

Signatures of Toponium Formation in the LHC Run 2 Data

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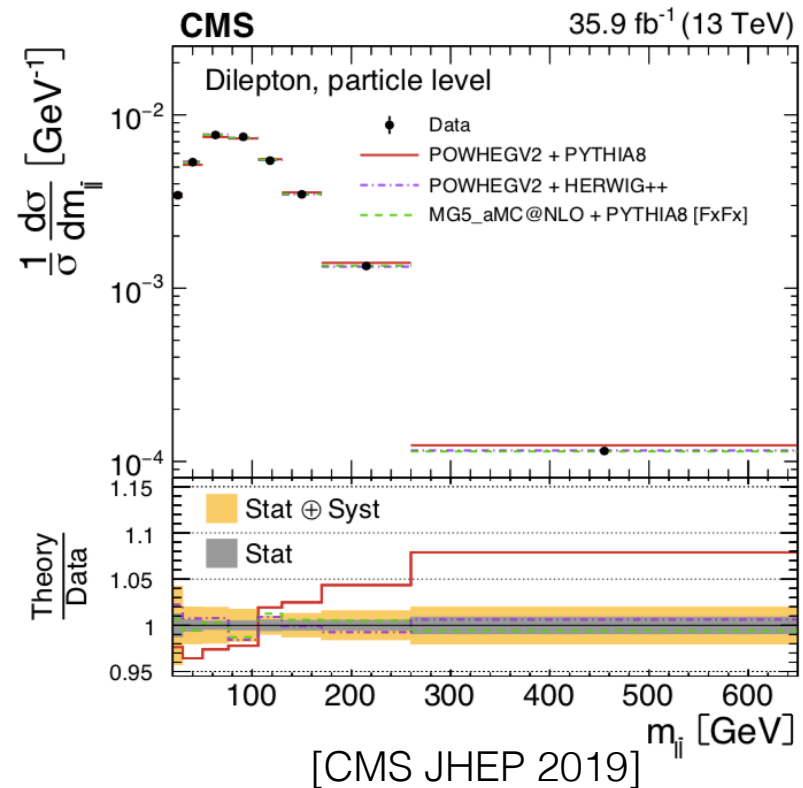
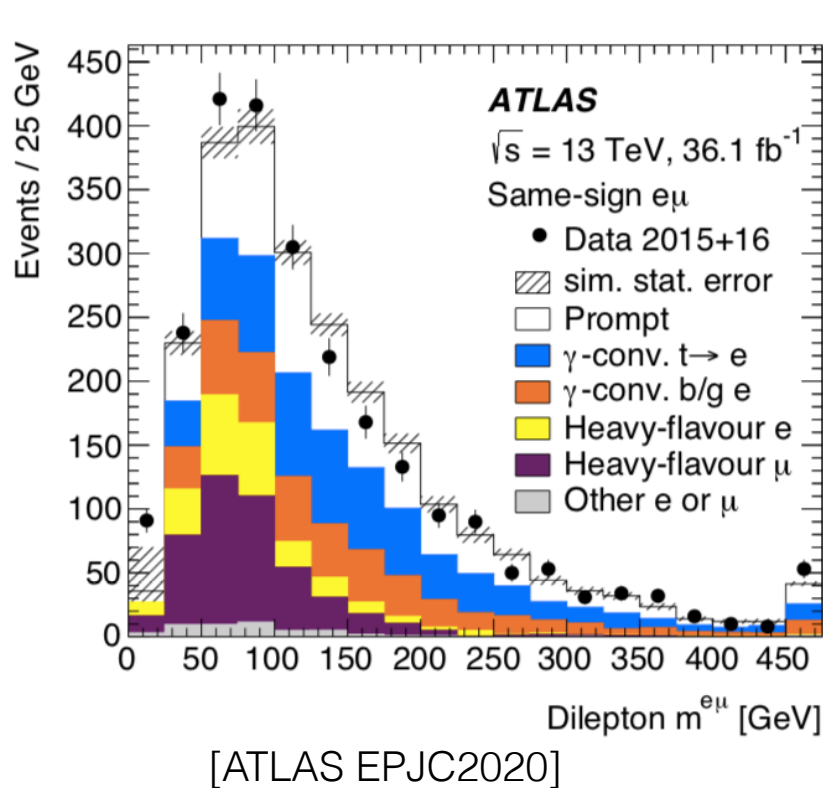
Phenomenology 2021 Symposium

