium (i.e. **T.O.V**), in spherical symmetry Argüelles, Krut, Rueda, Ruffini, PDU (2018)

$$\rho(r) = m \frac{2}{h^3} \int f(r, p) \left[1 + \frac{\epsilon(p)}{mc^2} \right] d^3 p,$$

$$P(r) = \frac{1}{3} \frac{2}{h^3} \int f(r, p) \left[1 + \frac{\epsilon(p)}{mc^2} \right]^{-1} \left[1 + \frac{\epsilon(p)}{2mc^2} \right] \epsilon d^3 p.$$

$$f(r, p) = \begin{cases} \frac{1 - e^{(\epsilon - \epsilon_c)/kT}}{e^{(\epsilon - \mu)/kT} + 1}, & \epsilon \leq \epsilon_c \\ 0, & \epsilon > \epsilon_c \end{cases}$$

$$\epsilon(p) = \sqrt{c^2 p^2 + m^2 c^4} - mc^2$$

4 free parameters

$$m, \beta = kT/mc^2, \theta = \mu/kT \text{ and } W = \epsilon_c/kT$$

$$\frac{d\hat{M}}{d\hat{r}} = 4\pi\hat{r}^2\hat{\rho}$$

$$\frac{dv}{d\hat{r}} = \frac{2(\hat{M} + 4\pi\hat{P}\hat{r}^3)}{\hat{r}^2(1 - 2\hat{M}/\hat{r})} \quad \longrightarrow \text{T.O.V}$$

$$\frac{d\theta}{d\hat{r}} = -\frac{1 - \beta_0(\theta - \theta_0)}{\beta_0} \frac{1}{2} \frac{dv}{d\hat{r}} \quad \longrightarrow \text{KLEIN}$$

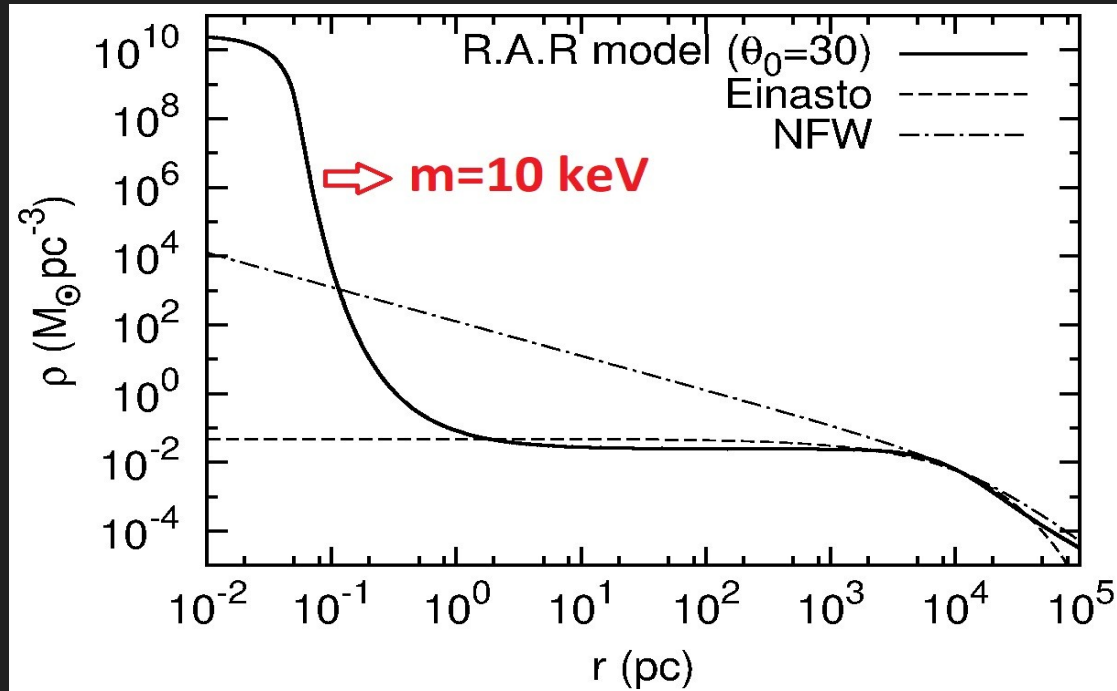
$$\beta(\hat{r}) = \beta_0 e^{\frac{\nu_0 - \nu(\hat{r})}{2}} \quad \longrightarrow \text{TOLMAN}$$

$$W(\hat{r}) = W_0 + \theta(\hat{r}) - \theta_0 \quad \longrightarrow \text{E conserv.}$$

$$M(0) = 0; \quad \nu_0 = 0; \quad \theta(0) = \theta_0 > 0; \quad \beta(0) = \beta_0; \quad W(0) = W_0$$

A novel "core – halo" Dark Matter profile for fermions

- The highly non-linear system of coupled ODE is solved fulfilling a **boundary condition problem in agreement with halo observables** Ruffini, Argüelles, Rueda, MNRAS (2015)



Example: Typical spiral halo

$R_h \sim 10^4 \text{ pc}$

$M_h \sim 10^{11} M_{\odot}$

The dense central core fulfills the 'quantum condition' :

$(\lambda_B > 3/l_c)$ satisfied for $\theta_0 > 10$

DM profiles **depend** on the **particle mass** (see next slides)

Thermodynamics of self-gravitating fermions: Stability

How do we obtain realistic DM halos in cosmology via this method ?

- One should **i) calculate** the power spectrum $P(k)$ in a given ($\sim 10^1$ keV) cosmology (CLASS)
- ii) apply the Press-Schechter formalism** to obtain $M_{\text{vir}} = M(R_{\text{vir}})$ at given z_{vir} ;

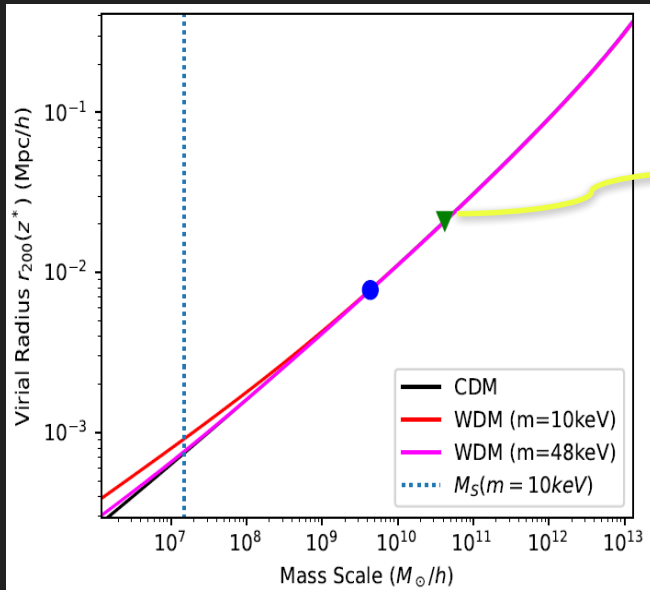
Mass variance \longrightarrow

$$\sigma^2(M) = \frac{1}{2\pi^2} \int_0^\infty P(k) W^2(k, R) k^2 dk$$

Window *top-hat* function

$$\sigma(M^*) = \delta_c(t)$$

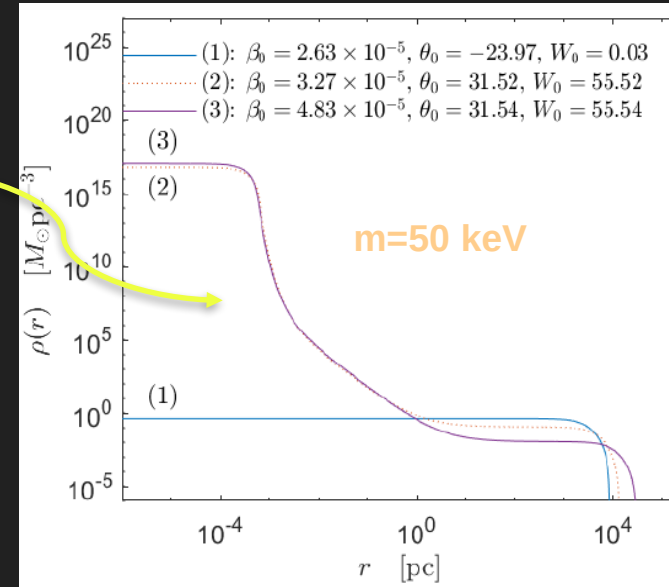
Critical overdensity (spherical collapse)



$$M_{\text{vir}} = 5.4 \times 10^{10} M_\odot$$

iii) Use the stable family of solutions obtained at violent relaxation (i.e. valid at z_{vir}), **in agreement with above virial constraints**

Argüelles et al. MNRAS (2021)



Turning point instability & last stable configuration

- Historically, the gravitational collapse of a degenerate (and relativistic) `star' was understood in terms of the onset of a thermodynamic instability at a Turning-Point (TP), e.g. at $dM/d\rho_0 = 0$
- However TPs don't provide a necessary condition for thermodynamic instability: the onset of instability can occur prior to the TP (or even without its existence) [Schiffrin & Wald \(2014\)](#)

For our case we have:

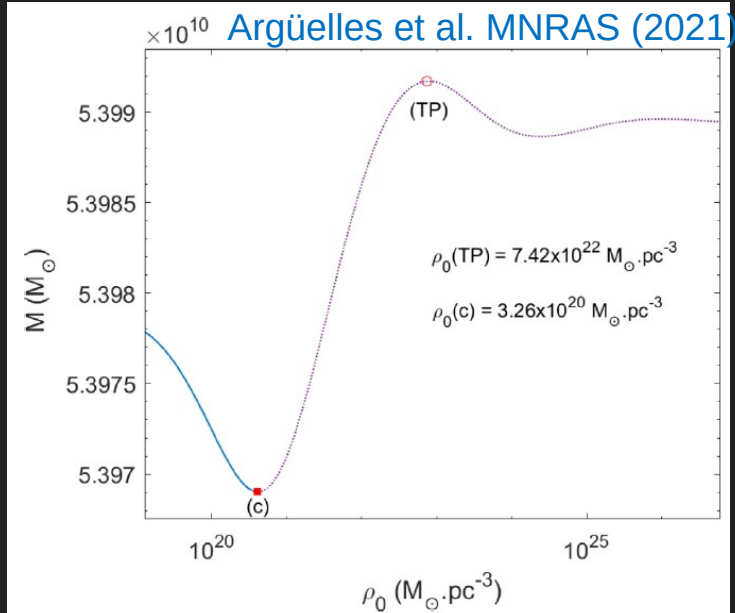
Turning point instabilities for relativistic stars and black holes

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Abstract

In the light of recent results relating dynamic and thermodynamic stability of relativistic stars and black holes, we re-examine the relationship between 'turning points'—i.e., extrema of thermodynamic variables along a 1-parameter family of solutions—and instabilities. We give a proof of Sorkin's general result—showing the existence of a thermodynamic instability on one side of a turning point—that does not rely on heuristic arguments involving infinite-dimensional manifold structure. We use the turning point results to prove the



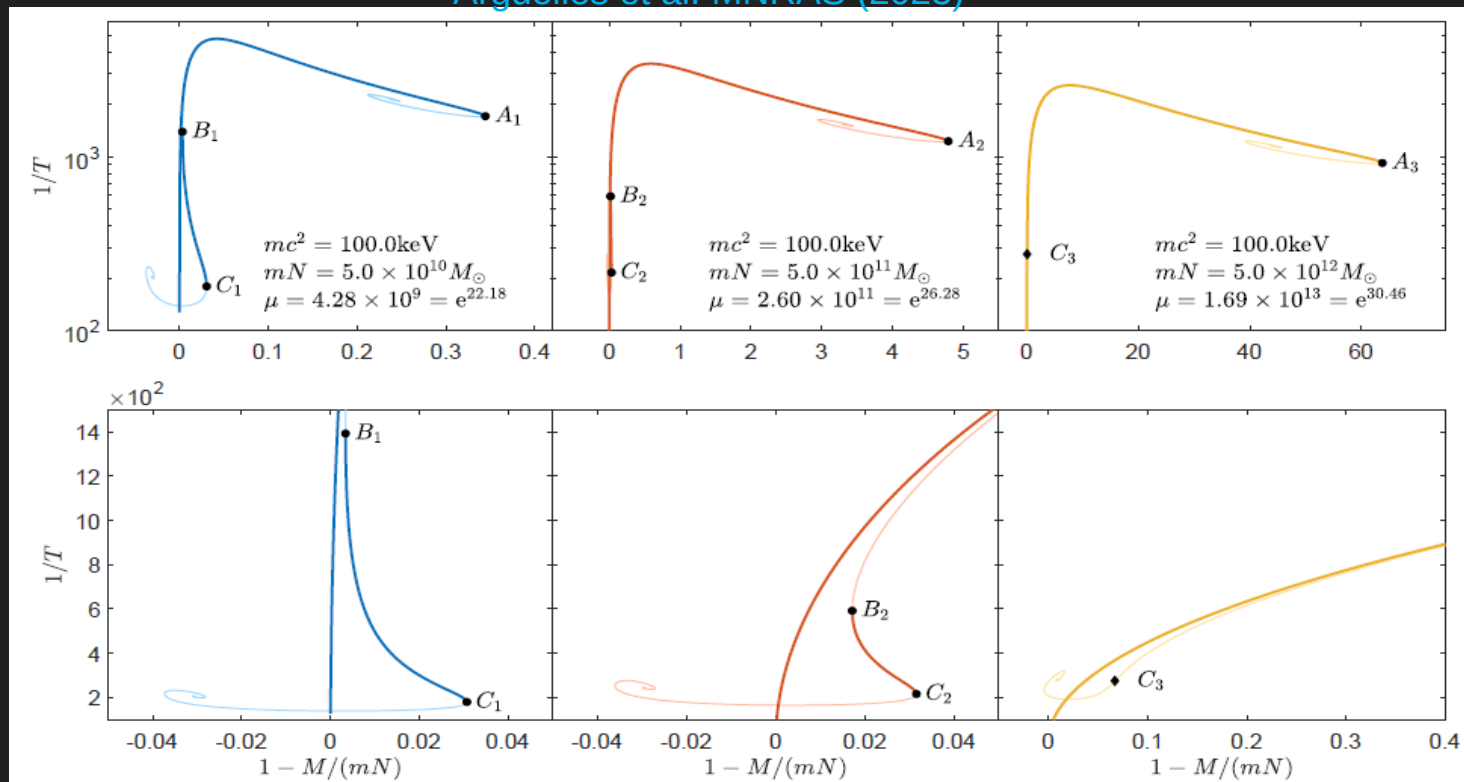
Phenomenology I: A new channel for SMBH formation

Stability analysis of fermionic halos in GR: $M_{\text{vir}} = 5 \times 10^{10} - 5 \times 10^{12} M_{\odot}$

Critical solutions (at C_i) fulfill with the boundary conditions from Cosmology at halo-formation ($M_{\text{vir}}; r_s$)

