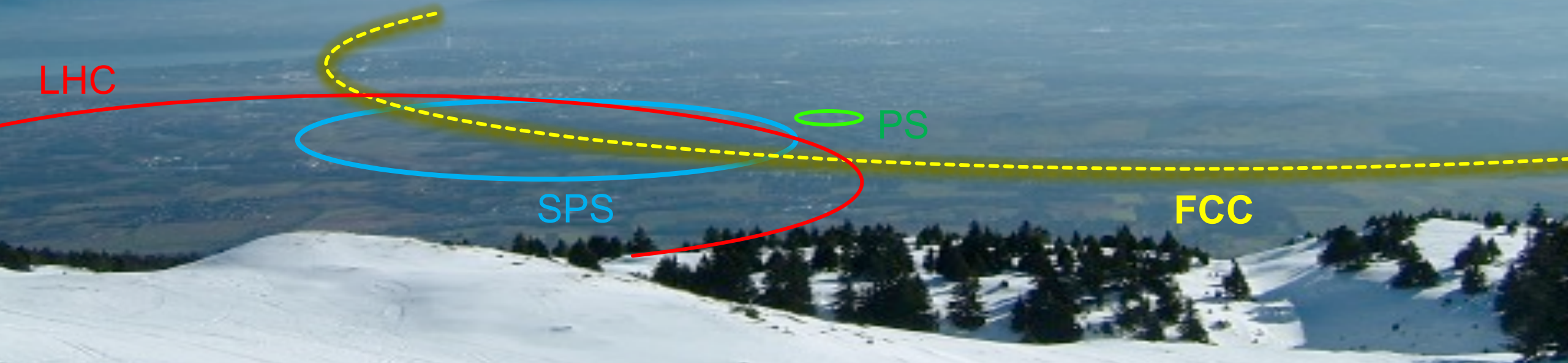


# FCC-ee – also a tau factory!

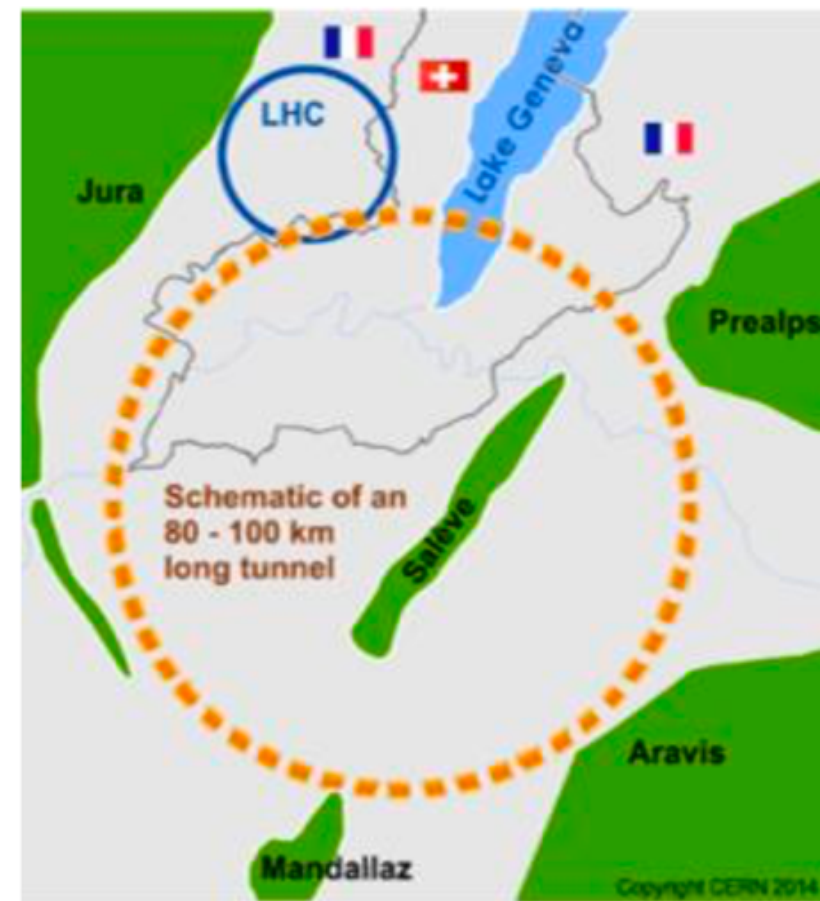
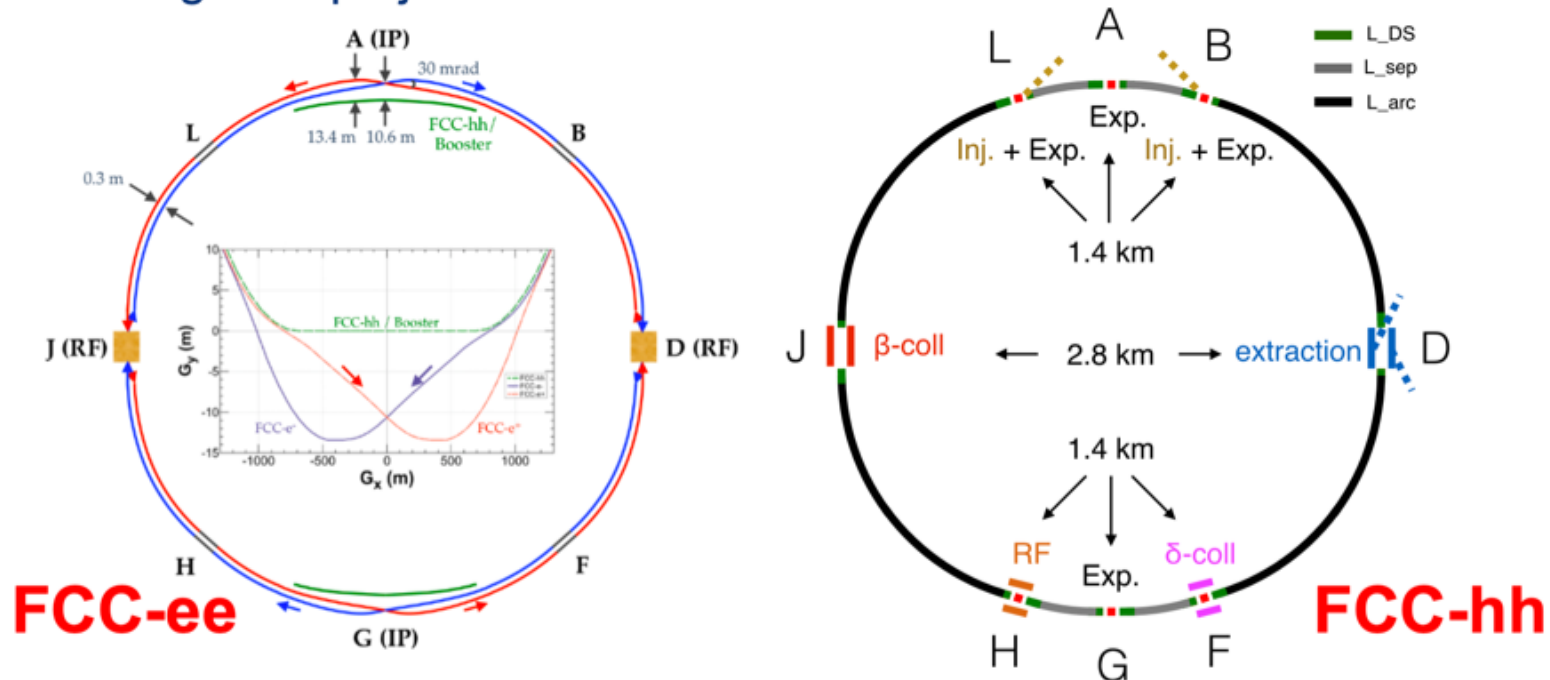
Mogens Dam  
Niels Bohr Institute



# The FCC integrated program inspired by successful LEP – LHC programs at CERN

**Comprehensive long-term program, maximizing physics opportunities**

- **Stage 1: FCC-ee (Z, W, H,  $t\bar{t}$ ) as Higgs factory, electroweak & and top factory at highest luminosities**
- **Stage 2: FCC-hh (~100 TeV) as natural continuation at energy frontier, with ion and eh options**
- Complementary physics
- Common civil engineering and technical infrastructures
- Building on and reusing CERN's existing infrastructure
- FCC integrated project allows seamless continuation of HEP after HL-LHC



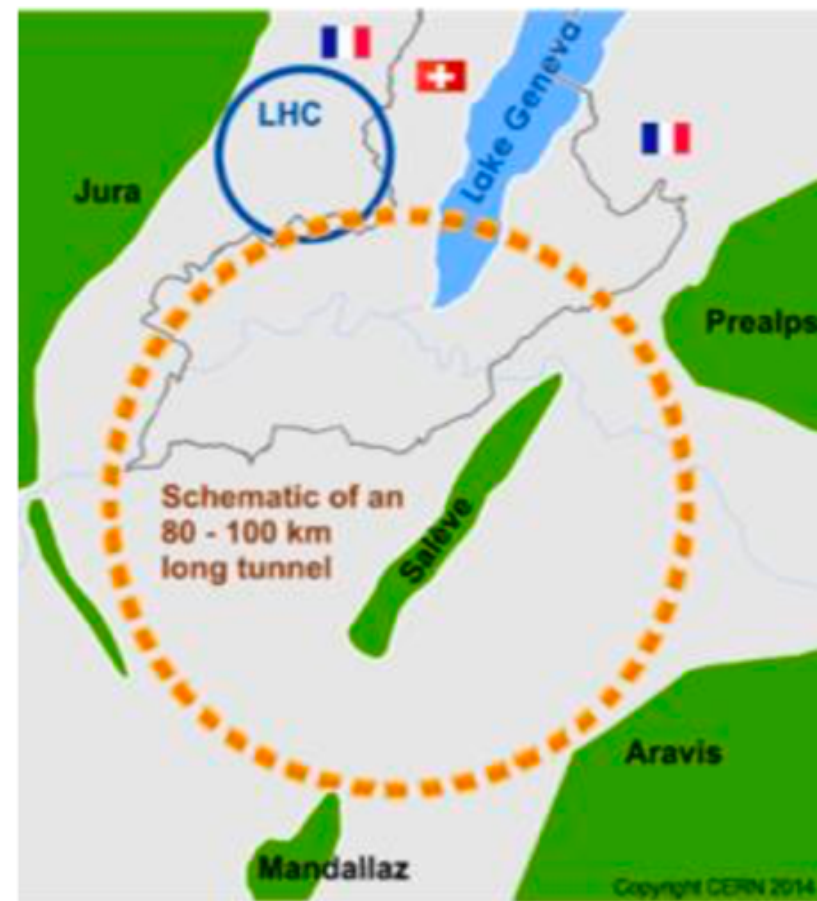
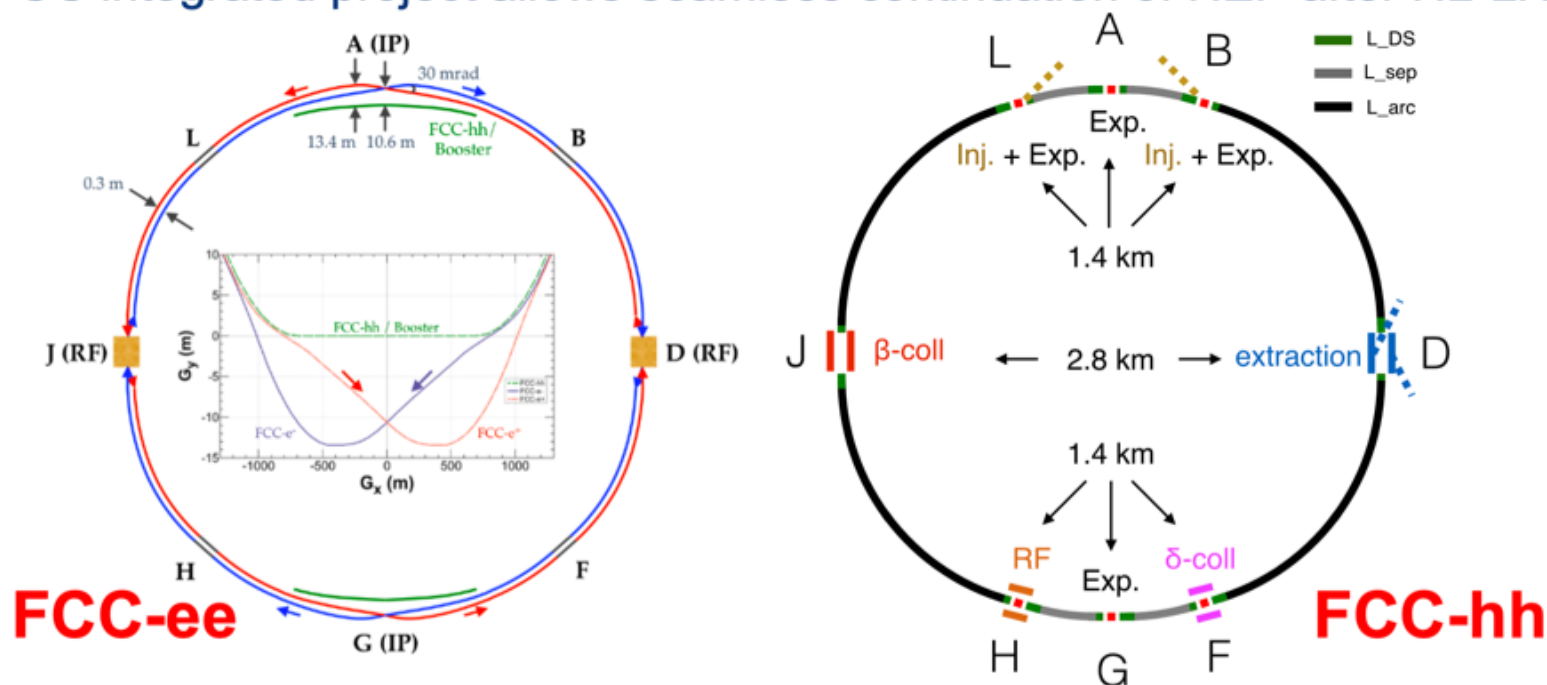


# The FCC integrated program inspired by successful LEP – LHC programs at CERN

and  $\tau$

Comprehensive long-term program, maximizing physics opportunities

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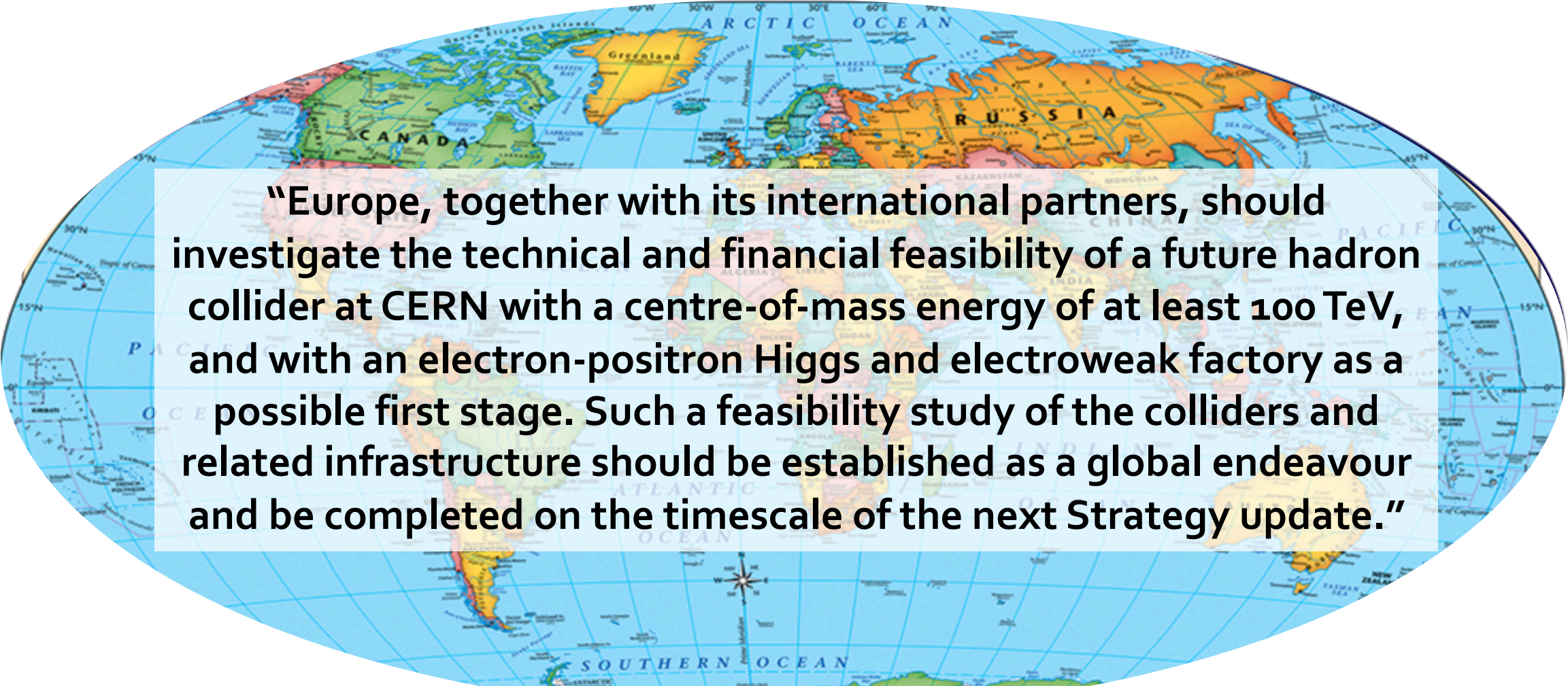


