

Global QCD Analysis of Pion Parton Distributions Including Lattice QCD Data

**P. C. Barry¹, C. Egerer¹, J. Karpie², W. Melnitchouk¹, C. Monahan^{1,3},
K. Orginos^{1,3}, Jian-Wei Qiu¹, D. Richards¹, N. Sato¹, R. S. Sufian^{1,3},
S. Zafeiropoulos⁴**

¹Jefferson Lab, ²Columbia University, ³College of William & Mary, ⁴Aix Marseille Univ

LaMET 2021

Tuesday, December 7th, 2021



contact: barryp@jlab.org



Overarching themes

1. Can the lattice QCD data provide **constraints** on PDFs beyond current experimental data?
2. What **systematic effects** are intrinsic to the lattice and how do we quantify them?
3. The **complementarity** of experimental and lattice QCD data.

Motivation

- QCD allows us to study the **structure of hadrons** in terms of **partons** (quarks, antiquarks, and gluons)
- Use **factorization theorems** to separate hard partonic physics out of soft, non-perturbative objects to quantify structure

Complicated inverse problem

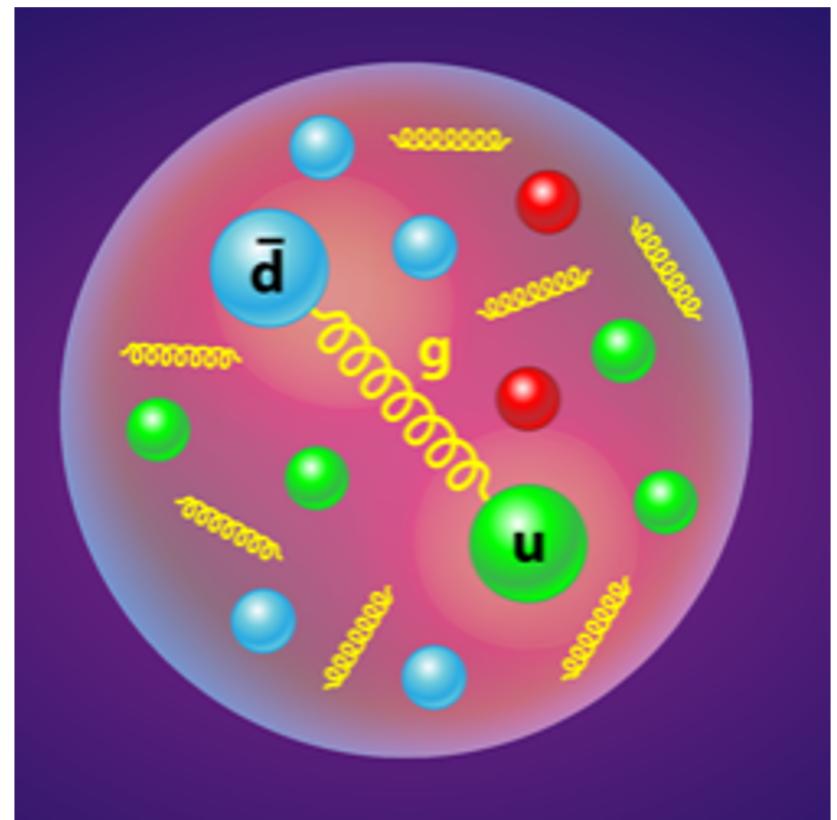
- Factorization theorems involve **convolutions** of **hard perturbatively calculable physics** and **non-perturbative objects**

$$\frac{d\sigma}{d\Omega} \propto \mathcal{H} \otimes f = \int_x^1 \frac{d\xi}{\xi} \mathcal{H}(\xi) f\left(\frac{x}{\xi}\right)$$

