

Phenomenology at the LHC of composite particles from strongly interacting Standard Model fermions via four-fermion operator of Nambu-Jona-Lasinio (NJL) type

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Physically compelling reasons for 4-fermion operator

- **Theoretical inconsistency** (NoGo theorem, [H. B. Nielsen and M. Ninomiya NPB \(1981\)](#), [NPB \(1981\)](#), [PLB \(1981\)](#)) of SM bilinear Lagrangian $\bar{\psi}\hat{O}\psi$ in fermion fields in a ultraviolet (UV) cutoff field theory
→ **Effective 4-fermion operator of Nambu-Jona-Lasinio (NJL) type** $-G(\bar{\psi}_L\psi_R)(\bar{\psi}_R\psi_L)$
([G. Preparata and S.-S. Xue PLB \(1991\)](#), [S.-S. Xue PLB \(1996\)](#), [NPB \(1997\)](#), [NPB \(2000\)](#))
 - The **effective coupling G** has two fixed points:
 - (i) In the weak-coupling **infrared (IR)** fixed point @ the electroweak scale
 - it gives rise to **SM physics** with tightly composite Higgs particle via the NJL mechanism
 - it offers possible solution to the hierarchy pattern of fermion masses
([Nambu-Jona-Lasinio PR \(1961\)](#), [PR\(1961\)](#), [W. A. Bardeen, C. T. Hill and M. Lindner PRD \(1990\)](#), [S.-S. Xue. PLB \(2013\)](#), [PLB \(2014\)](#))
 - (ii) In the strong-coupling **ultraviolet (UV)** fixed point @ at the composite scale $\Lambda \sim O(\text{TeV})$
 - **composite fermions (bosons)** form as bound states of three (two) SM elementary fermions and they couple to their constituents via effective contact interactions
- *Today we focus on LHC phenomenology of such composite fermions*

Effective field theory of massive composite particles at TeV

Composite fermions and *bosons* can be

- $F_R^f \sim \psi_R^f (\bar{\psi}_R^f \psi_L^f)$: bound states of *three SM fermions*
- $\Pi^f \sim (\bar{\psi}_R^f \psi_L^f)$: bound states of *two SM fermions*

The *effective coupling between the F (Π) and its constituents* is given by the following *contact interaction*, which describes composite particle production and decay

- $(g_*/\Lambda)^2 \bar{\psi}_L^f (\bar{\psi}_L^f \psi_R^f) F_R^f + \text{h. c.}$
 $\Lambda =$ composite scale = O(TeV), $g_*^2 = 4\pi$ and $4\pi/\Lambda^2 =$ geometric cross section in the order of magnitude of inelastic processes forming composite fermions
- $(F_\Pi/\Lambda)^2 (\bar{\psi}_L^f \psi_R^f) \Pi^f + \text{h. c.}$
 $(F_\Pi/\Lambda)^2$ Yukawa coupling between composite bosons and two fermionic constituents

Λ and F_Π are free parameters of the models

| Operator | Composite fermion F_R | Composite fermion \bar{F}_L | Composite boson Π |
|---|--|--|-------------------------------------|
| $(\bar{\nu}_L^e e_R)(\bar{d}_R^a u_{La})$ | $E_R^0 \sim e_R(\bar{d}_R^a u_{La})$ | $\bar{E}_L^0 \sim \bar{e}_L(\bar{u}_R^a d_{La})$ | $\Pi^+ \sim (\bar{d}_R^a u_{La})$ |
| $(\bar{e}_L \nu_R^e)(\bar{u}_R^a d_{La})$ | $N_R^- \sim \nu_R^e(\bar{u}_R^a d_{La})$ | $\bar{N}_L^+ \sim \bar{\nu}_L^e(\bar{d}_R^a u_{La})$ | $\Pi^- \sim (\bar{u}_R^a d_{La})$ |
| $(\bar{e}_L e_R)(\bar{d}_R^a d_{La})$ | $E_R^- \sim e_R(\bar{d}_R^a d_{La})$ | $\bar{E}_L^+ \sim \bar{e}_L(\bar{d}_L^a d_{Ra})$ | $\Pi_d^0 \sim (\bar{d}_R^a d_{La})$ |
| $(\bar{\nu}_L^e \nu_R^e)(\bar{u}_R^a u_{La})$ | $N_R^0 \sim \nu_R^e(\bar{u}_R^a u_{La})$ | $\bar{N}_L^0 \sim \bar{\nu}_L^e(\bar{u}_L^a u_{Ra})$ | $\Pi_u^0 \sim (\bar{u}_R^a u_{La})$ |

