

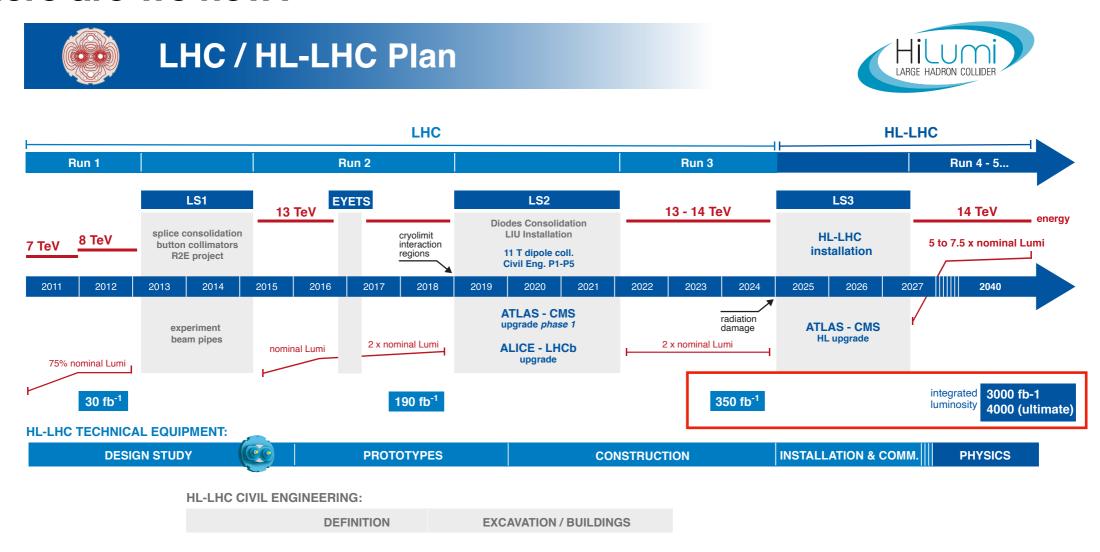
# A $W^{\pm}$ polarization analyzer from Deep Neural Networks

Taegyun Kim
Research Advisor: Dr. Adam Martin
Department of Physics, University of Notre Dame

arXiv:2102.05124

## Introduction

#### Where are we now?



https://project-hl-lhc-industry.web.cern.ch/content/project-schedule

- Entering HL-LHC: bring out small number of event signals
- Precision testing to find potential BSM signatures
- This research is about building a tool and show possibility

## **Theoretical Motivation**

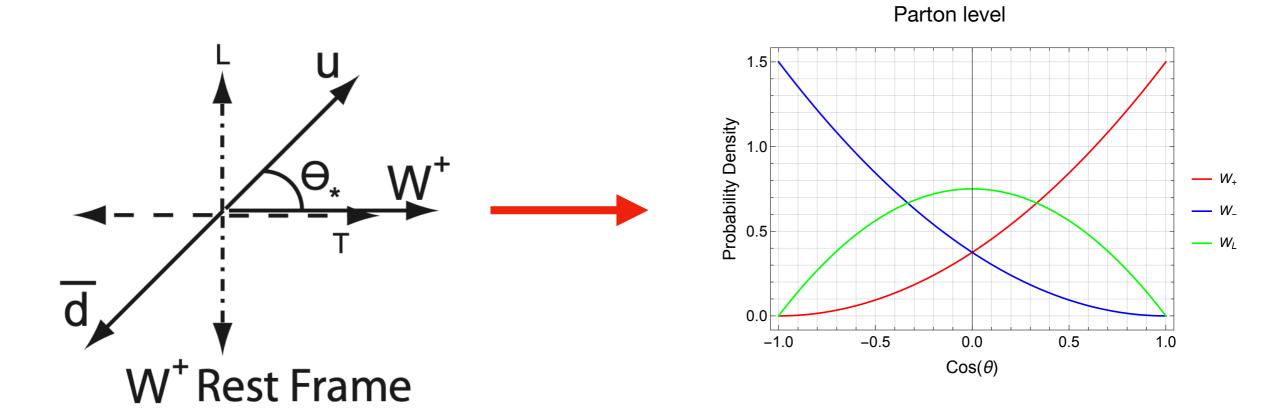
#### Massive vector boson final states

$$pp \to W^{\pm}W^{\mp}$$
 
$$pp \to W^{\pm}Z$$
 
$$pp \to ZZ$$

- Indirect approach of checking SM: polarization searches
  - Longitudinal vs. Transverse
- SM can predict polarization fraction
- Longitudinal polarization is sensitive to EWSB
- Some SMEFT operators can affect longitudinal fraction of a process

