

Matching Factors for Quasi-GPDs with Hybrid Renormalization

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LaMET Factorization Theorem

$$\tilde{q}(x, \Lambda, P_z) = \int \frac{dy}{|y|} Z\left(\frac{x}{y}, \frac{\mu}{P_z}, \frac{\Lambda}{P_z}\right) q(y, \mu) + \mathcal{O}\left(\frac{\Lambda_{\text{QCD}}^2}{P_z^2}, \frac{M^2}{P_z^2}\right) + \dots$$

- compensating the UV difference of quasi-PDF and PDF
- PDF in MS-bar, quasi-PDF in lattice spacing--- lattice action dependence, slow convergence (linear divergence, Wilson line mass subtraction scheme, [Ishikawa, Ma, Qiu, Yoshida; JWC, Ji, Zhang](#))

Non-perturbative renormalization (NPR)

Quark bilinear operators multiplicatively renormalized---

- (1) **Ratio scheme** (same operator, different states, Radyushkin)
- (2) **RI/MOM** (loop corrections removed at off shell momentum, Zhao & Stewart; Constantinou et al)

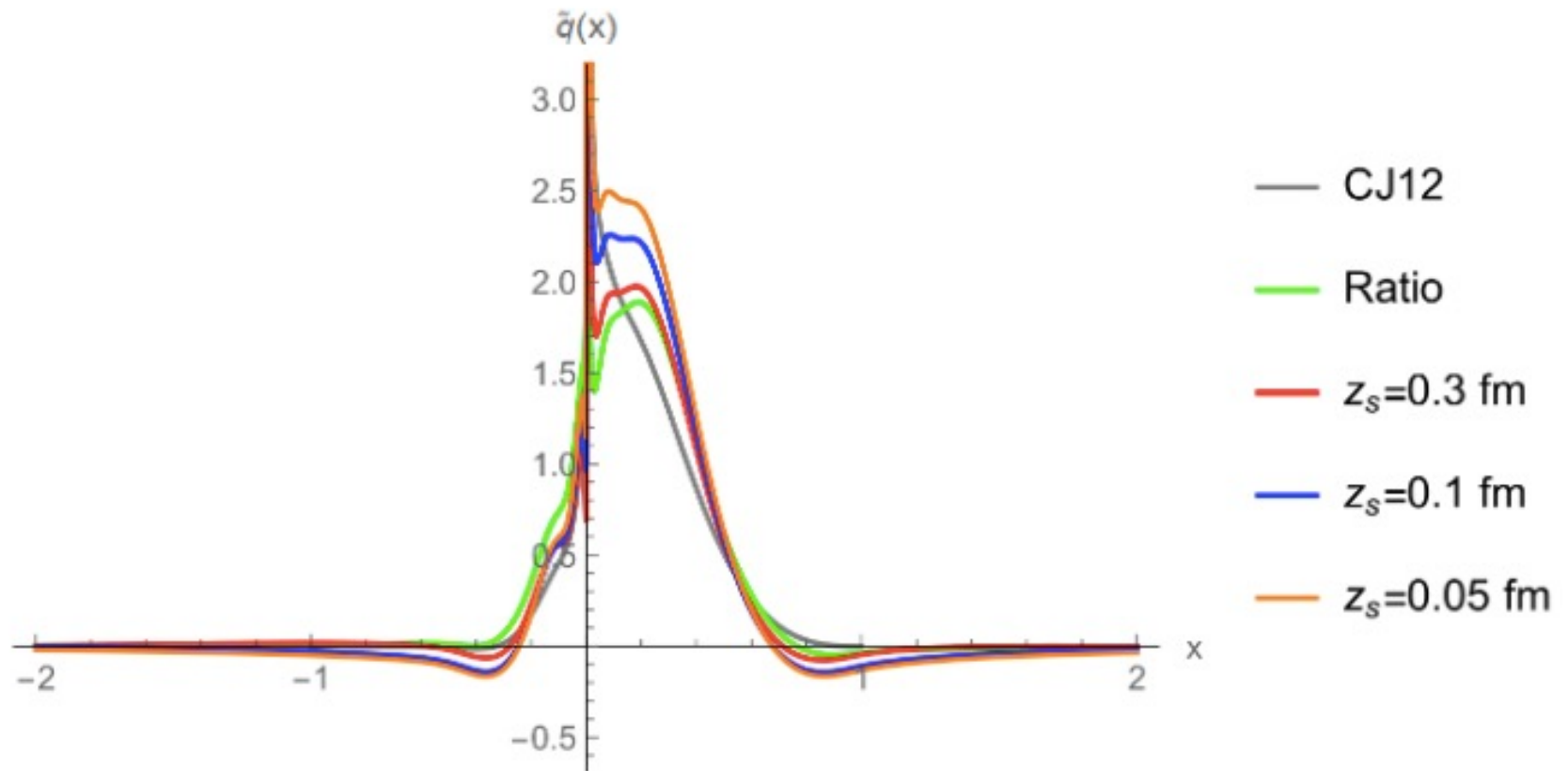
Then to continuum limit, lattice artifact gone
(**ChQCD (2012.05448)**): might not for RI/MOM)

