

Cosmology 2023 in Miramare,

Aug 28 – Sep 2,

Trieste, Italy



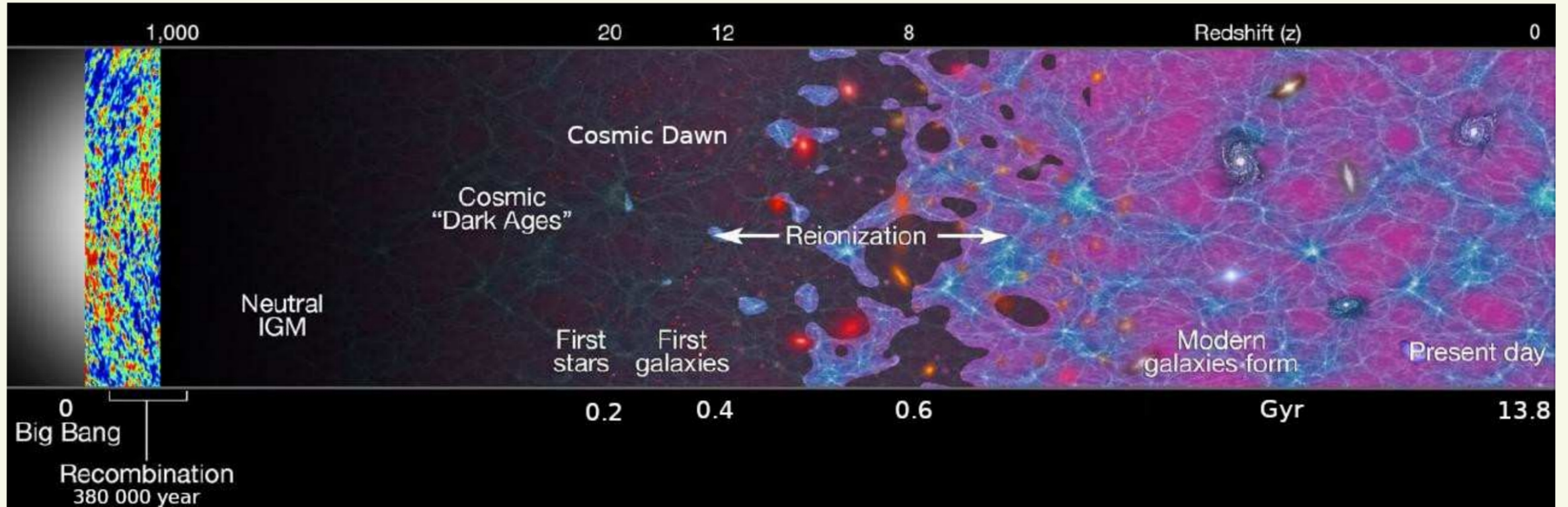
Global signal in the redshifted 21-cm line from Dark Ages as a cosmology test

B. Novosyadlyj^{1,2}, Yu. Kulinich¹

¹Ivan Franko National University of Lviv, Lviv, Ukraine

²International Center of Future Science, Jilin University, Changchun, China

Dark Ages: physical conditions



Robertson et al., Nature, 468, 49 (2010)

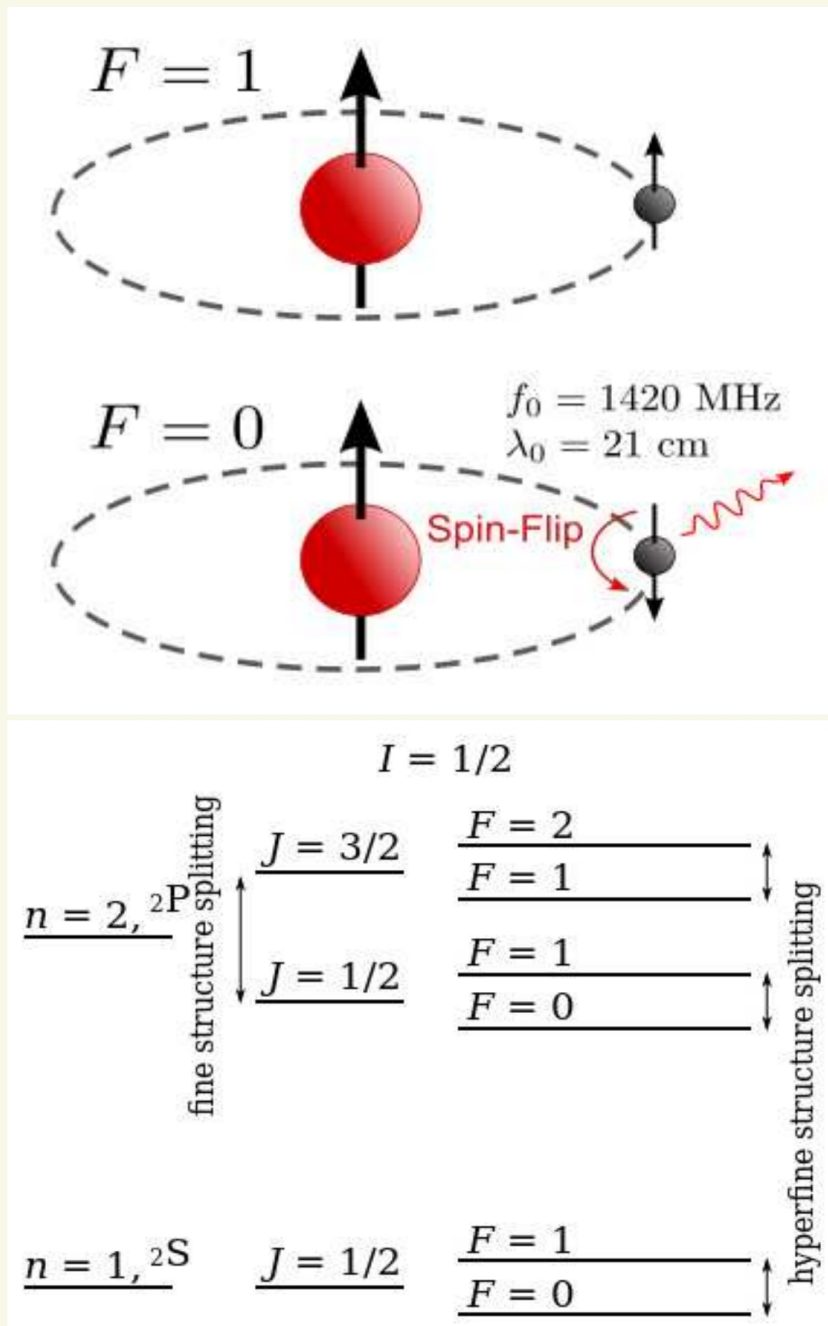
Physical conditions at $z = [1000 - 6]$:

$$T_{cmb} = [2730 - 20] \text{ K}, \quad T_m = [2730 - 2.0] \text{ K},$$

$$n_H = [2 \cdot 10^2 - 9 \cdot 10^{-5}] \text{ cm}^{-3}, \quad n_\gamma = 2 \cdot 10^9 n_b,$$

$$J_{fl}(\nu, z) > 0 \text{ at } z < 50.$$

Hydrogen atom lines: hyperfine 21-cm

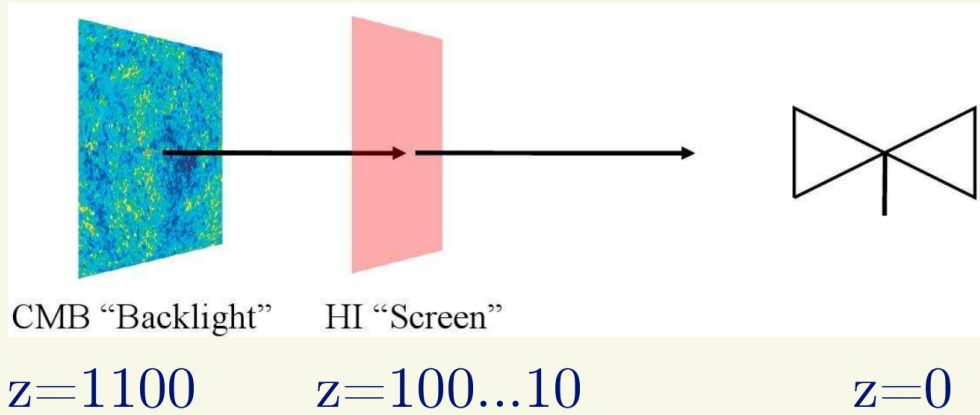


Theoretically predicted by H. van de Hulst in 1945.

It was first observed in 1951 by Evan & Purcel (Harvard University) and Muller & Oort (Leyden Radio Observatory).

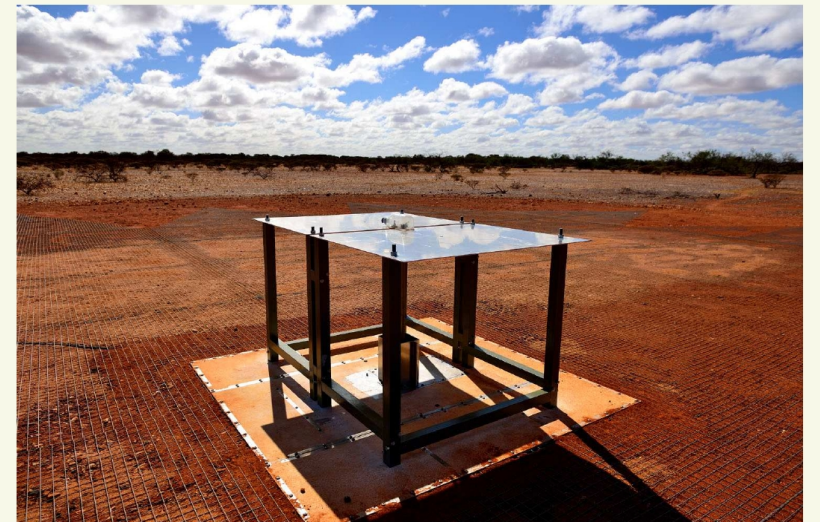
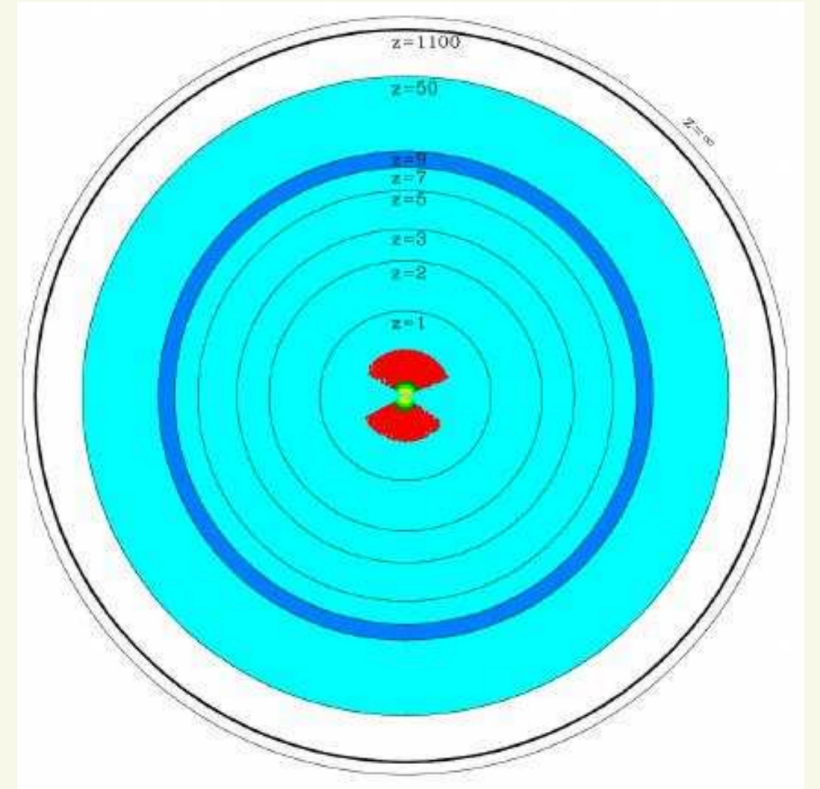
The possibility of 21-cm line emission or absorption by neutral H at high redshift has been considered by Hogan & Rees (1979), Scott & Rees (1990), Subramanian & Padmanabhan (1993), Kumar, Padmanabhan & Subramanian (1995), Bagla, Nath & Padmanabhan (1997), Madau, Meiksen & Rees (1997), Shaver et al. (1999), Tozzi et al. (2000), Zaldariaga et al. (2004):

H 21 cm line from the Dark Ages



The line is 21 cm in its own frame of reference: $\lambda_0 = 21$ cm,
 $\nu_0 = 1420$ MHz,
 $T_* \equiv h_P \nu_0 / k_B = 0.068$ K;

The 21 cm line in the Earth observer’s frame of reference:
 $\lambda_z = \lambda_0(1 + z)$, $\nu_z = \nu_0 / (1 + z)$;



$$-(1+z)H \frac{dx_{\text{HII}}}{dz} = R_{\text{HI}}x_{\text{HI}} + C_i n_i x_{\text{HI}} - \alpha_{\text{HII}} x_{\text{HII}} + \left[(1+z)H \frac{dx_{\text{HII}}}{dz} \right]_{n\text{SM}},$$