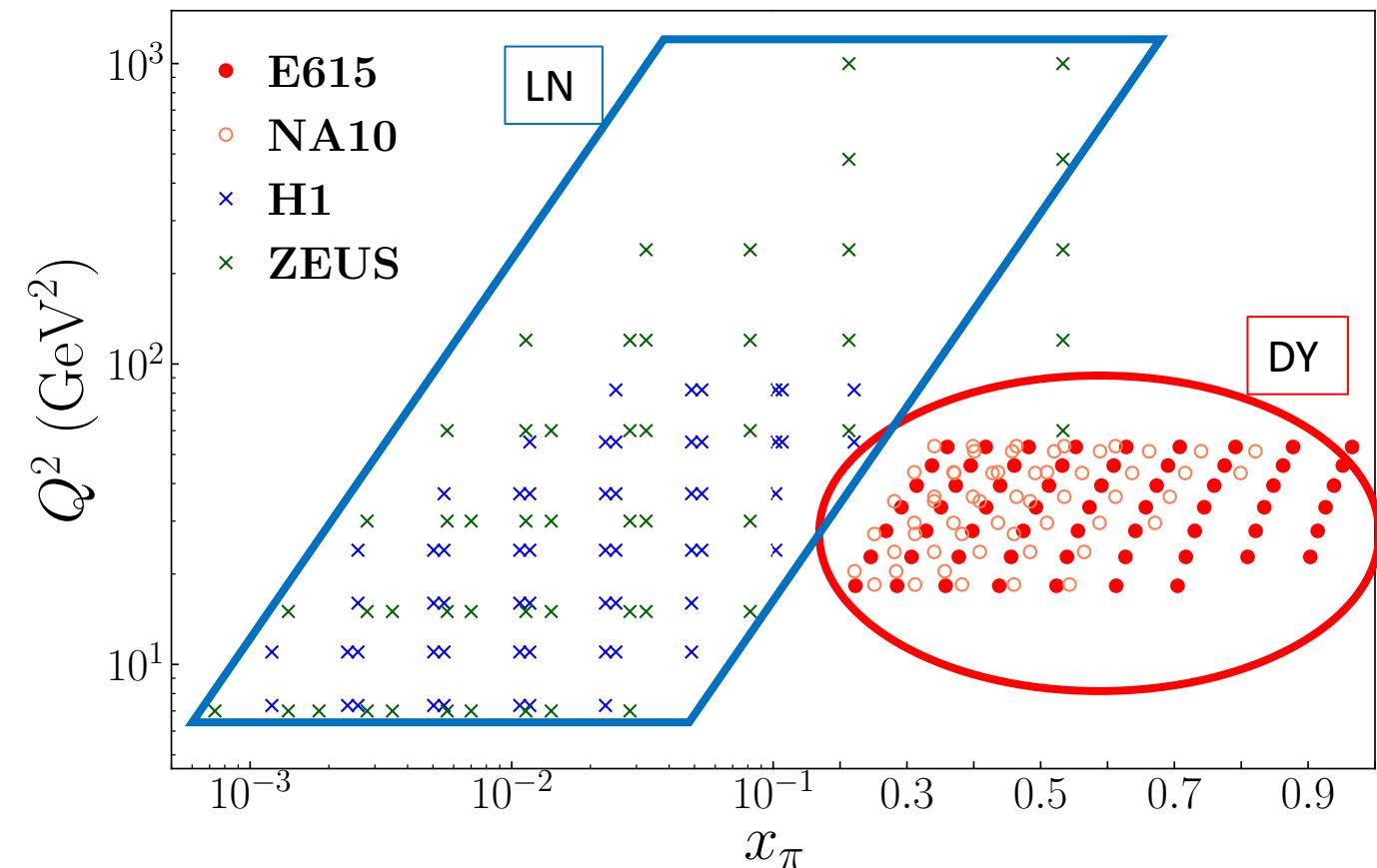
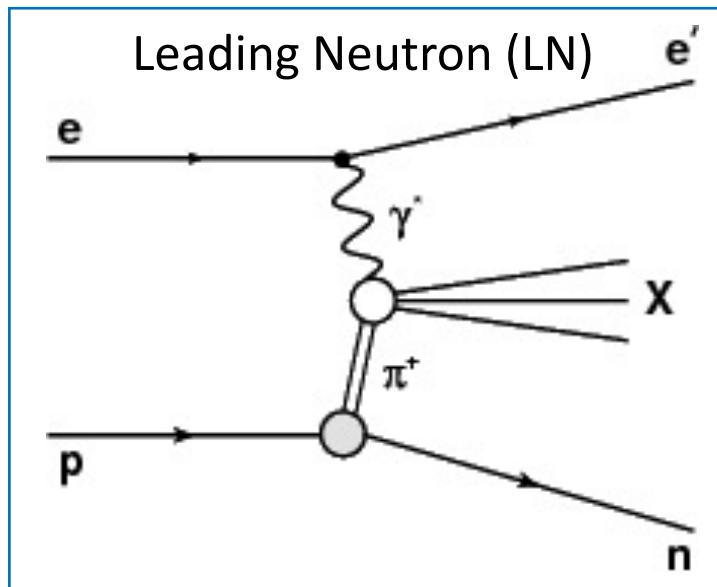
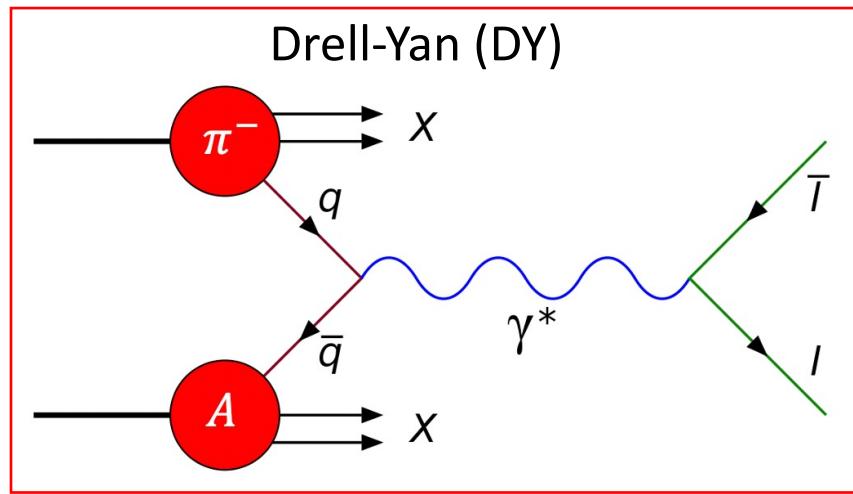
- Parametrize the **non-perturbative objects** and perform global fit
- “Good lattice cross sections” also follow this convolution structure

