

Search for tau LFV/LNV decays at Belle

Tau2021 (ONLINE)

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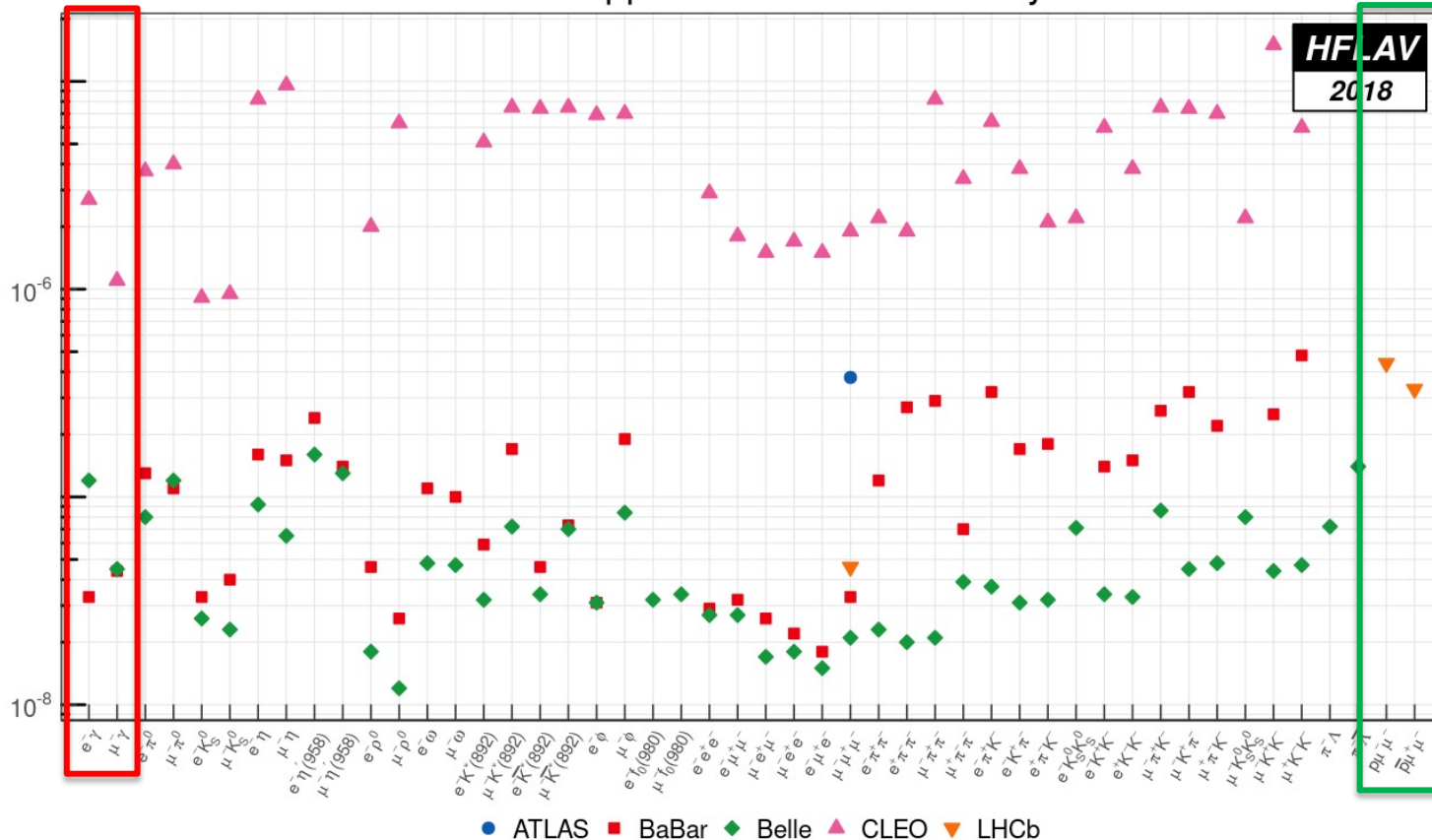
Introduction

- Two results using tau decays at Belle

- Tau LFV: $\tau \rightarrow \ell \gamma$ ($\ell = e, \mu$)
[K.Uno et al. arXiv:2103.12994](#)
accepted by JHEP
- Tau LNV/BNV: $\tau \rightarrow p \ell \ell'$ ($\ell^{(\prime)} = e, \mu$)
[D.Sahoo et al. PhysRevD.102.111101](#)

[HFLAV Summary Plot](#)

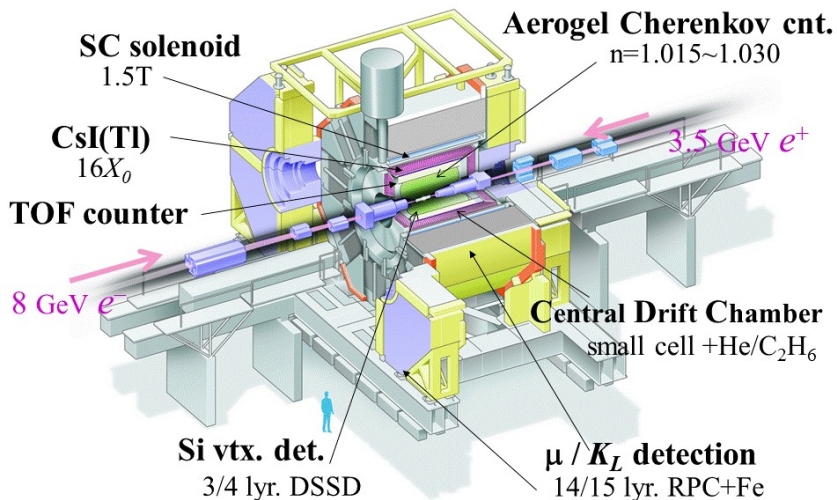
90% CL upper limits on τ LFV decays



Belle experiment

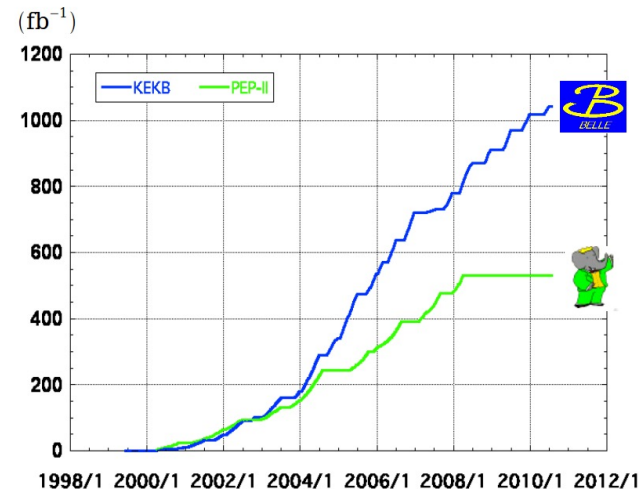
- Operation: 1999 - 2010
 - Collision: 8 GeV e^- , 3.5 GeV e^+
 - $\sigma(ee \rightarrow bb) \sim 1.1 \text{ nb}$, $\sigma(ee \rightarrow \tau\tau) \sim 0.9 \text{ nb} \rightarrow \tau \text{ factory!}$
 - Possible to use all $\Upsilon(nS)$ resonance data ($n = 1..5$)
 - Possible to use off resonance data ($\sim 100 \text{ fb}^{-1}$)
- \rightarrow In total, $9.1 \times 10^8 N_{\tau\tau}$ (Ref. BaBar: $4.8 \times 10^8 N_{\tau\tau}$)**

Belle Detector



Integrated luminosity of B factories

[Link](#)



> 1 ab^{-1}
On resonance:
 $\Upsilon(5S)$: 121 fb^{-1}
 $\Upsilon(4S)$: 711 fb^{-1}
 $\Upsilon(3S)$: 3 fb^{-1}
 $\Upsilon(2S)$: 25 fb^{-1}
 $\Upsilon(1S)$: 6 fb^{-1}
Off reson./scan:
 $\sim 100 \text{ fb}^{-1}$

$\sim 550 \text{ fb}^{-1}$
On resonance:
 $\Upsilon(4S)$: 433 fb^{-1}
 $\Upsilon(3S)$: 30 fb^{-1}
 $\Upsilon(2S)$: 14 fb^{-1}
Off resonance:
 $\sim 54 \text{ fb}^{-1}$