## W polarization

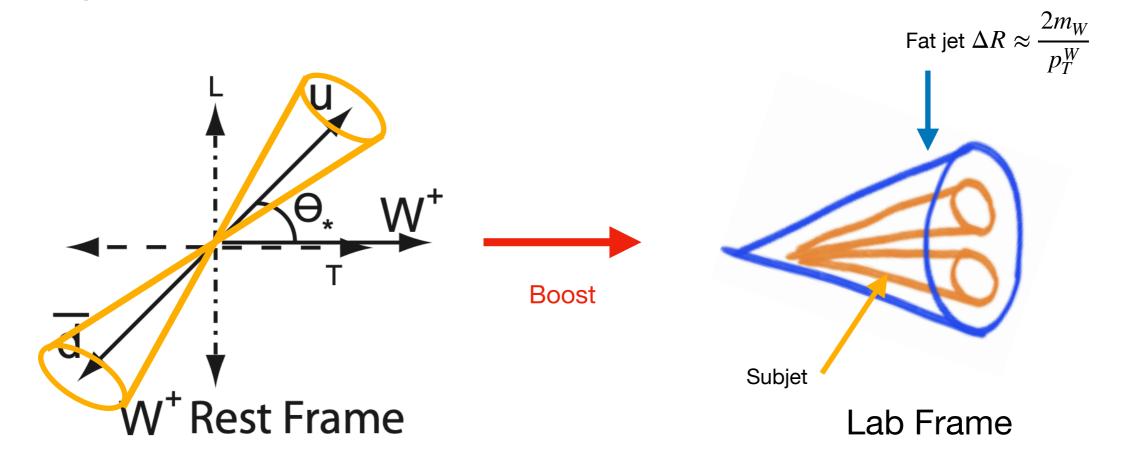
#### Decay of W



- There is a limitation in leptonically decaying W
- ullet Since W only interacts to the left handed particles, each polarization has distinct angular distribution
- Due to the deviation, it is possible to measure polarization fraction for diboson final states
- Large overlap in parton level distribution may suppress even by event tagging

## **Boosted** W Jet

## Decay of W



- Quark becomes QCD jet
- Due to the boost, collimation of the jet deduces the angular distribution signature
- Possible subjet signature
- After boost  $\theta^* \to \text{opening angle (sensitive to pT)}$
- At extreme high  $p_T^{W}$ , subjet signature can disappear

## **Machine Learning Motivation**

## **Machine Learning in HEP**

- The current most frequently used machine learning algorithm: Boosted Decision Tree (BDT) and Neural Network (NN)
- Major usage
  - Classification : PID, event identification

Our interest

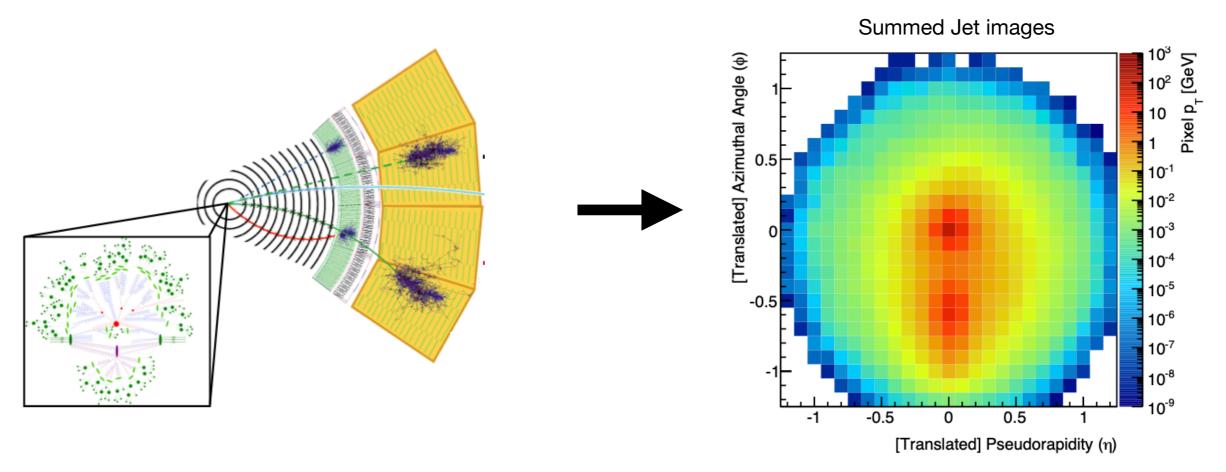
- Regression : predict particle energy
- Recent researches on: quark vs. gluon, QCD vs. top, W vs. QCD



ML(NN) technique to distinguish hadronic W's polarization to test on  $W^\pm Z$  final state

# Jet as an Image from Collider

## Adjust for HEP using jet image

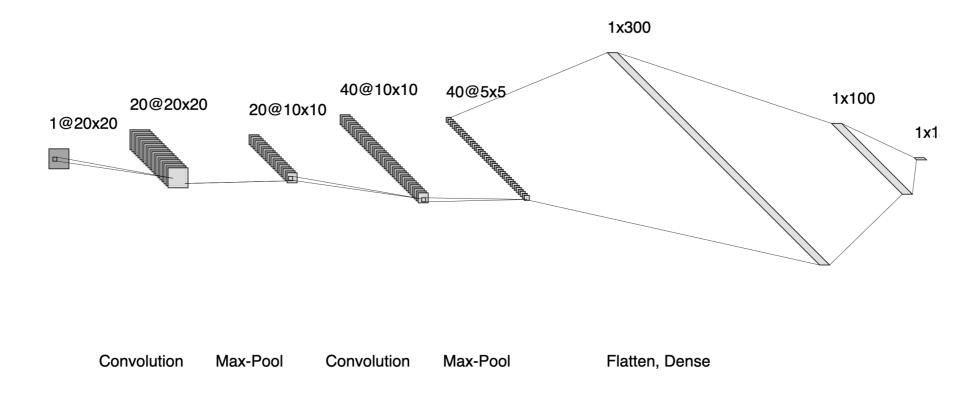


L. de Oliveira, M. Kagan, L. Mackey, B. Nachman, and A. Schwartzman, "Jet-images – deep learning edition,"

- In collider, images are created from outgoing particles
- Particles are plotted on pixelized  $\eta-\phi$  plane and their color is determined from  $p_T$

