

# Radiation



**Osaka University**

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# Quantized Energy flow

Energy flow is quantized.

Intensity is the number of photon

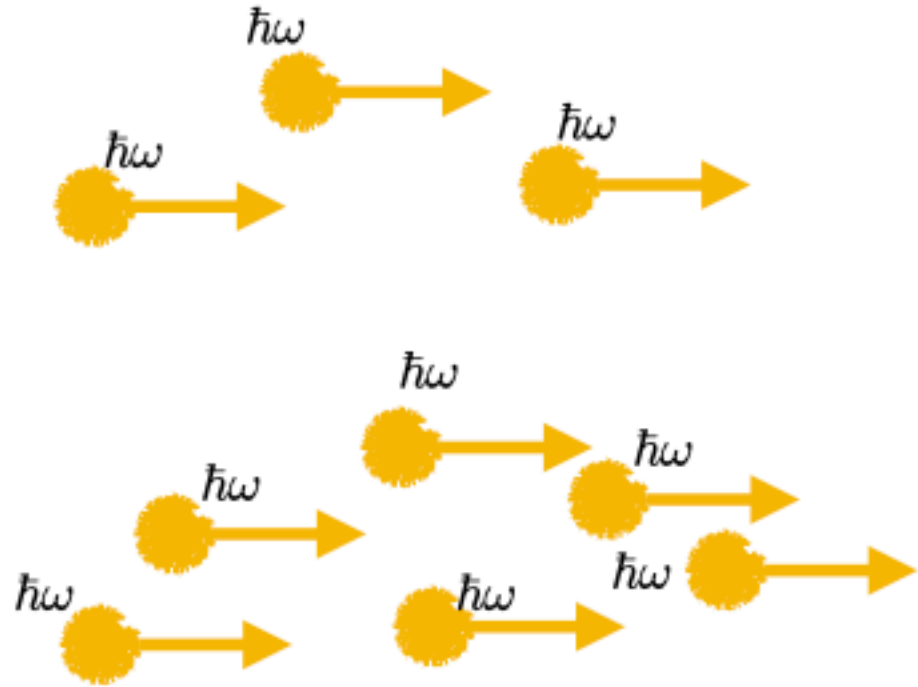


Photo from the Nobel Foundation archive.

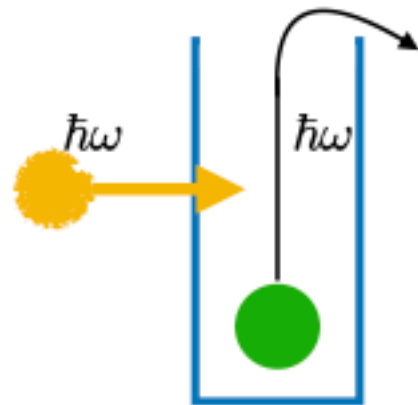
Max Planck

The Nobel Prize in Physics 1918

Prize motivation: "in recognition of the services he rendered to the advancement of Physics by his discovery of energy quanta"

# ionization

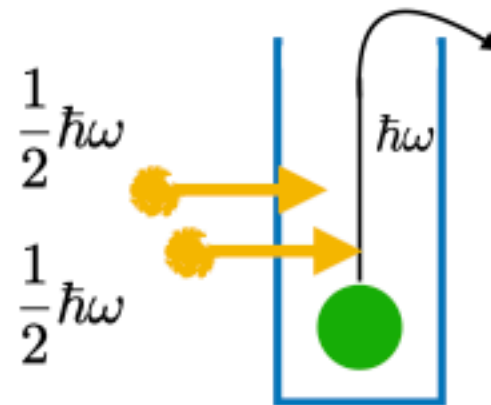
Energy deposit more than the binding energy is required



Single photon can ionize

Probability is proportional to the number of photon.

(Linear effect  $\propto I$  )



Single photon cannot ionize

Very high number density is required.

(Non linear effect  $\propto I^2$  )

High intensity Laser beam allows two photon absorption

Ionizing Radiation =

Each energy quanta has enough energy for ionization.

# photoelectric effect

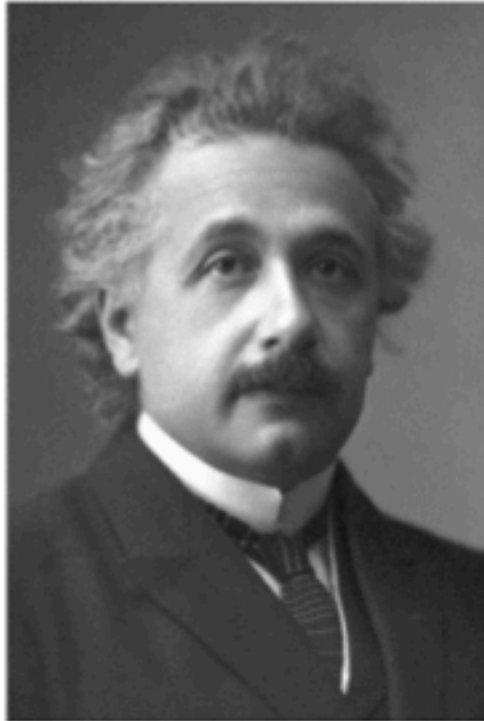


Photo from the Nobel  
Foundation archive.

## Albert Einstein

The Nobel Prize in Physics 1921

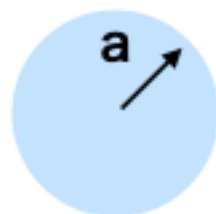
Prize motivation: "for his services to Theoretical Physics, and especially for his discovery of the law of the photoelectric effect"

# binding energy

The Feynman Lectures on Physics, Volume I

Chapter 38. The Relation of Wave and Particle Viewpoints 38-4 The size of an atom

The uncertainty principle  $\Delta x \Delta p \geq \frac{1}{2} \hbar$



The Kinetic Energy  $\frac{p^2}{2m}$  is of the order  $\frac{\hbar^2}{2ma^2}$

The Potential Energy is  $-\frac{1}{4\pi\epsilon_0} \frac{e^2}{a}$

The Total Energy is  $\frac{\hbar^2}{2ma^2} - \frac{1}{4\pi\epsilon_0} \frac{e^2}{a}$  it is minimum at  $a = \frac{4\pi\epsilon_0 \hbar^2}{me^2}$

Fine structure constant  $\alpha = \frac{1}{4\pi\epsilon_0} \frac{e^2}{\hbar c} = \frac{1}{137}$

The Total Energy is  $-\frac{1}{2} mc^2 \alpha^2 = -13.6 \text{ eV}$

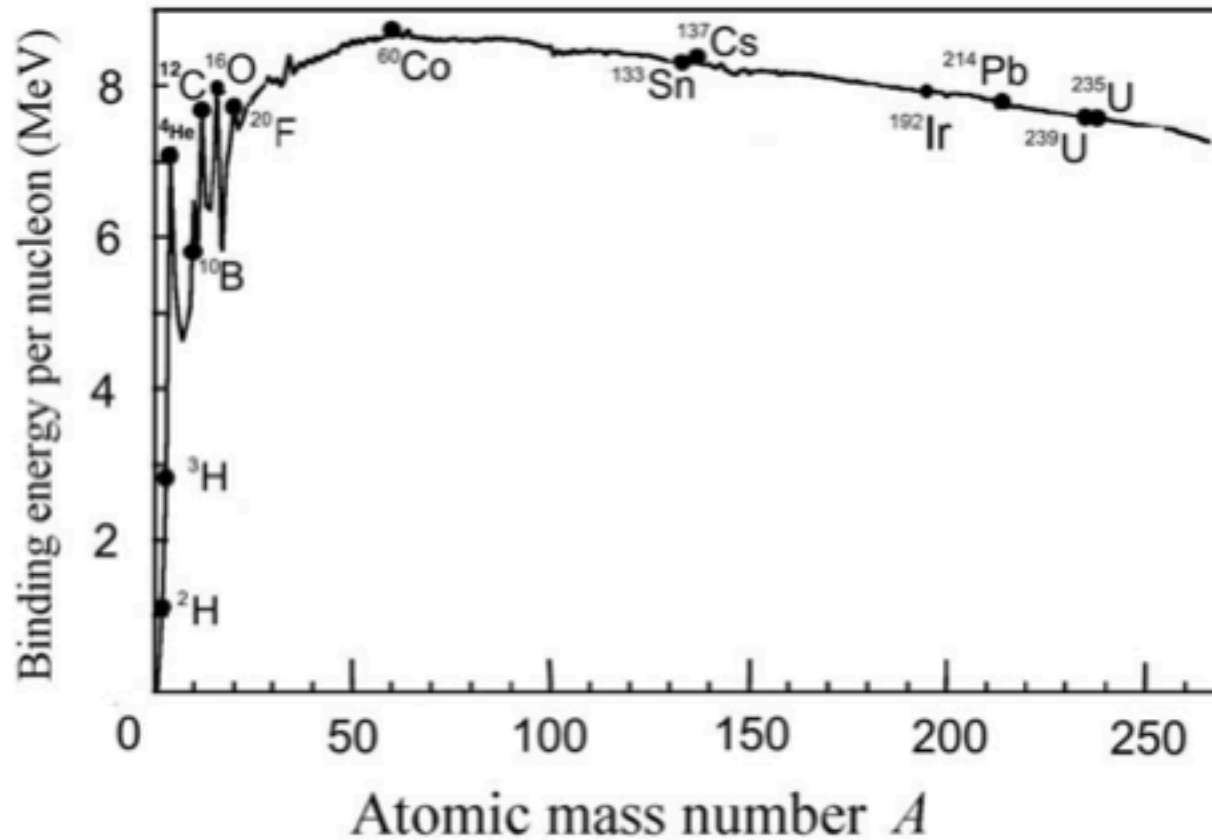


FIG. 1.1. Binding energy per nucleon in megaelectronvolts per nucleon against atomic mass number  $A$ . Data are from the National Institute of Science and Technology (NIST).