Search for tau LFV decays

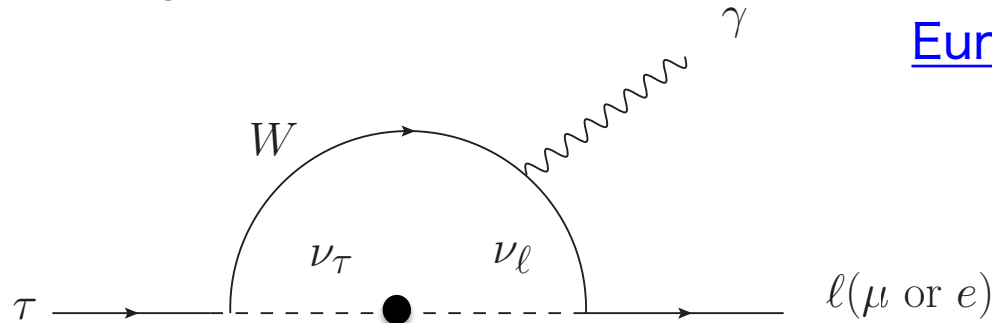
$$\tau \rightarrow \ell \gamma$$

Motivation: $\tau \rightarrow \ell\gamma$ ($\ell = e, \mu$)

Charged Lepton Flavor Violation (CLFV)

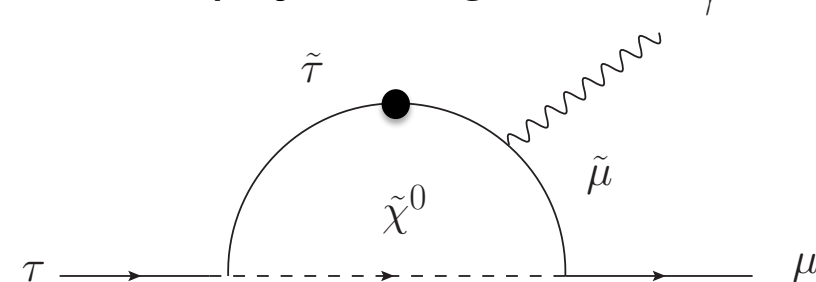
- Small probability via neutrino oscillations: $B(\tau \rightarrow \mu\gamma) < O(10^{-40})$

[Eur.Phys.J.C8,3\(1999\)](#)



- $\tau \rightarrow \ell\gamma$: Sizeable probability in several models

New physics (eg. SUSY)



Model	Reference
SM + ν Oscillations	EPJ C8 (1999) 513
SM + heavy Maj ν_R	PRD 66 (2002) 034008
Non universal Z'	PLB 547 (2002) 252
SUSY SO(10)	PRD 68 (2003) 033012
mSUGRA + seesaw	PRD 66 (2002) 115013
SUSY Higgs	PLB 566 (2003) 217

Observation of CLFV \rightarrow clear signature of new physics

$\tau \rightarrow \ell\gamma$: Sensitive to several models!

Past searches for $\tau \rightarrow \ell\gamma$

90%CL	Belle	BaBar
Luminosity	535 fb ⁻¹	516 fb ⁻¹
$N_{\tau\tau}$	4.8×10^8	4.8×10^8
$B(\tau \rightarrow \mu\gamma)$	4.5×10^{-8}	4.4×10^{-8}
$B(\tau \rightarrow e\gamma)$	12×10^{-8}	3.3×10^{-8}
Reference	PLB (2008)666	PRL (2010)021802

We updated the results of a search for $\tau \rightarrow \ell\gamma$

- Increased $N_{\tau\tau}$: $4.8 \times 10^8 \rightarrow 9.1 \times 10^8$ ($535 \text{ fb}^{-1} \rightarrow 988 \text{ fb}^{-1}$)
- Introduced new observables and improved selection
- Calibrated photon energy resolution using $ee \rightarrow \mu\mu\gamma$

Photon energy resolution calibration

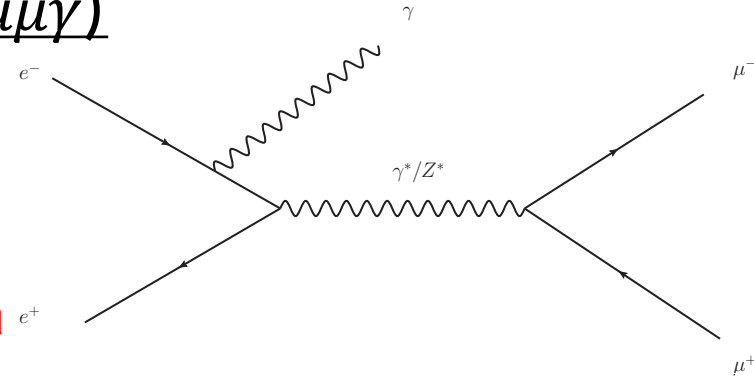
Revised the photon-energy resolution calibration

- Use radiative muon event ($ee \rightarrow \mu\mu\gamma$)

- Cover a broad energy range

Goal

- Measure the energy resolution in data
- Calibrate it in simulation to agree with that in data



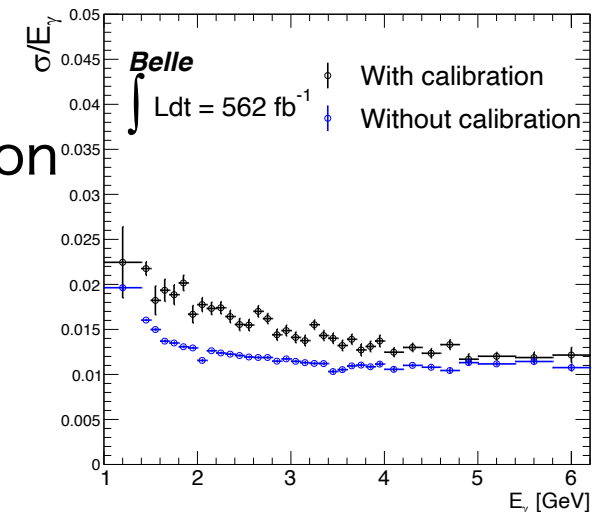
Evaluation

- Subtract E_{recoil} from E_γ for data and simulation

- $E_{\text{recoil}} = E_{\text{beam}} - E_{\mu^-} - E_{\mu^+}$
- E_γ : measured in the calorimeter

Energy range: 1 GeV – 6 GeV **NEW!**

- Calibrated resolution agrees with that in data



Analysis approach

Signal-side: $N_\ell = 1$ and $N_\gamma = 1$

Tag-side: 1 prong τ (Eg. $\ell\nu\nu, \pi\nu, \rho\nu$)

Signal region definition

- $M_{bc} = \sqrt{(E_{\text{beam}}^{\text{CM}})^2 - (p_{\ell\gamma}^{\text{CM}})^2}$ $E_{\text{beam}}^{\text{CM}} \sim \frac{\sqrt{s}}{2}$
- $\Delta E / \sqrt{s} = (E_{\ell\gamma}^{\text{CM}} - E_{\text{beam}}^{\text{CM}}) / \sqrt{s}$

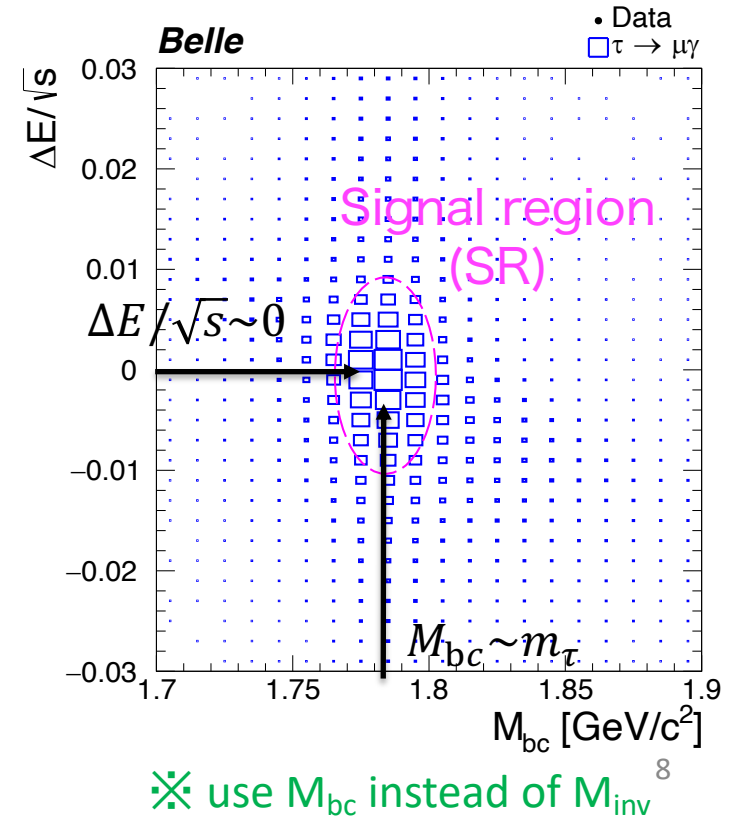
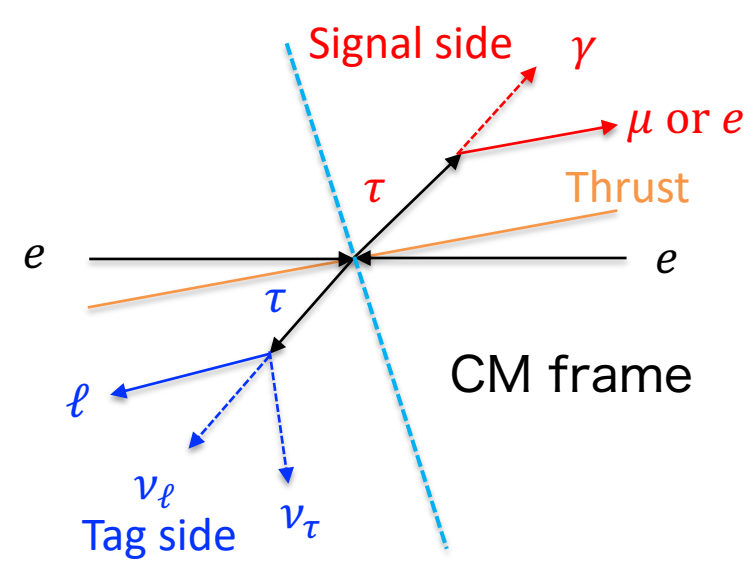
Background component