Comparison w/ other composite fermions models

Searches for composite fermions @ LHC rely on models such as

J.C. Pati, A. Salam, J.A. Strathdee, Are quarks composite?, Phys. Lett. B 59 (1975) 265, [https://doi.org/10.1016/0370-2693\(75\)90042-8](https://doi.org/10.1016/0370-2693(75)90042-8);

H. Harari, Composite models for quarks and leptons, Phys. Rep. 104 (1984) 159, [https://doi.org/10.1016/0370-1573\(84\)90207-2](https://doi.org/10.1016/0370-1573(84)90207-2);

O.W. Greenberg, C.A. Nelson, Composite models of leptons, Phys. Rev. D 10 (1974) 2567, <https://doi.org/10.1103/PhysRevD.10.2567>.

P. A. M. Dirac, Scientific American 208, 45 (1963).

H. Terazawa, K. Akama, and Y. Chikashige, Phys. Rev. D15, 480 (1977).

H. Terazawa, Phys.Rev. D22, 184 (1980).

E. Eichten and K. Lane, Physics Letters B 90, 125 (1980).

E. Eichten, K. D. Lane, and M. E. Peskin, Phys. Rev. Lett. 50, 811 (1983).

H. Terazawa, in Europhysics Topical Conference: Flavor Mixing in Weak Interactions Erice, Italy, March 4-12, 1984 (1984).

N. Cabibbo, L. Maiani, and Y. Srivastava, Phys. Lett. B139, 459 (1984).

U. Baur, M. Spira, and P. M. Zerwas, Phys. Rev. D 42, 815 (1990).

U. Baur, I. Hinchliffe, and D. Zeppenfeld, Int. J. Mod. Phys. A2, 1285 (1987).

Analogies

- the existence of composite fermions
- the existence of contact interaction, in addition to SM gauge interaction, as an effective approach for describing the effects of the unknown internal dynamics of compositeness

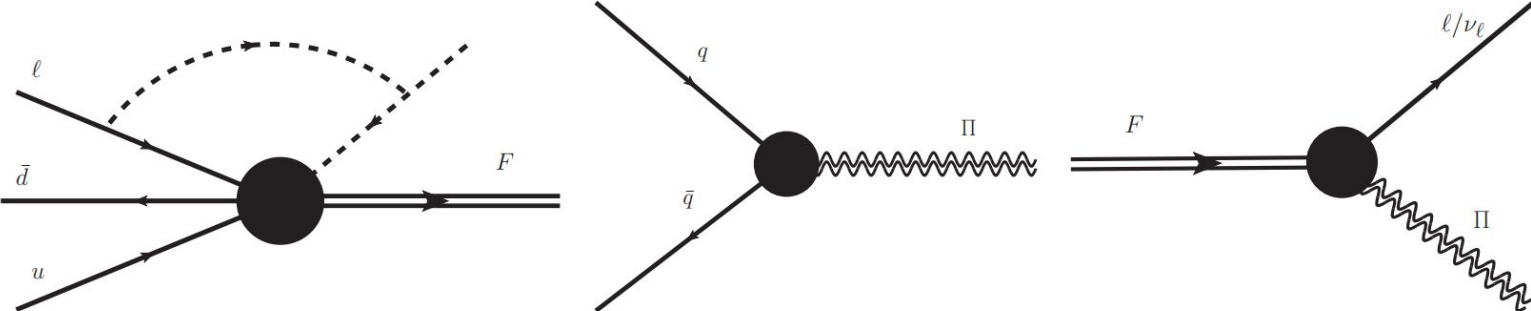
Differences

- composite fermions formed as bound states of SM fermions, not other fundamental particles (preons)
- strong four-fermion interactions of SM fermions at high energies with different contact interacting processes

→ Different phenomenology with a wide range of composite particles that would manifest via peculiar signatures (some of which not yet investigated @ LHC)

