

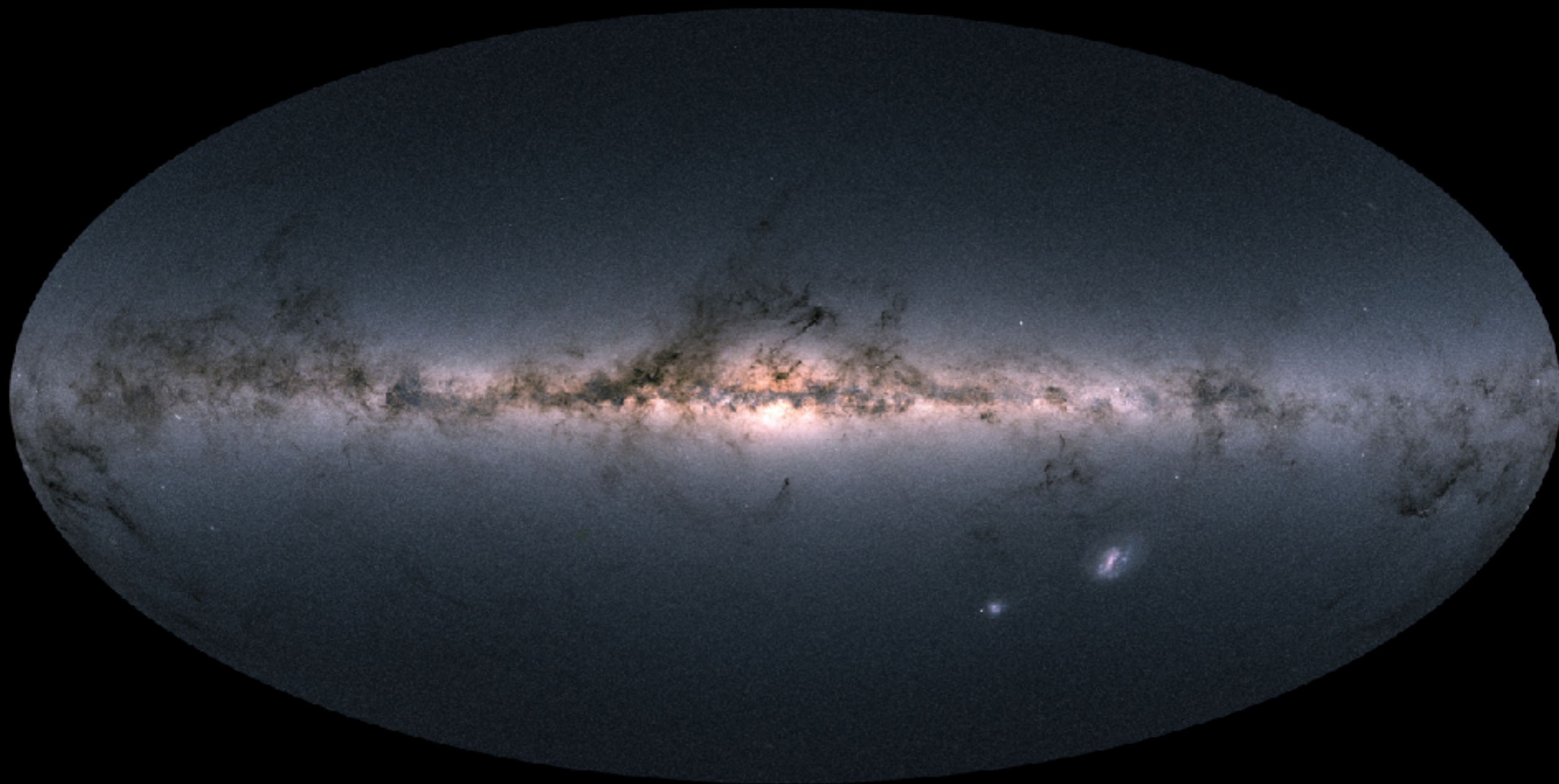
Exploring the Galaxy with Gaia

ASTRO 322

Erik Rosolowsky

Gaia - Global Astrometric Interferometer for Astrophysics
ESA Mission launched in Dec. 2013
Objective: locations and motions of 1 billion stars





→ GAIA: BRINGING THE GALAXY INTO FOCUS

Gaia Measurements

For $>10^9$ objects, Gaia precisely measures:

- Positions (Right Ascension / Declination)
- Brightnesses in three “colours”
- Stellar *parallax*
- *Proper motions*
- Radial velocities

Coordinates

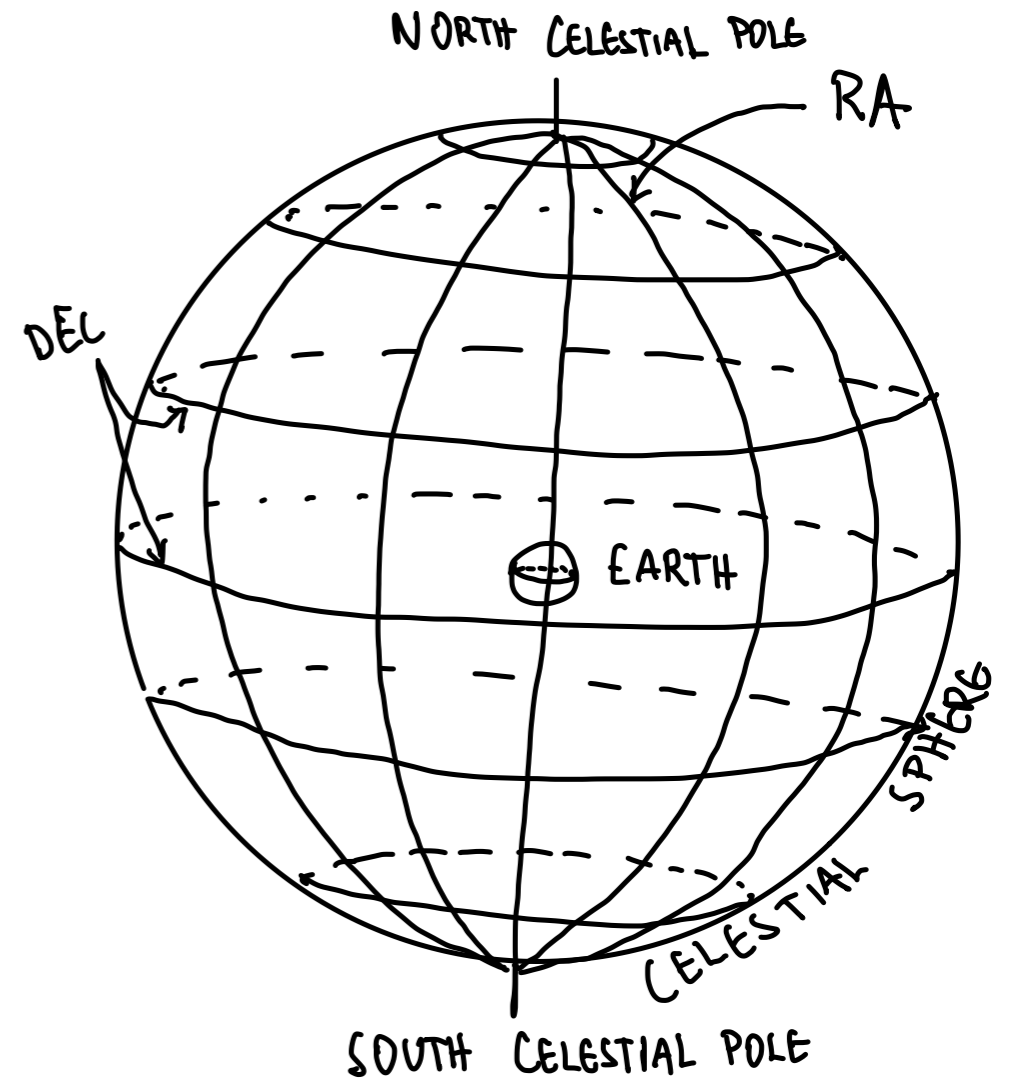
Measured on the *celestial sphere* in coordinates of:

Right Ascension (“RA”; longitude-like)

Declination (“Dec”; latitude-like)

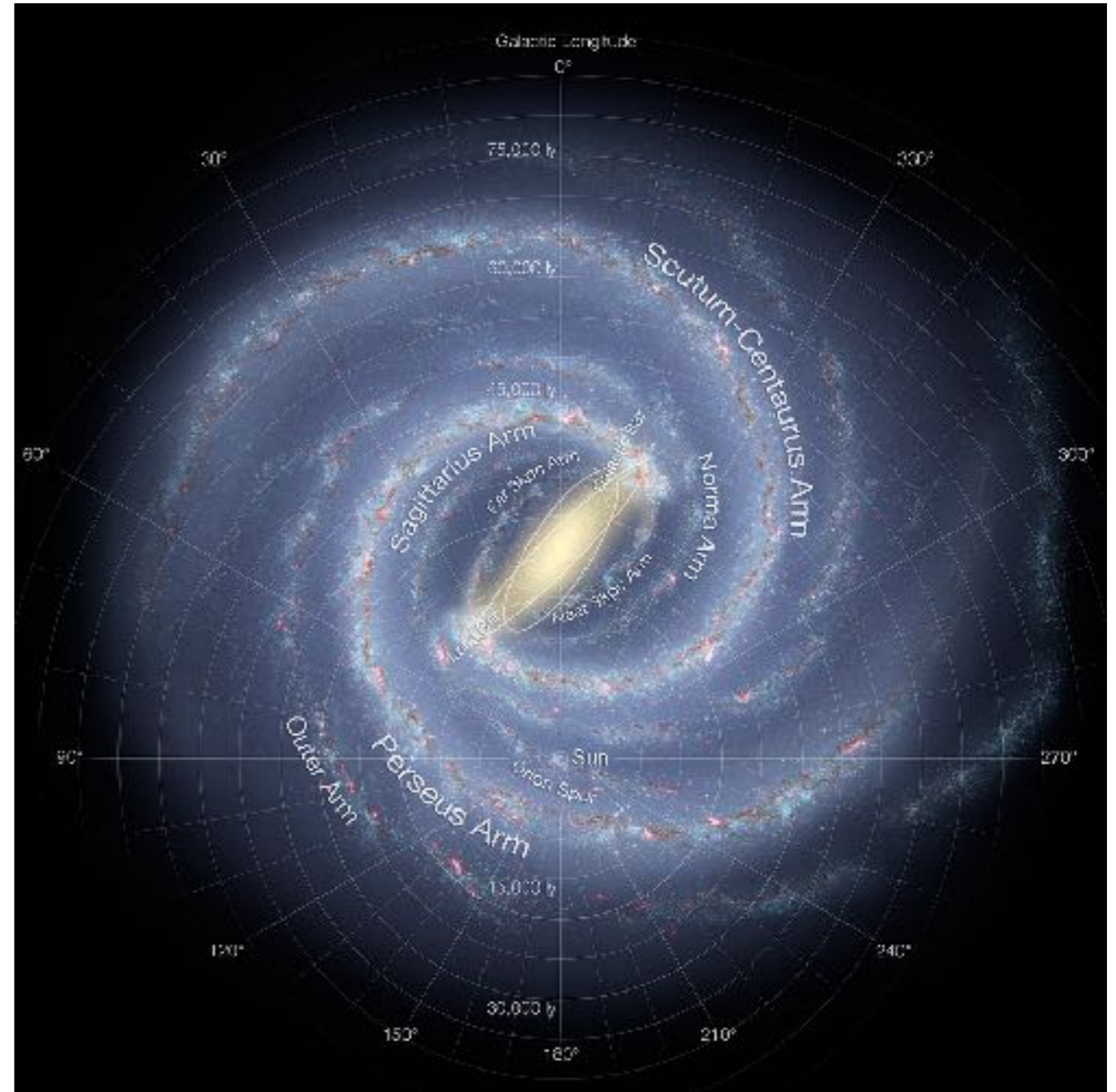
Declination is measured in degrees

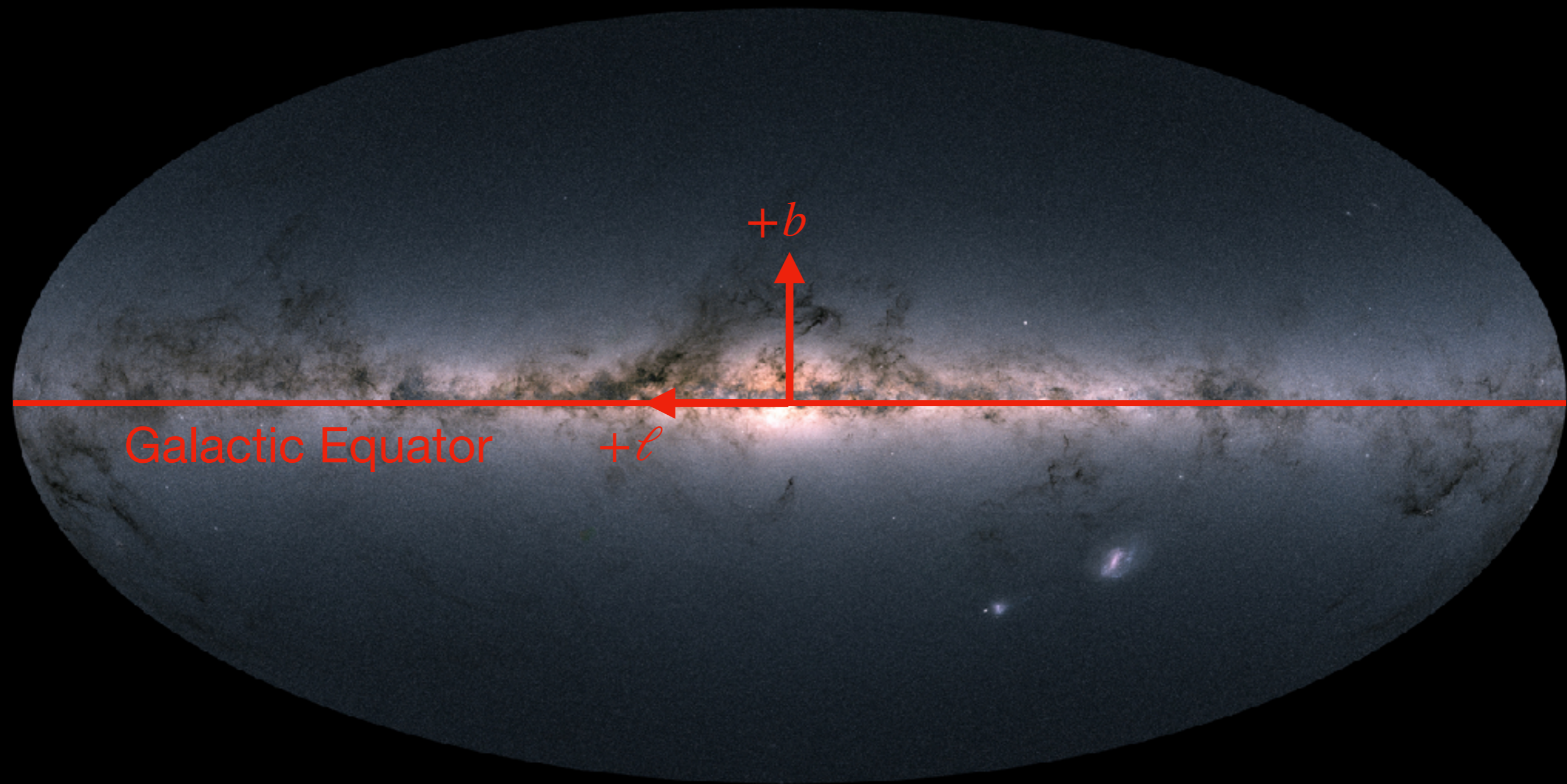
RA can be measured in degrees or units of time (??)



Galactic Coordinates

- ℓ = Galactic longitude
- b = Galactic latitude
- Usually measured in degrees.



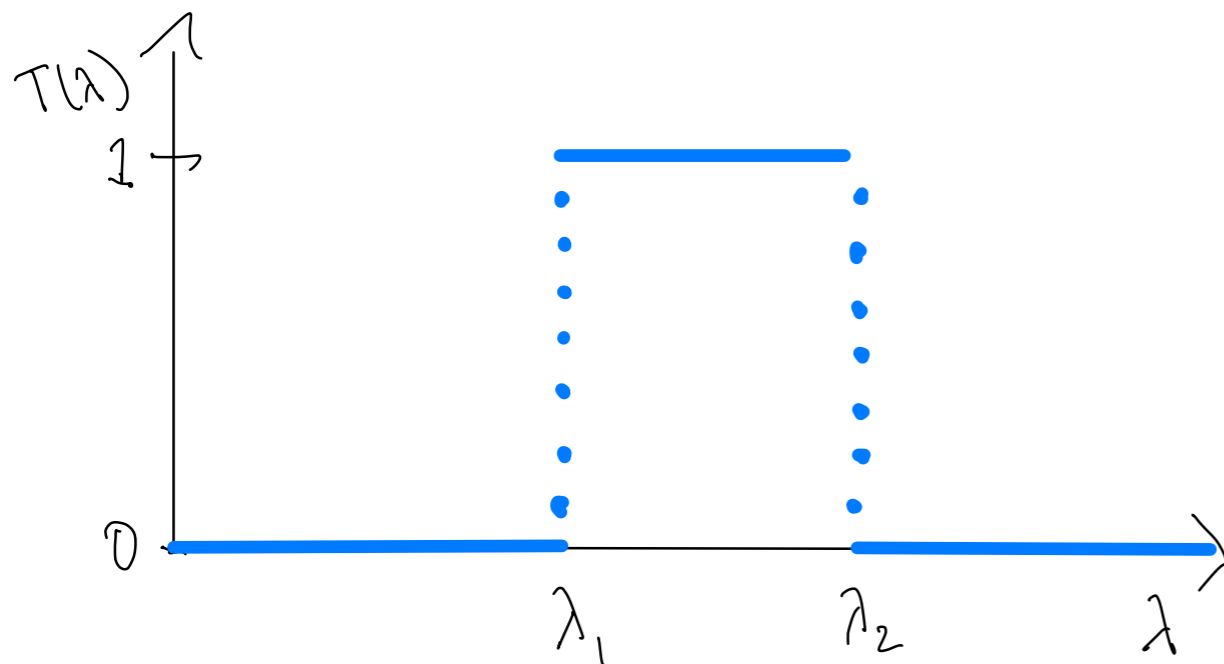


→ GAIA: BRINGING THE GALAXY INTO FOCUS

Quantifying Light

Filters and Colours

- CCD cameras are only sensitive to number of photons not their colour.
- Use filters to limit the range of wavelengths.

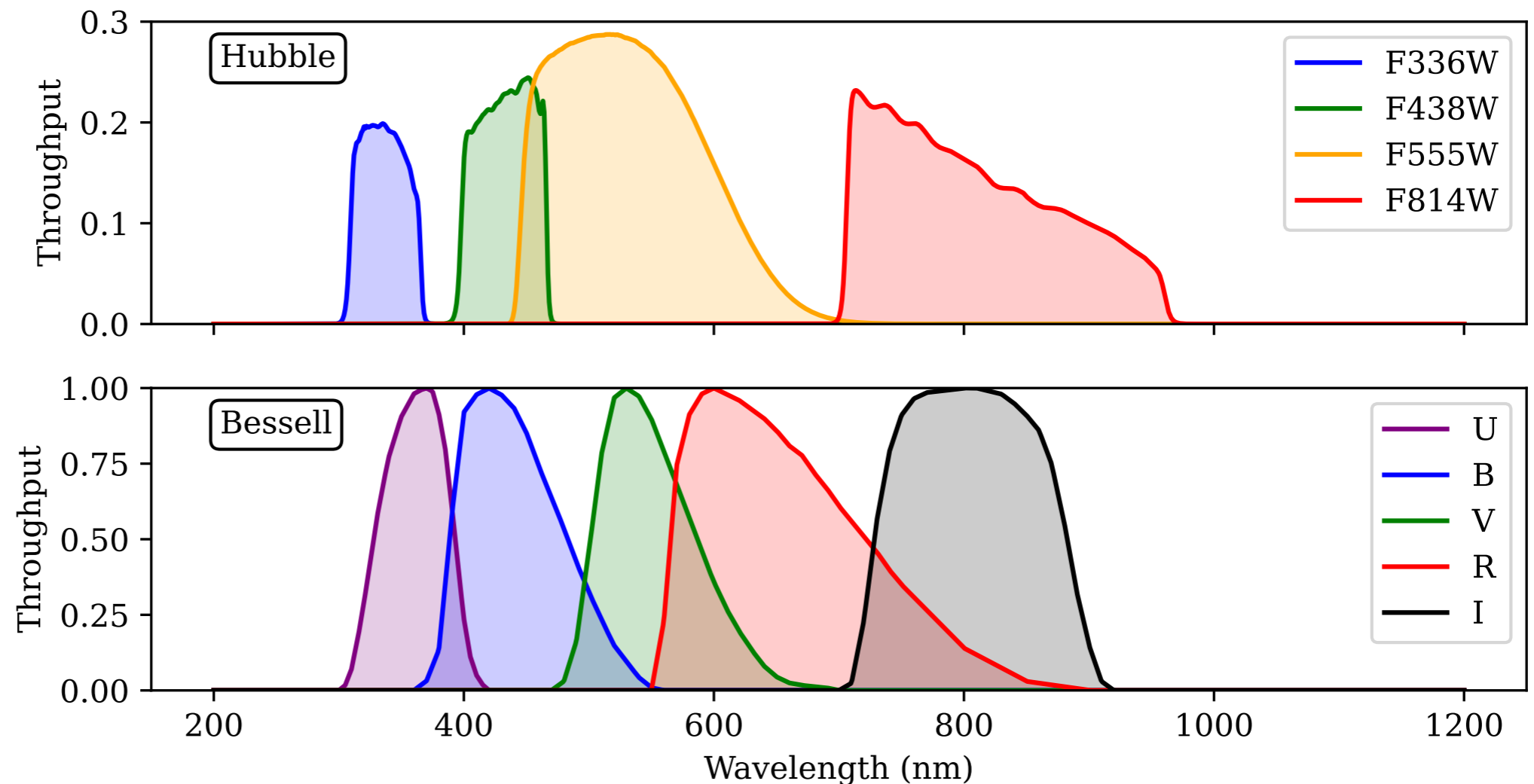


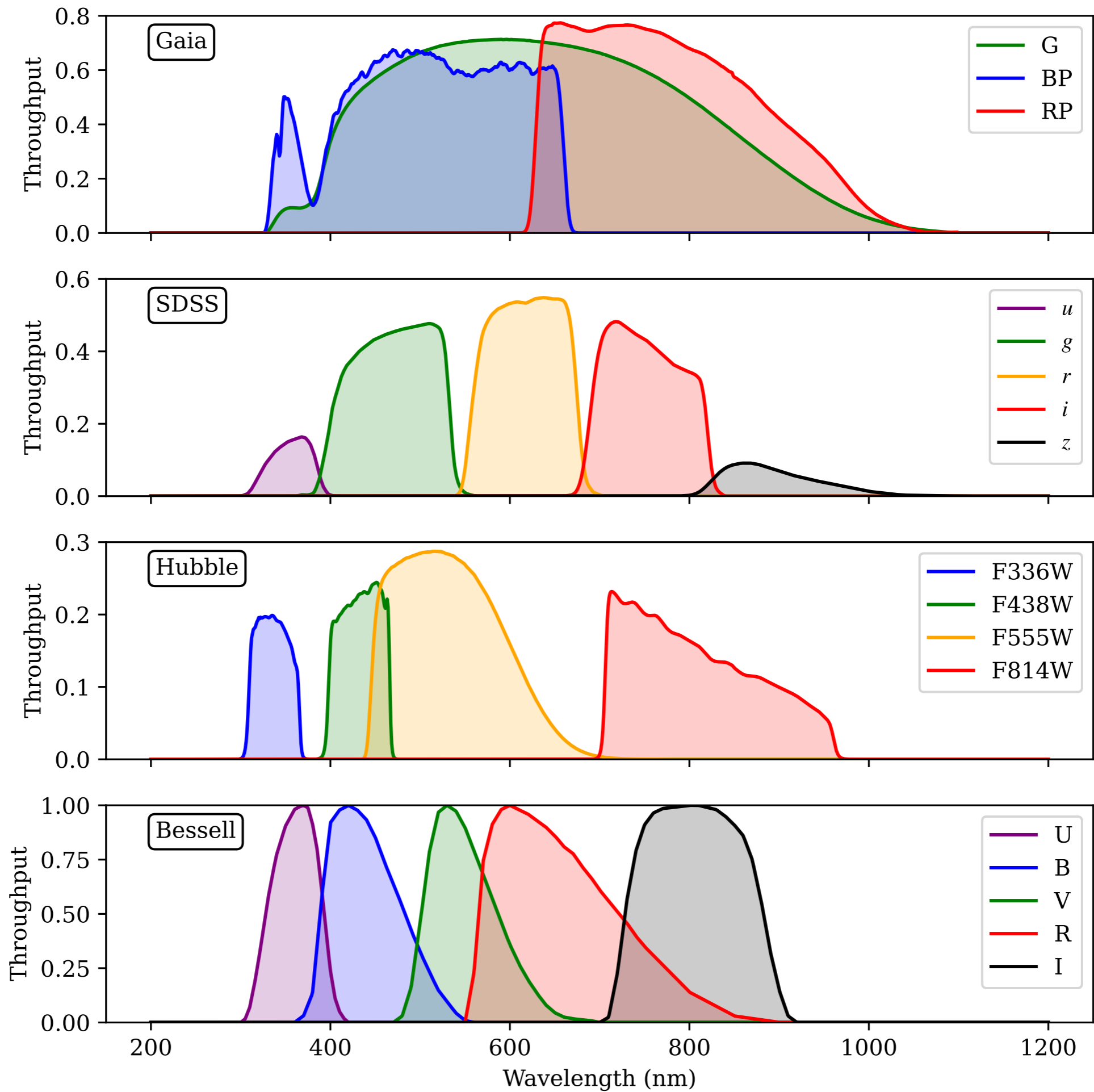
$$\begin{aligned} f_{\text{obs}} &= \int_0^{\infty} T(\lambda) f_{\lambda}(\lambda) d\lambda \\ f_{\text{obs}} &= \int_{\lambda_1}^{\lambda_2} T(\lambda) f_{\lambda}(\lambda) d\lambda \\ &= \int_{\lambda_1}^{\lambda_2} f_{\lambda}(\lambda) d\lambda. \end{aligned}$$