- $\tau \rightarrow \ell\nu\nu + \text{ISR } \gamma$ or beam bkg
- $ee \rightarrow \mu\mu/ee + \text{ISR } \gamma$ or beam bkg

Signal extraction

- Perform UEML fit to the SR

Unbinned Extended Maximum Likelihood

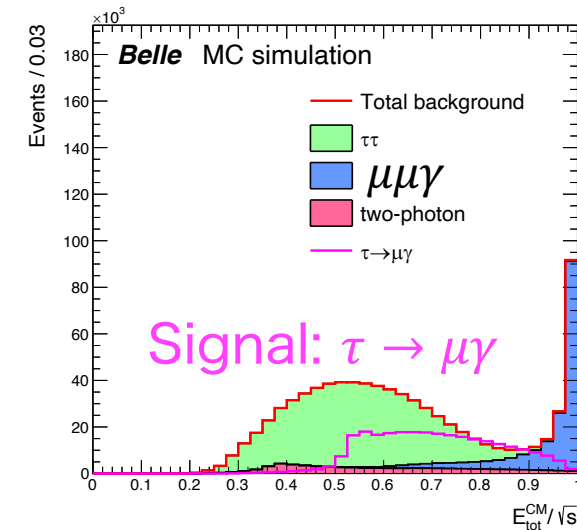
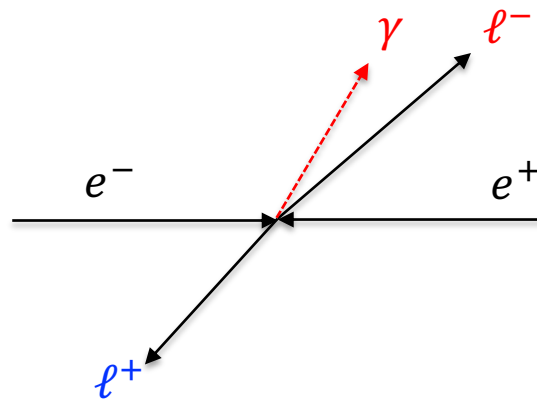
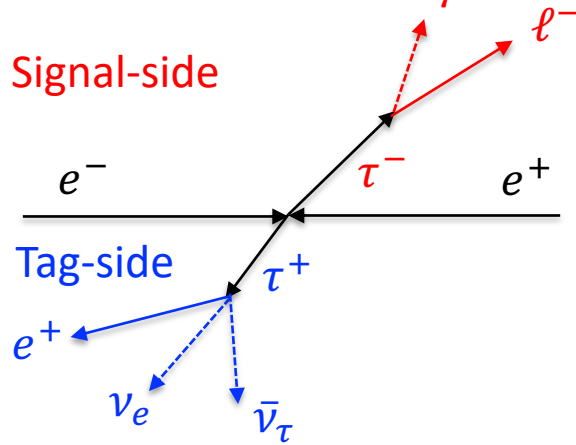


Event Selection 1

Several observables are used: eg. Total energy, missing angle

Signal: $\tau \rightarrow \ell\gamma$

Background: $ee \rightarrow \ell\ell\gamma$



Eg. Total energy in CM frame ($E_{\text{tot}}^{\text{CM}}/\sqrt{s}$)

- $\tau \rightarrow \ell\gamma$: $N_\nu > 0$ in tag-side, $ee \rightarrow \ell\ell\gamma$: $N_\nu = 0$

→ Signal distribution depends on tag-side decays ($\tau \rightarrow \ell\nu\nu, \pi\nu, \rho\nu$)

NEW!

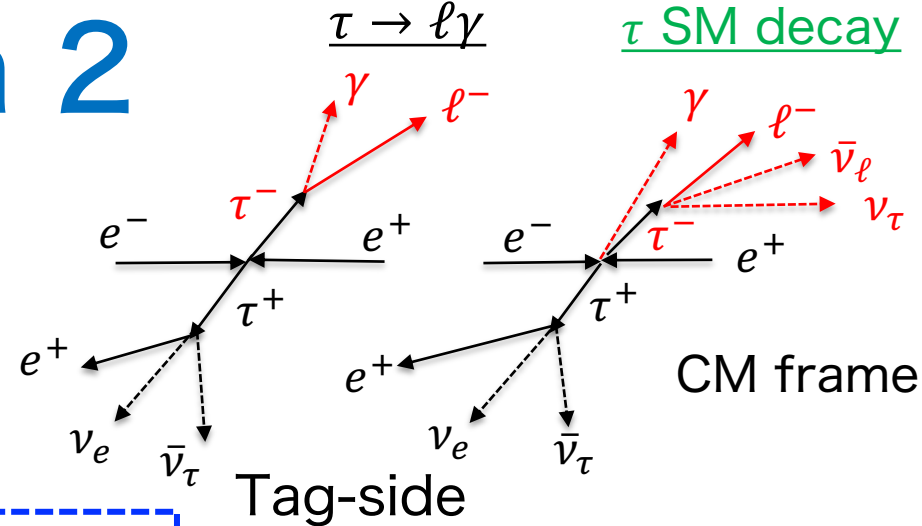
Optimized selection per channel: ℓ, π, ρ channel

※ All selection criteria are optimized to maximize search sensitivity

Event Selection 2

New observable

$$\xi_{\tau(\text{tag}),\text{track}(\text{tag})}^{\text{CM}} = \frac{(p_{\tau(\text{tag})}^{\text{CM}} \cdot p_{\text{track}(\text{tag})}^{\text{CM}})}{|p_{\tau(\text{tag})}^{\text{CM}}| |p_{\text{track}(\text{tag})}^{\text{CM}}|}$$



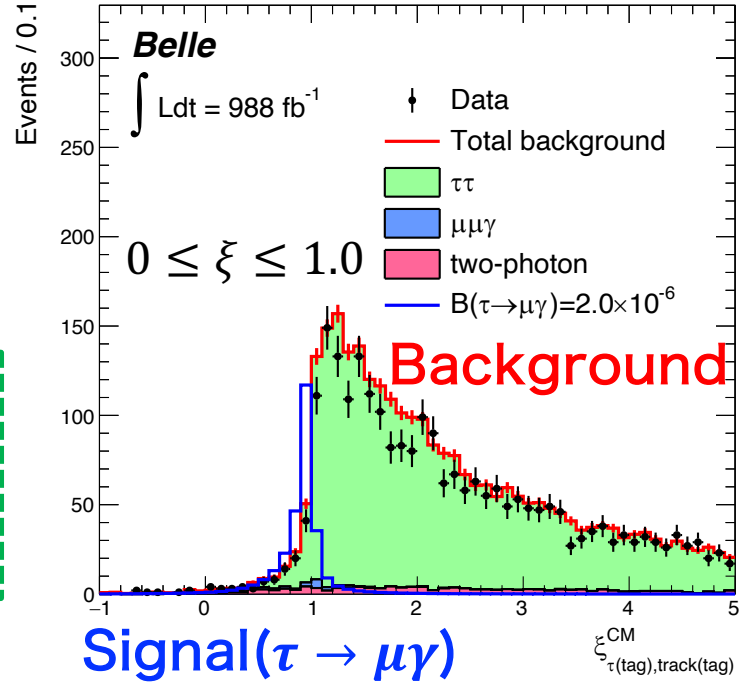
Ideal signal events,

$$p_{\tau(\text{tag})}^{\text{CM}} = -p_{\tau(\text{sig})}^{\text{CM}} = -(p_{\ell}^{\text{CM}} + p_{\gamma}^{\text{CM}})$$

$$\rightarrow \xi_{\tau(\text{tag}),\text{track}(\text{tag})}^{\text{CM}} = \cos \theta_{\tau(\text{tag}),\text{track}(\text{tag})}$$

$$\tau \text{ SM decay: } p_{\tau(\text{sig})}^{\text{CM}} \neq p_{\ell}^{\text{CM}} + p_{\gamma}^{\text{CM}}$$

$$\rightarrow \xi_{\tau(\text{tag}),\text{track}(\text{tag})}^{\text{CM}} \neq \cos \theta_{\tau(\text{tag}),\text{track}(\text{tag})}$$



NEW!

