

# A new solution to the Strong CP problem and the neutrino masses

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Work in Collaboration with  
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arXiv: 1904.05360

# Motivation

- The success of SM relies on few principles:
  - ▶ Lorentz invariance
  - ▶ Gauge-invariance
  - ▶ Renormalizability
- Naturally leads to:
  - ▶ Accidental flavour symmetries in the gauge sector

$$U(3)^5 = SU(3)^5 \times U(1)_B \times U(1)_L \times U(1)_Y \times U(1)_{PQ} \times U(1)_{e_R}$$

- ▶ Absence of FCNC at tree-level
- ▶ GIM suppression at loop level

# Motivation

- However the same procedure leads to
  - ▶ O(1) CP-violating in the QCD (Strong CP)
  - ▶ Instability of Higgs mass (Hierarchy)
- Other issues:
  - ▶ Smallness of the neutrino masses:
$$m_\nu \sim 10^{-2} - 10^{-4} \text{ eV}$$
  - ▶ Lack of Dark Matter candidate

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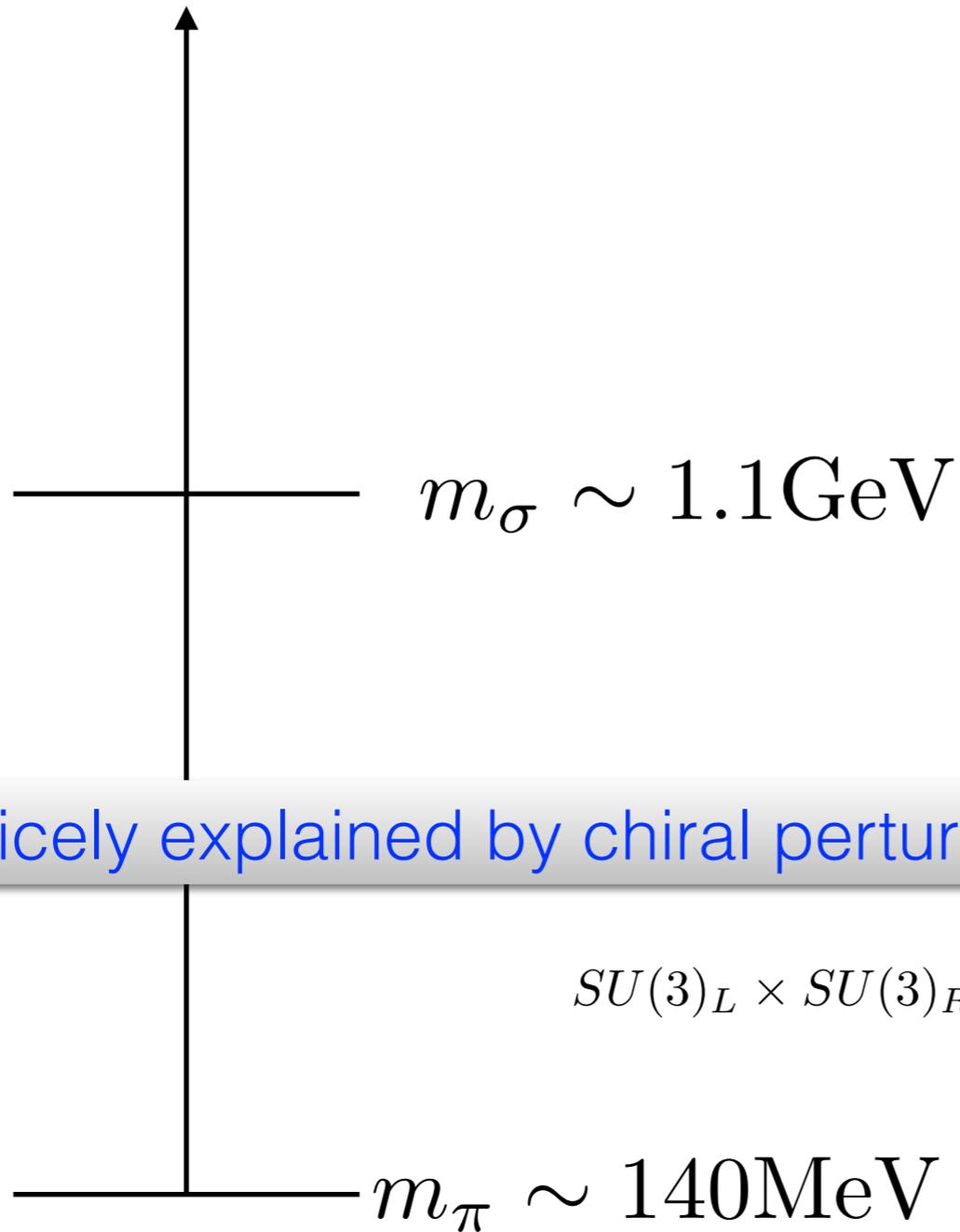
Focus of this talk