The Total Energy is  $-\frac{1}{2}mc^2\alpha^2 = -13.6 \text{ eV}$

Fine structure constant  $\alpha = \frac{1}{4\pi\epsilon_0} \frac{e^2}{\hbar c} = \frac{1}{137}$



**Nuclear force is  
Strong interaction**

**$\sim 1$**

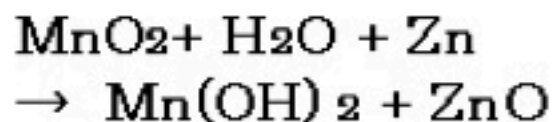
**Nucleon is 2000 times heavier**

# chemical energy

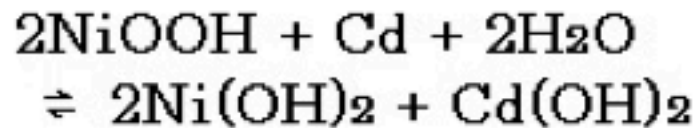
Battery voltage is related to the chemical interactions.



**Alkaline manganese  
battery (1.5V)**



**Ni-Cd  
battery (1.2V)**



# Thermal Energy

Energy of gas molecular is proportional to the temperature.

$$E = kT$$

k is Boltzmann constant  $8.6171\text{E-}5$  eV/K

at room temperature, it is about  $26$  meV =  $0.03$  eV

It is much lower than the ionization energy



# Gravitation



Free fall of 1 kg from 1m high

$$mgh = -10 \text{ J} = 6 \times 10^{19} \text{ eV}$$

It is large energy but each nucleon may get ...

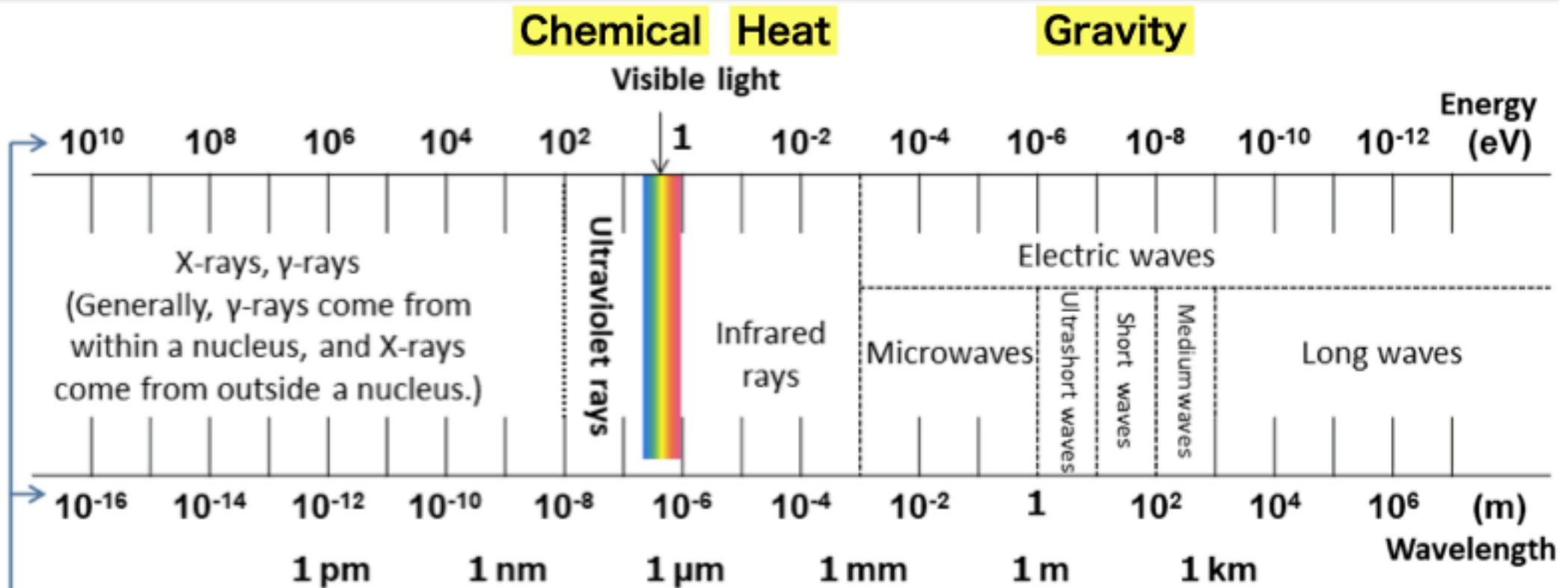
$$6 \times 10^{19} \text{ eV} / (1000 \times 6 \times 10^{23}) = 1 \times 10^{-7} \text{ eV} = 100 \text{ neV}$$

Compare to other Energy, it is several order smaller.

# Energy Scale ionizing radiation

Radiation

## Types of Electromagnetic Waves



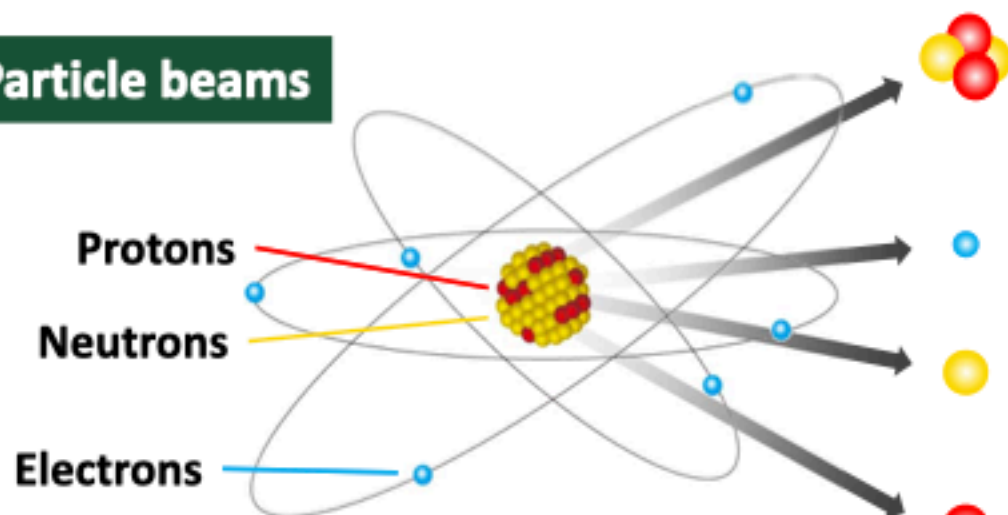
ionizing radiation

# Types of Ionizing Radiation

## Ionizing radiation

Radiation that causes ionization

### Particle beams



**$\alpha$ -particles** (helium nuclei ejected from a nucleus)

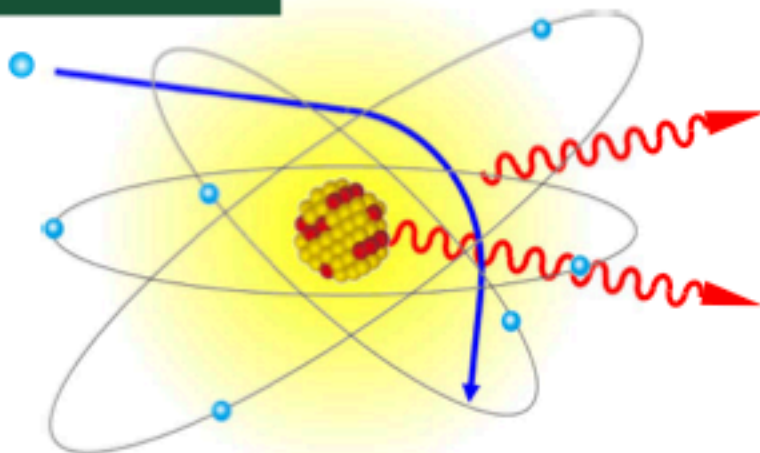
**$\beta$ -particles** (electrons ejected from a nucleus)

**Neutron beams** (produced in nuclear reactors, accelerators, etc.)

**Proton beams** (produced in accelerators, etc.)

### Electromagnetic waves

Electrons  
( $\beta$ -particles)



