

# Mineral Detection of Dark Matter



Minerals such as olivine could hold evidence of long-ago collisions between atomic nuclei and dark matter (Olena Shmahalo/Quanta Magazine).

*[Submitted on 17 Jan 2023]*

## Mineral Detection of Neutrinos and Dark Matter. A Whitepaper

Sebastian Baum, Patrick Stengel, Natsue Abe, Javier F. Acevedo, Gabriela R. Araujo, Yoshihiro Asahara, Frank Avignone, Levente Balogh, Laura Baudis, Yilda Boukhtouchen, Joseph Bramante, Pieter Alexander Breur, Lorenzo Caccianiga, Francesco Capozzi, Juan I. Collar, Reza Ebadi, Thomas Edwards, Klaus Eitel, Alexey Elykov, Rodney C. Ewing, Katherine Freese, Audrey Fung, Claudio Galelli, Ulrich A. Glasmacher, Arianna Gleason, Noriko Hasebe, Shigenobu Hirose, Shunsaku Horiuchi, Yasushi Hoshino, Patrick Huber, Yuki Ido, Yohei Igami, Yoshitaka Itow, Takenori Kato, Bradley J. Kavanagh, Yoji Kawamura, Shingo Kazama, Christopher J. Kenney, Ben Kilminster, Yui Kouketsu, Yukiko Kozaka, Noah A. Kurinsky, Matthew Leybourne, Thalles Lucas, William F. McDonough, Mason C. Marshall, Jose Maria Mateos, Anubhav Mathur, Katsuyoshi Michibayashi, Sharlotte Mkhonto, Kohta Murase, Tatsuhiro Naka, Kenji Oguni, Surjeet Rajendran, Hitoshi Sakane, Paola Sala, Kate Scholberg, Ingrida Semeneč, Takuya Shiraishi, Joshua Spitz, Kai Sun, Katsuhiko Suzuki, Erwin H. Tanin, Aaron Vincent, Nikita Vladimirov, Ronald L. Walsworth, Hiroko Watanabe

### MD $\nu$ DM community

- Groups across Europe, North America and Japan
- Astroparticle theorists, experimentalists, geologists, and materials scientists
- Next **MD $\nu$ DM workshop** in Washington DC January 2024

### Check out our whitepaper!

- History of mineral detectors
- Review of scientific potential for particle physics, reactor neutrinos and geoscience
- Summary of active and planned experimental efforts

# Trade large target mass for long exposure time

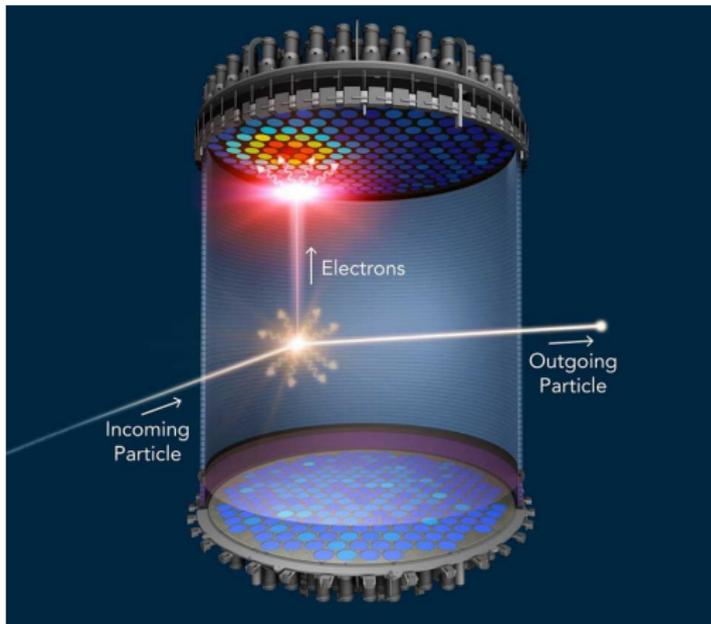


Figure: LUX-ZEPLIN (LZ) Collaboration / SLAC National Accelerator Laboratory

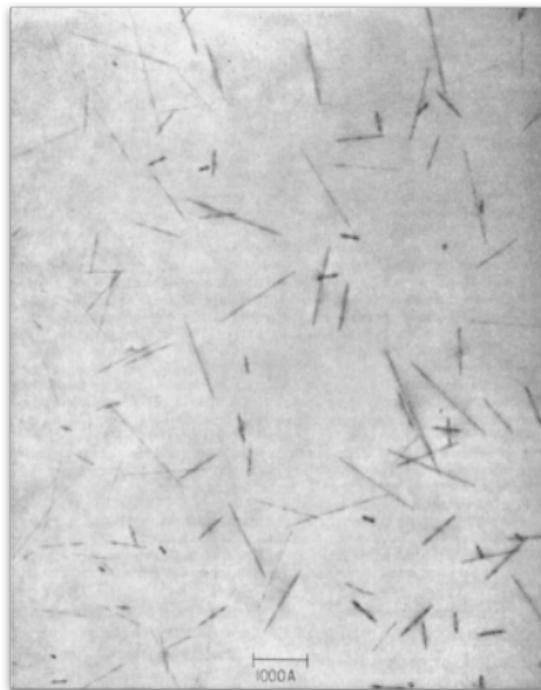
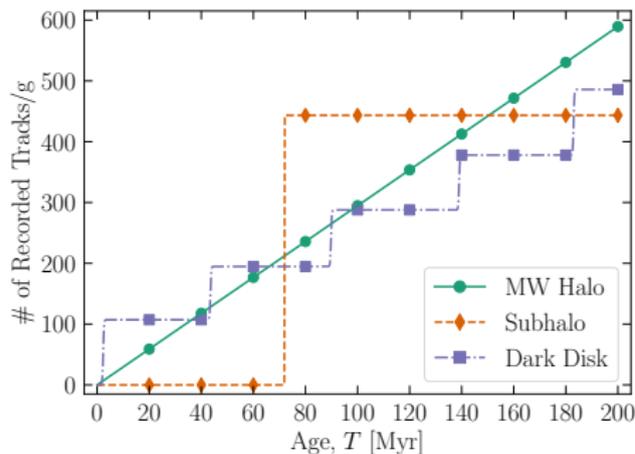
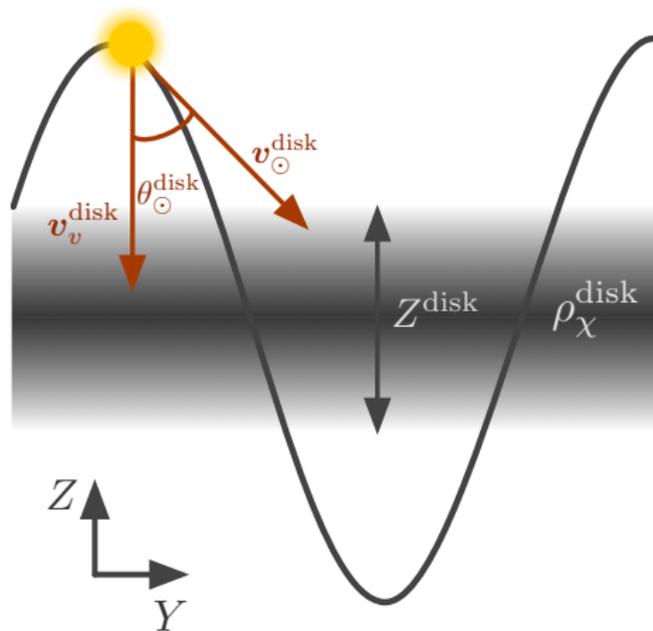