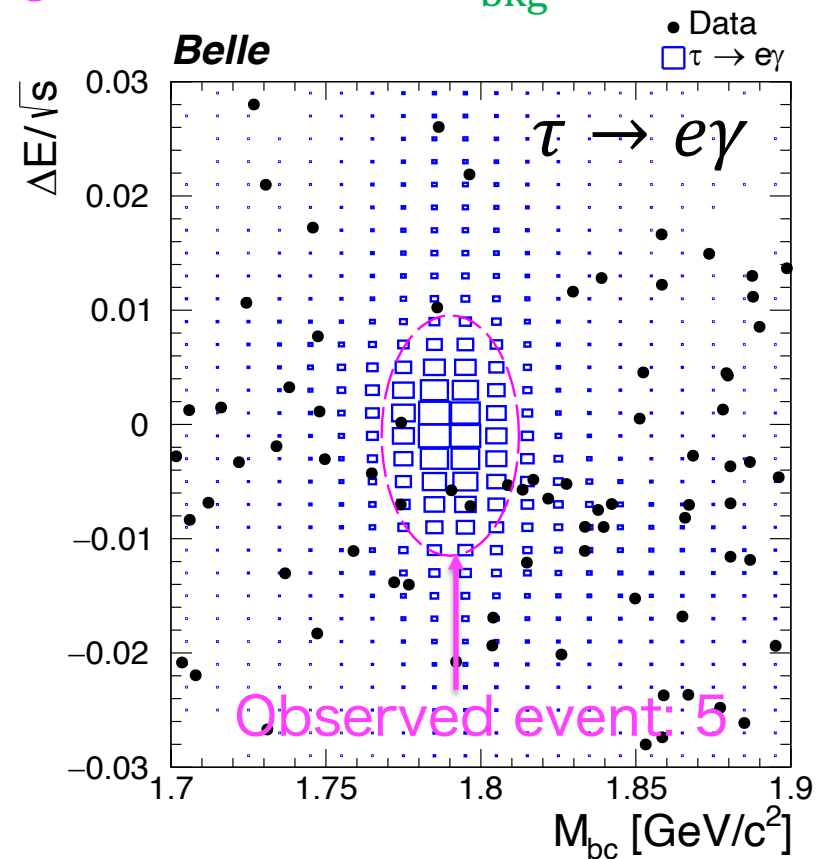
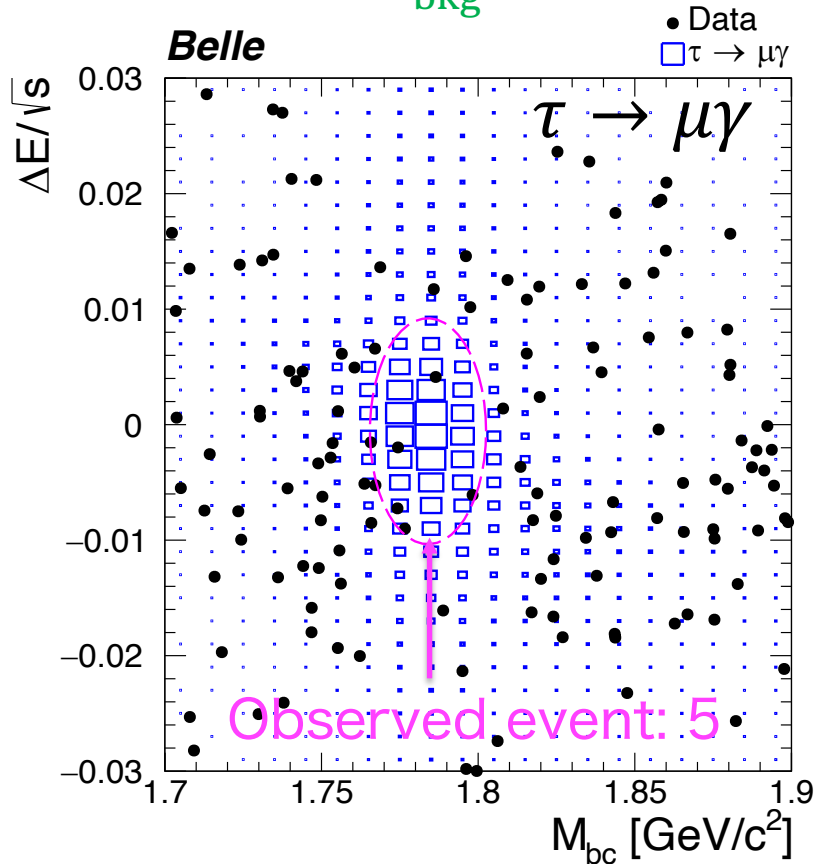
Good separation between signal and background 10

Result

Luminosity: $988 \text{ fb}^{-1} : 9.1 \times 10^8 N_{\tau\tau}$

Signal eff. = 3.7% $N_{\text{bkg}}^{\text{exp}} = 5.8 \pm 0.4$

Signal eff. = 2.9% $N_{\text{bkg}}^{\text{exp}} = 5.1 \pm 0.4$



Unbinned Extended ML fit result

$$s = -0.3_{-1.3}^{+1.8}, b = 5.3_{-2.3}^{+3.2}$$

$$s = -0.5_{-3.6}^{+4.4}, b = 5.5_{-4.1}^{+5.2}$$

No significant excess over SM background predictions

Upper limits at 90% CL

Upper limit on branching fraction at 90% CL

$$\mathcal{B}(\tau^\pm \rightarrow \mu^\pm \gamma) < \frac{\tilde{s}_{90}}{2\epsilon N_{\tau\tau}} = 4.2 \times 10^{-8},$$

$$\mathcal{B}(\tau^\pm \rightarrow e^\pm \gamma) < \frac{\tilde{s}_{90}}{2\epsilon N_{\tau\tau}} = 5.6 \times 10^{-8},$$

$B \times 10^{-8}$ at 90% CL	BaBar $N_{\tau\tau} = 4.8 \times 10^8$		Belle $N_{\tau\tau} = 4.8 \times 10^8$		Belle $N_{\tau\tau} = 9.1 \times 10^8$	
	Exp	Obs	Exp	Obs	Exp	Obs
$B(\tau \rightarrow \mu\gamma)$	8.2	4.4	8.0	4.5	4.9	4.2
$B(\tau \rightarrow e\gamma)$	9.8	3.3	12	12	6.5	5.6

- Expected limits: **factor 1.5 – 1.7 improved**
- Observed limits, $\tau \rightarrow \mu\gamma$: **Most stringent limit to the date**

Search for tau LNV/BNV
decays $\tau \rightarrow p \ell \ell'$

Motivation

Matter-antimatter asymmetry in nature

- Need Baryon number violation (BNV) Sakharov's condition
- BNV in charged lepton decays \rightarrow lepton number violation (LNV)

Past search in BNV/LNV

Belle: $\mathcal{B}(\tau^- \rightarrow \Lambda \pi^-) < 0.72 \times 10^{-7}$

Phys.Lett.B 632, 51-57 (2006)

Belle: $\mathcal{B}(\tau^- \rightarrow \bar{\Lambda} \pi^-) < 1.4 \times 10^{-7}$

Phys.Lett.B 632, 51-57 (2006)

CLEO: $\mathcal{B}(\tau^- \rightarrow \bar{p} \gamma) < 3.5 \times 10^{-6}$

Phys. Rev. D 59, 091303(R) (1999)

CLEO: $\mathcal{B}(\tau^- \rightarrow \bar{p} \pi^0) < 1.5 \times 10^{-5}$

Phys. Rev. D 59, 091303(R) (1999)

CLEO: $\mathcal{B}(\tau^- \rightarrow \bar{p} 2\pi^0) < 3.3 \times 10^{-5}$

Phys. Rev. D 59, 091303(R) (1999)

CLEO: $\mathcal{B}(\tau^- \rightarrow \bar{p} \eta) < 8.9 \times 10^{-6}$

Phys. Rev. D 59, 091303(R) (1999)

CLEO: $\mathcal{B}(\tau^- \rightarrow \bar{p} \pi^0 \eta) < 2.7 \times 10^{-5}$

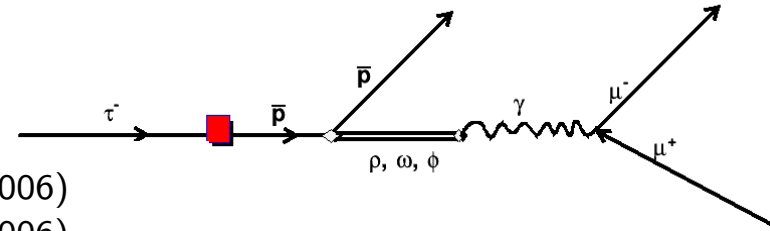
Phys. Rev. D 59, 091303(R) (1999)