## **Convolutional Neural Network (CNN)**

## Image recognition

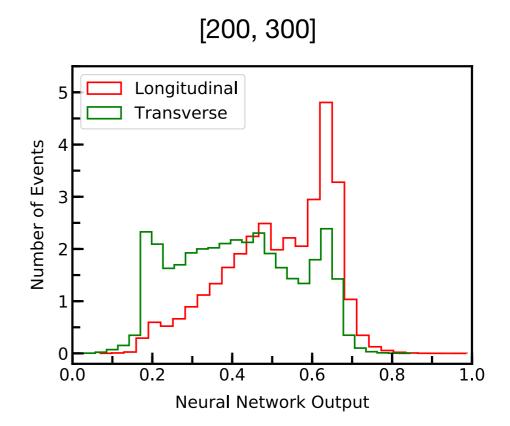


- Ordinary CNN structure : Convolution Flatten Dense
- The network is trained with simulated events (MadGraph + Pythia + Delphes) of boosted longitudinal and transverse W's respectively for tagging purposes
- Depending on  $p_T^W$ , images are separated into 2 bins: [200,300] and [400,500] since for fat jet,  $\Delta R \approx \frac{2m_W}{r^W}$

# **Testing on SM**

## Longitudinal fraction ( $f_L$ )

- Checking distribution can tell us how good the separation between two polarization
- Inhibits potential event by event tagging because of large overlap



- In order to apply for testing, we measure  $f_L$  of randomly selected events
- Test on WZ final state

SM

$p_T$ range	$\sigma(pp \to W^{\pm}(jj)Z(\ell\ell))$ (fb)	truth $\sigma_L/\sigma_{ m tot}$	predicted $f_L$
$200\mathrm{GeV} \leq p_T \leq 300\mathrm{GeV}$	6.67	0.265	$0.259 \pm 0.013$
$400\mathrm{GeV} \leq p_T \leq 500\mathrm{GeV}$	0.35	0.304	$0.300 \pm 0.033$

## **SMEFT in Diboson Final States**

#### **SMEFT** intro

$$\mathscr{L}_{SMEFT} = \mathscr{L}_{SM} + \sum_{D>4}^{\inf} \frac{1}{\Lambda^{D-4}} c_j^{(D)} \mathcal{O}_j^{(D)}$$

- SMEFT extends the SM Lagrangian by gauge invariant higher dim (D>4) operators
- ullet We will investigate boosted W cases

#### Relevant operators (SILH) for diboson final states

$$\mathcal{O}_{W} = \frac{ig}{2} \left( H^{\dagger} \sigma^{a} \overleftrightarrow{D}^{\mu} H \right) D^{\nu} W_{\mu\nu}^{a}$$

$$\mathcal{O}_{B} = \left( H^{\dagger} \sigma^{a} \overrightarrow{D}^{\mu} H \right) \partial^{\nu} B_{\mu\nu}$$

Longitudinal

$$\mathcal{O}_{2W} = -\frac{1}{2}D^{\mu}W^{a}_{\mu\nu}D_{\rho}W^{a\rho\nu}$$

$$\mathcal{O}_{3W} = \frac{1}{3!} g \epsilon_{abc} W^{a\nu}_{\mu} W^{b}_{\nu\rho} W^{c\rho\mu}$$

**Transverse** 

 $\mathcal{O}_{HW} = ig \left(D^{\mu}H\right)^{\dagger} \sigma^{a} \left(D^{\nu}H\right) W_{\mu\nu}^{a}$ 

$$\mathcal{O}_{HW} = ig' (D^{\mu}H)^{\dagger} (D^{\nu}H) B_{\mu\nu}$$

Da Liu, Lian-Tao Wang [arXiv: 1804.08688v1]

## **Possible Scenarios with SMEFT**

SM

$p_T$ range	$\sigma(pp \to W^{\pm}(jj)Z(\ell\ell))$ (fb)	truth $\sigma_L/\sigma_{ m tot}$	predicted $f_L$
$200\text{GeV} \leq p_T \leq 300\text{GeV}$	6.67	0.265	$0.259 \pm 0.013$
$400\mathrm{GeV} \leq p_T \leq 500\mathrm{GeV}$	0.35	0.304	$0.300 \pm 0.033$