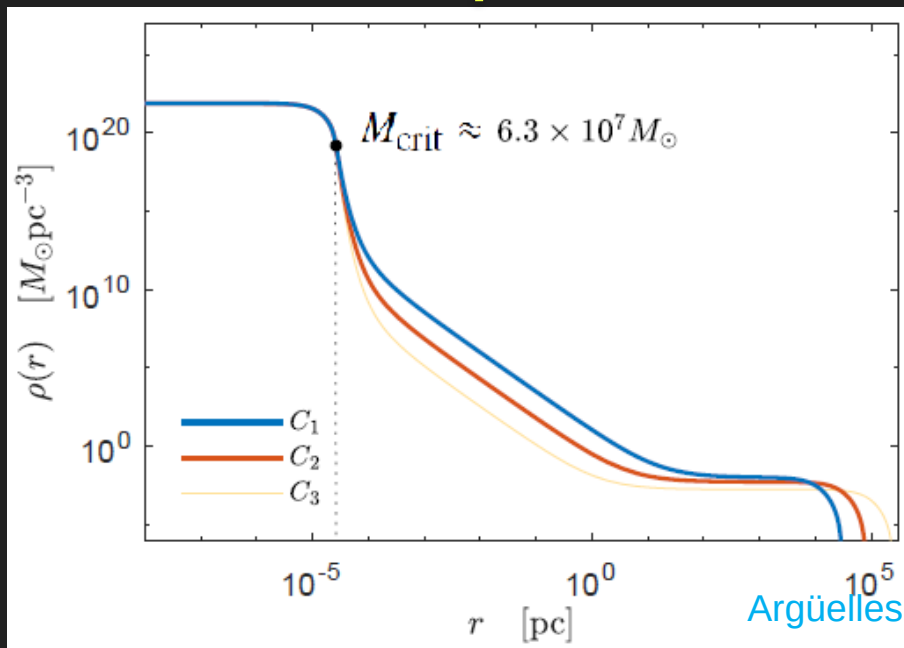
Stable Branch core-halo solutions correspond to B-C (The larger M the shorter the stable-branch up to M^*)

Argüelles et al. MNRAS (2023)

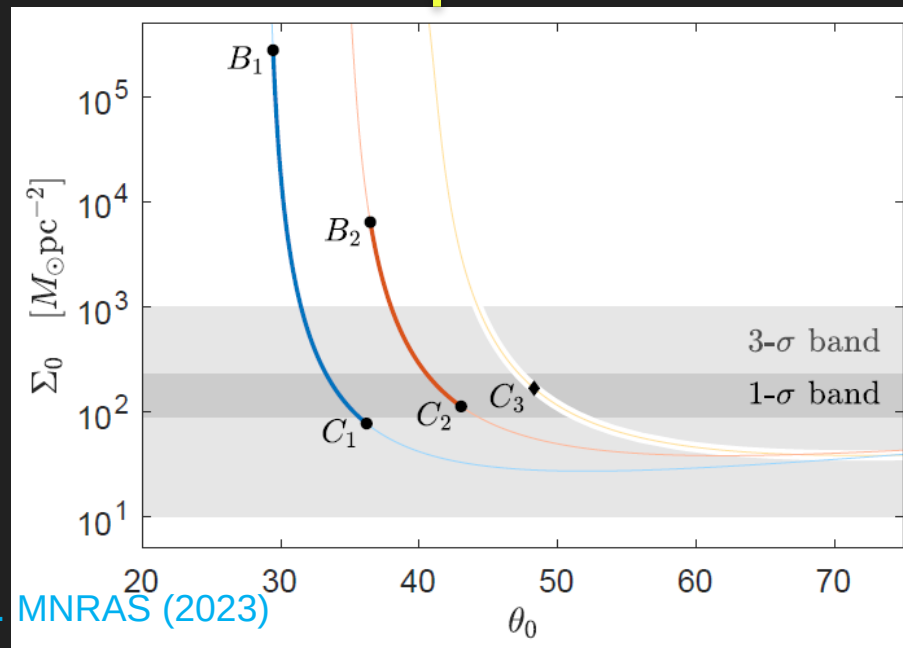


It does exist solutions of Einstein equations for self-gravitating systems of (neutral) fermions which gives hints to: (i) the mass of the DM particles; (ii) the formation of SMBH at the center of active galaxies; (iii) the phenomenology and stability of DM halos

Critical solutions (at C_i) fulfill with the boundary conditions at halo-formation (M_{vir} ; r_s)



Critical solutions fulfilling with the observational DM-Surface-density relation, $\Sigma_0 \propto \rho_o r_o = 190 M_{\odot}/\text{pc}^2$
 Donato, Gentile, Salucci et al. MNRAS (2009)



Argüelles et al. MNRAS (2023)

Growth of SMBH seeds formed from the gravitational collapse of DM cores

. We compute, in a Kerr metric, the evolution of mass and angular momentum of the BH using a geodesic general relativistic disc accretion model [Argüelles et al. MNRAS \(2023\)](#)

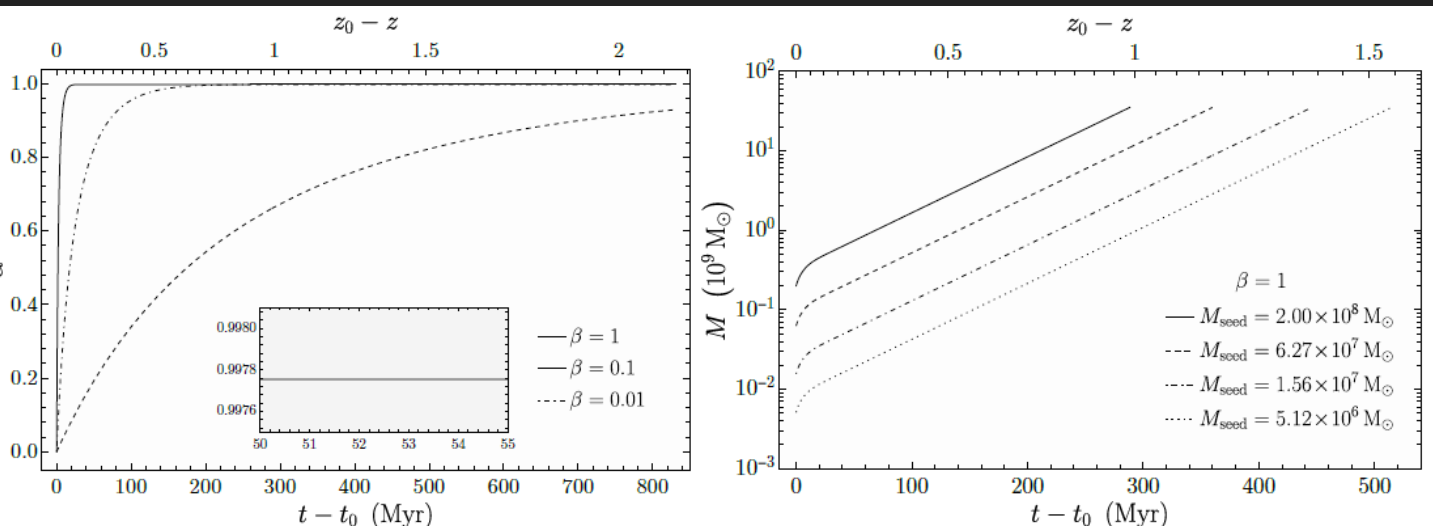
. The rate at which the rest-mass dm flows inward through the **local balance between gravitational acceleration and radiation pressure** (along z-axis) is calculated

$$\begin{aligned} \dot{M} &= \dot{M}_{\text{matter}} + \dot{M}_{\text{rad}} \\ \dot{J} &= \dot{J}_{\text{matter}} + \dot{J}_{\text{rad}} \end{aligned}$$

$$\begin{aligned} \dot{M}_{\text{matter}} &= \epsilon_0 \dot{m} \\ \dot{J}_{\text{matter}} &= l_0 \dot{m} \end{aligned}$$

$$\dot{m} \equiv \beta \dot{m}_{\text{crit}} = \frac{8\pi\beta M}{3\kappa \max\left\{\frac{f(x, \alpha)}{x^2}\right\}}$$

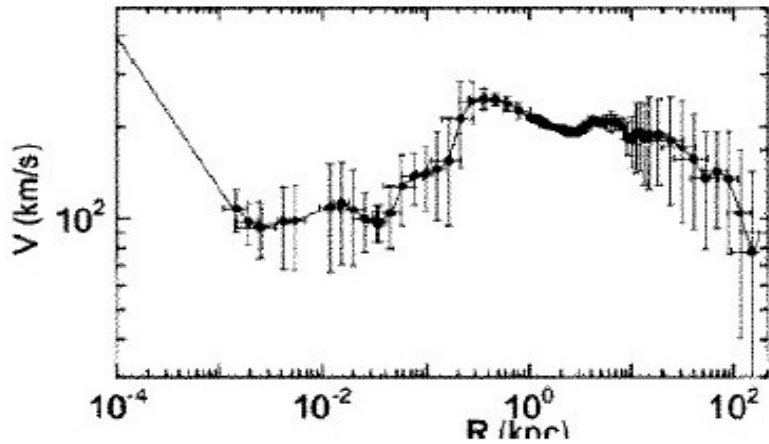
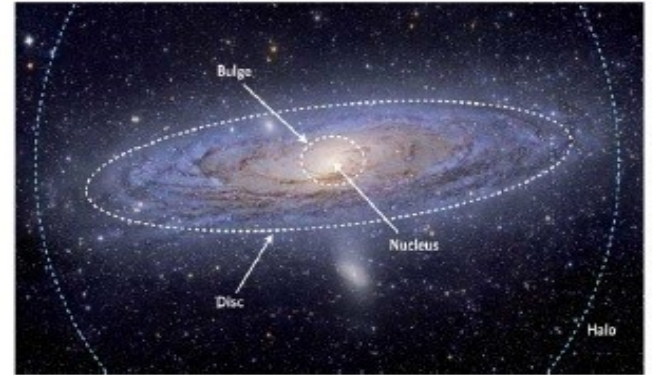
This BH-seeds are larger than typical baryonic-seeds (e.g. Pop. III stars), and can grow up to $10^9 - 10^{10} M_{\odot}$ in a fraction of 1st Gyr of the life of the Universe without invoking unrealistic accretion rates !



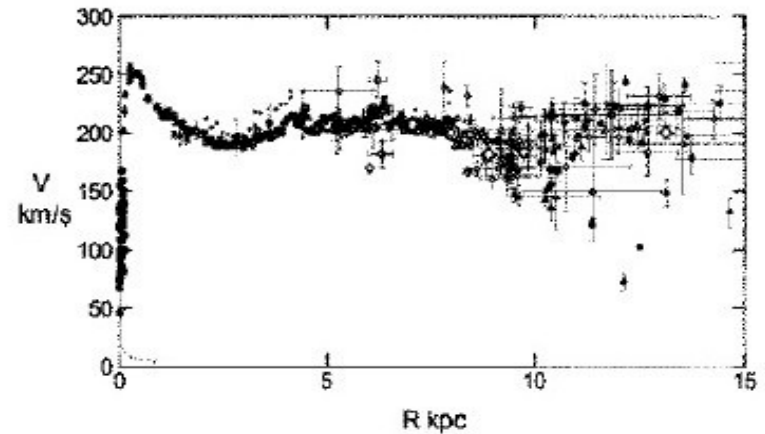
Phenomenology II - Below critical core-halo solutions:
The Milky Way (Rotation Curve and S-stars)

Milky Way observables: from central parsec to outer halo

- central pc governed by a dark compact object of mass $M_c \sim 4 \times 10^6 M_\odot$
- central kpc governed by an inner and main spheroidal Bulge
- central 10 kpc governed by a flat disk
- outer region governed by a DM spherical halo with $M_h(r = 25\text{kpc}) \approx 10^{11} M_\odot$

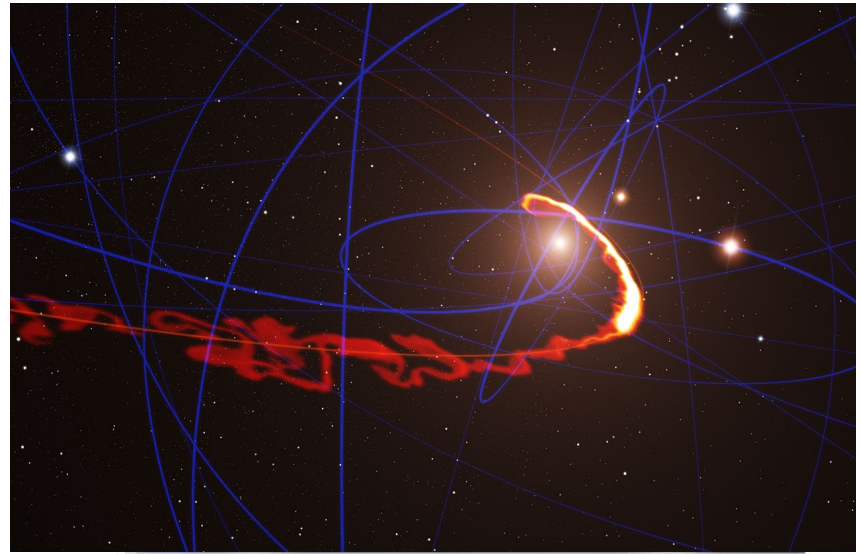
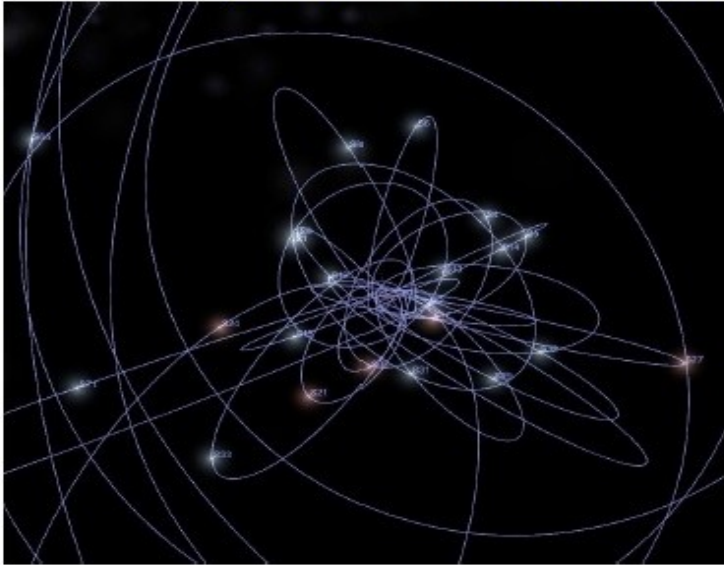


Y. Sofue, (PASJ) (2013)



Milky Way observables. Inside the central pc: the S-star cluster

- The central $10^{-3} \text{ pc} \lesssim r \lesssim 2 \text{ pc}$ consist in young S-stars and molecular gas obeying a Keplerian law ($v \propto r^{-1/2}$)
- The observational near-IR technics were developed in *S. Gillessen et al. (Apj) (2009)* and in *S. Gillessen et al. (Apj) (2015)* for S-stars and gas cloud G2



Observations implies $M_c \approx 4.2 \times 10^6 M_\odot$ within $r_{p(S2)} \approx 6 \times 10^{-4} \text{ pc}$

Fermionic 'core – halo' profiles: can their overall gravitational potential explain the Milky Way rotation curve as well as the S-star dynamics without the central BH hypothesis?