LHCb: $\mathcal{B}(\tau^- \rightarrow p \mu^- \mu^-) < 4.4 \times 10^{-7}$

Phys. Lett. B 724 (2013)

LHCb: $\mathcal{B}(\tau^- \rightarrow \bar{p} \mu^+ \mu^-) < 3.3 \times 10^{-7}$

Phys. Lett. B 724 (2013)



We search for six decays $\tau^- \rightarrow \bar{p} e^+ e^-$, $p e^- e^-$, $\bar{p} e^+ \mu^-$, $\bar{p} e^- \mu^+$, $p \mu^- \mu^-$ and $\bar{p} \mu^+ \mu^-$ using 921 fb^{-1} at Belle

✧ This search uses $\Upsilon(4S)$, $\Upsilon(5S)$ and off-resonance data

Analysis approach

Signal-side: Reconstruct p, ℓ, ℓ'

Tag-side: 1 prong τ decays

Signal region (SR) definition

$$M_{\text{rec}} = \sqrt{(E_{p\ell\ell'})^2 - (\vec{p}_{p\ell\ell'})^2}$$

$$\Delta E = (E_{p\ell\ell'}^{\text{CM}} - E_{\text{beam}}^{\text{CM}})$$

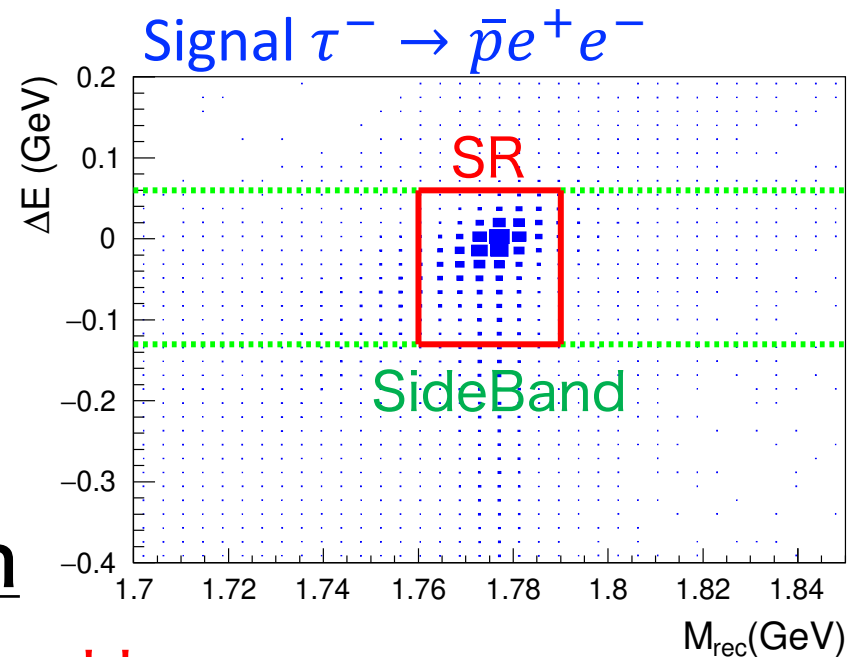
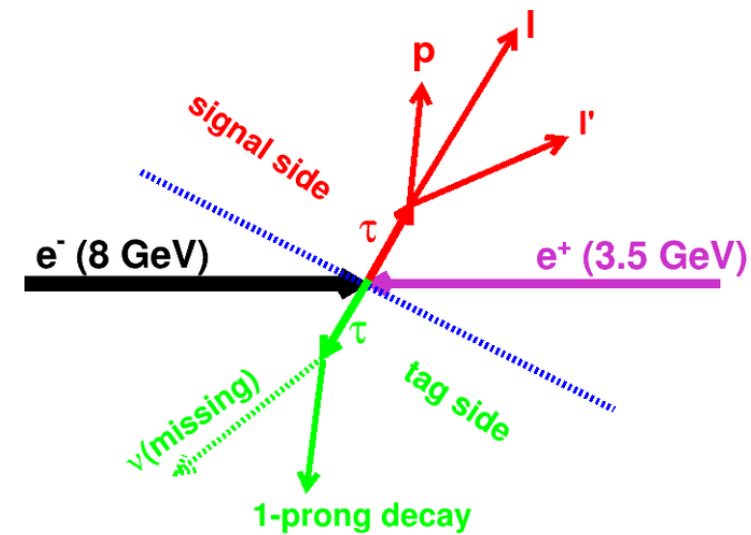
Background component

- $\tau\tau$ SM decay, $ee \rightarrow \ell\ell, ee \rightarrow e\ell\ell$

SideBand region definition

- $\Delta E - M_{\text{rec}}$ region outside **the red box**

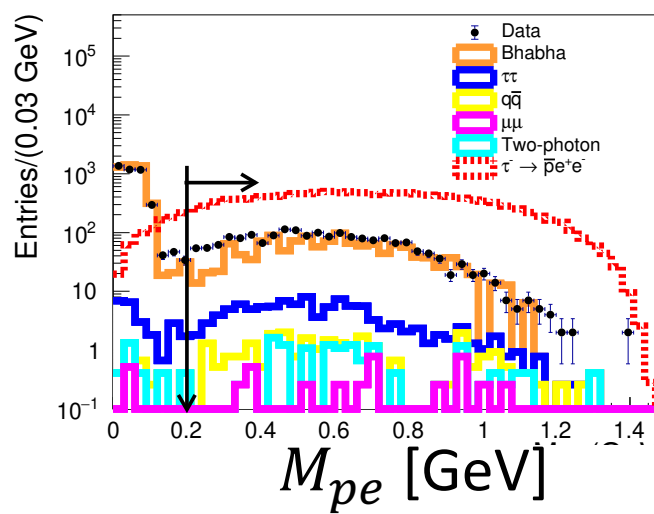
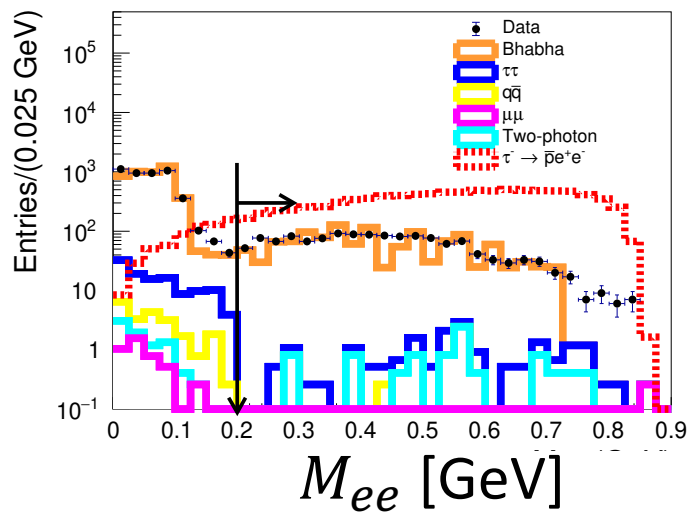
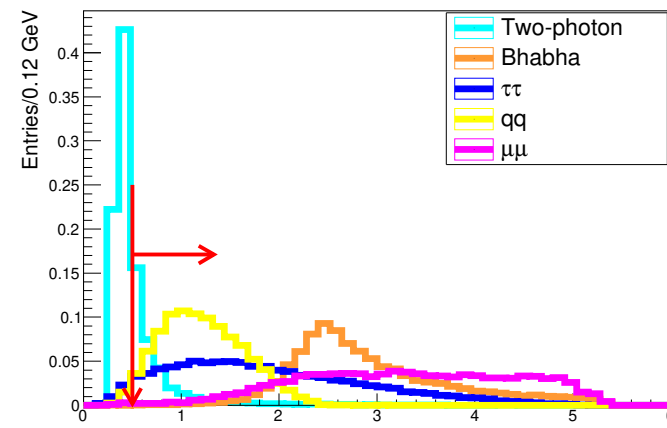
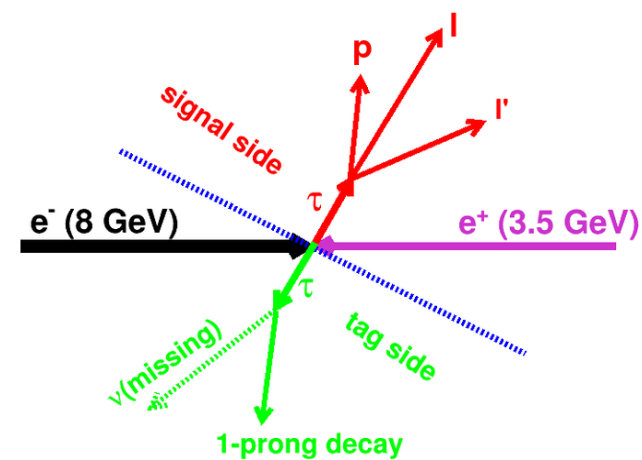
→ Used it to calculate expected N_{bkg} in the SR



