

# PDFs and Top Physics

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## Updates in PDFs relevant to Top Physics.

I will present the results from this recent [PDF4LHC](#) study, and the resulting new recommendation for combining PDFs sets for [LHC](#) calculations.

In order to put this into context I will summarise continuing updates in PDFs. This includes improvements and recent updates of particular PDF sets due to theory improvements and a variety of new data sets, including most of the up-to-date [LHC](#) data.

I will emphasise particular issues relevant for top physics.

# Recent PDF Updates - effect and treatment of LHC data

ABM12 PDFs S. Alekhin

## The ABM fit ingredients

DATA:

- DIS NC inclusive
- DIS charm production
- DIS  $\mu\mu$  CC production (NOMAD data)
- DIS charmed-hadron CC production (CHORUS data)
- fixed-target DY
- LHC DY distributions (CMS 4.7 1/fb)
- W+charm production (CMS and ATLAS data)

QCD:

- NNLO evolution
- NNLO massless DIS and DY coefficient functions
- NLO+ massive DIS coefficient functions (**FFN scheme**)
  - NLO + NNLO threshold corrections for NC
  - NNLO CC at  $Q \gg m_c$
  - running mass
- NNLO exclusive DY (DYNNLO 1.3 / FEWZ 3.1)
- NNLO inclusive  $t\bar{t}$  production ( pole / running mass )

Deuteron corrections in DIS:

- Fermi motion
- off-shell effects

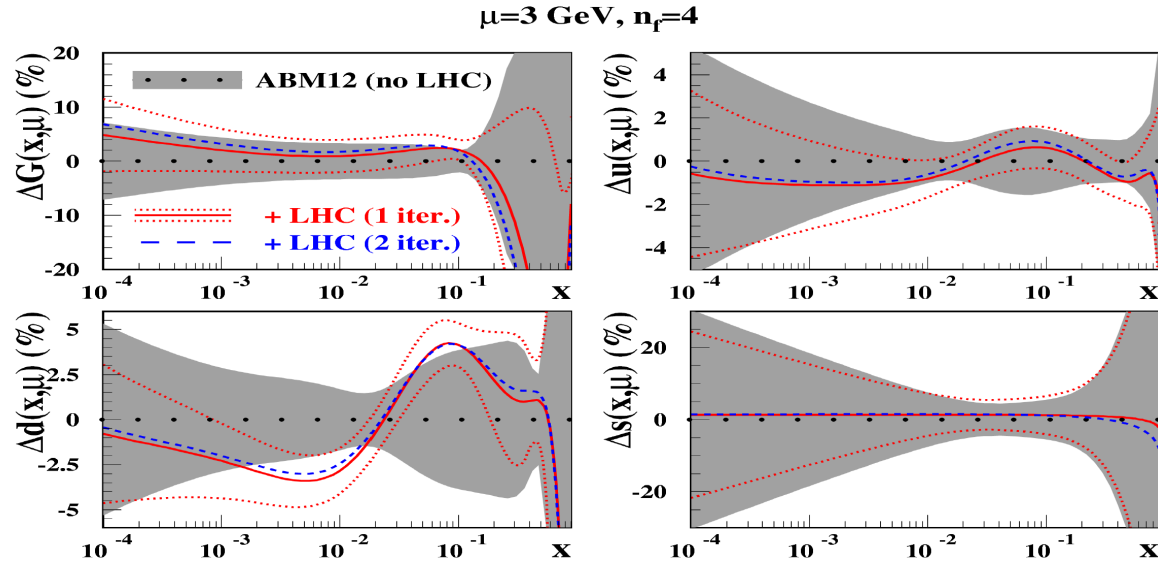
Power corrections in DIS:

- target mass effects
- dynamical twist-4 terms

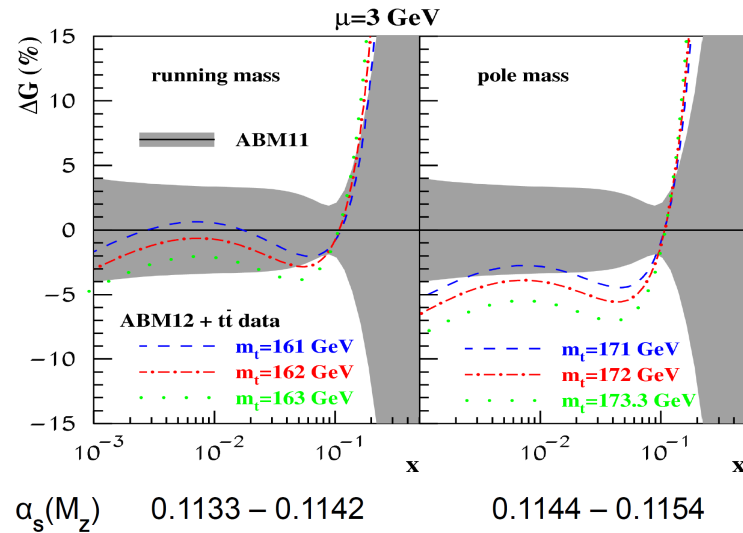
*The jet data are still not included: The NNLO corrections may be as big as 15-20%*

Gehrmann-De Ridder, Gehrmann, Glover, Pires JHEP 1302, 026 (2013) 2

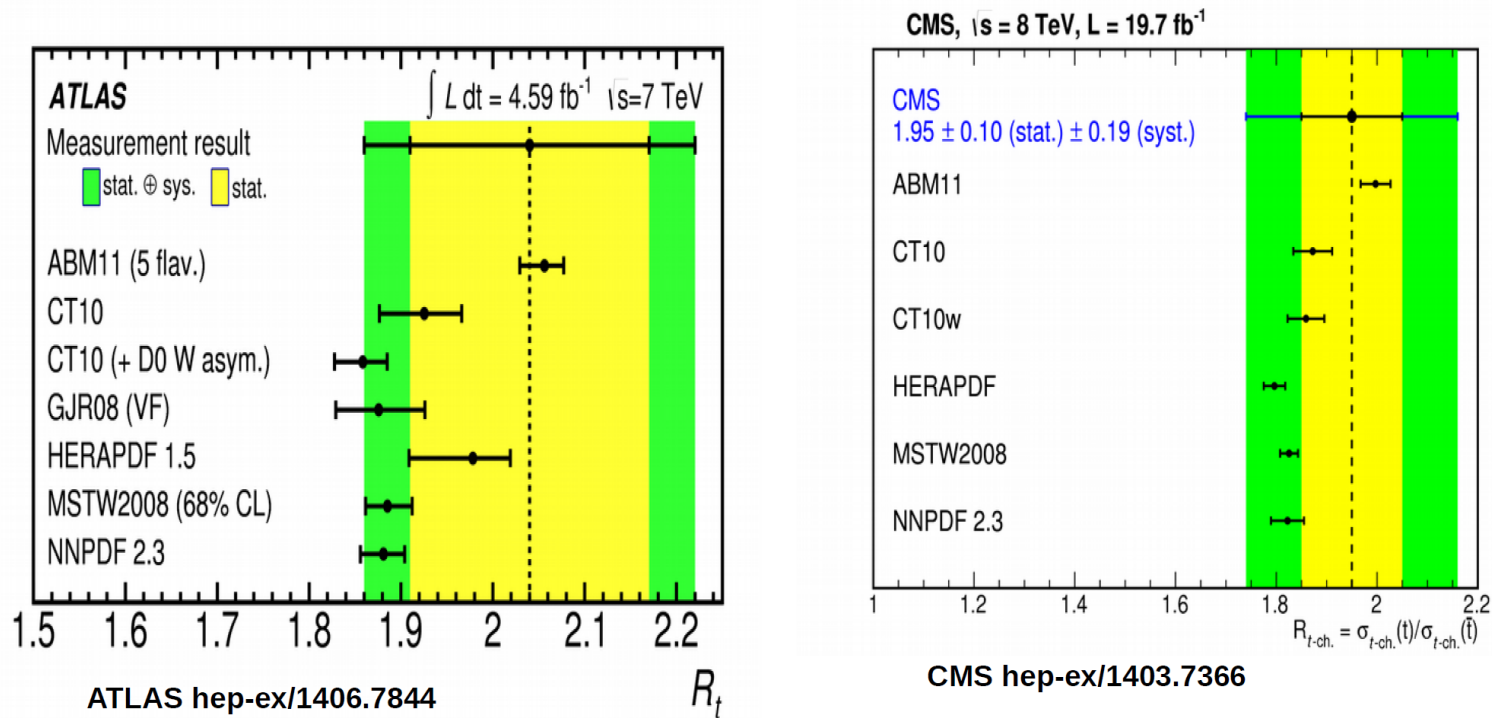
# Impact of the LHC DY data on the PDFs



Variation with  $m_t - \sigma_{t\bar{t}}$  a constraint on gluon.



# t-channel single-top production



- The ratio of t/tbar rates is driven by u/d → suppressed for the “truly global PDFs”

More on this later.

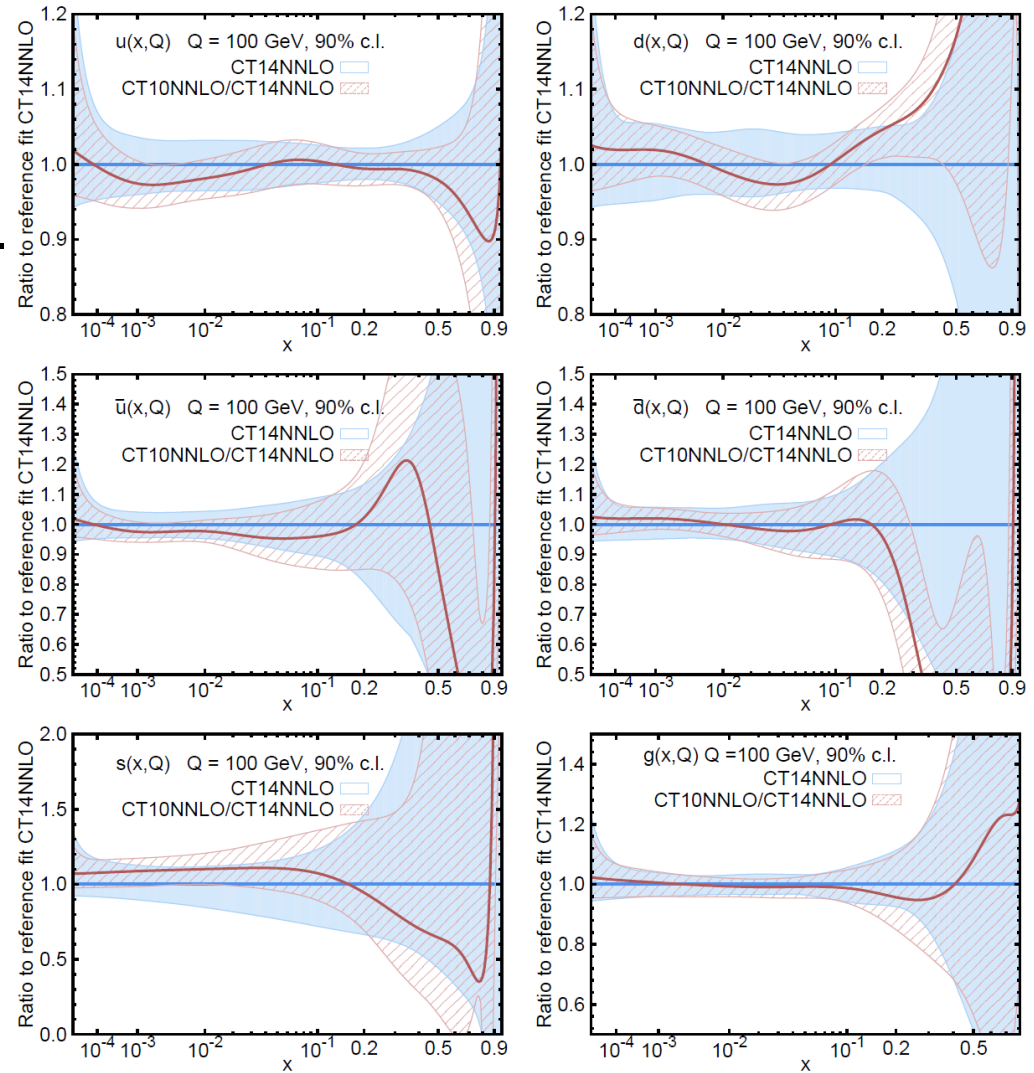
# CT14 PDF sets

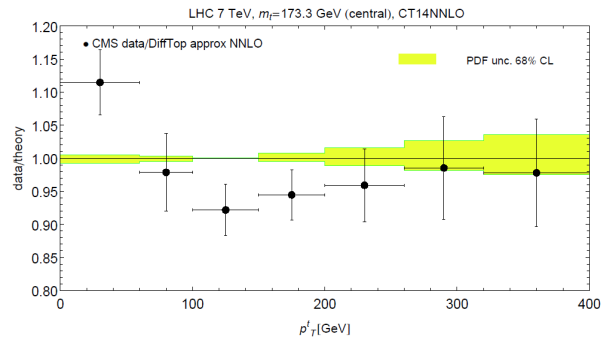
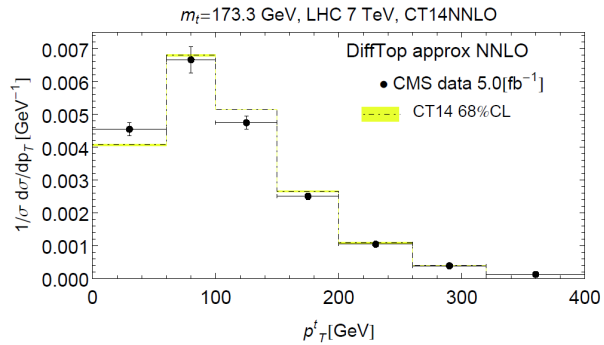
ID#	Experimental data set	$N_{pt}$	$\chi_e^2$	$\chi_e^2/N_{pt}$	$S_n$
101	BCDMS $F_2^p$ [23]	337	384	1.14	1.74
102	BCDMS $F_2^d$ [24]	250	294	1.18	1.89
104	NMC $F_2^d/F_2^p$ [25]	123	133	1.08	0.68
106	NMC $\sigma_{red}^p$ [25]	201	372	1.85	6.89
108	CDHSW $F_2^p$ [26]	85	72	0.85	-0.99
109	CDHSW $F_3^p$ [26]	96	80	0.83	-1.18
110	CCFR $F_2^p$ [27]	69	70	1.02	0.15
111	CCFR $x F_3^p$ [28]	86	31	0.36	-5.73
124	NuTeV $\nu\mu\mu$ SIDIS [29]	38	24	0.62	-1.83
125	NuTeV $\bar{\nu}\mu\mu$ SIDIS [29]	33	39	1.18	0.78
126	CCFR $\nu\mu\mu$ SIDIS [30]	40	29	0.72	-1.32
127	CCFR $\bar{\nu}\mu\mu$ SIDIS [30]	38	20	0.53	-2.46
145	H1 $\sigma_r^b$ [31]	10	6.8	0.68	-0.67
147	Combined HERA charm production [32]	47	59	1.26	1.22
159	HERA1 Combined NC and CC DIS [33]	579	591	1.02	0.37
169	H1 $F_L$ [34]	9	17	1.92	1.7

ID#	Experimental data set	$N_{pt}$	$\chi_e^2$	$\chi_e^2/N_{pt}$	$S_n$
201	E605 Drell-Yan process [36]	119	116	0.98	-0.15
203	E866 Drell-Yan process, $\sigma_{pd}/(2\sigma_{pp})$ [37]	15	13	0.87	-0.25
204	E866 Drell-Yan process, $Q^3 d^2\sigma_{pp}/(dQdx_F)$ [38]	184	252	1.37	3.19
225	CDF Run-1 electron $A_{ch}$ , $p_{T\ell} > 25$ GeV [39]	11	8.9	0.81	-0.32
227	CDF Run-2 electron $A_{ch}$ , $p_{T\ell} > 25$ GeV [40]	11	14	1.24	0.67
234	DØ Run-2 muon $A_{ch}$ , $p_{T\ell} > 20$ GeV [41]	9	8.3	0.92	-0.02
240	LHCb 7 TeV 35 pb <sup>-1</sup> $W/Z$ $d\sigma/dy_\ell$ [42]	14	9.9	0.71	-0.73
241	LHCb 7 TeV 35 pb <sup>-1</sup> $A_{ch}$ , $p_{T\ell} > 20$ GeV [42]	5	5.3	1.06	0.30
260	DØ Run-2 $Z$ rapidity [43]	28	17	0.59	-1.71
261	CDF Run-2 $Z$ rapidity [44]	29	48	1.64	2.13
266	CMS 7 TeV 4.7 fb <sup>-1</sup> , muon $A_{ch}$ , $p_{T\ell} > 35$ GeV [45]	11	12.1	1.10	0.37
267	CMS 7 TeV 840 pb <sup>-1</sup> , electron $A_{ch}$ , $p_{T\ell} > 35$ GeV [46]	11	10.1	0.92	-0.06
268	ATLAS 7 TeV 35 pb <sup>-1</sup> $W/Z$ cross sec., $A_{ch}$ [47]	41	51	1.25	1.11
281	DØ Run-2 9.7 fb <sup>-1</sup> electron $A_{ch}$ , $p_{T\ell} > 25$ GeV [14]	13	35	2.67	3.11
504	CDF Run-2 inclusive jet production [48]	72	105	1.45	2.45
514	DØ Run-2 inclusive jet production [49]	110	120	1.09	0.67
535	ATLAS 7 TeV 35 pb <sup>-1</sup> incl. jet production [50]	90	50	0.55	-3.59
538	CMS 7 TeV 5 fb <sup>-1</sup> incl. jet production [51]	133	177	1.33	2.51

Changes due to new data sets and new parameterisation (Bernstein polynomials - peak at specific  $x$ ).

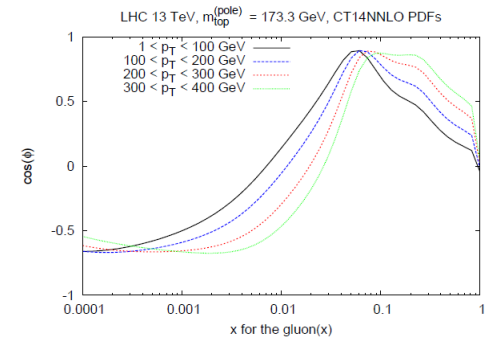
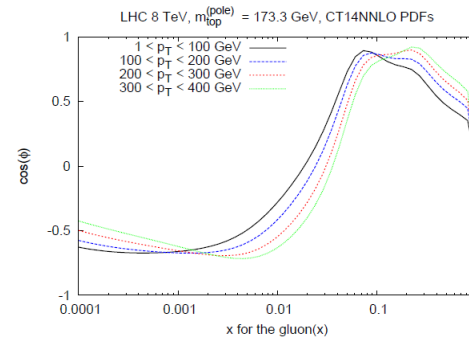
Some significant changes  
(strange smaller due to  
correction in charged  
current cross-section code).





$pp \rightarrow t\bar{t}$ (pb), PDF unc., $\alpha_s = 0.118$	7 TeV	8 TeV	13 TeV
68% C.L. (Hessian)	$177 + 4.8\% - 3.9\%$	$250 + 3.9\% - 3.5\%$	$820 + 2.6\% - 2.7\%$
68% C.L. (LM)		$+4.8\% - 4.6\%$	$+2.9\% - 2.9\%$
$pp \rightarrow t\bar{t}$ (pb), PDF + $\alpha_s$	7 TeV	8 TeV	13 TeV
68% C.L. (Hessian)	$+5.5\% - 4.6\%$	$+5.2\% - 4.4\%$	$+3.6\% - 3.5\%$
68% C.L. (LM)		$+5.1\% - 4.7\%$	$+3.6\% - 3.5\%$

TABLE V: CT14 NNLO total inclusive cross sections for top-quark pair production at LHC center-of-mass energies of 7, 8, 13 TeV.



Do not fit top data but make comparisons.



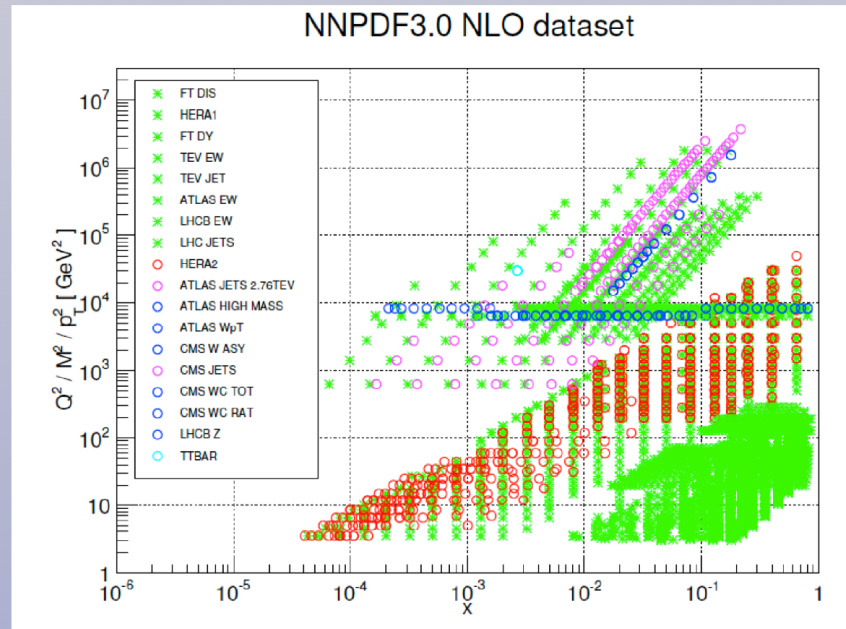
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**HERA structure function data:** HERA-II structure functions from H1 and ZEUS, combined HERA  $F_{2e}$  cross-sections

**LHC jet data:** CMS 7 TeV inclusive jets from 2011, ATLAS 2.76 TeV jets including their correlation with the 7 TeV jet data