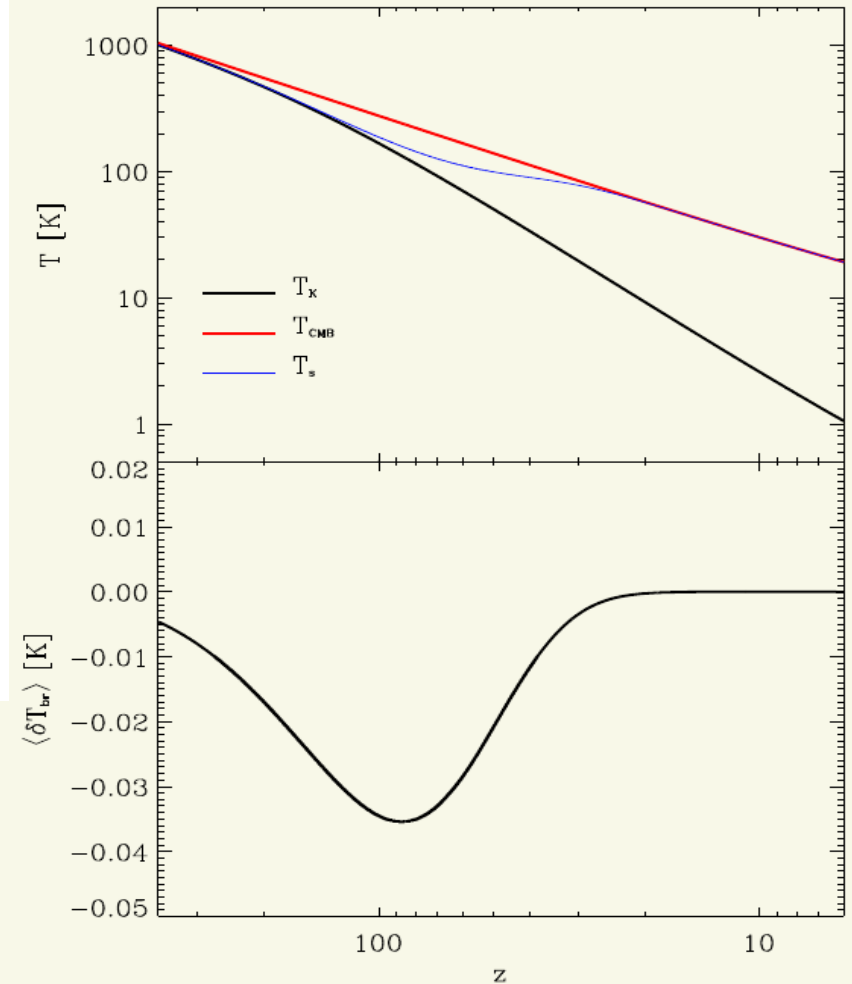
$$-\frac{3}{2} n_{\text{tot}} k_B (1+z) H(z) \frac{dT_b}{dz} = \Gamma_{\text{C}_{\text{cmb}}} - \Lambda_{\text{ad}} + \Gamma_{n\text{SM}} - \Lambda_{n\text{SM}},$$

$$H = H_0 \sqrt{\Omega_r (1+z)^4 + \Omega_m (1+z)^3 + \Omega_\Lambda},$$

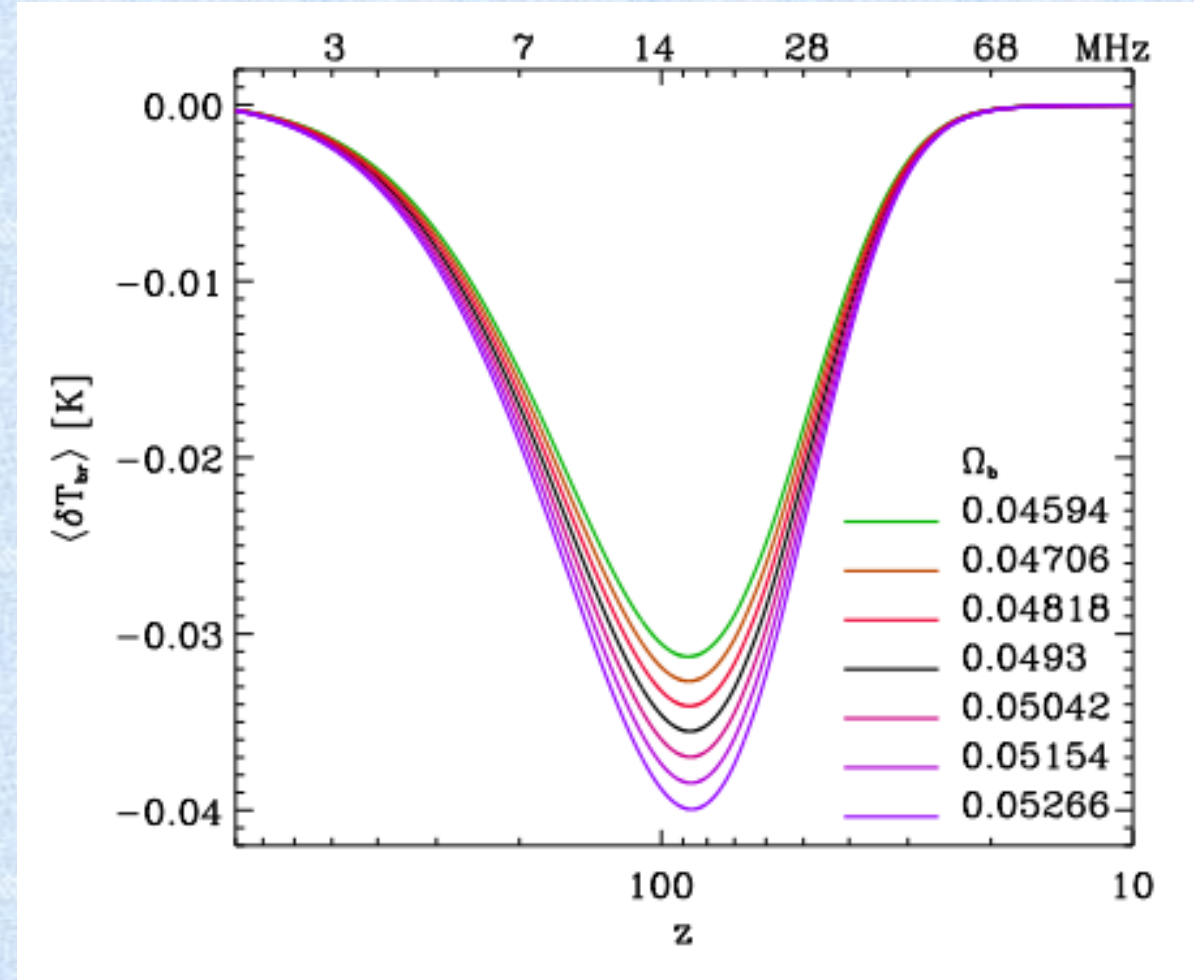
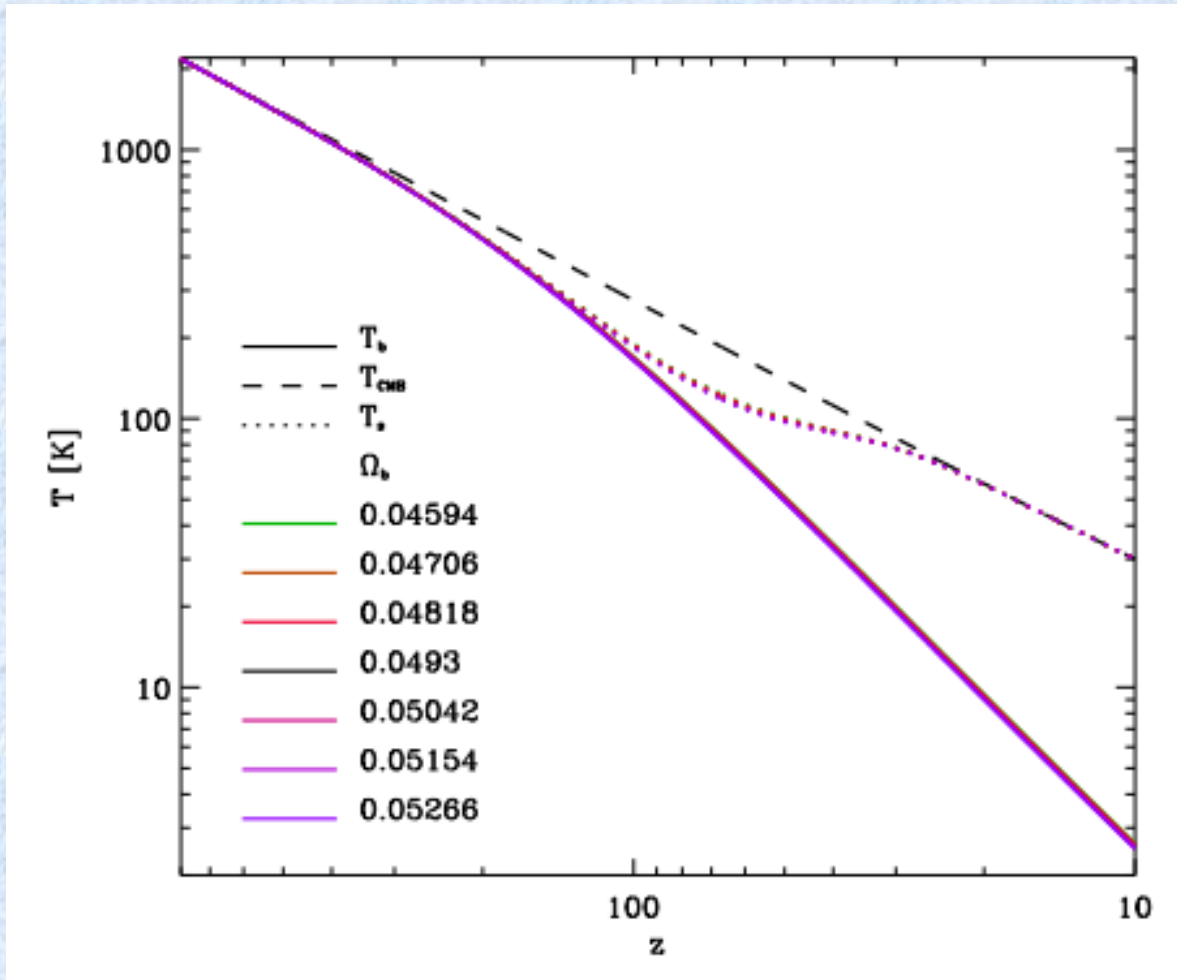
$$T_s \equiv \frac{k_B}{h_P \nu_{10}} \ln \frac{g_1 n_0}{g_0 n_1},$$

$$T_s = T_m(z) \frac{A_{10} T_{\text{cmb}}(z) + T_* C_{10}}{A_{10} T_m(z) + T_* C_{10}} \text{ K}$$

$$\delta T_{\text{br}}(z) = 0.023 (1 + \delta_b) x_{\text{HI}} \left[\left(\frac{0.15}{\Omega_m} \right) \left(\frac{1+z}{10} \right) \right]^{\frac{1}{2}} \left(\frac{\Omega_b h}{0.02} \right) \left[1 - \frac{T_{\text{cmb}}(z)}{T_s(z)} \right] \text{ K}$$



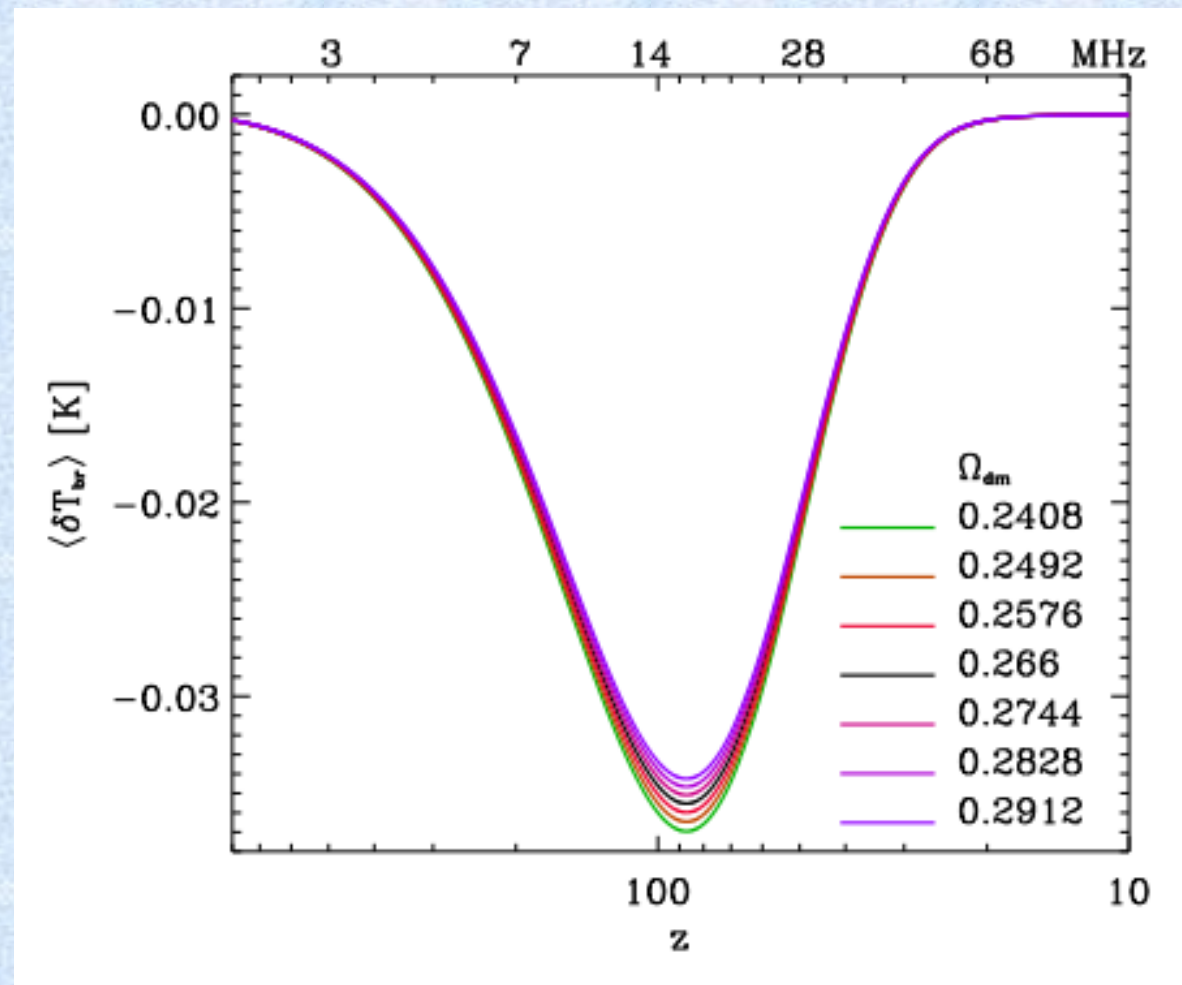
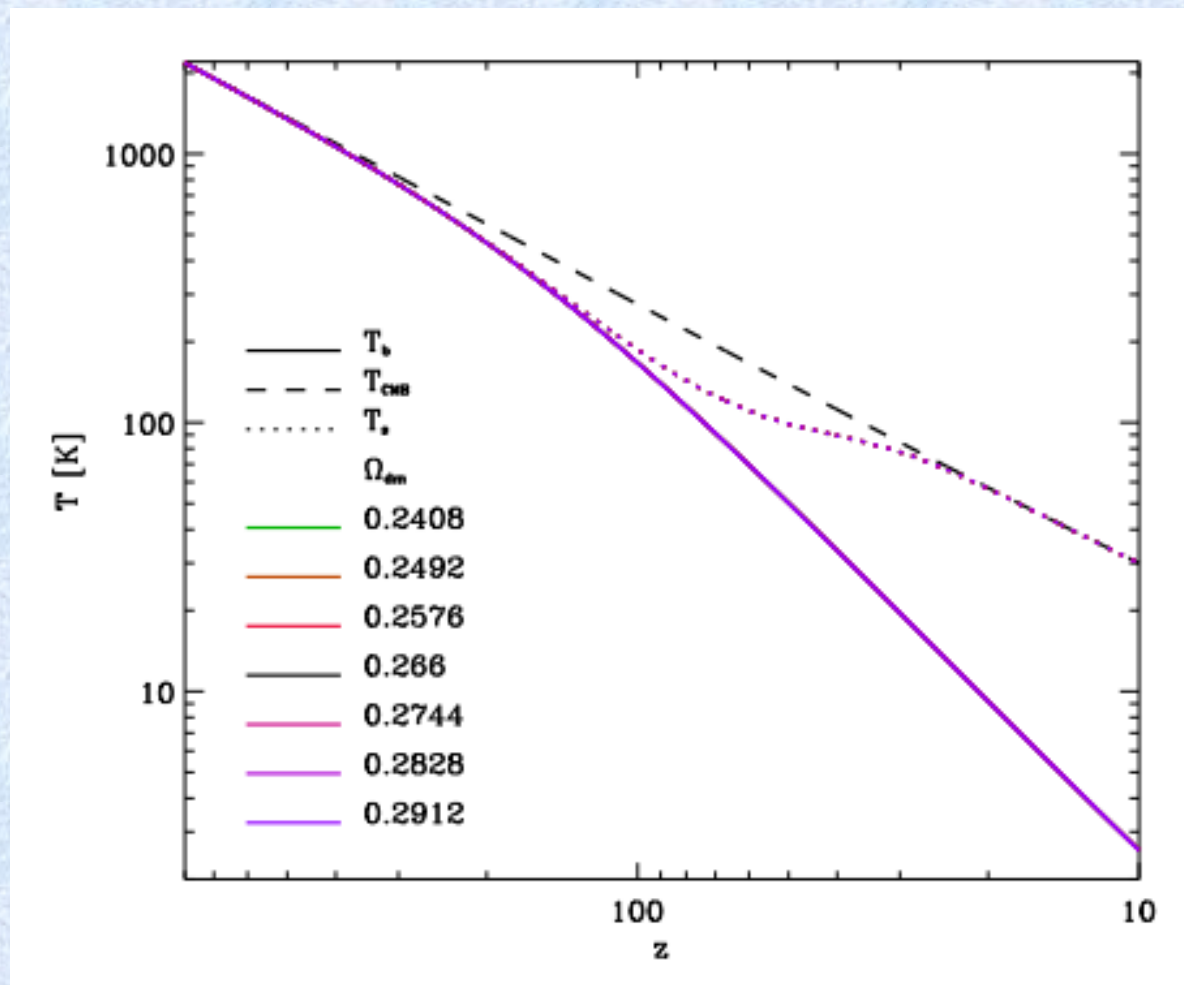
Standard cosmology: dependence on Ω_b