# $\theta$ term in QCD

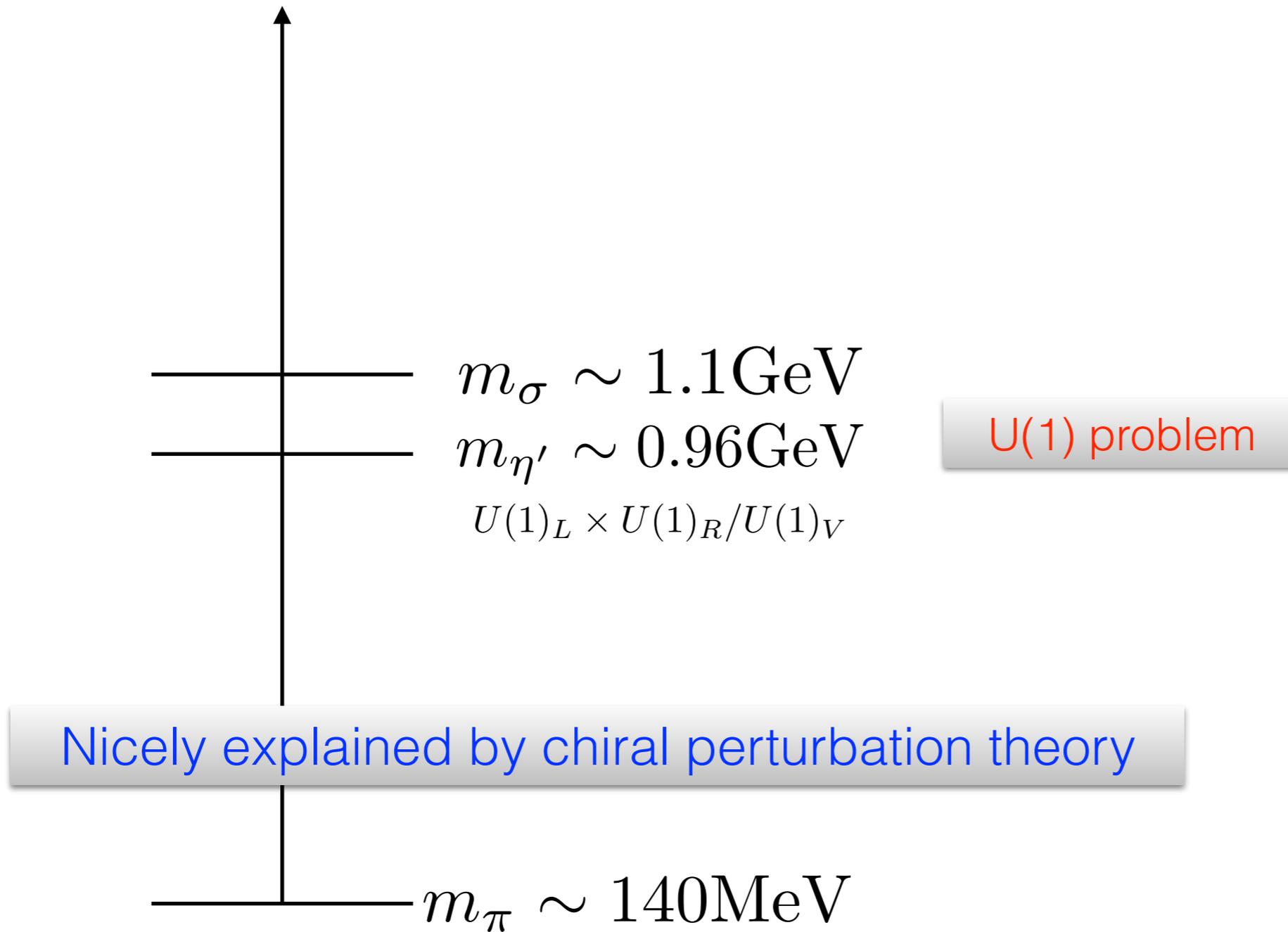
$$\mathcal{L} = -\frac{\theta g_s^2}{32\pi^2} G_{\mu\nu}^a \tilde{G}^{a\mu\nu}$$

- Allowed by gauge invariance, Lorentz invariance and Renormalizability
- Given the  $O(1)$  CP-violating phase in CKM matrices,  $\theta$  is expected to be  $O(1)$
- Total derivative at classical level, relevant at quantum