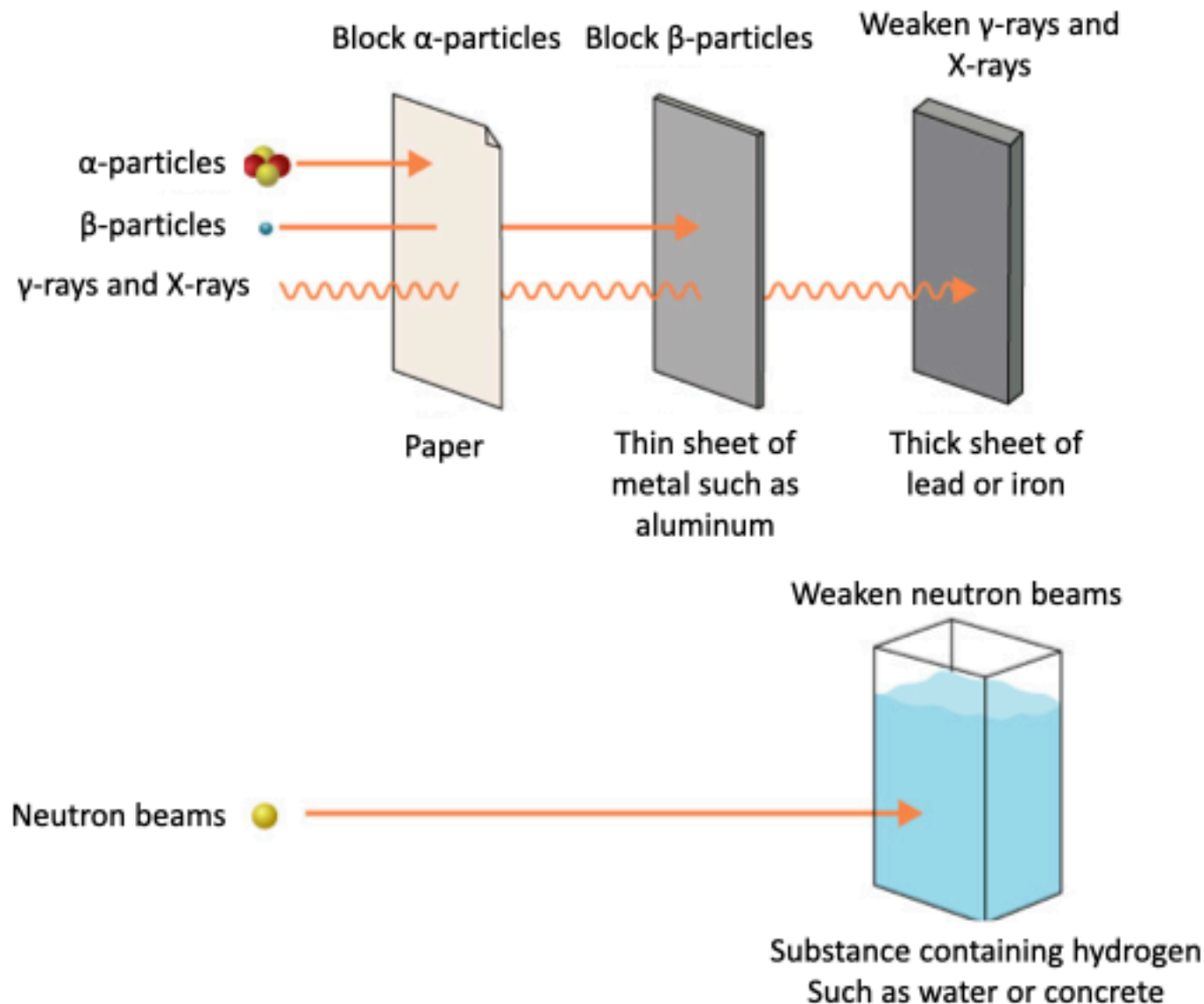
**X-rays** (generated outside a nucleus)

\* X-rays generated when electrons within an atom are caused to travel between orbits by incident electrons are called characteristic X-rays.

**$\gamma$ -rays** (emitted from a nucleus)

# Penetrating Power of Radiation

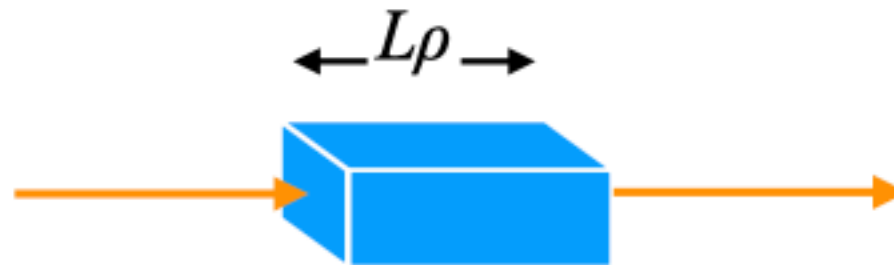
Radiation can be blocked by various substances.



# length



The interaction depends on the density.



$L\rho$  is proportional to the number of nucleon ( $\sim$  electron).

Most of radiation effect is described by  $\text{cm} \times \text{g}/\text{cm}^3 = \text{g}/\text{cm}^2$

# PASSAGE OF PARTICLES THROUGH MATTER

“Bethe-Bloch” equation,

$$-\left\langle \frac{dE}{dx} \right\rangle = K z^2 \frac{Z}{A} \frac{1}{\beta^2} \left[ \frac{1}{2} \ln \frac{2m_e c^2 \beta^2 \gamma^2 T_{\max}}{I^2} - \beta^2 - \frac{\delta(\beta\gamma)}{2} \right].$$



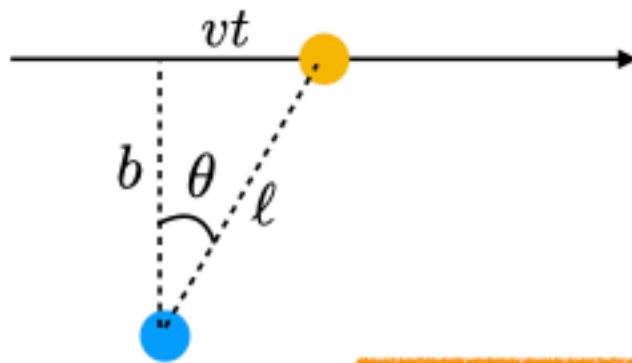
Heavy particle transfer energy to electron



Electron get Impulse =  $\Delta p$

$$F = \frac{ze^2}{4\pi\epsilon_0} \frac{1}{\ell^2}$$

$$F_{\perp} = \frac{ze^2}{4\pi\epsilon_0} \frac{b}{\ell^3}$$



$$\ell \cos \theta = b$$

$$b \tan \theta = vt, \quad \frac{bd\theta}{\cos^2 \theta} = vdt$$

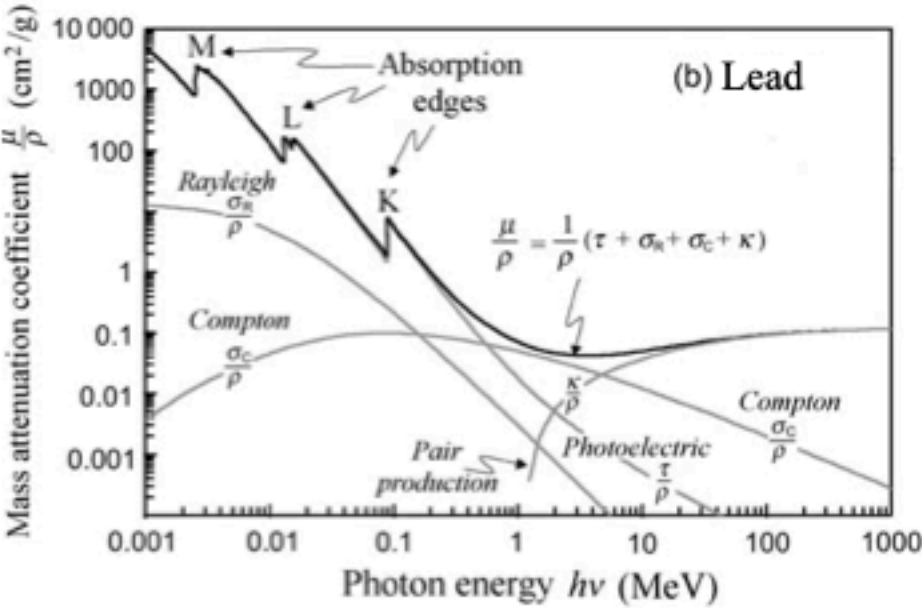
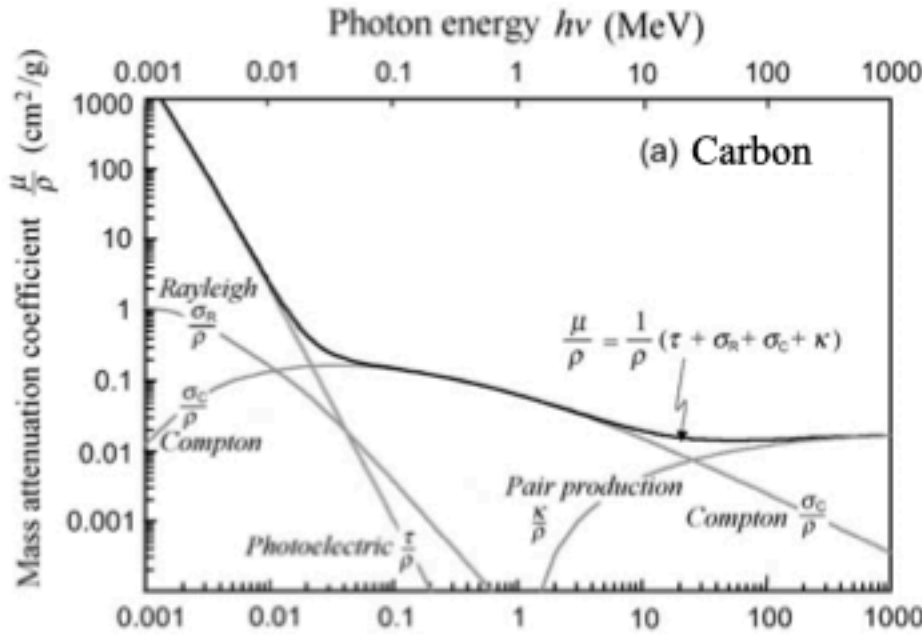
$$\Delta p = \int F_{\perp} dt = \frac{ze^2}{4\pi\epsilon_0} \int_{-\infty}^{\infty} \frac{b}{\ell^3} dt$$

$$\int F_{\perp} dt = \frac{ze^2}{4\pi\epsilon_0} \int_{-\pi/2}^{\pi/2} \frac{\cos^3 \theta}{b^2} \frac{bd\theta}{v \cos^2 \theta} = \frac{ze^2}{4\pi\epsilon_0} \int_{-\pi/2}^{\pi/2} \frac{\cos \theta}{b} \frac{d\theta}{v} = \frac{ze^2}{2\pi\epsilon_0} \frac{1}{bv}$$

$$\Delta E_e = \frac{\Delta p^2}{2m_e} = \frac{1}{2m_e} \left( \frac{ze^2}{2\pi\epsilon_0} \frac{1}{bv} \right)^2 = \frac{2z^2}{m_e c^2} \left( \frac{e^2}{4\pi\epsilon_0} \frac{1}{\hbar c} \right)^2 \frac{(\hbar c)^2}{\beta^2 b^2} = \frac{2z^2}{m_e c^2} \alpha^2 \frac{(\hbar c)^2}{\beta^2 b^2}$$

$$-\left\langle \frac{dE}{dx} \right\rangle = K z^2 \frac{Z}{A} \frac{1}{\beta^2} \left[ \frac{1}{2} \ln \frac{2m_e c^2 \beta^2 \gamma^2 T_{\max}}{I^2} - \beta^2 - \frac{\delta(\beta\gamma)}{2} \right]$$