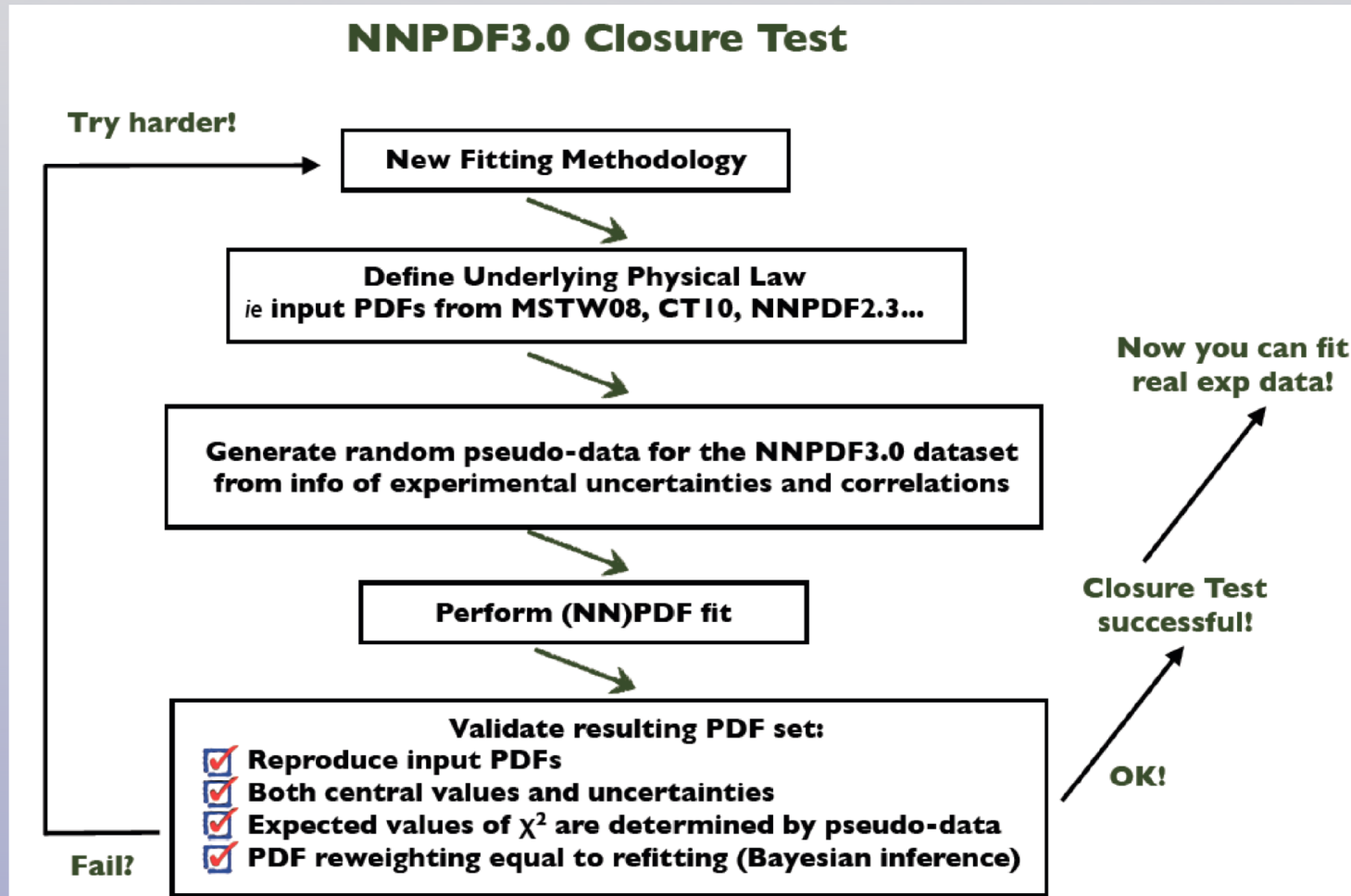
**LHC electroweak data:** CMS muon asymmetries from 2011, LHCb Z rapidity distributions from 2011, CMS W+charm production data, ATLAS and CMS Drell-Yan production, ATLAS W  $p_T$  distributions

**ATLAS and CMS top quark pair production data**



# Closure Testing

Validation and optimization of fitting strategy performed on closure test with known underlying PDF set

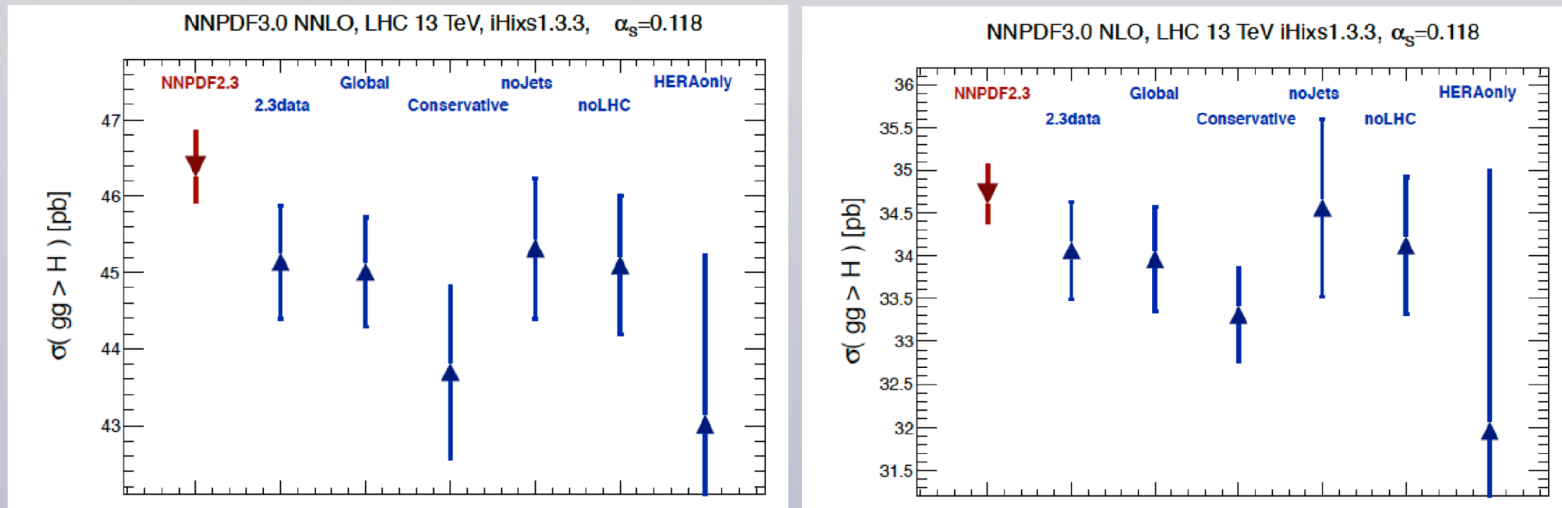


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Juan Rojo

PDF4LHC Meeting, CERN, 16/05/2013

# Higgs production in gluon fusion



- The softer **gg luminosity** in NNPDF3.0 leads to a **decrease in the ggH xsec** at the LHC 13 TeV
- The effect is more marked at NLO and NNLO, though even in the latter the pull is only **P ~1.5**
- The ggH process is different from many other LHC xsecs because there are **no direct experimental constraints on the gluon at  $x \sim 0.01$** , and thus predictions for **ggH** are more sensitive to modifications in the methodology or in the choice of dataset (that indirectly affects  $g(x)$  for  $x \sim 0.01$ )
- In NNPDF3.0, the changes in the **ggH xsec arise mostly from the improved fitting methodology**, validated on the closure tests

## MMHT2014 – Changes in theoretical treatment or procedures.

Continue to use extended parameterisation with Chebyshev polynomials, and freedom in deuteron nuclear corrections – change in  $u_V - d_V$  distribution.

Now use “optimal” GM-VFNS choice which is smoother near to heavy flavour transition points (more so at NLO)

Errors multiplicative not additive. Using  $\chi^2$  definition

$$\chi^2 = \sum_{i=1}^{N_{pts}} \left( \frac{D_i + \sum_{k=1}^{N_{corr}} r_k \sigma_{k,i}^{corr} - T_i}{\sigma_i^{uncorr}} \right)^2 + \sum_{k=1}^{N_{corr}} r_k^2,$$

where  $\sigma_{k,i}^{corr} = \beta_{k,i}^{corr} T_i$  and  $\beta_{k,i}^{corr}$  are the percentage error. Additive would use  $\sigma_{k,i}^{corr} = \beta_{k,i}^{corr} D_i$ .

Strange branching ratio. Now avoid those determined by fits to dimuon data relying on PDF input. Also apply error which feeds into PDFs. Use  $B_\mu = 0.092 \pm 10\%$  from [hep-ex/9708014](http://hep-ex/9708014).

Update in nuclear corrections ([de Florian et al](#)).

# Changes in data sets.

Replacement of HERA run I neutral and charged current data from HERA and ZEUS with combined data set.

Inclusion of HERA combined data on  $F_2^c(x, Q^2)$  and HERA  $F_L(x, Q^2)$  measurements.

Inclusion of CDF  $W$ -asymmetry data, D0 electron asymmetry and D0 muon asymmetry data.

LHC data on  $W, Z$

LHC jet data at NLO

Data set	LO	NLO	NNLO
BCDMS $\mu p F_2$ [125]	162 / 153	176 / 163	173 / 163
BCDMS $\mu d F_2$ [19]	140 / 142	143 / 151	143 / 151
NMC $\mu p F_2$ [20]	141 / 115	132 / 123	123 / 123
NMC $\mu d F_2$ [20]	134 / 115	115 / 123	108 / 123
NMC $\mu n / \mu p$ [21]	122 / 137	131 / 148	127 / 148
E665 $\mu p F_2$ [22]	59 / 53	60 / 53	65 / 53
E665 $\mu d F_2$ [22]	52 / 53	52 / 53	60 / 53
SLAC $ep F_2$ [23, 24]	21 / 18	31 / 37	31 / 37
SLAC $ed F_2$ [23, 24]	13 / 18	30 / 38	26 / 38
NMC/BCDMS/SLAC/HERA $F_L$ [20, 125, 24, 63, 64, 65]	113 / 53	68 / 57	63 / 57
E866/NuSea $pp$ DY [88]	229 / 184	221 / 184	227 / 184
ES66/NuSea $pd/pp$ DY [89]	29 / 15	11 / 15	11 / 15
NuTeV $\nu N F_2$ [29]	35 / 49	39 / 53	38 / 53
CHORUS $\nu N F_2$ [30]	25 / 37	26 / 42	28 / 42
NuTeV $\nu N xF_3$ [29]	49 / 42	37 / 42	31 / 42
CHORUS $\nu N xF_3$ [30]	35 / 28	22 / 28	19 / 28
CCFR $\nu N \rightarrow \mu\mu X$ [31]	65 / 86	71 / 86	76 / 86
NuTeV $\nu N \rightarrow \mu\mu X$ [31]	53 / 40	38 / 40	43 / 40
HERA $e^+p$ NC 820 GeV [61]	125 / 78	93 / 78	89 / 78
HERA $e^+p$ NC 920 GeV [61]	479 / 330	402 / 330	373 / 330
HERA $e^-p$ NC 920 GeV [61]	158 / 145	129 / 145	125 / 145
HERA $e^+p$ CC [61]	41 / 34	34 / 34	32 / 34
HERA $e^-p$ CC [61]	29 / 34	23 / 34	21 / 34
HERA $ep F_2^{\text{charm}}$ [62]	105 / 52	72 / 52	82 / 52
H1 99-00 $e^+p$ incl. jets [126]	77 / 24	14 / 24	—
ZEUS incl. jets [127, 128]	140/60	45 / 60	—
DØ II $p\bar{p}$ incl. jets [119]	125 / 110	116 / 110	119 / 110
CDF II $p\bar{p}$ incl. jets [118]	78 / 76	63 / 76	59 / 76
CDF II $W$ asym. [66]	55 / 13	32 / 13	30 / 13
DØ II $W \rightarrow \nu e$ asym. [67]	47 / 12	28 / 12	27 / 12
DØ II $W \rightarrow \nu \mu$ asym. [68]	16 / 10	19 / 10	21 / 10
DØ II $Z$ rap. [90]	34 / 28	16 / 28	16 / 28
CDF II $Z$ rap. [70]	95 / 28	36 / 28	40 / 28
ATLAS $W^+, W^-, Z$ [10]	94/30	38/30	39/30
CMS $W$ asymm $p_T > 35$ GeV [9]	10/11	7/11	9/11
CMS asymm $p_T > 25$ GeV, 30 GeV [77]	7/24	8/24	10/24
LHCb $Z \rightarrow e^+e^-$ [79]	76/9	13/9	20/9
LHCb $W$ asymm $p_T > 20$ GeV [78]	27/10	12/10	16/10
CMS $Z \rightarrow e^+e^-$ [84]	46/35	19/35	22/35
ATLAS high-mass Drell-Yan [83]	42/13	21/13	17/13
CMS double diff. Drell-Yan [86]	—	372/132	149/132
Tevatron, ATLAS, CMS $\sigma_{t\bar{t}}$ [91]–[97]	53/13	7/13	8/13
ATLAS jets (2.76 TeV+7 TeV) [108, 107]	162/116	106/116	—
CMS jets (7 TeV) [106]	150/133	138/133	—
All data sets	<b>3706 / 2763</b>	<b>3267 / 2996</b>	<b>2717 / 2663</b>

Table 5: The values of  $\chi^2/N_{\text{pts}}$ , for the data sets included in the global fit. For the NuTeV  $\nu N \rightarrow \mu\mu X$  data, the number of degrees of freedom is quoted instead of  $N_{\text{pts}}$ , since smearing effects mean nearby points are highly correlated. The details of corrections to data, kinematic cuts applied and definitions of  $\chi^2$  are contained in the text.

## MMHT2014 PDFs compared to MSTW2008 PDFs.

Use same “dynamic tolerance” prescription to determine eigenvectors.

Typical tolerance  $T = \Delta\chi^2 \sim 10$ .

We now have **25** eigenvector pairs, rather than the **20** in **MSTW** or even the **23** in **MMSTWW**.

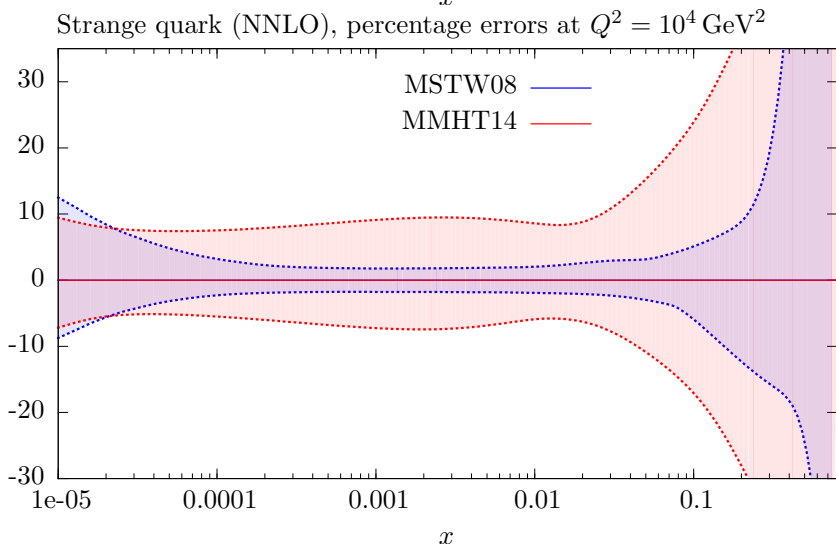
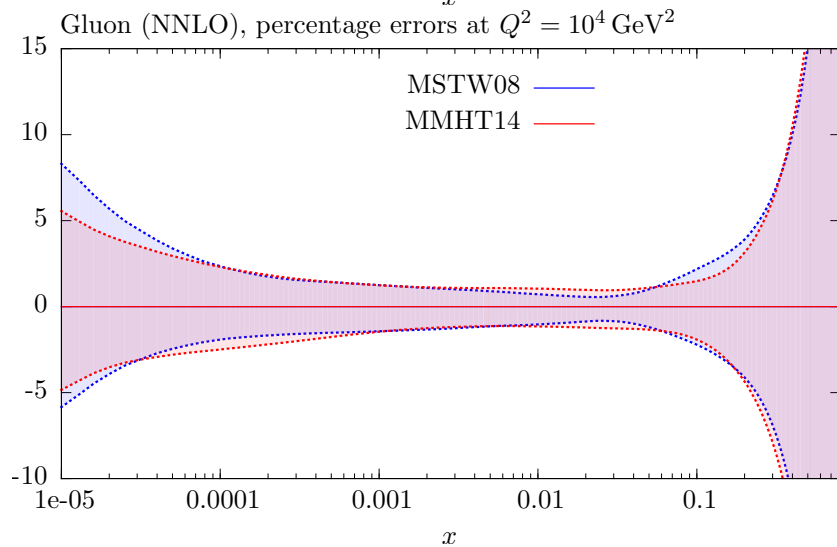
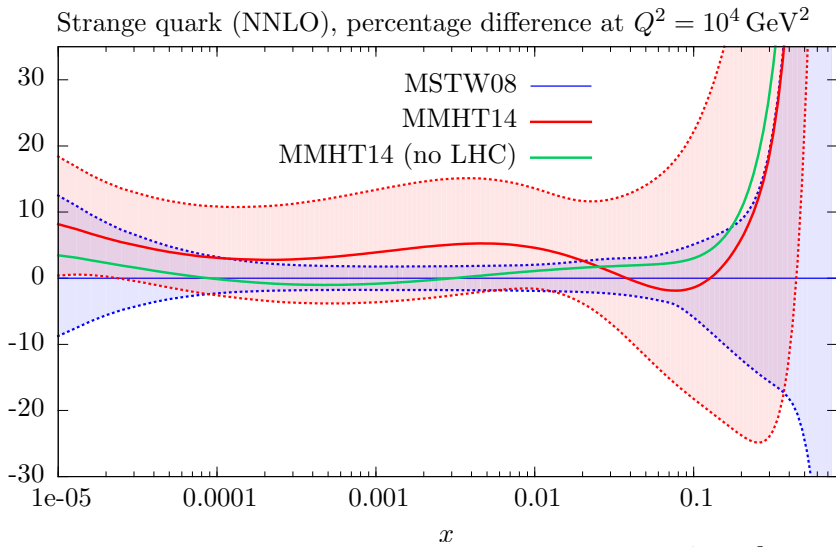
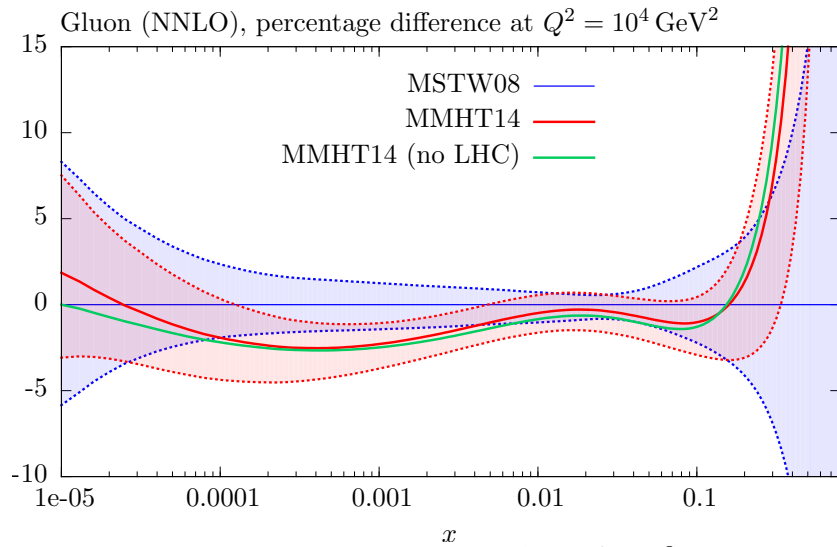
Eigenvector sets made available for  $\alpha_S(M_Z^2) = 0.135$  (**LO**),  $\alpha_S(M_Z^2) = 0.118, 0.120$  (**NLO**) and  $\alpha_S(M_Z^2) = 0.118$  (**NNLO**)

$\alpha_S(m_Z^2)$  coming out similar to **2008** fit. Still a **NLO/NNLO** difference. Both fairly compatible with global average, i.e.

**NLO** –  $\alpha_S(m_Z^2) = 0.1201$ , **NNLO** –  $\alpha_S(m_Z^2) = 0.1172$ .

$\alpha_S(m_Z^2)^{\text{world}} = 0.1186 \pm 0.0006$ . Decide to present **MMHT2014** PDFs with eigenvectors at round value of  $\alpha_S(m_Z^2) = 0.118$  at **NNLO** and at **NLO** also at  $\alpha_S(m_Z^2) = 0.120$ .

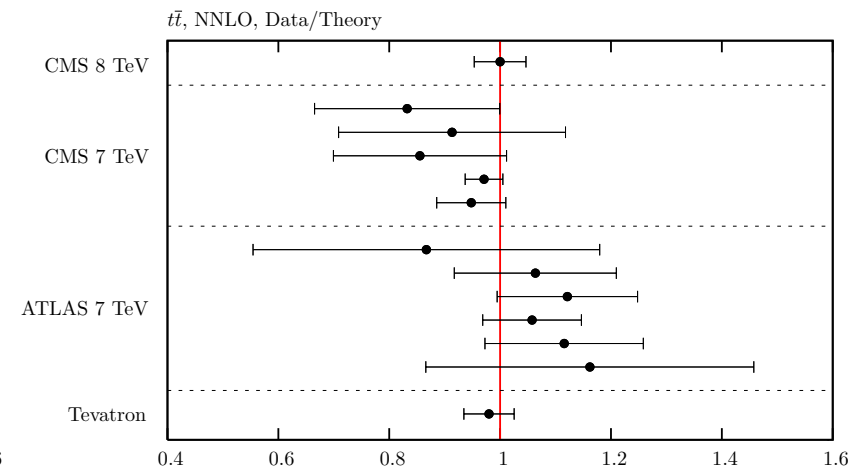
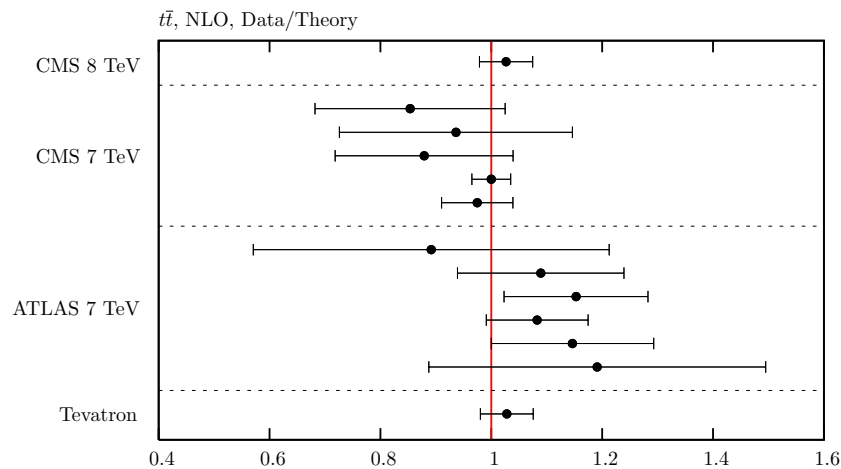
# Comparison of PDFs at NNLO



Change in NNLO PDFs from all updates. Almost no change in light sea quarks.

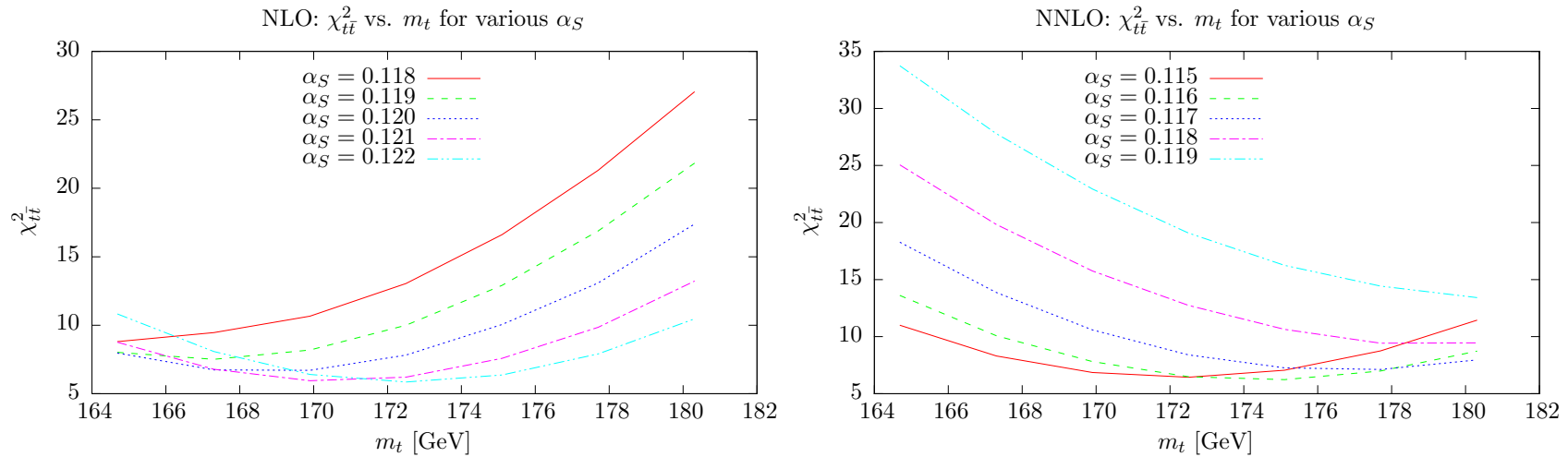
## LHC data on $t\bar{t}$

Include data on  $\sigma_{t\bar{t}}$  from Tevatron (combined cross section measurement from D0 and CDF), and all published data from ATLAS and CMS for 7TeV and one point at 8TeV. Use  $m_t = 172.5$  GeV (value used in Tevatron combination) with an error of 1 GeV, with  $\chi^2$  penalty applied. Predictions and fit good, with NLO preferring masses slightly below  $m_t = 172.5$  GeV and NNLO masses slightly above.