# The relevance of $\theta$ in QCD



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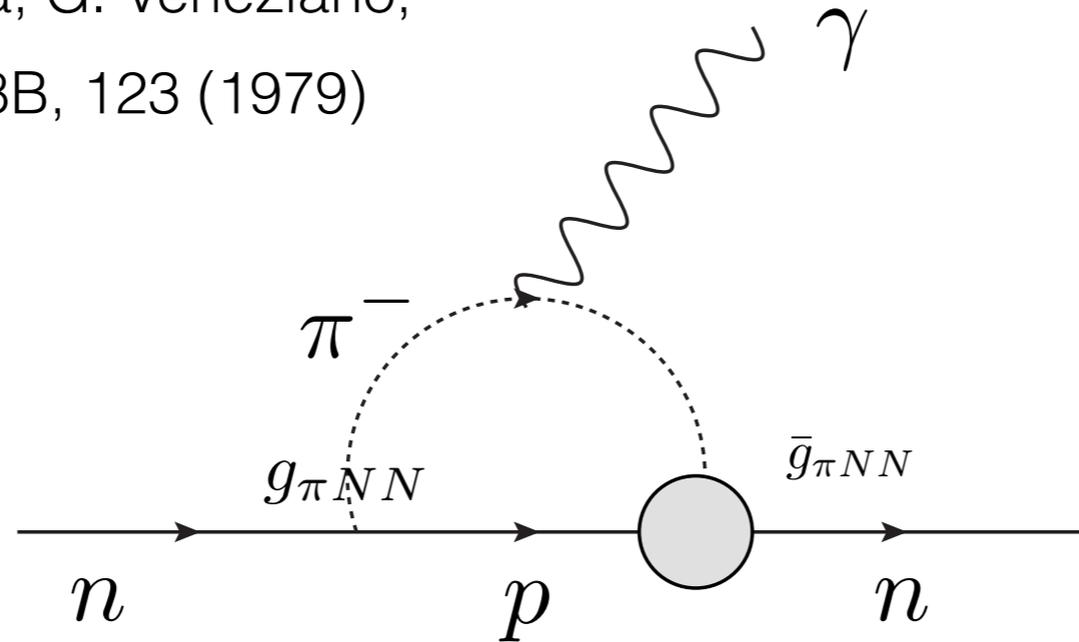
U(1) problem

$$\partial^\mu J_\mu^5 = \frac{g_s^2}{16\pi^2} G_{\mu\nu}^a \tilde{G}^{a\mu\nu}$$

- Total derivative at classical level
- Instanton configuration make it physical
- One instanton configuration  $e^{-\frac{8\pi^2}{g_s^2}}$

# The relevance of $\theta$ in QCD

R. J. Crewther, P. Di Vecchia, G. Veneziano,  
and E. Witten, Phys. Lett. 88B, 123 (1979)



$$\frac{d_n}{e} \sim \frac{g_{\pi NN} \bar{g}_{\pi NN}}{4\pi^2 M_N} \ln \frac{M_N}{m_\pi}, \quad \bar{g}_{\pi NN} \sim \theta_{QCD} \frac{m_{eff}}{F_\pi}, \quad m_{eff} \sim \frac{m_u m_d}{m_u + m_d}$$

Similar to QCD sum rules result

$$d_n \sim \theta_{QCD} \times (2.4 \pm 0.7) \times 10^{-16} \text{ e cm},$$

# The relevance of $\theta$ in QCD

$$\mathcal{L} = -\frac{\theta g_s^2}{32\pi^2} G_{\mu\nu}^a \tilde{G}^{a\mu\nu}$$

- Solution to U(1) problem makes it relevant
- CP-violating effects in QCD: nEDM,  $\eta \rightarrow \pi\pi$
- $|\theta| < 0.000000000013$  ( $10^{-10}$ ) [Call for an explanation!](#)

# Solutions to Strong CP

- Make  $\theta$  dynamical field: axion

R.D. Peccei and H. R. Quinn  
F. Wilczek  
S. Weinberg

- Make CP exact symmetries and break it spontaneously: Nelson-Barr Mechanism

A. E. Nelson  
S. M. Barr

- up quark is massless

H. Georgi and I. N. McArthur  
K. Choi, C.W. Kim and W.K. Sze  
T. Banks, Y. Nir and N. Seiberg  
W. A. Bardeen

$\eta'$  is the axion

# The role of quark

$$\mathcal{L} = -\frac{\theta g_s^2}{32\pi^2} G_{\mu\nu}^a \tilde{G}^{a\mu\nu}$$

- One flavour QCD

$$u_R \rightarrow e^{i\alpha} u_R \quad \mathcal{L} \rightarrow \alpha \frac{g_s^2}{32\pi^2} G_{\mu\nu}^a \tilde{G}^{a\mu\nu}$$

Only parameter invariant under field redefinition is physical

$$\theta_{\text{QCD}} = \theta + \arg[m_u]$$

- In general

$$\theta_{\text{QCD}} = \theta + \arg[\det M_q]$$

# Reinterpret the bound

- In a basis

$$\theta_{\text{QCD}} = \arg[m_u]$$

Canonical Basis

$$|m_u|(1\text{GeV}) \sim 3\text{MeV}$$

$$|\theta_{\text{QCD}}| < 1.3 \times 10^{-10} \Rightarrow \text{Im}[m_u] < 4.0 \times 10^{-4}\text{eV}$$