Outline

- Toponium
- Production of Toponium at the LHC
- Reconstruction of t and \bar{t}
- Observables of toponium

Top pair production at the LHC

- LHC is a top factory. With 140/fb of integrated luminosity, we expect about 100 million $t\bar{t}$ events and 5 million are dileptonic ones.



- ✱ Both ATLAS and CMS observed excess of Data over the 'SM' prediction at low $m(l\bar{l})$ bins.
 - ★ This may suggest that $t\bar{t}$ production near the threshold is underestimated in the 'SM' prediction
 - ★ Could it be a signal of toponium formation below the $t\bar{t}$ threshold?

Heavy Quarkonium

	spin triplet (J=1)	spin singlet (J=0)
$c\bar{c}$ (charmonium)	$J/\psi, \psi(2S)$	η_c
$b\bar{b}$ (bottomonium)	$\Upsilon, \Upsilon(2S), \Upsilon(3S),$ $\Upsilon(4S), \Upsilon(5S)$	$\eta_b, \eta_b(2S)$
$t\bar{t}$ (toponium)	$\theta_t(3g, C=-)$	$\eta_t(2g, C=+)$
e^+e^- (positronium)	ortho-positronium ${}^3S_1 \rightarrow \Upsilon\Upsilon(C=-)$	para-positronium ${}^1S_0 \rightarrow \Upsilon\Upsilon(C=+)$

Toponium: **Color singlet** bound state of top&anti-top quark

J=1 Spin triplet θ_t

J=0 Spin singlet η_t

$$\vec{S} = \vec{S}_q + \vec{S}_{\bar{q}}$$

$$S_z = S_{q,z} + S_{\bar{q},z}$$

Symmetric (S, S_z)

anti-Symmetric

$2s+1=3$
spin triplet

$$\left\{ \begin{array}{l} \uparrow\uparrow \quad (1, 1) \\ \frac{\uparrow\downarrow + \downarrow\uparrow}{\sqrt{2}} \quad (1, 0) \\ \downarrow\downarrow \quad (1, -1) \end{array} \right.$$

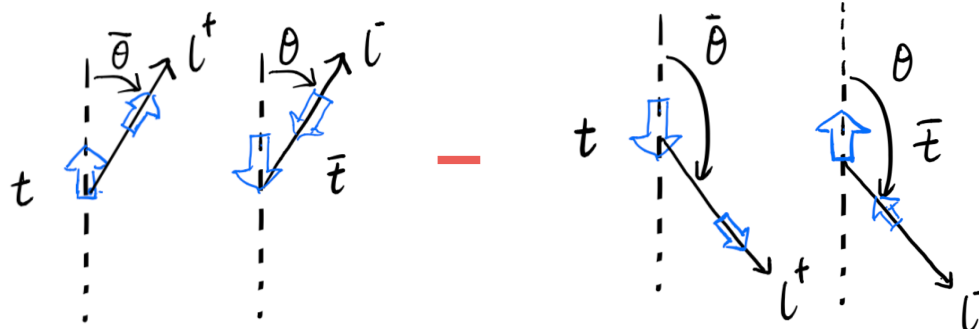
$$\left\{ \begin{array}{l} (S, S_z) \\ \frac{\uparrow\downarrow - \downarrow\uparrow}{\sqrt{2}} \quad (0, 0) \end{array} \right.$$

