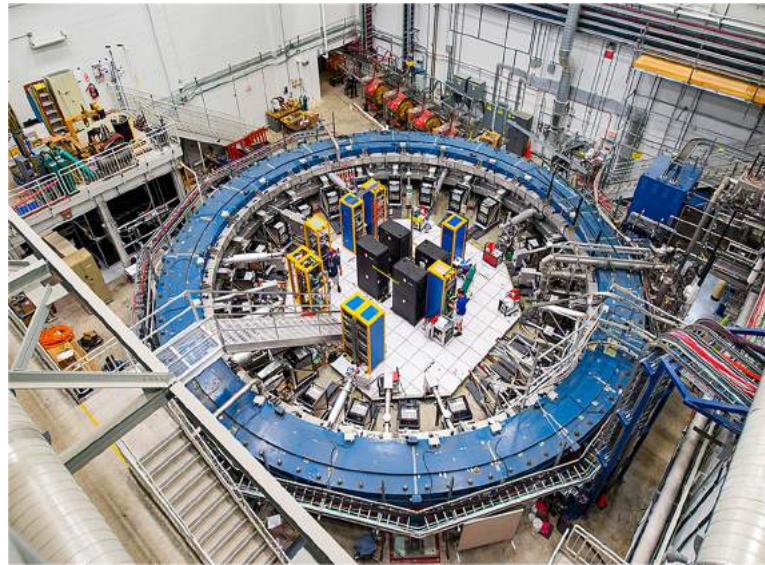


# Muon g-2 and $\Delta\alpha$ connection

Keshavarzi, Marciano, Passera and Sirlin  
Phys. Rev. D 102 (2020) 033002



Alex Keshavarzi

 @AlexKeshavarzi

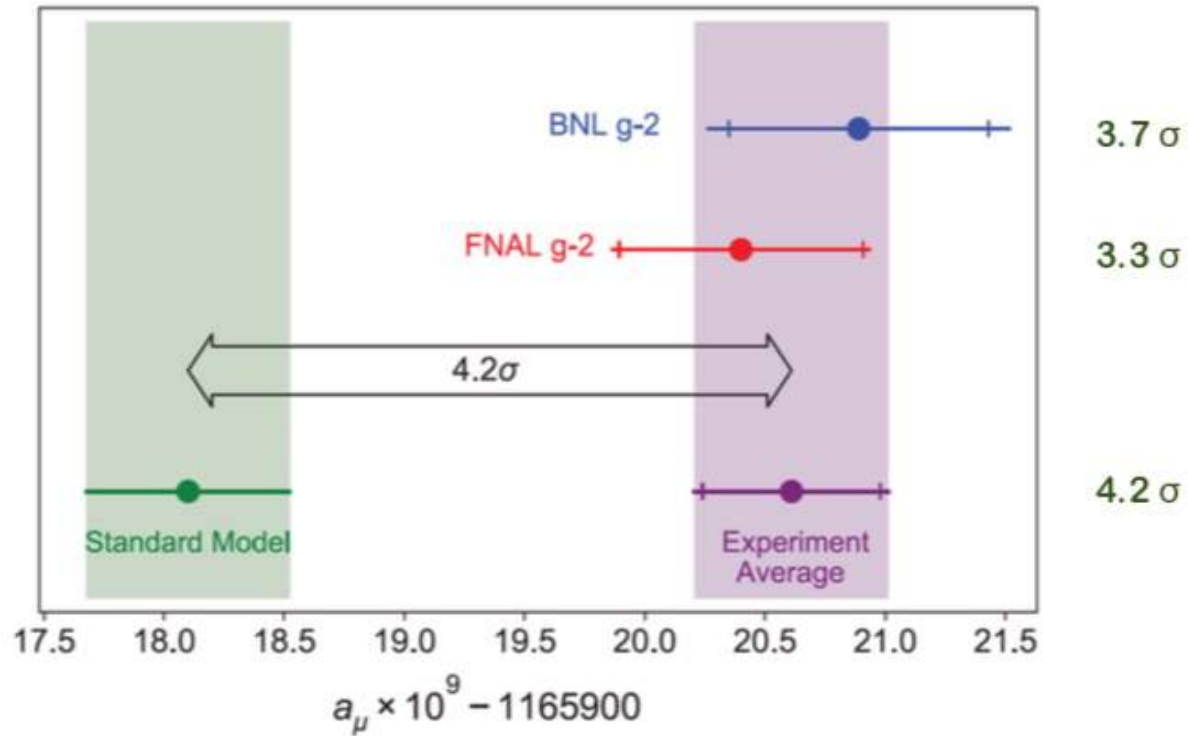
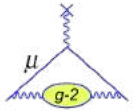
TAU21

29<sup>th</sup> September 2021

MANCHESTER  
1824

The University of Manchester

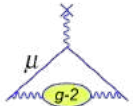
# Muon g-2: FNAL confirms BNL



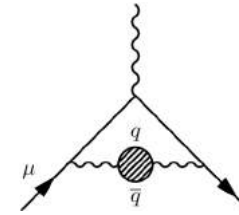
$a_\mu^{\text{EXP}} = (116592089 \pm 63) \times 10^{-11}$  [0.54ppm] BNL E821  
 $a_\mu^{\text{EXP}} = (116592040 \pm 54) \times 10^{-11}$  [0.46ppm] FNAL E989 Run 1  
 $a_\mu^{\text{EXP}} = (116592061 \pm 41) \times 10^{-11}$  [0.35ppm] WA

# Muon g-2 in the SM: HVP

$$\Delta a_\mu = 279(76) \times 10^{-11} \rightarrow 2.39(0.65) \text{ ppm}$$



- Hadronic Vacuum Polarisation - hadronic blob coupled to 2 photons.
- Two-point function - in principle, much easier than HLbL.
- Most precisely calculated from  $e^+e^- \rightarrow$  hadrons cross section data.



## Lattice (error ~ 1.6 ppm of $a_\mu^{\text{SM}}$ )

- Uncertainties dominated by finite volume, discretisation and isospin breaking systematics.

## Data-driven (error ~ 0.3 ppm of $a_\mu^{\text{SM}}$ )

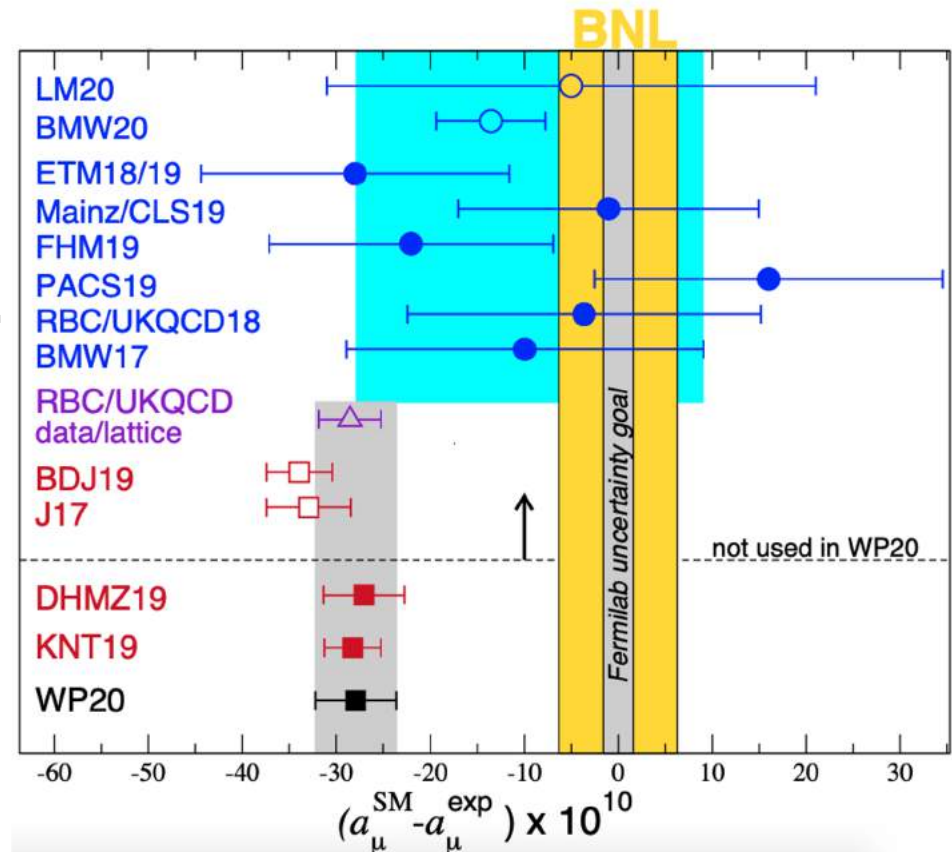
- Cross section data consistently combined and input into dispersion integral:

$$a_\mu^{\text{LOHVP}} = \frac{1}{4\pi^3} \int_{s_{th}}^{\infty} ds K(s) \sigma_{\text{had}}(s)$$

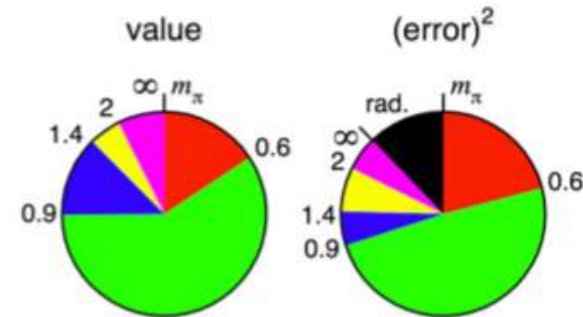
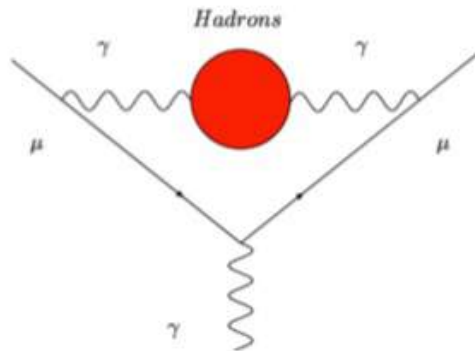
- Several groups have achieved this.

