

Triplet Charged Higgs at the LHC

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SM+Real Triplet

- SM with a $Y=0$ real $SU(2)$ triplet

$$\Phi = \begin{pmatrix} \phi^+ \\ \phi^0 \end{pmatrix}, \quad T = \begin{bmatrix} \frac{T^0}{\sqrt{2}} & T^+ \\ T^- & -\frac{T^0}{\sqrt{2}} \end{bmatrix}$$

$$V(\Phi, T) = m_\Phi^2 \Phi^\dagger \Phi + m_T^2 \text{Tr}(T^\dagger T) + \lambda_1 |\Phi^\dagger \Phi|^2 \\ + \lambda_2 (\text{Tr}|T^\dagger T|)^2 + \lambda_3 \Phi^\dagger \Phi \text{Tr}(T^\dagger T) + A(\Phi^\dagger T \Phi)$$

- EWSB condition: $\phi^0 = v_1 + \phi_r^0 + iG^0$ and $T^0 = v_T + T_r^0$

Doublet

- Particle spectrum: $h_1(h_{125}), h_2(\sim T^0), H^\pm(\sim T^\pm)$

Triplets

- $A(\Phi^\dagger T \Phi)$ term causes the mixing between doublet and triplet

- Triplets do not couple to fermions: as no $SU(2)$ gauge invariant vertex is possible.

Inert Triplet

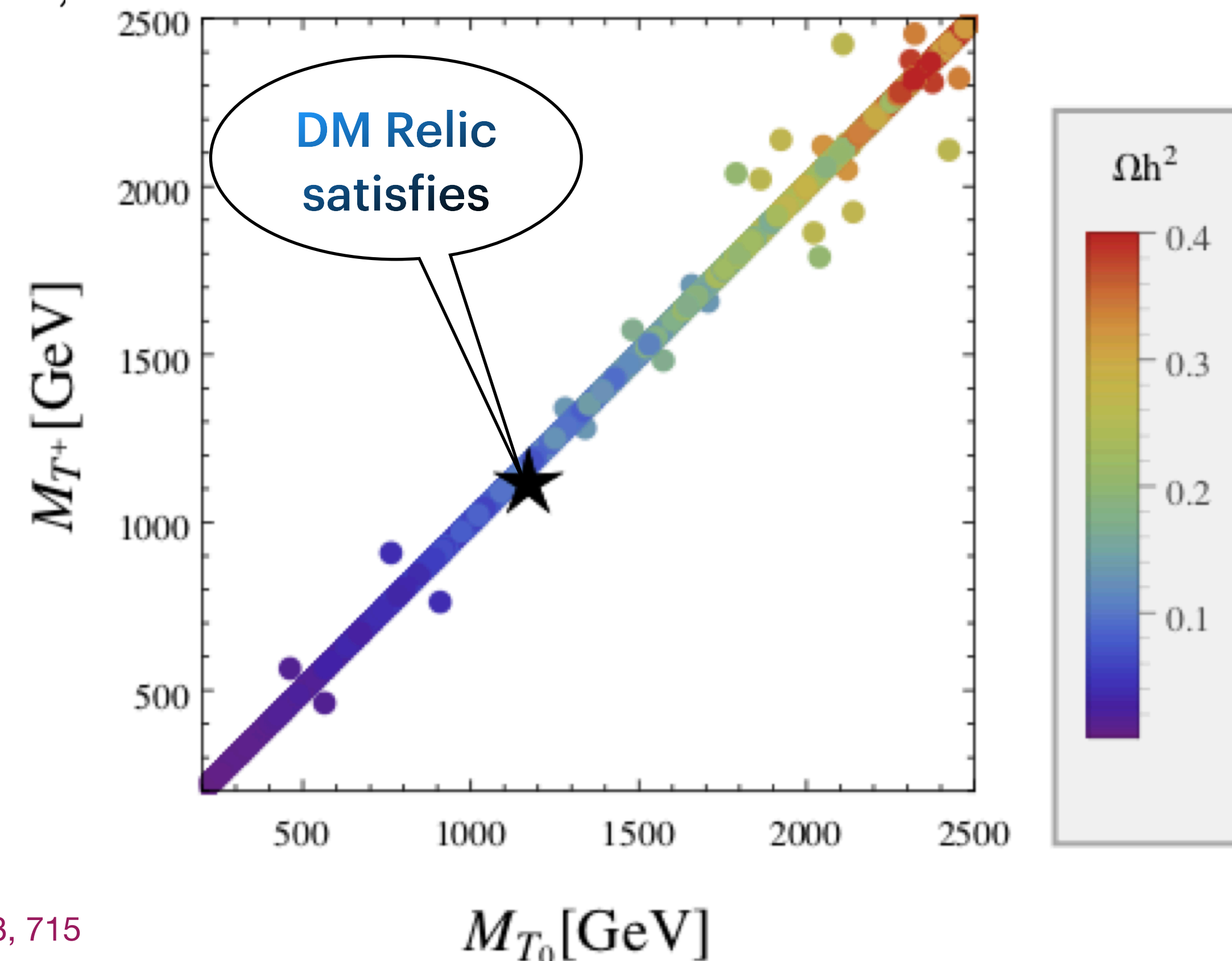
- If the triplet field is odd under Z_2 then potential takes a form