**“Europe, together with its international partners, should investigate the technical and financial feasibility of a future hadron collider at CERN with a centre-of-mass energy of at least 100 TeV, and with an electron-positron Higgs and electroweak factory as a possible first stage. Such a feasibility study of the colliders and related infrastructure should be established as a global endeavour and be completed on the timescale of the next Strategy update.”**

Feasibility study of the colliders (ee and hh) and related infrastructure

**FCC is the highest priority future initiative (plan A)**





**“Europe, together with its international partners, should investigate the technical and financial feasibility of a future hadron collider at CERN with a centre-of-mass energy of at least 100 TeV, and with an electron-positron Higgs and electroweak factory as a possible first stage. Such a feasibility study of the colliders and related infrastructure should be established as a global endeavour and be completed on the timescale of the next Strategy update.”**

Feasibility study of the colliders (ee and hh) and related infrastructure  
**FCC is the highest priority future initiative (plan A)**

◆ June 2021:

The FCC Feasibility Study (2021-2025) organization proposed to CERN council and approved unanimously

□ Council documents :

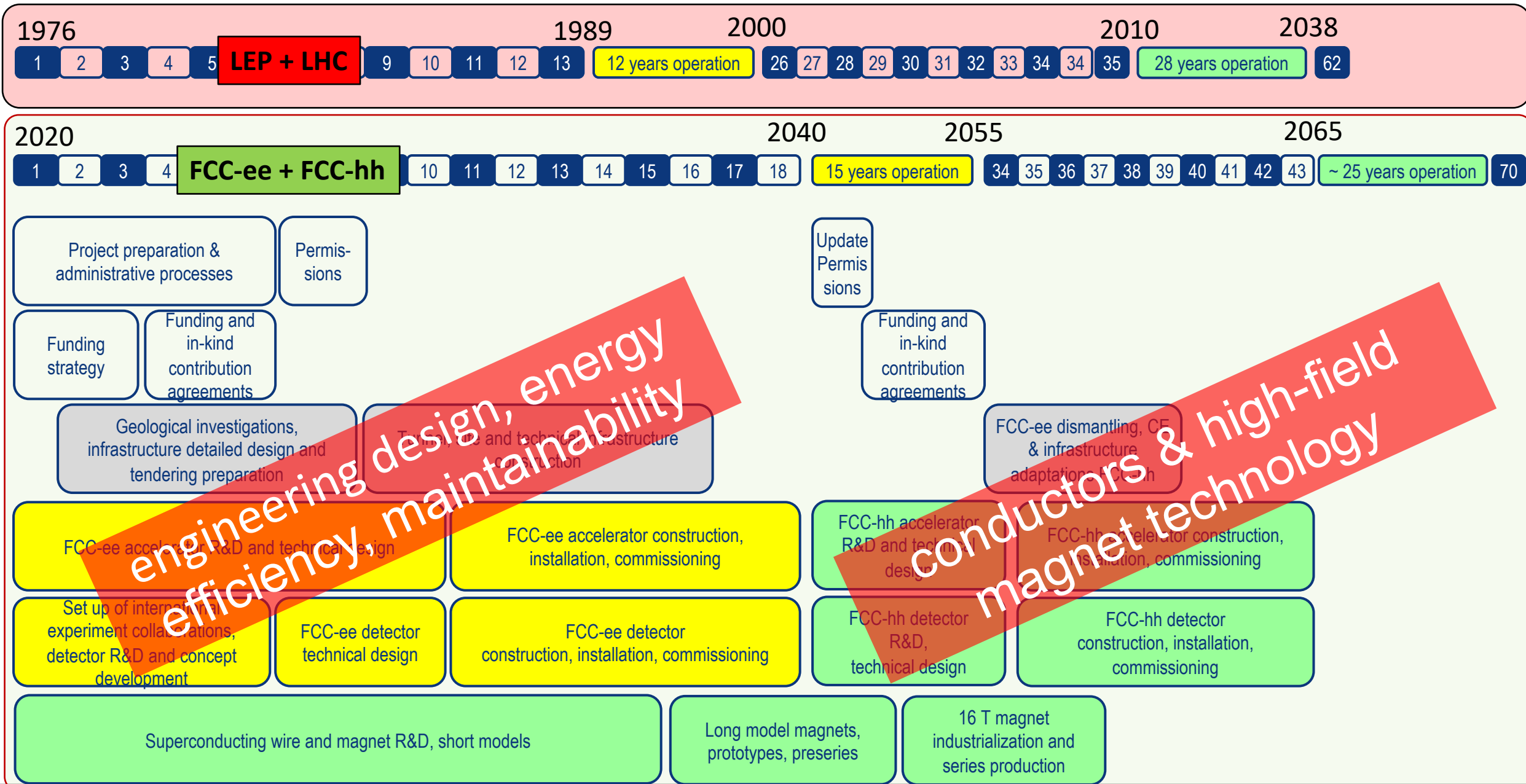
- ❖ Organisational structure of the FCC feasibility study <http://cds.cern.ch/record/2774006/files/English.pdf>
- ❖ Main deliverables and timeline of the FCC feasibility study <http://cds.cern.ch/record/2774007/files/English.pdf>

*"The focus will be on the tunnel and the first-stage collider (FCC-ee)"*

- Intermediate review mid 2023, delivery of Feasibility Study Report (FSR) end 2025, first collisions 2040+
  - Stress importance of communication towards **scientific community**, governments and funding agencies, industries and general public
- ◆ Work has started on placement in Geneva area (France and Switzerland)
- Reduce number of surface points from 12 to 8
    - ❖ This layout is consistent with later choice of 2 or 4IP for the  $e^+e^-$  collider
- ◆ In parallel, high field magnet R&D for FCC-hh will be carried out with high priority

**These events bring FCC-ee and FCC-hh one big step closer to reality**

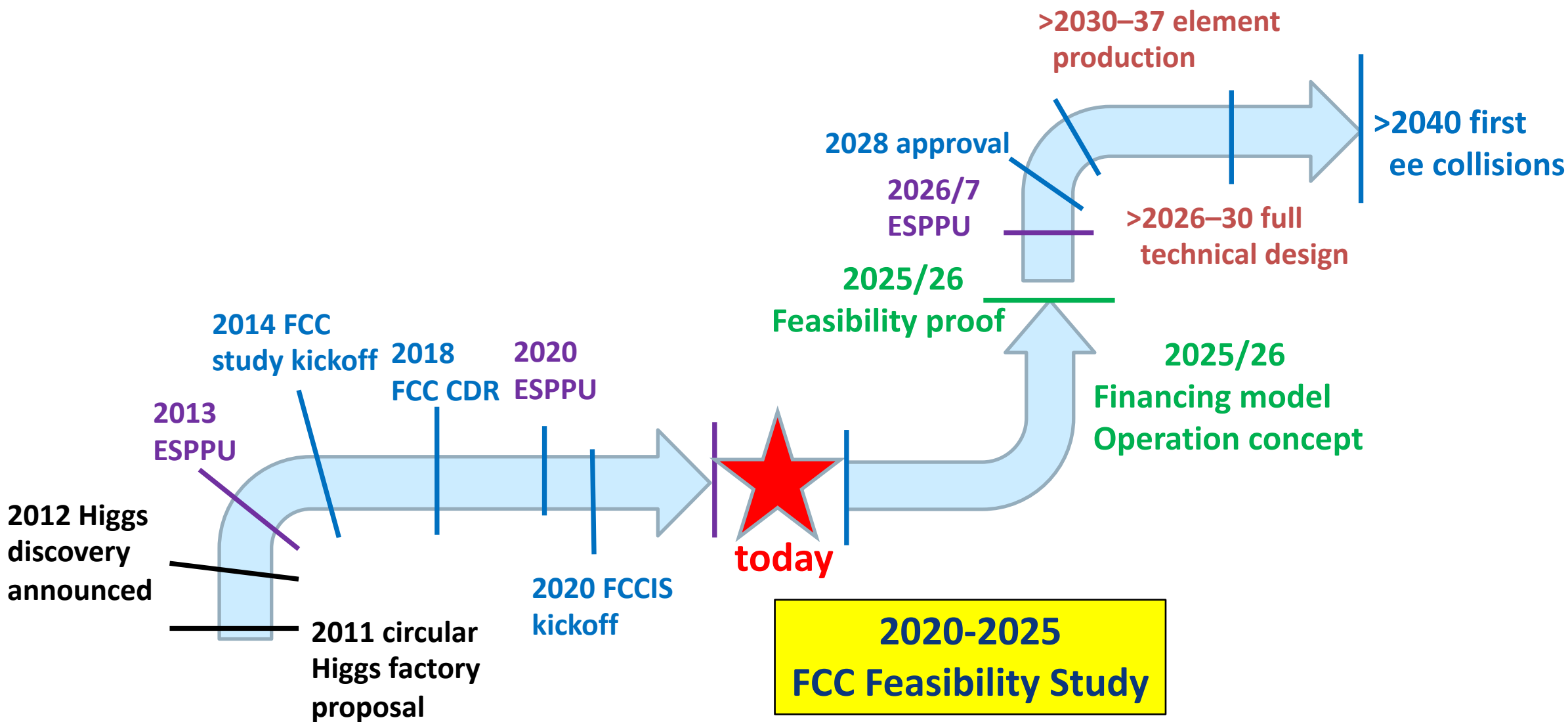
# FCC-INT Timeline (compared to LEP + LHC)



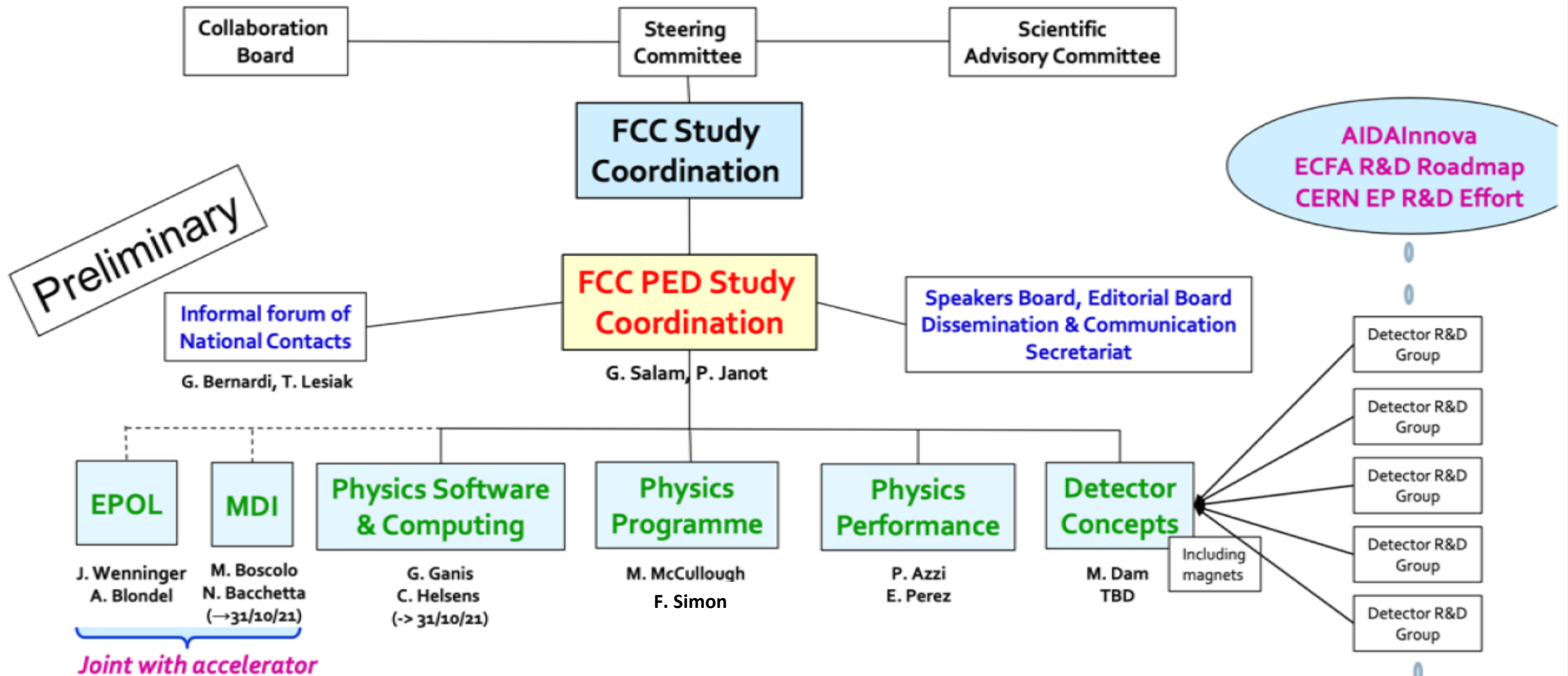
**engineering design, energy efficiency, maintainability**

**conductors & high-field magnet technology**





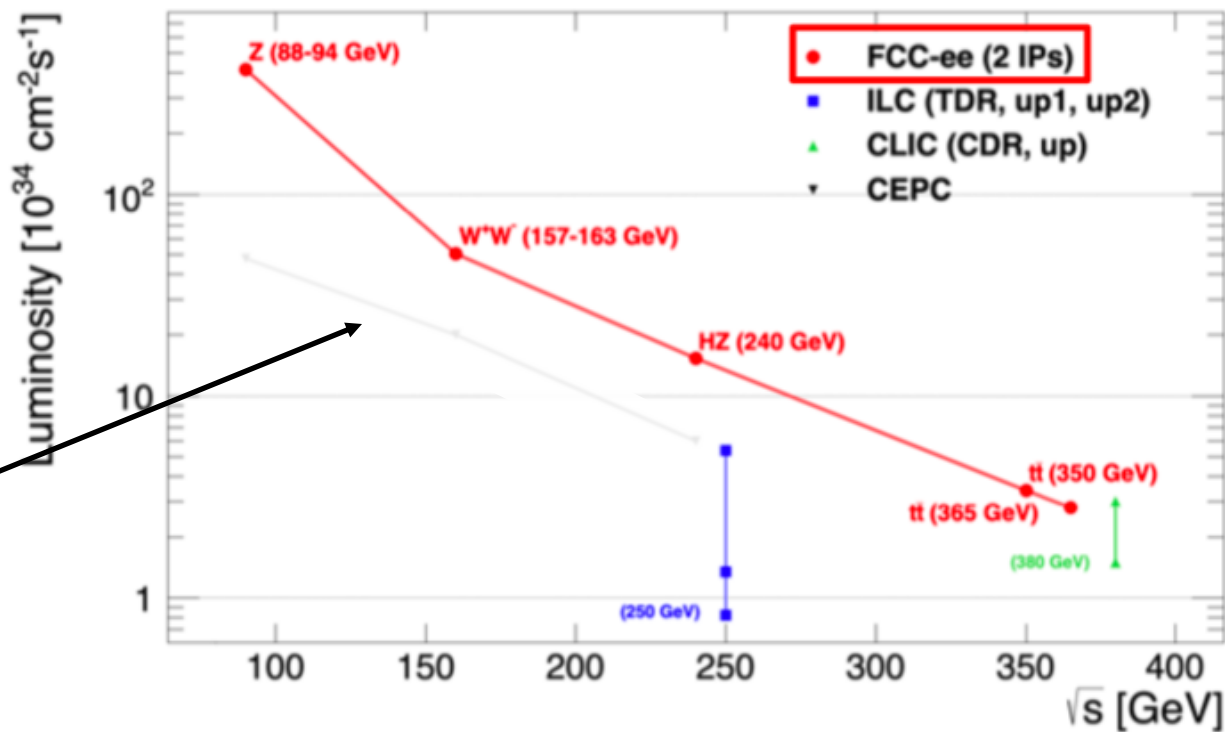
## The PED Pillar Organisation - preliminary



Patrick Janot and Gavin Salam

FCC PED General Physics meeting  
27 Sep 2021

3



Have removed CEPC projection.  
See talk by M. Ruan

In this talk, concentrate on the Z-pole energy point

Enormous statistics of Z bosons and of  $\tau$  leptons

|                              |                      |
|------------------------------|----------------------|
| Z decays                     | $5 \times 10^{12}$   |
| $Z \rightarrow \tau^+\tau^-$ | $1.7 \times 10^{11}$ |
| 1 vs. 3 prongs               | $4.2 \times 10^{10}$ |
| 3 vs. 3 prong                | $3.6 \times 10^9$    |
| 1 vs. 5 prong                | $2.8 \times 10^8$    |
| 1 vs. 7 prong                | $< 87,000$           |
| 1 vs 9 prong                 | ?                    |

|                      |                           |                    |                               |         |
|----------------------|---------------------------|--------------------|-------------------------------|---------|
| Z peak               | $E_{CM}: 91 \text{ GeV}$  | $5 \times 10^{12}$ | $e^+e^- \rightarrow Z$        | 4 years |
| WW threshold         | $E_{CM}: 161 \text{ GeV}$ | $10^8$             | $e^+e^- \rightarrow WW$       | 1 year  |
| ZH threshold         | $E_{CM}: 240 \text{ GeV}$ | $10^6$             | $e^+e^- \rightarrow ZH$       | 3 years |
| $t\bar{t}$ threshold | $E_{CM}: 350 \text{ GeV}$ | $10^6$             | $e^+e^- \rightarrow t\bar{t}$ | 5 years |



- a.  $\tau$  Polarisation Measurement
- b.  $\tau$ -lepton Properties and Lepton Universality
- c. Lepton Flavour Violating Z decays
- d. Lepton Flavour Violating  $\tau$  decays
- e.  $\tau$  leptons in B decays