Recommended Muon g-2 TI value from data-driven result:

$$a_\mu^{\text{HVP}} = 6845(40) \times 10^{-11}$$



# The LO hadronic contribution



Keshavarzi, Nomura, Teubner 2018

$$a_{\mu}^{\text{HLO}} = \frac{1}{4\pi^3} \int_{m_{\pi}^2}^{\infty} ds K(s) \sigma_{\text{had}}^{(0)}(s)$$

$$K(s) = \int_0^1 dx \frac{x^2 (1-x)}{x^2 + (1-x)(s/m_{\mu}^2)}$$

$$a_{\mu}^{\text{HLO}} = 6895 (33) \times 10^{-11}$$

F. Jegerlehner, arXiv:1711.06089

$$= 6939 (40) \times 10^{-11}$$

Davier, Hoecker, Malaescu, Zhang, arXiv:1908.00921

$$= 6928 (24) \times 10^{-11}$$

Keshavarzi, Nomura, Teubner, arXiv:1911.00367

$$= 6931 (40) \times 10^{-11} (0.6\%)$$

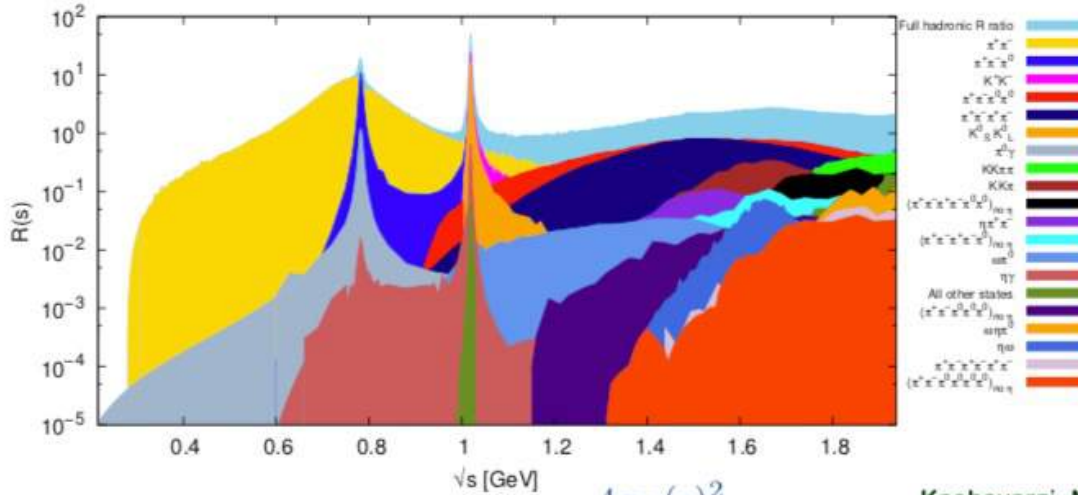
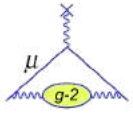
WP20 value

 WP20 value obtained merging conservatively DHMZ + KNT + constraints from CHHKs  
Colangelo, Hoferichter, Hoid, Kubis, Stoffer 2018-19

 Radiative Corrections to  $\sigma(s)$  are crucial. S. Actis et al, Eur. Phys. J. C66 (2010) 585

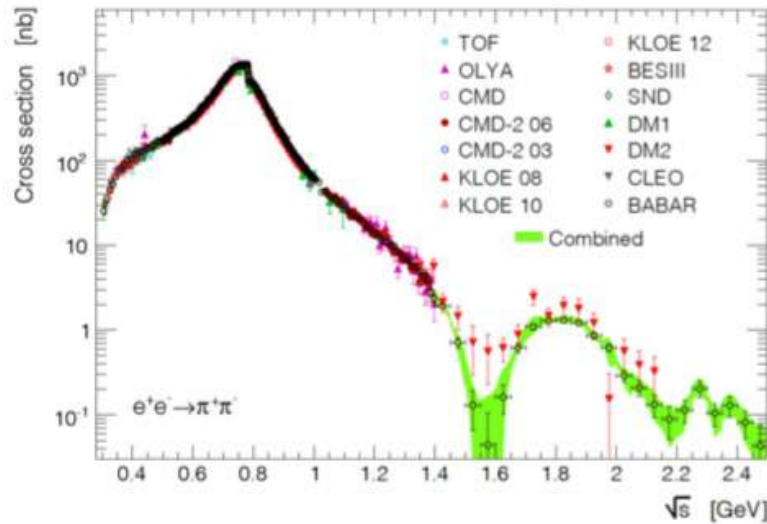


# Low energy hadronic cross section



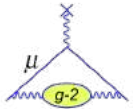
$$R(s) = \sigma(e^+e^- \rightarrow \text{hadrons}) / \frac{4\pi\alpha(s)^2}{3s}$$

Keshavarzi, Nomura Teubner  
PRD 2018



Davier, Hoecker, Malaescu, Zhang  
EPJC 2020

# Muon g-2: the discrepancy $\Delta a_\mu = 279(76) \times 10^{-11} \rightarrow 2.39(0.65)$ ppm



- Comparing the SM prediction with the measured muon g-2 value:

$$a_\mu^{\text{EXP}} = 116592061 (41) \times 10^{-11}$$

BNL+FNAL

$$a_\mu^{\text{SM}} = 116591810 (43) \times 10^{-11}$$

WP20

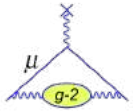
$$\Delta a_\mu = a_\mu^{\text{EXP}} - a_\mu^{\text{SM}} = 251 (59) \times 10^{-11}$$

4.2  $\sigma$

If BMW 2021 HLO instead of WP20, EXP & SM differ only by **1.6 $\sigma$**

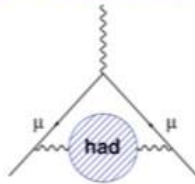
- Is  $\Delta a_\mu$  due to **new physics** beyond the SM? Could be due to:
  - NP at the weak scale and weakly coupled to SM particles
  - NP very heavy and strongly coupled to SM particles
  - NP very light ( $\Lambda \lesssim 1$  GeV) and feebly coupled to SM particles

# Hadronic cross section data



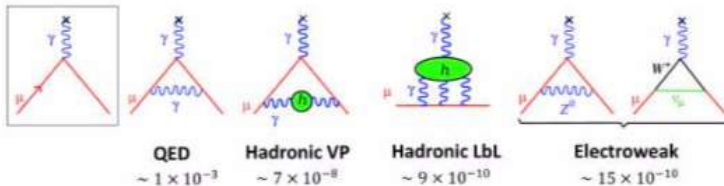
Experimentally measured hadronic cross section:

Muon g-2:  
hadronic vacuum polarisation contribution



$$a_{\mu}^{\text{had, VP}} = \frac{1}{4\pi^3} \int_{m_{\pi}^2}^{\infty} ds \sigma_{\text{had}}(s) K(s)$$

... sum with other SM contributions...



→ Determines  $a_{\mu}^{\text{SM}}$  and  $\Delta a_{\mu} = 3.7\sigma$

Increase cross section so that  $\Delta a_{\mu} = 0?$

→ Solves muon g-2 discrepancy

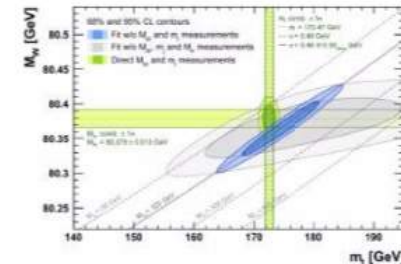
$\sigma_{\text{had}}$

Running QED coupling:  
hadronic contribution to running



$$\Delta\alpha_{\text{had}}^{(5)}(q^2) = \frac{q^2}{4\pi\alpha^2} \int_{m_{\pi}^2}^{\infty} ds \sigma_{\text{had}}(s) \frac{q^2}{(q^2 - s)}$$

... evaluate at  $q^2 = M_Z^2$  and input into **global EW fit...**



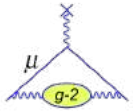
→ Predicts  $M_W, M_H, \sin^2 \theta_{\text{eff}}^{lep}$  and more...

Increase cross section so that  $\Delta a_{\mu} = 0?$

→ What happens to precision EW parameters?

# Muon g-2 and $\Delta\alpha$

Marciano, Passera and Sirlin  
Phys. Rev. D 78 (2008) 013009



- Can  $\Delta a_\mu$  be due to **hypothetical mistakes** in the hadronic  $\sigma(s)$ ?
- An upward shift of  $\sigma(s)$  also induces an increase of  $\Delta\alpha_{\text{had}}^{(5)}(M_Z)$ .
- Consider:

$$a_{\mu}^{\text{HLO}} \rightarrow a = \int_{4m_\pi^2}^{s_u} ds f(s) \sigma(s), \quad f(s) = \frac{K(s)}{4\pi^3}, \quad s_u < M_Z^2,$$

$$\Delta\alpha_{\text{had}}^{(5)} \rightarrow b = \int_{4m_\pi^2}^{s_u} ds g(s) \sigma(s), \quad g(s) = \frac{M_Z^2}{(M_Z^2 - s)(4\alpha\pi^2)},$$

and the increase

$$\Delta\sigma(s) = \epsilon\sigma(s)$$

$\epsilon > 0$ , in the range:

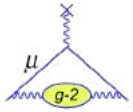
$$\sqrt{s} \in [\sqrt{s_0} - \delta/2, \sqrt{s_0} + \delta/2]$$

Note the very different energy-dependent weighting of the integrands...

Use precise and up-to-date compilation of total hadronic cross section from KNT  
Keshavarzi, Nomura and Teubner, Phys.Rev.D 101 (2020) 014029, arXiv:1911.00367



# Muon $g-2$ : connection with the SM Higgs



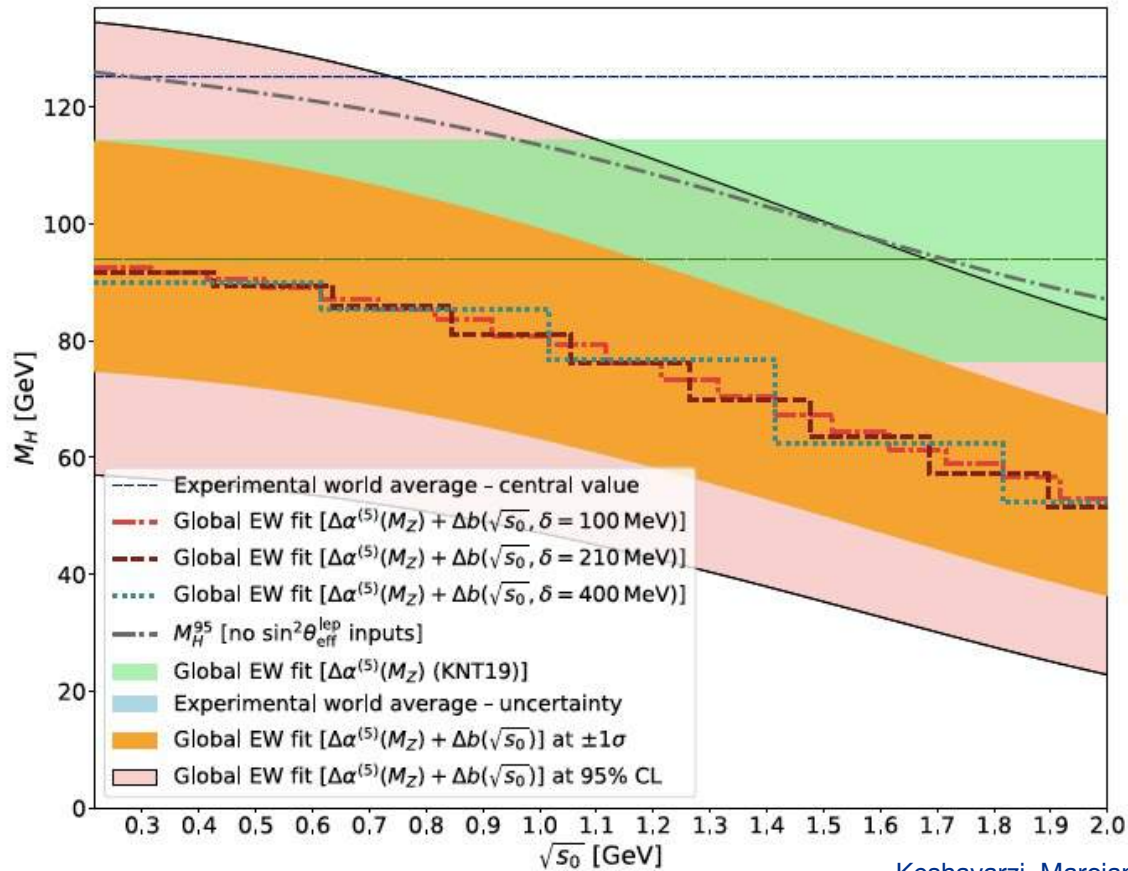
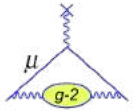
Major update: Higgs discovered, improved EW observables ( $M_W$ ,  $\sin^2\theta$ ,  $M_{\text{top}}$ , ...), updates to  $\sigma(s)$ , theory improvements, global fit, ...