$$\Omega_b + \Omega_{\text{dm}} + \Omega_{\Lambda} + \Omega_K = 1, \quad \Delta\Omega_b = -\Delta\Omega_{\Lambda}$$

$\Omega_b=0.0493$, $\Omega_{\text{dm}}=0.266$, $\Omega_{\Lambda}=0.6847$, $\Omega_K=0$, $H_0=67.36$ km/s·Mpc (*Planck collaboration, 2020*)

Standard cosmology: dependence on Ω_{dm}

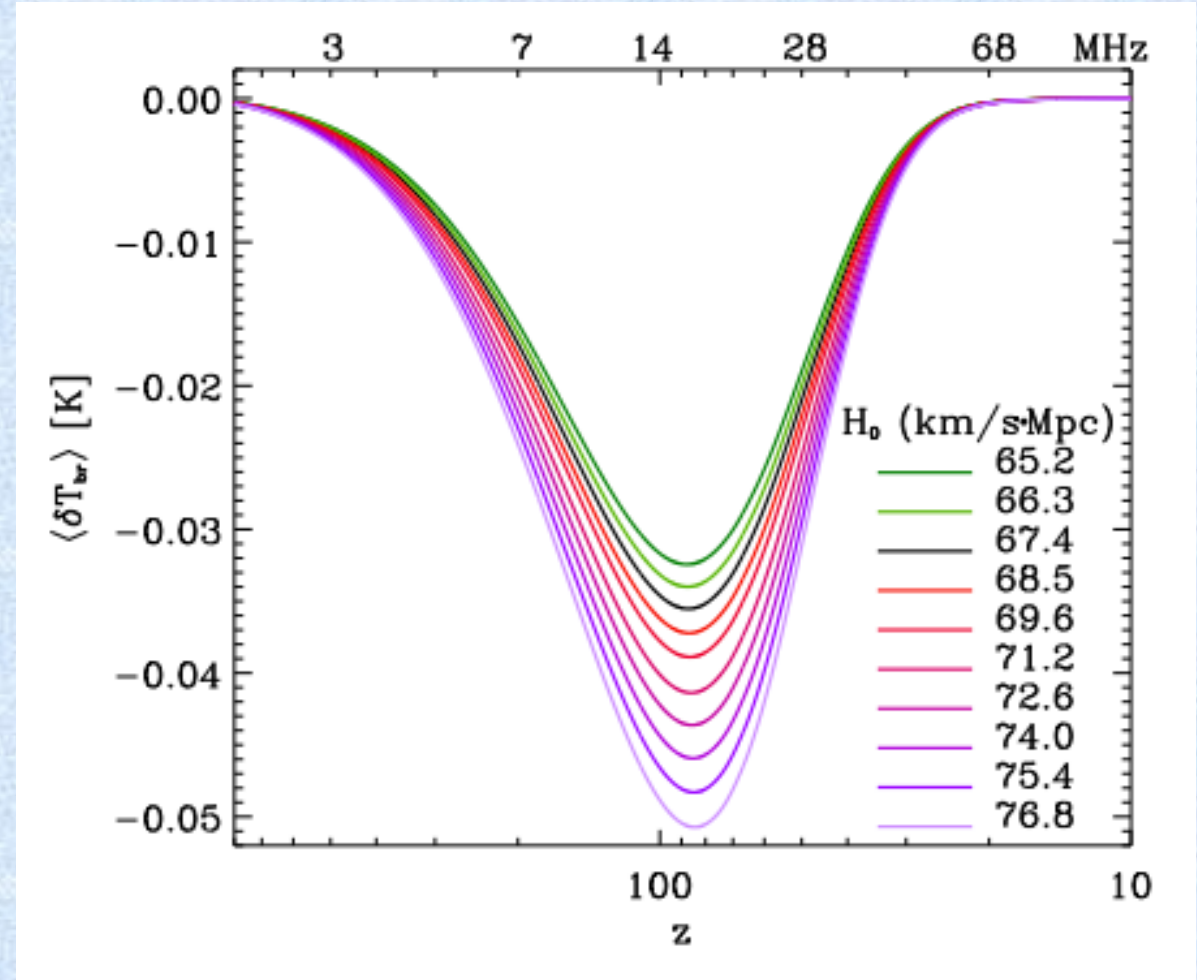
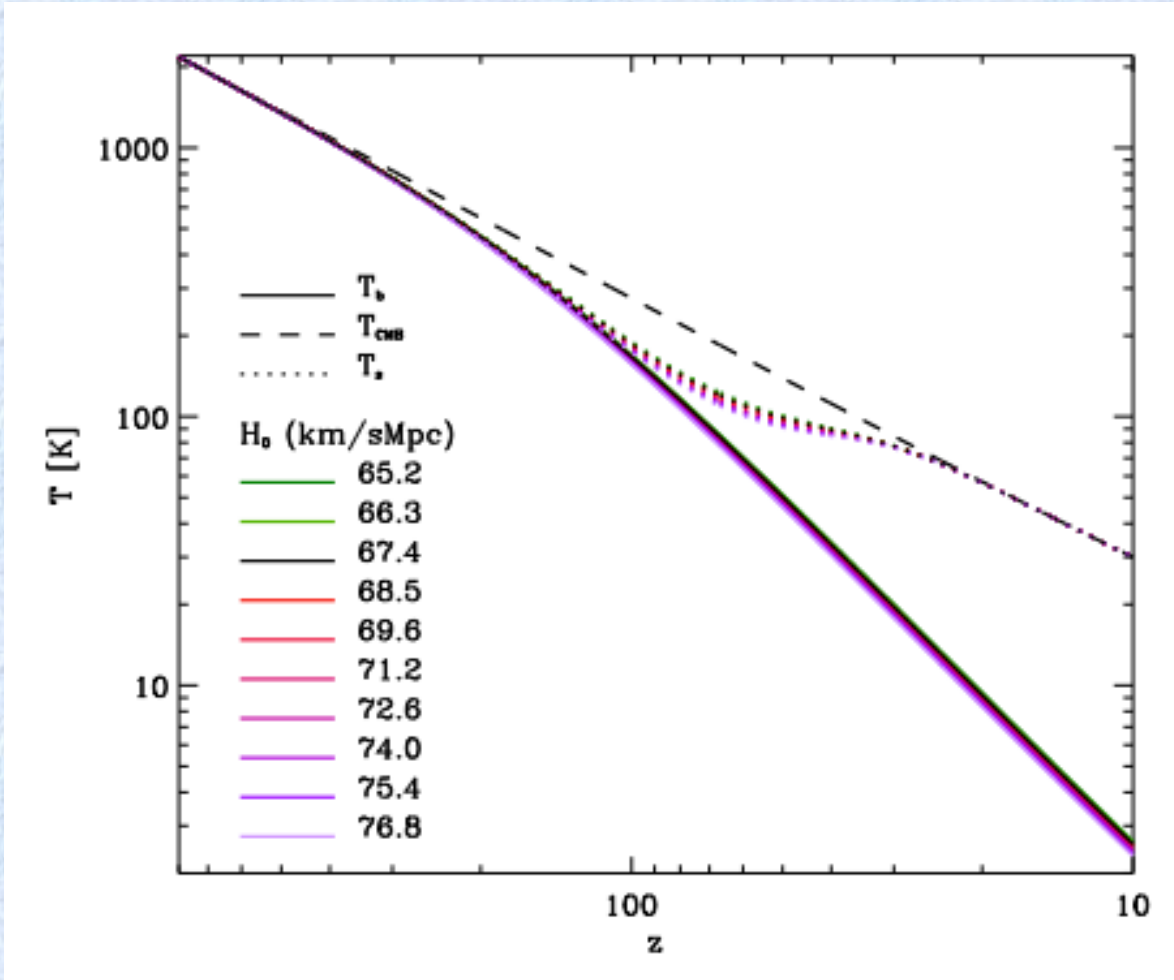


$$\Omega_{\text{b}} + \Omega_{\text{dm}} + \Omega_{\Lambda} + \Omega_{\text{K}} = 1,$$

$$\Delta\Omega_{\text{dm}} = -\Delta\Omega_{\Lambda}$$

$\Omega_{\text{b}}=0.0493$, $\Omega_{\text{dm}}=0.266$, $\Omega_{\Lambda}=0.6847$, $\Omega_{\text{K}}=0$, $H_0=67.36$ km/s·Mpc (*Planck collaboration, 2020*)

Standard cosmology: dependence on H_0

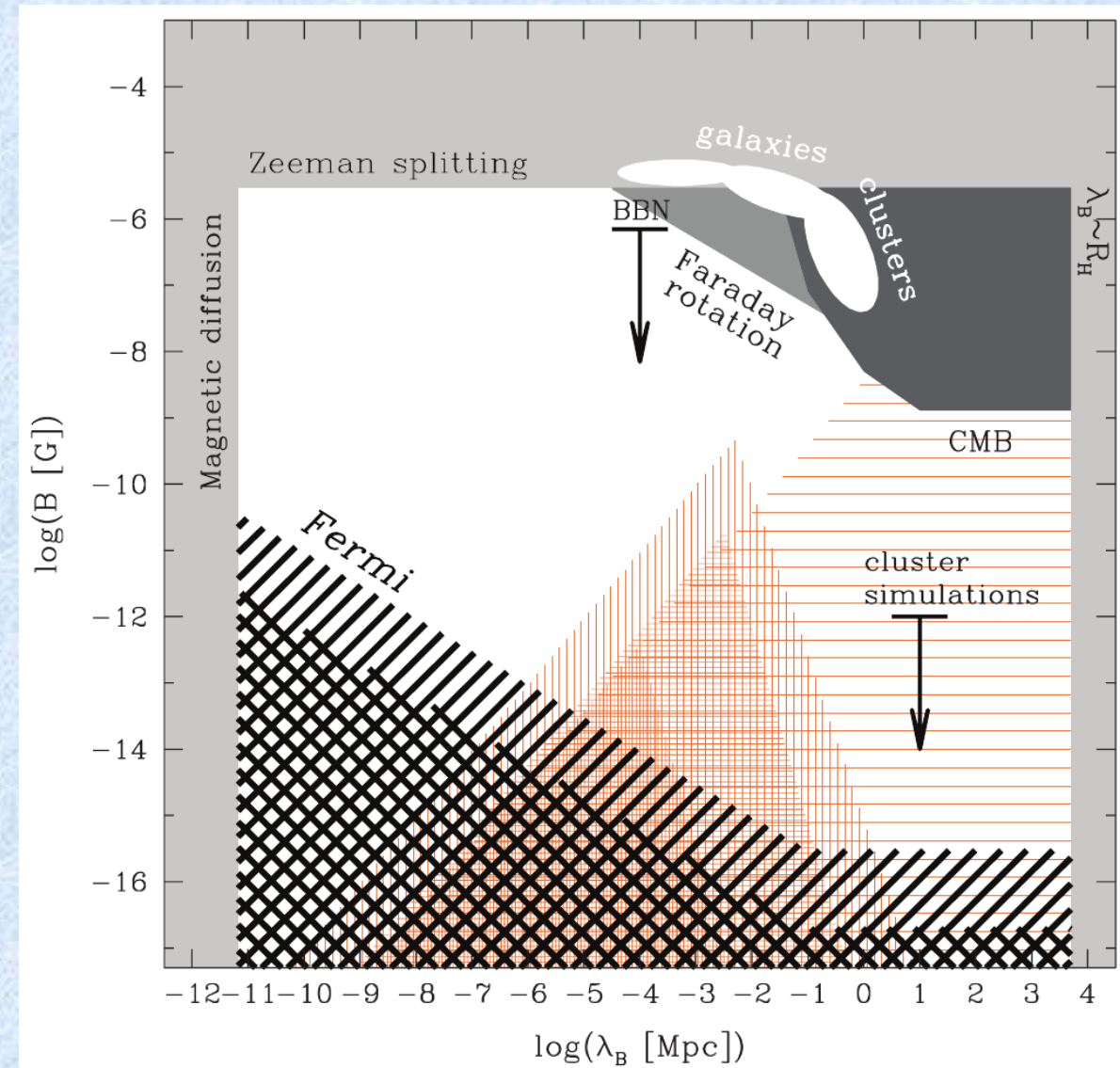


$\Omega_b=0.0493$, $\Omega_{\text{dm}}=0.266$, $\Omega_\Lambda=0.6847$, $\Omega_K=0$, $H_0=67.36$ km/s·Mpc (*Planck collaboration, 2020*)