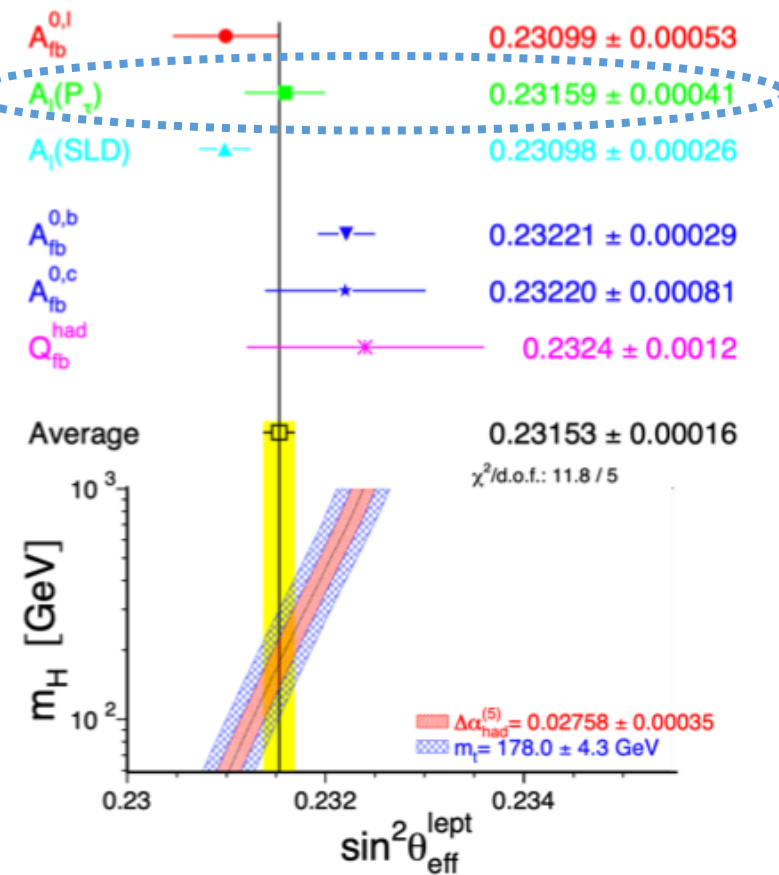
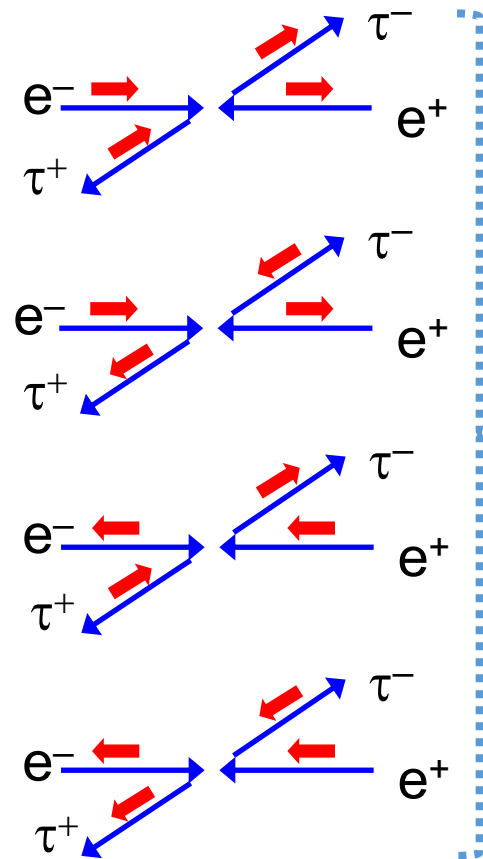
## References:

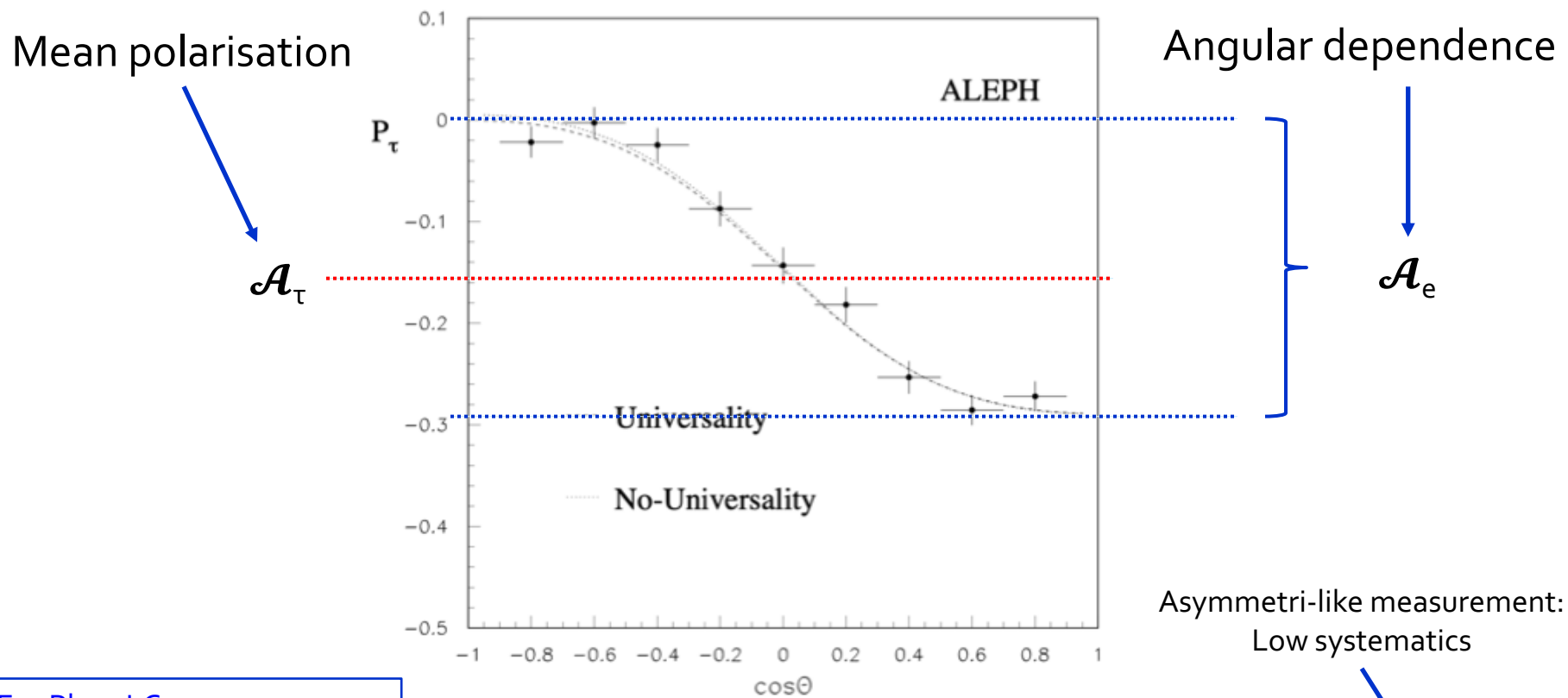
- FCC CDR Volume 1
- MD, *Tau-lepton Physics at the FCC-ee circular  $e^+e^-$  Collider*, SciPost Phys.Proc. 1 (2019) 041,  
DOI: [10.21468/SciPostPhysProc.1.041](https://doi.org/10.21468/SciPostPhysProc.1.041)
- MD, *The  $\tau$  challenges at FCC-ee*,  
*Eur. Phys. J. Plus* **136**, 963 (2021)  
DOI: [10.1140/epjp/s13360-021-01894-y](https://doi.org/10.1140/epjp/s13360-021-01894-y)
- Yasmine Amhis et al, *Prospects of  $B_c \rightarrow \tau\nu$  at FCC-ee*,  
[arXiv:2105.13333](https://arxiv.org/abs/2105.13333)

tau2018



# τ Polarisation Measurement





Eur.Phys.J.C20:401-430,2001

$$\mathcal{A}_\tau = 0.1451 \pm 0.0052 \pm 0.0029$$

$$\mathcal{A}_e = 0.1504 \pm 0.0068 \pm 0.0008$$

$$\Rightarrow \text{assuming universality: } \sin^2\theta_W^{\text{eff}} = 0.23130 \pm 0.00048$$



Use  $\tau$  decays as spin analysers (V-A)

- Two helicity states result in different kinematic distributions that are fitted to observed distribution of appropriate variables
- Divide (typically) into six decay modes

Important aspects

- Selection of  $e^+e^- \rightarrow \tau^+\tau^-$  events
  - Backgrounds from  $qq, ee, \mu\mu, \gamma\gamma$
- Interchannel separation
  - Mainly internally between  $h+n\pi^0$  states => **Photon** and  $\pi^0$  reconstruction
- Selection efficiency and backgrounds as function of kinematic variables
- Reconstruction of kinematic variables

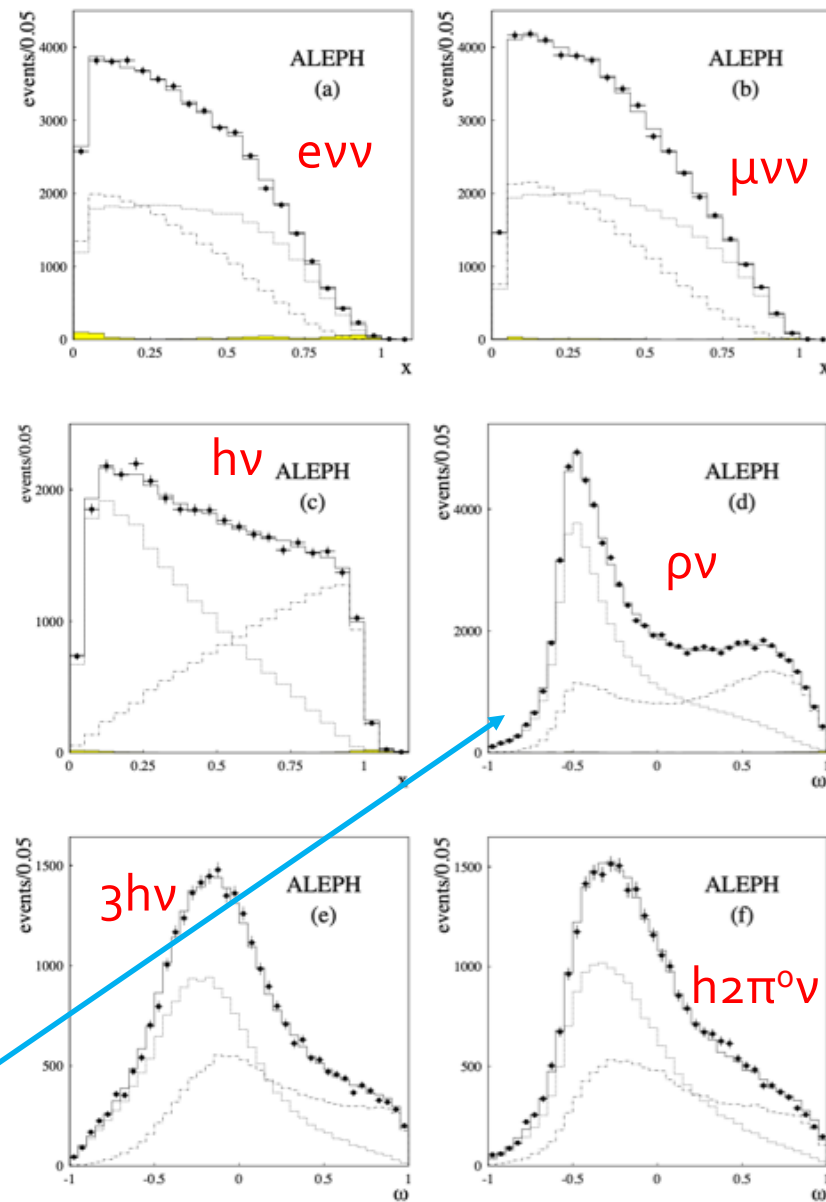
Example:  $\tau^- \rightarrow \rho^-\nu \rightarrow \pi^-\pi^0\nu$

- Here polarisation is extracted from two angles

$$\cos \theta \propto \frac{E_{\pi^-} + E_{\pi^0}}{E_{\text{beam}}} \quad \cos \psi \propto \frac{E_{\pi^-} - E_{\pi^0}}{E_{\pi^-} + E_{\pi^0}}$$

$\pi^- \pi^0$  energy      sum      difference

Combined into 1D "optimal observable"



## Obtained results

| Channel         | $\mathcal{A}_\tau$ (%)    | $\mathcal{A}_e$ (%)       |
|-----------------|---------------------------|---------------------------|
| hadron          | $15.21 \pm 0.98 \pm 0.49$ | $15.28 \pm 1.30 \pm 0.12$ |
| rho             | $13.79 \pm 0.84 \pm 0.38$ | $14.66 \pm 1.12 \pm 0.09$ |
| a1(3h)          | $14.77 \pm 1.60 \pm 1.00$ | $13.58 \pm 2.11 \pm 0.40$ |
| a1(h2 $\pi^0$ ) | $16.34 \pm 2.06 \pm 1.52$ | $15.62 \pm 2.72 \pm 0.47$ |
| electron        | $13.64 \pm 2.33 \pm 0.96$ | $14.09 \pm 3.17 \pm 0.91$ |
| muon            | $13.64 \pm 2.09 \pm 0.93$ | $11.77 \pm 2.77 \pm 0.25$ |
| pion inclusive  | $14.93 \pm 0.83 \pm 0.87$ | $14.91 \pm 1.11 \pm 0.17$ |
| Combined        | $14.44 \pm 0.55 \pm 0.27$ | $14.58 \pm 0.73 \pm 0.10$ |

Eur.Phys.J.C20:401-430,2001

Most precise channels

systematics

| Source            |      |        | $\mathcal{A}_\tau$ |            |      |       |         |
|-------------------|------|--------|--------------------|------------|------|-------|---------|
|                   | $h$  | $\rho$ | 3h                 | h2 $\pi^0$ | e    | $\mu$ | Incl. h |
| selection         | -    | 0.01   | -                  | -          | 0.14 | 0.02  | 0.08    |
| tracking          | 0.06 | -      | 0.22               | -          | -    | 0.10  | -       |
| ECAL scale        | 0.15 | 0.11   | 0.21               | 1.10       | 0.47 | -     | -       |
| PID               | 0.15 | 0.06   | 0.04               | 0.01       | 0.07 | 0.07  | 0.18    |
| misid.            | 0.05 | -      | -                  | -          | 0.08 | 0.03  | 0.05    |
| photon            | 0.22 | 0.24   | 0.37               | 0.22       | -    | -     | -       |
| non- $\tau$ back. | 0.19 | 0.08   | 0.05               | 0.18       | 0.54 | 0.67  | 0.15    |
| $\tau$ BR         | 0.09 | 0.04   | 0.10               | 0.26       | 0.03 | 0.03  | 0.78    |
| modelling         | -    | -      | 0.70               | 0.70       | -    | -     | 0.09    |
| MC stat           | 0.30 | 0.26   | 0.49               | 0.63       | 0.61 | 0.63  | 0.26    |
| TOTAL             | 0.49 | 0.38   | 1.00               | 1.52       | 0.96 | 0.93  | 0.87    |

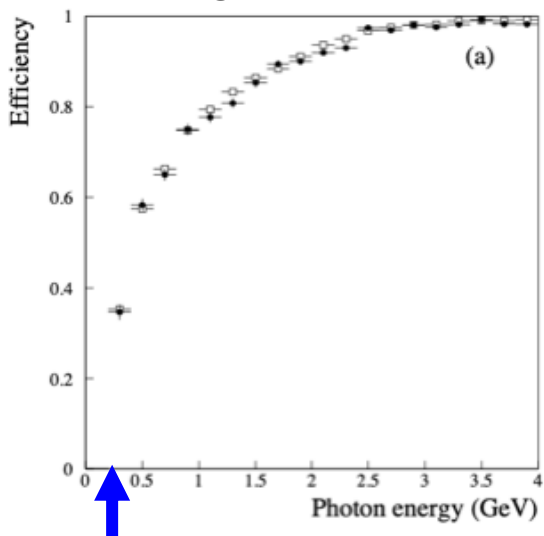
  

| Source            |      |        | $\mathcal{A}_e$ |            |      |       |         |
|-------------------|------|--------|-----------------|------------|------|-------|---------|
|                   | $h$  | $\rho$ | 3h              | h2 $\pi^0$ | e    | $\mu$ | Incl. h |
| tracking          | 0.04 | -      | -               | -          | -    | 0.05  | -       |
| non- $\tau$ back. | 0.11 | 0.09   | 0.04            | 0.22       | 0.91 | 0.24  | 0.17    |
| modelling         | -    | -      | 0.40            | 0.40       | -    | -     | -       |
| TOTAL             | 0.12 | 0.09   | 0.40            | 0.47       | 0.91 | 0.25  | 0.17    |

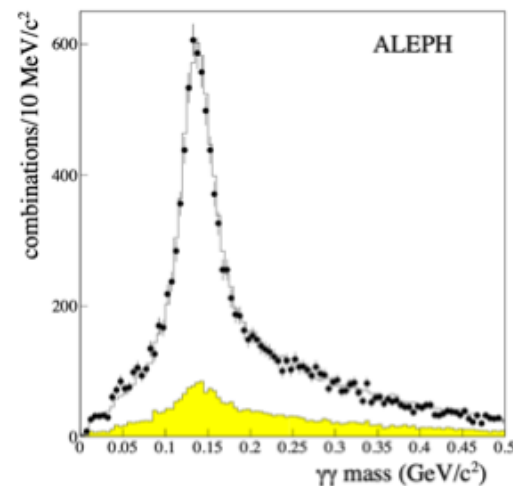
- LEP measurement statistics limited
- At FCC-ee,  $\sim 10^{5-6}$  larger statistics:  
Need (much) reduced systematics

The single most important systematics (on the most precise channels) is due to photon and  $\pi^0$  identification

Foton reconstruction efficiency.  
Starting at 250 MeV



$\gamma\gamma$  mass of additional photons in hemispheres  
where one  $\pi^0$  has been already identified