Figure: Price+Walker '63

# Mineral detectors can look for signals “averaged” over geological timescales or for time-varying signals

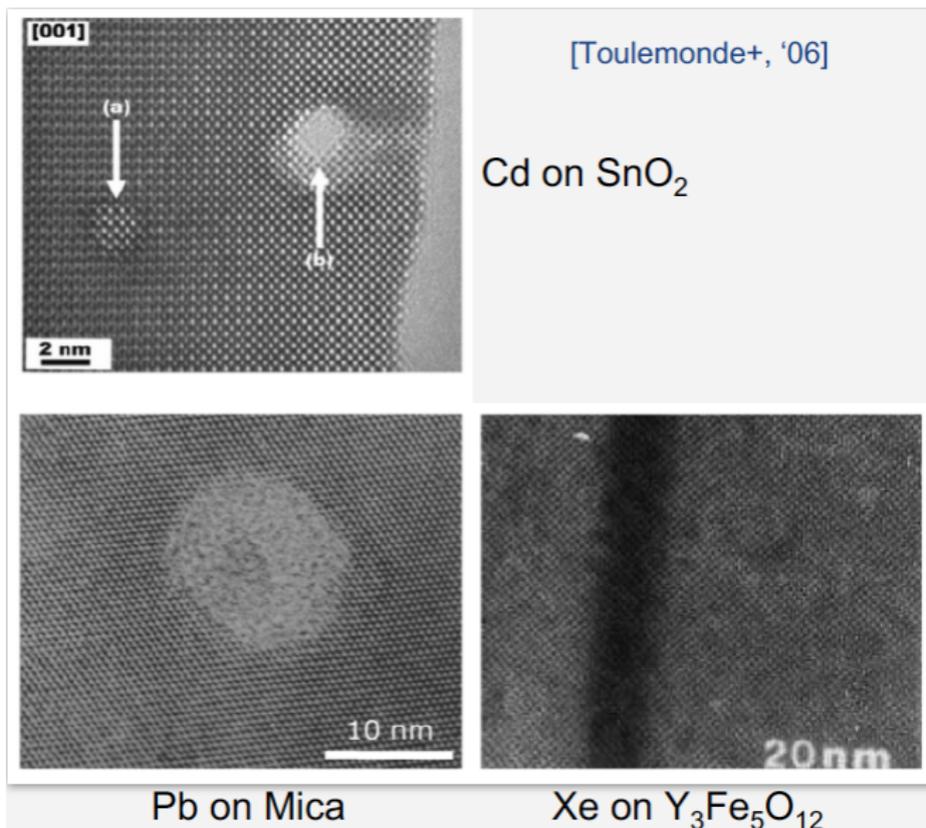


**Figure:** Time dependent DM signals in series of gypsum detectors for  $m_{\chi}^{\text{disk}} = 100 \text{ GeV}$ ,  $\sigma_{\chi p}^{\text{disk}} = 10^{-43} \text{ cm}^2$  and  $\Sigma^{\text{disk}} = 10 M_{\odot}/\text{pc}^2$ , 2107.02812



**Figure:** Dark Disk cartoon, 2107.02812

# Modern TEM allows for accurate characterization of tracks



# Cleaving and etching limits $\epsilon$ and can only reconstruct 2D

## Readout scenarios for different $x_T$

- HIBM+pulsed laser could read out 10 mg with nm resolution
- SAXs at a synchrotron could resolve 15 nm in 3D for 100 g

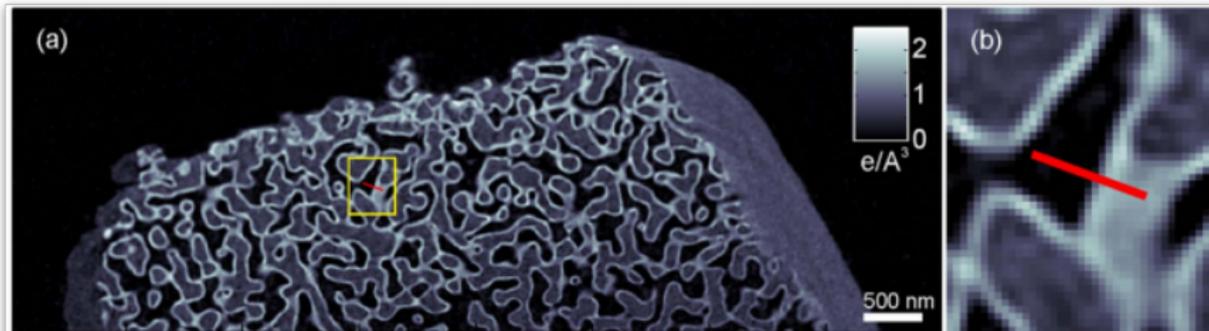
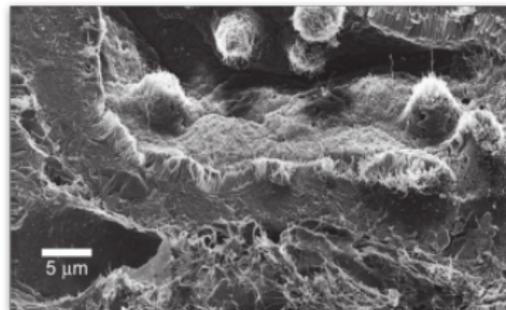
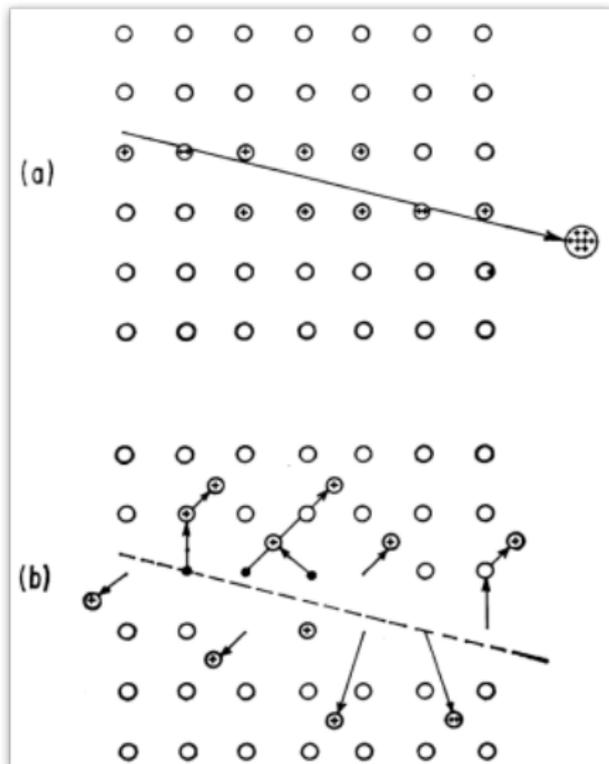


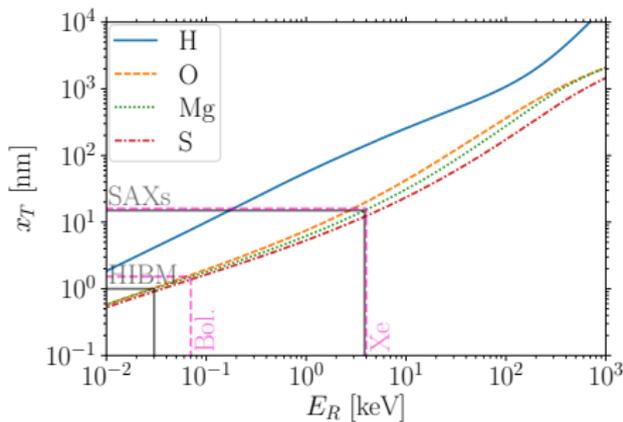
Figure: HIM rodent kidney Hill+ '12, SAXs nanoporous glass Holler+ '14