Non-standard cosmology: primordial stochastic magnetic field

Heating of baryonic gas caused by

- decaying magnetic turbulence,
- ambipolar diffusion



Heating due to decaying turbulence of the primordial magnetic field (Sethi & Subramanian 2005; Chluba et al. 2015):

$$\begin{aligned}\Gamma_{mf dt} &= 1.5\rho_{mf}H(z)[f_D(z)]^{n_B+3}\frac{ma^m}{(a+1.5\ln((1+z_{cr})/(1+z)))^{m+1}} \quad \text{for } z < z_{cr}, \\ \Gamma_{mf dt} &= 1.5\rho_{mf}H(z)\frac{m}{a}[f_D(z)]^{n_B+3}\exp\left\{-\frac{(z-z_{cr})^2}{5000}\right\}\left(\frac{1+z_{cr}}{1+z}\right)^4 \quad \text{for } z \geq z_{cr},\end{aligned}\quad (42)$$

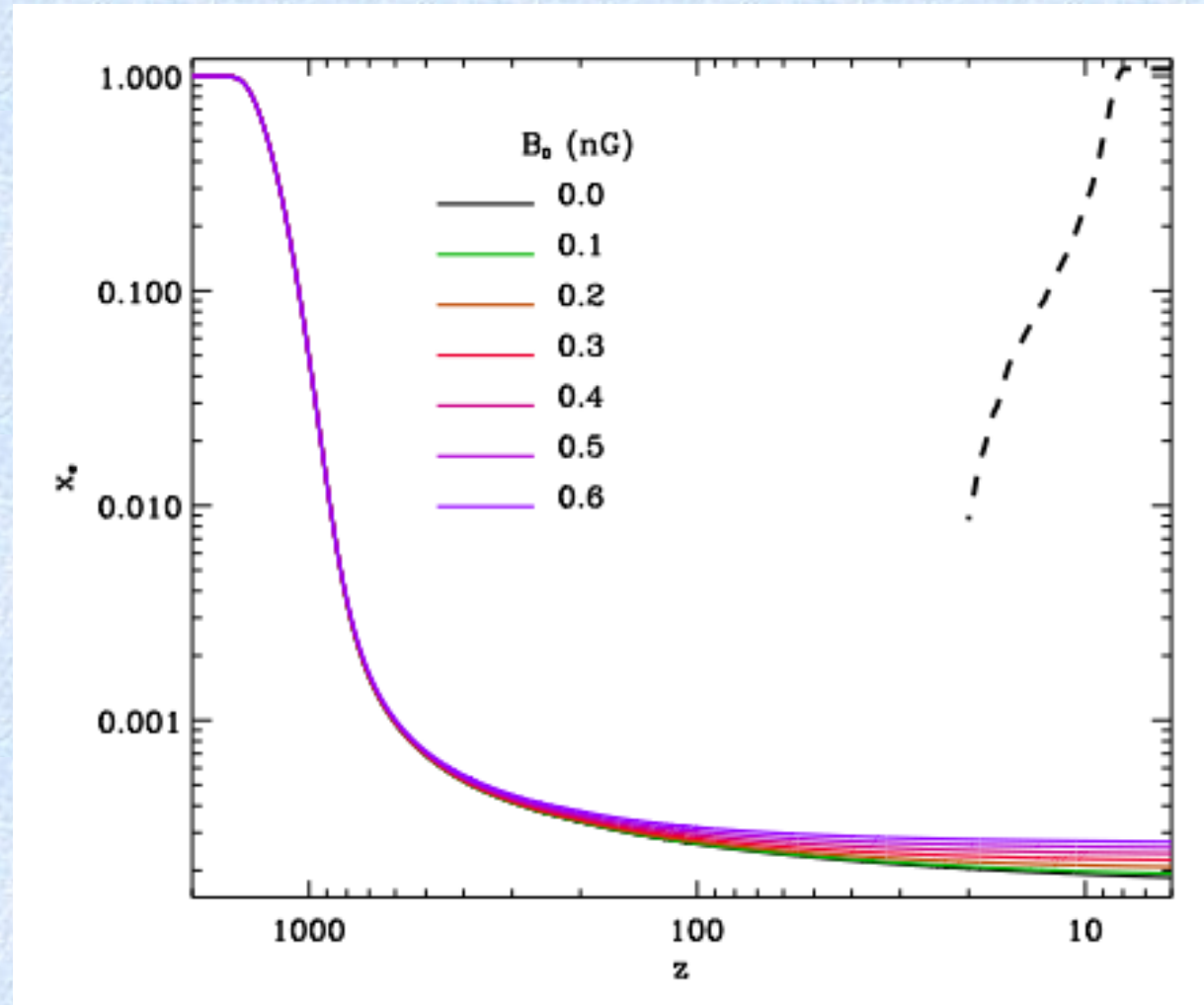
where $z_{cr} = 1088$, $\rho_{mf} = 3.98 \cdot 10^{-21} (B_0/\text{nG})^2 (1+z)^4 \text{ J}\cdot\text{m}^{-3}$, $n_B = -2.9$, $a = \ln(1+t_d/t_{\text{rec}})$, $m \equiv 2(n_B+3)/(n_B+5)$, $t_d/t_{\text{rec}} = 14.8/(B_0k_D)$, $k_D = (2.89 \cdot 10^4 h)^{1/(n_B+5)} B_\lambda^{-2/(n_B+5)} k_\lambda^{(n_B+3)/(n_B+5)} \text{ Mpc}^{-1}$, $\lambda = 1 \text{ Mpc}$, $B_\lambda = B_{1\text{Mpc}} = B_0$, $k_\lambda = k_{1\text{Mpc}} = 2\pi \text{ Mpc}^{-1}$. The factor $f_D(z)^{n_B+3}$ describes the energy loss by the primordial magnetic field (see Minoda et al. (2019)), which we approximate as $[f_D(z)]^{n_B+3} \simeq 0.6897525 + 0.2944149 \cdot 10^{-3}z - 0.3805730 \cdot 10^{-6}z^2 + 0.2259742 \cdot 10^{-9}z^3 + 0.6354026 \cdot 10^{-13}z^4$ for $z < 1178$, fixed values of n_B and k_D (for $z \geq 1178$ $f^{n_B+3}(z) \equiv 1$).

Heating due to ambipolar diffusion caused by the primordial magnetic field (Chluba et al. 2015; Minoda et al. 2019):

$$\Gamma_{mf ad} = \frac{1-x_{\text{HII}}}{g(T_b)x_{\text{HII}}}[f_D(z)]^{2n_B+8}\left[\frac{(1+z)k_D}{3.086 \cdot 10^{22}}\frac{\rho_{mf}}{\rho_b}\right]^2 f_L, \quad (43)$$

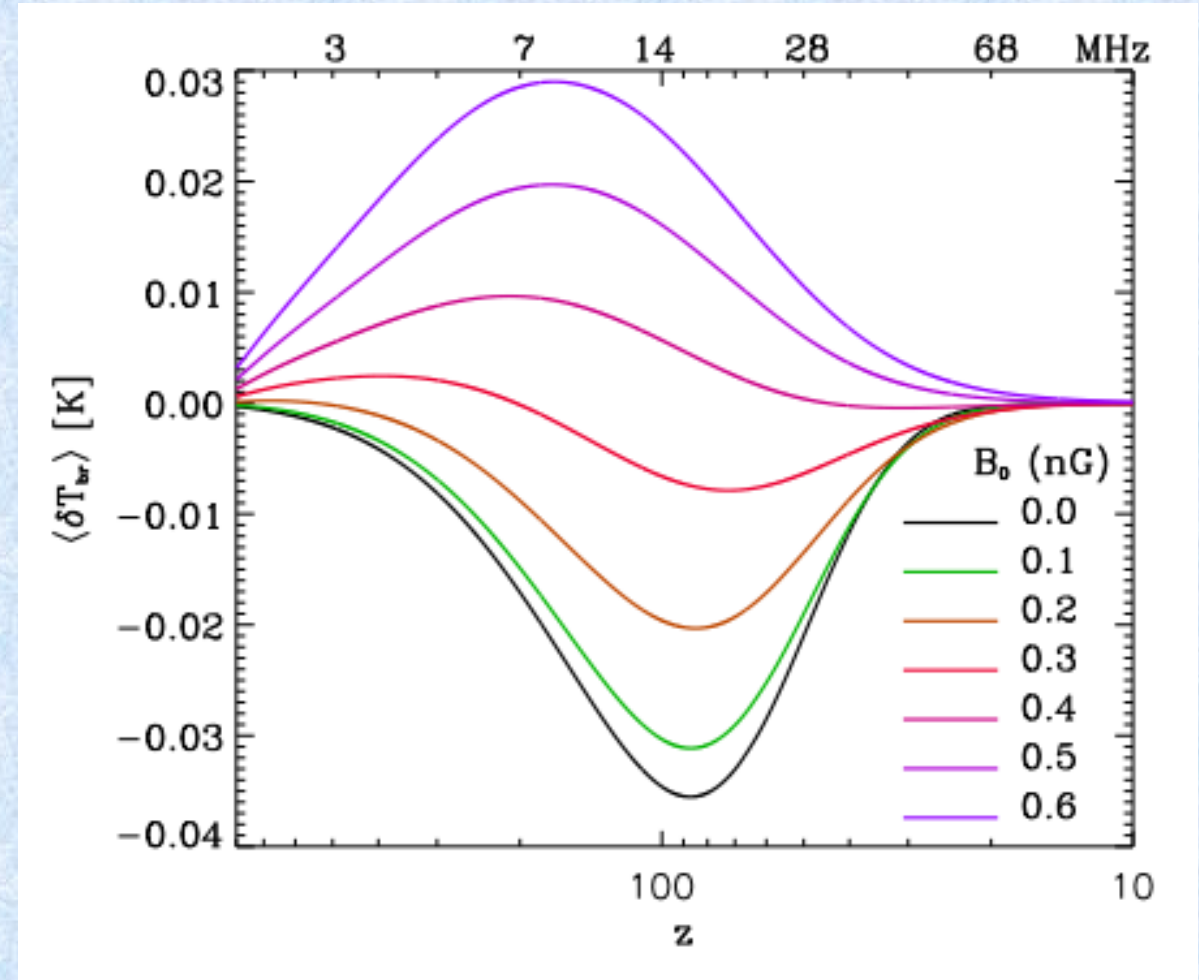
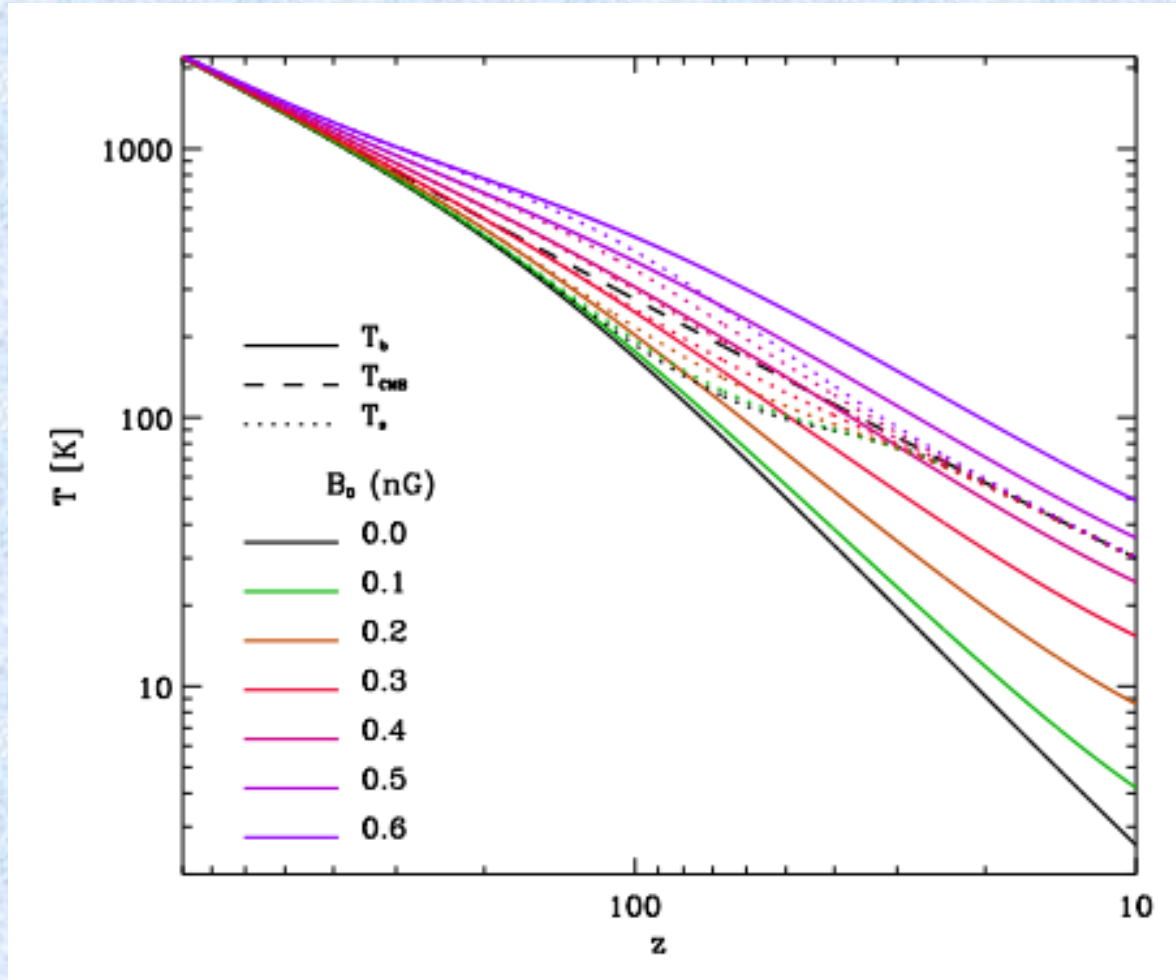
where $x_{\text{HII}} = n_{\text{HII}}/n_H$, $f_L = 0.8313(n_B+3)^{1.105}(1.0 - 0.0102(n_B+3))$, $g(T_b) = 1.95 \cdot 10^{11}T_b^{0.375} \text{ m}^3/\text{s}/\text{kg}$, $\rho_b = \rho_{cr}^{(0)}\Omega_b(1+z)^3$, $k_D = 286.91(B_0/\text{nG})^{-1} \text{ Mpc}^{-1}$.