Using Gfitter

Parameter	Input value	Reference	Fit result	Result w/o input value
$M_W$ (GeV)	80.379(12)	[5]	80.359(3)	80.357(4)(5)
$M_H$ (GeV)	125.10(14)	[5]	125.10(14)	$94^{+20+6}_{-18-6}$
$\Delta\alpha_{\text{had}}^{(5)}(M_Z^2) \times 10^4$	276.1(1.1)	[23]	275.8(1.1)	272.2(3.9)(1.2)
$m_t$ (GeV)	172.9(4)	[5]	173.0(4)	...
$\alpha_s(M_Z^2)$	0.1179(10)	[5]	0.1180(7)	...
$M_Z$ (GeV)	91.1876(21)	[5]	91.1883(20)	...
$\Gamma_Z$ (GeV)	2.4952(23)	[5]	2.4940(4)	...
$\Gamma_W$ (GeV)	2.085(42)	[5]	2.0903(4)	...
$\sigma_{\text{had}}^0$ (nb)	41.541(37)	[108]	41.490(4)	...
$R_l^0$	20.767(25)	[108]	20.732(4)	...
$R_c^0$	0.1721(30)	[108]	0.17222(8)	...
$R_b^0$	0.21629(66)	[108]	0.21581(8)	...
$\bar{m}_c$ (GeV)	1.27(2)	[5]	1.27(2)	...
$\bar{m}_b$ (GeV)	$4.18^{+0.03}_{-0.02}$	[5]	$4.18^{+0.03}_{-0.02}$	...
$A_{\text{FB}}^{0,l}$	0.0171(10)	[108]	0.01622(7)	...
$A_{\text{FB}}^{0,c}$	0.0707(35)	[108]	0.0737(2)	...
$A_{\text{FB}}^{0,b}$	0.0992(16)	[108]	0.1031(2)	...
$A_{\ell}$	0.1499(18)	[75,108]	0.1471(3)	...
$A_c$	0.670(27)	[108]	0.6679(2)	...
$A_b$	0.923(20)	[108]	0.93462(7)	...
$\sin^2\theta_{\text{eff}}^{\text{lep}}(Q_{\text{FB}})$	0.2324(12)	[108]	0.23152(4)	0.23152(4)(4)
$\sin^2\theta_{\text{eff}}^{\text{lep}}(\text{Had Coll})$	0.23140(23)	[100]	0.23152(4)	0.23152(4)(4)

Keshavarzi, Marciano, Passera and Sirlin  
Phys. Rev. D 102 (2020) 033002

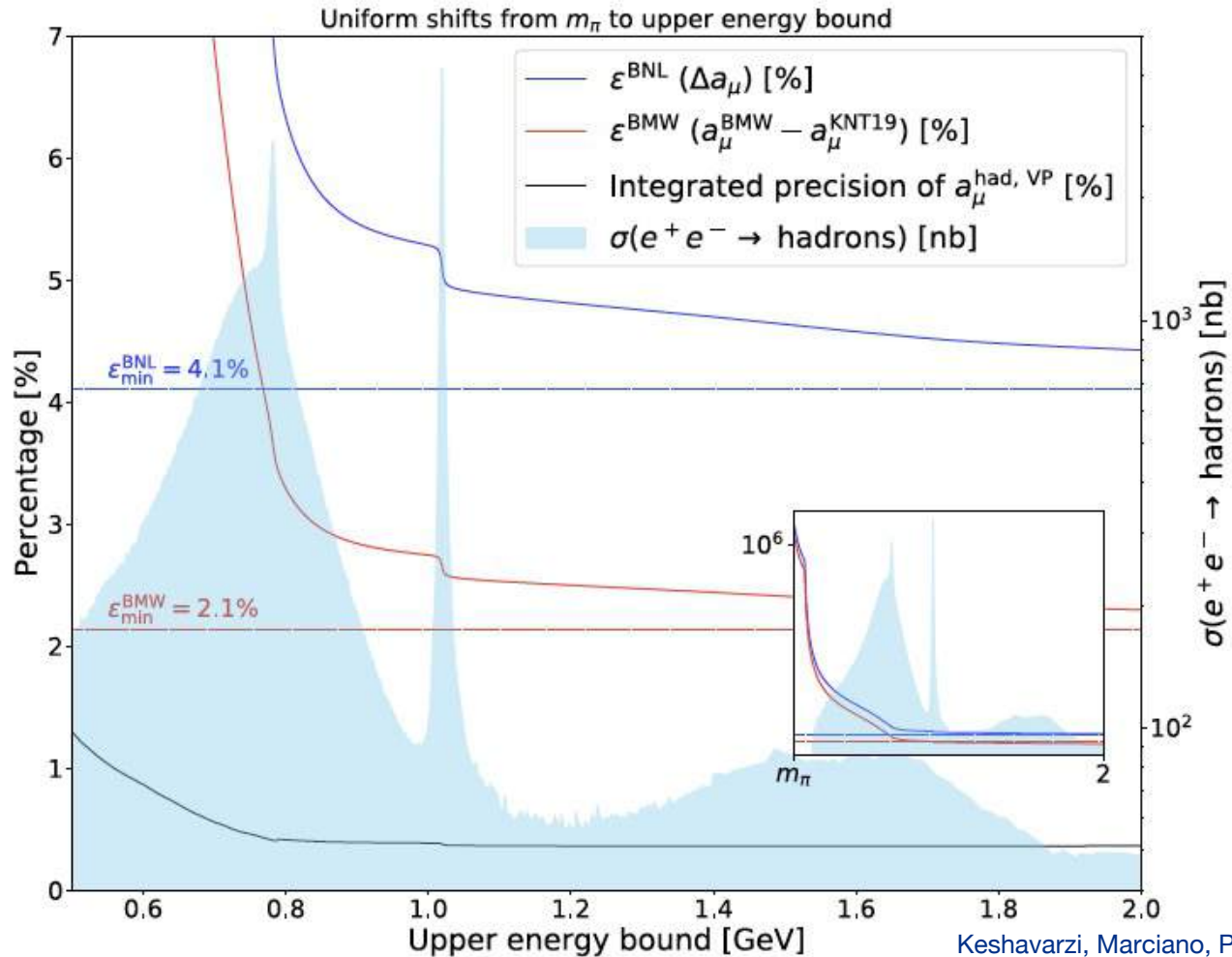
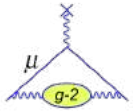
# Muon g-2: connection with the SM Higgs



Keshavarzi, Marciano, Passera and Sirlin  
Phys. Rev. D 102 (2020) 033002

**Shifts  $\Delta\sigma(s)$  to fix  $\Delta a_\mu$  are possible,  
but conflict with the EW fit if they occur above  $\sim 1 \text{ GeV}$**

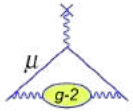
# How large are the required shifts?



Keshavarzi, Marciano, Passera and Sirlin  
Phys. Rev. D 102 (2020) 033002

Shifts below  $\sim 1$  GeV conflict with the quoted exp. precision of  $\sigma(s)$

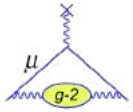
# $a_\mu \leftrightarrow \Delta\alpha$ : recent related literature



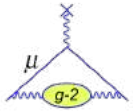
- Crivellin, Hoferichter, Manzari and Montull, “Hadronic vacuum polarization:  $(g-2)_\mu$  versus global electroweak fits,” arXiv:2003.04886.
- Eduardo de Rafael, “On Constraints Between  $\Delta\alpha_{\text{had}}(M_Z^2)$  and  $(g_\mu-2)_{\text{HVP}}$ ,” arXiv:2006.13880.
- Malaescu and Schott, “Impact of correlations between  $a_\mu$  and  $\alpha_{\text{QED}}$  on the EW fit,” arXiv:2008.08107.
- Colangelo, Hoferichter and Stoffer, “Constraints on the two-pion contribution to hadronic vacuum polarization,” arXiv:2010.07943.



# Conclusions

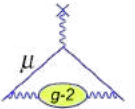


- Fermilab's Muon  $g-2$  Experiment has confirmed BNL's result: the discrepancy between experiment and SM increases to  $4.2\sigma$ .
- The BMWc lattice QCD result weakens the exp-SM discrepancy. It must be confirmed or refuted by other lattice calculations.
- Both the hadronic contributions to the muon  $g-2$  and the running QED coupling depend on the measured hadronic cross section.
- This connection between  $g-2$  and  $\Delta\alpha$  allows the impact of the muon  $g-2$  discrepancy on the EW fit to be explored.
- Increases to the hadronic cross section to solve muon  $g-2$  discrepancy affect the predictions of EW precision observables.
- This study excludes shifts to hadronic cross section above 0.7 GeV to bridge muon  $g-2$  discrepancy.
- However, the required shifts to the hadronic cross section below 0.7 GeV are large and unlikely.