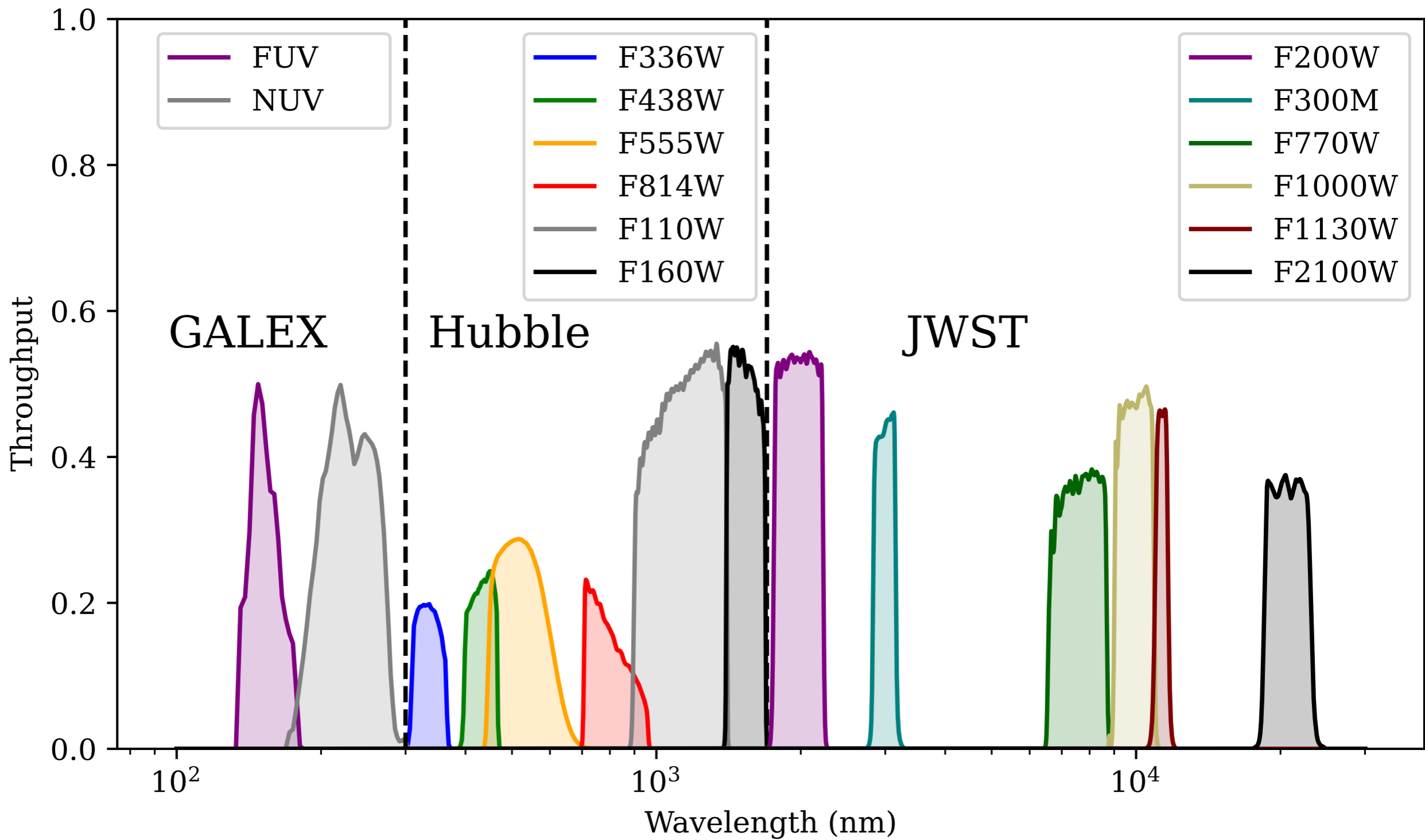
Quantifying Light

Filters and Colours

- Actual filters are more complicated
- Filters have standard names







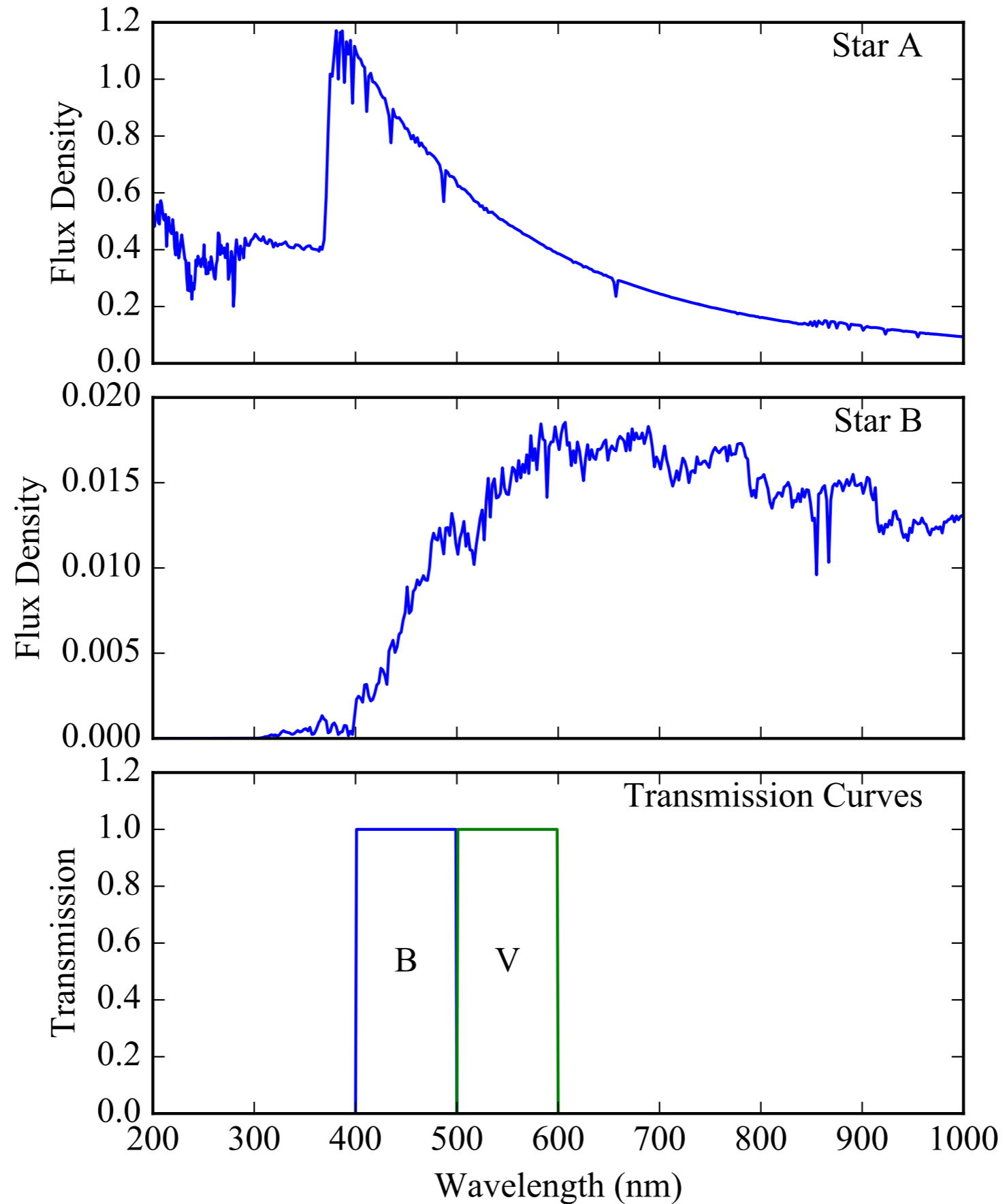
Quantifying Light

Filters and Colours

- A *colour* or *colour index* is the difference between the fluxes measured in two filters

$$g' - r' = -2.5 \log_{10} \left(\frac{f_{\text{obs},g'}}{f_{\text{obs},r'}} \right) = -2.5 \log_{10} \left(\frac{\int_0^\infty T_{g'}(\lambda) f_\lambda(\lambda) d\lambda}{\int_0^\infty T_{r'}(\lambda) f_\lambda(\lambda) d\lambda} \right)$$

Example: estimate the $B-V$ colour index of Star A.

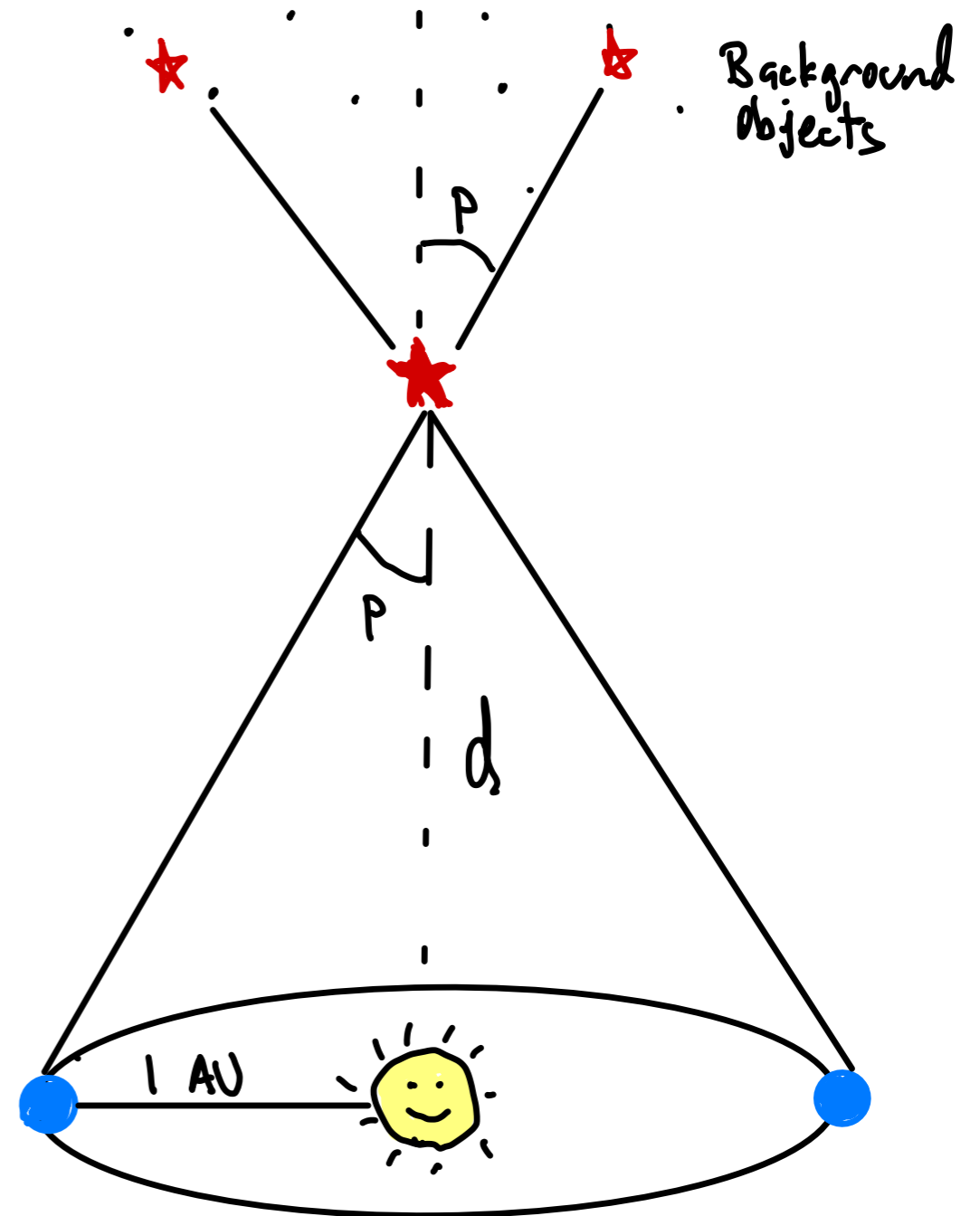


Parallax

Apparent motion of a nearby object with respect to a background objects.

Parallax tells us the **distance** to objects

$$d = \frac{1 \text{ AU}}{\tan p} \approx \frac{1 \text{ AU}}{p}$$



Proper Motion

Motion of a star with respect to more distant background stars

Caused by stars actually moving through space



Barnard's Star
Image from S. Quirk; Public Domain

Proper motion

Proper motion is in contrast with parallax motion.

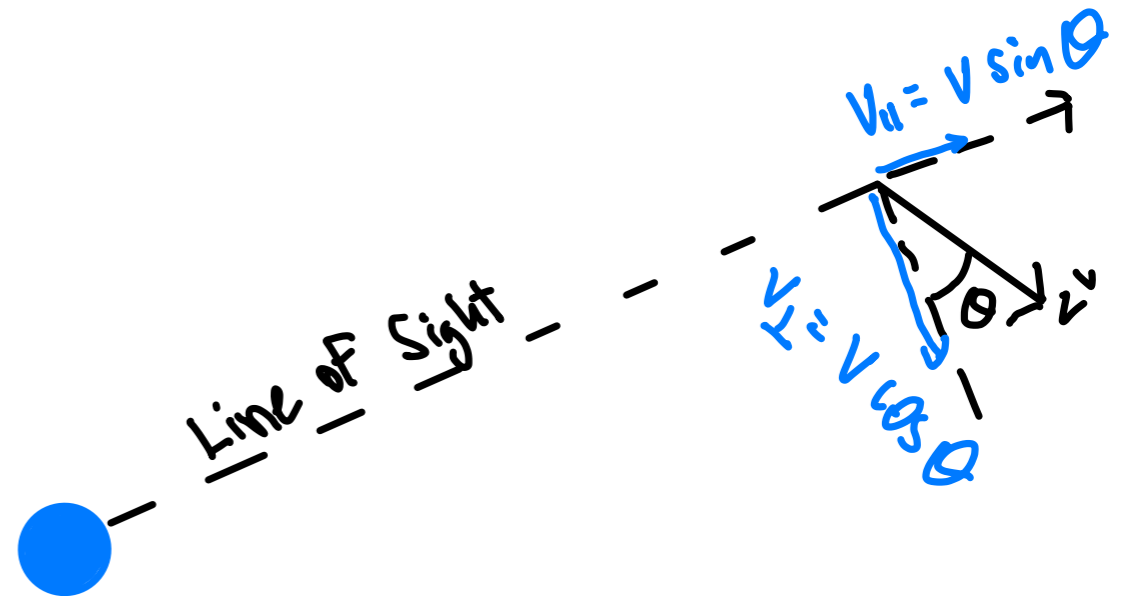
Actual change in coordinates because of motion of stars.

Measured in angular speed.

$$\boldsymbol{\mu} = (\mu_{\alpha} \cos \delta, \mu_{\delta})$$

cos(dec) because of longitude line convergence

$$\left(\frac{v_{\perp}}{\text{km s}^{-1}} \right) = 4.74 \left(\frac{d}{1 \text{ pc}} \right) \left(\frac{|\boldsymbol{\mu}|}{1 \text{ ''/yr}} \right).$$



Radial velocities

Measure the “radial”
velocity of sources from
lines in a stellar spectrum:

$$\frac{v_r}{c} = \frac{\lambda_{\text{obs}} - \lambda_{\text{rest}}}{\lambda_{\text{rest}}}$$

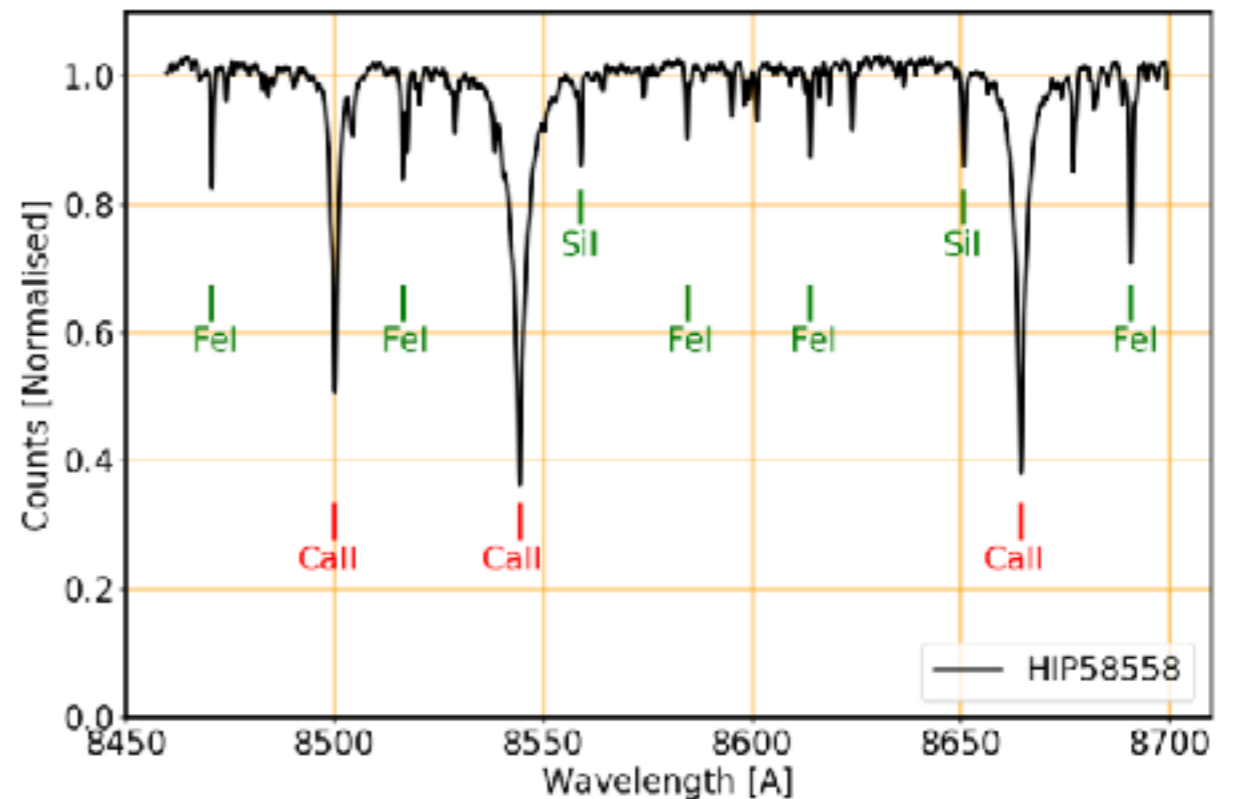


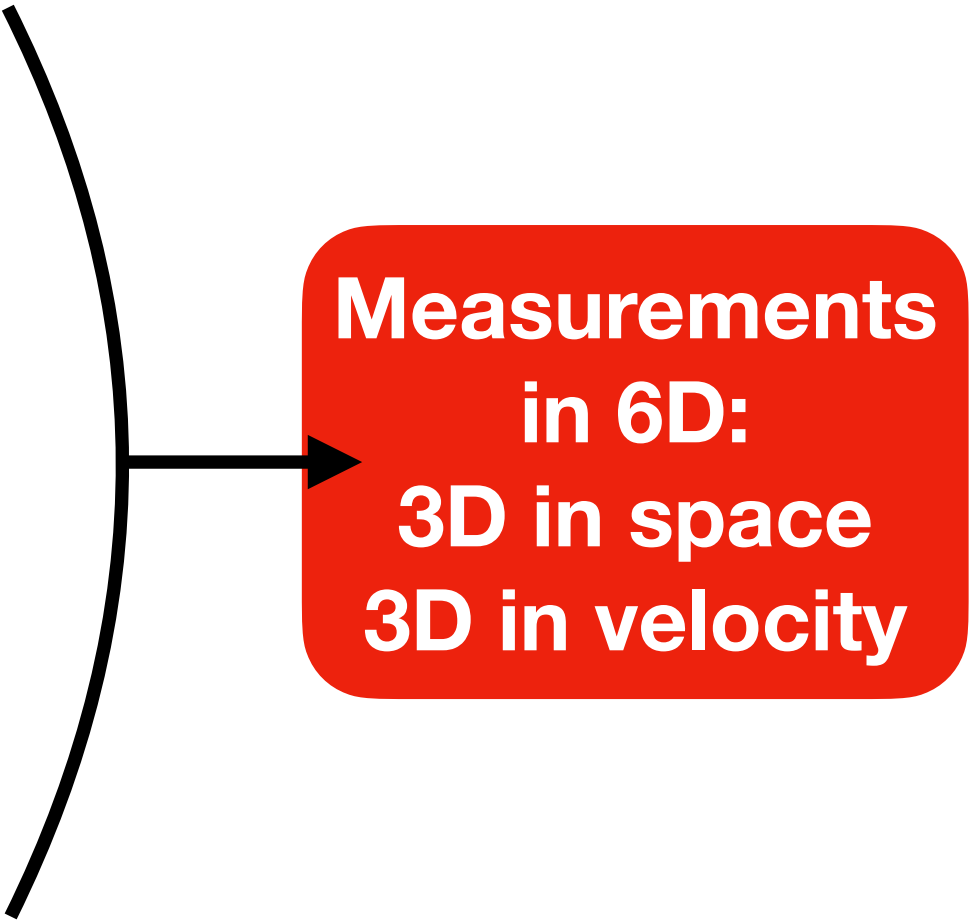
Fig. 1: RVS spectrum of the star HIP 58558.

From Gaia Data Release 2 by Katz et al. (2018)

Gaia Measurements

For $>10^9$ objects, Gaia precisely measures:

- Positions (Right Ascension / Declination)
- Brightnesses in three “colours”
- Stellar *parallax*
- *Proper motions*
- Radial velocities



**Measurements
in 6D:
3D in space
3D in velocity**

All measurements not available for all objects!

→ HOW MANY STARS WILL THERE BE IN THE SECOND GAIA DATA RELEASE?