Hint: Need to solve the former boundary condition problem searching for a set of free R.A.R parameters able to fulfill:

$M_c = 4.2 \times 10^6 \text{ Mo}$ Gillessen et al., Apj (2017)

$M(r = 20 \text{ kpc}) = 9 \times 10^{10} \text{ Mo}$ Sofue, PASJ (2013)

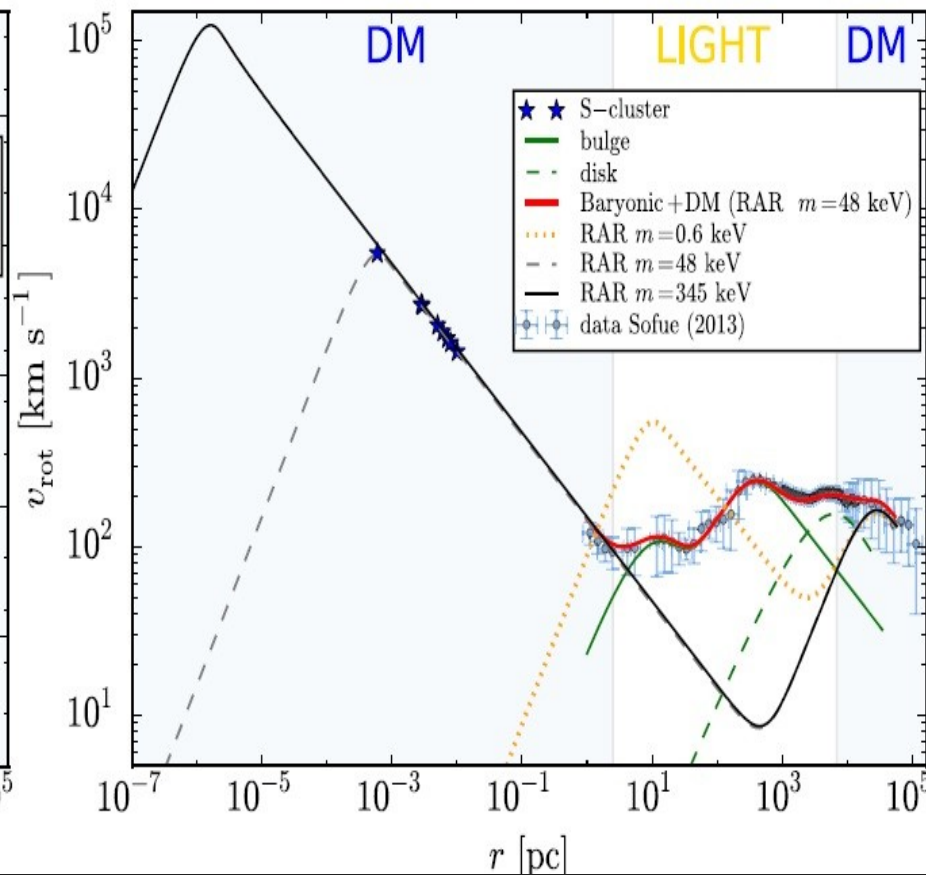
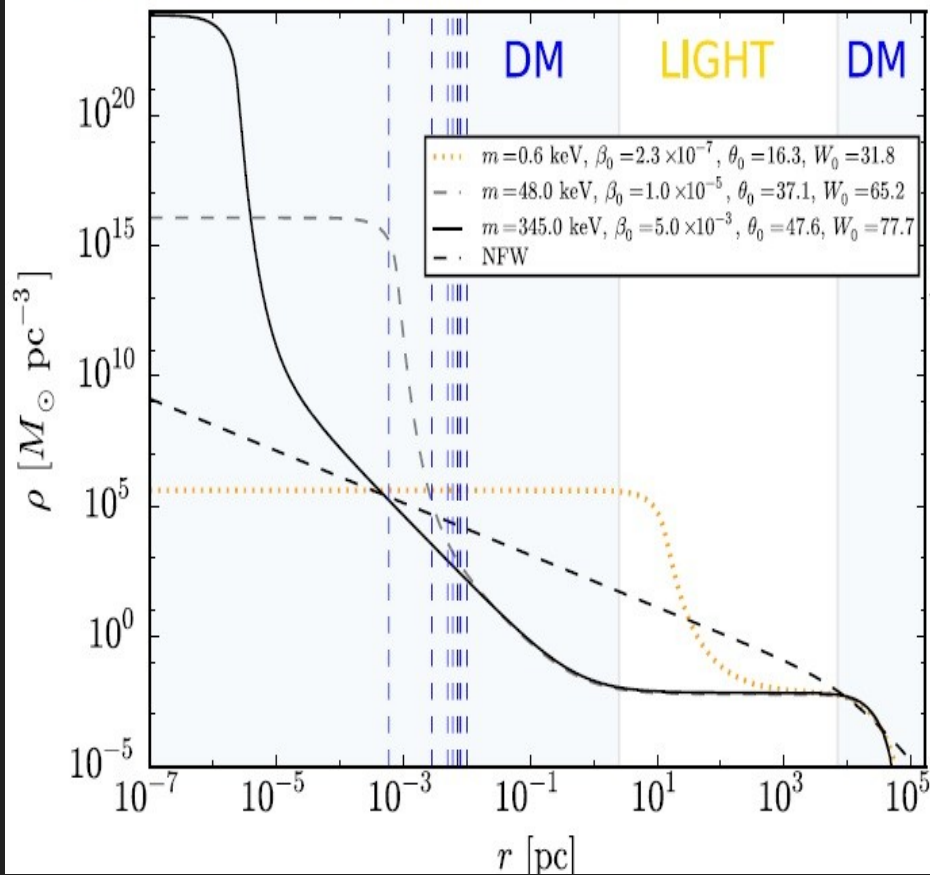
$M(r = 40 \text{ kpc}) = 2 \times 10^{11} \text{ Mo}$ Gibbons, Belokurov and Evans, MNRAS (2014)

Novel constraints on fermionic dark matter from galactic observables I: The Milky Way



Physics of the Dark Universe 21 (2018) 82–89

C.R. Argüelles^{a,b,*}, A. Krut^{b,c,d}, J.A. Rueda^{b,c,e}, R. Ruffini^{b,c,e}



Phenomenology II: The S2-star at the Milky Way Center



S2 star

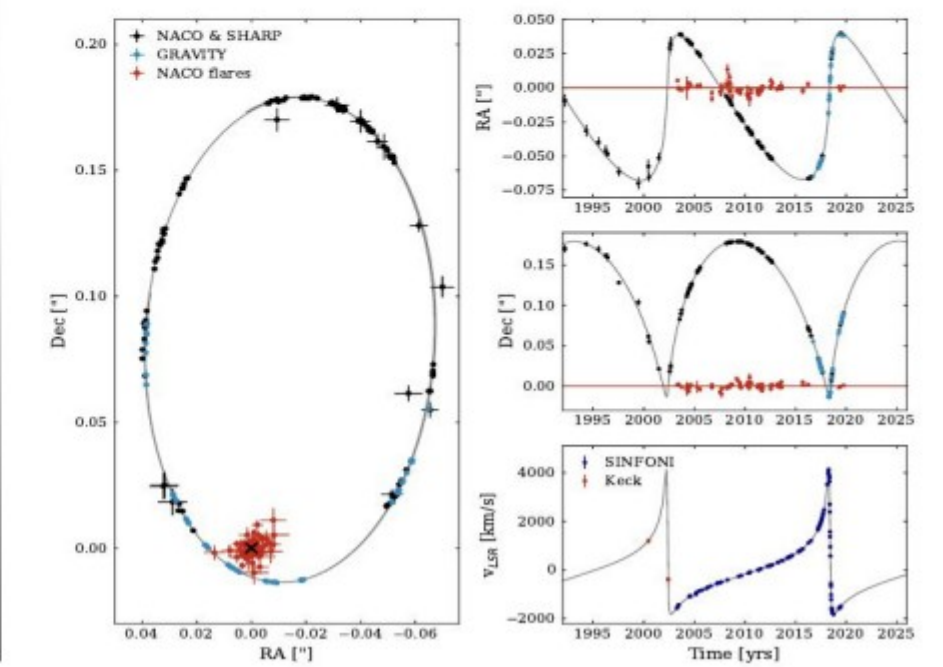
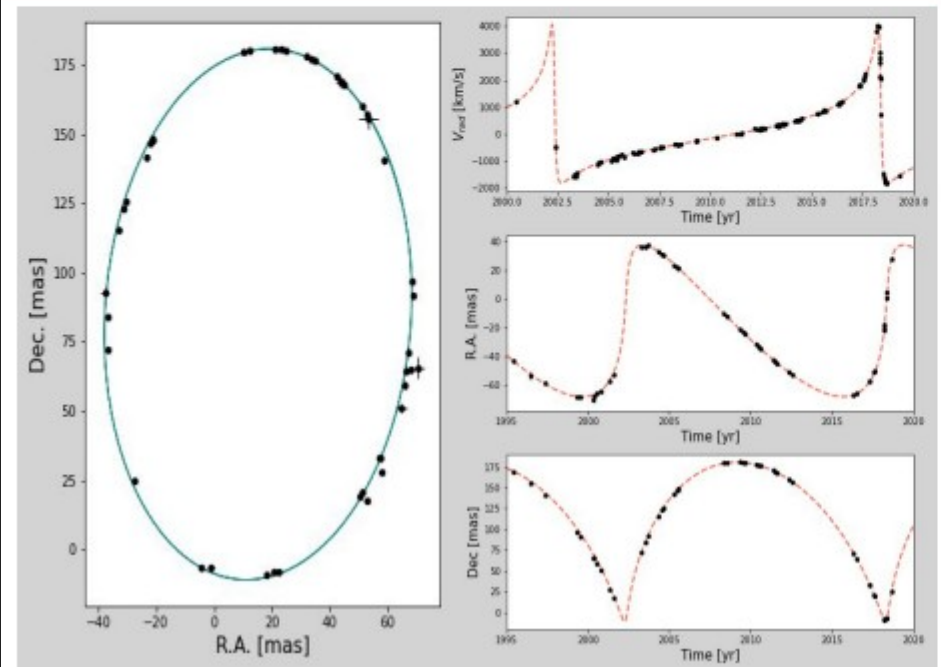
Gravity Collaboration 2020

$BH - M_{BH} = 4.26 \times 10^6 M_{\odot}$

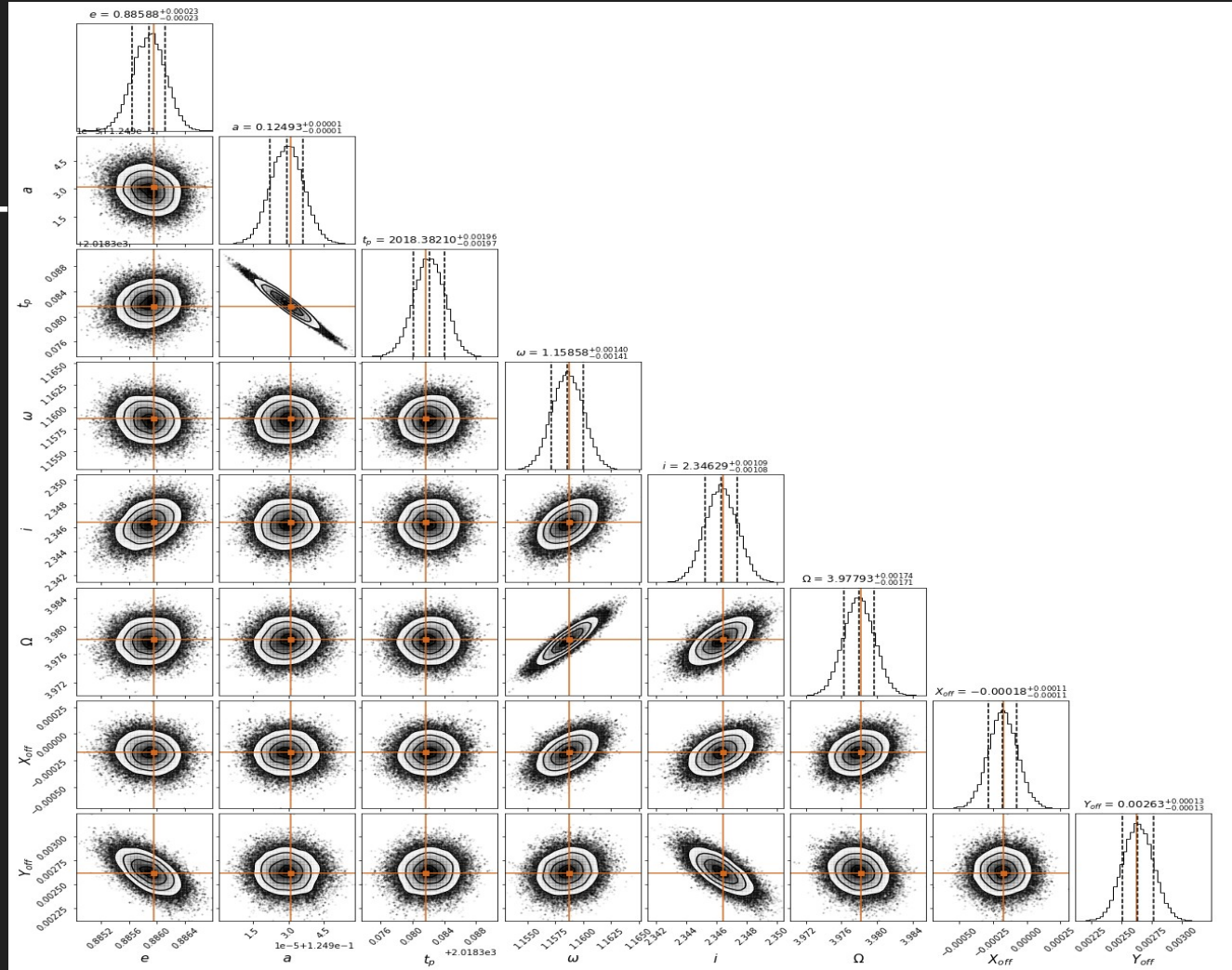
RAR - $mc^2 = 100 \text{ keV}$

e	a [arcsec]	T [yr]	ω [$^{\circ}$]	i [$^{\circ}$]	Ω [$^{\circ}$]	t_p [yr]	$\Delta\phi$ [min/rev]
0.886	0.125	16.05	66.4	134.4	227.9	2018.38	11.8

e	a [arcsec]	T [yr]	ω [$^{\circ}$]	i [$^{\circ}$]	Ω [$^{\circ}$]	t_p [yr]	$\Delta\phi$ [min/rev]
0.885	0.125	16.05	66.26	134.6	228.2	2018.38	12.1

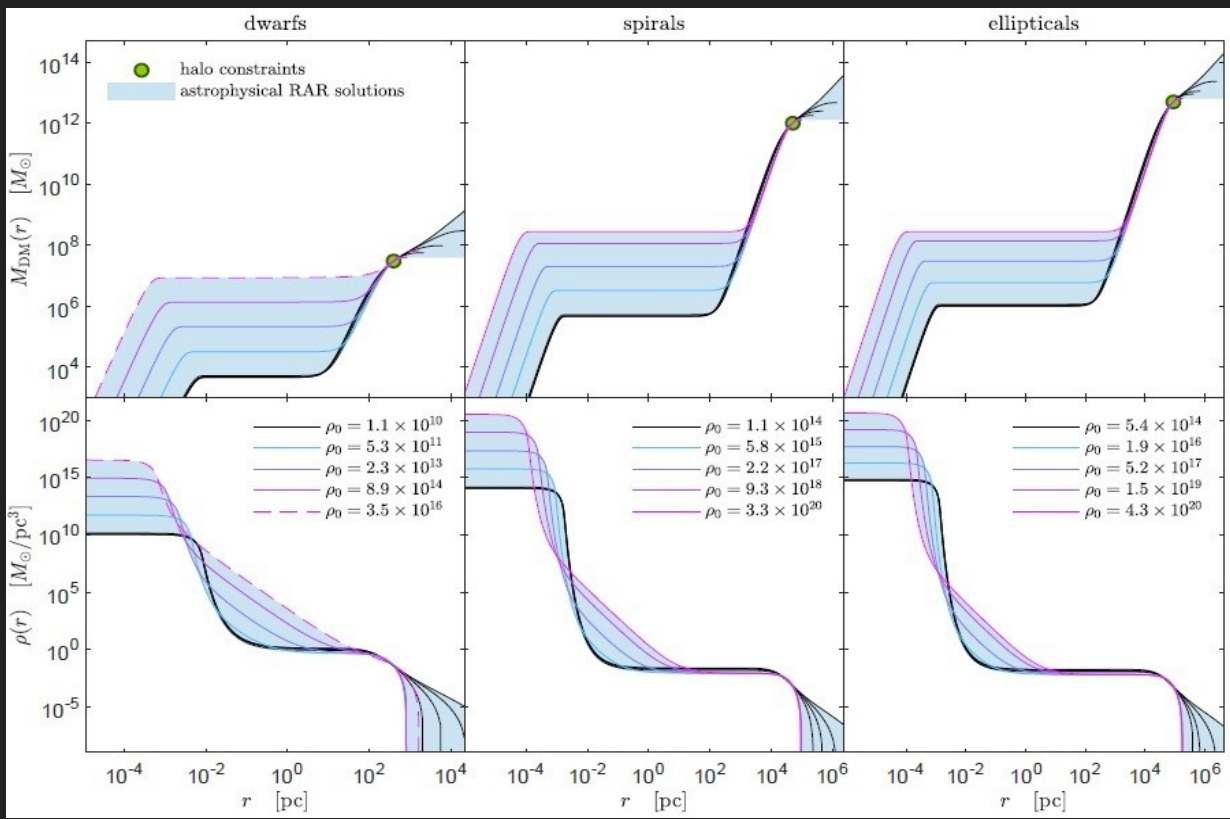


Posteriors of the S2-
star orbital
parameters
determined from a
Monte-Carlo Markov-
Chain method within a
core-halo non-critical
solution ($m=100$ keV)



