

Getting Chirality Right

single scalar leptoquarks
and lepton magnetic dipole moments

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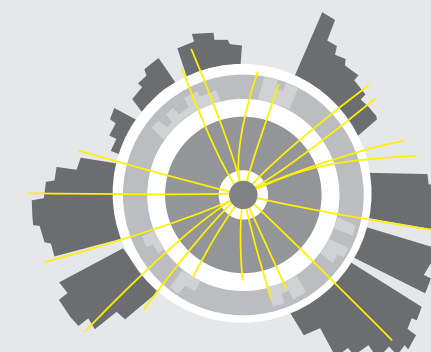
Phenomenology 2021 Symposium, University of Pittsburgh



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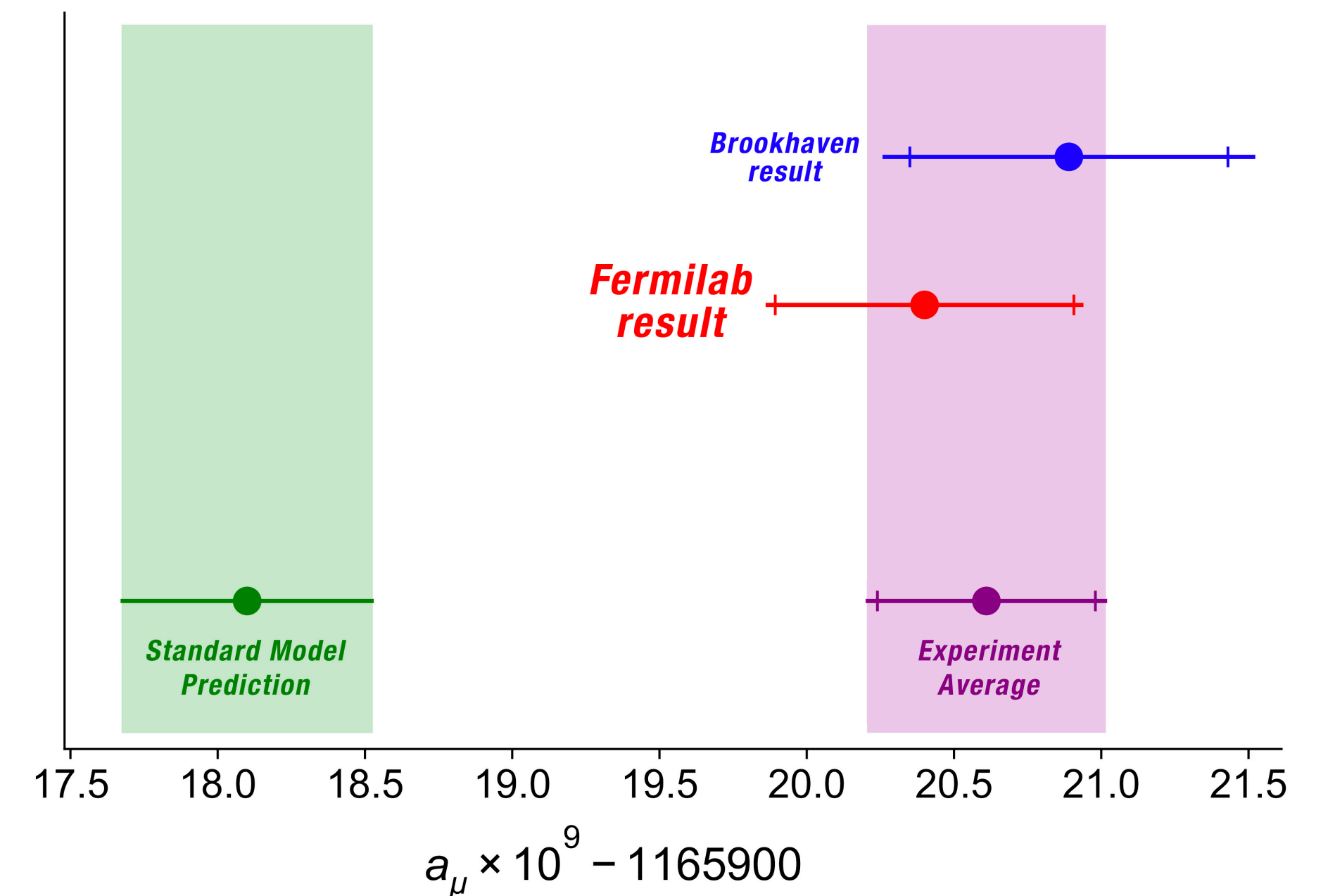
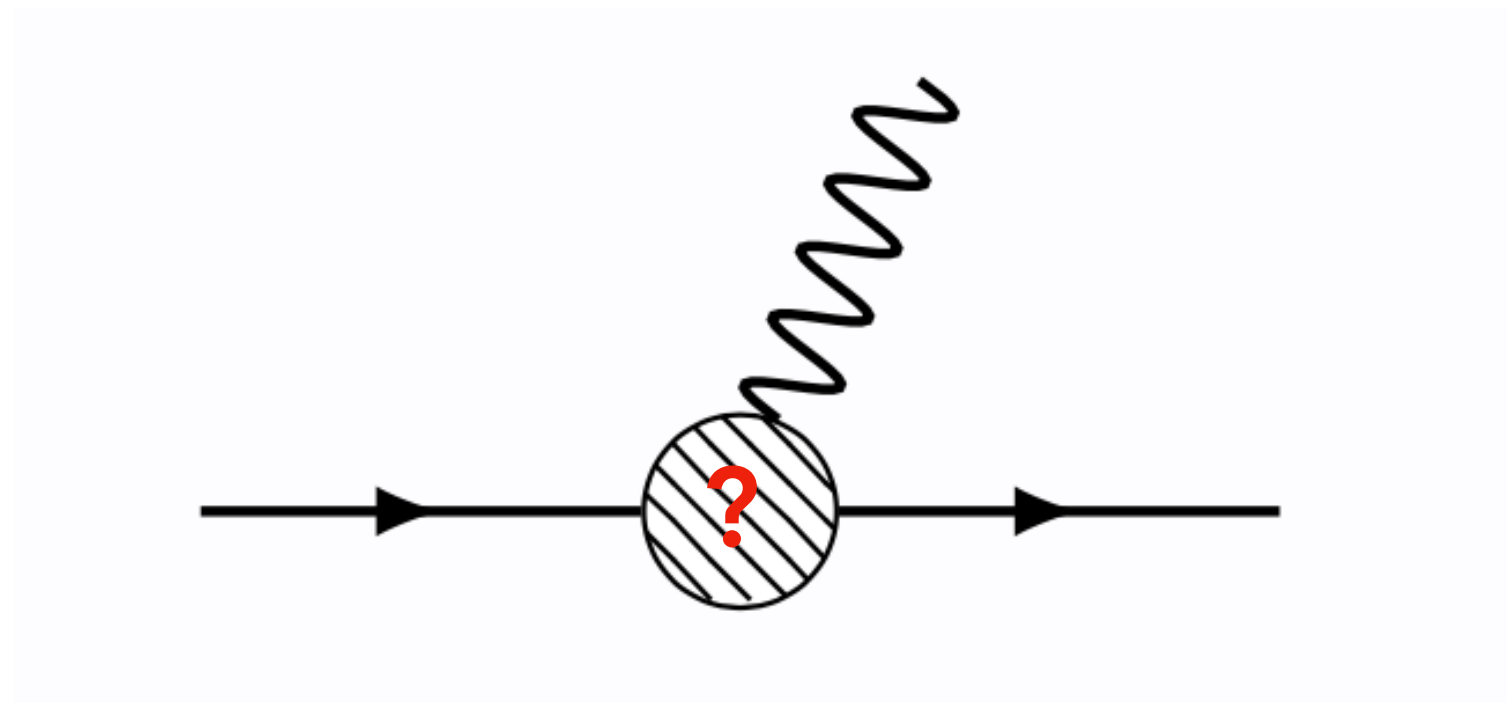
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(g-2) of the muon