$$V(\Phi, T) = m_\Phi^2 \Phi^\dagger \Phi + m_T^2 \text{Tr}(T^\dagger T) + \lambda_1 |\Phi^\dagger \Phi|^2 + \lambda_2 (\text{Tr}|T^\dagger T|)^2 + \lambda_3 \Phi^\dagger \Phi \text{Tr}(T^\dagger T)$$

- Triplet does not get vev and neutral component T^0 can become lightest inert particle (ITP) and a candidate dark matter.
- In this case triplet and doublet does not mix at all.
- Both T^0, T^\pm are pure triplets and do not couple to fermions directly
- T^0 does not couple to Z boson also
- There is no tree-level mass splitting between
- At one-loop the mass splitting is $\Delta m(T^\pm, T^0) = m_{T^\pm} - m_{T^0} = 166 \text{ MeV}$

Constraints from DM relic

- The dominating annihilation channel for T^0 is $T^0 T^0 \rightarrow W^\pm W^\mp$
- The sub-dominant co-annihilation is $T^0 T^\pm \rightarrow ZW^\mp$
- The DM relic satisfies at $\Omega_{\text{DM}} h^2 = 0.1199 \pm 0.0027$,
- This gives strict lower bound of 1176 GeV on the DM mass



Charged Higgs Phenomenology

- The charged Higgs cannot directly decay to τ, ν or t, τ
- However, having SU(2) charged it couples to W^\pm boson
- Due to less mass gap, it has three body decays: $T^\pm \rightarrow (W^\pm)^* T^0 \rightarrow \ell + \cancel{p}_T, 2j + \cancel{p}_T$
- This leads to displaced rest mass decay length of the order of meter
- The searches in LHC and other collider may depend on the details below

Masses in GeV	Decay Modes	BR in %	Decay Width in GeV	Decay Length in m
$M_{T_0} = 1178.60$	$T^\pm \rightarrow T_0 \bar{d}u$	72.72	7.58×10^{-17}	2.64
$M_T^\pm = 1178.76$	$T^\pm \rightarrow T_0 \nu \ell^\pm$	24.30		

- The relevant production modes can be $pp \rightarrow T^\pm T^\mp, T^\pm T^0$

Displaced mono-lepton plus missing energy

- Due to TeV scale mass and purely electroweak processes, the cross-sections are small
- One can only expect healthy numbers at 100 TeV collider
- A demand of $n_\ell \geq 1 + 1 \text{ mm} \leq d \leq 10 \text{ m}$
with a displaced charged lepton can probe such scenario with early data at the LHC/FCC at 100 TeV
- The addition of scalar also enhances the vacuum stability
- Bounds can come from perturbativity More @HiggsIV by Shilpa Jangid