# Photon Interactions



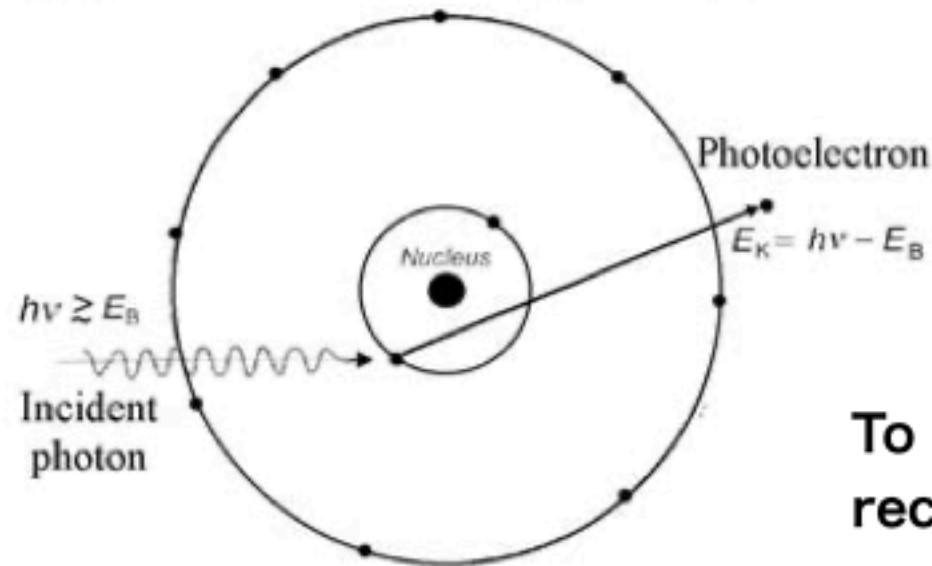
Photoelectric effect  
Compton Scattering  
Pair Production

FIG. 1.5. Mass attenuation coefficient  $\mu/\rho$  against photon energy  $h\nu$  in the range from 1 keV to 1000 MeV for carbon (a) and lead (b). In addition to the total coefficients  $\mu/\rho$ , the individual coefficients for the photoelectric effect, Rayleigh scattering, Compton scattering and pair production (including triplet production) are also shown. Data are from the National Institute of Science and Technology (NIST).



# photoelectric effect

(a) *Photoelectric effect* ( $\tau$ )



**To preserve energy and momentum, the recoil of nucleus is needed.**

# Compton scattering

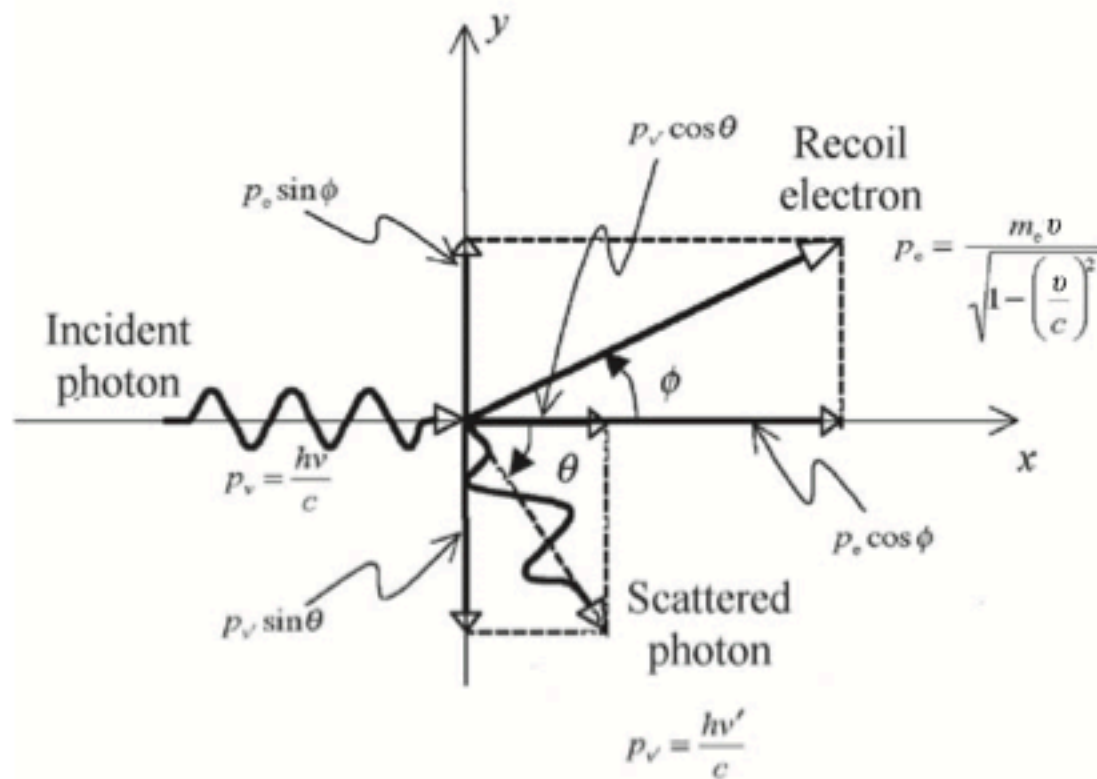
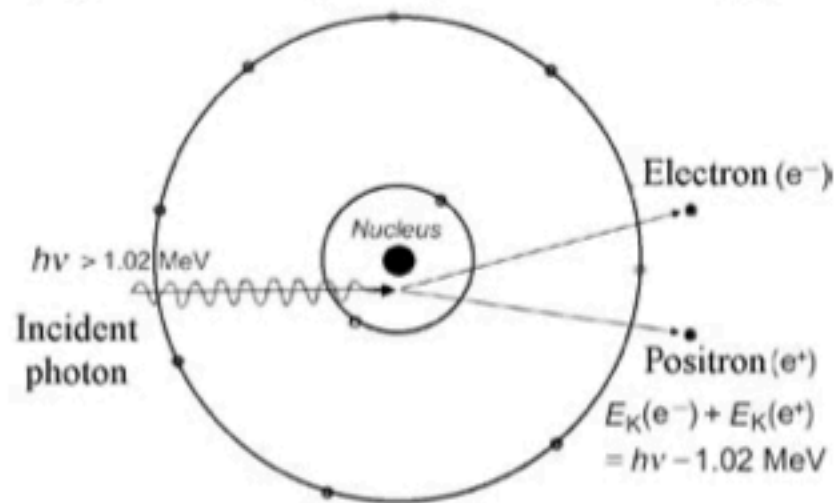


FIG. 1.7. Schematic diagram of the Compton effect in which an incident photon of energy  $h\nu = 1 \text{ MeV}$  interacts with a 'free and stationary' electron. A photon with energy  $h\nu' = 0.505 \text{ MeV}$  is produced and scattered with a scattering angle  $\theta = 60^\circ$ .

Since Compton interaction is a photon interaction with a free electron, the Compton atomic attenuation coefficient depends linearly on the absorber atomic number  $Z$

# Pair production

(d) Nuclear pair production ( $\kappa_N$ )



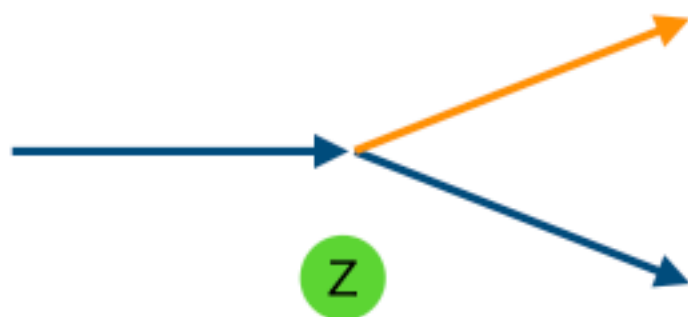
To preserve energy and momentum, the recoil of nucleus is needed.

Photon must energetic more than 2 x electron mass.