- I hopefully won't need to explain this in too much detail, as it has made waves in recent months.
- Long-standing anomaly — perhaps hinting at new physics that couples to muons
- Many papers investigate possible new physics explanations
- Other muonic anomalies, e.g. $b \rightarrow s \mu \mu$, corroborate the idea of LFV in BSM physics



Deviation from SM prediction	Significance
$\Delta a_\mu = (2.86 \pm 0.76) \times 10^{-9}$	4.2σ

(g-2) of the electron

- Established precision test for the SM and QED:

- 'Measuring' the fine structure constant, α , assumes:

$$a_e^{\text{SM}}(\alpha) = a_e^{\text{Exp}} \implies \alpha$$

- This would assume no anomaly! So we require a determination of α independent of g-2.
- Two conflicting experimental results for α , via interferometry experiments, disagree by more than 5 sigma:
 - Using Cs, anomaly opposite sign to the muon
 - Using Rb, anomaly (?) in the same sign as the muon

Deviation from SM prediction	Significance
$\Delta a_\mu = (2.86 \pm 0.76) \times 10^{-9}$	4.2σ
$\Delta a_e^{\text{Cs}} = -(0.88 \pm 0.36) \times 10^{-12}$ <small>Parker et al 1812.04130</small>	2.5σ
$\Delta a_e^{\text{Rb}} = (4.8 \pm 3.0) \times 10^{-13}$ <small>Morel et al 2020, INSPIRE: 1837309</small>	1.6σ

So far, no resolution to this disagreement

(g-2) anomalies

$$\mathcal{L}_{a_\ell} = \bar{\ell} \left(\boxed{a_\ell} \frac{e}{4m_\ell} \sigma_{\mu\nu} - d_\ell \frac{i}{2} \sigma_{\mu\nu} \gamma_5 \right) \ell F^{\mu\nu}$$

Magnetic dipole
moment

$$\Delta a_\ell = a_\ell^{\text{exp}} - a_\ell^{\text{SM}}$$

Deviation from SM prediction

Significance

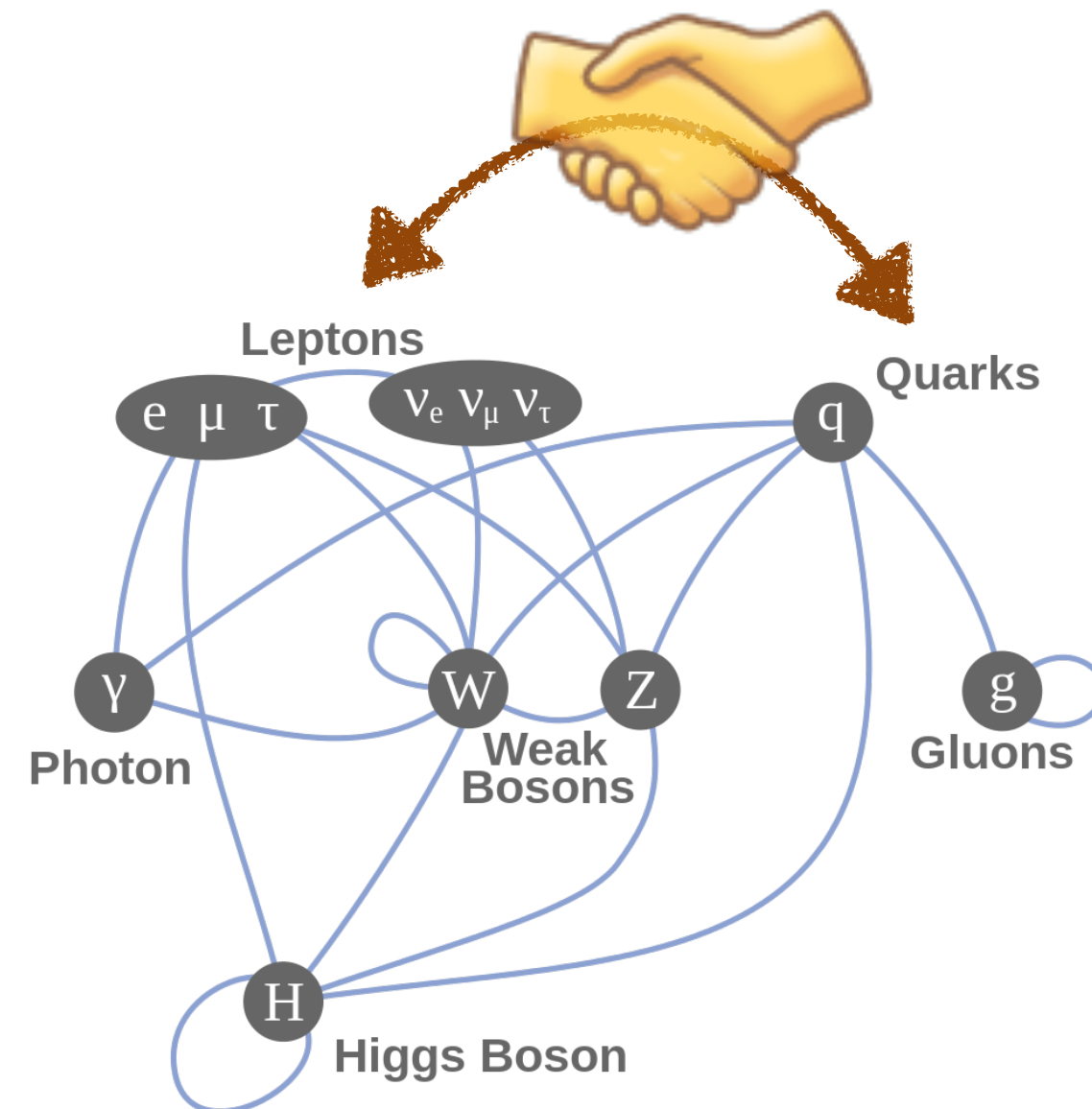
$\Delta a_\mu = (2.86 \pm 0.76) \times 10^{-9}$	4.2 σ
$\Delta a_e = -(0.88 \pm 0.36) \times 10^{-12}$	2.5 σ

While electron g-2 is still unresolved, we focus on the more significant anomaly, also because it is a more interesting problem to tackle.

The Problem

- Anomalies in the electron and muon magnetic dipole moments
- Deviations have **opposite sign**, but comparable magnitude
- Could there be a common origin via flavour-violating couplings?