Migration matrix (part)

reconstructed

|           | $e$   | $\mu$ | $h$   | $h\pi^0$ | $h2\pi^0$ | $h3\pi^0$ | $h4\pi^0$ | $3h$  |
|-----------|-------|-------|-------|----------|-----------|-----------|-----------|-------|
| $e$       | 73.26 | 0.01  | 0.41  | 0.45     | 0.34      | 0.25      | 0.74      | 0.02  |
| $\mu$     | 0.01  | 74.49 | 0.63  | 0.22     | 0.07      | 0.21      | 0.33      | 0.01  |
| $h$       | 0.25  | 0.75  | 65.03 | 3.56     | 0.34      | 0.06      | 0.00      | 1.44  |
| $h\pi^0$  | 1.02  | 0.26  | 4.70  | 68.19    | 11.31     | 2.15      | 0.49      | 0.48  |
| $h2\pi^0$ | 0.12  | 0.01  | 0.33  | 5.67     | 57.68     | 23.13     | 7.57      | 0.08  |
| $h3\pi^0$ | 0.01  | 0.00  | 0.07  | 0.41     | 6.92      | 43.06     | 38.15     | 0.01  |
| $h4\pi^0$ | 0.00  | 0.00  | 0.02  | 0.05     | 0.67      | 6.25      | 25.26     | 0.00  |
| $3h$      | 0.01  | 0.02  | 0.25  | 0.07     | 0.03      | 0.00      | 0.00      | 67.98 |

true

⇒ Key: Overall detector design; good ECAL pattern recognition essential



- ◆ Tau leptons decay, hence we can measure their polarisation
- ◆ But muons also decay

□ Look for events



❖ For FCC-ee statistics, 1.2 million decays per meter flight distance

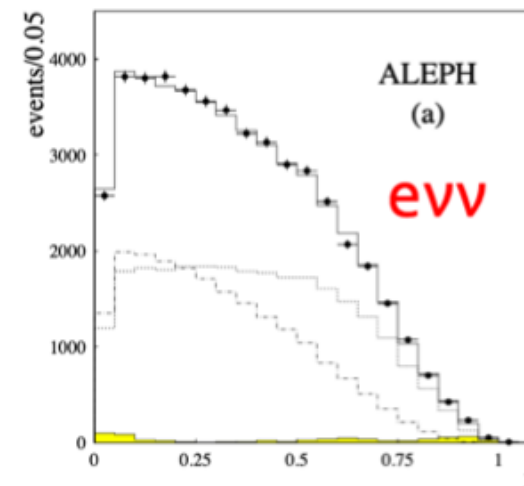
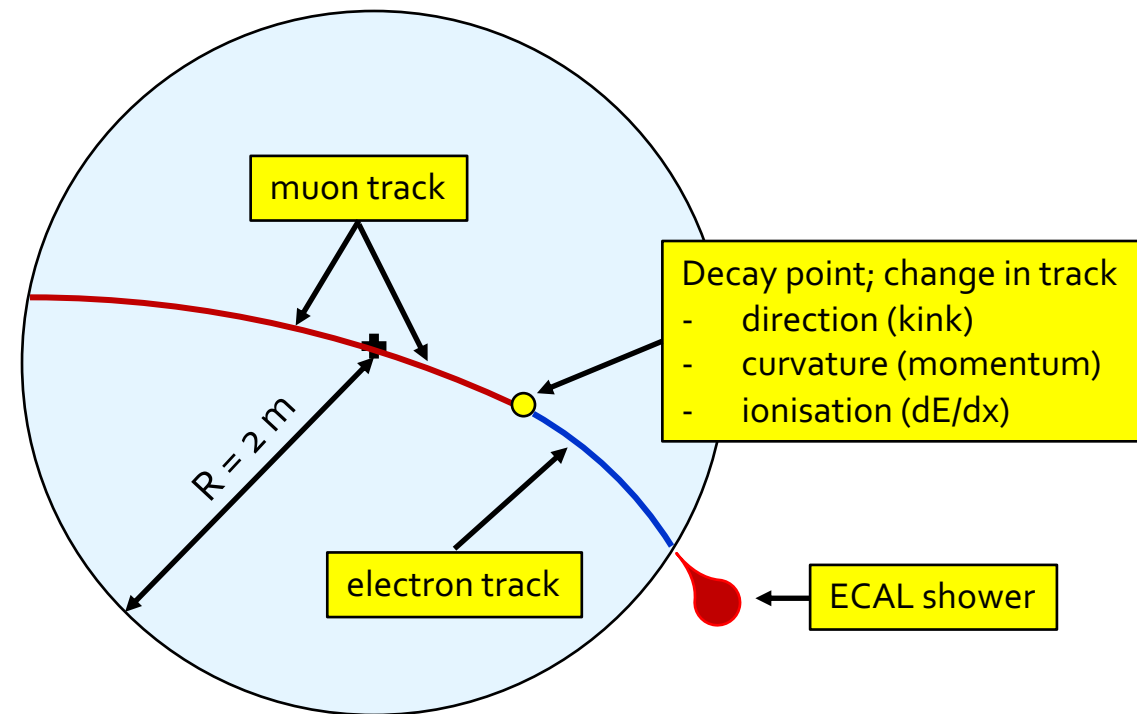
- For robust measurement, aim to measure track both before and after decay point

❖ Complemented by calorimetric estimate of electron momentum

- 1 million well reconstructed events will result in a measurement to a statistical precision of

$\delta P_\mu \approx 0.0045$

- Slightly better than full tau polarisation measurement from LEP



Situation similar to this, but with  $\sim 30$  times the statistics

◆ Measure muon polarisation in decays

$Z \rightarrow \tau\tau$  followed by  $\tau \rightarrow \mu\nu\nu$  followed by  $\mu \rightarrow e\nu\nu$

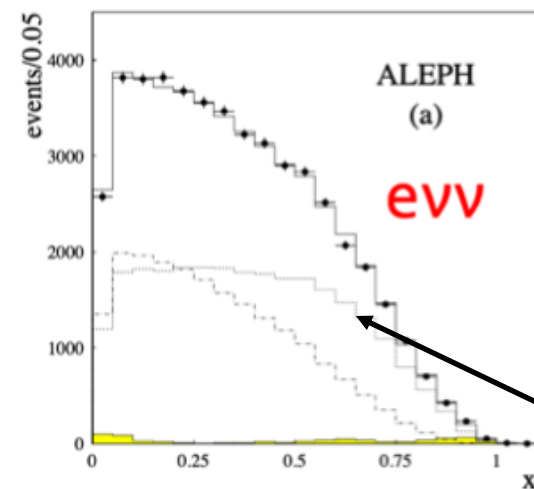
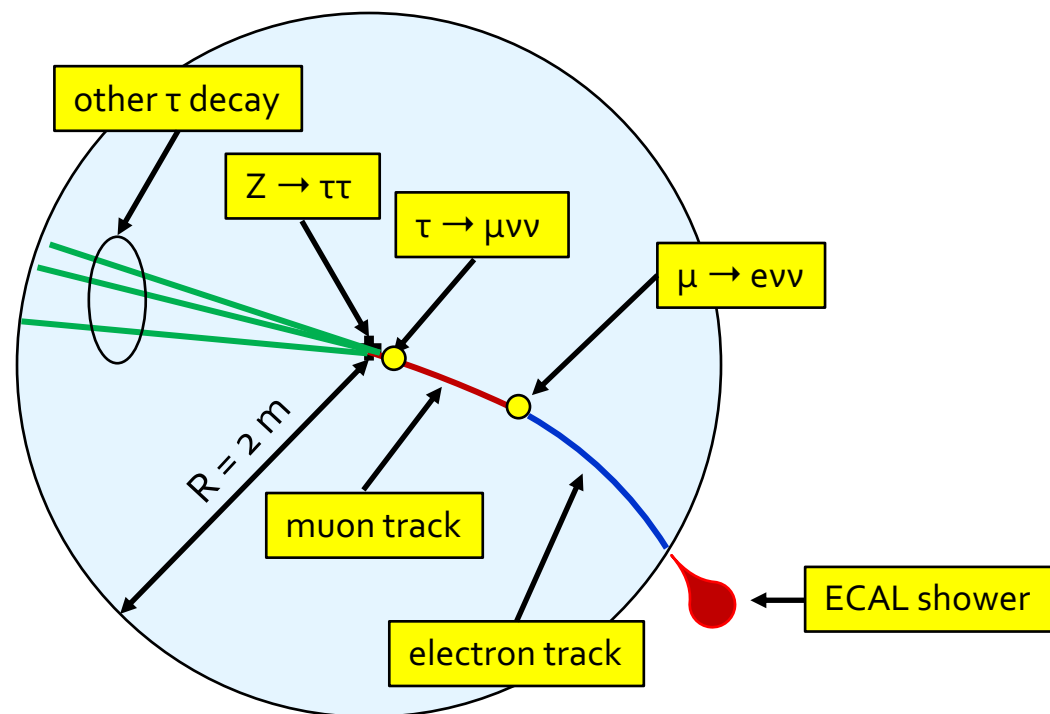
❖ For FCC-ee statistics, few  $\times 100,000$  decays per meter flight distance

□ Essential to measure sizeable track length both before and after decay point

- ❖ Establish decay point / that decay actually happened
- ❖ Measure momentum before & after decay point  $\Rightarrow x = p_e / p_\mu$
- ❖ Complemented by calorimetric estimate of electron momentum

□ 100,000 well reconstructed events would result in a measurement to a statistical precision of about

$\delta P_\mu \approx 0.015$

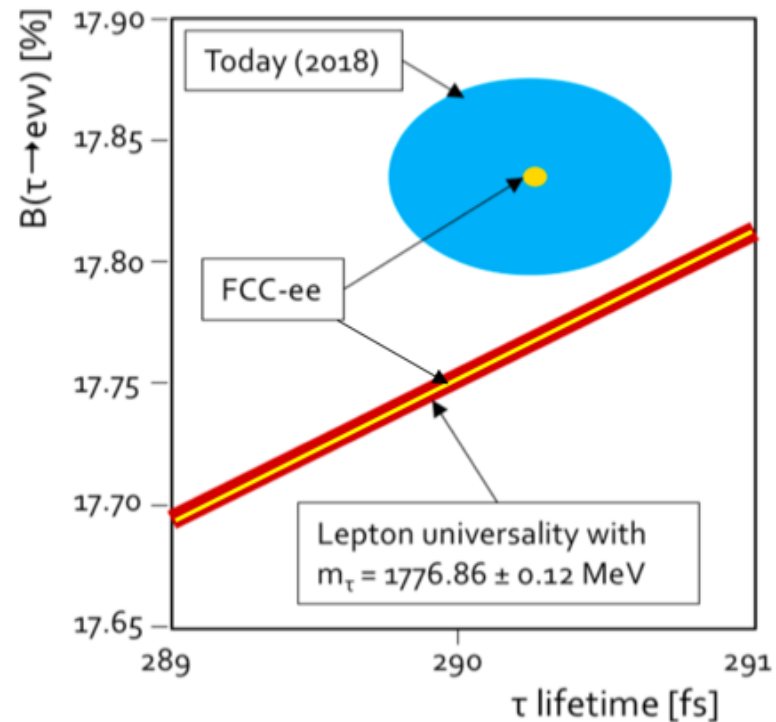


Situation similar to this with somewhat higher statistics

CC weak interaction (V-A):  
Expect to measure  $P_\mu = -1$

# $\tau$ -lepton properties and Lepton Universality

- Mass
- Lifetime
- Leptonic branching fractions



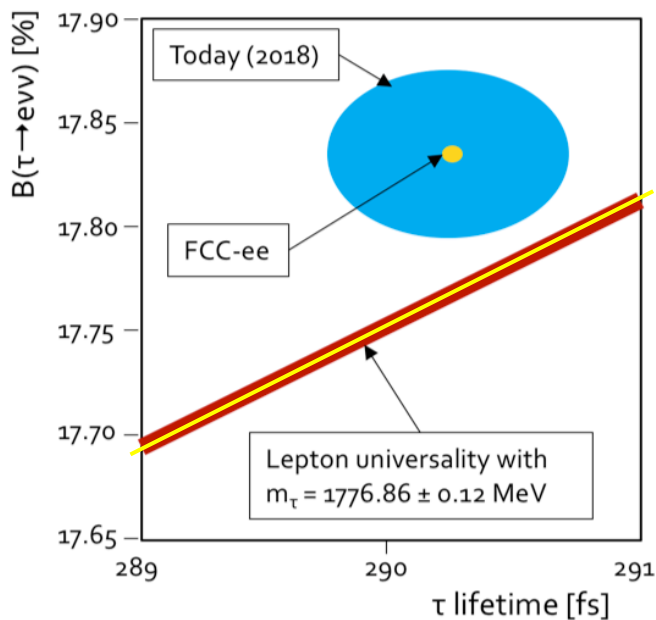
The Fermi constant is measured in  $\mu$  decays and defined by

$$\left(G_F^\mu\right)^2 = 192\pi^3 \frac{\tau_\mu}{m_\mu^5} \quad (\text{known to } 0.5 \text{ ppm})$$

Similarly, can define Fermi constant measured in  $\tau$  decays by

$$\left(G_F^\tau\right)^2 = 192\pi^3 \frac{\tau_\tau}{m_\tau^5} \cdot \frac{1}{\mathcal{B}(\tau \rightarrow e\nu\nu)} \quad (\text{known to } 1700 \text{ ppm})$$

Universality supported by current data  
-  $1\sigma$  error ellipse (blue) consistent with mass (red)



Shown in yellow: "guestimates" on FCC-ee precisions

$$\frac{\delta G_F^\tau}{G_F^\tau} = \frac{5}{2} \frac{\delta m_\tau}{m_\tau} \oplus \frac{1}{2} \frac{\delta \tau_\tau}{\tau_\tau} \oplus \frac{1}{2} \frac{\delta \mathcal{B}}{\mathcal{B}}$$

Today:

67 ppm  
BES

1700 ppm  
Belle

1700 ppm  
LEP

FCC-ee: Will see  $3 \times 10^{11}$   $\tau$  decays  
Statistical uncertainties at the 10 ppm level  
How well can we control systematics?

$m_\tau$  Use  $J/\psi$  mass as reference (known to 2 ppm)

tracking

$\tau_\tau$  Laboratory flight distance of 2.2 mm  
 $\Rightarrow$  10 ppm corresponds to 22 nm (!)

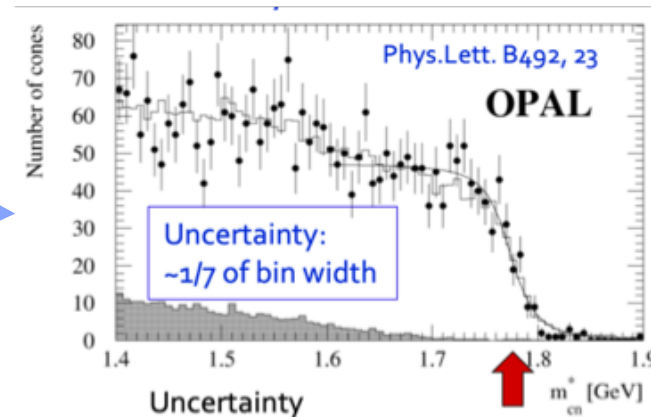
vertex detector

$\mathcal{B}$  No improvement since LEP (statistics limited)  
Depends primarily  $e^-/\pi^-$  (&  $e^-/\rho^-$ ) separation

ECAL  
dE/dx



| Observable                          | Measurement   | Current precision  | FCC-ee stat.  | Possible syst.  | Challenge                    |
|-------------------------------------|---|--------------------|---------------|-----------------|------------------------------|
| $m_\tau$ [MeV]                      | Threshold / inv. mass endpoint                              | $1776.86 \pm 0.12$ | <b>0.004</b>  | <b>0.04 (?)</b> | Mass scale                   |
| $\tau_\tau$ [fs]                    | Flight distance   | $290.3 \pm 0.5$ fs | <b>0.001</b>  | <b>0.04</b>     | Vertex detector alignment    |
| $B(\tau \rightarrow e\nu\nu)$ [%]   | Selection of $\tau^+\tau^-$ , identification of final state | $17.82 \pm 0.05$   | <b>0.0001</b> | <b>0.003</b>    | Efficiency, bkg, Particle ID |
| $B(\tau \rightarrow \mu\nu\nu)$ [%] |   | $17.39 \pm 0.05$   |               |                 |                              |