Event Selection

Several observables are used

- Maximum p_T of charged tracks
- Event shape variable: Thrust
- $\cos\theta_{\text{tag,miss}}^{\text{CM}}$ and θ_{miss}
- γ conversion veto
 - Photon conversion in the detector material constitutes a major bkg for $\tau^- \rightarrow \bar{p}e^-e^+, pe^-e^-, \bar{p}e^+\mu^-, p\mu^-\mu^+$

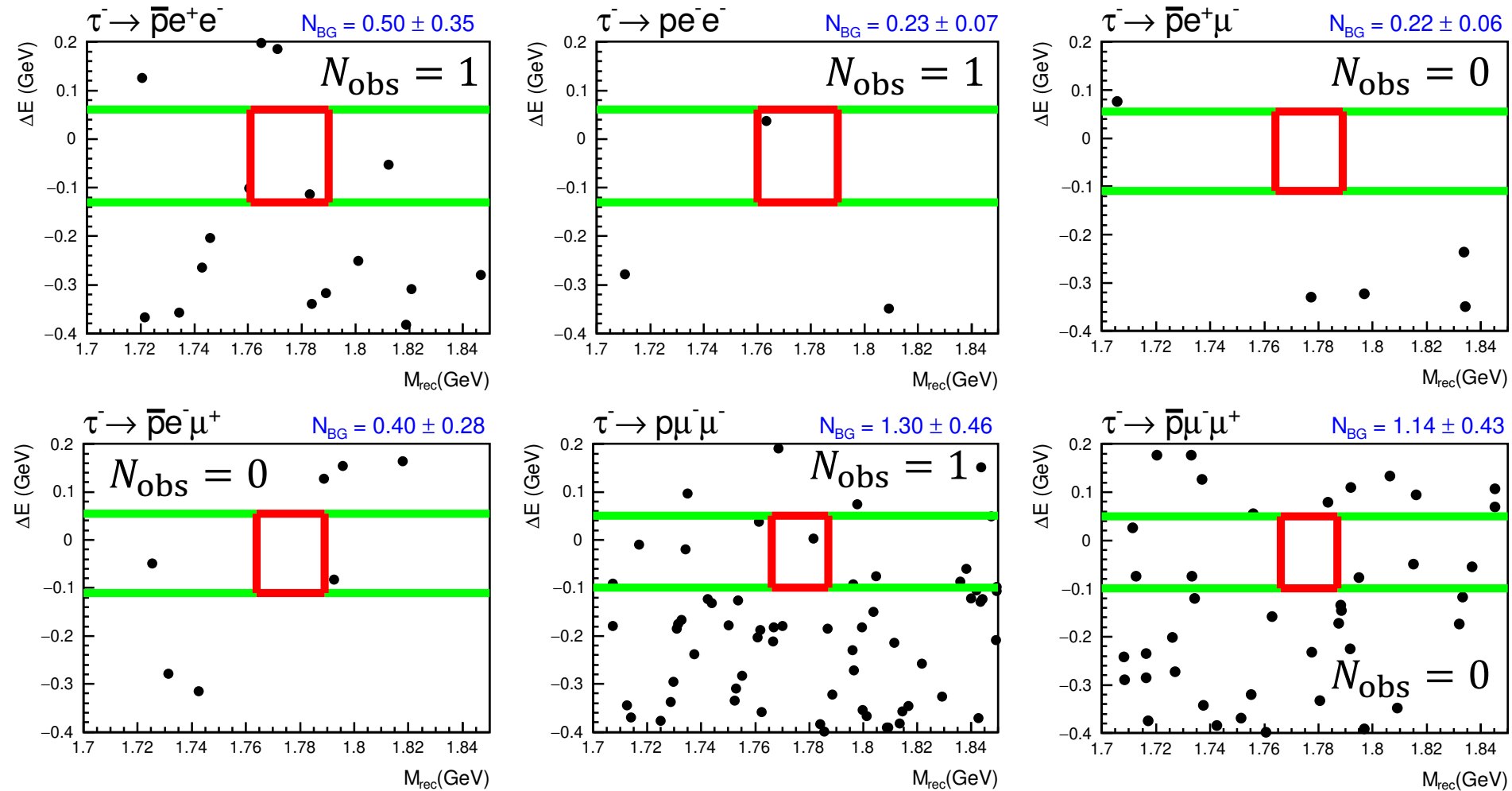


p_T^{max} [GeV]

Assume electron mass hypothesis

Result

Luminosity: 921 fb^{-1} ($8.4 \times 10^8 N_{\tau\tau}$)



No significant excess over SM background predictions

Upper limits

Upper limit on branching fraction at 90% CL

$$\mathcal{B}(\tau^- \rightarrow p\mu^- \mu^-) < \frac{N_{\text{sig}}^{\text{UL}}}{2N_{\tau\tau}\epsilon},$$

$$N_{\tau\tau} = 8.4 \times 10^8$$

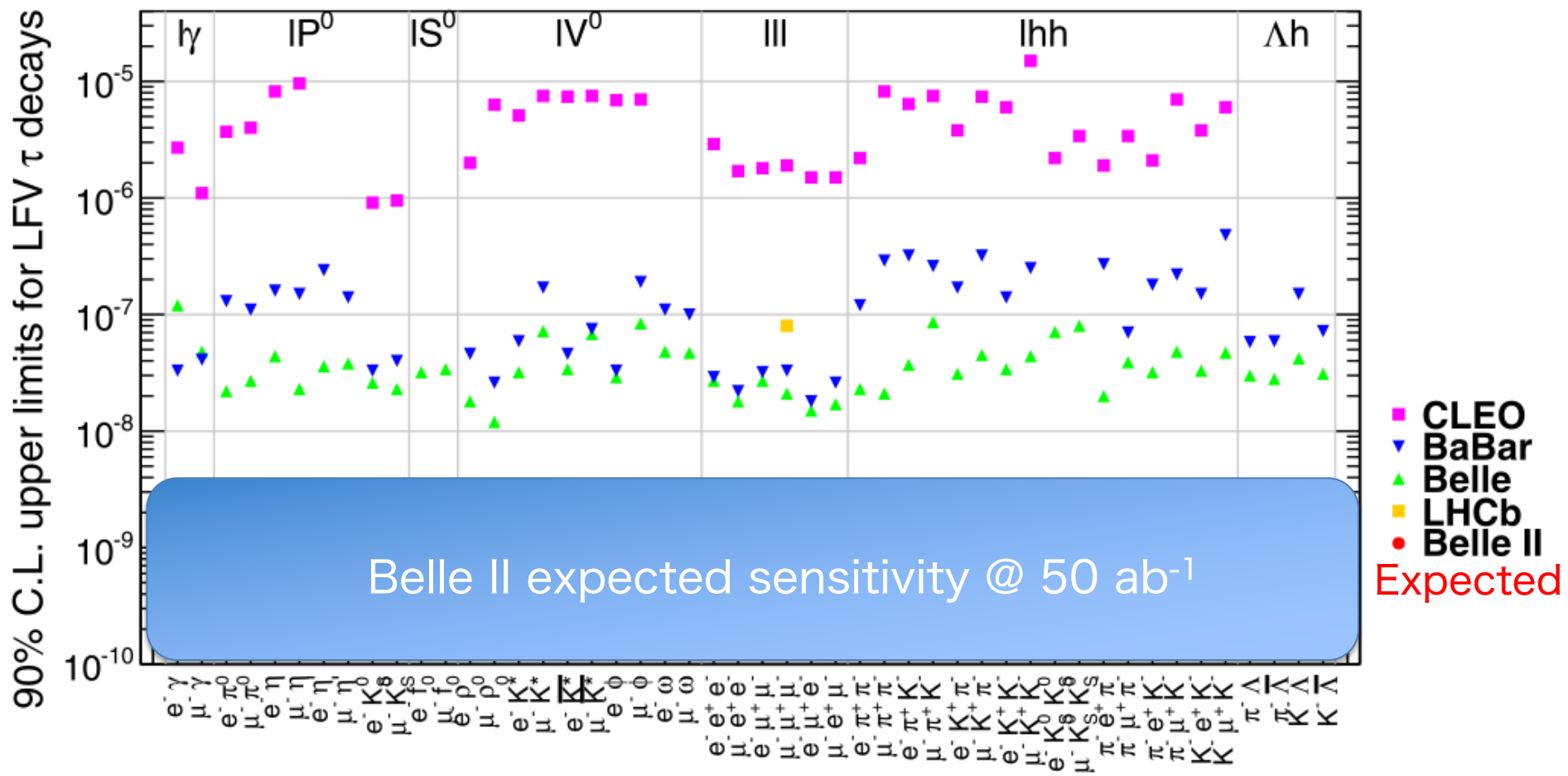
Channel	ϵ (%)	N_{bkg}	N_{obs}	$N_{\text{sig}}^{\text{UL}}$	$\mathcal{B} (\times 10^{-8})$
$\tau^- \rightarrow \bar{p}e^+ e^-$	7.8	0.50 ± 0.35	1	3.9	< 3.0
$\tau^- \rightarrow pe^- e^-$	8.0	0.23 ± 0.07	1	4.1	< 3.0
$\tau^- \rightarrow \bar{p}e^+ \mu^-$	6.5	0.22 ± 0.06	0	2.2	< 2.0
$\tau^- \rightarrow \bar{p}e^- \mu^+$	6.9	0.40 ± 0.28	0	2.1	< 1.8
$\tau^- \rightarrow p\mu^- \mu^-$	4.6	1.30 ± 0.46	1	3.1	< 4.0
$\tau^- \rightarrow \bar{p}\mu^- \mu^+$	5.0	1.14 ± 0.43	0	1.5	< 1.8

$$\text{LHCb: } \mathcal{B}(\tau^- \rightarrow p\mu^- \mu^-) < 4.4 \times 10^{-7}$$

$$\text{LHCb: } \mathcal{B}(\tau^- \rightarrow \bar{p}\mu^+ \mu^-) < 3.3 \times 10^{-7}$$

- $\tau^- \rightarrow p\mu^- \mu^-$, $\tau \rightarrow \bar{p}\mu^- \mu^+$: One order improve
- Other four channels: First measurement

Expected sensitivity at Belle II



Belle II data taking: 50 ab^{-1}

- Search sensitivity: $< 0(10^{-9}) \rightarrow$ Stay tuned!