Non-standard cosmology: primordial magnetic field, ionization



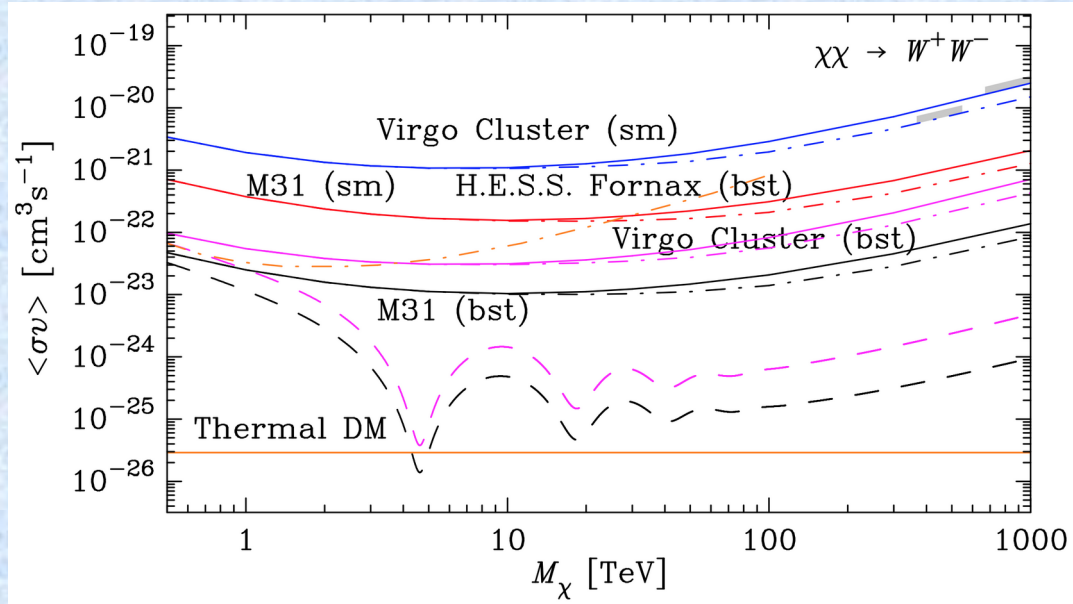
SM: $\Omega_b=0.0493$, $\Omega_{dm}=0.266$, $\Omega_\Lambda=0.6847$, $\Omega_K=0$, $H_0=67.36$ km/s·Mpc (Planck collaboration, 2020)

Non-standard cosmology: primordial magnetic field



SM: $\Omega_b=0.0493$, $\Omega_{\text{dm}}=0.266$, $\Omega_\Lambda=0.6847$, $\Omega_K=0$, $H_0=67.36$ km/s·Mpc (Planck collaboration, 2020)

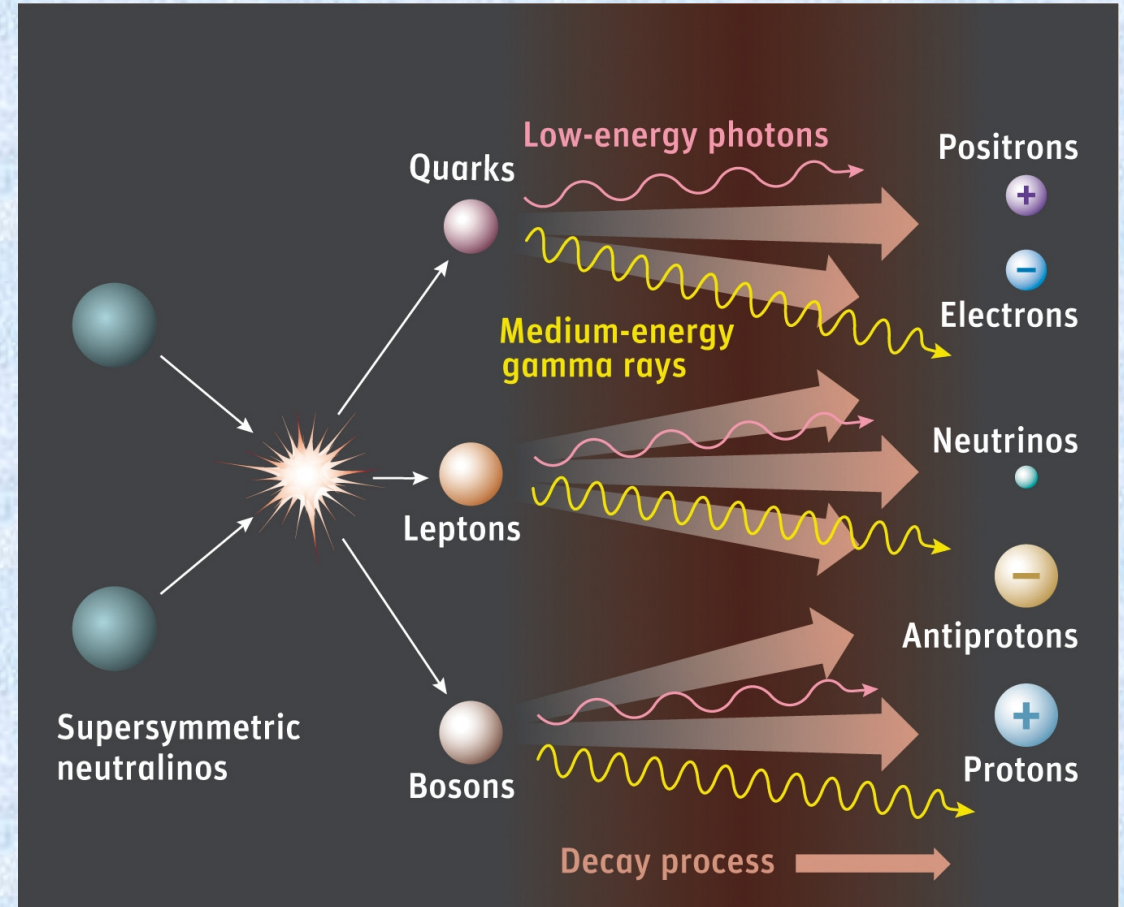
Non-standard cosmology: self-annihilating dark matter



Abeyskara et al. [HAWC Collaboration]. PRD, 90, 122002 (2014)

Energy deposit into

- heating of baryonic gas,
- ionization of hydrogen and helium,
- excitation of atoms and molecules



Marcus Woo, Fermi Gamma-ray Space Telescope

Non-standard cosmology: self-annihilation dark matter, ionization

The heating function of baryonic matter and the rate of ionization of hydrogen and helium atoms due to self-annihilation of dark matter particles ([Chluba 2010](#)):

$$\Gamma_{dman} = 1.6 \cdot 10^{-12} g_h f_{dman} \epsilon_0 n_H (1+z)^3 \text{ erg/cm}^3\text{s},$$

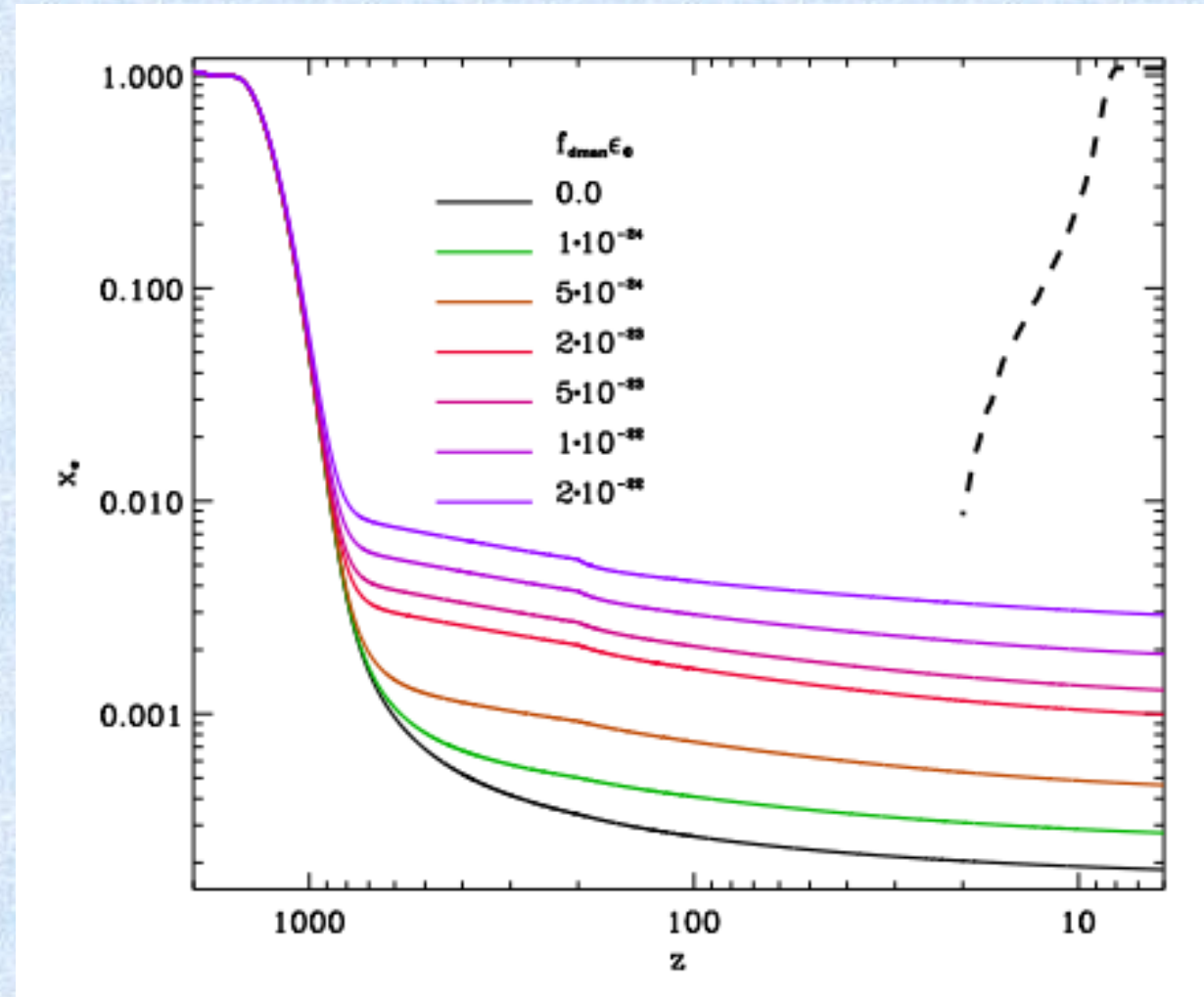
$$\frac{dx_{HI}}{dt} = -7.35 \cdot 10^{-2} g_{ion}^{(HI)} \frac{f_{dman} \epsilon_0 n_H}{n_{HI} (1+f_{He})} (1+z)^3,$$

$$\frac{dx_{HeI}}{dt} = 4.065 \cdot 10^{-2} g_{ion}^{(HeI)} \frac{f_{dman} \epsilon_0 n_H f_{He}}{n_{HeI} (1+f_{He})} (1+z)^3.$$

Here

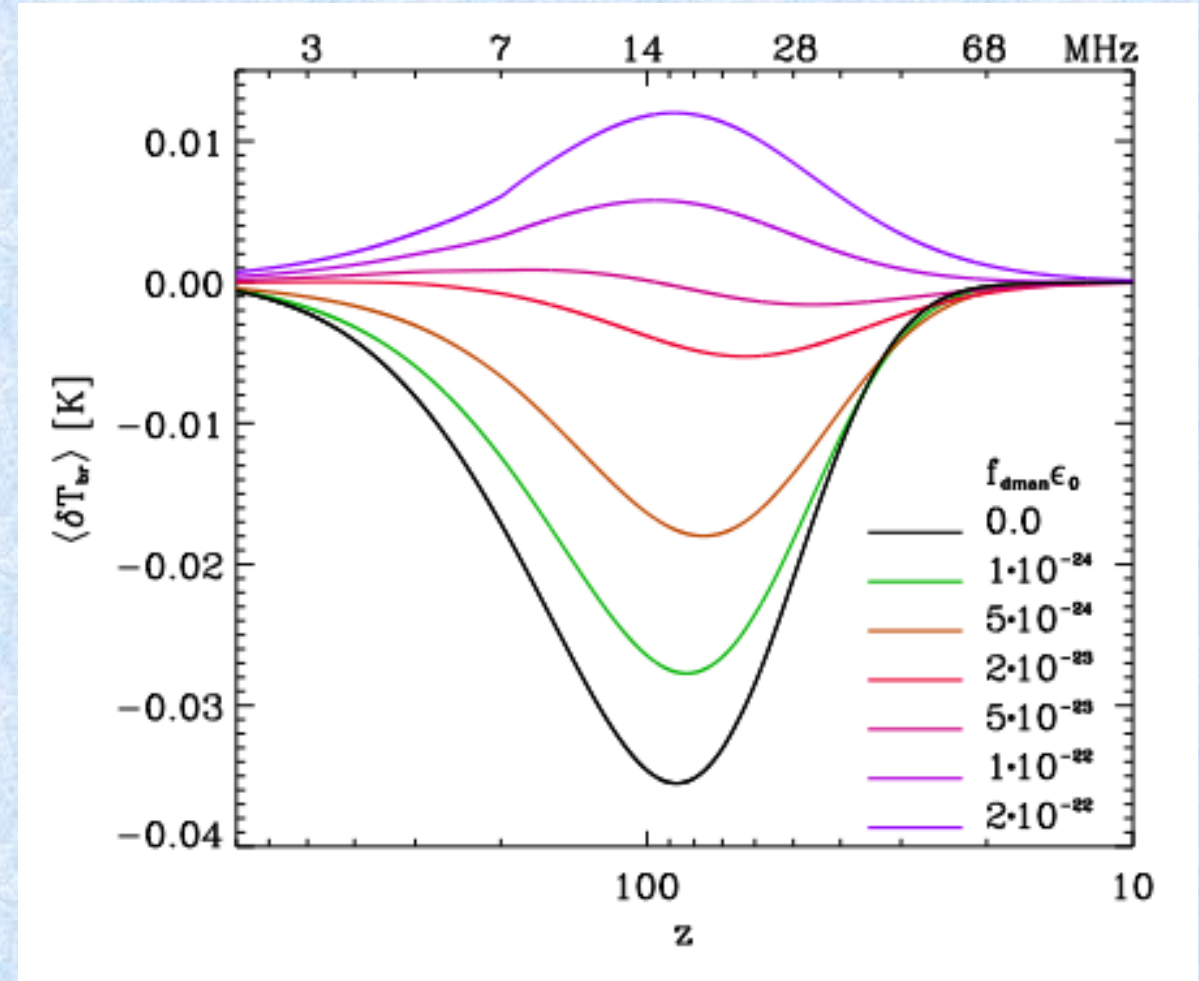
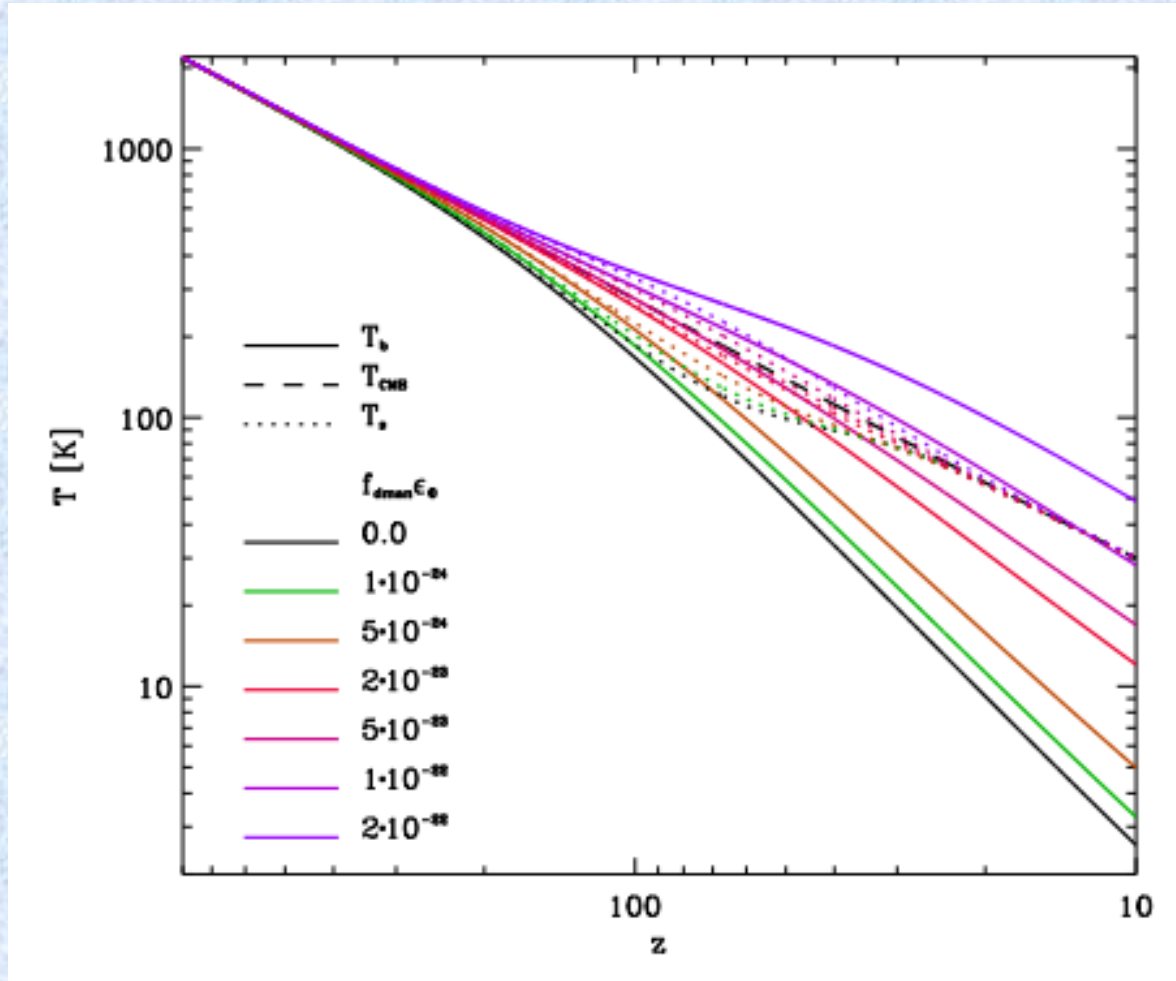
$$\epsilon_0 = 5 \cdot 10^{-25} \left[\frac{100\text{GeV}}{M_{dm}} \right] \left[\frac{\Omega_{dm} h^2}{0.13} \right]^2 \left[\frac{\langle \sigma v \rangle}{10^{-26} \text{cm}^2/\text{s}} \right]$$