Complex $Y=0$ Triplet

we consider a complex triplet with $Y = 0$ hypercharge, namely

$$T = \frac{1}{\sqrt{2}} \begin{pmatrix} t_0 & \sqrt{2} t_1^+ \\ \sqrt{2} t_2^- & -t_0 \end{pmatrix}. \quad (t_1^+)^* \neq t_2^- \text{ and } t_0 \text{ is also complex.}$$

- The scalar potential is given by $V = V_1 + V_2$,

$$V_1 = \mu^2 \Phi^\dagger \Phi + \frac{\lambda_H}{2} \Phi^\dagger \Phi \Phi^\dagger \Phi + m_T^2 \text{tr}[T^\dagger T] + \frac{\lambda_T}{2} \text{tr}[T^\dagger T] \text{tr}[T^\dagger T] + \frac{\lambda_{T'}}{2} \text{tr}[T^\dagger T T^\dagger T] \\ + \frac{\lambda_{HT}}{2} \Phi^\dagger \Phi \text{tr}[T^\dagger T] + \kappa_{HT} (\text{tr}[\Phi^\dagger T \Phi] + \text{h.c.}),$$

Z_3 Symmetric

$$V_2 = \left(m_T'^2 \text{tr}[T T] + \frac{\lambda_T^{(2)}}{2} \text{tr}[T T T T] + \frac{\lambda_T^{(3)}}{2} \text{tr}[T^\dagger T T T] \right. \\ \left. + \frac{\lambda_{HT}^{(2)}}{2} \Phi^\dagger \Phi \text{tr}[T T] \right) + \text{h.c.}..$$

- The EWSB conditions: $\Phi_0 = \frac{1}{\sqrt{2}} (v + \phi_0 + i \sigma_0)$, $t_0 = \frac{1}{\sqrt{2}} (v_T + \phi_0^t + i \sigma_0^t)$.

$$\rho^{\text{ex}} = 1.00038 \pm 0.00020, \quad \implies v_T \lesssim 5 \text{ GeV}.$$

Complex $Y=0$ Triplet: Pseudoscalar

- Unlike real $Y=0$ triplet, it has a pseudoscalar

- The Physical pseudo scalar is pure triplet $a_P = \sigma_0^t$.

- The mass of the pseudo scalar is

$$m_{a_P}^2 = \kappa_{HT} \frac{v^2}{2v_T} - 4m_T'^2 - \lambda_{HT}^{(2)} v^2 - (4\lambda_T^{(2)} + \lambda_T^{(3)}) v_T^2,$$

- Being $Y=0$, it does not couple to fermions and Z boson

- Being pseudoscalar it does not couple to $W^\pm W^\mp, ZZ$

- Corresponding loop-level couplings are also zero

- Thus without any additional discrete symmetry a_P is promoted as the dark matter candidate

Complex $Y=0$ Triplet: CP-even neutral Higgs boson

- For CP-even scalar both doublet and triplet fields mix

$$h_D = \frac{1}{N_{h_D}} \left((8v^2 \kappa_{HT}^3 + \dots) \phi_0 + 16 \kappa_{HT}^3 v v_T \phi_0^t \right),$$

$$h_T = \frac{1}{N_{h_T}} \left((-2\kappa_{HT} v_T + (\lambda_{HT} + 2\lambda_{HT}^{(2)} - 4\lambda_H) v_T^2) \phi_0 + \kappa_{HT} v \phi_0^t \right).$$

- With masses

$$m_{h_D}^2 = \lambda_H v^2 - 2\kappa_{HT} v_T + 2 \left(\lambda_{HT} + 2\lambda_{HT}^{(2)} - 2\lambda_H \right) v_T^2,$$

$$m_{h_T}^2 = \frac{\kappa_{HT}}{2v_T} (v^2 + 4v_T^2) + \left(4\lambda_H - 2\lambda_{HT} - 4\lambda_{HT}^{(2)} + \lambda_T + \frac{\lambda_{T'}^2}{+} 2(\lambda_T^{(2)} + \lambda_T^{(3)}) \right) v_T^2$$