$2s+1=1$
spin singlet

t and t spin polarisation in $J^{PC}=0^{-+}$ toponium η_t

$$|\eta_t\rangle = \frac{|\uparrow\rangle_t |\downarrow\rangle_{\bar{t}} - |\downarrow\rangle_t |\uparrow\rangle_{\bar{t}}}{\sqrt{2}}$$

$\mathcal{M}: \eta_t$

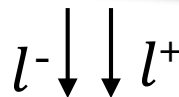


$|\mathcal{M}|^2:$

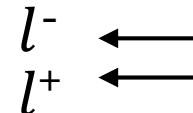
$$\begin{aligned} & \left(\cos \frac{\bar{\theta}}{2} \cos \frac{\theta}{2} \right)^2 \\ &= \frac{1 + \cos \bar{\theta}}{2} \frac{1 + \cos \theta}{2} \\ &= 1 \quad \text{when } \theta = \bar{\theta} = 0 \end{aligned}$$



$$\begin{aligned} & \left(\sin \frac{\bar{\theta}}{2} \sin \frac{\theta}{2} \right)^2 \\ &= \frac{1 - \cos \bar{\theta}}{2} \frac{1 - \cos \theta}{2} \\ &= 1 \quad \text{when } \theta = \bar{\theta} = \pi \end{aligned}$$

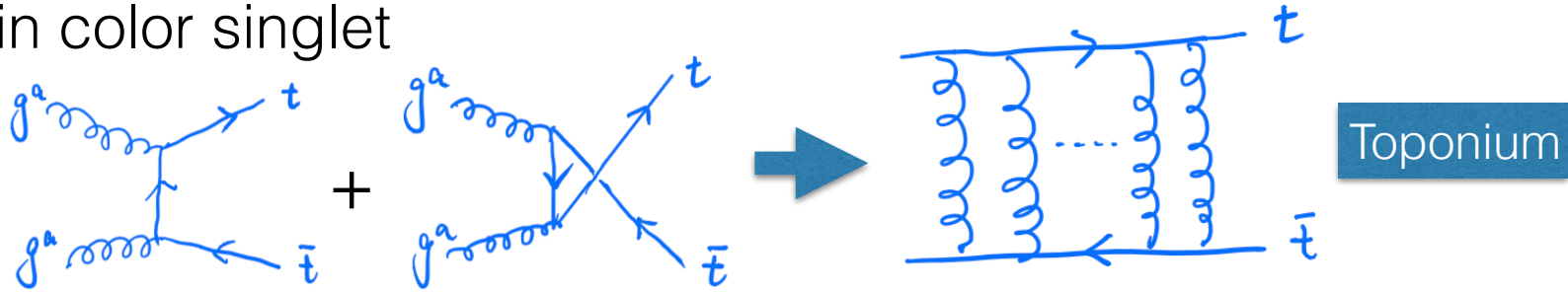


$$\begin{aligned} & + 2 \left(\cos \frac{\bar{\theta}}{2} \cos \frac{\theta}{2} \right) \left(\sin \frac{\bar{\theta}}{2} \sin \frac{\theta}{2} \right) \cos(\bar{\phi} - \phi) \\ &= \frac{1}{2} \sin \bar{\theta} \sin \theta \cos(\bar{\phi} - \phi) \\ &= \frac{1}{2} \quad \text{when } \theta = \bar{\theta} = \frac{\pi}{2}, \bar{\phi} - \phi = 0 \end{aligned}$$