# Backups

# Magnetic moments



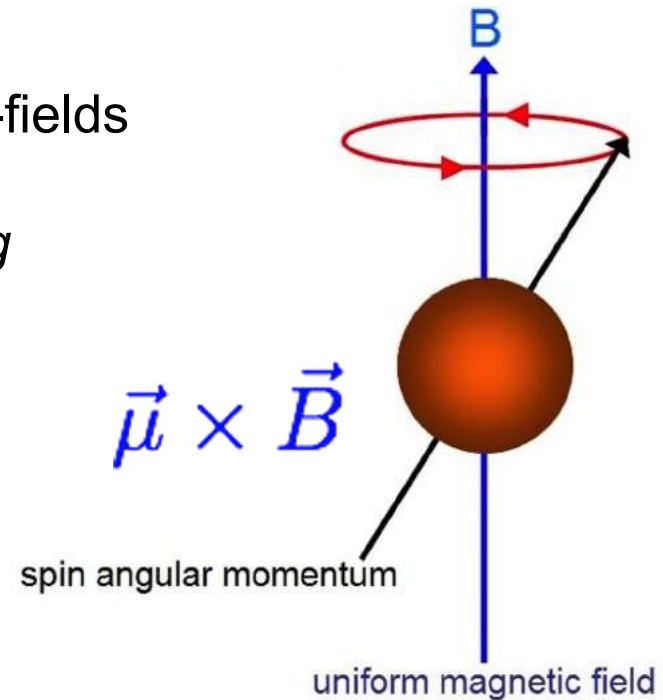
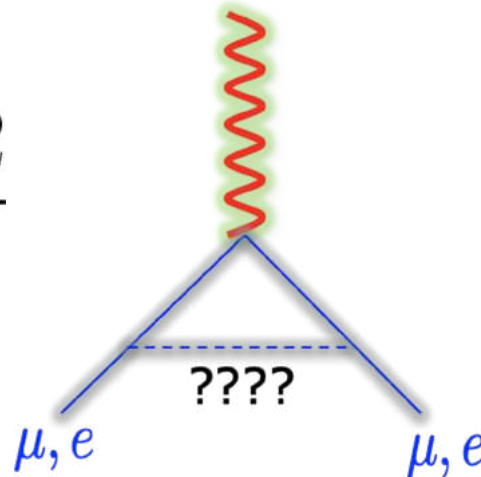
The muon has an intrinsic magnetic moment that is coupled to its spin via the gyromagnetic ratio  $g$ :

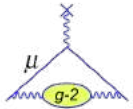
$$\vec{\mu} = g \frac{e}{2m_\mu} \vec{S}$$

Magnetic moment (spin) interacts with external B-fields

Makes spin precess at frequency determined by  $g$

$$a_\mu = \frac{g - 2}{2}$$





# Muon g-2 Theory

arXiv.org > hep-ph > arXiv:2006.04822

Search...  
Help | Advanced

High Energy Physics – Phenomenology

[Submitted on 8 Jun 2020]

## The anomalous magnetic moment of the muon in the Standard Model

T. Aoyama, N. Asmussen, M. Benayoun, J. Bijnens, T. Blum, M. Bruno, I. Caprini, C. M. Carloni Calame, M. Cè, G. Colangelo, F. Curciarello, H. Czyż, I. Danilkin, M. Davier, C. T. H. Davies, M. Della Morte, S. I. Eidelman, A. X. El-Khadra, A. Gérardin, D. Giusti, M. Golterman, Steven Gottlieb, V. Gülpers, F. Hagelstein, M. Hayakawa, G. Herdoiza, D. W. Hertzog, A. Hoecker, M. Hoferichter, B.-L. Hoid, R. J. Hudspith, F. Ignatov, T. Izubuchi, F. Jegerlehner, L. Jin, A. Keshavarzi, T. Kinoshita, B. Kubis, A. Kupich, A. Kupść, L. Laub, C. Lehner, L. Lellouch, I. Logashenko, B. Malaescu, K. Maltman, M. K. Marinković, P. Masjuan, A. S. Meyer, H. B. Meyer, T. Mibe, K. Miura, S. E. Müller, M. Nio, D. Nomura, A. Nyffeler, V. Pascalutsa, M. Passera, E. Perez del Rio, S. Peris, A. Portelli, M. Procura, C. F. Redmer, B. L. Roberts, P. Sánchez-Puertas, S. Serednyakov, B. Schwartz, S. Simula, D. Stöckinger, H. Stöckinger-Kim, P. Stoffer, T. Teubner, R. Van de Water, M. Vanderhaeghen, G. Venanzoni, G. von Hippel, H. Wittig, Z. Zhang, M. N. Achasov, A. Bashir, N. Cardoso, B. Chakraborty, E.-H. Chao, J. Charles, A. Crivellin, O. Deineka, A. Denig, C. DeTar, C. A. Dominguez, A. E. Dorokhov, V. P. Druzhinin, G. Eichmann, M. Fael, C. S. Fischer, E. Gámiz, Z. Gelzer, J. R. Green, S. Guellati-Khelifa, D. Hatton, N. Hermansson-Truedsson et al. (32 additional authors not shown)

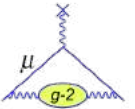
## The Muon g-2 Theory Initiative





# Muon g-2 in the SM

$$\Delta a_\mu = 279(76) \times 10^{-11} \rightarrow 2.39(0.65) \text{ ppm}$$



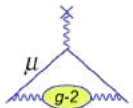
- $a_\mu$  arises due to quantum corrections / higher order interactions / loop contributions
- All SM particles contribute  $\rightarrow$  Calculate and sum all sectors of the SM:

$$a_\mu^{\text{SM}} = a_\mu^{\text{QED}} + a_\mu^{\text{EW}} + a_\mu^{\text{HVP}} + a_\mu^{\text{HLbL}}$$

			$a_\mu^{\text{SM}}$ portion	$\delta a_\mu^{\text{SM}}$ portion
<b>QED</b>		Perturbative (Known to five-loop)	$\sim 99.99\%$	$\sim 0.001\%$
<b>EW</b>		Perturbative (Known to two-loop)	$\sim 1 \text{ ppm}$	$\sim 0.2\%$
<b>HVP</b>		Non-perturbative (Data-driven & lattice)	$\sim 59 \text{ ppm}$	$\sim 84\%$
<b>HLbL</b>		Non-perturbative (Data-driven & lattice)	$\sim 1 \text{ ppm}$	$\sim 16\%$

# Muon g-2 in the SM: QED

$$\Delta a_\mu = 279(76) \times 10^{-11} \rightarrow 2.39(0.65) \text{ ppm}$$



$$a_\mu^{\text{QED}} = (1/2)(\alpha/\pi) \quad \text{Schwinger 1948}$$

$$+ 0.765857426 (16) (\alpha/\pi)^2$$

Sommerfeld; Petermann; Suura&Wichmann '57; Elend '66; MP '04

$$+ 24.05050988 (28) (\alpha/\pi)^3$$

Remiddi, Laporta, Barbieri ... ; Czarnecki, Skrzypek '99; MP '04;  
Friot, Greynat & de Rafael '05, Ananthanarayan, Friot, Ghosh 2020

$$+ 130.8780 (60) (\alpha/\pi)^4$$

Kinoshita & Lindquist '81, ... , Kinoshita & Nio '04, '05;  
Aoyama, Hayakawa, Kinoshita & Nio, 2007, Kinoshita et al. 2012 & 2015;  
Steinhauser et al. 2013, 2015 & 2016 (all electron &  $\tau$  loops, analytic);  
Laporta, PLB 2017 (mass independent term) **COMPLETED!**

$$+ 750.86 (88) (\alpha/\pi)^5 \text{ COMPLETED!}$$

Kinoshita et al. '90, Yelkhovsky, Milstein, Starshenko, Laporta, ...  
Aoyama, Hayakawa, Kinoshita, Nio 2012, 2015, 2017 & 2019.  
Volkov 1909.08015:  $A_1^{(10)}$ [no lept loops] at variance, but negligible  $\delta a_\mu \sim 6 \times 10^{-14}$

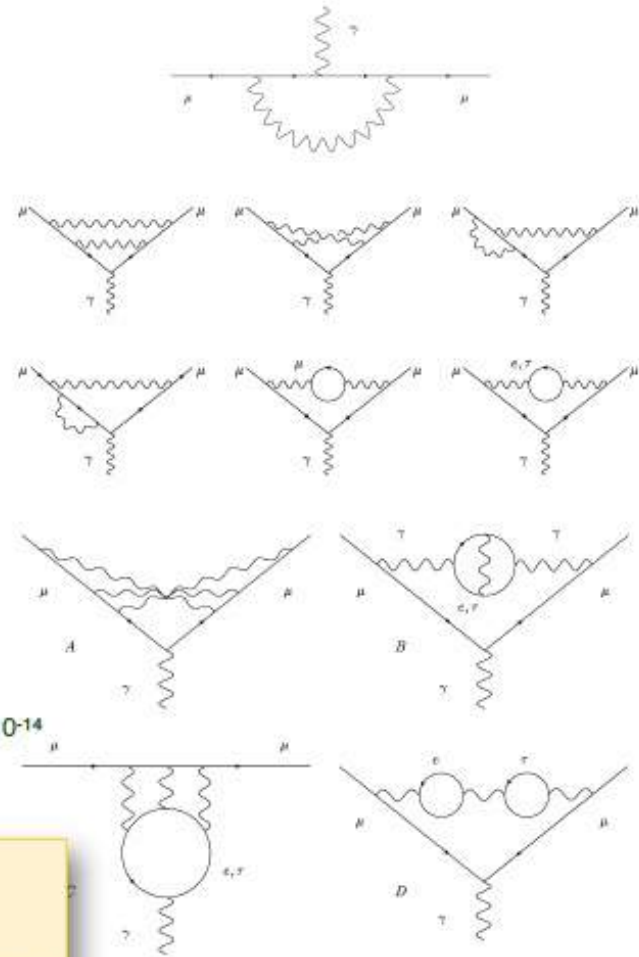
Adding up, we get:

$$a_\mu^{\text{QED}} = 116584718.931 (19)(100)(23) \times 10^{-11}$$

mainly from 4-loop coeff. unc.  $\leftarrow$  6-loop  $\leftarrow$  from  $\alpha(\text{Cs})$

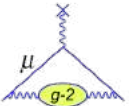
$\alpha = 1/137.035999046(27)$  [0.2ppb] Parker et al 2018

WP20 value

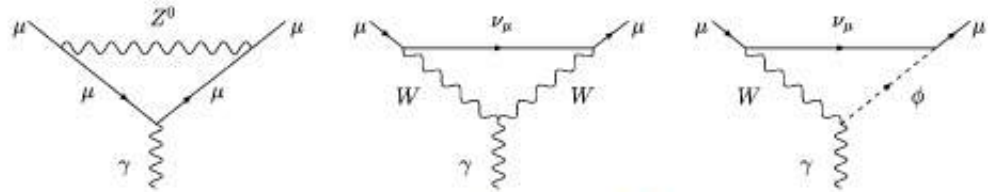


# Muon g-2 in the SM: EW

$$\Delta a_\mu = 279(76) \times 10^{-11} \rightarrow 2.39(0.65) \text{ ppm}$$



● One-loop term:



$$a_\mu^{\text{EW}}(1\text{-loop}) = \frac{5G_\mu m_\mu^2}{24\sqrt{2}\pi^2} \left[ 1 + \frac{1}{5} (1 - 4\sin^2\theta_W)^2 + O\left(\frac{m_\mu^2}{M_{Z,W,H}^2}\right) \right] \approx 195 \times 10^{-11}$$