Global  $\chi^2$  depends on  $m_t$  but minimises at very similar  $\alpha_S(M_Z^2)$  for a rather wide range.



However, fit quality to  $\sigma_{t\bar{t}}$  data alone very sensitive to  $m_t$  and  $\alpha_S(M_Z^2)$  interplay.

Values determined by free best fit using  $m_t = 172.5 \text{ GeV} \pm 1 \text{ GeV}$  are  $m_t(\text{NLO, NNLO}) = 171.7, 174.2 \text{ GeV}$ , as opposed to world average of  $m_t = 173.34 \pm 0.76 \text{ GeV}$ .

Be conservative on  $\alpha_S(M_Z^2)$  constraints direct from  $\sigma_{t\bar{t}}$ , but similar constraints from other sets.

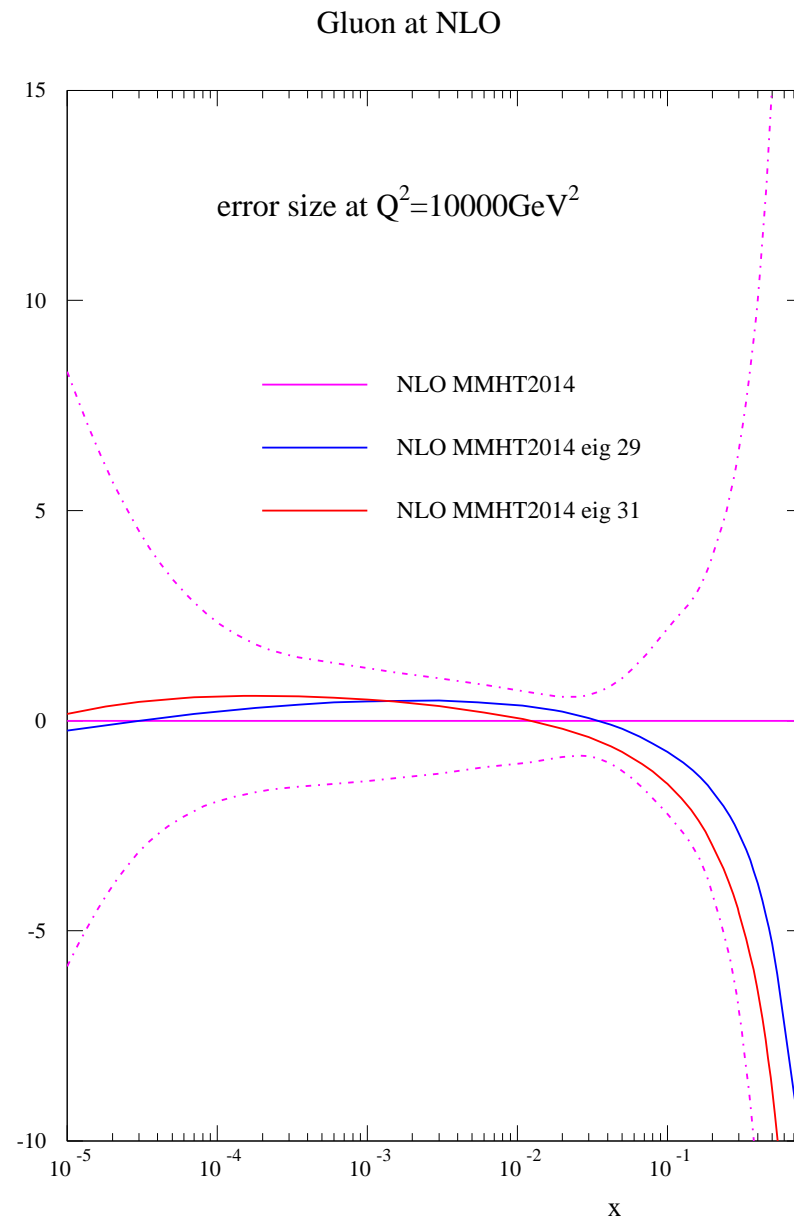
In the **NLO** fit the inclusive  $t\bar{t}$  cross section does not constrain any eigenvectors. Best fit  $m_t = 171.7\text{GeV}$  (lower if  $\alpha_S(M_Z^2) = 0.118$ ).

Nearly constrains eigenvector number **29** and **31**.

Both correspond to decreased gluon at high  $x$  only.

**29** also corresponds to lower high- $x$  sea and constrained mainly by **NuTeV**  $F_3(x, Q^2)$  data.

**31** primarily constrained by **CDF** jet data.



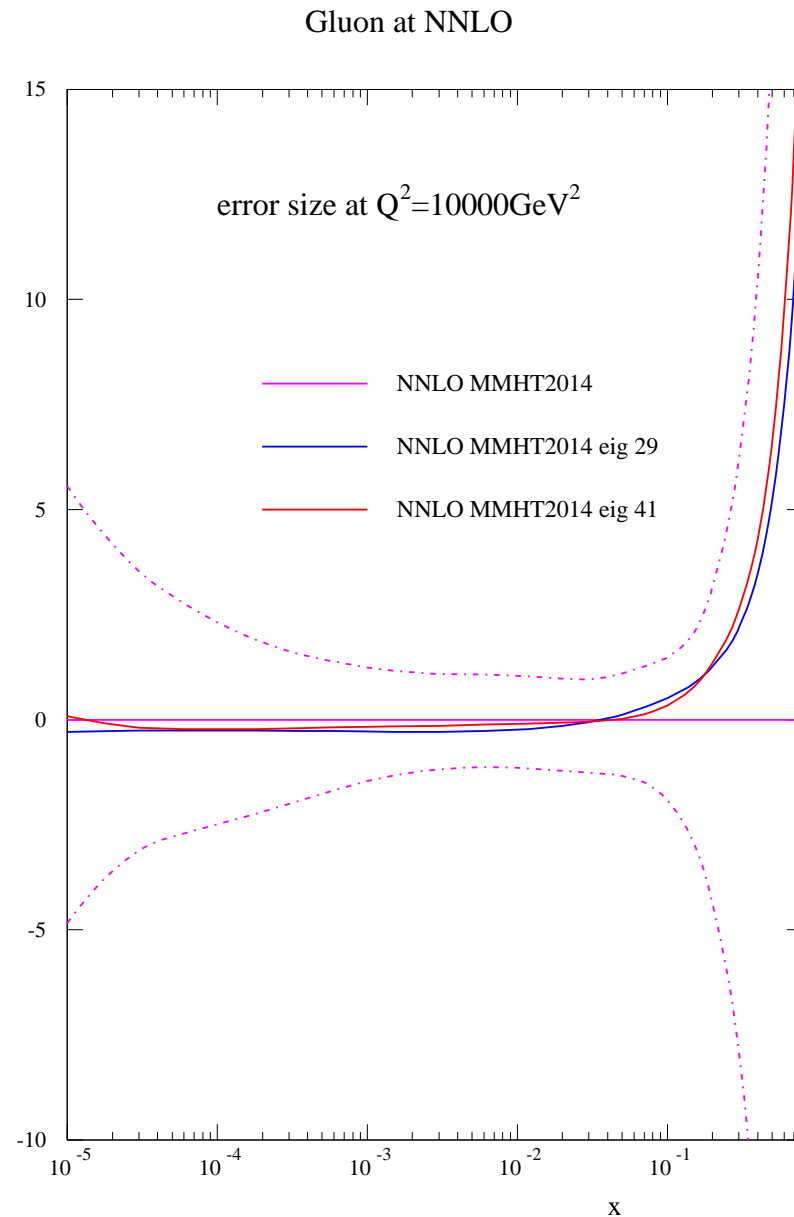
In the NNLO fit the inclusive  $t\bar{t}$  cross section constrains one eigenvector.

At NNLO preferred  $m_t = 174.1\text{GeV}$ .

Constrains eigenvector number 29 and (nearly) 41.

Both correspond to increased gluon at high  $x$  only.

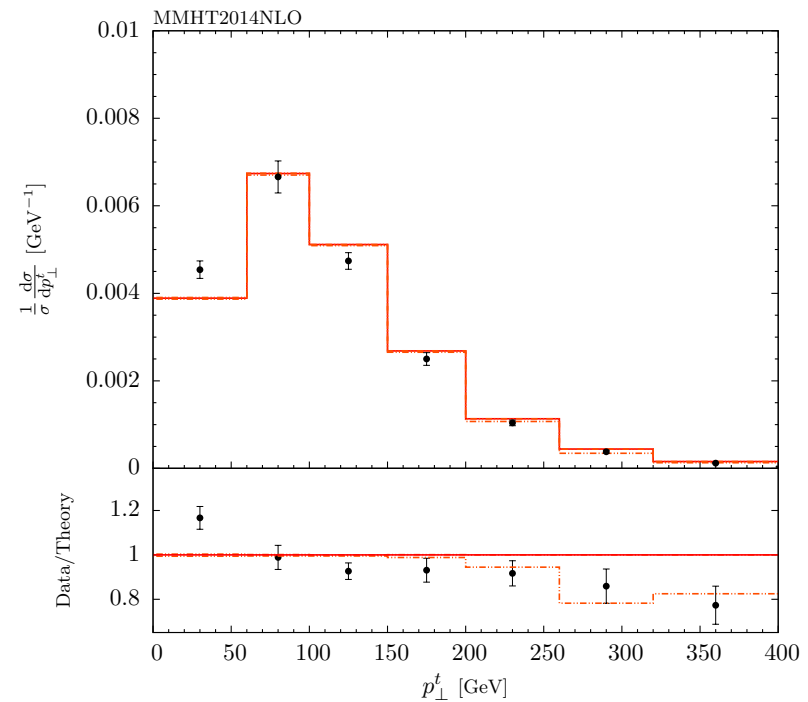
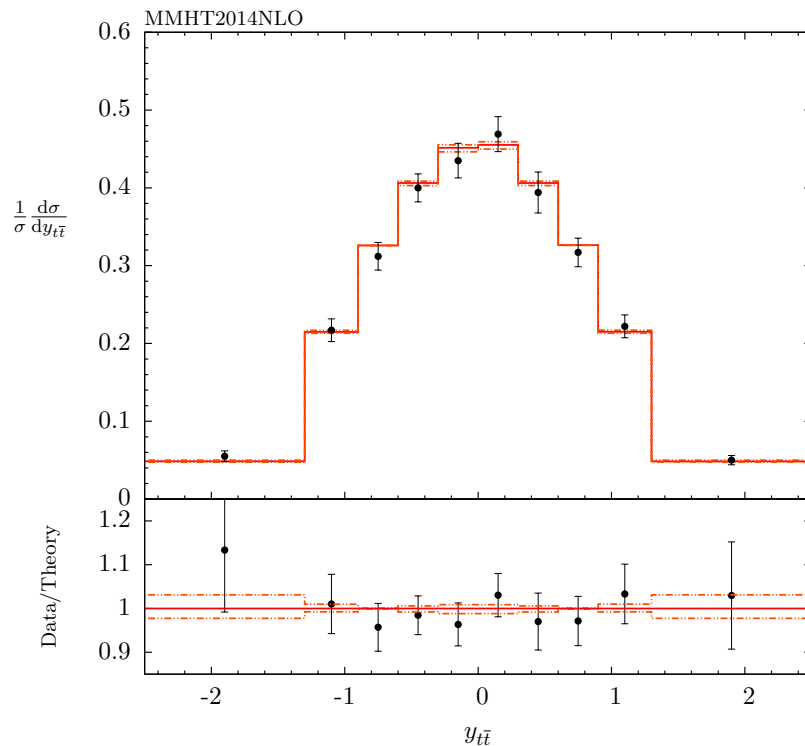
41 also corresponds to strange normalisation and constrained also by ATLAS  $W, Z$  data.



## New data sets for fit – $t\bar{t}$ differential distributions.

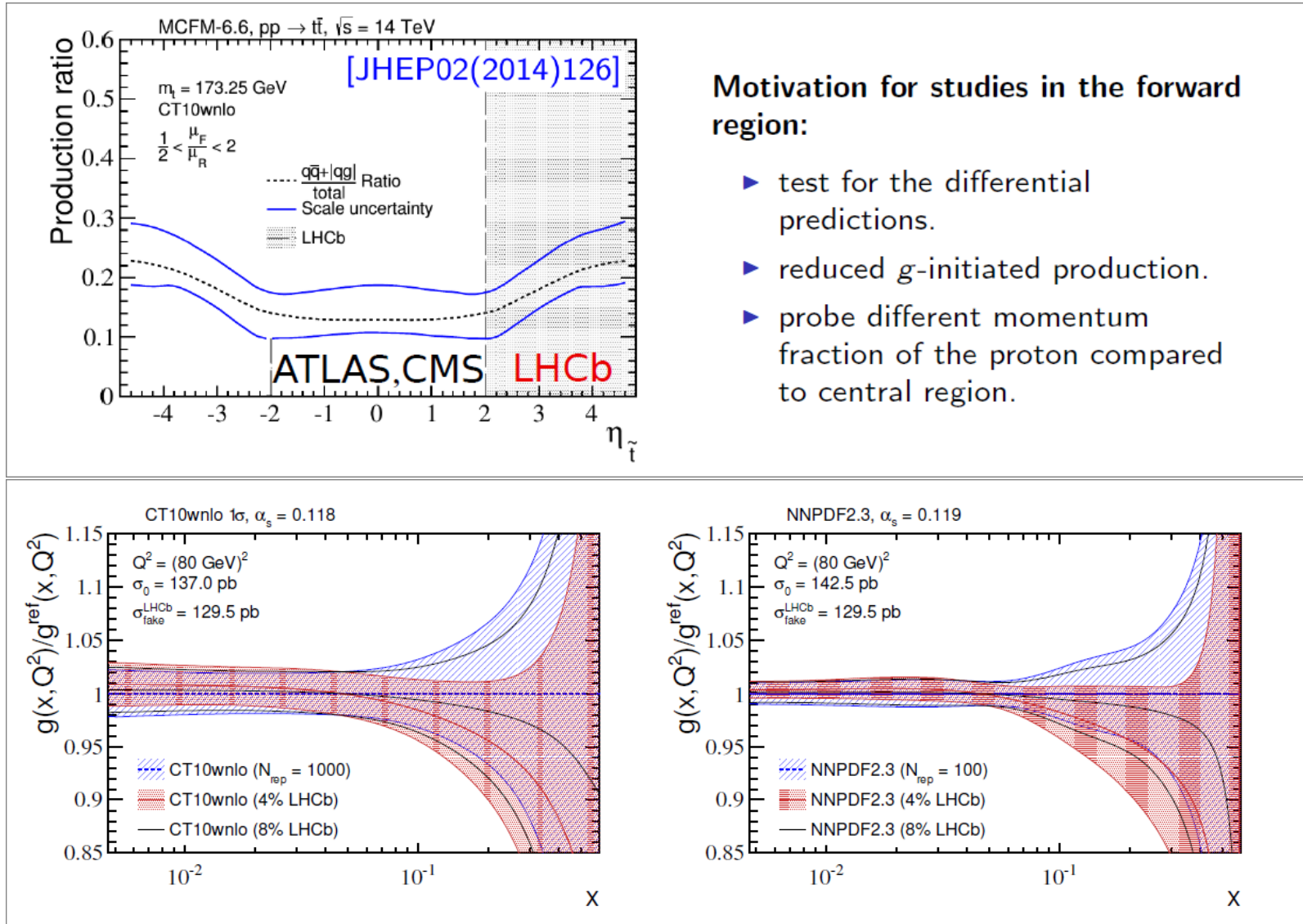
Variety of data sets not in PDF determination as they did not meet cut-off date and/or missing NNLO corrections.

For example, differential  $t\bar{t}$  production (show CMS below).  $y_{t\bar{t}}$  distribution at NLO very good,  $p_t$  distribution off in shape ( $m_{t\bar{t}}$  somewhere in between).



Interesting to see NNLO corrections.

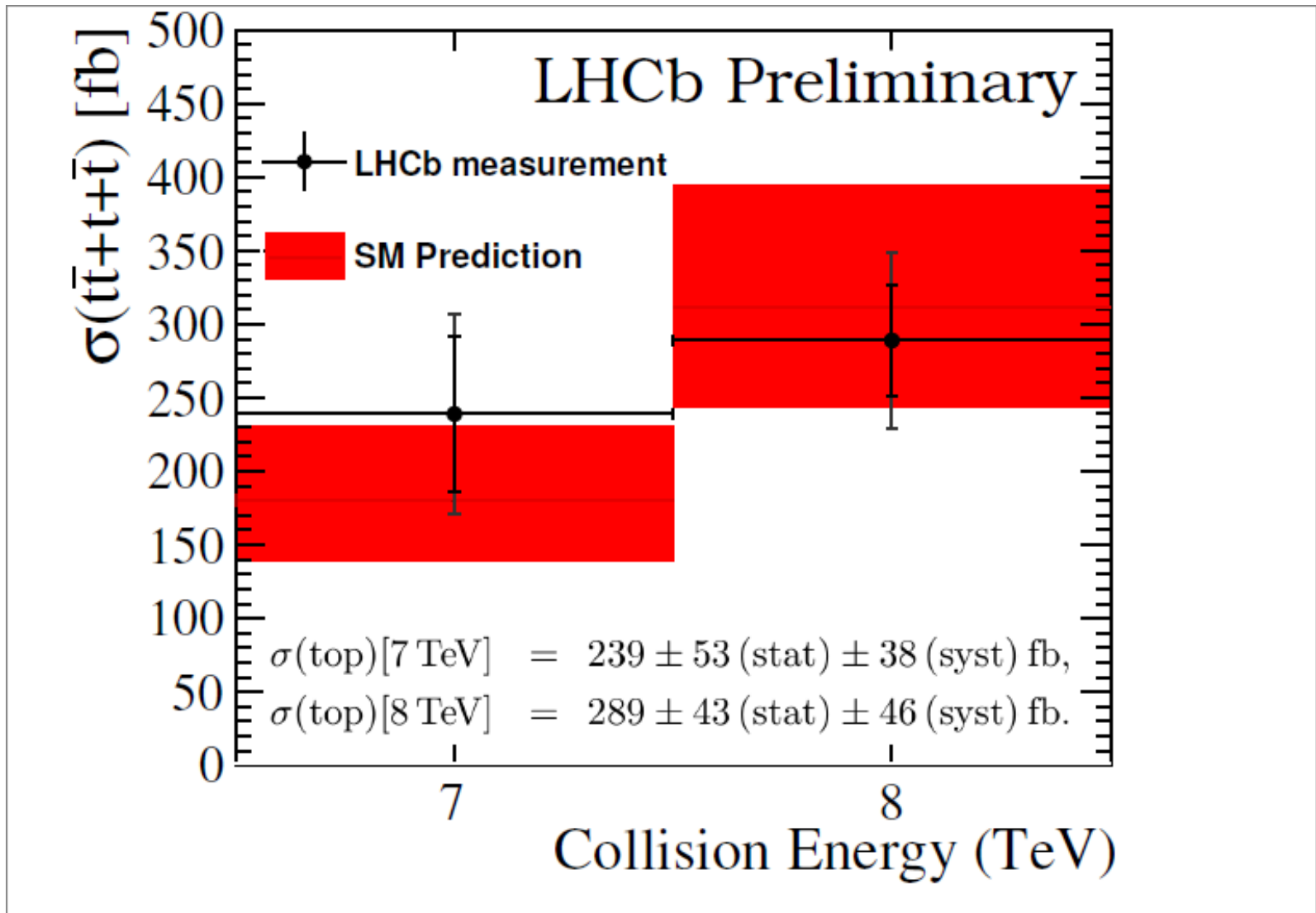
# LHCb Measurement.



Motivation for studies in the forward region:

- ▶ test for the differential predictions.
- ▶ reduced  $g$ -initiated production.
- ▶ probe different momentum fraction of the proton compared to central region.

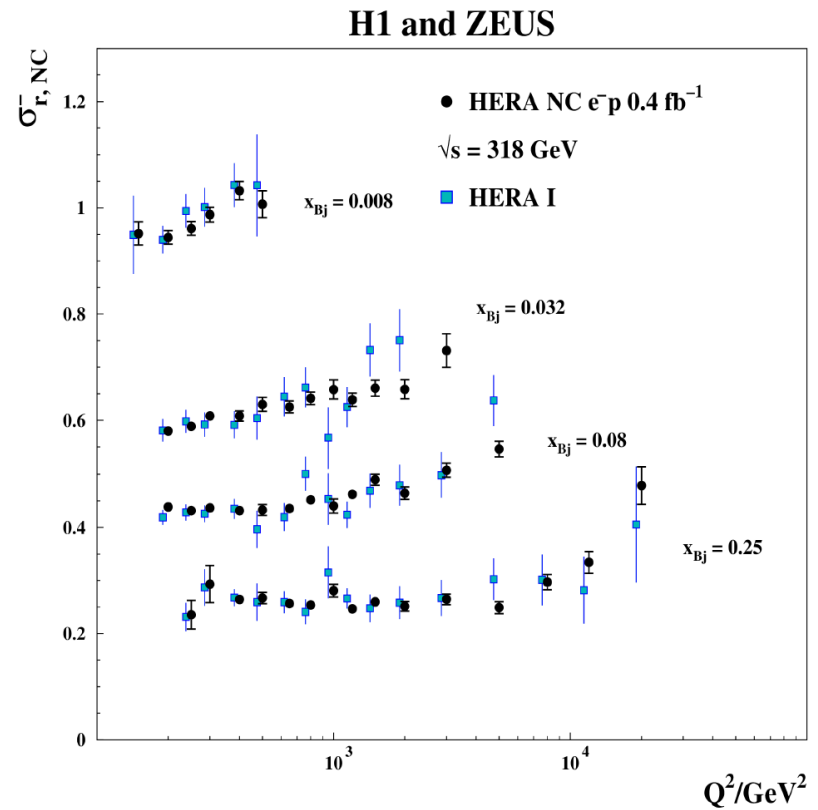
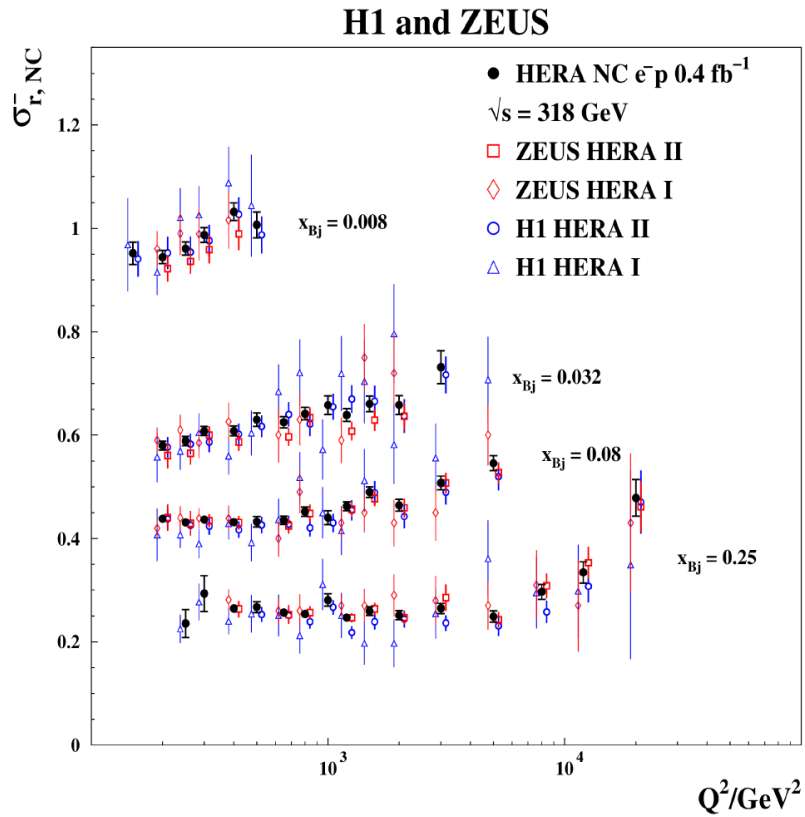
More impact if in some disagreement with expectation. **Gauld**



First measurement in good agreement with theory.