is the dimensionless parameter, f_{dman} is fraction of self-annihilating dark matter, and $[n_H] = \text{cm}^{-3}$.



SM: $\Omega_b=0.0493$, $\Omega_{dm}=0.266$, $\Omega_\Lambda=0.6847$, $\Omega_K=0$, $H_0=67.36 \text{ km/s}\cdot\text{Mpc}$ (*Planck collaboration, 2020*)

Non-standard cosmology: self-annihilating dark matter

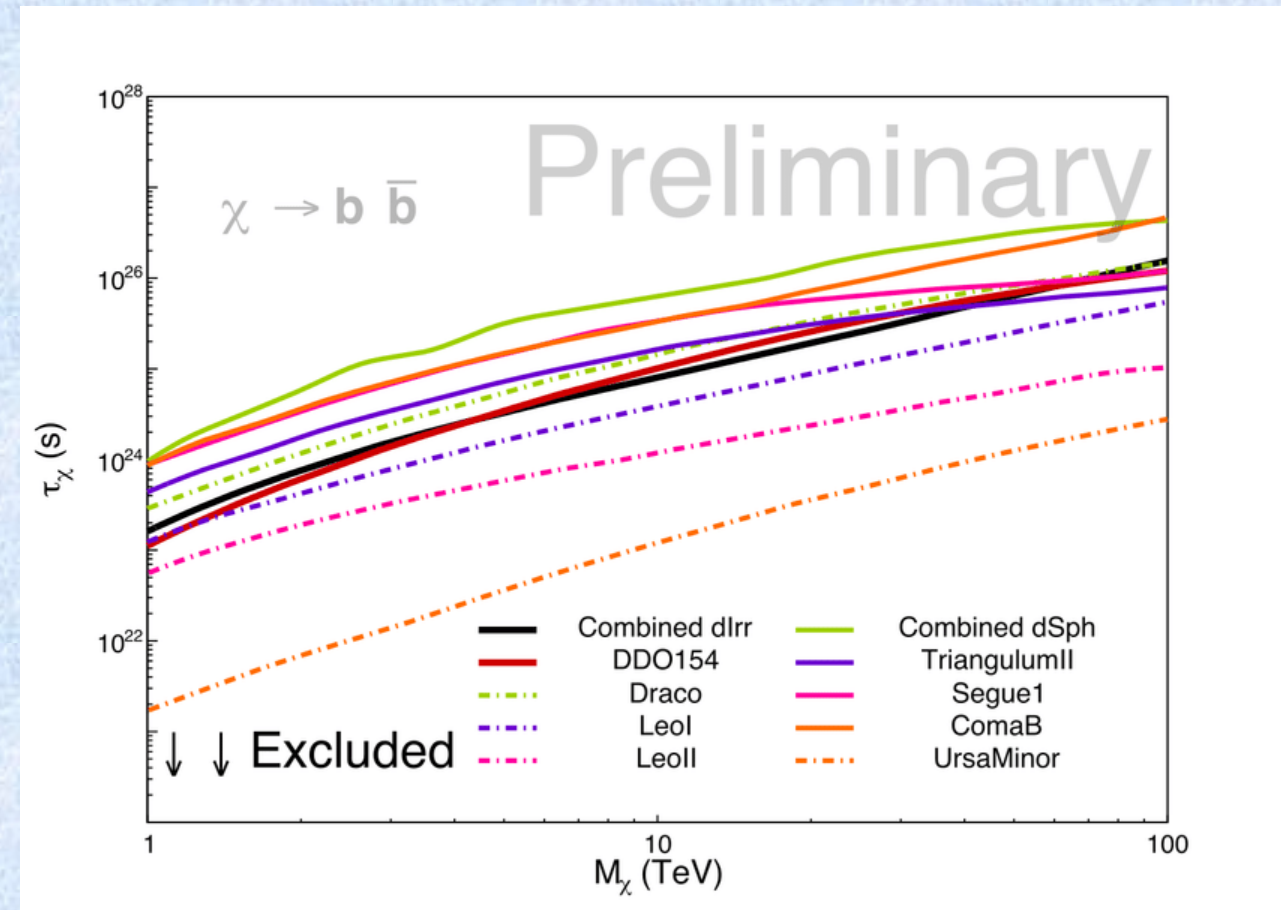


SM: $\Omega_b=0.0493$, $\Omega_{\text{dm}}=0.266$, $\Omega_\Lambda=0.6847$, $\Omega_K=0$, $H_0=67.36$ km/s·Mpc (Planck collaboration, 2020)

Non-standard cosmology: decaying dark matter

Energy deposit into

- heating of baryonic gas,
- ionization of hydrogen and helium,
- excitation of atoms and molecules



Non-standard cosmology: decaying dark matter, ionization

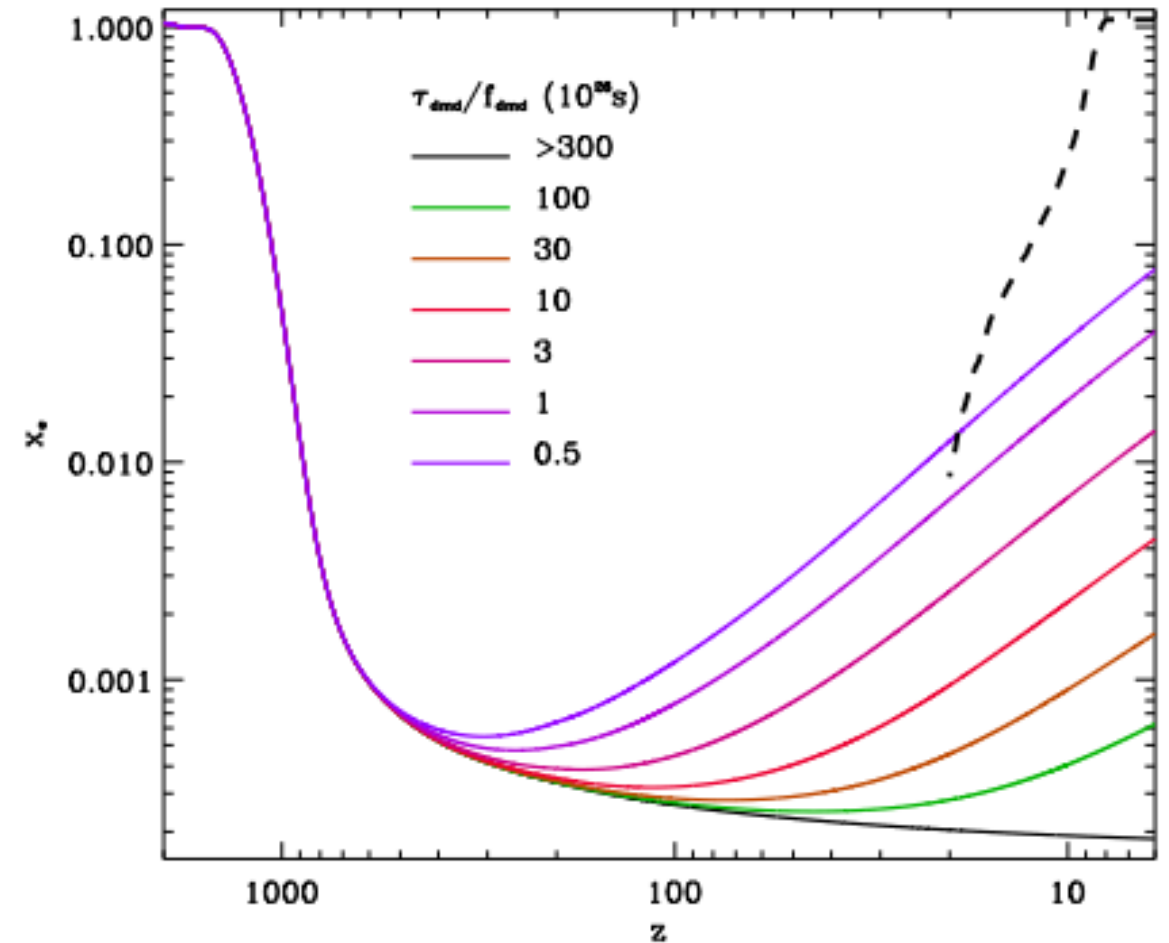
The heating function of baryonic matter and the rate of ionization of hydrogen and helium atoms due to decay of dark matter particles (Chluba 2010; Liu & Slatyer 2018):

$$\Gamma_{dmd} = 1.69 \cdot 10^{-8} g_h \frac{f_{dmd} \Omega_{dm} h^2}{\tau_d} (1+z)^3 \quad \frac{\text{erg}}{\text{cm}^3 \text{s}},$$

$$\frac{dx_{HI}}{dt} = -774.68 g_{ion}^{(HI)} \frac{f_{dmd} \Omega_{dm} h^2}{n_{HI} \tau_d (1+f_{He})} (1+z)^3,$$