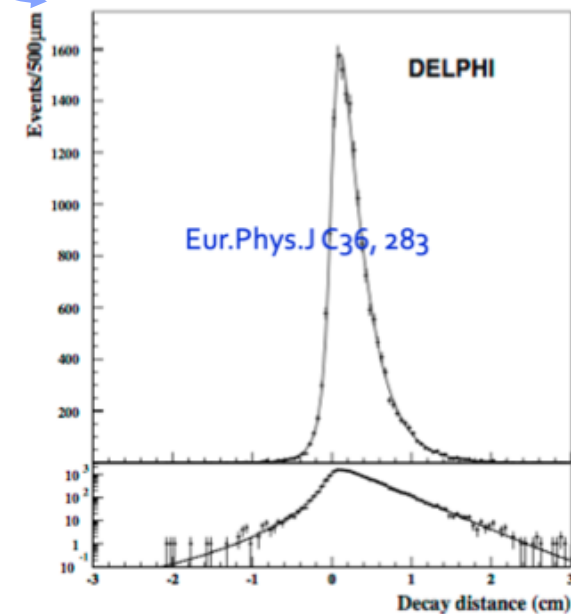
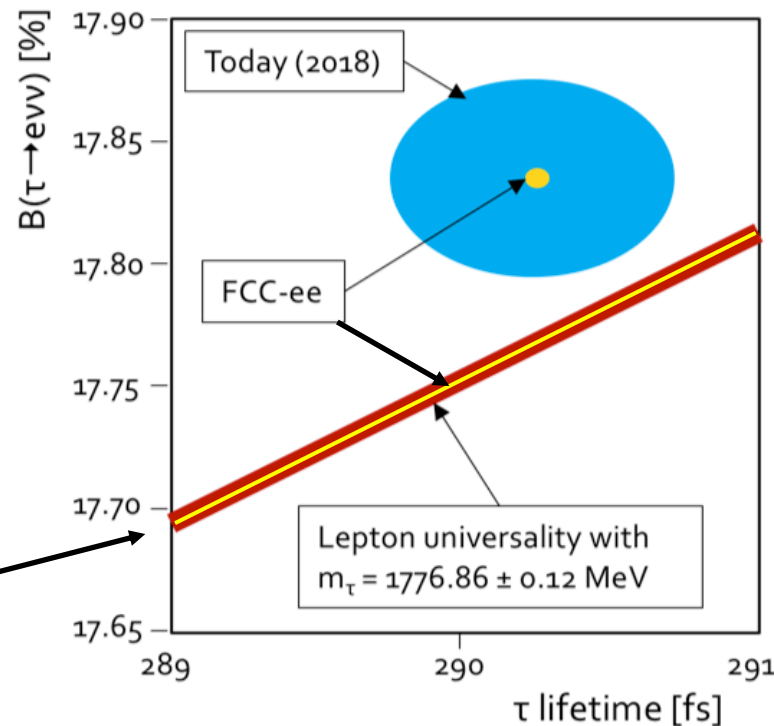


### Lepton Universality Tests:

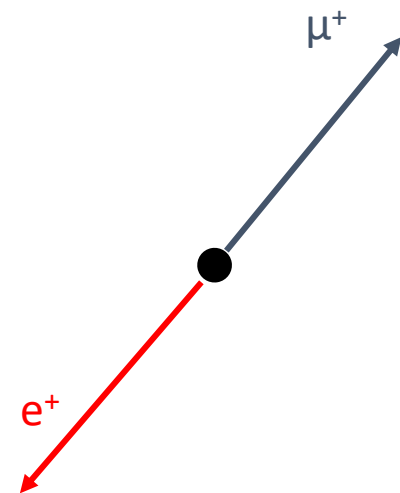
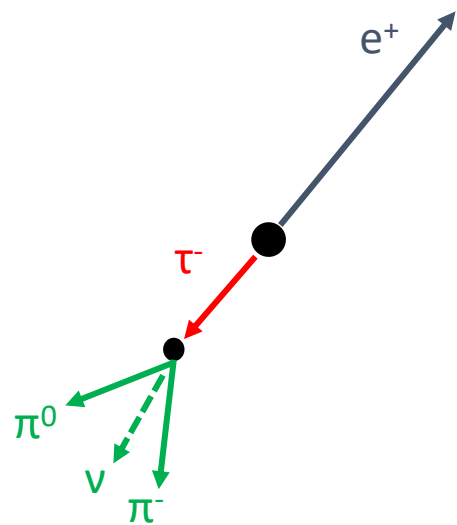
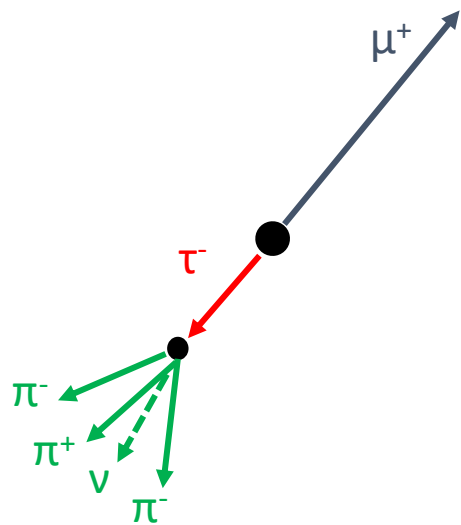
| Quantity         | Measurement   | Current precision   | FCC-ee precision                                     |
|------------------|---|---------------------|--|
| $ g_\mu/g_e $    | $\Gamma_{\tau \rightarrow \mu} / \Gamma_{\tau \rightarrow e}$ | $1.0018 \pm 0.0014$ | <b>Improvement by one order of magnitude or more</b> |
| $ g_\tau/g_\mu $ | $\Gamma_{\tau \rightarrow e} / \Gamma_{\mu \rightarrow e}$    | $1.0030 \pm 0.0015$ |  |

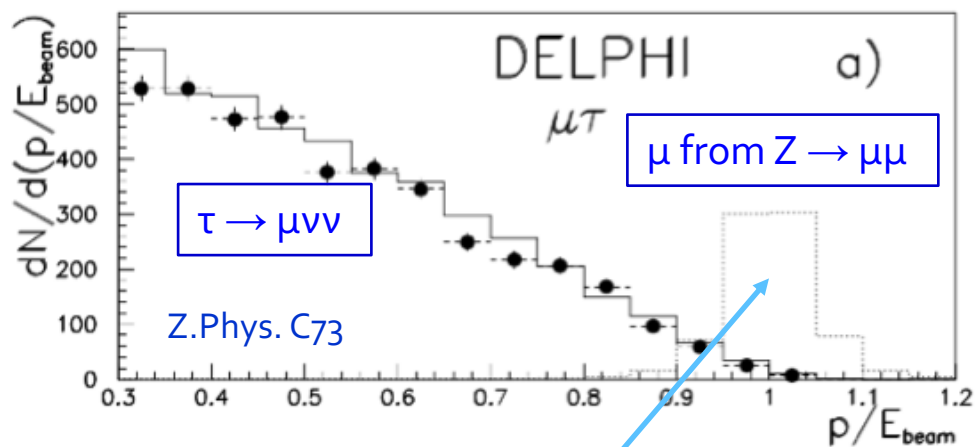
With the precise FCC-ee measurements of lifetime and BRs,  $m_\tau$  could become the limiting measurement in the universality test

$$\left(\frac{g_\tau}{g_\mu}\right)^2 \approx \frac{\tau_\mu}{\tau_\tau} B(\tau^- \rightarrow e^- \bar{\nu}_e \nu_\tau) \left(\frac{m_\mu}{m_\tau}\right)^5$$



# LFV Z decays





DELPHI momentum resolution at  $p_T = 45.6$  GeV :

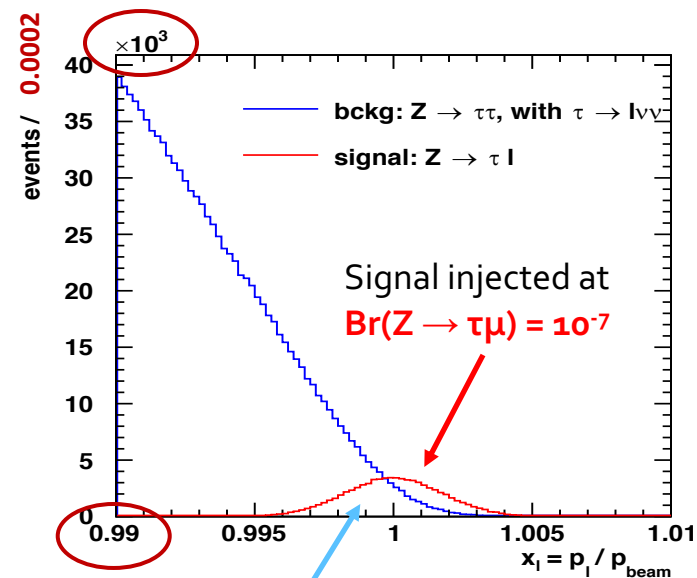
$$\sigma(p_T)/p_T = 2.7 \times 10^{-2}$$

Limit set at

$$\text{Br}(Z \rightarrow \mu\tau) < 12 \times 10^{-6}$$

- Best at LEP
- World's best until recently:
  - ❖ ATLAS now at  $9.5 \times 10^{-6}$

FCC-ee study with  $5 \times 10^{12}$  Z decays



Assumed momentum resolution at  $p_T = 45.6$  GeV including contribution ( $0.9 \times 10^{-3}$ ) from beam-energy spread:

$$\sigma(p_T)/p_T = 1.8 \times 10^{-3}$$

Findings:

- Sensitivity scales  $\sim$  linear in momentum resolution
- Irreducible background (from  $\tau \rightarrow \mu\nu\nu$ )  $\Rightarrow$  sensitivity  $\propto 1/\sqrt{\mathcal{L}}$
- Similar sensitivity for  $Z \rightarrow e\tau$
- Sensitivity for signals down to

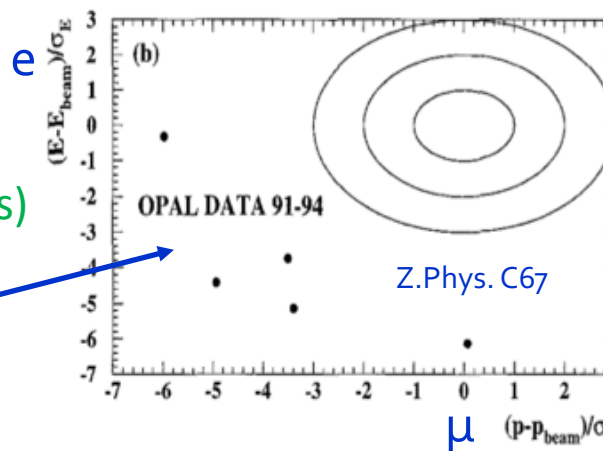
$$\text{BRs of } \sim 10^{-9}$$

◆ Current limit:

- **7.5 x 10<sup>-7</sup>** LHC/ATLAS (20 fb<sup>-1</sup>; no candidates)
- **1.7 x 10<sup>-6</sup>** LEP/OPAL (4.0 x 10<sup>6</sup> Z decays: no candidates)

◆ In e<sup>+</sup>e<sup>-</sup>, clean experimental signature:

- Beam energy electron vs. beam energy muon



◆ Main experimental challenge:

- **Catastrophic bremsstrahlung energy loss** of muon in electromagnetic calorimeter
  - ❖ Muon would deposit (nearly) full energy in ECAL: Misidentification  $\mu \rightarrow e$
  - ❖ NA62: Probability of muon to deposit more than 95% of energy in ECAL: **4 x 10<sup>-6</sup>**
  - ❖ Possible to reduce by
    - ECAL longitudinal segmentation: Require energy > mip in first few radiation lengths
    - Aggressive veto on HCAL energy deposit and muon chamber hits
  - ❖ If dE/dx measurement available, (some) independent e/μ separation at 45.6 GeV
    - Could give handle to determine misidentification probability P(μ → e)

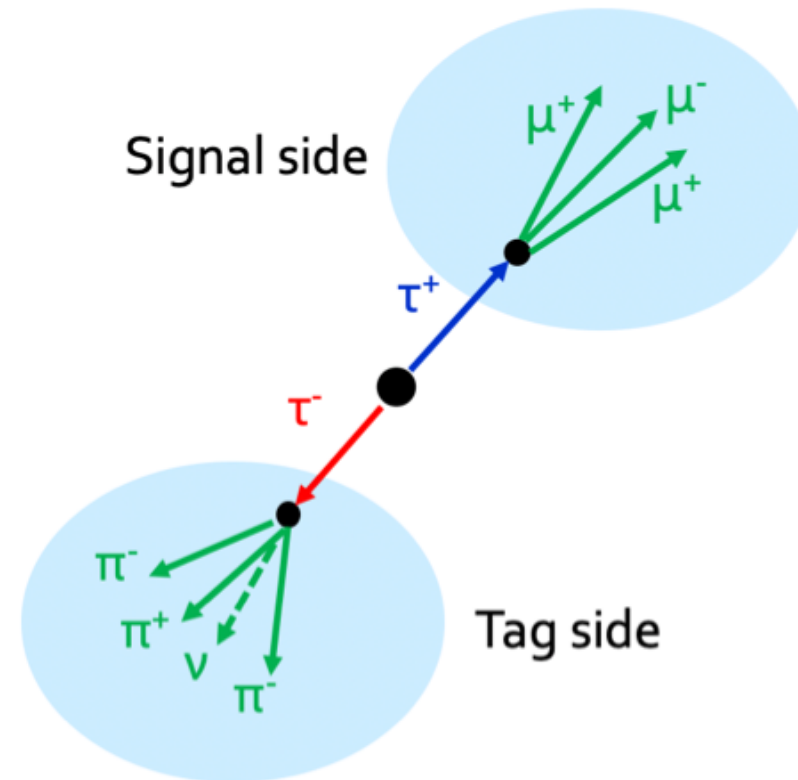
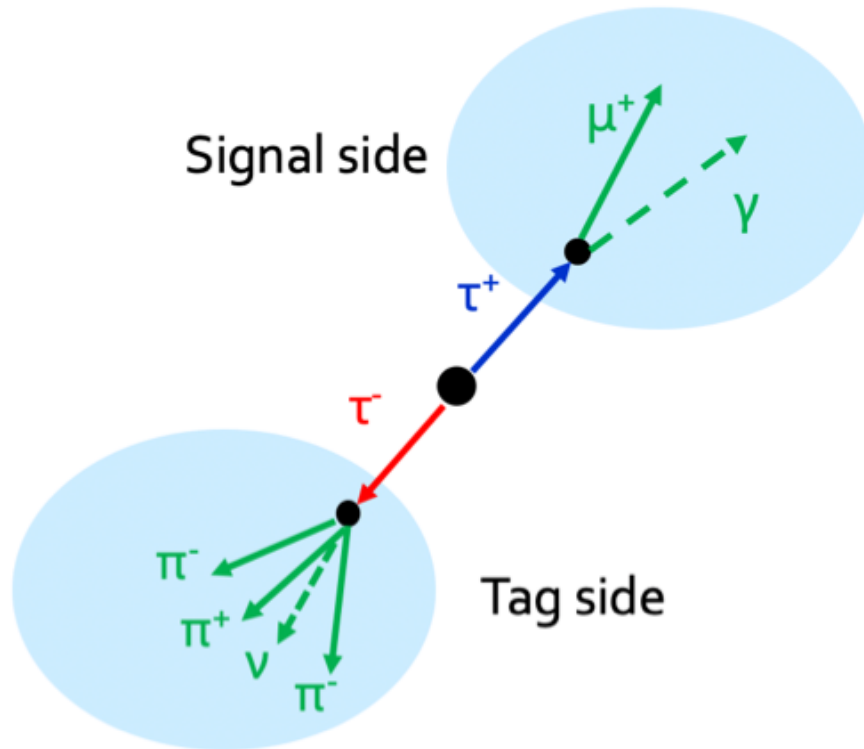


**10<sup>-10</sup> – 10<sup>-8</sup>**  
sensitivity depending on  
detector design and  
performance

◆ FCC-ee:

- Misidentification from catastrophic energy loss corresponds to limit of about **Br(Z → eμ) ≈ 10<sup>-8</sup>**
- Possibly do  $\mathcal{O}(10)$  better than that **Br(Z → eμ) ~ 10<sup>-9</sup>** (probably even **10<sup>-10</sup>** with IDEA dE/dx)

# LFV $\tau$ decays





◆ **Current limits:**

- $\text{Br}(\tau^- \rightarrow e^- \gamma) < 3.3 \times 10^{-8}$       BaBar, 10.6 GeV;  $4.8 \times 10^8 e^+e^- \rightarrow \tau^+\tau^-$  : 1.6 expected bckg
- $\text{Br}(\tau^- \rightarrow \mu^- \gamma) < 4.4 \times 10^{-8}$       3.6 expected bckg

◆ **Main background:** Radiative events (IRS+FSR),  $e^+e^- \rightarrow \tau^+\tau^-\gamma$

- $\tau \rightarrow \mu \gamma$  decay faked by combination of  $\gamma$  from ISR/FSR and  $\mu$  from  $\tau \rightarrow \mu \nu$

◆ **At FCC-ee, with  $1.7 \times 10^{11} \tau^+\tau^-$  events, what can be expected?**

- Boost 8-9 times higher than at B-factories
- Detector resolutions rather different, probably especially ECAL
- Parametrised study of signal and the main background,  $e^+e^- \rightarrow \tau^+\tau^-\gamma$ , performed
  - ❖ Presented at tau2018
- From study (assuming 25% signal & background efficiency), projected BR sensitivity

$2 \times 10^{-9}$

- With the recently suggested crystal ECAL, possible a factor of about 6-10 better