- Neutrino mass

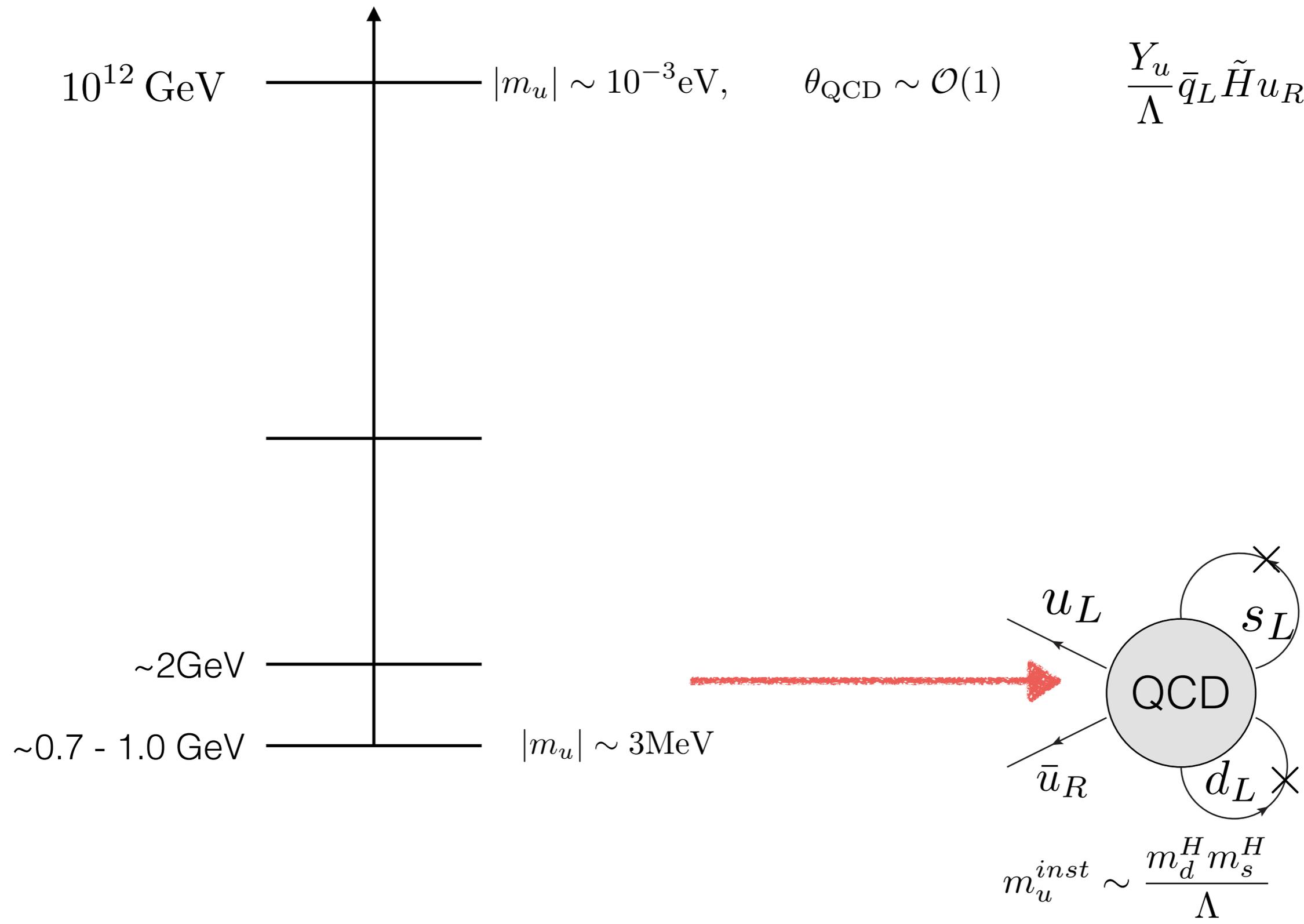
$$\text{NH} : m_3 \sim 0.05\text{eV}, \quad m_2 \sim 0.0086\text{eV}$$