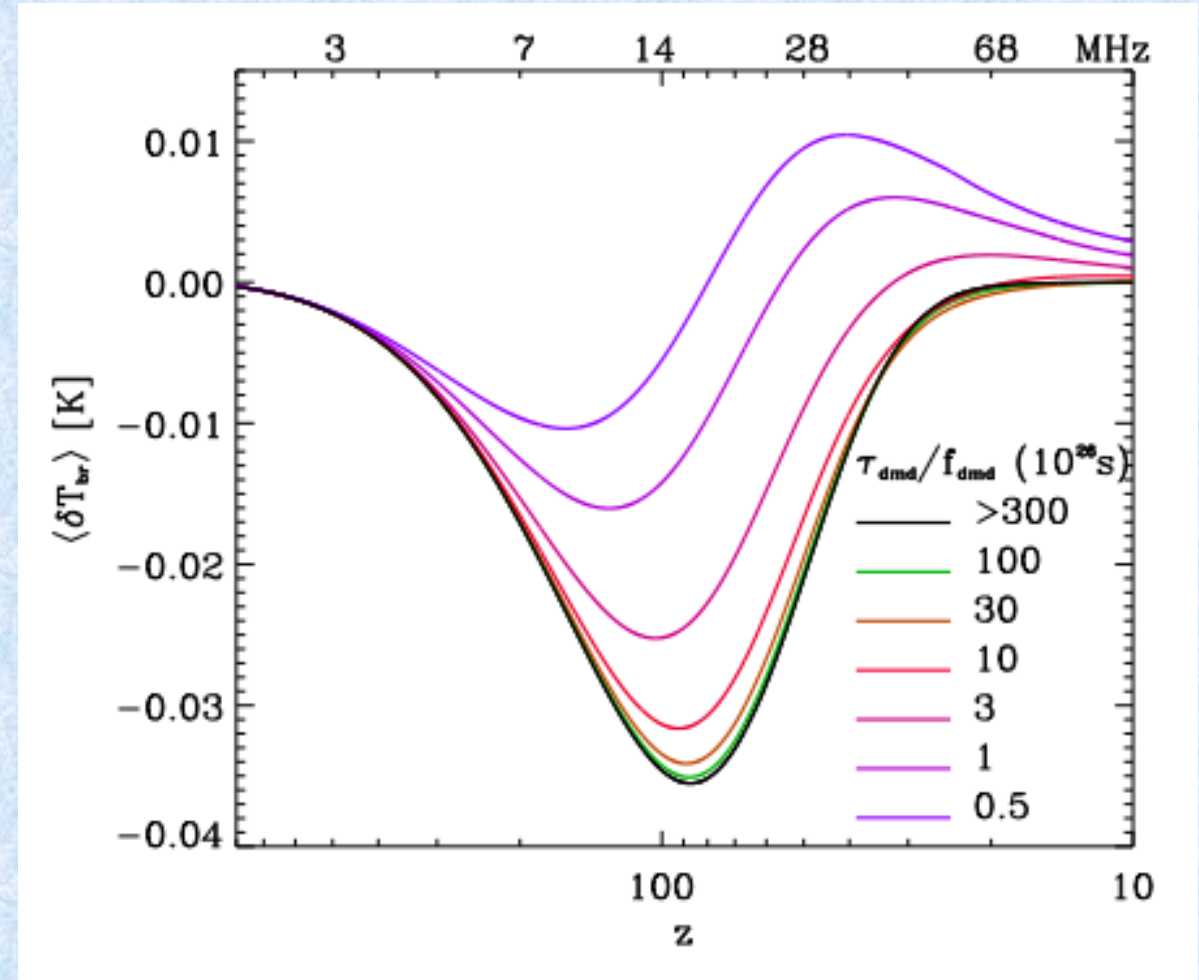
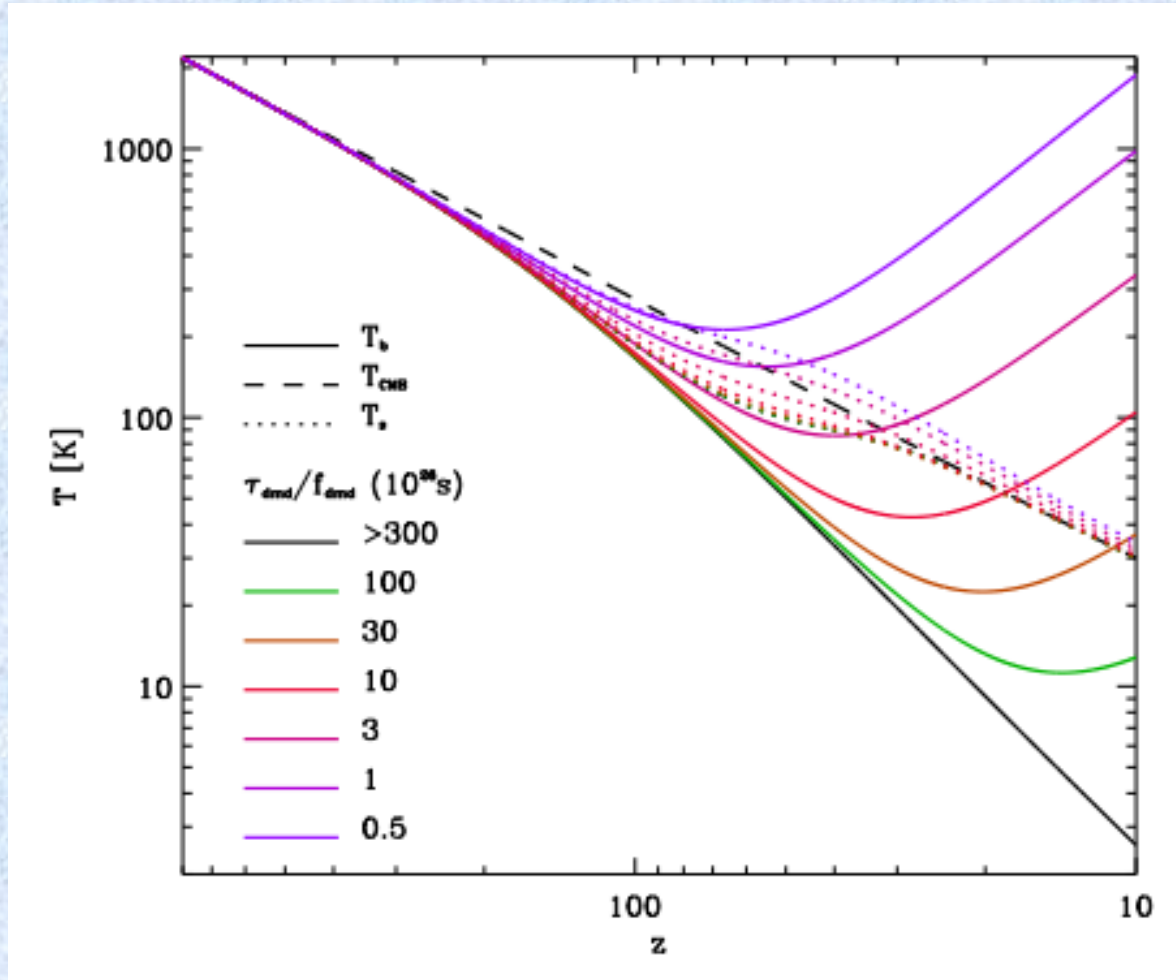
$$\frac{dx_{HeI}}{dt} = -428.28 g_{ion}^{(HeI)} \frac{f_{dmd} \Omega_{dm} h^2 f_{He}}{n_{HeI} \tau_d (1+f_{He})} (1+z)^3$$

Here $[\tau_d]=\text{s}$, $[n_{HI}]=[n_{HeI}]=\text{cm}^{-3}$.



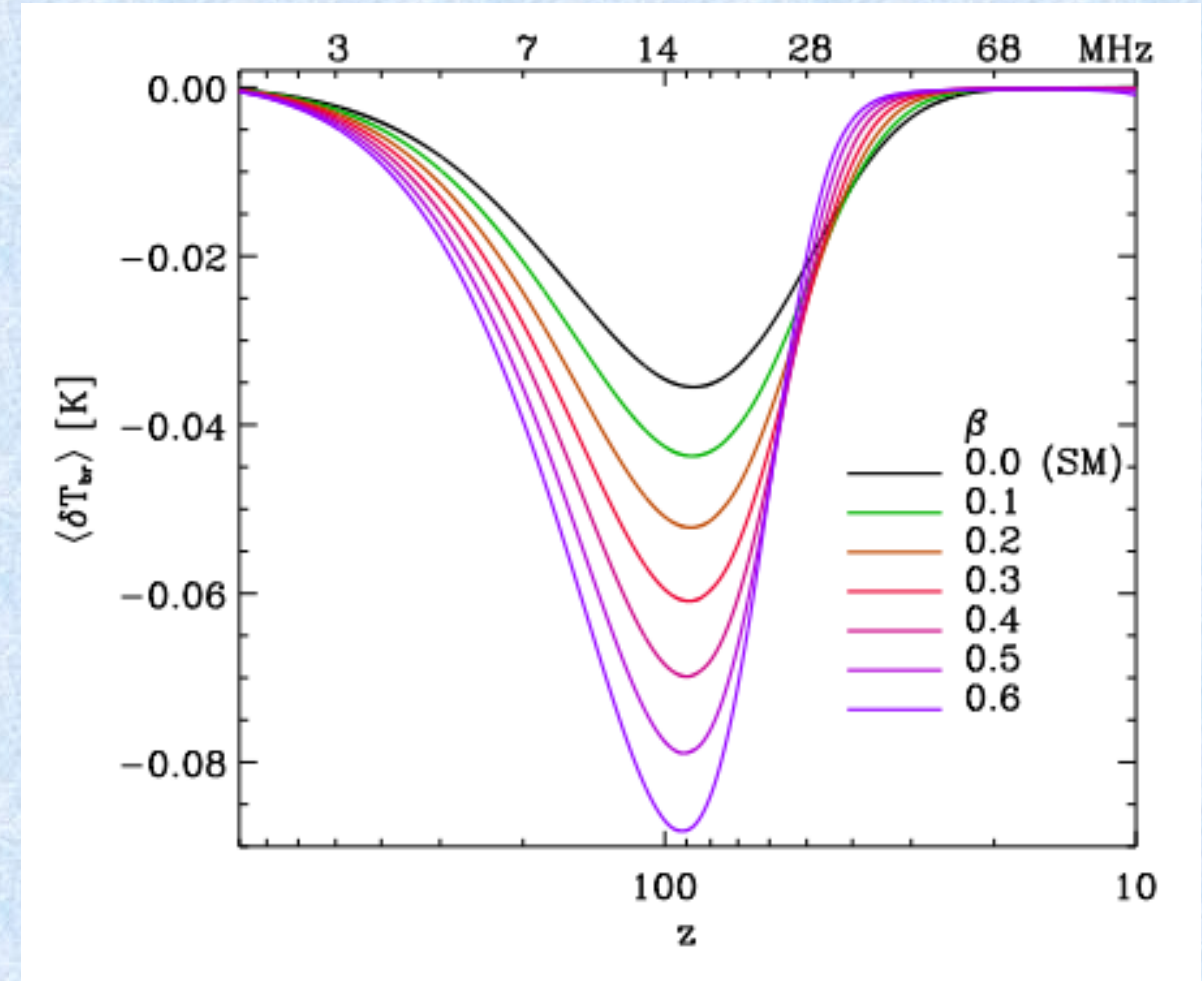
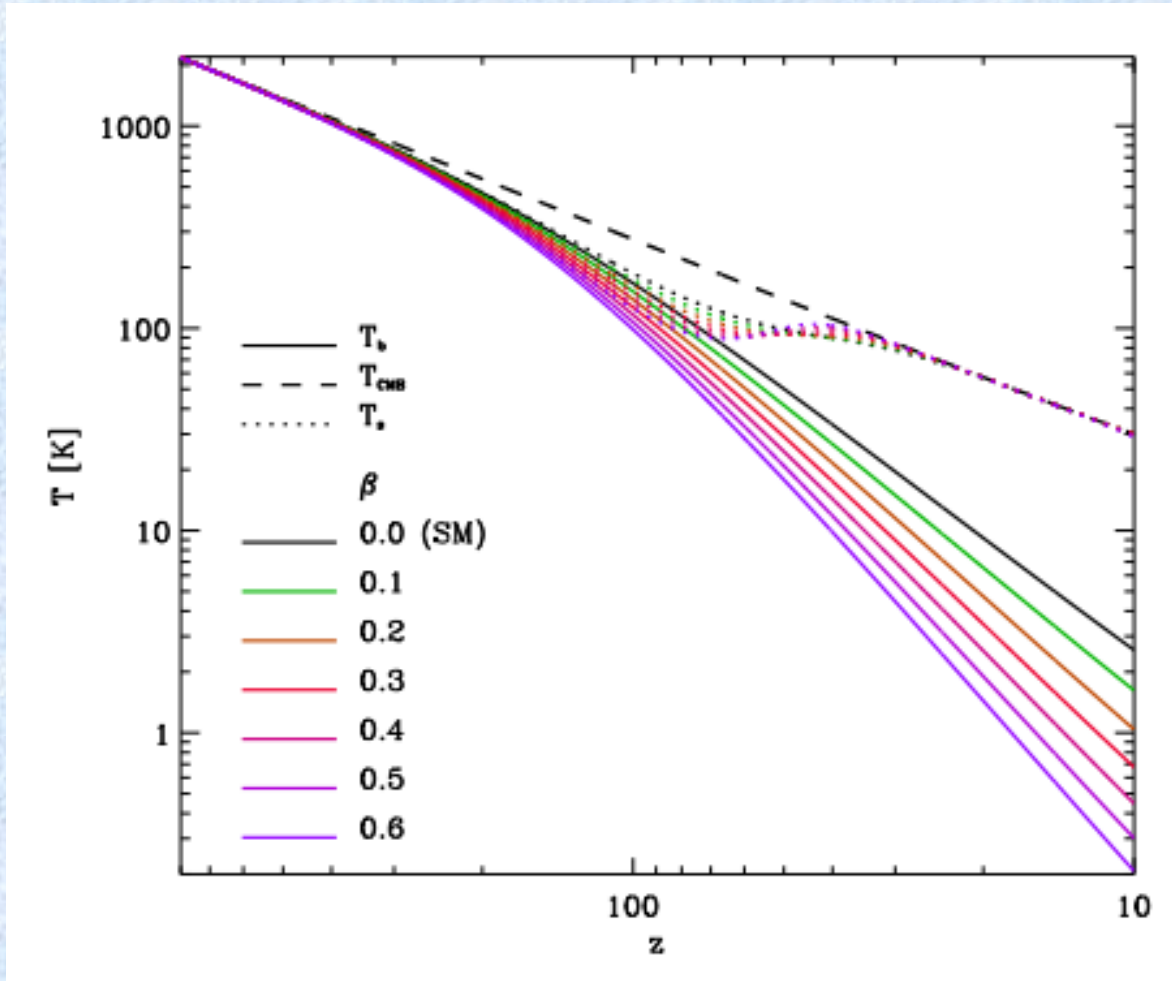
SM: $\Omega_b=0.0493$, $\Omega_{dm}=0.266$, $\Omega_\Lambda=0.6847$, $\Omega_K=0$, $H_0=67.36$ km/s·Mpc (Planck collaboration, 2020)

Non-standard cosmology: decaying dark matter



SM: $\Omega_b=0.0493$, $\Omega_{\text{dm}}=0.266$, $\Omega_\Lambda=0.6847$, $\Omega_K=0$, $H_0=67.36$ km/s·Mpc (Planck collaboration, 2020)

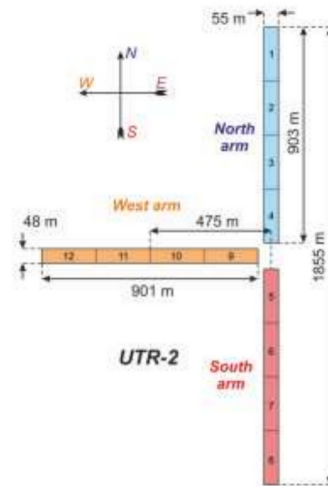
Non-standard cosmology: additional cooling ($\Lambda_{\text{add.cool.}} = \beta \cdot \Lambda_{\text{ad}}$)



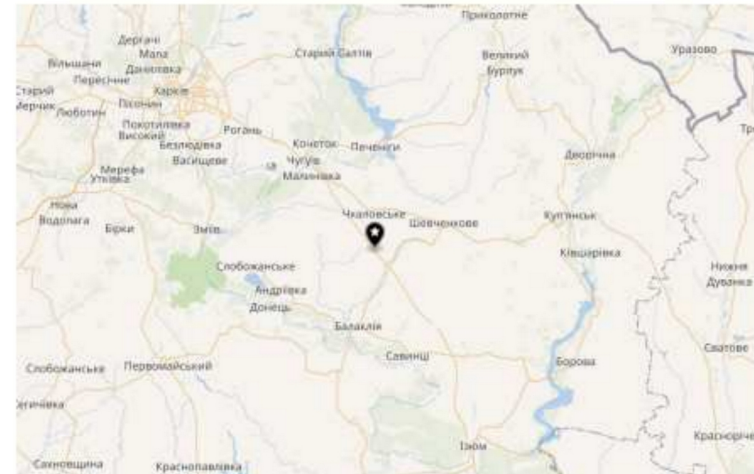
SM: $\Omega_b=0.0493$, $\Omega_{\text{dm}}=0.266$, $\Omega_\Lambda=0.6847$, $\Omega_K=0$, $H_0=67.36$ km/s·Mpc (Planck collaboration, 2020)

The Ukrainian Radio Telescope UTR-2 is the world's largest low-frequency radio telescope at 8-30 MHz

The half-width of absorption line H 21 cm is at $z \sim 150 - 50$, that for Earth observers is at $\nu_{21} \sim 9 - 28$ MHz!