2008.00338

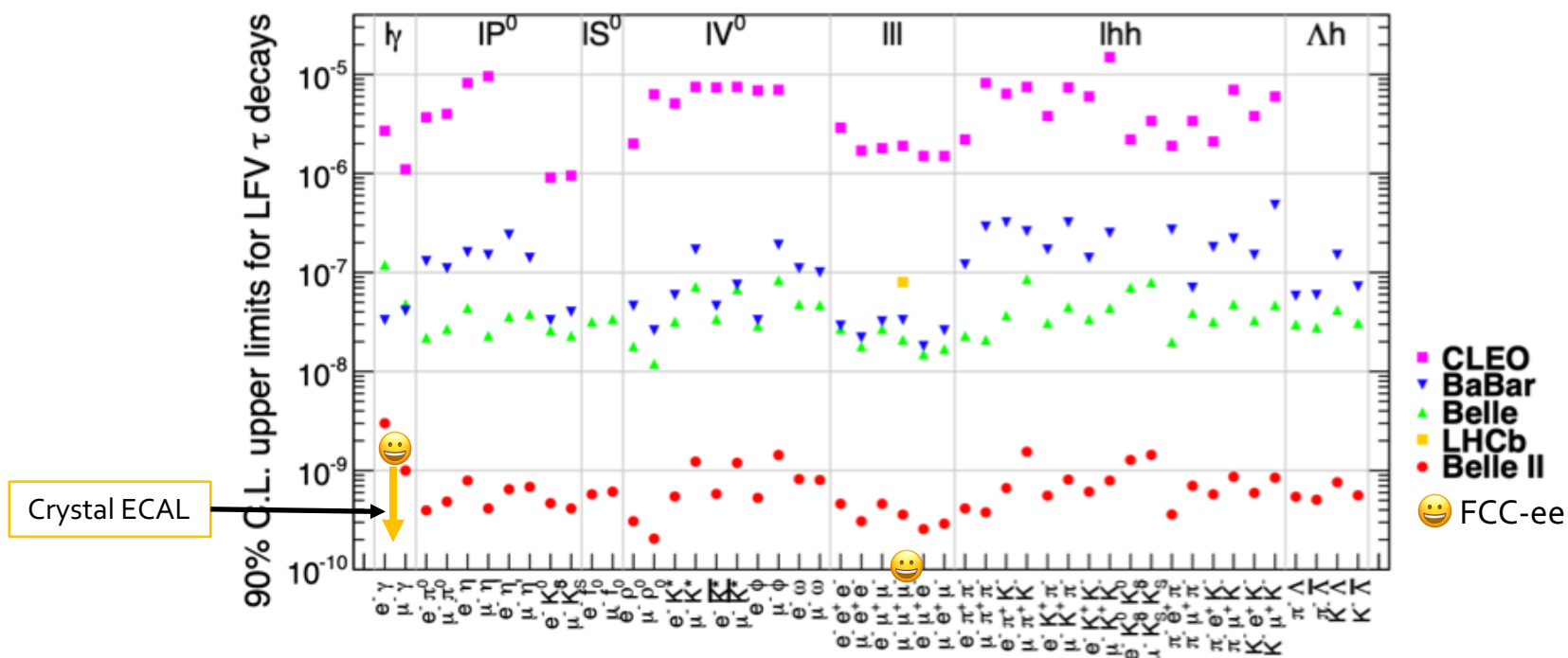
◆ Current limits:

- All 6 combs. of  $e^\pm, \mu^\pm$  :  $Br \lesssim 2 \times 10^{-8}$  Belle@10.6 GeV;  $7.2 \times 10^8 e^+e^- \rightarrow \tau^+\tau^-$  : no candidates
- $\mu^-\mu^+\mu^-$  :  $Br < 4.6 \times 10^{-8}$  LHCb  $2.0 \text{ fb}^{-1}$  : background candidates

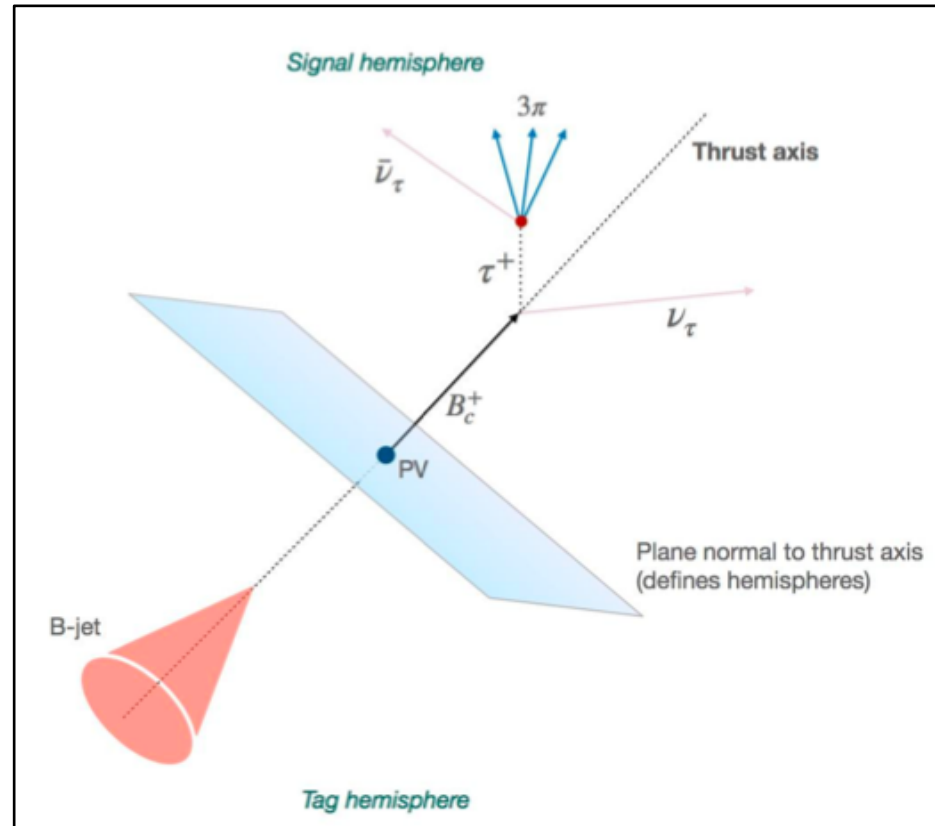
◆ FCC-ee prospects

- Expect this search to have *very low* background, even with FCC-ee like statistics
- Should be able to have sensitivity down to BRs of  $\lesssim 10^{-10}$

◆ Many more decay modes to search for when time comes. Need PID for most

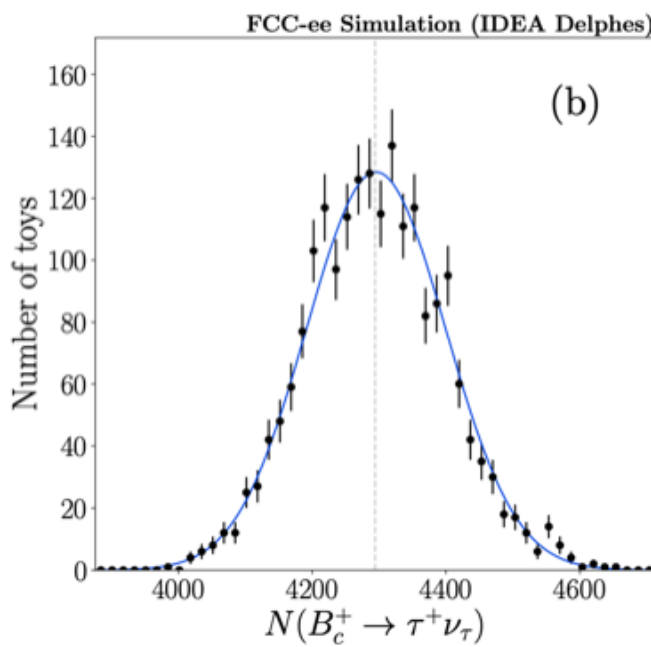
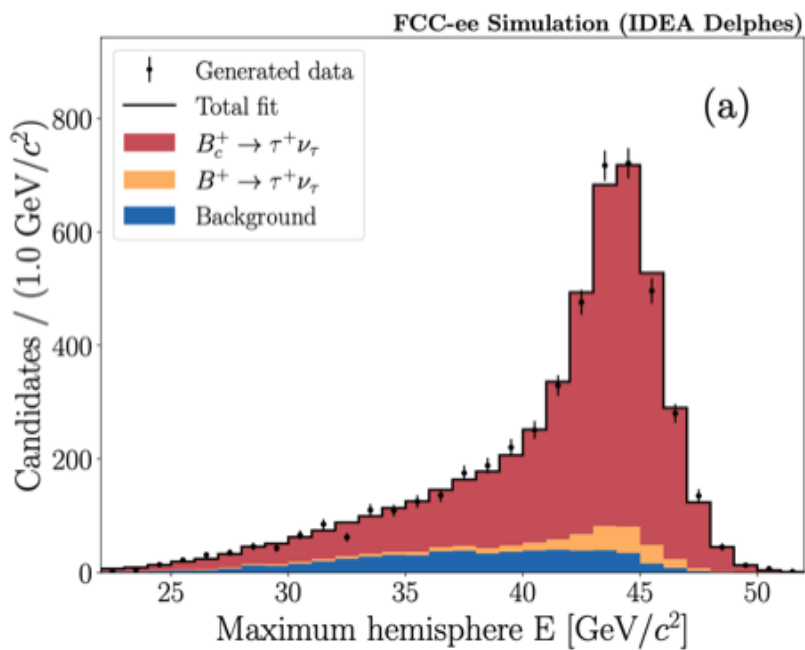
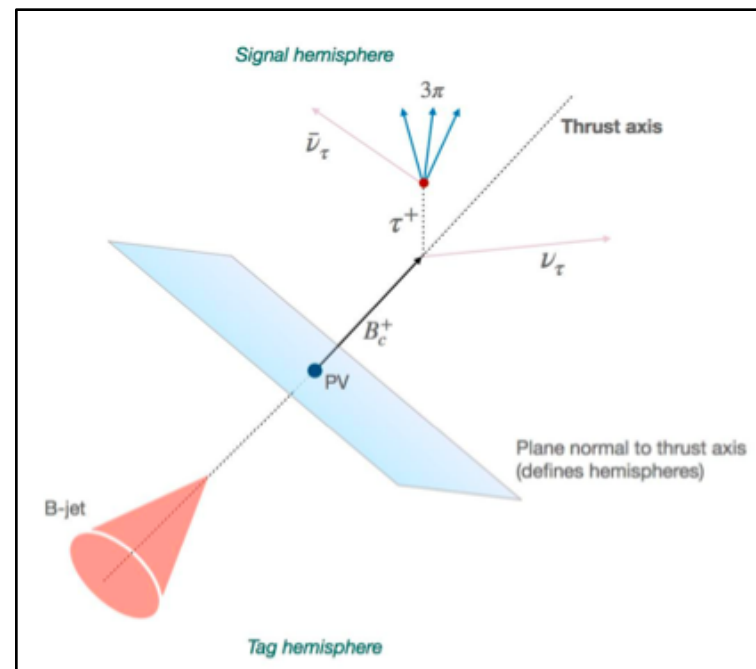


# $\tau$ leptons in b decays



- ◆  $B_c \rightarrow \tau \nu_\tau$  process has same Feynman vertex factors as  $b \rightarrow c \tau \nu_\tau$ 
  - Measurement of  $R(D)$  and  $R(D^*)$  show  $\sim 3\text{-}4 \sigma$  tension in SM
- ◆ Exploit three-prong decay of  $\tau$
- ◆ Delphes simulation (IDEA Detector)
- ◆ Reject backgrounds from  $Z \rightarrow bb/cc/qq$  using
  - Event level energy properties
  - Properties of the reconstructed  $3\pi$  candidate
  - Two stage MVA approach

[arXiv:2105.13330](https://arxiv.org/abs/2105.13330)



- ◆ Toy dataset generated from signal and background PDFs
  - Signal measured with 2.4% precision

# Summary

- ◆ From  $5 \times 10^{12}$  Z decays, FCC-ee will produce  $1.7 \times 10^{11}$   $\tau^+\tau^-$  pairs
- ◆ Factor  $\sim 3$  higher statistics than Belle2 projection; plus higher boost ( $\gamma = 25$ )
  - Boost is advantageous for many studies
- ◆ Potential for very precise  $\sin^2\theta_W$  determination via  $\tau$  polarisation measurement
- ◆ Improve **Lepton universality test** by 1-2 orders of magnitude down to at least  $\mathcal{O}(10^{-4})$  level [ $\mathcal{O}(10^{-4})$  statistically]
  - Substantial improvement in  $\tau$  lifetime
  - Substantial improvement in  $\tau$  branching fractions
  - Potential for improved measurement of  $\tau$  mass
- ◆ Improved sensitivity to **lepton flavour violating Z decays** by factor  $\mathcal{O}(10^{3-4})$ 
  - Sensitivities down to  $10^{-9}$
- ◆ Searches for **lepton flavour violating  $\tau$  decays**; sensitivities comparable to Belle2
  - Range from  $\lesssim 10^{-10}$  to **few  $\times 10^{-9}$**
- ◆ Plus hadronic branching ratios and spectral functions,  $\alpha_s$ ,  $v_\tau$  mass, ...
- ◆ Prospects for very precise lepton universality  $\tau$  lepton tests in b-physics
- ◆ And of course Higgs, etc...



# Summary - Detector requirements

Precision  $\tau$  physics sets very strong detector requirements; good benchmark

## ◆ Vertexing

- Lifetime measurement to  $10^{-4}$  corresponds to  $0.22 \mu\text{m}$  flight distance

## ◆ Tracking

- Two (or rather multi) track separation: measure 3-, 5-, 7-, 9- ... prong decays
- Extremely good control of momentum and mass scale
  - ❖  $\tau$  mass measurement
  - ❖ Sensitivity of search for flavour violating Z decays, e.g.  $Z \rightarrow \mu\tau$ , scales linearly in momentum resolution at 45.6 GeV
- Low material budget: Minimize secondary tracks from hadronic interaction in material

## ◆ Calorimetry

- Clean  $\gamma$  and  $\pi^0$  reconstruction from  $\sim 0.2$  to 45 GeV is key to precision  $\tau$  physics
- Collimated topologies: Important to be able to separate  $\gamma$ s from closely lying hadronic showers

## ◆ PID

- Necessary if one desires to separate  $\pi/K$  modes (0 – 45 GeV momentum range)
- $e/\pi$  separation at low momenta (where calorimetric separation is most difficult)
- **Redundancy**: Provides valuable handle to create test samples for study of calorimetry
  - ❖ For IDEA drift chamber, even for  $e/\mu$  separation

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Precision  $\tau$  physics sets very strong detector requirements; good benchmark

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- Low material budget: Minimum material

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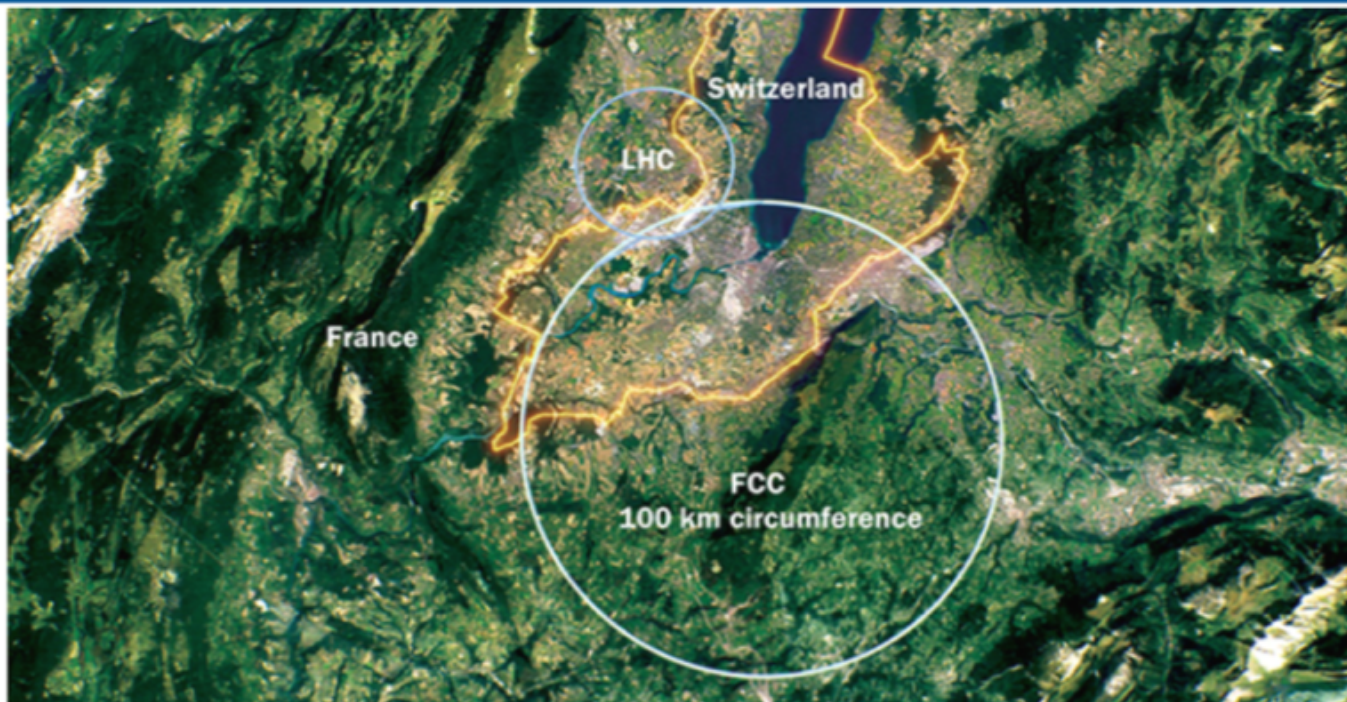
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**Design your detector with care!  
Better start now**

resolution at 45.6 GeV

spares

Fabiola Gianotti  
FCC Week,  
June 2021



- ❑ **Tunnel:** assess geological, technical, administrative, environmental feasibility → aim is to demonstrate there is no show-stopper for ~ 100 km ring in Geneva region
  - ❑ **Technologies:** superconducting high-field magnets and RF accelerating structures; high-efficiency power production; energy saving and other sustainable technologies
  - ❑ **Funding:** development of funding model for first-stage machine (tunnel and FCC-ee, total ~ 10 BCHF) and identification of substantial resources from outside CERN's budget
  - ❑ **“Consensus building”:** gathering scientific, political, societal support → communication campaign targeting scientists, governmental and other authorities, industry, general public
- Complete a Feasibility Study Report by end 2025