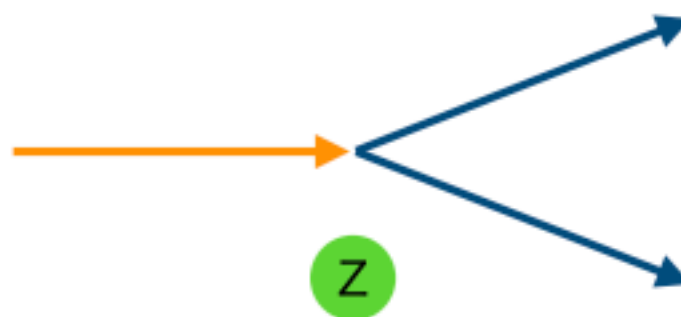
# Photon and electron interactions in matter

High-energy electrons predominantly lose energy in matter by bremsstrahlung, and high-energy photons by  $e^+e^-$  pair production.

**bremsstrahlung**



**pair production**



## Radiation length

radiation length  $X_0$ , usually measured in  $\text{g cm}^{-2}$ . It is both (a) the mean distance over which a high-energy electron loses all but  $1/e$  of its energy by bremsstrahlung, and (b)  $\frac{7}{9}$  of the mean free path for pair production by a high-energy photon

**It causes electromagnetic shower**

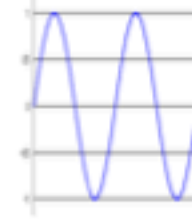
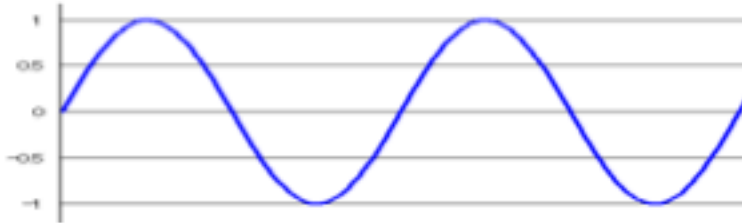
# Atomic and Nuclear Properties of Materials

**Table 6.1** Abridged from [pdg.lbl.gov/AtomicNuclearProperties](https://pdg.lbl.gov/AtomicNuclearProperties) by D.E. Groom (2017). See web pages for more detail about entries in this table and for several hundred others. Parentheses in the  $dE/dx$  and density columns indicate gases at 20° C and 1 atm. Boiling points are at 1 atm. Refractive indices  $n$  are evaluated at the sodium D line blend (589.2 nm); values  $\gg 1$  in brackets indicate  $(n - 1) \times 10^6$  for gases at 0° C and 1 atm.

Material	$Z$	$A$	$\langle Z/A \rangle$	Nucl.coll. length $\lambda_T$ {g cm <sup>-2</sup> }	Nucl.inter. length $\lambda_I$ {g cm <sup>-2</sup> }	Rad.len. $X_0$ {g cm <sup>-2</sup> }	$dE/dx _{\min}$ { MeV g <sup>-1</sup> cm <sup>2</sup> }	Density {g cm <sup>-3</sup> } ({g ℓ <sup>-1</sup> })	Melting point (K)	Boiling point (K)	Refract. index @ Na D
H <sub>2</sub>	1	1.008(7)	0.99212	42.8	52.0	63.05	(4.103)	0.071(0.084)	13.81	20.28	1.11[132.]
D <sub>2</sub>	1	2.014101764(8)	0.49650	51.3	71.8	125.97	(2.053)	0.169(0.168)	18.7	23.65	1.11[138.]
He	2	4.002602(2)	0.49967	51.8	71.0	94.32	(1.937)	0.125(0.166)		4.220	1.02[35.0]
Li	3	6.94(2)	0.43221	52.2	71.3	82.78	1.639	0.534	453.6	1615.	
Be	4	9.0121831(5)	0.44384	55.3	77.8	65.19	1.595	1.848	1560.	2744.	
C diamond	6	12.0107(8)	0.49955	59.2	85.8	42.70	1.725	3.520			2.419
C graphite	6	12.0107(8)	0.49955	59.2	85.8	42.70	1.742	2.210	Sublimes at 4098. K		
N <sub>2</sub>	7	14.007(2)	0.49976	61.1	89.7	37.99	(1.825)	0.807(1.165)	63.15	77.29	1.20[298.]
O <sub>2</sub>	8	15.999(3)	0.50002	61.3	90.2	34.24	(1.801)	1.141(1.332)	54.36	90.20	1.22[271.]
F <sub>2</sub>	9	18.998403163(6)	0.47372	65.0	97.4	32.93	(1.676)	1.507(1.580)	53.53	85.03	[195.]
Ne	10	20.1797(6)	0.49555	65.7	99.0	28.93	(1.724)	1.204(0.839)	24.56	27.07	1.09[67.1]
Al	13	26.9815385(7)	0.48181	69.7	107.2	24.01	1.615	2.699	933.5	2792.	
Si	14	28.0855(3)	0.49848	70.2	108.4	21.82	1.664	2.329	1687.	3538.	3.95
Cl <sub>2</sub>	17	35.453(2)	0.47951	73.8	115.7	19.28	(1.630)	1.574(2.980)	171.6	239.1	[773.]
Ar	18	39.948(1)	0.45059	75.7	119.7	19.55	(1.519)	1.396(1.662)	83.81	87.26	1.23[281.]
Ti	22	47.867(1)	0.45961	78.8	126.2	16.16	1.477	4.540	1941.	3560.	
Fe	26	55.845(2)	0.46557	81.7	132.1	13.84	1.451	7.874	1811.	3134.	
Cu	29	63.546(3)	0.45636	84.2	137.3	12.86	1.403	8.960	1358.	2835.	
Ge	32	72.630(1)	0.44053	86.9	143.0	12.25	1.370	5.323	1211.	3106.	
Sn	50	118.710(7)	0.42119	98.2	166.7	8.82	1.263	7.310	505.1	2875.	
Xe	54	131.293(6)	0.41129	100.8	172.1	8.48	(1.255)	2.953(5.483)	161.4	165.1	1.39[701.]
W	74	183.84(1)	0.40252	110.4	191.9	6.76	1.145	19.300	3695.	5828.	
Pt	78	195.084(9)	0.39983	112.2	195.7	6.54	1.128	21.450	2042.	4098.	
Au	79	196.966569(5)	0.40108	112.5	196.3	6.46	1.134	19.320	1337.	3129.	
Pb	82	207.2(1)	0.39575	114.1	199.6	6.37	1.122	11.350	600.6	2022.	
U	92	[238.02891(3)]	0.38651	118.6	209.0	6.00	1.081	18.950	1408.	4404.	

$$\hbar c = 197 \text{ eV nm}$$

$$\hbar c = 197 \text{ MeV fm}$$



1 keV = 1.2 nm (~size of atom)  
20MeV = 60 fm (~size of atomic nuclei)

molecule → atomic nucleus

## Naturally Occurring or Artificial

Radionuclides	Radiation being emitted	Half-life
Thorium-232 (Th-232)	$\alpha$ , $\gamma$	14.1 billion years
Uranium-238 (U-238)	$\alpha$ , $\gamma$	4.5 billion years
Potassium-40 (K-40)	$\beta$ , $\gamma$	1.3 billion years
Plutonium-239 (Pu-239)	$\alpha$ , $\gamma$	24,000 years
Carbon-14 (C-14)	$\beta$	5,730 years
Cesium-137 (Cs-137)	$\beta$ , $\gamma$	30 years
Strontium-90 (Sr-90)	$\beta$	29 years
Tritium (H-3)	$\beta$	12.3 years
Cesium-134 (Cs-134)	$\beta$ , $\gamma$	2.1 years
Iodine-131 (I-131)	$\beta$ , $\gamma$	8 days
Radon-222 (Rn-222)	$\alpha$ , $\gamma$	3.8 days

Artificial radionuclides are shown in red letters.

$\alpha$ :  $\alpha$  (alpha) particles,  $\beta$ :  $\beta$  (beta) particles,  $\gamma$ :  $\gamma$  (gamma)-rays