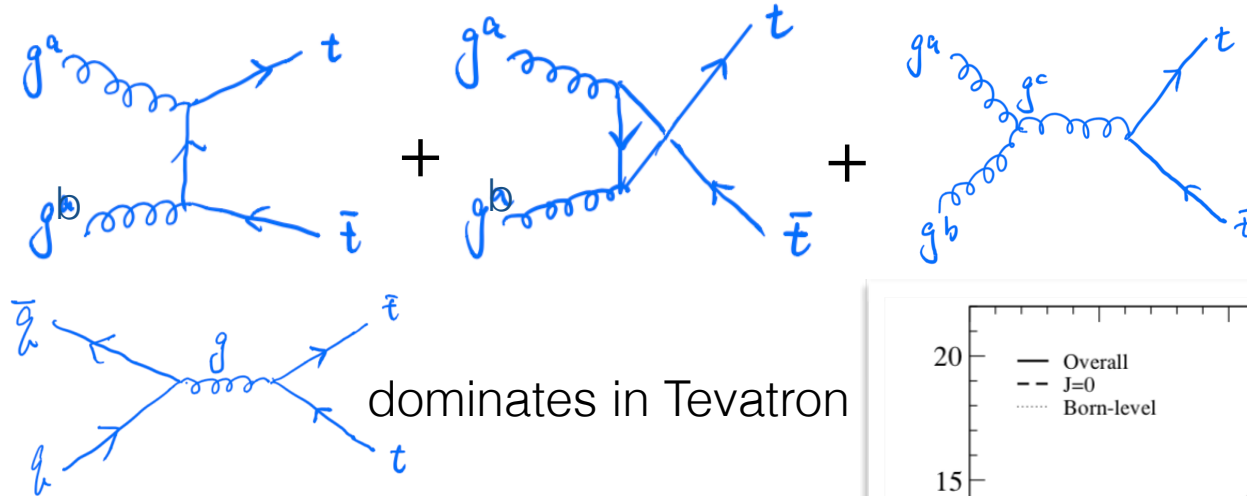


Toponium Production at hadron Colliders

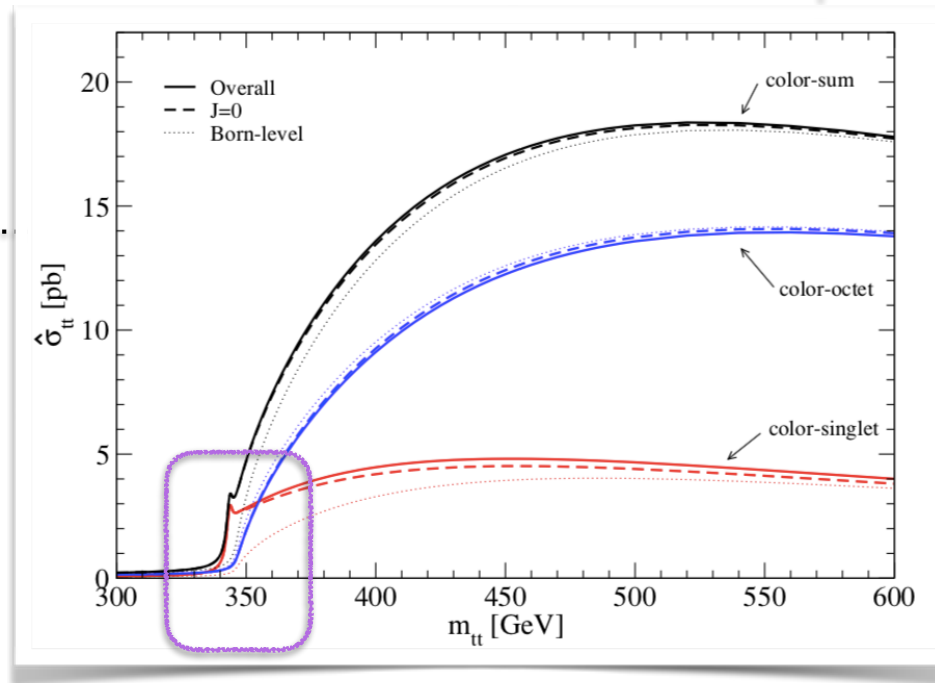
- $t\bar{t}$ in color singlet



- $t\bar{t}$ in color octet



- ❖ The colour-singlet dominates at the threshold
 - the gg -singlet channel dominates
- ❖ The $J=0$ state dominates
 - $L=S=0$
- ❖ The toponium η_t couples to quarks and gluons