Fermionic core-halo profiles: From dwarf to elliptical galaxies

- The same fermionic model can be applied to other galaxy types, from dwarf, to ellipticals, to galaxy clusters Argüelles, Krut, Rueda, Ruffini, PDU (2019)



For $m \sim 50$ keV we make a full coverage of free parameters of the theory, for realistic boundary conditions inferred from observables :

DWARFS: eight best resolved MW satellites

$$r_{h(d)} = 400 \text{ pc}$$

$$M_{h(d)} = 3 \times 10^7 M_{\odot}$$

SPIRALS: sample of nearby disk galaxies from THINGS

$$r_{h(s)} = 50 \text{ kpc}$$

$$M_{h(s)} = 1 \times 10^{12} M_{\odot}$$

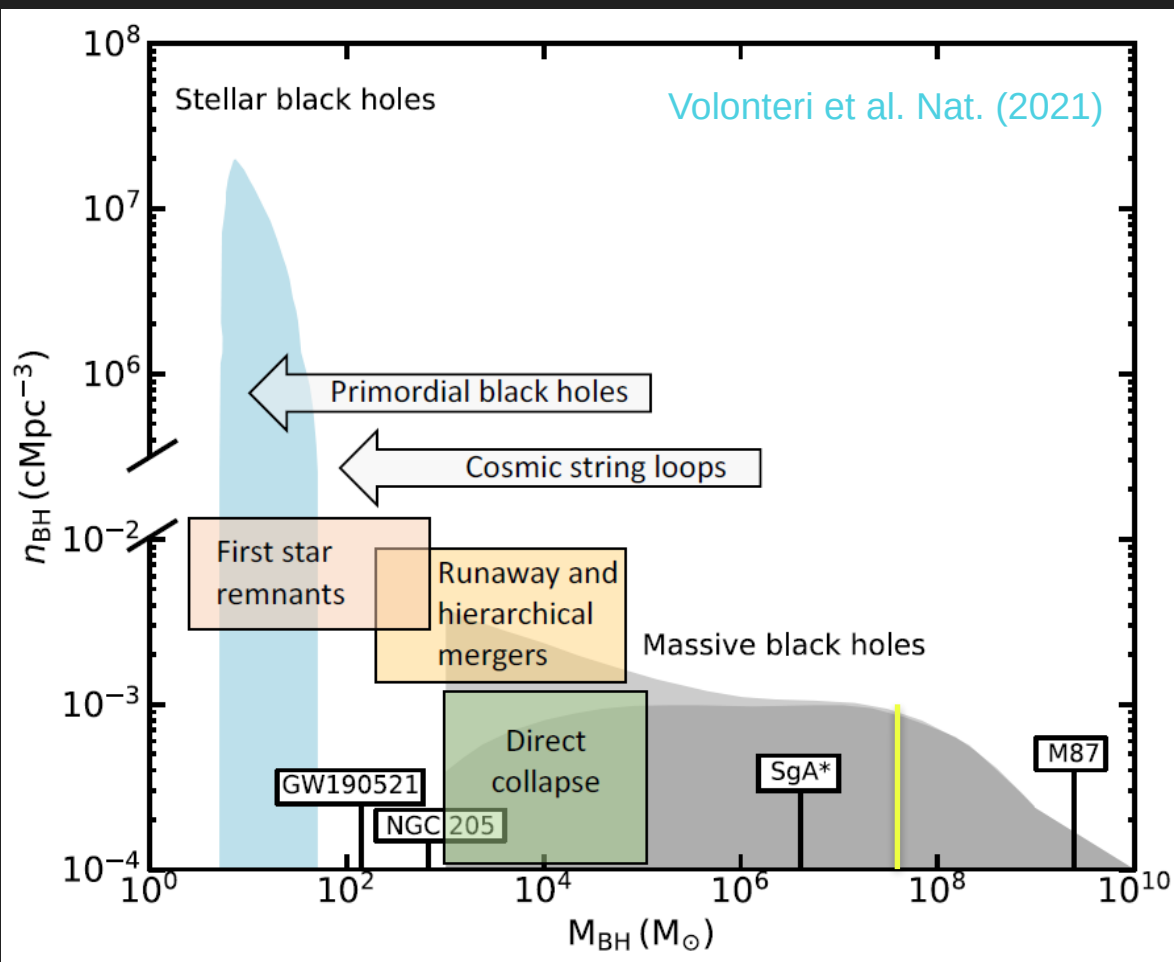
ELLIPTICALS: sample analyzed via weak lens

$$r_{h(e)} = 90 \text{ kpc}$$

$$M_{h(e)} = 5 \times 10^{12} M_{\odot}$$

Discussion: standard SMBH formation channels

Different Massive BH formation channels: Baryonic & Early Universe channels



(I) Baryonic channels:

- Pop. III stars (1st stars remnants)
- Direct collapse of gas clouds
- Runaway collisions in star clusters

(II) Early Universe channels: (poorly constrained epochs)

- Topological defects (cosmic strings, domain walls)

(III) DM channels:

- **Fermionic DM core-collapse**
- **SIDM (grav. catastrophe)**

Back up slides

Novel SMBH formation scenario from DM core-collapse

This solution may provide initial **seed** for the **formation of observed SMBHs** in active galaxies such as M87 (without the need of unrealistic super – Eddington accretion rates)

The degeneracy pressure of the DM core cannot support its own weight and undergo a core-collapse towards a **SMBH-seed from DM** ! (i.e. without the need of barionic matter)

Argüelles et al. MNRAS (2021)

$$M_{\text{crit}} \approx 0.384 \frac{m_{\text{Pl}}^3}{m^2} \approx 6.274 \times 10^9 \left(\frac{10 \text{ keV}}{mc^2} \right)^2 M_{\odot}$$

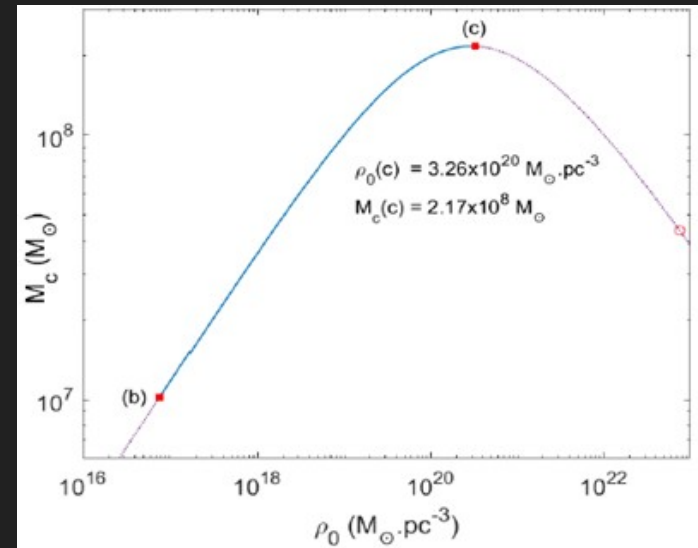
Turning point instabilities for relativistic stars and black holes

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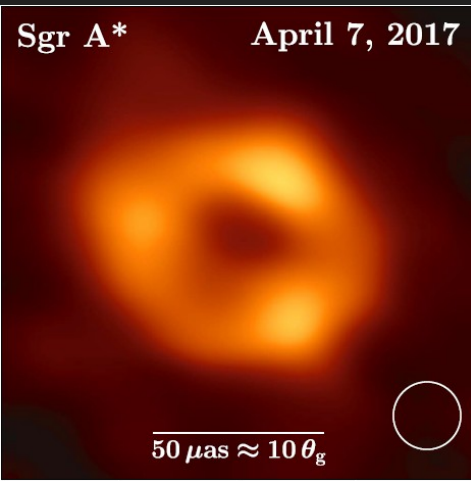
Abstract

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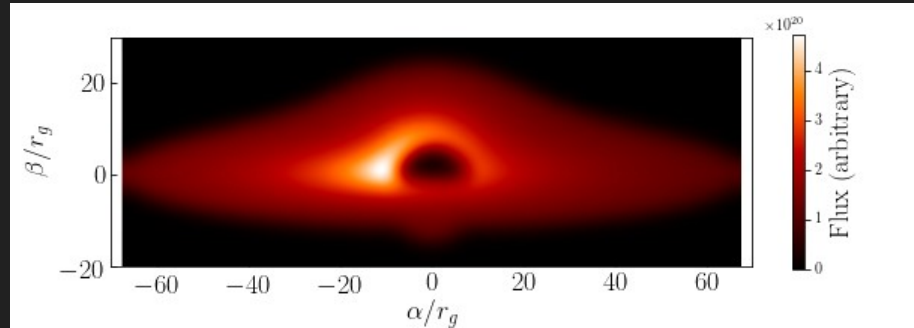
The shadow of SgrA*

How does this DM model stands with the recent EHT results on SgrA*?



EHT collaboration, ApJL (2022)

- The EHT analysis support an image dominated by a bright thick ring with diameter of $52 \mu\text{as} \sim 10 R_g/D$ ($R_g = GM/c^2$) The EHT collaboration, ApJL (2022)
- Does exist any fermion-core compact enough to deflect light in a similar fashion than the BH ? **YES !**
Solution prior to core-collapse has a maximal light deflection at $5 R_g !$

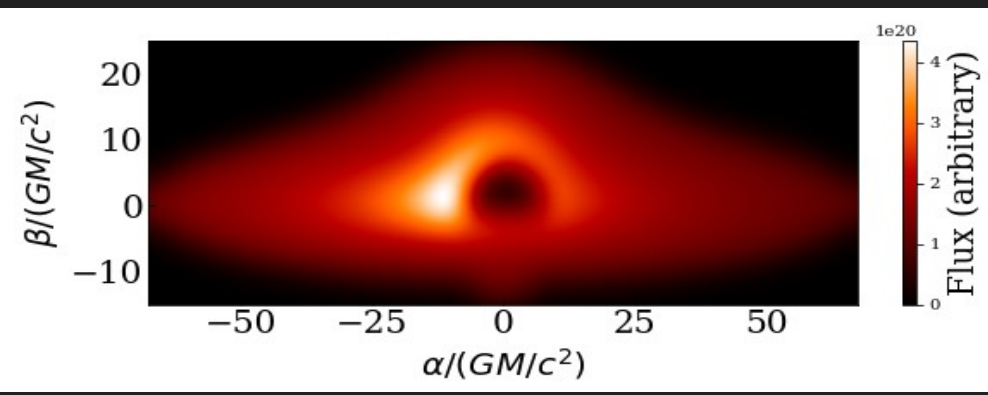


Pelle, Argüelles, et al (In prep.)

Done with a GR ray-tracing code: **Skylight**
Pelle, Reula, et al., MNRAS (2022)

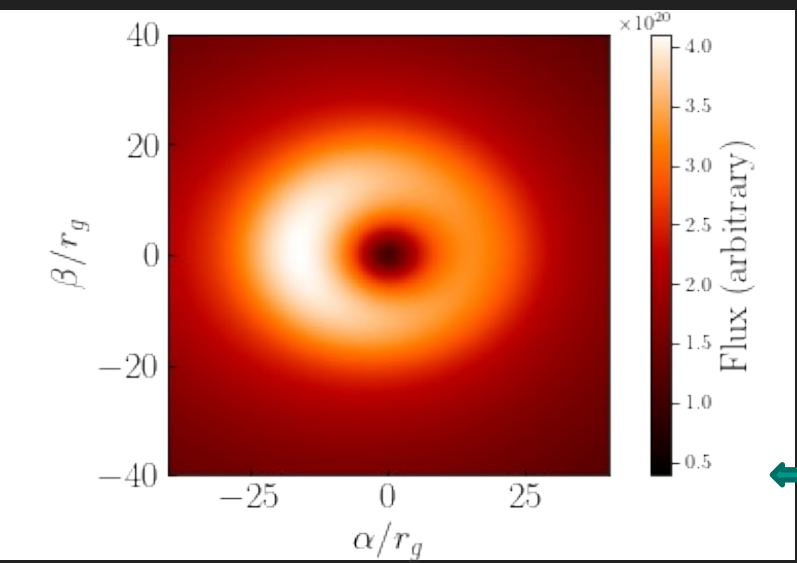
- DM fermion-cores (not yet collapsed) can develop light-images similar to the BH case, with a shadow feature !

How does the RAR model stands with the recent EHT results on SgrA*?