<https://glueviz.org>

Glue: multi-dimensional linked-data exploration

Home

Install

Documentation

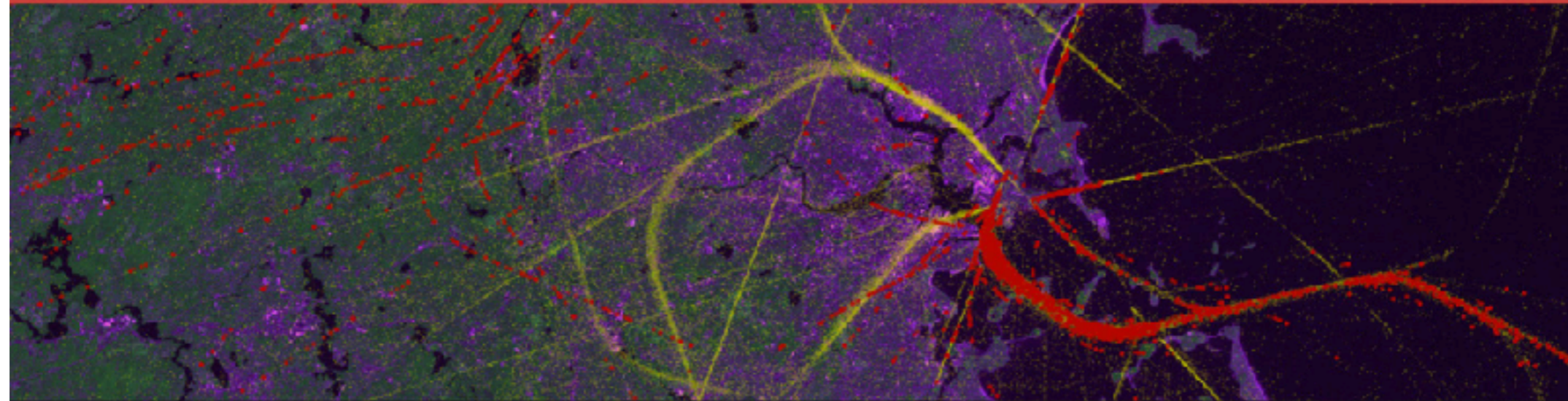
Team

Get involved

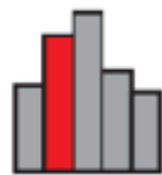
Plugins

glue-con events

Consulting services



Glue is an open-source Python library to explore relationships within and between related datasets



Linked Visualizations



Flexible linking across data



Full scripting capability

Data on Google Drive

https://drive.google.com/drive/folders/1x9bWCXdzw1Aq8eB_y5o2ft2XsK0Geyw1?usp=share_link





Image credit: NASA, ESA,
AURA/Caltech, Palomar
Observatory

Astronomy Data types

Catalogues - Spreadsheet-like data showing objects with measured properties

Images - Astronomical images plus “metadata” which describes what’s in the image

Formats:

FITS - Flexible Image Transport System

csv - Comma separated values

Glue Use

Follow along at home!!

'source_id' — Gaia source identifier
'mg' — Absolute magnitude in the Gaia G band
'phot_g_mean_mag' — Apparent magnitude in the Gaia G band
'bp_rp' — Gaia Blue-Red colour
'parallax' — Parallax angle in milliarcseconds
'parallax_error' — Uncertainty in the parallax
'ra' — Right Ascension
'dec' — Declination
'pmra' — Proper motion in the RA direction
'pmdec' — Proper motion in the Dec direction
'pmra_error' — Uncertainty in pmra
'pmdec_error' — Uncertainty in pmdec
'radial_velocity' — Radial velocity of star in km/s
'radial_velocity_error' — Uncertainty in radial velocity
'e_bp_min_rp_val' — line-of-sight reddening $E(BP-RP)$, a measure of dust
'a_g_val' — Dust extinction in the G band
'l' — Galactic longitude
'b' — Galactic latitude
'ecl_lat' — Ecliptic latitude
'ecl_lon' — Ecliptic longitude

Gaia Data

Exercise 1

Use the Glue software program to identify the Pleiades star cluster using the Gaia satellite data and proper motion selection. Make a histogram of the parallax of stars in this proper motion selected sample.

Calculate the distance to the Pleiades given the peak in the histogram.

Stars

A “black box” set of physics

- Basic stellar structure and physical processes
- Observed stellar properties
- The HR Diagram
- Stellar winds and supernovae
- Evolutionary tracks

Key properties of stars

1. Initial mass (range from $0.08 < M/M_{\odot} \lesssim 300$)
2. Chemical composition
Described by mass fractions of:
 X - Hydrogen. Typically 0.72-0.75
 Y - Helium. Typically 0.25-0.26
 Z - “Metals” everything else. Typically 0-0.02
3. Binary / multiple stellar system
4. Initial angular momentum

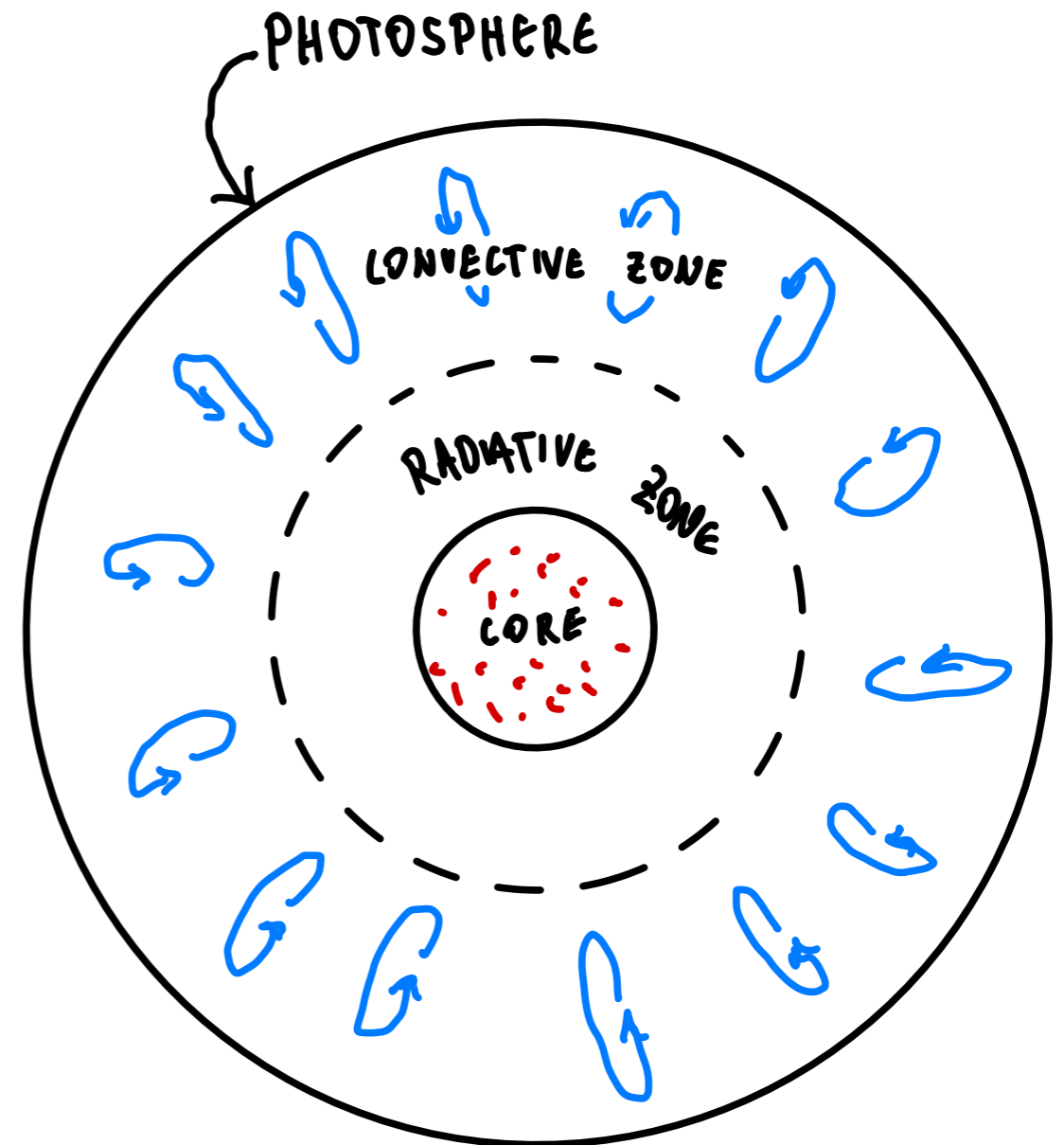
Stellar anatomy

Stars - nearly spherical gas structures, generates energy through nuclear fusion.

Core - central fusion engine

Envelope - Outer layers

Photosphere - “surface” of star where light flows out



Essential Stellar Physics

Hydrostatic equilibrium

Force balance between *pressure gradient* and *self-gravity* is dominant physics in star

Required central pressure to support against gravity:

$$P \sim \frac{GM^2}{R^4}$$

Pressure provided by:

1. Gas pressure
2. Radiation pressure
3. Degeneracy pressure

Essential Stellar Physics

Equations of state

Gas pressure (perfect gas law)

$$P_{\text{gas}} = nkT \quad (k = 1.38 \times 10^{-23} \text{ J/K})$$

Radiation pressure

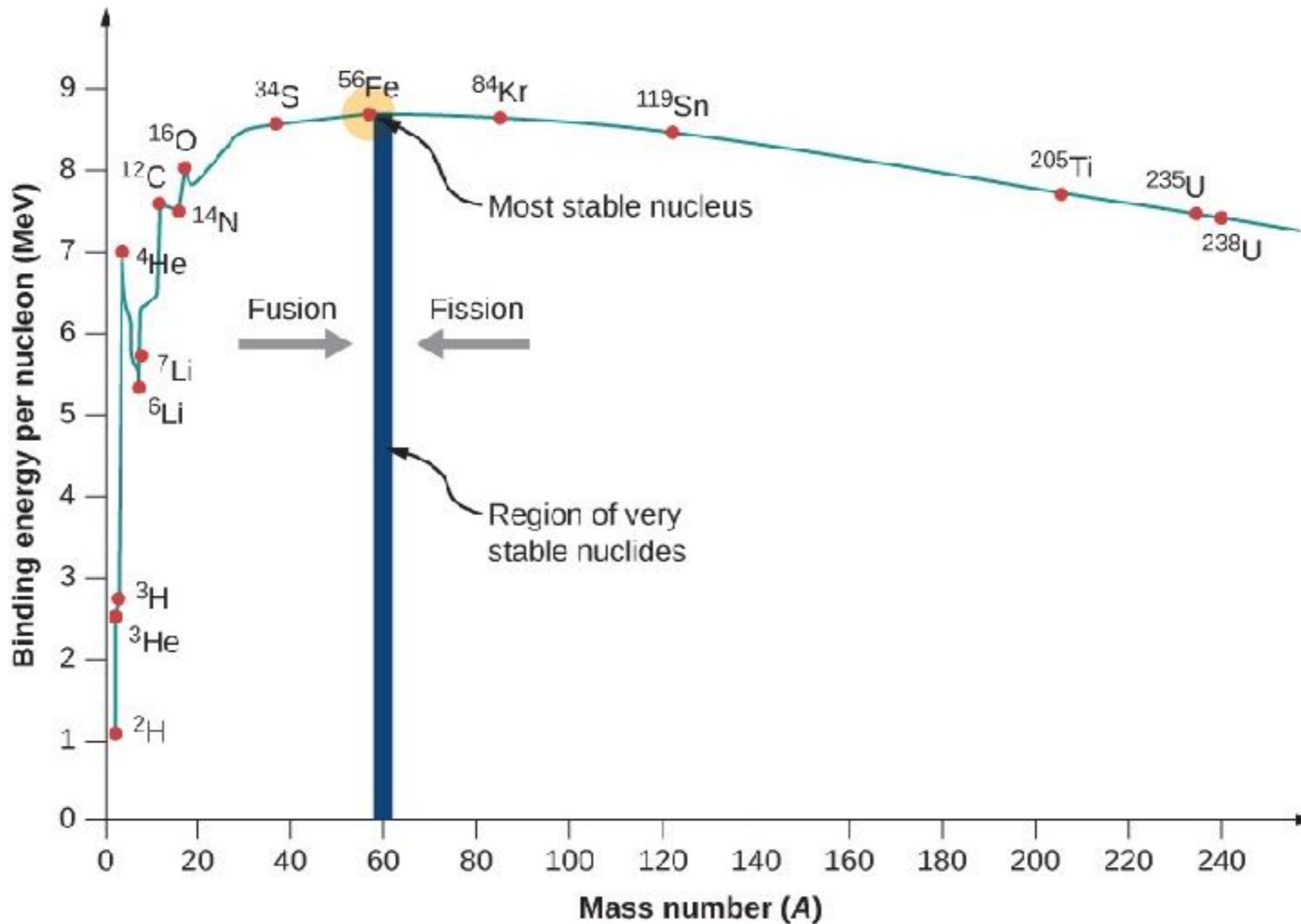
$$P_{\text{rad}} = \frac{4}{3} \frac{\sigma_{\text{SB}} T^4}{c} \quad (\sigma_{\text{SB}} = 5.67 \times 10^{-8} \text{ W/m}^2/\text{K}^4)$$

Degeneracy Pressure

$$P_{\text{deg}} = K_1 \left(\frac{\rho}{\text{kg m}^{-3}} \right)^{5/3} \quad \text{where } \rho \text{ is the mass density}$$

Essential Stellar Physics

Nuclear Fusion

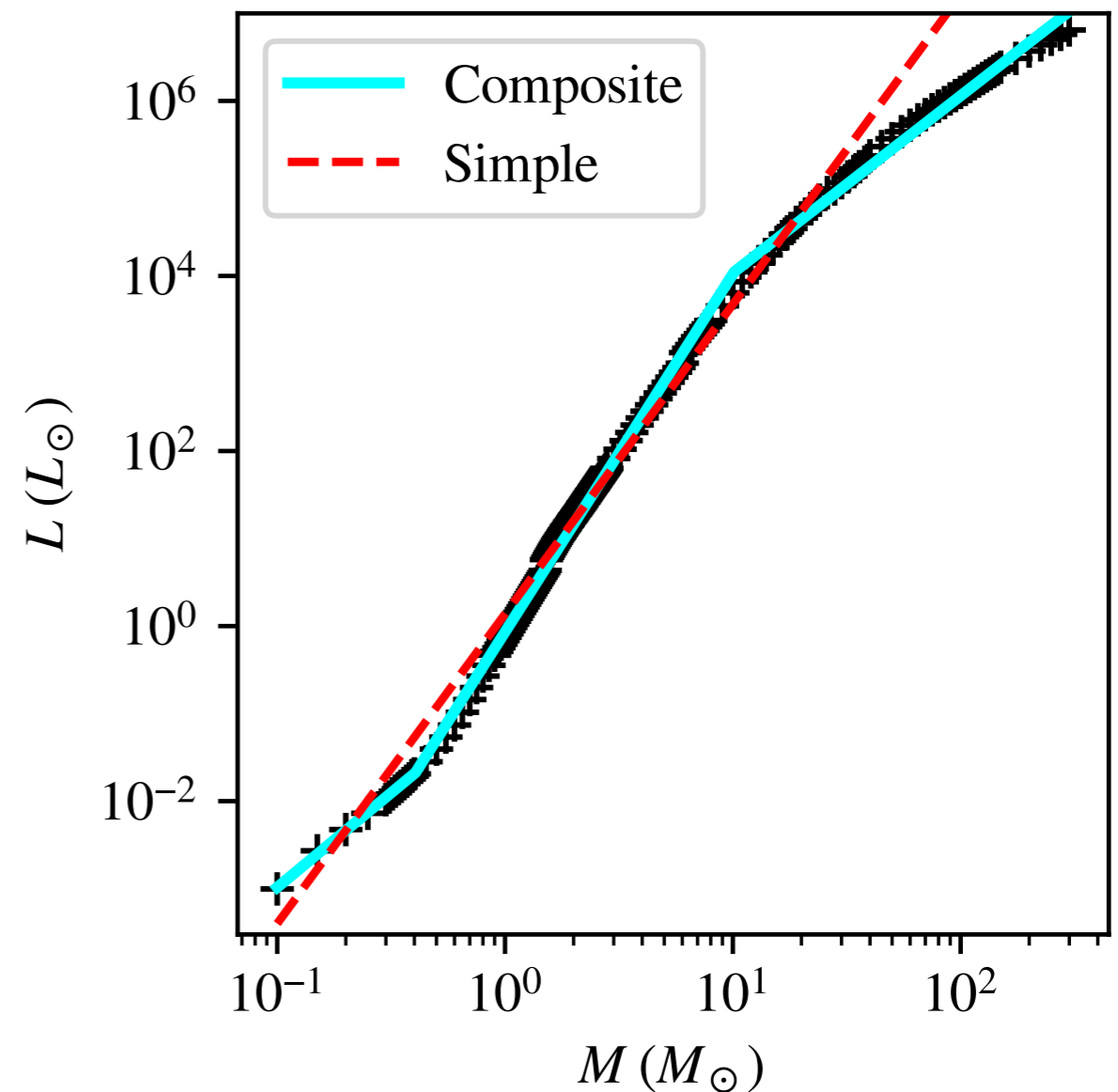


Observed Stellar Properties

Mass-Luminosity relationship

Main sequence stars
(hydrogen fusion in
core) follow
approximately:

$$L = 1 L_{\odot} \left(\frac{M}{M_{\odot}} \right)^{3.5}$$

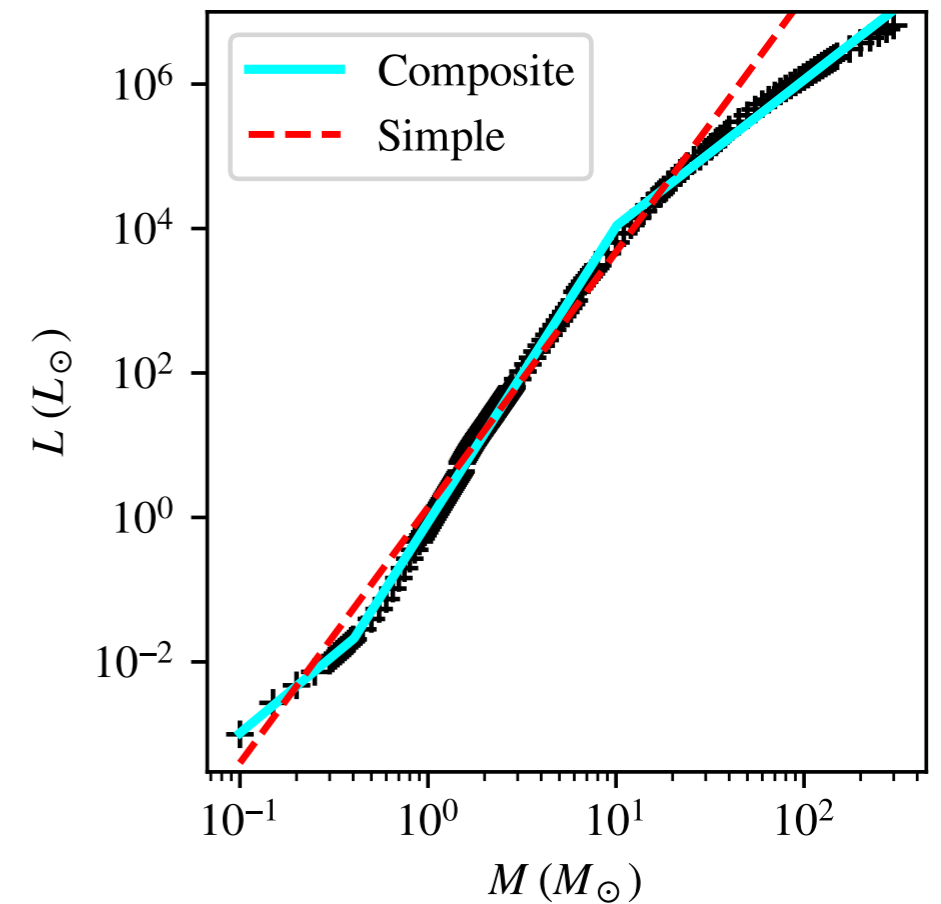


Observed Stellar Properties

Mass-Luminosity relationship

Fancier “composite”
version

$$\frac{L}{L_{\odot}} = \begin{cases} 0.16(M/M_{\odot})^{2.1} & ; \quad M/M_{\odot} < 0.4 \\ 1.00(M/M_{\odot})^{4.1} & ; \quad 0.4 < M/M_{\odot} < 10 \\ 126.(M/M_{\odot})^{2.0} & ; \quad 10 < M/M_{\odot} \end{cases}$$



Observed Stellar Properties

Implied stellar lifetimes

Mass-luminosity relationship implies main sequence lifetime of stars

$$\tau_{\text{MS}} = \tau_{\text{MS},\odot} \left(\frac{M}{M_{\odot}} \right) \left(\frac{L}{L_{\odot}} \right)^{-1} = 10^{10} \text{ yr} \left(\frac{M}{M_{\odot}} \right)^{-2.5}$$

High mass stars have short lifetimes.

- Shortest lifetime is ~ 3 Myr.
- All stars with $M < 0.9 M_{\odot}$ have not evolved off the main sequence in the age of the Universe (14 Gyr)

Observed Stellar Properties

Stellar spectra

Classified by the lines in the spectrum.