Phenomenology of composite particles at the TeV scale

- The Feynman diagram representations for the composite fermions F and boson (Π) are



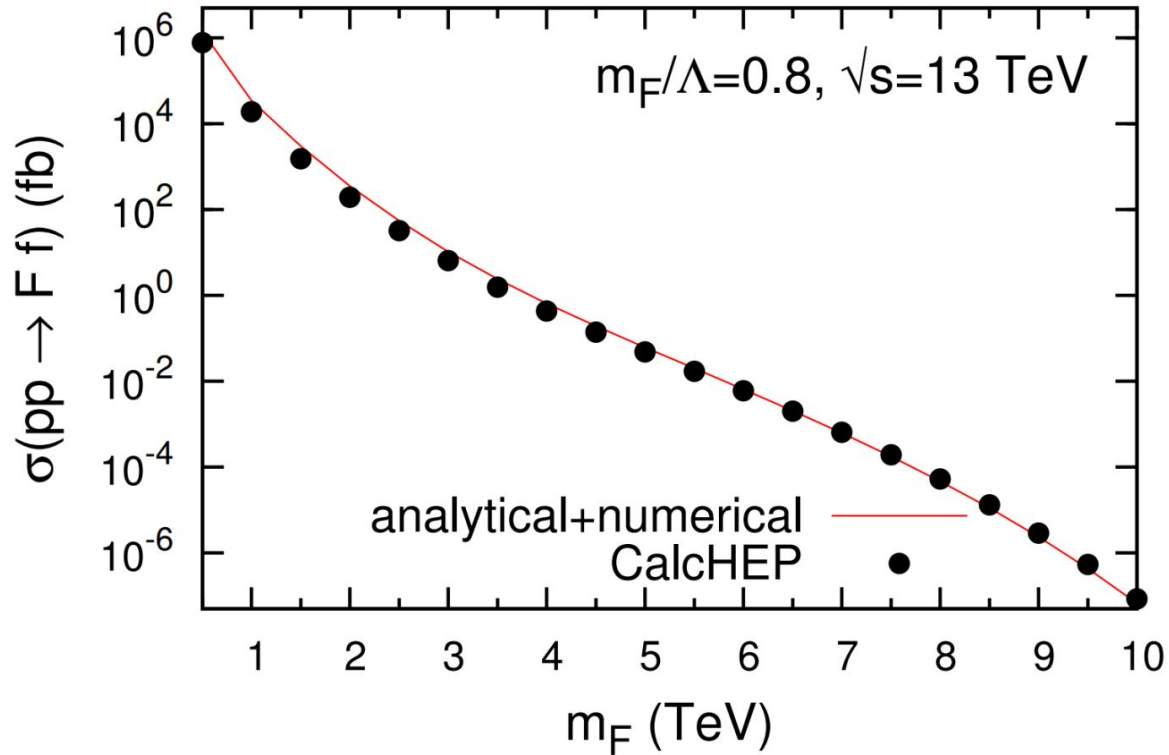
- Today, we describe the [phenomenology at the LHC](#) considering the [most left diagram](#)
- By a crossing symmetry applied to the fermion line $f \rightarrow f^\dagger$ (dashed line) the same diagram describes a $2 \rightarrow 2$ production process:

$$q\bar{q} \rightarrow fF$$

f is a SM fermion

F is a composite fermion, whose flavour correspond to the SM flavour of f

Production cross-section for the process $pp \rightarrow fF$



Good agreement between analytical+numerical calculation and the results of the CalcHEP simulation, which validates the model implementation

Decay of the composite fermion F and decay chain $pp \rightarrow fF$

Decay of the composite fermion F through 2 different channels

- $F \rightarrow \bar{f} qq'$
- $F \rightarrow \bar{f} \Pi^{0,\pm}$

Note that

- if $\Pi = \Pi^+$ or $\Pi^- \rightarrow$, only $\Pi \rightarrow qq'$ is allow
- if $\Pi = \Pi^0$, $\Pi \rightarrow \tilde{G}\tilde{G}'$ ($G = \gamma, Z, W$) is also possible. This case turns out to be negligible (see below)