Scalar LQs



Symbol	$SU(3)_C \otimes SU(2)_L \otimes U(1)_Y$
\tilde{S}_1	$(\mathbf{3}, \mathbf{1}, -4/3)$
S_1	$(\mathbf{3}, \mathbf{1}, -1/3)$
S_3	$(\mathbf{3}, \mathbf{3}, -1/3)$
\bar{S}_1	$(\mathbf{3}, \mathbf{1}, 2/3)$
R_2	$(\mathbf{3}, \mathbf{2}, 7/6)$
\tilde{R}_2	$(\mathbf{3}, \mathbf{2}, 1/6)$

- Leptoquarks (LQ) are hypothetical particles which directly couple SM leptons and quarks
- There are a finite set of scalar LQ (for a review, see arXiv: 1603.04993)
- LQ masses and Yukawa couplings between SM and BSM fields are generically *free* parameters, e.g.

$$\mathcal{L}_\ell = \overline{\ell^{(c)}} \left[\boxed{y^R P_R} + \boxed{y^L P_L} \right] q \phi^\dagger + h.c.$$

Left-handed coupling

Right-handed coupling

Chiral scalar LQs

Left-handed coupling

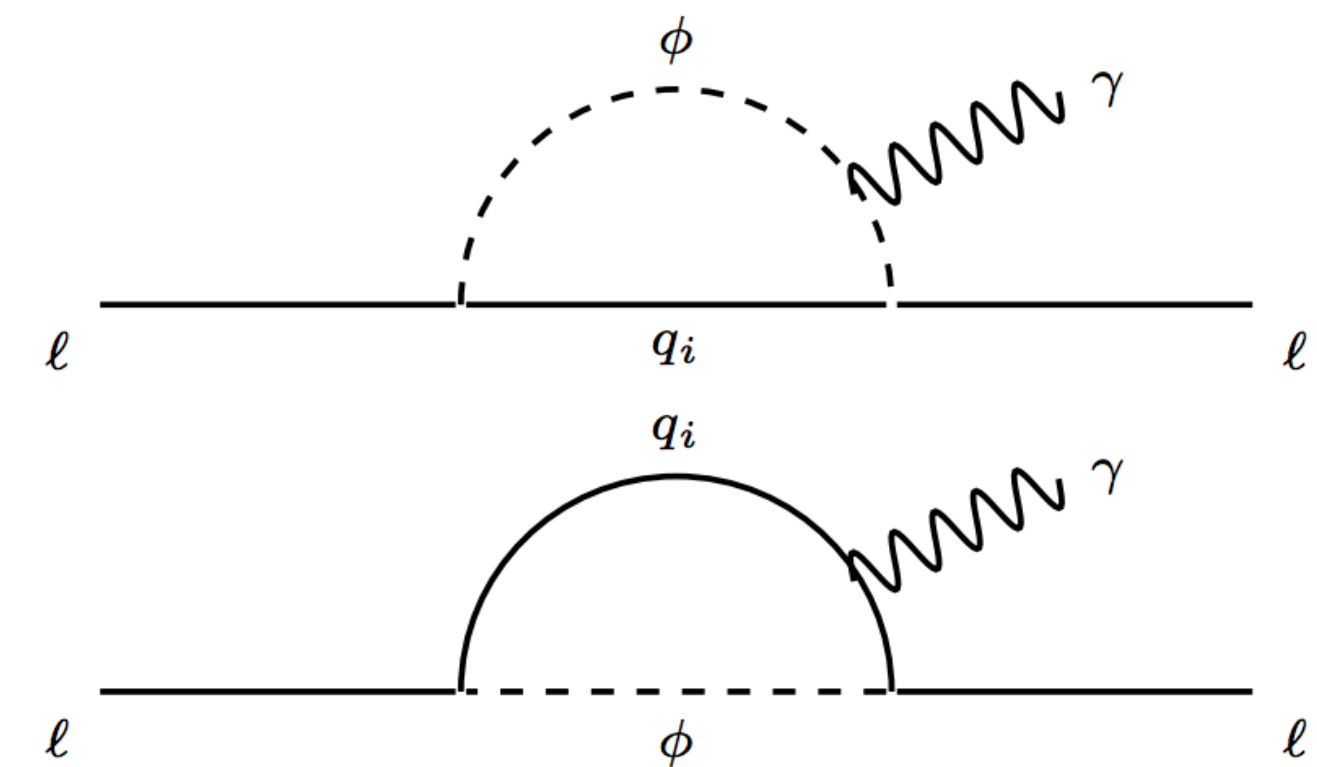
$$\mathcal{L}_\ell = \overline{\ell^{(c)}} \left[y^R P_R + y^L P_L \right] q \phi^\dagger + h.c.$$

Right-handed coupling

Symbol	$SU(3)_C \otimes SU(2)_L \otimes U(1)_Y$	$(g-2)_\ell$ at 1L
\tilde{S}_1	$(\mathbf{3}, \mathbf{1}, -4/3)$	\times
S_1	$(\mathbf{3}, \mathbf{1}, -1/3)$	\checkmark
S_3	$(\mathbf{3}, \mathbf{3}, -1/3)$	\times
\bar{S}_1	$(\mathbf{3}, \mathbf{1}, 2/3)$	\times
R_2	$(\mathbf{3}, \mathbf{2}, 7/6)$	\checkmark
\tilde{R}_2	$(\mathbf{3}, \mathbf{2}, 1/6)$	\times

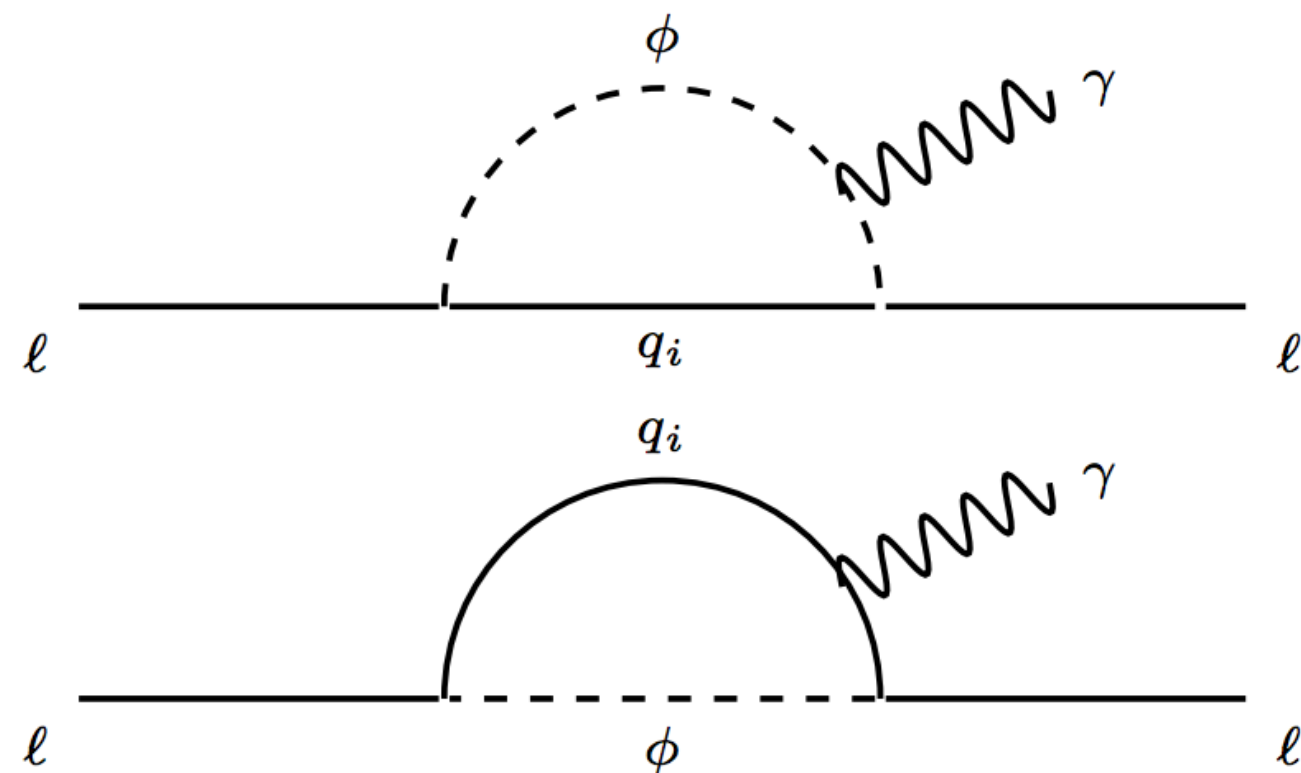
The highlighted LQ are (maximally) chiral