Stellar spectral types

O B A F G K M L T Y

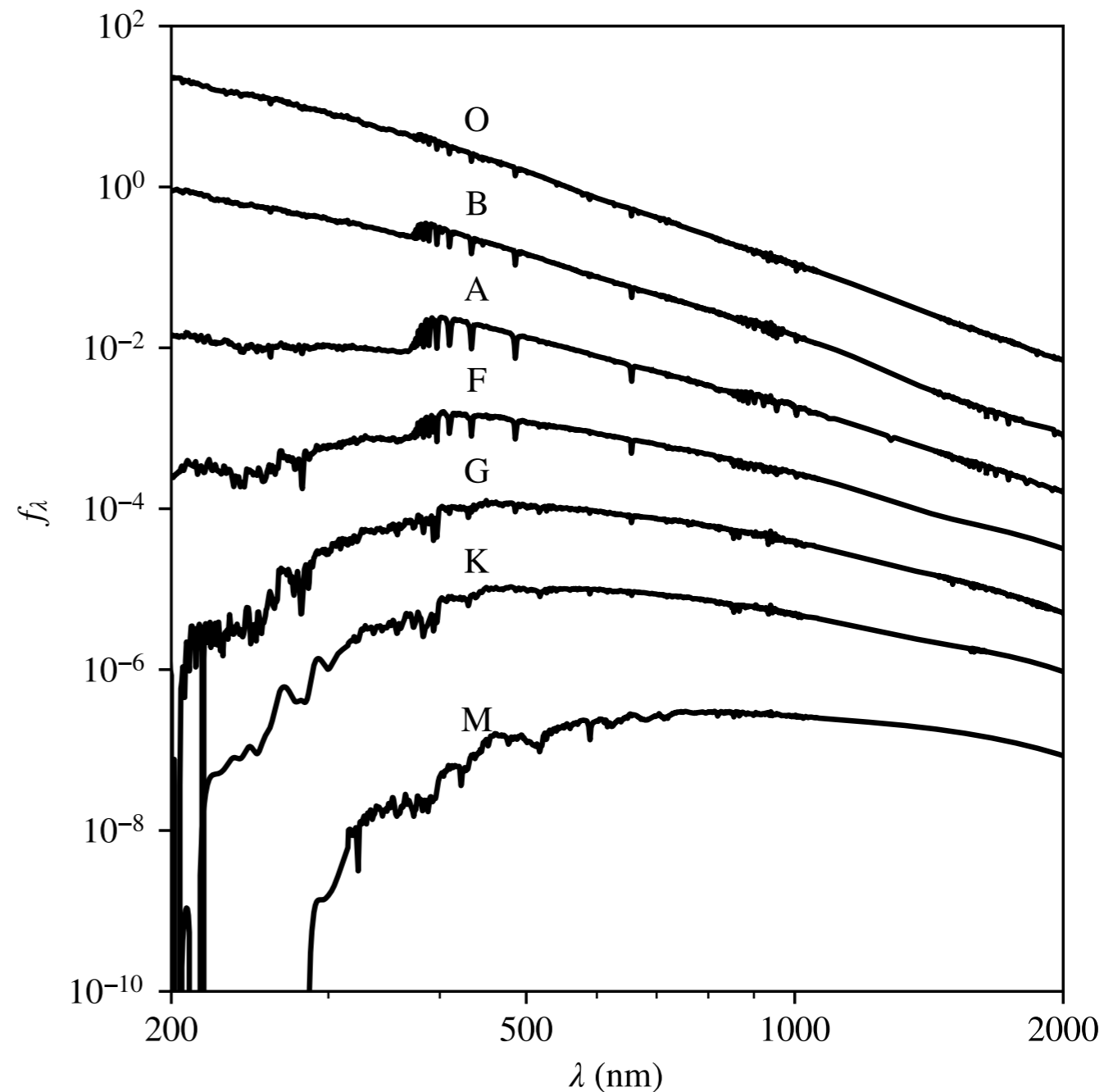
F9 G0 G1 G2 G9 K0

T_{eff} order:

O = hottest star

M = coolest star

L, T, Y = brown dwarfs



Observed Stellar Properties

Stellar spectra

Stellar luminosity classes

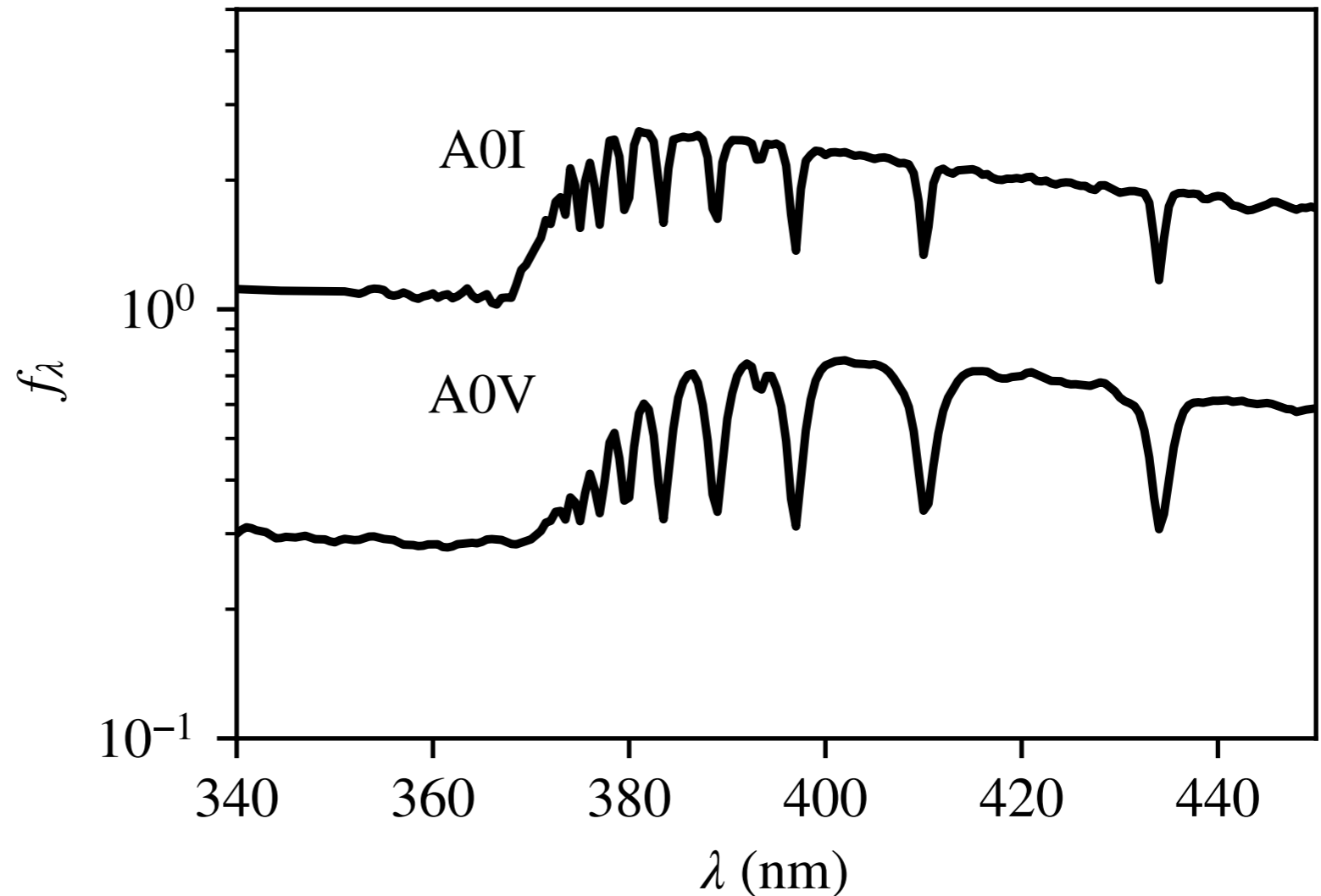
I - Supergiants

II, III - Giants

IV - Subgiants

V - Dwarfs

VI - Subdwarfs



Observed Stellar Properties

Stellar spectra

Stellar luminosity classes

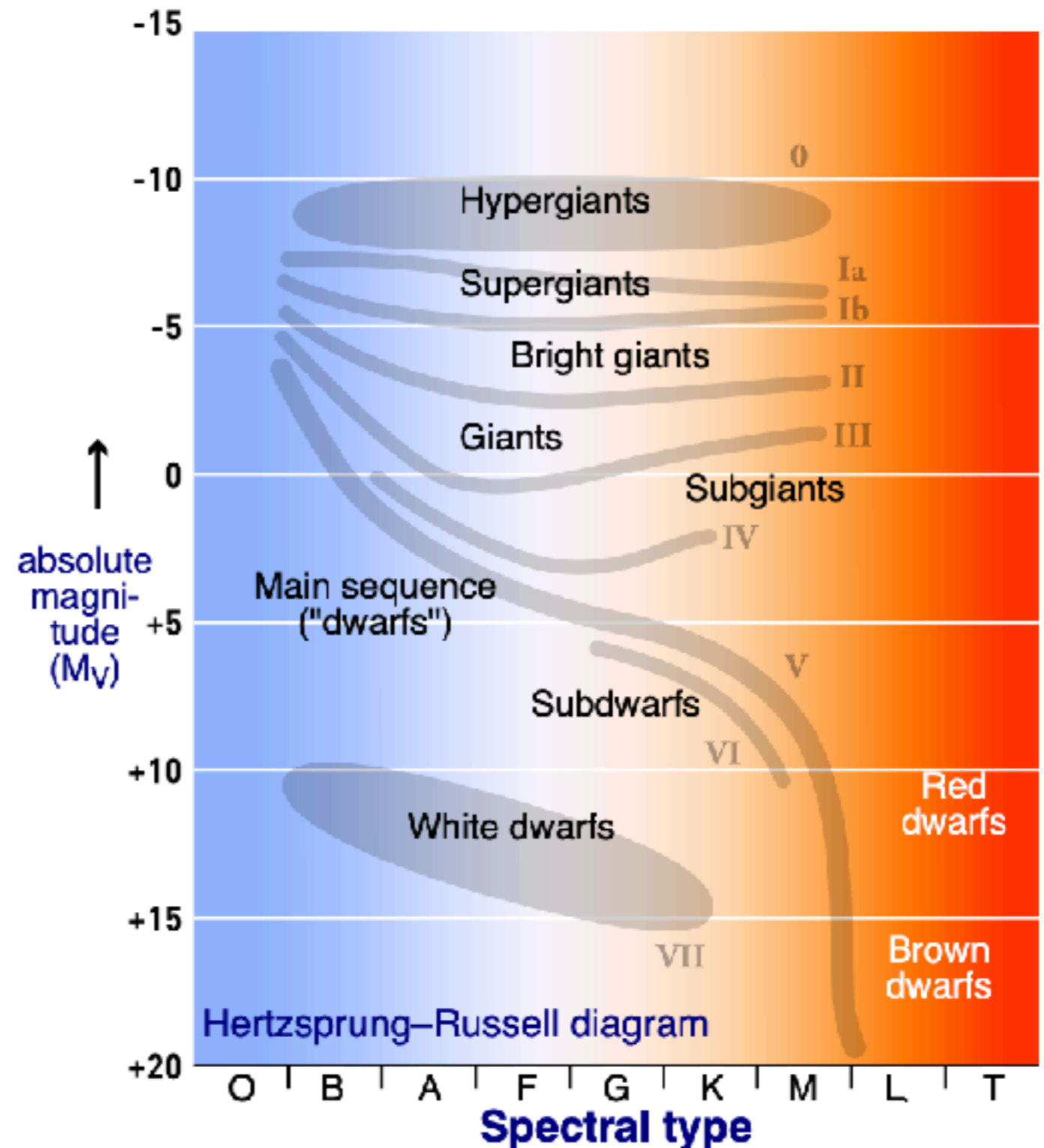
I - Supergiants

II, III - Giants

IV - Subgiants

V - Dwarfs

VI - Subdwarfs



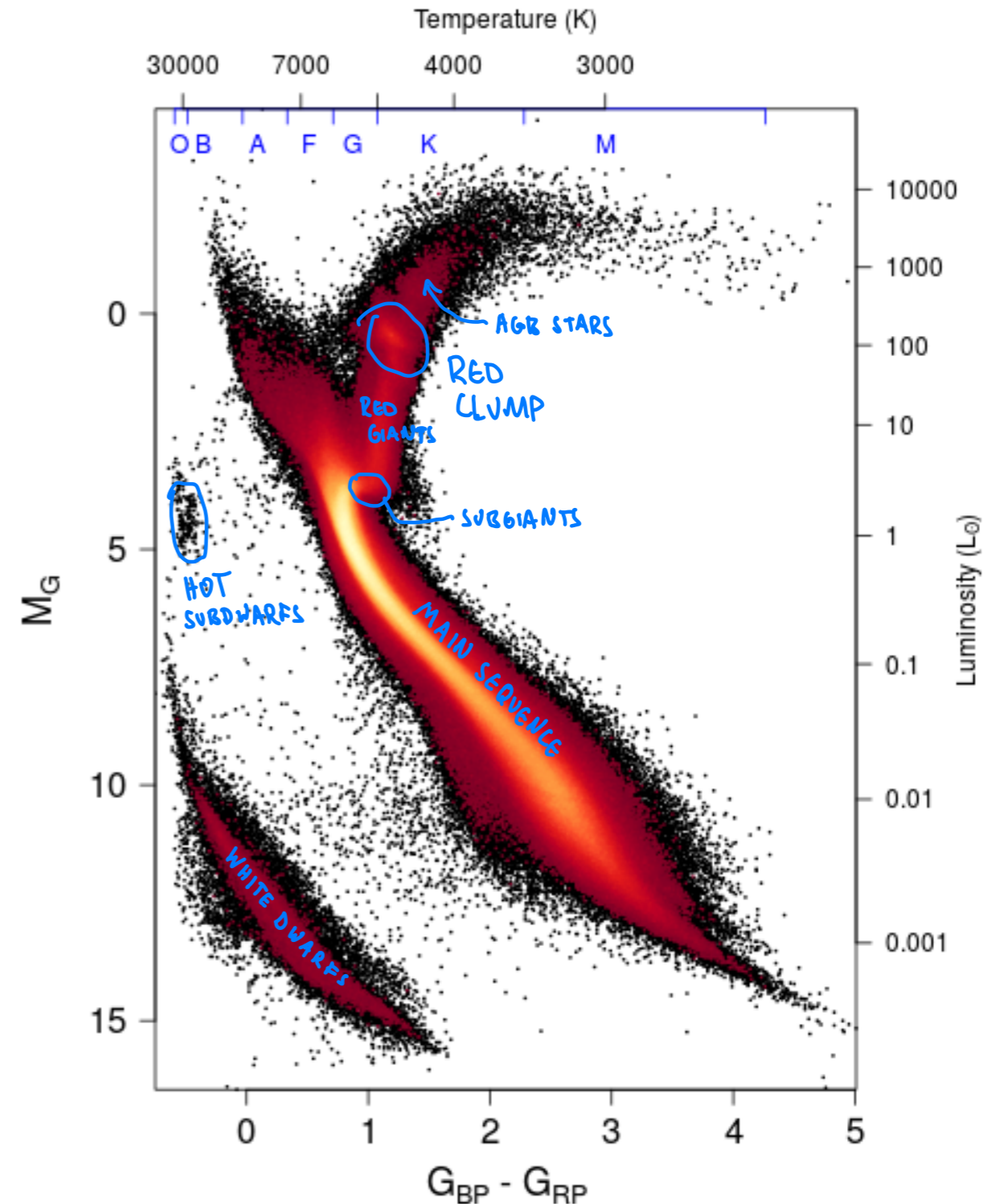
Observed Stellar Properties

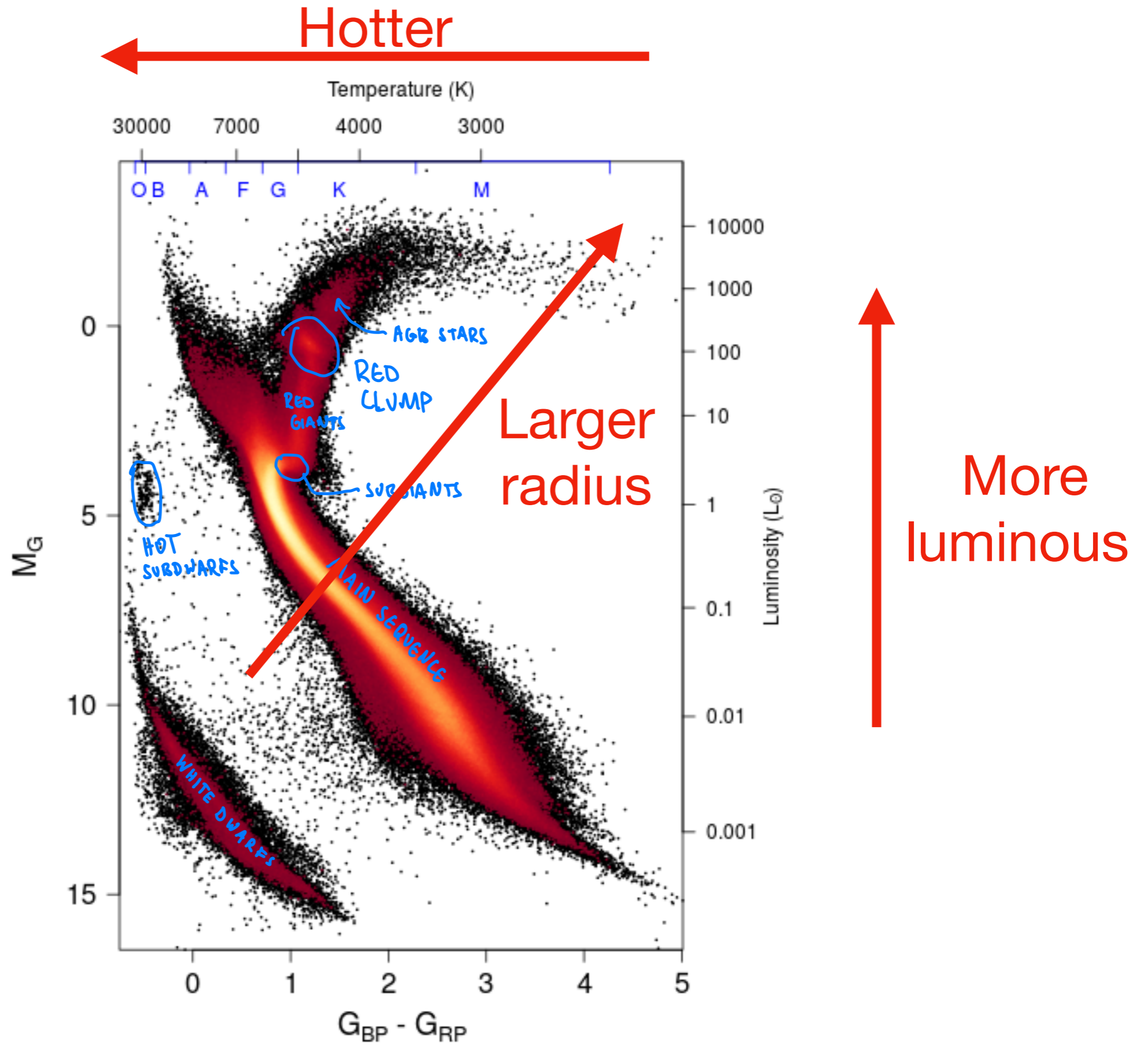
The Hertzsprung-Russell Diagram

Plot of Luminosity / absolute magnitude vs colour index / temperature

Identify groups of stars and classify them

HR magic - groups of stars share common physical properties.





Gaia Data

Exercise 2

Select a cluster from the open cluster Gaia data.

Calculate the average distance to this cluster using the data in the Gaia file.

Make an observational HR diagram of the cluster using Glue.

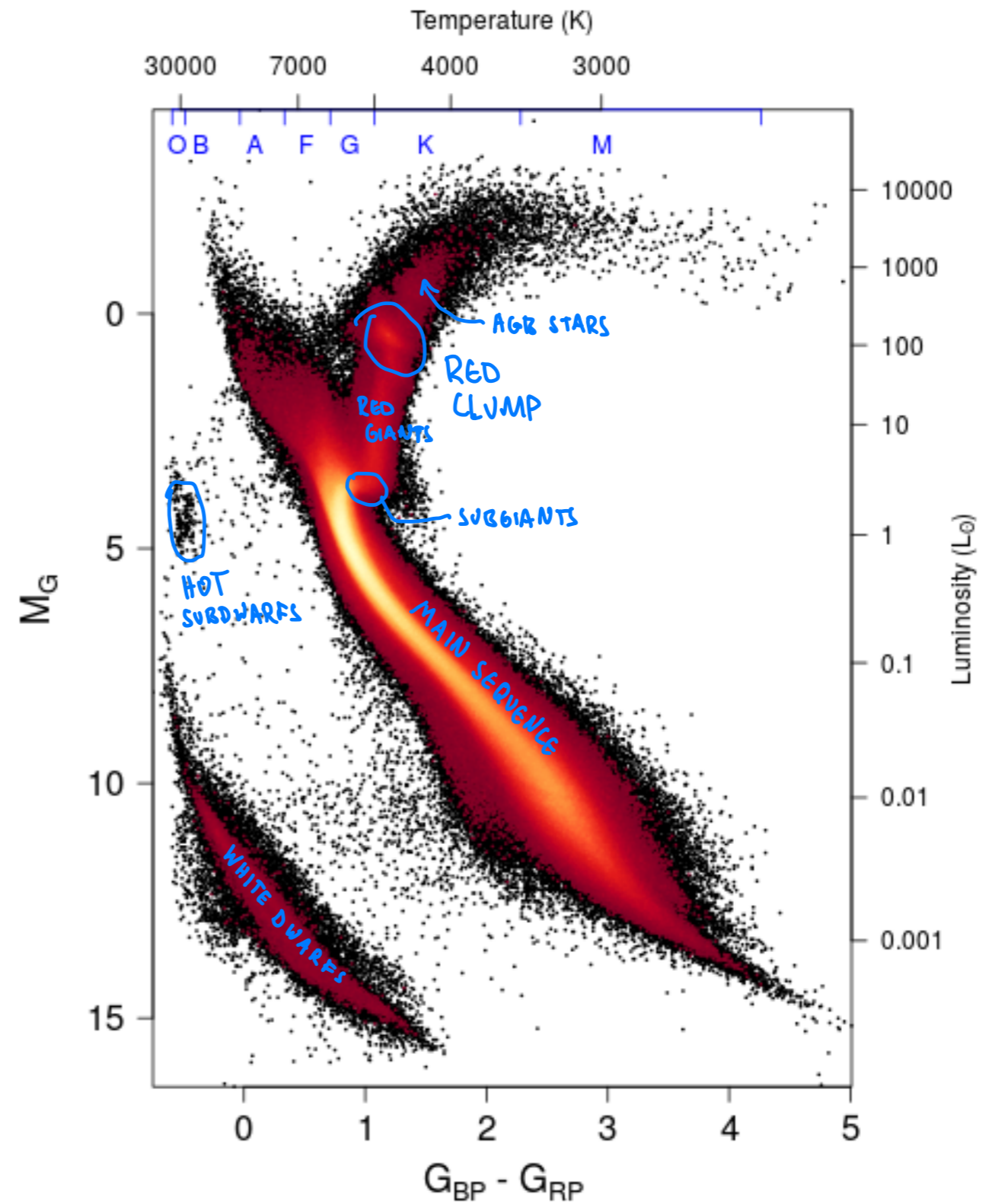
Identify:

- Main sequence stars
- The main sequence turnoff
- A binary star system
- Red giants
- White dwarfs

Stellar populations

The Goal

“Resolved”



Stellar Populations

The ingredients

- **Initial mass function** - the PDF of stellar masses from the star formation process
- **Metallicity of formed stars** - The enrichment process
- **Companion frequency** - Fraction of stars in binary / multiple systems with other stars or brown dwarfs
- **Star formation history** - Mass of stars formed over time (next time)

The Initial Mass Function

Star Formation

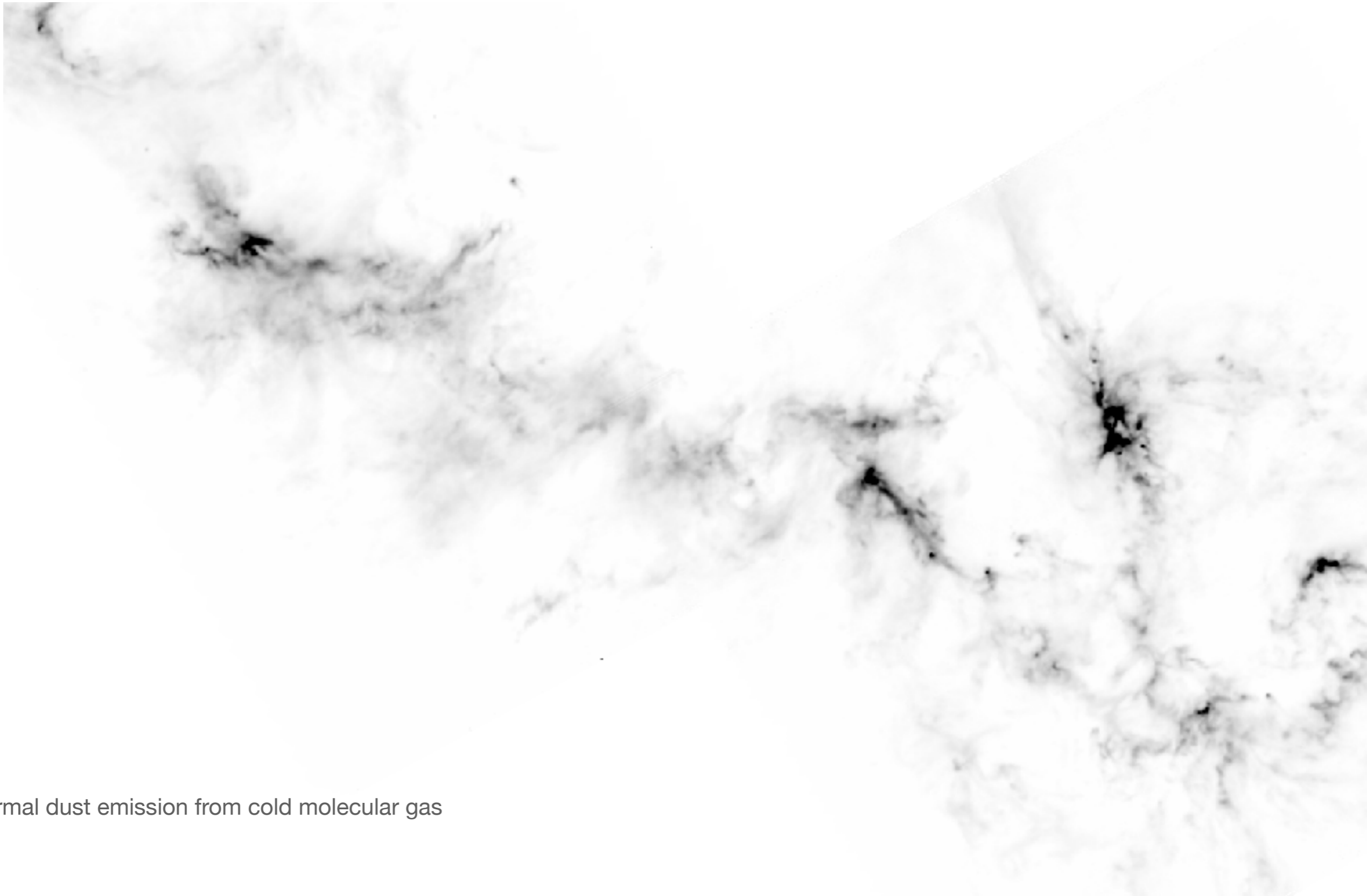
What is the characteristic mass of stars that form?