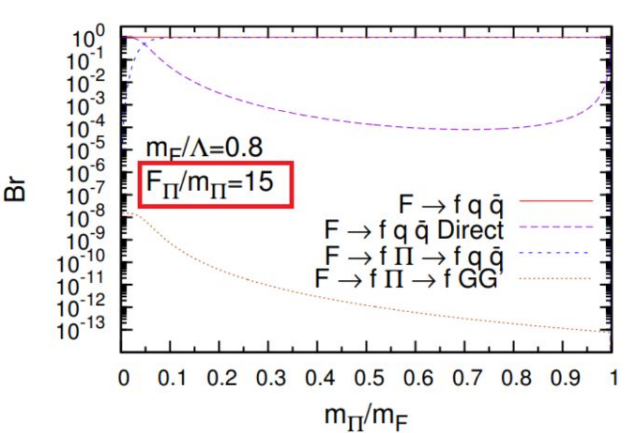
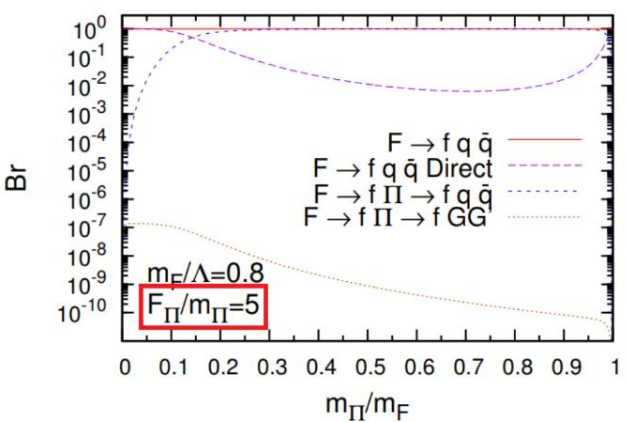
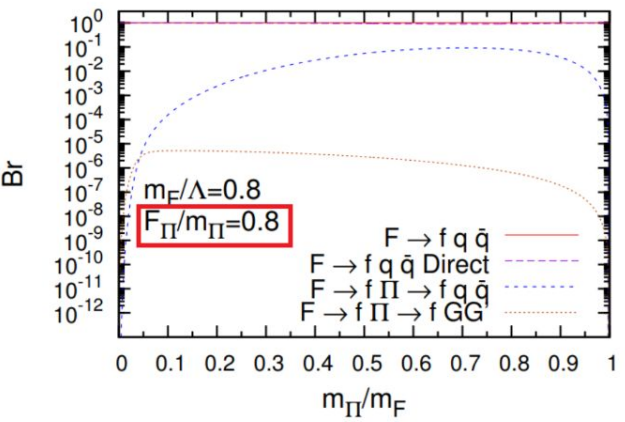
Full decay chain is

- $pp \rightarrow fF \rightarrow \bar{f}fqq'$
- $pp \rightarrow fF \rightarrow \bar{f}f \Pi^{0,\pm}$

For a given Λ , the effective theory of composite particles is fully characterized in terms of the coupling F_Π , and the masses m_F and m_Π