- Maximally-chiral (also just called 'chiral') LQ have both L and R couplings
- *Could* generate sizeable corrections to $(g-2)$ at one-loop via:



Chiral scalar LQs

$$\mathcal{L}_\ell = \overline{\ell^{(c)}} [y^R P_R + y^L P_L] q \phi^\dagger + h.c.$$



S_1	$(\mathbf{3}, \mathbf{1}, -1/3)$
R_2	$(\mathbf{3}, \mathbf{2}, 7/6)$

$$\Delta a_\ell = -\frac{3m_\ell}{8\pi^2 m_\phi^2} \sum_q \left[\overset{\text{sign-definite}}{m_\ell (|y_\ell^R|^2 + |y_\ell^L|^2) \kappa} + \overset{\text{variable sign}}{m_q \text{Re}(y_\ell^{L*} y_\ell^R) \kappa'} \right]$$

For these two LQ, we can exploit this variable sign term to give flavour-dependent, opposite sign, corrections

Flavour ansatz

- I will preface this next discussion by saying that the what I'm about to discuss **isn't** showing a basis-dependence of a physical result (that would be ludicrous!)
- My argument here is that: *a choice of basis can affect how clear it is to make definitive claims about a model's viability.*

Flavour ansatz

How easy is it to turn on or off couplings between particular flavours?

The answer lies in the choice of *where* I put the CKM.

$$\mathcal{L}_{\text{int}}^{S_1} = (\overline{L}_L^c \lambda_{LQ} Q_L + \overline{e}_R^c \lambda_{eu} u_R) S_1^\dagger + h.c.,$$



EWSB and rotating fields
into mass-eigenstates

Recalling that: $V = \mathcal{L}_u^\dagger \mathcal{L}_d$

1. $\mathcal{R}_e \lambda_{eu} \mathcal{R}_u \mapsto y^{Seu}, \quad \mathcal{L}_e \lambda_{LQ} \mathcal{L}_u \mapsto y^{SLQ}$

$$\mathcal{L}^{S_1} \supset y_{ij}^{SLQ} \left[\overline{e}_{L,i}^c u_{L,j} - V_{jk} \overline{\nu}_{L,i}^c d_{L,k} \right] S_1^\dagger$$

‘Up-type’ $+ y_{ij}^{Seu} \overline{e}_{R,i}^c u_{R,j} S_1^\dagger + h.c.,$

2. $\mathcal{R}_e \lambda_{eu} \mathcal{R}_u \mapsto y^{Seu}, \quad \mathcal{L}_e \lambda_{LQ} \mathcal{L}_d \mapsto y'^{SLQ},$

$$\mathcal{L}^{S_1} \supset y_{ij}'^{SLQ} \left[V_{jk}^\dagger \overline{e}_{L,i}^c u_{L,k} - \overline{\nu}_{L,i}^c d_{L,j} \right] S_1^\dagger$$

‘Down-type’ $+ y_{ij}^{Seu} \overline{e}_{R,i}^c u_{R,j} S_1^\dagger + h.c.,$

'Up-type' and 'down-type' bases

1. $\mathfrak{R}_e \lambda_{eu} \mathfrak{R}_u \mapsto y^{Seu}$, $\mathfrak{L}_e \lambda_{LQ} \mathfrak{L}_u \mapsto y^{SLQ}$

$$\mathcal{L}^{S_1} \supset y_{ij}^{SLQ} \left[\overline{e_{L,i}^c} u_{L,j} - V_{jk} \overline{\nu_{L,i}^c} d_{L,k} \right] S_1^\dagger$$

'Up-type' $+ y_{ij}^{Seu} \overline{e_{R,i}^c} u_{R,j} S_1^\dagger + h.c.,$

2. $\mathfrak{R}_e \lambda_{eu} \mathfrak{R}_u \mapsto y^{Seu}$, $\mathfrak{L}_e \lambda_{LQ} \mathfrak{L}_d \mapsto y'^{SLQ}$,

$$\mathcal{L}^{S_1} \supset y'_{ij}{}^{SLQ} \left[V_{jk}^\dagger \overline{e_{L,i}^c} u_{L,k} - \overline{\nu_{L,i}^c} d_{L,j} \right] S_1^\dagger$$

'Down-type' $+ y_{ij}^{Seu} \overline{e_{R,i}^c} u_{R,j} S_1^\dagger + h.c.,$

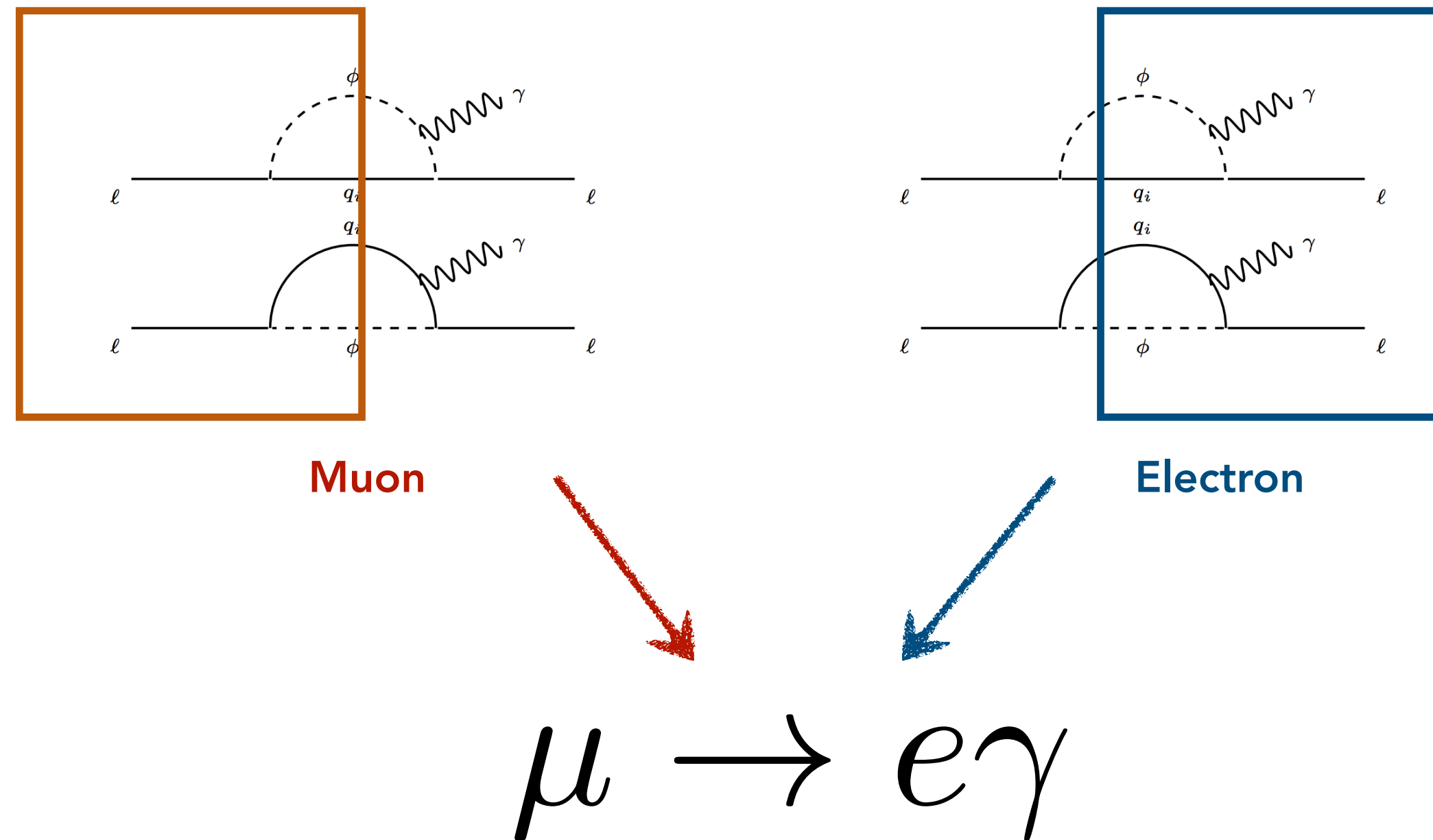
- Now imagine we want to switch-off a particular coupling: e.g. as above