Summary

Tau LFV: $\tau \rightarrow \ell\gamma$ ($\ell = e, \mu$)

- Use full data and improve analysis technique
- No significant excess over the predicted background

$$B(\tau \rightarrow \mu\gamma) < 4.2 \times 10^{-8} \quad \rightarrow \text{Most stringent limit}$$
$$B(\tau \rightarrow e\gamma) < 5.6 \times 10^{-8} \quad \text{at 90\% CL}$$

Tau BNV/LNV: $\tau \rightarrow p\ell\ell'$ ($\ell^{(\prime)} = e, \mu$)

- $B(\tau^- \rightarrow p\mu^- \mu^-) < 4.0 \times 10^{-8}, B(\tau^- \rightarrow \bar{p}\mu^- \mu^+) < 1.8 \times 10^{-8}$
- Upper limit at LHCb: $\sim 10^{-7}$ → One order improve
- $\tau^- \rightarrow \bar{p}e^+ e^-, pe^- e^-, \bar{p}e^+ \mu^-, \bar{p}e^- \mu^+$: **First measurement**

Backup

Previous analysis and Mbc

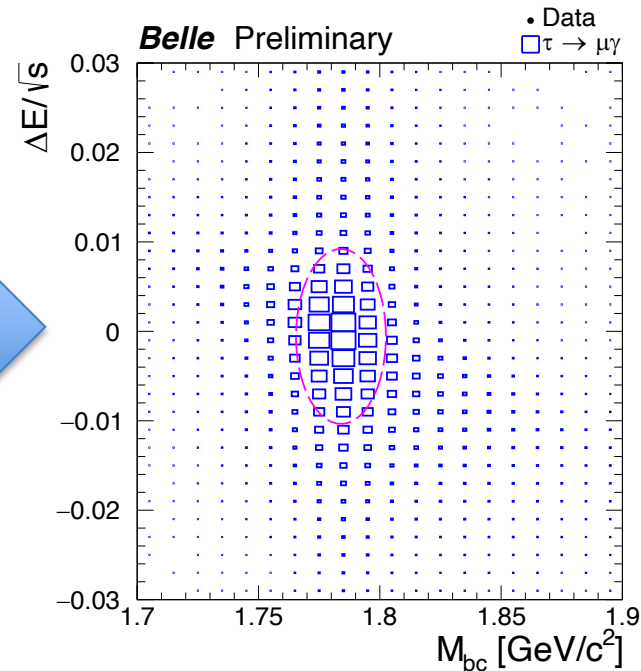
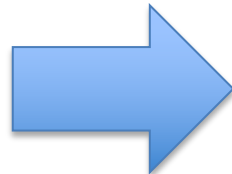
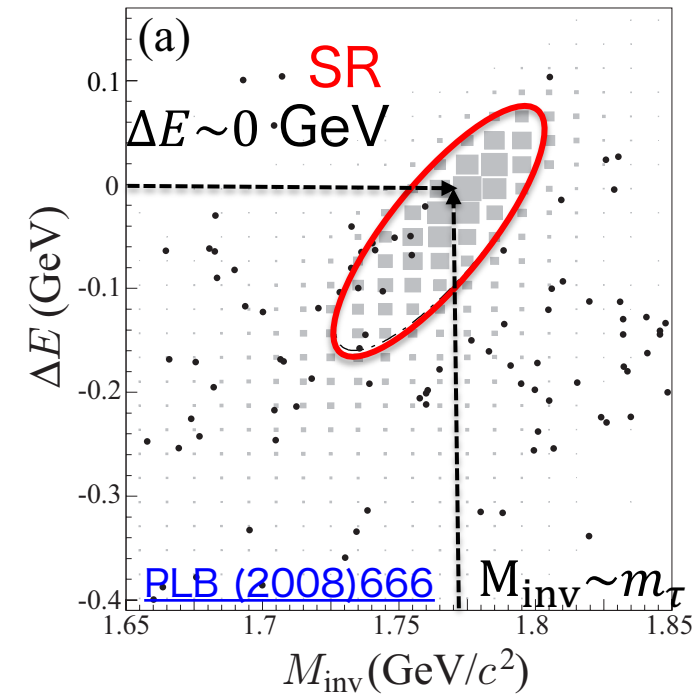
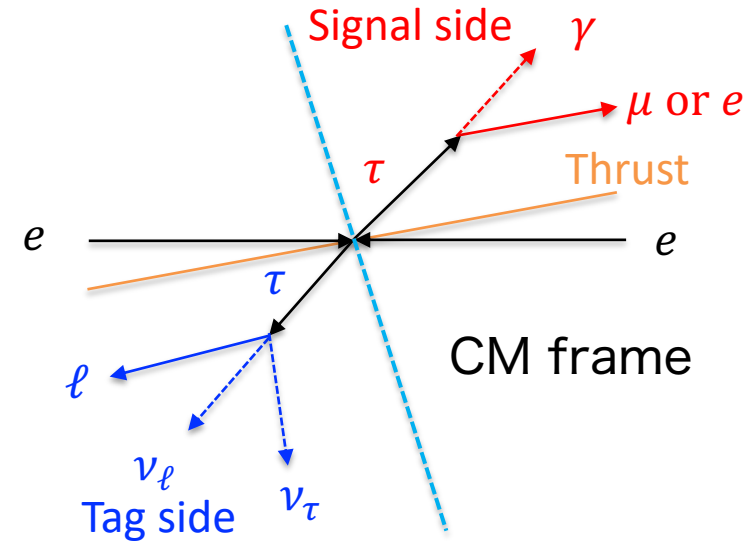
Beam constrained mass: $M_{bc} = \sqrt{\left(\frac{\sqrt{s}}{2}\right)^2 - (p_{\mu\gamma}^{CM})^2}$

※ Scale $|p_{\gamma}^{CM}| = \left(\frac{\sqrt{s}}{2} - p_{\mu}^{CM}\right)$

Previous analysis

$$M_{inv} = \sqrt{(E_{\mu\gamma})^2 - (p_{\mu\gamma})^2}$$

$$\Delta E = E_{\mu\gamma}^{CM} - E_{beam}^{CM}$$



Background estimation

Make background PDFs depending on M_{bc} , $\Delta E/\sqrt{s}$.