## 1. Shift longitudinal fraction with cross section shift

	$p_T$ range	$\sigma(pp \to W^{\pm}Z)$ (fb)	truth $\sigma_L/\sigma_{tot}$	predicted $f_L$
0	$200\mathrm{GeV} \le p_T \le 300\mathrm{GeV}$	6.93	0.311	$0.297 \pm 0.010$
$O_W$	$400\mathrm{GeV} \le p_T \le 500\mathrm{GeV}$	0.42	0.439	$0.391 \pm 0.033$
0	$200\mathrm{GeV} \le p_T \le 300\mathrm{GeV}$	6.58	0.258	$0.254 \pm 0.011$
$O_{3W}$	$400\mathrm{GeV} \le p_T \le 500\mathrm{GeV}$	0.50	0.198	$0.181 \pm 0.043$

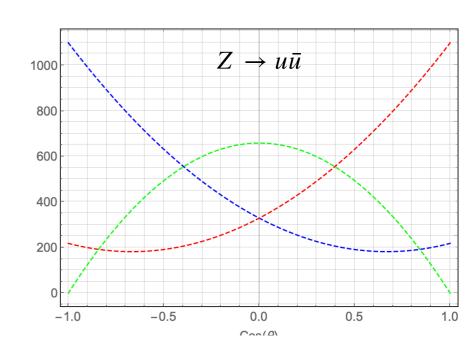
## 2. Shift longitudinal fraction without cross section shift

$$SM + \mathcal{O}_W + \mathcal{O}_{3W}$$

$p_T$ range	$\sigma(pp \to W^{\pm}Z)$ (fb)	truth $\sigma_L/\sigma_{tot}$	predicted $f_L$
$200 \text{ GeV} \le p_T \le 300 \text{ GeV}$	6.68	0.202	$0.207\pm0.011$
$400 \text{ GeV} \le p_T \le 400 \text{ GeV}$	0.34	0.285	$0.282 \pm 0.044$

## Conclusion/Discussion

- Simple CNN can be used to tag  $W^\pm$  polarization though event by event tagging is suppressed
- Ensemble analysis using network's output average values can help to predict  $f_L$
- Network prediction can catch small  $f_L$  deviations originated from dim 6 operators
- If cross section changes, polarization measurement can clear out degeneracies between EFT operators
- Possible applicability on Z jets
- Potential limits
  - $W^{\pm}$  vs. Z vs. QCD is not perfectly separable
  - Cuts that can cause polarization interference



# Thank you

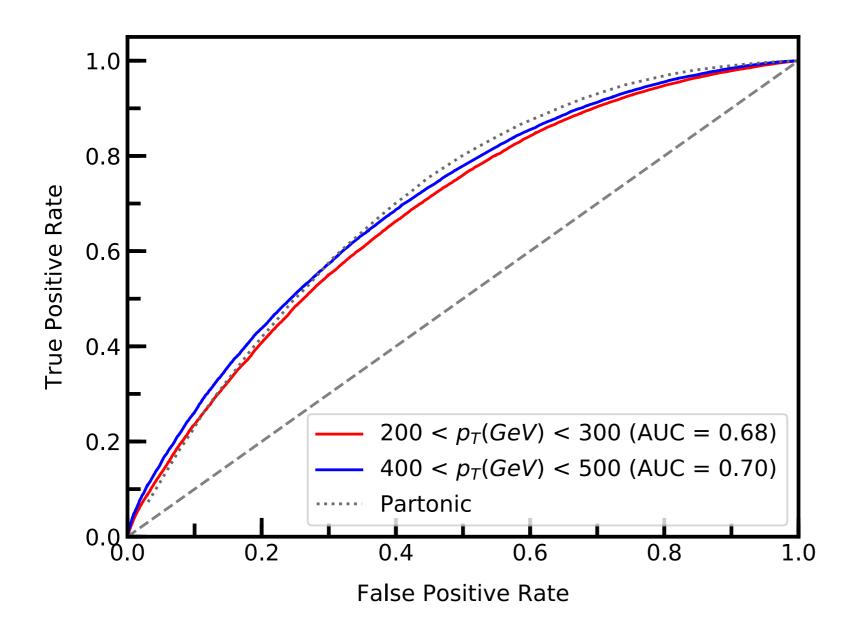
## References

- (1) Aaboud, M., Aad, G., Abbott, B., Abdinov, O. et al. (2019). Measurement of  $W^{\pm}Z$  production cross sections and gauge boson polarization in pp collisions at  $\sqrt{s}=13$  TeV with the ATLAS detector. The European Physical Journal C, 79(6).
- (2) D. Liu and L.-T. Wang, "Prospects for precision measurement of diboson processes in the semileptonic decay channel in future LHC runs," Physical Review D 99 (Mar, 2019). <a href="http://dx.doi.org/10.1103/PhysRevD.99.055001">http://dx.doi.org/10.1103/PhysRevD.99.055001</a>.
- (3) Carleo, Giuseppe et al. "Machine learning and the physical sciences". Reviews of Modern Physics 91. 4(2019).
- (4) Stirling, W. J. et al. "Electroweak gauge boson polarisation at the LHC". Journal of High Energy Physics 2012. 7(2012).
- (5) "scikit-hep/pyjet: 1.6.0 (version 1.6.0),"