...Where do stars form?



Image credit: Adam Block and Tim Puckett

Protostars found in gas with $n_{\text{H}_2} \sim 10^8 \text{ m}^{-3}$ and $T = 10 \text{ K}$



Thermal dust emission from cold molecular gas

The Initial Mass Function

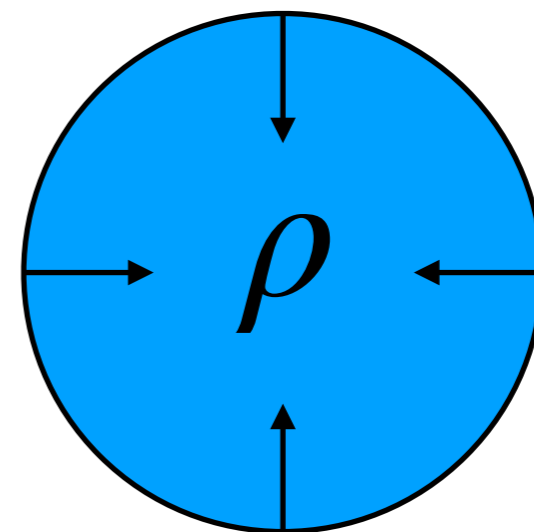
Star Formation

What is the characteristic mass of stars that form?

Dominant forces: pressure tries to resist gravitational collapse.

Set $t_{\text{ff}} = t_{\text{cross}}$, i.e. a free-fall time compared to crossing time. Free fall time for uniform cloud of mass density ρ is

$$t_{\text{ff}} = \sqrt{\frac{3\pi}{32G\rho}}$$



The Initial Mass Function

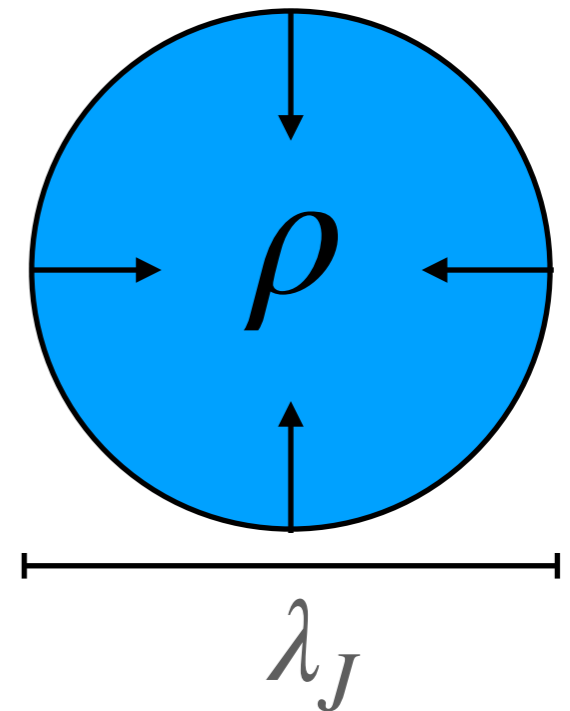
Star Formation

Set $t_{\text{ff}} = t_{\text{cross}}$, i.e. a free-fall time compared to crossing time.

$$t_{\text{ff}} = \sqrt{\frac{3\pi}{32G\rho}}$$

Sound crossing time for a pressure wave is

$$t_{\text{cross}} = \frac{\ell_J}{c_s}; \quad c_s = \sqrt{\frac{kT}{m}}$$



The Initial Mass Function

Star Formation

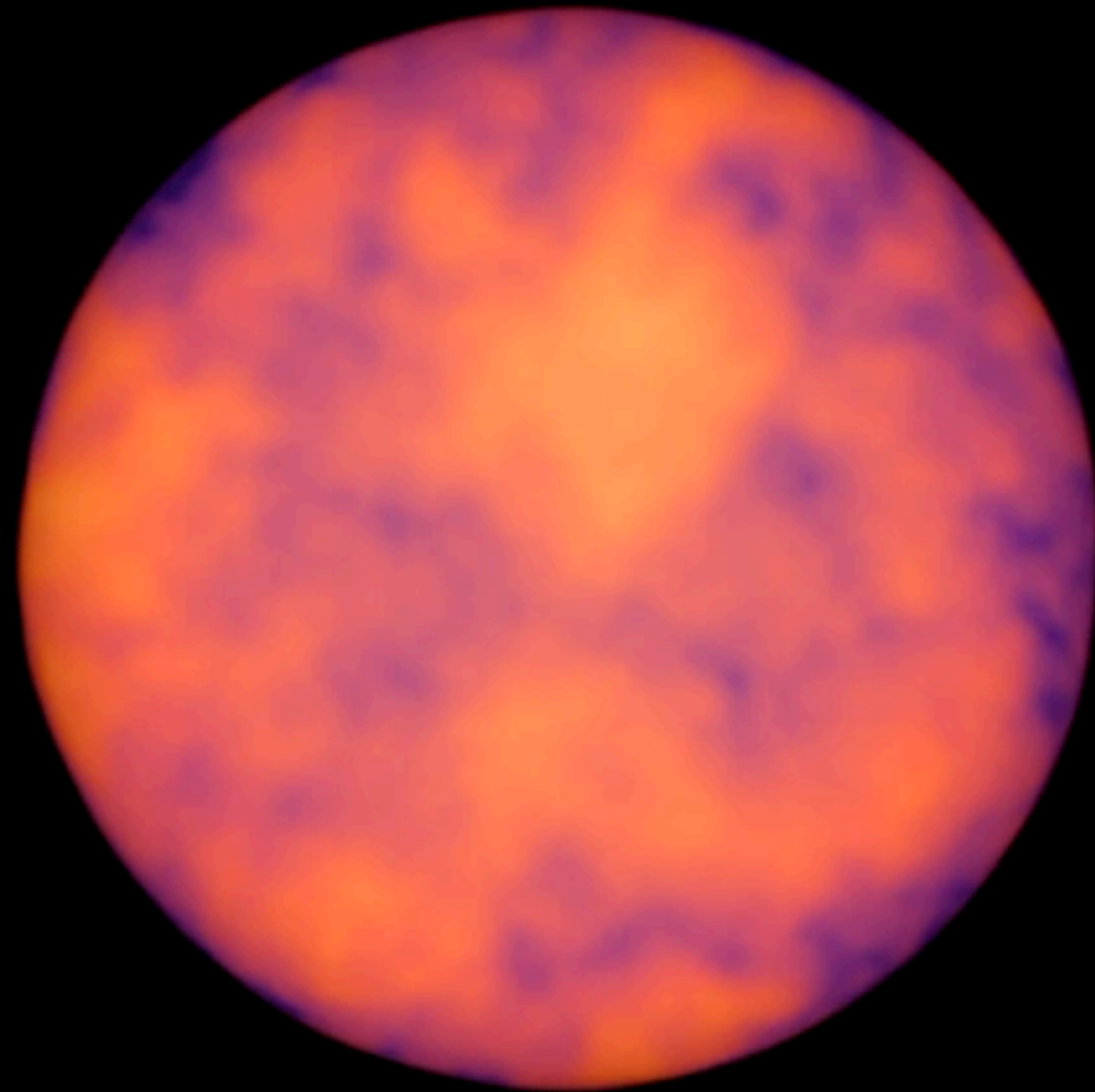
Solve to get λ_J :

$$\ell_J = \left(\frac{3\pi kT}{32Gm\rho} \right)^{1/2}$$

Set $M_J \sim \rho \ell_J^3$ to get the **Jeans mass**:

$$M_J = \frac{\pi^{3/2}}{8} \frac{c_s^3}{G^{3/2} \rho^{1/2}}$$

$$M_J = 6.9 M_{\odot} \left(\frac{T}{10 \text{ K}} \right)^{3/2} \left(\frac{n_{\text{H}_2}}{10^8 \text{ m}^{-3}} \right)^{-1/2}$$



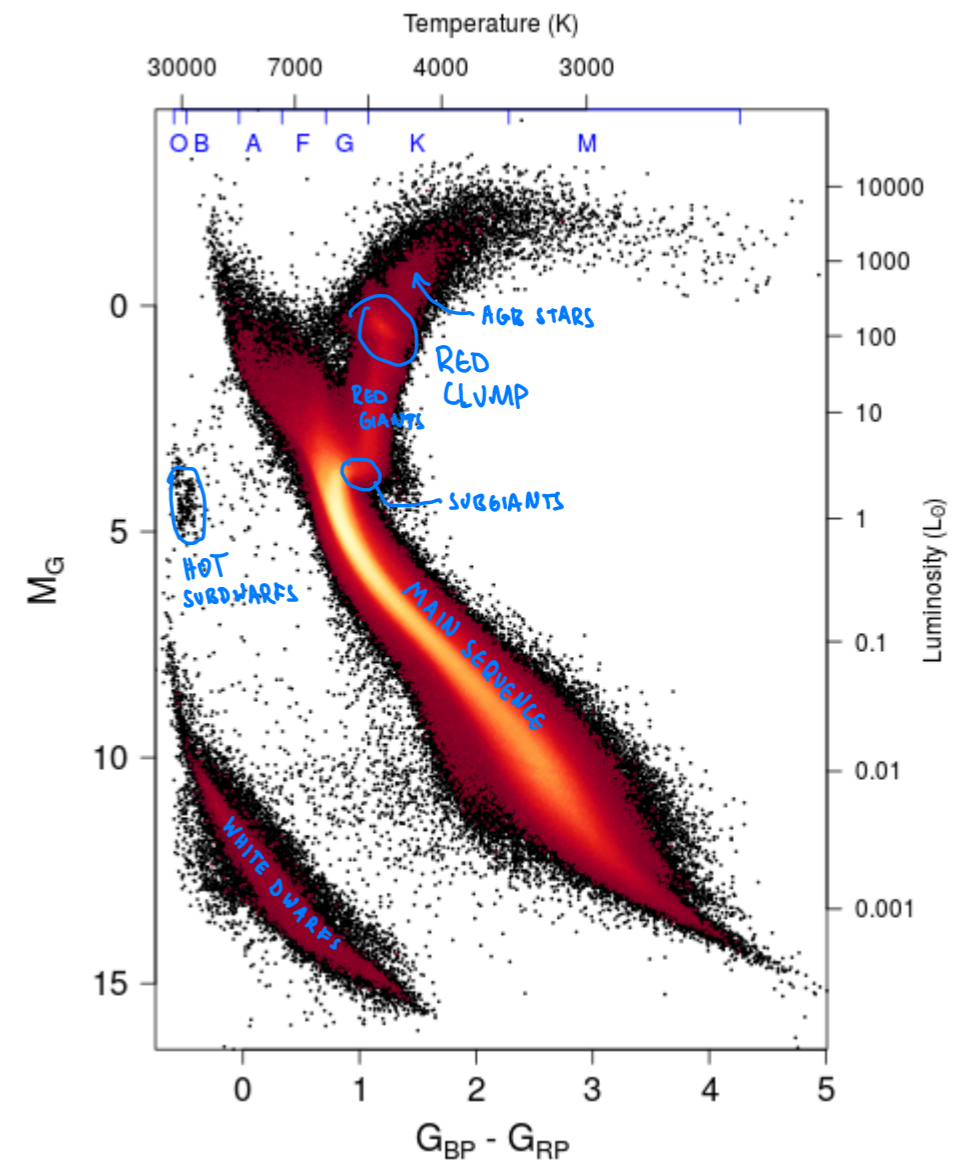
The Initial Mass Function

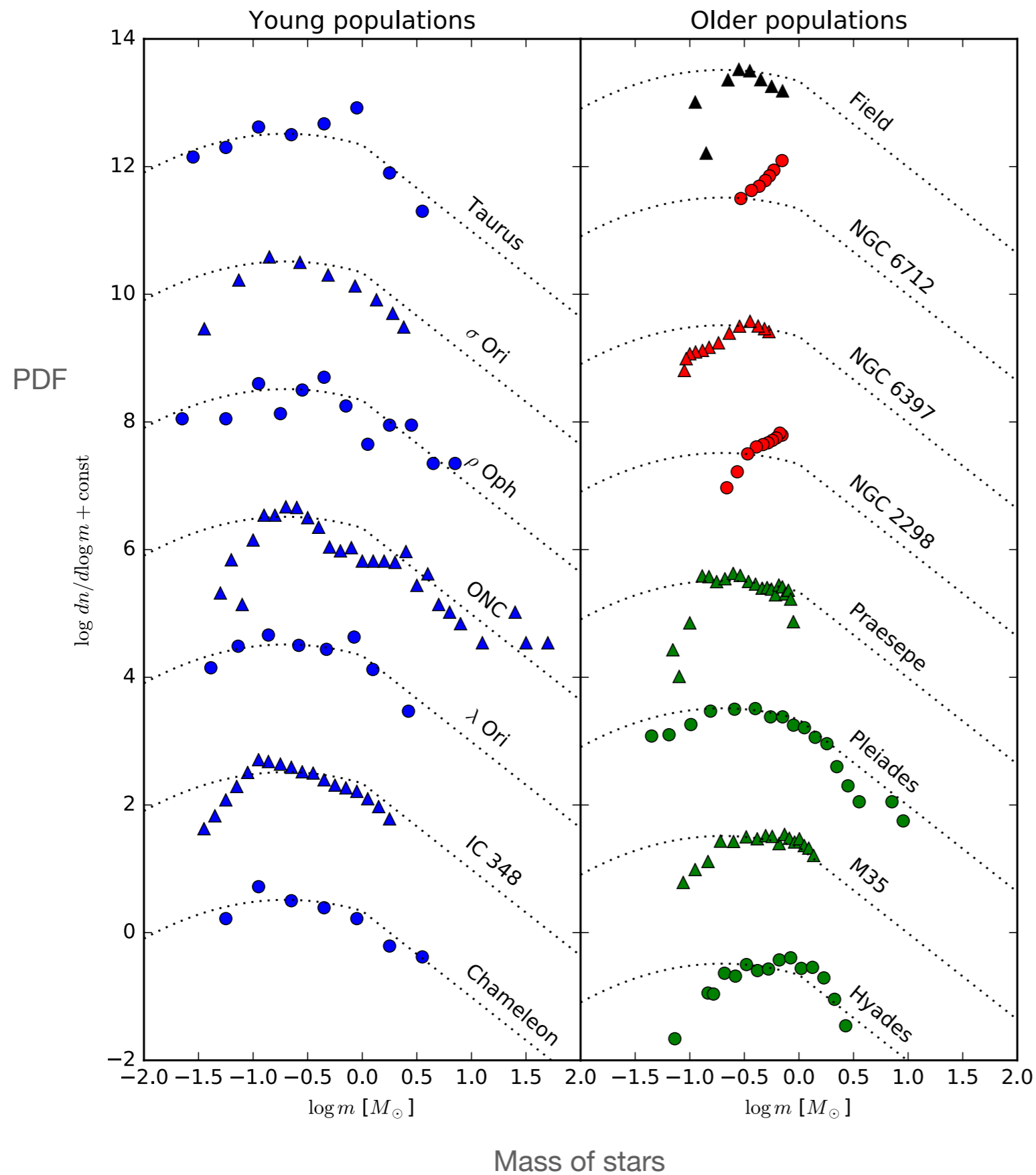
Functional forms of the IMF

“Field” stars affected by evolution

High mass stars have died, low mass stars still here

Examine masses of stars in regions of star formation, all stars similar age!





Local initial mass functions are all similar (?!)

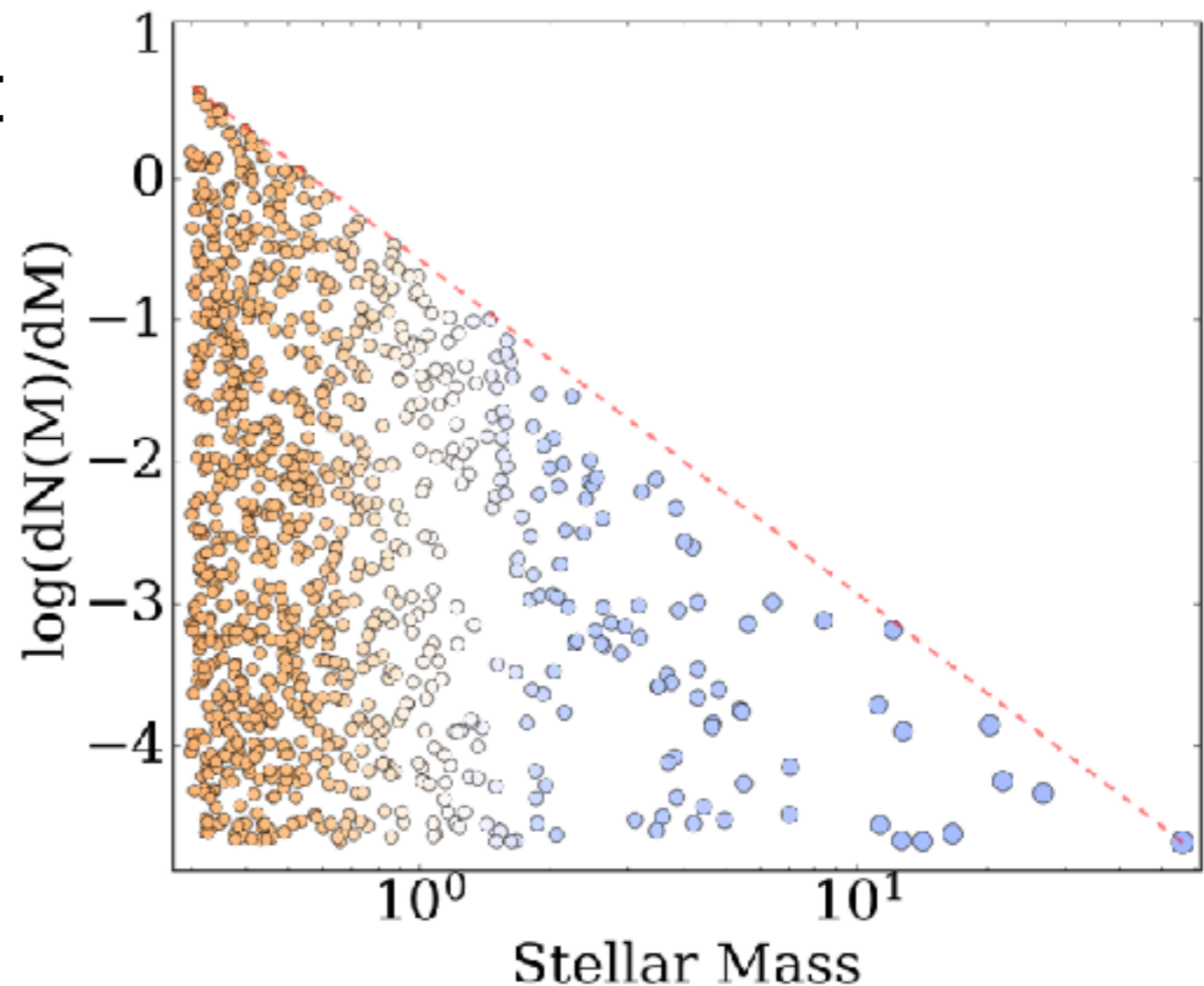
The Initial Mass Function

Functional forms of the IMF

Describe IMF with different functional forms. Simplest is **Salpeter IMF**:

$$\frac{dN}{dM} = c_{\star} M^{-2.35}$$

where c_{\star} is a constant set by individual stellar formation event.

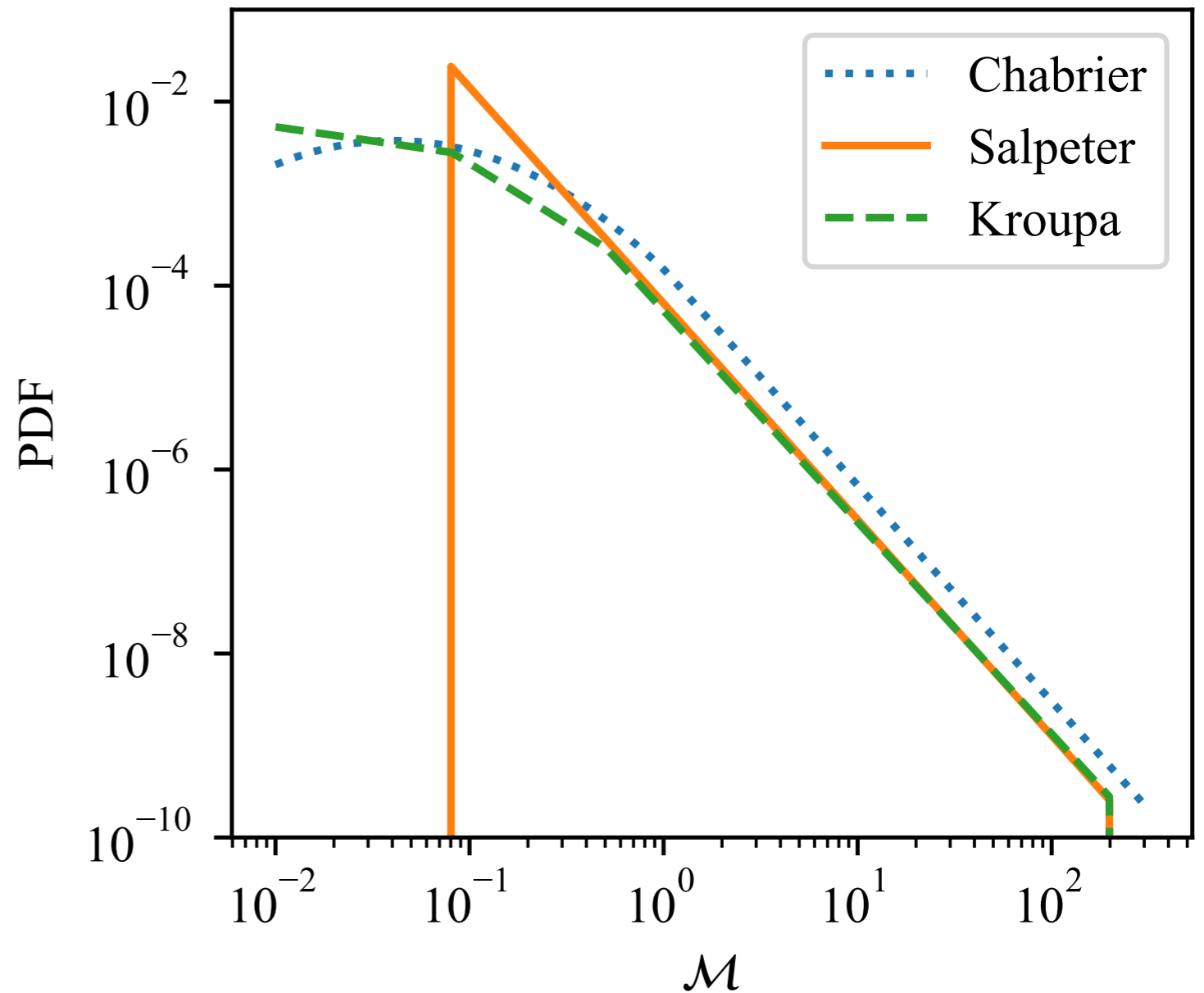


The Initial Mass Function

Functional forms of the IMF

Chabrier and Kroupa forms capture a turnover at low mass.

Open question: lowest mass objects made by SF?



Simple Stellar Populations

SSPs are a population of stars that

- (1) formed at the same time from gas with
- (2) the same metallicity.

Stars in SSPs have different masses.

Clusters are the classic example of SSPs.