- Blurred (Gaussian filter) monochromatic Image ($\lambda=1.3$ mm) caused by light rays coming from an accretion disk (S&S) onto the stable DM core, seen by a far observer

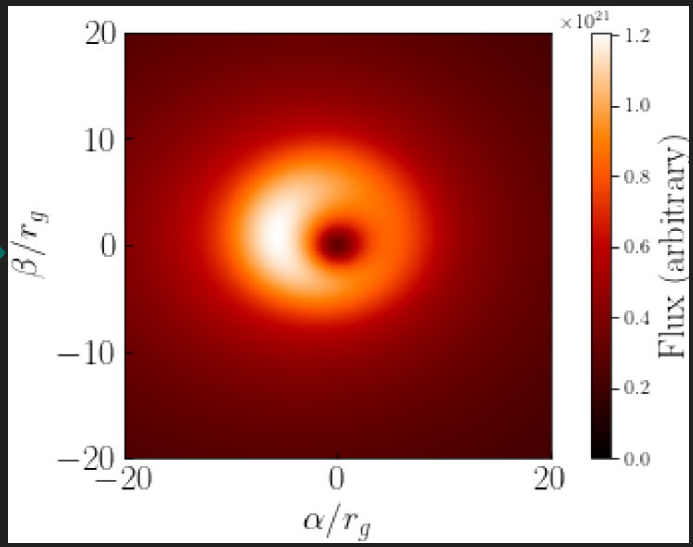
Edge-on view



Face-on view

$m=378 \text{ keV}/c^2$

$m=300 \text{ keV}/c^2$



Pelle, Argüelles, et al (In preparation)

Phenomenology II:

different galaxy types, and galaxy relations

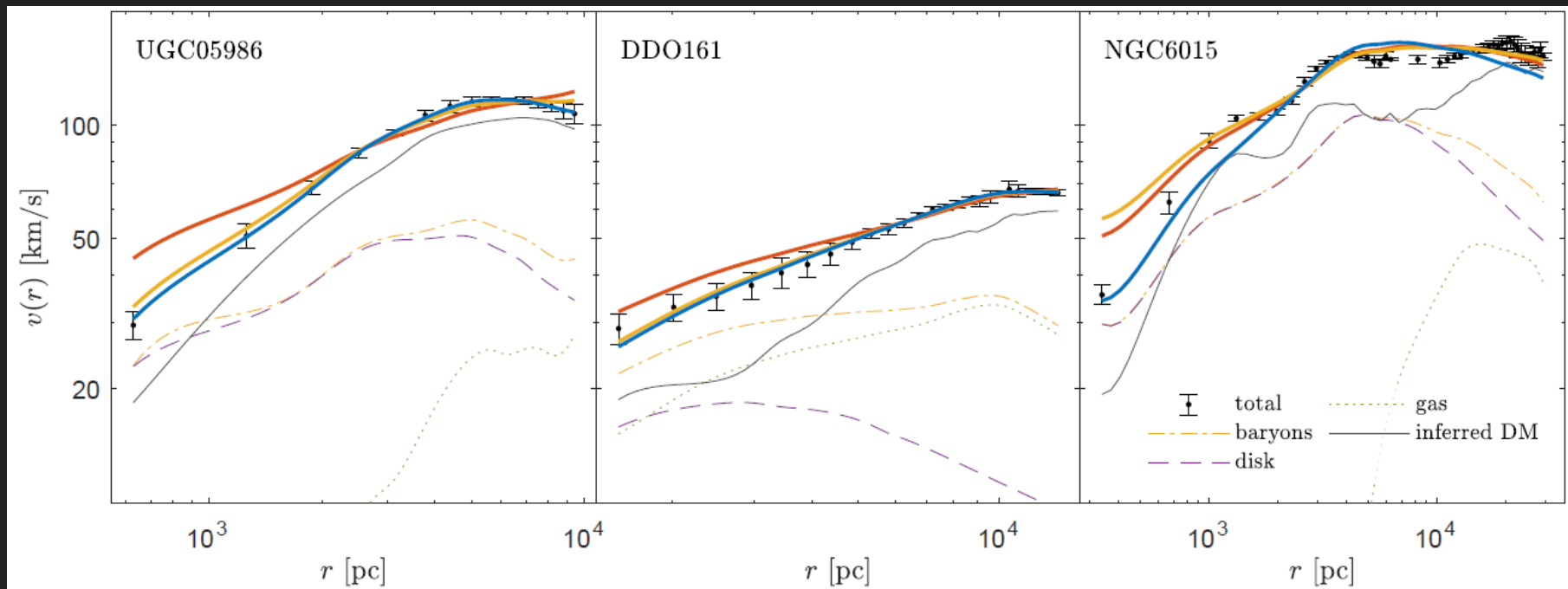
Testing the RAR model with the SPARC data-set of 120 disk galaxies

(Blue): Fermionic DM
(Yellow): gNFW; **(Red):** NFW

$$V_{\text{bar}}^2 = \Upsilon_b V_b^2 + \Upsilon_d V_d^2 + V_g^2$$
$$V_{\text{DM}}^2 = V_{\text{tot}}^2 - V_{\text{bar}}^2$$

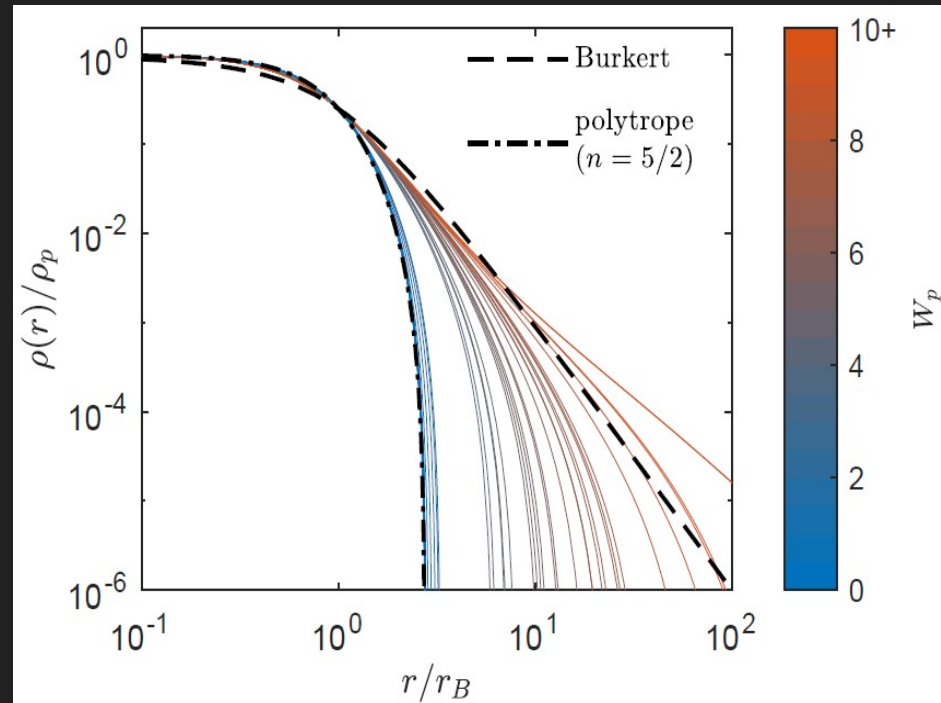
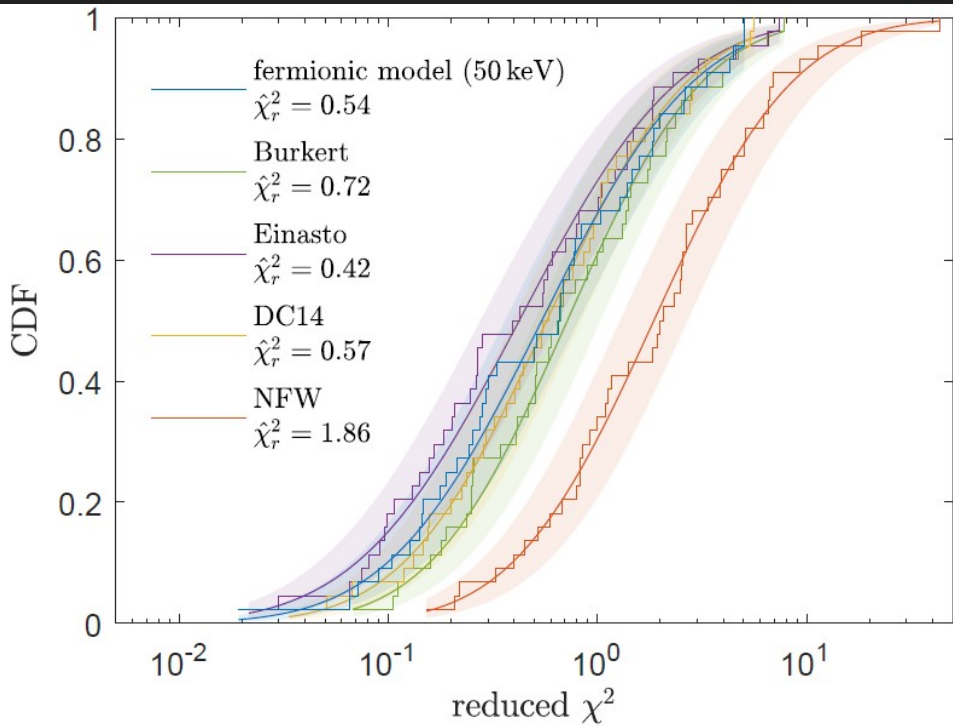


$$\chi^2(\mathbf{p}) = \sum_{i=1}^N \left[\frac{V_i - v(r_i, \mathbf{p})}{\Delta V_i} \right]^2$$



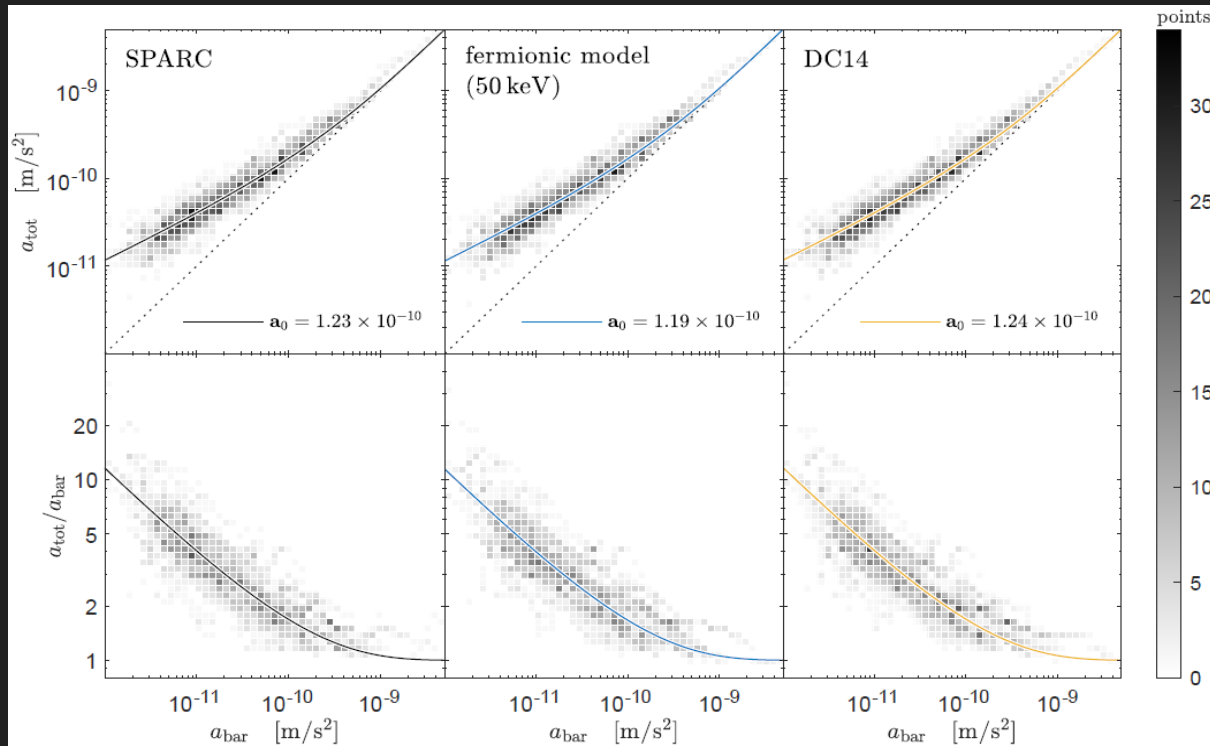
Testing the RAR model with the SPARC data-set of 120 disk galaxies

- RAR profiles which best-fit SPARC galaxies can develop halo shapes similar to Burkert
- Cuspy (NFW) DM profiles are clearly disfavoured w.r.t cored profiles by the SPARC RCs



The RAR model explains the Radial Acceleration Relation and the BTFR

Radial Acceleration Relation: Non linear correlation between the radial acceleration caused by the total matter, and the one generated by the baryons only: **Valid at any resolved galaxy radii !**




$$a_{\text{tot}} = \frac{a_{\text{bar}}}{1 - e^{-\sqrt{a_{\text{bar}}/a_0}}}$$

These acceleration relations DO NOT imply of any new physics (i.e. MOND), and can be reproduced by the LCDM, and by the fermionic halos obtained from a MEP



What does lie at the Milky Way centre? Insights from the S2-star orbit precession

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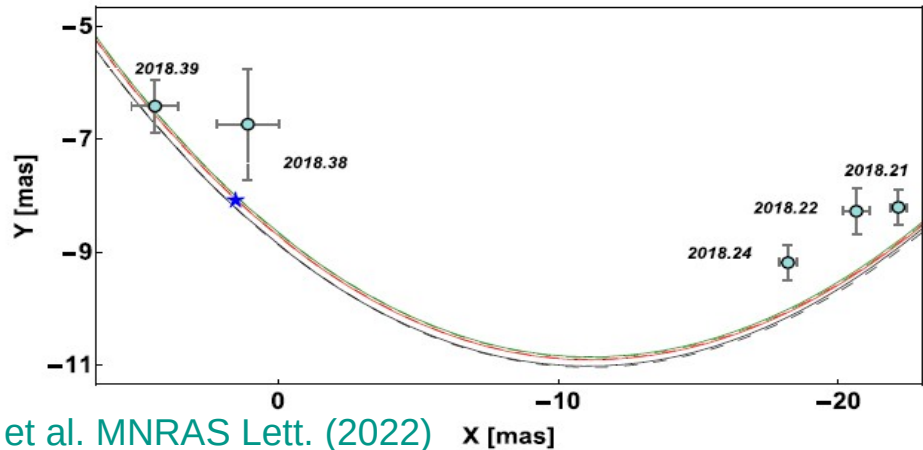
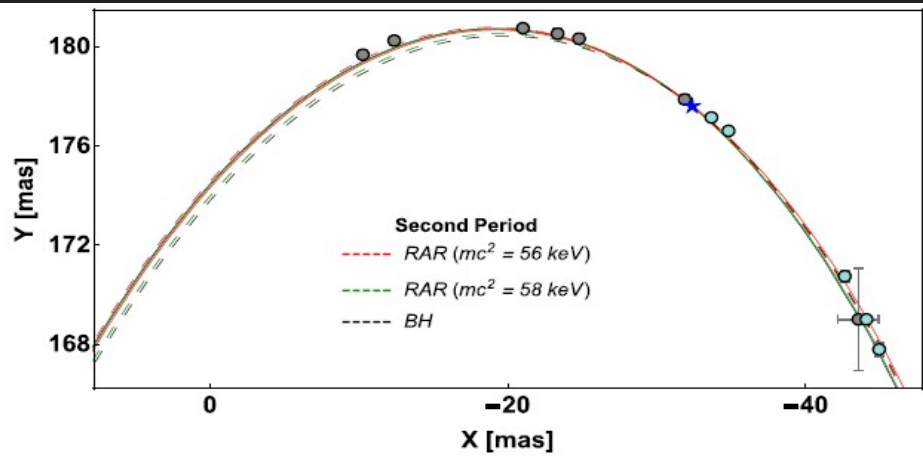
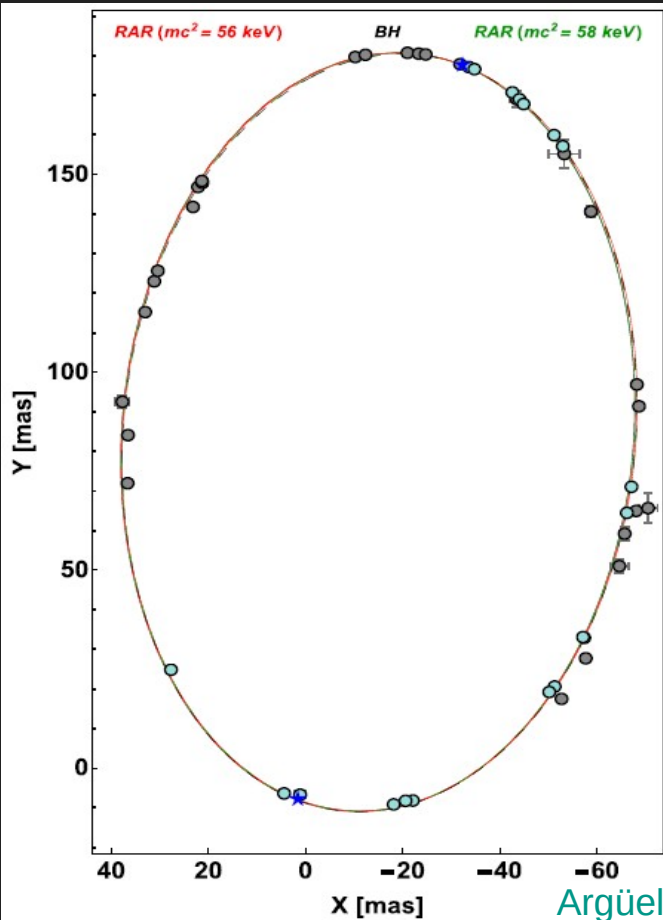
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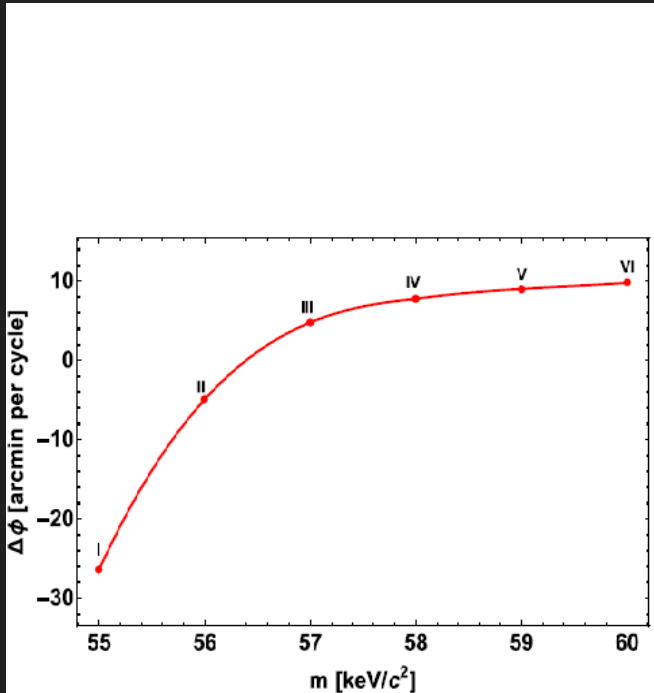
ABSTRACT