Simplified model for η_t production and decay at the LHC

$$\mathcal{L}_{\eta_t} = \frac{1}{2} \partial_\mu \phi_{\eta_t} \partial^\mu \phi_{\eta_t} - \frac{1}{2} m_{\eta_t} \phi_{\eta_t}^2 - \frac{1}{4} g_{gg\eta_t} \phi_{\eta_t} \phi_{\eta_t} G_{\mu\nu}^a \tilde{G}^{a\mu\nu} - i g_{t\eta_t} \phi_{\eta_t} \bar{t} \gamma_5 t$$

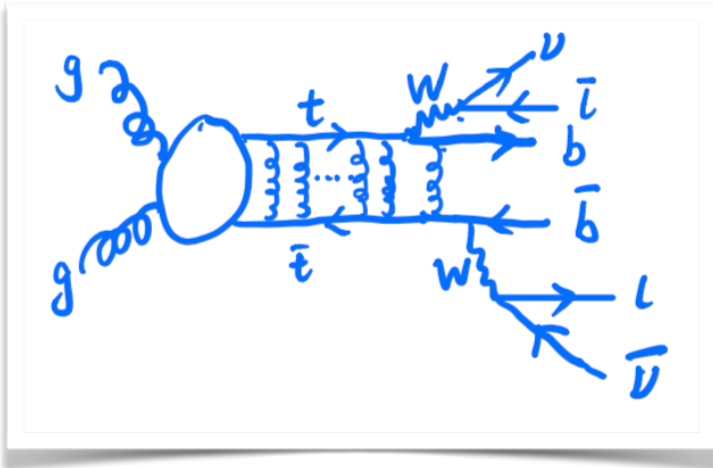
$$M_{\sigma, \bar{\sigma}} = M(\eta_t \rightarrow t(p, \sigma/2) \bar{t}(\bar{p}, \bar{\sigma}/2))$$

$$\rho_{\sigma\bar{\sigma}; \sigma'\bar{\sigma}'}^{\eta_t} = \frac{M_{\sigma\bar{\sigma}} M_{\sigma'\bar{\sigma}'}^*}{\sum_{\sigma\bar{\sigma}} |M_{\sigma\bar{\sigma}}|^2}$$

\sqrt{s}	$\sigma(\eta_t)$ [pb]	$\sigma(t\bar{t})$ [pb]	Ratio
7 TeV	1.55	172	0.0090
8 TeV	2.19	246	0.0089
13 TeV	6.43	810	0.0079
14 TeV	7.54	954	0.0079

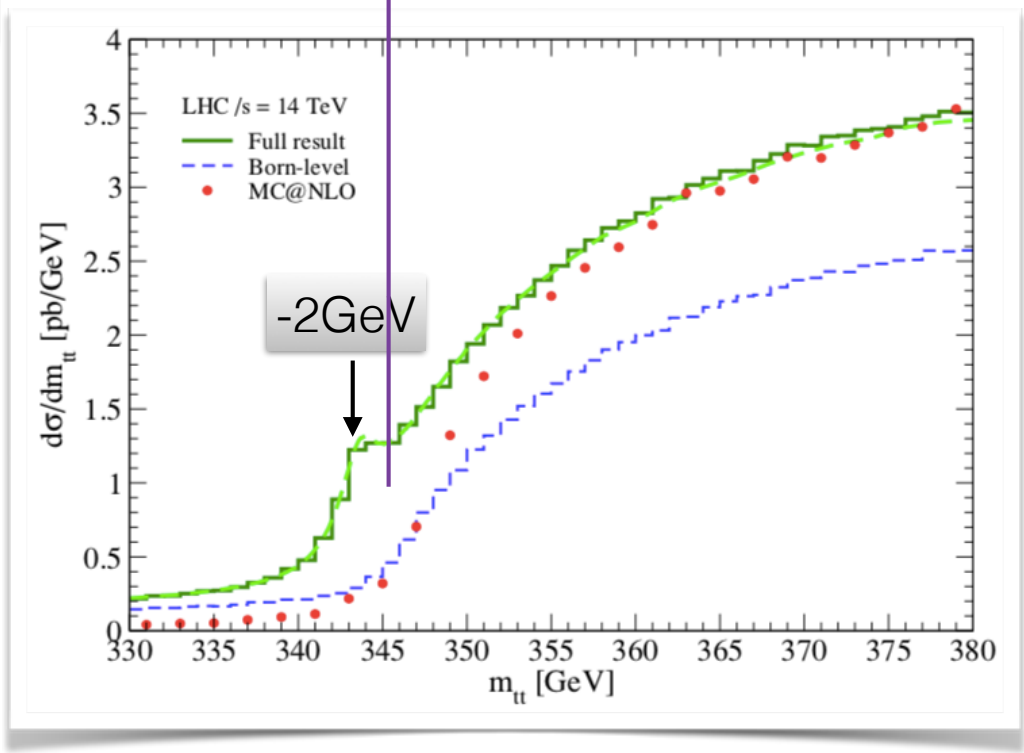
- * Cross section of η_t at 7 and 14 TeV are from [Y. Sumino and H. Yokoya, JHEP2010]
- * Cross section of $t\bar{t}$ from [M Czakon, P.Fiedler and A.Mitov PRL2013, M.Czakon, A. Ferrogli, D.Heymes, A.Mitov, B.Pecjak, X.Wang, and L.Yang JHEP 2018]