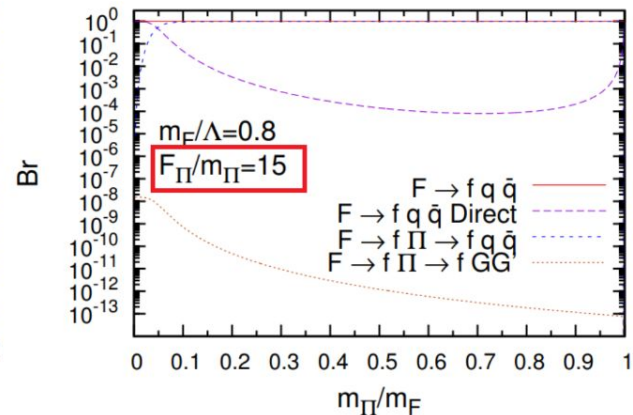
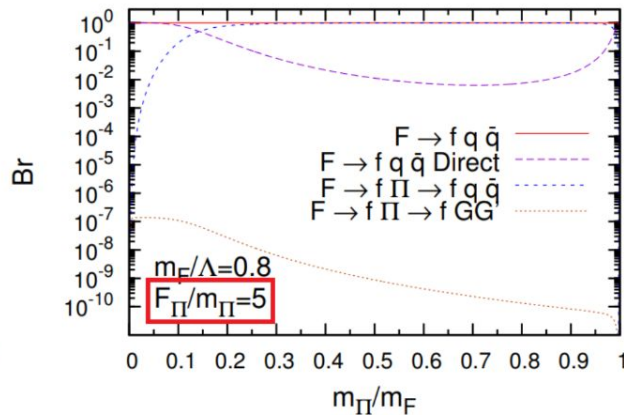
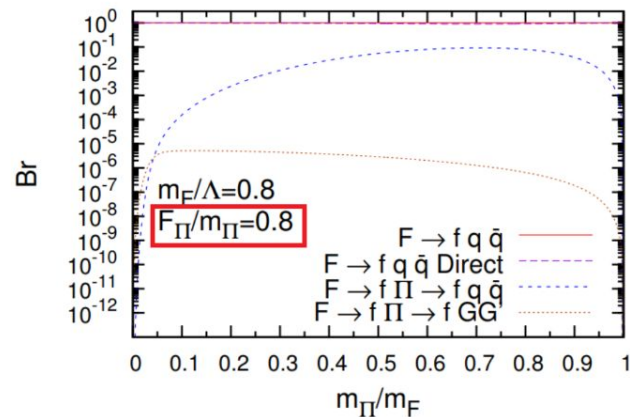
- $m_F/\Lambda < 1$ ($m_\Pi/\Lambda < 1$): insight into the dynamics of composite fermion (boson) formation
- F_Π/m_Π : m_Π and F_Π represent the same dynamics of composite boson formation
- $m_\Pi/m_F < 1$: to take into account F as composed by a composite boson and an elementary SM fermion

Decay branching fraction of F



- $F \rightarrow f\Pi \rightarrow fG\tilde{G}'$ always negligible
- $\Pi^0 \rightarrow \tilde{G}\tilde{G}'$ is the only case to depend from $m_F/\Lambda < 1$, which means the decay of F is fully characterized by the 2 parameters F_Π/m_Π and $m_\Pi/m_F < 1$
- the $\text{Br}(F \rightarrow fq\bar{q} \text{ direct})$ and $\text{Br}(F \rightarrow f\Pi \rightarrow fq\bar{q} \text{ indirect})$ tend to swap each other for different values of F_Π/m_Π this is important in terms of the signal topology, as it determines whether an intermediate resonance is produced

Relevant channels for the process $pp \rightarrow fF$ at the LHC



| F_{Π}/m_{Π} | m_{Π}/m_F | Channel | Resonances | Topology | Experimental features |
|-------------------|----------------------|--|------------|-----------------------------------|---|
| 15 | $[\sim 0.2, \sim 1]$ | $fF \rightarrow f(\bar{f}\Pi) \rightarrow f(\bar{f}(qq'))$ | F, Π | Resolved w/ $\Pi \rightarrow qq'$ | identification of Π and F |
| | ≤ 0.2 | $fF \rightarrow f(\bar{f}\Pi) \rightarrow f(\bar{f}(qq'))$ | F, Π | Boosted | identification of F ; Π large-radius jet; 2-prong, no V boson tag |
| ≤ 0.8 | $[0,1]$ | $fF \rightarrow f(\bar{f}qq')$ | F | Fully resolved | same of $F_{\Pi}/m_{\Pi} = 10$ |