# Half life

~~1 → 1/2 → 0~~

1 → 1/2 → 1/4 → 1/8 → 1/16 → 1/32 → 1/64

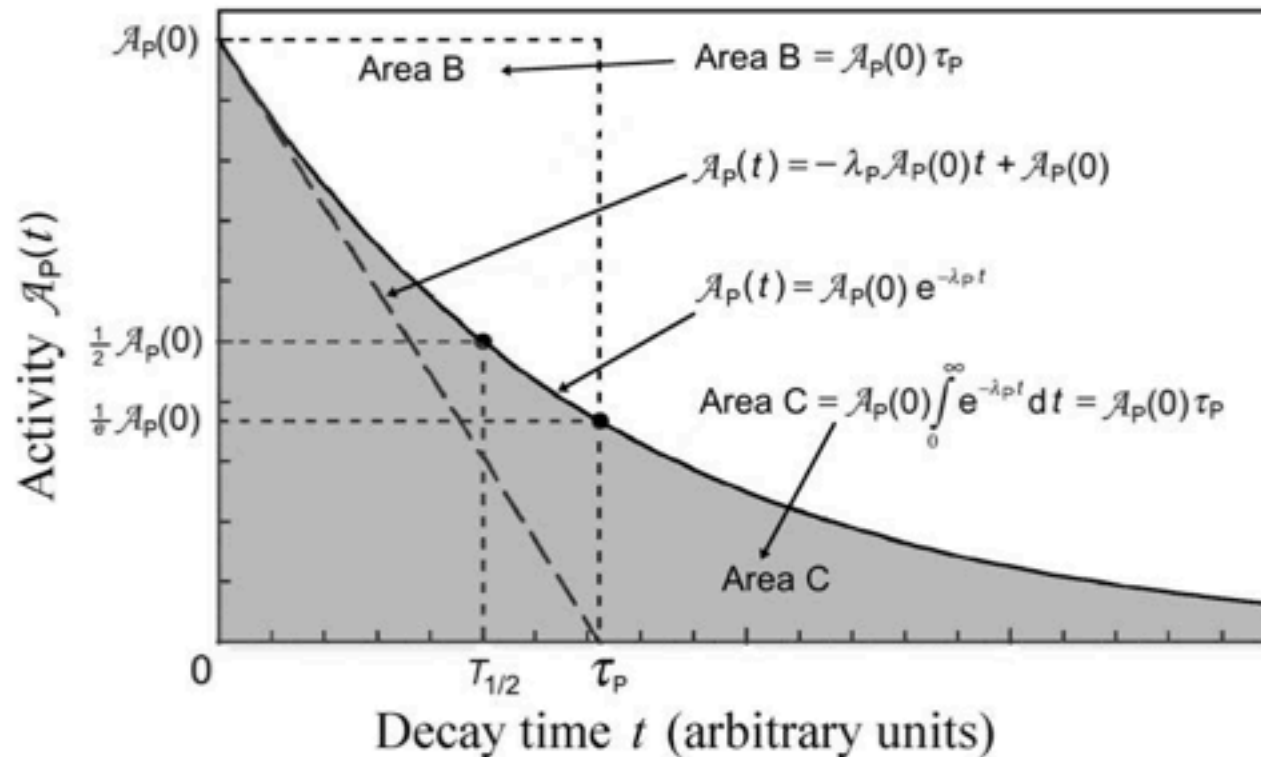


FIG. 1.3. Activity  $\mathcal{A}_p(t)$  plotted against time  $t$  for a simple decay of a radioactive parent  $P$  into a stable or unstable daughter  $D$ . The concepts of half-life  $(T_{1/2})_p$  and mean life  $\tau_p$  are also illustrated. The area under the exponential decay curve from  $t = 0$  to  $t = \infty$  is equal to the product  $\mathcal{A}_p(0)\tau_p$  where  $\mathcal{A}_p(0)$  is the initial activity of the parent  $P$ . The slope of the tangent to the decay curve at  $t = 0$  is equal to  $\lambda_p \mathcal{A}_p(0)$  and this tangent crosses the abscissa axis at  $t = \tau_p$ .



# Nuclei with Long Half-lives

## Example

Radioactive materials that had existed in the universe since before the birth of the earth and were taken into the earth upon its birth



## Series

A radioactive nucleus repeats disintegration until becoming stable, accompanying changes in nuclides each time.

- **Uranium-238**
- **Thorium-232**
- **Uranium-235**

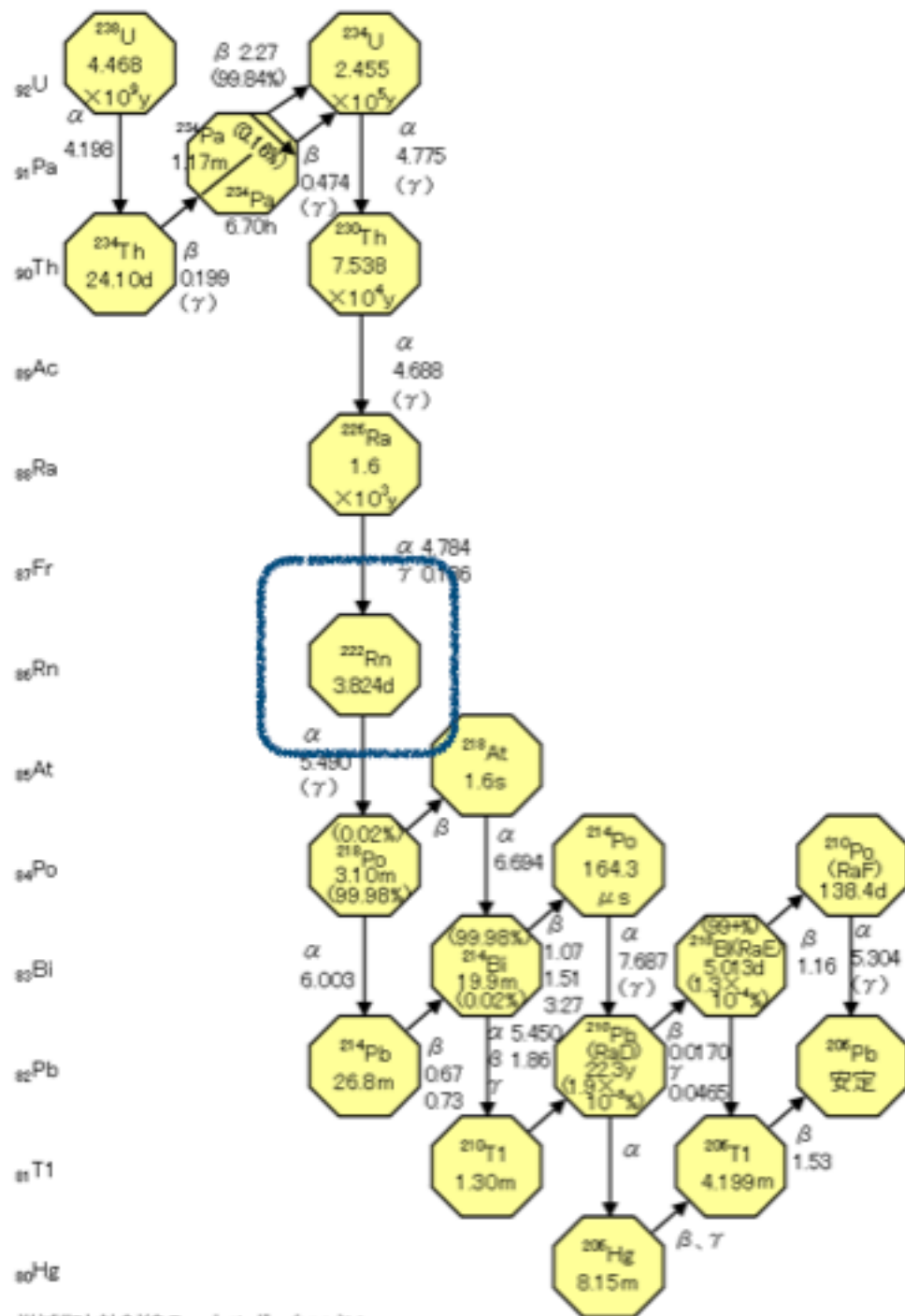
Half-life: 4.5 billion years

## Non-series

A radioactive nucleus directly disintegrates into a stable nucleus.

- **Potassium-40**
- **Rubidium-87, etc.**

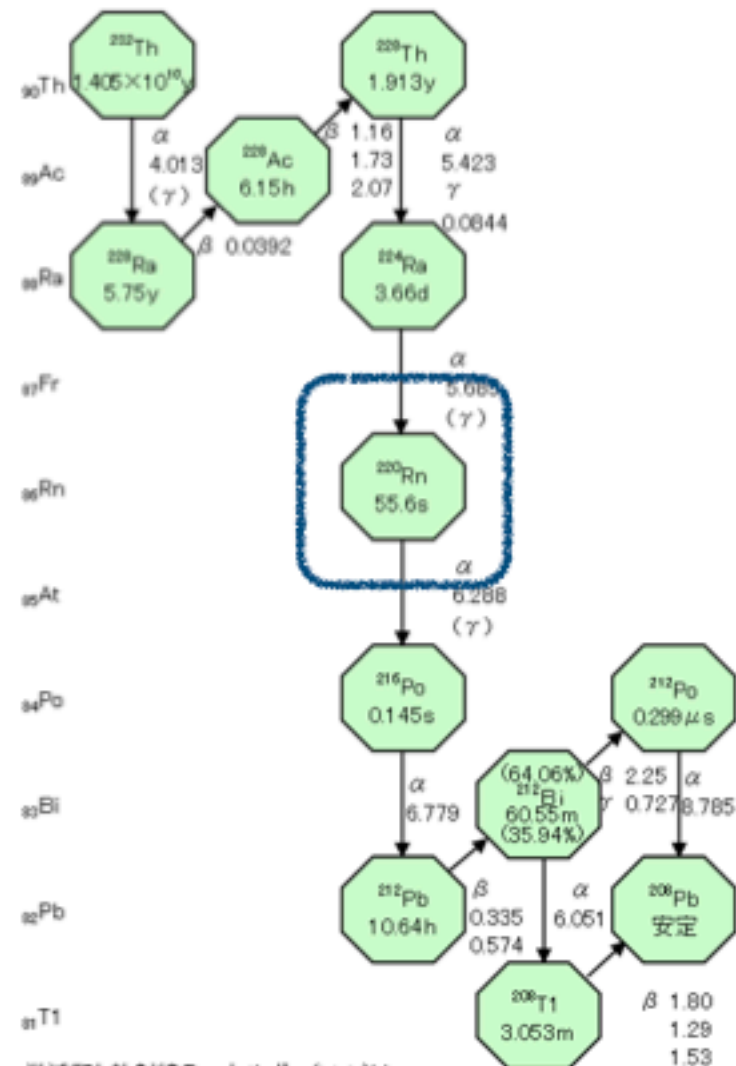
Half-life: 1.3 billion years



半減期と放射線のエネルギー(MeV)は  
 Evaluated Nuclear Structure Data File(1965年2月)