- The model parameters get constraints from the recent Higgs boson mass and branching measurements at ATLAS and CMS experiments at the LHC

Complex $Y=0$ Triplet: Charged Higgs boson

- The charged Higgs spectrum is more complex with h_0^\pm as charged Goldstone

$$h_T^+ = \frac{2v_T}{\sqrt{v^2 + 4v_T^2}} \phi^+ + \frac{2v}{\sqrt{2}\sqrt{v^2 + 4v_T^2}} (t_2^-)^* + \frac{2v}{\sqrt{2}\sqrt{v^2 + 4v_T^2}} t_1^+,$$

$$h_P^+ = -\frac{1}{\sqrt{2}} (t_2^-)^* + \frac{1}{\sqrt{2}} t_1^+,$$

$$h_0^+ = -\frac{v}{\sqrt{v^2 + 4v_T^2}} \phi^+ + \frac{\sqrt{2}v_T}{\sqrt{v^2 + 4v_T^2}} (t_2^-)^* + \frac{\sqrt{2}v_T}{\sqrt{v^2 + 4v_T^2}} t_1^+.$$

- h_T^\pm Is the orthogonal to Goldstone is a mixed but mostly triplet charged Higgs
- h_P^\pm stays as pure triplet charged Higgs and does not couple to fermions

- The mass spectrum looks like

$$m_{h_T^\pm}^2 = \kappa_{HT} \left(\frac{v^2}{2v_T} + 2v_T \right),$$

$$m_{h_P^\pm}^2 = \kappa_{HT} \frac{v^2}{2v_T} - 4m_T'^2 - \lambda_{HT}^{(2)} v^2 - (2\lambda_T^{(2)} + \lambda_T^{(3)} + \frac{\lambda_{T'}}{2}) v_T^2$$

- With a tree-level splitting with the pseudo scalar

$$m_{h_P^\pm}^2 - m_{a_P}^2 = \left(2\lambda_T^{(2)} + \frac{\lambda_{T'}}{2} \right) v_T^2$$

Decays of the Charged Higgs bosons

- Odd number of pure state in a vertex i.e. a_P or h_P^\pm , vanishes

$$g_{a_P h_{i=P,T}^+ W^-} = -\frac{g_L}{2} \left(\mathcal{R}_{21}^P \mathcal{R}_{i1}^C - \sqrt{2} \mathcal{R}_{22}^P (\mathcal{R}_{i2}^C - \mathcal{R}_{i3}^C) \right),$$

$$g_{Z h_{i=P,T}^+ W^-} = -\frac{i}{2} g_L \left(g_Y v \sin \theta_W \mathcal{R}_{i1}^C + \sqrt{2} g_L v_T \cos \theta_W (\mathcal{R}_{i2}^C - \mathcal{R}_{i3}^C) \right).$$

- $g_{a_P h_T^+ W^-}$, $g_{Z h_P^+ W^-}$ vanish but $g_{Z h_T^+ W^-}$ remains non-zero.
- Appearance of pure states twice makes the vertices non-zero e.g. $a_P h_P^+ W^-$
- The pure triplet nature acts effectively as an odd number in a discrete symmetry

Z_3 Symmetric limit

- In the Z_3 symmetric limit $T \rightarrow e^{\frac{2\pi i}{3}} T$ and others remain invariant
- The V_2 part of the potential goes to zero leaving

$$m_{a_P}^2 = \kappa_{HT} \frac{v^2}{2v_T}, \quad m_{h_P^\pm}^2 = \kappa_{HT} \frac{v^2}{2v_T} + \frac{\lambda_{T'}}{2} v_T^2, \quad m_{h_T^\pm}^2 = \kappa_{HT} \left(\frac{v^2}{2v_T} + 2v_T \right)$$