LH coupling between electron and top-quark

1.	$y_{13}^{SLQ} = 0$	Simple
2.	$y'_{1j}{}^{SLQ} V_{j3}^\dagger = 0$	Messy

We should guide our basis choice by looking at what couplings we want to control the most — motivated by observables and constraints

A downside of the 'down-type' basis



- If we *did* work in the down-type quark basis, this makes it hard for us to determine a viable zero texture for the Yukawas
- Why? It turns out that because of:

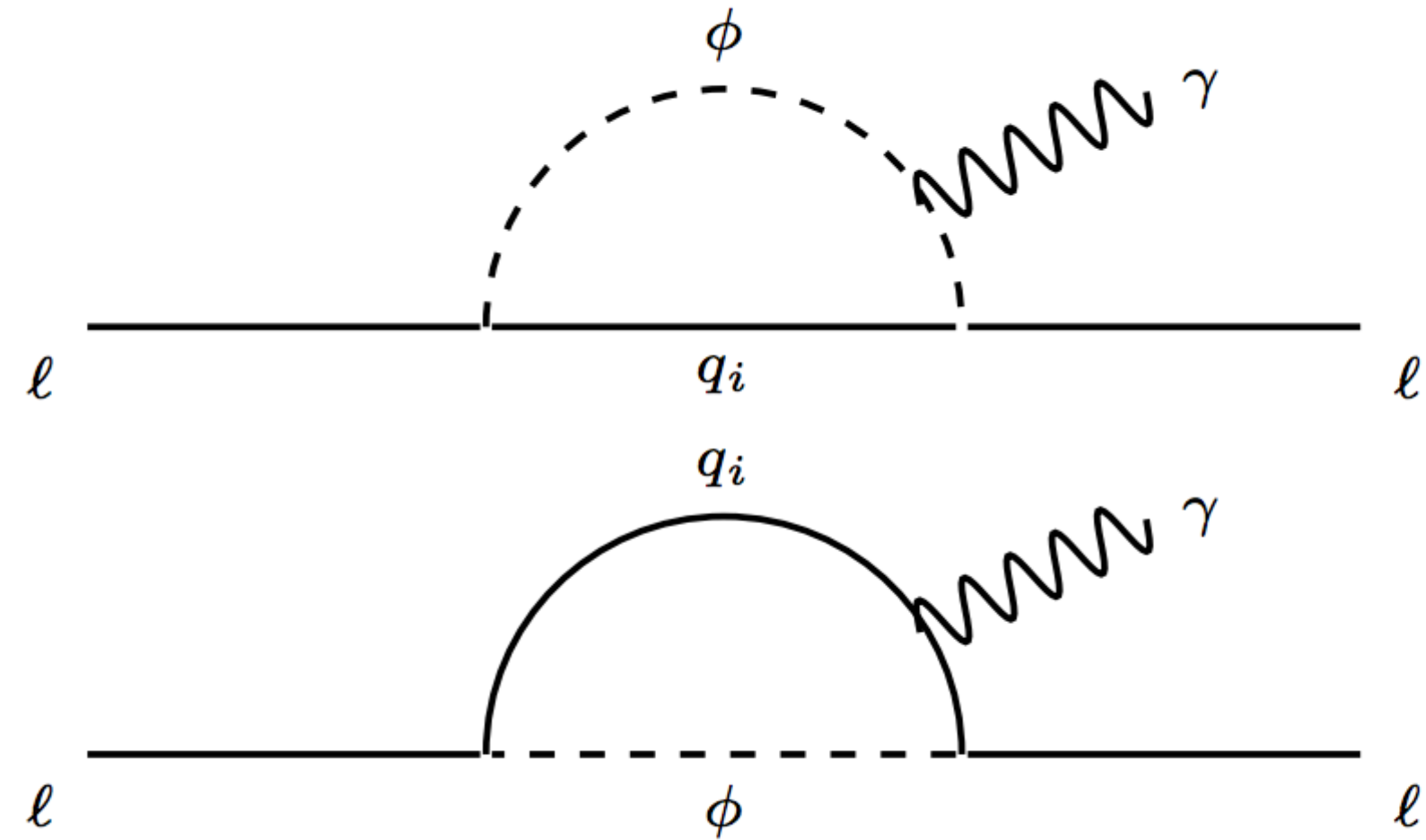
A. The enhancement of a **top-quark** in the loop

B. The strength of the MEG constraint $\mu \rightarrow e \gamma$

Even if just a 'small' coupling to the top is generated for both lepton flavours, we hit the MEG limit — **invalidating the model**

You can see how one may be tempted to rule out all scalar LQ models if you only looked in the down-type basis.

Establishing the models



Adopting the ‘up-type’ basis :

- Contribution to (g-2) of the electron is via a **charm**-containing loop
- Contribution to (g-2) of the muon is via a **top**-containing loop
- Constraints from MEG in particular avoided by having different intermediate SM quarks coupling for each g-2
- Restrict all NP couplings to real values.

$$\mathbf{y}^L \sim \begin{pmatrix} 0 & \blacksquare & 0 \\ 0 & 0 & \blacksquare \\ 0 & 0 & 0 \end{pmatrix}, \quad \mathbf{y}^R \sim \begin{pmatrix} 0 & \blacksquare & 0 \\ 0 & 0 & \blacksquare \\ 0 & 0 & 0 \end{pmatrix} \begin{matrix} u & c & t \\ e & \mu & \tau \end{matrix}$$

$$\Delta a_\ell^{S_1} \sim -\frac{m_\ell m_q}{4\pi^2 m_{S_1}^2} \left[\frac{7}{4} - 2 \log \left(\frac{m_{S_1}}{m_q} \right) \right] \text{Re}(y_{\ell q}^{L*} y_{\ell q}^R),$$

$$\Delta a_\ell^{R_2} \sim \frac{m_\ell m_q}{4\pi^2 m_{R_2}^2} \left[\frac{1}{4} - 2 \log \left(\frac{m_{R_2}}{m_q} \right) \right] \text{Re}(y_{\ell q}^{L*} y_{\ell q}^R),$$

Single mass scans

Now that we have two viable models, assessing constraints using two different scan methods:

Method 1: Fixed RH couplings around (g-2)