図2 ウラン( $^{238}\text{U}$ )壊変系列

[出典] 日本アイソトープ協会(編):アイソトープ手帳、丸善(2002年7月)、p.13

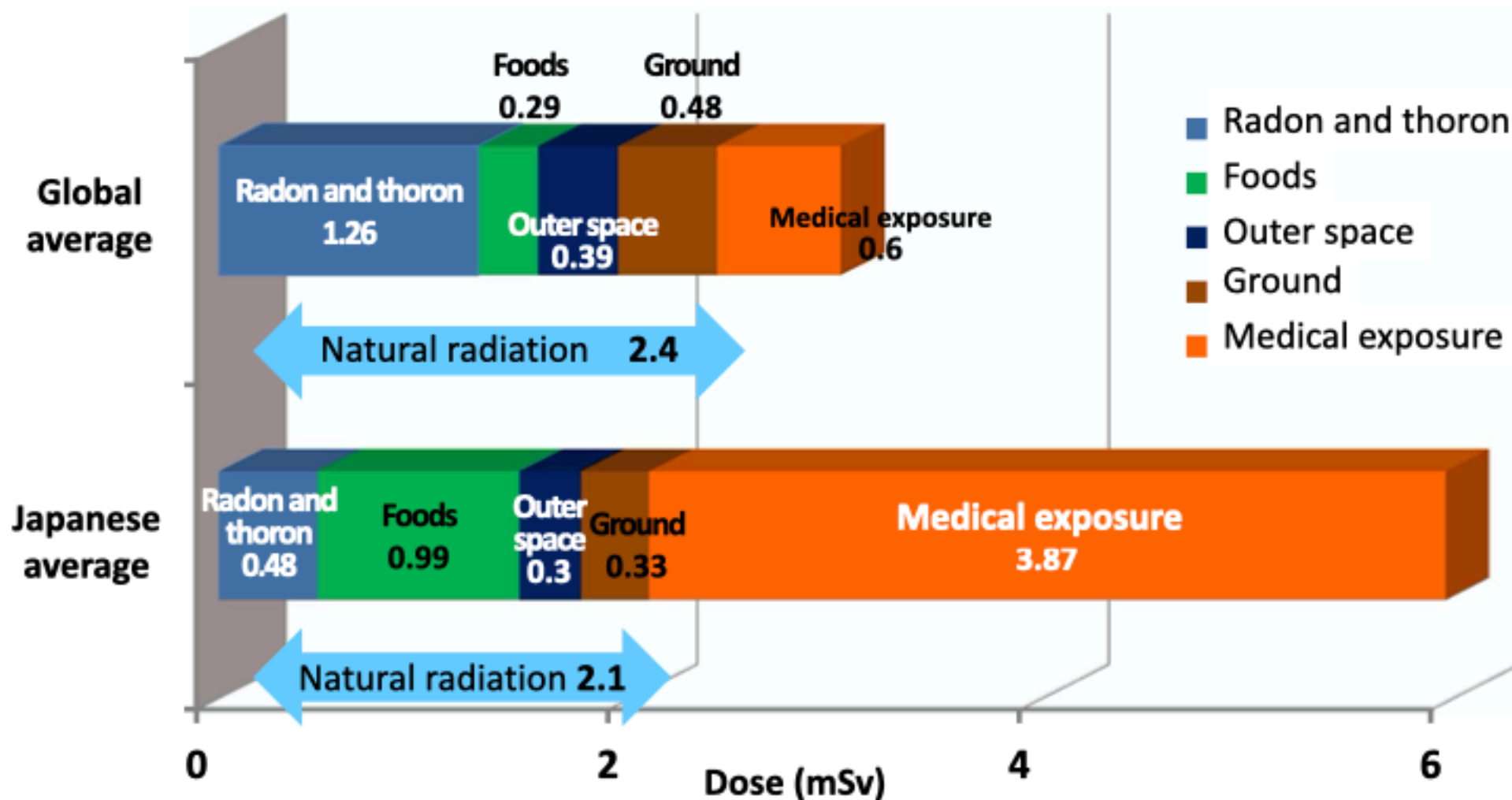


半減期と放射線のエネルギー(MeV)は  
 Evaluated Nuclear Structure Data File(1995年2月)

図3 トリウム( $^{232}\text{Th}$ )壊変系列

[出典] 日本アイソトープ協会(編):アイソトープ手帳、丸善(2002年7月)、p.12

## Exposure in daily life (annual)



Sources: Prepared based on the 2008 UNSCEAR (United Nations Scientific Committee on the Effects of Atomic Radiation) Report; and "Environmental Radiation in Daily Life (2011)," Nuclear Safety Research Association

# Natural Radioactive Materials in the Body and Foods

## Radioactive materials in the body



When body weight is 60kg

Potassium-40	※ 1	4,000Bq
Carbon-14	※ 2	2,500Bq
Rubidium-87	※ 1	500Bq
Tritium	※ 2	100Bq
Lead and polonium	※ 3	20Bq

- ※ 1 Nuclides originating from the Earth
- ※ 2 Nuclides derived from N-14 originating from cosmic rays
- ※ 3 Nuclides of the uranium series originating from the Earth

## Radioactivity concentrations (Potassium-40) in foods



Rice: 30; Milk: 50; Beef: 100; Fish: 100; Dry milk: 200; Spinach: 200;  
 Potato chips: 400; Green tea: 600; Dried *shiitake*: 700; Dried kelp: 2,000 (Bq/kg)

Bq: becquerels    Bq/kg: becquerels/kilogram

Source: Prepared based on "Research on Data about Living Environment Radiation (1983)," Nuclear Safety Research Association

## Nuclear power plant accidents so far



1979 Three Mile Island Nuclear Accident



1986 Chernobyl nuclear accident

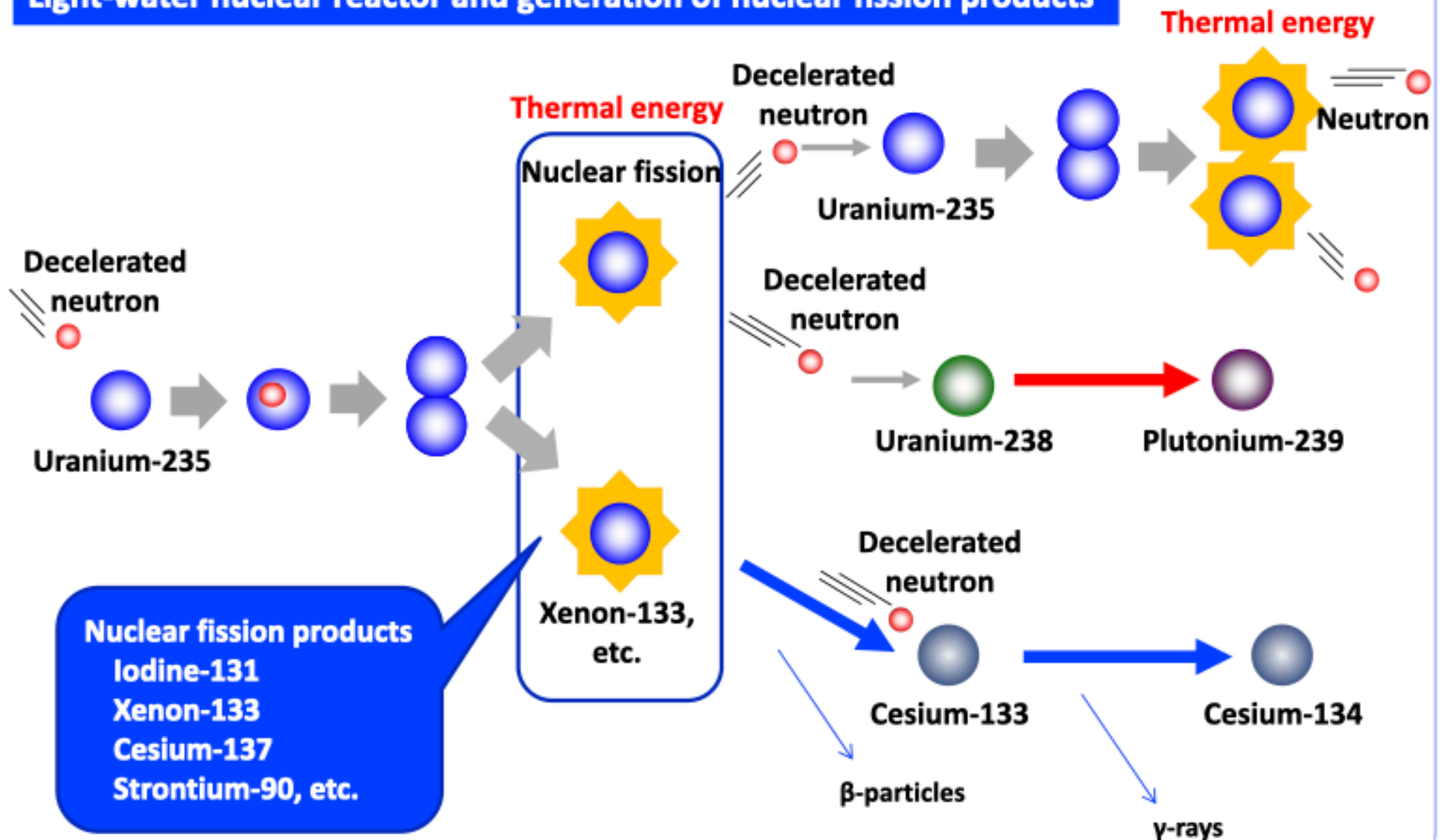


2011 Fukushima Daiichi Nuclear Power Plant Accident

# Support for the urgent refugee from the radioactive contamination area



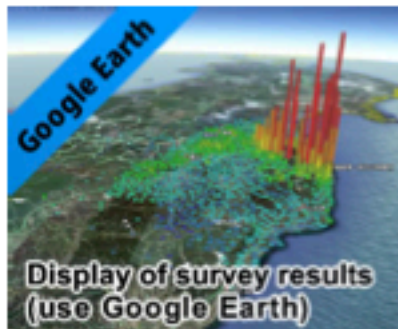
## Light-water nuclear reactor and generation of nuclear fission products