Pions

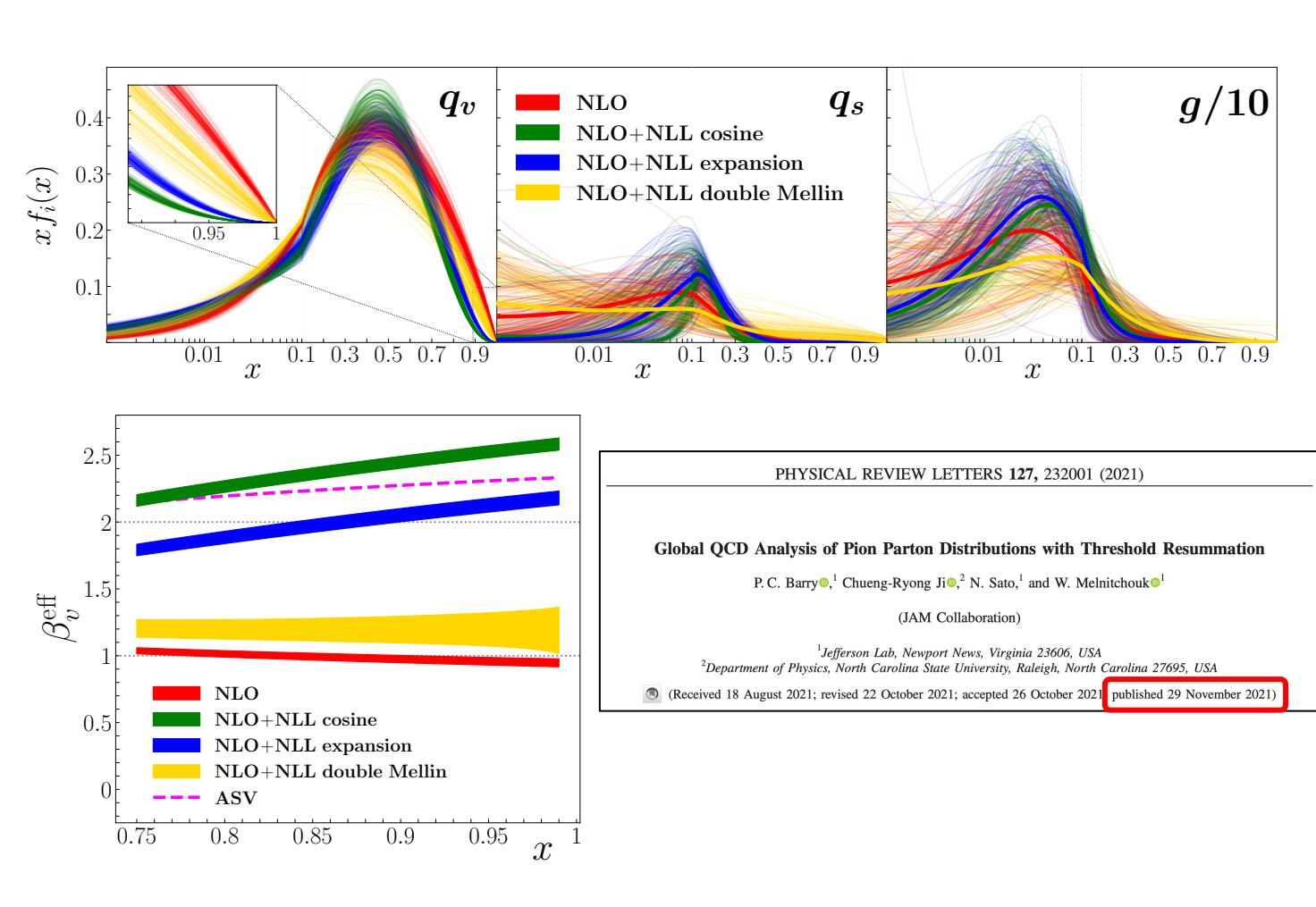
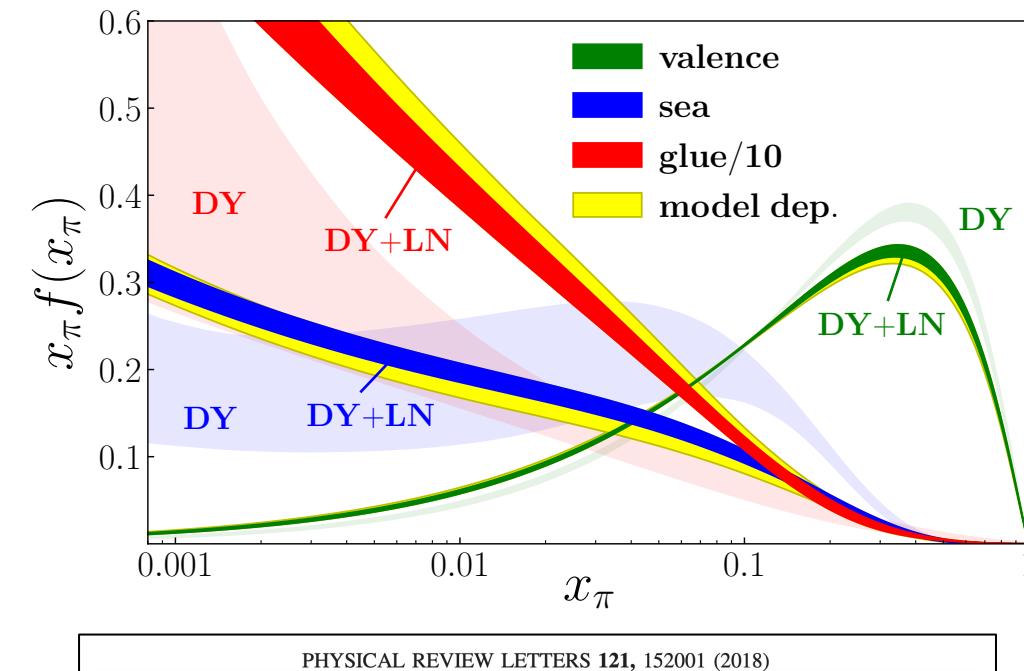
- Pion is the **Goldstone boson** associated with spontaneous symmetry breaking of chiral $SU(2)_L \times SU(2)_R$ symmetry
- Lightest hadron
- Made up of q and \bar{q} constituents



Experiments to probe pion structure



Global analyses to experimental data



Lattice QCD observables

- Lattice calculation gives the **reduced pseudo Ioffe time distribution**

$$\mathfrak{M}(\nu, z^2) = \frac{\mathcal{M}(\nu, z^2)}{\mathcal{M}(0, z^2)}$$

$\nu = p \cdot z$
“Ioffe time”

- The **UV divergences** arising from choosing the spacelike z **cancel** from taking the ratio at the rest frame $p_z = 0$

B. Joó, et al., Phys. Rev. D **100**, 114512 (2019).

Fitting the Data and Systematic Effects

$$\text{Re}[\mathfrak{M}(\nu, z^2)] = \int_0^1 dx q_v(x, \mu_{\text{lat}}) \mathcal{C}^{\text{Rp-ITD}}(x\nu, z^2, \mu_{\text{lat}}) + z^2 B_1(\nu)$$
$$+ \frac{a}{|z|} P_1(\nu) + e^{-m_\pi(L-z)} F_1(\nu) + \dots,$$

Valence quark distribution in pion

Wilson coefficients for matching

Systematic Effects to parametrize

- $z^2 B_1(\nu)$: power corrections
- $\frac{a}{|z|} P_1(\nu)$: lattice spacing errors
- $e^{-m_\pi(L-z)} F_1(\nu)$: finite volume corrections