1972: Jackiv, Weinberg; Bars, Yoshimura; Altarelli, Cabibbo, Maiani; Bardeen, Gastmans, Lautrup; Fujikawa, Lee, Sanda; Studenikin et al. '80s

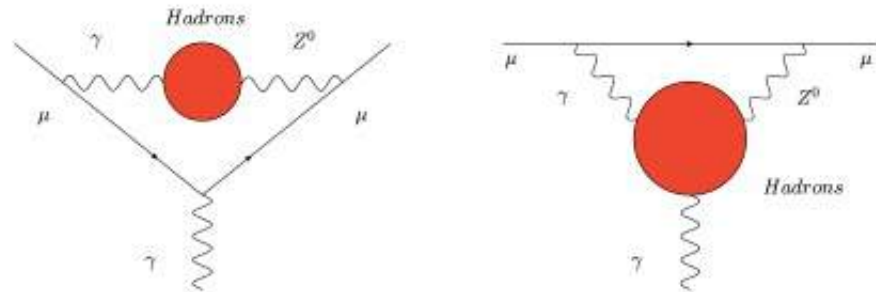
● One-loop plus higher-order terms:

$$a_\mu^{\text{EW}} = 153.6 (1.0) \times 10^{-11}$$

Kukhto et al. '92; Czarnecki, Krause, Marciano '95; Knecht, Peris, Perrotet, de Rafael '02; Czarnecki, Marciano and Vainshtein '02; Degrassi and Giudice '98; Heinemeyer, Stockinger, Weiglein '04; Gribouk and Czarnecki '05; Vainshtein '03; Gnendiger, Stockinger, Stockinger-Kim 2013, Ishikawa, Nakazawa, Yasui, 2019.

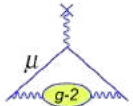
Hadronic loop uncertainties (and 3-loop nonleading logs).

WP20 value

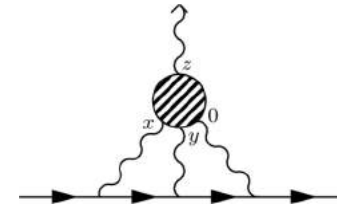


# Muon g-2 in the SM: HLbL

$$\Delta a_\mu = 279(76) \times 10^{-11} \rightarrow 2.39(0.65) \text{ ppm}$$



- HLbL scattering - hadronic blob coupled to 3 off-shell/1 on-shell photon.
- Four point function - notoriously difficult to calculate.
- Previously only calculated from models with large systematics.

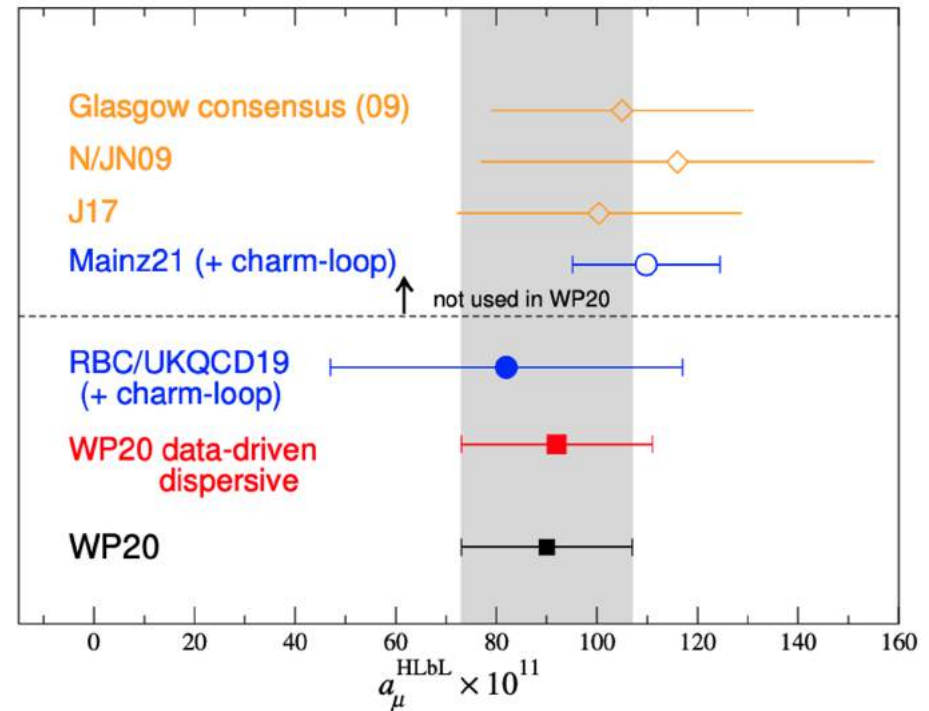


## Data-driven (error ~ 0.2 ppm of $a_\mu^{\text{SM}}$ )

- Model-independent dispersive evaluation, using data (e.g.  $\pi$ ,  $\eta$ ,  $\eta'$  TFFs) as input for hadronic insertions.

## Lattice (error ~ 0.3 ppm of $a_\mu^{\text{SM}}$ )

- Model-independent evaluation, computed on discretized Euclidean spacetime (lattice) in finite volume.



Recommended Muon g-2  
TI result (before Mainz):

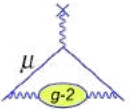
$$a_\mu^{\text{HLbL}} = 92(18) \times 10^{-11}$$

**Improved, but still evolving.**  
**Still systematics dominated**  
**(goal < 10% uncertainty)**

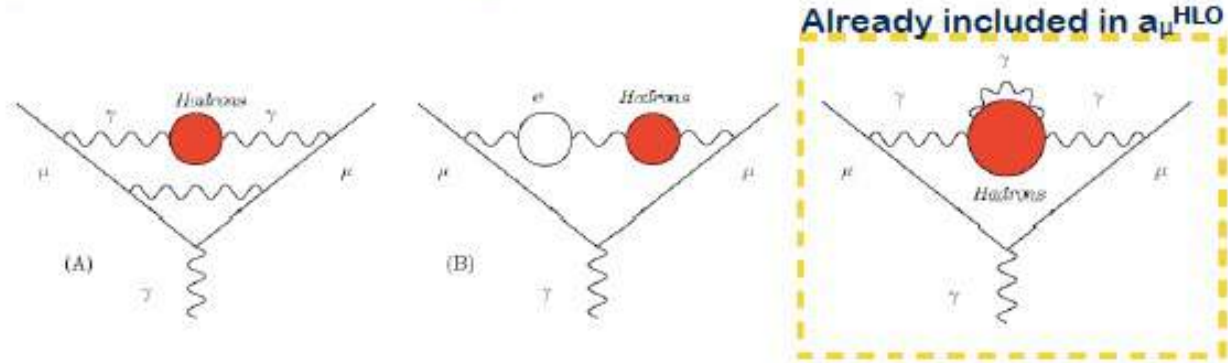


# Muon g-2: NLO HVP

$$\Delta a_\mu = 279(76) \times 10^{-11} \rightarrow 2.39(0.65) \text{ ppm}$$



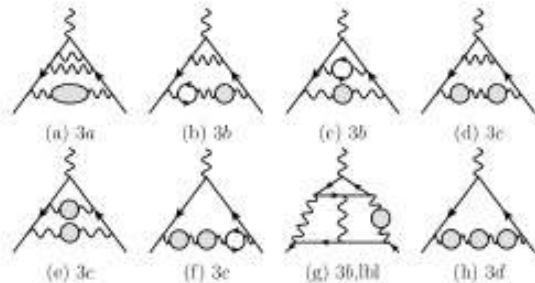
- $O(\alpha^3)$  contributions of diagrams containing HVP insertions:



$$a_\mu^{\text{HNLO}}(\text{vp}) = -98.3 (7) \times 10^{-11}$$

Krause '96; Keshavarzi, Nomura, Teubner 2019; WP20.

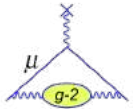
- $O(\alpha^4)$  contributions of diagrams containing HVP insertions:



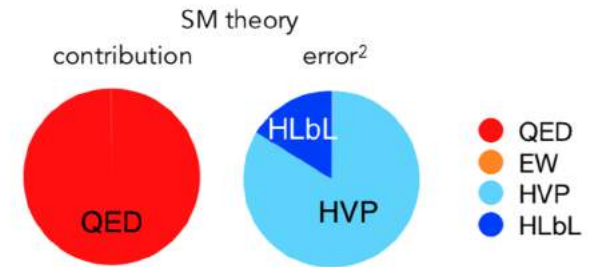
$$a_\mu^{\text{HNNLO}}(\text{vp}) = 12.4 (1) \times 10^{-11}$$

Kurz, Liu, Marquard, Steinhauser 2014

# Muon g-2 in the SM and Outlook



Contribution	Value $\times 10^{11}$
Experiment (E821)	116 592 089(63)
HVP LO ( $e^+e^-$ )	6931(40)
HVP NLO ( $e^+e^-$ )	-98.3(7)
HVP NNLO ( $e^+e^-$ )	12.4(1)
HVP LO (lattice, $udsc$ )	7116(184)
HLbL (phenomenology)	92(19)
HLbL NLO (phenomenology)	2(1)
HLbL (lattice, $uds$ )	79(35)
HLbL (phenomenology + lattice)	90(17)
QED	116 584 718.931(104)
Electroweak	153.6(1.0)
HVP ( $e^+e^-$ , LO + NLO + NNLO)	6845(40)
HLbL (phenomenology + lattice + NLO)	92(18)
Total SM Value	116 591 810(43)
Difference: $\Delta a_\mu := a_\mu^{\text{exp}} - a_\mu^{\text{SM}}$	279(76)



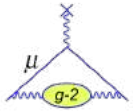
$$\Delta a_\mu = 279(76) \times 10^{-11} \rightarrow 2.39(0.65) \text{ ppm}$$

Muon g-2 theory initiative recommended result:

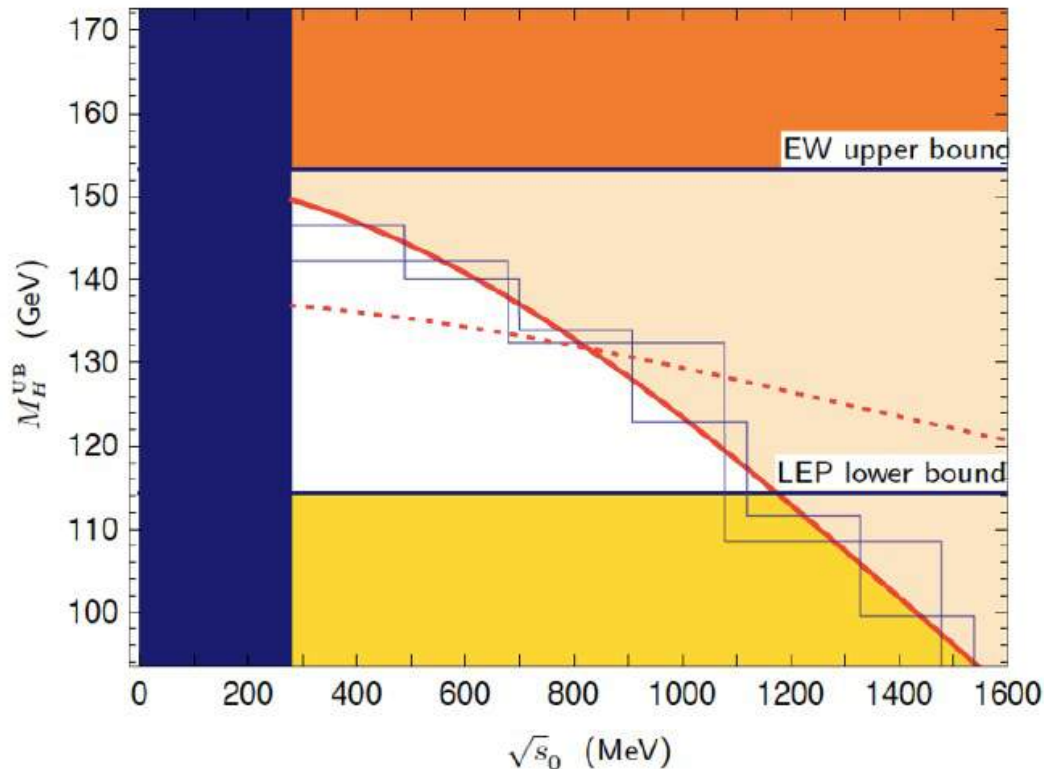
$$a_\mu^{\text{SM}} = 116\,591\,810(43) \times 10^{-11} \text{ (0.37 ppm)}$$

Results in  $3.7\sigma$  discrepancy when compared to BNL measurement.

# Muon $g-2$ : connection with the SM Higgs

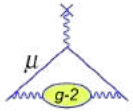


How much does the  $M_H$  upper bound from the EW fit change when we shift up  $\sigma(s)$  by  $\Delta\sigma(s)$  [and thus  $\Delta\alpha_{\text{had}}^{(5)}(M_Z)$ ] to fix  $\Delta a_\mu$  ?

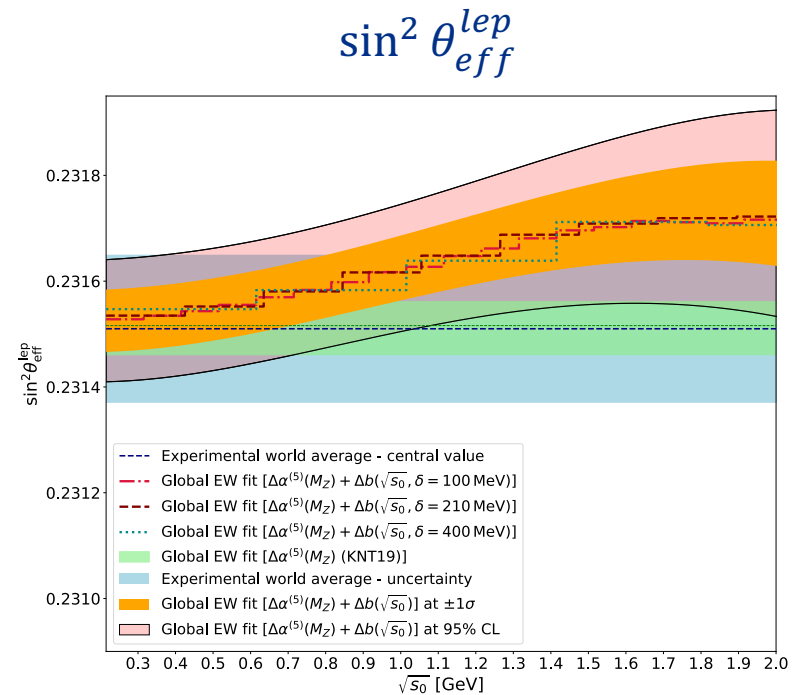
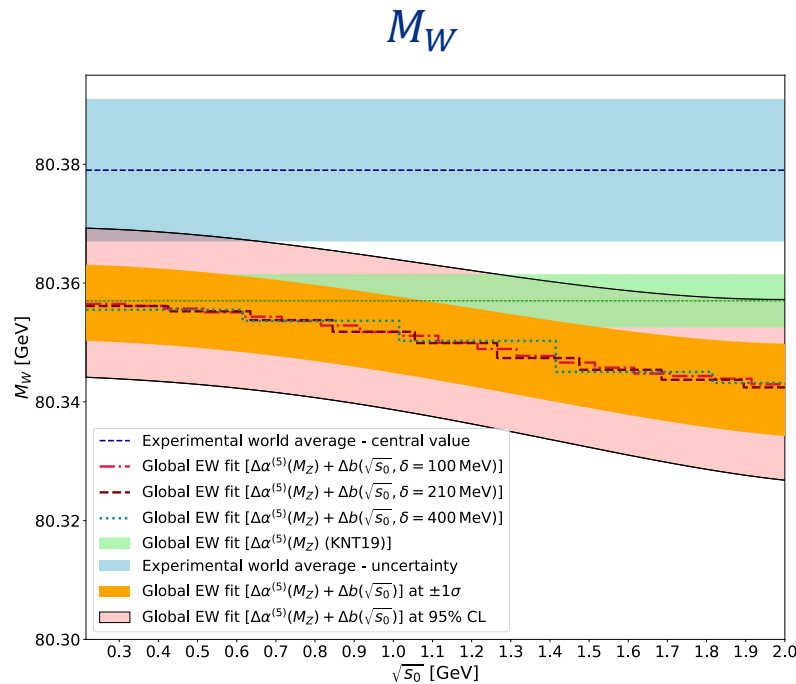


Marciano, MP, Sirlin, PRD 2008

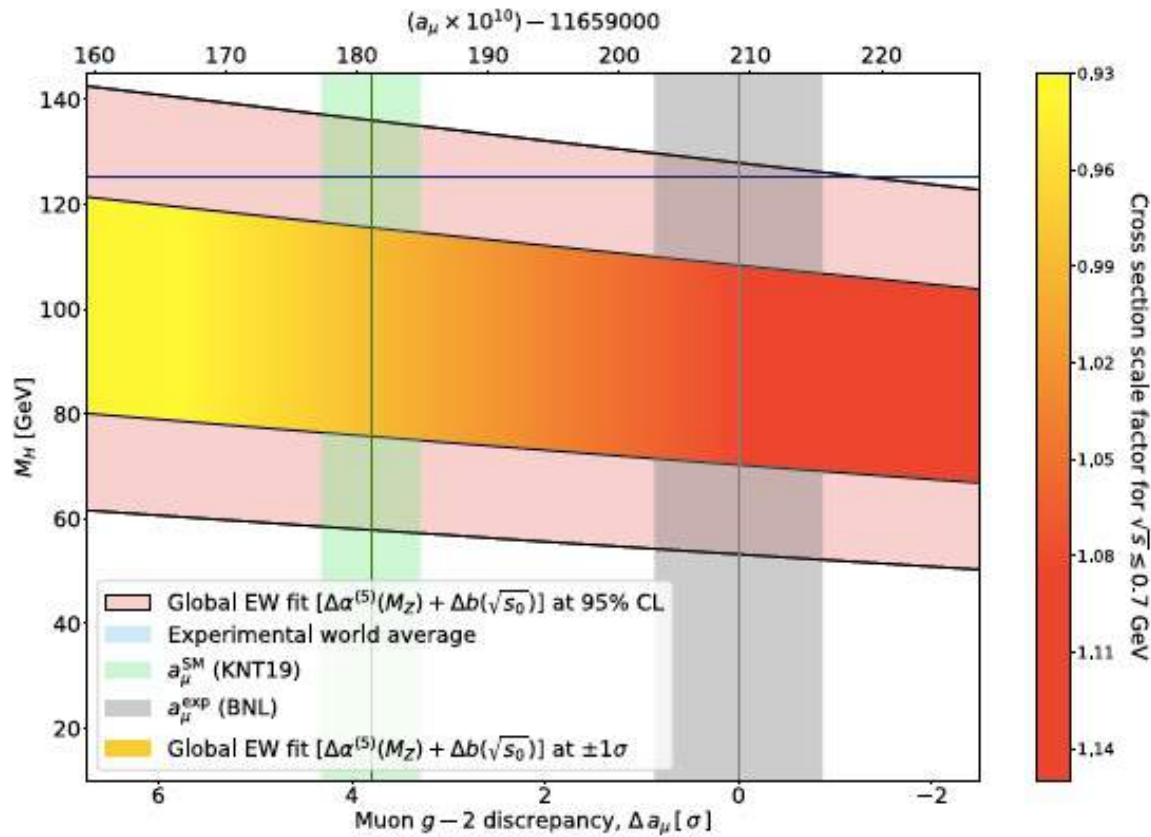
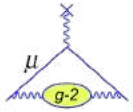
# Muon g-2: connection with EW sector



- Shift KNT hadronic cross section in fully energy-dependent (point-like and binned) analysis to account for  $\Delta\alpha_\mu$ .
- Input new values of  $\Delta\alpha$  into Gfitter to predict EW observables.
- Analysis greatly constrained from precise EW observables measurements and comprehensive hadronic cross section data.