# HERA+II combination data.

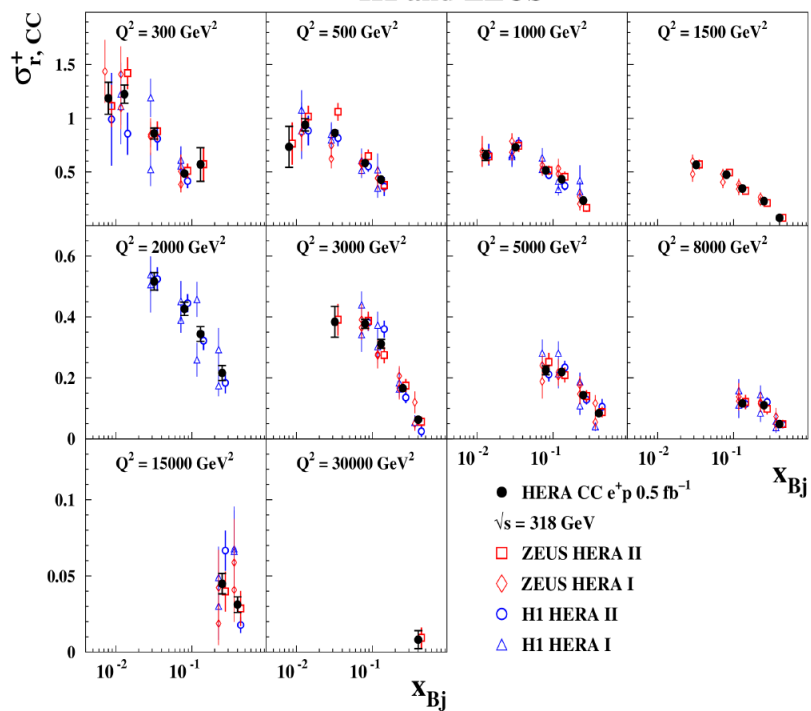
## Averaged cross sections: NC e-p



# Averaged cross sections: CC $e^\pm p$

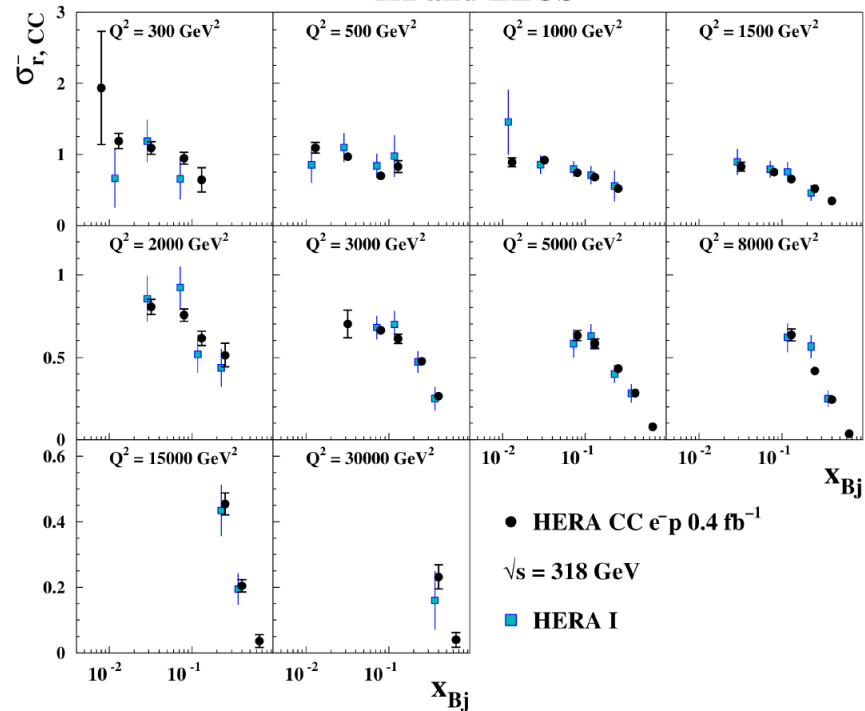
## CC $e^+p$

### H1 and ZEUS



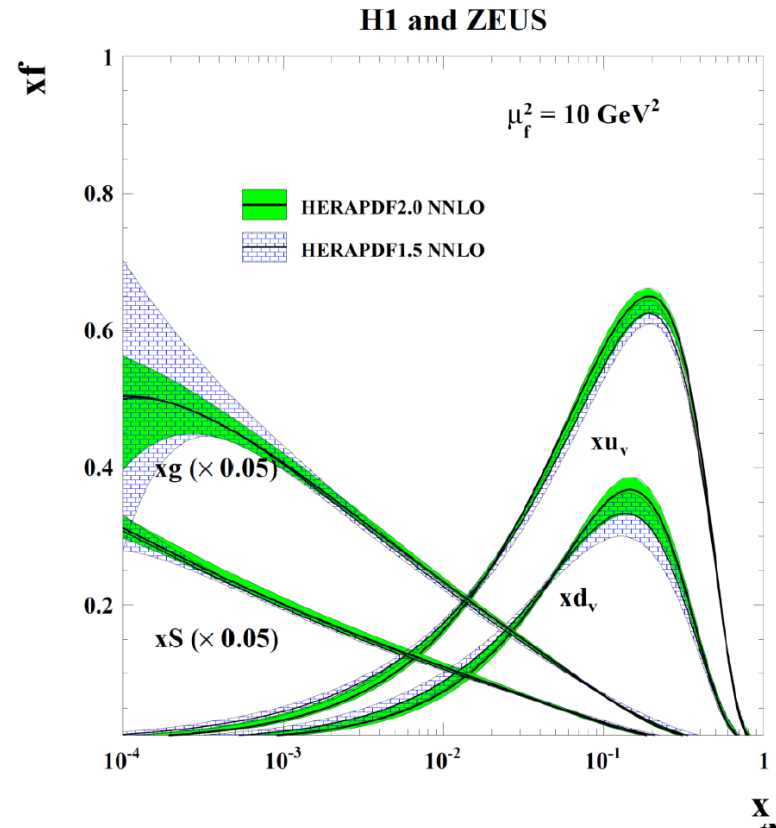
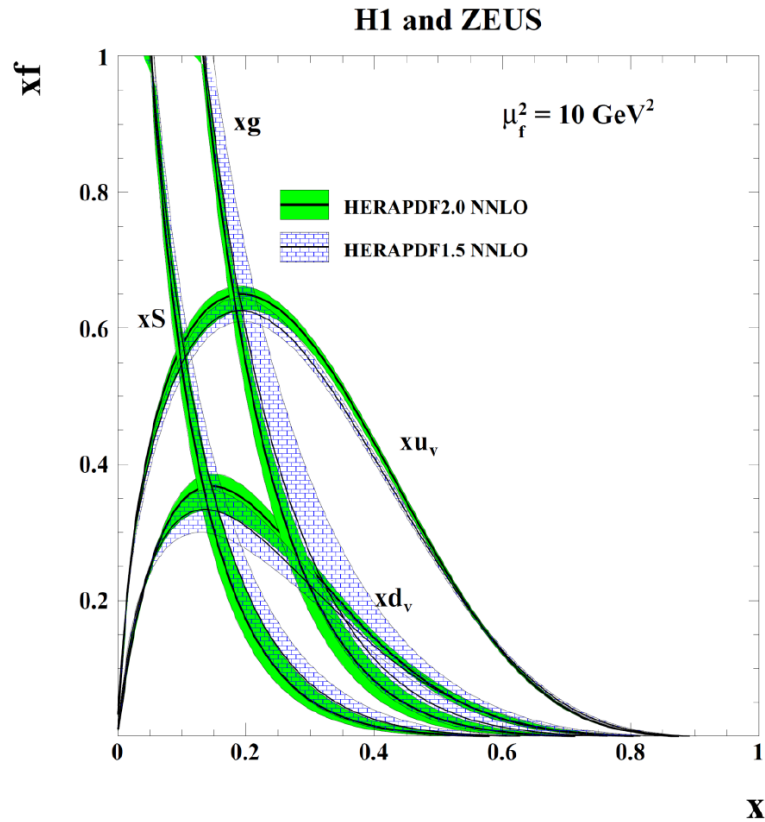
## CC $e^-p$

### H1 and ZEUS





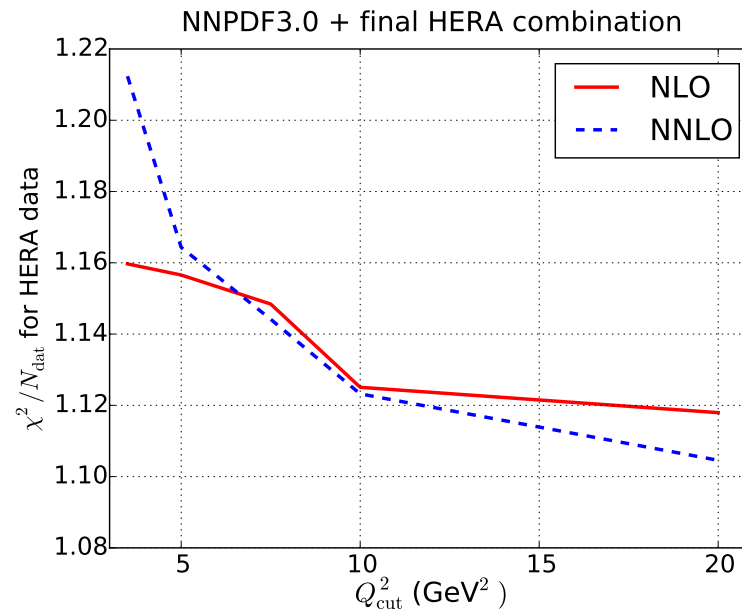
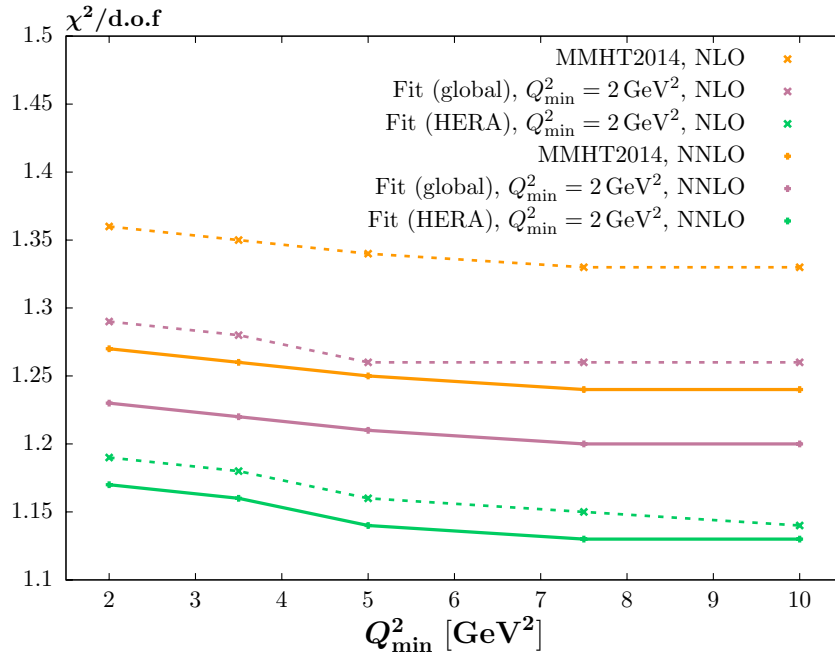
Compare HERAPDF2.0 to HERAPDF1.5 at NNLO



Make HERAPDF PDFs more precise, but in general a bit further from other PDFs in some places, e.g high- $x$  up quark.

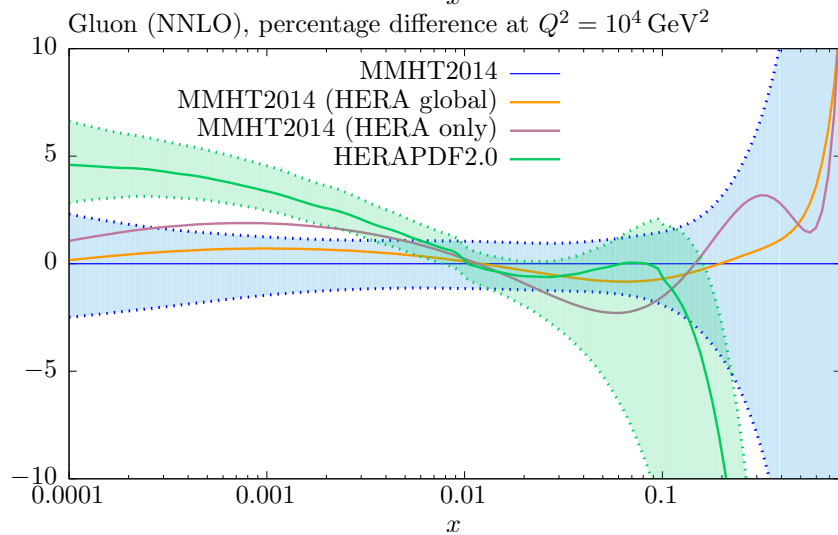
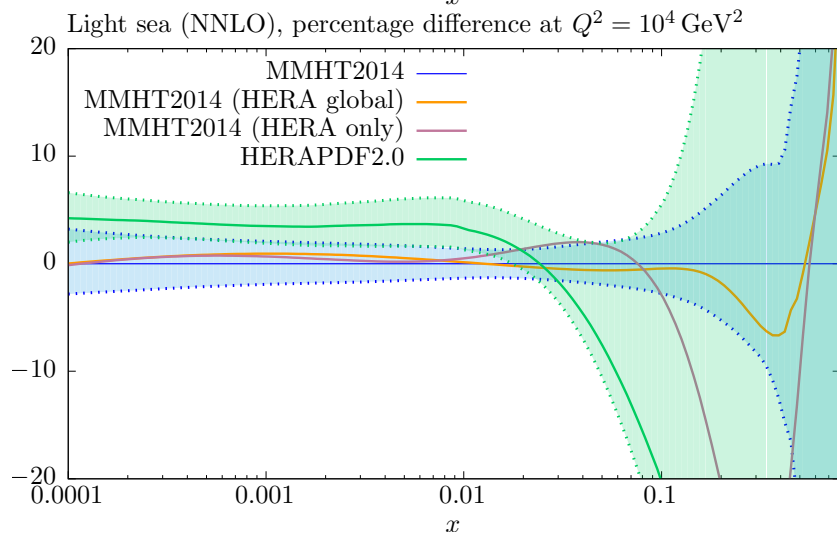
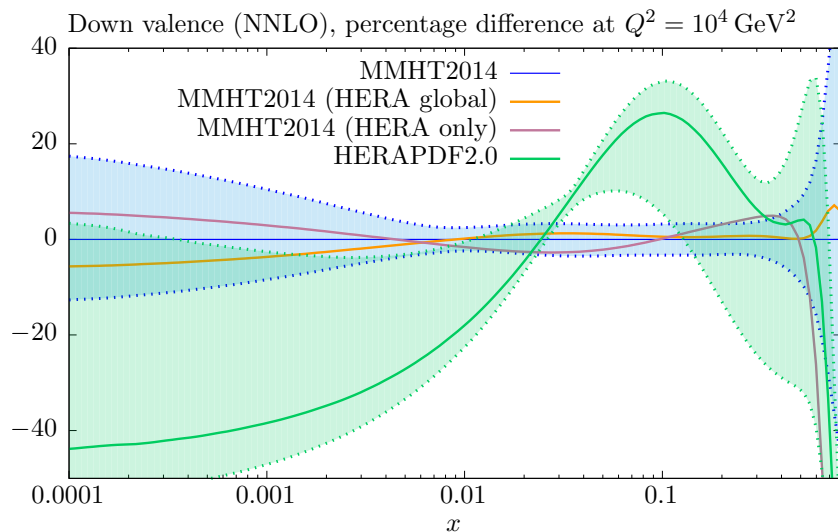
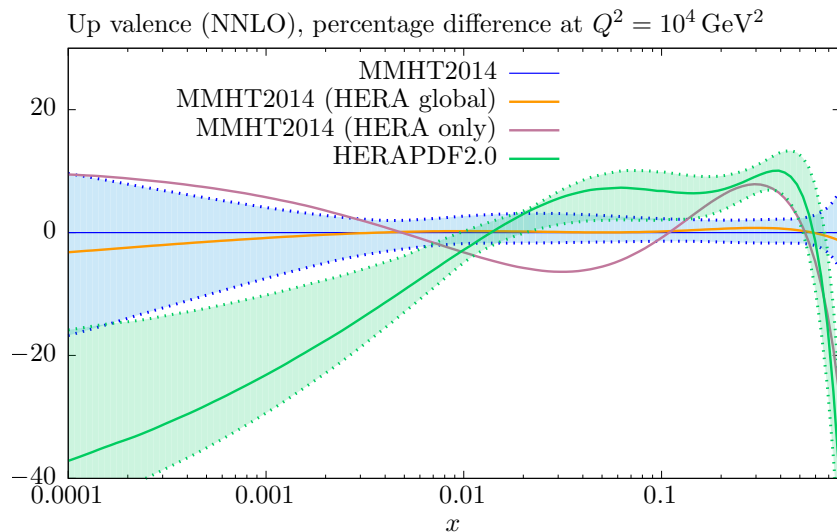
## HERA II Combined data in other PDFs

Good fits possible with little deterioration for other data seen for both **MSTW** and **NNPDF**



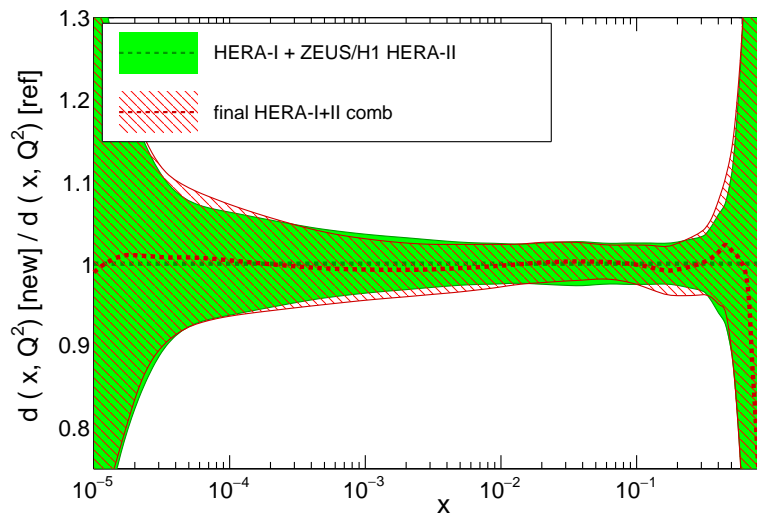
Also look at effect of changing the  $Q^2$  cut, at both **NLO** and **NNLO**

Improvement in  $\chi^2$  with  $Q_{\min}^2$ , but other than **NNPDF** at **NNLO** not dramatic.

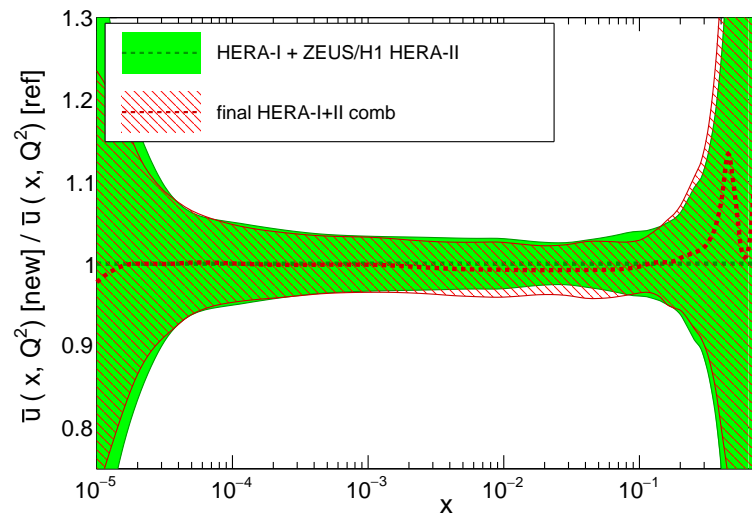


HERA II modified PDFs very well within MMHT2014 uncertainties.  
 PDFs from HERA II data only fit in some ways similar to HERAPDF2.0.  
 Predictions for e.g.  $gg \rightarrow H$  change by  $< 0.2\%$  for full range of LHC energies.