Other potential systematic corrections the data is not sensitive to

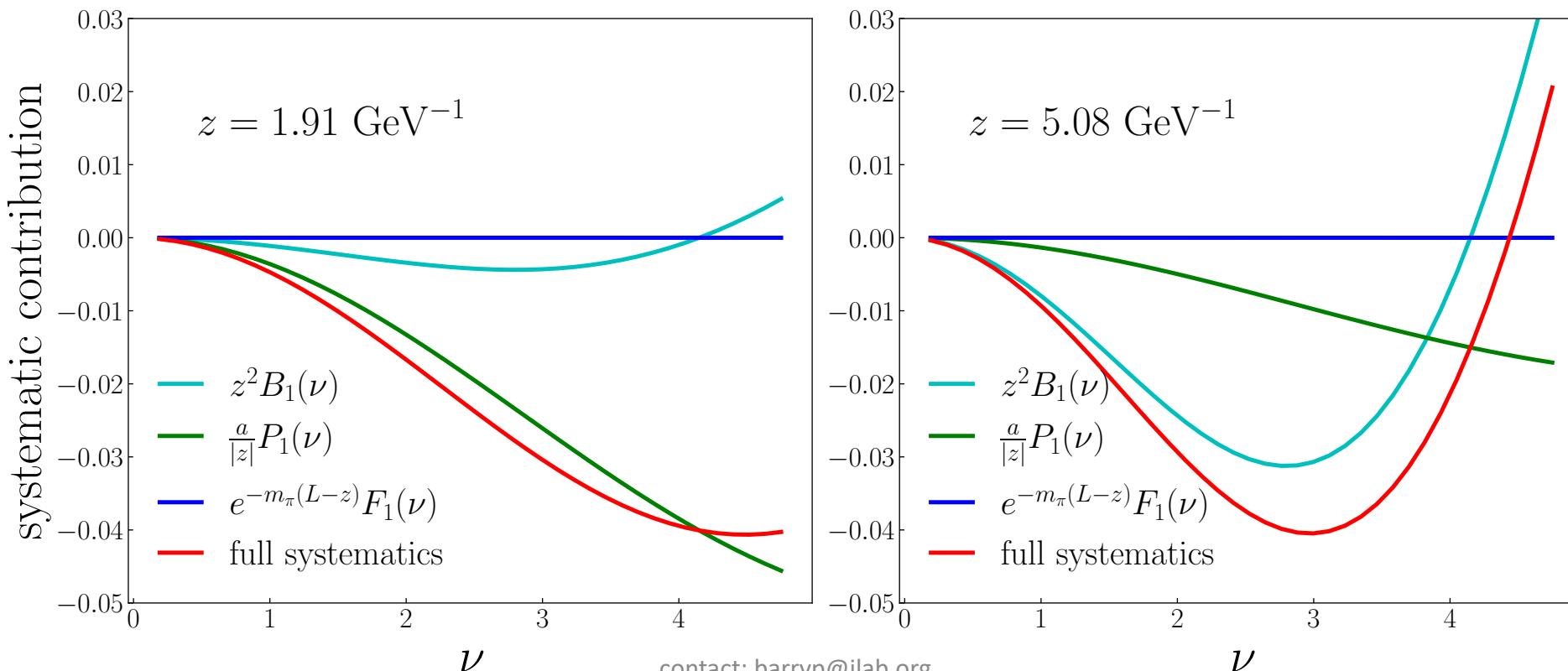
Resulting χ^2_{red}

- Scenario A: only experimental data
- Scenario B: include lattice data without fitting systematic effects
- Scenario C: Include systematics

Process	Experiment	Scenario A		Scenario B		Scenario C	
		N_{dat}	χ^2_{red}	N_{dat}	χ^2_{red}	N_{dat}	χ^2_{red}
DY	E615	61	0.82	61	0.82	61	0.82
	NA10 (194 GeV)	36	0.53	36	0.54	36	0.55
	NA10 (286 GeV)	20	0.81	20	0.79	20	0.88
LN	H1	58	0.35	58	0.39	58	0.37
	ZEUS	50	1.48	50	1.69	50	1.61
Rp-ITD	a127m415L	—	—	18	1.06	18	1.07
	a127m415	—	—	8	2.63	8	1.50
Total		225	0.80	251	0.92	251	0.88

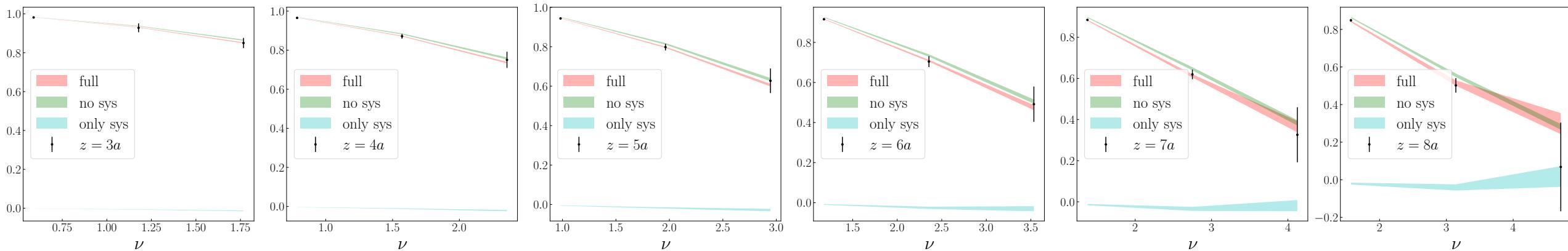
Systematic Effects

- Red curve shows the total sum of systematic corrections to the leading power terms