Explain the small scale

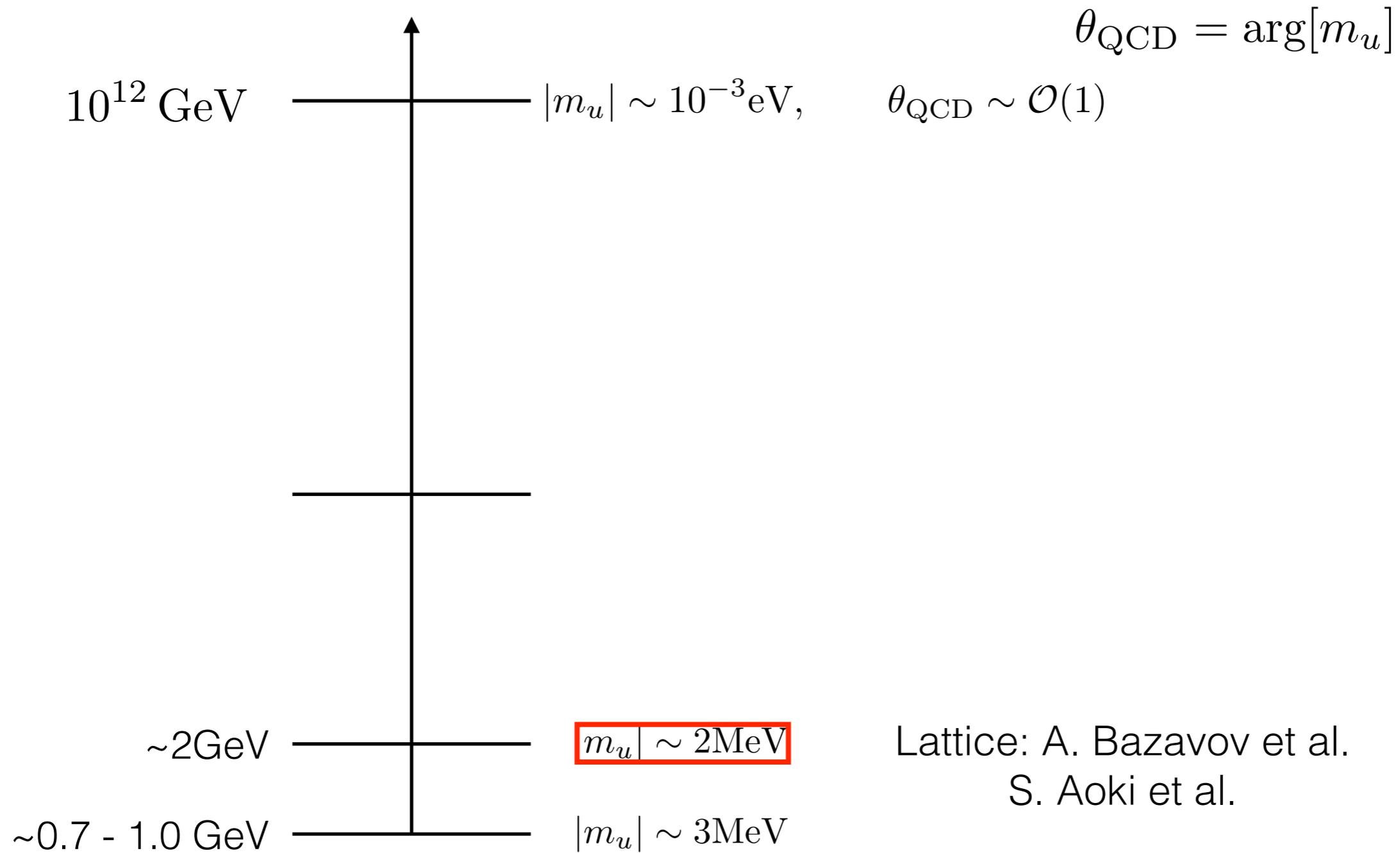
# Tiny up quark mass

$$\theta_{\text{QCD}} = \arg[m_u]$$

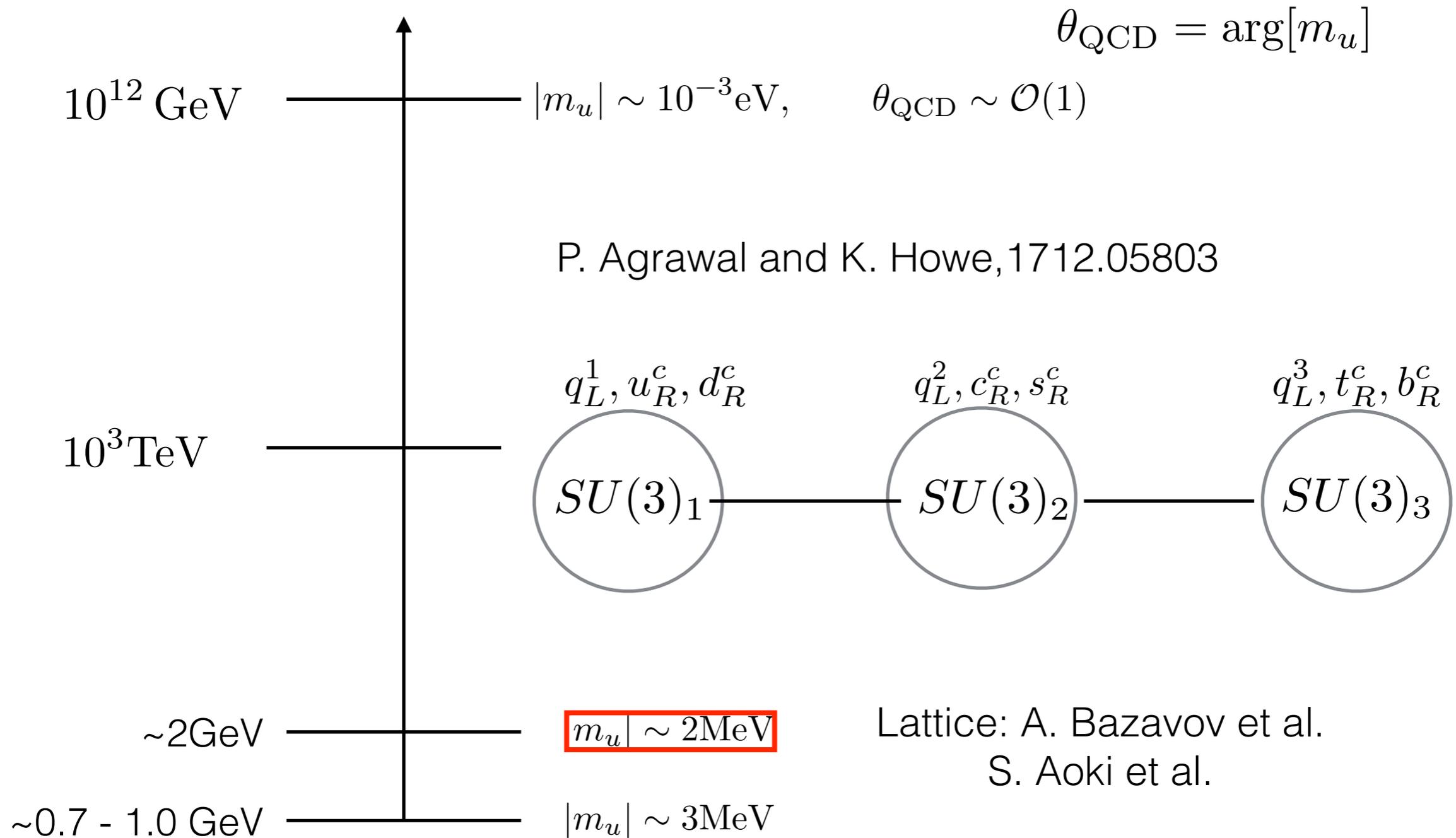
$$\frac{Y_u}{\Lambda} \bar{q}_L \tilde{H} u_R S$$