Why Hybrid Renormalization?

- NPR should not remove unquantified nonperturbative IR effect---not the case for ratio & RI/MOM schemes. Long ($> Z_s \sim 0.3$ fm) Wilson line op. renormalize by Wilson line mass subtraction scheme instead---Hybrid renormalization (X. Ji, Y. Liu, A. Schäfer, W. Wang, Y.B. Yang, J.H. Zhang, Y. Zhao, 2008.03886)
- **Hybrid-ratio** scheme preferred.

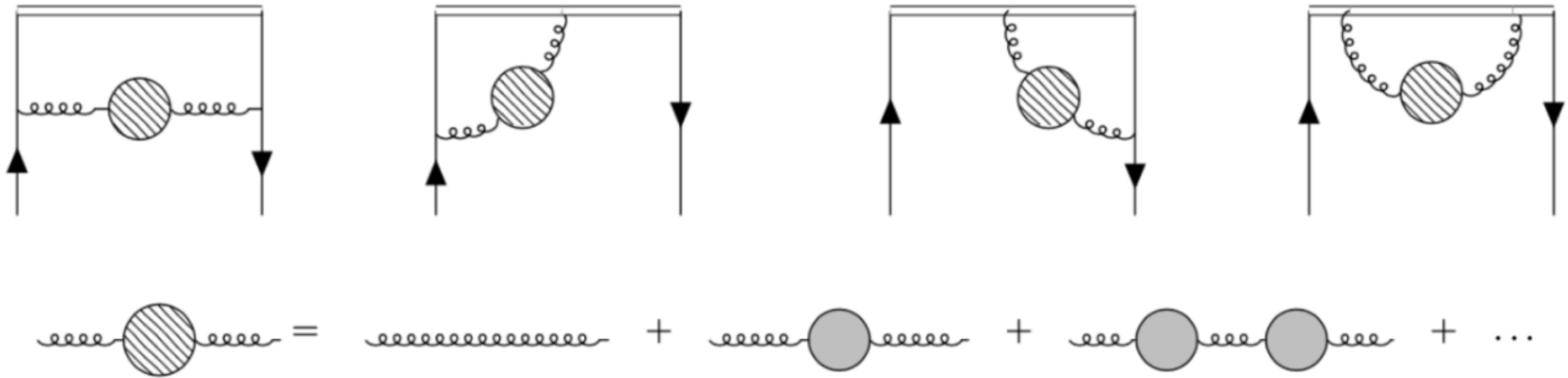
QPDF: Hybrid-Ratio to MS-bar Matching

(Chien-Yu Chou, JWC, 2204.08343)



u-d in proton; $Z_s = 0.3$ fm is close to infinity!