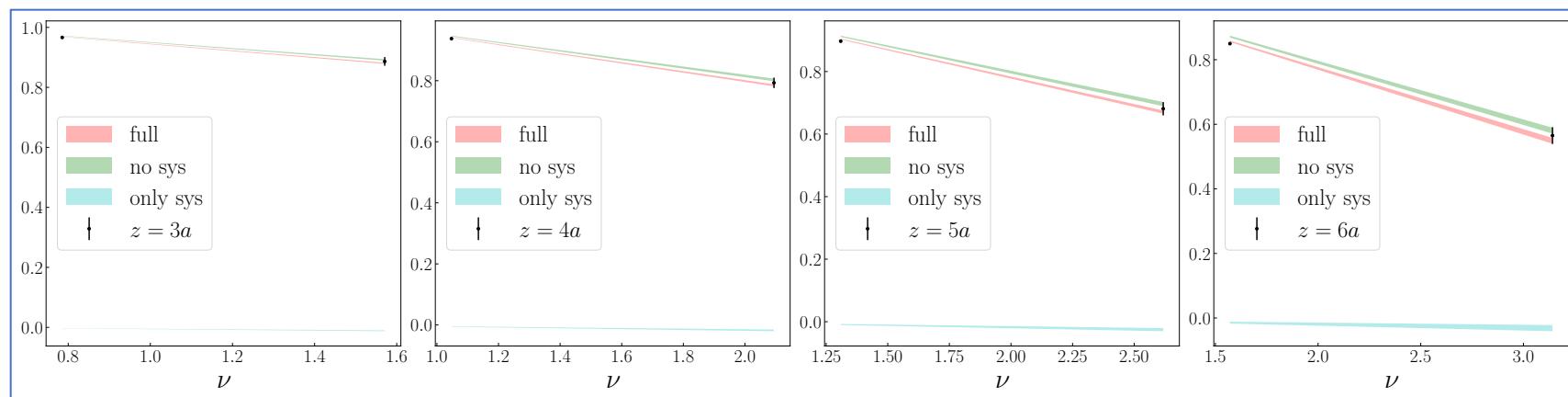


Fits to the data

Larger lattice volume



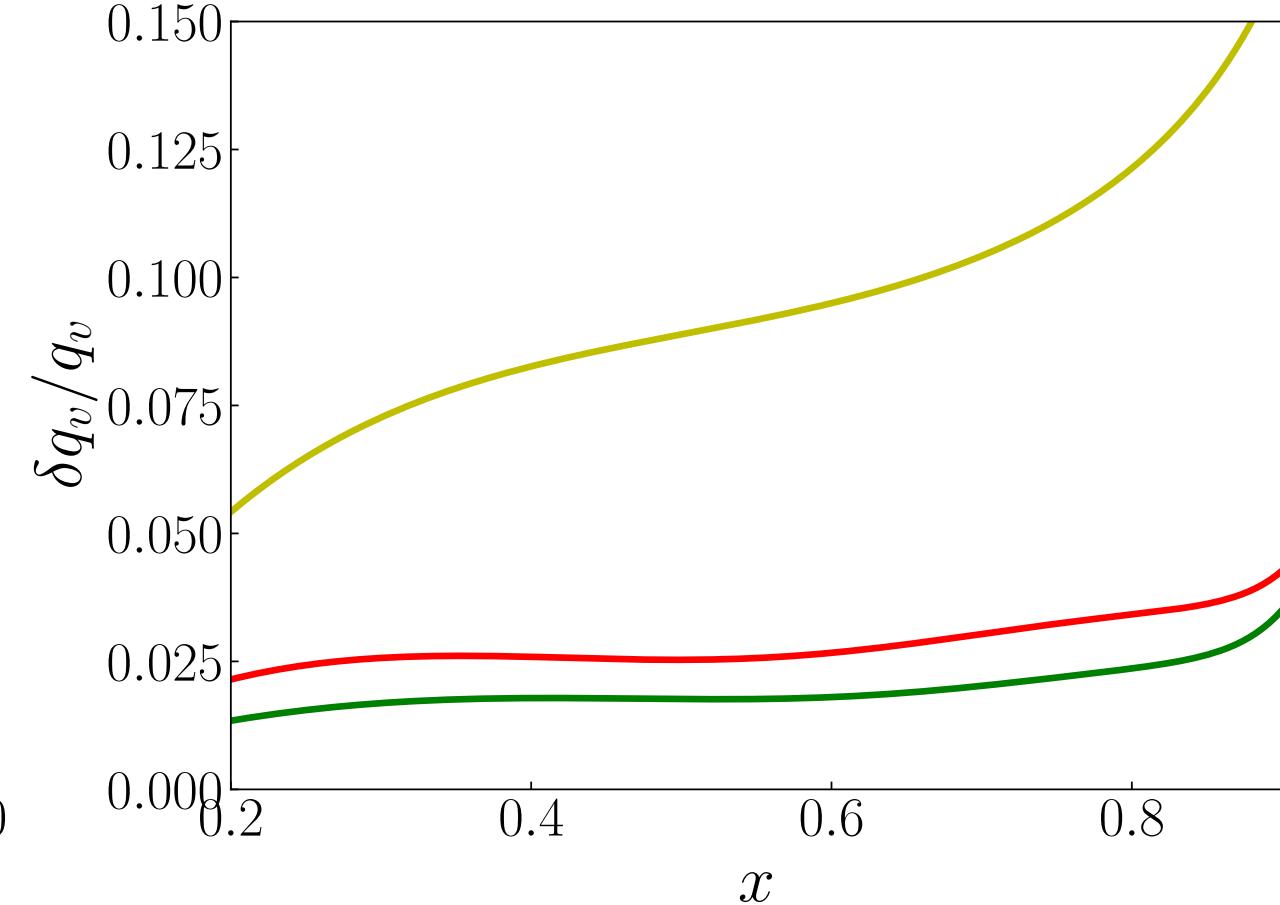
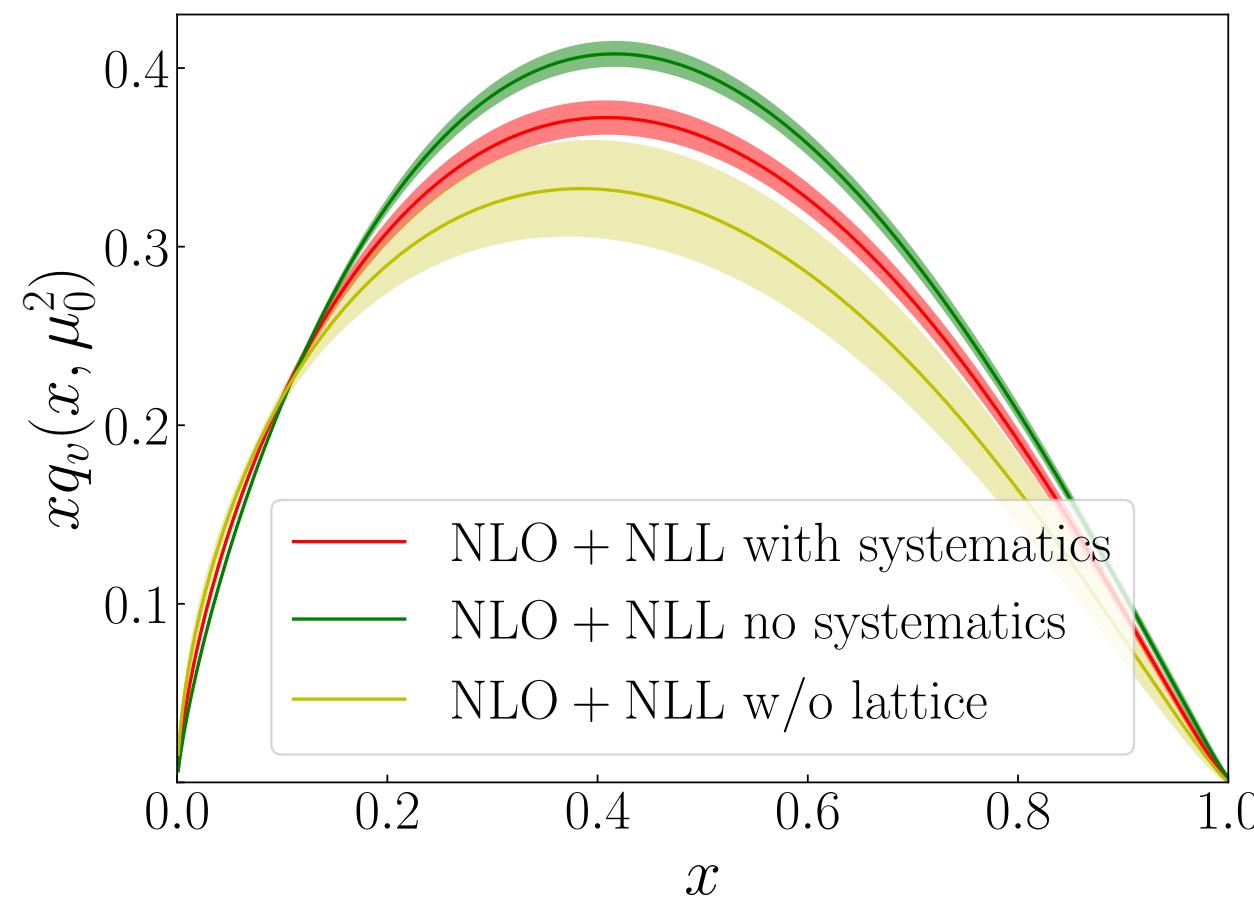
Smaller lattice volume



- Systematic effects shown in blue, are very small at low momentum and Ioffe time, ν