# Backup slides

# **Training Quality**

#### **Distribution check**

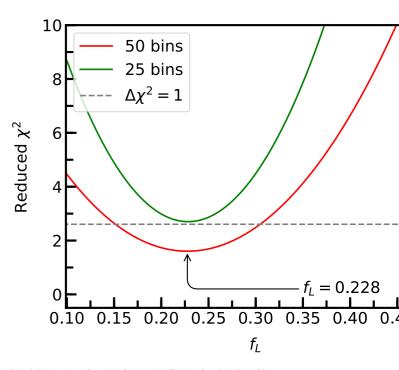


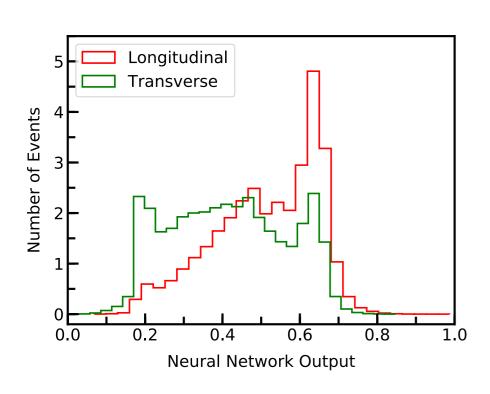
- Checking distribution can tell us how good the separation between Logi and trans is.
- Inhibits potential event by event tagging since accuracy is ~ 60%
- Ensemble distribution checking to find longitudinal fraction  $(f_I)$

# **Simpler Method**

## Network output average method

- Template fitting method depends on finding "sweet spot" for  $f_L$ 
  - number of bins
  - find minimum  $\chi^2(f_L)$
- Simplify by treating output distribution as probability distribution





$$\int x dx \left( D_u(x) = f_L D_L(x) + (1 - f_L) D_T(x) \right)$$

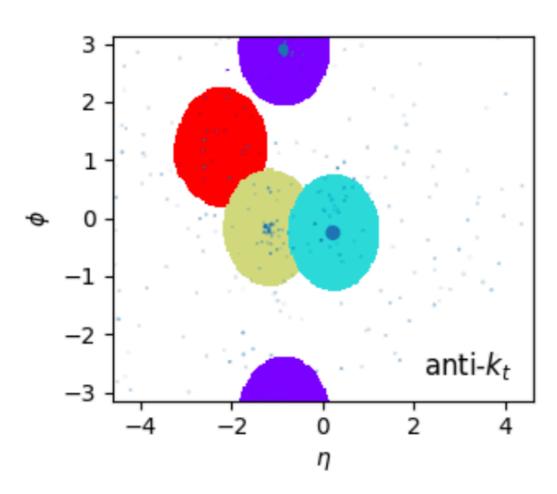
$$\left\langle x_u \right\rangle = f_L \left\langle x_L \right\rangle + (1 - f_L) \left\langle x_T \right\rangle$$

$$f_L = \frac{\left\langle x_u \right\rangle - \left\langle x_T \right\rangle}{\left\langle x_L \right\rangle - \left\langle x_T \right\rangle}$$

Confirmed that both yield the same result

# **Jet Images**

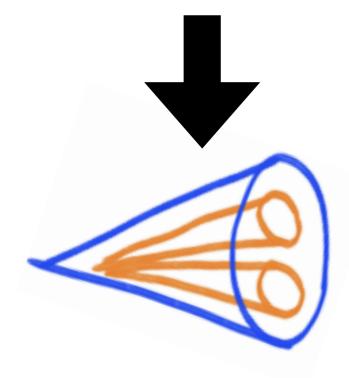
## **Network friendly form**



https://github.com/scikit-hep/pyjet

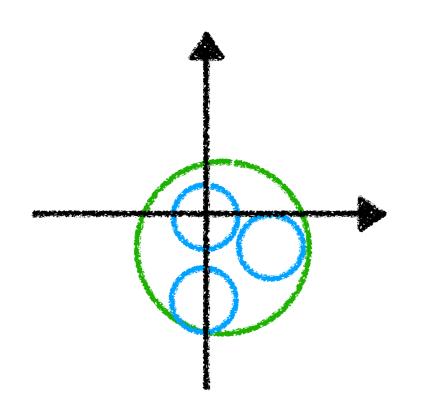
#### Bring out subjet signature

- 1. Identify jet with clustering algorithm
- 2. Check if clustered jet lies under  $p_T$  bin range
- 3. Select jets with correct angular position
- 4. Recluster to identify subjets