It has been recently demonstrated that both, a classical Schwarzschild black hole (BH), and a dense concentration of self-gravitating fermionic dark matter (DM) placed at the Galaxy centre, can explain the precise astrometric data (positions and radial velocities) of the S-stars orbiting Sgr A*. This result encompasses the 17 best resolved S-stars, and includes the test of general relativistic effects such as the gravitational redshift in the S2-star. In addition, the DM model features another remarkable result: The dense core of fermions is the central region of a continuous density distribution of DM whose diluted halo explains the Galactic rotation curve. In this Letter, we complement the above findings by analysing in both models the relativistic periapsis precession of the S2-star orbit. While the Schwarzschild BH scenario predicts a unique prograde precession for S2, in the DM scenario, it can be either retrograde or prograde, depending on the amount of DM mass enclosed within the S2 orbit, which, in turn, is a function of the DM fermion mass. We show that all the current and publicly available data of S2 cannot discriminate between the two models, but upcoming S2 astrometry close to next apocentre passage could potentially establish if Sgr A* is governed by a classical BH or by a quantum DM system.

Testing the DM-core alternative to the BH with the S-2 star precession

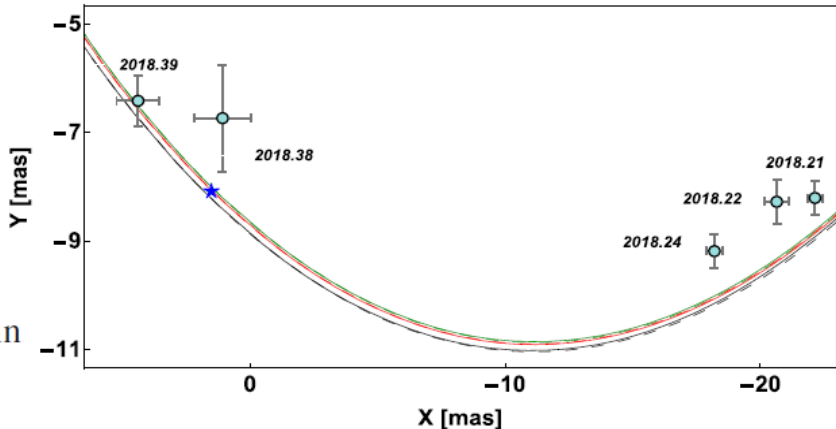
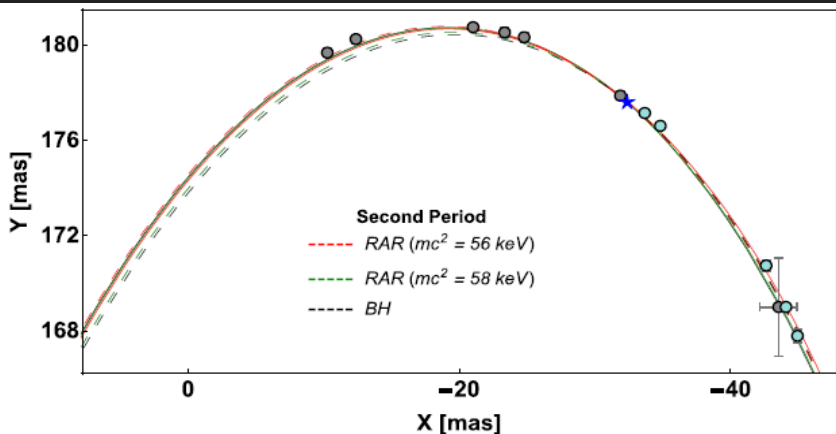


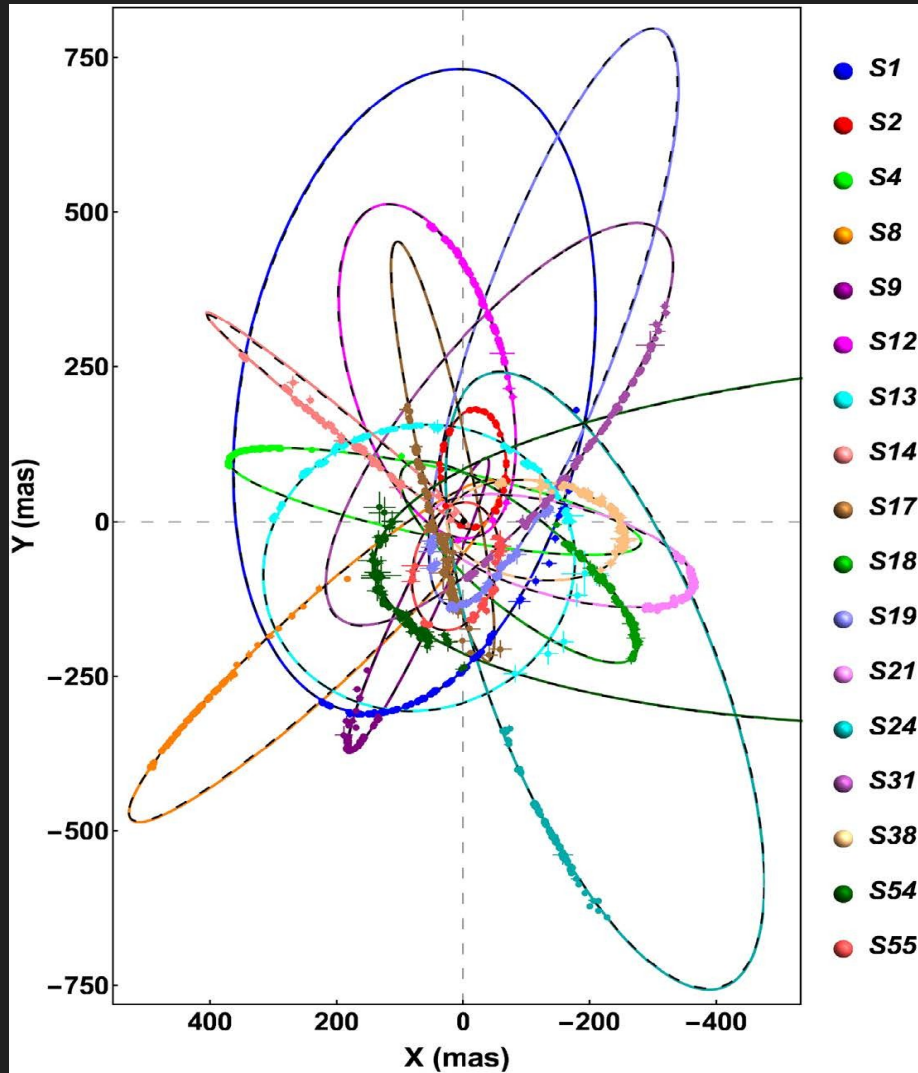
Testing the DM-core alternative with the S-2 star precession



$$\Delta\phi_{\text{BH}} = 6\pi GM_{\text{BH}}/[c^2 a(1 - e^2)] \approx 12 \text{ arcmin}$$

Argüelles et al. MNRAS Lett. (2022)





THEORETICAL and OBSERVED 17 best-resolved S-star orbits around SgrA*

THEORETICAL MODELS: calculated by solving the geodesic equation of a test particle in the gravitational field of:

1) Schwarzschild BH of $4.07 \times 10^6 \text{ Mo}$

$$\langle \bar{\chi}^2 \rangle_{\text{BH}} = 1.6$$

2) Fermionic DM distribution with $M_c = 3.5 \times 10^6 \text{ Mo}$ (fermion mass $m = 56 \text{ keV}$)

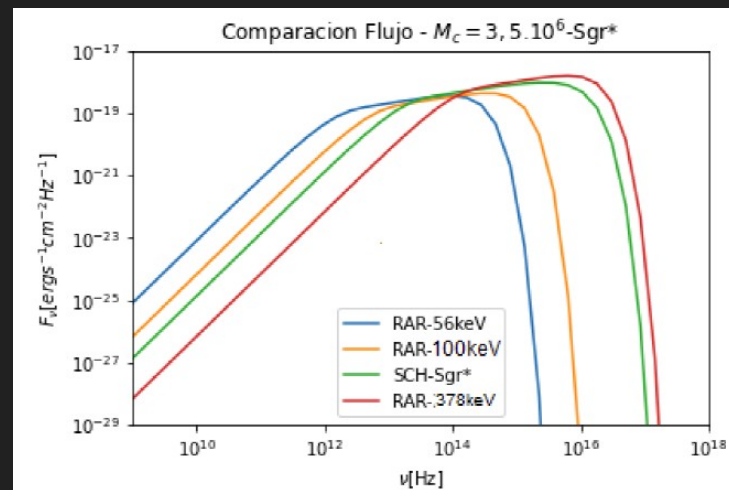
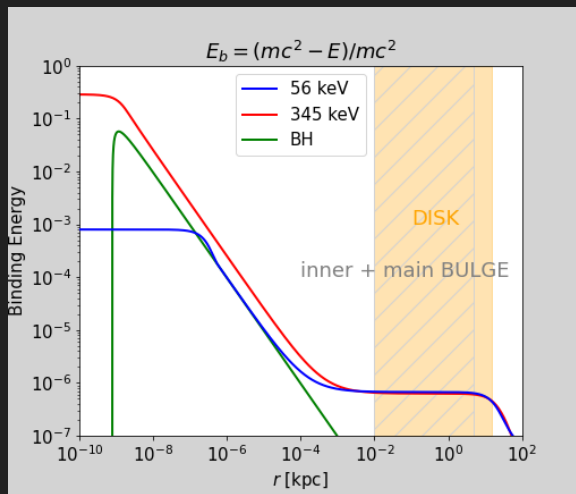
$$\langle \bar{\chi}^2 \rangle_{\text{RAR}} = 1.5$$

Disc accretion for horizonless dark compact objects: the fermion core

- Emitted flux for different fermion-core compactities (i.e. different DM particle masses) compared with the BH case
- The case of a Milky Way –like galaxy (shown as example)

Efficiency of energy extraction from the central object

$$E_{binding} = \frac{m - E_c}{m} = 1 - \sqrt{A(r) \left(1 + \frac{r_c A'(r_c)}{2A(r_c) - r_c A'(r_c)} \right)}$$



- The fermion core is transparent and therefore the disc can enter inside the core, where the efficiency saturates

mc^2 [keV]	R_{in} [kpc]	Efficiency [%]
56	$3,58 \cdot 10^{-8}$	0.07
100	$7,57 \cdot 10^{-9}$	0.37
378	$1,01 \cdot 10^{-10}$	28.5

- Minimal extension of SM (ν MSM) adding 3 right-handed STERILE ($Q_{SM} = 0$) neutrinos [T. Asaka, S. Blanchet, M. Shaposhnikov *PLB* \(2005\) 0503065](#)

Three Generations
of Matter (Fermions) spin $\frac{1}{2}$

	I	II	III		
mass →	2.4 MeV	1.27 GeV	171.2 GeV	0	0
charge →	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	0	0
name →	u up	c charm	t top	g gluon	
	Left Right	Left Right	Left Right	0	0
Quarks	d down	s strange	b bottom	γ photon	
	Left Right	Left Right	Left Right	0	0
	0 ν_e N_1 electron neutrino sterile neutrino	0 ν_μ N_2 muon neutrino sterile neutrino	0 ν_τ N_3 tau neutrino sterile neutrino	91.2 GeV 0 Z^0 weak force	>116 GeV 0 H Higgs boson
Leptons	0.511 MeV e electron	105.7 MeV μ muon	1.777 GeV τ tau	80.4 GeV ± 1 W^\pm weak force	spin 0
	Left Right	Left Right	Left Right		

Bosons (Forces) spin 1

- Group-invariance in ν MSM model: $SU(3) \times SU(2) \times U(1)$ remains unchanged!

$$\mathcal{L} = \mathcal{L}_{SM} + i\nu_R \partial_\mu \gamma^\mu \nu_R - g \bar{L}_R \phi - M/2 \bar{\nu}_R^c \nu_R \quad (2)$$

- A Lagrangian extension including for self-interactions \mathcal{L}_I under self-gravity was analyzed [C. Argüelles, N. Mavromatos, et al. *JCAP* \(2016\) 1502.00136](#)

$$\mathcal{L} = \mathcal{L}_{GR} + \mathcal{L}_{\nu R} + \mathcal{L}_V - g_V V_\mu J^\mu$$

Effects of self-interacting right handed neutrinos in RAR - halos

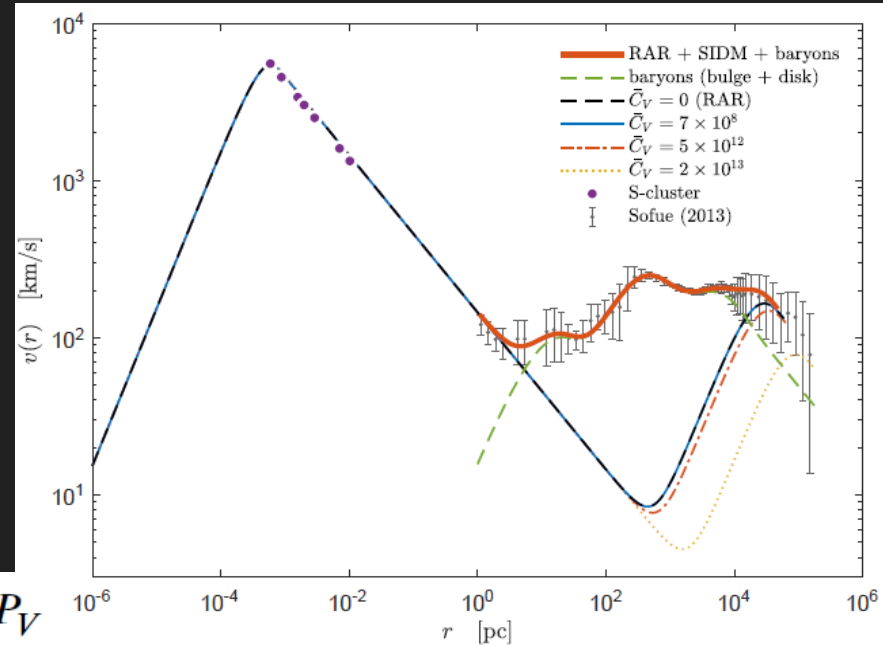
- The Higgs portal term in the Lagrangian is neglected given the bulk of sterile neutrinos live longer than the age of the Universe

$$\mathcal{L}_{N_{R1}} = i \overline{N}_{R1} \gamma^\mu \nabla_\mu N_{R1} - \frac{1}{2} m \overline{N}_{R1}^c N_{R1},$$

$$\mathcal{L}_V = -\frac{1}{4} V_{\mu\nu} V^{\mu\nu} + \frac{1}{2} m_V^2 V_\mu V^\mu,$$

$$\mathcal{L}_I = -g_V V_\mu J_V^\mu = -g_V V_\mu \overline{N}_{R1} \gamma^\mu N_{R1},$$

$$\mathcal{L}_{GR} = -\frac{R}{16\pi G},$$



- We work in the Relativistic Mean Field theory approx. fields are replaced by their mean values in its ground state .