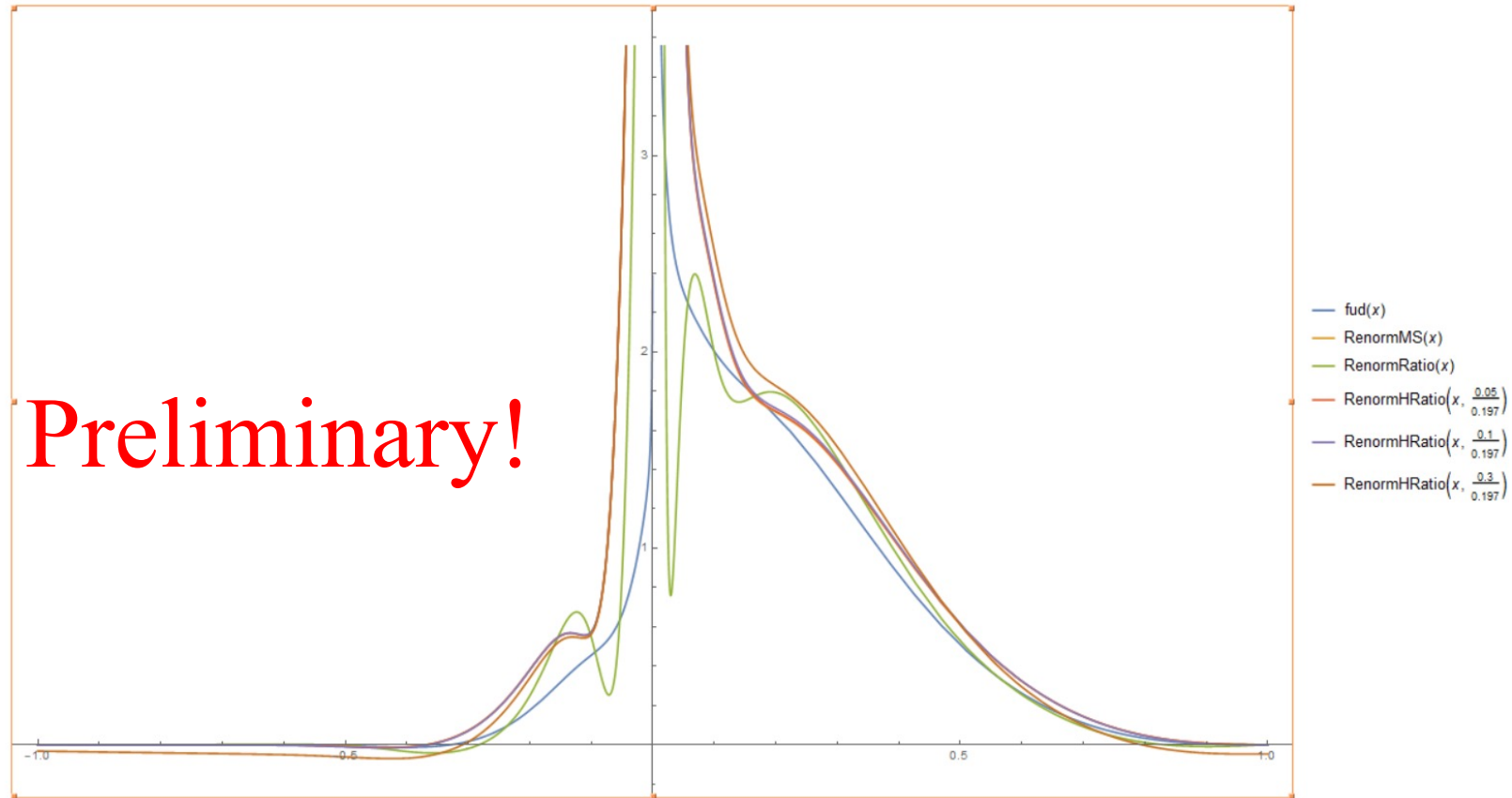
Renormalon in LaMET



Braun, Vladimirov and Zhang (1810.00048):
 power correction $\mathcal{O}(\Lambda_{\text{QCD}}^2/x^2 P_z^2)$