my emphasis

**double ring  $e^+e^-$  collider  $\sim 100$  km**

**follows footprint of FCC-hh,**  
except around IPs

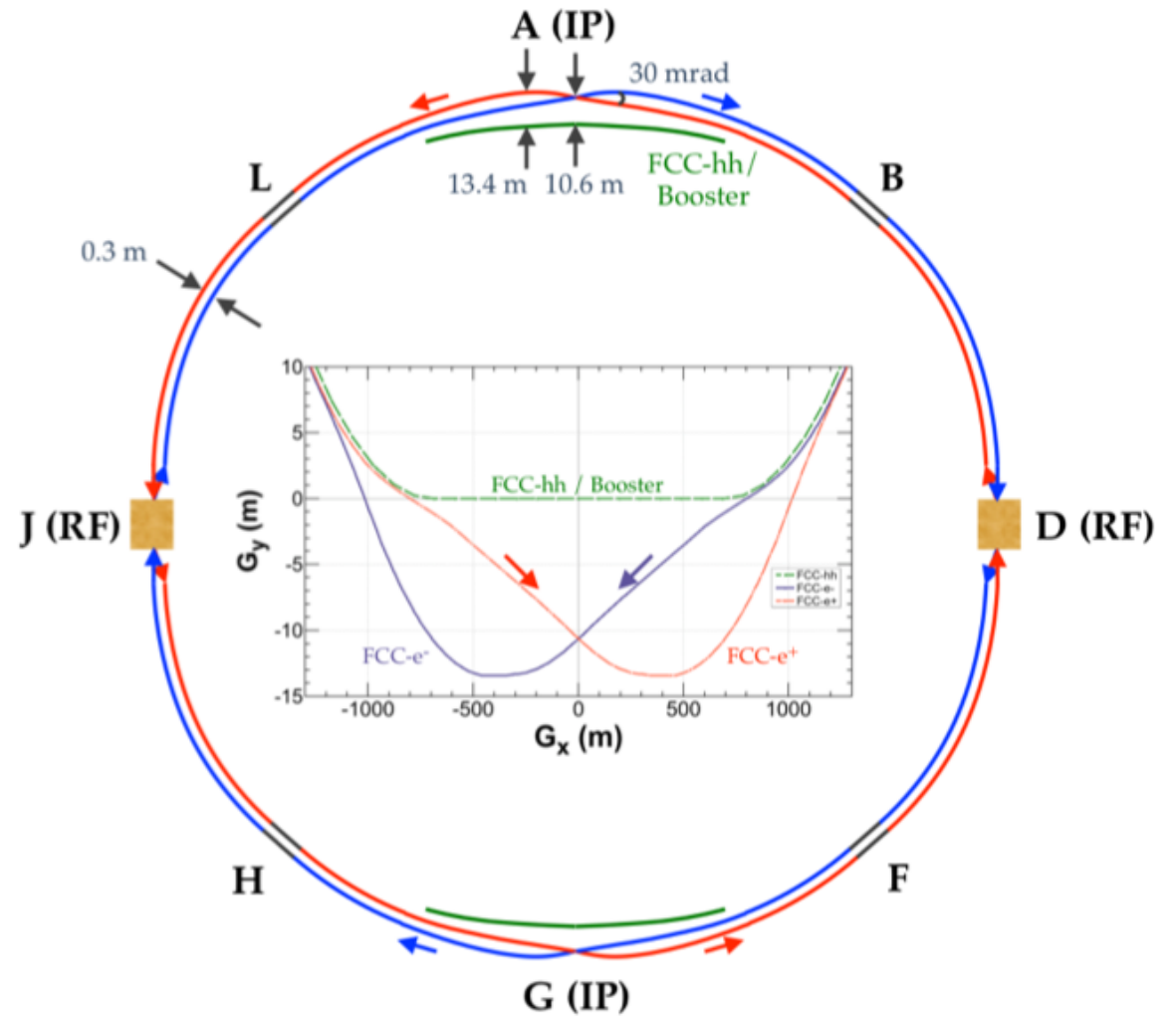
**asymmetric IR layout & optics**  
to limit synchrotron radiation  
towards the detector

**presently 2 IPs** (alternative layout  
with 4 IPs under study)

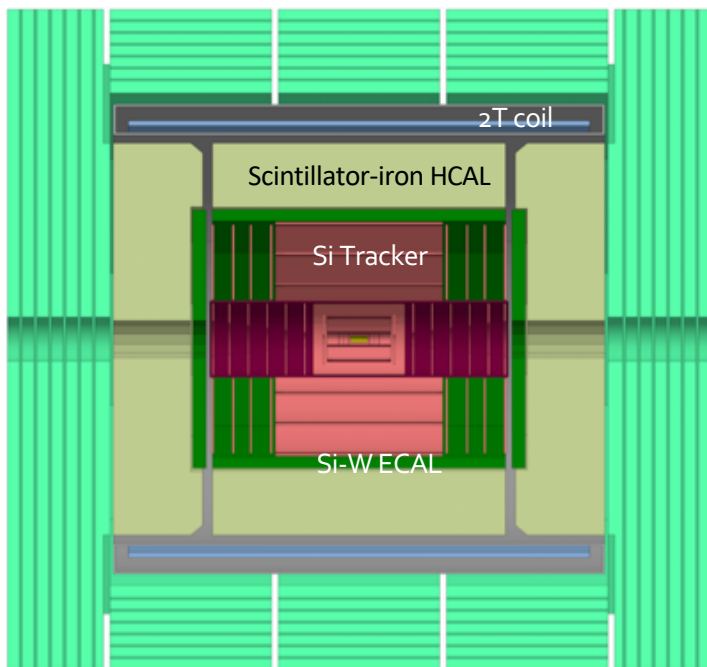
**large horizontal crossing angle 30 mrad,**  
**crab-waist optics**

**synchrotron radiation power 50 MW/beam**  
at all beam energies

**top-up injection scheme;**  
requires **booster synchrotron in collider tunnel**

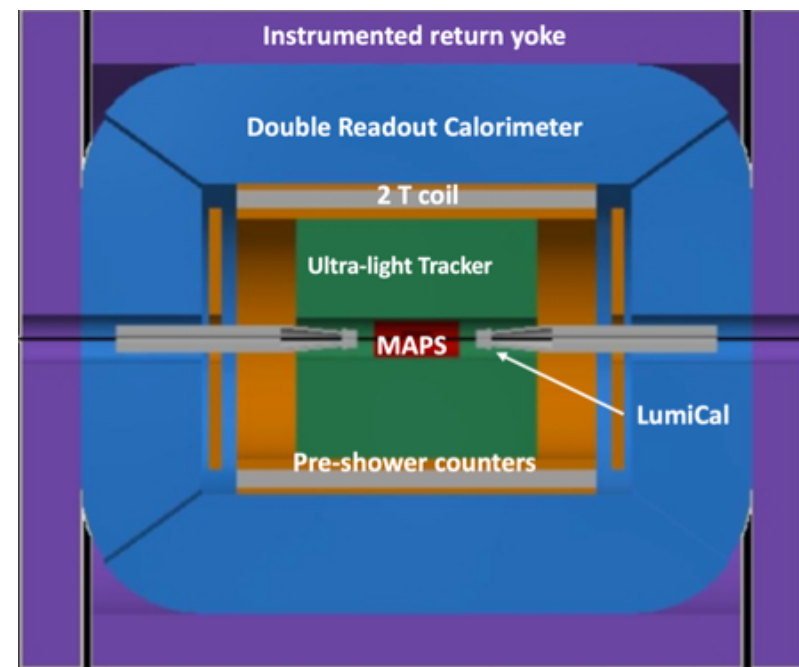






CLD

- ◆ Consolidated option based on the detector design developed for CLIC
  - All silicon vertex detector and tracker
  - 3D-imaging highly-granular calorimeter system
  - Coil *outside* calorimeter system
- ◆ Proven concept, understood performance



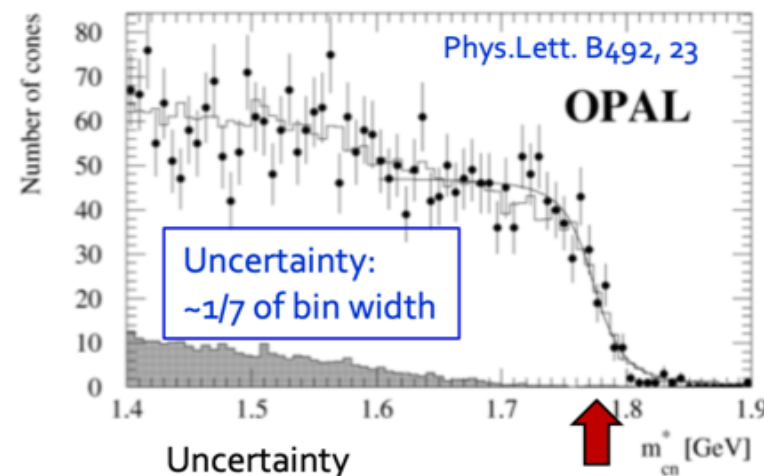
IDEA

- ◆ New, innovative, possibly more cost-effective design
  - Silicon vertex detector
  - Short-drift, ultra-light wire chamber
  - Dual-readout calorimeter
  - Thin and light solenoid coil *inside* calorimeter system

# Tau Mass (i)

- ◆ **Current world average:**  $m_\tau = 1776.86 \pm 0.12 \text{ MeV}$
- ◆ **Best in world: BES3 (threshold scan)**  $m_\tau = 1776.91 \pm 0.12 \text{ (stat.)}^{+0.10}_{-0.13} \text{ (syst.) MeV}$
- ◆ **Best at LEP: OPAL**  $m_\tau = 1775.1 \pm 1.6 \text{ (stat.)} \pm 1.0 \text{ (syst.) MeV}$

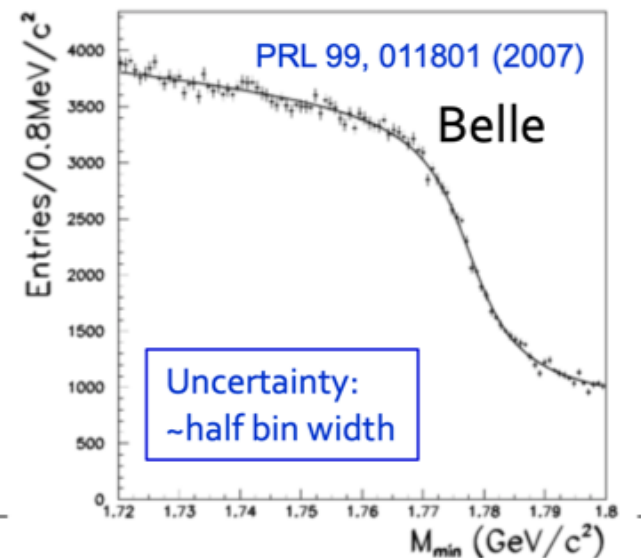
- **About factor 10 from world's best**
- **Main result from endpoint of distribution of pseudo-mass in  $\tau \rightarrow 3\pi^\pm(n\pi^0)\nu_\tau$**
- **Dominant systematics**
  - ❖ **Momentum scale: 0.9 MeV**
  - ❖ **ECAL scale: 0.25 MeV (including also  $\pi^0$  modes)**
  - ❖ **Dynamics of  $\tau$  decay: 0.10 MeV**



- ◆ **Same method from Belle**
  - **Main systematics**
    - ❖ **Beam energy & tracking system calib.: 0.26 MeV**
    - ❖ **Parameterisation of the spectrum edge: 0.18 MeV**

$$m_\tau = 1776.61 \pm 0.13 \text{ (stat.)} \pm 0.35 \text{ (syst.) MeV}$$

Pseudo-mass:  $M_{min} = \sqrt{M_{3\pi}^2 + 2(E_{beam} - E_{3\pi})(E_{3\pi} - P_{3\pi})}$



## ◆ Prospects for FCC-ee:

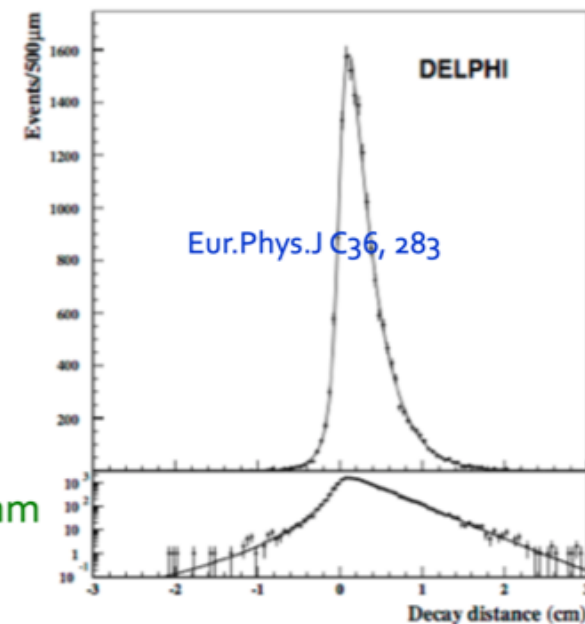
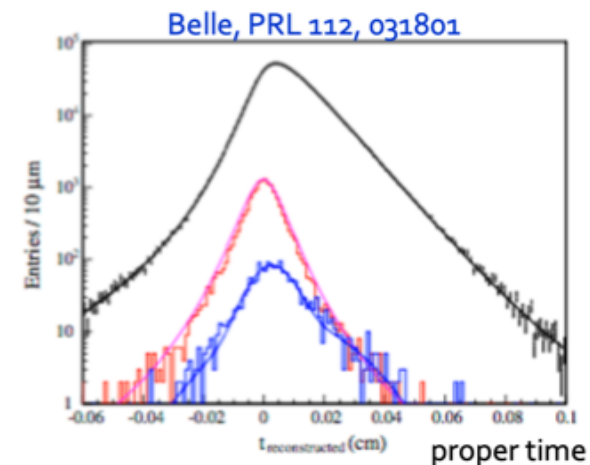
- 3 prong, 5 prongs, (perhaps even 7 prongs?)
- Statistics  $10^5$  times OPAL:  $\delta_{\text{stat}} = 0.004 \text{ MeV}$
- Systematics:
  - ❖ At FCC-ee,  $E_{\text{BEAM}}$  determined to better than 0.1 MeV ( $\sim 1$  ppm) from resonant spin depolarisation
    - Negligible effect on  $m_\tau$
  - ❖ Control of mass scale
    - Suggest to exploit  $10^9 J/\psi \rightarrow \mu\mu$  from Z decays as reference, with  $m(J/\psi)$  known to 0.006 MeV (2 ppm) from KEDR
  - ❖ Reduce uncertainty from parametrisation of spectrum edge by use of theoretical spectrum checked against high statistics data
  - ❖ Cross checks using 5-prongs
- Overall systematics:
  - ❖ Study to be performed to shed more light on this. Improvement with respect to current measurements seems possible. Suggest

$$\delta_{\text{syst}} \lesssim 0.04 \text{ MeV}$$

⇒ **Key:** precise control of momentum scale also in dense, multi-prong topologies

# Tau Lifetime (i)

- ◆ **Current world average:**  $\tau_\tau = 290.3 \pm 0.5$  fs
- ◆ **Best in world (Belle):**  $\tau_\tau = 290.17 \pm 0.53_{\text{stat}} \pm 0.22_{\text{syst}}$  fs
  - Large statistics:  $711 \text{ fb}^{-1}$  @  $Y(4s)$ :  $6.3 \times 10^8 \tau^+\tau^-$  events
  - Use 3 vs. 3 prong events (1.1M events); reconstruct 2 secondary vertices + primary vertex
  - Measure flight distance  $\Rightarrow$  proper time
  - Dominant systematics: Vertex detector alignment to  $\sim 0.25 \mu\text{m}$ 
    - ❖ Vertex detector outside 15 mm beam pipe
- ◆ **Best at LEP (DELPHI):**  $\tau_\tau = 290.0 \pm 1.4_{\text{stat}} \pm 1.0_{\text{syst}}$  fs
  - Low statistics:  $\sim 250,000 \tau^+\tau^-$  events
  - Three methods:
    - ❖ Decay length ( $1\nu_3 + 3\nu_3$ ), impact parameter difference ( $1\nu_1$ ), miss distance ( $1\nu_1$ )
  - Lowest systematics from decay length method ( $1\nu_3$ )
    - ❖ Dominant systematics: Vertex detector alignment to  $7.5 \mu\text{m}$ 
      - Alignment with data ( $q\bar{q}$  events): statistics limited
    - ❖ Vertex detector:  $7.5 \mu\text{m}$  point resolution at 63, 90, and 109 mm



# Tau Lifetime (ii)

- ◆ Prospects at FCC-ee

- Small beam-pipe radius (15 mm): Vertex detector with 3  $\mu\text{m}$  space points at 18, 38, 58 mm  
[DELPHI: 7.5  $\mu\text{m}$  @63, 90, 109 mm]

- Impact parametre resolution ~5 times better than at LEP for relevant momenta

- ❖ DELPHI:  $a = 20 \mu\text{m}$ ,  $b = 65 \mu\text{m}$

- ❖ Belle:  $a = 19 \mu\text{m}$ ,  $b = 50 \mu\text{m}$

- ❖ FCC-ee:  $a = 3 \mu\text{m}$ ,  $b = 15 \mu\text{m}$

$$\sigma(d_0) = \sqrt{a^2 + b^2 \cdot \text{GeV}^2 / (p^2 \sin^3(\theta))}.$$

- Assume same alignment uncertainty as Belle:

- ❖ 0.25  $\mu\text{m}$ , i.e. factor 30 improvement wrt DELPHI.