Near Threshold



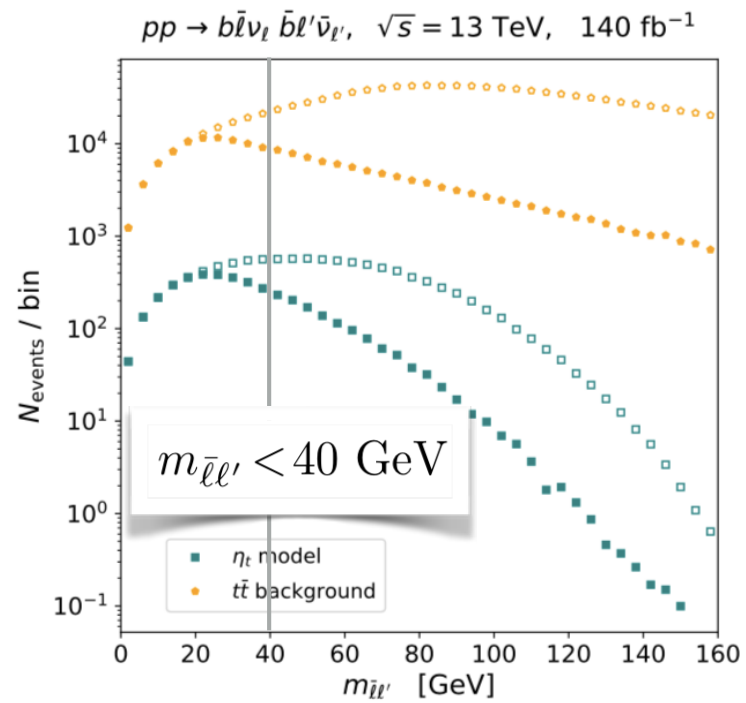
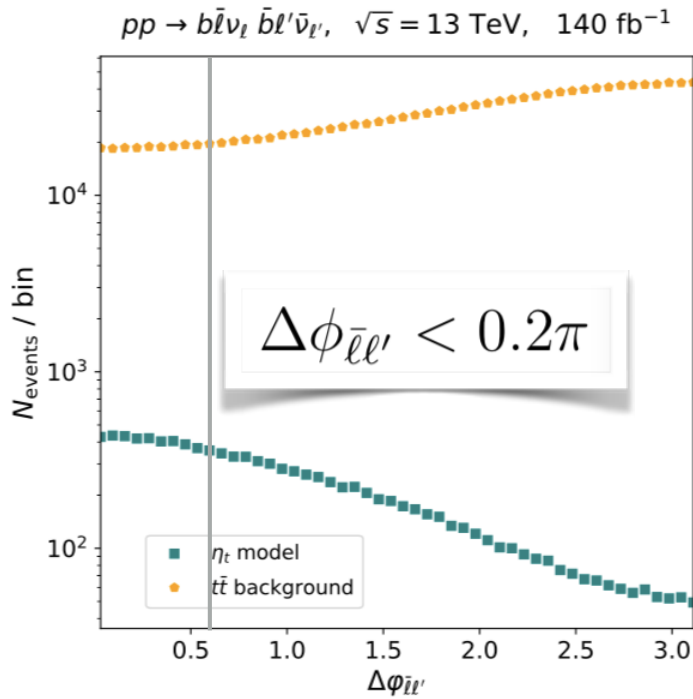
$$|M|^2 \rightarrow |M|^2 \left| \frac{G(E; p^*)}{G_0(E; p^*)} \right|^2$$