Hybrid-ratio renormalon ambiguity

w/ Yi-Xian Chen

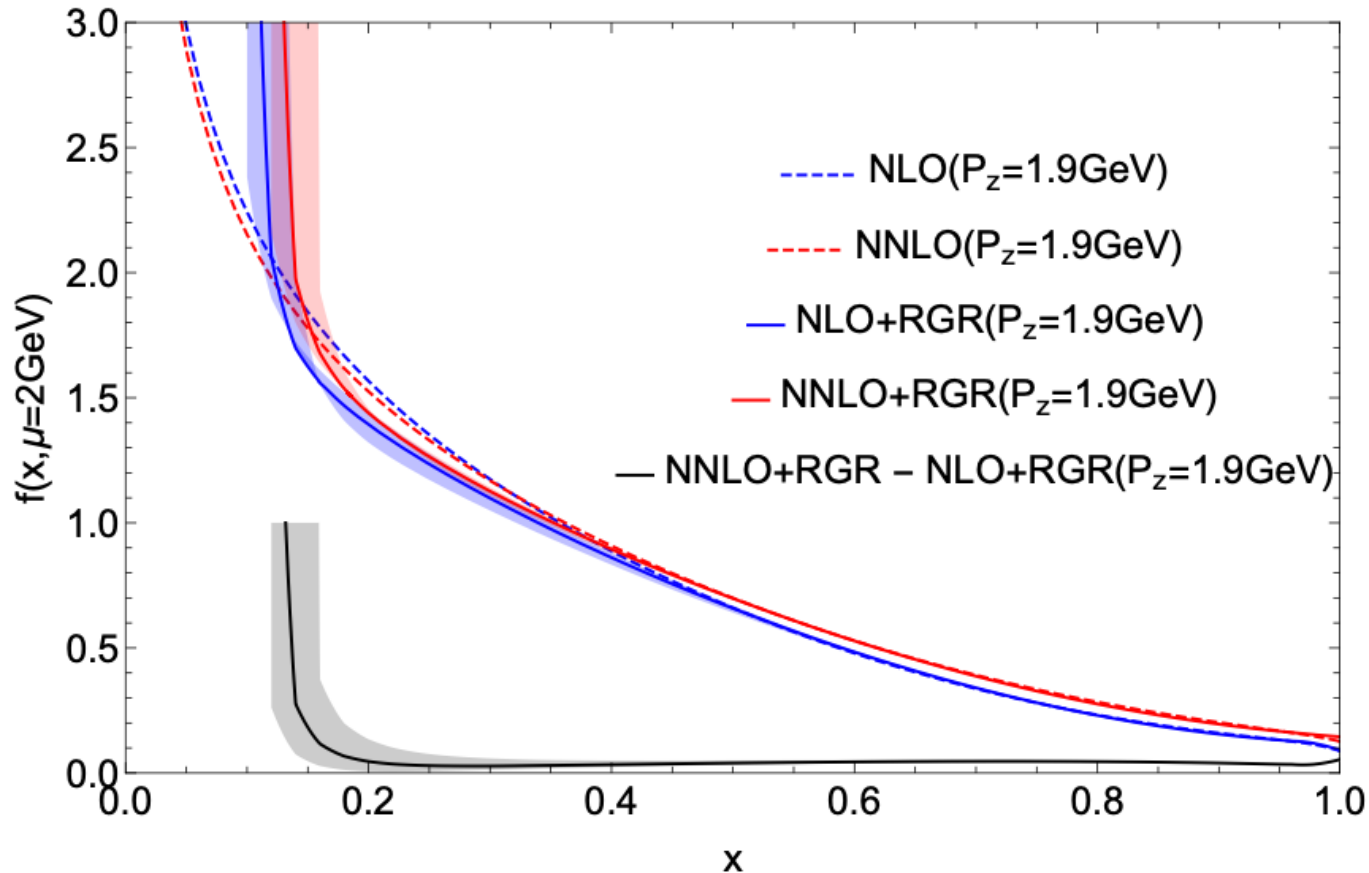


u-d in proton

Hybrid-ratio closer to MS-bar than ratio

--- $Z_s = 0.3$ fm is close to zero!