# **Jet Images**

## **Network friendly form**

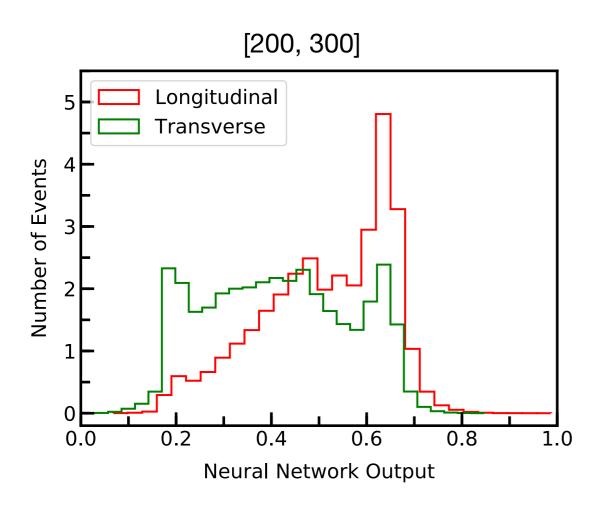


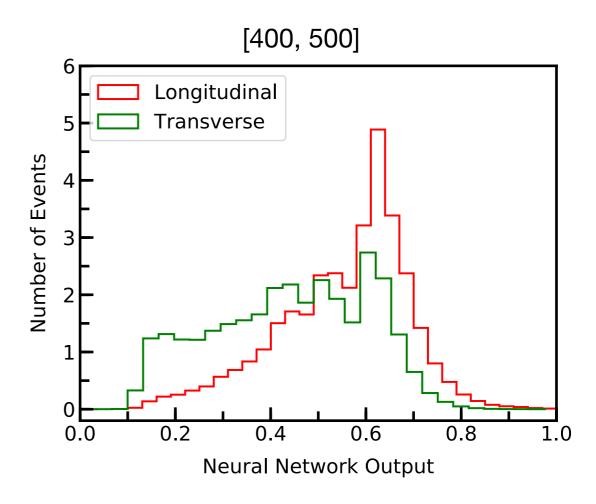
Reduce image discrepancies by putting into consistent orientation

- 1. Translate to centralize the highest  $p_T$  subjet
- 2. Rotate so that the second highest  $p_T$  subjet below the highest
- 3. Reflect
- 4. Pixelize
- 5. Normalize

# **Training Quality**

#### **Distribution check**





- Checking distribution can tell us how good the separation between two polarization
- Inhibits potential event by event tagging because of large overlap
  - Putting decision threshold would contain large contamination
- Ensemble distribution checking to find longitudinal fraction  $(f_I)$

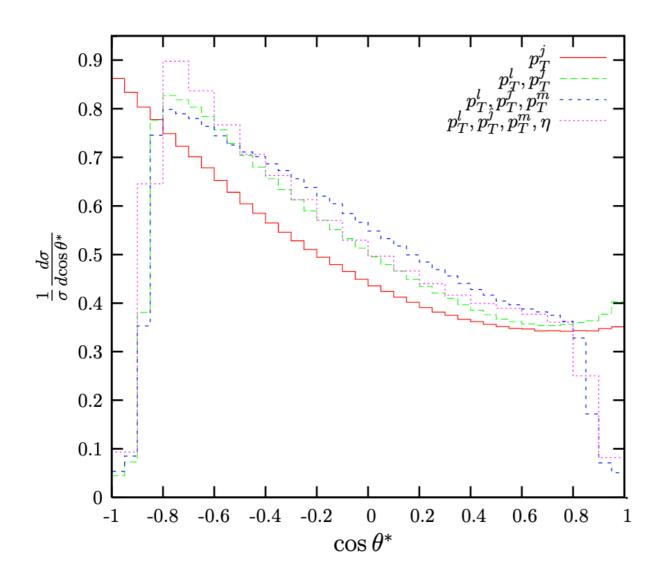
## **Kinematic Cut Effect**

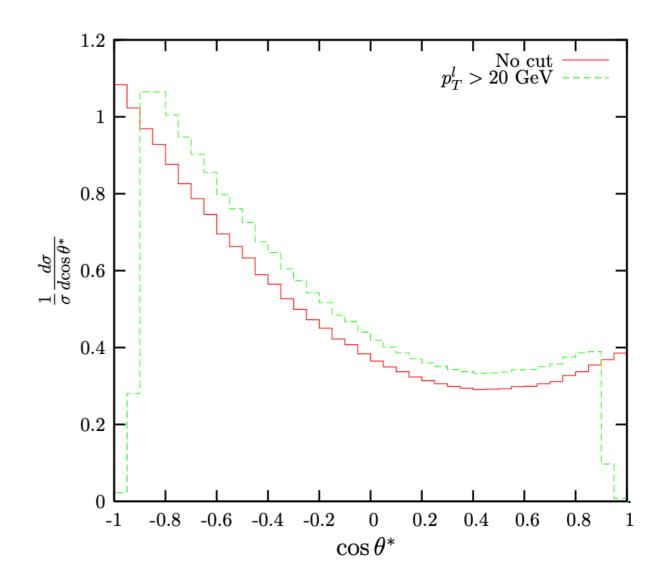
W rest frame 
$$\frac{1}{\sigma}\frac{d\sigma}{d\mathrm{cos}\theta^*} = \frac{3}{8}(1-\mathrm{cos}\theta^*)^2f_L + \frac{3}{8}(1+\mathrm{cos}\theta^*)^2f_R + \frac{3}{4}\mathrm{sin}^2\theta^*f_0,$$

$$\begin{split} \frac{1}{\sigma} \frac{d\sigma}{d \mathrm{cos} \theta^* d \phi^*} &= \frac{3}{16\pi} [(1 + \mathrm{cos}^2 \theta^*) + A_0 \frac{1}{2} (1 - 3 \mathrm{cos}^2 \theta^*) + A_1 \mathrm{sin} 2\theta^* \mathrm{cos} \phi^* \\ &+ A_2 \frac{1}{2} \mathrm{sin}^2 \theta^* \mathrm{cos} 2\phi^* + A_3 \mathrm{sin} \theta^* \mathrm{cos} \phi^* + A_4 \mathrm{cos} \theta^*], \end{split}$$