# Mineral detectors look for damage from recoiling nuclei

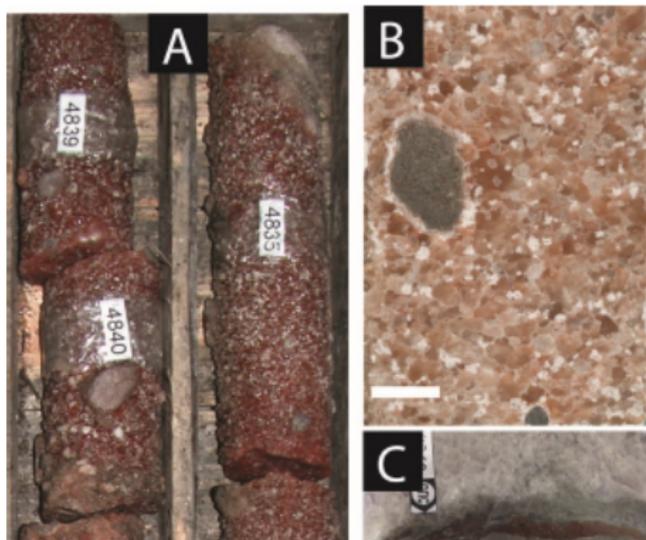


## Track length from stopping power

$$x_T(E_R) = \int_0^{E_R} dE \left| \frac{dE}{dx_T}(E) \right|^{-1}$$



# Cosmogenic backgrounds suppressed in deep boreholes



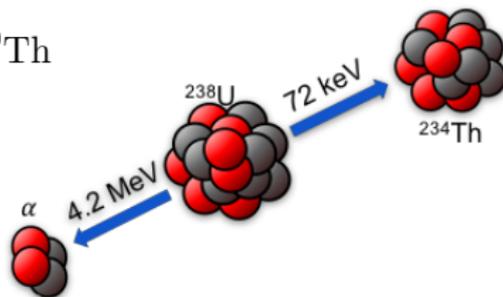
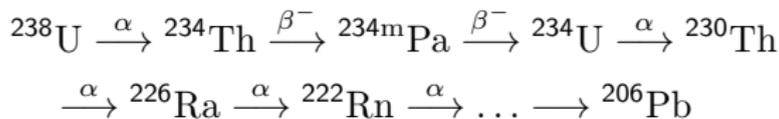
**Figure:**  $\sim 2$ Gyr old Halite cores from  $\sim 3$ km, as discussed in Blättler+ '18

Depth	Neutron Flux
2 km	$10^6/\text{cm}^2/\text{Gyr}$
5 km	$10^2/\text{cm}^2/\text{Gyr}$
6 km	$10/\text{cm}^2/\text{Gyr}$
50 m	$70/\text{cm}^2/\text{yr}$
100 m	$30/\text{cm}^2/\text{yr}$
500 m	$2/\text{cm}^2/\text{yr}$

Need minerals with low  $^{238}\text{U}$

- Marine evaporites with  $C^{238} \gtrsim 0.01$  ppb
- Ultra-basic rocks from mantle,  $C^{238} \gtrsim 0.1$  ppb

# Radiogenic backgrounds from $^{238}\text{U}$ contamination

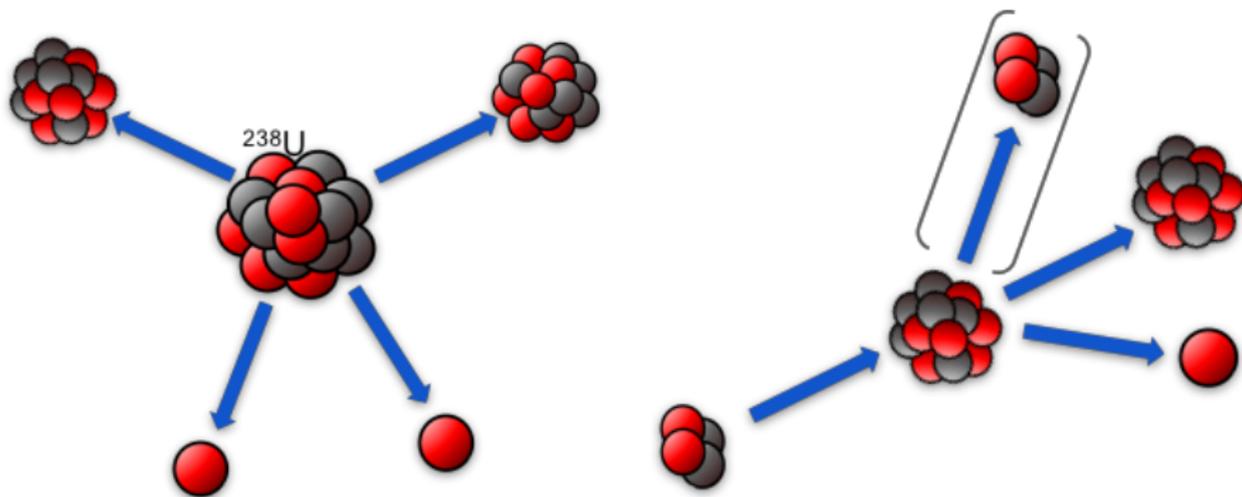


Nucleus	Decay mode	$T_{1/2}$
$^{238}\text{U}$	$\alpha$	$4.468 \times 10^9$ yr
$^{234}\text{Th}$	SF	$8.2 \times 10^{15}$ yr
$^{234\text{m}}\text{Pa}$	$\beta^-$ (99.84 %)	24.10 d
	IT (0.16 %)	1.159 min
$^{234}\text{Pa}$	$\beta^-$	6.70 d
$^{234}\text{U}$	$\alpha$	$2.455 \times 10^5$ yr

“ $1\alpha$ ” events difficult to reject without additional decays

- Reject  $\sim 10 \mu\text{m}$   $\alpha$  tracks
- Without  $\alpha$  tracks, filter out monoenergetic  $^{234}\text{Th}$

# Fast neutrons from SF and $(\alpha, n)$ interactions



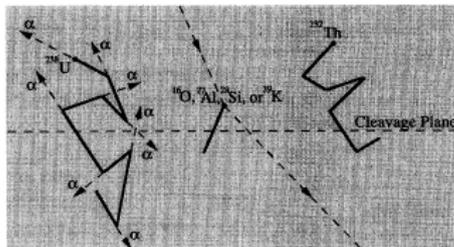
SF yields  $\sim 2$  neutrons with  $\sim \text{MeV}$

Each neutron will scatter elastically  
10-1000 times before moderating

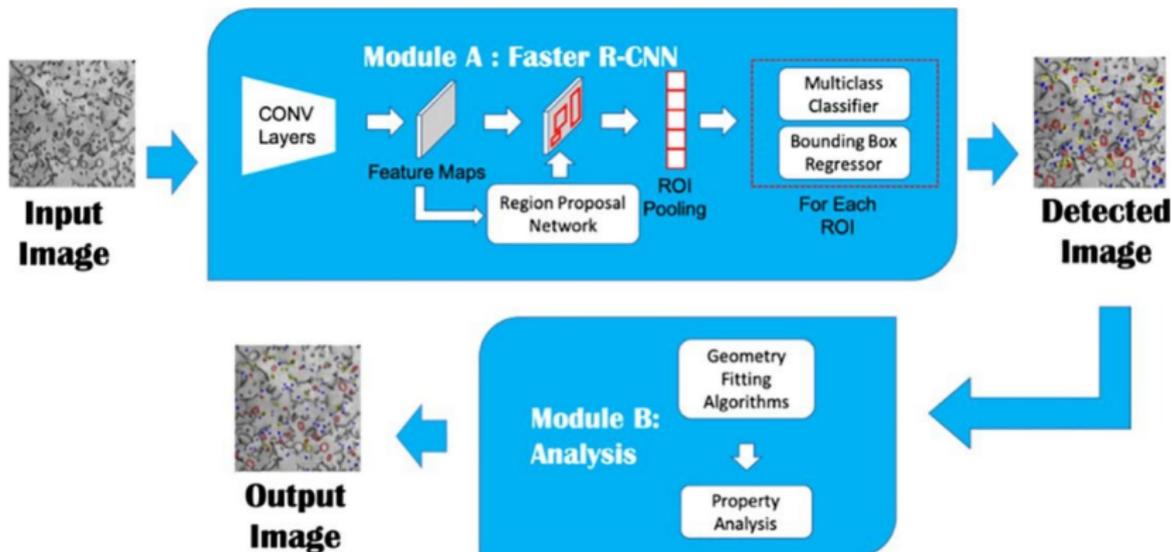
$(\alpha, n)$  rate low, many decay  $\alpha$ 's