$$\rho = \rho_C + \rho_V, \quad P = P_C + P_V$$

$$\rho_V = P_V = 1/2 C_V n^2$$

$$C_V = g_V^2 / m_V^2$$

Effects of self-interactions in particle physics (nuMSM) constraints

- The cross section constraints from colliding galaxy clusters [D. Harvey et al. Science \(2015\)](#)

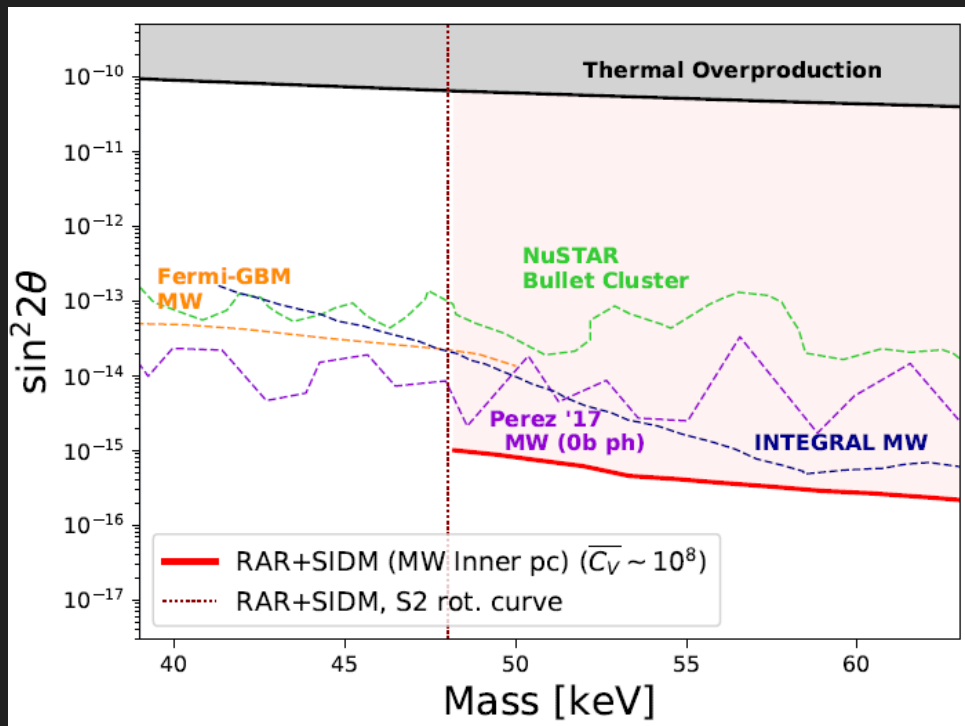
$$0.1 \leq \frac{\sigma_{\text{SIDM}}/m}{\text{cm}^2 \text{g}^{-1}} \leq 0.47$$

- Theoretical cross-section for the SI sterile neutrinos [Argüelles, et al. JCAP \(2016\)](#)

$$\sigma_{\text{core}}^{\text{tot}} \approx \frac{(g_V/m_V)^4}{4^3 \pi} 29 m^2$$



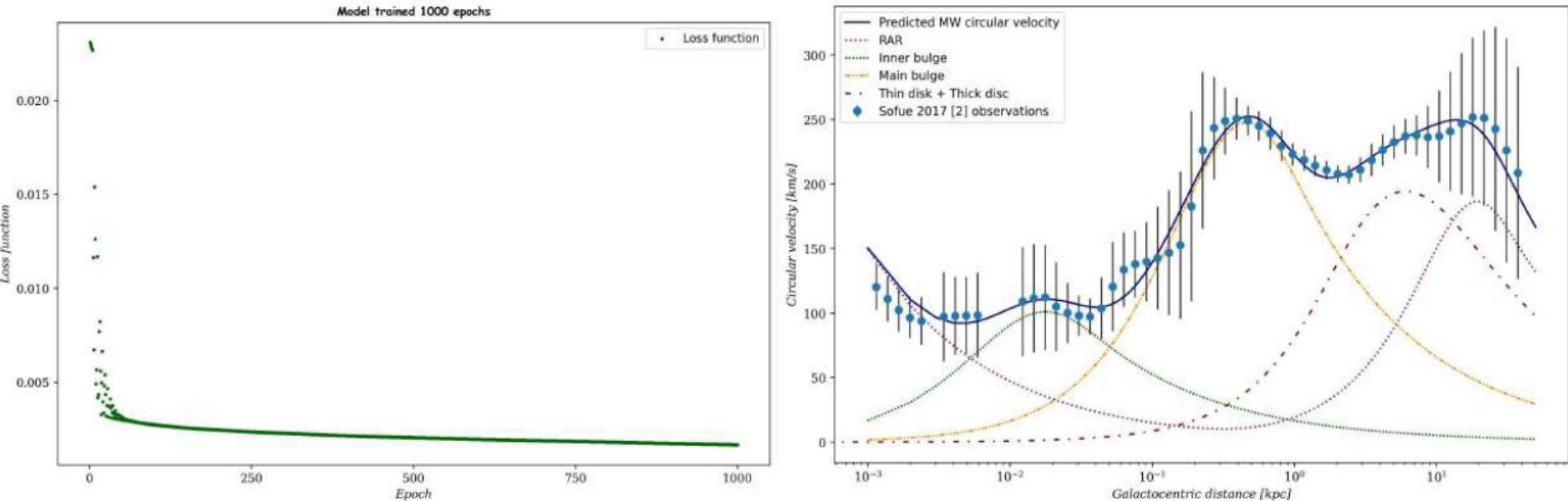
$$\bar{C}_V \equiv \left(\frac{g_V}{m_V} \right)^2 G_F^{-1} \in (2.6 \times 10^8, 7 \times 10^8),$$



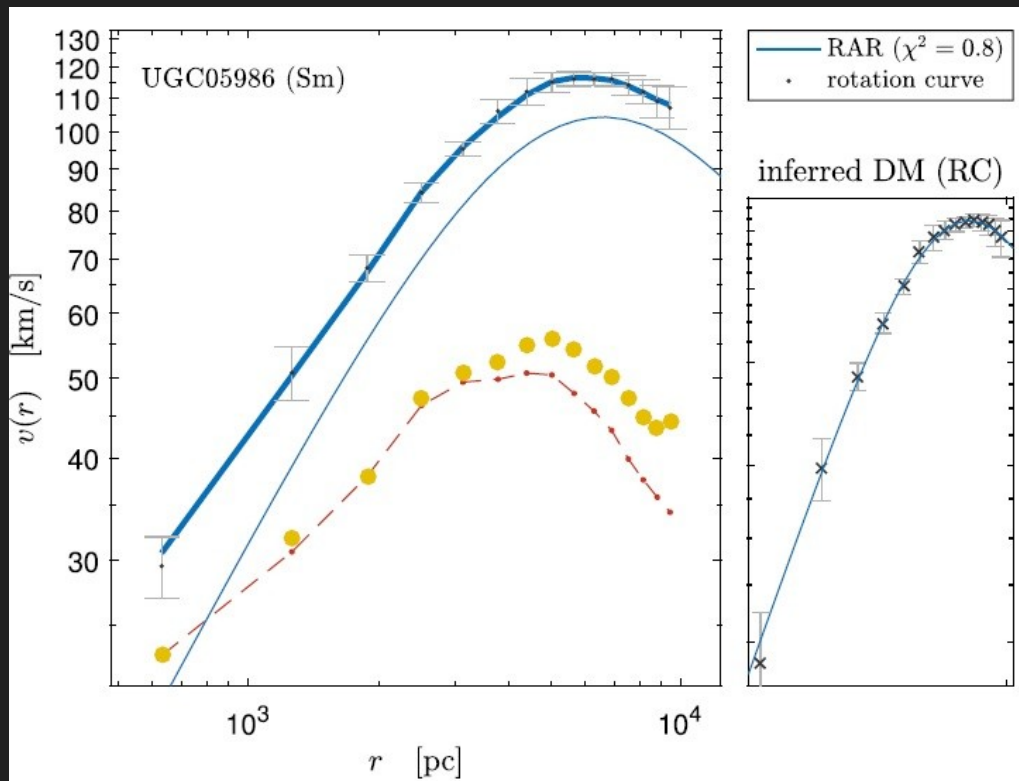
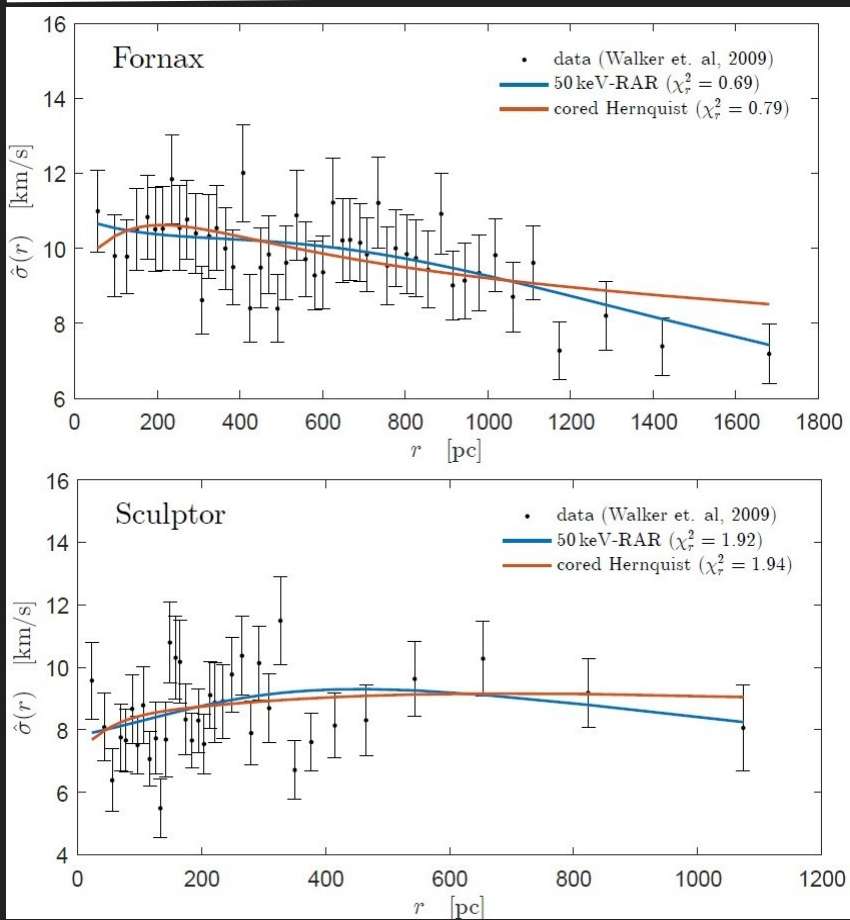
NuMSM parameter-space is relaxed by an **additional production channel of s-neutrinos** via the $V\mu$ decay (lowering the bounds on interaction angle) [Yunis, Argüelles, Mavromatos, et al. PDU \(2020\)](#)

Rotation Curve fitting using state-of-the-art Machine Learning

- We use machine learning tools (gradient descent, through **PyTorch**) to fit the observed Milky Way RC: **Very useful to test semi-analytical models for DM (such as RAR, or Fuzzy DM)** : can include **> 10** free parameters (Baryonic + DM), minimizing the Loss-function in few hs time



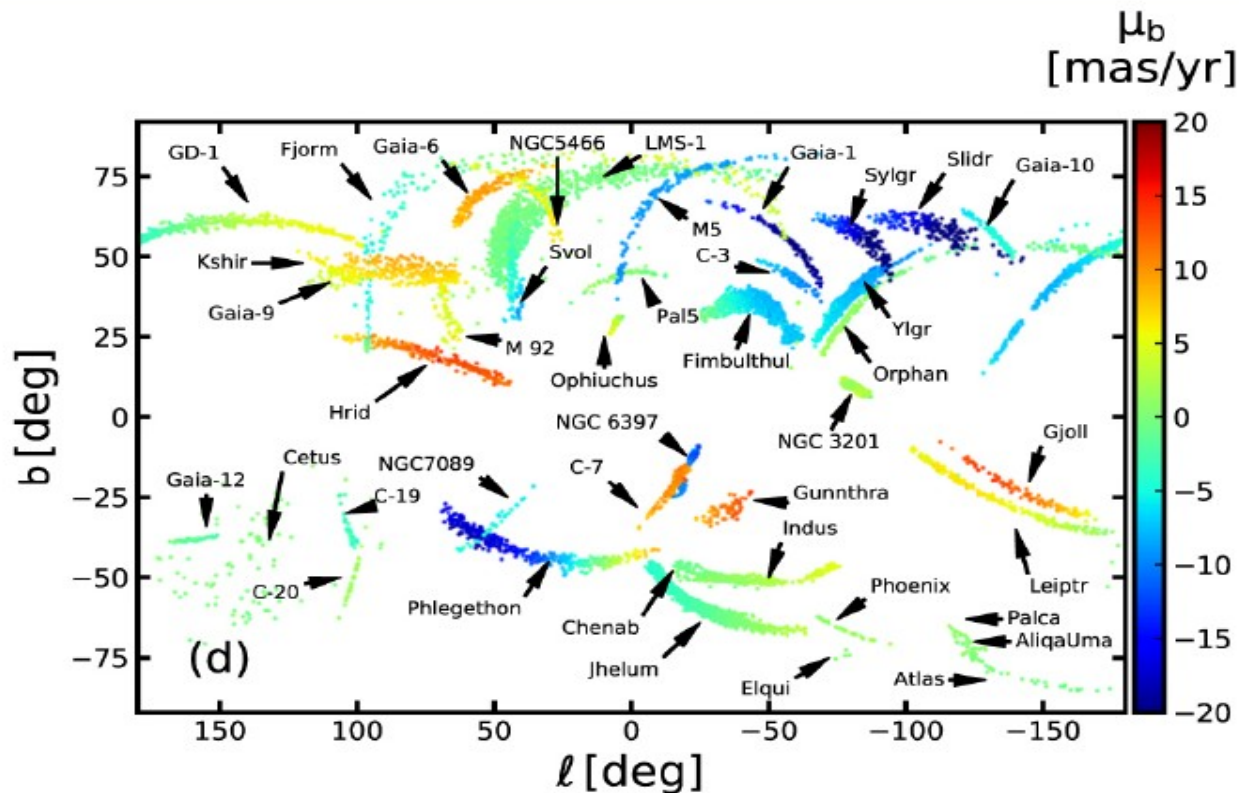
L.o.S dispersion velocity data and high resolution rotation curves in disk galaxies are well reproduced by the model



Applications: Galactic Scales (Stellar-Stream tracers)