• Integrating over  $\phi^*$  will give the same result but kinematic cut can change

## **Kinematic Cut Effect**





## **Kinematic Cut Effect**

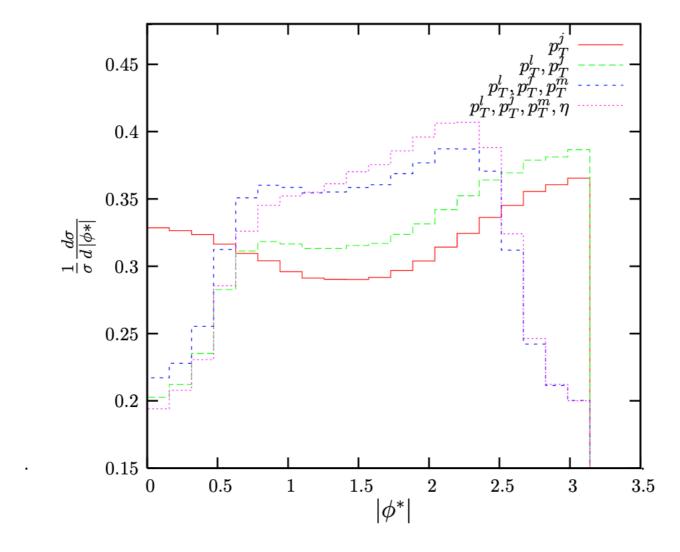


Figure 9: Normalised azimuthal angle distributions for a set of different selection cuts imposed on final-state leptons and jets for  $W^+ + 1$  jet production at 7 TeV.

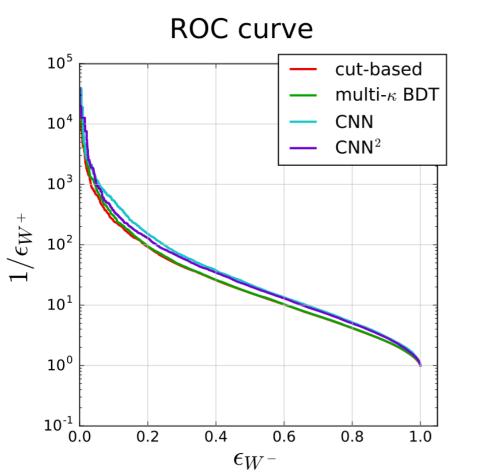
## W vs. Z

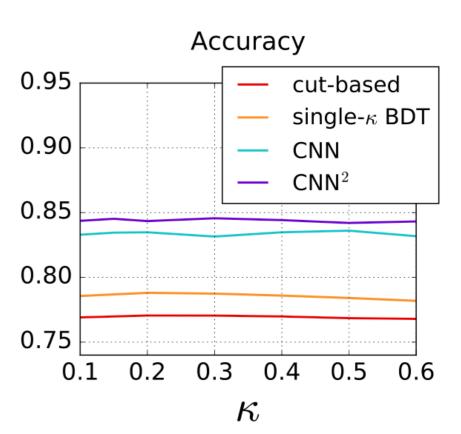
## Jet charge

PhysRevD.101.053001

Additional observable : 
$$\mathcal{Q}_{\kappa} = \frac{1}{(p_{T,J})^{\kappa}} \sum_{i \in J} q_i \times (p_T^i)^{\kappa}$$

- Depending on  $\kappa$ , separation may change.
  - Need to find optimal value of  $\kappa$
- Input is pT and Q\_K depth=2 image





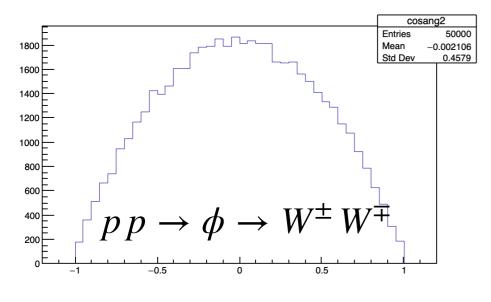
# **Preparing Samples**

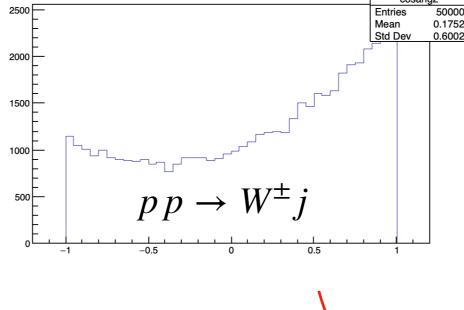
## **Training / Validation**

Longitudinal 
$$p\,p o \phi o W^\pm\,W^\mp$$
 Created with heavy Higgs

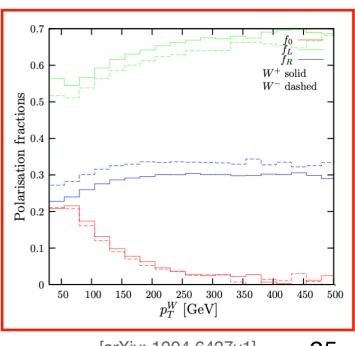
Transverse 
$$pp o W^{\pm}j$$

- MadGraph + Pythia + Delphes
- We separate into  $p_T$  bins of W jet: [200,300] and [400,500]
- To make sure the quality of sample, we plotted W decay in parton level





Why asymmetric?