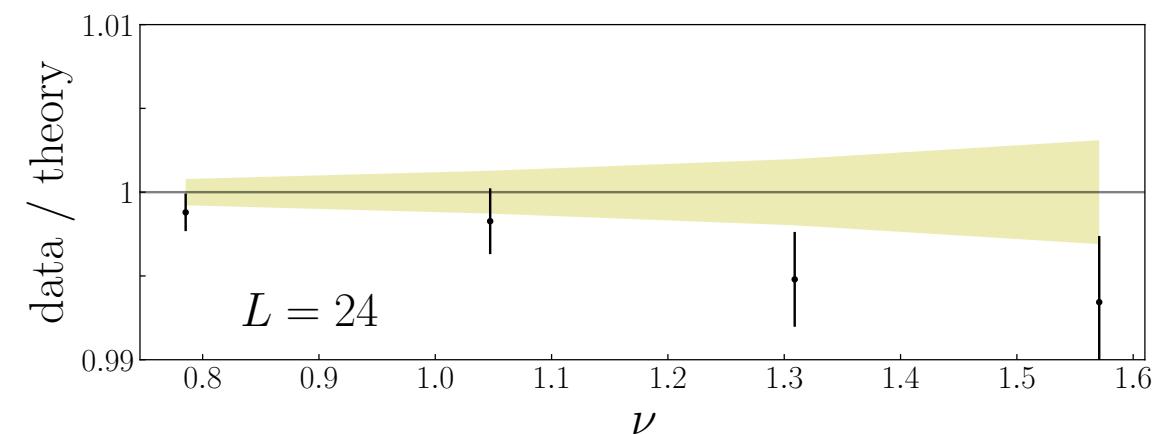
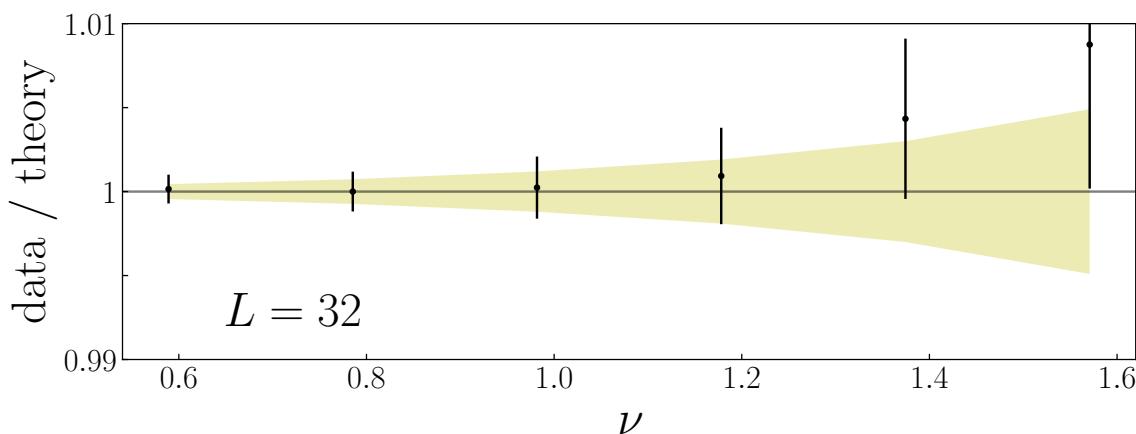
Effect on q_v^π

- Sizeable effect even when including systematics



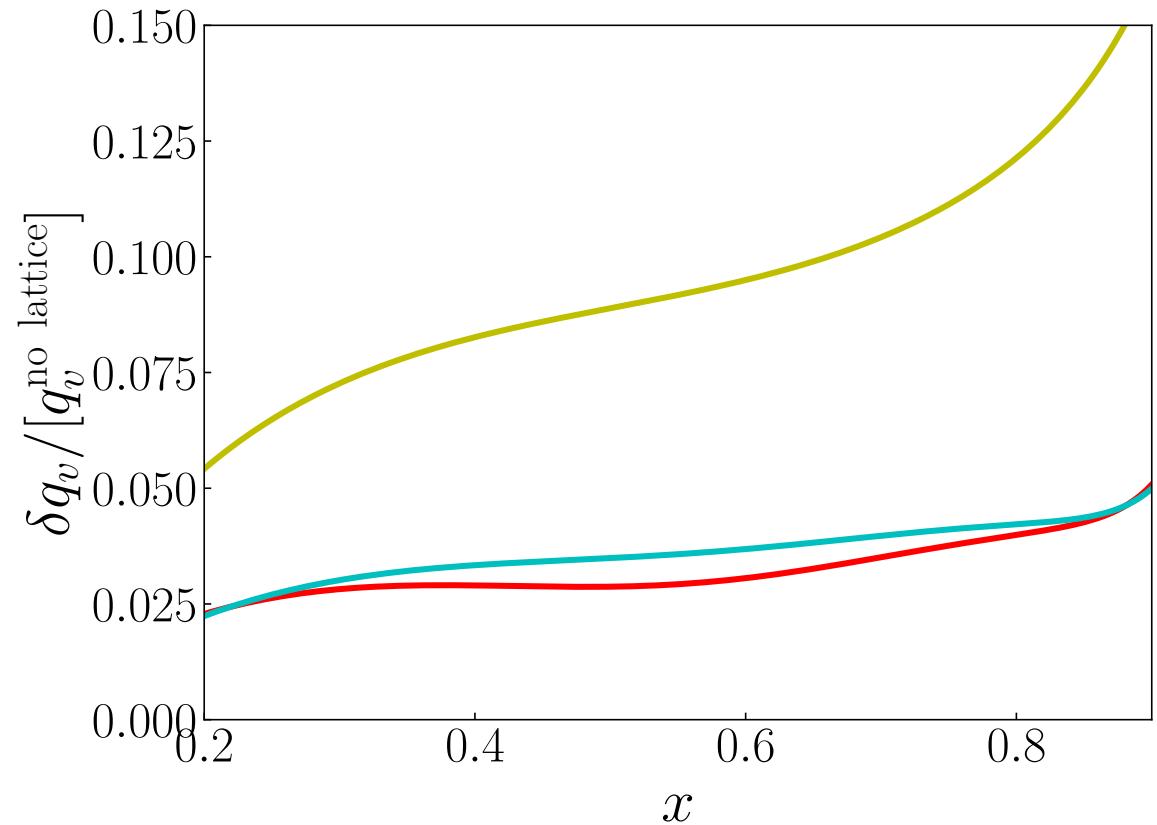
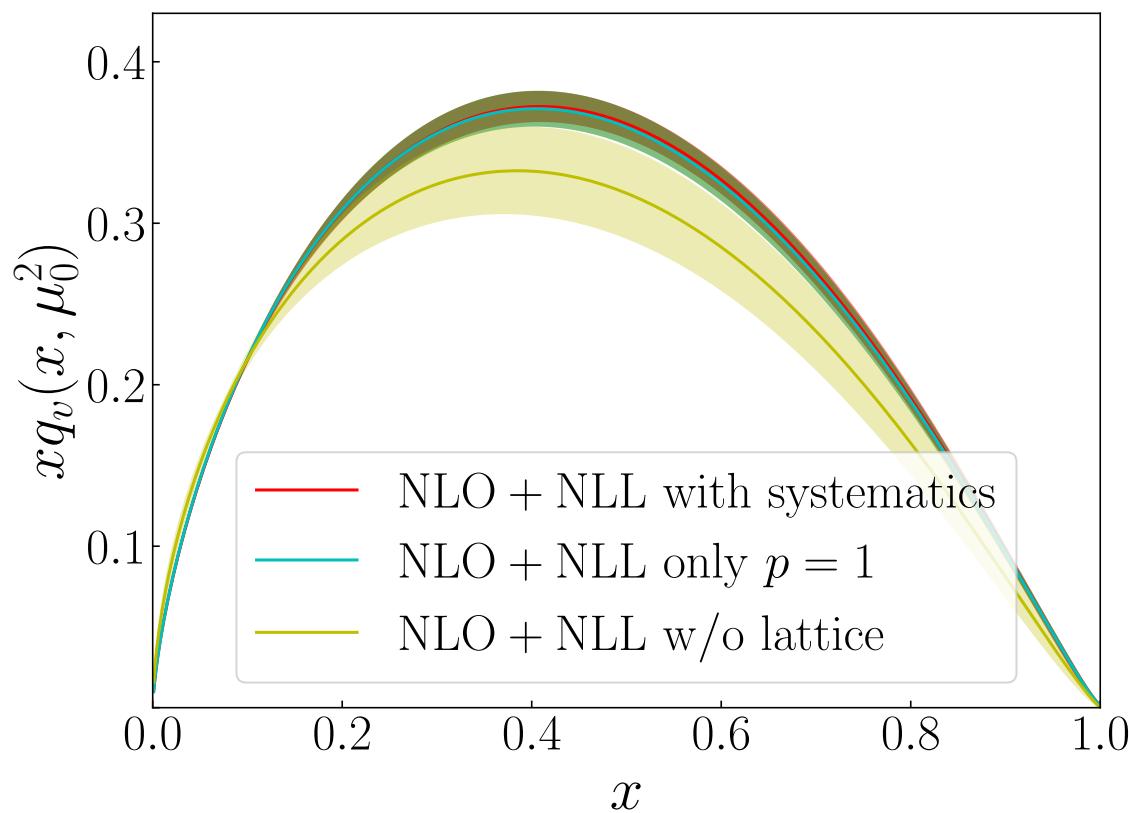
Fitting smallest momentum