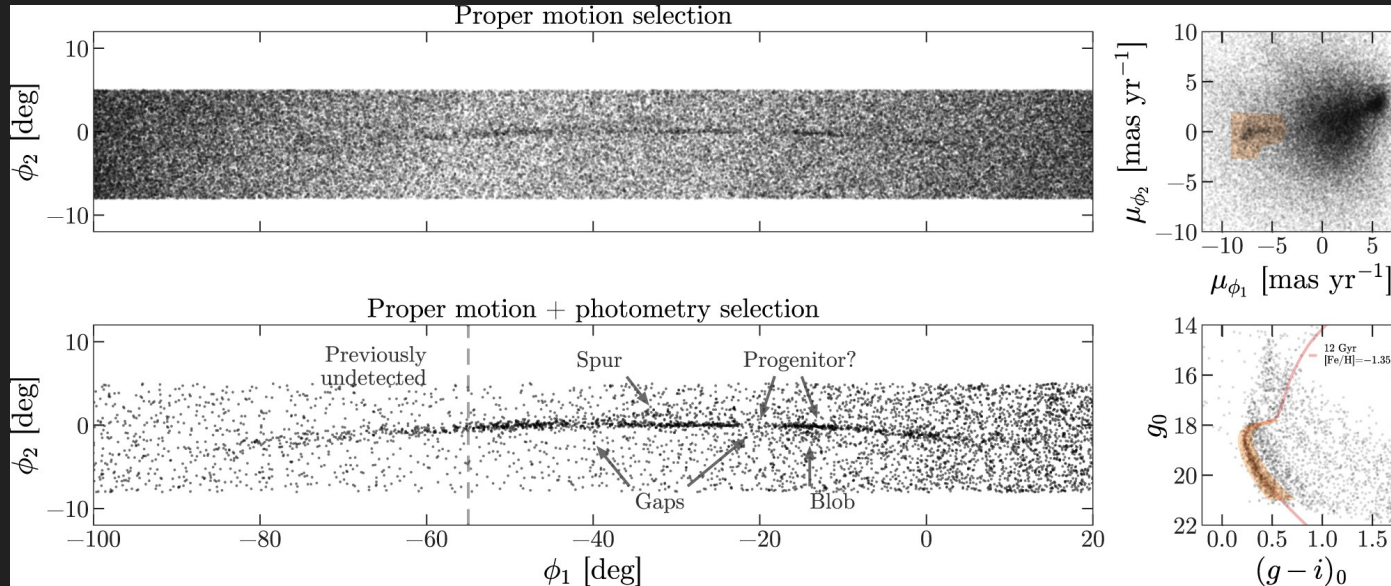
Stellar streams in the Galaxy: key tracers of the gravitational potential

41 stellar streams comprising 9192 Gaia EDR3 stars



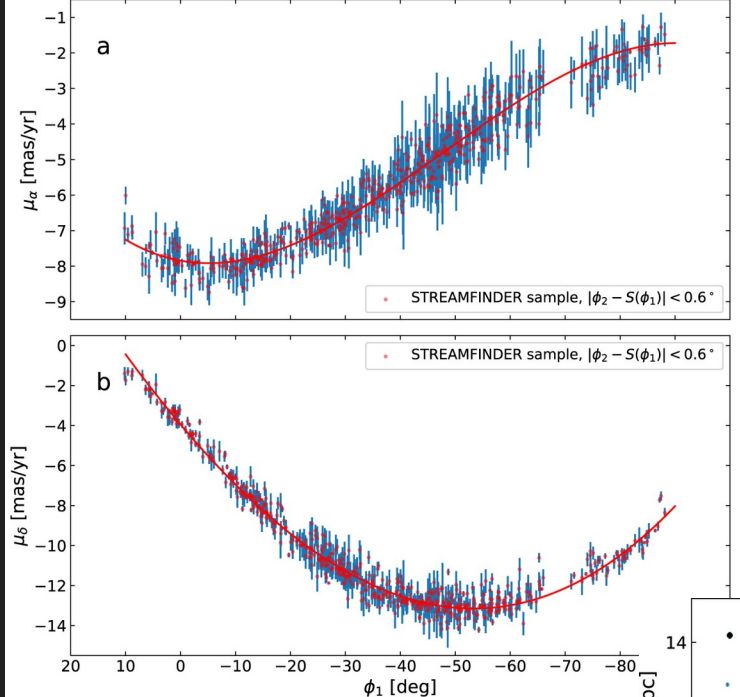
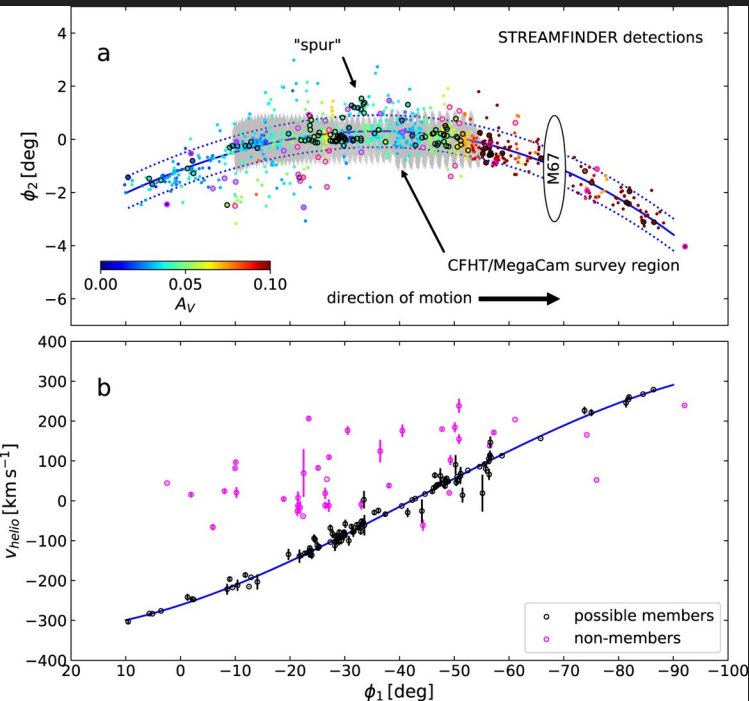
Constraining the fermionic DM model with the GD-1 stream

- A cold stream (GD-1) travelling through the halo (shown in self-coordinates along the stream) [Price-Whelan & Bonaca, Apj \(2018\)](#)

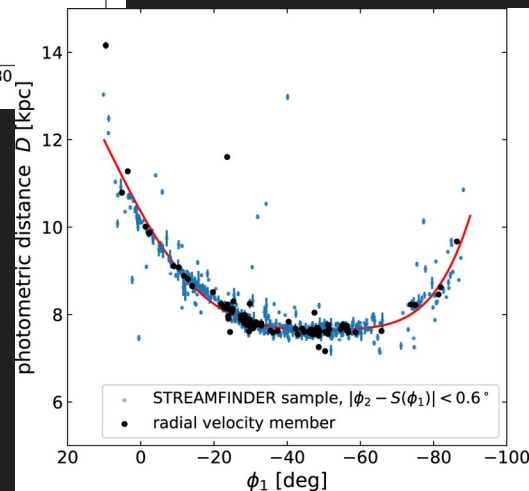


- Can the Gd-1 observables be explained for a Milky Way composed of baryons + fermionic DM model ?

GD-1 observables



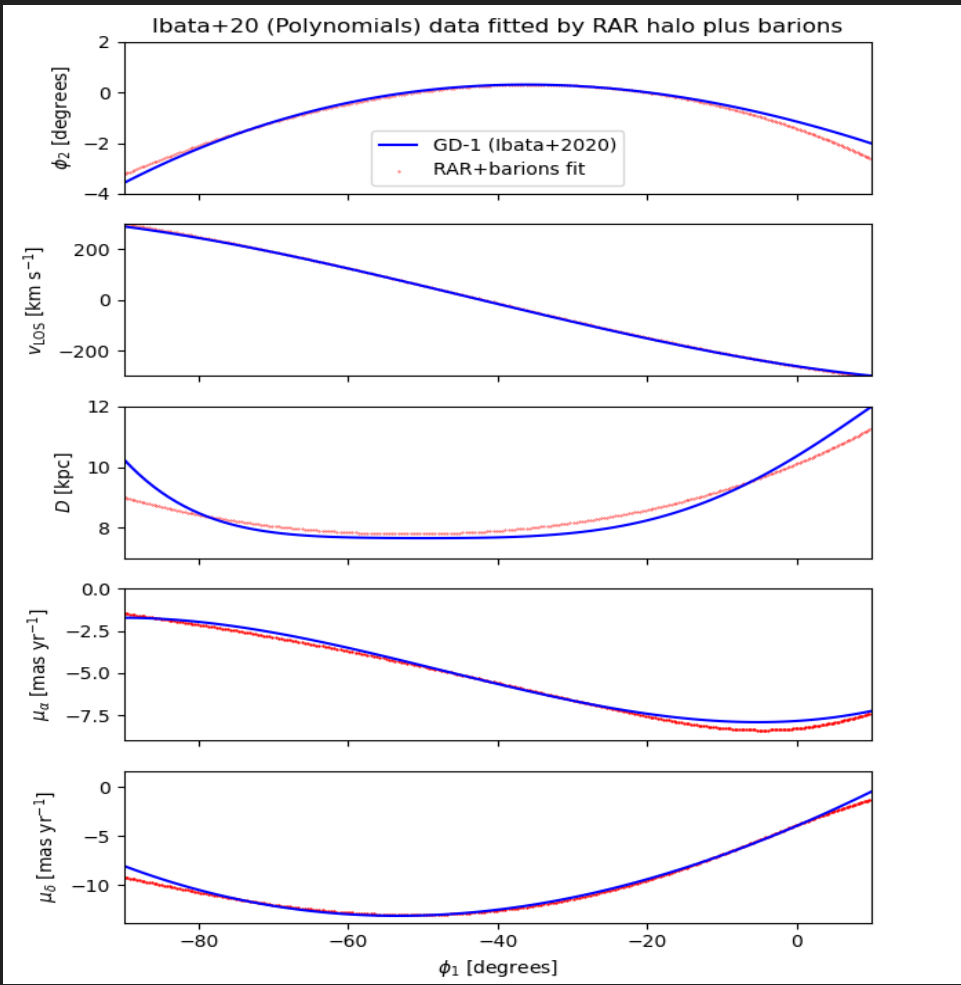
Ibata, et al. Apj (2020)



STREAMFINDER (Gaia DR2): 811 star candidate members;

Cross correlation with spectroscopy: 156 stars in RV sample

Best-fit RAR model parameters to GD-1



Full model: **Galaxy potential + GD-1 stream**

Galaxy potential: RAR(θ_0, W_0) + Baryons (fixed)

(m and β_0 fixed to fulfill $M_c = M_*(\text{SgrA}^*)$
in agreement with S-stars)

GD-1 stream: Orbit (IC) (6 parameters)

We find a best fit parameters

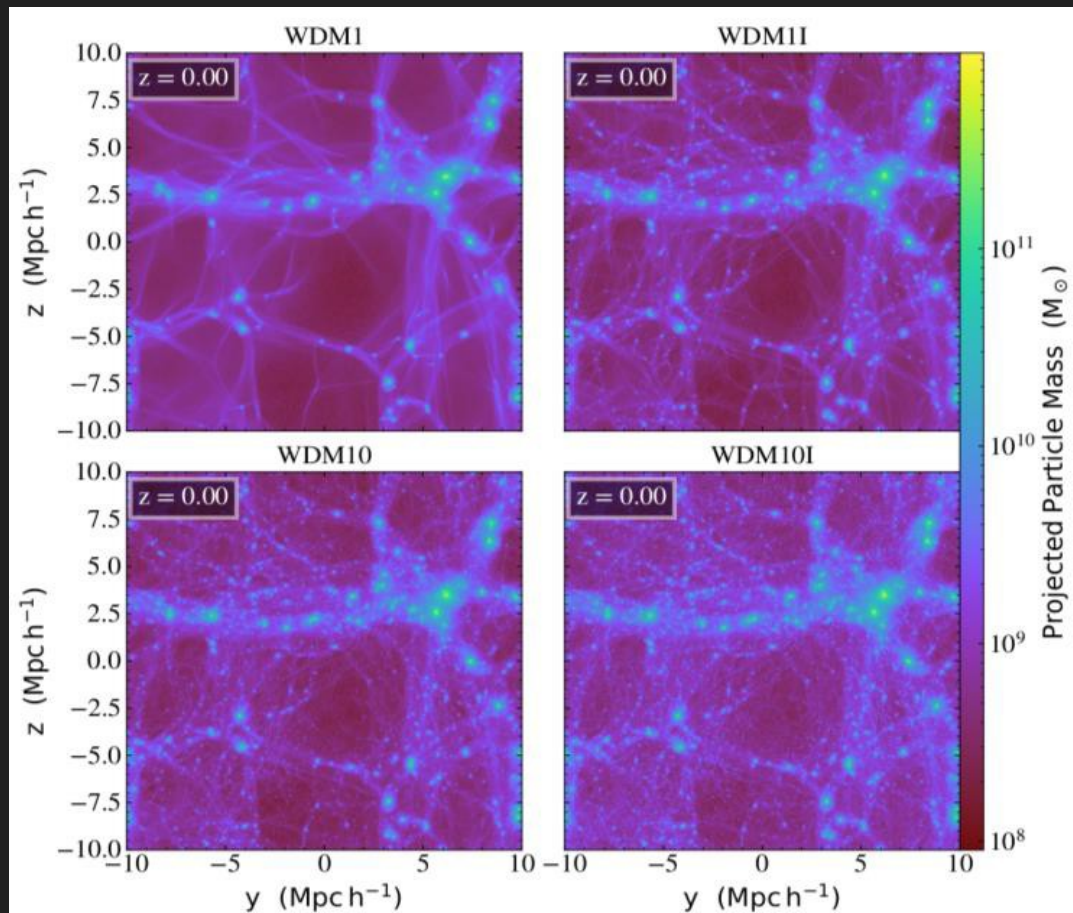
$\theta_0 = 36.2$; $W_0 = 63.6$

In Good agreement with overall rotation curve
(independent tracer!)

Mestre, Argüelles, et al. (In preparation)

Applications: Cosmological Scales (non linear regime)

N-body simulations in SI-WDM cosmologies (Gadget-4)



4 cosmologies ($z=0$),
corresponding to different
Power Spectrums within a SI-
WDM model: (Box size: 20
Mpc/h; $N=512^3$ particles,
softening length: 1 kpc)

WDM1: $m=1$ keV

WDM1 I : $m=1$ keV ($C_v \neq 0$)

WDM10: $m=10$ keV

WDM10 I: $m=10$ keV ($C_v \neq 0$)

On the growth of supermassive black holes formed from the gravitational collapse of fermionic dark matter cores

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ABSTRACT

Observations support the idea that supermassive black holes (SMBHs) power the emission at the center of active galaxies. However, contrary to stellar-mass BHs, there is a poor understanding of their origin and physical formation channel. In this article, we propose a new process of SMBH formation in the early Universe that is not associated with baryonic matter (massive stars) or primordial cosmology. In this novel approach, SMBH seeds originate from the gravitational collapse of fermionic dense dark matter (DM) cores that arise at the center of DM halos as they form. We show that such a DM formation channel can occur before star formation, leading to heavier BH seeds than standard baryonic channels. The SMBH seeds subsequently grow by accretion. We compute the evolution of the mass and angular momentum of the BH using a geodesic general relativistic disk accretion model. We show that these SMBH seeds grow to $\sim 10^9 - 10^{10} M_{\odot}$ in the first Gyr of the lifetime of the Universe without invoking unrealistic (or fine-tuned) accretion rates.

Key words: galaxies: nuclei — quasars: supermassive black holes — galaxies: formation — galaxies: structure — galaxies: high-redshift — dark matter