# Tiny up quark mass



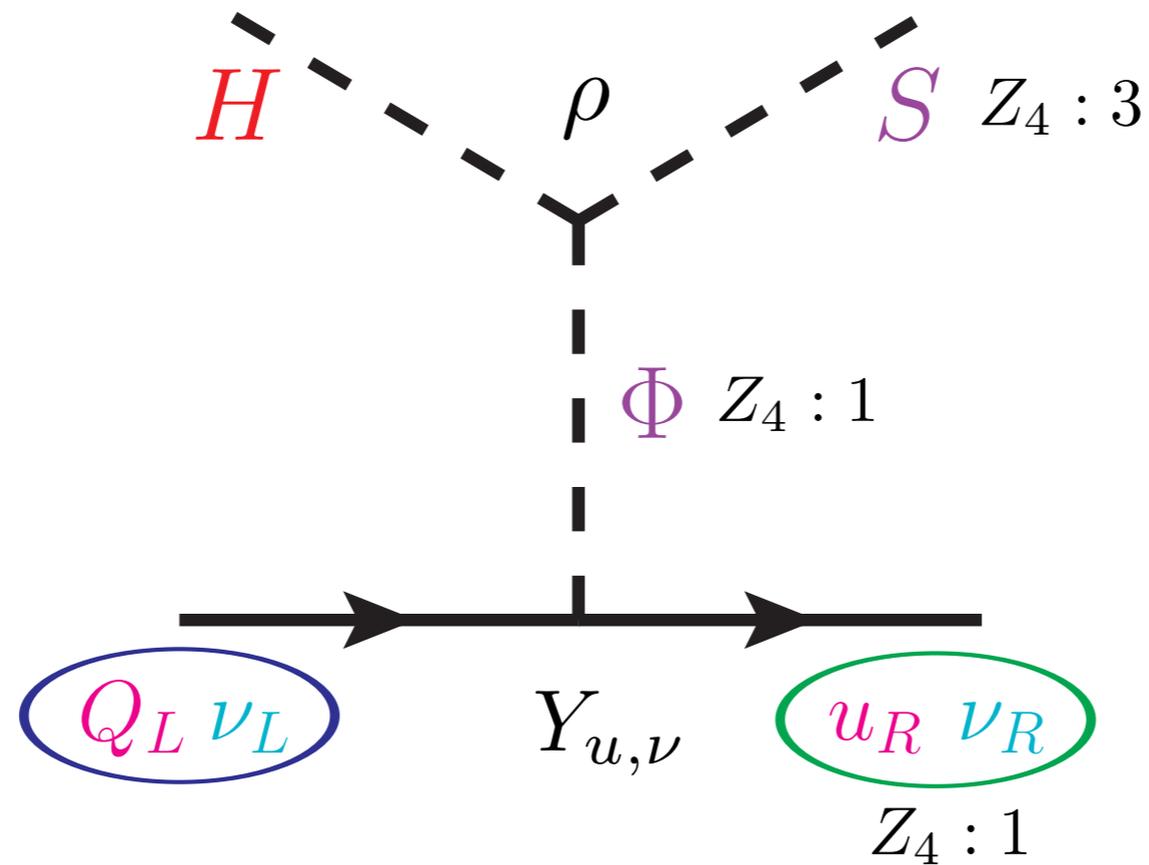
# Bypass the lattice



# Dirac seesaw

P.-H. Gu and H.-J. He, hep-ph/0610275.