Heavy targets better for  $(\alpha, n)$  and  
bad for neutron moderation, need H

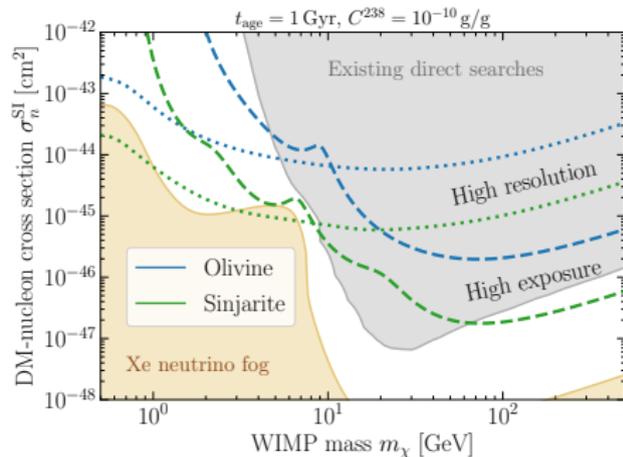
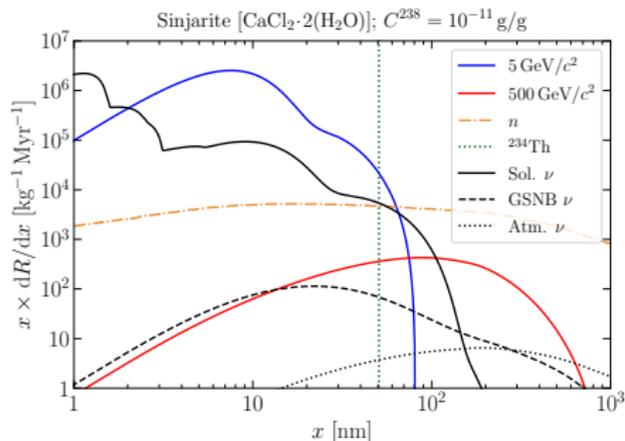
# Quick aside on data analysis and $\alpha$ -recoil background



- 15 nm resolution of 100 g sample  
 $\Rightarrow 10^{19}$  mostly empty voxels
- 1 Gyr old with  $C^{238} = 0.01$  ppb  
 $\Rightarrow 10^{13}$  voxels for  $\alpha$ -recoil tracks



# Use track length spectra to pick out WIMP signal



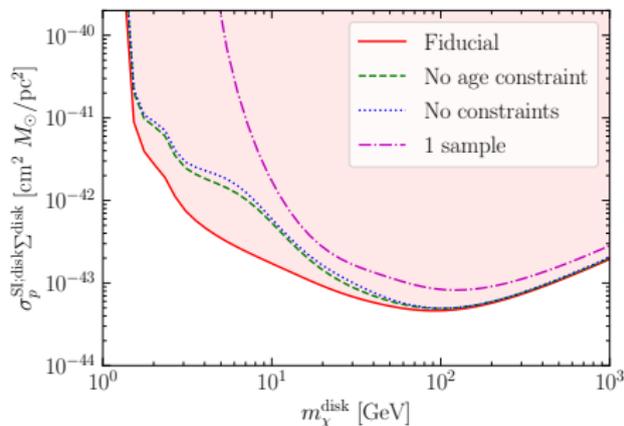
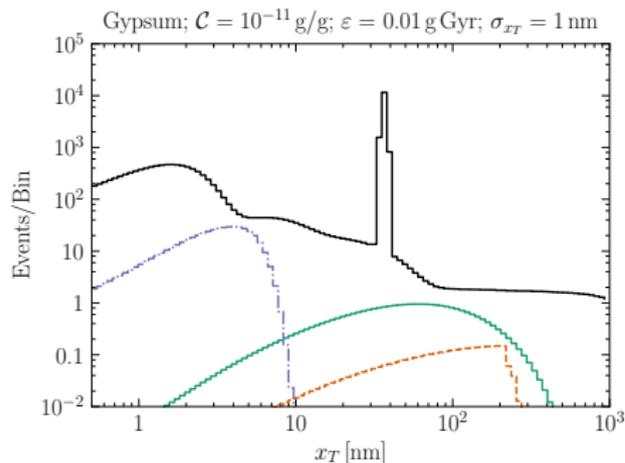
## Different background regimes

- Solar  $\nu$ 's peak at short track lengths relevant for lighter DM
- Flat spectrum of radiogenic neutrons limits heavier WIMPs

## Read-out threshold vs exposure

- Need larger samples to be competitive at heavier masses
- Can potentially go into the neutrino fog at low masses

# Measure time-varying signals with a series of samples



Dark disk transit every  $\sim 45$  Myr

Spectra from **dark disk** crossing,  
**MW halo**, **combined backgrounds**

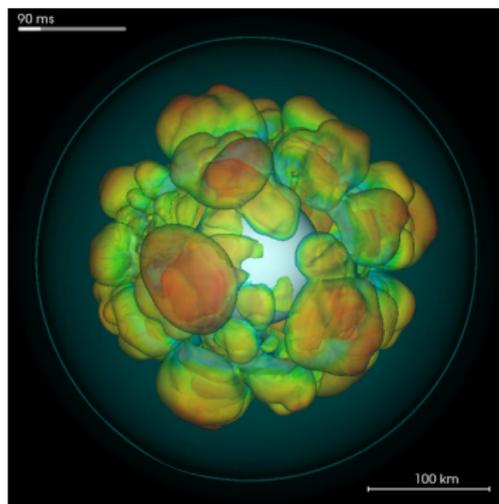
$$m_{\chi}^{\text{disk}} = 100 \text{ GeV} \quad \sigma_{\chi p}^{\text{disk}} = 10^{-43} \text{ cm}^2$$

$$m_{\chi} = 500 \text{ GeV} \quad \sigma_{\chi p} = 5 \times 10^{-46} \text{ cm}^2$$

Ages  $t = 20, 40, 60, 80, 100$  Myr

- Systematic uncertainty  
 $\Delta_t = 5\%$ ,  $\Delta_M = 0.1\%$ ,  
 $\Delta_C = 10\%$ ,  $\Delta_{\Phi} = 100\%$
- $> 1$  samples more important

# Mineral detectors could probe rare and/or previous events



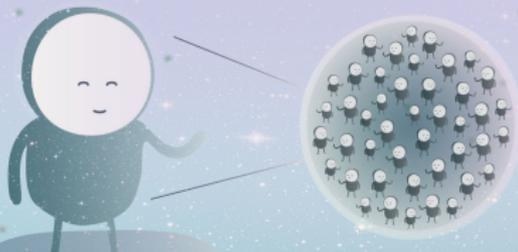
## Look for DM and astrophysical $\nu$ 's

- WIMP DM (**2106.06559**), substructure (2107.02812), composite DM (2105.06473)
- Measure solar (2102.01755), galactic CC SN (**1906.05800**), atmospheric (**2004.08394**)  $\nu$ 's