# Survey of Fukushima Soil Radioactivities

~ Radioactivity maps displayed by the Google Earth, Google map ~

TOP Update About Participants Download



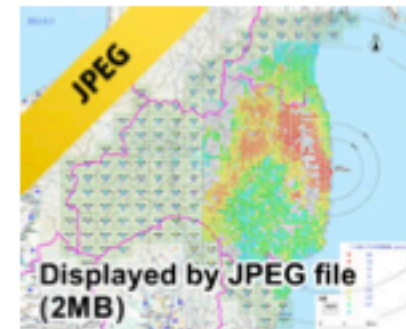
Display of survey results  
(use Google Earth)  
○ High speed PC ✕ Smart phone  
✕ Tablet, Ipad



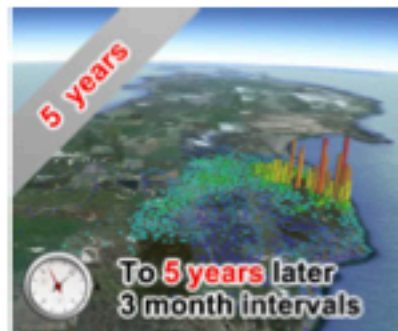
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○ Low speed PC ○ Smart phone  
○ Tablet, Ipad



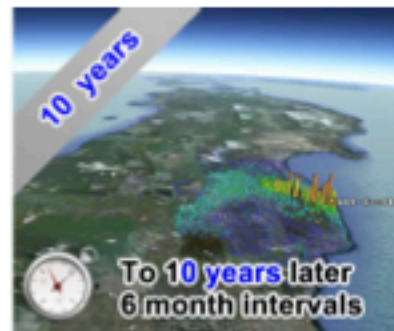
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○ Low speed PC ○ Smart phone  
○ Tablet, Ipad



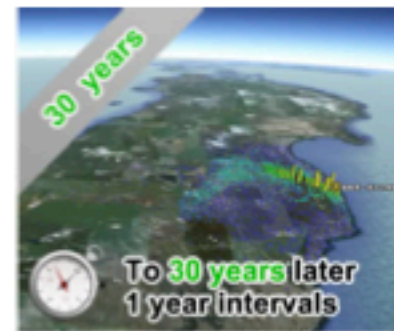
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(2MB)  
○ Low speed PC ○ Smart phone  
○ Tablet, Ipad



To 5 years later  
3 month intervals  
○ High speed PC ✕ Smart phone  
✕ Tablet, Ipad



To 10 years later  
6 month intervals  
○ High speed PC ✕ Smart phone  
✕ Tablet, Ipad

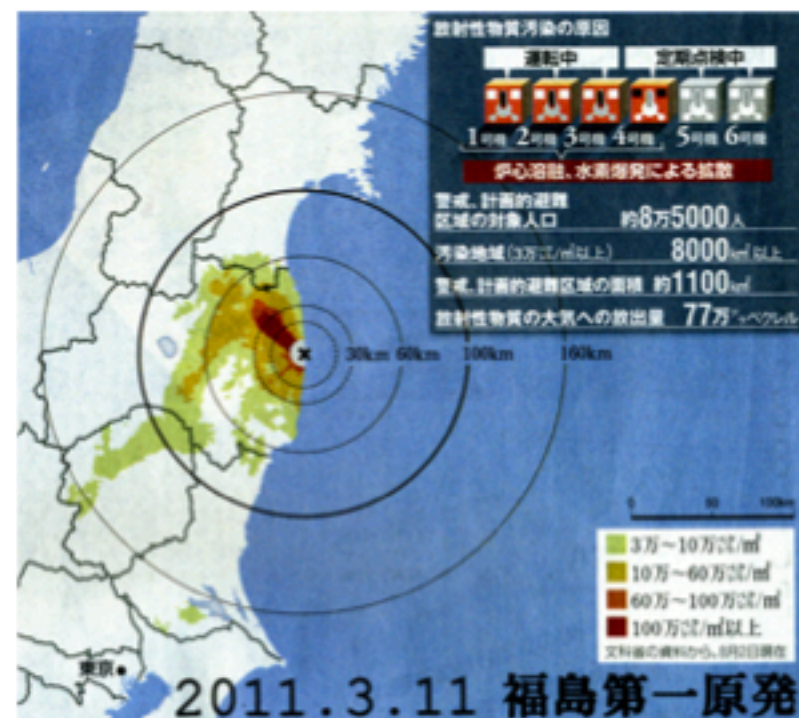
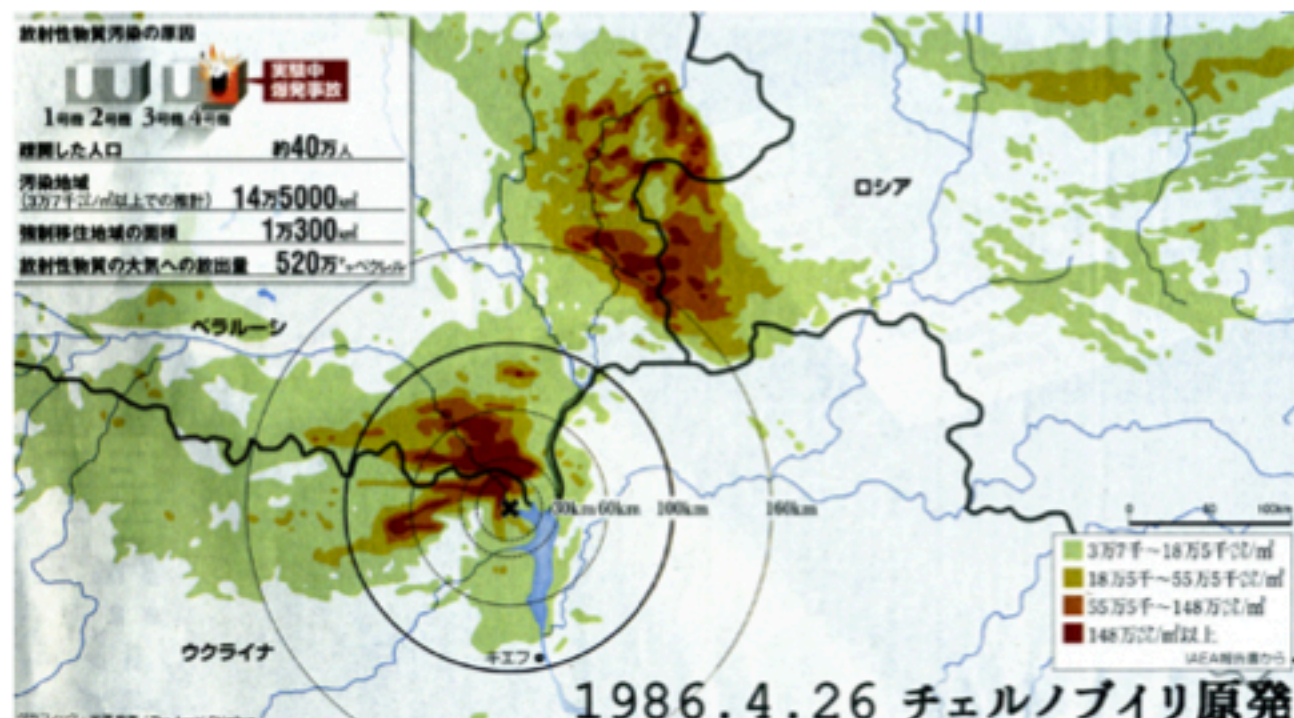


To 30 years later  
1 year intervals  
○ High speed PC ✕ Smart phone  
✕ Tablet, Ipad



# Comparing the **Chernobyl** and **Fukushima** nuclear accidents at the same scale

## Accumulation of cesium-137 in soil



(朝日新聞2011.9.11)

- 18.5万~55.5万Bq/m<sup>2</sup> 自主移住 (希望すれば移住可) 区域
- 55.5万~148万Bq/m<sup>2</sup> 一次的にしろ移住が必要な区域
- 148万Bq/m<sup>2</sup>以上 永久的な移住が必要な区域

- 10万~60万Bq/m<sup>2</sup>
- 60万~100万Bq/m<sup>2</sup>
- 100万Bq/m<sup>2</sup>以上

# Decontamination Methods

Decontamination has been conducted in accordance with the circumstances of respective areas.

Specific methods differ by location.

Effective methods differ depending on the status of contamination with radioactive materials. First, ambient dose rates are measured, and an optimal method is selected on a case-by-case basis. Radiation doses are measured before and after decontamination work to confirm the effects.



Case  
1

Decontamination methods employed in areas with relatively low radiation doses

• The following are examples.



●Cleaning of eaves and gutters of private houses



●Mowing of vegetation (Provided by Date City)



●Removal of sludge from ditches (Provided by Fukushima City)

Case  
2

Decontamination methods employed in areas with relatively high radiation doses (in addition to the above methods)



●Scraping off of topsoil of school yards (Provided by JAEA)



●Washing of building roofs, etc.



●Scraping off of garden soil, etc. (Provided by Date City)

Prepared based on the website, "Environmental Remediation," of the Ministry of the Environment