* Multiple gluon exchange effects are evaluated by using Green's function of the non-relativistic Hamiltonian with Coulomb potential. [V.S.Fadin and V.A.Khoze (JETP1987) (Sov. J. Nucl. Phys1988)]



[Y.Sumino and H.Yokoya, JHEP2010]

Distributions



Cut	$t\bar{t}$	Toponium	Ratio
Initial	113,000,000	900,000	0.0079
Di-lepton	5,160,000	41,000	0.0079
$p_T, \eta , \Delta R$	1,450,000	10,300	0.0071
$\Delta\phi_{\bar{\ell}\ell'}$	189,000	4,060	0.021
$m_{\bar{\ell}\ell'}$	82,000	2,760	0.033
$m_T(\bar{\ell}\ell' b\bar{b}; \nu_e \bar{\nu}_{e'})$	43,300	2,460	0.057
$t\bar{t}$ kinematical fit	21,700	1,420	0.066

$\sqrt{s} = 13 \text{ TeV}$

140 fb^{-1}

$m_t = 173.3 \text{ GeV}$

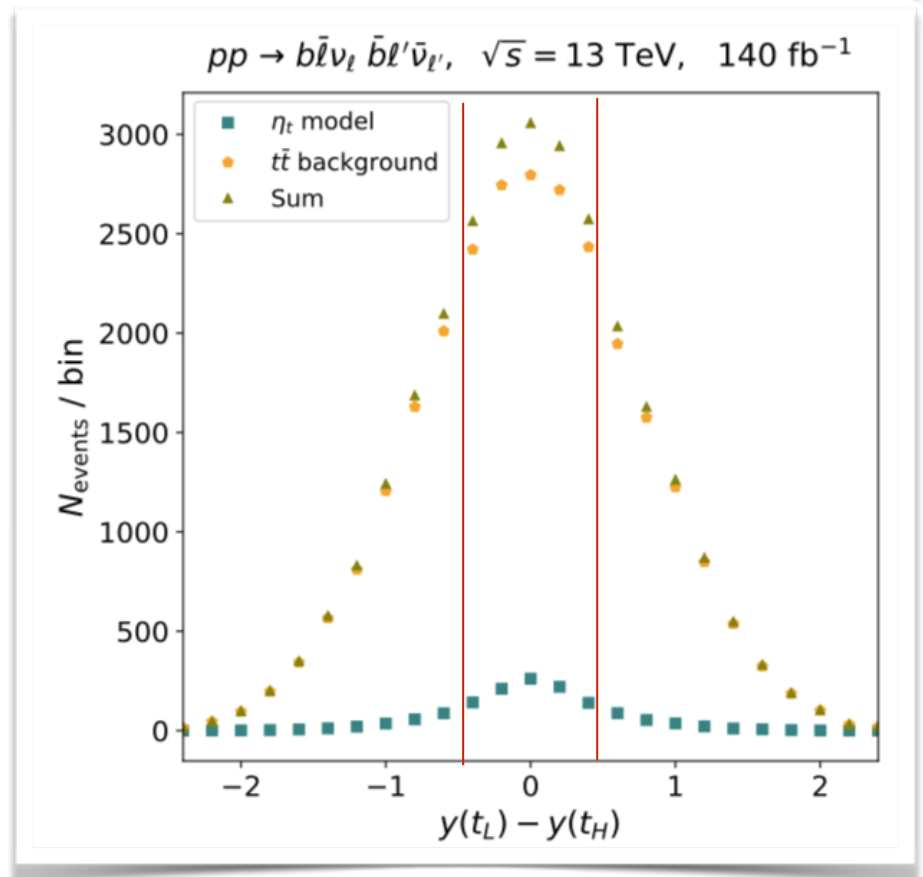
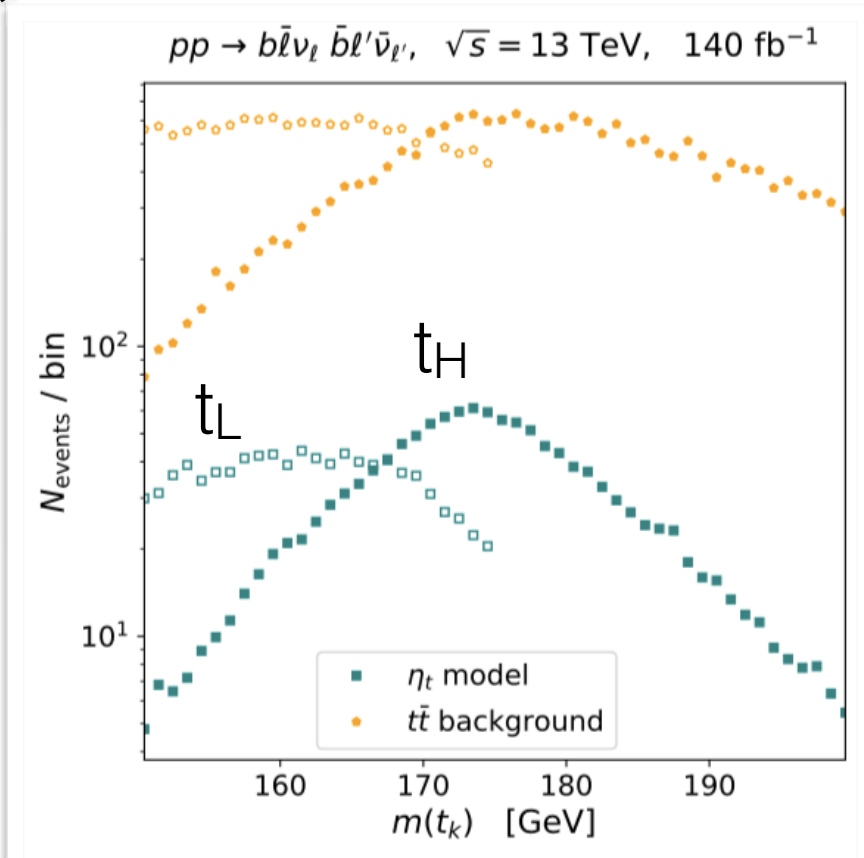
$p_T > 25 \text{ GeV}$

$|\eta| < 2.5$

$\Delta R > 0.4$

$m_T(\bar{\ell}\ell' b\bar{b}; \nu_e \bar{\nu}_{e'}) < 320 \text{ GeV}$

kinematical reconstruction of t and \bar{t}



t and \bar{t} can be reconstructed since the t and \bar{t} momentum p in the $t\bar{t}$ rest frame is small ($\lesssim 20 \text{ GeV}$). By assuming $\vec{p}_t^\top = \vec{p}_{\bar{t}}^\top$ for the selected events, we can reconstruct t and \bar{t} .

$|y_t - y_{\bar{t}}|$ should also be small for the toponium events.

- Toponium contribution can enhance the cross section by 10% near $|\Delta y| = 0$.