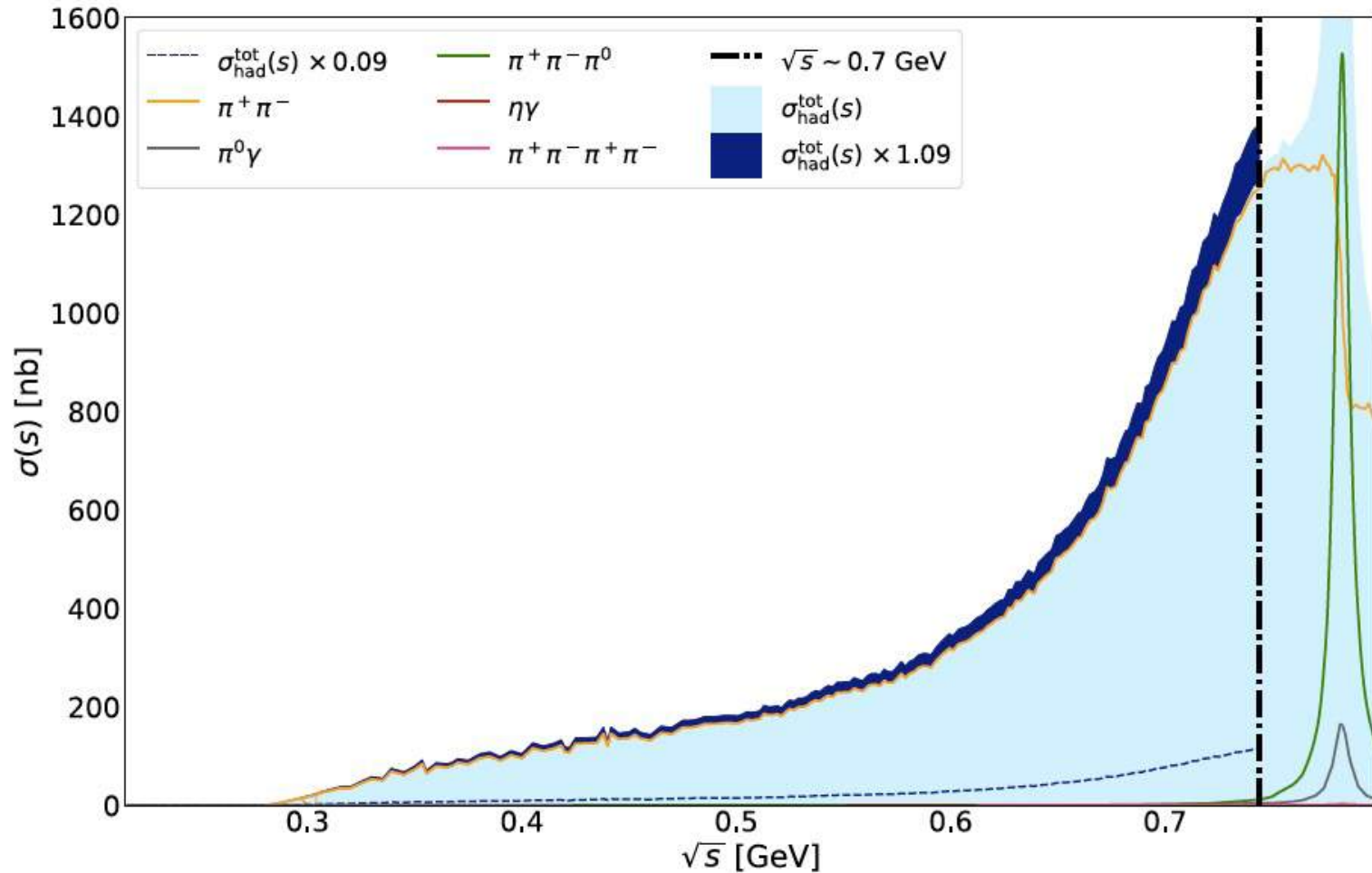
# Muon g-2: connection with SM Higgs



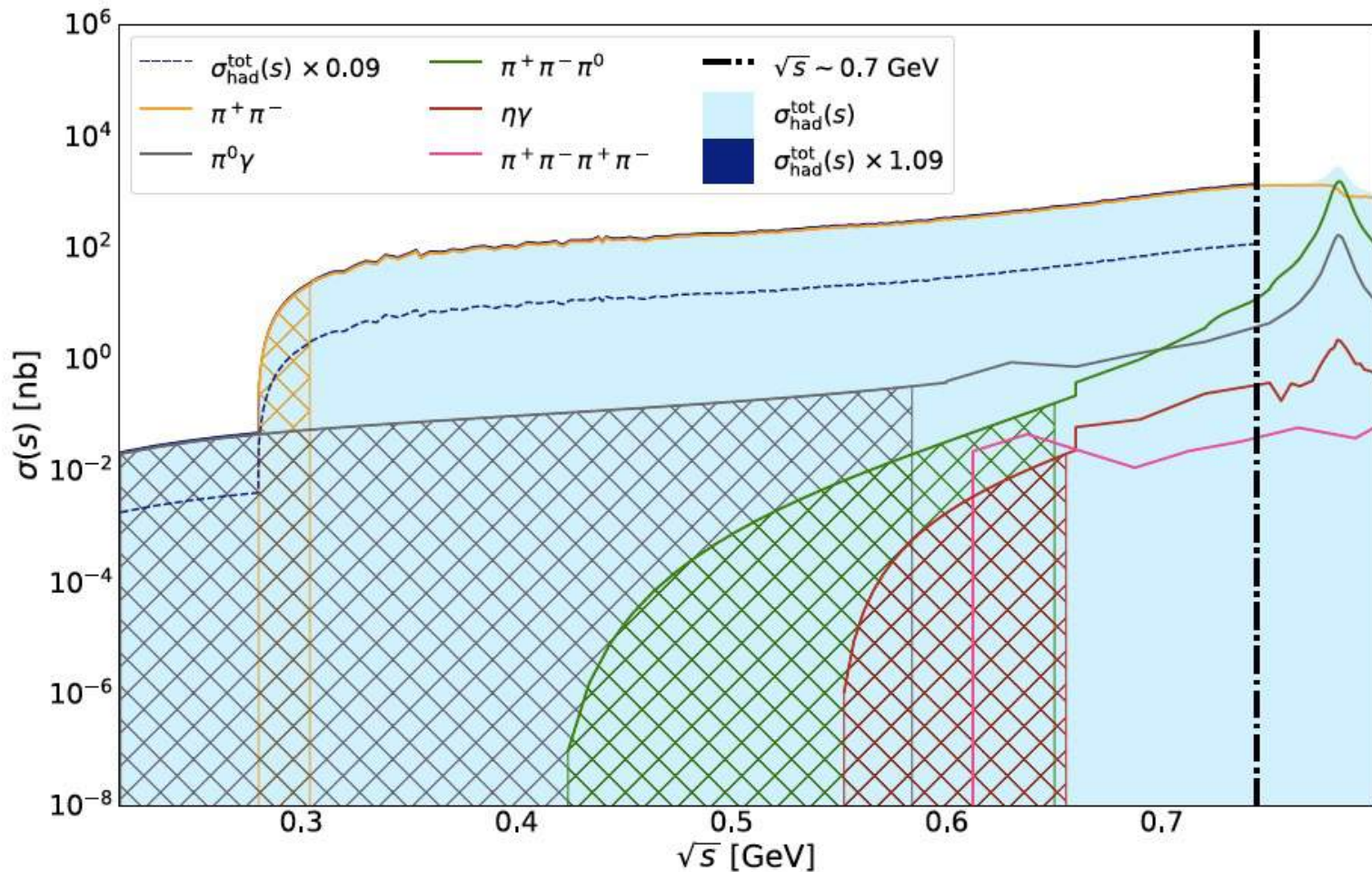
Uniform scaling of  $\sigma(s)$  below  $\sim 0.7$  GeV? +9% required!

Keshavarzi, Marciano, MP, Sirlin, PRD 2020



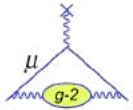


Keshavarzi, Marciano, MP, Sirlin, PRD 2020



Keshavarzi, Marciano, MP, Sirlin, PRD 2020

# Electron g-2



- The 2008 measurement of the electron g-2 is:

$$a_e^{\text{EXP}} = 11596521807.3 (2.8) \times 10^{-13} \quad \text{Hanneke et al, PRL100 (2008) 120801}$$

vs. old (factor of 15 improvement,  $1.8\sigma$  difference):

$$a_e^{\text{EXP}} = 11596521883 (42) \times 10^{-13} \quad \text{Van Dyck et al, PRL59 (1987) 26}$$

- Equate  $a_e^{\text{SM}}(\alpha) = a_e^{\text{EXP}}$  → “g<sub>e</sub>-2” determination of alpha:

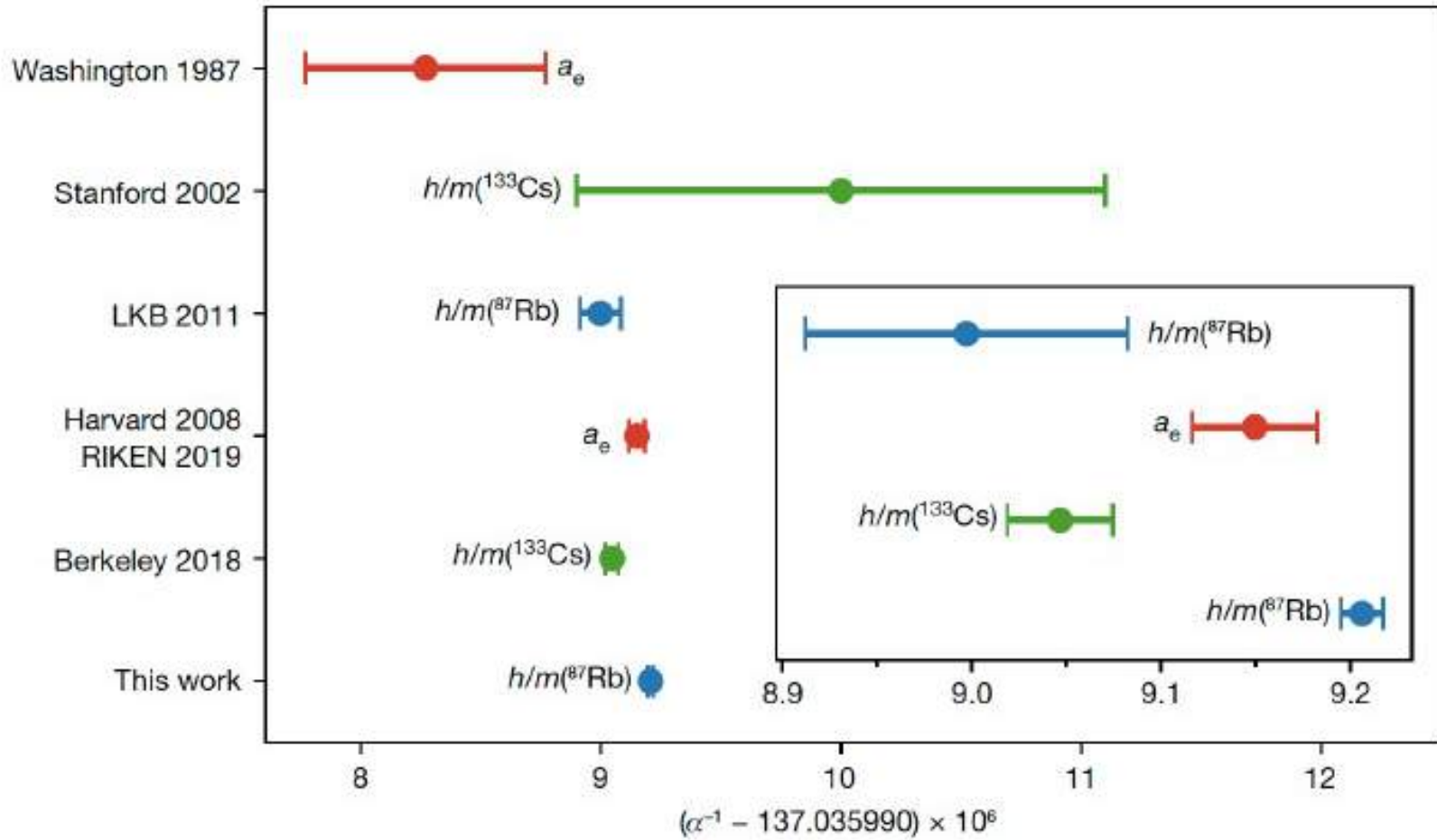
$$\alpha^{-1} = 137.035\,999\,151 (33) \quad [0.24 \text{ ppb}]$$

- The best determination of  $\alpha$  is obtained via atomic interferometry:

$$\alpha^{-1} = 137.035\,999\,046 (27) [0.20 \text{ ppb}] \quad \text{Parker et al, Science 360 (2018) 192 (Cs)}$$

$$\alpha^{-1} = 137.035\,999\,206 (11) [0.08 \text{ ppb}] \quad \text{Morel et al, Nature 588 (2020) 61 (Rb)}$$

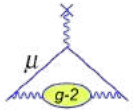
2018 → 2020: improvement in precision, but  $5.4\sigma$  difference!