- In the limit of $\lambda_{T'} \rightarrow 0$, the pure pseudo scalar and pure charged Higgs are degenerate at the tree-level
- An one-loop splitting of 166 MeV between h_P^\pm, a_P comes as the real triplet case
- However, mass splitting between h_T^\pm, a_P can be larger proportional to $2\kappa_{HT}v_T$
- h_P^\pm gives rise to displaced charged lepton
- h_T^\pm Have prompt decays

Custodial Limit

- In the Custodial limit $v_T \rightarrow 0$ and we get $\rho \equiv 1$
- The mass spectrum and fields take the following form

$$\begin{aligned}
 m_{h_D}^2 &= \lambda_H v^2, & h_D &= \phi_0, \\
 m_{h_T}^2 &= m_T^2 + 2m_T'^2 + \frac{1}{2} \left(\frac{\lambda_{HT}}{2} + \lambda_{HT}^{(2)} \right) v^2, & h_T &= \phi_0^t, \\
 m_{a_P}^2 &= m_T^2 - 2m_T'^2 + \frac{1}{2} \left(\frac{\lambda_{HT}}{2} - \lambda_{HT}^{(2)} \right) v^2, & a_P &= \sigma_0^t, \\
 m_{h_{T/P}^\pm}^2 &= m_T^2 \pm 2m_T'^2 + \frac{1}{2} \left(\frac{\lambda_{HT}}{2} \pm \lambda_{HT}^{(2)} \right) v^2, & h_{T/P}^\pm &= \frac{1}{\sqrt{2}} (t_1^\pm \pm (t_2^\mp)^*).
 \end{aligned}$$

- Both the charged Higgs bosons are pure triplet and none decays to ZW
- In the Z_3 limit h_T^\pm, h_P^\pm become degenerate with a_P, h_T at the tree-level

Dark Matter Phenomenology

- From Higgs data we get a lower bound of $h_{T/P}^{\pm} \gtrsim 600 \text{ GeV}$
- Similar to the real triplets dominant annihilation modes is $a_P a_P \rightarrow W^{\pm} W^{\mp}$
- The co-annihilation mode is $a_P h_P^{\pm} \rightarrow ZW^{\mp}$
- However, $\sigma(a_P h_T^{\pm} \rightarrow ZW^{\mp}) = 0$ due to purity non-conservation