C. Bonilla, J. M. Lamprea, E. Peinado,  
and J. W. F. Valle, 1710.06498



$$-Y_\nu \frac{\rho}{m_\Phi^2} S \bar{\ell}_L \tilde{H} \nu_R$$

$$-Y_u \frac{\rho}{m_\Phi^2} S \bar{q}_L \tilde{H} u_R$$

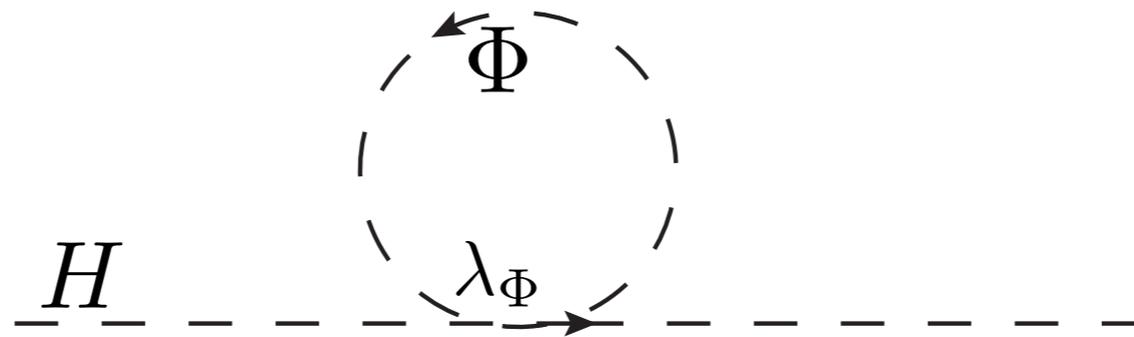
$$m_\nu \sim Y_\nu \frac{\rho v_S v}{2m_\Phi^2}, \quad m_u^H \sim Y_u \frac{\rho v_S v}{2m_\Phi^2}.$$

$$\lambda_S S^4$$

No axion-like Goldstone!

# Dirac seesaw

$$m_\Phi \simeq 6 \times 10^{12} \text{ GeV} \left( \frac{Y_\nu}{0.1} \right) \left( \frac{\rho}{0.1 m_\Phi} \right) \left( \frac{v_S}{v} \right),$$



leads to a physical contribution to the Higgs mass

$$\delta m_H^2 \sim \frac{\lambda_\Phi}{16\pi^2} m_\Phi^2$$

Need engineering

$$\lambda_\Phi \sim 10^{-19}$$

# SUSY extension

Superpotential

$$W = -Y_\nu L \Phi_u \nu_R^c - Y_u Q \Phi_u u_R^c \\ + \mu H_u H_d + m_\Phi \Phi_u \Phi_d + \lambda H_u \Phi_d S + \frac{\kappa}{3} S^3$$

$Z_3$

$$\Phi_u : 2, \quad \Phi_d : 1, \quad u_R^c : 1, \quad \nu_R^c : 1, \quad S : 2.$$

$$\mathcal{L}_{\text{eff}}^y = -Y_\nu \frac{\lambda}{m_\Phi} L H_u \nu_R^c S - Y_u \frac{\lambda}{m_\Phi} Q H_u u_R^c S + \dots$$