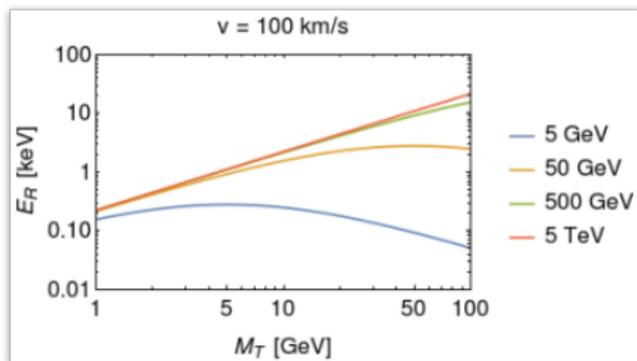
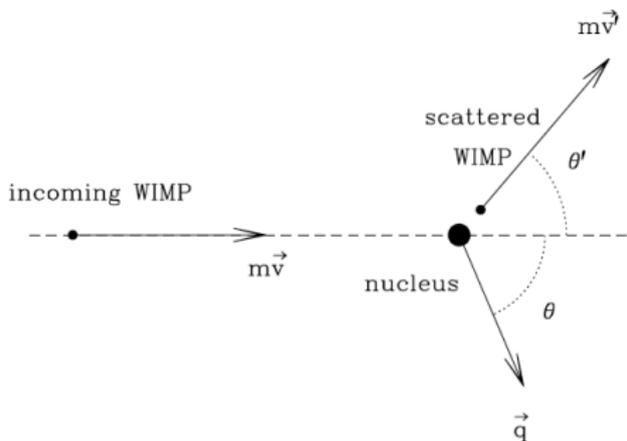
## Feasibility of mineral detectors

- Determine efficiency of effective 3D recoil track reconstruction
- Need model of geological history
- Radiopure samples from depth
- **Find a way to handle the data**

## COMPOSITE DARK MATTER



# Spin- and velocity-independent WIMP-nucleus scattering



Rate per unit time per unit mass

$$\frac{dR}{dE_R} = \frac{n_X}{2} \frac{\sigma_{Xp}^{SI}}{\mu_{Xp}^2} A^2 F(q)^2 \eta(v_q)$$

Scattering kinematics  $\Rightarrow$  event rate

- Account for **finite size** of nucleus
- Convolute with **WIMP flux**
- Write **cross section** in terms of WIMP-nucleon interaction

# Scattering cross sections $\Rightarrow$ scattering rates

$$\frac{d^2\sigma}{dq^2 d\Omega_q} = \frac{d\sigma}{dq^2} \frac{1}{2\pi} \delta\left(\cos\theta - \frac{q}{2\mu_{\chi T} v}\right) \simeq \frac{\sigma_0 F(q)^2}{8\pi\mu_{\chi T}^2 v} \delta\left(v\cos\theta - \frac{q}{2\mu_{\chi T}}\right)$$

$$\frac{d^2R}{dE_R d\Omega_q} = 2M_T \frac{N_T}{M_T N_T} \int \frac{d^2\sigma}{dq^2 d\Omega_q} n_X v f(v) d^3v \simeq \frac{\sigma_0 F(q)^2}{4\pi\mu_{\chi T}} n_X \hat{f}(v_q, \hat{q})$$

## Differential cross section

- $\delta$ -function imposes **kinematics**
- $\sigma_0$  is velocity and momentum independent cross section for **scattering off pointlike nucleus**

$$F(q) \simeq \frac{9 [\sin(qR) - qR \cos(qR)]^2}{(qR)^6}$$

## Differential scattering rate

- Rate per unit time per unit **detector mass** for **all nuclei**
- Convolute cross section with **astrophysical WIMP flux**

$$\sigma_0^{SI} = \frac{4}{\pi} \mu_{\chi T}^2 [Z f_s^p + (A - Z) f_s^n]^2$$

# Velocity distribution in the Standard Halo Model (SHM)

Integrate Radon transform

$$\int \hat{f}(v_q, \hat{\mathbf{q}}) d\Omega_q = 2\pi\eta(v_q)$$

Mean inverse speed

$$\eta(v_q) = \int_{v > v_q} \frac{f(\mathbf{v})}{v} d^3v$$

Maxwellian in halo frame

$$\tilde{f}(\mathbf{v}) \sim \left( \frac{3}{2\pi\sigma_v^2} \right)^{3/2} e^{-3v^2/2\sigma_v^2}$$

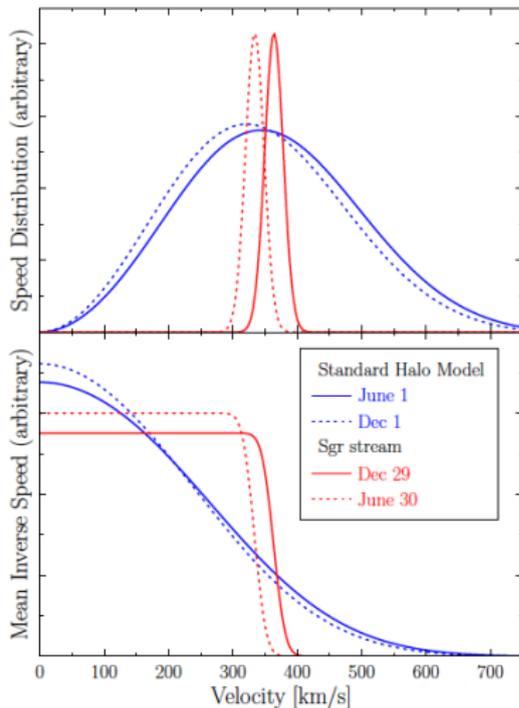


Figure: 1209.3339

# Conventional direct detection searches for WIMPs

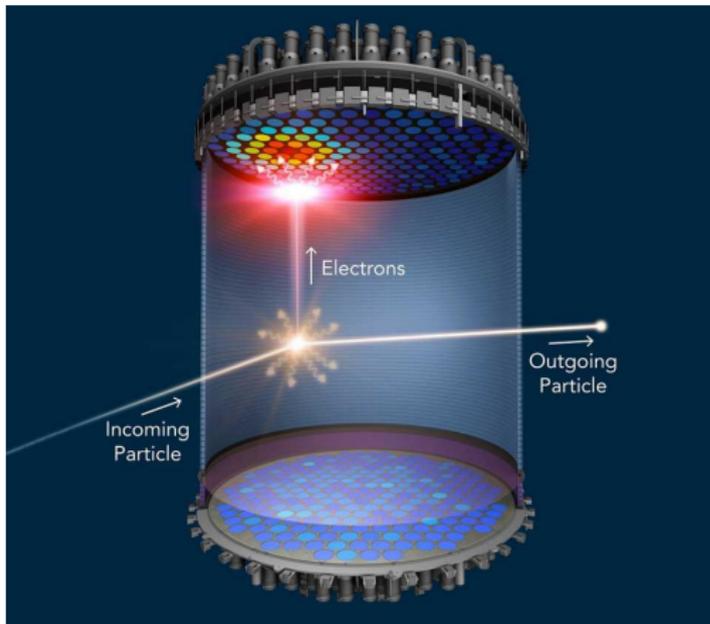


Figure: LUX-ZEPLIN (LZ) Collaboration / SLAC National Accelerator Laboratory

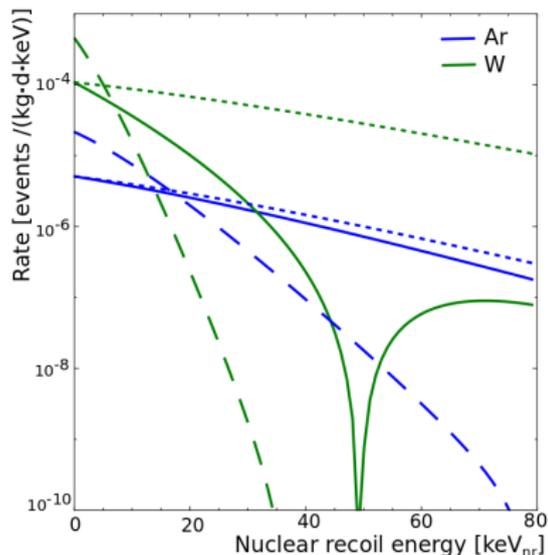


Figure: Event rate for  $m_X = 100$  GeV and  $\sigma_{Xp}^{SI} = 10^{-45}$  cm<sup>2</sup> (solid),  $m_X \rightarrow 25$  GeV (dashed) and  $F(q) \rightarrow 1$  (dotted), 1509.08767