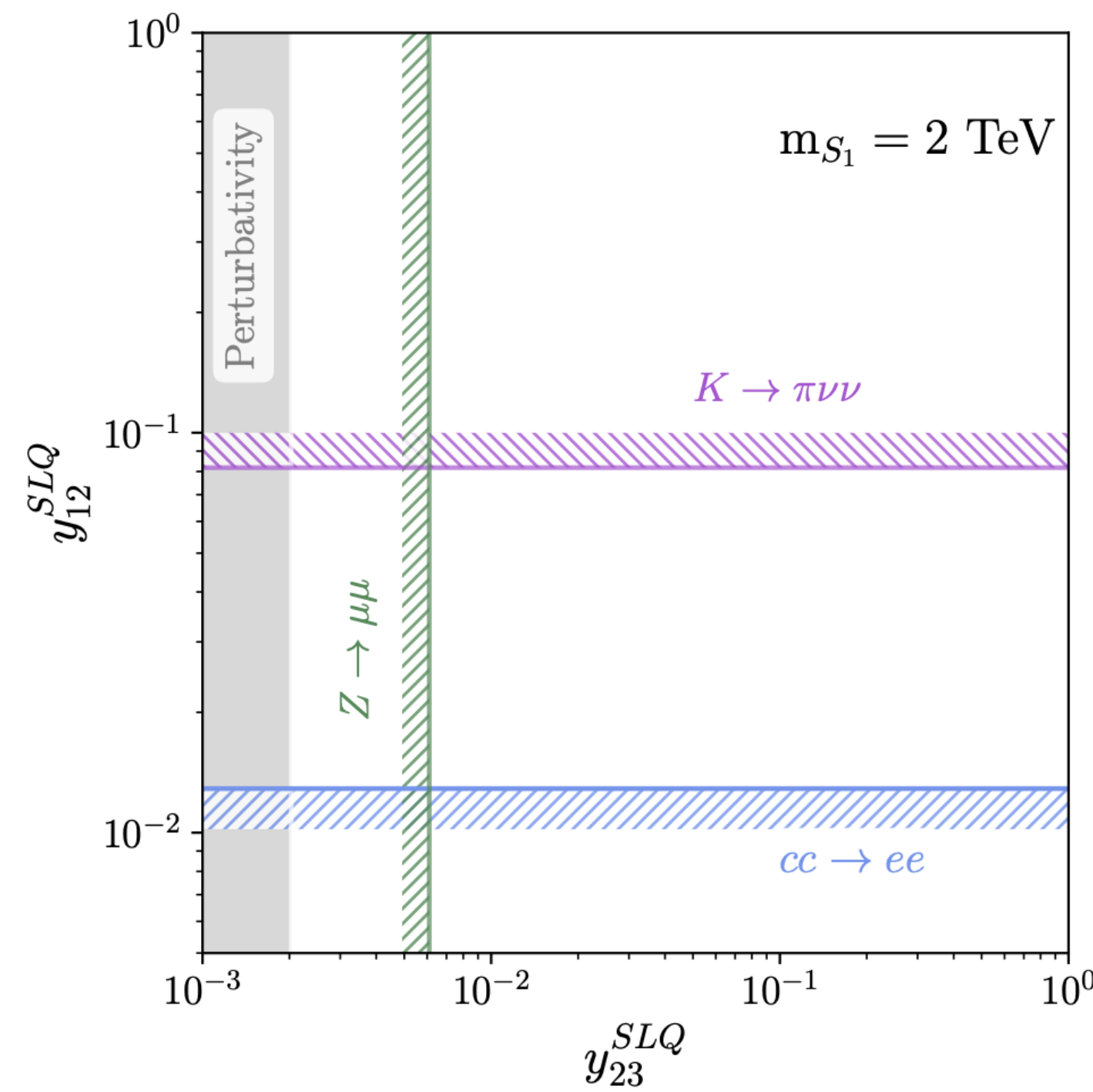
1. Logarithmically sample 2 x LH couplings
2. Calculate RH couplings according to (g-2), outputting real-value generating point closest to central values
3. Check generated RH coupling under perturbativity constraint.
4. Check other constraints

Method 2: decoupled electron and muon sectors

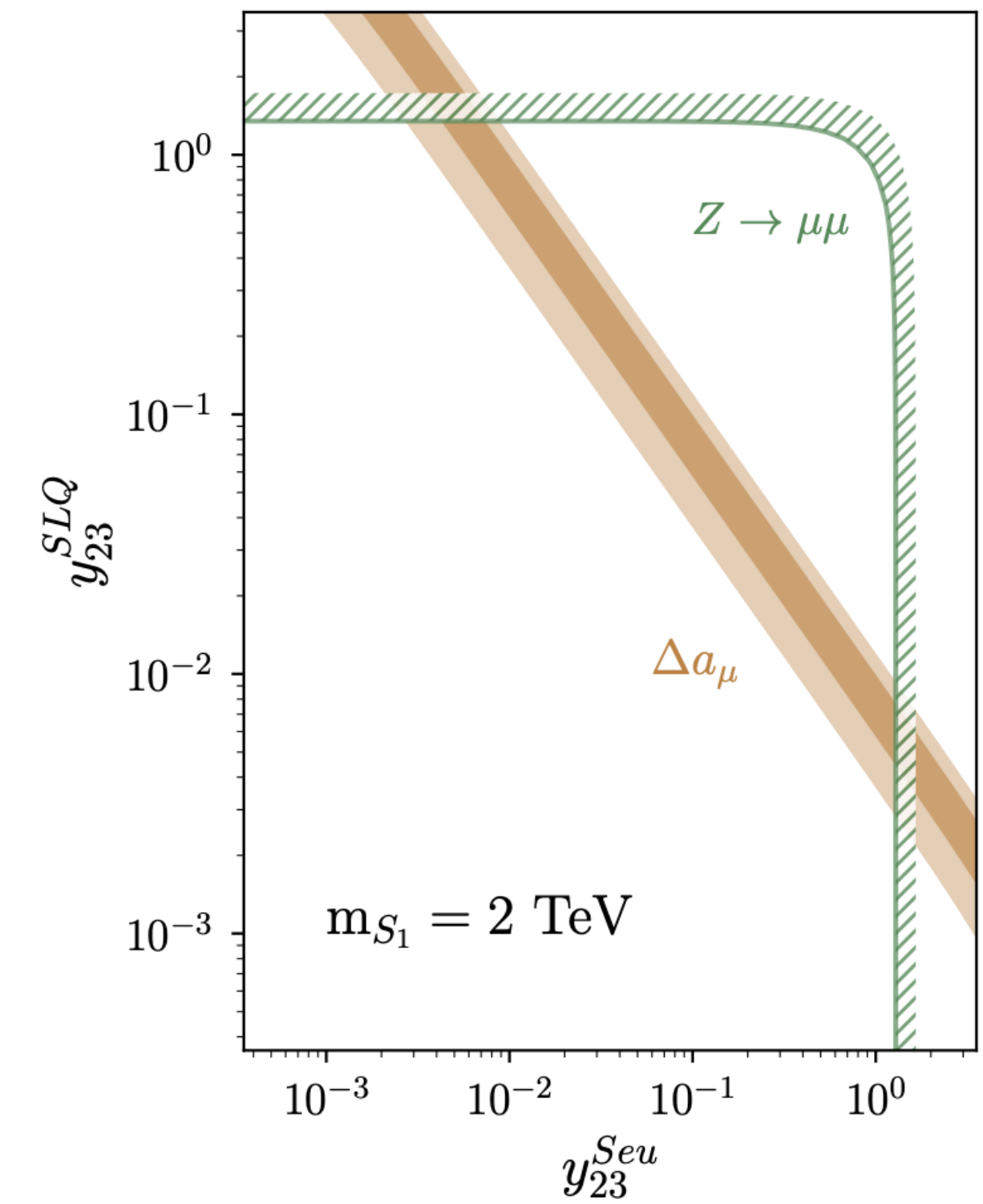
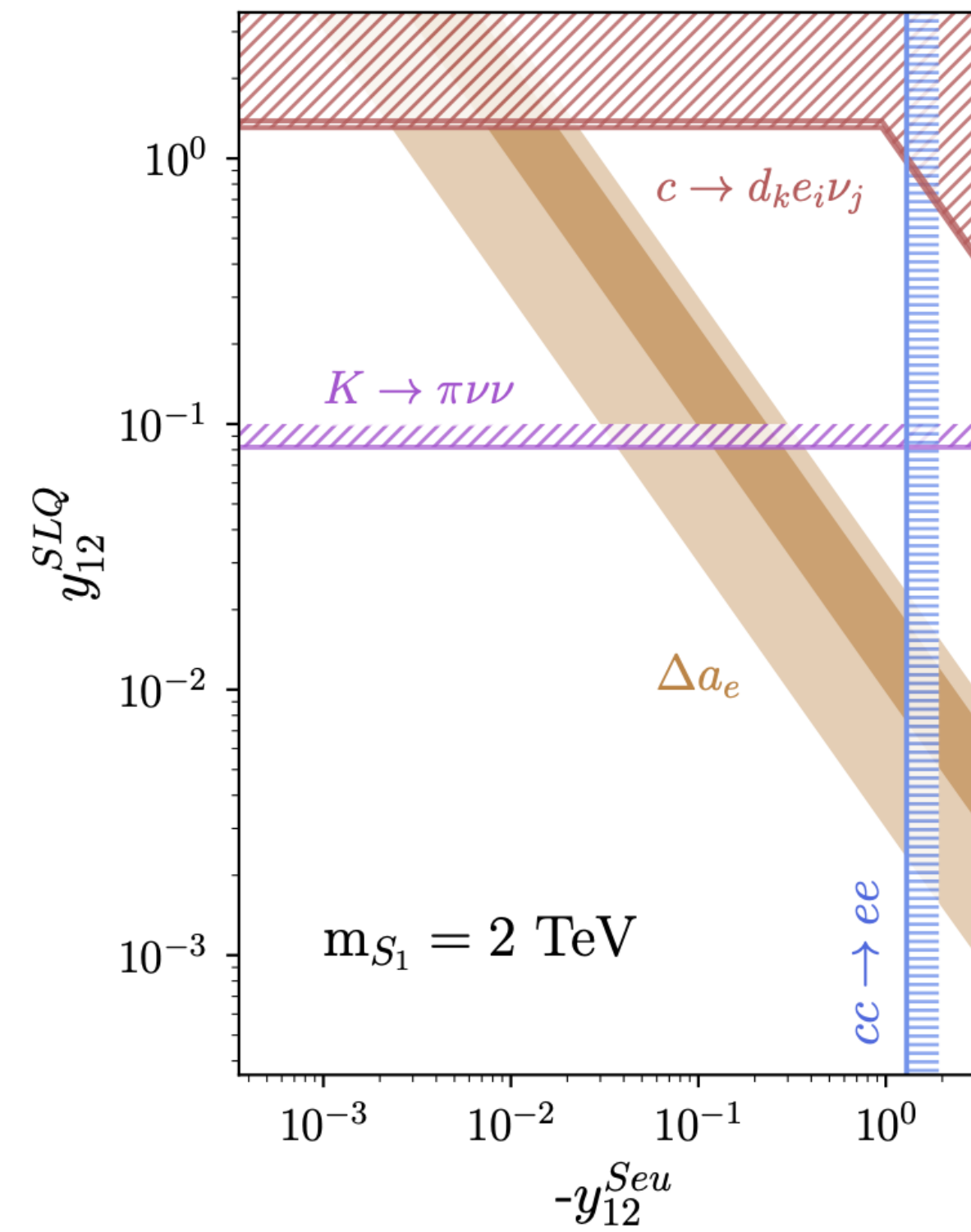
separately sampling LH and RH couplings
logarithmically