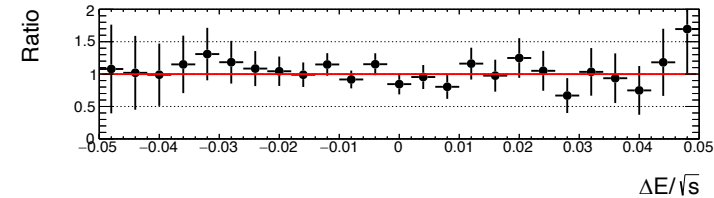
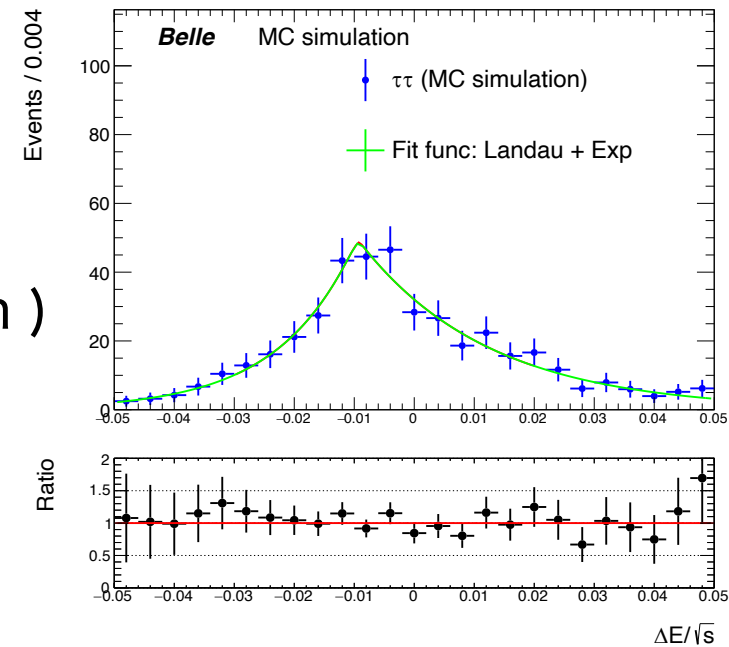
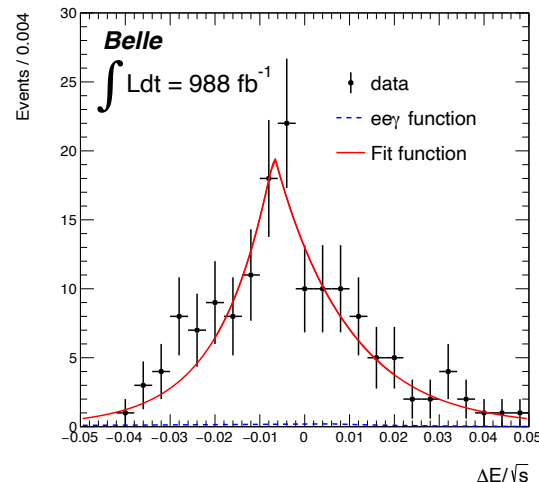
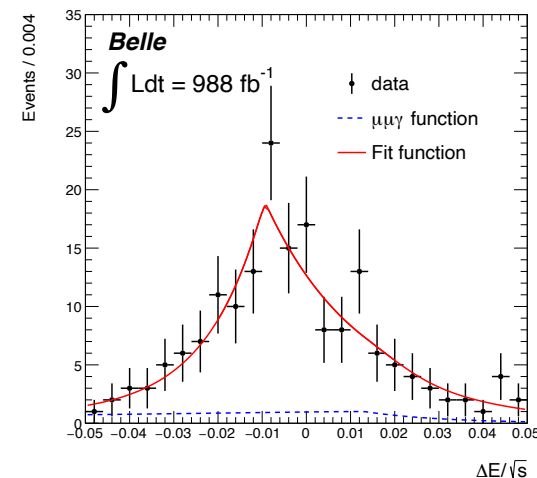
- $\tau\tau, \mu\mu\gamma$ background events: Determine PDFs using MC simulation
 - $ee\gamma$: Determine PDF using the data by applying the eID in tag-side
- M_{bc} , $\Delta E/\sqrt{s}$: almost independent from one another

- Background PDF = $F(M_{bc}) \times G(\Delta E/\sqrt{s})$

The total background PDFs:

- $C_0 F_{\tau\tau} + C_1 G_{\mu\mu\gamma}$ or $C_2 F_{\tau\tau} + C_3 G_{ee\gamma}$

→ C_i by fitting the data (in sideband region)

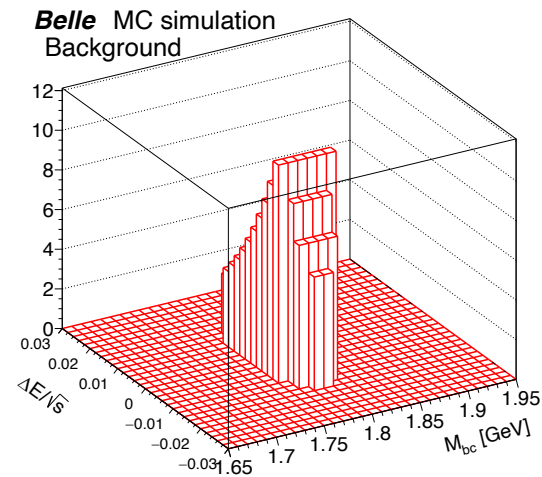
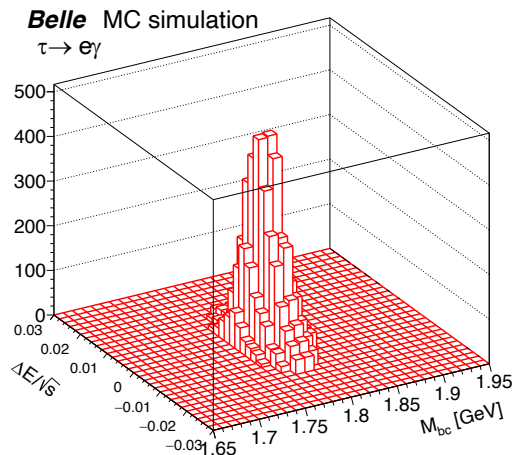


Likelihood fit

2D unbinned maximum likelihood fit

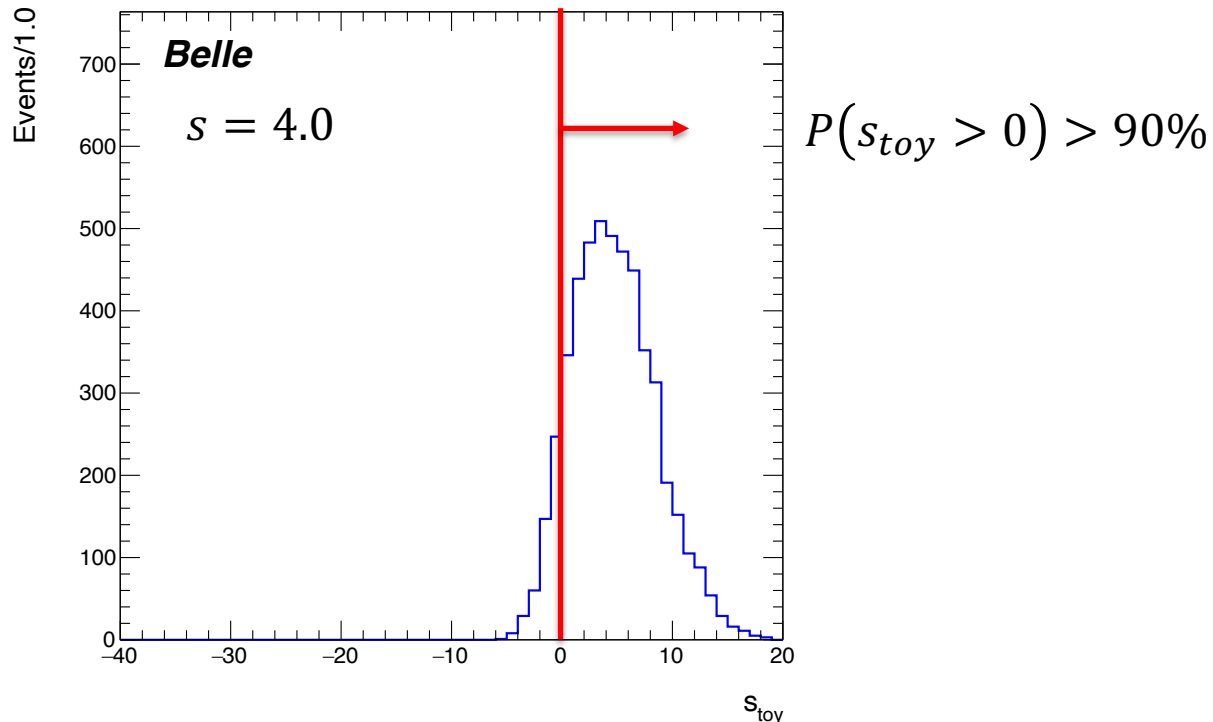
$$\mathcal{L} = \frac{e^{-(s+b)}}{N!} \prod_{i=1}^N (sS_i + bB_i).$$

- s : number of signal from fit
- b : number of background from fit
- S_i : Signal PDF \rightarrow use signal MC simulation
- B_i : Background PDF



How to get upper limits

- Signal event: Poisson(s), Background event: Poisson(b)
- Generate eg. 10000 toys based on each PDF
- b : Expected background event
- s is varied until finding s_{toy} , where $P(s_{\text{toy}} > s_{\text{obs}})$ is 90% → s_{90}
 - In order to get expected limit, we assume $s_{\text{obs}} = 0$



Observed upper limit

- 2D likelihood fit is performed to the data
 - $s_{obs} = -0.25_{-1.27}^{+1.78}$ for $\tau \rightarrow \mu\gamma$
 - $s_{obs} = -0.49_{-3.64}^{+4.37}$ for $\tau \rightarrow e\gamma$
- Observed s_{90} and upper limit is
 - $s_{90} = 2.8$, $Br(\tau \rightarrow \mu\gamma) < 4.2 \times 10^{-8}$ for $\tau \rightarrow \mu\gamma$
 - $s_{90} = 3.0$, $Br(\tau \rightarrow e\gamma) < 5.6 \times 10^{-8}$ for $\tau \rightarrow e\gamma$