Same consideration applies to values of F_{Π}/m_{Π} between 0.8 and 15

Relevant signatures for investigating the process $pp \rightarrow fF$ at LHC

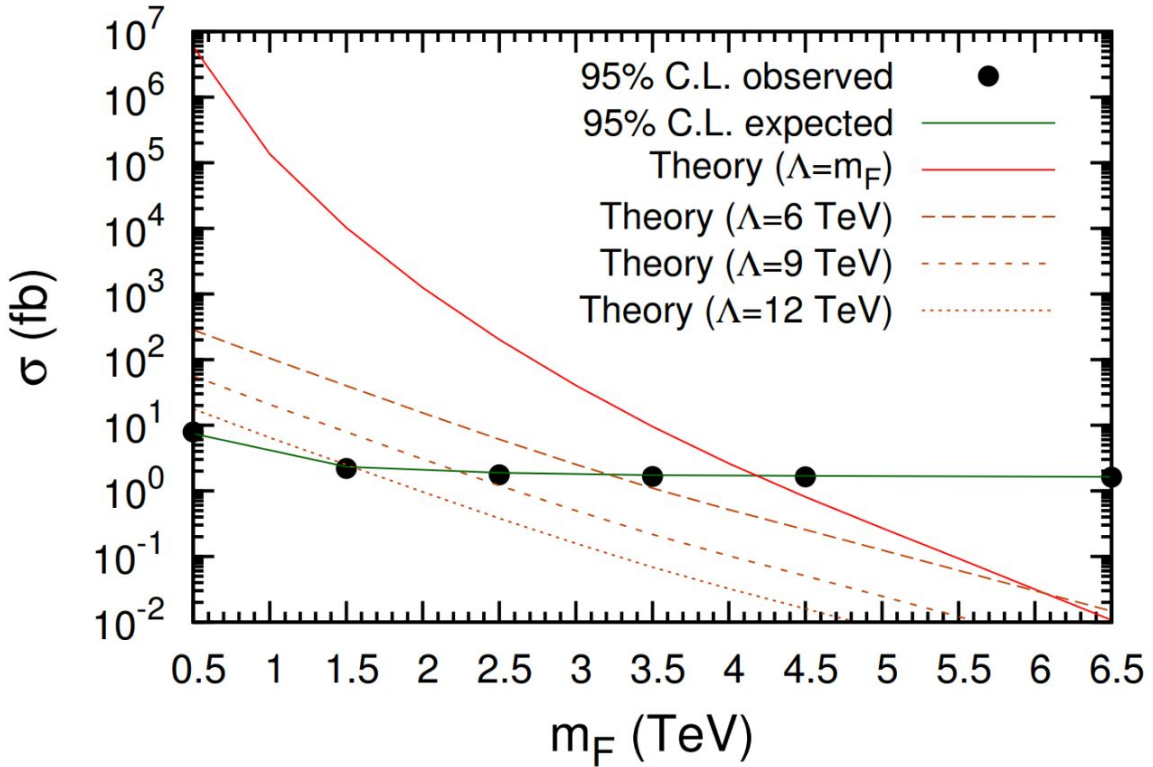
f = SM fermion; F = composite fermion, whose flavour correspond to the SM flavour of f
 F particles not necessarily mass degenerate \rightarrow each flavour searched for separately

| f | F | Topology | Final state | LHC searches | Features not exploited in LHC searches |
|--------|---------------|-----------------------------------|---------------------------|--------------|--|
| e | E | Fully resolved | $e^\pm(e^\mp qq')$ | [28, 48] | E identification |
| | | Resolved w/ $\Pi \rightarrow qq'$ | $e^\pm(e^\mp(qq'))$ | [48, 52] | E, Π identification |
| | | Boosted | $e^\pm e^\mp J$ | [28] | 2-prong, no V boson tag, boosted Π decay |
| μ | M | Fully resolved | $\mu^\pm(\mu^\mp qq')$ | [28, 48] | M identification |
| | | Resolved w/ $\Pi \rightarrow qq'$ | $\mu^\pm(\mu^\mp(qq'))$ | [48, 52] | M, Π identification |
| | | Boosted | $\mu^\pm \mu^\mp J$ | [28] | 2-prong, no V boson tag, boosted Π decay |
| τ | \mathcal{T} | Fully resolved | $\tau^\pm(\tau^\mp qq')$ | [49] | \mathcal{T} identification |
| | | Resolved w/ $\Pi \rightarrow qq'$ | $\tau^\pm(\tau^\mp(qq'))$ | [49] | \mathcal{T}, Π identification |
| | | Boosted | $\tau^\pm \tau^\mp J$ | n/a | |
| ν | N | Fully resolved | $\nu(\nu qq')$ | [50, 51] | N identification |
| | | Resolved w/ $\Pi \rightarrow qq'$ | $\nu(\nu(qq'))$ | [50, 51] | N, Π identification |
| | | Boosted | $\nu\nu J$ | [55] | 2-prong, no V boson tag, boosted Π decay |
| j | J | Fully resolved | $j(j qq')$ | n/a | |
| | | Resolved w/ $\Pi \rightarrow qq'$ | $j(j(qq'))$ | n/a | |
| | | Boosted | jjJ | n/a | |
| c | C | Fully resolved | $c(c qq')$ | n/a | |
| | | Resolved w/ $\Pi \rightarrow qq'$ | $c(c(qq'))$ | n/a | |
| | | Boosted | ccJ | n/a | |
| b | B | Fully resolved | $b(b qq')$ | n/a | |
| | | Resolved w/ $\Pi \rightarrow qq'$ | $b(b(qq'))$ | n/a | |
| | | Boosted | bbJ | n/a | |
| t | T | Fully resolved | $t(\bar{t} qq')$ | n/a | |
| | | Resolved w/ $\Pi \rightarrow qq'$ | $t(\bar{t}(qq'))$ | n/a | |
| | | Boosted | $t\bar{t}J$ | n/a | |