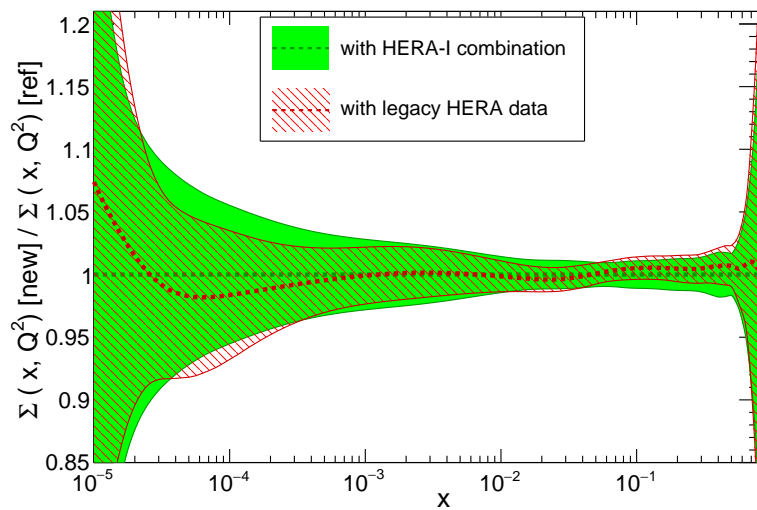
NNPDF3.0 NLO Global,  $Q^2=10^2 \text{ GeV}^2$



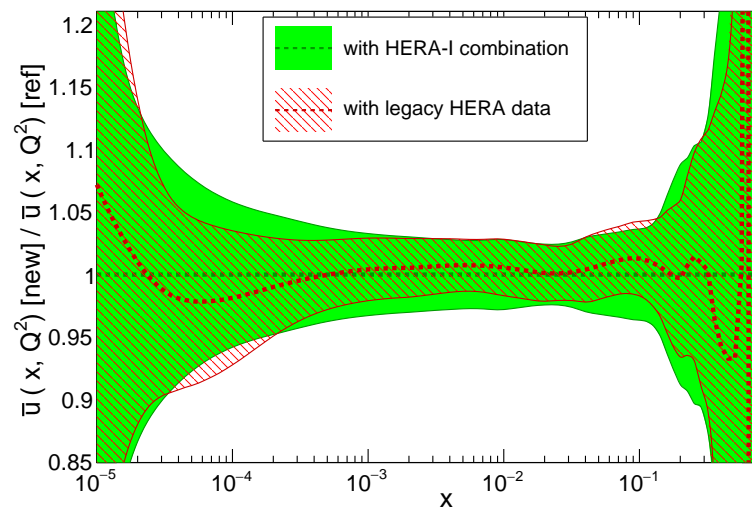
NNPDF3.0 NLO Global,  $Q^2=10^2 \text{ GeV}^2$



NNPDF3.0 NNLO Global,  $Q^2=10^2 \text{ GeV}^2$

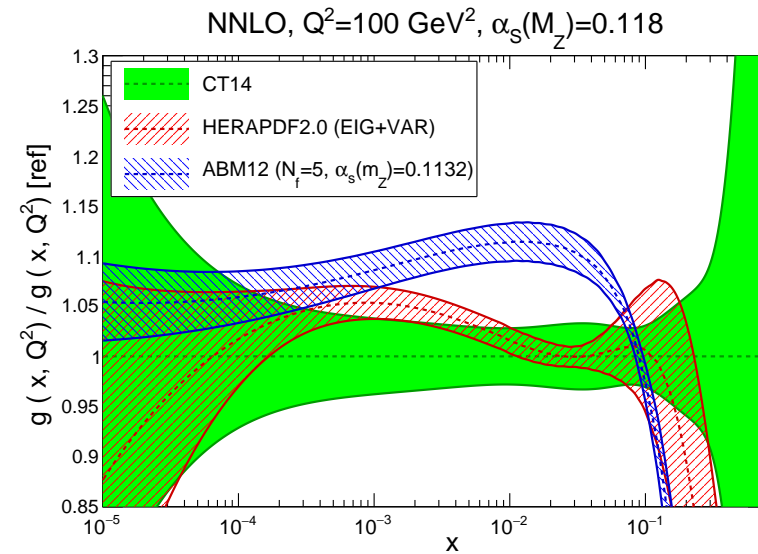
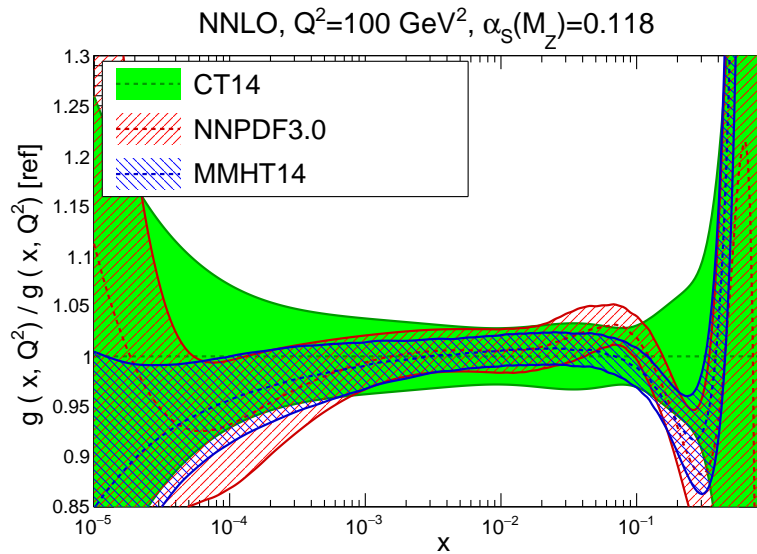
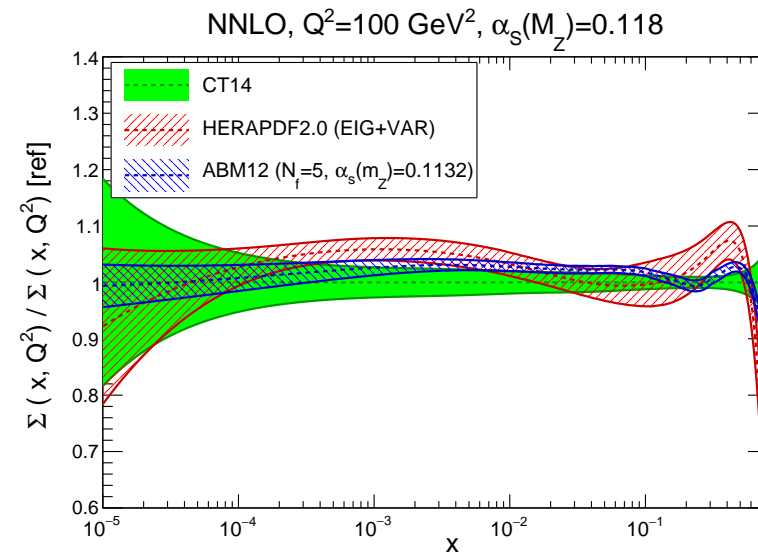
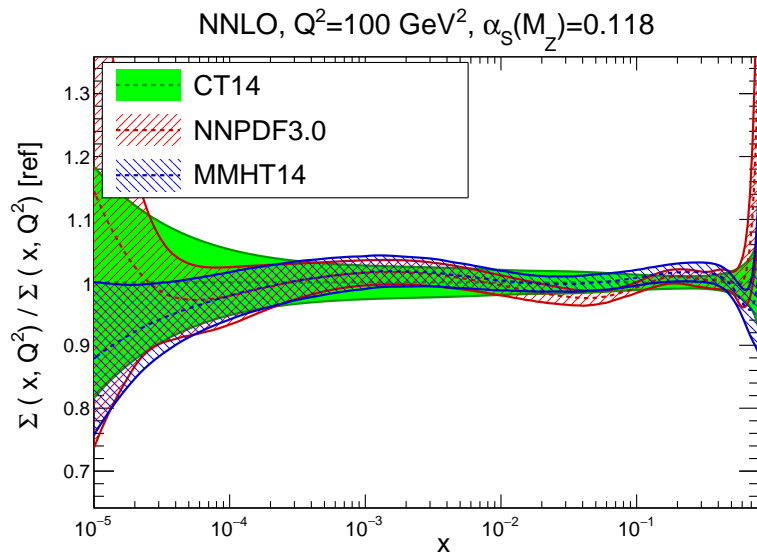


NNPDF3.0 NNLO Global,  $Q^2=10^2 \text{ GeV}^2$

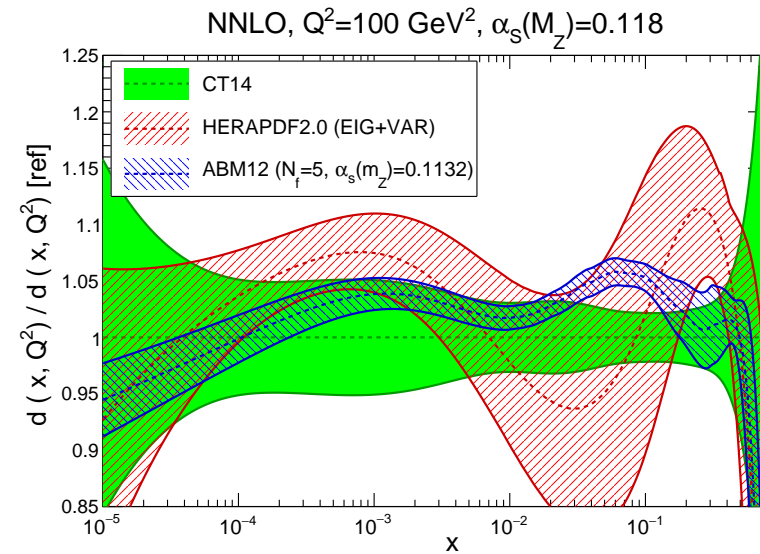
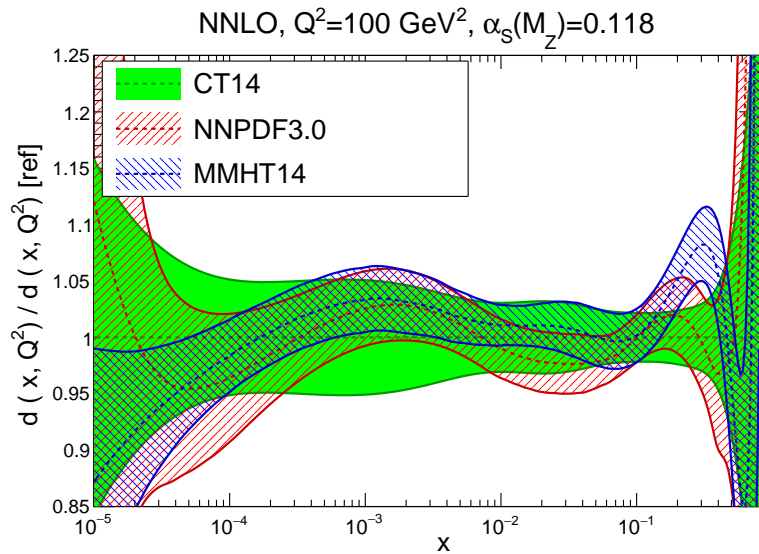
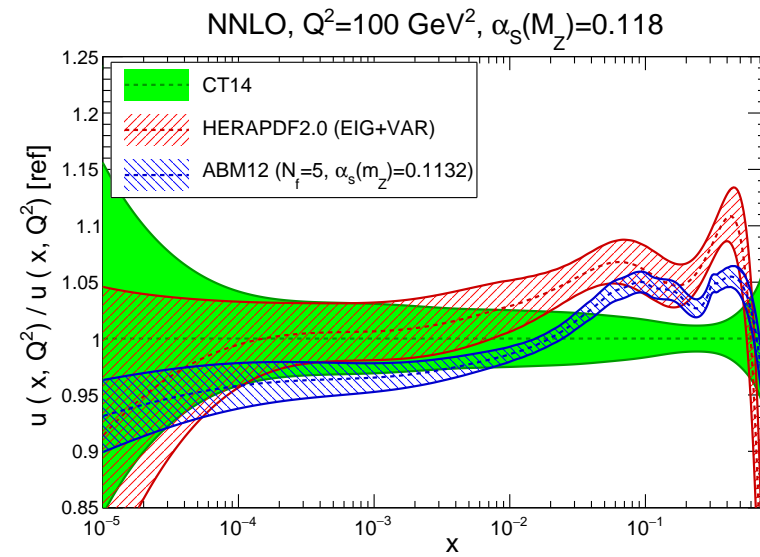
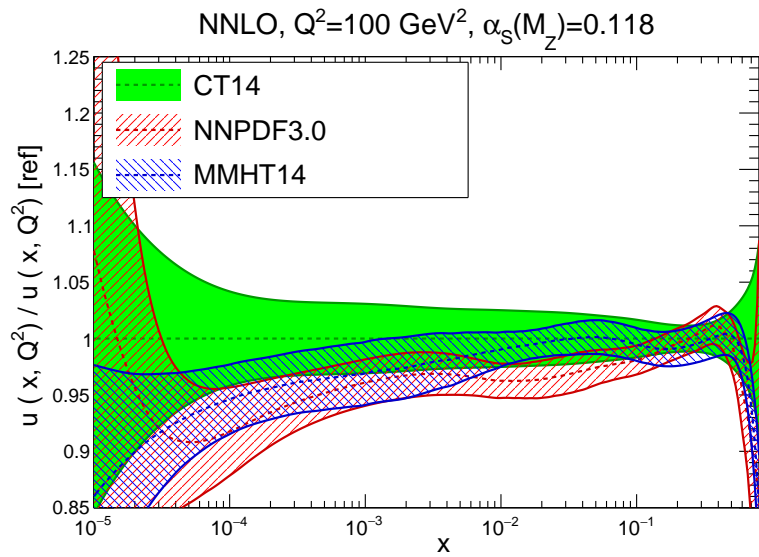


Similar results for **NNPDF3.0**.

# Comparison of state-of-the-art PDFs

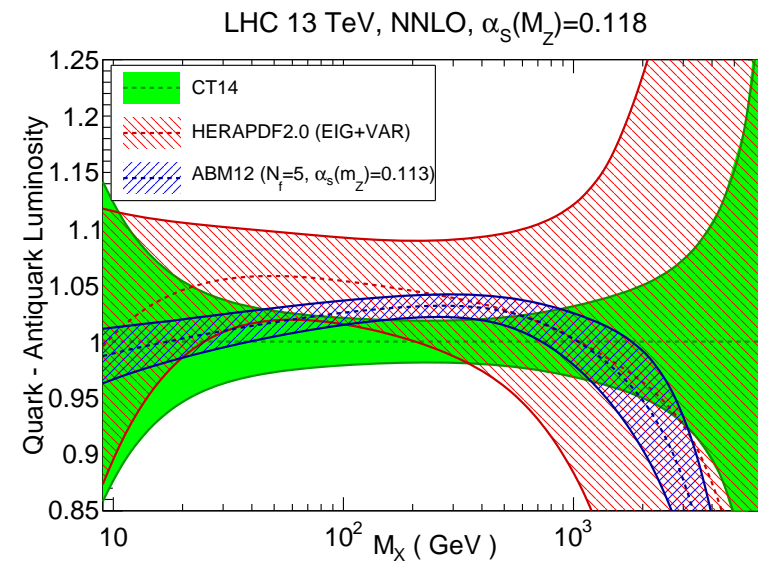
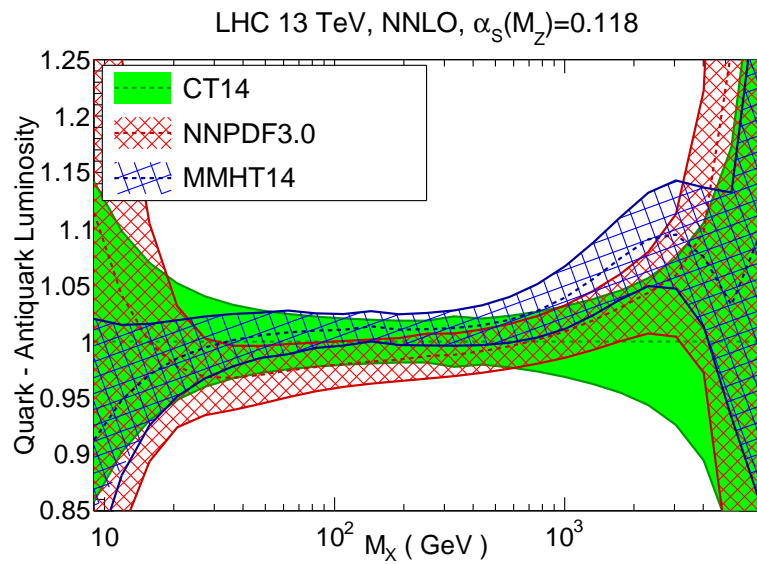
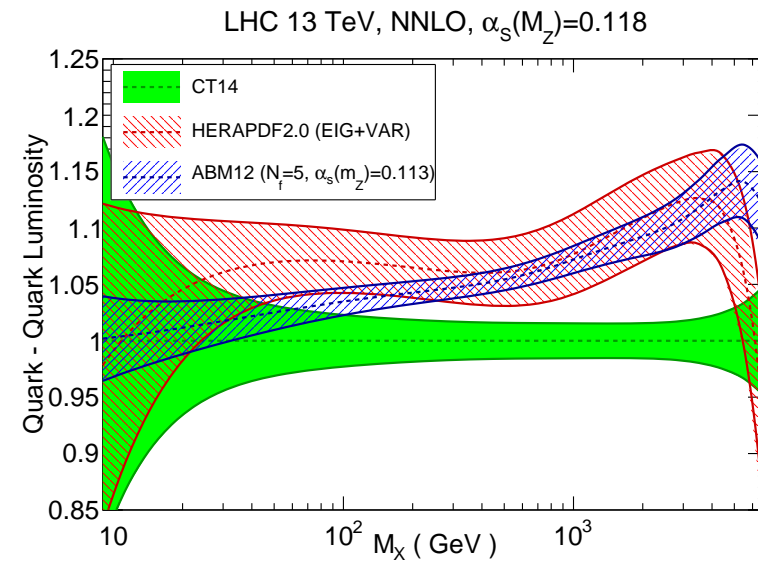
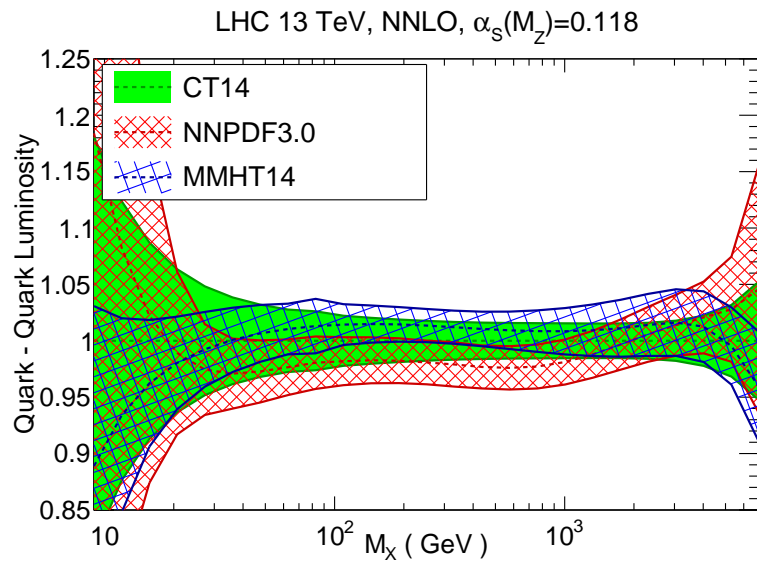


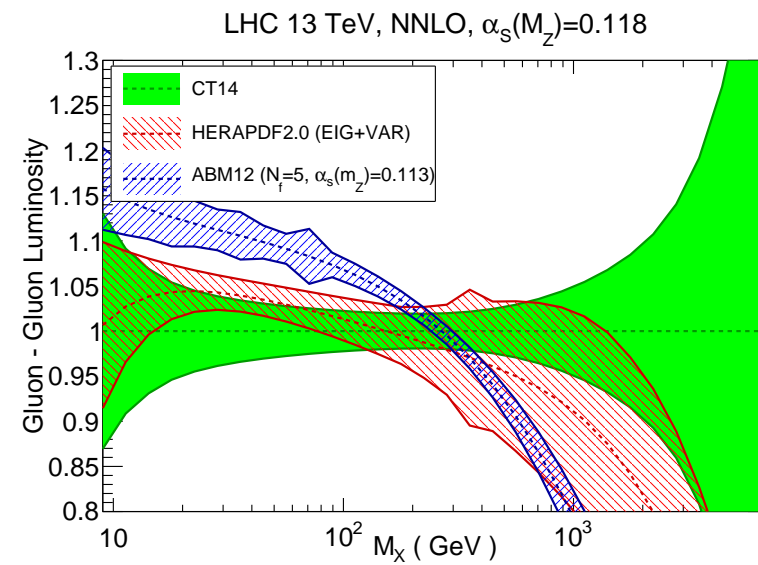
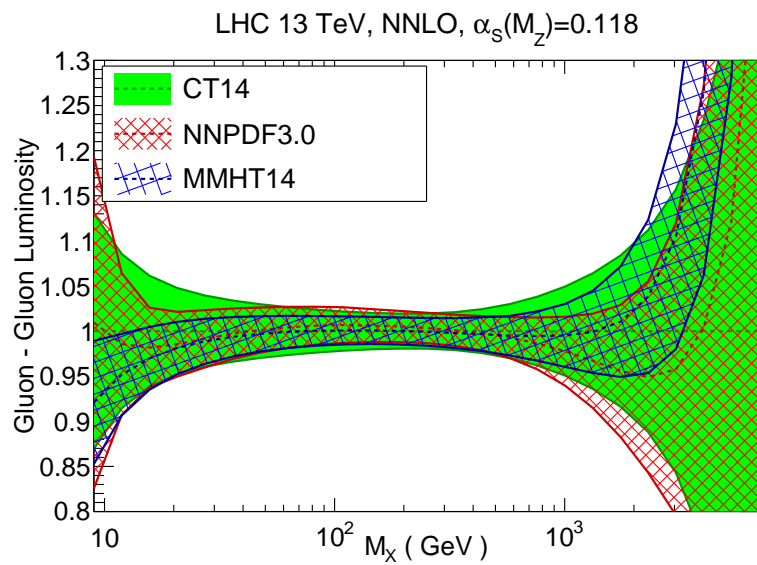
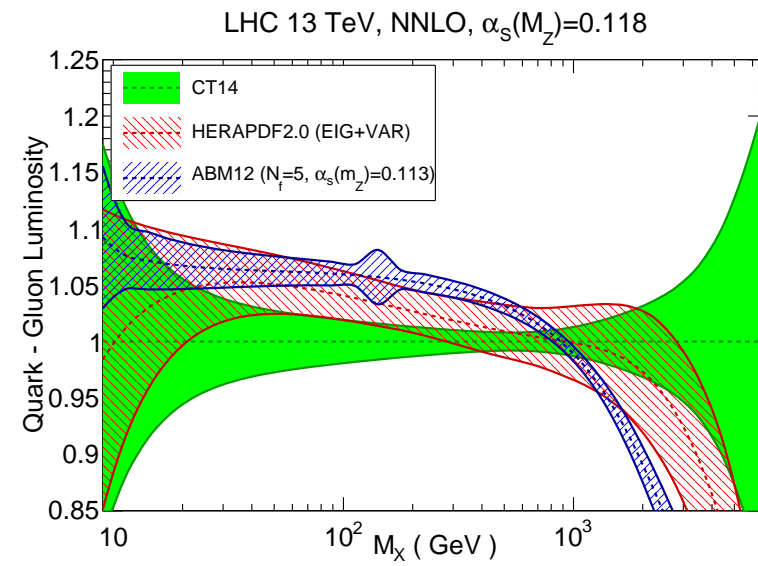
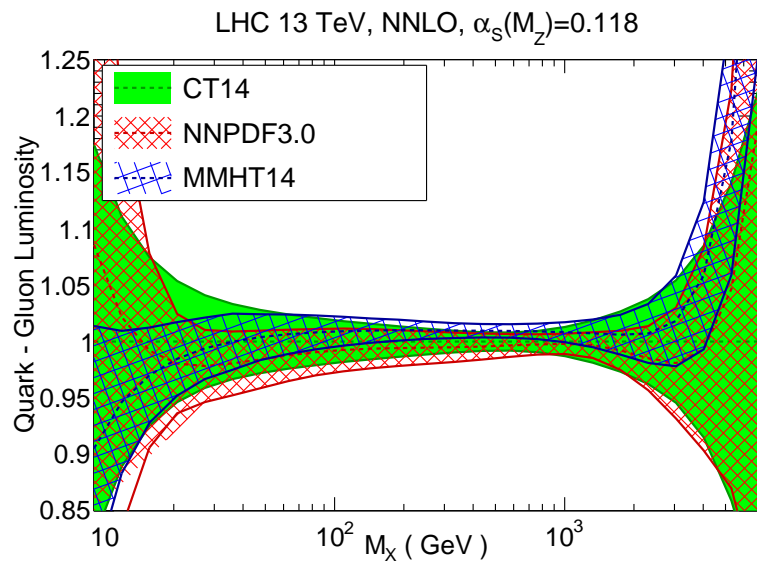
Some excellent agreement between CT14, MMHT2104 and NNPDF3.0.



Some significant differences in some PDF sets in central values and uncertainty.

# Comparison of PDF luminosities





*gg* luminosity now almost perfect agreement for “global” sets.