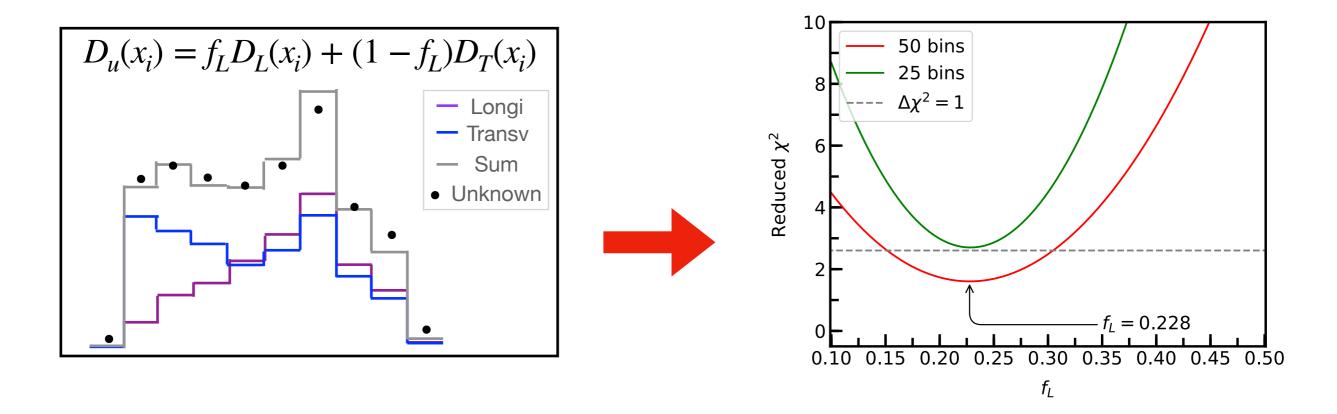


[arXiv: 1204.6427v1]

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# **Analysis**

#### **Template fit method**



- Consider each pure polarization histogram as "template" that can be applied to the unknown sample
- Fit quality is determined by  $\chi^2$  distance test

$$\chi^{2}(f_{L}) = \sum_{i=1}^{B} \frac{(O_{i} - N_{s}(f_{L}L_{i} + (1 - f_{L})T_{i}))^{2}}{N_{s}(f_{L}L_{i} + (1 - f_{L})T_{i})}$$

# **Test on Unknown Samples**

## SM testing using average method

$$pp \to W^{\pm}Z$$

$p_T$ range	truth $\sigma_L/\sigma_{tot}$	predicted $f_L$
[200,300]	0.265	0.259 ± ?
[400,500]	0.304	0.300 ± ?

- Output average method can predict well for both  $p_T$  bins
- Estimate error on our prediction can tell us the precision
- Truth value is calculated from MadGraph

## **Uncertainty**

## **Small experiments**

- From large test set, we randomly select subset (N number of events) to obtain  $f_L$
- N is determined from expected number of events at particular luminosity
- At current LHC luminosity ~ 2000 events at low  $p_T$  and 200 events at high  $p_T$
- At High Lumi LHC ~ 20k events at low  $p_T$  and 2k events at high  $p_T$
- By iterating the process, we can obtain average value with standard deviation

	300 fb <sup>-1</sup>	3000 fb <sup>-1</sup>
[200,300]	0.044	0.010
[400,500]	0.130	0.033

## **Experimental Results**

#### **ATLAS** result

ATLAS Result  $(36 \text{fb}^{-1})$ 

	$f_0$				
	Data	Powheg+Pythia		MATRIX	
$W^+$ in $W^+Z$	$0.26 \pm 0.08$	0.233 ±	0.004	0.2448 ±	0.0010
$W^-$ in $W^-Z$	$0.32 \pm 0.09$	$0.245 \pm$	0.005	$0.2651 \pm$	0.0015
$W^{\pm}$ in $W^{\pm}Z$	$0.26 \pm 0.06$	$0.2376 \pm$	0.0031	$0.2506 \pm$	0.0006
$Z$ in $W^+Z$	$0.27 \pm 0.05$	$0.225 \pm$	0.004	$0.2401 \pm$	0.0014
$Z$ in $W^-Z$	$0.21 \pm 0.06$	$0.235 \pm$	0.005	$0.2389 \pm$	0.0015
$Z$ in $W^{\pm}Z$	$0.24 \pm 0.04$	$0.2294 \pm$	0.0033	$0.2398 \pm$	0.0014

ATLAS Collaboration [arXiv:1902.05759]

- 1. Previous attempts from ATLAS collaboration to measure polarization with leptonic final states
  - Leptonic final state: small branching ratio
  - Complication in  $\nu$  reconstruction
- 2. If we can use hadronic W, we gain more statistics but need to deal with hadronic jets