- 8 different final states times 3 possible topologies = 24 distinct signatures
- F quark flavors appear to be completely unexplored
- For $F = N$, the ν pair stands for the pairs of the SM left-handed neutrino ν_L^e and/or sterile right-handed neutrino ν_R^e , as the latter is a candidate of dark-matter particles

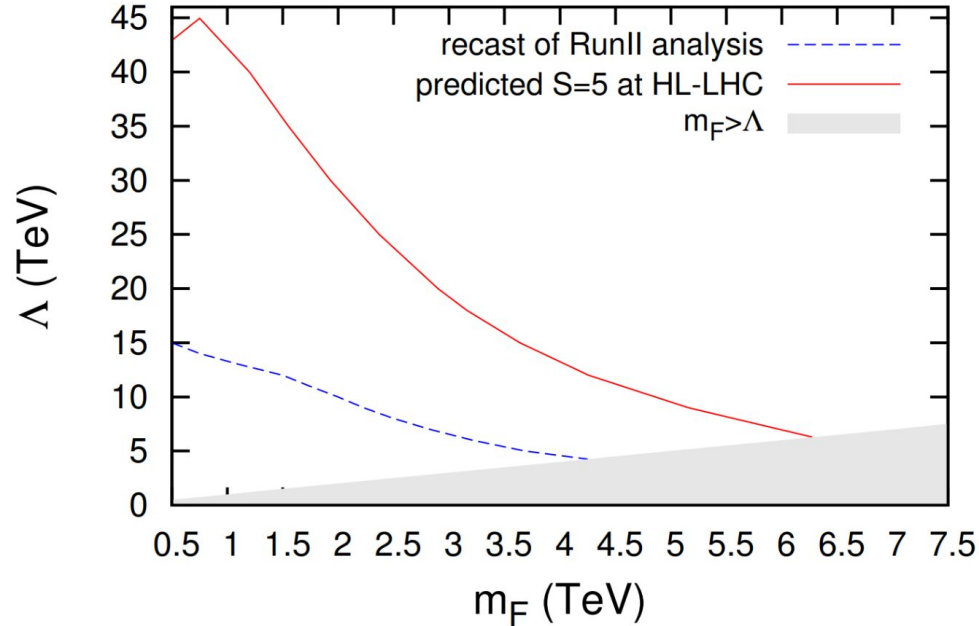
Constraint of the model for $F = E$

Recast of the CMS search (link) that probed the final state $eeqq$ (2.3 fb^{-1} , $\sqrt{s} = 13 \text{ TeV}$)



Sensitivity for $F = E$ at High-Lumi LHC (3 ab^{-1})

$$p_T e_1 (e_2) [j_1] \geq 180 (80) [210] \text{ GeV}; m_{ee} \geq 300 \text{ GeV}$$
$$N_s = L\sigma_s\epsilon_s, \quad N_b = L\sigma_b\epsilon_b, \quad S = \frac{N_s}{\sqrt{N_b}}$$



Wide region of the model phase space where the existence of the composite fermions can be investigated (even with a simple analysis)