# Randomly distributed “Hessian” PDF sets. G. Watt, RST

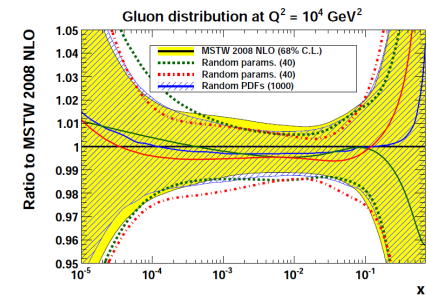
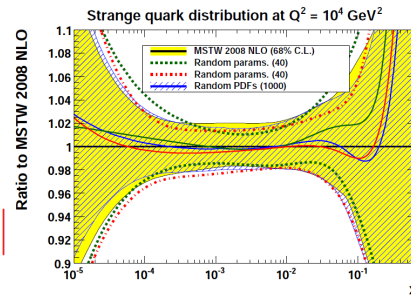
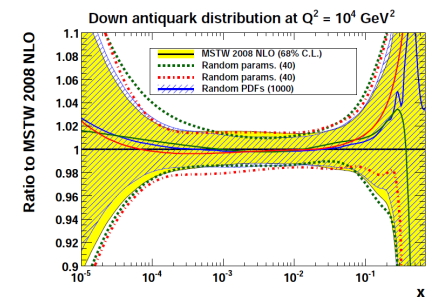
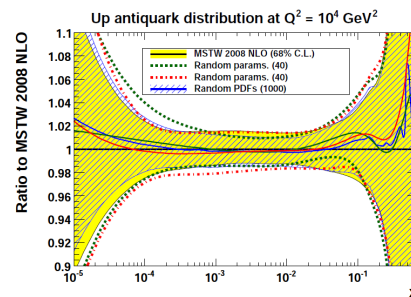
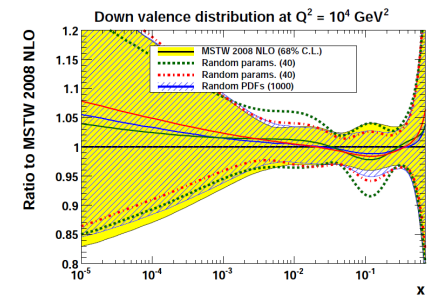
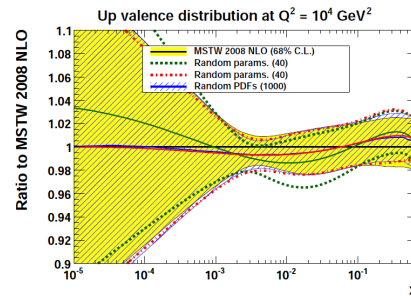
Study supported correctness of “dynamic tolerance” approach. Easiest in Hessian study with eigenvectors.

However, can generate “random” PDF sets directly from parameters and variation from eigenvectors.

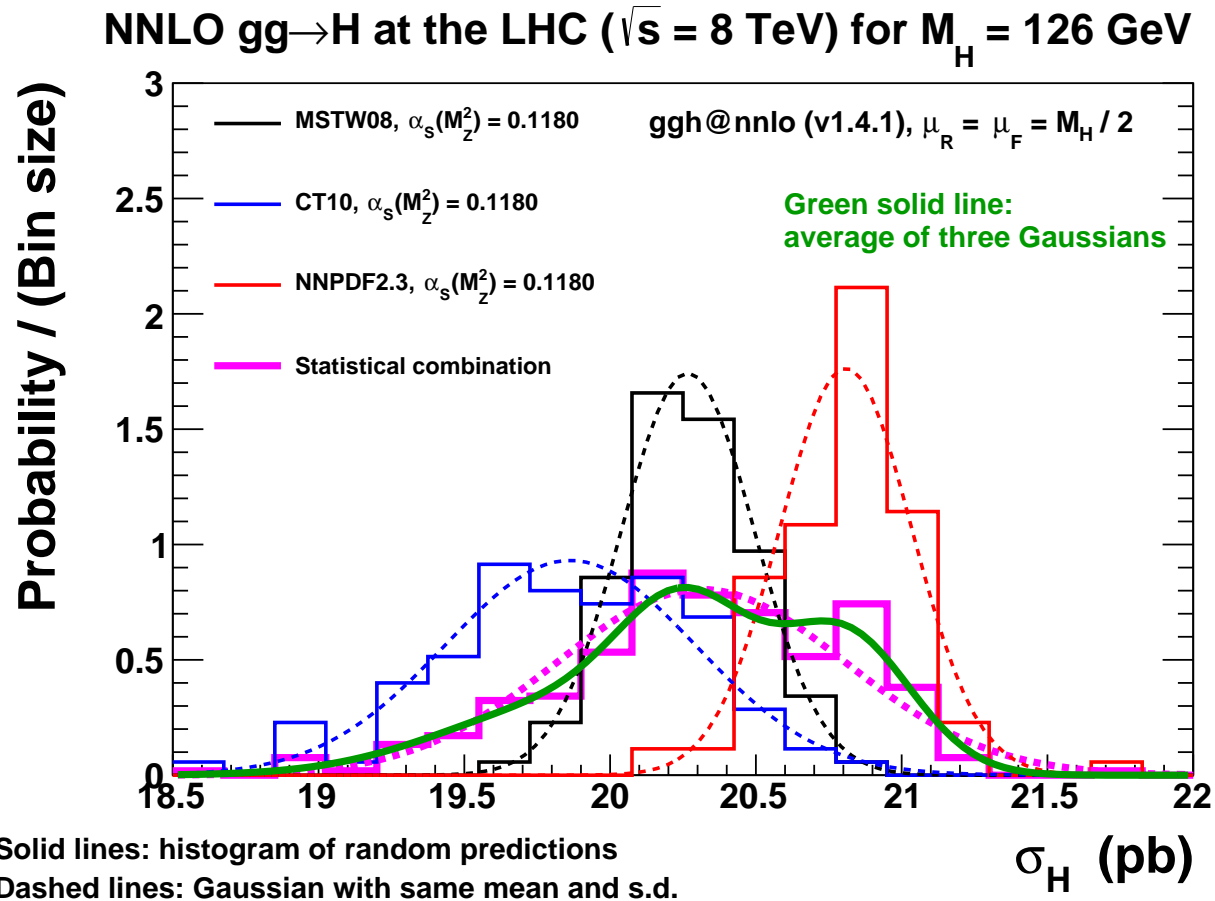
$$a_i(\mathcal{S}_k) = a_i^0 + \sum_{j=1}^n e_{ij}(\pm t_j^\pm) |R_{jk}|$$

( $k = 1, \dots, N_{\text{pdf}}$ ). Or from eigenvectors directly (see LHCb study and De Lorenzi thesis). Far quicker.

$$F(\mathcal{S}_k) = F(S_0) + \sum_j [F(S_j^\pm) - F(S_0)] |R_{jk}|$$

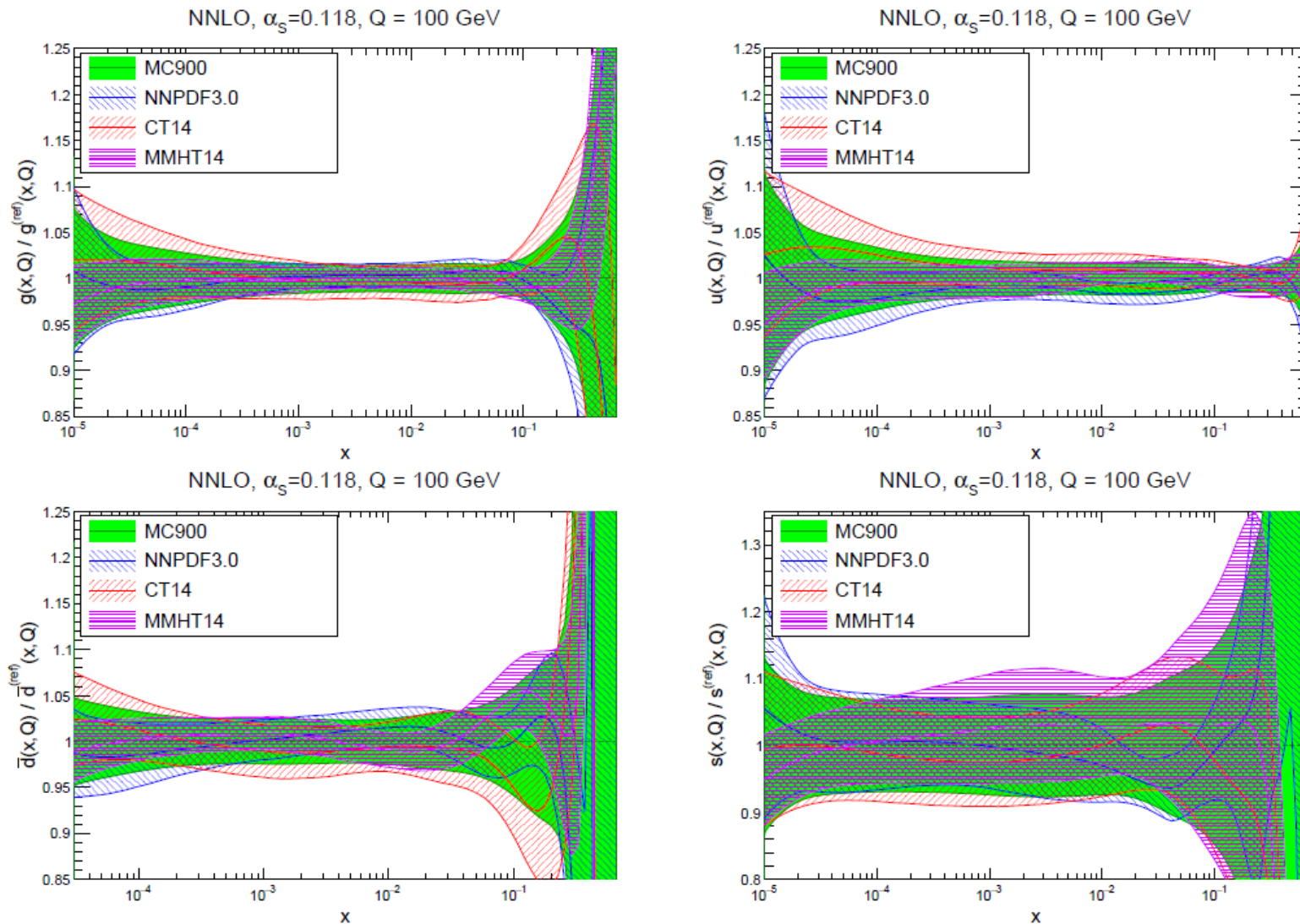


Can combine different PDF sets either at PDF level or predictions, e.g. Higgs cross section (Plot by **G. Watt** - original example.)



Slightly smaller uncertainty and shifted central value than envelope method if disagreement between individual predictions.

# Comparison of Combination to Individual PDFs



Works well if PDFs are fairly compatible - both in central value and uncertainty.

## The New PDF4LHC Prescription

Perform a Monte Carlo combination of the included PDF sets.

Sets entering into the combination must satisfy requirements, i.e. be compatible for combination.  $\alpha_S(M_Z^2) = 0.118$

Deliver a single combined PDF set - either **Monte Carlo** or **Hessian** form for combined PDF.

- **Monte Carlo** - A set of PDF replicas is delivered. The mean is the central value and the standard deviation the uncertainty.
- **Hessian** - A central set and eigenvectors representing orthogonal sources of uncertainty are delivered. Uncertainty obtained by summing each uncertainty source in quadrature.

In each case a single combined set at both  $\alpha_S(M_Z^2) = 0.1165$  and  $\alpha_S(M_Z^2) = 0.1195$  is provided to give  $\alpha_S(M_Z^2)$  uncertainty (i.e.  $\Delta\alpha_S(M_Z^2) = 0.118$ ) to be added in quadrature with other uncertainties.

## Three Options Provided

**PDF4LHC15-mc:** A compressed **Monte Carlo** set with  $N_{\text{rep}} = 100$ .

**PDF4LHC15-30:** A symmetric **Hessian** set with  $N_{\text{eig}} = 30$ . (Meta-PDF approach - refit combination to functional form.)

**PDF4LHC15-100:** A symmetric **Hessian** set with  $N_{\text{eig}} = 100$ . (MC-H representing eigenvectors on linear basis of replica.)

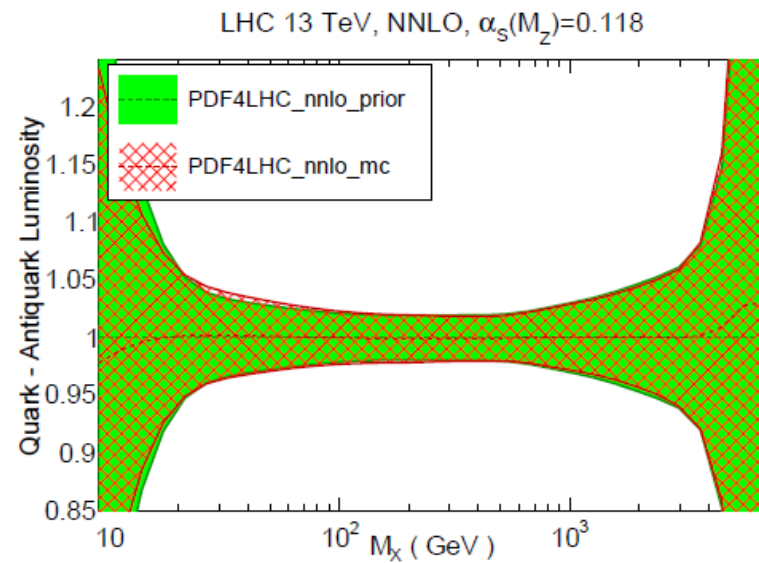
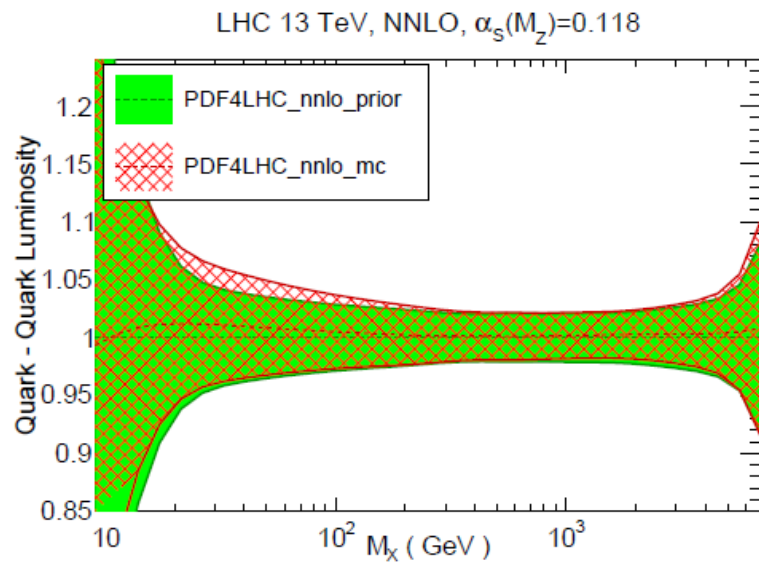
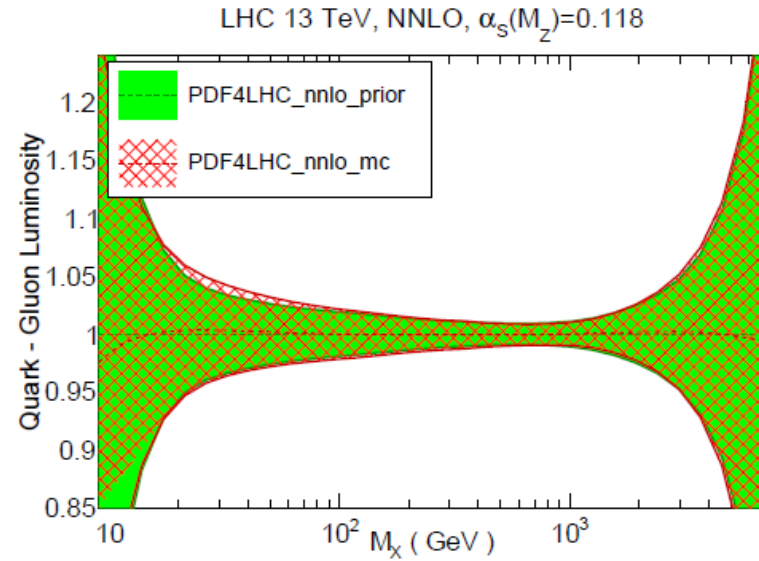
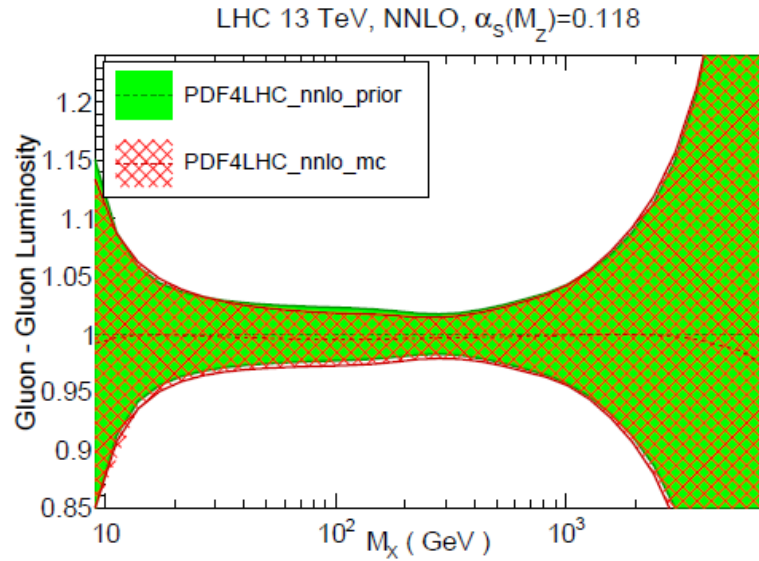
Some suggestions for which ones to use

**Monte Carlo** contains non-gaussian features – important for searches at high masses (high  $x$ ).

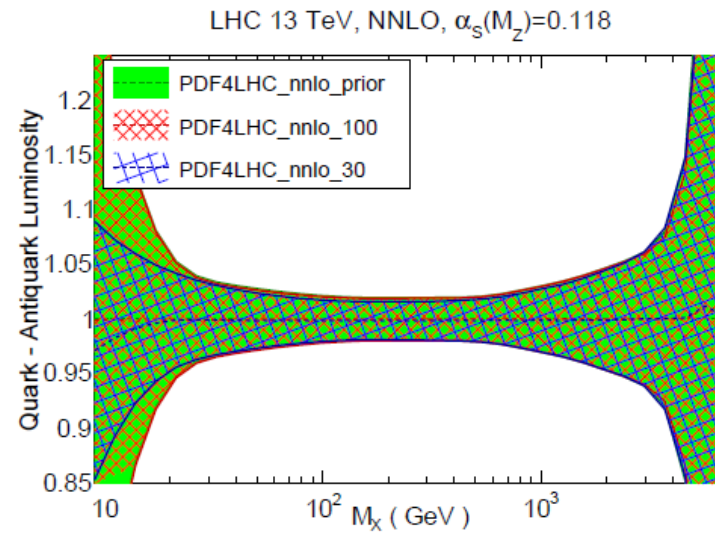
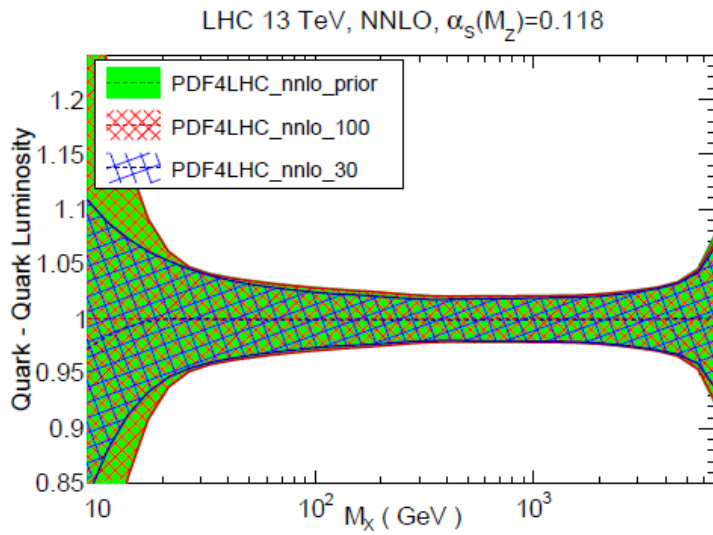
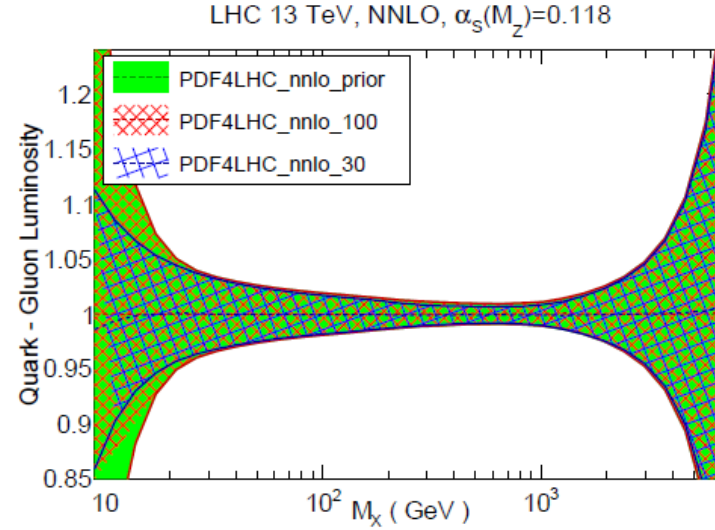
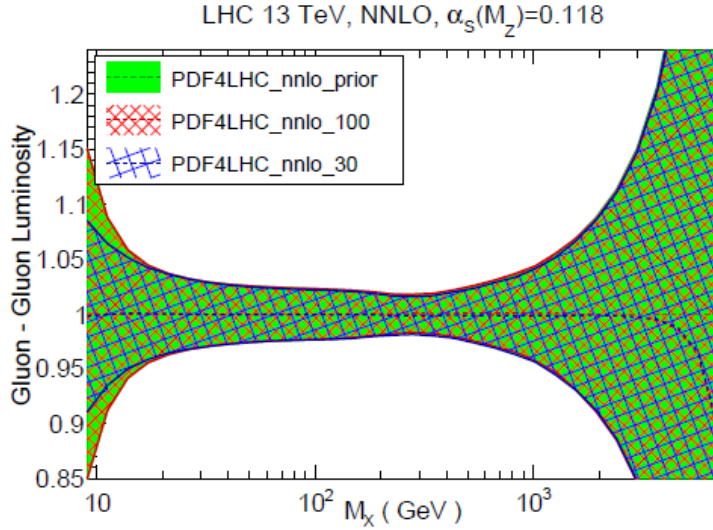
**Hessian 30** set has good precision and useful for many experimental needs and when using nuisance parameters.