# Different ways to look for DM-induced nuclear recoils

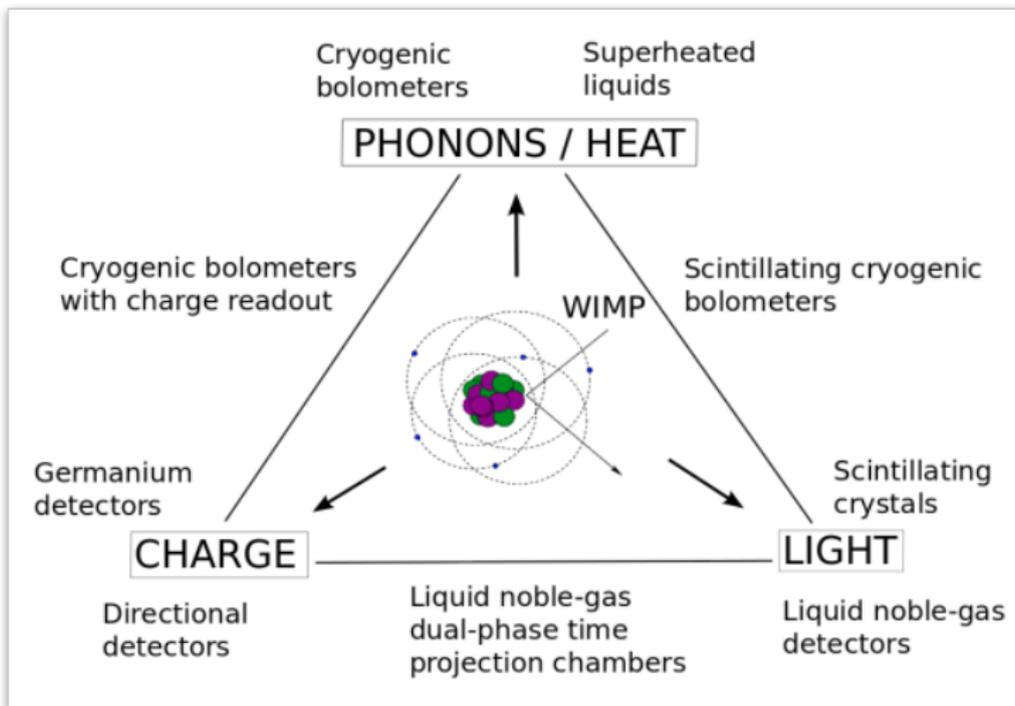
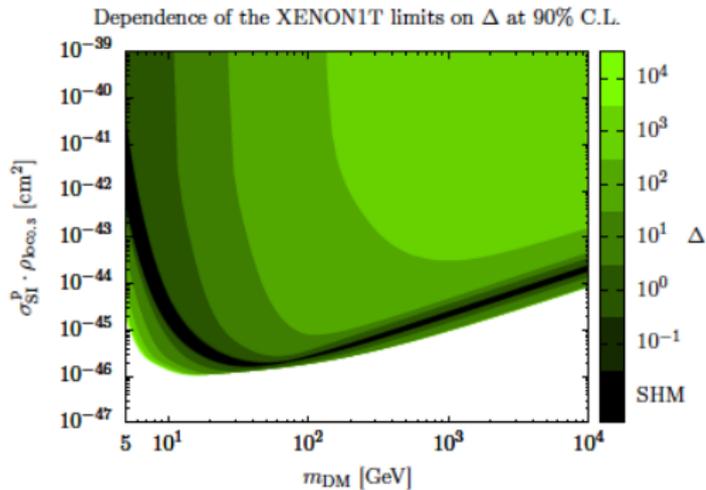
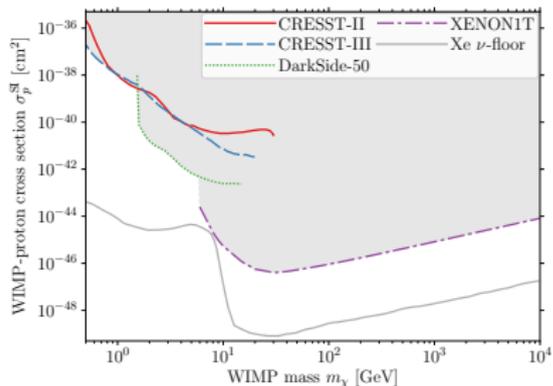


Figure: 1509.08767

# Current limits on $\sigma_{Xp}^{SI}$ and astrophysical uncertainties

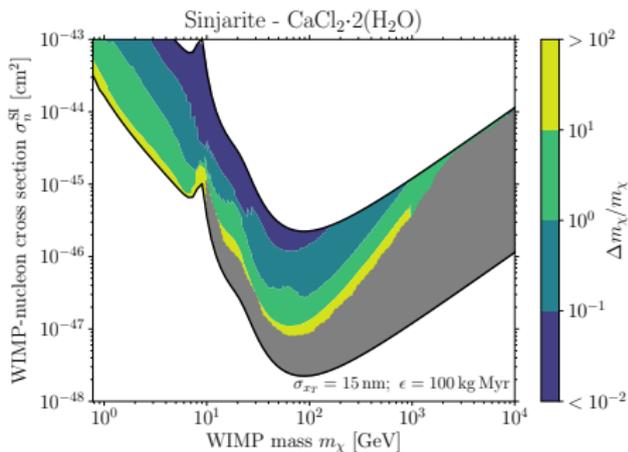
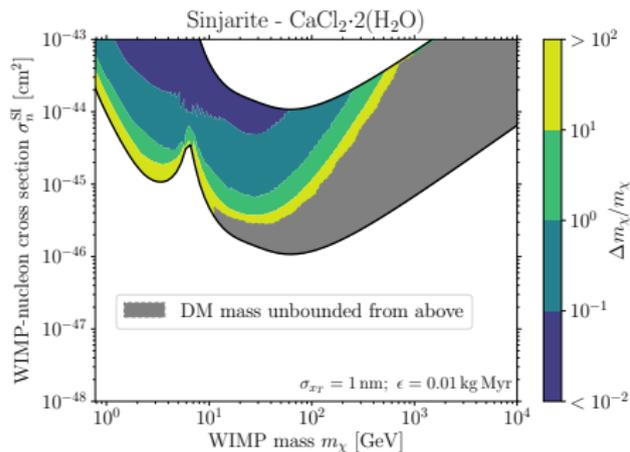


When the smoke clears, we have

$$\frac{dR}{dE_R} = \frac{n_X}{2} \frac{\sigma_{Xp}^{SI}}{\mu_{Xp}^2} A^2 F(q)^2 \eta(v_q)$$

Figure: 1806.08714, variations of  $\sigma_v$  and  $v_{esc}$  in SHM and variations away from MB in SHM  $\Delta \leq |f(\mathbf{v}) - f_{MB}(\mathbf{v})|/f_{MB}(\mathbf{v})$  for  $f(\mathbf{v})$  composed of a large number of streams.