- The $p = 1$ points are the most precise, and removing larger momentum can be constructive



Fitting smallest momentum

- These points provide biggest constraints



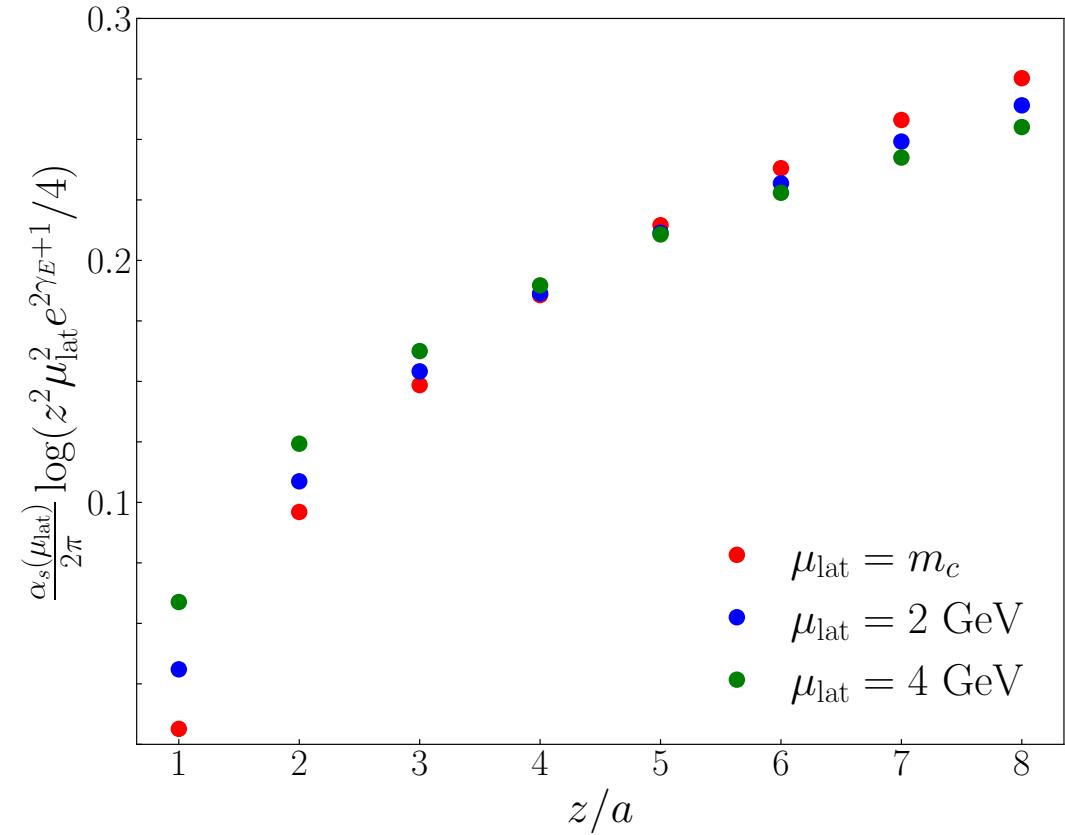
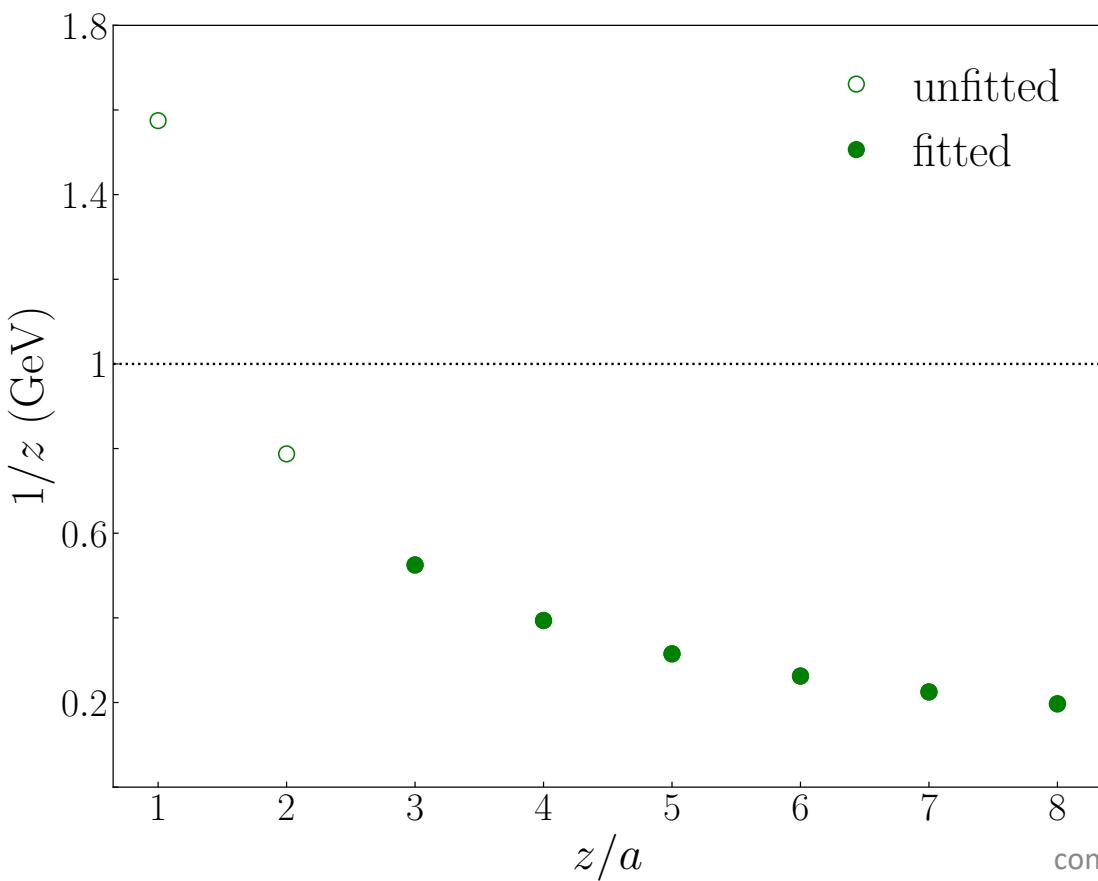
Summary