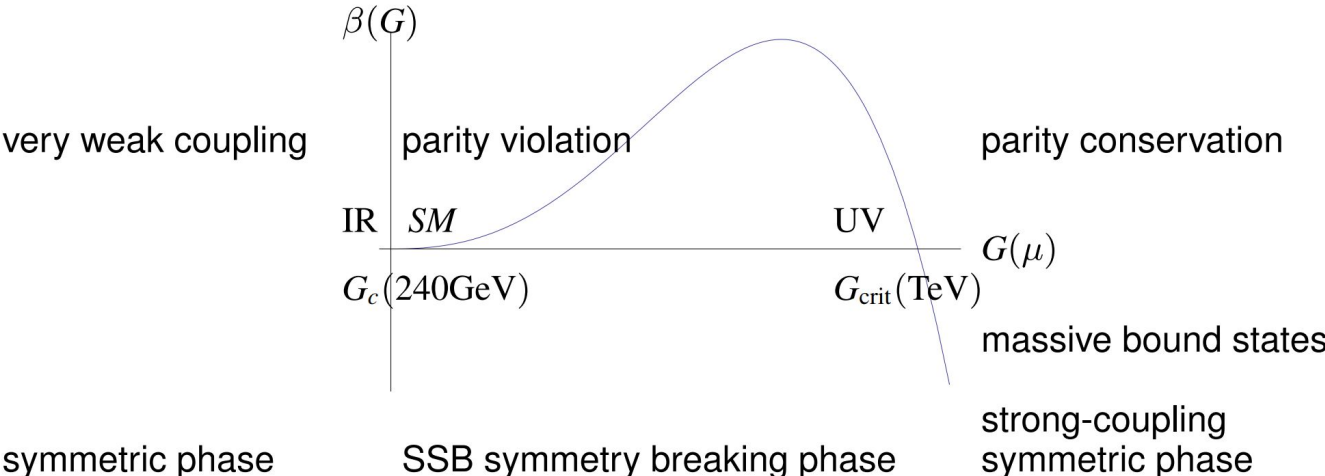
Summary and conclusion

- New composite states from 4-fermion operator of NJL are well motivated from a theoretical point of view (see e.g. [S.-S. Xue JHEP \(2016\)](#), [S.-S. Xue JHEP \(2017\)](#) and references therein)
 - Weak coupling regime: 4-fermion NJL operators w/ IR-fixed point that renders the elegant Higgs mechanism at low energies
 - Strong coupling regime: 4-fermion NJL operators w/ UV-fixed point that would render F (Π) as bound states of three (two) SM elementary leptons or quarks, and a contact interactions at energies $O(\text{TeV})$
- We have studied the cross-sections, branching ratios, and topologies with which the F particles can manifest. [We find out that](#)
 - for given \sqrt{s} and Λ values, they can be [investigated](#) comprehensively relying on only [two parameters](#): F_{Π}/m_{Π} and m_{Π}/m_F
 - 8 different final states times 3 possible topologies = [24 distinct signatures](#)
 - [F quark flavors appear to be completely unexplored](#)
 - Even signatures already explored have a wide potential of discovery with the increasing statistics accumulated at the LHC
 - For $F = N$ there is a [possible candidate of dark-matter particle](#)
- Given the broad variety of new composite particles that could manifest in non-previously examined signatures at the LHC, [we would like to encourage their investigations at future searches at the LHC](#)
- There is an ongoing effort to outline the phenomenology for the direct production of composite boson

Back up

4-fermion operators and IR UV-fixed points

For the reason (**No-Go theorem**) that the SM bilinear Lagrangian $\bar{\psi}\hat{O}\psi$ in fermion fields is inconsistent in a UV cutoff field theory, effective four-fermion operators of Nambu-Jona-Lasinio type $-G(\bar{\psi}_L\psi_R)(\bar{\psi}_R\psi_L)$ must be originated by some unknown dynamics at the cutoff Λ .



- No-Go theorem: H.B. Nielsen and M. Ninomiya, Nucl. Phys. B 185 (1981) 20 and B 193 (1981) 173;
- G. Preparata and S.-S. Xue, PLB264(1991)35; S.-S. Xue, PLB381(1996)277; NPB486 (1997) 282, B580 (2000) 365, . . .