# Multiple nuclei and large $\epsilon$ allow for optimal $\Delta m_\chi/m_\chi$



# Nuclear recoil spectrum depends on neutrino energy

$$\frac{dR}{dE_R} = \frac{1}{m_T} \int dE_\nu \frac{d\sigma}{dE_R} \frac{d\phi}{dE_\nu}$$

- **Quasi-elastic** for  $E_\nu \gtrsim 100$  MeV
- **Resonant  $\pi$  production** at  $E_\nu \sim$  GeV
- **Deep inelastic** for  $E_\nu \gtrsim 10$  GeV

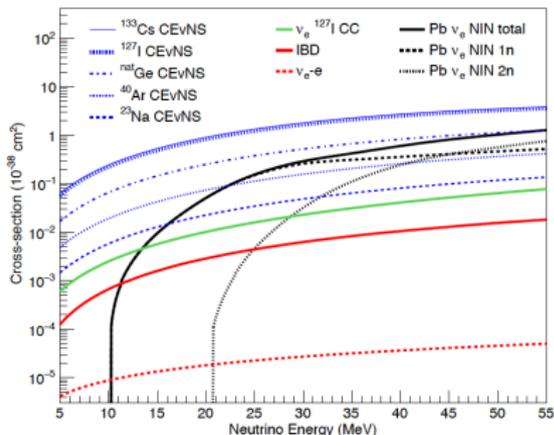


Figure: COHERENT, 1803.09183

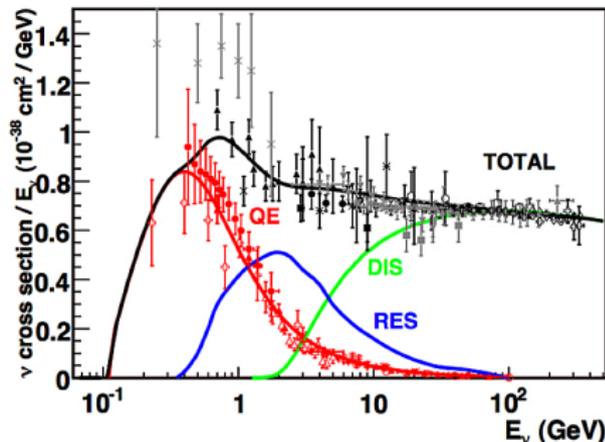


Figure: Inclusive CC  $\sigma_{\nu N}$ , 1305.7513

# Solar $\nu$ 's produced in fusion chains from H to He

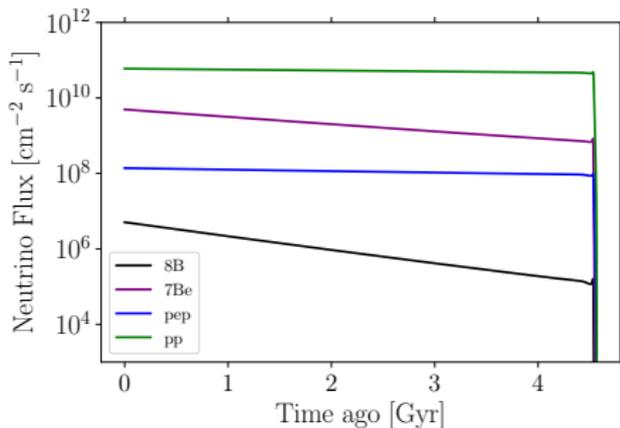
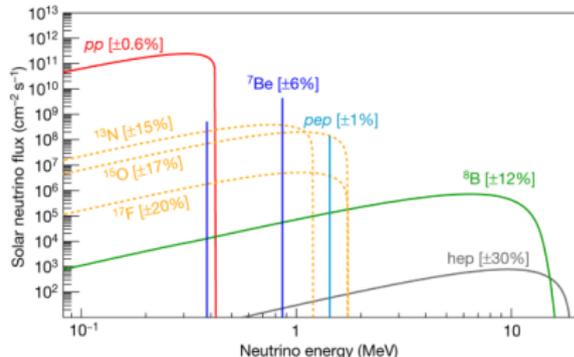
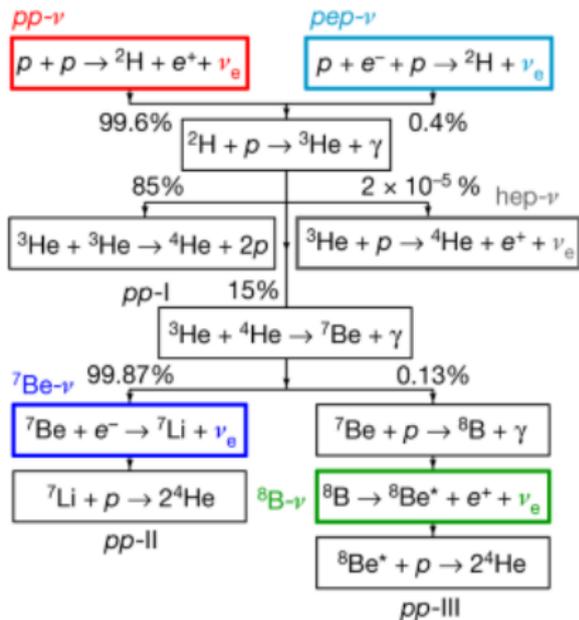


Figure: Today's flux at Borexino (Nature, 2018) and time dependence of GS metallicity model, 2102.01755

# Galactic contribution to $\nu$ flux over geological timescales

$$\frac{d\phi}{dE_\nu} = \dot{N}_{\text{CC}}^{\text{gal}} \frac{dn}{dE_\nu} \int_0^\infty dR_E \frac{f(R_E)}{4\pi R_E^2}$$

Only  $\sim 2$  SN 1987A events/century

- Measure galactic CC SN rate
- Traces star formation history

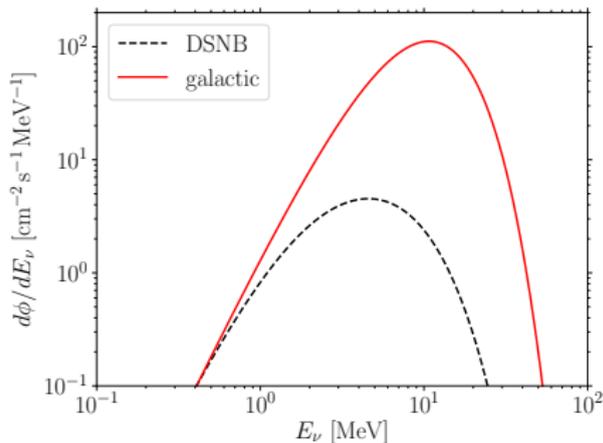
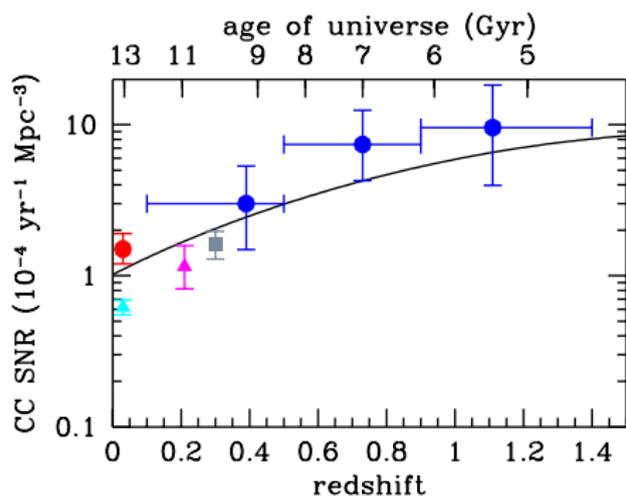