S_1 leptoquark: benchmark mass

Method 1

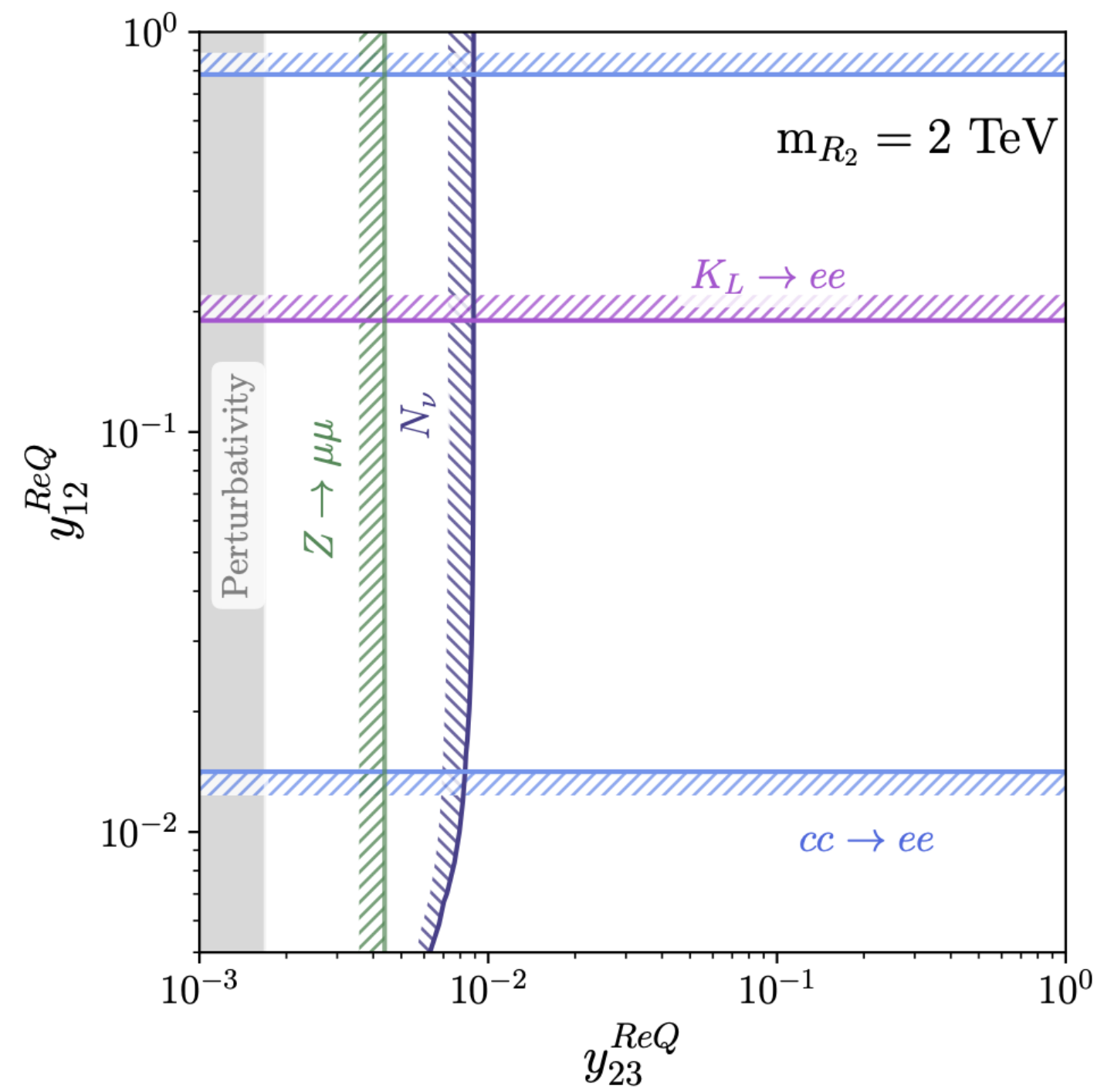


Method 2

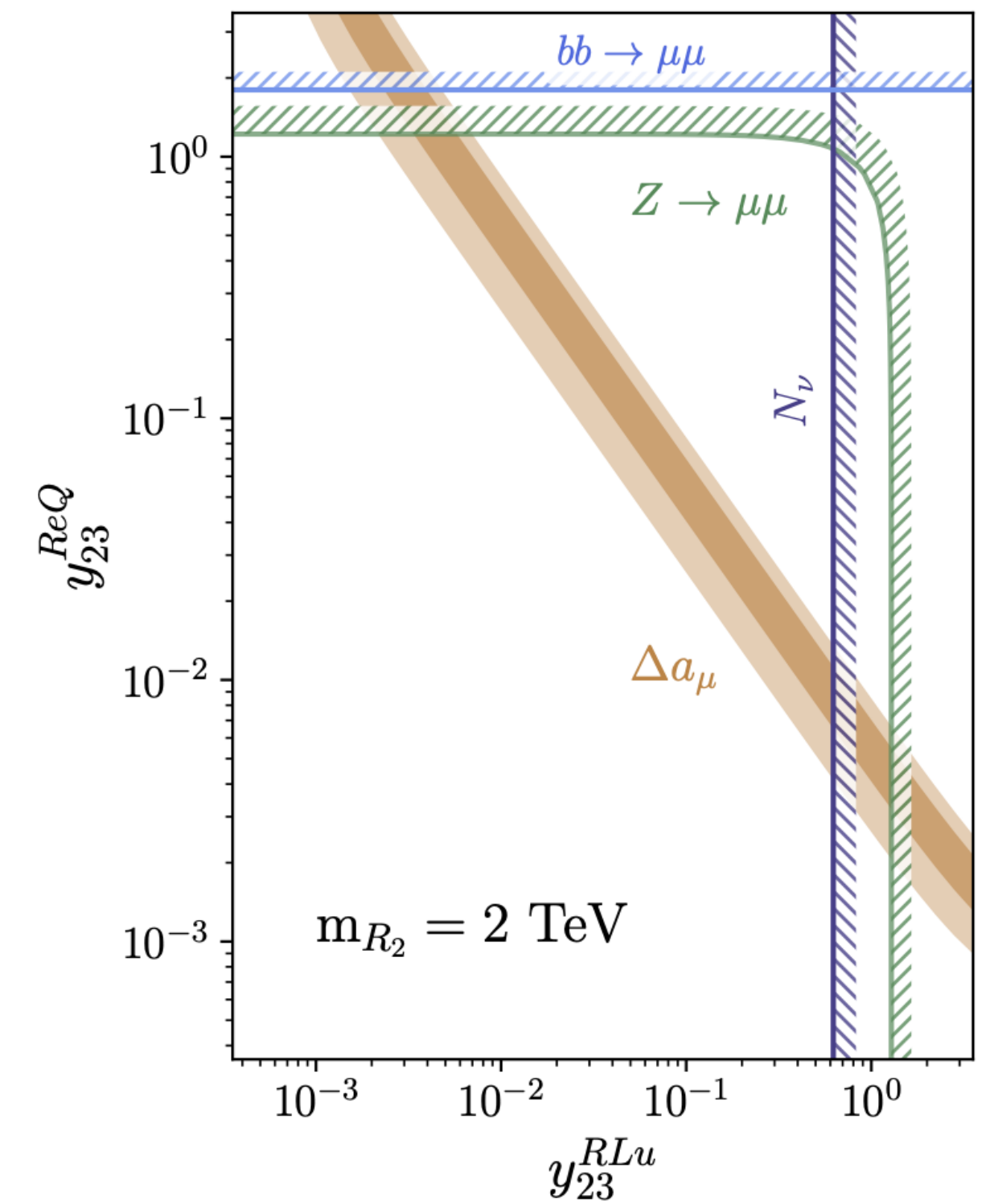
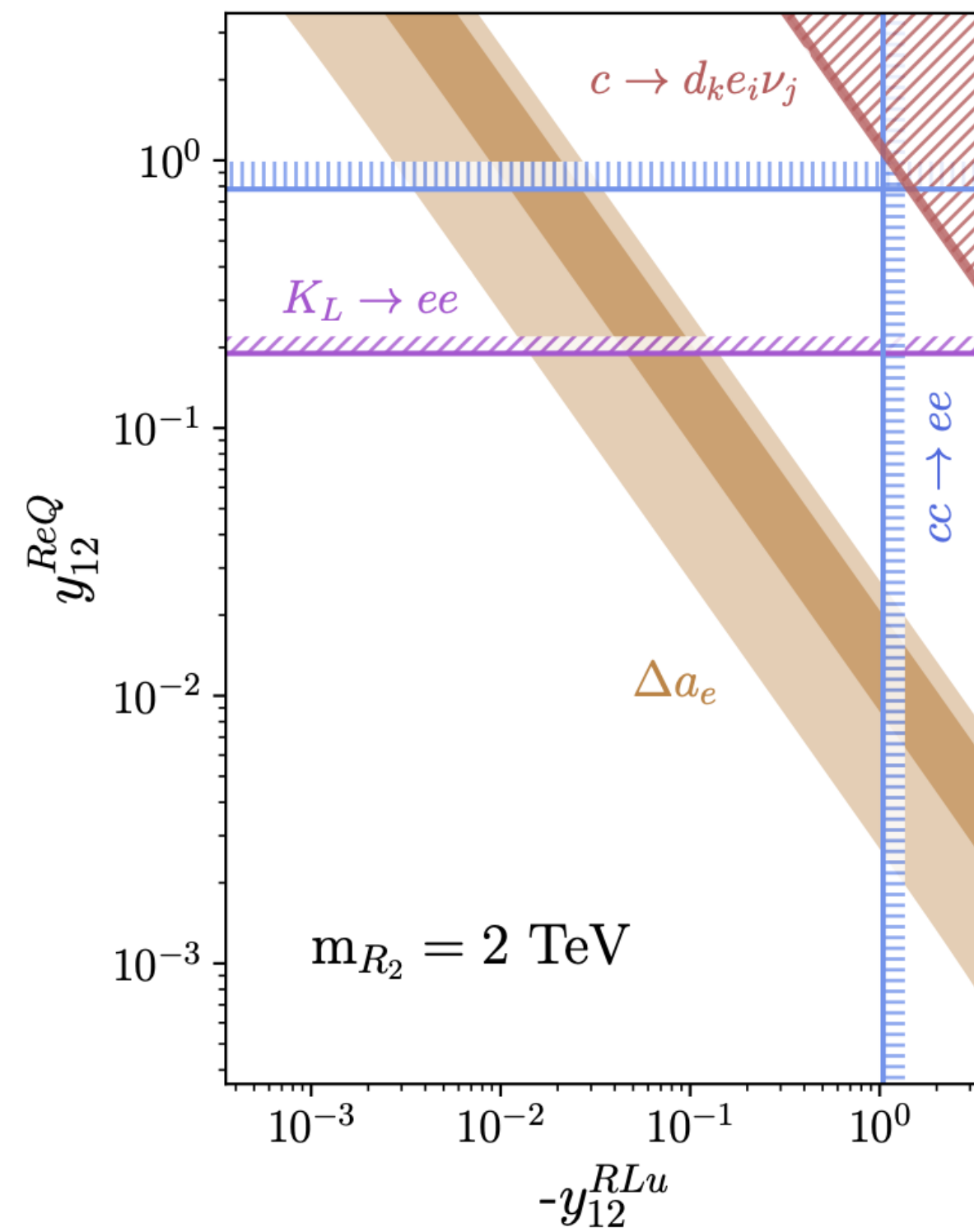


R₂ leptoquark: benchmark mass

Method 1



Method 2



Conclusions

Based on *Phys.Rev.D* 102 (2020) 7, 075037 • e-Print: 2002.12544 [hep-ph]

- We have argued the viability of single LQ simultaneous solutions to anomalies in $g-2$ of the electron and muon.
- Identified the two maximally chiral scalar LQ, capable of generating sign-dependent contributions to leptonic $g-2$ observables.
- LFV constraints can be avoided by allowing contribution to the electron $g-2$ from charm-containing loops, and muon $g-2$ from top-containing loops.
- Extending to complex couplings motivates consideration of EDMs as well as $g-2$ (manuscript in preparation)