- Lattice QCD data are consistent with experimental data *and* constrain the valence quark distribution by 50-80% depending on x
- Systematic effects on the lattice have been rigorously quantified with the help of experimental data
- Focusing on data with smallest momentum will be instructive to the large- x regions of the valence quark distribution
- Final results for current-current correlator analysis coming soon
- This global analysis prefers $\beta_\nu^{\text{eff}} \sim 1$

Backup

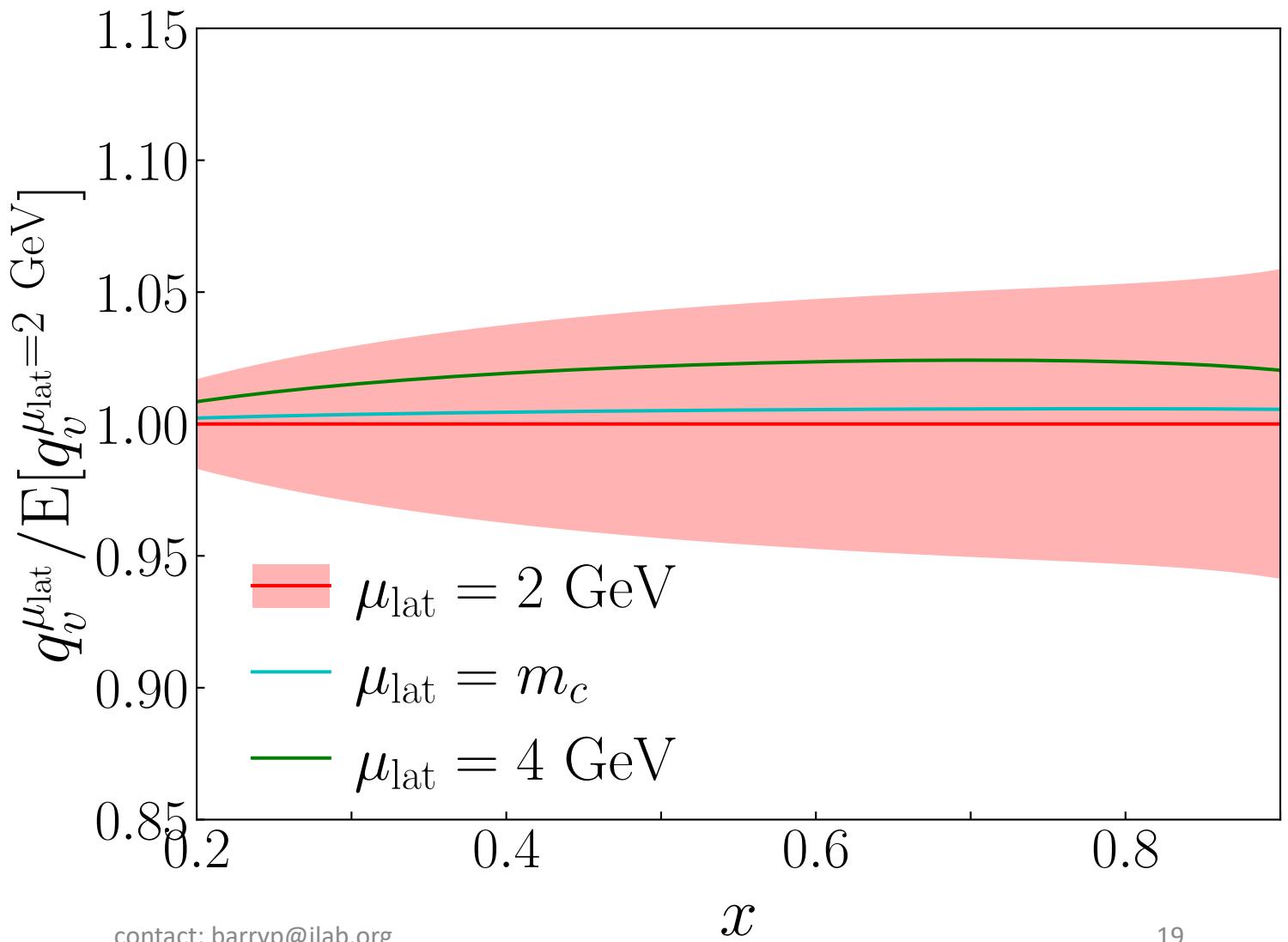
Scale setting

- $1/z$ is not quite perturbative, but fixing a scale doesn't spoil perturbation



Varying scale

- Choosing a scale
 $\mu = m_c$ or $\mu = 4\text{GeV}$ agrees with the case when $\mu = 2\text{GeV}$



Comparing with NLO

- Region from expt+lattice fits where NLO and NLO+NLL agree shows where lattice constrains the PDF in x