Figure: Cosmic CC SNR, 1403.0007

# Atmospheric $\nu$ 's originating from CR interactions

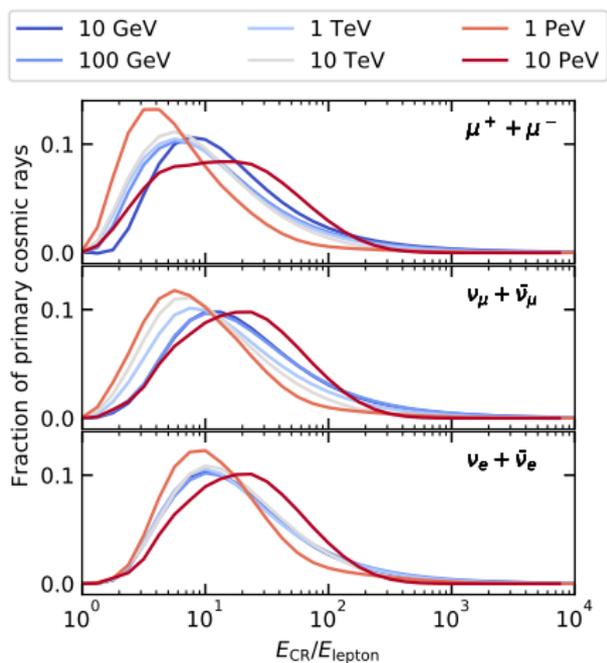


Figure:  $E_{CR}$  to leptons, 1806.04140

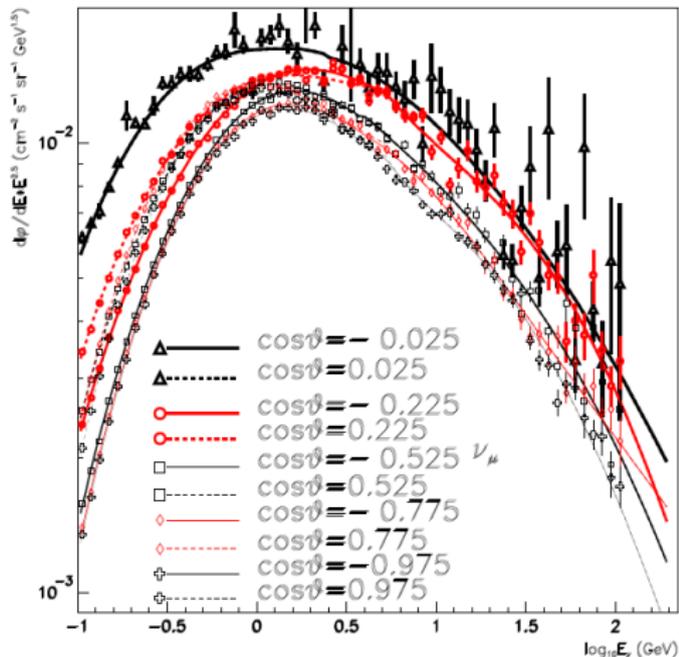
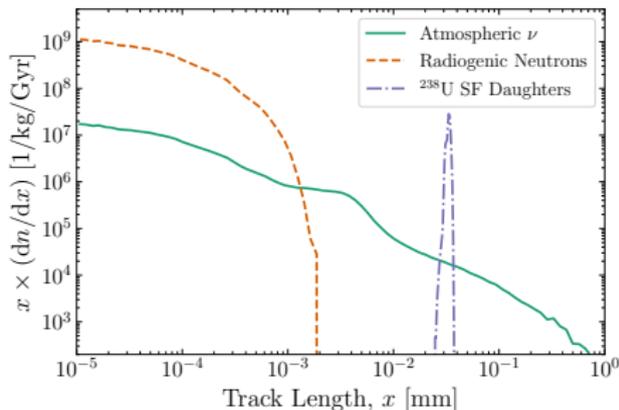
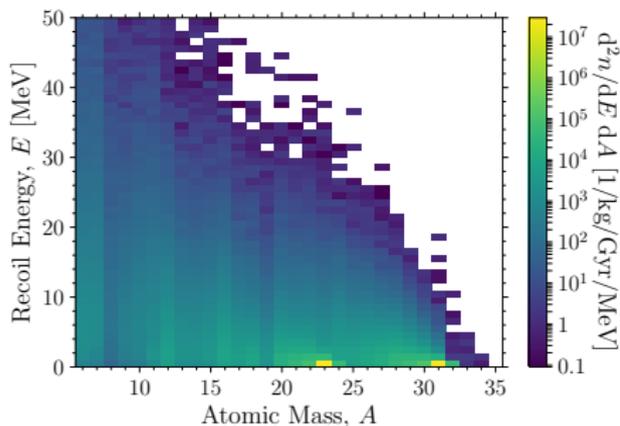


Figure: FLUKA simulation of  $\nu_\mu$  flux at SuperK for solar max, hep-ph/0207035

# Recoil spectra from atmospheric $\nu$ 's incident on NaCl(P)



## Recoils of many different nuclei

- Low energy peak from QE neutrons scattering  $^{23}\text{Na}$ ,  $^{31}\text{P}$
- High energy tail of lighter nuclei produced by DIS

## Background free regions for $\gtrsim 1 \mu\text{m}$

- Radiogenic n-bkg confined to low  $x$ , regardless of target
- Subdominant systematics from atmosphere, heliomagnetic field

# Semi-analytic range calculations and SRIM agree with data

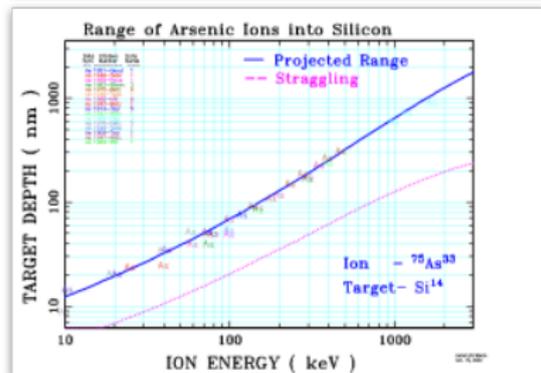
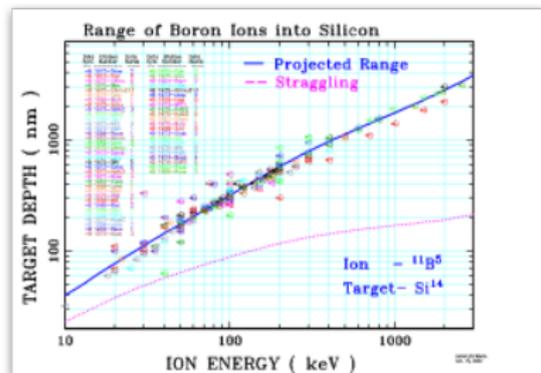
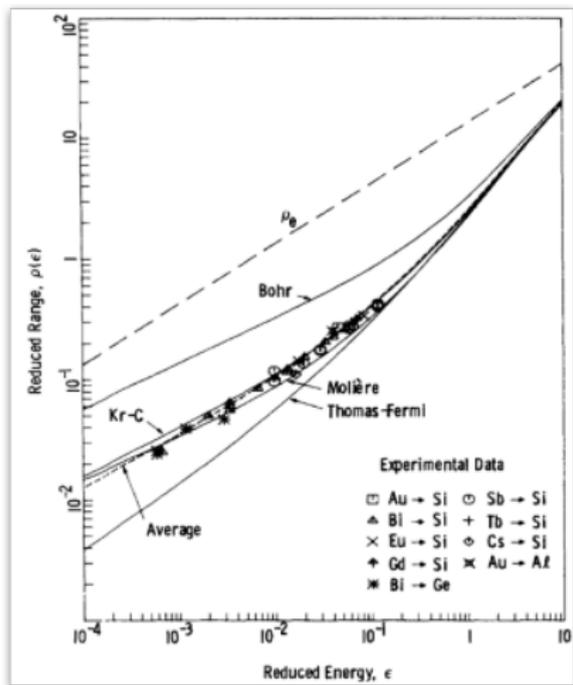


Figure: Wilson, Hagmark+ '76