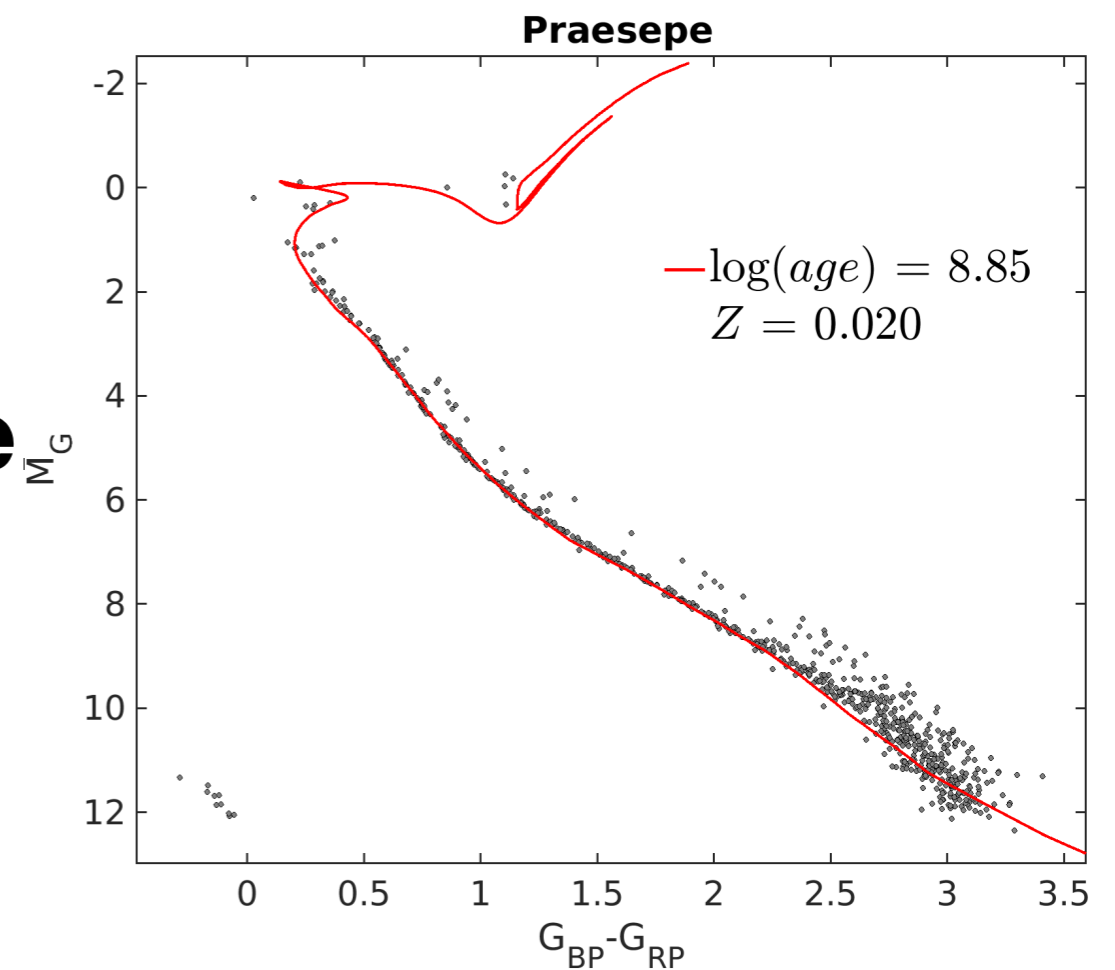
Praesepe (Beehive cluster)

Simple Stellar Populations

Isochrones

Stars evolve at different rates based on their mass.

Stars in SSPs fall along *isochrones* - locus of stars with different masses but **same age**



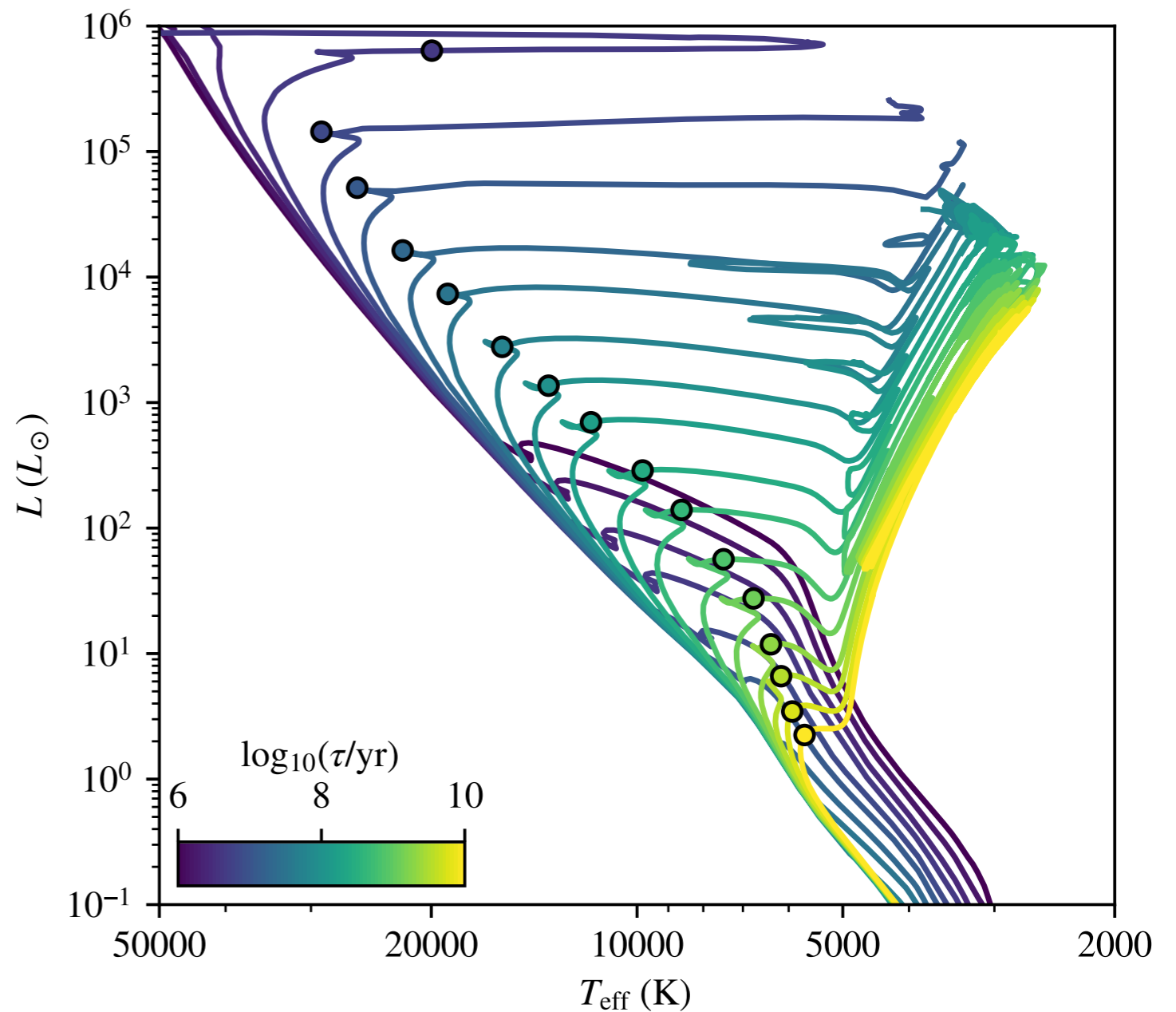
Simple Stellar Populations

Isochrones

Solar metallicity
isochrones

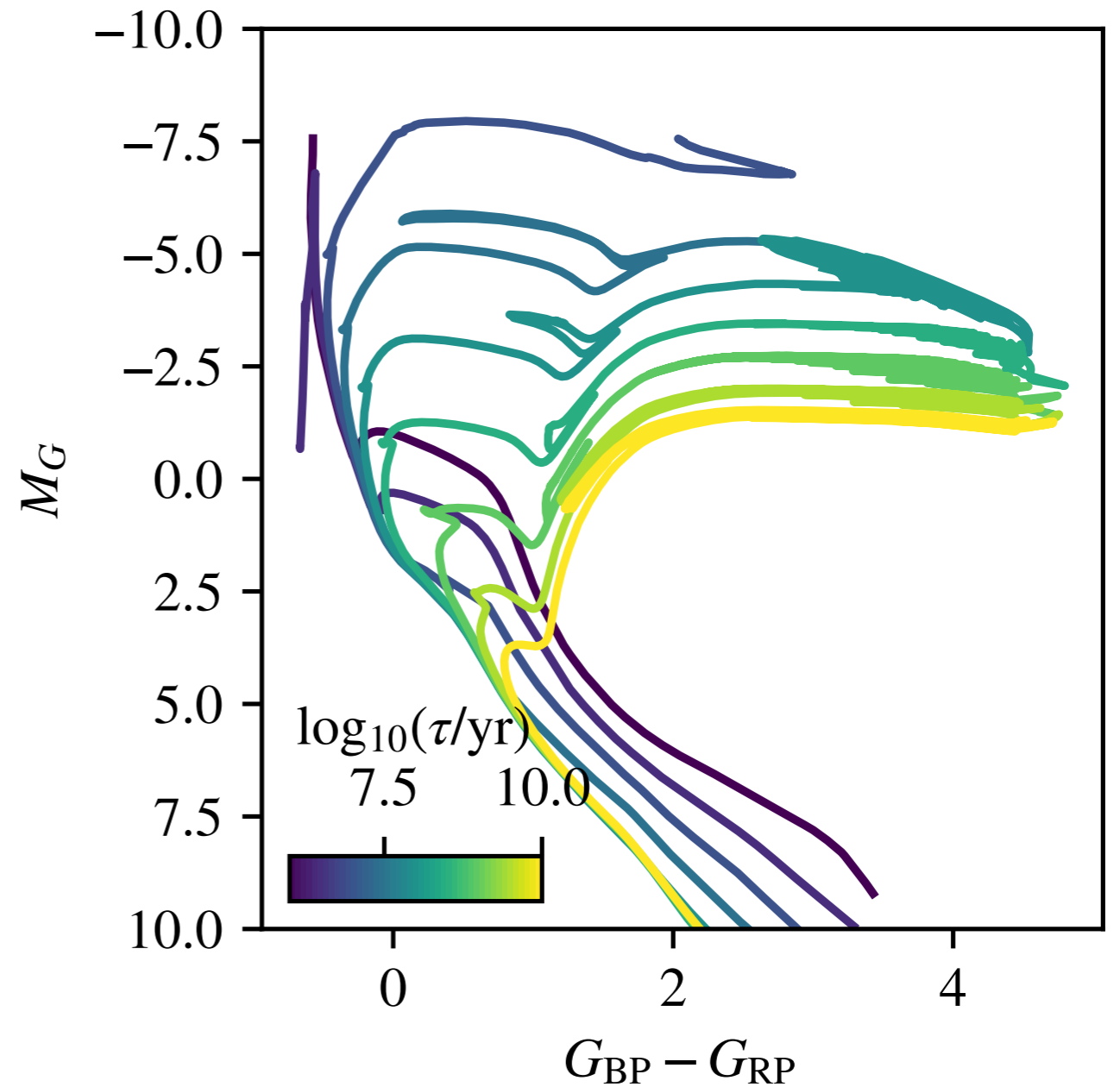
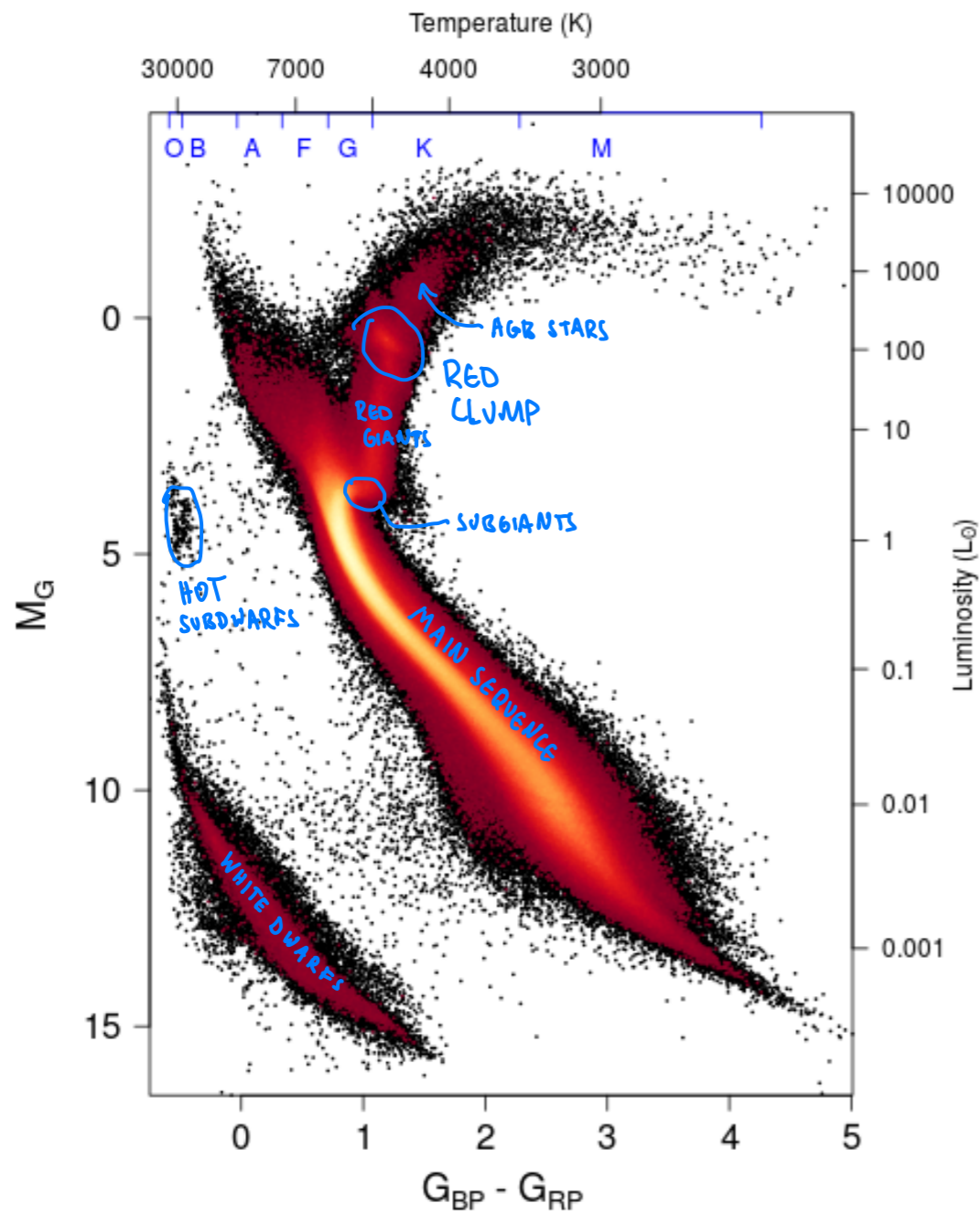
High mass stars evolve
onto the MS faster
than low mass.

Main sequence turn off
(MSTO) marked with •



Simple Stellar Populations

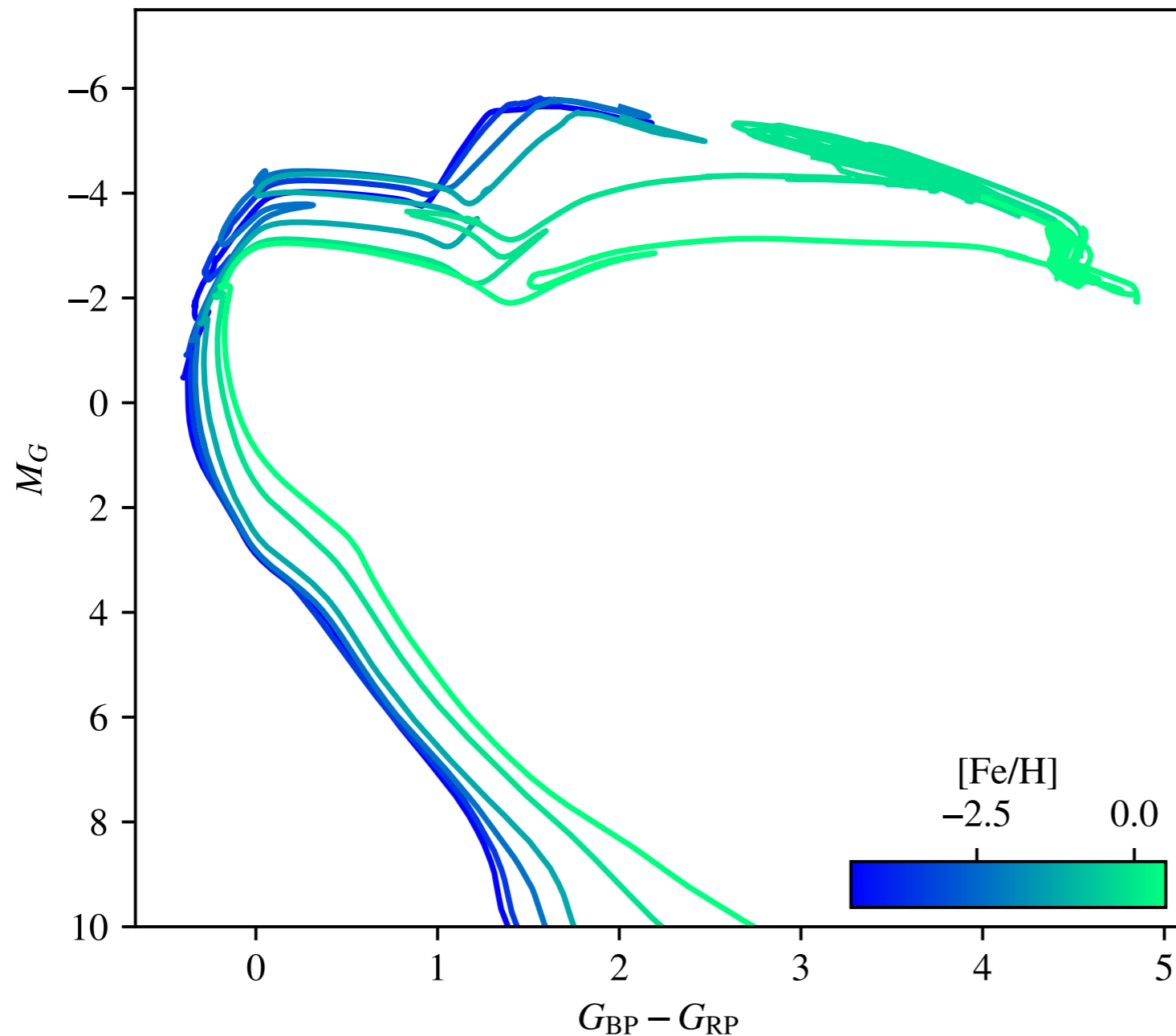
Isochrones



Match into isochrones into Gaia passbands

Simple Stellar Populations

Metallicity variation



Lower metallicity systems shifted in HR diagram

Gaia Data

Exercise 3

Select a cluster from the open cluster Gaia data.

Find an isochrone that's the best fitting representation of the cluster.

Simple Stellar Populations

Binary Stars

- Companion frequency:

$$CF = \frac{N_{\star \text{ in multiples}}}{N_{\text{systems}}}$$

e.g., Polaris is a “triple”

- Low mass ($M < 1 M_{\odot}$) stars tend to be single.
- High-mass stars ($M > 10 M_{\odot}$) tend to be twins. Otherwise, random draw from IMF.
- Nearly all multiples are coeval (formed together)

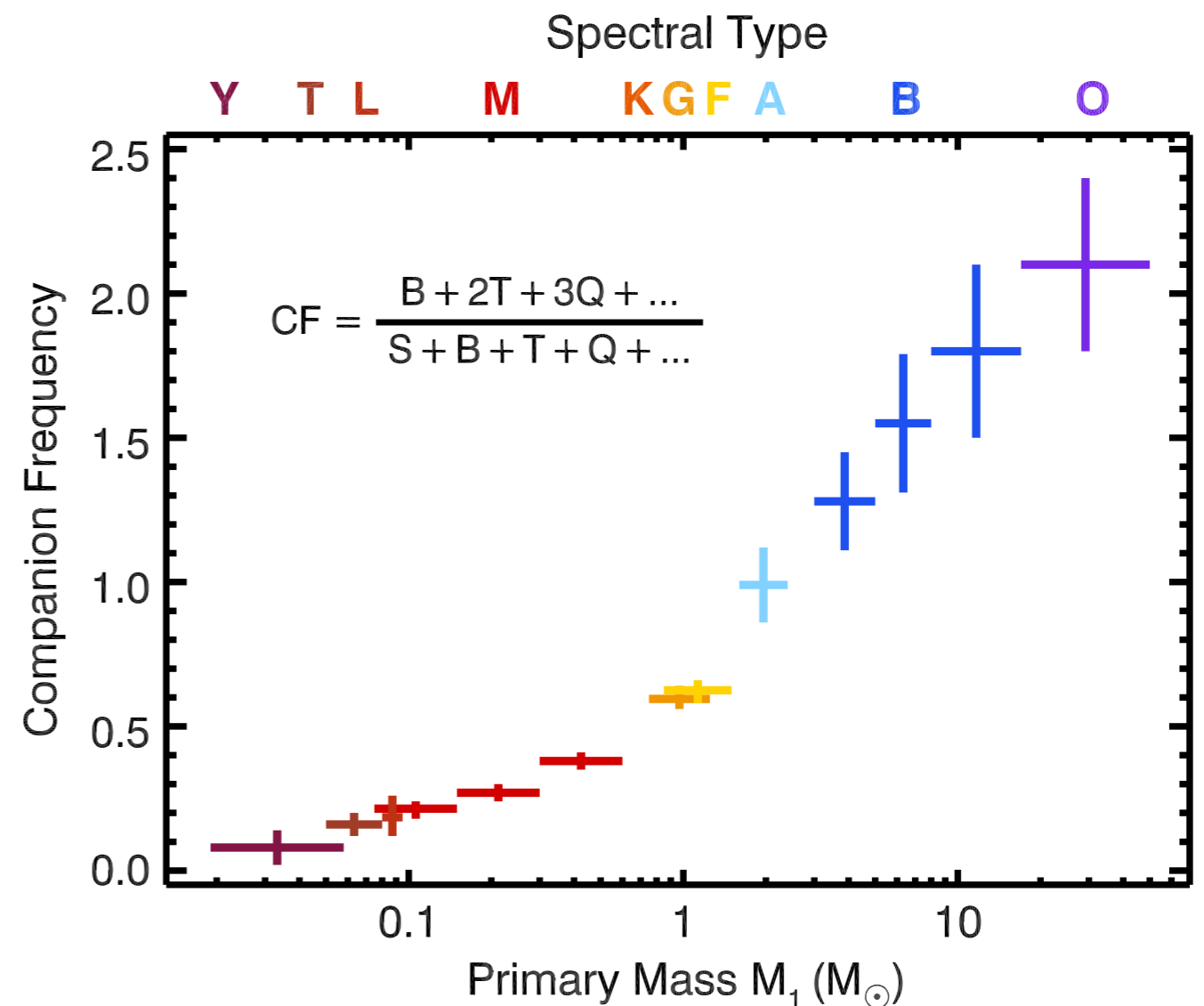


Figure from Offner et al. (2022)