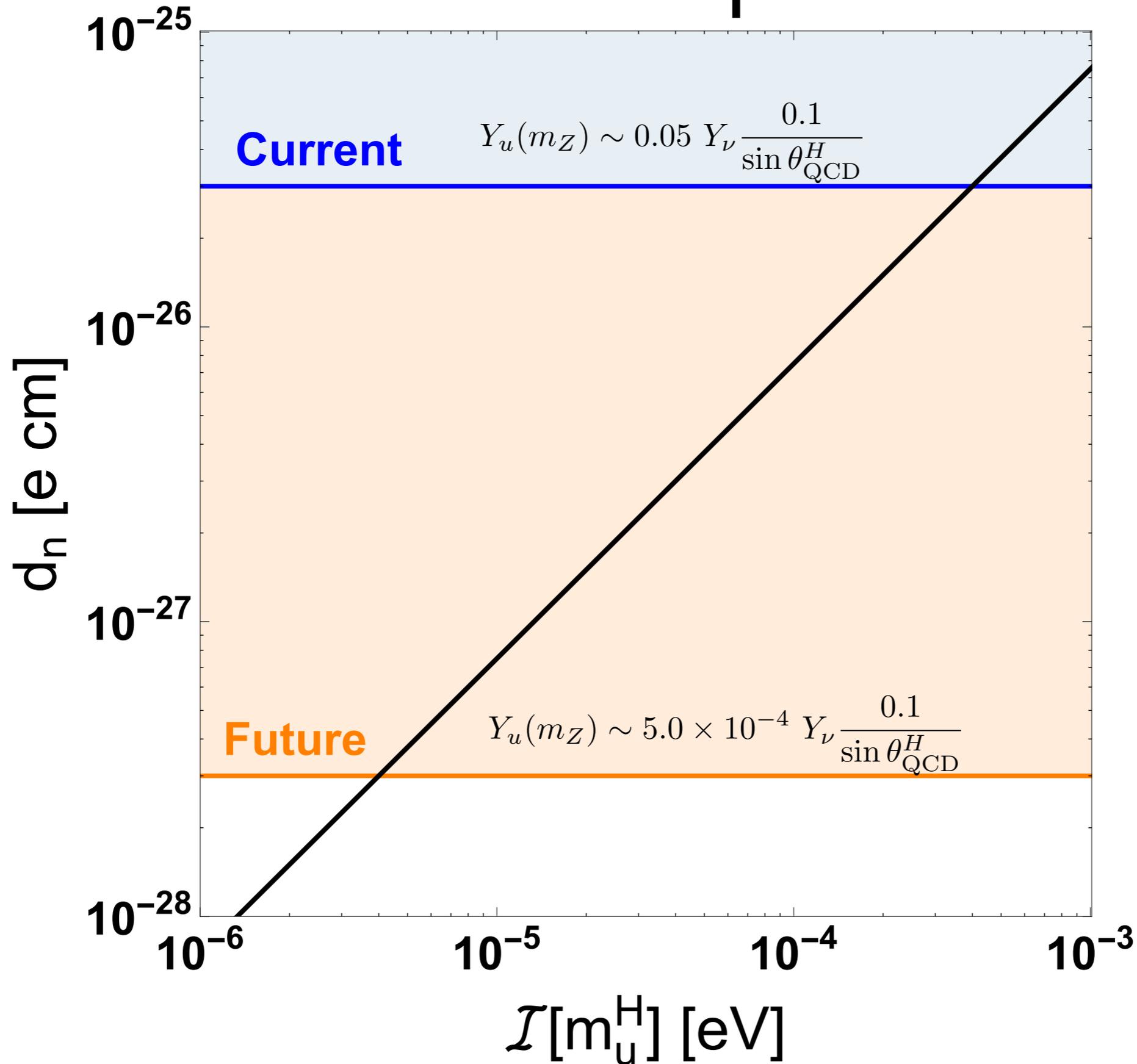
$$m_\nu \sim Y_\nu \frac{\lambda v_u v_S}{m_\Phi}, \quad m_u^H \sim Y_u \frac{\lambda v_u v_S}{m_\Phi}.$$

# nEDM experiments

Present Limit  $3 \times 10^{-26} e \text{ cm}$

Experiment	Sensitivity [e cm]
PSI	$< 1 \times 10^{-27}$
TRIUMF (TUCAN)	$1 \times 10^{-27}$
SNS	$< 3 \times 10^{-28}$
PNPI-ILL-PTI	$10^{-27} - 10^{-28}$
LANL EDM	$3 \times 10^{-27}$
Munich/ILL	$\mathcal{O}(10^{-28})$

# nEDM Prospective



# Conclusion

- A  $\nu$  solution to Strong CP
- Dirac seesaw related two scale  
 $m_\nu$  and  $\text{Im}[m_u^H]$
- A non-zero nEDM is predicted
- It is naturally within the reach of the next generation of experiments

# Backup

$$\bar{g}_{\pi NN} = \theta_{\text{QCD}} \frac{\mu_{\text{eff}}}{F_\pi} \frac{M_\Xi - M_N}{2|m_s| - |m_u| - |m_d|}, \quad \mu_{\text{eff}} \equiv \frac{|m_u m_d m_s|}{|m_u m_d| + |m_u m_s| + |m_d m_s|},$$

$$\text{NH} : m_3 \sim 0.05 \text{ eV}, \quad m_2 \sim 0.0086 \text{ eV}$$

$$\text{IH} : m_1 \sim 0.05 \text{ eV}, \quad m_2 \sim 0.05 \text{ eV}$$

$$V_{\text{SUSY}} = \mu^2 |H_u|^2 + |\mu H_d + \lambda \Phi_d S|^2 + |m_\Phi \Phi_u + \lambda H_u S|^2 + m_\Phi^2 |\Phi_d|^2 + |\kappa S^2 + \lambda H_u \Phi_d|^2, \quad (18)$$

$$V_{\text{soft}} = m_{\Phi_u}^2 |\Phi_u|^2 + m_{\Phi_d}^2 |\Phi_d|^2 + m_S^2 S^* S + \dots + (a_\lambda H_u \Phi_d S + b_\lambda \Phi_u^\dagger H_u S + a_\kappa S^3 + \dots + h.c.),$$

$$\Lambda_\chi \sim 0.7 - 1.0 \text{ GeV}$$