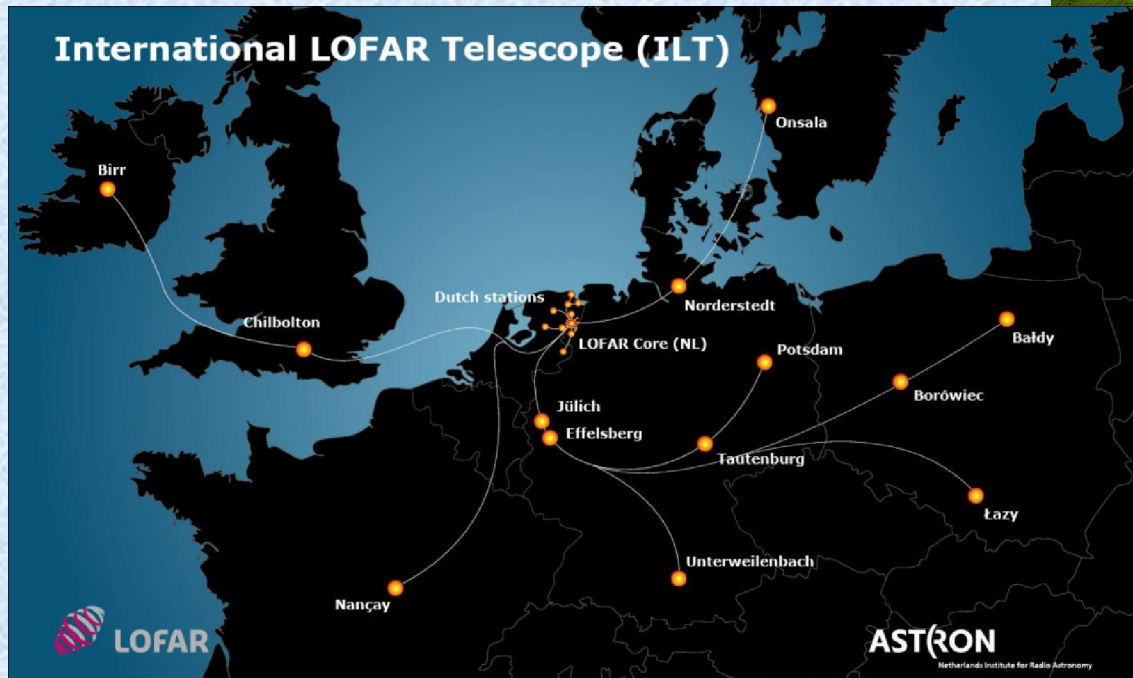


The UTR-2 consists of an array of 2040 dipole elements in two arms each containing 6 rows of elements, oriented in a T shape: a north-south arm consisting of 1440 elements covering an area of 1800×60 meters, and an east-west arm consisting of 600 elements covering an area of 900×60 meters. The basic element is a broadband **cage dipole** 1.8 m in diameter and 8 m long made of galvanized steel wire, mounted 3.5 m above the ground, with a **balun** to connect it to the transmission line. The dipoles are all oriented along the east-west axis, with the spacing between rows of 7.5 m in east-west direction and 9 m in north-south. It has a total area of 150,000 square metres (1,600,000 sq ft), and a resolution of about 40 arcminutes at the middle frequency 16.7 MHz. The operating frequency range is 8–33 MHz. The sensitivity is about 10 mJy.



LOFAR

The Low-Frequency Array (LOFAR) is a large radio telescope, with an antenna network located mainly in the Netherlands, and spreading across other European countries.



Low Band Antenna (LBA) and High Band Antenna (HBA), optimized for 10-80 MHz and 120-240 MHz respectively

The Lunar Surface Electromagnetic Explorer (LuSEE-Night)



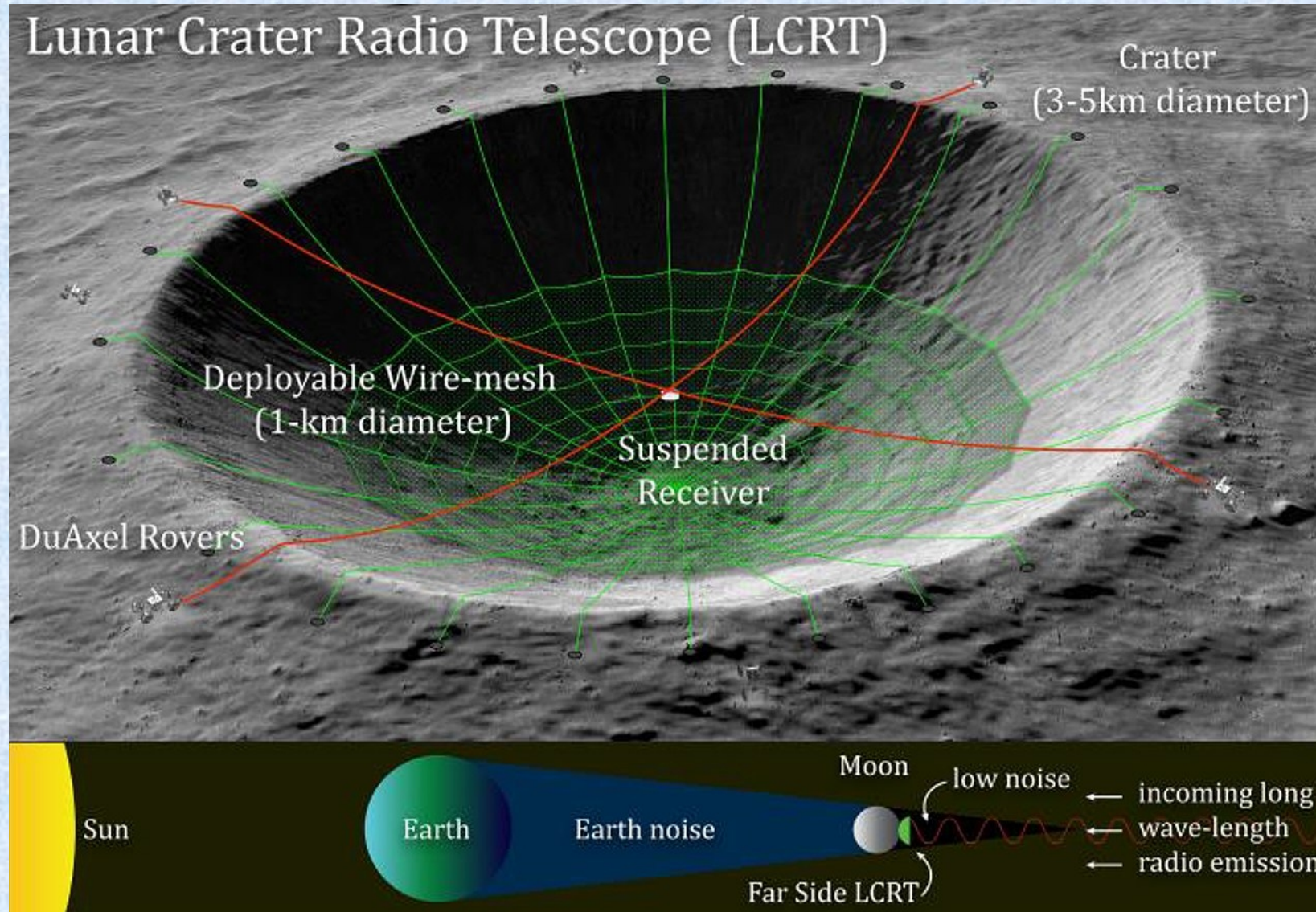
LuSEE-Night: 0.1-50 MHz, Lunar radio telescope (expected launch 2025/2026)

The Dark Ages Radio Explorer (DARE)



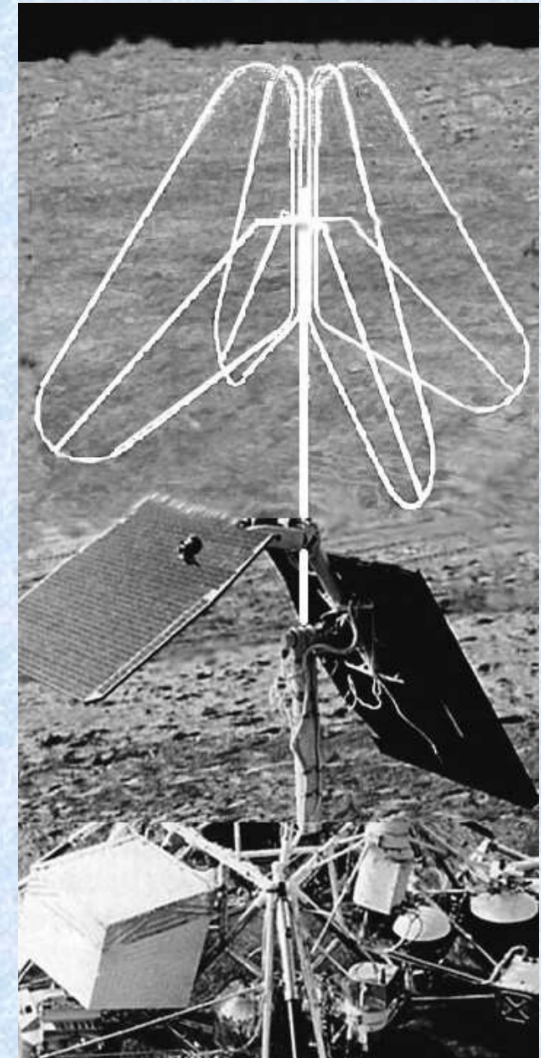
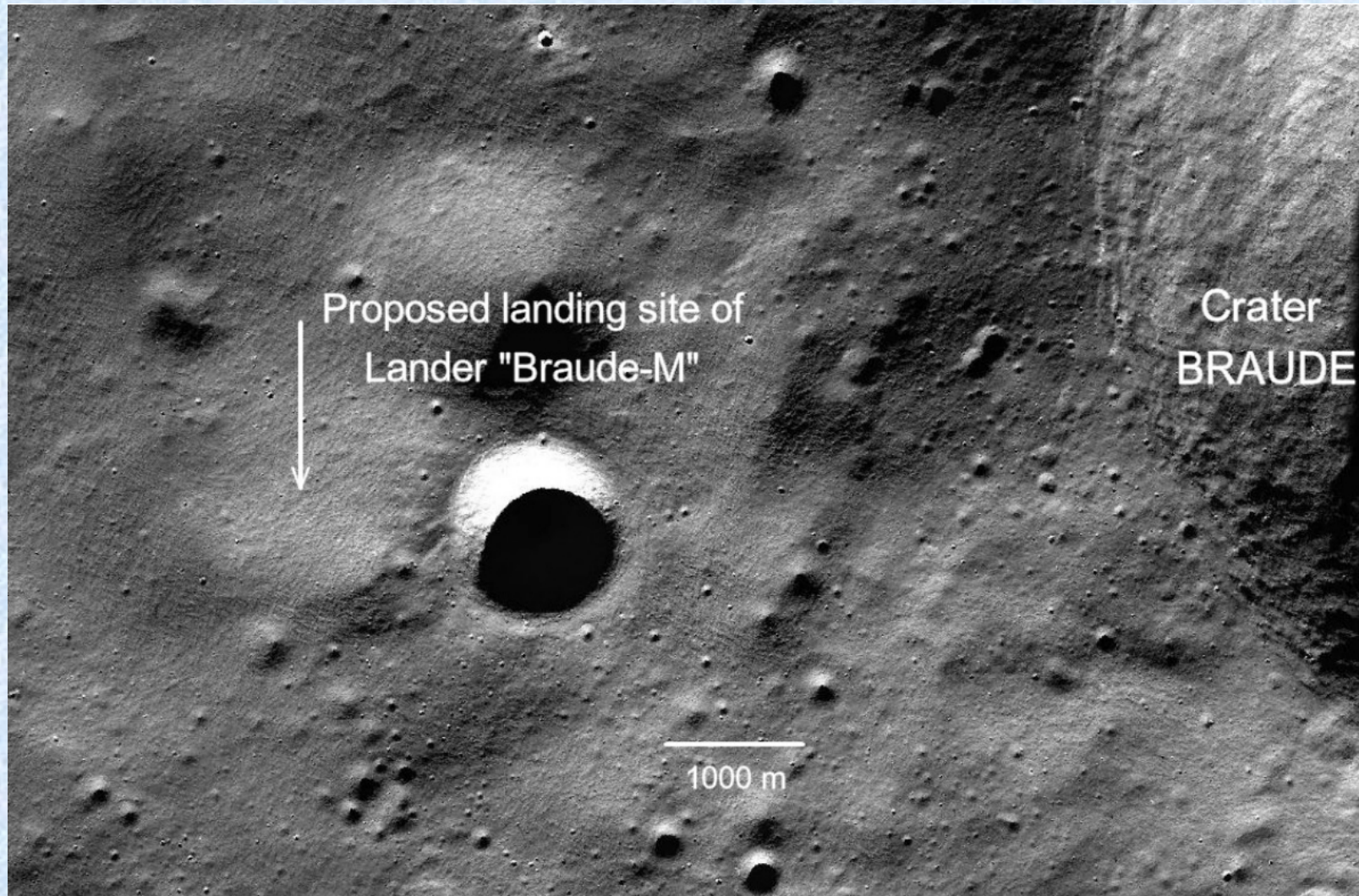
DARE: 40-120 MHz, Lunar orbiter (expected to launch in

Lunar Crater Radio Telescope (LCRT)



LCRT: 10-30 MHz, D 350 m (NASA proposal)

Big Radio Astronomy Universe, Demonstrating Exploration on the Moon ("BRAUDE-M")



Conclusions

- In the standard cosmological model, an absorption line of 21 cm of neutral hydrogen is formed during the Dark Ages at $30 \leq z \leq 300$ with a differential brightness temperature $\delta T_{br} \approx -35$ mK at $z \approx 87$. The frequency of the line in the absorption trough is 16 MHz, the effective half-width of the line is 12 MHz.
- The depth of line is moderately sensitive to Ω_b and H_0 , weakly sensitive to Ω_{dm} , and insensitive to other parameters of the standard Λ CDM model.
- The line is very sensitive to additional mechanisms of heating or cooling of baryonic matter during the Dark Ages, so it can be a good test of non-standard cosmological models.
- In the models with **decaying** and **self-annihilating dark matter**, as well as with a **primordial magnetic field**, the temperature of baryonic matter in this period is higher the larger is the fraction of these energy components of dark matter, f_{dmd} and f_{dman} , and strength of magnetic field B_0 . The depth of the **absorption line decreases** and **transitions to emission** at values of the component parameters lower than the upper limits on them, which result from the set of available observed data.