**Hessian 100** set has optimal precision if running time not a problem or extreme accuracy needed.

# Comparison of PDF luminosities for MC Compression

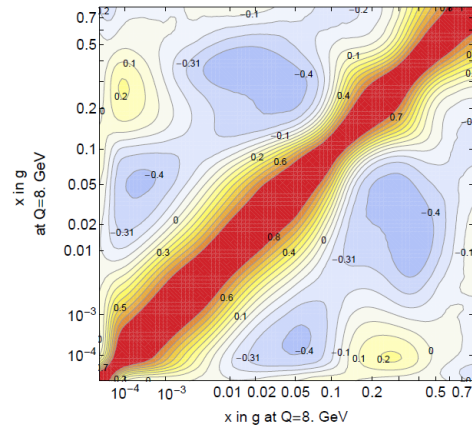


# Comparison of PDF luminosities for Hessian Compression

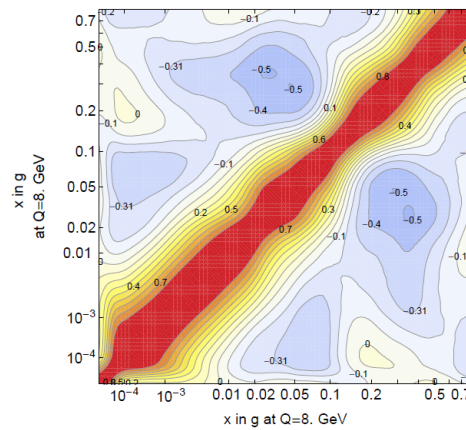


# PDF correlations in Compressed sets

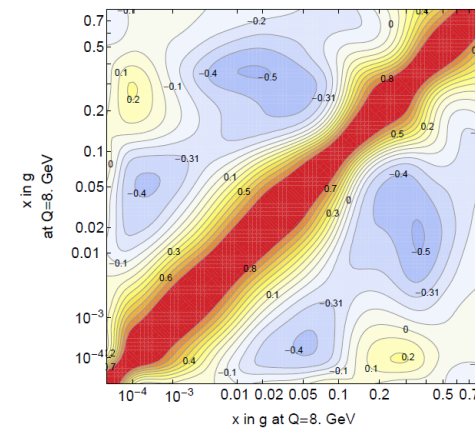
STARTING COMBINED SET  
Correlation between MC900 PDF's



GLUON-GLUON CORRELATION  
COMPRESSED MC SET  
Correlation between CMC-100 PDF's



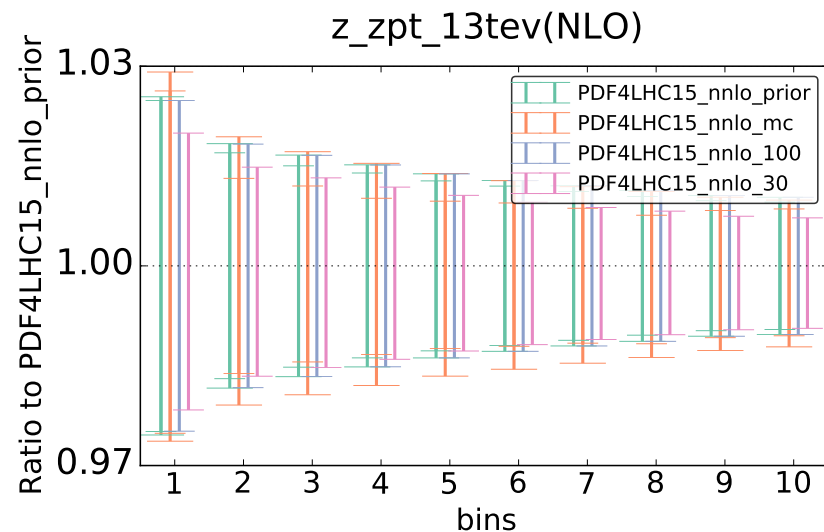
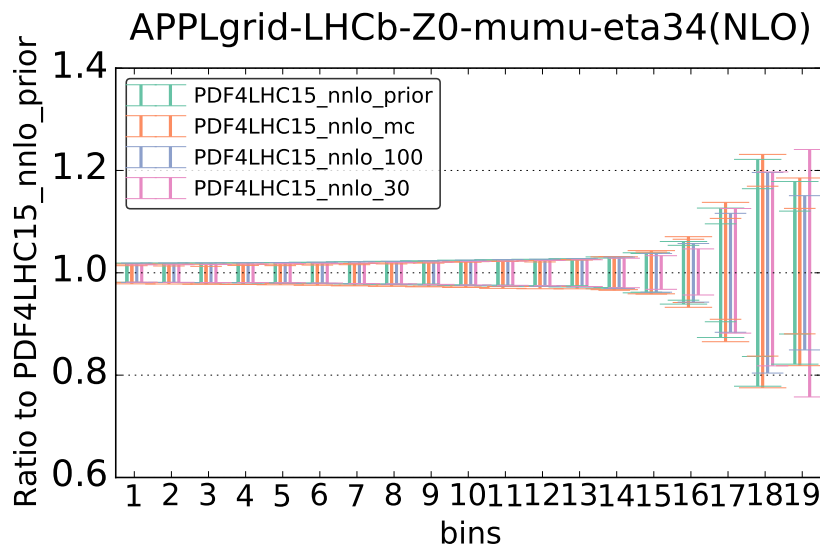
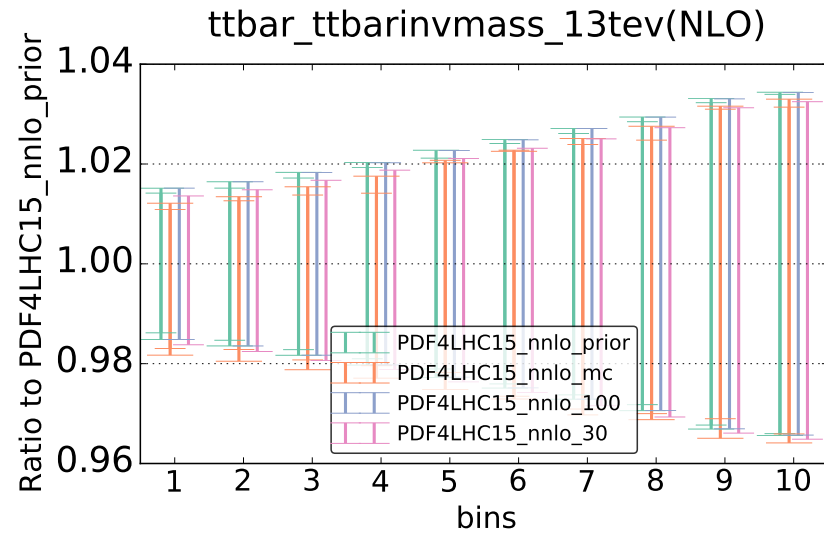
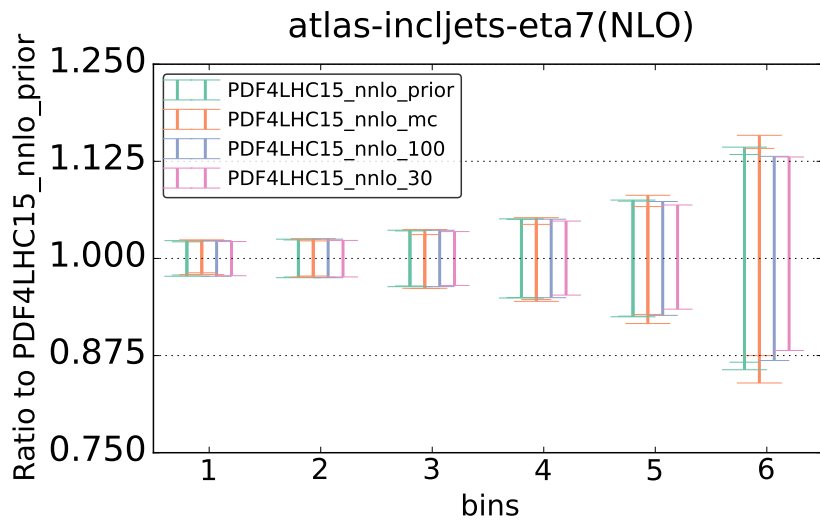
META-PDF SET  
Correlation between META-100 PDF's



Correlations in PDFs preserved extremely well in compression.



# Results using compressed sets for some LHC quantities



Generally all sets work pretty well, even in more extreme regions of kinematics.

There are basically two kinds of situation.

- For assessment of the PDF uncertainty in searches, discovery, acceptance corrections ... (e.g. Higgs, Susy). **Use the PDF4LHC prescription.**
- When comparing predictions to theory in well-determined standard model processes, e.g. jets,  $W$ ,  $Z$  distributions, top pair cross sections ... **Use the individual PDF sets (ABM, CT, HERAPDF, JR, MMHT, NNPDF)**

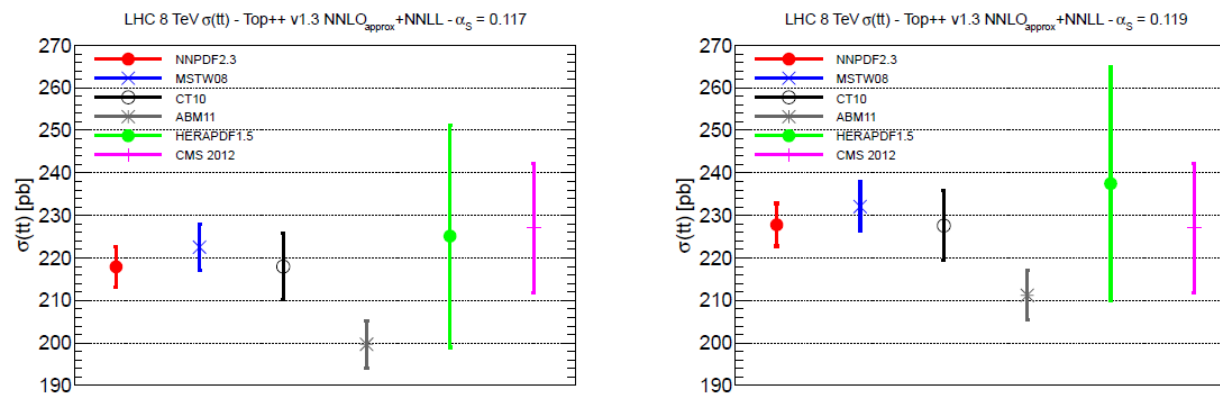


Figure 10: Comparison of the predictions for the top quark pair production at LHC 8 TeV obtained using various NNLO PDF sets. Left plot: results for  $\alpha_S(M_Z) = 0.117$ . Right plot: results for  $\alpha_S(M_Z) = 0.119$ . We also show the recent CMS 8 TeV measurements.

## Conclusions

All PDF sets have been recently updated with either new data inputs or improvements in methodology, or in many cases both.

Generally good agreement between the sets which fit to global data, both in central values and uncertainties. Improved considerably compared to earlier versions for the gluon.

Some discrepancies with other sets due to different data and/or different procedures (e.g. treatment of heavy quarks). HERA I + II combination does not significantly alter global PDFs.

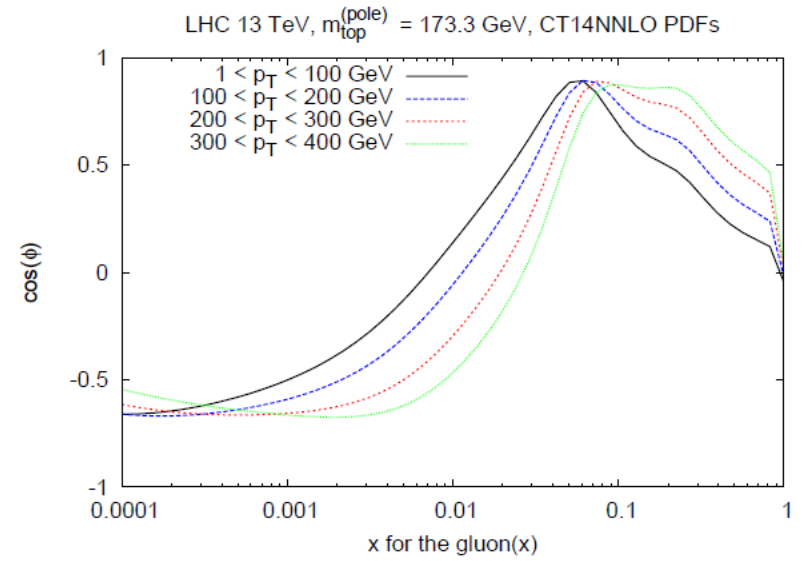
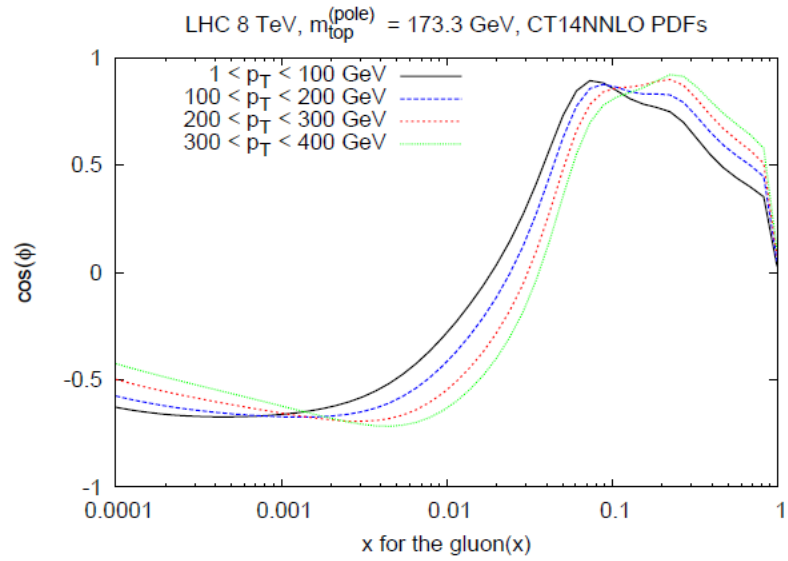
Inclusive top pair production used in some cases and compared to in others. Most PDFs give good predictions, but distinct interplay between  $\alpha_S(M_Z^2)$  and  $m_{top}$ .

More information will be obtained from differential distributions. Fits at NLO not perfect. Very interesting and useful to see full NNLO.

New ways of combining PDFs → PDF4LHC recommendation update.

For many top measurements want to compare and discriminate between PDFs, not check agreement with PDF4LHC prescription value.

# BACK-UP



## MMHT2014 PDFs compared to MSTW2008 PDFs.

Use same “dynamic tolerance” prescription to determine eigenvectors.

Typical tolerance  $T = \Delta\chi^2 \sim 10$ .

We now have **25** eigenvector pairs, rather than the **20** in **MSTW** or even the **23** in **MMSTWW**.

Eigenvector sets made available for  $\alpha_S(M_Z^2) = 0.135$  (**LO**),  $\alpha_S(M_Z^2) = 0.118, 0.120$  (**NLO**) and  $\alpha_S(M_Z^2) = 0.118$  (**NNLO**)

In addition the central sets are available at

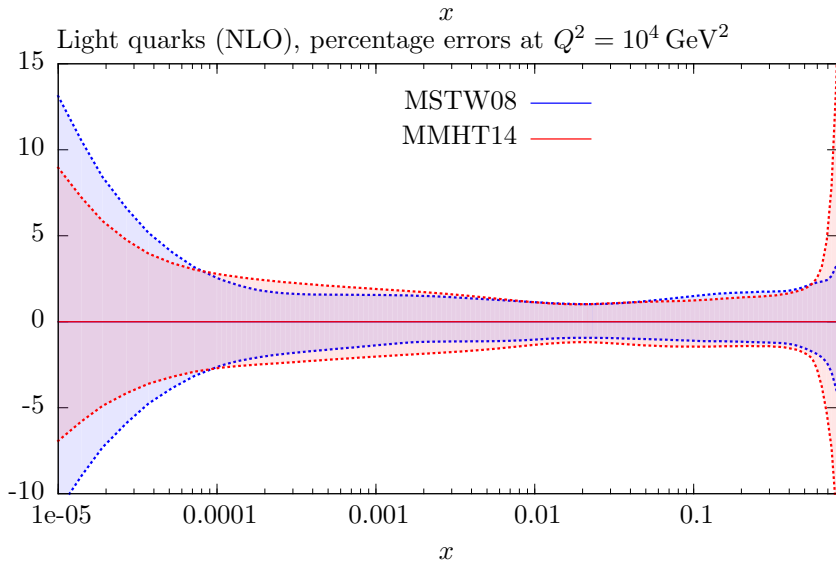
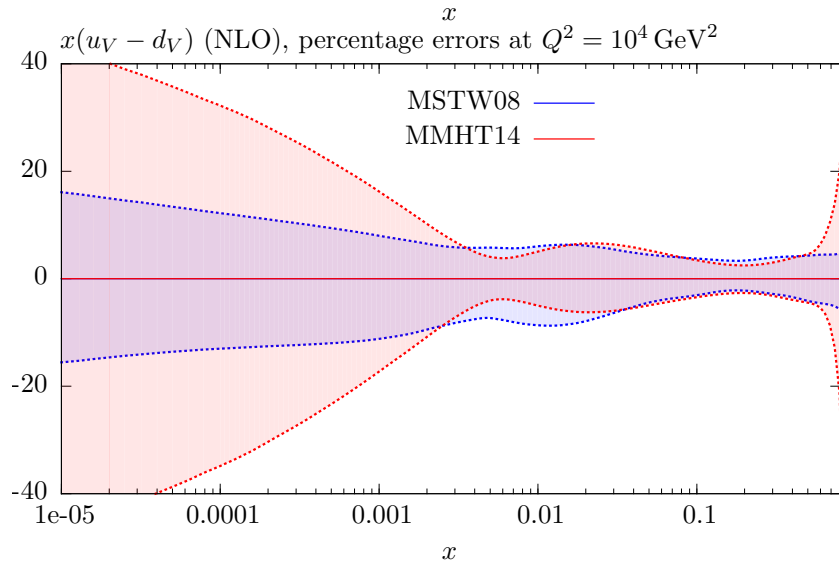
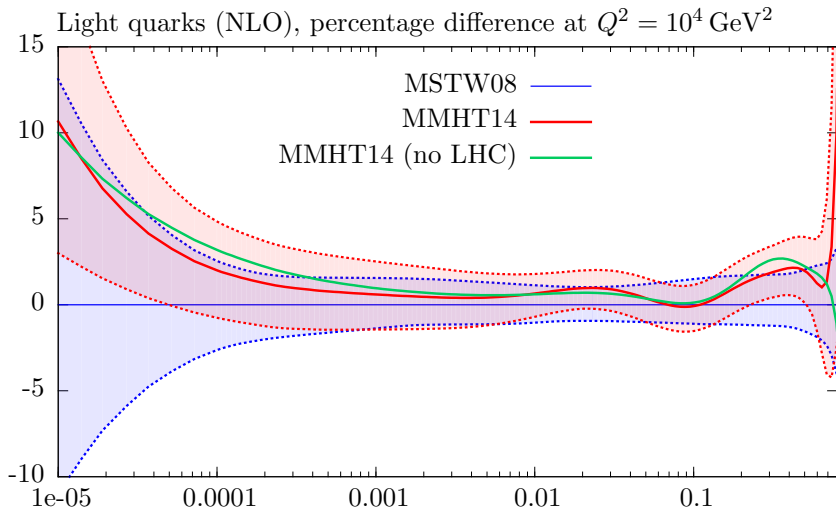
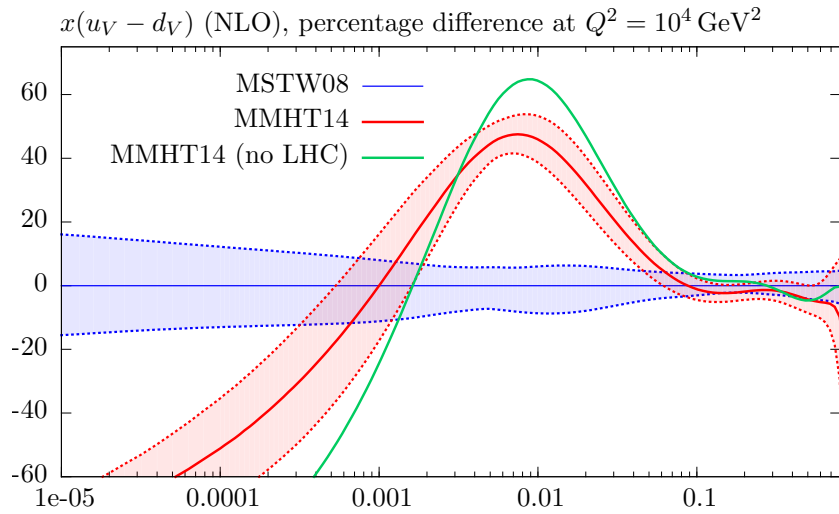
**LO**  $\alpha_S(M_Z^2) = 0.134, 0.135, 0.136$

**NLO**  $\alpha_S(M_Z^2) = 0.117, 0.118, 0.119, 0.120, 0.121$

**NNLO**  $\alpha_S(M_Z^2) = 0.117, 0.118, 0.119$

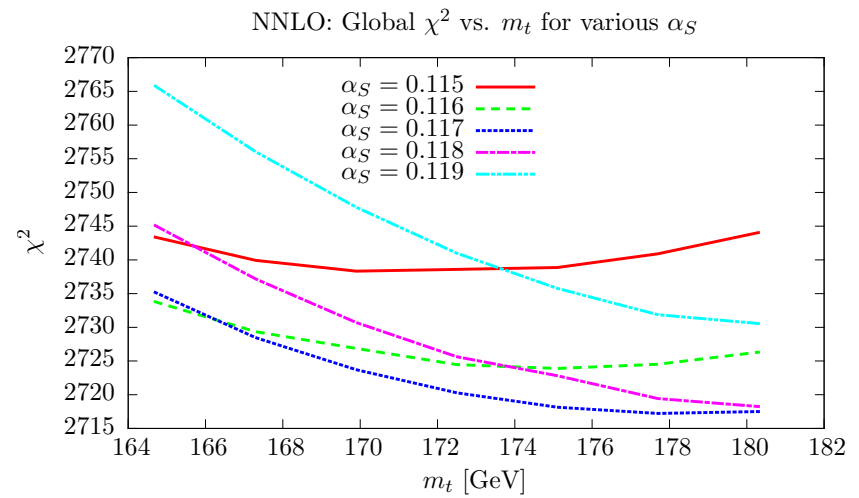
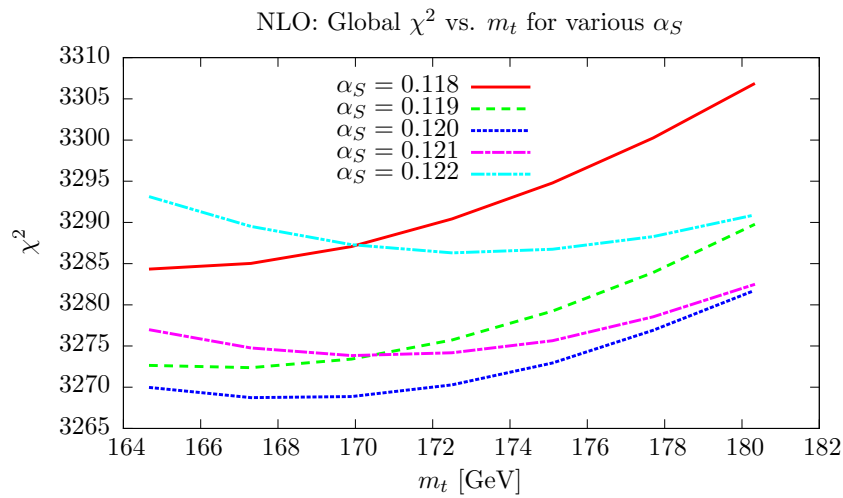
This allows the **PDF** +  $\alpha_S$  uncertainty to be calculated, if using the prescription of adding in quadrature.