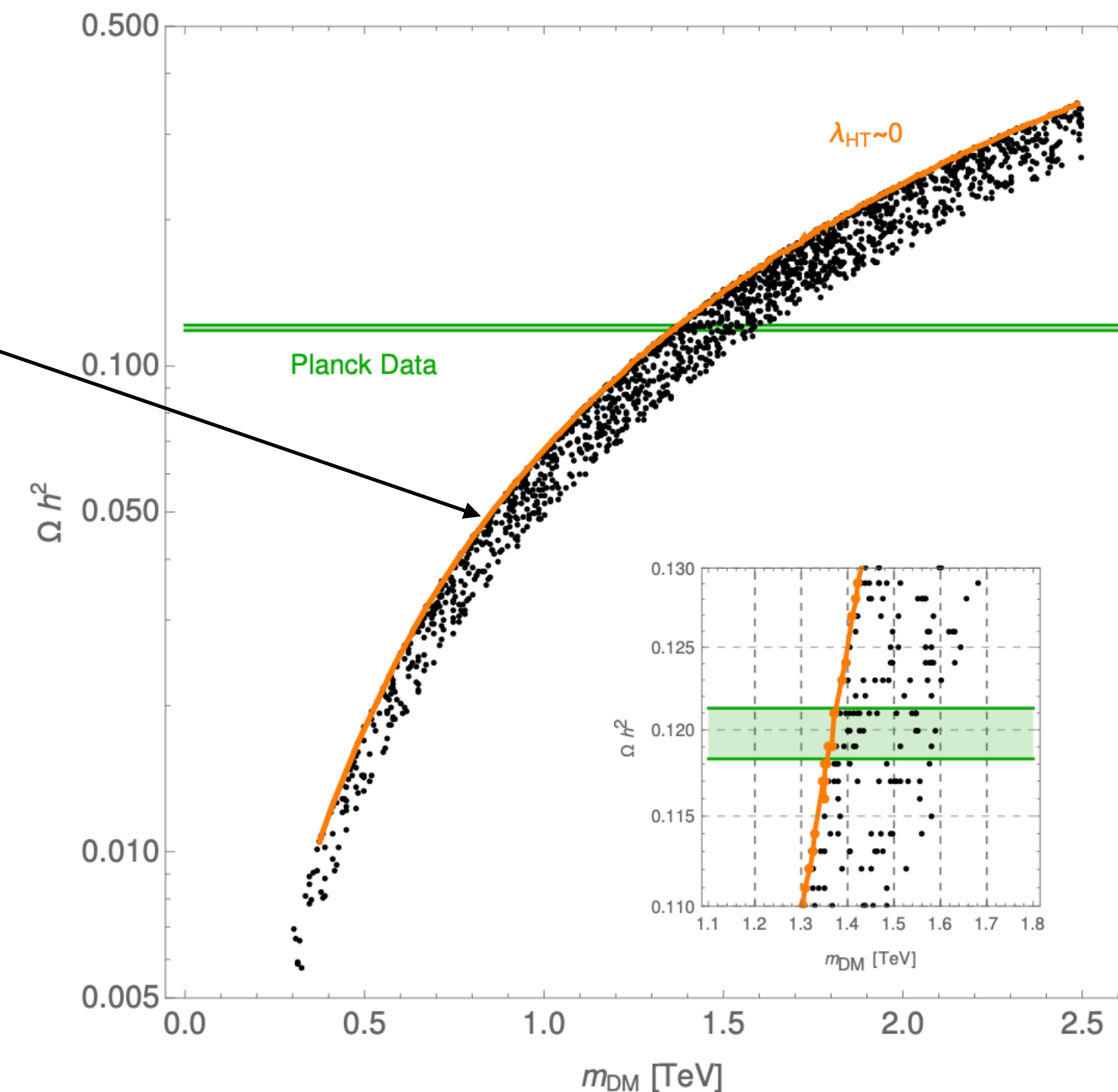
- This implies

$$m_{DM}^{min} \equiv m_{a_P}^{min} \sim 1.35 \text{ TeV},$$

corresponds to the $\lambda_{HT} \sim 0$ case.