Real Stellar Populations

Multiple stellar populations

Observational effects

Biases, numbers of stars

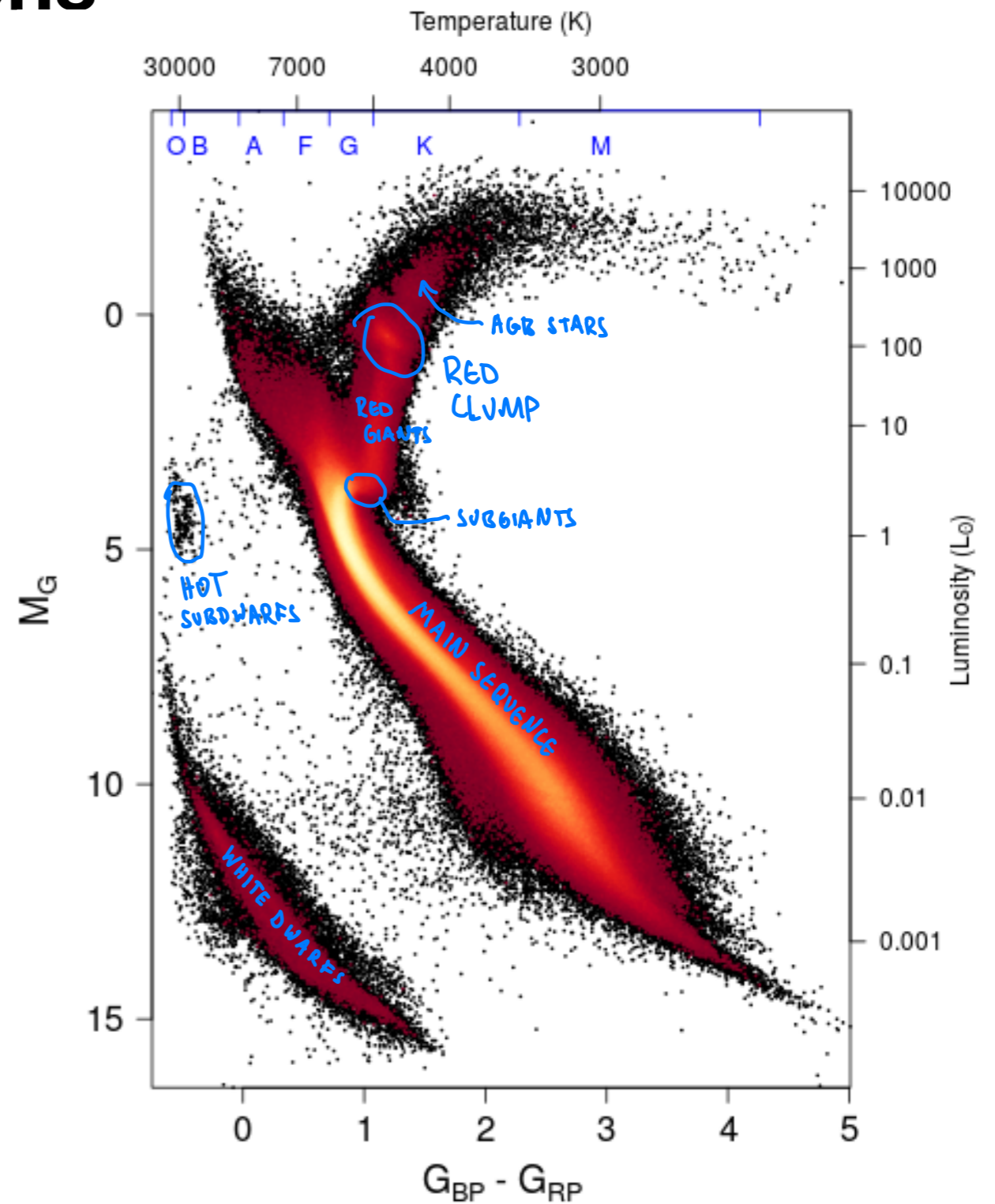
Dust

Causes extinction and reddening

Non-simple populations

Star formation history

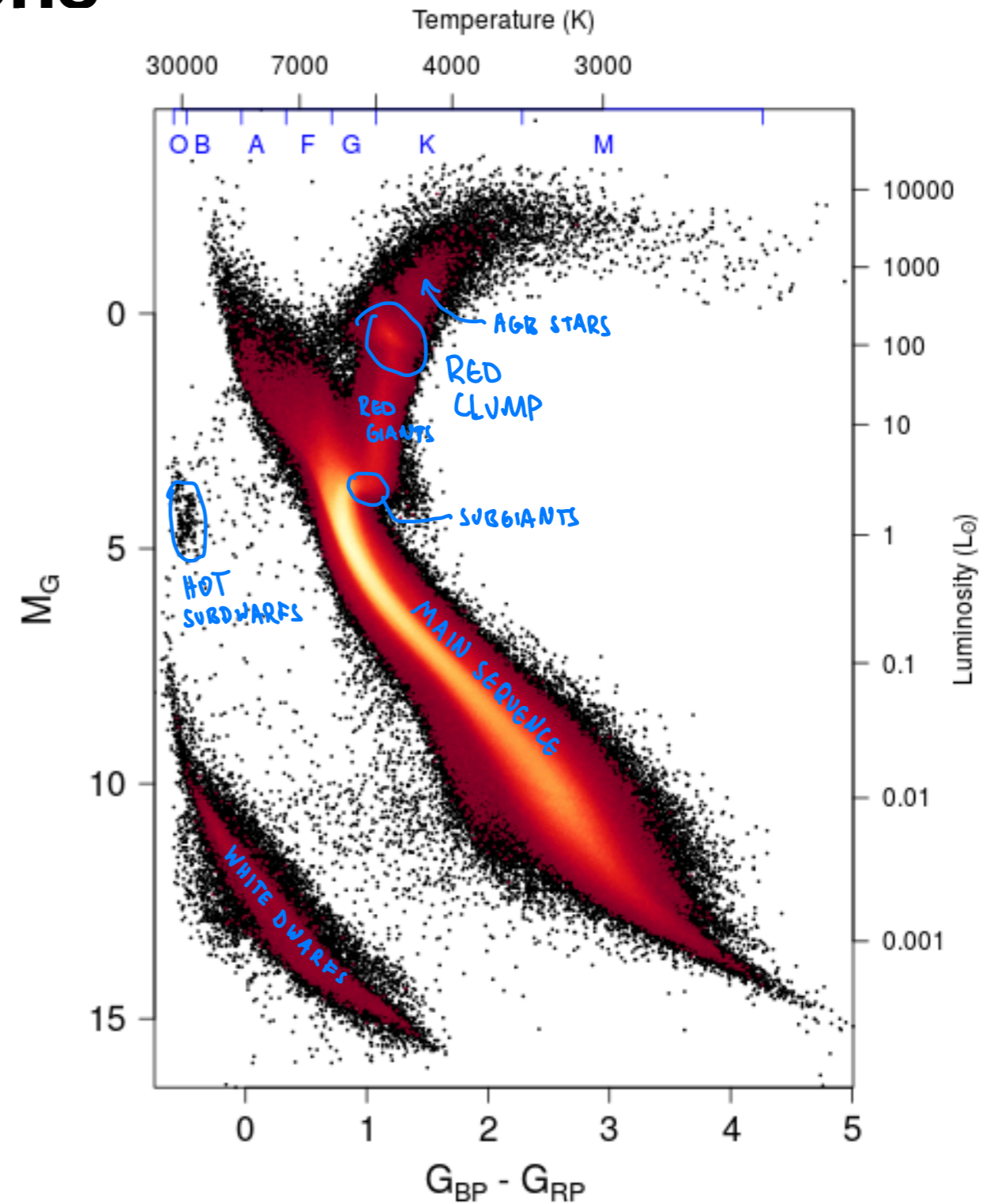
Metallicity varies with time and space



Real Stellar Populations

Multiple stellar populations

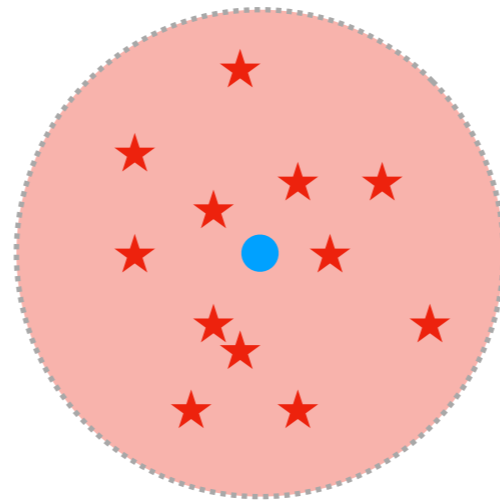
Why is the most common star in the Gaia sample of the HR diagram a sun-like star?



Real Stellar Populations

Multiple stellar populations

Luminosity bias - we can see more luminous objects over a larger volume than we can see faint objects.

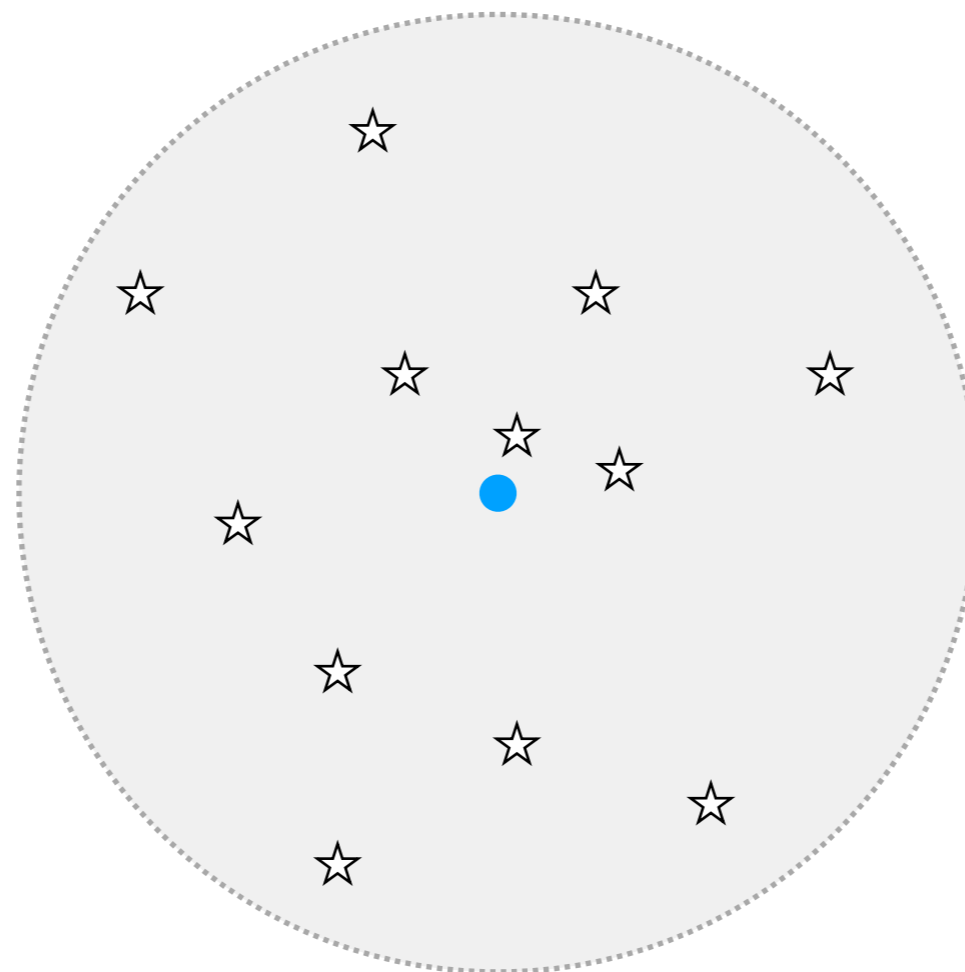


M0V stars

Real Stellar Populations

Multiple stellar populations

Luminosity bias - we can see more luminous objects over a larger volume than we can see faint objects.



V_{complete}

Volume over which a survey is *complete*, meaning we see all objects of that type.

A0V stars

Real Stellar Populations

Multiple stellar populations

The observed ratio of stars reflect three main factors:

$$\left(\frac{N_{\text{high}}}{N_{\text{low}}} \right)_{\text{observed}} = \left(\frac{N_{\text{high}}}{N_{\text{low}}} \right)_{\text{formed}} \left(\frac{\tau_{\text{high}}}{\tau_{\text{low}}} \right) \left(\frac{V_{\text{high}}}{V_{\text{low}}} \right)$$

1. The relative number of stars that are formed (IMF)
2. How long those stars live (stellar evolution)
3. How far away we can see those stars (observational effects)

Real Stellar Populations

Multiple stellar populations

For this example, the V_{complete} for the bright stars is $10^{12} \times$ larger than for the faint stars.

Overcomes rarity of high mass stars from IMF.

Short lifetimes of high mass stars will reduce their relative frequency.

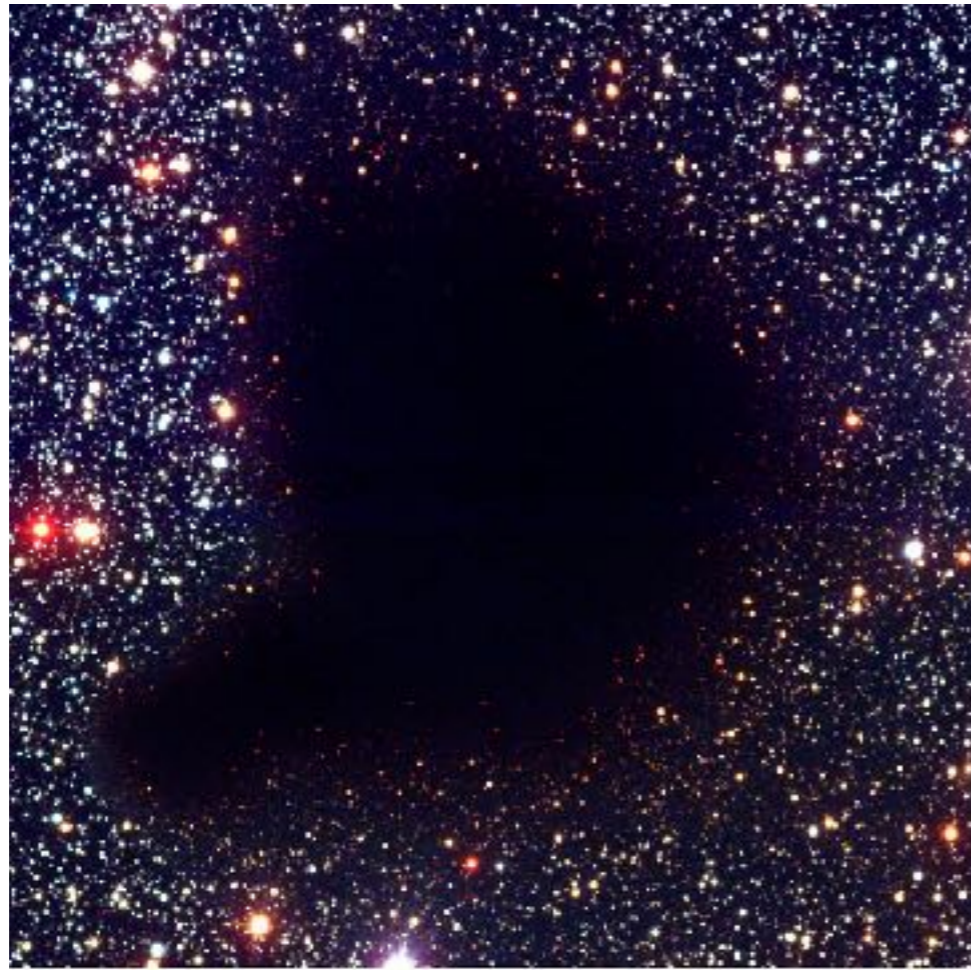
Density of stars in HRD is a product of (1) observational selection (2) star formation history, and (3) lifetimes of stars at that stage.

Real Stellar Populations

Dust

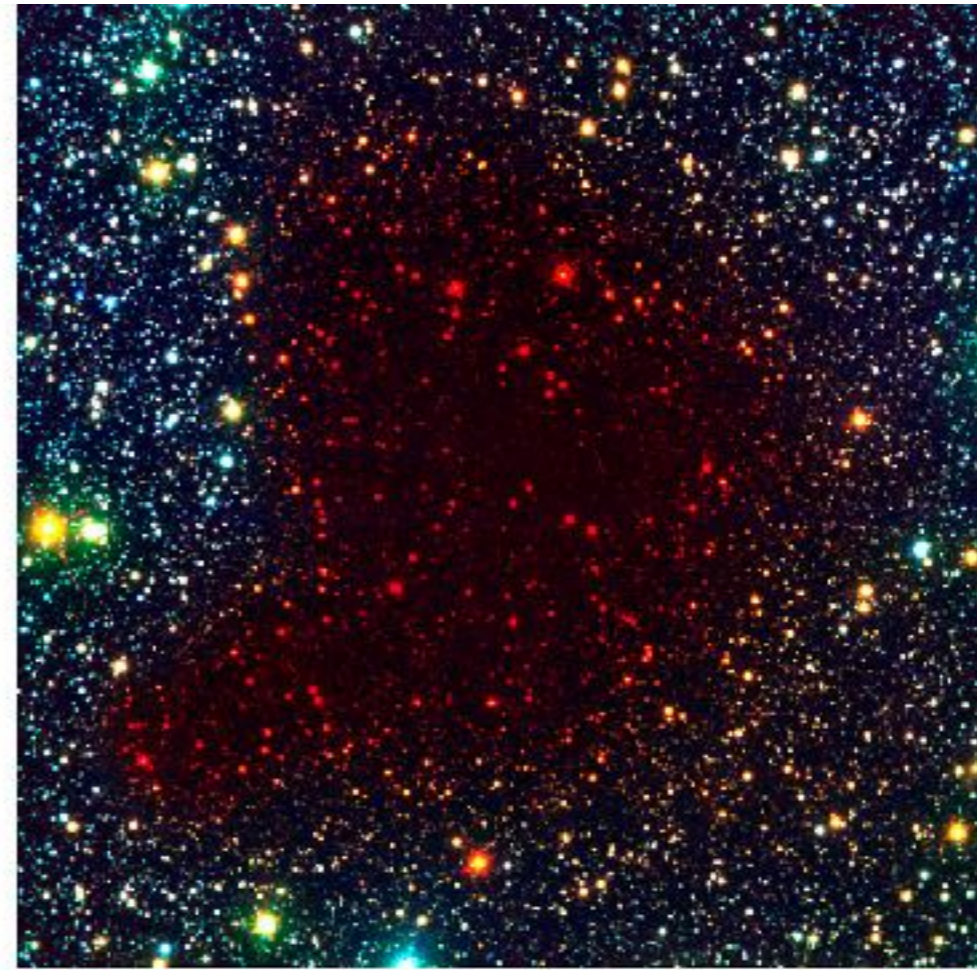
Interstellar dust is mixed throughout the neutral gas in the Galaxy. The effect of dust:

- (1) blocks optical light
- (2) blocks bluer light more than red light
- (3) reradiates absorbed light in the infrared



B, V, I

Optical-only image



Optical + Infrared (in red) band

B, I, K

Long wavelength observations can “see through” the dust to embedded or background sources.

Real Stellar Populations

Dust

$\tau_\lambda \equiv n\sigma\ell$ is the *optical depth*

We usually represent the extinction in the magnitude system using the variable A .

$$A_\lambda = 1.086\tau_\lambda$$

Real Stellar Populations

Cross sections

Cross section is a general concept:

$$\sigma = \frac{N_{\text{coll}}/N_{\text{targets}}}{N_{\text{incident}}/A}$$

where N_{coll} is the number of collisions per number of targets N_{targets} , and N_{incident} is the number of particles passing through a total area A .

When $\sigma = \pi r^2$, this is the geometric cross section.

Example: Imagine a long hallway with 70 watermelons suspended from the ceiling at different heights and random positions. The hallway has a cross sectional area of 10 m^2 . You stand at one end and fire 100 bullets down the hall with your trusty physics lab issued AK-47. Because of excessive recoil and perhaps some liquor before you headed down to do physics, your shots are essentially randomly shot down the hallway. You count a total of 35 exploded watermelons after the storm of bullets. What is the cross section of a watermelon?

Real Stellar Populations

Reddening

Reddening occurs because $A_{\lambda_1} > A_{\lambda_2}$ if $\lambda_1 < \lambda_2$

(dust blocks blue light better than red light).

Specifically, dust blocks like with $\sigma_{\lambda} \propto \lambda^{-1}$ and scatters light with $\sigma_{\lambda} \propto \lambda^{-4}$.

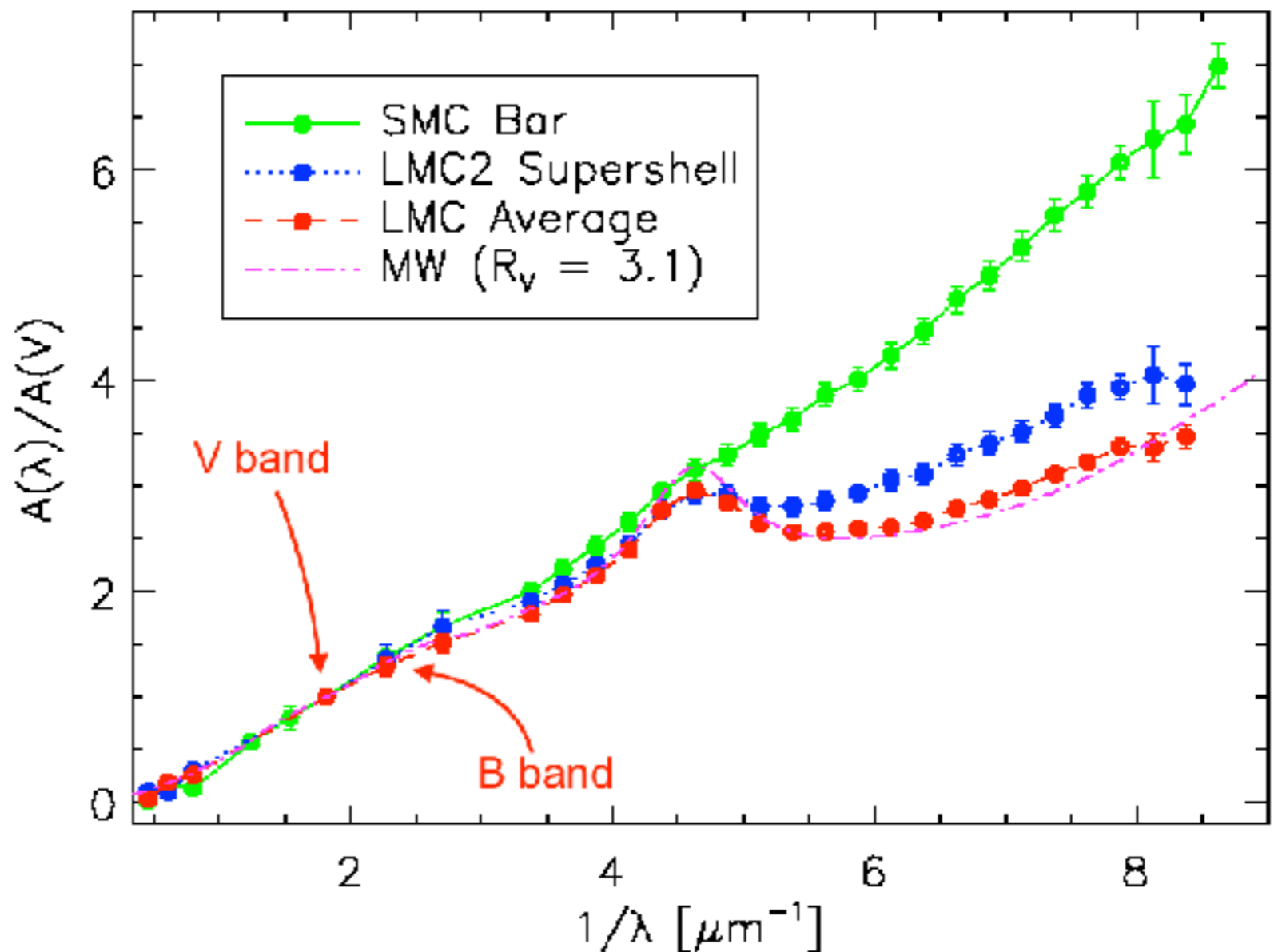
Real Stellar Populations

Reddening Curve

Compare extinction to a reference waveband. Usually the V band at $\lambda = 550$ nm