# Comparison of PDFs at NLO

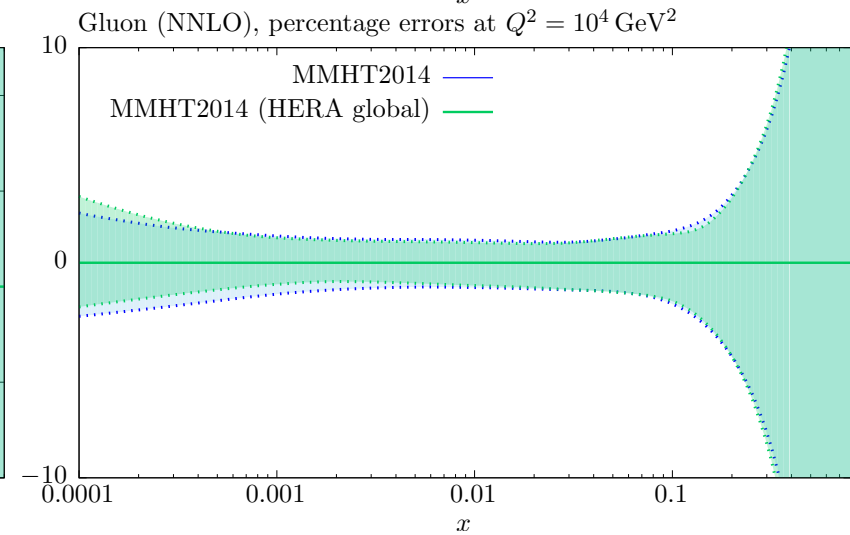
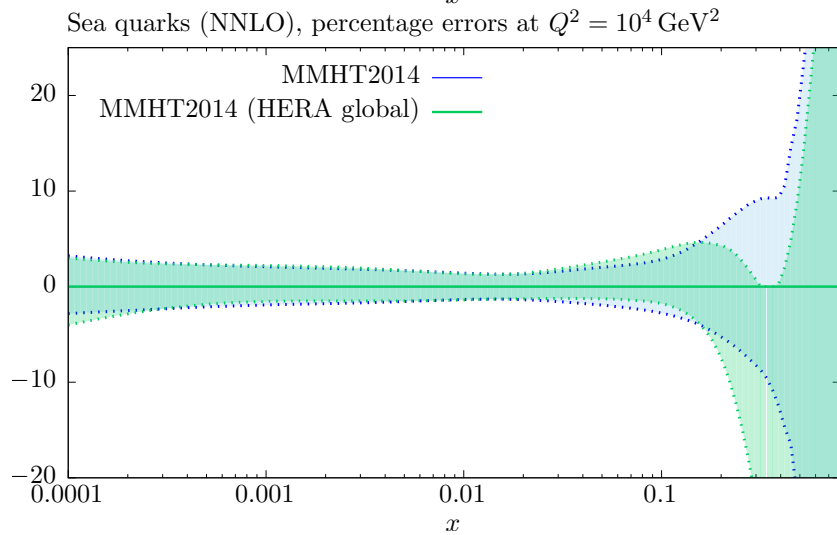
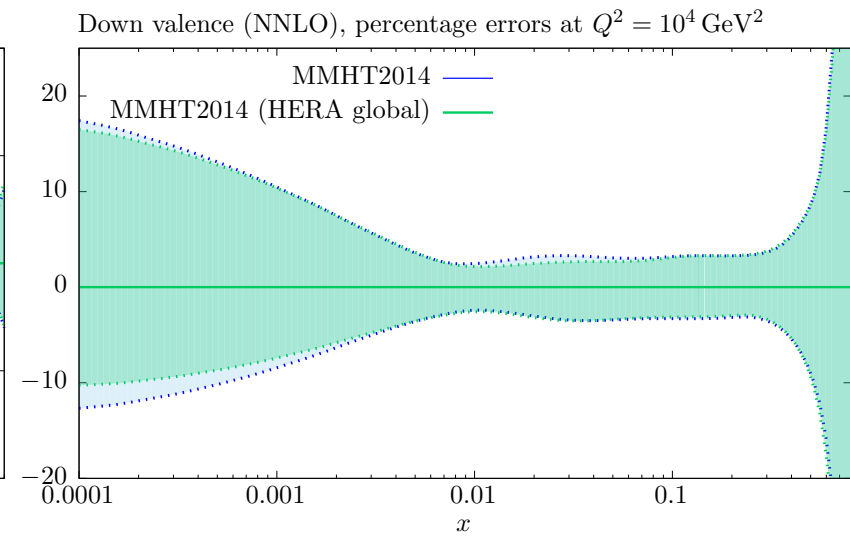
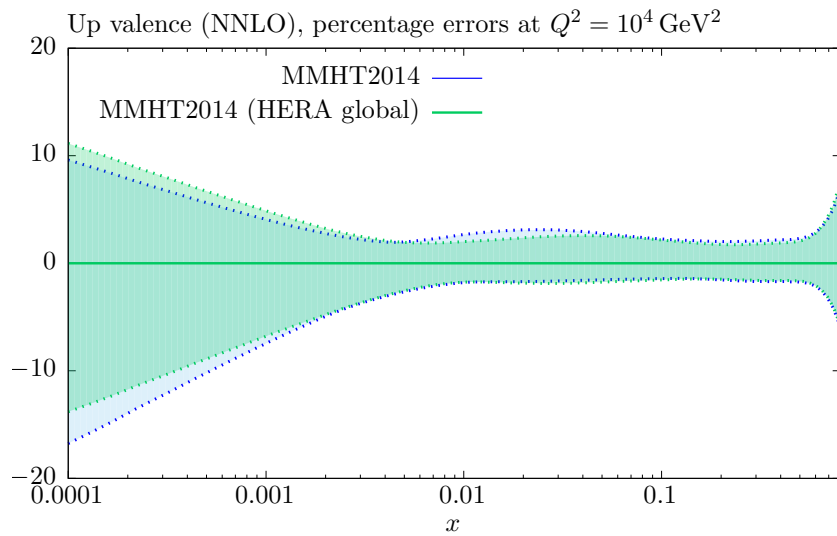


Change in NLO PDFs from all updates, including LHC data updates.

Global  $\chi^2$  depends on  $m_t$  but minimises at very similar  $\alpha_S(M_Z^2)$  for a rather wide range.







Uncertainties (preliminary) quite similar to **MMHT2014**.

Most obvious improvement in gluon for  $x \sim 0.001$ .

## LHC data on jets

At **NLO** include **CMS** data and **ATLAS 7 TeV + 2.76 TeV** data. **ATLAS**  $\chi^2 = 107/116$  and **CMS**  $\chi^2 = 143/133$  before included directly.

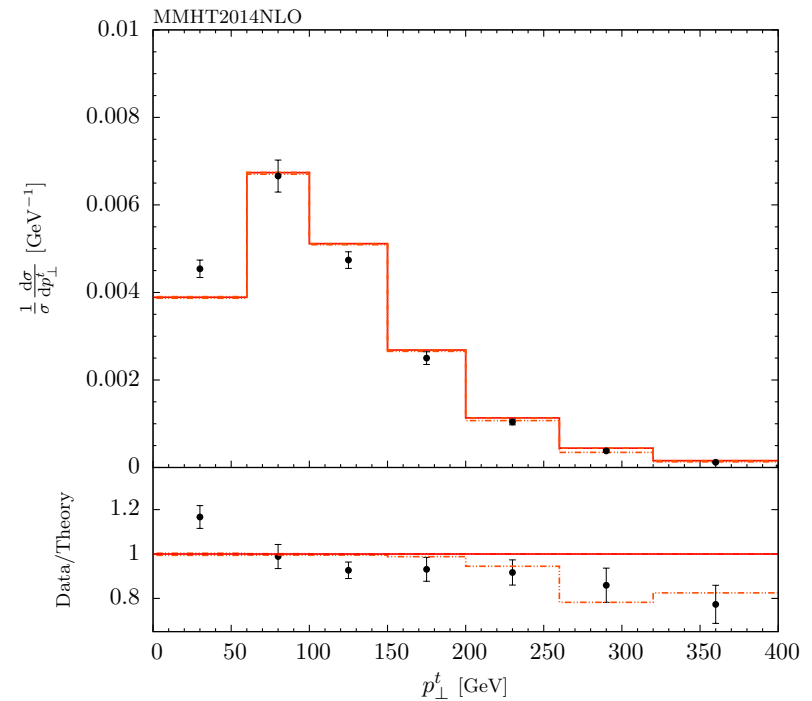
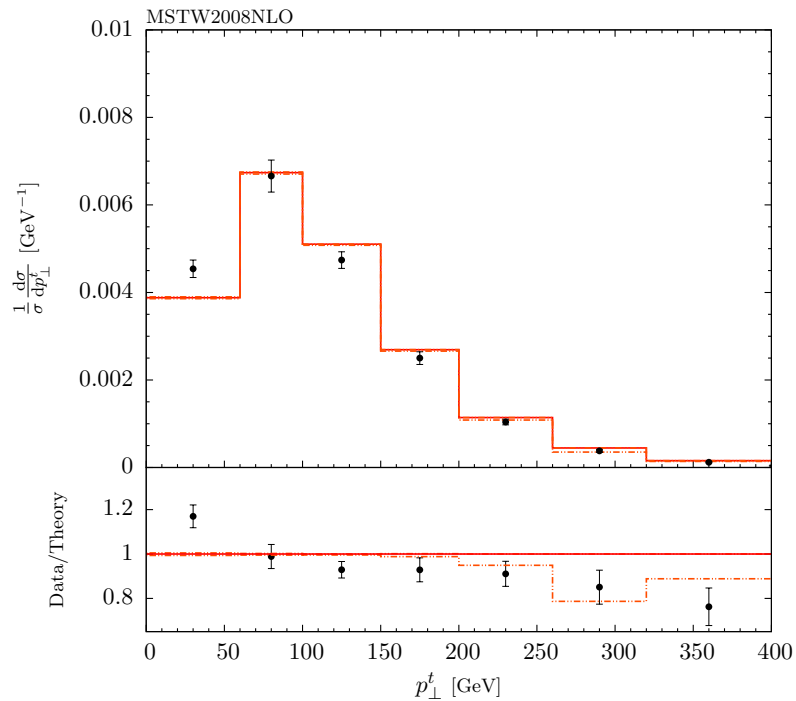
Enormous project of full **NNLO** calculation (**Gehrmann-de-Ridder et al.**) nearing completion. Some indications of full form.

As default at **NNLO** still fit **Tevatron** data which are relatively near to threshold. However, omit **LHC** data. Investigate inclusion of **K**-factor.

data set	$N_{pts}$	MMSTWW	MMHT14 (no LHC)	MMHT14 (with LHC)
<b>NLO</b>				
ATLAS (2.76+7 TeV)	116	107	107	106
CMS (7 TeV)	133	140	143	138
<b>NNLO small</b>				
ATLAS (2.76+7 TeV)	116	(107)	(123)	(122) 115
CMS (7 TeV)	133	(142)	(137)	(138) 137
<b>NNLO large K-factor</b>				
ATLAS (2.76+7 TeV)	116	(117)	(132)	(132) 126
CMS (7 TeV)	133	(145)	(137)	(139) 139

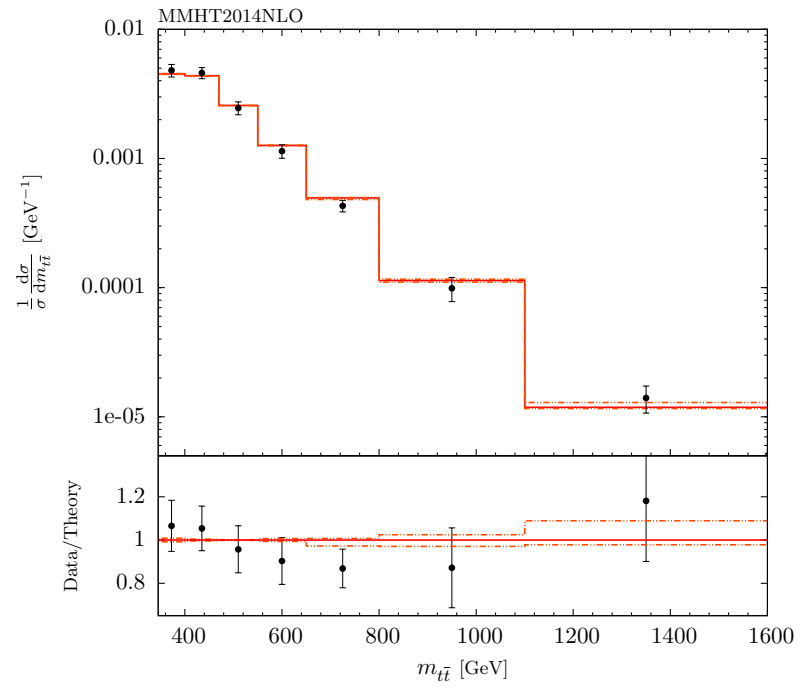
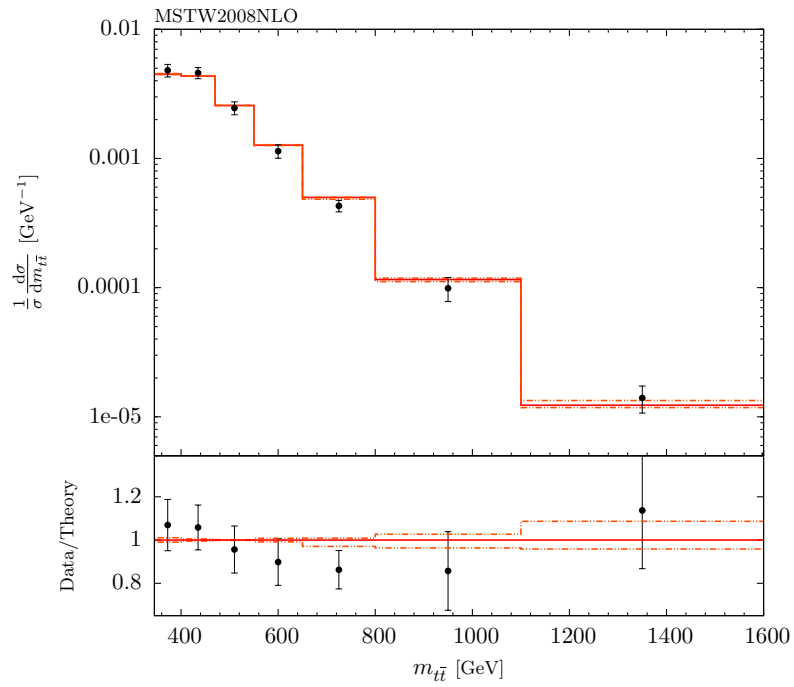
# New results – plots by Harland-Lang

## $p_T$ distributions - CMS data

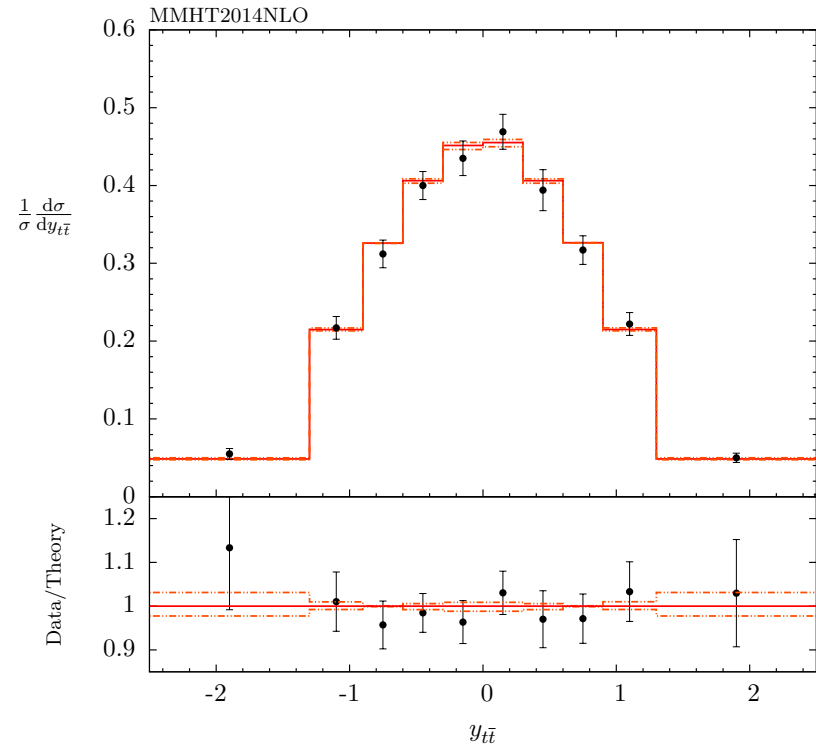
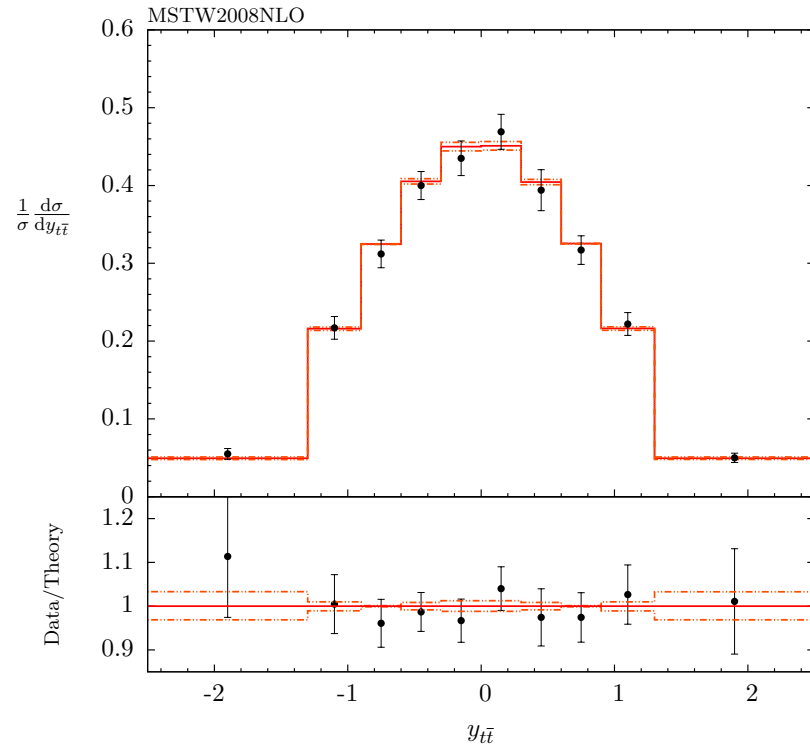


Very little difference between **MSTW2008** and **MMHT2014** predictions.

# $m_{t\bar{t}}$ distributions - CMS data

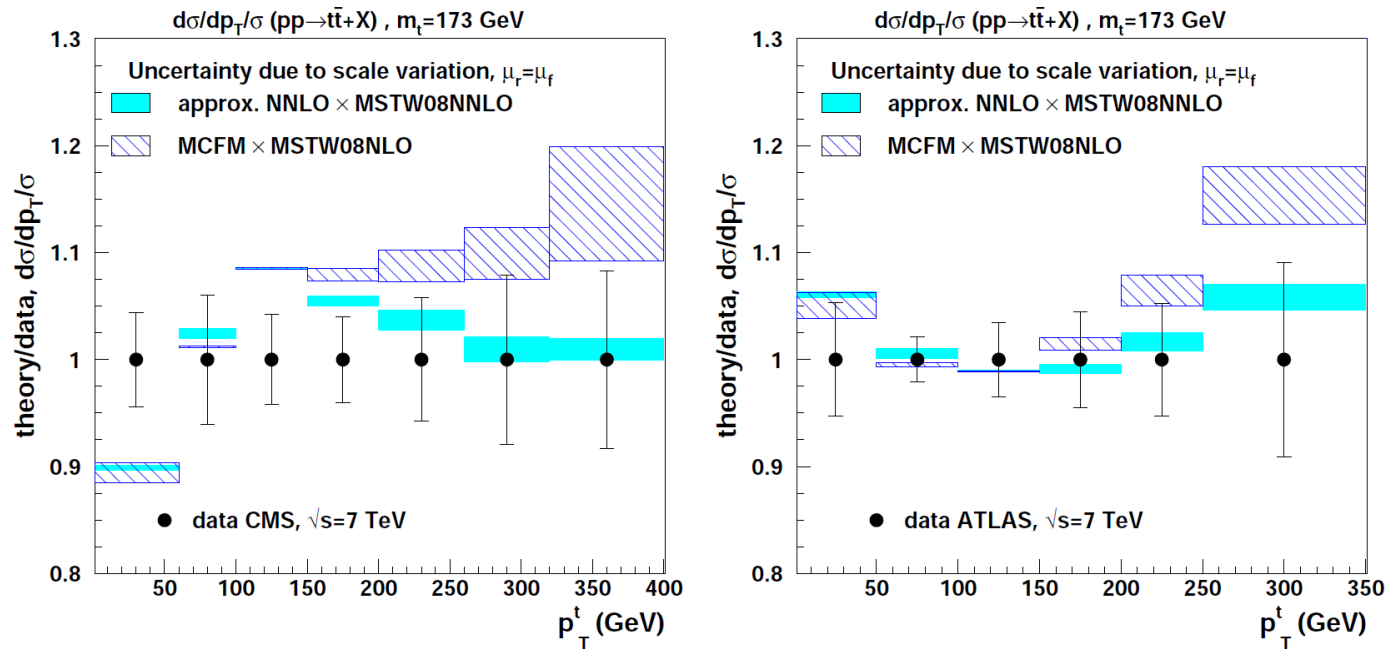


# $y_{t\bar{t}}$ distributions - CMS data



# Differential Data

As it improves differential top production data will help constrain the gluon.



However, here potentially inclusion of **NNLO** is very important as available approximation using threshold resummation (Guzzi, Lipka, Moch) implies. Softer PDF currently preferred at **NLO**, contrary to requirement of inclusive cross-section, may be misleading.

## NNLO total cross sections

	MSTW08	MMHT14 no LHC	MMHT14
$W$ Tevatron (1.96 TeV)	$2.746^{+0.049}_{-0.042}$	2.803	$2.782^{+0.056}_{-0.056}$
$Z$ Tevatron (1.96 TeV)	$0.2507^{+0.0048}_{-0.0041}$	0.2574	$0.2559^{+0.0052}_{-0.0046}$
$W^+$ LHC (7 TeV)	$6.159^{+0.111}_{-0.099}$	6.214	$6.197^{+0.103}_{-0.092}$
$W^-$ LHC (7 TeV)	$4.310^{+0.078}_{-0.069}$	4.355	$4.306^{+0.067}_{-0.076}$
$Z$ LHC (7 TeV)	$0.9586^{+0.020}_{-0.014}$	0.9695	$0.9638^{+0.014}_{-0.013}$
$W^+$ LHC (14 TeV)	$12.39^{+0.22}_{-0.21}$	12.49	$12.48^{+0.22}_{-0.18}$
$W^-$ LHC (14 TeV)	$9.33^{+0.16}_{-0.16}$	9.39	$9.32^{+0.15}_{-0.14}$
$Z$ LHC (14 TeV)	$2.051^{+0.035}_{-0.033}$	2.069	$2.065^{+0.035}_{-0.030}$
Higgs Tevatron	$0.853^{+0.028}_{-0.029}$	0.877	$0.874^{+0.024}_{-0.030}$
Higgs LHC (7 TeV)	$14.40^{+0.17}_{-0.23}$	14.54	$14.56^{+0.21}_{-0.29}$
Higgs LHC (14 TeV)	$47.50^{+0.47}_{-0.74}$	47.61	$47.69^{+0.63}_{-0.88}$
$t\bar{t}$ Tevatron	$7.19^{+0.17}_{-0.12}$	7.54	$7.51^{+0.21}_{-0.20}$
$t\bar{t}$ LHC (7 TeV)	$171.1^{+4.7}_{-4.8}$	176.5	$175.9^{+3.9}_{-5.5}$
$t\bar{t}$ LHC (14 TeV)	$953.3^{+16}_{-18}$	969.0	$969.9^{+16}_{-20}$

Few changes greater than one sigma (PDF uncertainty only).