Same as Leading Log Resummation!



Pion u-d valance quark PDF---Yushan Su, Jack Holligan, Xiangdong Ji, Fei Yao, Jian-Hui Zhang, Rui Zhang (2209.01236)

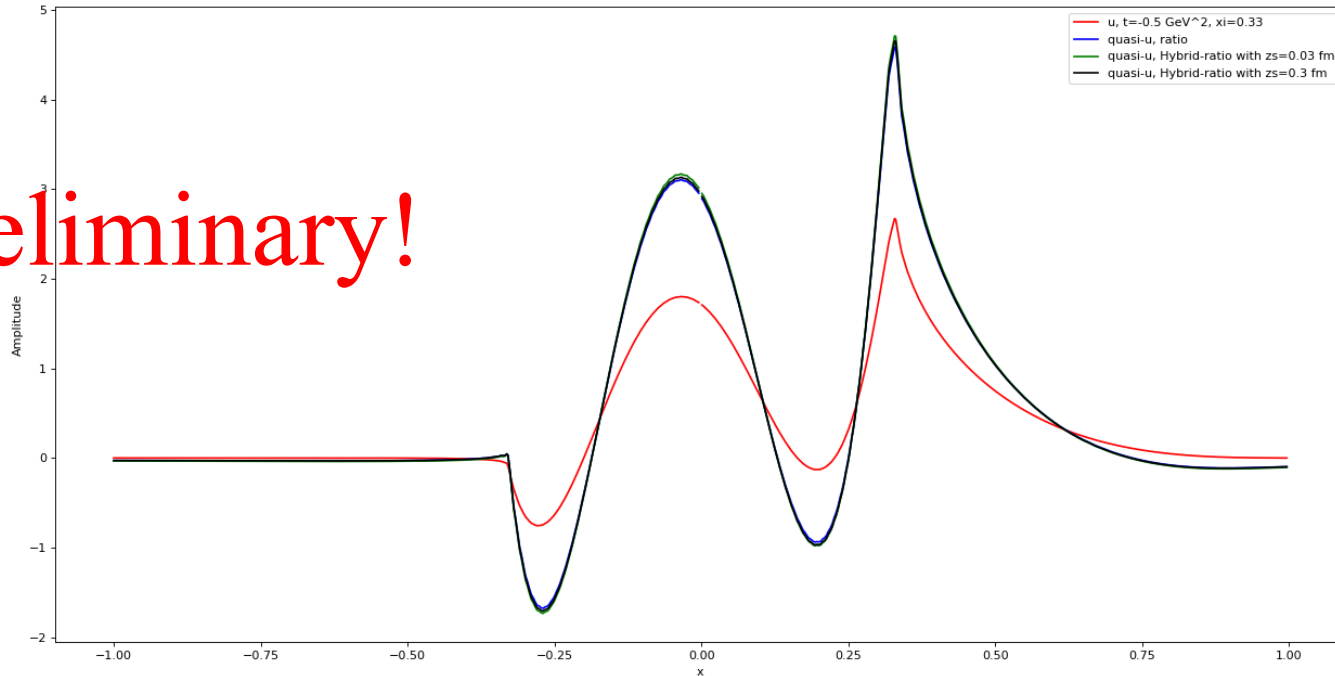
QGPDs in Hybrid-Ratio Scheme

- GPDs, depend on (x, x_i, t)
- Hybrid-ratio kernel = ratio kernel (t independent) + Z_s depend term (x_i and t independent)
- $x_i = 0$, Hybrid-ratio kernel = PDF kernel

Unpol. QGPD H

w/ Yi-Xian Chen, Chien-Yu Chou

Preliminary!