Morel et al, Nature 588 (2020) 61



# Electron g-2



- Using the best determinations of  $\alpha$  (which differ by  $5.4\sigma$ ):

$$\alpha = 1/137.035\,999\,046\,(27) \text{ [Cs 2018]}$$

$$\alpha = 1/137.035\,999\,206\,(11) \text{ [Rb 2020]}$$

$$a_e^{\text{SM}} = 115\,965\,218\,16.16\,(0.11)\,(0.08)\,(2.28) \times 10^{-13} \text{ [Cs18]}$$
$$= 115\,965\,218\,02.64\,(0.11)\,(0.08)\,(0.93) \times 10^{-13} \text{ [Rb20]}$$

$\delta C_5^{\text{qed}}$     $\delta a_e^{\text{had}}$    from  $\delta\alpha$

$$a_e^{\text{EXP}} = 115\,965\,218\,07.3\,(2.8) \times 10^{-13} \text{ Hanneke et al, PRL 2008}$$

- The (EXP – SM) difference is:

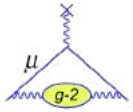
$$\Delta a_e = a_e^{\text{EXP}} - a_e^{\text{SM}} = -8.9\,(3.6) \times 10^{-13} \text{ [2.5}\sigma\text{] [Cs18]}$$
$$= +4.7\,(3.0) \times 10^{-13} \text{ [1.6}\sigma\text{] [Rb20]}$$

QED 5-loop:  $a_e^{\text{QED5}} = 4.6 \times 10^{-13}$

- NP sensitivity limited only by the experimental errors in  $\alpha$  and  $a_e$ .  
May soon play a pivotal role in probing NP in the leptonic sector.



# Electron g-2: new physics



- Using  $\alpha(\text{Rb2020})$ , the sensitivity is  $\delta\Delta a_e = 3.0 \times 10^{-13}$ , ie ( $\times 10^{-13}$ ):

$$\underbrace{(0.1)_{\text{QED5}}, (0.1)_{\text{HAD}}, (0.9)_{\delta\alpha}}_{(0.2)_{\text{TH}}}, (2.8)_{\delta a_e^{\text{EXP}}}$$

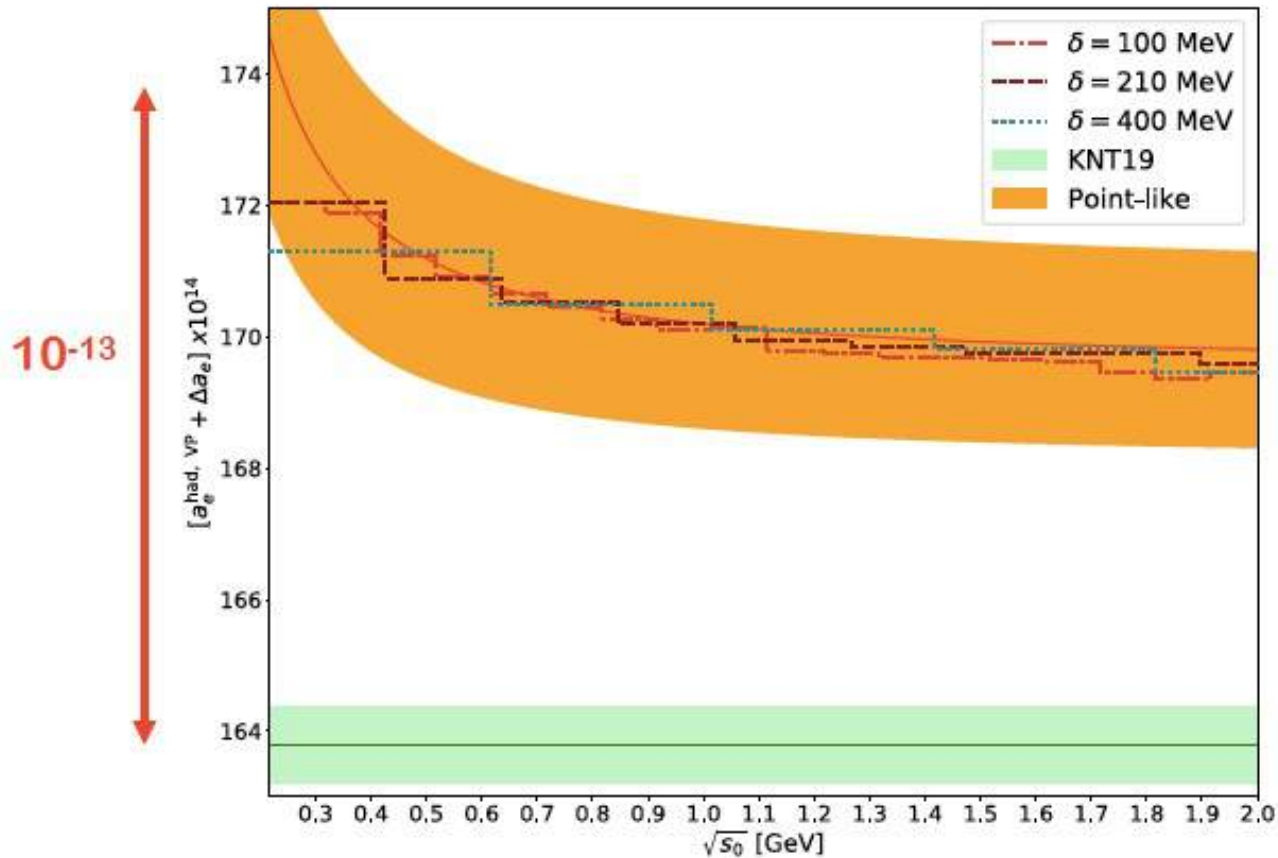
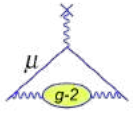
- The  $(g-2)_e$  experimental error may soon drop below  $10^{-13} \rightarrow$   
 **$a_e$  sensitivity below  $10^{-13}$  may soon be reached!**
- In a broad class of BSM theories, contributions to  $a_l$  scale as

$$\frac{\Delta a_{\ell_i}}{\Delta a_{\ell_j}} = \left( \frac{m_{\ell_i}}{m_{\ell_j}} \right)^2 \quad \text{This Naive Scaling leads to:}$$

$$\Delta a_e = \left( \frac{\Delta a_\mu}{3 \times 10^{-9}} \right) 0.7 \times 10^{-13}; \quad \Delta a_\tau = \left( \frac{\Delta a_\mu}{3 \times 10^{-9}} \right) 0.8 \times 10^{-6}$$

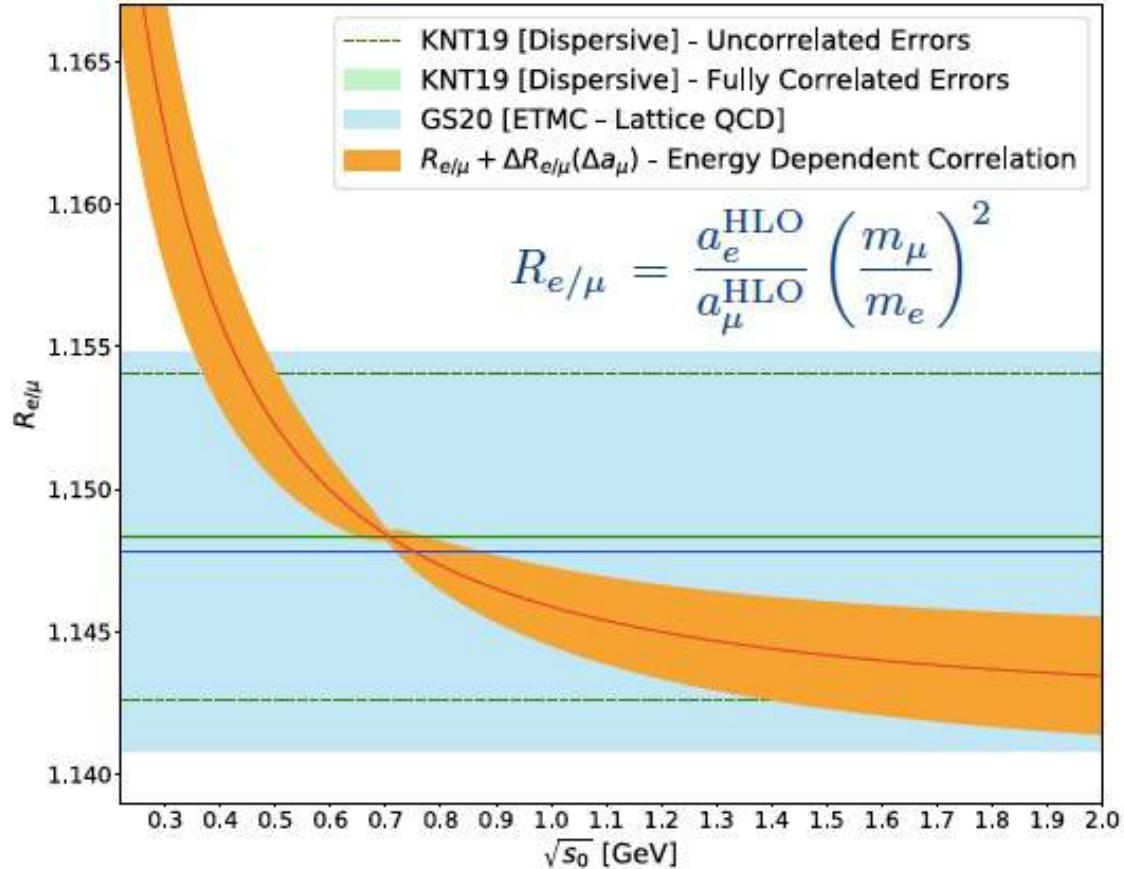
Giudice, Paradisi & MP, JHEP 2012

# Shift of electron $g-2$



Shifts  $\Delta\sigma(s)$  to fix  $\Delta a_\mu$  only slightly change  $\Delta a_e$

Keshavarzi, Marciano, MP, Sirlin, PRD 2020



Good agreement between lattice [Giusti & Simula 2020] and KNT19.  
Possible future bounds on very low energy shifts  $\Delta\sigma(s)$ ?

Keshavarzi, Marciano, MP, Sirlin, PRD 2020