- Whereas

$$m_{DM}^{max} \equiv m_{a_P}^{max} \sim 1.60 \text{ TeV}.$$

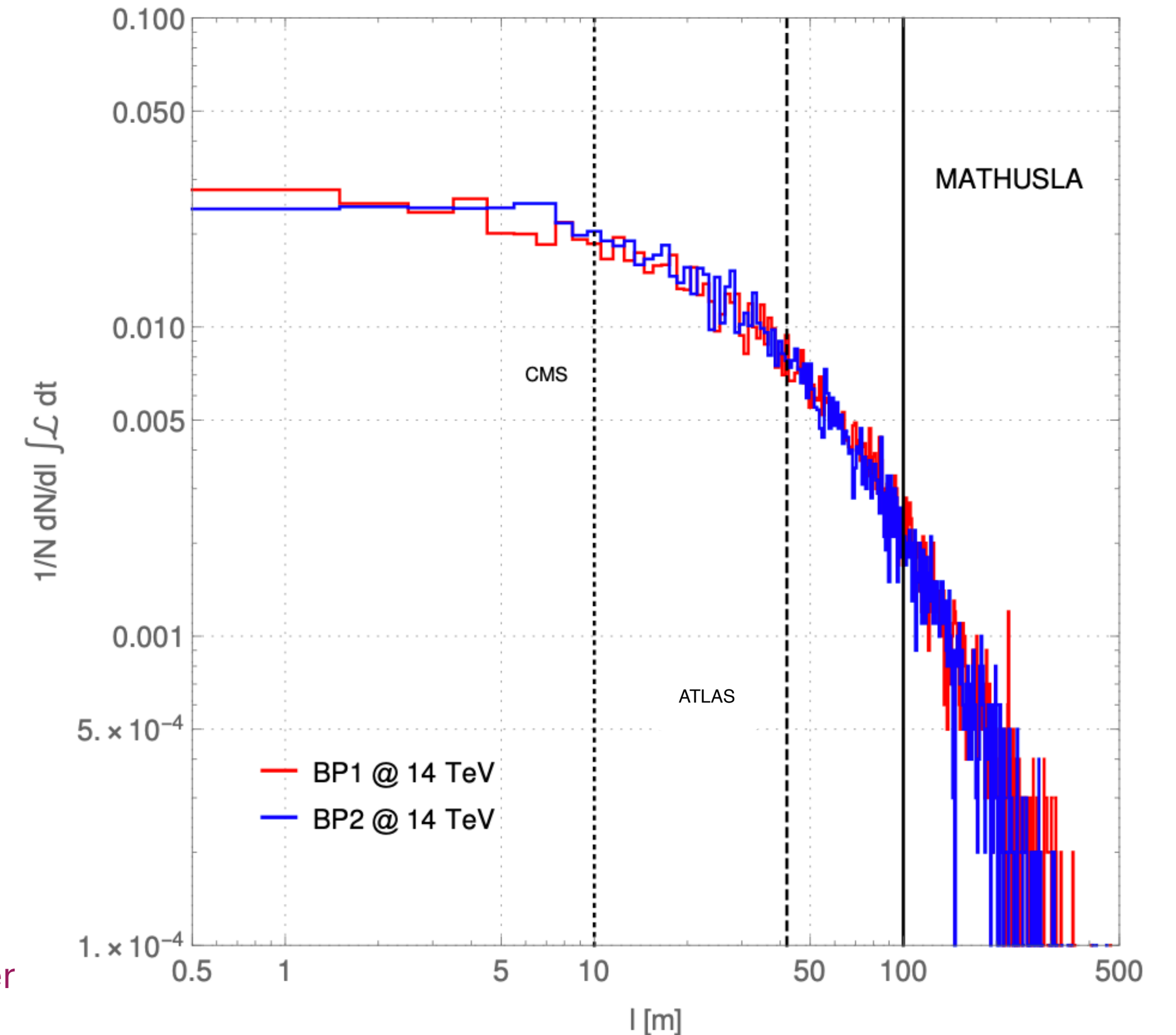


LHC Phenomenology

- The existence of two triplet charged Higgs bosons but phenomenologically different h_T^\pm, h_P^\pm
- h_T^\pm has prompt decay with dominant modes $Br(h_T^+ \rightarrow W^+ Z) \sim Br(h_T^+ \rightarrow W^+ h_D) \sim 0.48$.
- h_T^\pm decays to tb is restricted to $\sim 4\%$
- h_P^\pm Has displaced decay of width $\sim 10^{-16}$ GeV
 $h_P^\pm \rightarrow a_P(W^\pm)^*$, where the W^\pm remains off-shell.
- Along with LHC muon collider can also probe the triplet charged Higgs bosons with

$$\frac{\sigma_\mu^{14 \text{ TeV}}(X)}{\sigma_p^{14 \text{ TeV}}(X)} = 10^4 - 10^2, \quad \sigma_\mu^{14 \text{ TeV}}(X) \gtrsim 10^2 \sigma_p^{100 \text{ TeV}}(X)$$

More @BSMV by A. Costantini on 26/05: (New) Physics at multi-TeV muon Collider



Conclusions

- The real $Y=0$, triplet gives rise to one charged Higgs with displaced decay
- The complex $Y=0$, triplet gives rise to one displaced and one prompt decays of Charged Higgs bosons
- For the real case to have a dark matter we need a Z_2 symmetry
- In case of complex $Y=0$ triplet, purity of triplet behaves like a discrete symmetry
- Displaced Mono/di-lepton plus missing energy can probe the real $Y=0$ triplet
- Existence of both displaced and prompt lepton plus missing energy can probe $Y=0$ complex triplet
- Muon collider and be promising along with the LHC

THANK

You!