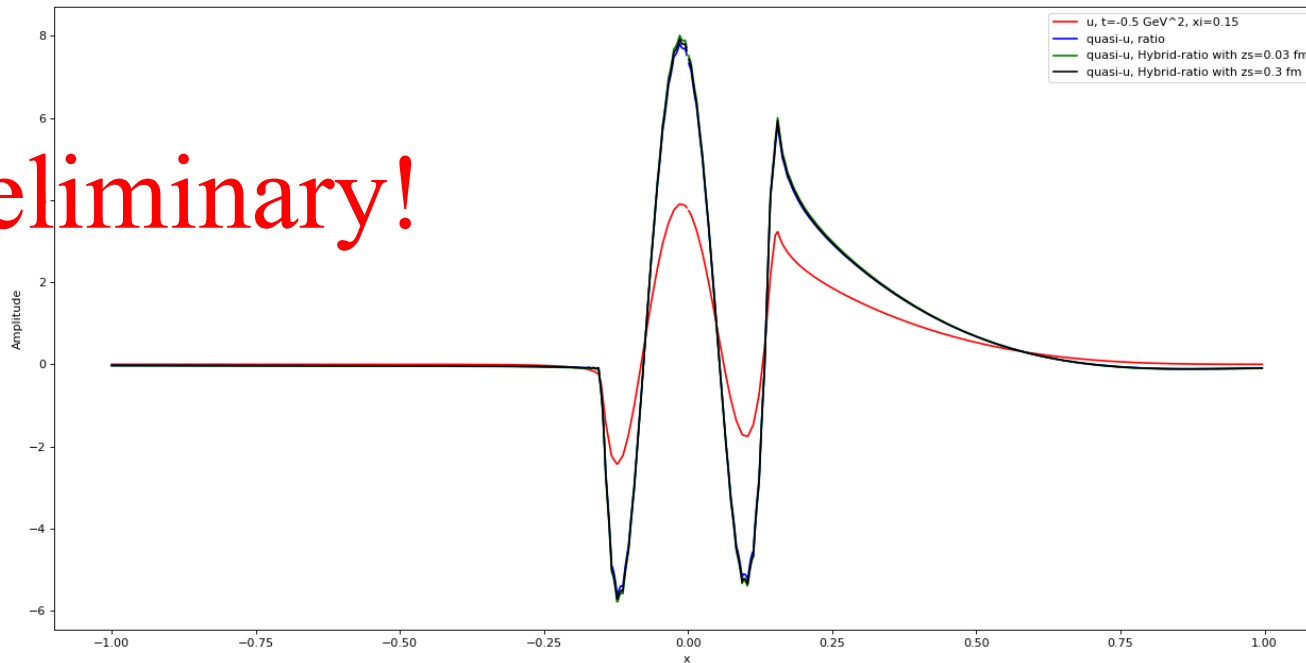
u quark in proton; $t=-0.5 \text{ GeV}^2$, $\xi=0.33$
 $Z_s = 0.3 \text{ fm}$ is close to infinity!

GPD model: Yuxun Guo, Xiangdong Ji, M. Gabriel Santiago, Kyle Shiells,
Jinghong Yang (2302.07279)

Unpol. QGPD H

w/ Yi-Xian Chen, Chien-Yu Chou

Preliminary!



u quark in proton; $t=-0.5 \text{ GeV}^2$, $\xi=0.15$
 $Z_s = 0.3 \text{ fm}$ is close to infinity!

GPD model: Yuxun Guo, Xiangdong Ji, M. Gabriel Santiago, Kyle Shiells,
Jinghong Yang (2302.07279)

Summary

Hybrid-ratio scheme

- (a) Renormalon ambiguity in PDF close to $\overline{\text{MS}}$ -bar scheme ($Z_s = 0.3$ fm is close to zero). Bubble sum same as leading log resummation
- (b) QGPD close to ratio scheme ($Z_s = 0.3$ fm is close to infinity)