The *reddening* value is usually given as

$$R_V = \frac{A_V}{A_B - A_V} \approx 3.1$$



Real Stellar Populations

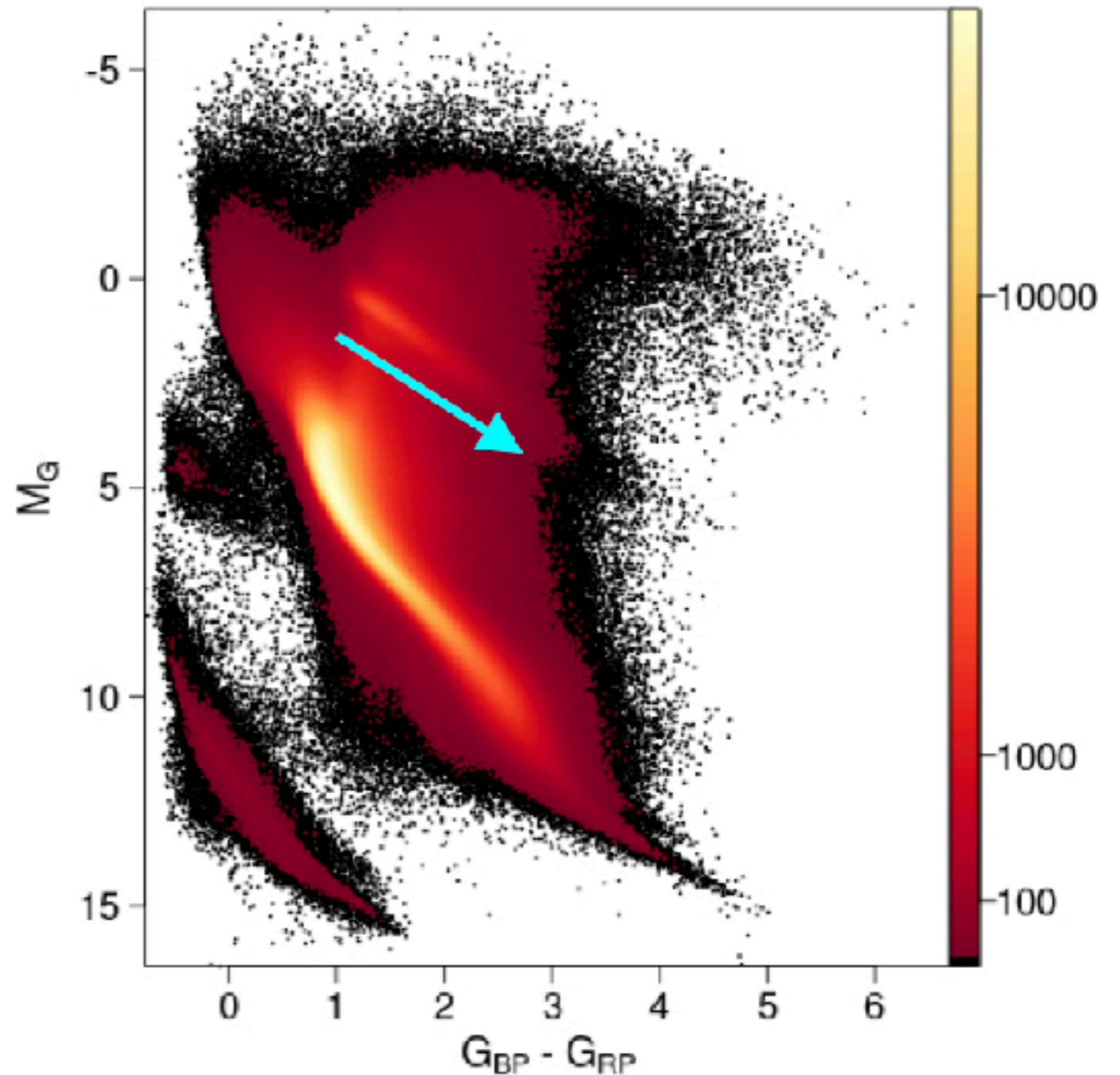
Reddening Vector

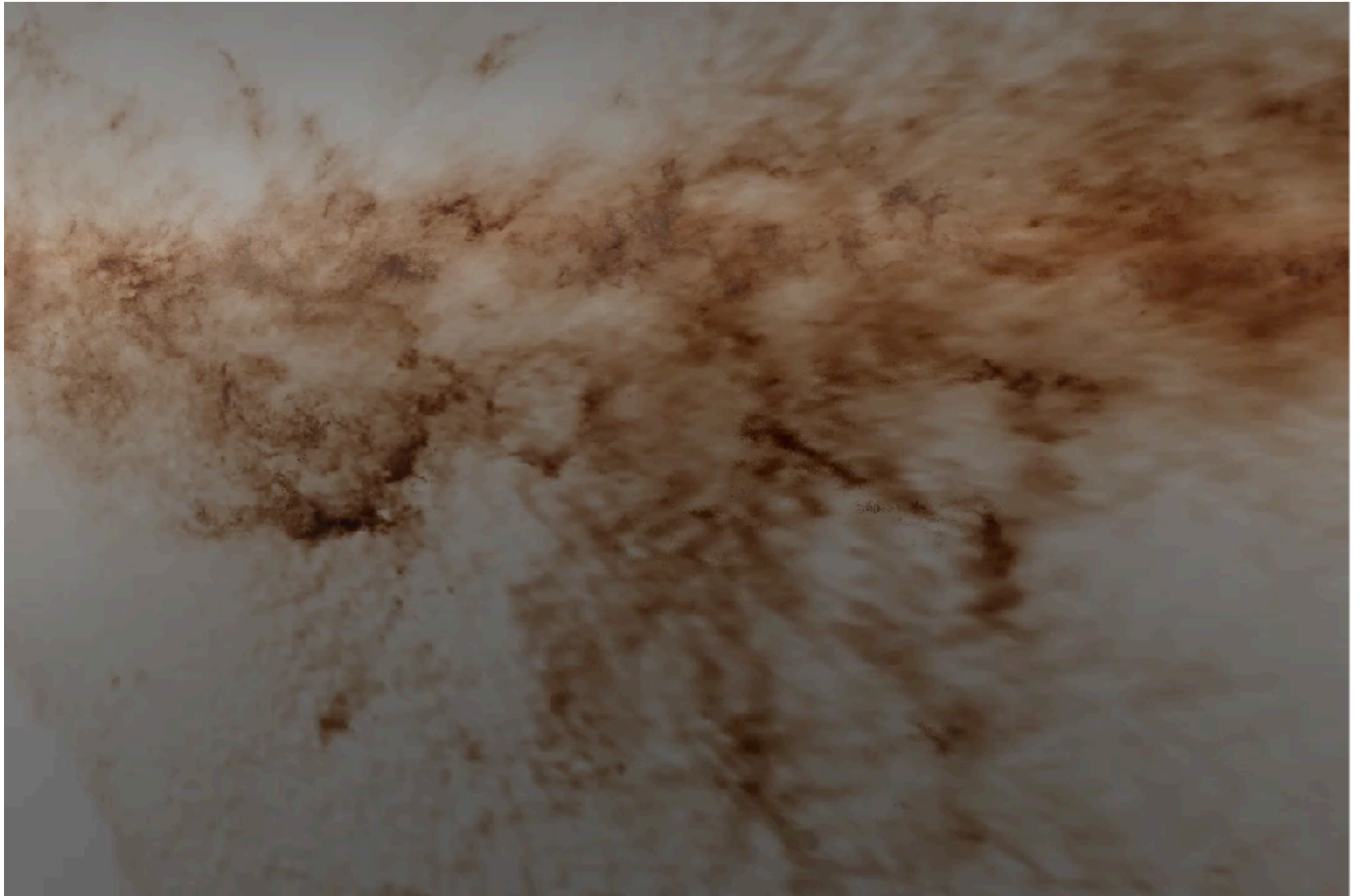
The slope of reddening relative to extinction shows up in the HR Diagram.

For Gaia:

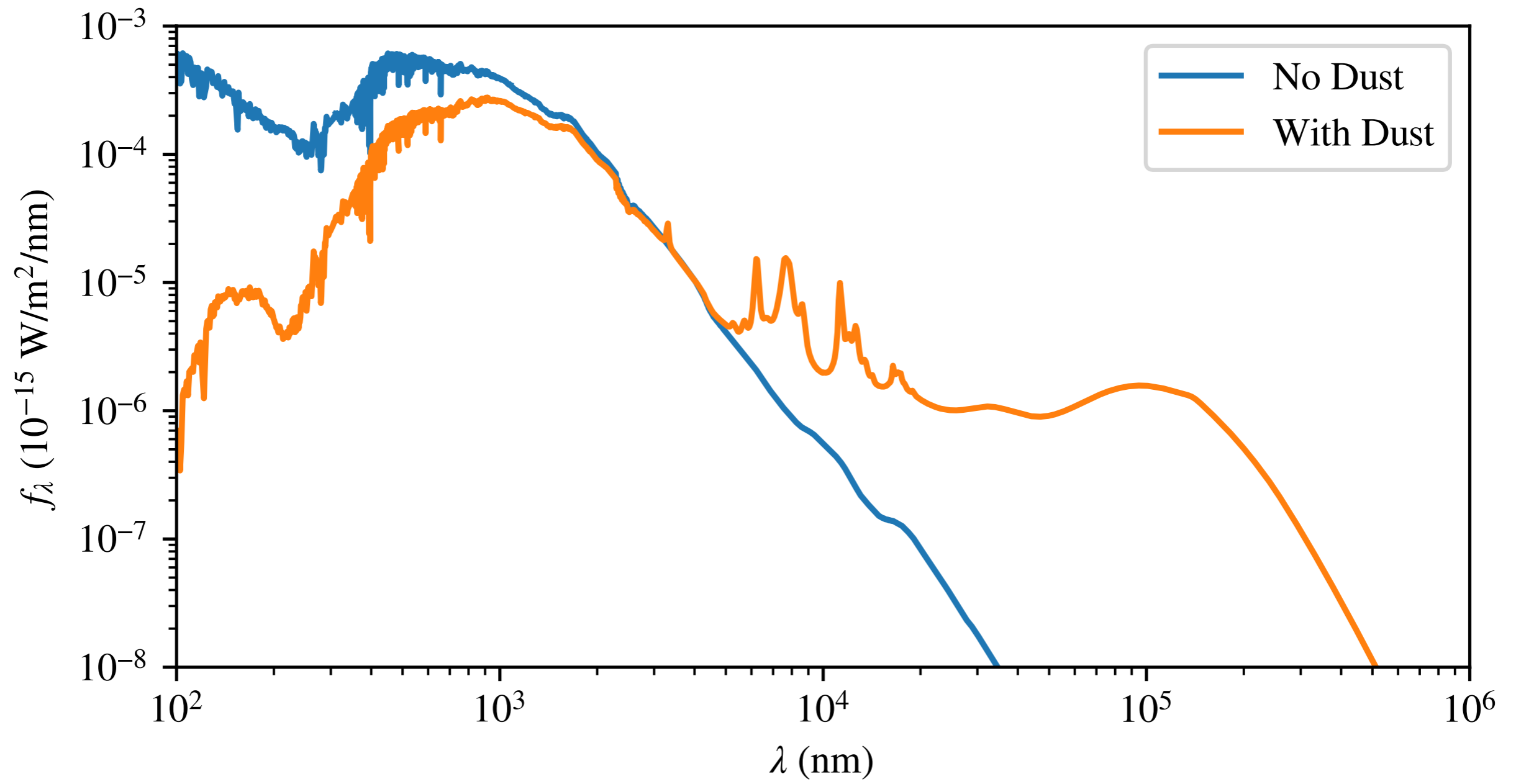
$$R_G \approx \frac{A_G}{A_{BP} - A_{RP}} \approx 1.8$$

Note how red clump is “smeared” out. Bigger displacement = Bigger reddening.





Green et al. Dust mapping with PanSTARRS
<http://argonaut.skymaps.info/>



Real Stellar Populations

Star Formation Histories

Predict the density of stars in the HR Diagram

Set by the $\dot{M}_\star(t)$, also known as star formation rate, SFR.

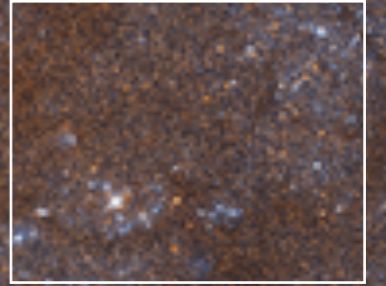
Number of stars on MS at mass M is

$$N_{\star,M} = f_M \int_0^{t_{\text{stop}}} \dot{N}_\star dt = f_M \int_0^{t_{\text{stop}}} \frac{\dot{M}_\star}{\langle M \rangle} dt$$

Where t_{stop} is smaller of MS lifetime or age of Universe

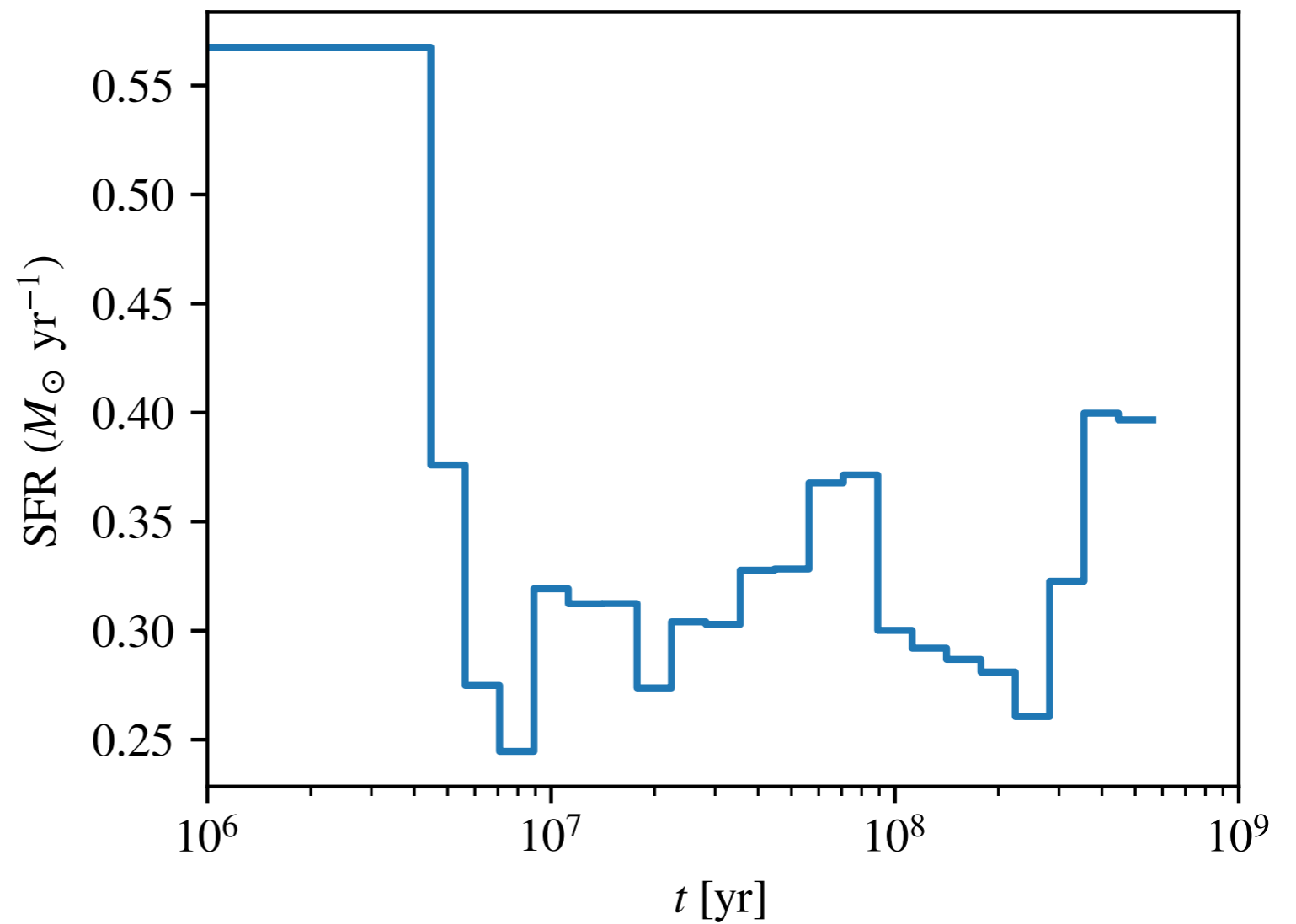
Able to Infer SFR vs time

Pan-Chromatic Andromeda Treasury - Triangulum Extension Region (PHATTER)

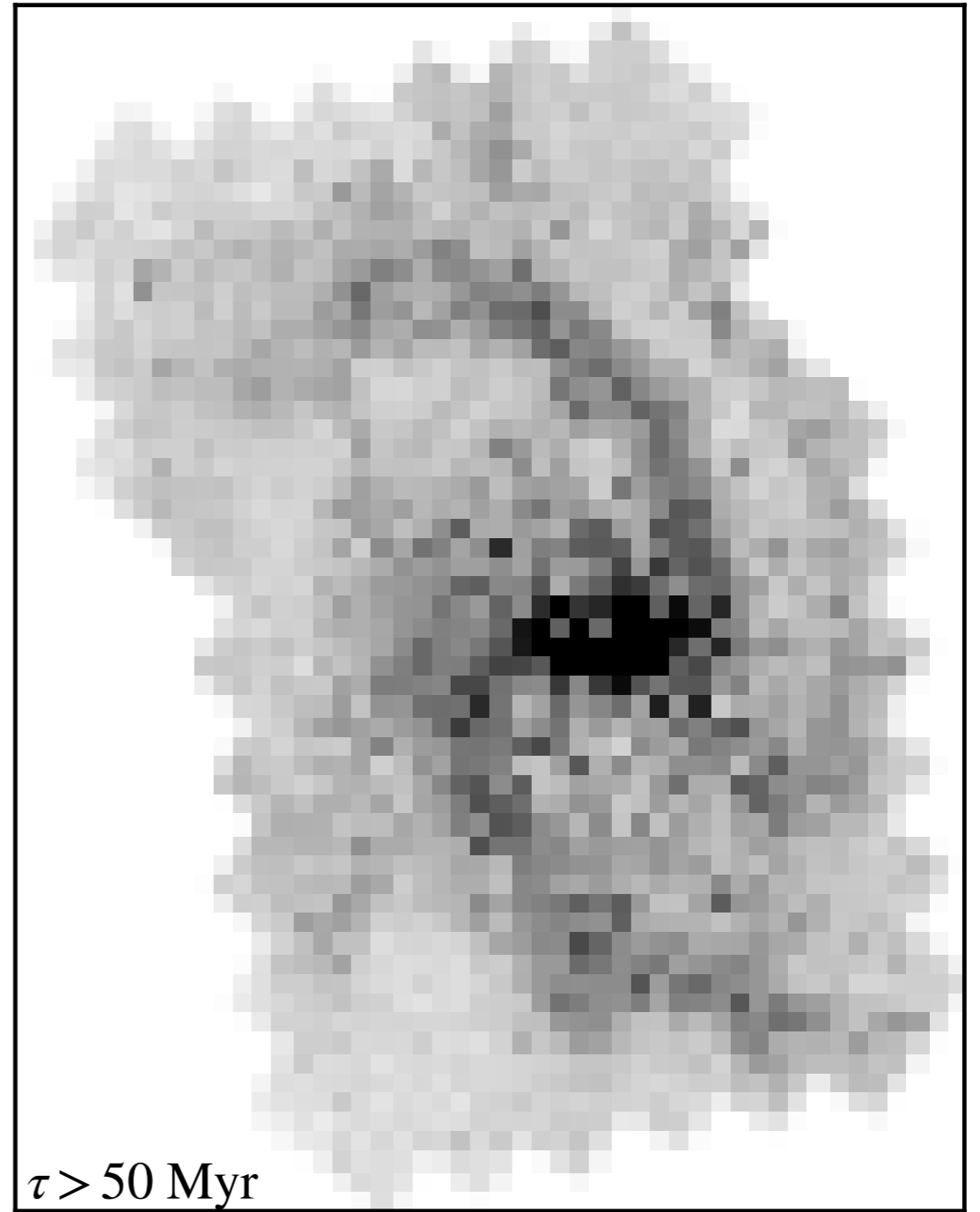
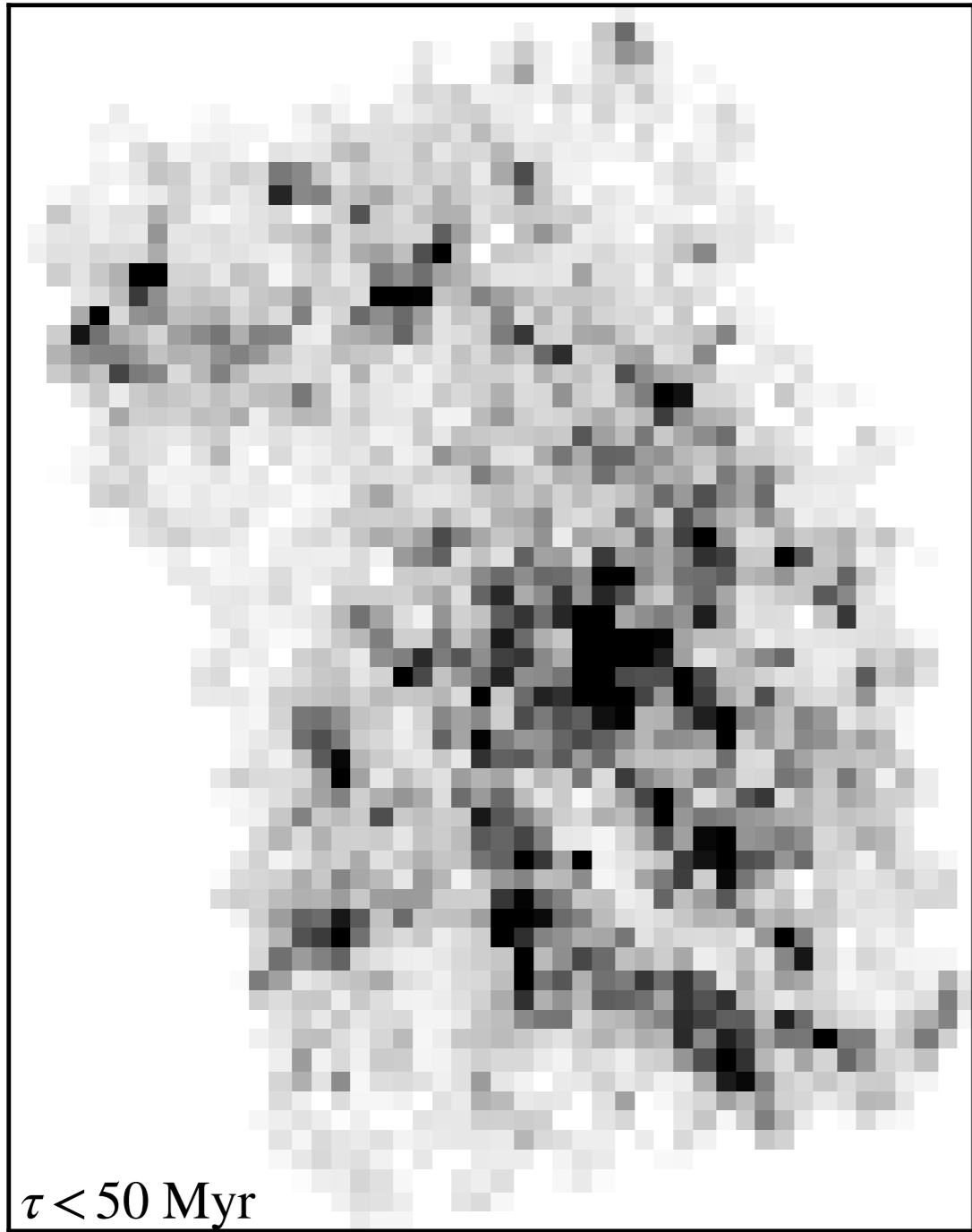




Star density on HR diagram gives us ability to reconstruct SFH of a galaxy.



SFH of M33
Lazzarini et al. (2022)



SFH of M33
Lazzarini et al. (2022)

Gaia Data

Exercise 4

Use the `gaia_field_stars.csv` file from eClass and Glue to make a plot of the HR diagram of stars. Your HR diagram should colour each star by its extinction value A_G

Use the values of A_G and $E(BP - RP)$ in the data file (`ag_gspphot` and `ebpminrp_gspphot` respectively) to make a new HR diagram with each star's position corrected for extinction and reddening.

Make a plot of $E(BP - RP)$ as a function of galactic latitude b . Explain the feature you see in this plot.

Gaia Data

Exercise 4

Plot an extinction-and-reddening-corrected HR diagram, and calculate the mean distance from the midplane of the Galactic coordinate systems for red clump stars $\langle z_{\text{gal}} \rangle$.

Using the same HR diagram, plot a histogram of the differences in heights of the red clump stars from this average value $z_{\text{gal}} - \langle z_{\text{gal}} \rangle$.

Estimate the scale height H of the red clump stars by calculating the standard deviation of z_{gal} for that subset of stars.

Using a similar approach as in the previous problem, calculate the scale height for massive main sequence stars with $BP - RP < 0.5$. Compare your result to the previous problem and explain why these answers should be different.