- ❖ Possible systematics on flight distance method: 1.3/30 fs

$$\delta_{\text{syst}} = 0.04 \text{ fs} \quad ; \quad \delta_{\text{stat}} = 0.001 \text{ fs}$$

- ◆ Further prospects: lifetime can be measured with different systematics in many modes

- $1\nu 1$ : impact parameter difference, miss distance

- $1\nu 3$ : flight distance

- $3\nu 3$  ( $4 \times 10^9$  events): flight distance sum

⇒ **Key:** Careful design and precise control of vertex detector



# Tau Leptonic Branching Fractions

- ◆ World average

- $B(\tau \rightarrow e\nu\nu) = 17.82 \pm 0.05 \%$  ;  $B(\tau \rightarrow \mu\nu\nu) = 17.39 \pm 0.05 \%$

- ◆ Dominated by Aleph @ LEP

- $B(\tau \rightarrow e\nu\nu) = 17.837 \pm 0.072_{\text{stat}} \pm 0.036_{\text{syst}} \%$  ;  $B(\tau \rightarrow \mu\nu\nu) = 17.319 \pm 0.070_{\text{stat}} \pm 0.032_{\text{syst}} \%$

- ◆ Three uncertainty contributions dominant in the Aleph measurement

- ❖ Selection efficiency: 0.021 / 0.020 %

- ❖ Non- $\tau^+\tau^-$  background: 0.029 / 0.020 %

- ❖ Particle ID: 0.019 / 0.021 %

- All of these were limited by statistics: size of test samples, etc.

- ◆ Prospects at FCC-ee

- Enormous statistics:

$$\delta_{\text{stat}} = 0.0001 \%$$

- Systematic uncertainty is hard to (gu)estimate at this point.

- ❖ Depends intimately on the detailed performance of the detector(s)

- At the end of the day, between LEP experiments,  $\delta_{\text{syst}}$  varied by factor ~3

- Lesson: **Design your detector with care!**

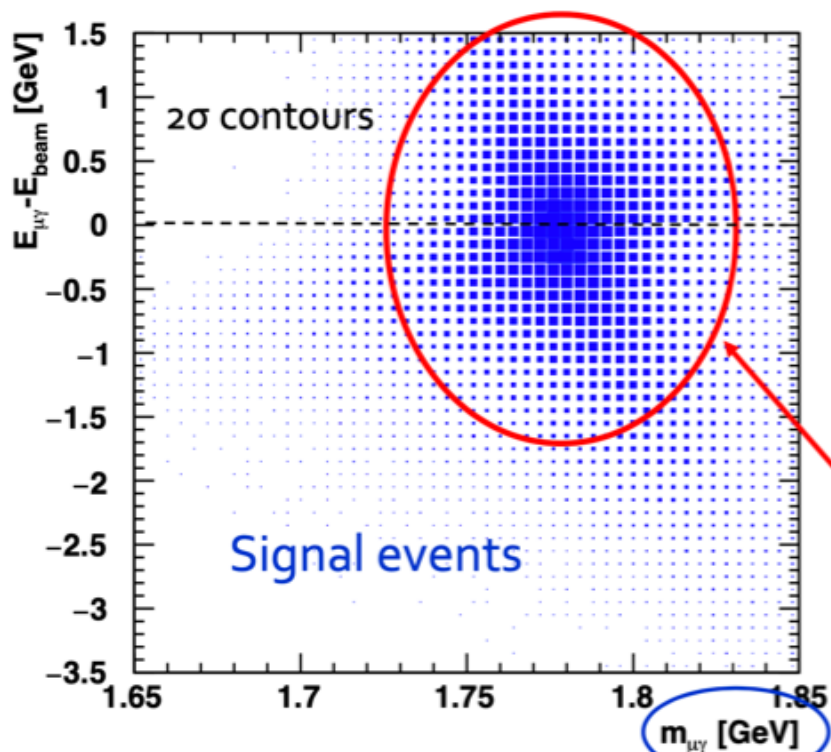
With the large statistics, will learn a lot. Suggest a factor 10 improvement wrt Aleph:

$$\delta_{\text{syst}} = 0.003 \%$$

⇒ **Key:** Many ingredients; tracking, calorimetry, overall detector design

# $\tau \rightarrow \mu\gamma$ Study – The signal

◆ Generate signal events with pythia8:  $e^+e^- \rightarrow Z \rightarrow \tau^+\tau^-(\gamma)$ , with  $\tau^- \rightarrow \mu\gamma$



Smear with assumed FCC-ee detector resolutions (ILC-like detector):

- Muon momentum [GeV]  
 $\sigma(p_T)/p_T = 2 \times 10^{-5} \times p_T \oplus 1 \times 10^{-3}$
- Photon ECAL energy [GeV]  
 $\sigma(E)/E = 0.165/\sqrt{E} \oplus 0.010/E \oplus 0.011$
- Photon ECAL spatial [mm]  
 $\sigma(x) = \sigma(y) = (6/E \oplus 2) \text{ mm}$

FCC-ee effective resolution for  $\tau \rightarrow \mu\gamma$

$$\sigma(m_{\gamma\mu}) = 26 \text{ MeV}; \quad \sigma(E_{\gamma\mu}) = 850 \text{ MeV}$$

In order to de-correlate the E and m variables, this mass is in fact the measured mass scaled by measured energy over beam energy:

$$m_{\gamma\mu} = m_{\text{raw}} \times (E_{\gamma\mu}/E_{\text{beam}})$$

Recent suggestion: Crystal ECAL for FCC-ee

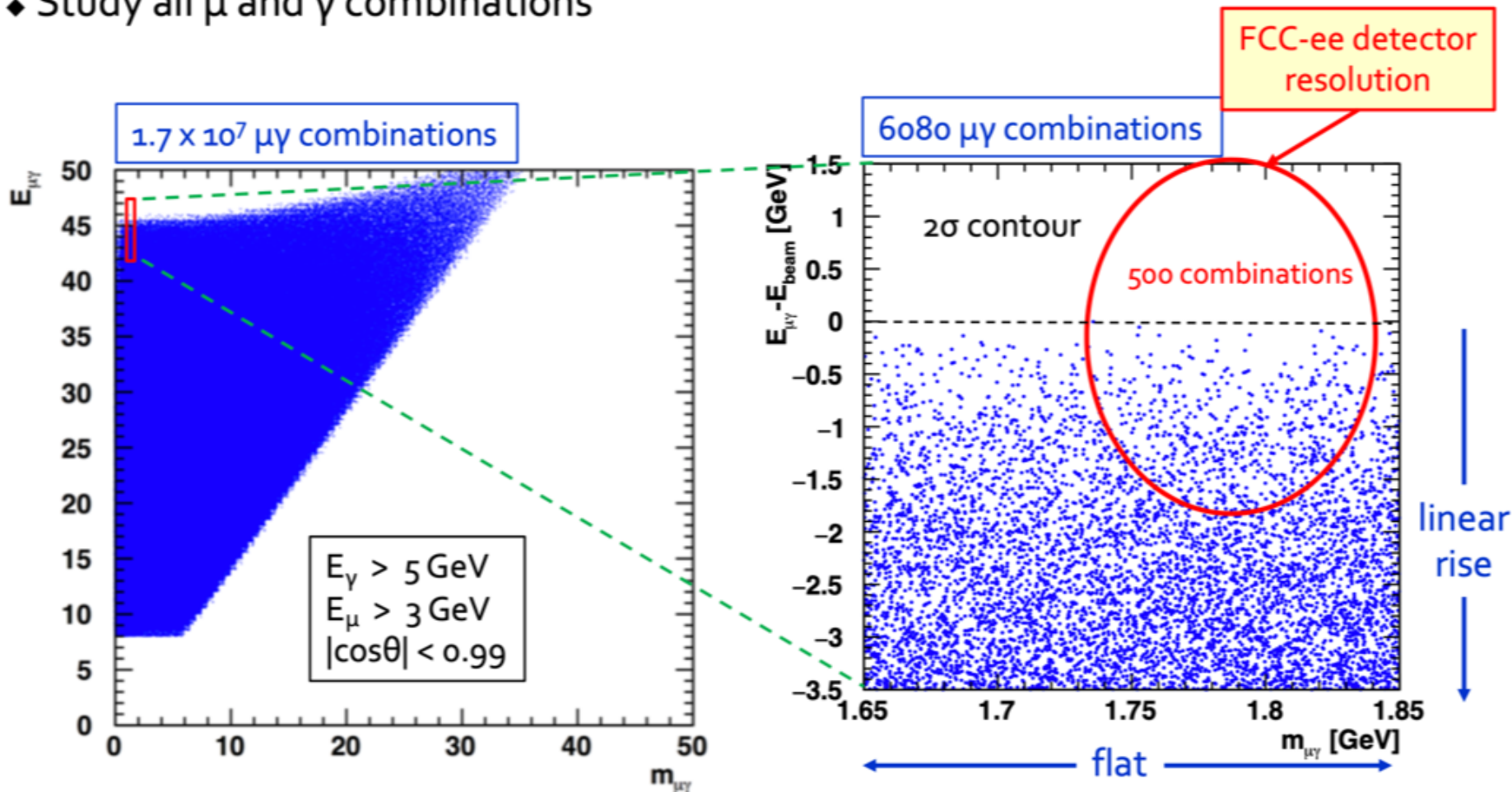
$$\sigma(E)/E = 0.03/\sqrt{E} \oplus 0.011$$

Resolution ellipse factor  $\sim 4$  smaller in both directions

2008.00338

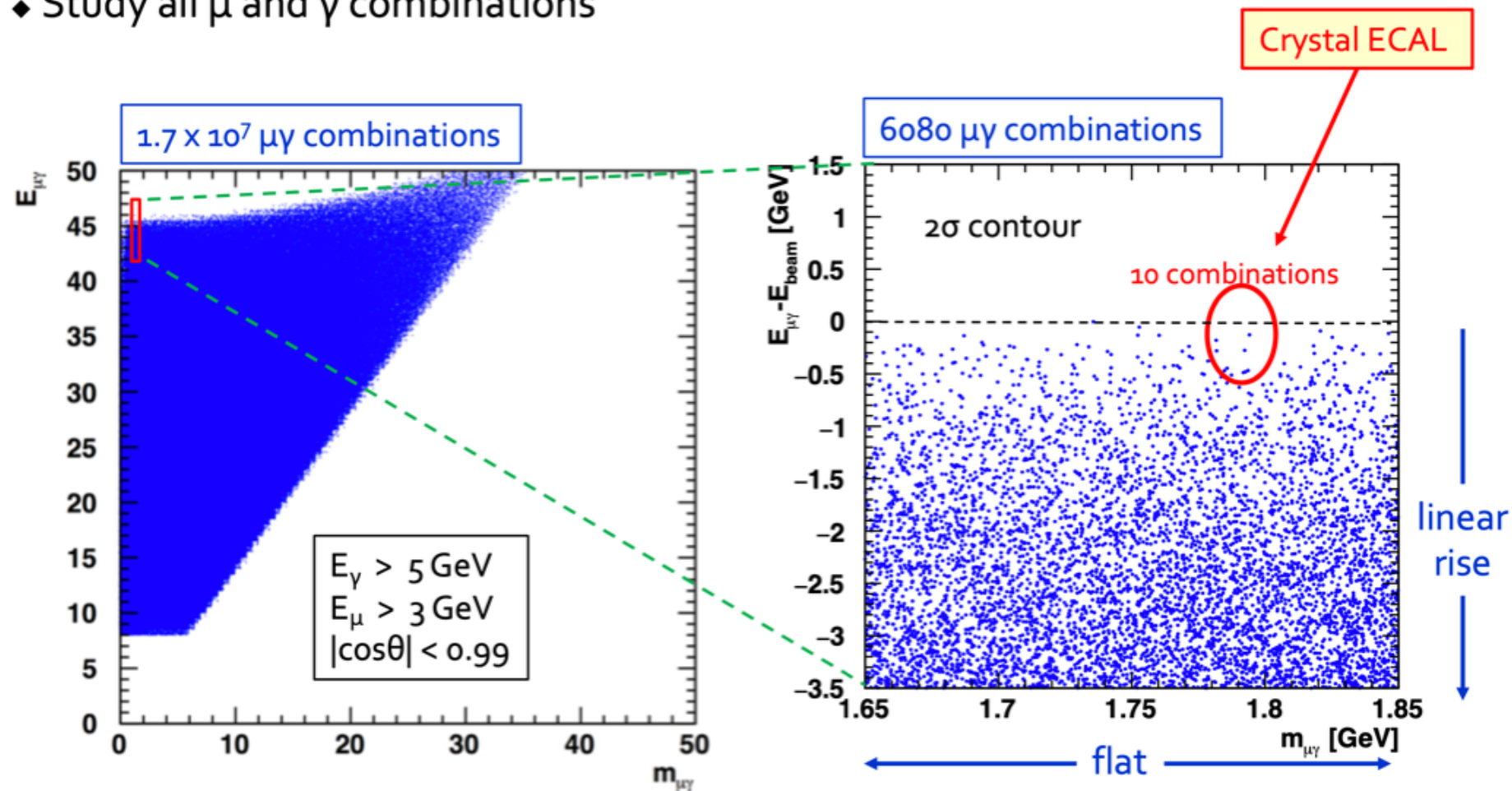
# $\tau \rightarrow \mu\gamma$ Study – The background

- ◆ Background: Generate  $5 \times 10^8$  events  $e^+e^- \rightarrow Z \rightarrow \tau^+\tau^-(\gamma) \rightarrow (\mu^+\nu\nu)(\mu^-\nu\nu)(\gamma)$ 
  - $1 \times 10^9$   $\tau \rightarrow \mu\nu\nu$  decays corresponding to
    - ◆  $5.7 \times 10^9$   $\tau$  decays from  $8.4 \times 10^{10}$  Z decays (1.6% of full FCC-ee statistics)
- ◆ Study all  $\mu$  and  $\gamma$  combinations



# $\tau \rightarrow \mu\gamma$ Study – The background

- ◆ Background: Generate  $5 \times 10^8$  events  $e^+e^- \rightarrow Z \rightarrow \tau^+\tau^-(\gamma) \rightarrow (\mu^+\nu\nu)(\mu^-\nu\nu)(\gamma)$ 
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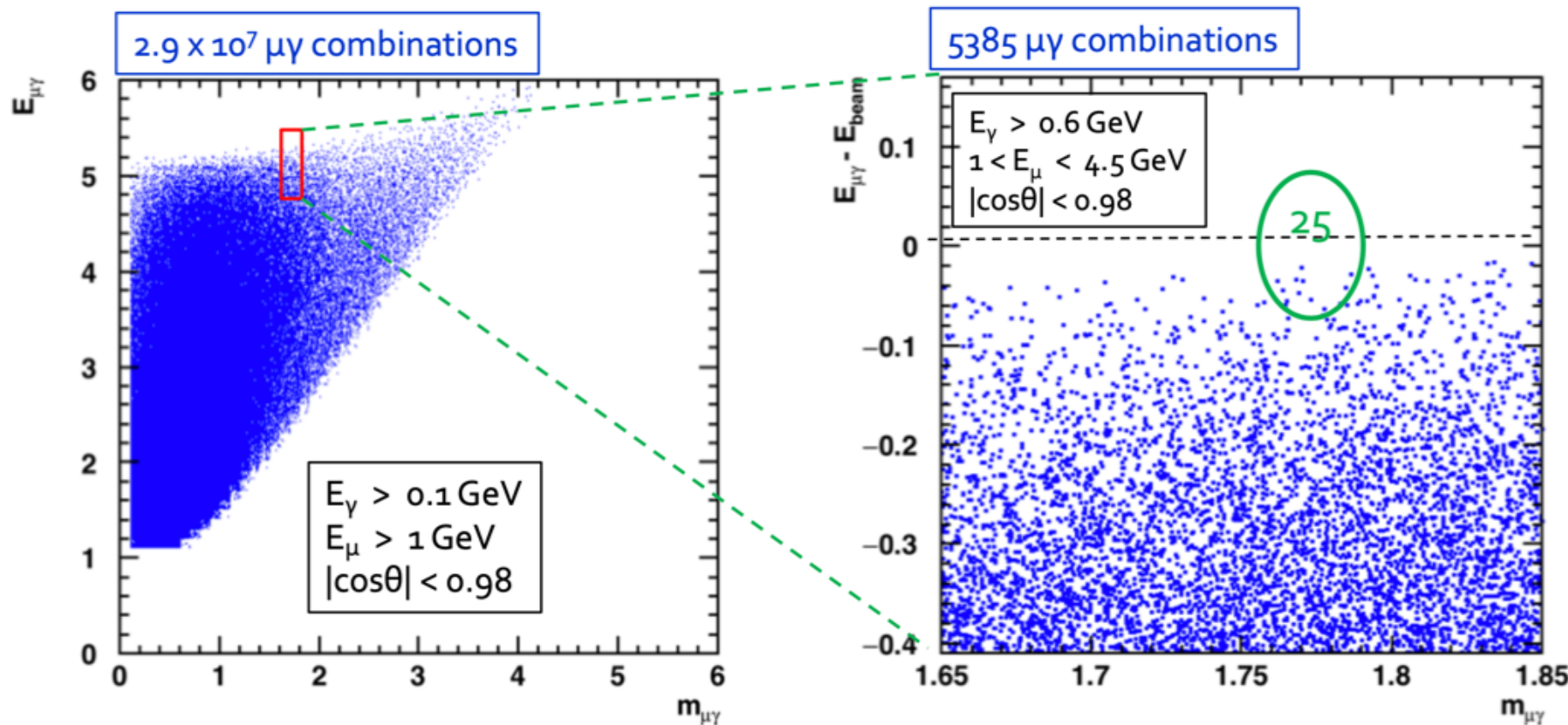




# $\tau \rightarrow \mu\gamma$ Study – Check of method

**Cross check:** Perform similar study at B-factory,  $\sqrt{s} = 10.6$  GeV

□ Again  $5 \times 10^8$  events  $e^+e^- \rightarrow Z \rightarrow \tau^+\tau^-(\gamma) \rightarrow (\mu^+\nu\nu)(\mu^-\nu\nu)(\gamma)$



From this study, estimated limit:  $1.9 \times 10^{-9}$

Compare to my extrapolation of current BaBar limit:  $\sim 3-4 \times 10^{-9}$

Agrees within a factor 2  
Not too bad